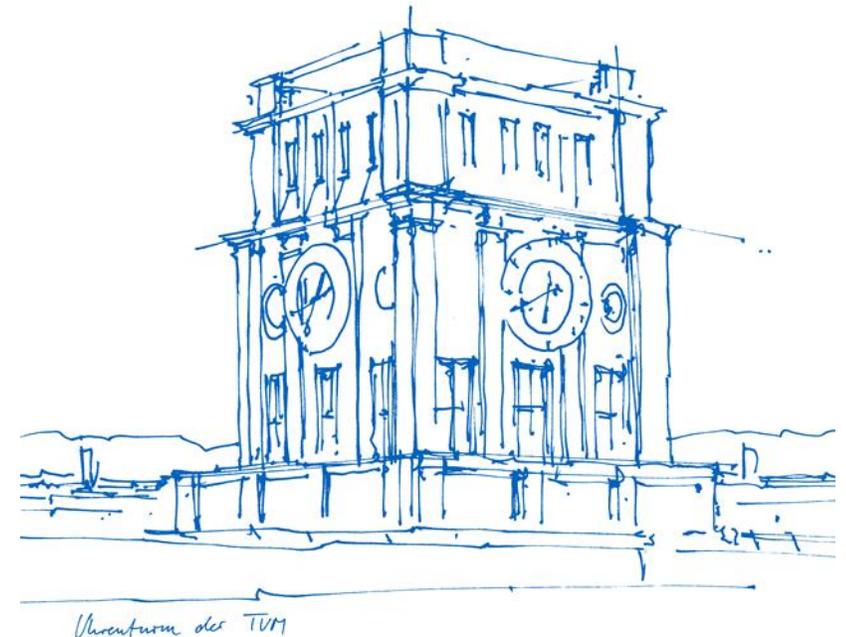


# Measuring the radiative width of the $\rho(770)$ and testing the chiral anomaly at COMPASS

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13<sup>th</sup> workshop on  $e^+e^-$  Collisions from Phi to Psi – August 18, 2022



- Quantum Chromodynamics (QCD) as true theory of strong interaction
- Lagrange density of QCD:

$$\mathcal{L}_{QCD} = \sum_{f=\{u,d,c,s,t,b\}} \sum_{i,j=1}^{N_c} \bar{\psi}_{f,j} (i\gamma^\mu D_{i,\mu}^j - m_f \delta_i^j) \psi^{f,i} - \frac{1}{4} \sum_{a=1}^{N_c^2-1} G_{\mu\nu}^a G_a^{\mu\nu}$$

- Flavor symmetries?

- Quantum Chromodynamics (QCD) as true theory of strong interaction
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Flavor symmetry breaking term ( $m_u \neq m_d \neq m_s$ )

- Flavor symmetries? -> only approximate symmetries
  - **$SU(2)$** :  $m_u \approx m_d$  -> isospin symmetry
  - **$SU(3)$** :  $m_u \approx m_d \approx m_s$  -> the eightfold way

- Quantum Chromodynamics (QCD) as true theory of strong interaction
- Lagrange density of QCD:

$$\mathcal{L}_{QCD} = \sum_{\substack{f=\{u,d, \\ c,s,t,b\}}} \sum_{i,j=1}^{N_c} \bar{\psi}_{f,j} (i\gamma^\mu D_{i,\mu}^j - m_f \delta_i^j) \psi^{f,i} - \frac{1}{4} \sum_{a=1}^{N_c^2-1} G_{\mu\nu}^a G_a^{\mu\nu}$$

- Approximate flavor symmetries in chiral limit ( $m_u = m_d = m_s = 0$ ):

$$SU(3)_R \times SU(3)_L$$

- Left- and right-handed fields decouple for massless particles
- Chirality can directly be translated to parity of particle  
→ mass-degenerate doublets of states with opposite parity

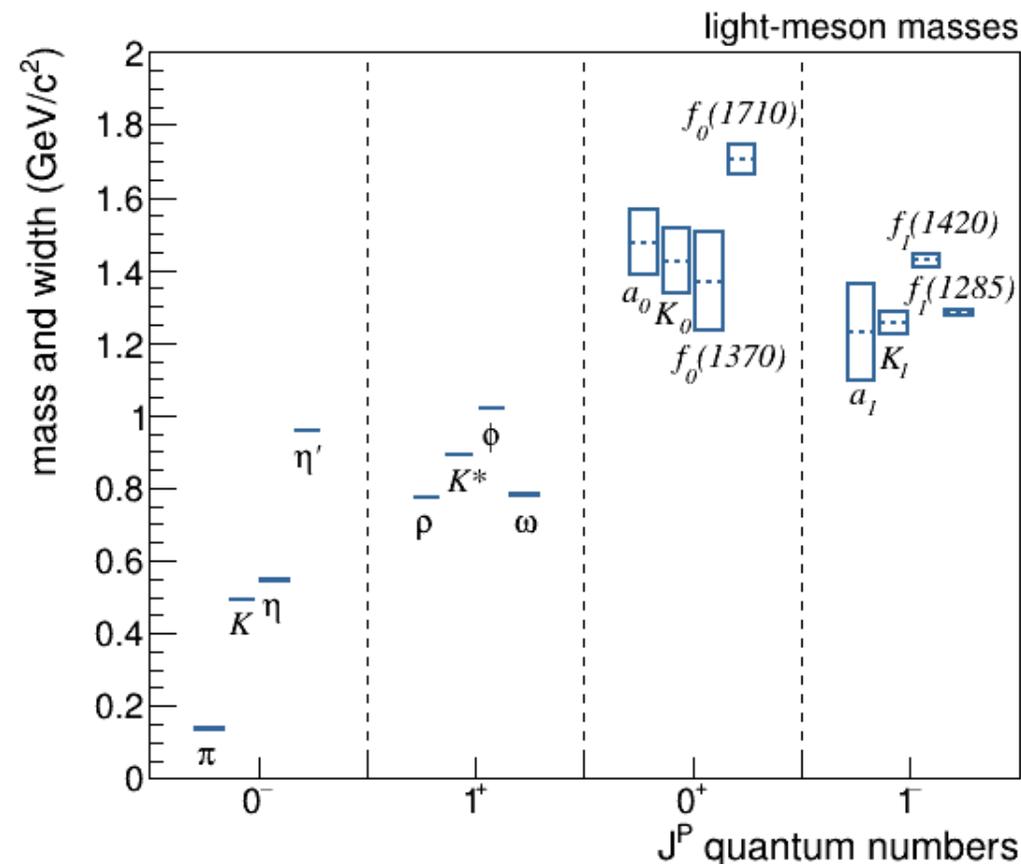
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- Approximate flavor symmetries in chiral limit ( $m_u = m_d = m_s = 0$ ):

## $SU(3)_R \times SU(3)_L$

- Left- and right-handed fields decouple for massless particles
- Chirality can directly be translated to parity of particle  
→ mass-degenerate doublets of states with opposite parity
- Why does chiral symmetry not manifest itself in the spectrum (in contrast to isospin and eightfold way)?  
→ Nambu-Goldstone mechanism for spontaneous/dynamic breakdown of chiral symmetry



## Spontaneous symmetry breaking

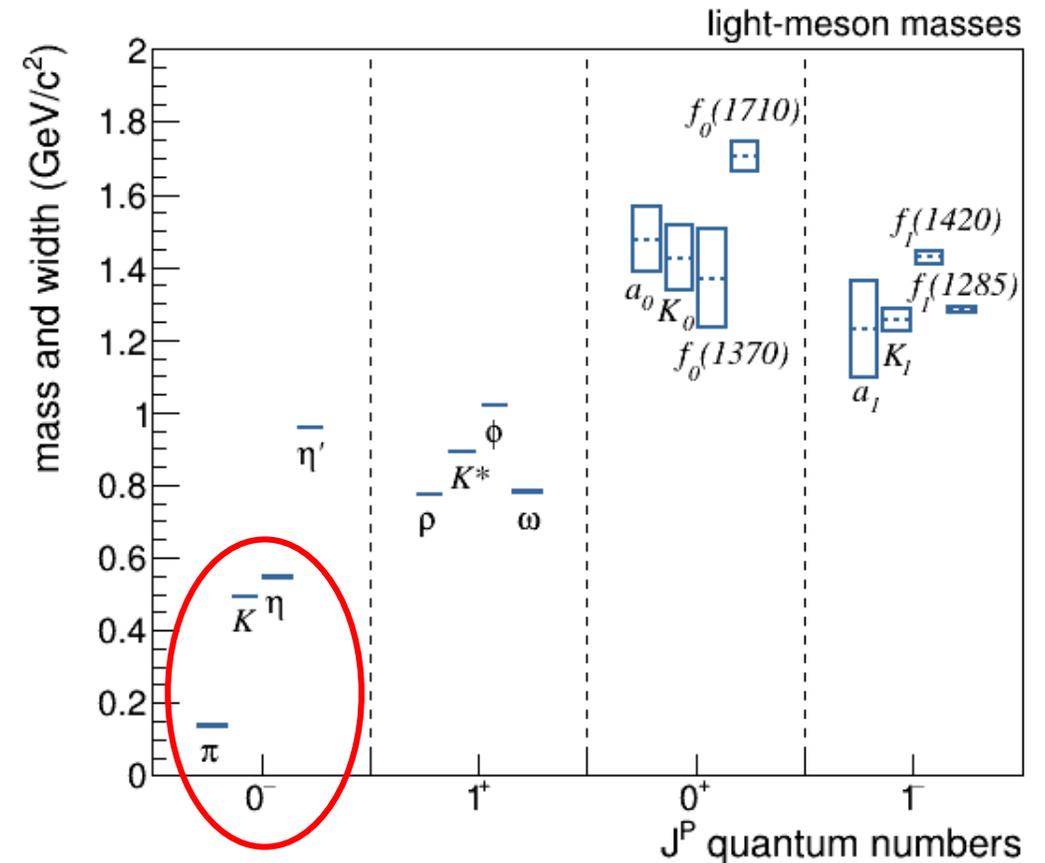
⇒ Eight massless, spinless Goldstone bosons

$$(\pi^\pm, \pi^0, K^\pm, K^0, \bar{K}^0, \eta)$$

⇒ Explicit breaking of chiral symmetry due to the small quark masses -> Goldstone bosons acquire mass

⇒  $SU(3)_R \times SU(3)_L \rightarrow SU(3)_V$

⇒ Chiral Perturbation Theory: effective Lagrangian with power-counting scheme as low-energy theory for QCD makes use of chiral symmetry



(almost) massless Goldstone bosons

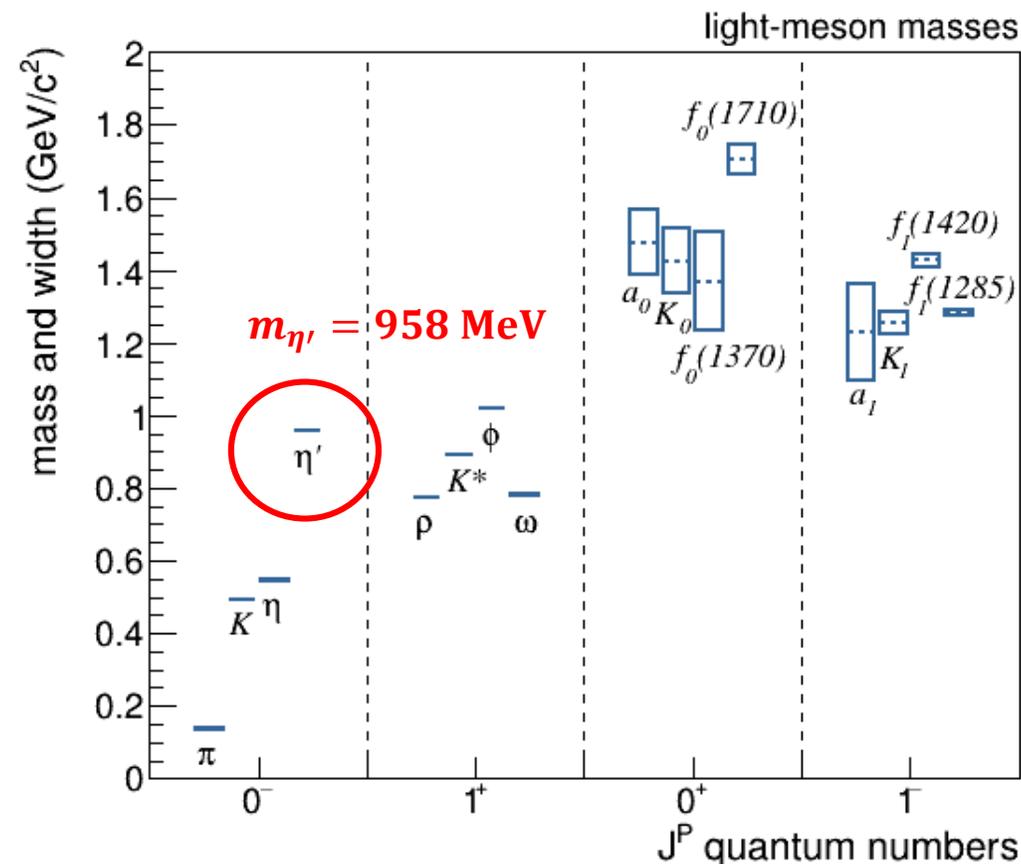
- Lagrange density of QCD:

$$\mathcal{L}_{QCD} = \sum_{f=\{u,d,c,s,t,b\}} \sum_{i,j=1}^{N_c} \bar{\psi}_{f,j} (i\gamma^\mu D_{i,\mu}^j - m_f \delta_i^j) \psi^{f,i} - \frac{1}{4} \sum_{a=1}^{N_c^2-1} G_{\mu\nu}^a G_a^{\mu\nu}$$

- Features *axial*  $U(1)$ -symmetry in chiral limit:

$$\psi(x) \rightarrow e^{i\theta\gamma_5} \psi(x)$$

- No ninth “unnaturally light” meson
- **Anomalous** symmetry breaking: symmetry of the Lagrangian does not lead to conserved Noether currents
- **Anomaly:** Symmetry of classical Lagrangian violated at quantum level



- Chiral anomaly in ChPT taken into account by Wess-Zumino-Witten (WZW) term
- Describes coupling of odd number of Goldstone bosons:

$SU(2)$ flavor	$SU(3)$ flavor
$\pi^0 \rightarrow \gamma\gamma$	$K^+ K^- \rightarrow \pi^+ \pi^- \pi^0$
$\gamma \pi^- \rightarrow \pi^- \pi^0$	$\eta \rightarrow \pi^+ \pi^- \gamma$
$\pi^+ \rightarrow e^+ \nu_e \gamma$	$K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$
etc.	etc.

- Effective theory  $\rightarrow$  pion decay constant measured from leptonic decays of the charged pion ( $\pi^\pm \rightarrow \mu^\pm + \nu$ )

$F_{\pi\gamma\gamma}$

•  $F_{\pi\gamma\gamma} = \frac{e^2 N_C}{12\pi^2 F_\pi} = 2.52 \cdot 10^{-2} \text{GeV}^{-1}$

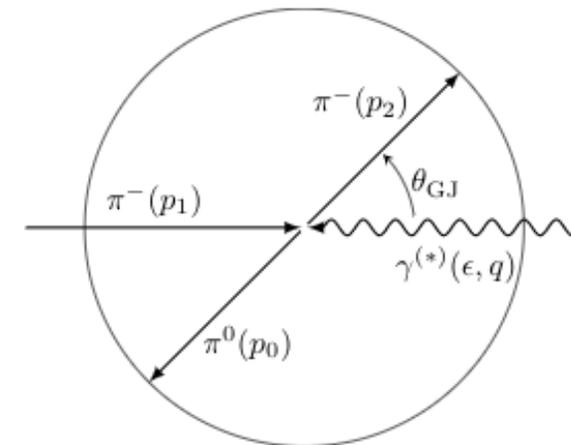
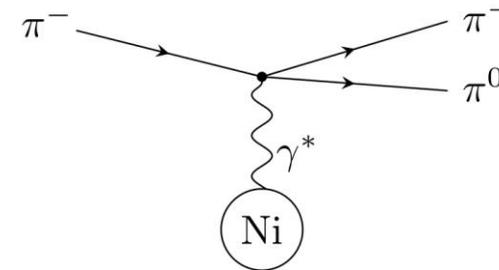
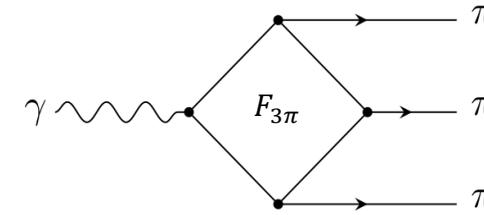
$F_{3\pi}$

•  $F_{3\pi} = \frac{e N_C}{12\pi^2 F_\pi^3} = (9.78 \pm 0.05) \text{GeV}^{-3}$

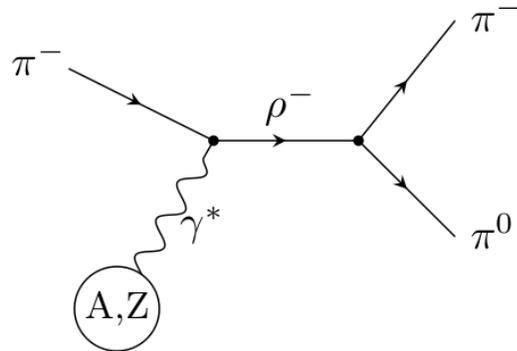
- $F_{3\pi}$ : Direct coupling of  $\gamma$  to  $3\pi$  - process proceeds primarily via the chiral anomaly => one of the most definitive tests of low-energy QCD
- Accessible in Primakoff reactions via:  $\pi^- \gamma^* \rightarrow \pi^- \pi^0$
- Challenges:
  1. Explicit chiral symmetry breaking:

$$F_{3\pi} = \frac{eN_C}{12\pi^2 F_\pi^3} = (9.78 \pm 0.05)\text{GeV}^{-3} = F(s = t = u = 0)$$

2. Coherent background from  $\rho(770)$  production



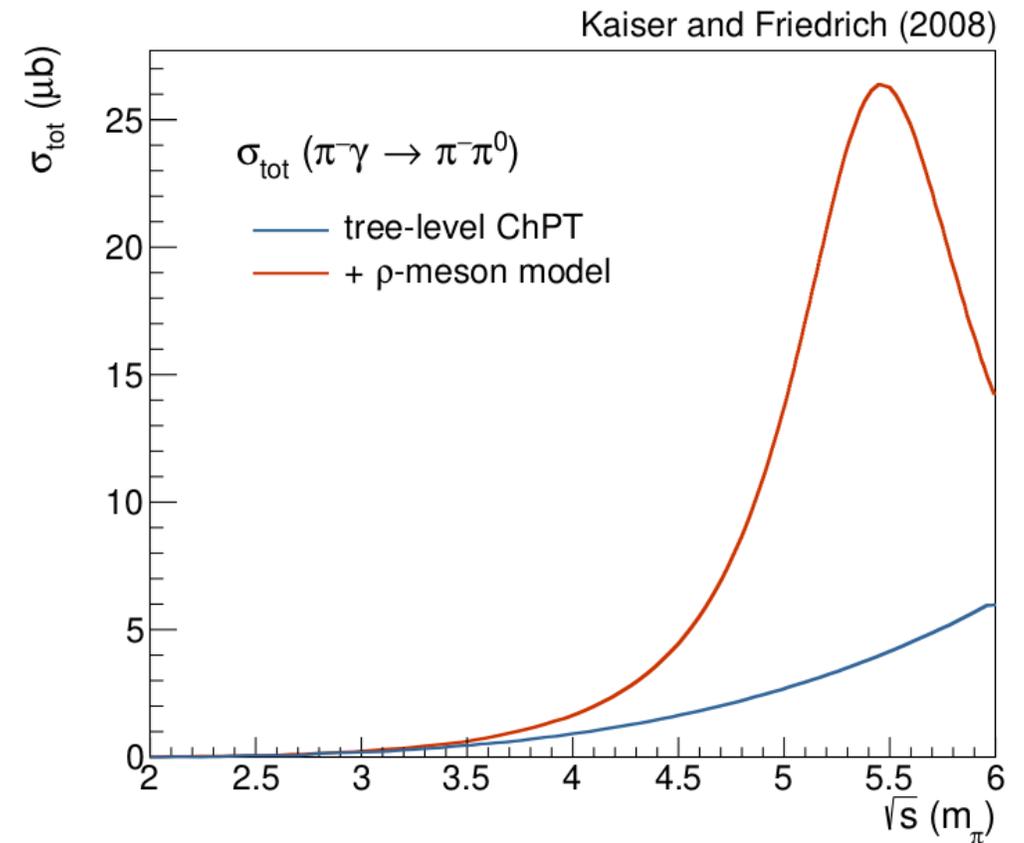
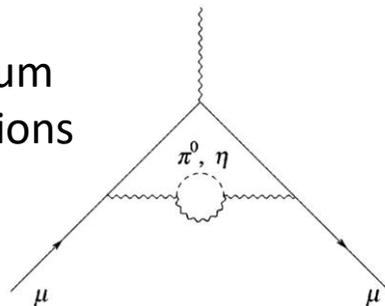
- Background from  $\rho(770)$  production (strong and electromagnetic)



⇒ possibility of extraction of radiative width of  $\rho$ -meson:

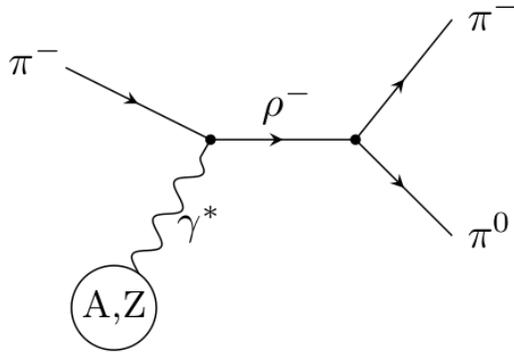
$$\Gamma_{(\rho \rightarrow \pi\gamma)} / \Gamma_{\text{tot}} \approx 4.5 \cdot 10^{-4}$$

⇒ contributes to hadronic vacuum polarization terms in calculations of  $g - 2$  of  $e$  and  $\mu$



[Kaiser, N. and Friedrich, J. M., EPJA 36 no. 2, \(2008\) 181–188](#)

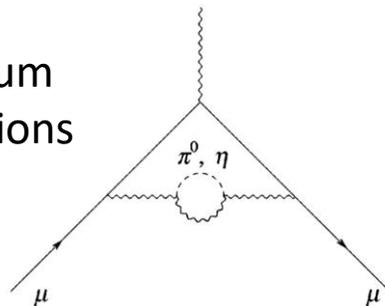
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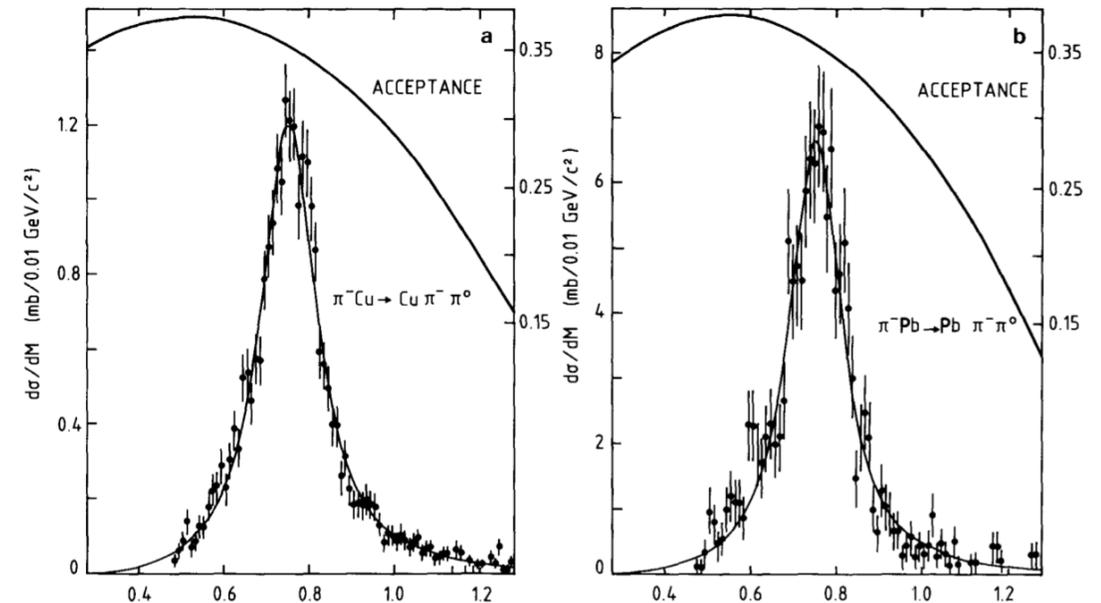
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[Capraro, L. et al. NPB 288 \(1987\) 659-680](#) at CERN (SPS):

- From fit of  $d\sigma/dt$  for  $\rho$  production:  
 $\Gamma(\rho \rightarrow \pi\gamma) = (81 \pm 4 \pm 4) \text{ keV}$

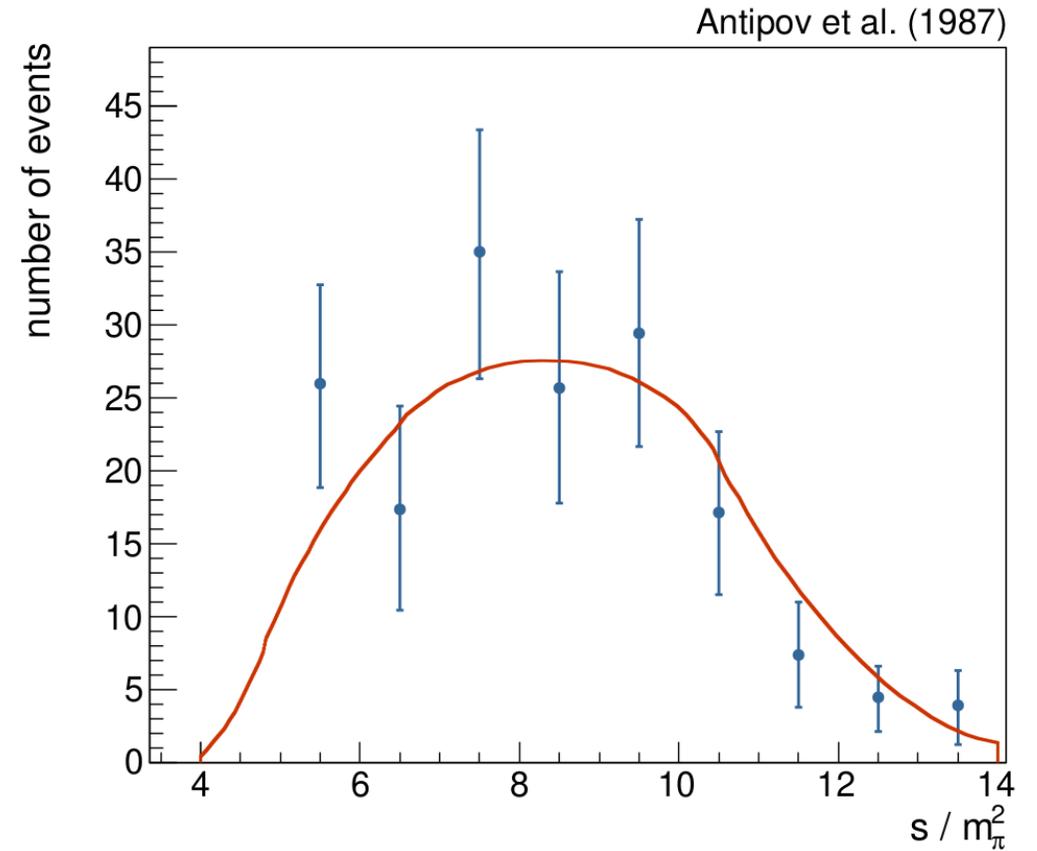


[Antipov, Y. et al. PRD 36 \(1987\) 101103](#) using data from Serpukhov experiments

Problem of explicit chiral symmetry breaking:

As previously noted, the value  $F^{3\pi}$  is supposed to vary slowly with  $s, t, q^2 \ll m_\rho^2$  so that  $F^{3\pi} \simeq F^{3\pi}(0)$ .

$$\Rightarrow \bar{F}_{3\pi} = (12.9 \pm 0.9 \pm 0.5) \text{ GeV}^{-3}$$



[Ametller, L. et al. PRD 64 \(2001\) 094009](#)

PHYSICAL REVIEW D, VOLUME 64, 094009

## Electromagnetic corrections to $\gamma\pi^\pm \rightarrow \pi^0\pi^\pm$

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(Received 11 July 2001; published 3 October 2001)

The amplitude for the anomalous transitions  $\gamma\pi^\pm \rightarrow \pi^0\pi^\pm$  is analyzed within chiral perturbation theory including electromagnetic interactions. The presence of a  $t$ -channel one-photon exchange contribution induces sizable  $\mathcal{O}(e^2)$  corrections which enhance the cross section in the threshold region and bring the theoretical prediction into agreement with available data. In the case of the crossed reaction  $\gamma\pi^0 \rightarrow \pi^+\pi^-$ , the same contribution appears in the  $s$  channel and its effects are small.

DOI: 10.1103/PhysRevD.64.094009

PACS number(s): 12.39.Fe, 11.30.Rd, 13.60.Le, 13.75.-n

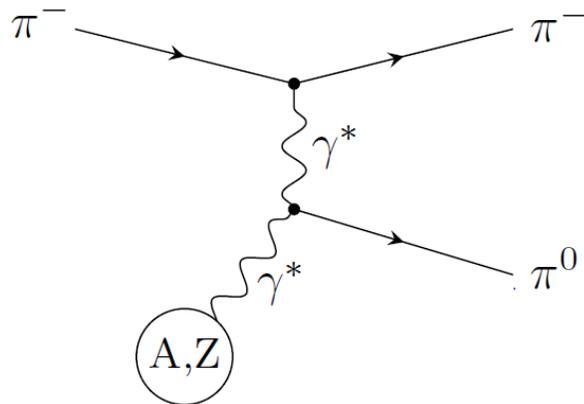
Reanalysis of Serpukhov data using chiral expansion:

$$F_{3\pi}(s, t, u) = F_{3\pi}(f^{(0)}(s, t, u) + f^{(1)}(s, t, u) + f^{(2)}(s, t, u) + \dots)$$

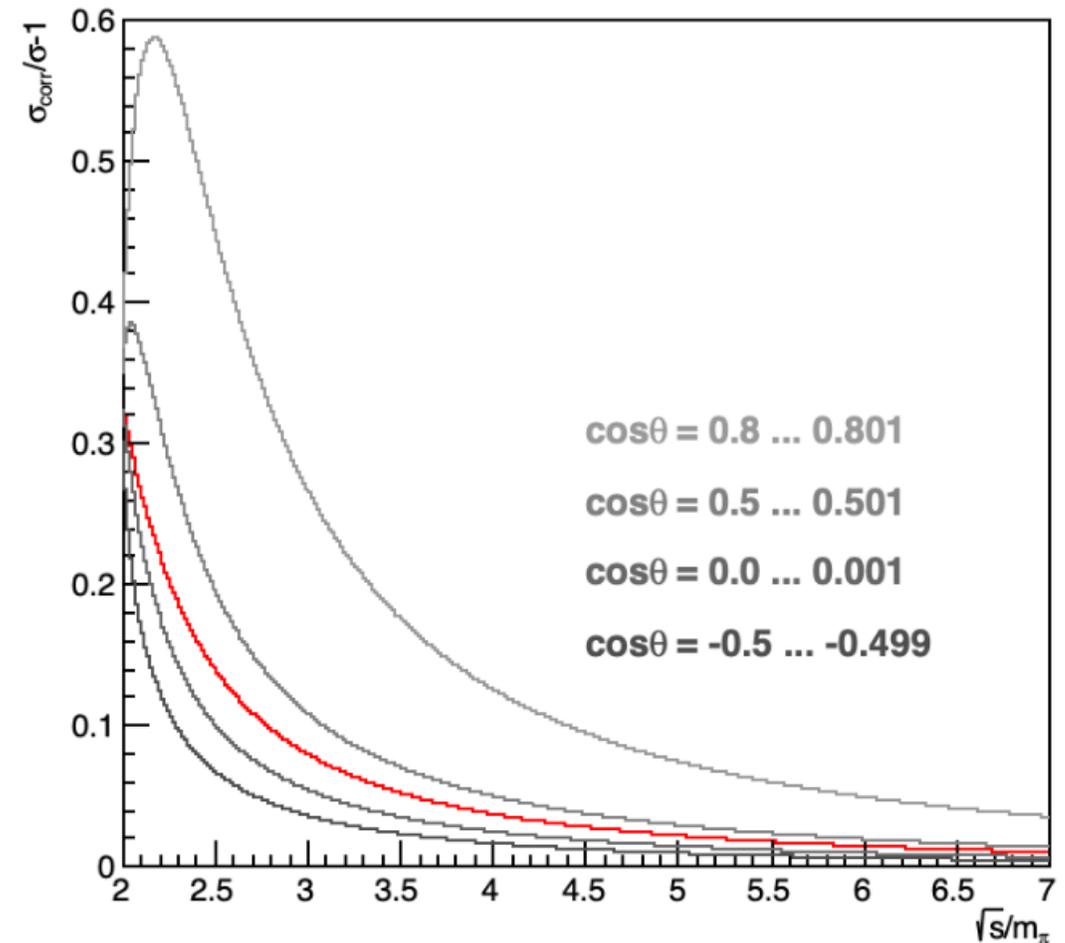
- Extrapolation using one loop and two loop corrections:

$$F_{3\pi} = (11.4 \pm 1.3) \text{ GeV}^{-3}$$

- Electro-magnetic corrections => significant contribution to  $f^{(0)}(s, t, u)$  when isospin breaking effects are taken into account.

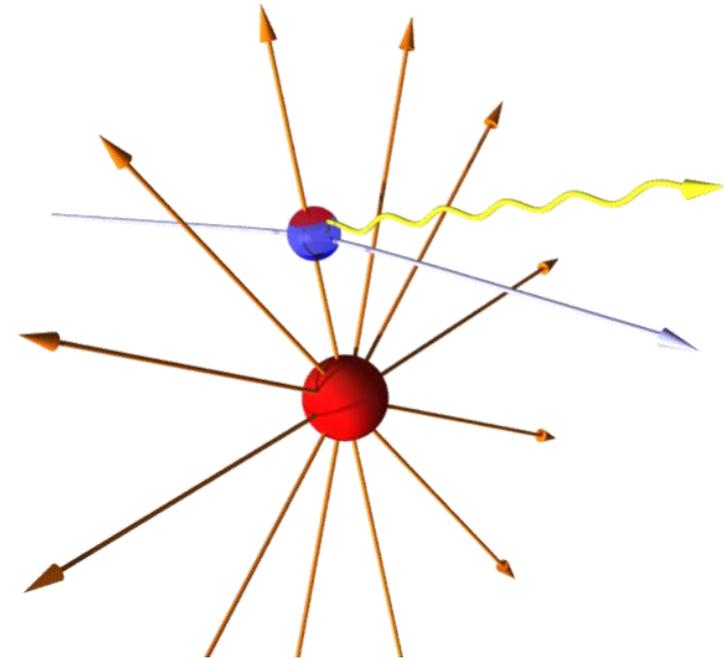


- Integrated correction amounts to 32% at threshold  
 $\Rightarrow F_{3\pi} = (10.7 \pm 1.2) \text{ GeV}^{-3}$
- Precision of previous measurements:  $\mathcal{O}(10\%)$   
 $\Rightarrow$  More precise experimental determination desirable



[Ametller, L. et al. PRD 64 \(2001\) 094009](#)

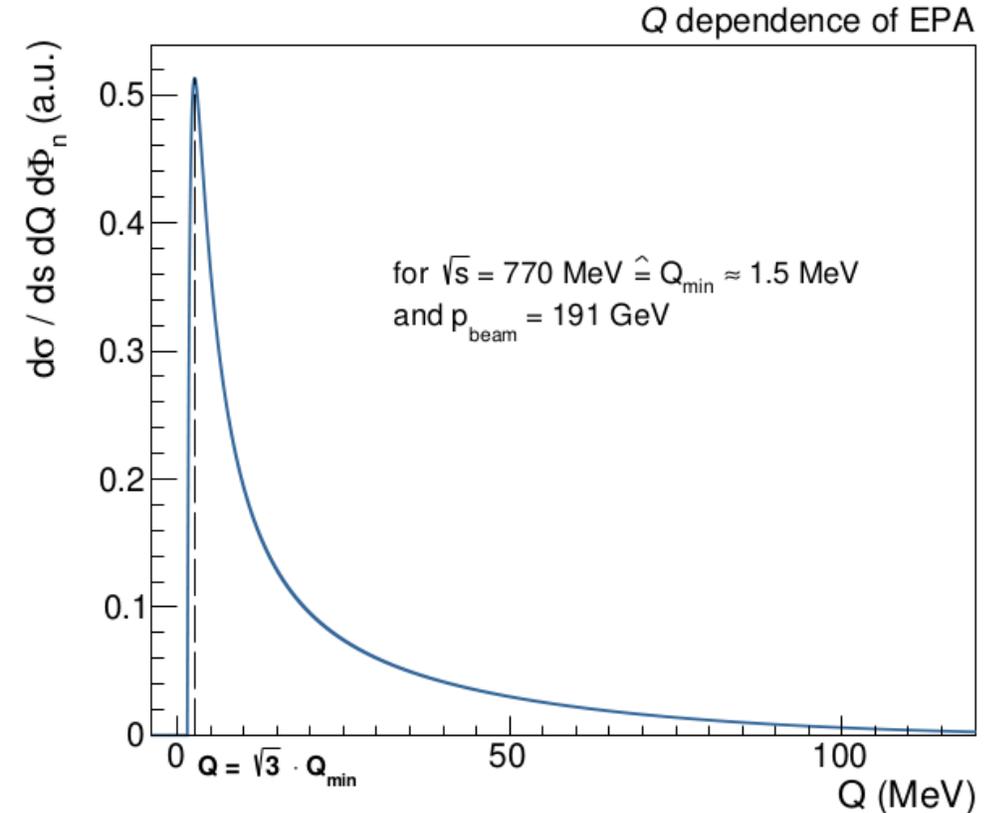
- Idea dates back to Henry Primakoff (“photon target”)
- Photon is provided by the strong Coulomb field of a nucleus (typical field strength at  $d = 5R_{Ni}$ :  $E \approx 300$  kV/fm)
- Coulomb field of nucleus is a source of quasi-real ( $P_\gamma^2 \ll m_\pi^2$ ) photons
- Large impact parameters (ultra-peripheral scattering)

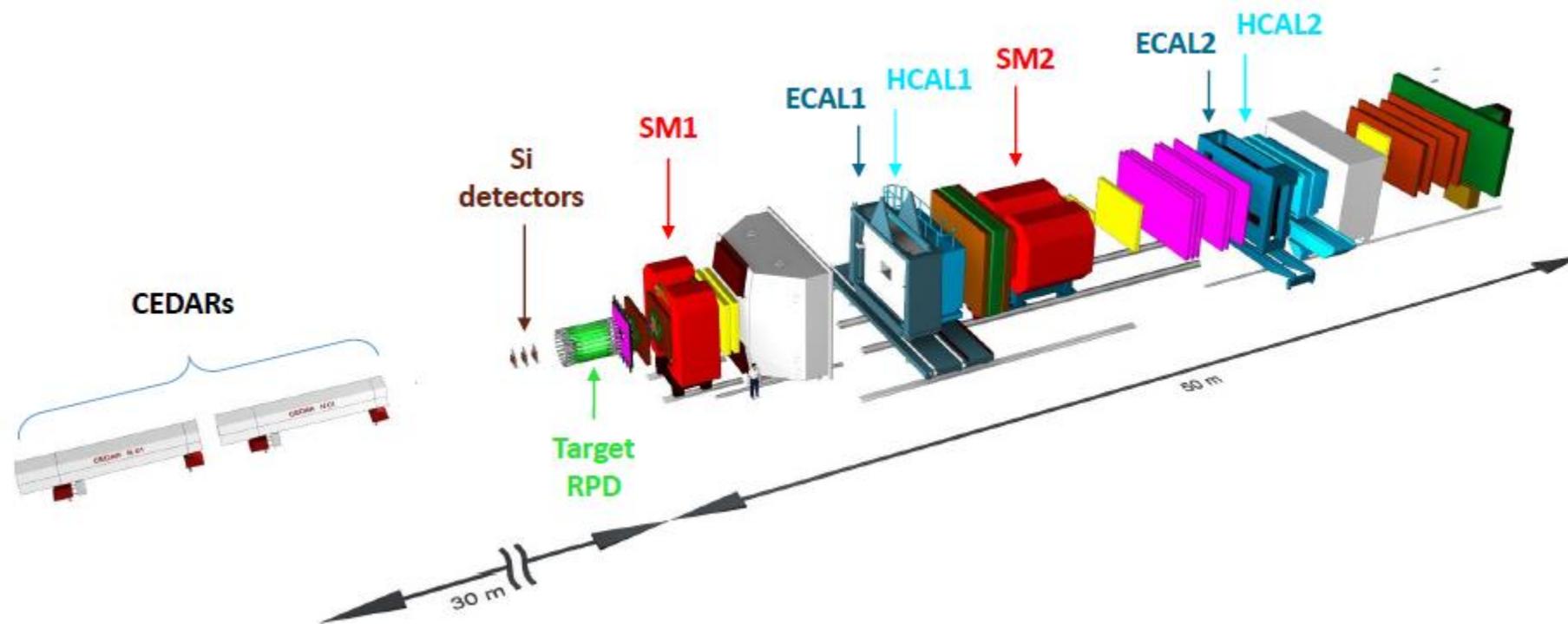


- Coulomb field of relativistic charge  $\approx$  flux of quasi-real photons  
Equivalent photon approximation (single-photon exchange)

$$\frac{d\sigma}{ds dQ^2 d\Phi_n} = \underbrace{\frac{Z^2 \alpha}{\pi(s - m_\pi^2)} F^2(Q^2)}_{\text{Flux of quasi-real photons}} \underbrace{\frac{Q^2 - Q_{\min}^2}{Q^4}}_{\pi\gamma \text{ scattering cross section}} \cdot \frac{d\sigma_{\pi\gamma \rightarrow X}}{d\Phi_n}$$

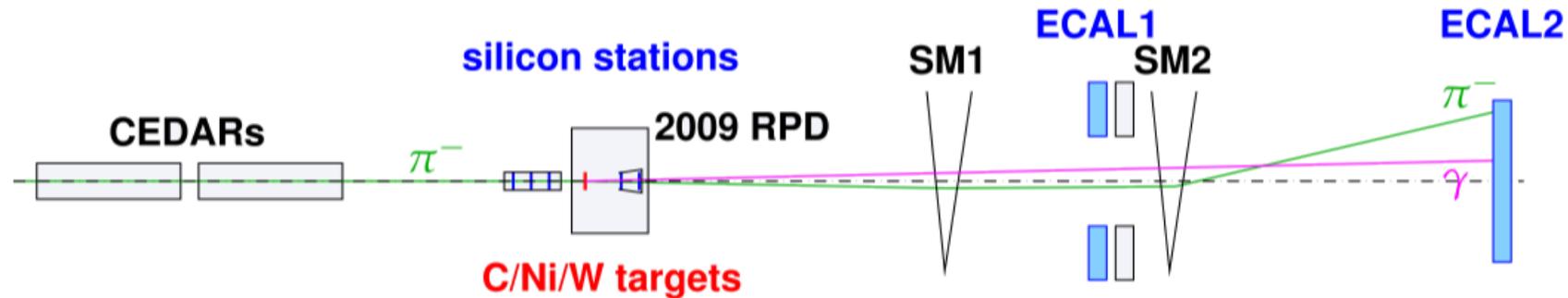
- Beam pions scatter off equivalent photons
- Peak at tiny momentum transfers  $Q^2 \approx 10^{-5} \text{GeV}^2/c^2$





- 190 GeV negative hadron beam
- Beam PID
- Nuclear target(s): Ni and W
- Calorimetric trigger on neutrals
- Two stage spectrometer (LAS and SAS) with tracking and calorimeter

[Abbon, P. et al. NIM A 779 \(2014\) 69–115](#)



- 190 GeV negative hadron beam: 96.8%  $\pi^-$ , 2.4%  $K^-$ , 0.8%  $\bar{p}$
- Beam particle identification by Cherenkov detectors
- 4mm Ni target disk ( $\approx 25\% X/X_0$ )
- Measure scattered  $\pi^-$  and produced photons (number of photons depends on final state)
- Select exclusive events at very low  $Q^2$
- For absolute cross-section measurements:  
Luminosity determination via free Kaon decays  
( $K^- \rightarrow \pi^- \pi^0$  or  $K^- \rightarrow \pi^- \pi^0 \pi^0$ )

- Dispersive framework to deduce  $F_{3\pi}$  from a fit to the  $\pi^-\pi^0$  mass distribution up to 1.0 GeV including the  $\rho(770)$ -resonance:

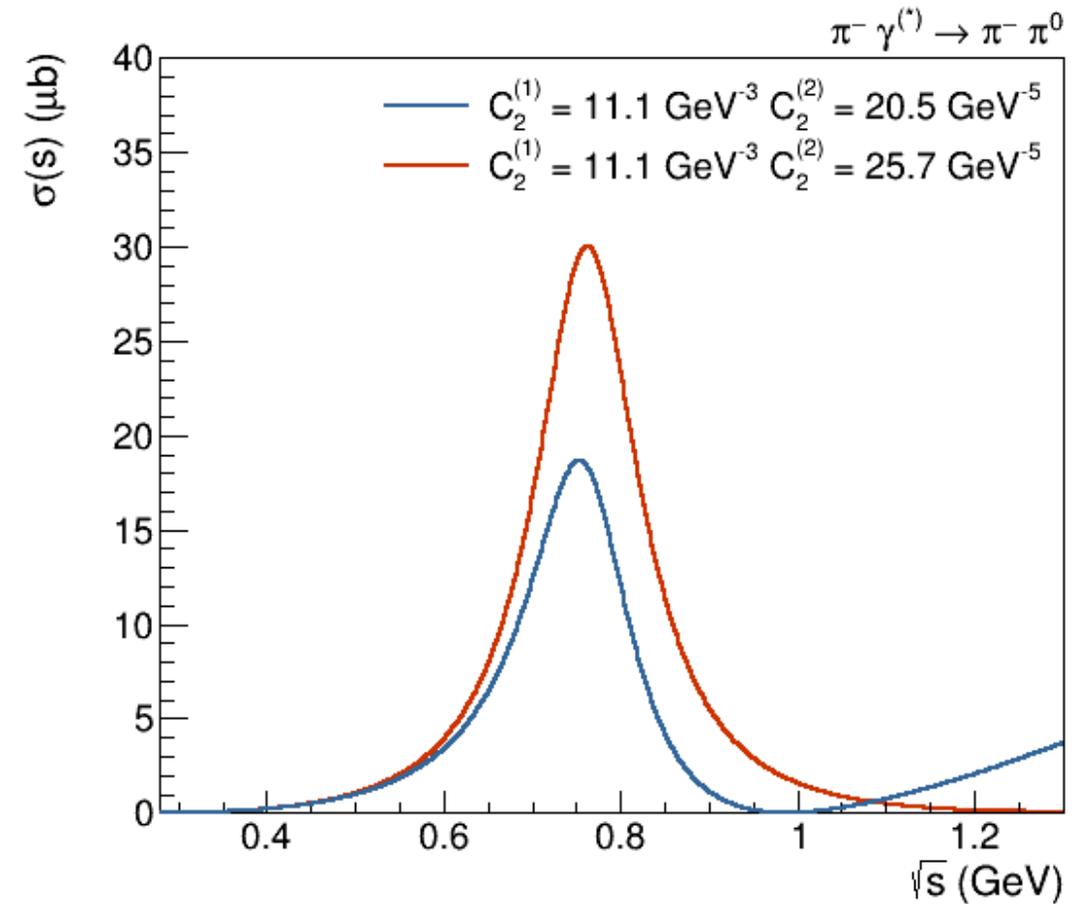
$$\sigma(s) = \frac{(s - 4m_\pi^2)^{3/2}(s - m_\pi^2)}{1024\pi\sqrt{s}} \int_{-1}^1 dz(1 - z^2) |\mathcal{F}(s, t, u)|^2$$

With

$$\mathcal{F}(s, t, u) = C_2^{(1)} \mathcal{F}_2^{(1)}(s, t, u) + C_2^{(2)} \mathcal{F}_2^{(2)}(s, t, u) - \frac{2e^2 F_\pi^2 F_{3\pi}}{t}$$

$C_2^{(1)}, C_2^{(2)}$  : fit parameters

$\mathcal{F}_2^{(1)}(s, t, u), \mathcal{F}_2^{(2)}(s, t, u)$ : provided by theory colleagues (Kubis, Hoferichter)

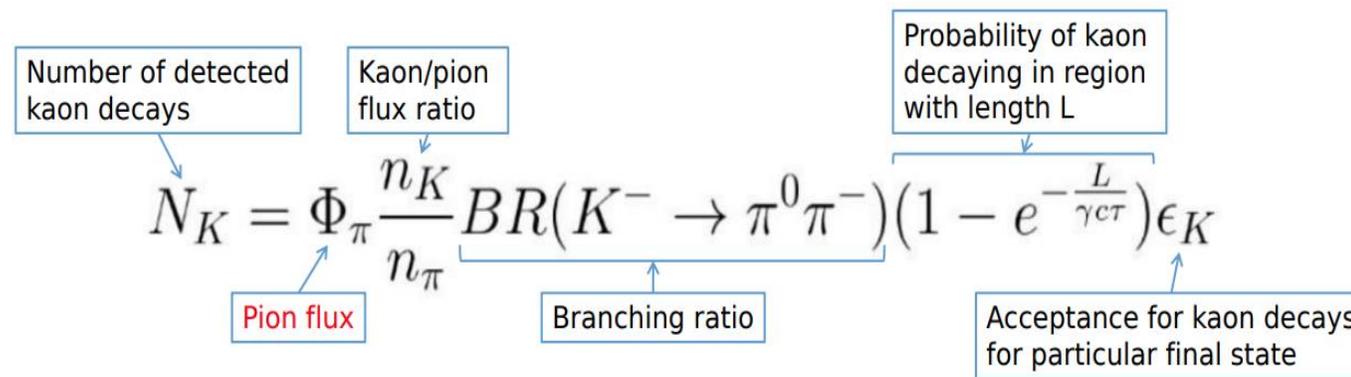


[M. Hoferichter, B. Kubis, and D. Sakkas, \*PRD\* \*\*86\*\* \(2012\) 116009](#)

- Needed for absolute cross section measurement: effective integrated luminosity (DAQ dead time taken into account)

$$\text{Effective luminosity: } L_{eff} = L \cdot (1 - \epsilon_{DAQ})$$

- Luminosity can be determined via free decays of beam kaons in the beam:
  - Use CEDARs to tag kaons
  - Measure free decays where no material
  - Exclusive events with zero momentum transfer



The diagram shows the equation 
$$N_K = \Phi_\pi \frac{n_K}{n_\pi} BR(K^- \rightarrow \pi^0 \pi^-) (1 - e^{-\frac{L}{\gamma c \tau}}) \epsilon_K$$
 with several annotations in boxes and arrows:

- Number of detected kaon decays** points to  $N_K$ .
- Pion flux** points to  $\Phi_\pi$ .
- Kaon/pion flux ratio** points to  $\frac{n_K}{n_\pi}$ .
- Branching ratio** points to  $BR(K^- \rightarrow \pi^0 \pi^-)$ .
- Probability of kaon decaying in region with length L** points to  $(1 - e^{-\frac{L}{\gamma c \tau}})$ .
- Acceptance for kaon decays for particular final state** points to  $\epsilon_K$ .

Decay channel	$\Gamma_i/\Gamma$	Remark
$K^- \rightarrow \mu^- \bar{\nu}_\mu$	$(63.56 \pm 0.11) \%$	Does not deposit energy in ECAL2 (Primakoff-trigger)
$K^- \rightarrow \pi^- \pi^0$	$(20.67 \pm 0.08) \%$	Similar systematics as Primakoff $\pi^- \rightarrow \pi^- \pi^0$ channel
$K^- \rightarrow \pi^- \pi^- \pi^+$	$(5.583 \pm 0.024) \%$	Does not deposit energy in ECAL2 (Primakoff-trigger)
$K^- \rightarrow e^- \pi^0 \bar{\nu}_e$	$(5.07 \pm 0.08) \%$	Non exclusive, missing energy
$K^- \rightarrow \mu^- \pi^0 \bar{\nu}_\mu$	$(3.352 \pm 0.033) \%$	Non exclusive, missing energy
$K^- \rightarrow \pi^- \pi^0 \pi^0$	$(1.760 \pm 0.023) \%$	Used to determine $\pi/K$ -ratio in the beam
others	$< 10^{-4}$	No significant contribution to background expected

- Different channels may form background for each other, but give possibility to crosscheck results

	Used for luminosity determination
	Considered as background process

$$L_{2\pi, \text{eff}} = 5.21 \pm 0.04_{\text{stat}} \text{ nb}^{-1}$$

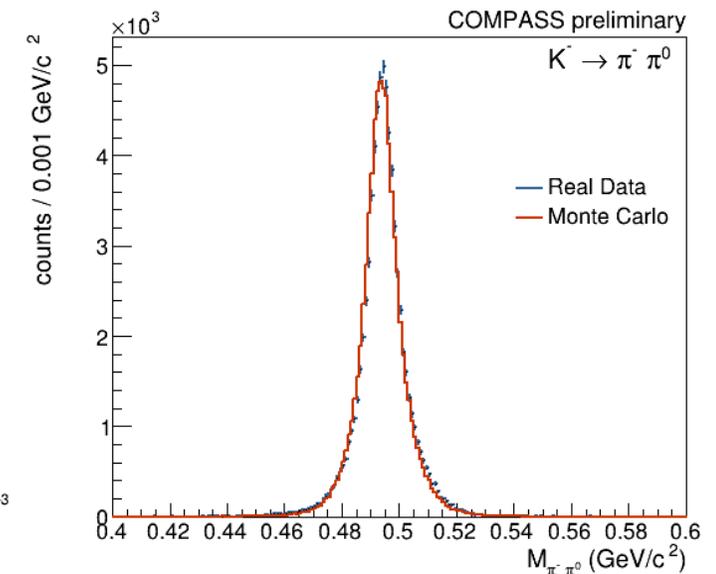
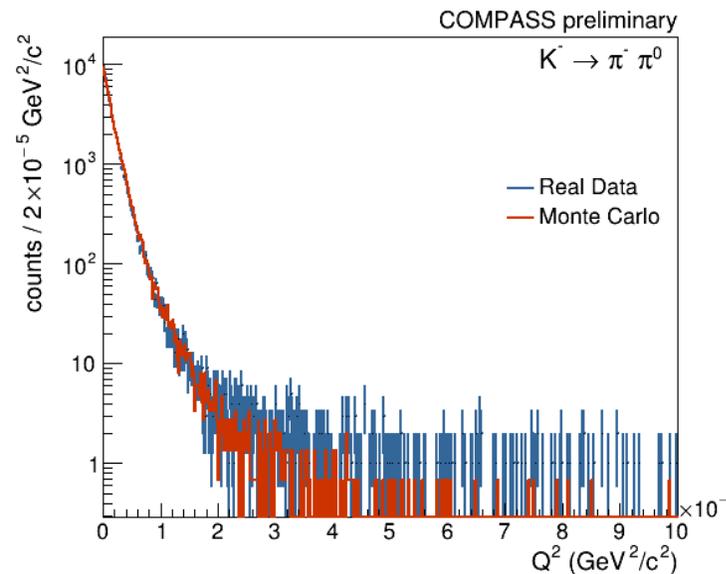
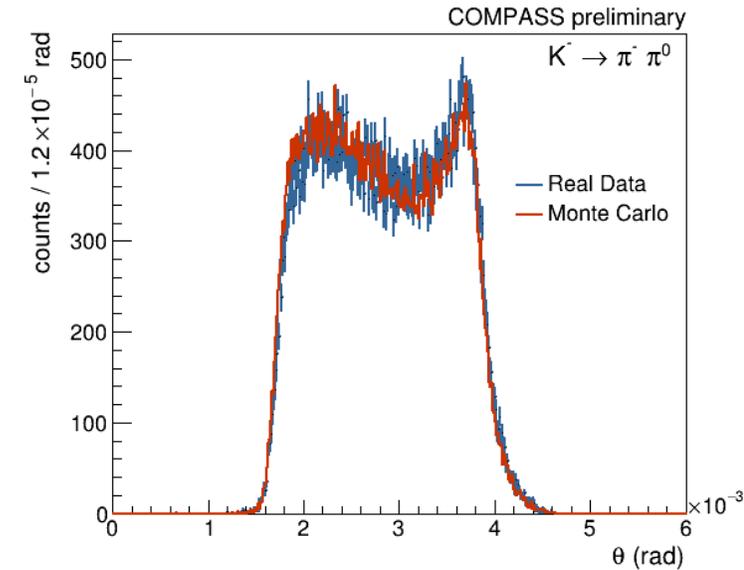
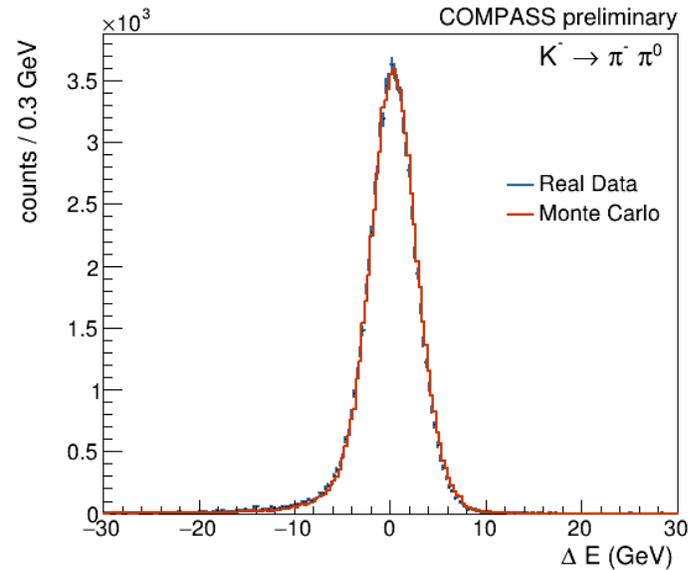
$$L_{3\pi, \text{eff}} = 5.06 \pm 0.12_{\text{stat}} \text{ nb}^{-1}$$

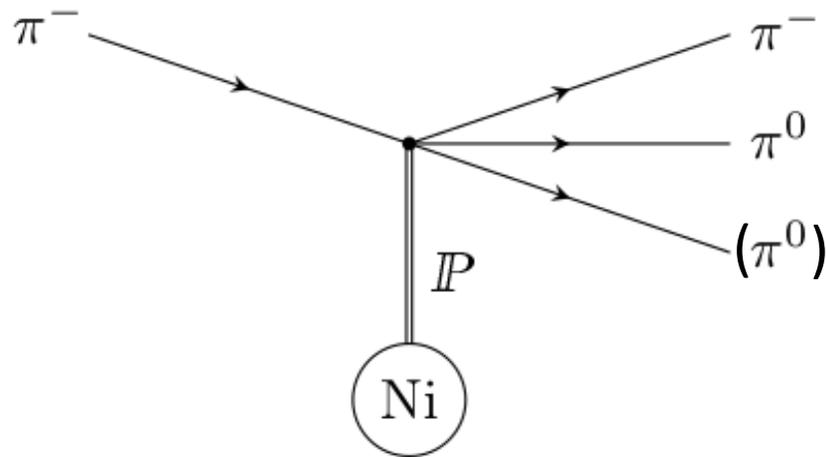
Largest contributions to systematic uncertainty:

- CEDAR tag efficiency: 7%
- ECAL reconstruction: 5%
- kaon/pion beam ratio: 2.5%

Result:

$$L_{\text{eff}} = 5.21 \pm 0.48_{\text{syst}} \pm 0.04_{\text{stat}}$$

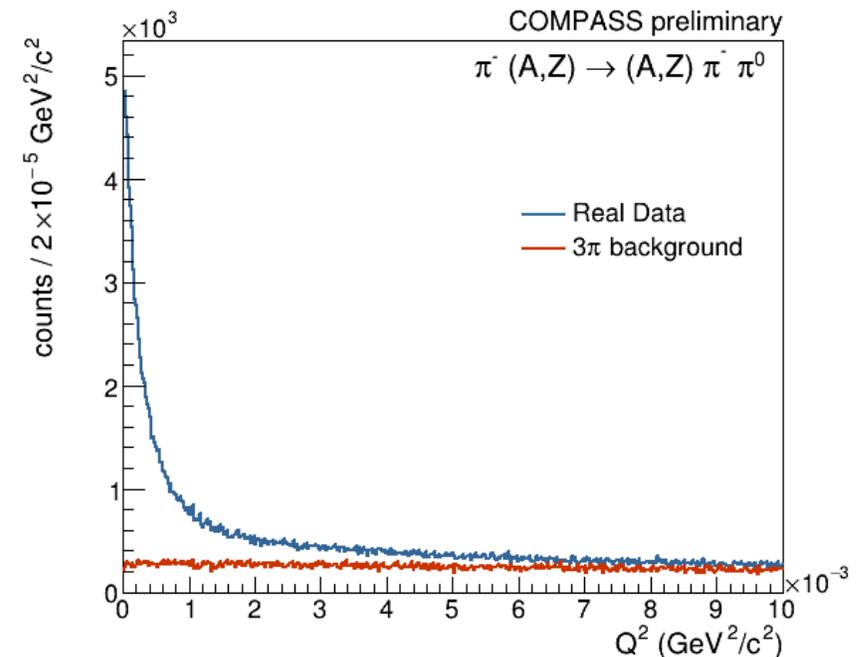




- $\pi^- \pi^0$ -final state forbidden by  $G$ -parity conservation
- Large cross section for  $\pi^- \pi^0 \pi^0$  final state  $\Rightarrow$  loss of one (soft)  $\pi^0$
- Approach: determine leakage from  $3\pi$  MC data with  $2\pi$  event selection

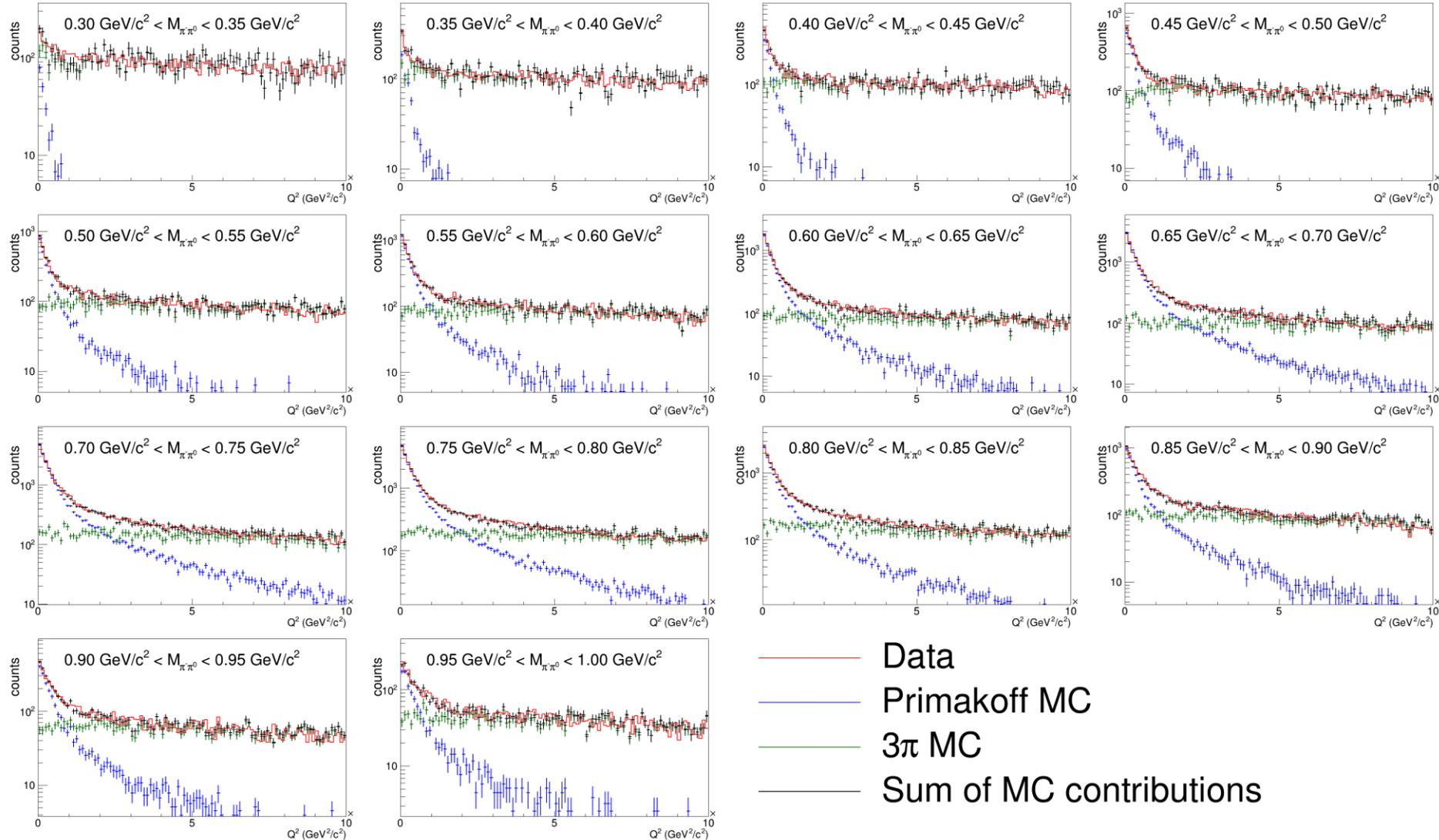
## Approach for $3\pi$ leakage:

- Select diffractive  $3\pi$  events
- Develop partial-wave model
- Weight  $3\pi$  Monte Carlo data set according to model
- Subtract from  $2\pi$  event sample

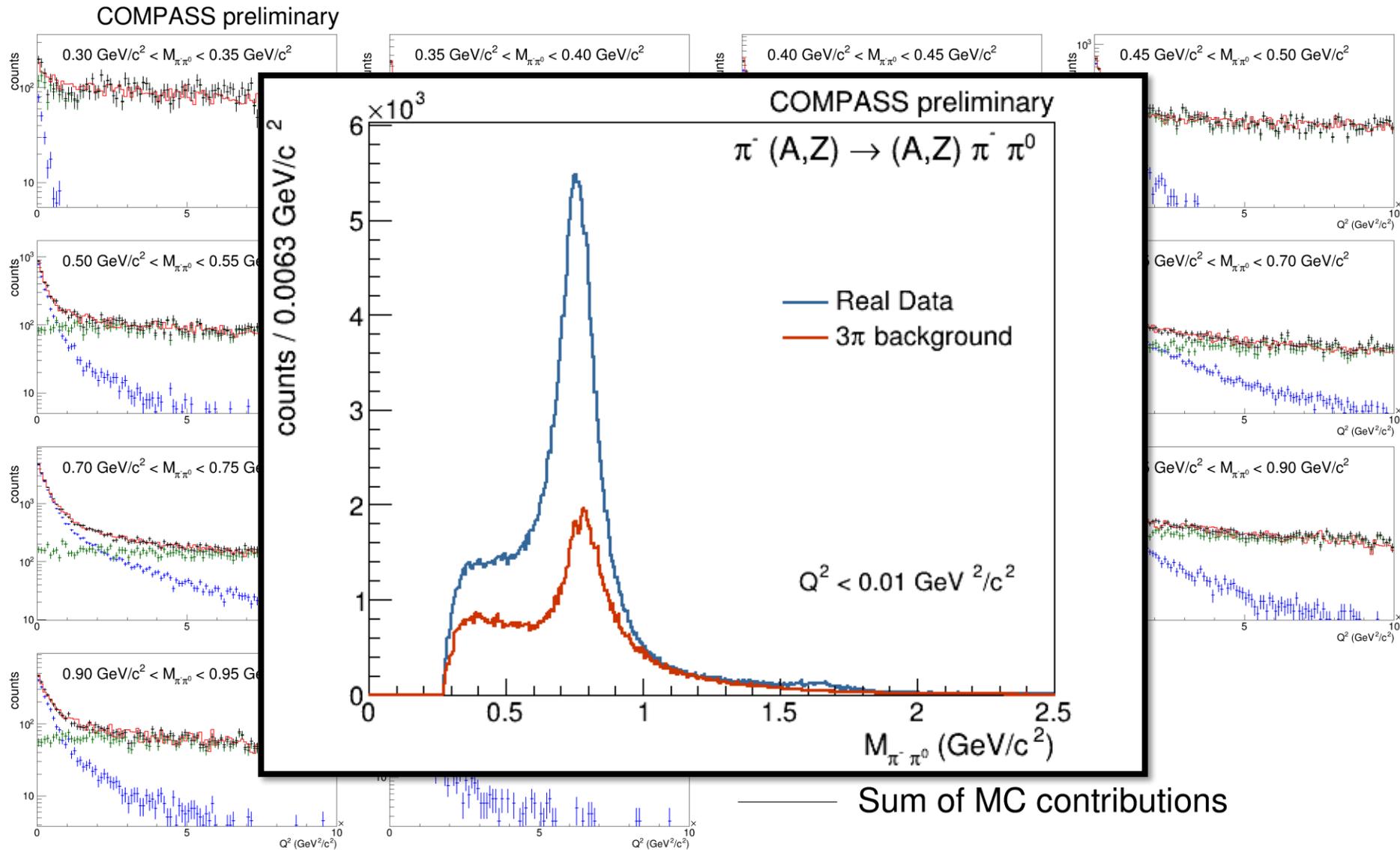


# Scaling of $3\pi$ Monte Carlo background prediction

COMPASS preliminary



# Scaling of $3\pi$ Monte Carlo background prediction



- Selection:  $Q^2 < 1.296 \cdot 10^{-3} \text{ GeV}^2/c^2$

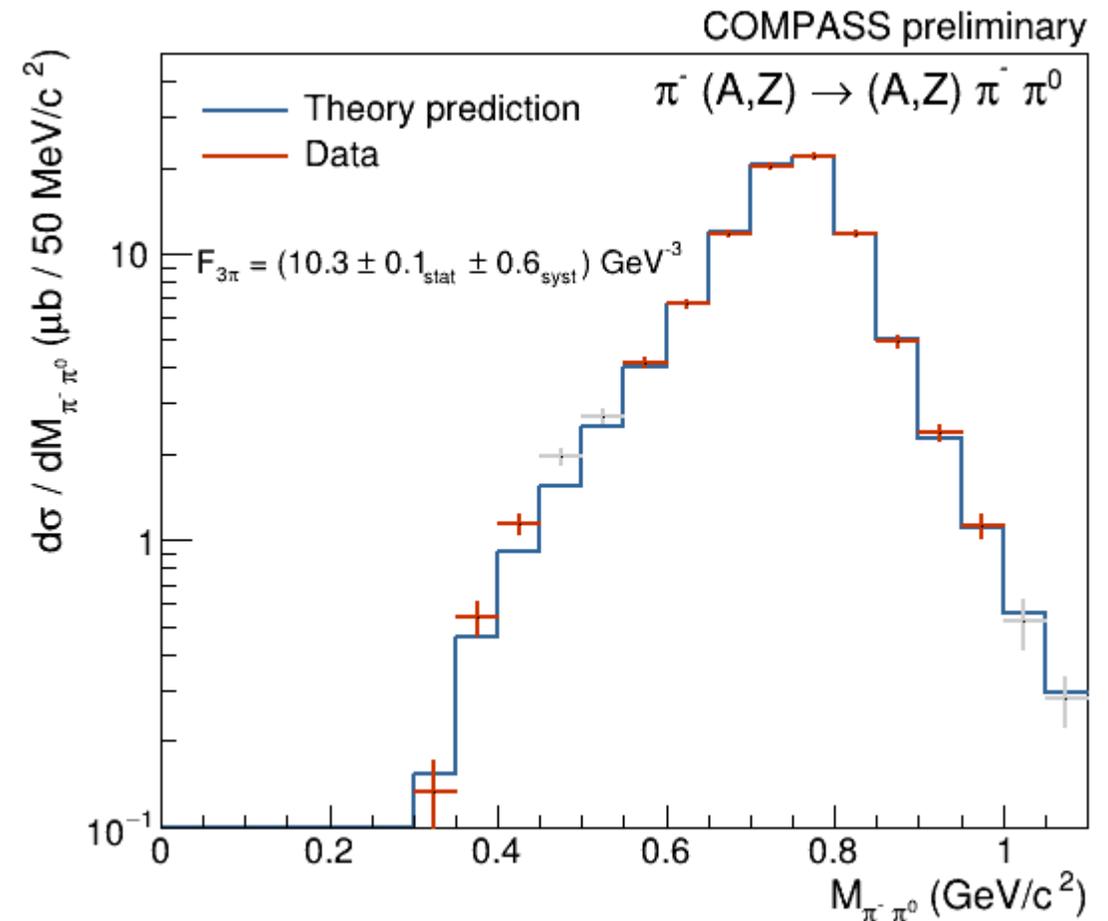
$$c_2^{(1)} = (10.5 \pm 0.1_{stat} \pm 0.6_{syst}) \text{ GeV}^{-3}$$

$$c_2^{(2)} = (24.5 \pm 0.1_{stat}^{+2.9}_{-1.4_{syst}}) \text{ GeV}^{-5}$$

$$F_{3\pi} = (10.3 \pm 0.1_{stat} \pm 0.6_{syst}) \text{ GeV}^{-3}$$

$$\Gamma_{\rho \rightarrow \pi\gamma} = \left( 76 \pm 1_{stat}^{+10}_{-8} \text{ }_{syst} \right) \text{ keV}$$

- Preliminary result for  $F_{3\pi}$  in agreement with theory prediction from ChPT
- Lower systematics to be expected



- COMPASS: First combined measurement of  $F_{3\pi}$  and  $\Gamma_{\rho \rightarrow \pi\gamma}$

$$F_{3\pi} = (10.3 \pm 0.1_{stat} \pm 0.6_{syst}) \text{GeV}^{-3}$$

$$\Gamma_{\rho \rightarrow \pi\gamma} = (76 \pm 1_{stat}^{+10} \pm 8_{syst}) \text{keV}$$

- Intensive test of systematics:
  - Different  $K^-$  decay channels
  - Studies on different background contributions ( $\omega$  and  $\pi$  exchange)
- Accompanied with intensive analysis of  $\pi^- \text{Ni} \rightarrow \pi^- \pi^0 \pi^0 \text{Ni}$  for background estimation

[Capraro, L. et al. NPB 288 \(1987\) 659-680](#) at CERN (SPS):

$$\Gamma_{\rho \rightarrow \pi\gamma} = (81 \pm 4 \pm 4) \text{keV}$$

Obtained by fitting  $d\sigma/dt$  distribution (separation of nuclear and Coulomb processes)

- Neglecting chiral production of  $\pi^- \pi^0$
- Presumably underestimation of systematics ( $3\pi$  leakage, beam composition)

$\Gamma(\pi^\pm \gamma)$						$\Gamma_3$
VALUE (keV)	DOCUMENT ID	TECN	CHG	COMMENT		
<b>68 ± 7</b>	<b>OUR FIT</b>			Error includes scale factor of 2.3.		
<b>68 ± 7</b>	<b>OUR AVERAGE</b>			Error includes scale factor of 2.2. See the ideogram below.		
81 ± 4 ± 4	CAPRARO	87	SPEC	-	200 $\pi^- \text{A} \rightarrow \pi^- \pi^0 \text{A}$	
59.8 ± 4.0	HUSTON	86	SPEC	+	202 $\pi^+ \text{A} \rightarrow \pi^+ \pi^0 \text{A}$	
71 ± 7	JENSEN	83	SPEC	-	156-260 $\pi^- \text{A} \rightarrow \pi^- \pi^0 \text{A}$	

- COMPASS: First combined measurement of  $F_{3\pi}$  and  $\Gamma_{\rho \rightarrow \pi\gamma}$

$$F_{3\pi} = (10.3 \pm 0.1_{stat} \pm 0.6_{syst}) \text{GeV}^{-3}$$

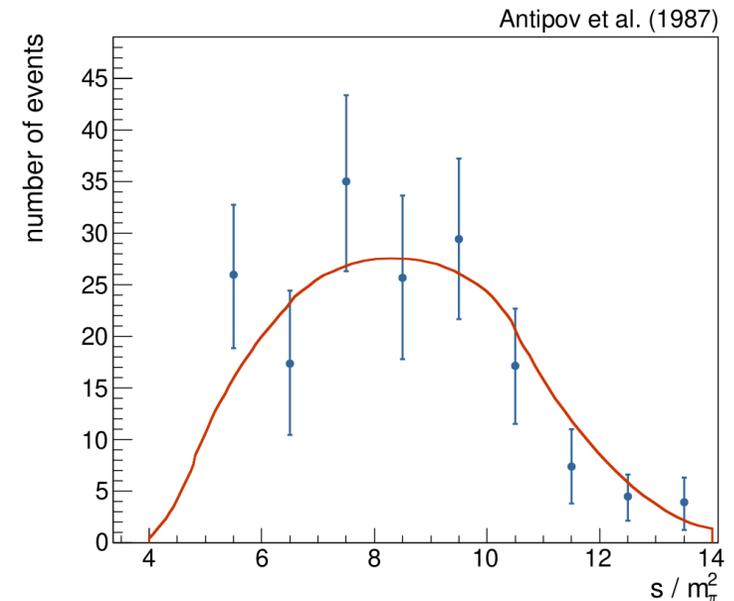
$$\Gamma_{\rho \rightarrow \pi\gamma} = (76 \pm 1_{stat}^{+10}_{-8} \pm 8_{syst}) \text{keV}$$

- Intensive test of systematics:
  - Different  $K^-$  decay channels
  - Studies on different background contributions ( $\omega$  and  $\pi$  exchange)
- Accompanied with intensive analysis of  $\pi^- \text{Ni} \rightarrow \pi^- \pi^0 \pi^0 \text{Ni}$  for background estimation

[Antipov, Y. et al. PRD 36 \(1987\) 101103](#)  
and reanalyzed by  
[Ametller, L. et al. PRD 64 \(2001\) 094009](#)

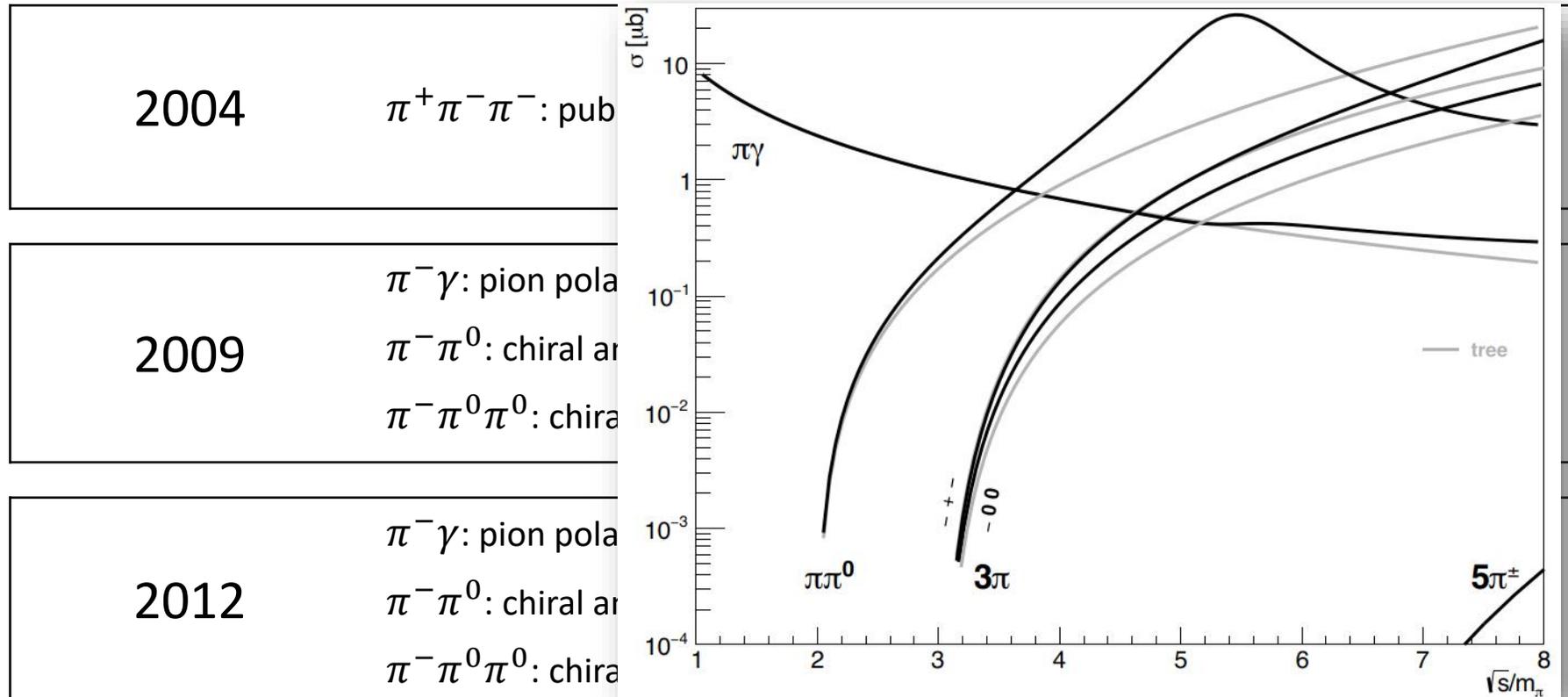
$$F_{3\pi} = (10.7 \pm 1.2) \text{GeV}^{-3}$$

- Neglecting  $s$ -channel production of  $\rho$  meson
- No proper consideration of systematics



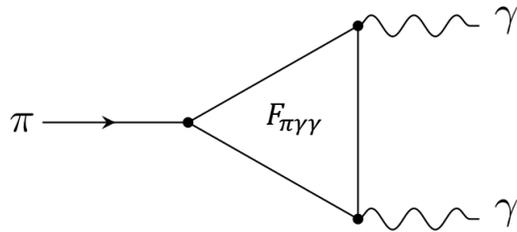
**Thank you for your attention**

2004	$\pi^+\pi^-\pi^-$ : published result	→ PRL 108 (2012) 192001
2009	$\pi^-\gamma$ : pion polarizabilities $\pi^-\pi^0$ : chiral anomaly $\pi^-\pi^0\pi^0$ : chiral dynamics	→ Phys. Rev. Lett. 114 (2015) 06002 Presented in this talk
2012	$\pi^-\gamma$ : pion polarizabilities $\pi^-\pi^0$ : chiral anomaly $\pi^-\pi^0\pi^0$ : chiral dynamics	4x larger data set compared to 2009 No results yet, MC still incomplete



- First definitive measurement of  $\pi^0$ -lifetime in 1963:

$$\tau_{\text{exp}}(\pi^0) = (9.5 \pm 1.5) \cdot 10^{-17} \text{ s} \neq \tau_{\text{PCAC}}(\pi^0) \approx 10^{-13} \text{ s}$$



- Adler, Bell, Jackiw, Bardeen 1969: calculation of triangle diagram

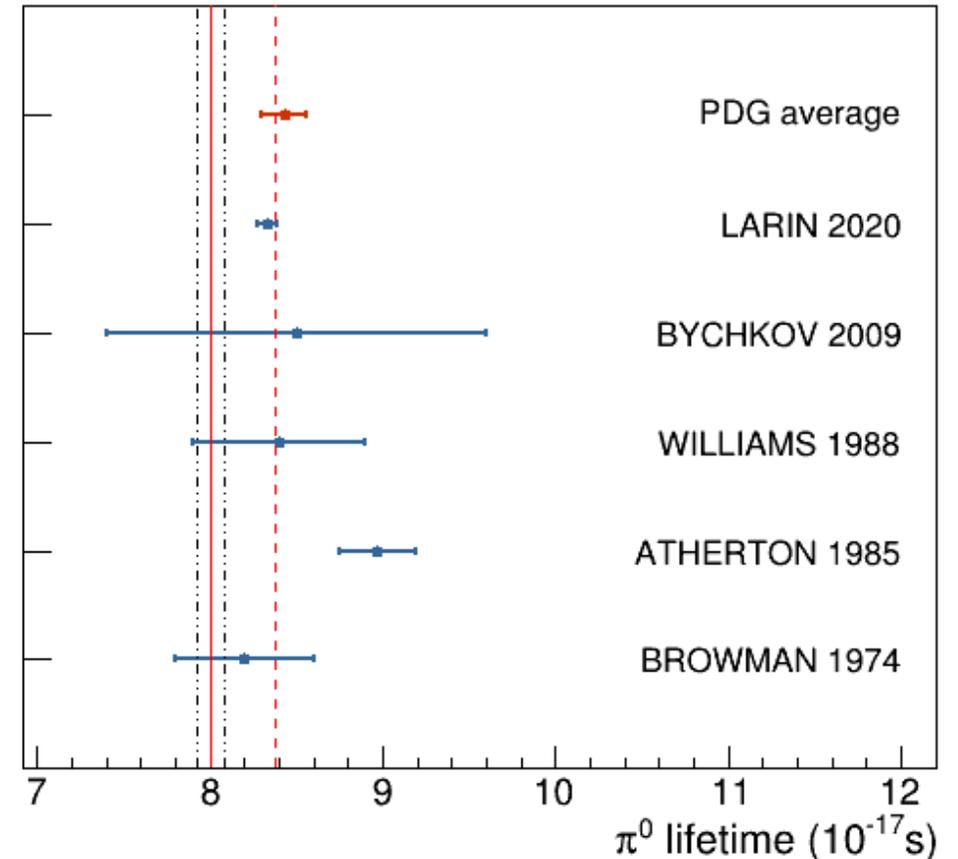
$$\Gamma^{\text{anom}}(\pi^0 \rightarrow \gamma\gamma) = F_{\pi\gamma\gamma}^2 \cdot \frac{m_{\pi^0}^3}{64\pi} = \left( \frac{e^2 N_c}{12\pi^2 F_\pi} \right)^2 \frac{m_{\pi^0}^3}{64\pi} = 7.75 \text{ eV}$$

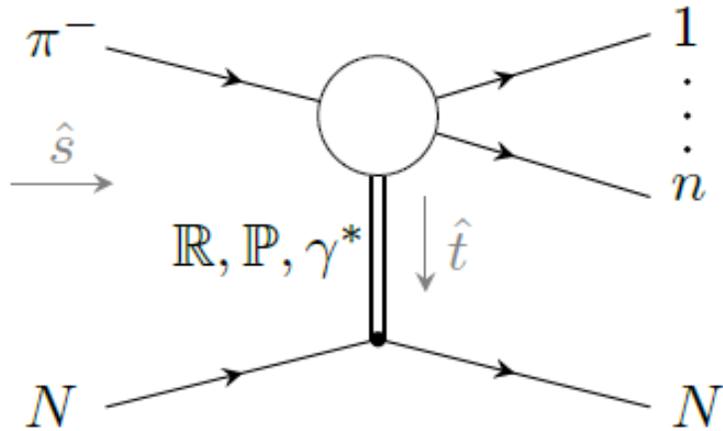
$$\begin{aligned} \tau(\pi^0) &= \text{BR}(\pi^0 \rightarrow \gamma\gamma) \cdot \frac{\hbar}{\Gamma^{\text{anom}}(\pi^0 \rightarrow \gamma\gamma)} \\ &= 8.38 \cdot 10^{-17} \text{ s} \end{aligned}$$

- Moussalam and Kampf 2009: NLO-calculation in chiral perturbation theory

$$\tau_{\text{NLO}}(\pi^0) = (8.04 \pm 0,11) \cdot 10^{-17} \text{ s}$$

$\pi^0$  lifetime measurements

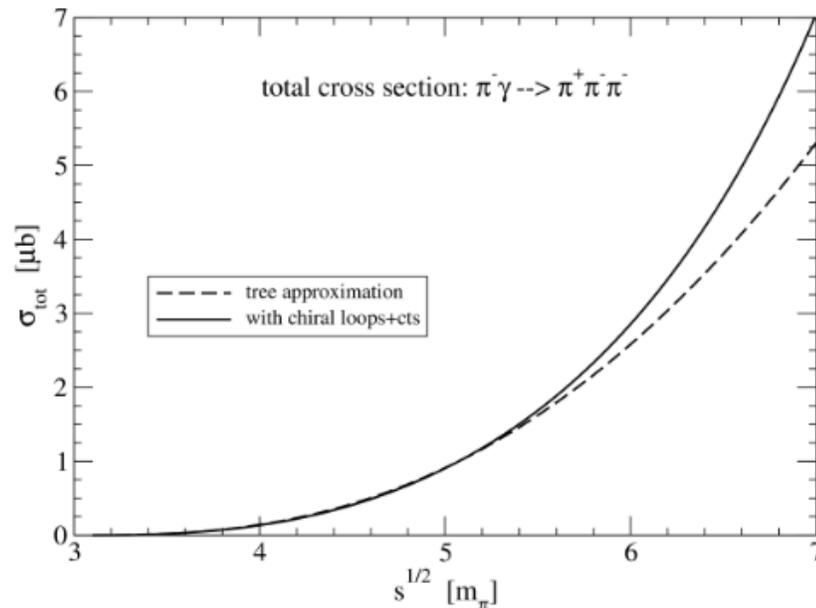
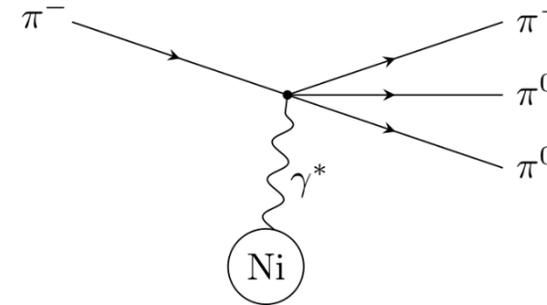




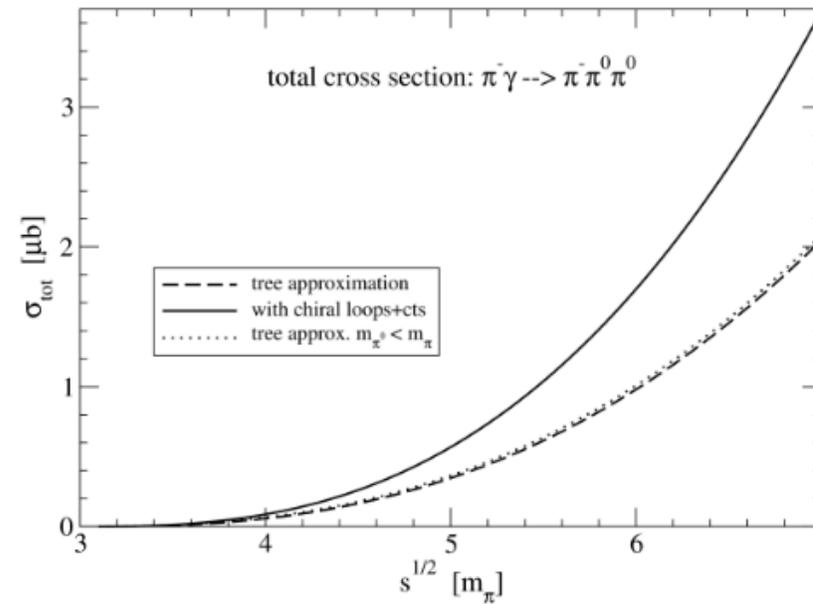
- Strong and electromagnetic production of mesons
- Electromagnetic production via Primakoff effect with sharp  $Q^2$  distribution
- Pomeron exchange:  $\pi^- \pi^0$  final state forbidden due to  $G$ -parity conservation, but: large cross-section for  $\pi^- \pi^0 \pi^0$ -final state  $\rightarrow$  loss of one (soft)  $\pi^0$  as main background

	Primakoff	$\mathbb{P}$ (strong)	$\mathbb{R}$ (strong)
$\sigma(s)$	$\propto \ln(\sqrt{s})$	$\propto \text{const.}$	$\propto 1/\sqrt{s}$
$\sigma(A_{\text{target}})$	$\propto \text{const.}$	$\propto A^{2/3}$	$\propto A^{2/3}$
$\sigma(Z_{\text{target}})$	$\propto Z^2$	$\propto \text{const.}$	$\propto \text{const.}$
$\sigma(t)$	$\propto \frac{Q^2 - Q_{\text{min}}^2}{Q^4} = \frac{\hat{t}'}{\hat{t}^2}$	$\propto e^{-b\hat{t}'}$	$\propto g(\hat{t}) \cdot e^{-b\hat{t}'}$ for small $\hat{t}$

- Direct (point-like) coupling of photon to 4 pions
- Prediction from ChPT at tree- and loop-level available

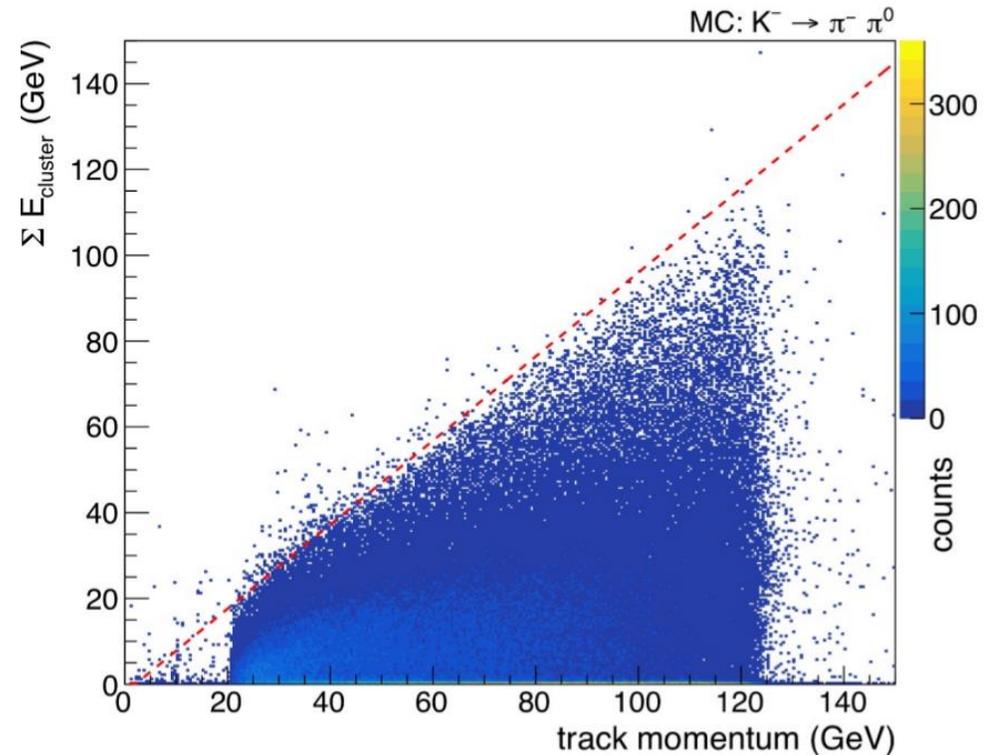
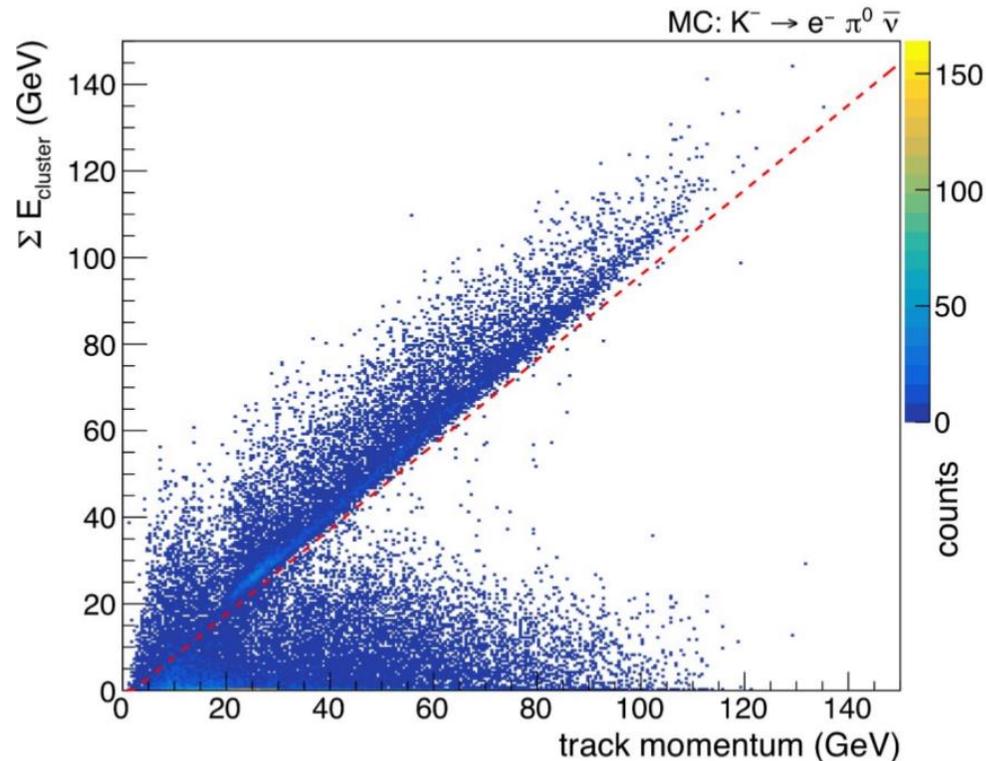


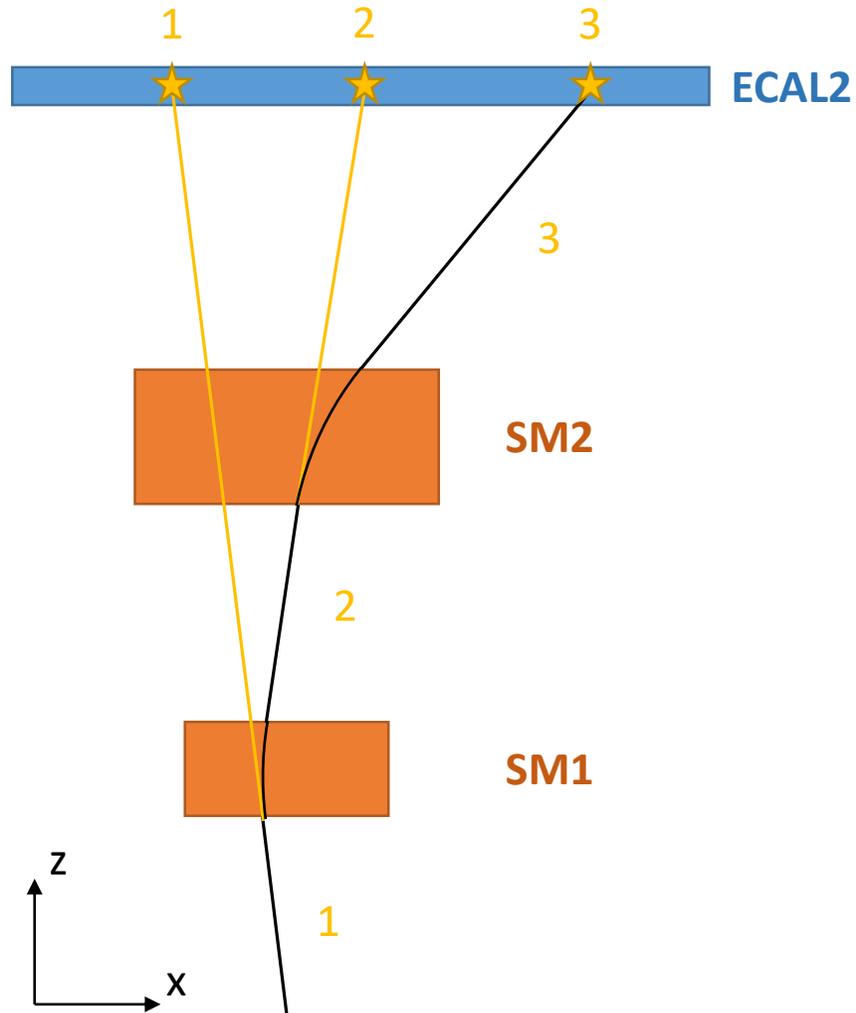
[Grabmüller S. \(2012\). Cryogenic Silicon Detectors and Analysis of Primakoff Contributions to the Reaction  \$\pi^- Pb \rightarrow\$](#)



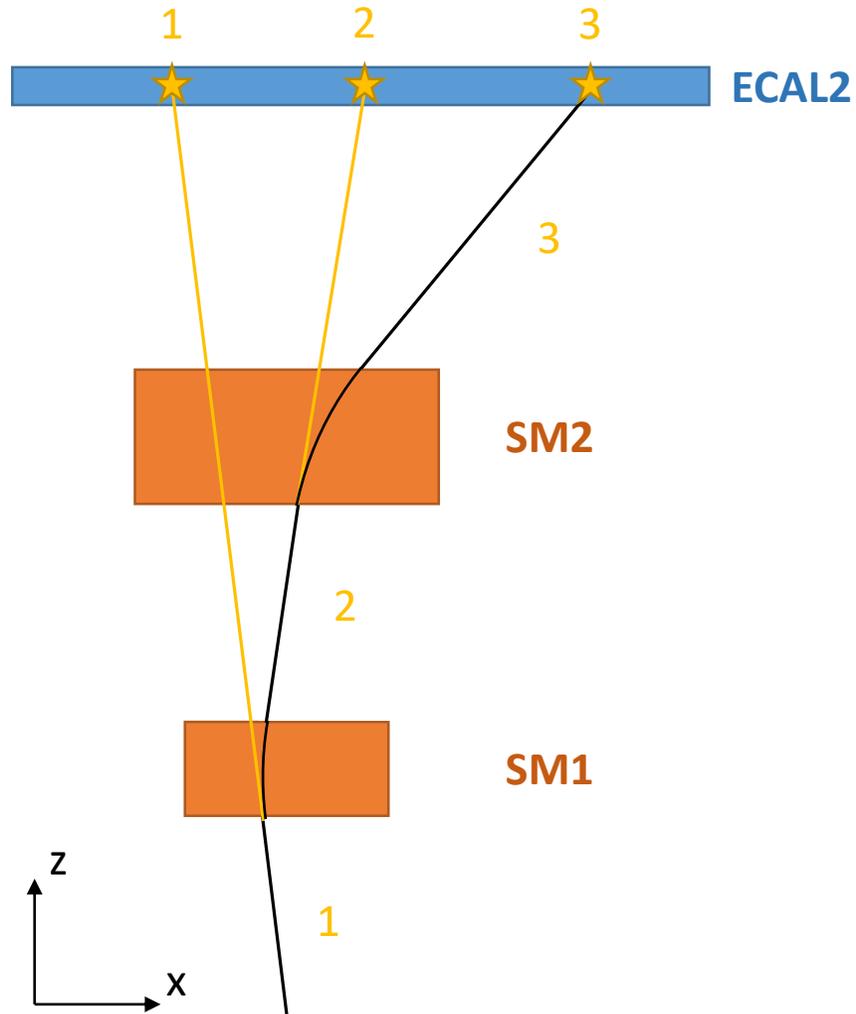
[Krämer M. \(2016\) Evaluation and Optimization of a digital calorimetric trigger and analysis of  \$\pi^- Ni \rightarrow\$](#)

- Naive idea:  $E/p$  in calorimeter
- Possible discrimination line can be identified
- Still: many electrons deposit less energy than expected
- Reason: energy loss due to Bremsstrahlung in the spectrometer





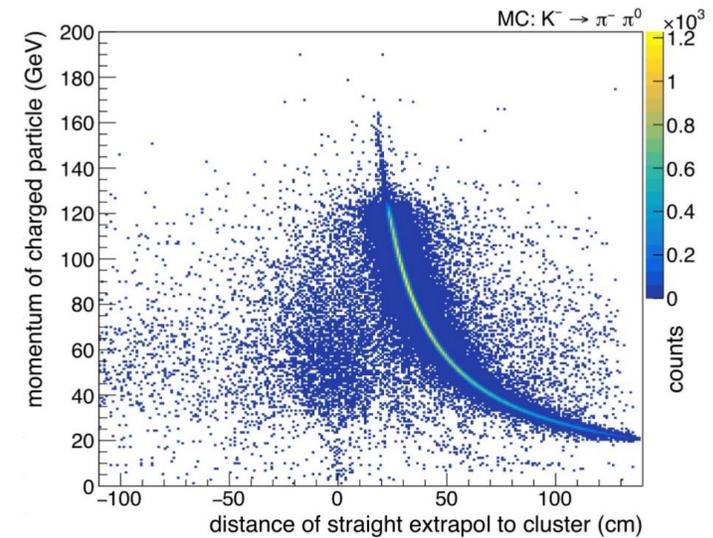
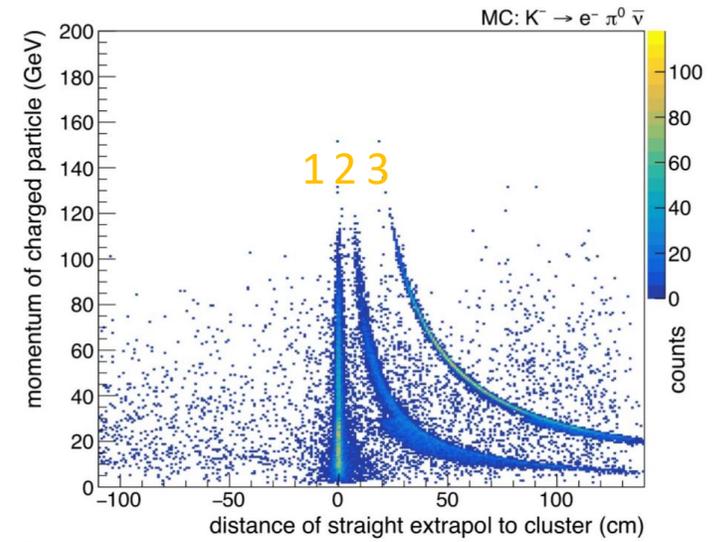
- Charged particle radiates photons while propagating through matter
- Deflection in dipole magnets dependent on momentum of charged track
- 3 distinct regions with increased probability for Bremsstrahlung
- Electrons have higher probability for Bremsstrahlung than pions



Electrons

vs

pions



- Selection:  $Q^2 < 1.296 \cdot 10^{-3} \text{ GeV}^2/c^2$
- Trigger on energy deposit in central part of electromagnetic calorimeter ( $E_{\text{trig}} > 68 \text{ GeV}$ )
- Minimum energy of  $\pi^0 \rightarrow$  maximum scattering angle of  $\pi^-$  in Gottfried-Jackson frame

