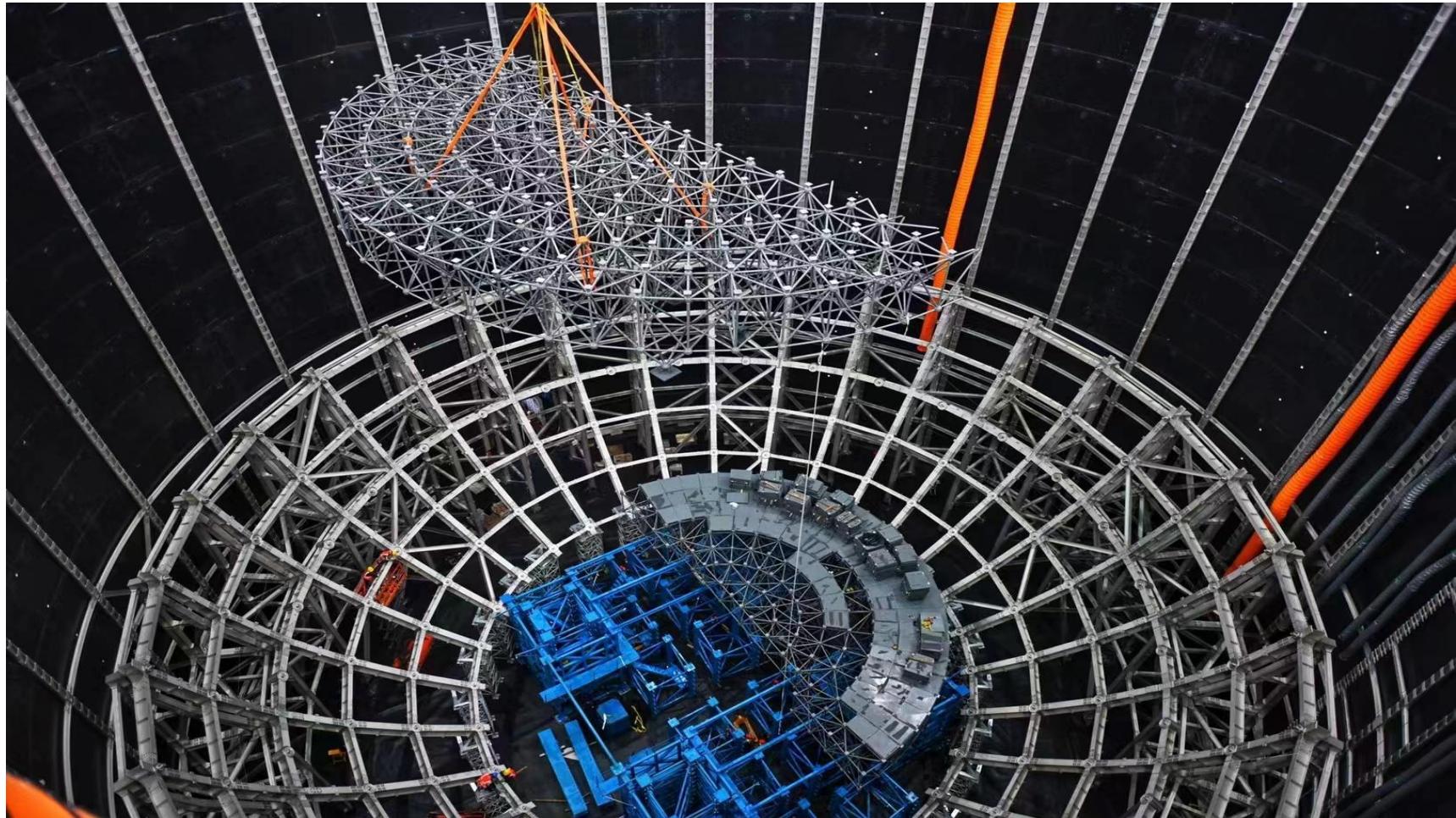


国内中微子实验相关结果



凌家杰（中山大学）
第三届粒子物理前沿研讨会
2022/07/23





The 3-neutrino Mixing

B. Pontecorvo, Z. Maki, M. Nakagawa, S. Sakata, E. Majorana

$$|\nu_\alpha\rangle = \sum_{i=1}^3 U_{\alpha i}^* |\nu_i\rangle$$



$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} e^{i\eta_1} & 0 & 0 \\ 0 & e^{i\eta_2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

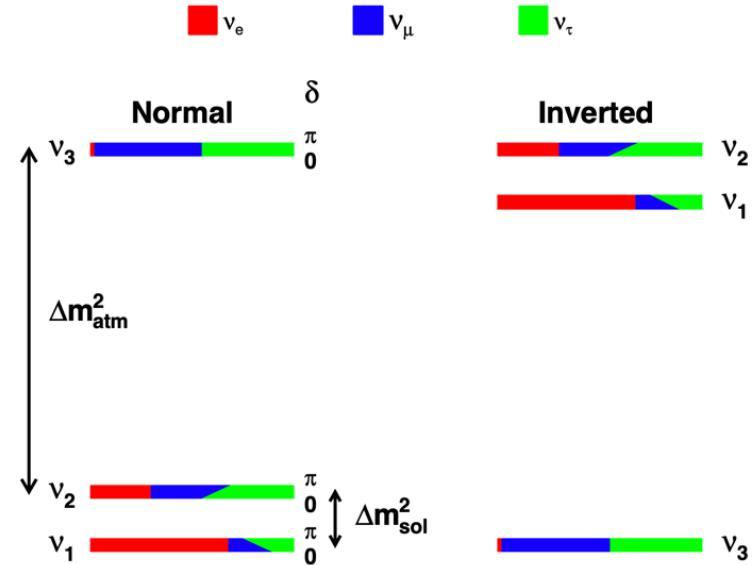
$$c_{ij} = \cos\theta_{ij} \quad s_{ij} = \sin\theta_{ij}$$

Three mixing angles: θ_{23} , θ_{13} , θ_{12}

$$c_{12}^2 \equiv \cos^2\theta_{12} = \frac{|U_{e1}|^2}{1-|U_{e3}|^2} \quad s_{12}^2 \equiv \sin^2\theta_{12} = \frac{|U_{e2}|^2}{1-|U_{e3}|^2}$$

$$s_{13}^2 \equiv \sin^2\theta_{13} = |U_{e3}|^2$$

$$s_{23}^2 \equiv \sin^2\theta_{23} = \frac{|U_{\tau 3}|^2}{1-|U_{e3}|^2} \quad c_{23}^2 \equiv \cos^2\theta_{23} = \frac{|U_{\tau 3}|^2}{1-|U_{e3}|^2}$$



Current Status of PMNS Parameters

| NuFIT 4.0 | θ_{12} (°) | θ_{23} (°) | θ_{13} (°) | δ_{CP} (°) | Δm_{21}^2 ($\times 10^{-5}$ eV 2) | Δm_{32}^2 ($\times 10^{-3}$ eV 2) |
|------------------------------|-------------------------|----------------------|------------------------|----------------------|---|---|
| Normal | $33.44^{+0.77}_{-0.74}$ | $49.2^{+0.9}_{-1.2}$ | $8.57^{+0.12}_{-0.12}$ | 197^{+27}_{-24} | $7.42^{+0.21}_{-0.20}$ | $2.443^{+0.026}_{-0.028}$ |
| Inverted | $33.45^{+0.78}_{-0.75}$ | $49.3^{+0.9}_{-1.1}$ | $8.60^{+0.12}_{-0.12}$ | 282^{+26}_{-30} | $7.42^{+0.21}_{-0.20}$ | $-2.498^{+0.028}_{-0.028}$ |
| Relative 1σ precision | 2.3% | 2.0% | 1.4% | 13.2% | 2.7% | 1.1% |

JHEP 09 (2020) 178

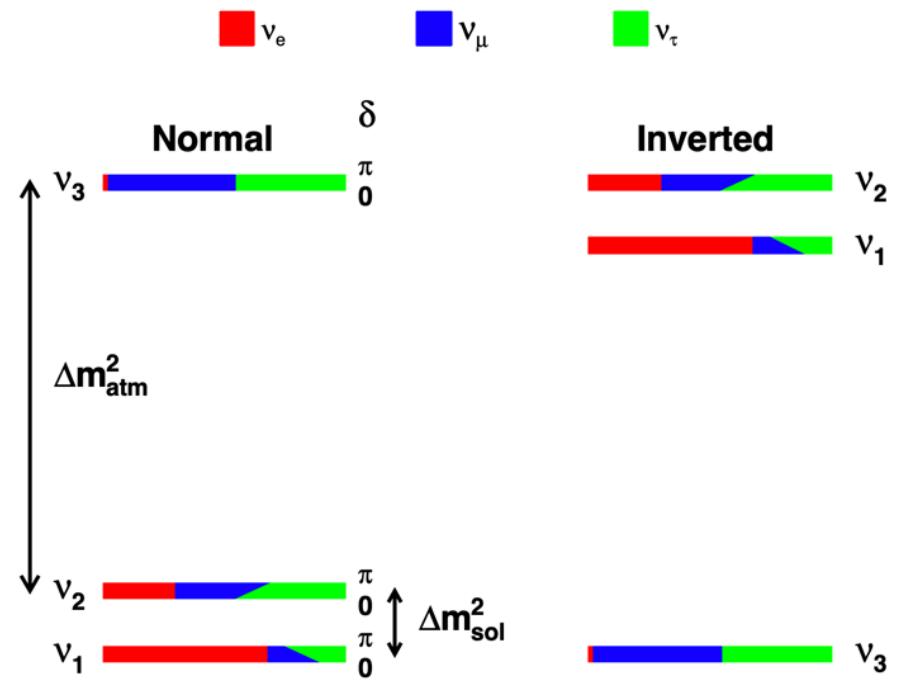
Well measured: θ_{12} , θ_{13} , Δm_{21}^2 , $|\Delta m_{32}^2|$

Not-so-well measured: θ_{23} Octant, δ_{CP} , neutrino mass ordering (sign of Δm_{32}^2)

- $\theta_{23} > \pi/4$ is mildly preferred with $\Delta\chi^2 = 0.53$ (2.2 with SK – atm)
- Normal mass ordering is slightly preferred with $\Delta\chi^2 = 2.7$ (7.1 with SK – atm)

Open Questions of Massive Neutrinos

- What's the neutrino mass ordering?
- Are neutrinos responsible for the matter anti-matter asymmetry?
- Are neutrinos Dirac or Majorana particles?
- What is the neutrino mass?
- Do sterile neutrinos exist?
- Why neutrino mass is so tiny?
-



$$\text{NO : } |\Delta m_{31}^2| = |\Delta m_{32}^2| + \Delta m_{21}^2$$
$$\text{IO: } |\Delta m_{31}^2| = |\Delta m_{32}^2| - \Delta m_{21}^2$$



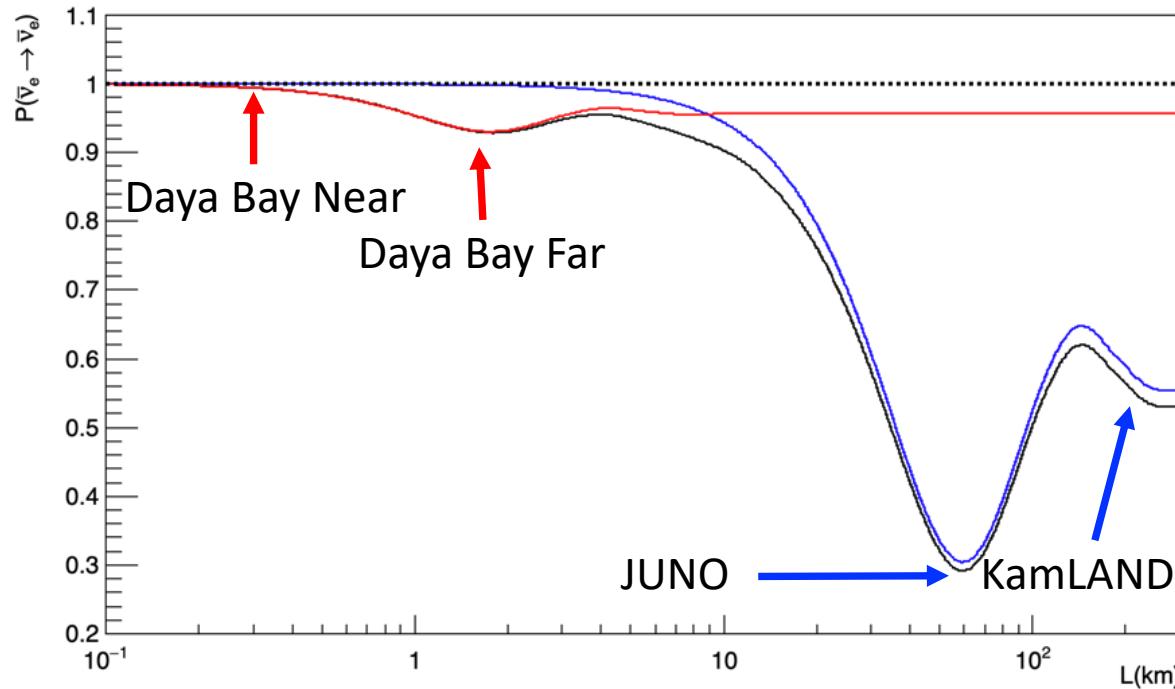
Reactor Antineutrino Oscillation

$$P_{\alpha\beta} = |\langle v_\beta | v_\alpha(t) \rangle|^2 = \delta_{\alpha\beta} - 4 \sum_{i<j}^3 \text{Re}[U_{\alpha i} U_{\beta i}^* U_{\alpha j}^* U_{\beta j}] \sin^2 \Delta_{ij} + 2 \sum_{i<j}^3 \text{Im}[U_{\alpha i} U_{\beta i}^* U_{\alpha j}^* U_{\beta j}] \sin 2\Delta_{ij}$$

$$\begin{aligned} P(\bar{\nu}_e \rightarrow \bar{\nu}_e) &= 1 - \sin^2 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32}) - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} \\ &\approx 1 - \boxed{\sin^2 2\theta_{13} \sin^2 \Delta_{ee}} - \boxed{\cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21}} \end{aligned}$$

$$\Delta_{ij} = \Delta m_{ij}^2 \frac{L}{4E}$$

Immune to CP violation and matter effects



Key for a precise measurement:

✓ Baseline Optimization

$$L(\text{m}) \sim \frac{\pi \cdot E (\text{MeV})}{2.54 \cdot \Delta m^2 (\text{eV}^2)}$$

✓ Large statistics

Large $\bar{\nu}_e$ flux

Massive target mass

✓ Background control

Large overburden

Detector shielding

✓ Systematics control

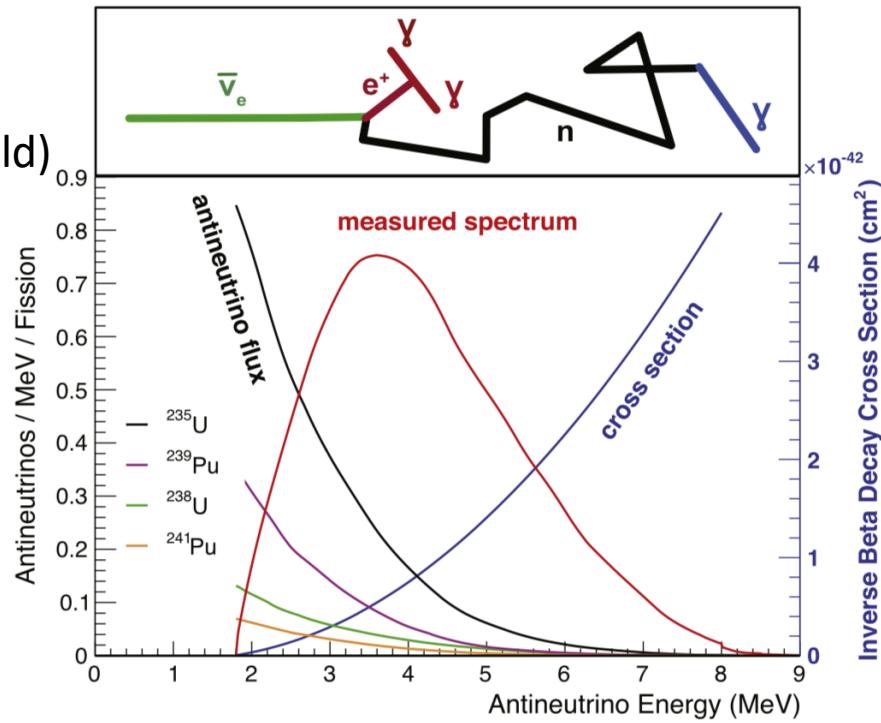
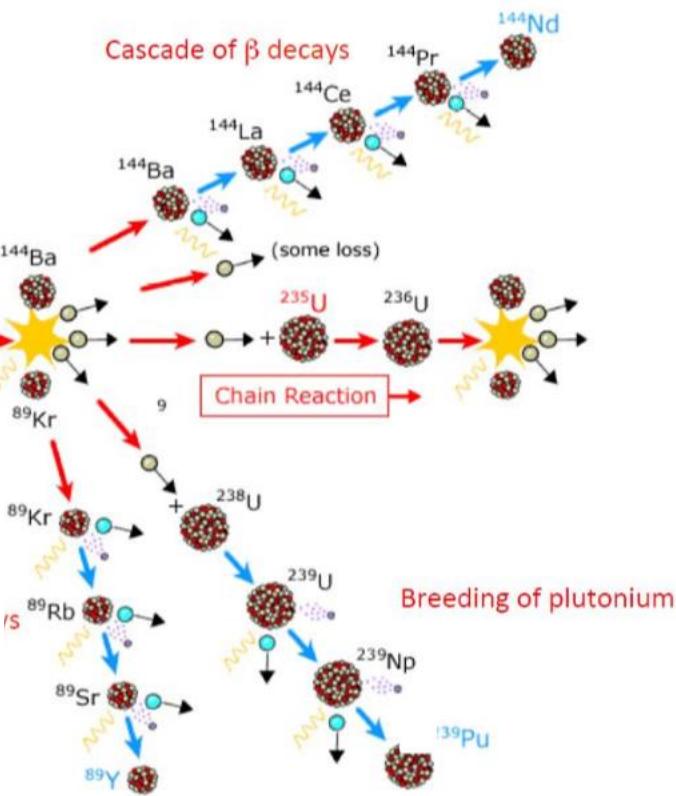
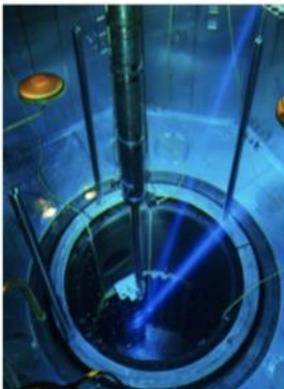
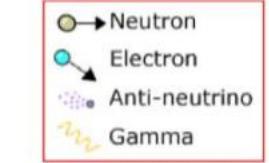
Relative Far/Near measurement



Reactor $\bar{\nu}_e$ Production and Detection

Source: Pure $\bar{\nu}_e$ from cascade of beta decays

- ~ 200 MeV / fission
- $\sim 2 \times 10^{20} \bar{\nu}_e/\text{GW}_{\text{th}}/\text{Sec}$ (1/5 above IBD threshold)



Inverse Beta decay (IBD) $\bar{\nu}_e + p \rightarrow n + e^+$

Coincidence signals to suppress background

- Prompt: $E_{\text{prompt}} \approx E_{\bar{\nu}} - 0.8 \text{ MeV}$
- Delayed: nH (2.2 MeV) or nGd (~8 MeV)

The Daya Bay and JUNO Site

| NPP | Daya Bay | Huizhou | Lufeng | Yangjiang | Taishan |
|--------|-------------|---------|---------|-------------|-------------|
| Status | Operational | Planned | Planned | Operational | Operational |
| Power | 17.4 GW | 17.4 GW | 17.4 GW | 17.4 GW | 9.2 GW |



Daya Bay Layout

Far Hall

1540 m from Ling Ao I
1910 m from Daya Bay
324 m overburden

Relative Measurement:

3 Experimental Halls (EH)
8 “identical” antineutrino
detectors (AD)

EH3
(AD-4, 5, 6, 7)

Ling Ao Near Hall
470 m from Ling Ao I
558 m from Ling Ao II
100 m overburden

EH2
(AD-3, 8)

Daya Bay Near Hall
363 m from Daya Bay
93 m overburden

EH1
(AD-1, 2)

Daya Bay Cores

Entrance

Tunnels

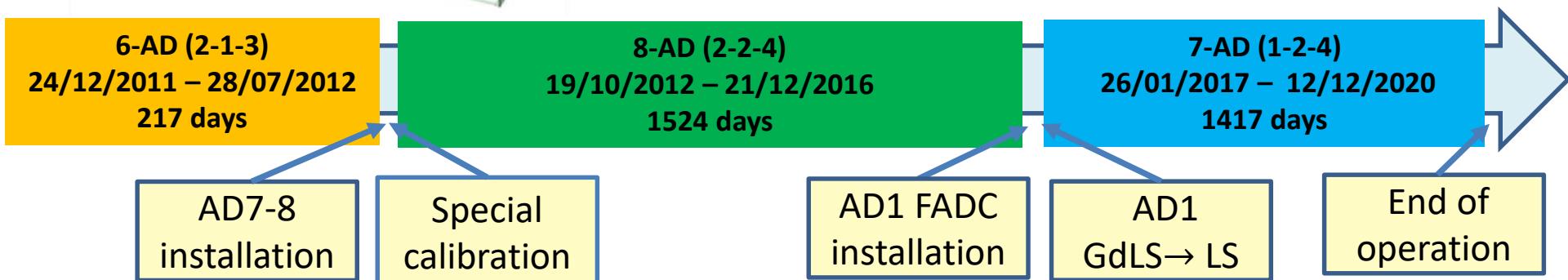
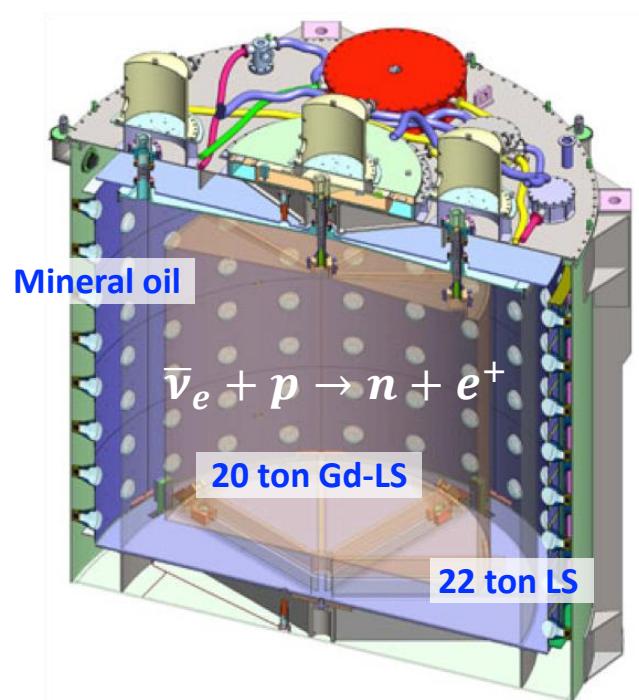
Ling Ao II Cores
Ling Ao I Cores

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- 17.4 GW_{th} power
- 8 operating detectors
- 160 t total target mass



Antineutrino Detector (AD) System

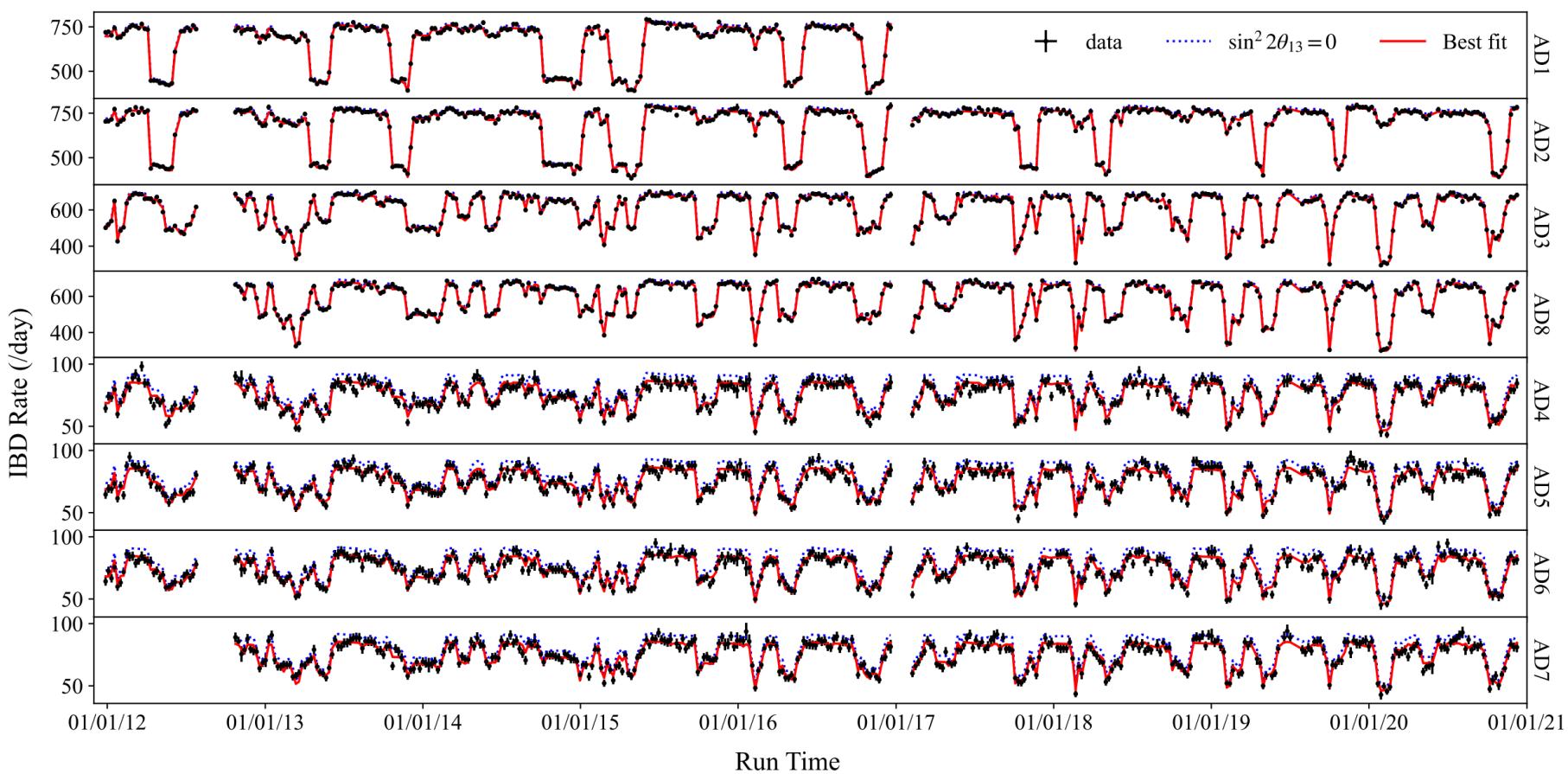




5.5 Million nGd IBD Candidates

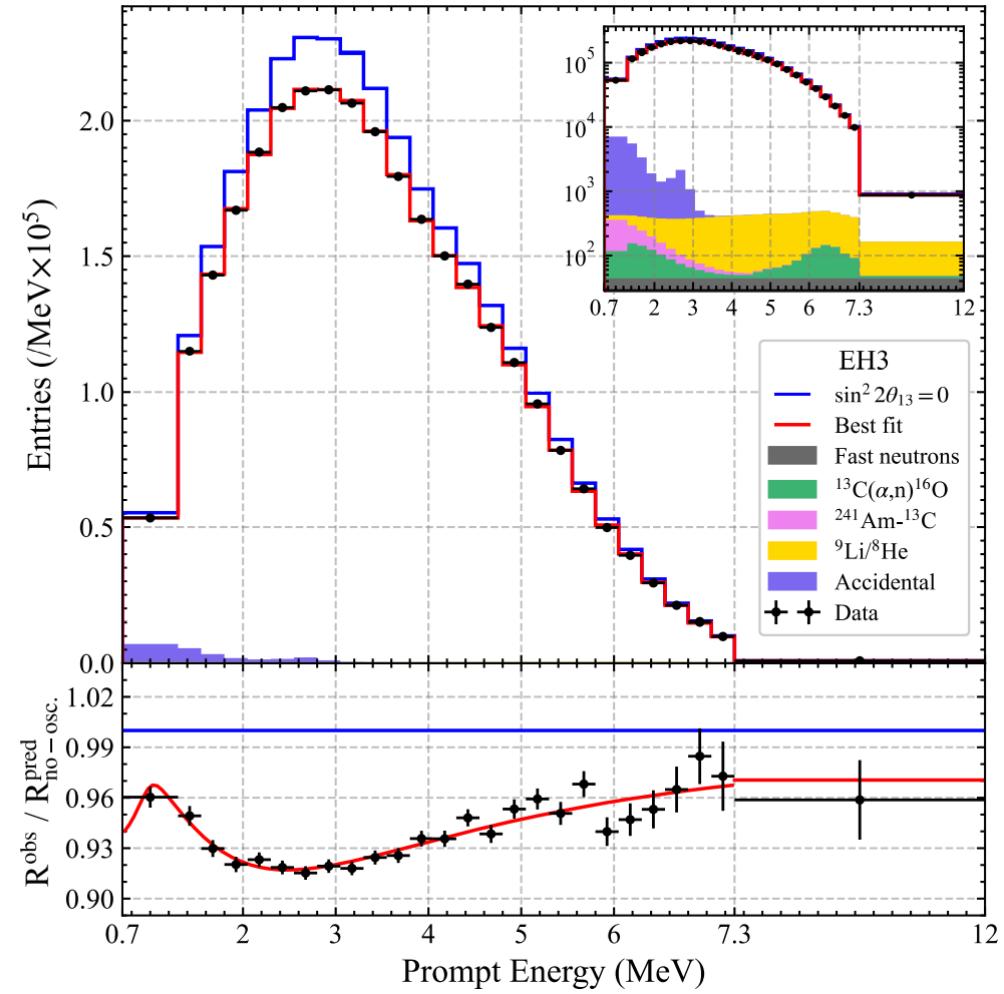
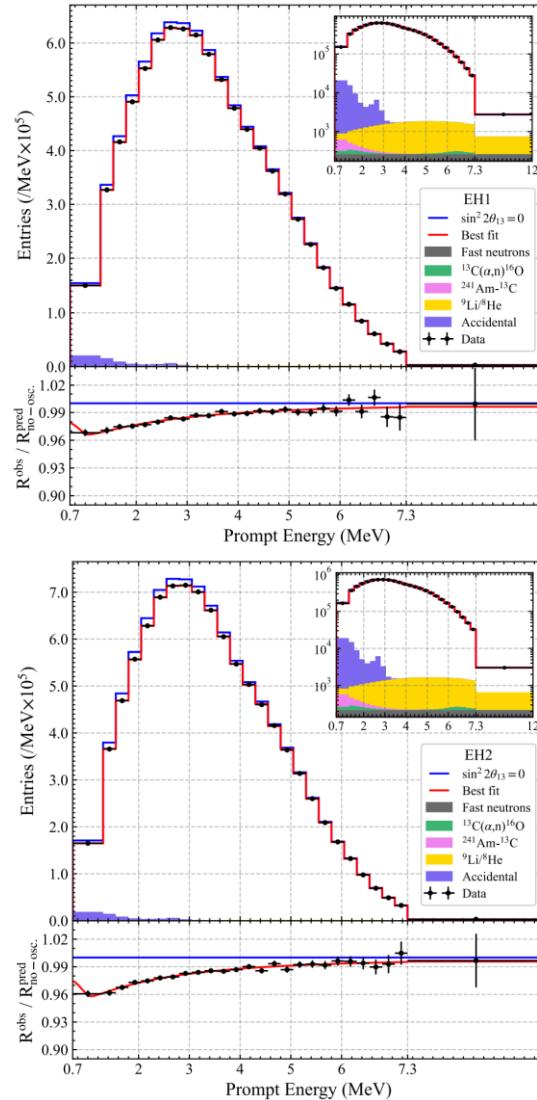
- 24/12/2011 – 12/12/2020 (3158 days)
 - ~2700 days of good data
- World largest IBD data sample
 - 5.5 M IBDs

| Site | EH1 (Near) | EH2 (Near) | EH3 (Far) |
|----------------|------------|------------|-----------|
| IBD candidates | 2,236,810 | 2,544,894 | 764,414 |



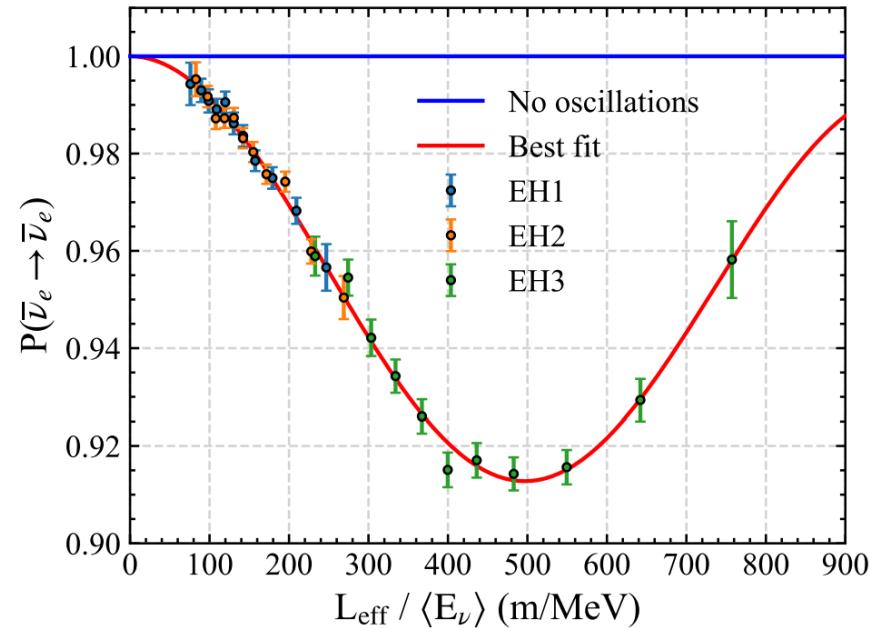
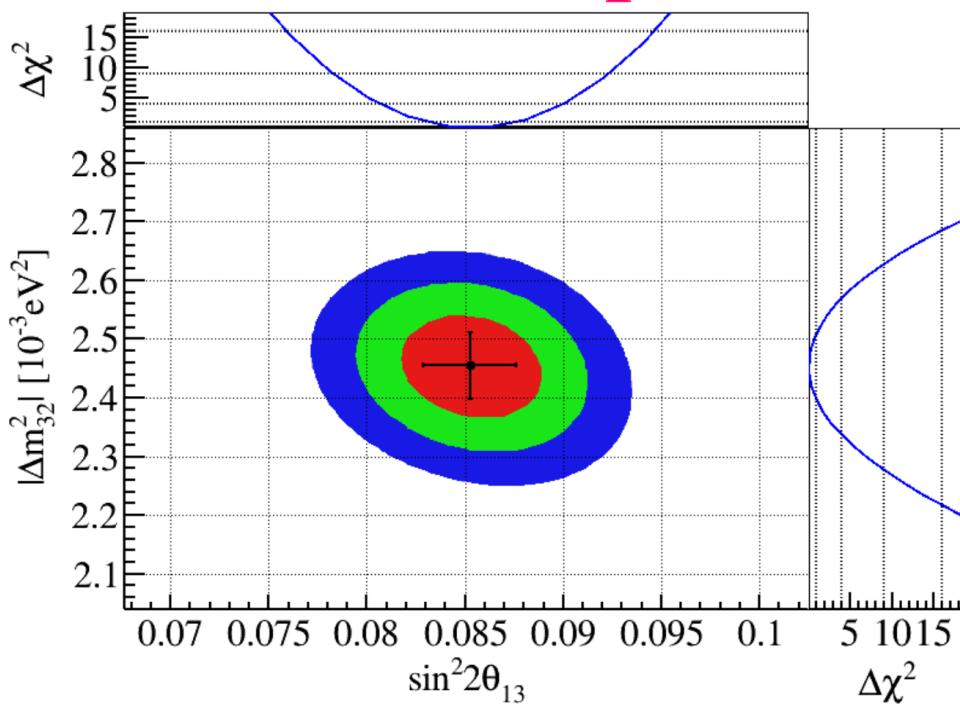


Prompt Energy Spectra





Rate+Spectra Oscillation Results



Best-fit results: $\chi^2/\text{ndf} = 559/518$

$$\sin^2 2\theta_{13} = 0.0853^{+0.0024}_{-0.0024} \quad (2.8\% \text{ precision})$$

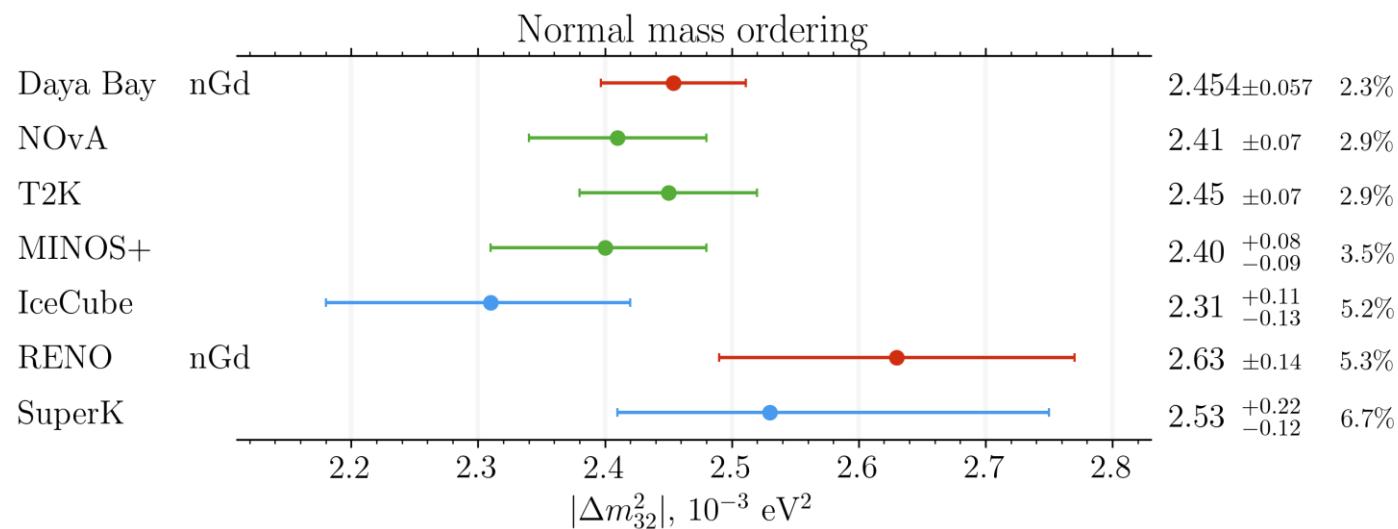
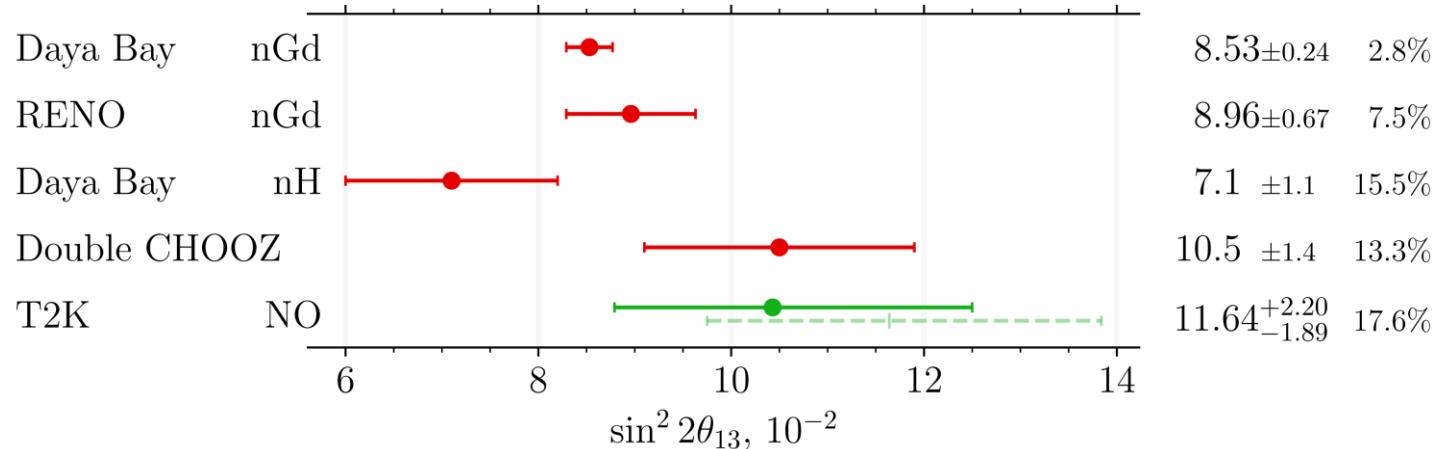
Normal hierarchy: $\Delta m_{32}^2 = + (2.454^{+0.057}_{-0.057}) \times 10^{-3} \text{ eV}^2$

(2.3% precision)

Inverted hierarchy: $\Delta m_{32}^2 = - (2.559^{+0.057}_{-0.057}) \times 10^{-3} \text{ eV}^2$

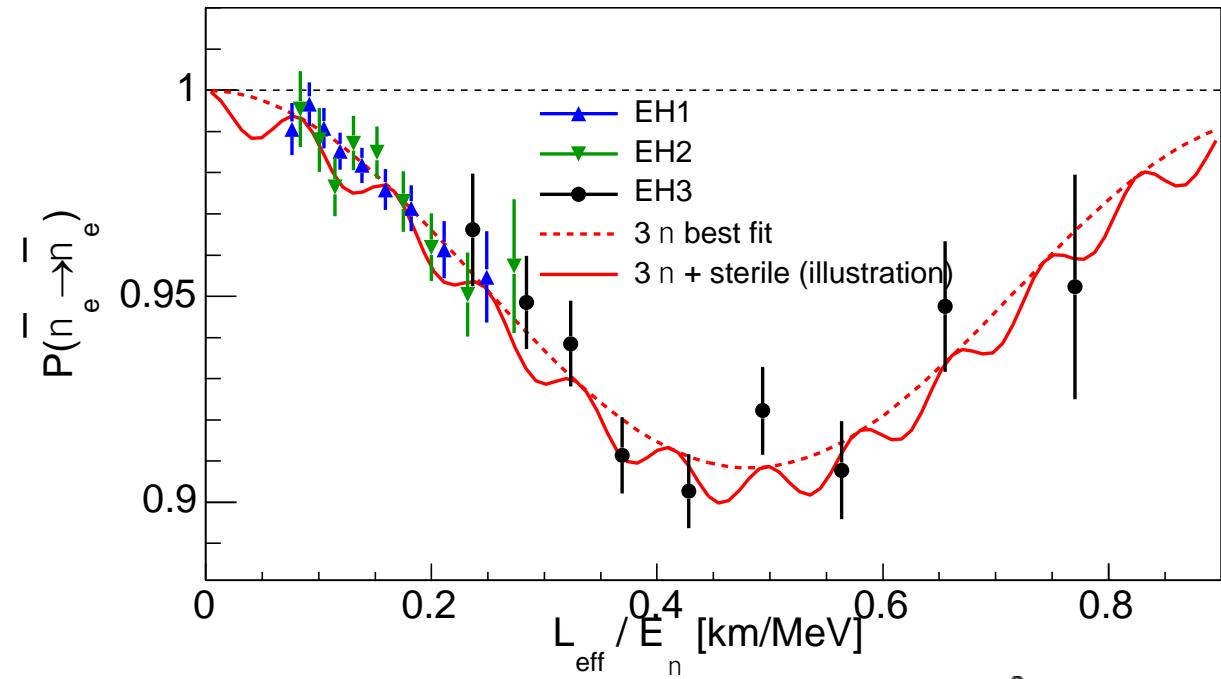
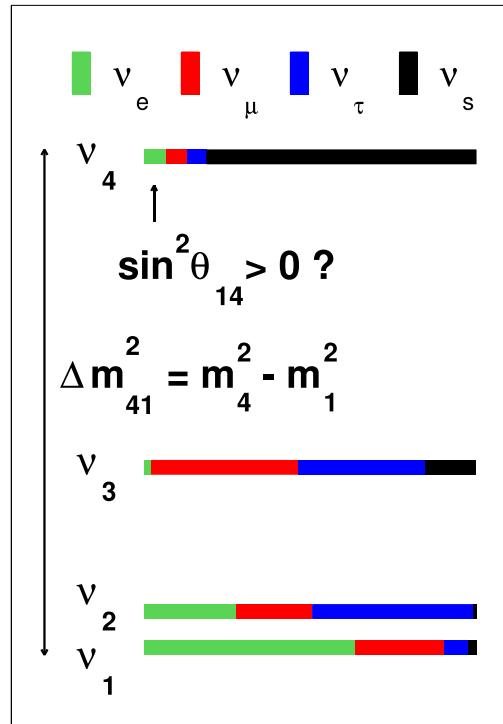


Precision Measurements



World most precise measurement of $\sin^2 2\theta_{13}$ and $|\Delta m^2_{32}|$

light sterile neutrino oscillation



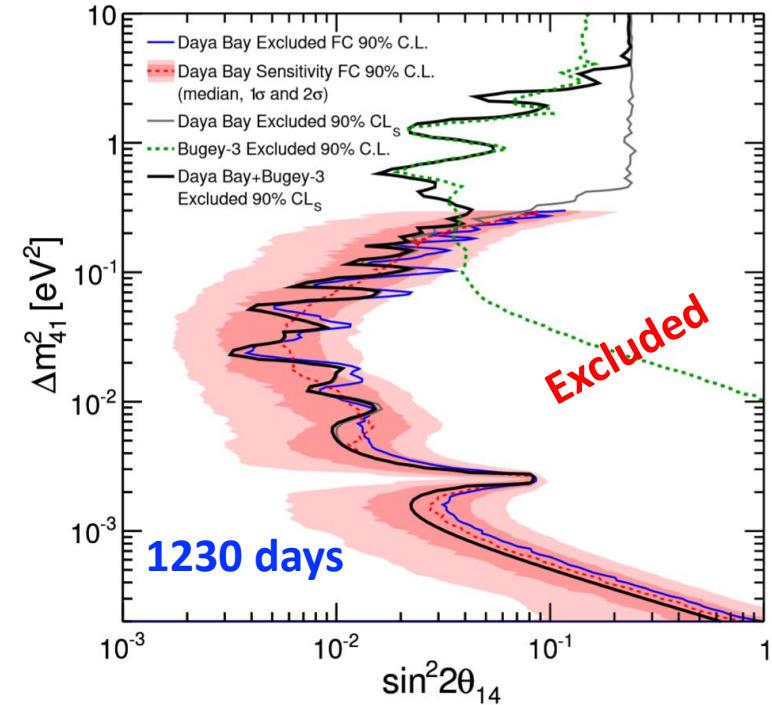
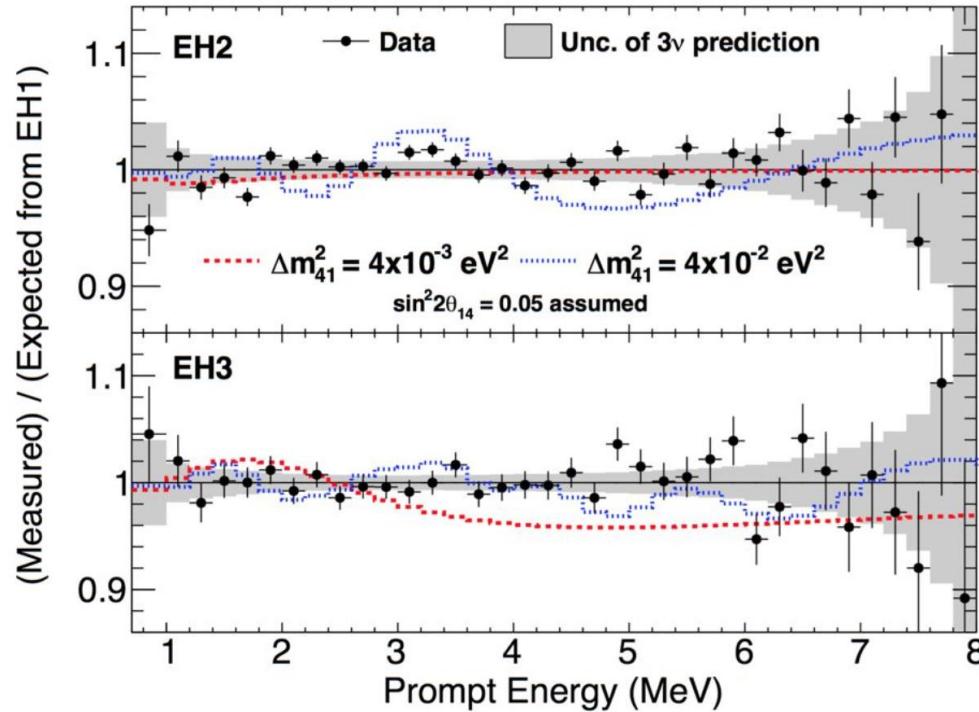
$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) @ 1 - \cos^4 q_{14} \sin^2 2q_{13} \sin^2 \left(\frac{Dm_{ee}^2 L}{4E_n} \right) - \sin^2 2q_{14} \sin^2 \left(\frac{Dm_{41}^2 E}{4E_n} \right)$$

- A minimum extension of the 3-v model: 3(active) + 1(sterile)-v model
- Search for a higher frequency oscillation pattern besides $|\Delta m_{ee}^2|$



Sterile Neutrino Search

PRL 125, 071801 (2020)



- Data is consistent with 3-v model; No light sterile neutrino signal observed
- Consistent results from Feldman-Cousins and CLs methods

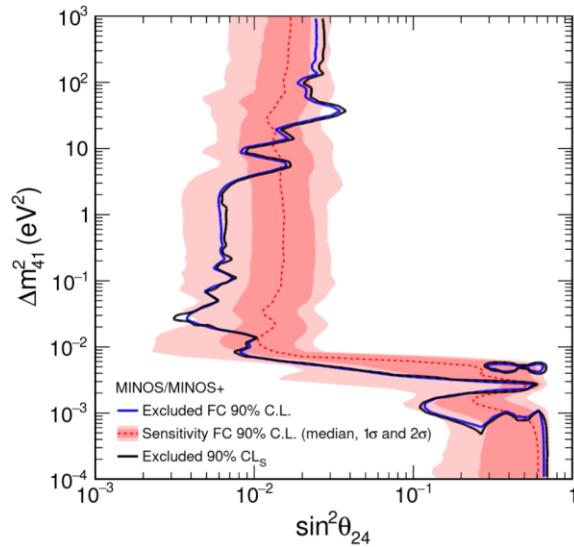
The most stringent upper limit for light sterile neutrinos ($\Delta m^2 < 0.2 \text{ eV}^2$)



Joint Sterile Neutrino Searches

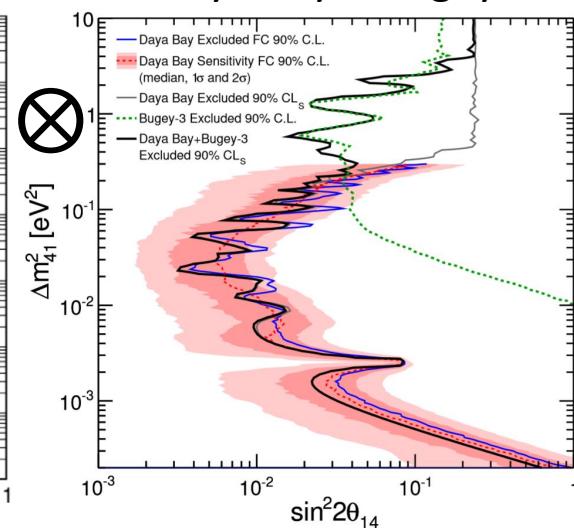
PRL 122 091803 (2019)

MINOS/MINOS+



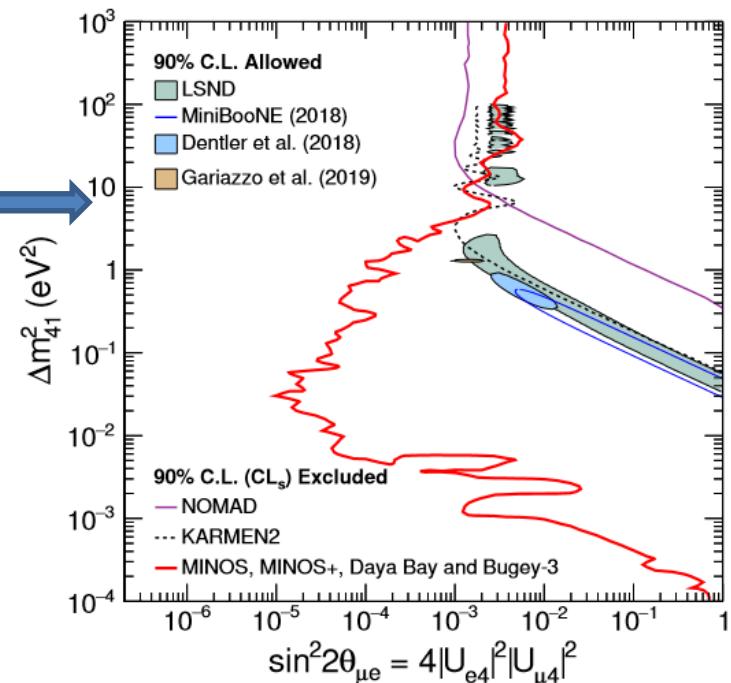
$$|U_{\mu 4}|^2 = \sin^2 \theta_{24} \cos^2 \theta_{14}$$

Daya Bay + Bugey-3



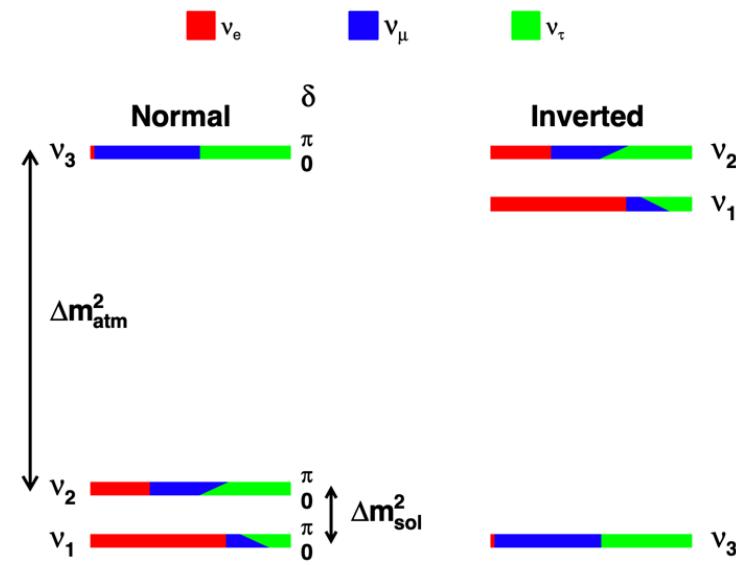
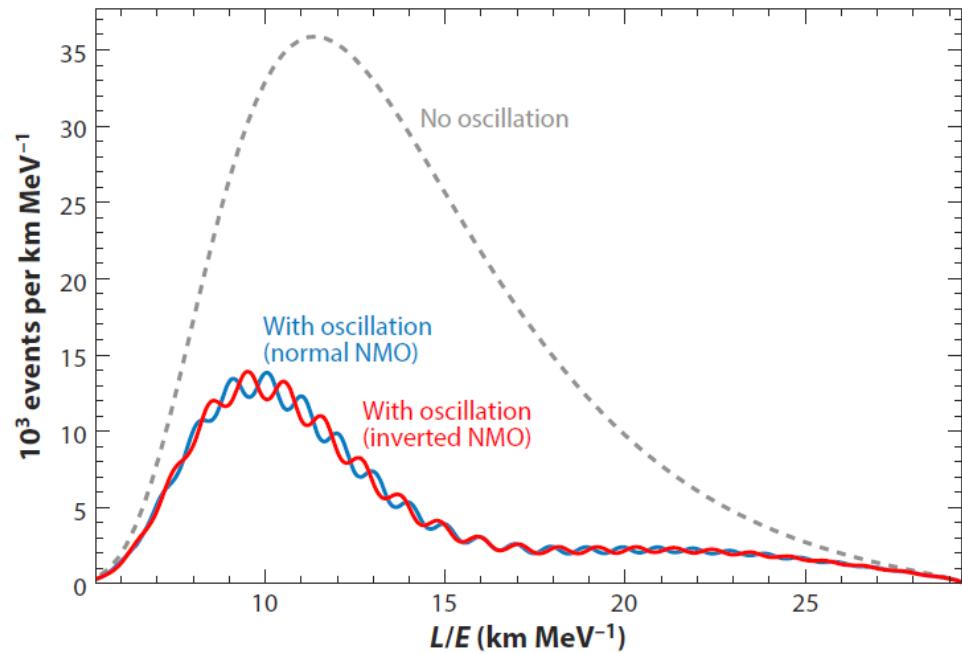
$$|U_{e4}|^2 = \sin^2 \theta_{14}$$

PRL 125, 071801 (2020)



- The combined results can exclude the LSND and MiniBooNE signal region at $\Delta m_{41}^2 < 5$ eV 2 at 90% C.L.

Neutrino Oscillation at Jiangmen Underground Neutrino Observatory (JUNO)



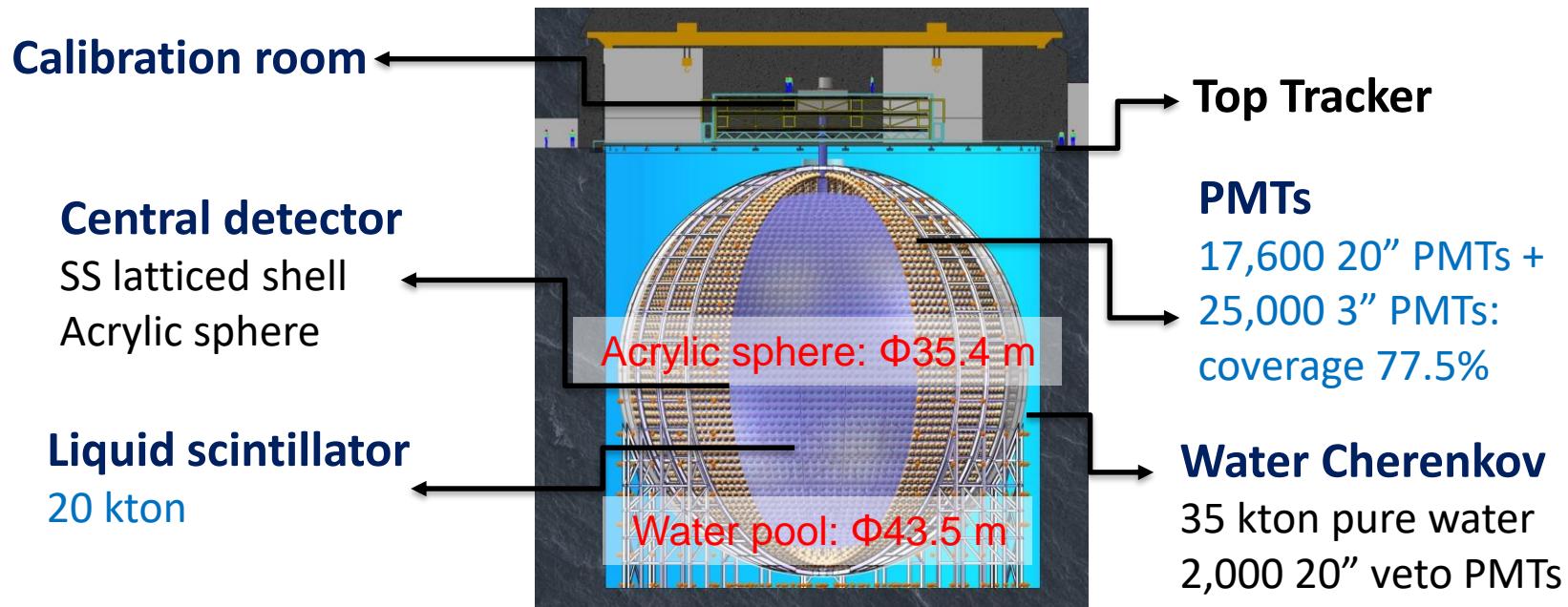
$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} - \sin^2 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32})$$

NO : $|\Delta m^2_{31}| = |\Delta m^2_{32}| + \Delta m^2_{21}$
 IO: $|\Delta m^2_{31}| = |\Delta m^2_{32}| - \Delta m^2_{21}$

- S.T. Petcov et al., PLB533(2002)94
 S.Choubey et al., PRD68(2003)113006
 J. Learned et al., PRD78, 071302 (2008)
 L. Zhan, Y. Wang, J. Cao, L. Wen, PRD78:111103, 2008, PRD79:073007, 2009
 J. Learned et al., arXiv:0810.2580
 Y.F Li et al, PRD 88, 013008 (2013)
 ...

JUNO Detector Design

| | KamLAND | Borexino | Daya Bay | JUNO |
|---------------------|---------|----------|----------------------|------|
| LS Mass [kton] | 1 | 0.278 | $\sim 0.04 \times 8$ | 20 |
| E resolution@ 1 MeV | 6% | 5% | 8% | 3% |
| Photo-coverage | 34% | 30% | 12% | 77% |
| E calibration | 1.4% | 1% | 0.5% | 1% |



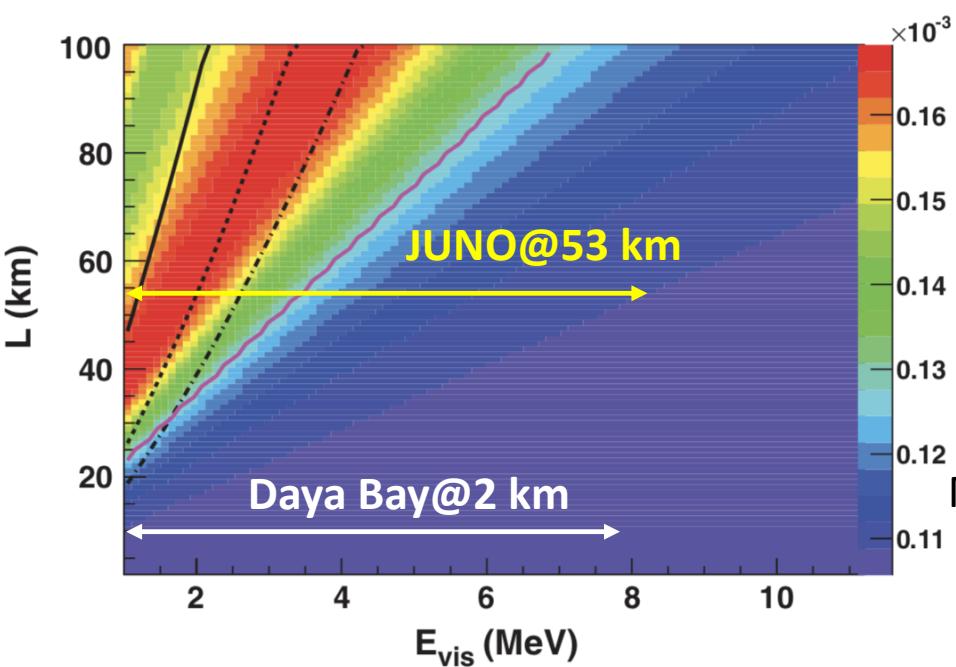
Neutrino Mass Ordering (NMO)

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$$

$$= 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} - \sin^2 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32})$$

$$= 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} - 2 \sin^2 \theta_{13} \cos^2 \theta_{13} \\ + 2 \sin^2 \theta_{13} \cos^2 \theta_{13} \sqrt{1 - 4 \sin^2 \theta_{12} \cos^2 \theta_{12} \sin^2 \Delta_{21}} \cos(2\Delta_{32} \pm \phi_{ee})$$

+ : Normal
- : Inverted



X.Qian et al. Phys. Rev.D.87, 033005 (2013)

$$\Delta_{ij} = 1.27 \frac{\Delta m_{ij}^2 L(m)}{E \text{ (MeV)}}$$

$$\tan \phi = \frac{\cos^2 \theta_{12} \sin 2\Delta_{21}}{\cos^2 \theta_{12} \cos 2\Delta_{21} + \sin^2 \theta_{12}}$$

$$\Delta m_{\phi_{ee}}^2 (\text{eV}^2) = \frac{\phi}{1.27} \cdot \frac{E(\text{m})}{L(\text{MeV})}$$

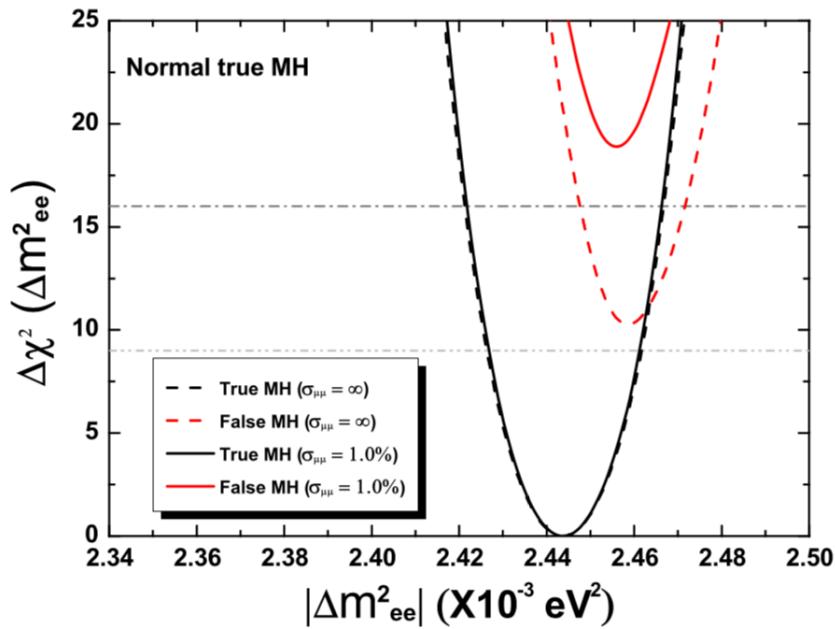
Mass ordering degeneracy at a certain L and E:

$$|\Delta m_{32}^2(\text{IO})| = |\Delta m_{32}^2(\text{NO})| + \Delta m_{\phi}^2(L, E)$$

The degeneracy of NMO can be broken with the reactor neutrino energy spectrum when the detector baseline > ~50 km.

Sensitivity of NMO Determination

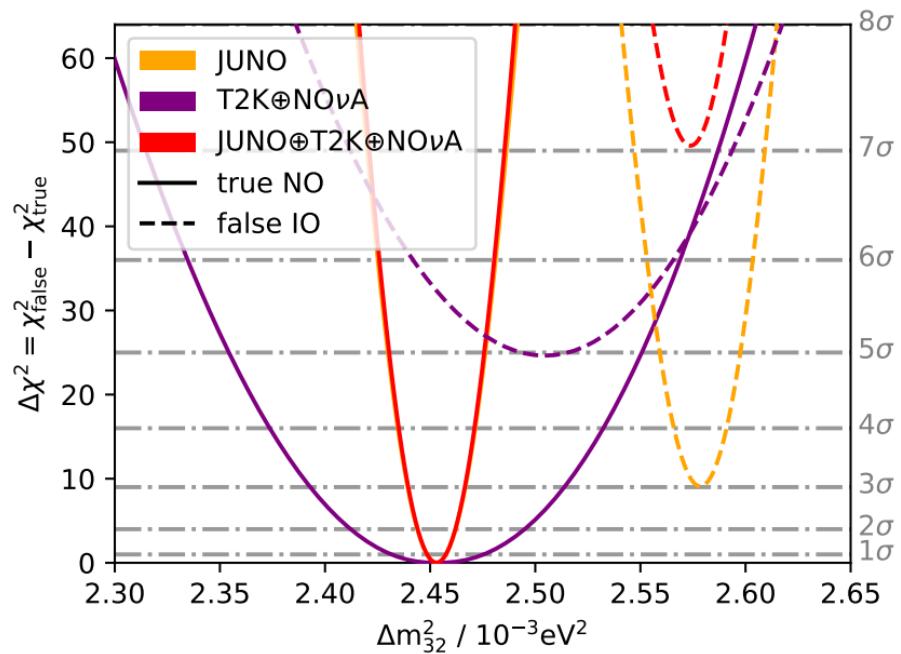
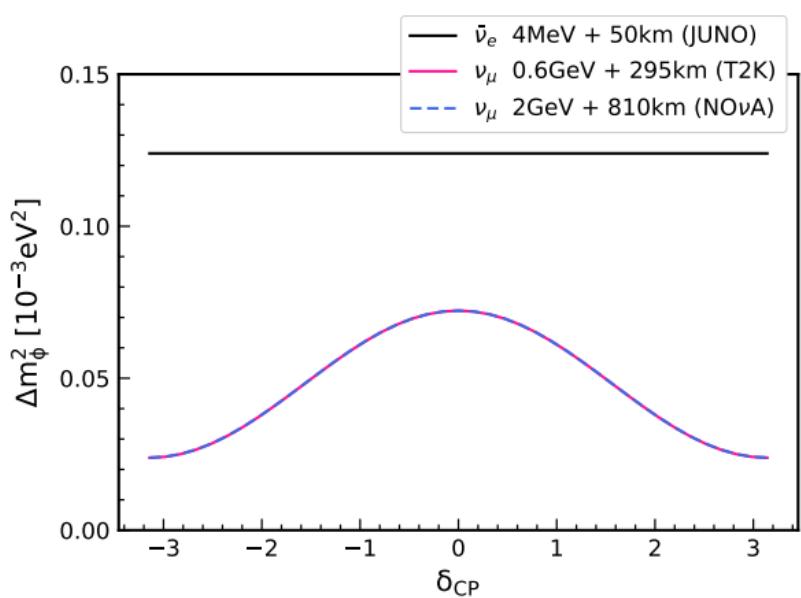
| Event type | Rate (per day) | Rate uncertainty (relative) | Shape uncertainty |
|--|----------------|-----------------------------|-------------------|
| IBD candidates | 60 | — | — |
| Geo- ν s | 1.1 | 30% | 5% |
| Accidental signals | 0.9 | 1% | negligible |
| Fast- n | 0.1 | 100% | 20% |
| ^9Li - ^8He | 1.6 | 20% | 10% |
| ^{13}C (α , n) ^{16}O | 0.05 | 50% | 50% |



JUNO MO sensitivity with 6 years' data assuming full reactor power

| | Size | $\Delta\chi^2_{\text{MO}}$ |
|----------------|---------|----------------------------|
| Ideal | 52.5 km | +16 |
| Core distr. | Real | -3 |
| DYB & HZ | Real | -1.7 |
| Spectral Shape | 1% | -1 |
| B/S (rate) | 6.3% | -0.6 |
| B/S (shape) | 0.4% | -0.1 |

NMO Sensitivity with External ν_μ Constraints



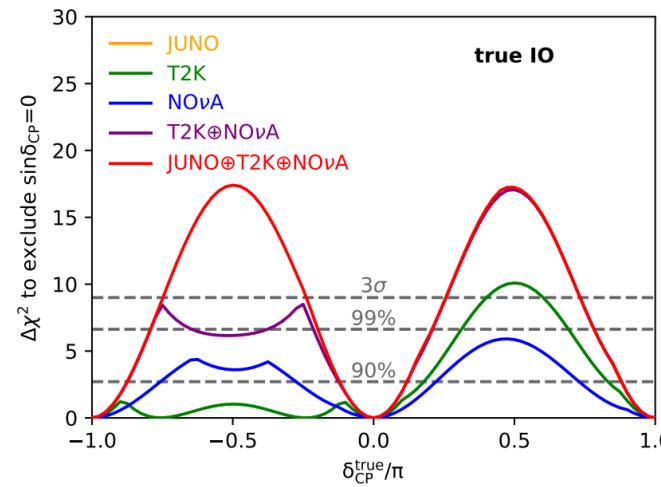
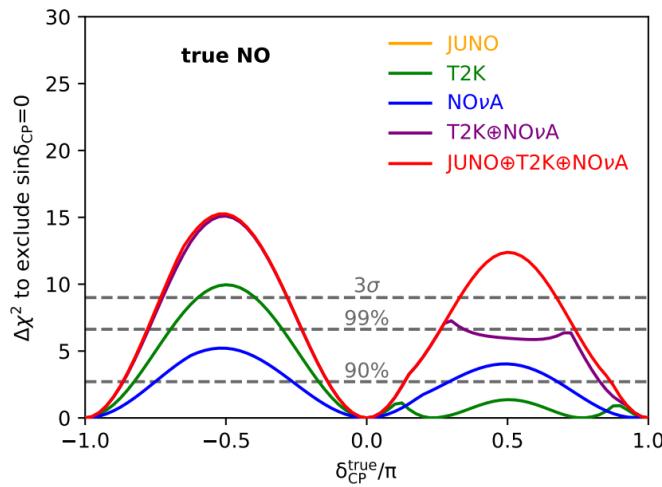
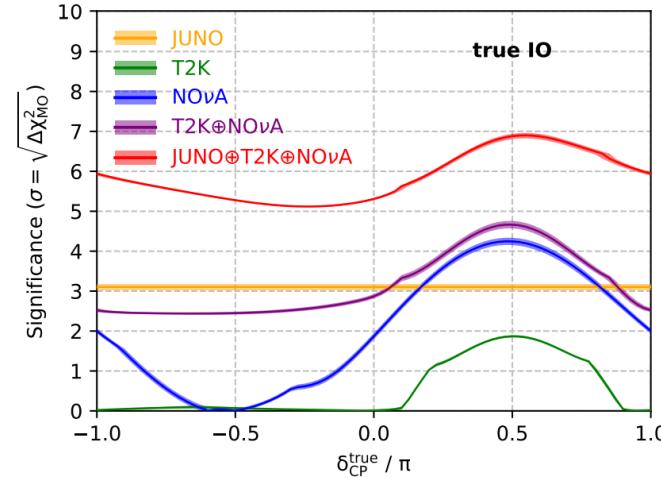
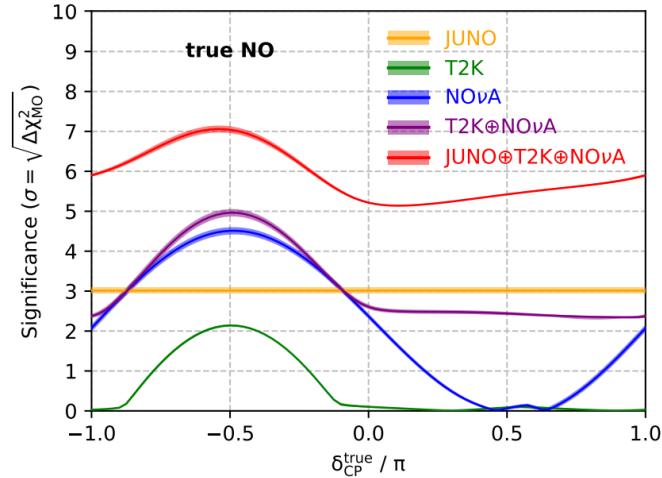
$$\Delta m_{ee}^2 = \cos^2 \theta_{12} \Delta m_{31}^2 + \sin^2 \theta_{12} \Delta m_{32}^2$$

$$\Delta m_{\mu\mu}^2 = \sin^2 \theta_{12} \Delta m_{31}^2 + \cos^2 \theta_{12} \Delta m_{32}^2 + \cos \delta_{CP} \sin \theta_{13} \sin 2\theta_{12} \tan \theta_{23} \Delta m_{21}^2$$

Sensitivity with 100k events (20k ton LS + 6 years with 26GW_{th} reactor power)

- 3% energy resolution@1 MeV, <1% energy calibration
- $\Delta\chi^2 > 9$ ($\Delta\chi^2 > 16$ with external 1% $|\Delta m_{\mu\mu}^2|$ constraint)

Sensitivity to NMO and CPV

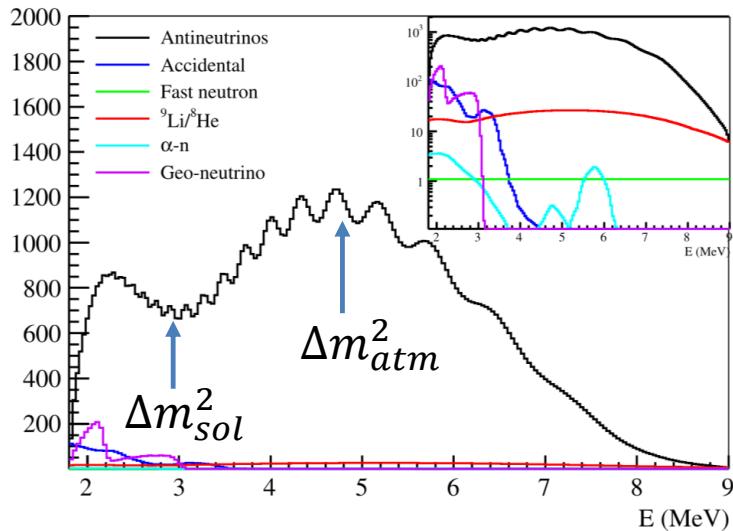


Precision Measurement at JUNO

Current precision

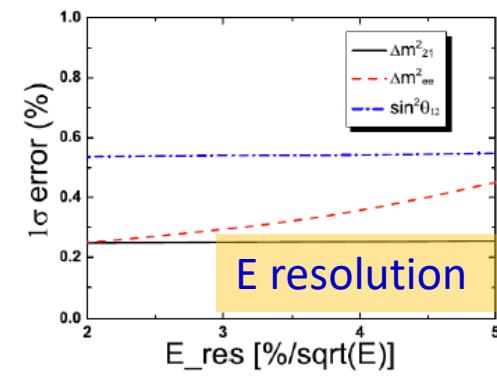
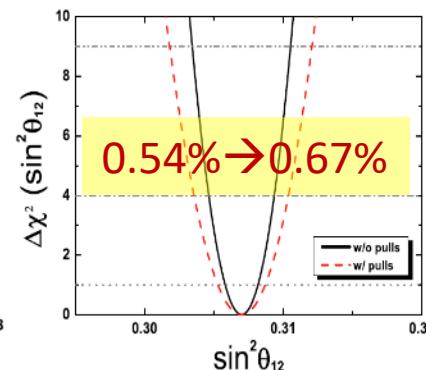
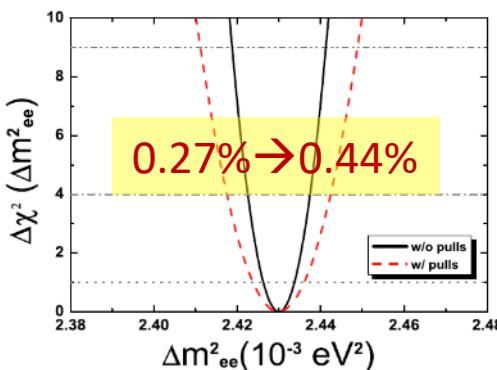
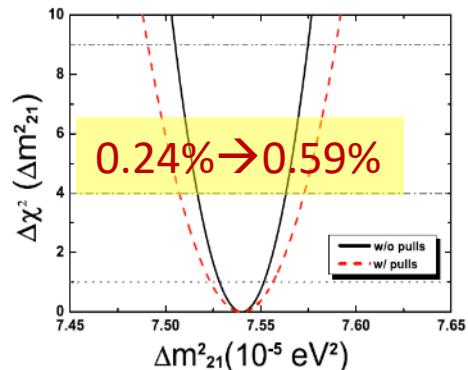
| | Δm_{21}^2 | $ \Delta m_{31}^2 $ | $\sin^2 \theta_{12}$ | $\sin^2 \theta_{13}$ | $\sin^2 \theta_{23}$ | δ |
|----------------------|-------------------|---------------------|----------------------|----------------------|----------------------|----------|
| Dominant Exps. | KamLAND | T2K | SNO+SK | Daya Bay | NO ν A | T2K |
| Individual 1σ | 2.4% | 2.6% | 4.5% | 3.4% | 5.2% | 70% |
| Nu-FIT 4.0 | 2.4% | 1.3% | 4.0% | 2.9% | 3.8% | 16% |

Probing the unitarity of U_{PMNS} to $\sim 1\%$, more precise than CKM matrix elements!



| | Statistics | +BG, +1% b2b +1% EScale , +1% EnonL |
|----------------------|------------|--|
| $\sin^2 \theta_{12}$ | 0.54% | 0.67% |
| Δm_{21}^2 | 0.24% | 0.59% |
| Δm_{32}^2 | 0.27% | 0.44% |

J. Phys. G43:030401 (2016)



Unitarity Conditions

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \cdot \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

$$|U_{\alpha 1}^{3\nu}|^2 + |U_{\alpha 2}^{3\nu}|^2 + |U_{\alpha 3}^{3\nu}|^2 = 1, \quad \alpha = e, \mu, \tau,$$

$$|U_{ei}^{3\nu}|^2 + |U_{\mu i}^{3\nu}|^2 + |U_{\tau i}^{3\nu}|^2 = 1, \quad i = 1, 2, 3,$$

$$U_{\alpha 1}^{3\nu} U_{\beta 1}^{3\nu,*} + U_{\alpha 2}^{3\nu} U_{\beta 2}^{3\nu,*} + U_{\alpha 3}^{3\nu} U_{\beta 3}^{3\nu,*} = 0, \quad \alpha, \beta = e, \mu, \tau, \quad \alpha \neq \beta,$$

$$U_{ei}^{3\nu} U_{ej}^{3\nu,*} + U_{\mu i}^{3\nu} U_{\mu j}^{3\nu,*} + U_{\tau i}^{3\nu} U_{\tau j}^{3\nu,*} = 0, \quad i, j = 1, 2, 3, \quad i \neq j.$$

Global Neutrino Data

Various neutrino experimental data can provide constraints on the different neutrino mixing elements

- Different energy scale
- Different baseline
- Different systematics

| Types | Exps | Measurements |
|---|--------------------------------|--|
| MBL Reactor | RENO, Daya Bay Double Chooz | $4 U_{e3} ^2(U_{e1} ^2 + U_{e2} ^2)$ |
| LBL Reactor | KamLAND | $4 U_{e1} ^2 U_{e2} ^2$ |
| Solar | SNO | $ U_{e2} ^2$ |
| LBL Accelerator $(\nu_\mu \rightarrow \nu_\mu)$ | NOvA, T2K | $4 U_{\mu 3} ^2(U_{\mu 1} ^2 + U_{\mu 2} ^2)$ |
| LBL Accelerator $(\nu_\mu \rightarrow \nu_e)$ | NOvA, T2K | $4\Re[U_{e3}U_{\mu 3}^*(U_{e1}U_{\mu 1}^* + U_{e2}U_{\mu 2}^*)]$ |
| LBL Accelerator $(\nu_\mu \rightarrow \nu_\tau)$ | OPERA | $4\Re[U_{\tau 3}U_{\mu 3}^*(U_{\tau 1}U_{\mu 1}^* + U_{\tau 2}U_{\mu 2}^*)]$ |

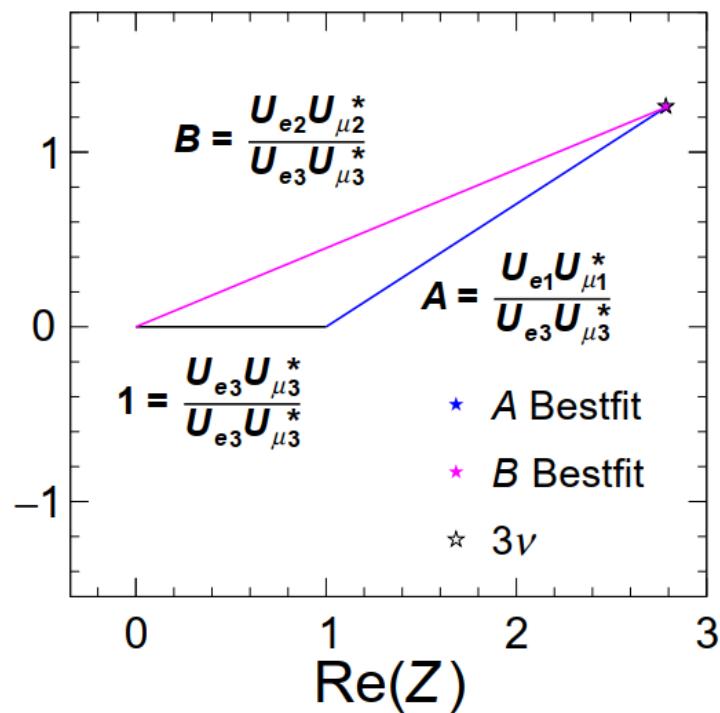
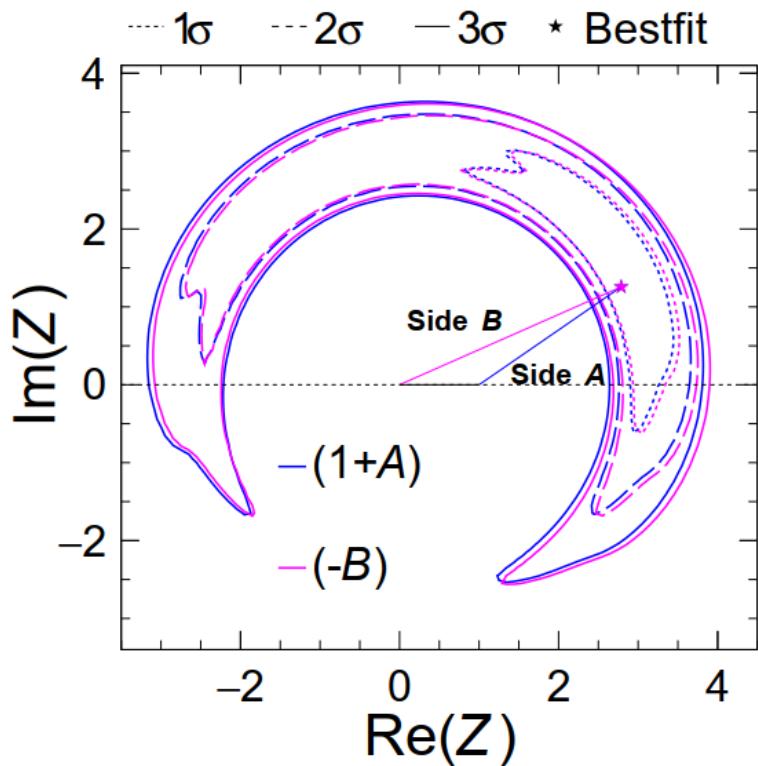
Unitarity Triangle

Matrix Orthogonal Test

$$U_{e1}U_{\mu 1}^* + U_{e2}U_{\mu 2}^* + U_{e3}U_{\mu 3}^* = 0$$

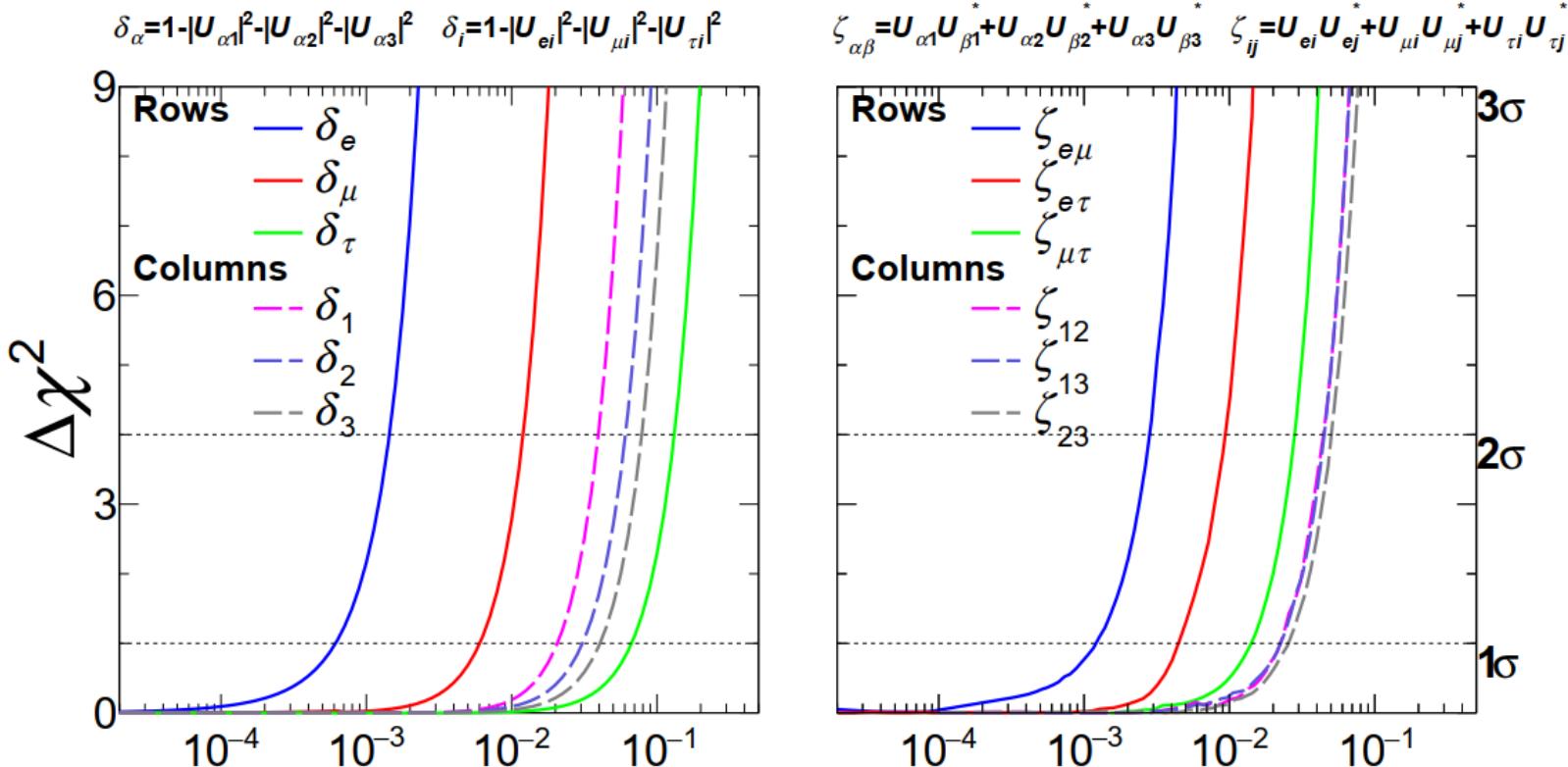
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$$\frac{U_{e1}U_{\mu 1}^*}{U_{e3}U_{\mu 3}^*} + \frac{U_{e2}U_{\mu 2}^*}{U_{e3}U_{\mu 3}^*} + 1 = 0$$



Unitarity Test

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- Electron-type neutrinos have the best unitarity constraints due to large data sample
- Tau-type neutrinos are very limited by the experimental data



Summary

- Daya Bay has made the most precise measurements on $\sin^2 2\theta_{13}$ and $|\Delta m_{32}^2|$ with 2.8% and 2.3% precision
- Daya Bay set the most stringent upper limit for light sterile neutrino with $\Delta m_{41}^2 < 0.2 \text{ eV}^2$
 - A joint fit with MINOS/MINOS+ is able to exclude most of LSND/MiniBooNE signal region
- JUNO can measure NMO with 3σ sensitivity with 6 years
 - boost to $>5\sigma$ with accelerator experiments