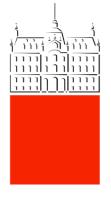
# The 2022 International Workshop on the High Energy Circular Electron Positron Collider

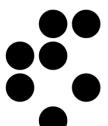
## Theory of Flavour at FCC(-ee)

Jernej F. Kamenik

Main reference: FCC CDR Vol 1. Eur. Phys. J.C 79 (2019) 6, 474 (with updates)



Univerza v Ljubljani



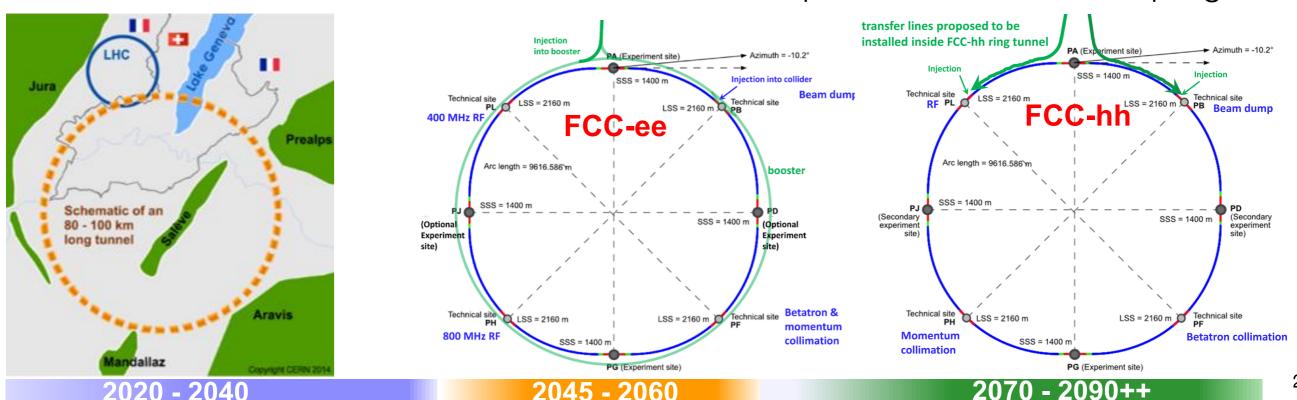
Institut "Jožef Stefan"



## Future Circular Collider integrated program @CERN

see talk by M. Benedikt

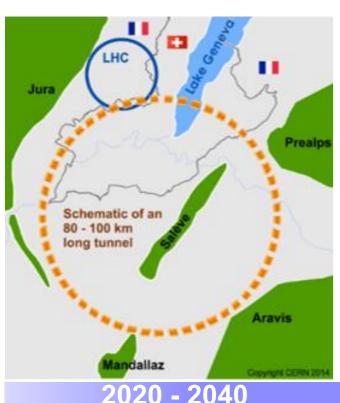
- inspired by successful LEP LHC programs
- population of the second representation of th
  - ►Stage 1: FCC-ee (Z, W, H, tt) as Higgs factory, electroweak & top factory at highest luminosities
  - stage 2: FCC-hh (~100 TeV) as natural continuation at energy frontier, with ion and eh options
- allows seamless continuation of HEP after completion of the HL-LHC program

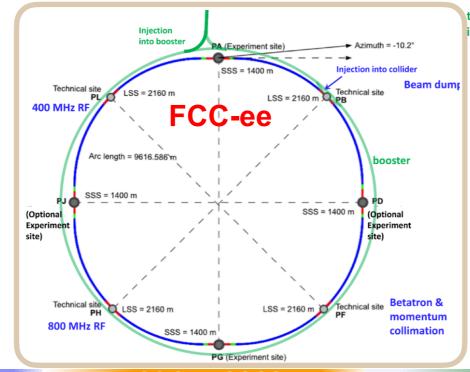


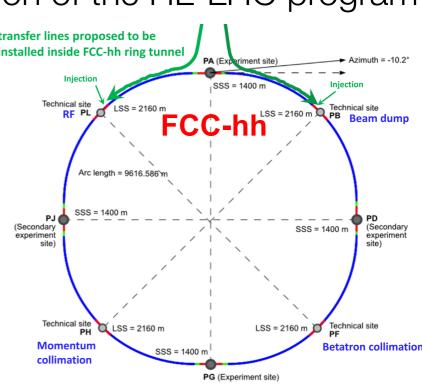
## Future Circular Collider integrated program @CERN

see talk by M. Benedikt

- inspired by successful LEP LHC programs
- page problems in the second street in
  - DEStage 1: FCC-ee (Z, W, H, tt) as Higgs factory, electroweak & top factory at highest luminosities
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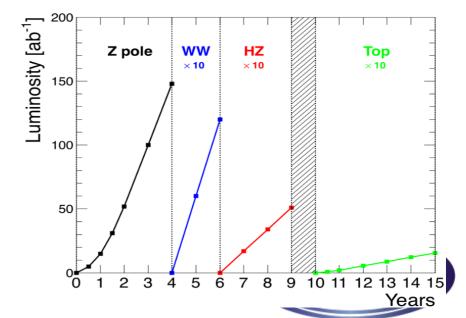
## Scope of Flavour Physics & FCC (-ee)

FCCIS-P1-WP2-D2.1

- Flavour physics reach with O(10<sup>13</sup>) Z decays (10<sup>8</sup> W, 10<sup>6</sup> Higgs, top)
  - rare decays of c- and b-hadrons and CP violation in the heavy-quark sector





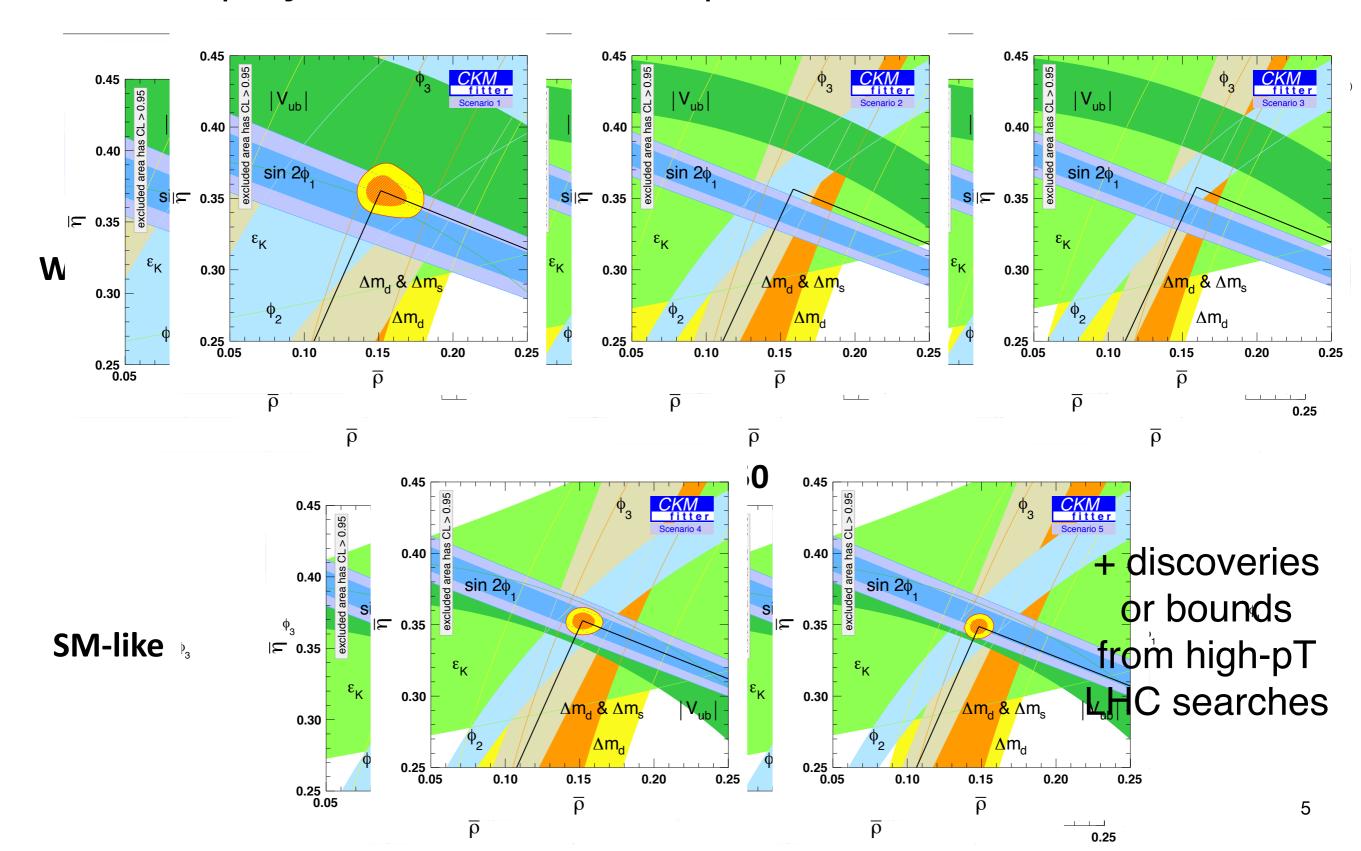


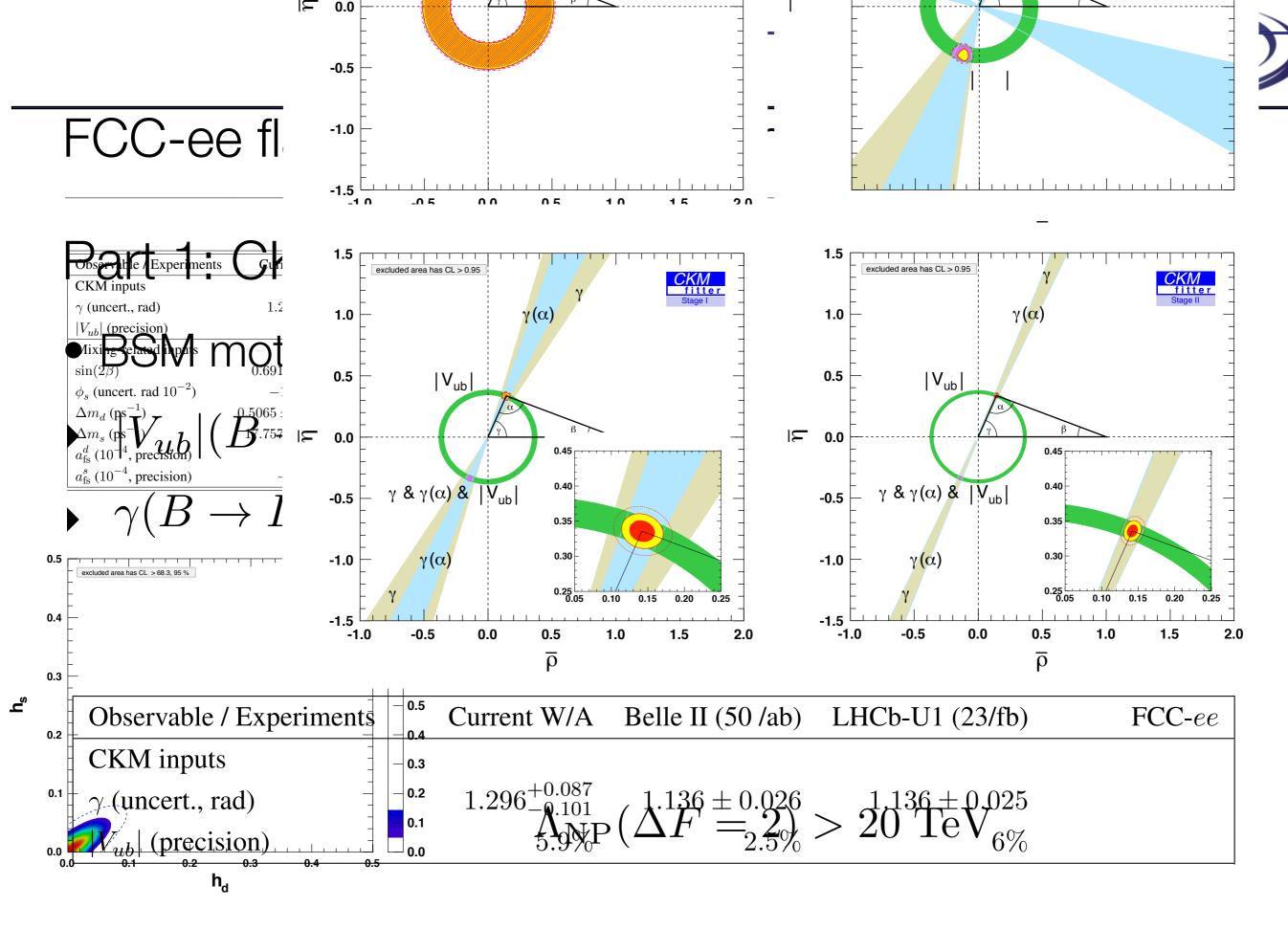
 In the context of ultimate potential of the LHCb upgrade and Belle II experiments.

Working point	Lumi. / IP $[10^{34} \text{ cm}^{-2}.\text{s}^{-1}]$	Total lumi. (2 IPs)	Run time	Physics goal
Z first phase	100	$26 \text{ ab}^{-1} / \text{year}$	2	
Z second phase	200	$52 \text{ ab}^{-1} / \text{year}$	2	$150 \text{ ab}^{-1}$

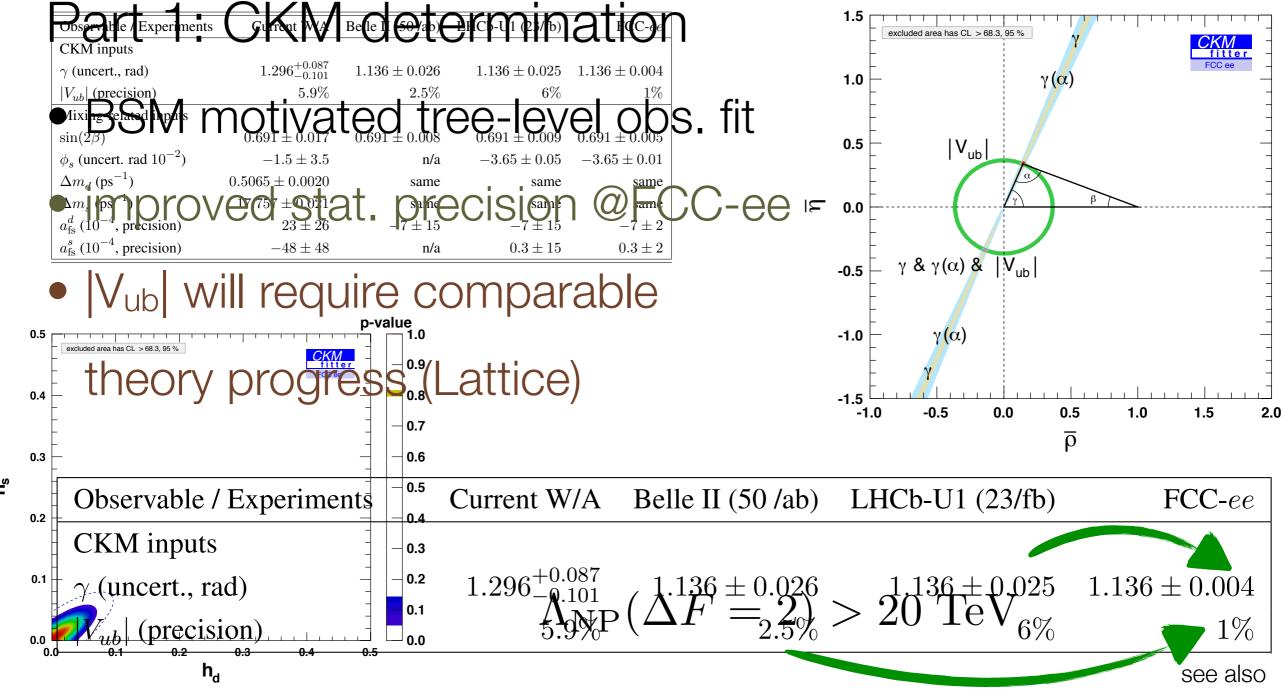
Particle production $(10^9)$	$B^0$	$B^-$	$B_s^0$	$\Lambda_b$	$c\overline{c}$	$\tau^-\tau^+$
Belle II	27.5	27.5	n/a	n/a	65	45
FCC-ee	400	400	100	100	800	220

## Flavor physics circa 2030: possible scenarios



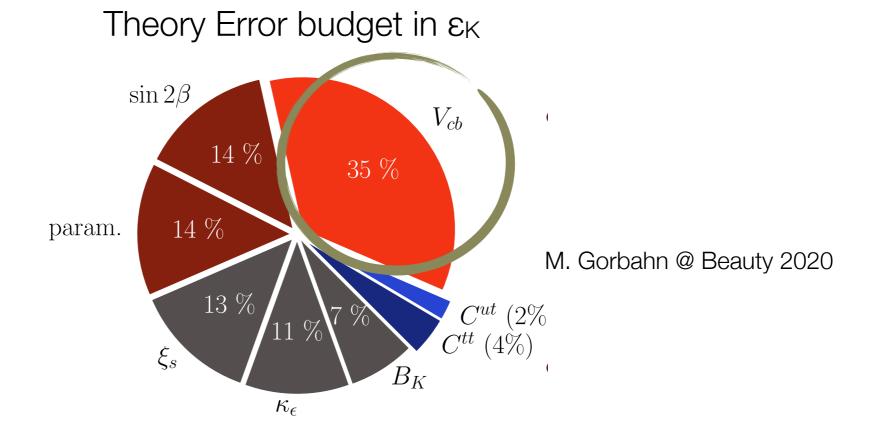






### Part 1: CKM determination

- Complementary measurements of |V<sub>cb</sub>| (and |V<sub>ub</sub>|)
  - CKM fit requires knowledge of |Vub/Vcb|
  - Th. predictions of CPV in K decays rely on |V<sub>cb</sub>|



### Part 1: CKM determination

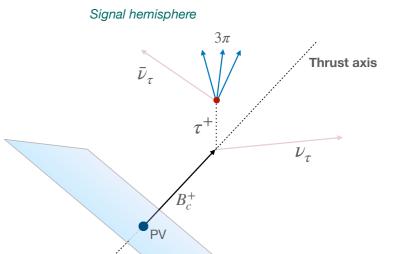
- Complementary measurements of |V<sub>cb</sub>| (and |V<sub>ub</sub>|)
  - ▶ using  $B_{\text{U,C}} \to \mu \nu$ ,  $T \nu$   $Br(B^- \to \tau^- \bar{\nu}(\gamma))_{\text{SM}} = 1.13(1) \times 10^{-4} \left(\frac{f_B}{0.2 \text{GeV}}\right)^2 \left(\frac{|V_{ub}|}{4 \times 10^{-3}}\right)^2$   $\left[\frac{\Gamma(B^+ \to \tau^+ \nu)}{\Gamma(B_c^+ \to \tau^+ \nu)}\right]_{SM^*} = 0.782 \left|\frac{V_{ub} f_B}{V_{cb} f_{B_c}}\right|^2$
  - Theoretically cleaner compared to exclusive semileptonic decays

### Part 1: CKM determination

- Complementary measurements of |V<sub>cb</sub>| (and |V<sub>ub</sub>|)
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  - ► Exp. feasibility studies of B<sub>c</sub>→τν: important normalizing mode

$$\mathcal{B}(B_c^+ \to J/\psi \mu^+ \nu_\mu)$$

relative signal yield precision O(few %)



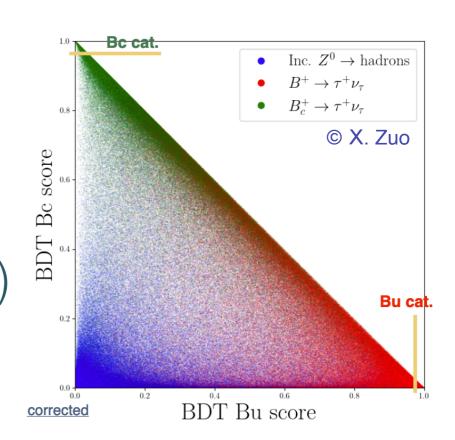
Amhis et al., 2105.13330 Zheng et al., 2007.08234 Plane normal to thrust axis (defines hemispheres)

### Part 1: CKM determination

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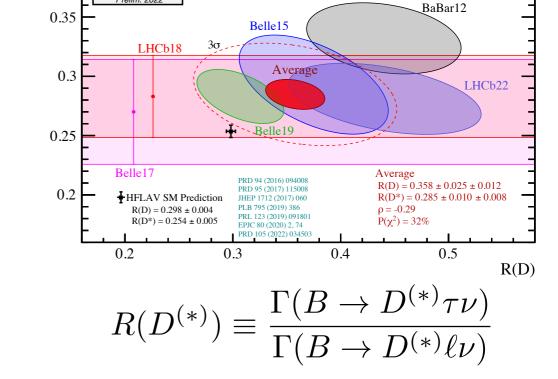
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alternative test of LFU in c.c.

### B decays



see also talk by X. Jiang

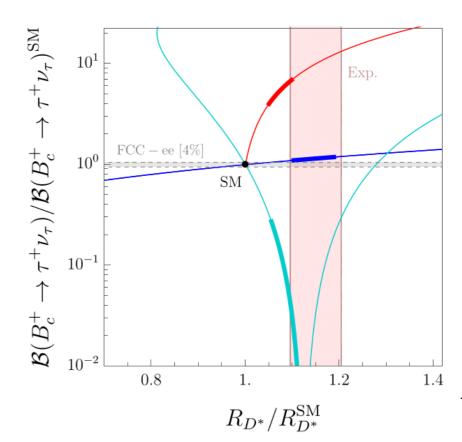
 $\Delta \chi^2 = 1.0$  contours

### Part 1: CKM determination

- Complementary measurements of |V<sub>cb</sub>| (and |V<sub>ub</sub>|)
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alternative test of LFU in c.c.
B decays



### Part 1: CKM determination

- Complementary measurements of  $|V_{cb}|$  (and  $|V_{ub}|$ ) Beyond Z-pole?
  - ▶ using B<sub>u,c</sub>→μν,τν

Wusing on-shell W→cb

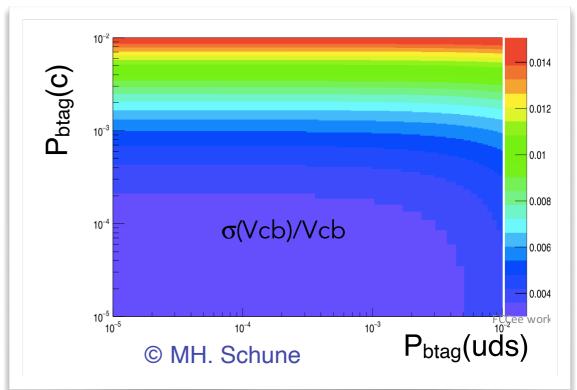
- $\sigma(e^+e^- \to W^+W^-) \sim 10 \mathrm{pb}$  (in energy range of FCC-ee)
- ▶ With SM value of  $\mathcal{B}(W^+ \to c\bar{b}) \sim 10^{-3}$  a precision of  $\delta V_{cb}/V_{cb} \sim 0.1\%$  might be within reach...
- Relies crucially on efficient c- and b-jet identification

see e.g. Tomohiko Tanabe. ILD@ILC. IAS Program on High Energy Physics 2017, HKUST

### Part 1: CKM determination

Beyond 4-pholie? b-jet c-jet uds-jet

Wusing on-shell W→cb



- $\sigma(e^+e^- \to W^+W^-) \sim 10 \mathrm{pb}$  (in energy range of FCC-ee)
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see e.g. Tomohiko Tanabe. ILD@ILC. IAS Program on High Energy Physics 2017, HKUST

### Part 2: CPV in $\Delta B=2$

Observable / Experiments	Current W/A	Belle II (50 /ab)	LHCb-U1 (23/fb)	FCC-ee
Mixing-related inputs				
$\sin(2\beta)$	$0.691 \pm 0.017$	$0.691 \pm 0.008$	$0.691 \pm 0.009$	
$\phi_s$ (uncert. rad $10^{-2}$ )	$-1.5 \pm 3.5$	n/a	$-3.65 \pm 0.05$	
$\Delta m_d  (\mathrm{ps}^{-1})$	$0.5065 \pm 0.0020$	same	same	
$\Delta m_s  (\mathrm{ps}^{-1})$	$17.757 \pm 0.021$	same	same	
$a_{\rm fs}^d$ (10 <sup>-4</sup> , precision)	$23 \pm 26$	$-7 \pm 15$	$-7 \pm 15$	
$a_{\rm fs}^s$ (10 <sup>-4</sup> , precision)	$-48 \pm 48$	n/a	$0.3 \pm 15$	

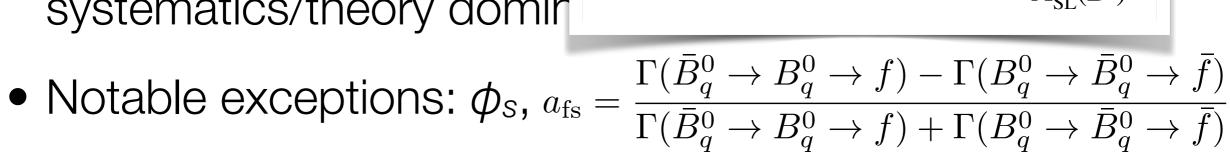
- Uncertainties in most  $\Delta B$ =2 observables will start to be systematics/theory dominated
- Notable exceptions:  $\phi_s$ ,  $a_{fs} = \frac{\Gamma(\bar{B}_q^0 \to B_q^0 \to f) \Gamma(B_q^0 \to \bar{B}_q^0 \to f)}{\Gamma(\bar{B}_q^0 \to B_q^0 \to f) + \Gamma(B_q^0 \to \bar{B}_q^0 \to \bar{f})}$

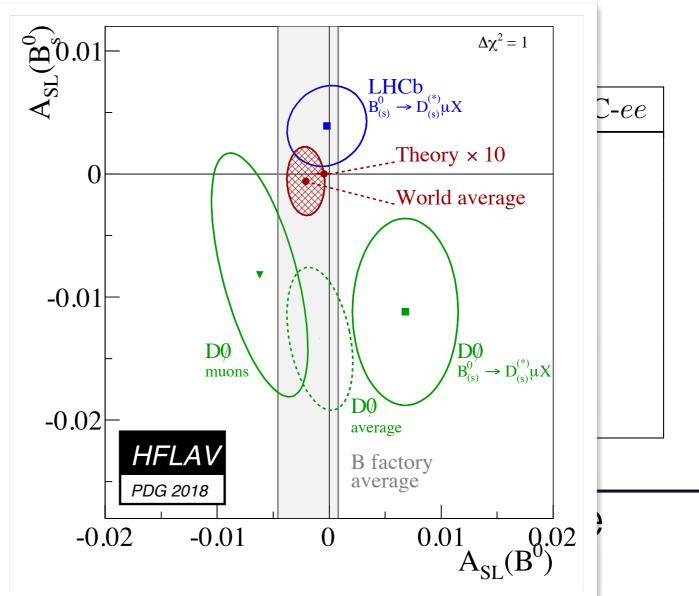
# $F_{a_{\mathrm{fs}}} = F_{a_{\mathrm{fs}}} = F_{a_{\mathrm{fs}$

### Part 2: CPV in $\Delta B=2$

	Observable / Experiments	Current W/A
= -	-Maxing related input $10^{-4}$	,
= +(	$2.22 \pm 0.27 \times 10^{-5} \ \phi_s$ (uncert. rad $10^{-2}$ )	$0.691 \pm 0.017$
' (	$\phi_s$ (uncert. rad $10^{-2}$ )	$-1.5 \pm 3.5$
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### Part 2: CPV in $\Delta B=2$

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Mixing-related inputs				
$\sin(2\beta)$	$0.691 \pm 0.017$	$0.691 \pm 0.008$	$0.691 \pm 0.009$	$0.691 \pm 0.005$
$\phi_s$ (uncert. rad $10^{-2}$ )	$-1.5 \pm 3.5$	n/a	$-3.65 \pm 0.05$	$-3.65 \pm 0.01$
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$a_{\rm fs}^s$ (10 <sup>-4</sup> , precision)	$-48 \pm 48$	n/a	$0.3 \pm 15$	$0.3 \pm 2$

- Significant improvement in both observables @FCC-ee
- Observation of CPV in  $B_d$  mixing possible ( $a_{fs}$ )

S. Monteil @ FCC Flavour WS 2022

• Not included  $(\alpha_s, \gamma_s, \beta_s)$  from  $(B_s \rightarrow D_s K, B \rightarrow DK, B_s \rightarrow \varphi \varphi)$ 

Aleksan, Oliver & Perez, 2107.02002, 2107.0531

competitive precision on γ... theory limit?

Combining 1 & 2: Impact on CPV BSM in  $\Delta B=2$ 

Model-independent parametrization of BSM in  $\Delta F$ =2

$$\langle B_q | \mathcal{H}_{\Delta B=2}^{\text{SM+NP}} | \bar{B}_q \rangle = \langle B_q | \mathcal{H}_{\Delta B=2}^{\text{SM}} | \bar{B}_q \rangle \left( 1 + h_q e^{i\sigma_q} \right)$$

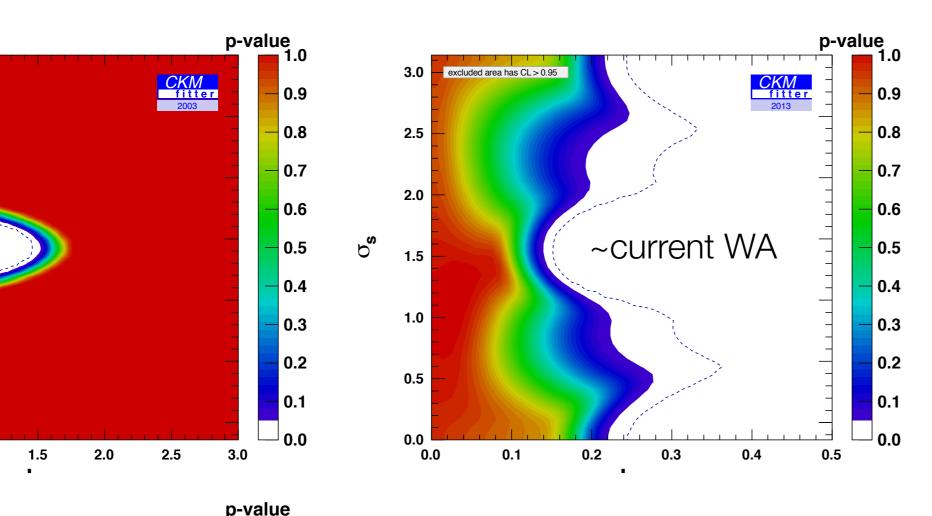
### Assumptions:

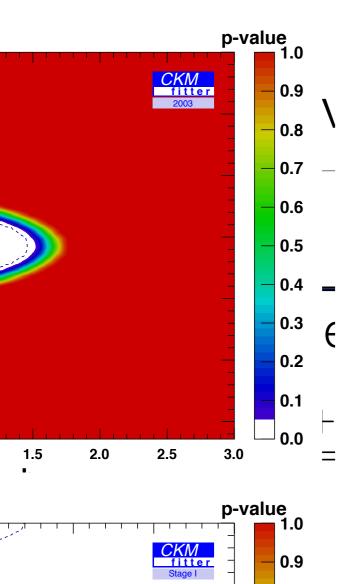
- ▶ NP only at short distances (UV)
- CKM unitary (& determined from NP free obs.)

## Combining 1 & 2: Impact on CPV BSM in $\Delta B=2$

Model-independent parametrization of BSM in  $\Delta F$ =2

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0.8

0.7

0.6

0.5

0.4

0.3

0.2

0.1

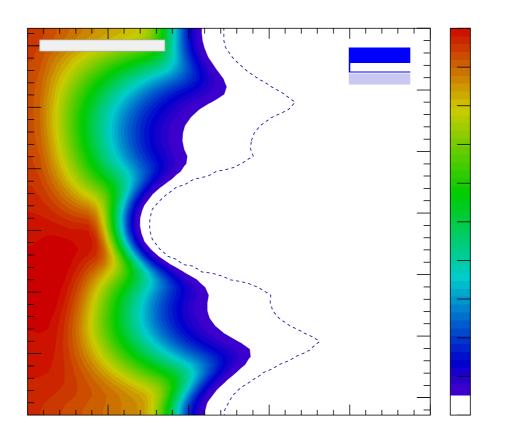
0.0

0.5

0.4

0.3

hs

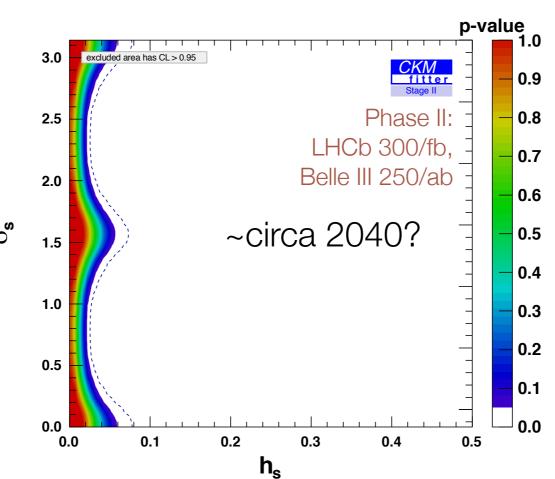


s & explorations

Sign  $\Delta B=2$ 

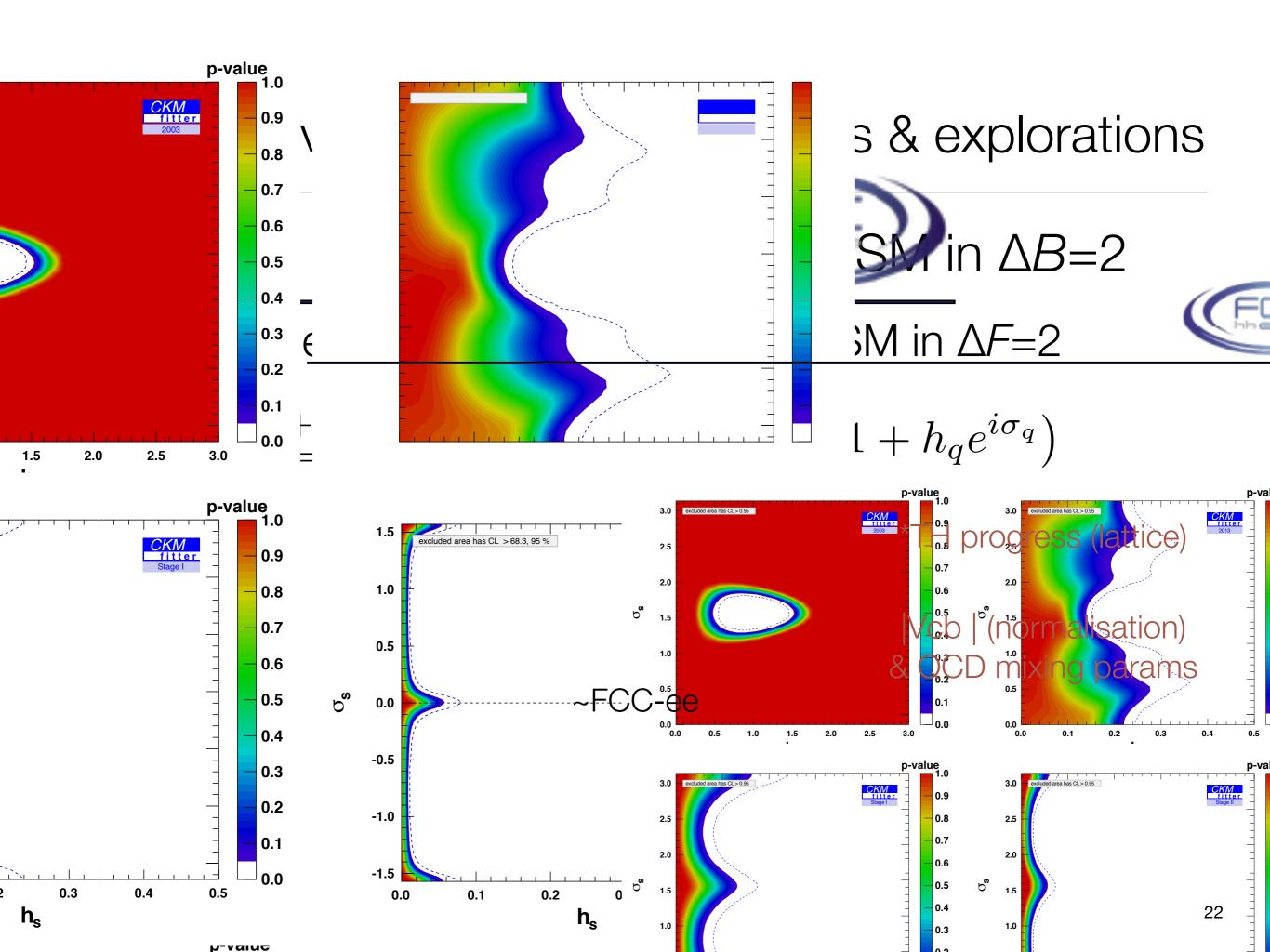
 $SM \text{ in } \Delta F=2$ 

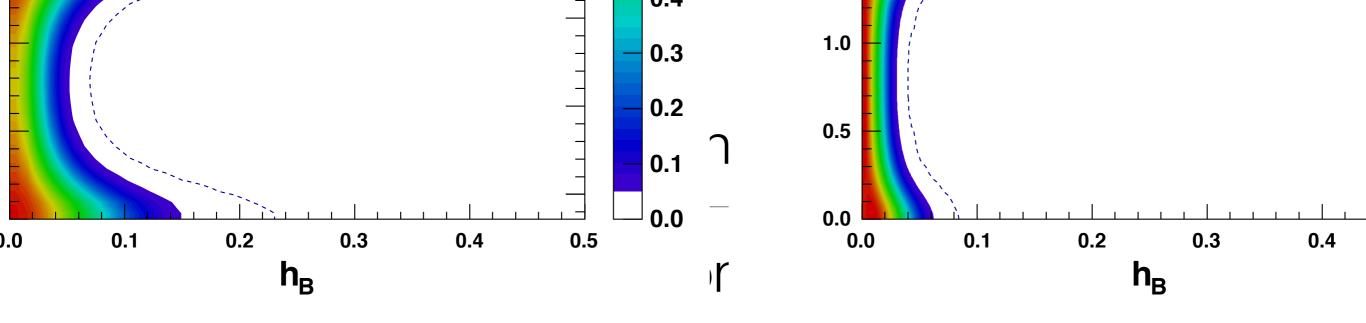
$$1 + h_q e^{i\sigma_q}$$



\*TH progress (lattice)

|Vcb | (normalisation) & QCD mixing params





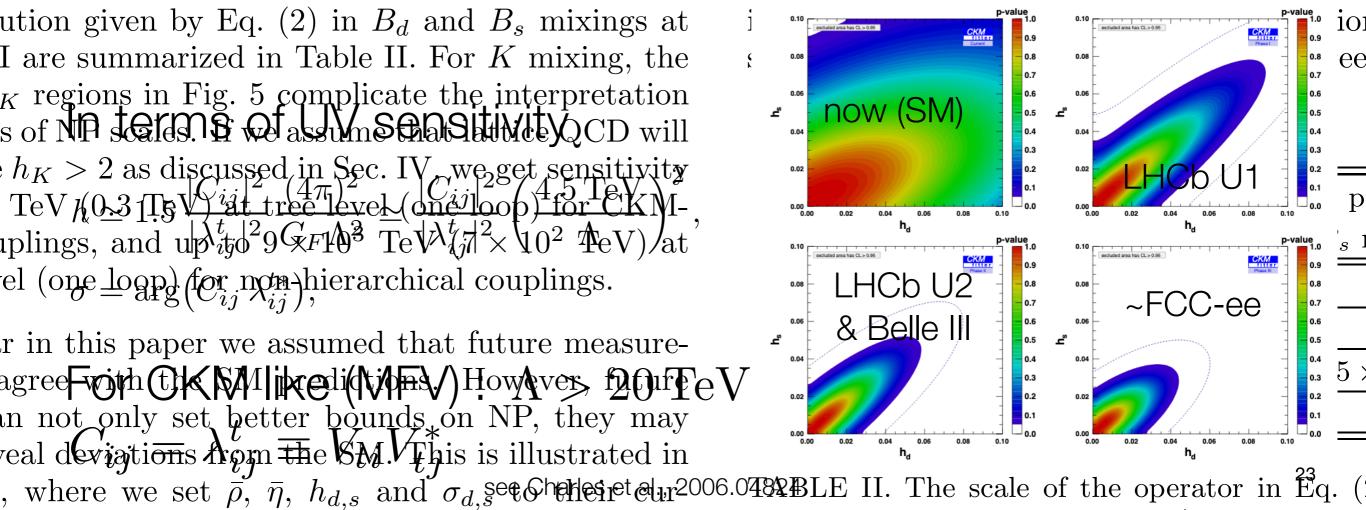
The past CP3 it of left and present to pright tropstraints on U3 temporary where  $h_B \equiv h_d = h_s$ , of the plots show future sensitivities for the Stage I and Stage II scenarios described in the text, assuming the stage I1 and I2 are the sensitivities for the Stage I3 and I3 are the sensitivities for the Stage I3 and I3 are the sensitivities for the stage I3 and I4 are the sensitivities for the stage I4 and I5 are the sensitivities for the stage I5 and I5 are the stage I5 and I5 are the sensitivities for the stage I5 and I5 are the sensitivities for the stage I5 and I5 are the sensitivities for the stage I5 and I5 are the sensitivities for the stage I5 and I5 are the sensitivities for the stage I5 and I5 are the sensitivities for the stage I5 and I5 are the sensitivities for the stage I5 and I6 are the sensitivities for the stage I6 and I7 are the sensitivities for the stage I6 and I7 are the sensitivities for the stage I6 and I7 are the sensitivities for the stage I6 and I7 are the sensitivities for the stage I6 and I7 are the sensitivities for the stage I6 and I7 are the sensitivities for the stage I7 and I8 are the sensitivities for the stage I8 and I8 are the sensitivities for the stage I8 are the stage I8 are the sensitivities for the stage I8 are the sensitivities fo nt with the SM. The dotted curves show the 99.7% CL contours.

$$\langle B_q | \mathcal{H}_{\Delta B=2}^{\text{SM+NP}} | B_q \rangle = \langle B_q | \mathcal{H}_{\Delta B=2}^{\text{SM}} | B_q \rangle \left( 1 + h_q e^{i\sigma_q} \right)$$

ution given by Eq. (2) in  $B_d$  and  $B_s$  mixings at I are summarized in Table II. For K mixing, the K regions in Fig. 5 complicate the interpretation s of Nn terms wtall mseasthlety CD will  $h_K > 2$  as discussed in Sec. IV, we get sensitivity TeV 10-3 [TeV) ist tree level (dne jloop) for CKM-

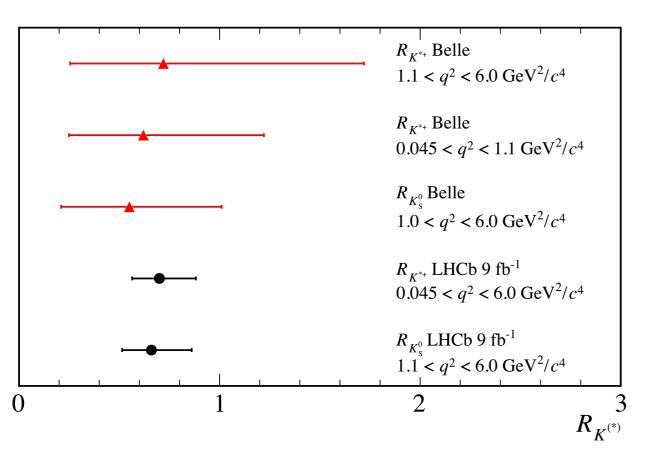
r in this paper we assumed that future measure- ${
m agree}$  Fight (CM) incompletely However, 120 if  ${
m EeV}$ n not only set better bounds on NP, they may real deviations from the SM. This is illustrated in

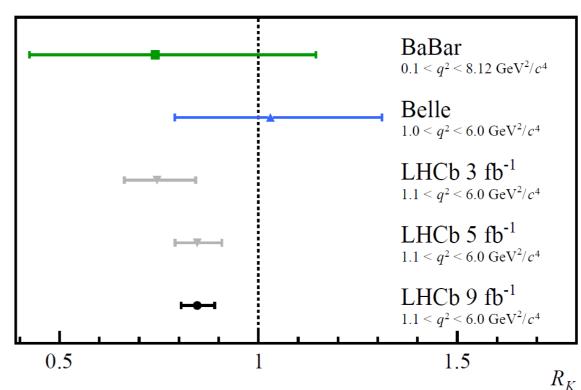
rel (one logp) (for non), hierarchical couplings.



### Part 3: Rare b-hadron decays to taus

Motived by current intriguing exp. situation in rare B decays





$$R_H \equiv \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{\mathrm{d}\mathcal{B}(B \to H\mu^+\mu^-)}{\mathrm{d}q^2} \mathrm{d}q^2}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{\mathrm{d}\mathcal{B}(B \to He^+e^-)}{\mathrm{d}q^2} \mathrm{d}q^2}$$

### Part 3: Rare b-hadron decays to taus

Motived by current intriguing exp. situation in rare B decays

• FCC-ee (unique) probe of SM predictions for B  $\rightarrow$  K<sup>(\*)</sup>  $\tau^+\tau^-$ 

```
R_{K^+}^{\mu\tau} = 0.87 \pm 0.02 \quad , \quad R_{K^0}^{\mu\tau} = 0.87 \pm 0.02 \quad , \quad \text{15 GeV}^2 < q^2 < 22 \text{ GeV}^2 \quad \text{J.F.K. et al., 1705.11106} \\ \text{Li \& Liu, 2012.00665} \quad R_{K^{*+}}^{\mu\tau} = 2.44 \pm 0.09 \quad , \quad R_{K^{*0}}^{\mu\tau} = 2.45 \pm 0.08 \quad , \quad \quad \text{15 GeV}^2 < q^2 < 19.2 \text{ GeV}^2.
```

- + Complete kinematical reconstruction
- Access to angular observables, tau polarization
- Detailed study of backgrounds & detector requirements in progress

FCC-ee flavour photographic benchmarks & explorations

Part 3: Rare b-hadron decays to taus

Motived by

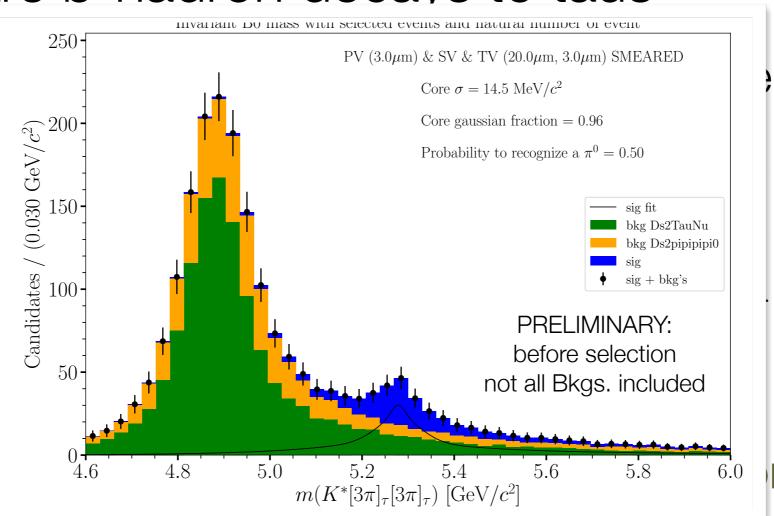
• FCC-ee

$$R_{K^+}^{\mu au} = 0.87 \, \pm$$

$$R_{K^{*+}}^{\mu\tau} = 2.44 \, \pm \,$$

+ Comple

Access



B decays

**→ K**(\*) **T**+**T**-

J.F.K. et al., 1705.11106 Li & Liu, 2012.00665

 Detailed study of backgrounds & detector requirements in progress

## Part 3: Rare b-hadron decays to taus

Motived by current intriguing exp. situation in rare B decays

• FCC-ee (unique) probe of SM predictions for B  $\rightarrow$  K<sup>(\*)</sup>  $\tau^+\tau^-$ 

J.F.K. et al., 1705.11106 Li & Liu, 2012.00665

• Potentially also complementary leptonic mode  $B_{(s)} \rightarrow \tau^+\tau^-$ 

$$BR(B_s \to \tau^+ \tau^-) = (7.73 \pm 0.49) \times 10^{-7}$$
  
 $BR(B_d \to \tau^+ \tau^-) = (2.22 \pm 0.19) \times 10^{-8}$ 

Bobeth et al., 1311.0903 see also U. Haisch, 1206.1230

(Expected sensitivity at Belle II to BRs of O (10<sup>-4</sup>) ~ O(10<sup>-5</sup>))

see also LHCb-CONF-2016-011

Part 3: Rare b-hadron decays to taus, neutrinos

Motived by current intriguing exp. situation in rare B decays

• FCC-ee (unique) probe of SM predictions for B  $\rightarrow$  K<sup>(\*)</sup>  $\tau^+\tau^-$ 

J.F.K. et al., 1705.11106 Li & Liu, 2012.00665

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Bobeth et al., 1311.0903 see also U. Haisch, 1206.1230

(Expected sensitivity at Belle II to BRs of O (10<sup>-4</sup>) ~ O(10<sup>-5</sup>))

see also LHCb-CONF-2016-011

• Potential improvement also on B  $\rightarrow$  K<sup>(\*)</sup>vv (beyond Belle II)

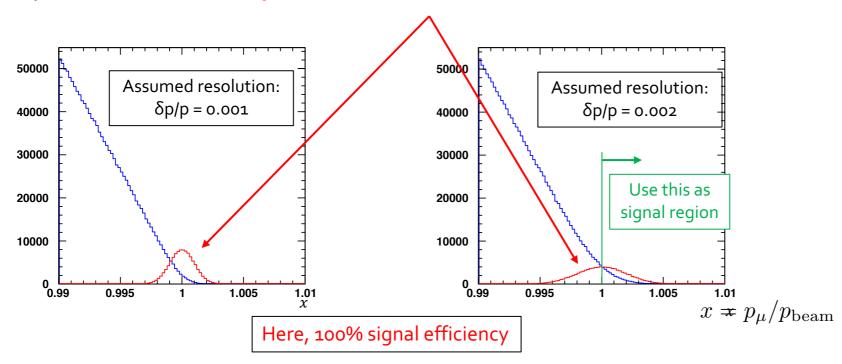
S. Descotes-Genon et al., 2208.10880

including time-dependent measurements / probes of CPV

see talk by S. Descotes-Genon

### Insert signal and smear track momenta

• In these plots, assume  $Br(Z \rightarrow \tau \mu) = 10^{-7}$ , i.e. 100,000 muons



#### Sensitivity to signal:

- Since number of background events is high, use primitive estimator:  $s/\sqrt{b}$
- s and b are number of signal and background events, respectively, in signal region
  - - Eventually one will do more sophisticated statistical analysis, but for now...
- 95% c.l. corresponds approximately to number of signal events equal:  $s_{95} = 2\sqrt{b}$

Mogens Dam / NBI Copenhagen

1st FCC Physics Workshop

19 January 2017

### at least 3 orders of magnitude

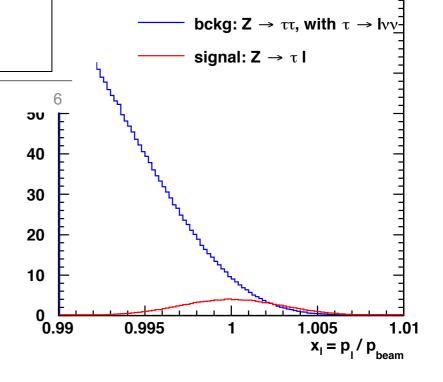
M. Dam, SciPostPhys.Proc.1,041(2019) see also De Romeri et al. JHEP 1504 (2015) 051

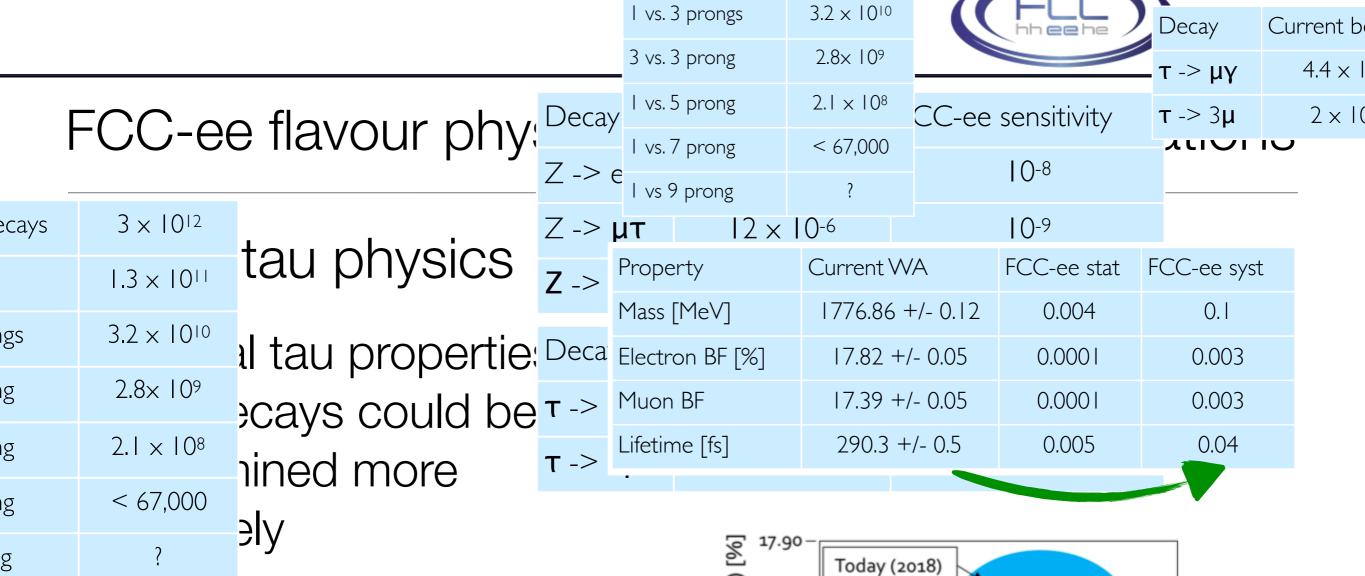
## 3 explorations



### $x \neq p_{\mu}/p_{\text{beam}}$ | T decays

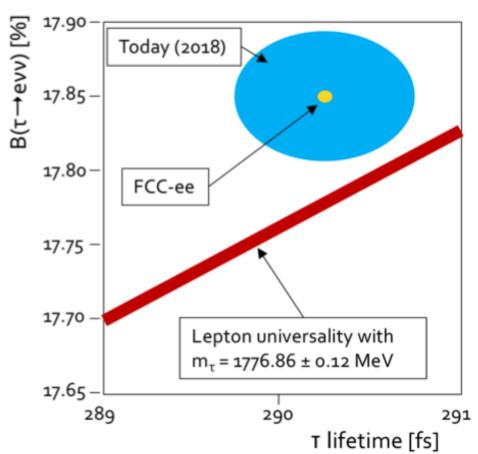
Iliana & Masip, hep-ph/0207328 X. Marcano, J. Roy, 2107.10273





- Interesting implications Current WA FCC-ee stat FCC-ee syst for LFU (in tau decays) 0.1 0.003 Allwicher, Isidori, Semilovic, 2109.03833 | 1**7/13Damy\_SoiP**5stPhys.**Proo000**41(2019) 0.003 Eur. Phys. J. Plus 136, 963 (2021) 0.005 0.04 290.3 +/- 0.5
- Would possibly require improved calculations

g



### Conclusions

- FCC-ee could be a powerful and competitive probe of flavour physics post-2030
  - FCC-ee can compete favourably with ultimate precision of LHCb and Belle II
  - There are processes for which FCC-ee / CEPC are unique see also talk by A. Kwok
  - Luminosity is key. Many measurements reported here are statistically limited?!

### Conclusions

- FCC-ee could be a powerful and competitive probe of flavour physics post-2030
- Effort underway to understand exp. precision with which rare decays of c- and b-hadrons and CP violation in heavy-quark sector & LFV processes could be measured
  - Full exploitation of the FCC-ee potential will require significant progress in theory: Lattice QCD, EM (EW) corrections,...

### Conclusions

- FCC-ee could be a powerful and competitive probe of flavour physics post-2030
- Effort underway to understand exp. precision with which rare decays of c- and b-hadrons and CP violation in heavy-quark sector & LFV processes could be measured
- Less explored areas include flavour studies using top & Higgs decays, spectroscopy, quarkonium physics, flavor conversion @ high-pT
  - Examples: top & Higgs decays to exclusive hadronic final states see e.g. Mangano & Melia, 1410.7475 Mangano & Melia, 1410.7475 Kagan et al., 1406.1722 see e.g. Garland et al., 2112.05127