

Explanation of W boson mass anomaly and flavor physics in a model with extra U(1) gauge symmetry

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Based on K.Nagao, TN, H.Okada, arXiv: 2206.15256

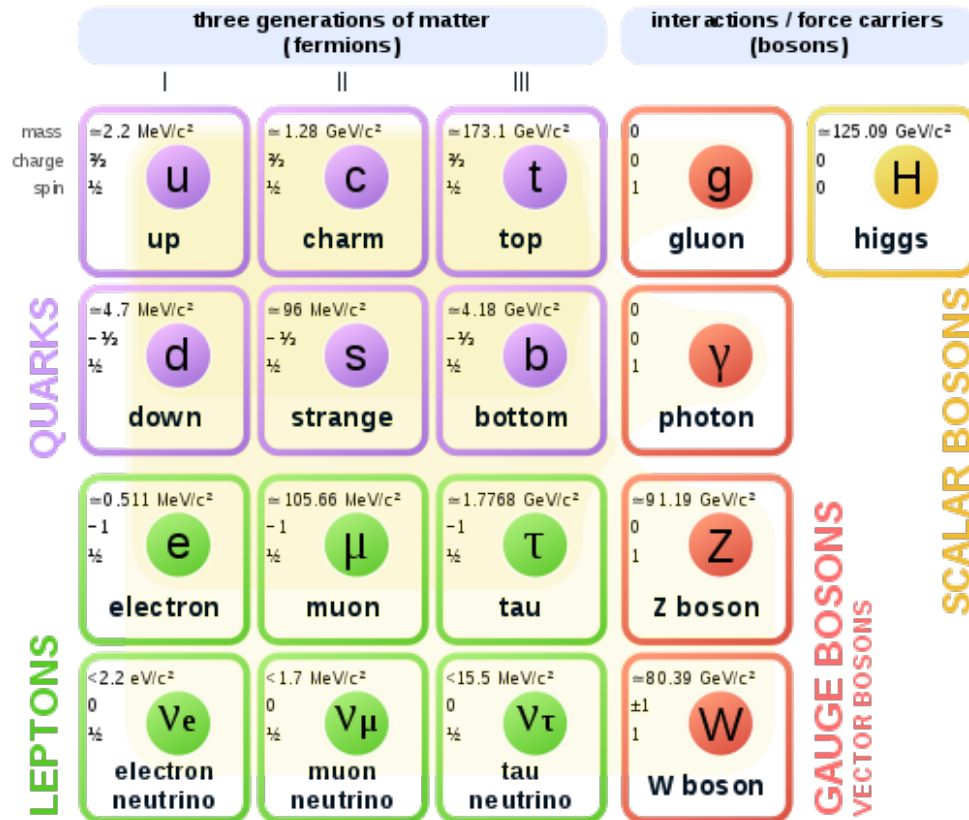
Out line of the talk

- 1. Introduction**
- 2. A model with leoptophobic $U(1)$**
- 3. Phenomenology of the model**
- 4. Summary**

1. Introduction

The standard model (SM) of particle physics is successful

Standard Model of Elementary Particles



The SM is based on gauge symmetry $SU(3)_c \times SU(2)_L \times U(1)_Y$

However there should be beyond the SM (BSM) physics

1. Introduction

There are some experimental anomalies that can be hints of new physics

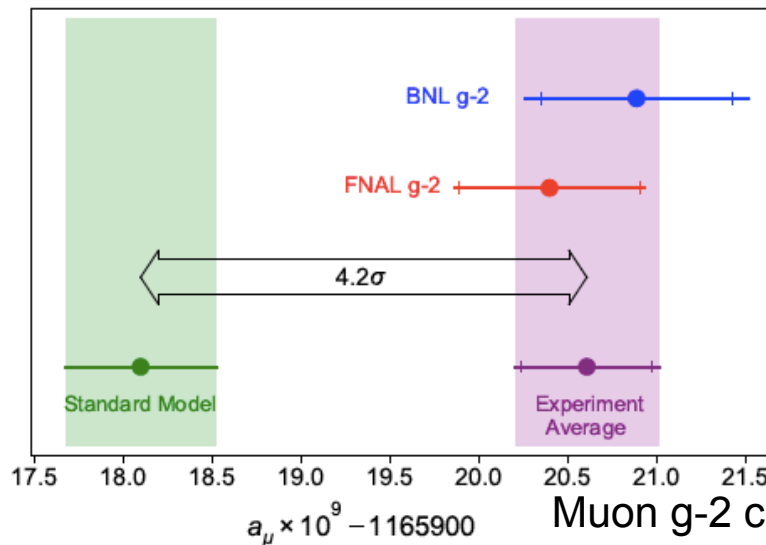
CDF II W boson mass

$$m_W = (80.433 \pm 0.0064_{\text{stat}} \pm 0.0069_{\text{syst}}) \text{ GeV} \quad (\text{CDFII collaboration, 2022})$$

SM prediction: $80.357 \pm 0.006 \text{ GeV}$ (PDG)

CDF II W boson mass is deviated from the SM prediction by 7σ

Muon anomalous dipole magnetic moment (muon g-2)



$$a_\mu^{BNL} = (11659208.9 \pm 5.4 \pm 3.3) \times 10^{-10}$$

$$a_\mu^{FNAL} = (11659204.0 \pm 5.1 \pm 1.9) \times 10^{-10}$$

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (25.1 \pm 5.9) \times 10^{-10}$$

Combined result (4.2σ deviation)

Muon g-2 collaboration, PRL126 (2021)

They can be explained by extending the SM

1. Introduction

One simple extension of the SM

⇒ A model with extra $U(1)$ gauge symmetry

◆ The SM is based on gauge symmetry

⇒ The BSM would be also described by gauge symmetry

◆ It restricts interactions :

good for **phenomenological model building**

- Controlling interactions by symmetry
- It provide new neutral gauge boson: **Z' boson**
- $U(1)$ breaking scalar VEV \rightarrow Higgs physics
- Explaining experimental anomalies: **muon $g-2$, W boson mass**
- Etc.

1. Introduction

An extra U(1) would appear from higher scale

◆ From grand unified theory (GUT)

$$SO(10) \supset SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \supset SU(3) \times SU(2)_L \times U(1)_R \times U(1)_{B-L}$$

$$E_6 \supset SO(10) \times U(1)_\psi \supset SU(5) \times U(1)_\psi \times U(1)_\chi$$

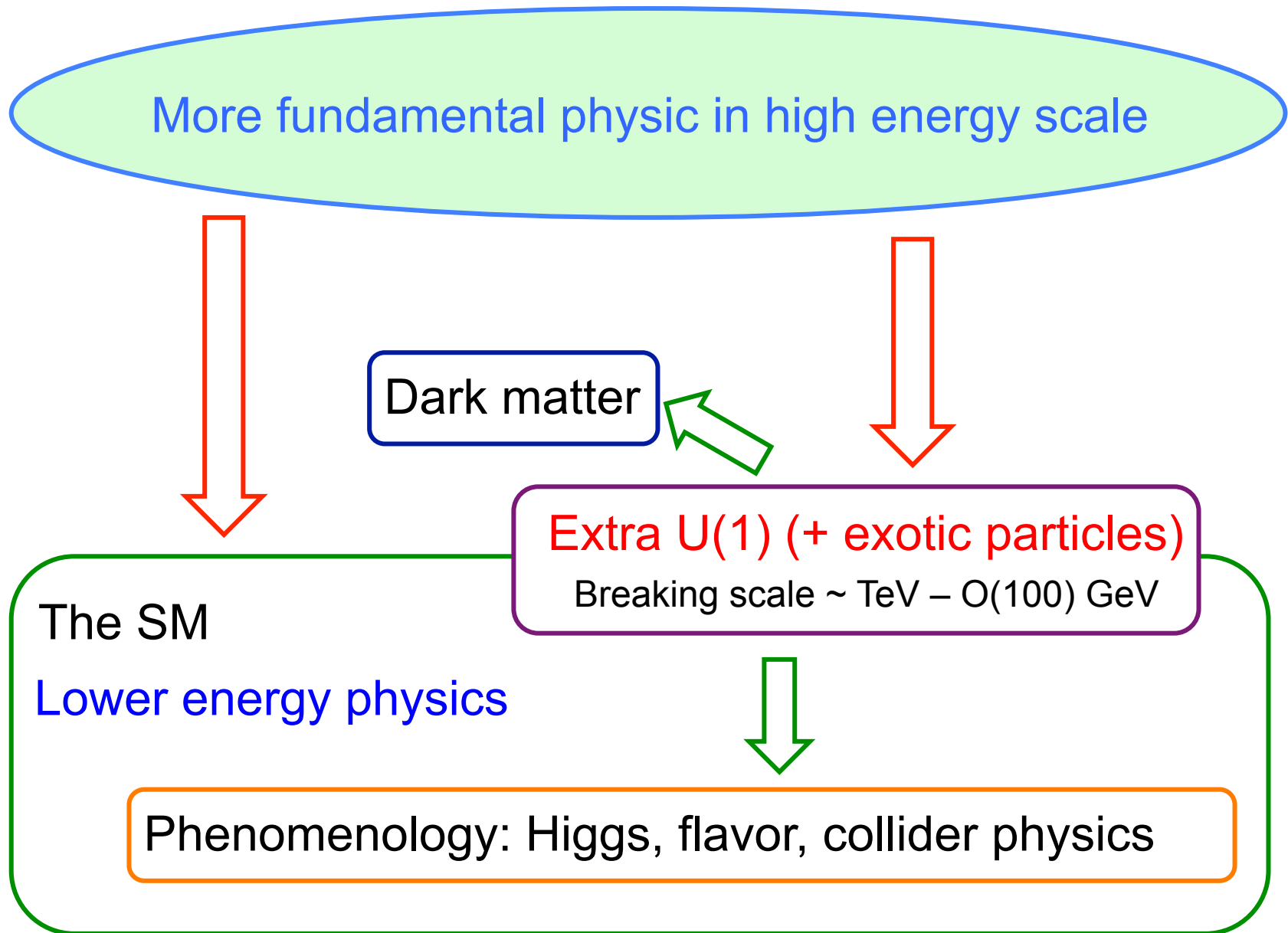
◆ From other gauge extended theories

◆ From string theory

◆ Etc.

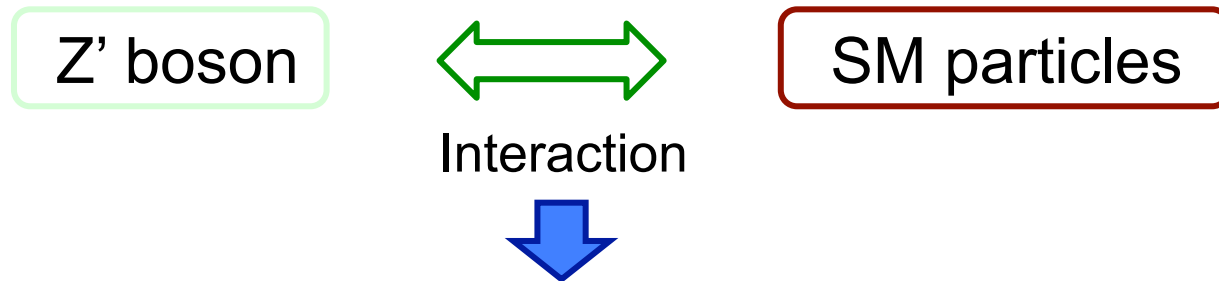
In ~TeV scale we may just see the SM + extra U(1) gauge symmetry

1. Introduction



1. Introduction

Phenomenology of a new model: Z'



Experimentally tested and models should satisfy constraints

Models can be excluded/confirmed in future experiments

□ For heavy Z' case (TeV scale or higher)

- Direct test at collider experiments: LHC, CEPC, ILC, etc.
- Indirect test by scattering process:
- Constraint from flavor physics: e.g. flavor dependent Z'

□ For light Z' case (less than GeV scale)

- It can be tested by low energy experiments
- Direct production at lower energy collider: like Belle II experiment etc.

1. Introduction

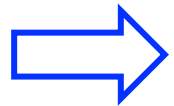
Phenomenology a new model: exotic signals

In a model we often have exotic particles



Some exotic signatures can be induced

For example, to explain muon $g-2$ we may need lepton flavor dependent interactions



Flavor violating signal can be induced

Tera-Z factory at CEPC is good opportunity to test such signal
If flavor violation affect Z-interactions (10^{12} Z production)

In this talk, I would like to show such an example

Out line of the talk

1. Introduction
2. A model with leoptophobic $U(1)$
3. Phenomenology of the model
4. Summary

2. A model with leptophobic U(1)

Structure of the model

(K.Nagao, TN, H.Okada, arXiv: 2206.15256)

	Q_L^a	u_R^a	d_R^a	L_L^a	e_R^a	N_R^a	N_L^a	E_L^a	E_R^a	H	φ_1	φ_2
$SU(3)_C$	3	3	3	1	1	1	1	1	1	1	1	1
$SU(2)_L$	2	1	1	2	1	1	1	1	1	2	1	1
$U(1)_Y$	$\frac{1}{6}$	$\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{1}{2}$	-1	0	0	-1	-1	$\frac{1}{2}$	0	0
$U(1)_R$	0	1	-1	0	0	1	0	0	-1	1	-1	$-\frac{1}{2}$

New fermions

New scalars

- ❖ Gauge anomalies are canceled between the SM fermion and new ones
- ❖ Gauge symmetry is broken by scalar VEVs
- ❖ SM leptons are not charged under new U(1)
- ❖ We don't have Yukawa interaction $\bar{L}_L e_R H$

2. A model with leptophobic U(1)

Lagrangian of the model

$$-\mathcal{L}_Y = (y_\ell)_{ab} \bar{L}_L^a H E_R^b + (y_E)_{aa} \varphi_1 \bar{E}_L^a E_R^a + (m_{Ee})_{ab} \bar{E}_L^a e_R^b \\ + (y_D)_{ab} \bar{L}_L^a \tilde{H} N_R^b + (y_N)_{aa} \varphi_1 \bar{N}_L^a N_R^a + (M_{N_L})_{ab} \bar{N}_L^a N_L^{cb} + \text{h.c.},$$

$$\mathcal{V} = \mu_1^2 |\varphi_1|^2 - \mu_2^2 |\varphi_2|^2 - \mu_H^2 |H|^2 + \lambda_H |H|^4 + \lambda_1 |\varphi_1|^4 + \lambda_2 |\varphi_2|^4 - \mu_3 (\varphi_1^* \varphi_2 \varphi_2 + \text{h.c.}) \\ + \lambda_3 |\varphi_1|^2 |H|^2 + \lambda_4 |\varphi_2|^2 |H|^2 + \lambda_5 |\varphi_1|^2 |\varphi_2|^2.$$

Scalar fields

$$H = \begin{bmatrix} w^+ \\ \frac{v+r+iz}{\sqrt{2}} \end{bmatrix}, \quad \varphi_{1,2} = \frac{v'_{1,2} + r'_{1,2} + iz'_{1,2}}{\sqrt{2}},$$

- Neutral scalar can mix: we consider r - r'_1 mixing
- We take mixing angle θ to be free parameter
- SM Higgs mass: m_h , heavy Higgs mass m_H

$$(r, r'_1)^T = O_R(h, H)^T,$$

$$, O_R = \begin{bmatrix} c_\theta & s_\theta \\ -s_\theta & c_\theta \end{bmatrix}$$

2. A model with leptophobic U(1)

Neutral gauge boson mass

New U(1) and electroweak symmetry breaking by scalar VEVs



Z-Z' mass matrix after symmetry breaking

$$m_{Z_{SM}Z'}^2 \simeq \frac{1}{4} \begin{bmatrix} (g_1^2 + g_2^2)v^2 & -2\sqrt{g_1^2 + g_2^2}g'v^2 \\ -2\sqrt{g_1^2 + g_2^2}g'v^2 & 4g'^2(v^2 + v_2'^2) \end{bmatrix} = m_{Z'}^2 \begin{bmatrix} \epsilon_1^2 & -\epsilon_1\epsilon_2 \\ -\epsilon_1\epsilon_2 & 1 + \epsilon_2^2 \end{bmatrix}$$



Diagonalization: $V m_{Z_{SM}Z'}^2 V^T \equiv \text{Diag}(m_Z^2, m_{Z_R}^2)$

$$m_Z^2 \approx m_{Z_{SM}}^2 (1 - \epsilon_2^2), \quad m_{Z_R}^2 \approx m_{Z'}^2 (1 + \epsilon_1^2 \epsilon_2^2),$$

$$V \approx \begin{bmatrix} c_Z & s_Z \\ -s_Z & c_Z \end{bmatrix}, \quad \theta_Z = \frac{1}{2} \tan^{-1} \left[\frac{2\epsilon_1\epsilon_2}{1 + \epsilon_2^2 - \epsilon_1^2} \right].$$

2. A model with leptophobic U(1)

Charged lepton mass

$$\begin{pmatrix} \bar{e}_L \\ \bar{E}_L \end{pmatrix}^T \mathcal{M}_\varepsilon \begin{pmatrix} e_R \\ E_R \end{pmatrix} = \begin{pmatrix} \bar{e}_L \\ \bar{E}_L \end{pmatrix}^T \begin{bmatrix} 0 & m_{eE} \\ m_{Ee} & M_E \end{bmatrix} \begin{pmatrix} e_R \\ E_R \end{pmatrix},$$
$$\mathcal{M}_\varepsilon \mathcal{M}_\varepsilon^\dagger = \begin{bmatrix} m_{eE} m_{eE}^\dagger & m_{eE} M_E \\ M_E m_{eE}^\dagger & M_E^2 + m_{Ee} m_{Ee}^\dagger \end{bmatrix}, \quad \mathcal{M}_\varepsilon^\dagger \mathcal{M}_\varepsilon = \begin{bmatrix} m_{Ee}^\dagger m_{Ee} & m_{Ee}^\dagger M_E \\ M_E m_{Ee} & M_E^2 + m_{eE}^\dagger m_{eE} \end{bmatrix}$$

$$m_{eE} \equiv y_\ell v / \sqrt{2}, \quad M_E \equiv y_E v' / \sqrt{2}.$$

SM charged lepton masses are obtained by diagonalizing the mass matrix

$$\Rightarrow (e_{L(R)}, E_{L(R)}) \rightarrow \underline{V_{L(R)}} \ell_{L(R)}$$

Unitary matrix

The mixing between lepton and heavy lepton modifies gauge interaction

2. A model with leptophobic U(1)

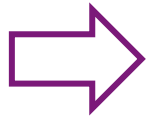
Modification of Z-lepton interactions

Due to lepton mixing, we obtain

$$\frac{g_2}{c_W} \left[\left(-\frac{1}{2} \sum_{a=1}^3 V_{L_{ia}}^\dagger V_{L_{aj}} + s_W^2 \delta_{ij} \right) \bar{\ell}_{L_i} \gamma^\mu \ell_{L_j} + s_W^2 \delta_{ij} \bar{\ell}_{R_i} \gamma^\mu \ell_{R_j} \right] Z_\mu$$

Z-interaction associated with left-handed charged lepton is modified

Note: we have flavor violating interaction (lepton FCNC)



Lepton flavor violating Z boson decay

It would be tested by Z-factory : Tera-Z/CEPC

2. A model with leptophobic U(1)

Neutrino mass in the model

In our model neutrino mass can be obtained via Yukawa terms

$$(y_D)_{ab} \bar{L}_L^a \tilde{H} N_R^b + (y_N)_{aa} \varphi_1 \bar{N}_L^a N_R^a + (M_{N_L})_{ab} \bar{N}_L^a N_L^{cb} + \text{h.c.}$$



After spontaneous symmetry breaking, mass matrix is induced

$$M_N = \begin{bmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M \\ 0 & M & M_{N_L} \end{bmatrix}$$

In the basis of (ν_L^c, N_R, N_L^c)

$$m_D \equiv v y_D / \sqrt{2} \text{ and } M \equiv y_N v'_1 / \sqrt{2}.$$



$$m_\nu \simeq m_D M^{-1} M_{N_L} (M^T)^{-1} m_D^T.$$

Inverse seesaw mechanism is realized

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3. Phenomenology of the model

Explanation of W mass anomaly by Z-Z' mixing

Z-Z' mixing modify relation between Z and W masses

⇒ Shift of T parameter

It can be interpreted as shift of W boson mass



CDF II W boson mass can be fitted

Here we consider fitting in terms of T parameter:

$$0.09 \leq \Delta T \leq 0.14.$$

The range of new physics contribution to T for fitting data including CDF II

3. Phenomenology of the model

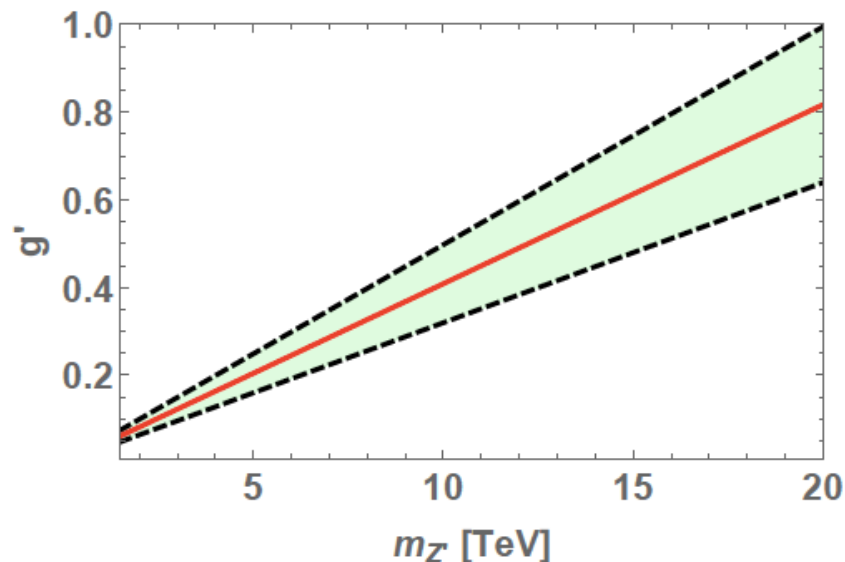
Explanation of W mass anomaly by Z-Z' mixing

We obtain modification of T-parameter

$$\Delta T = \frac{1}{\alpha_{\text{em}}} \frac{m_{Z_{SM}}^2 - m_Z^2}{m_{Z_{SM}}^2} \simeq \frac{\epsilon_2^2}{\alpha_{\text{em}}}, \quad \Rightarrow \quad \Delta T \simeq \frac{v^2}{\alpha_{\text{em}}} \frac{g'^2}{m_{Z'}^2} = \frac{4m_W^2}{g_2^2 \alpha_{\text{em}}} \frac{g'^2}{m_{Z'}^2}$$

To resolve W boson mass anomaly

$$0.09 \leq \Delta T \leq 0.14. \quad \Rightarrow \quad 20 \text{ TeV} \lesssim \frac{m_{Z'}}{g'} (= v_2') \lesssim 31 \text{ TeV}$$



3. Phenomenology of the model

Constraints from $Z \rightarrow \ell\bar{\ell}$ decay

Mixing between lepton and heavy lepton modify Z interaction

$$\frac{g_2}{c_W} \left[\left(-\frac{1}{2} \sum_{a=1}^3 V_{Lia}^\dagger V_{La_j} + s_W^2 \delta_{ij} \right) \bar{\ell}_{Li} \gamma^\mu \ell_{Lj} + s_W^2 \delta_{ij} \bar{\ell}_{Ri} \gamma^\mu \ell_{Rj} \right] Z_\mu$$

Decay widths of Z to charged lepton pair is

$$\Gamma(Z \rightarrow \ell_i \bar{\ell}_j) \simeq \frac{g_2^2}{24\pi c_W^2} m_Z \left[\left| -\frac{1}{2} \sum_{a=1}^3 V_{Lia}^\dagger V_{La_j} + s_W^2 \delta_{ij} \right|^2 + s_W^4 \delta_{ij} \right]$$

BRs are deviated from the SM

$$\Delta \text{BR}(Z \rightarrow \ell_i \bar{\ell}_j) = \frac{\Gamma(Z \rightarrow \ell_i \bar{\ell}_j) - \Gamma(Z \rightarrow \ell_i \bar{\ell}_j)_{SM}}{\Gamma_Z^{\text{tot}}} \quad \text{for } i = j,$$

$$\text{BR}(Z \rightarrow \ell_i \bar{\ell}_j) = \frac{\Gamma(Z \rightarrow \ell_i \bar{\ell}_j)}{\Gamma_Z^{\text{tot}}} \quad \text{for } i \neq j,$$

LFV Z decay

3. Phenomenology of the model

Muon g-2 and LFV processes

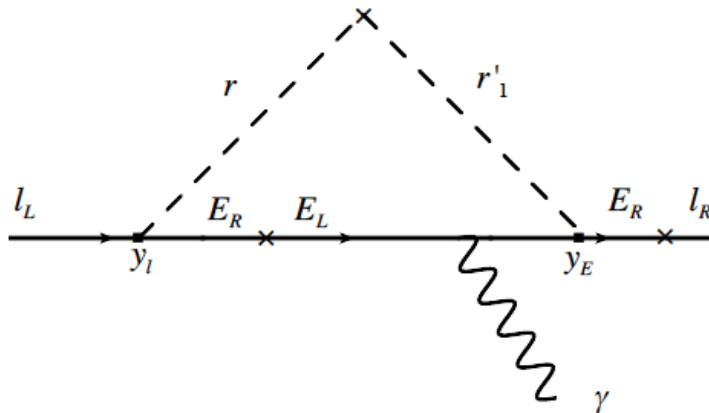
Relevant Lagrangian in mass basis

$$\mathcal{L}_{LFV} = (Y_{\alpha\beta}c_\theta - \tilde{Y}_{\alpha\beta}s_\theta)h\bar{\ell}_\alpha P_R \ell_\beta + (Y_{\alpha\beta}s_\theta + \tilde{Y}_{\alpha\beta}c_\theta)H\bar{\ell}_\alpha P_R \ell_\beta + h.c.,$$

$$Y_{\alpha\beta} \equiv \frac{1}{\sqrt{2}} \sum_{a=1,2,3} \sum_{b=1,2,3} (V_L^\dagger)_{\alpha,a} (y_\ell)_{ab} (V_R)_{b+3,\beta},$$

$$\tilde{Y}_{\alpha\beta} \equiv \frac{1}{\sqrt{2}} \sum_{a=1,2,3} \sum_{b=1,2,3} (V_L^\dagger)_{\alpha,a+3} (y_E)_{aa} (V_R)_{a+3,\beta}.$$

One-loop diagram inducing muon g-2 and LFVs $l \rightarrow l' \gamma$



Dominant contribution

3. Phenomenology of the model

Muon g-2 and LFV processes

Analytic formula

$$\text{BR}(\ell_\beta \rightarrow \ell_\alpha \gamma) \simeq \frac{12\pi^2 C_{\beta\alpha}}{(4\pi)^4 m_{\ell_\beta}^2 G_F^2} (|a_{L_{\alpha\beta}}|^2 + |a_{R_{\alpha\beta}}|^2),$$

$$\Delta a_\mu \simeq -\frac{m_\mu}{(4\pi)^2} (a_{L_{22}} + a_{R_{22}}),$$

$$a_{L_{\alpha\beta}} \approx -\frac{1}{4} (Y_{\alpha\rho}^\dagger c_\theta - \tilde{Y}_{\alpha\rho}^\dagger s_\theta) D_{E_\rho} (Y_{\rho\beta}^\dagger c_\theta - \tilde{Y}_{\rho\beta}^\dagger s_\theta) F(h_1, D_{E_\rho}) \\ - \frac{1}{4} (Y_{\alpha\rho}^\dagger s_\theta + \tilde{Y}_{\alpha\rho}^\dagger c_\theta) D_{E_\rho} (Y_{\rho\beta}^\dagger s_\theta + \tilde{Y}_{\rho\beta}^\dagger c_\theta) F(h_2, D_{E_\rho}),$$

$$a_{R_{\alpha\beta}} \approx -\frac{1}{4} (Y_{\alpha\rho} c_\theta - \tilde{Y}_{\alpha\rho} s_\theta) D_{E_\rho} (Y_{\rho\beta} c_\theta - \tilde{Y}_{\rho\beta} s_\theta) F(h_1, D_{E_\rho}) \\ - \frac{1}{4} (Y_{\alpha\rho} s_\theta + \tilde{Y}_{\alpha\rho} c_\theta) D_{E_\rho} (Y_{\rho\beta} s_\theta + \tilde{Y}_{\rho\beta} c_\theta) F(h_2, D_{E_\rho}),$$

$$F(m_{h_i}, D_{E_\rho}) \approx \frac{m_{h_i}^4 - 4m_{h_i}^2 D_{E_\rho}^2 + 3D_{E_\rho}^4 - 2m_{h_i}^2 (m_{h_i}^2 - 2D_{E_\rho}^2) \ln \left[\frac{m_{h_i}^2}{D_{E_\rho}^2} \right]}{(m_{h_i}^2 - D_{E_\rho}^2)^3},$$

$$C_{21} \approx 1, C_{31} \approx 0.1784, C_{32} \approx 0.1736, h_1 \equiv h, h_2 \equiv H$$

3. Phenomenology of the model

Numerical analysis

Free parameters: $\{(y_\ell)_{ab}, (y_E)_{aa}, (m_{Ee})_{ab}, \sin \theta, m_H\}$



Searching solution to explain muon g-2

Constraints:

$$\text{BR}(\mu \rightarrow e\gamma) \leq 4.2 \times 10^{-13}, \quad \text{BR}(\tau \rightarrow \mu\gamma) \leq 4.4 \times 10^{-8}, \quad \text{BR}(\tau \rightarrow e\gamma) \leq 3.3 \times 10^{-8}$$

$$\Delta\text{BR}(Z \rightarrow e^\pm e^\mp) < \pm 4.2 \times 10^{-5}, \quad \Delta\text{BR}(Z \rightarrow \mu^\pm \mu^\mp) < \pm 6.6 \times 10^{-5},$$

$$\Delta\text{BR}(Z \rightarrow \tau^\pm \tau^\mp) < \pm 8.3 \times 10^{-5}, \quad \text{BR}(Z \rightarrow e^\pm \mu^\mp) < 7.5 \times 10^{-7},$$

$$\text{BR}(Z \rightarrow e^\pm \tau^\mp) < 9.8 \times 10^{-6}, \quad \text{BR}(Z \rightarrow \mu^\pm \tau^\mp) < 1.2 \times 10^{-5}.$$

3. Phenomenology of the model

Benchmark point

Input	
v'_1/GeV	284
m_H/GeV	245
$\sin \theta$	0.250
$[(y_\ell)_{11}, (y_\ell)_{12}, (y_\ell)_{13}]$	$[-0.000512, 0.00520, 0.00236]$
$[(y_\ell)_{21}, (y_\ell)_{22}, (y_\ell)_{23}]$	$[-0.000105, 0.000624, 0.0643]$
$[(y_\ell)_{31}, (y_\ell)_{32}, (y_\ell)_{33}]$	$[0.000148, 0.0145, 0.0647]$
$[(m_{eE})_{11}, (m_{eE})_{12}, (m_{eE})_{13}]/\text{GeV}$	$[0.674, 16.8, 5.92]$
$[(m_{eE})_{21}, (m_{eE})_{22}, (m_{eE})_{23}]/\text{GeV}$	$[-16.2, -46.3, 22.3]$
$[(m_{eE})_{31}, (m_{eE})_{32}, (m_{eE})_{33}]/\text{GeV}$	$[-12.2, 69.5, 19.8]$
$[(y_E)_{11}, (y_E)_{22}, (y_E)_{33}]$	$[-3.26, 3.43, -3.41]$

Output	
$[m_{E_1}, m_{E_2}, m_{E_3}]/\text{GeV}$	$[655, 690, 694]$
Δa_μ	2.11×10^{-9}
$\text{BR}(\mu \rightarrow e\gamma)$	3.59×10^{-13}
$\text{BR}(\tau \rightarrow e\gamma)$	9.91×10^{-11}
$\text{BR}(\tau \rightarrow \mu\gamma)$	2.22×10^{-8}
$\Delta\text{BR}(Z \rightarrow e^\pm e^\mp)$	-1.55×10^{-9}
$\Delta\text{BR}(Z \rightarrow \mu^\pm \mu^\mp)$	-6.11×10^{-7}
$\Delta\text{BR}(Z \rightarrow \tau^\pm \tau^\mp)$	-3.82×10^{-5}
$\Delta\text{BR}(Z \rightarrow e^\pm \mu^\mp)$	6.27×10^{-17}
$\Delta\text{BR}(Z \rightarrow e^\pm \tau^\mp)$	3.83×10^{-14}
$\Delta\text{BR}(Z \rightarrow \mu^\pm \tau^\mp)$	3.64×10^{-11}

❖ We can get sizable muon g-2 while satisfying LFV constraints

3. Phenomenology of the model

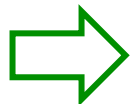
Z' signature at the LHC

$$pp \rightarrow Z' \rightarrow \bar{E}E, jj, NN$$

Extra fermions decays into SM fermion + Higgs boson

$$\begin{aligned} E_a &\rightarrow \ell_i h, \\ N_a &\rightarrow \nu_i h, \nu_i Z, \ell_i W, \end{aligned} \quad \Gamma(Z' \rightarrow f\bar{f}) = \frac{g'^2 N_c}{12\pi} m_{Z'} \sqrt{1 - \frac{4m_f^2}{m_{Z'}^2}} \left(1 - \frac{m_f^2}{m_{Z'}^2}\right)$$

Signal of Z' at collider experiments:

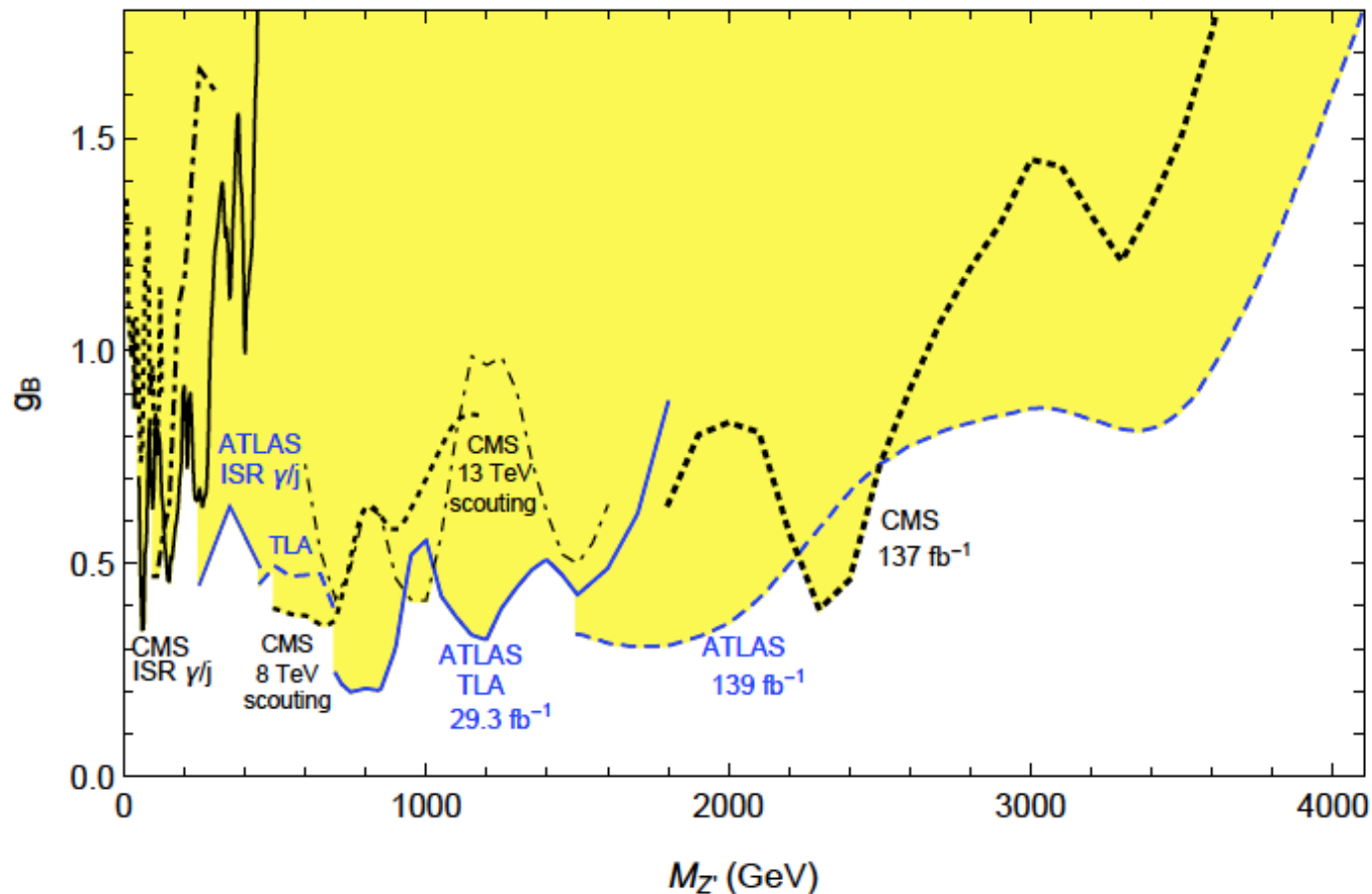


Dijet, lepton+Higgs, lepton+W, Z/h + missing energy

3. Phenomenology of the model

Current constraints (from dijet mode)

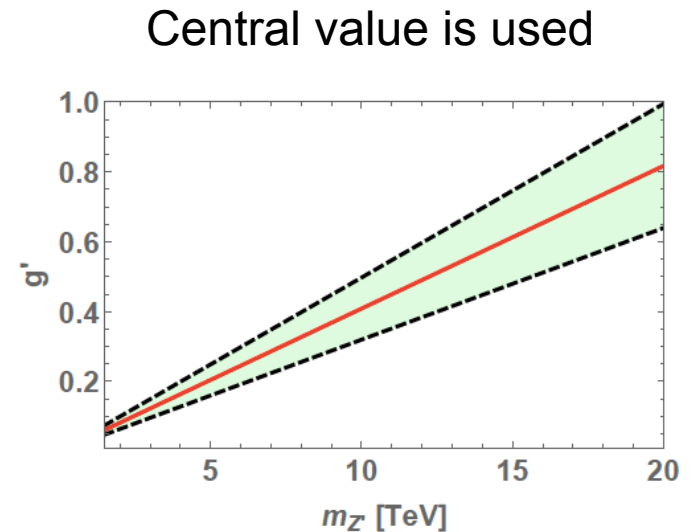
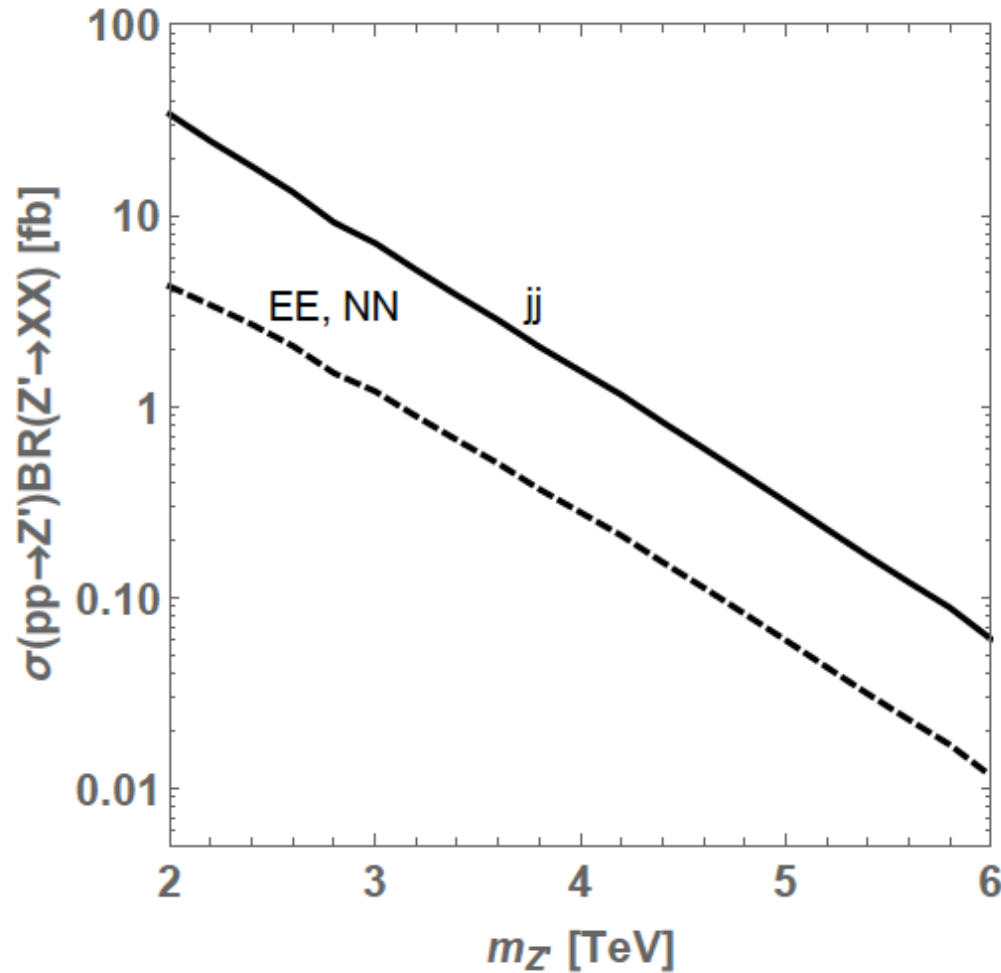
(Taken from B.A.Dobrescu, F.Yu, arXiv: 2112.05392)



Our gauge coupling explaining W boson mass anomaly is below the constraint

3. Phenomenology of the model

Cross sections for Z' signature at the LHC 14 TeV



✓ Gauge coupling is chosen to get best fit value of ΔT for W mass anomaly

3. Phenomenology of the model

Modification of leptonic Z boson decay

Predictions in our benchmark point

$\Delta\text{BR}(Z \rightarrow e^\pm e^\mp)$	-1.55×10^{-9}
$\Delta\text{BR}(Z \rightarrow \mu^\pm \mu^\mp)$	-6.11×10^{-7}
$\Delta\text{BR}(Z \rightarrow \tau^\pm \tau^\mp)$	-3.82×10^{-5}
$\Delta\text{BR}(Z \rightarrow e^\pm \mu^\mp)$	6.27×10^{-17}
$\Delta\text{BR}(Z \rightarrow e^\pm \tau^\mp)$	3.83×10^{-14}
$\Delta\text{BR}(Z \rightarrow \mu^\pm \tau^\mp)$	3.64×10^{-11}

Prospect of sensitivity at tera-Z factory of CEPC (10^{12} Z)

$$\text{BR}(Z \rightarrow \mu e)_{\text{CEPC}} \lesssim 3 \times 10^{-9} \text{ [1}/\sqrt{N} \text{ scaling]}, 7 \times 10^{-12} \text{ [1}/N \text{ scaling]},$$

$$\text{BR}(Z \rightarrow \tau e)_{\text{CEPC}} \lesssim 2 \times 10^{-8} \text{ [1}/\sqrt{N} \text{ scaling]}, 4 \times 10^{-11} \text{ [1}/N \text{ scaling]},$$

$$\text{BR}(Z \rightarrow \tau \mu)_{\text{CEPC}} \lesssim 2 \times 10^{-8} \text{ [1}/\sqrt{N} \text{ scaling]}, 5 \times 10^{-11} \text{ [1}/N \text{ scaling]},$$

(CEPC-CDR vol.2)

It would be possible to test $\tau\mu$ mode at tera-Z/CEPC

Also precision measurement of $\tau^+\tau^-$ could find a deviation

Summary

Extension of the SM with extra $U(1)$ gauge symmetry

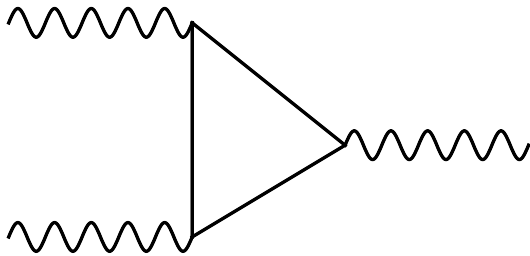
- ✓ Z' boson from extra $U(1)$
- ✓ Z' boson can induce interesting phenomenology
- ✓ Extra $U(1)$ model may explain experimental anomalies

□ A model with leptophobic $U(1)$

- ✓ Explaining muon $g-2$
- ✓ CDF W boson anomaly is also explained
- ✓ LFV and collider physics


Gauge anomaly free conditions

In constructing an extra $U(1)_X$ gauge symmetric model charge assignment of fermion contents should be anomaly free



$$\sum_f \left(\text{Tr}[T_i T_j T_k]_R - \text{Tr}[T_i T_j T_k]_L \right) = 0$$

T_i : generator of gauge group


$$\left\{ \begin{array}{ll} [\text{SU}(3)_c]^2 U(1)_X & [\text{SU}(2)_L]^2 U(1)_X \\ [\text{U}(1)_Y]^2 U(1)_X & [\text{U}(1)_X]^2 U(1)_Y \\ [\text{U}(1)_X]^3 & [\text{gravity}]^2 U(1)_X \end{array} \right.$$

Conditions in addition to the SM gauge anomaly free conditions