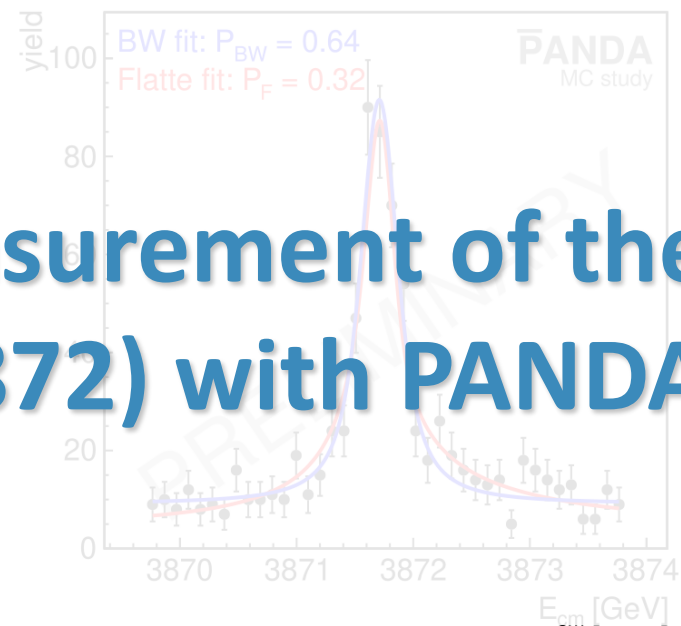


# Line shape measurement of the $\chi_{c1}(3872)$ with PANDA



**Klaus Götzen and Frank Nerling for the PANDA Collaboration**  
*GSI Darmstadt*

*PhiPsi Workshop 2022*

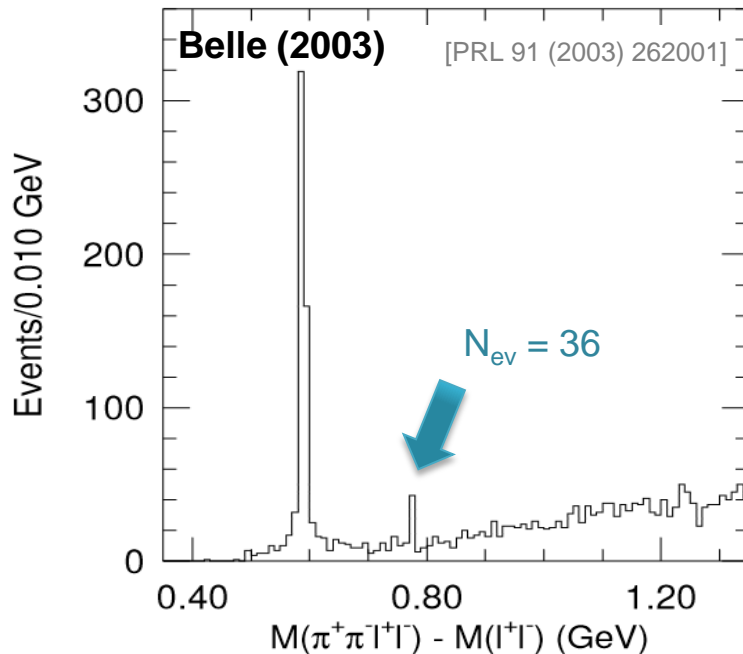
*13th International Workshop on  $e^+e^-$  Collisions from Phi to Psi*

*Aug. 15-19, 2022*

# INTRODUCTION

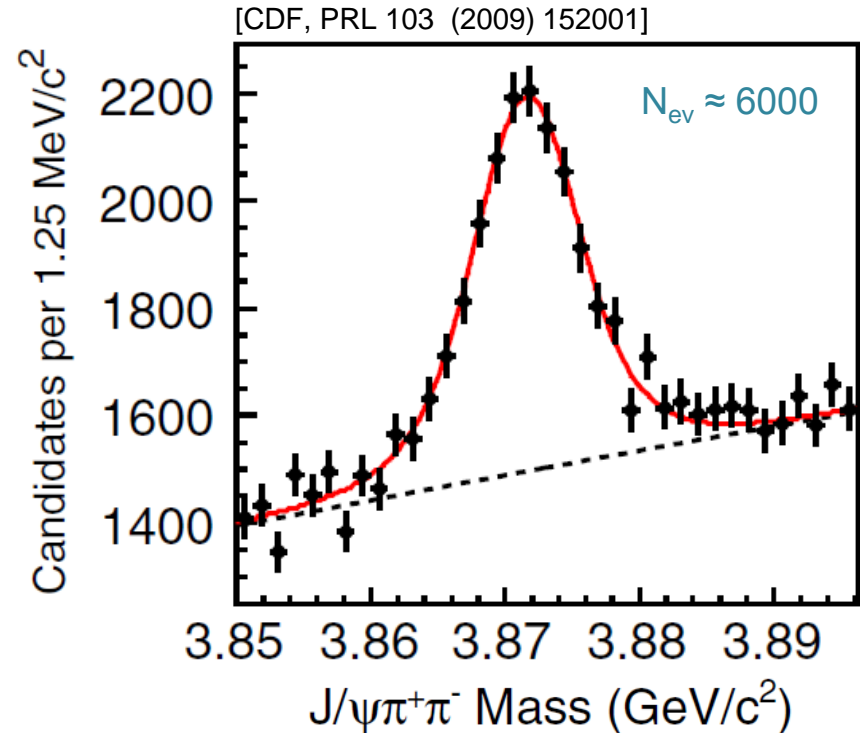
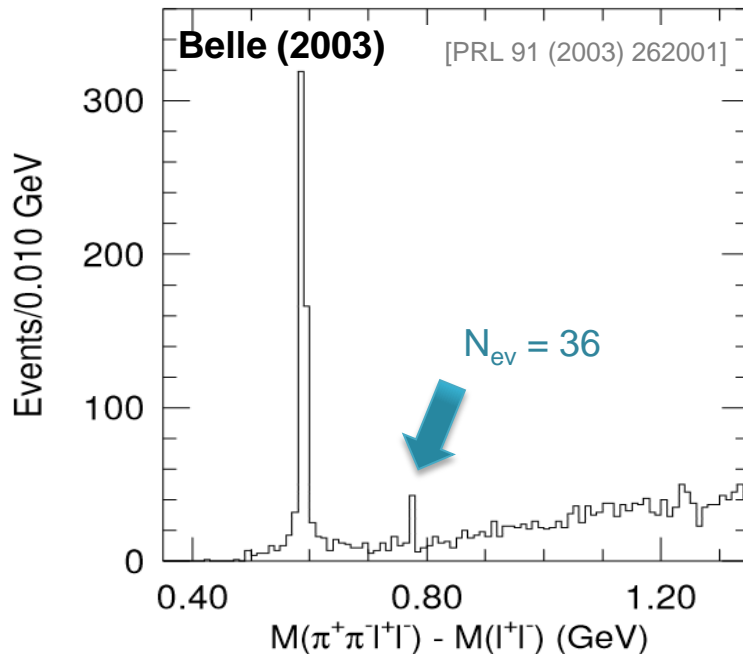
# Why Lineshapes are Important

- $\chi_{c1}(3872)$  discovered 2003 is 1<sup>st</sup> of charmonium-like XYZ states
- Nature is still **not understood even after 20 years!**



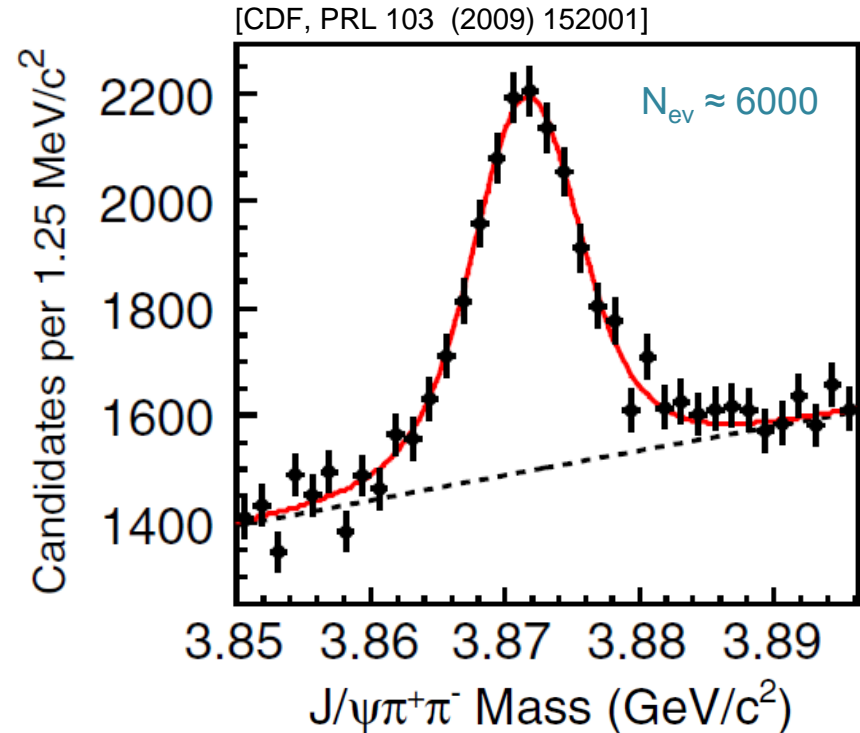
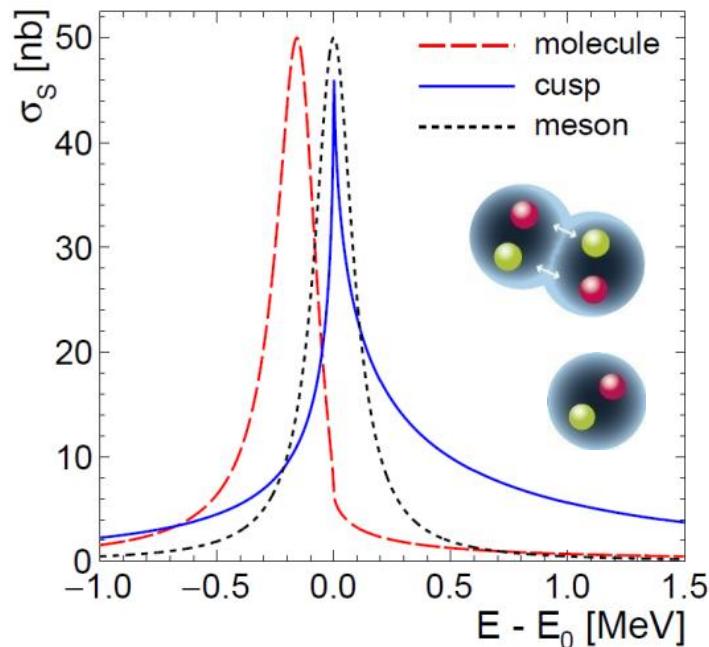
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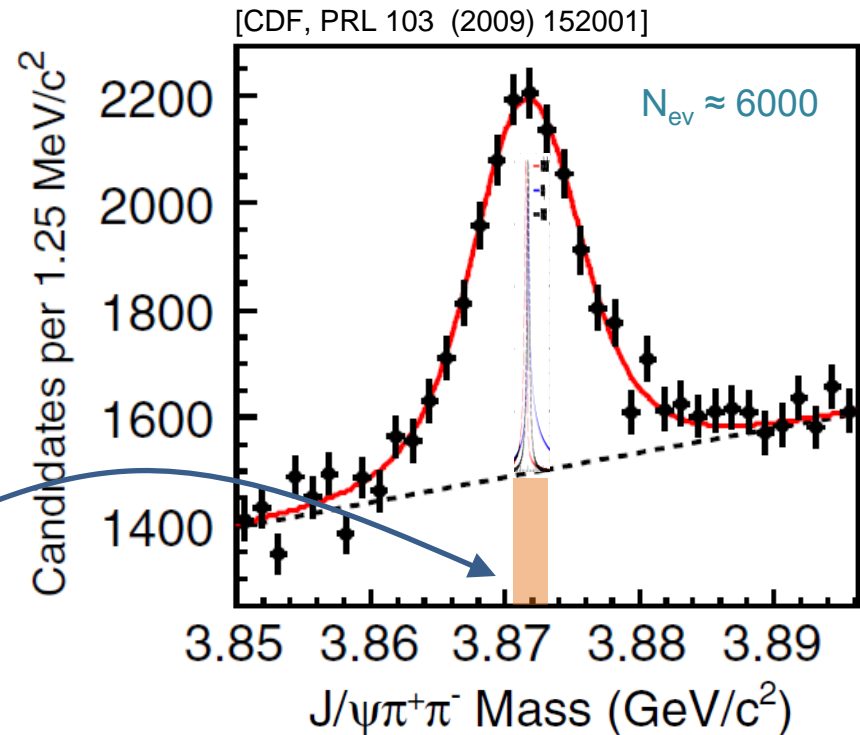
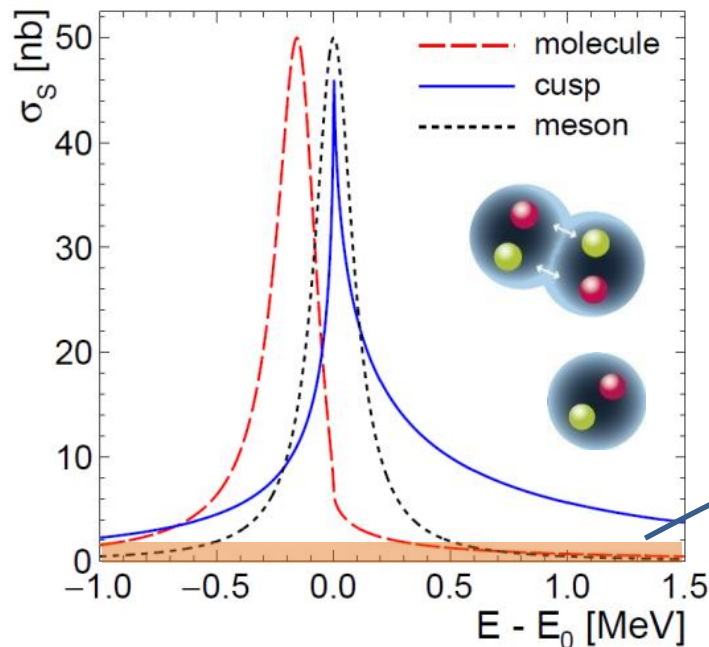
# Why Lineshapes are Important

- $\chi_{c1}(3872)$  discovered 2003 is 1<sup>st</sup> of charmonium-like XYZ states
- Possible solution:
  - Different internal structure  $\rightarrow$  different production/decay dynamics
  - Line shape of resonance reveals nature!



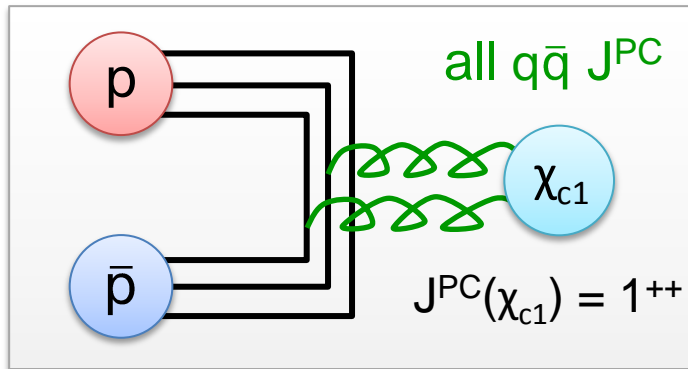
# Why Lineshapes are Important

- $\chi_{c1}(3872)$  discovered 2003 is 1<sup>st</sup> of charmonium-like XYZ states
- Possible solution:
  - Different internal structure  $\rightarrow$  different production/decay dynamics
  - Line shape of resonance reveals nature!
  - High resolution needed to resolve structures!



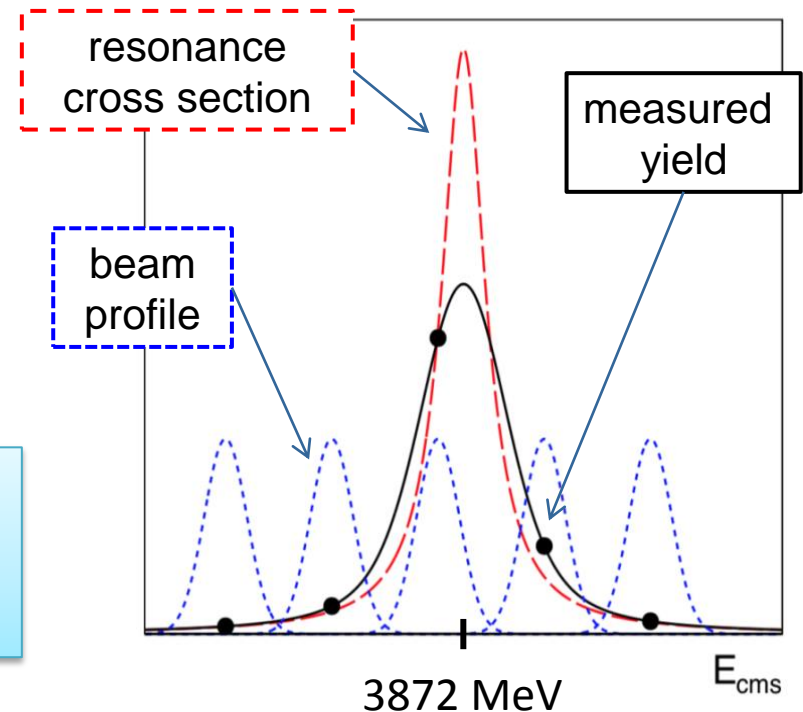
# Overcome Detector Resolution $\Rightarrow$ Formation

- Formation reaction  $\rightarrow$  produce  $\chi_{c1}(3872)$  [ $J^{PC} = 1^{++}$ ] w/o recoils



- Beam energy spread  $\rightarrow$  resolution
- Measure yield at different  $E_{\text{cms}}$

Typical Detector Resolution  $\approx 5 \text{ MeV}$   
PANDA Beam Resolution  $\approx 0.05 \text{ MeV}$

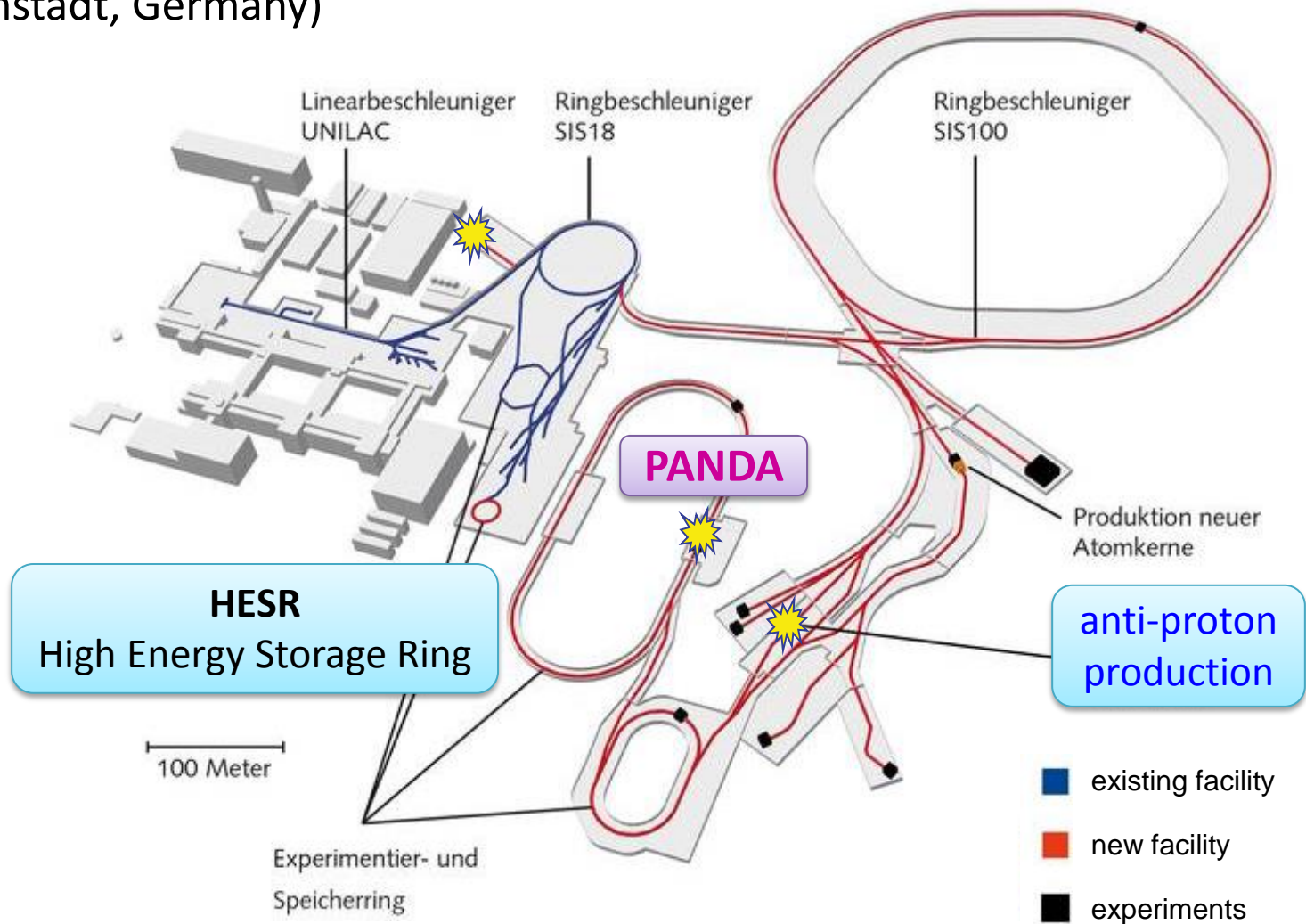


PANDA at FAIR



# PANDA at FAIR

Facility for Antiproton and Ion Research  
(GSI, Darmstadt, Germany)





# FAIR Construction Site

- Good progress at construction site





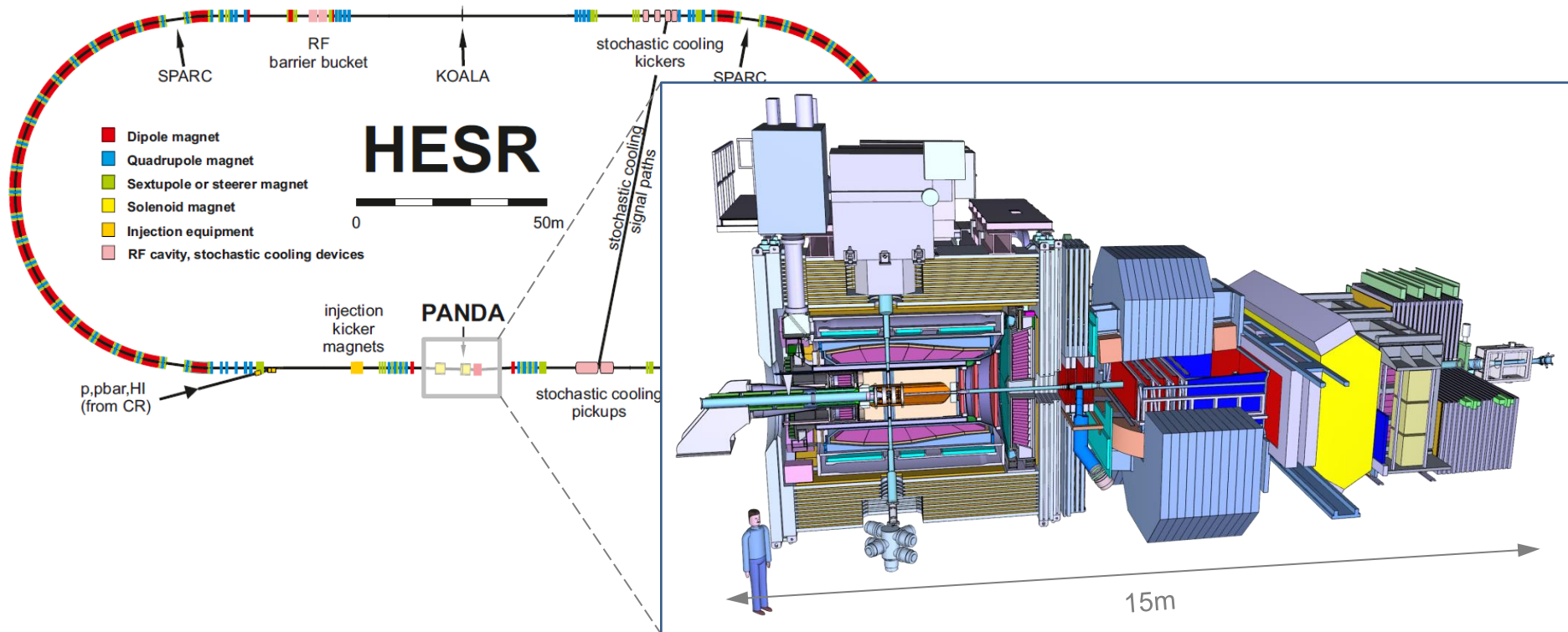
# FAIR Construction Site

- Good progress at construction site

April 2022  
Transfer building



# PANDA and HESR



HESR mode	$dp/p$	$L_{\max}$ [1/cm <sup>2</sup> ·s]	$dE_{\text{cm}}$ [keV]
High Luminosity (HL)	$1 \cdot 10^{-4}$	$2.0 \cdot 10^{32}$	168
High Resolution (HR)	$2 \cdot 10^{-5}$	$2.0 \cdot 10^{31}$	34
Phase 1 Mode (P1)	$5 \cdot 10^{-5}$	$2.0 \cdot 10^{31}$	84

@  $E_{\text{cm}} = 3872 \text{ MeV}$

# SENSITIVITY STUDY



# Comprehensive Sensitivity Study

Eur. Phys. J. A (2019) 55: 42  
DOI 10.1140/epja/i2019-12718-2

[<https://arxiv.org/abs/1812.05132>]

THE EUROPEAN  
PHYSICAL JOURNAL A

Regular Article – Experimental Physics

## Precision resonance energy scans with the PANDA experiment at FAIR

Sensitivity study for width and line shape measurements of the  $X(3872)$

- Reaction:  $\bar{p}p \rightarrow \chi_{c1}(3872) \rightarrow J/\psi (\rightarrow e^+e^- / \mu^+\mu^-) \rho^0 (\rightarrow \pi^+\pi^-)$
- Determine the precision for line-shape measurement at PANDA of
  - Breit-Wigner Width  $\Gamma$
  - Flatté Energy  $E_f$
- Investigated Parameter Space:

Total beam time:  $T = 40 \times 2d = 80 d$

Cross section assumption:  $\sigma_{\text{peak}}(\bar{p}p \rightarrow \chi_{c1}) = 20 \dots 150 \text{ nb}$

BW Width:  $\Gamma = [50, 70, 100, 180, 250, 500] \text{ keV}$

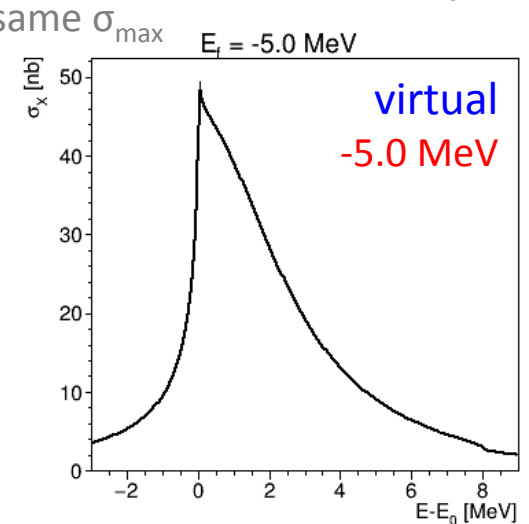
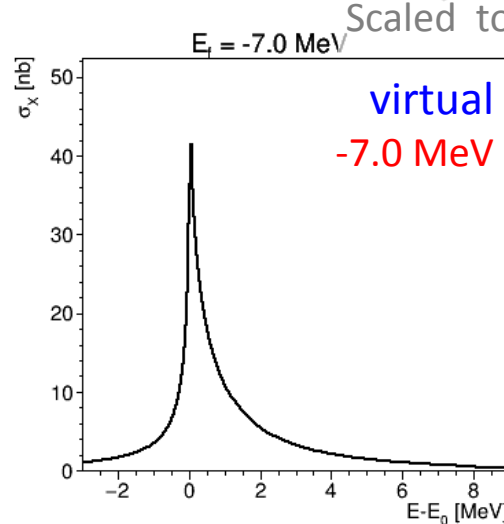
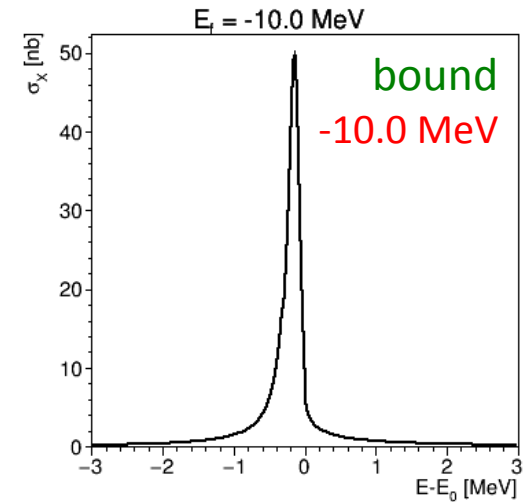
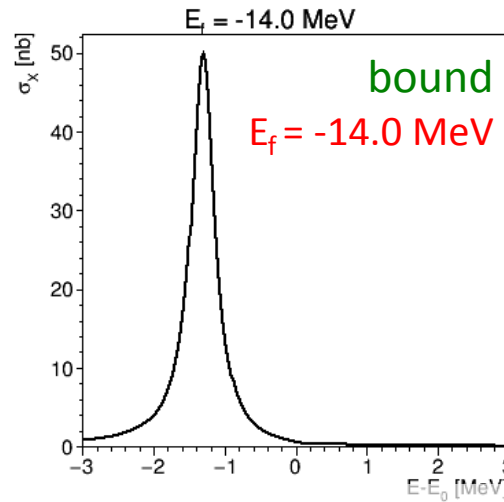
Flatté energy:  $E_f = [-10.0, -9.5, -9.0, -8.8, -8.3, -8.0, -7.5, -7.0] \text{ MeV}$

# Flatté Model

- Line shapes for Flatté model [Hanhart et al, PRD 76 (2007) 034007]
- Channel:  $\chi_{c1}(3872) \rightarrow J/\psi \rho^0$

$$\sigma(E; E_f) \sim \frac{\Gamma_{\pi^+\pi^- J/\psi}(E)}{|D(E; E_f)|^2}$$

(with  $f_\rho=0.00047$ ,  $f_\omega=0.00271$ ,  
 $g=0.137$ ,  $\Gamma_0=1.0$  MeV)

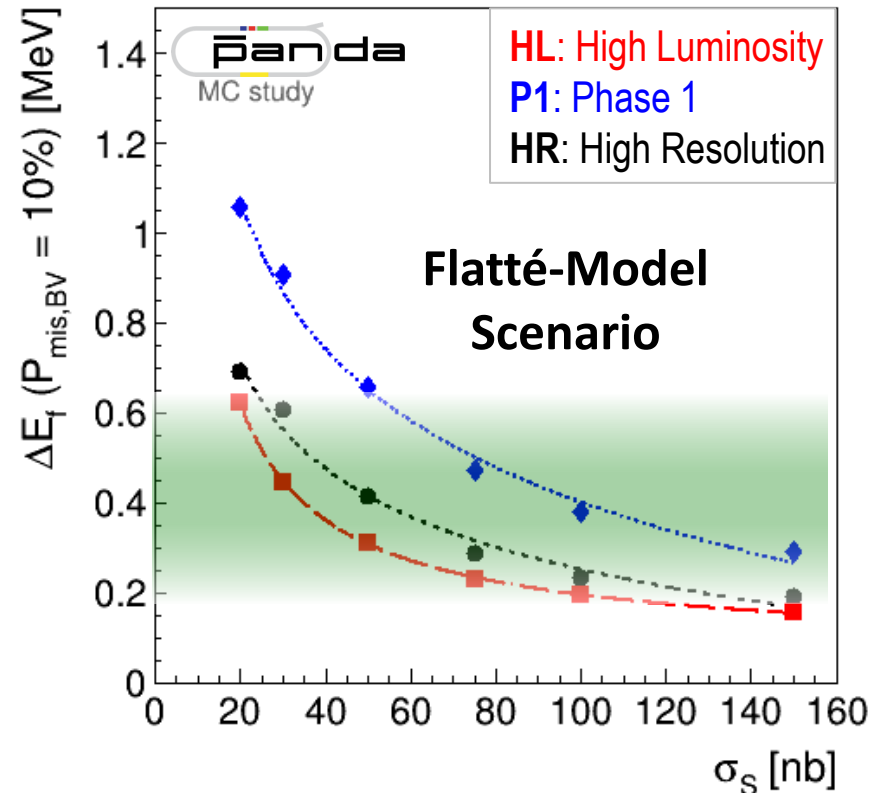
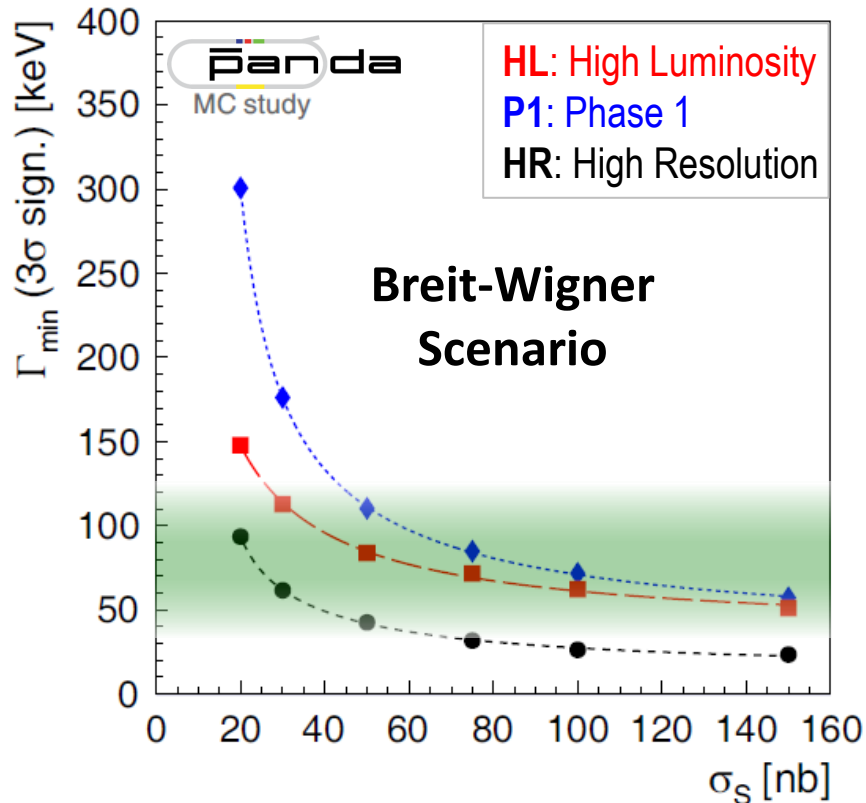


Scaled to same  $\sigma_{\text{max}}$

# Precise Line Shape Sensitivity Study

- Expected **sensitivity** for **BW Width  $\Gamma$**  & **Flatté Parameter  $E_f$**
- **Breit-Wigner**:  $3\sigma$  precision at down to  $\Gamma = \mathcal{O}(50 - 100)$  keV!
- **Flatté**: Precision in **sub-MeV range**!

[Eur. Phys. J. A 55 (2019) 3, 42, arXiv:1812.05132]





# LHCb Measurement of $\chi_{c1}(3872)$



[Phys.Rev.D 102 (2020) 9, 092005]  
[https://arxiv.org/abs/2005.13419]

CERN-EP-2020-086  
LHCb-PAPER-2020-008  
May 27, 2020

## Study of the lineshape of the $\chi_{c1}(3872)$ state

### Abstract

A study of the lineshape of the  $\chi_{c1}(3872)$  state is made using a data sample corresponding to an integrated luminosity of  $3\text{fb}^{-1}$  collected in  $pp$  collisions at centre-of-mass energies of 7 and 8 TeV with the LHCb detector. Candidate  $\chi_{c1}(3872)$  mesons from  $b$ -hadron decays are selected in the  $J/\psi\pi^+\pi^-$  decay mode. Describing the lineshape with a Breit–Wigner function, the mass splitting between the  $\chi_{c1}(3872)$  and  $\psi(2S)$  states,  $\Delta m$ , and the width of the  $\chi_{c1}(3872)$  state,  $\Gamma_{\text{BW}}$ , are determined to be

$$\begin{aligned}\Delta m &= 185.588 \pm 0.067 \pm 0.068 \text{ MeV}, \\ \Gamma_{\text{BW}} &= 1.39 \pm 0.24 \pm 0.10 \text{ MeV},\end{aligned}$$

where the first uncertainty is statistical and the second systematic. Using a Flatté-inspired lineshape, two poles for the  $\chi_{c1}(3872)$  state in the complex energy plane are found. The dominant pole is compatible with a quasi-bound  $D^0\bar{D}^{*0}$  state but a quasi-virtual state is still allowed at the level of 2 standard deviations.

# LHCb Findings

- Breit Wigner fit

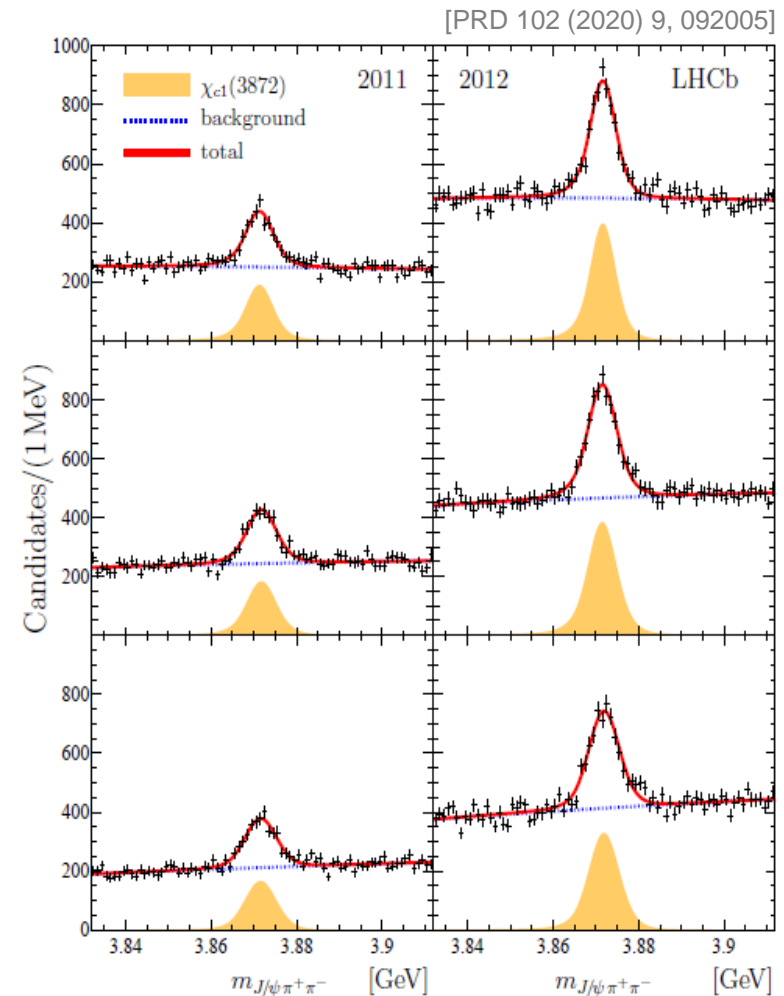
$$m_{\chi_{c1}(3872)} = 3871.695 \pm 0.067 \pm 0.068 \pm 0.010 \text{ MeV}$$

$$\Gamma_{\text{BW}} = 1.39 \pm 0.24 \pm 0.10 \text{ MeV}$$

[previous Belle result:  $\Gamma < 1.2 \text{ MeV}$  (CL90)]

- Flatté model fit

Mode [MeV]		Mean [MeV]	FWHM [MeV]
$3871.69^{+0.00+0.05}_{-0.04-0.13}$		$3871.66^{+0.07+0.11}_{-0.06-0.13}$	$0.22^{+0.06+0.25}_{-0.08-0.17}$
$g$	$f_\rho \times 10^3$	$\Gamma_0$ [MeV]	$m_0$ [MeV]
$0.108 \pm 0.003$	$1.8 \pm 0.6$	$1.4 \pm 0.4$	3864.5 (fixed)
(Flatté energy $E_f = -7.2 \text{ MeV}$ )			



# LHCb Findings

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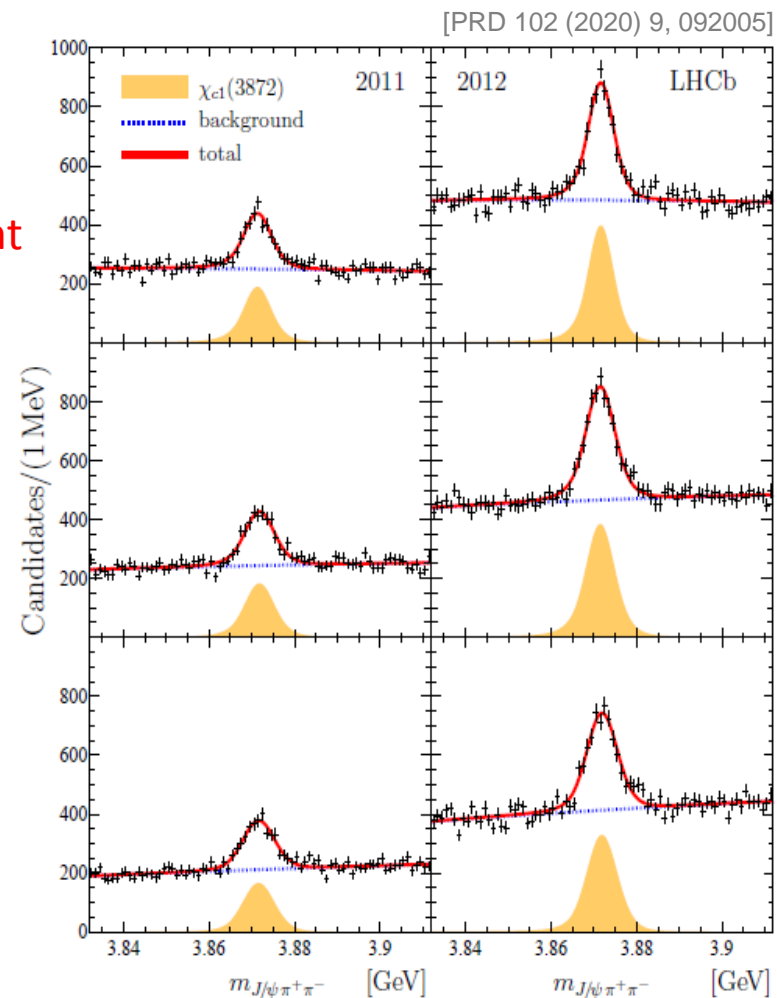
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Factor 6.3, analysis dependent

- Flatté model fit

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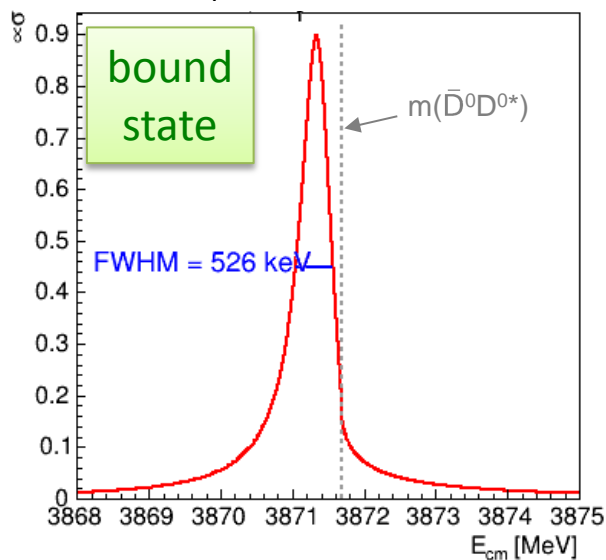
→ Need to discriminate models!



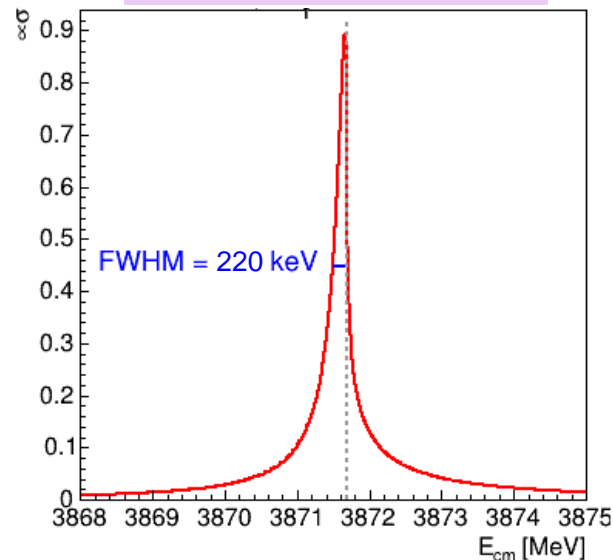
# $J/\psi\pi^+\pi^-$ Lineshapes

- Flatté Model with LHCb setting  
⇒ Slight changes in  $E_f$  range

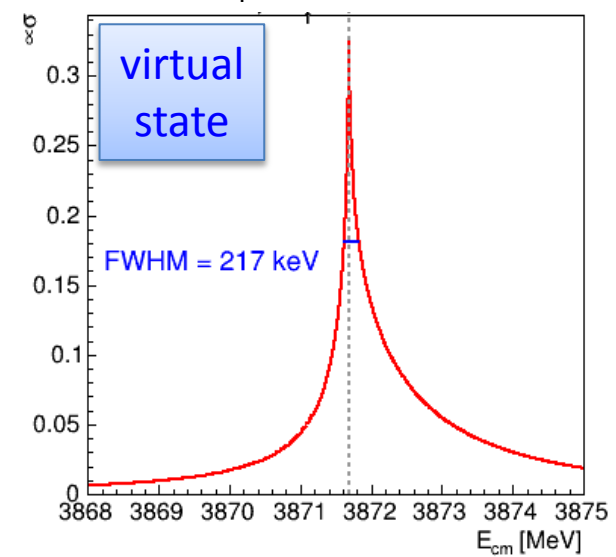
$E_f = -8.7$  MeV



set by LHCb  
 $E_f = -7.2$  MeV



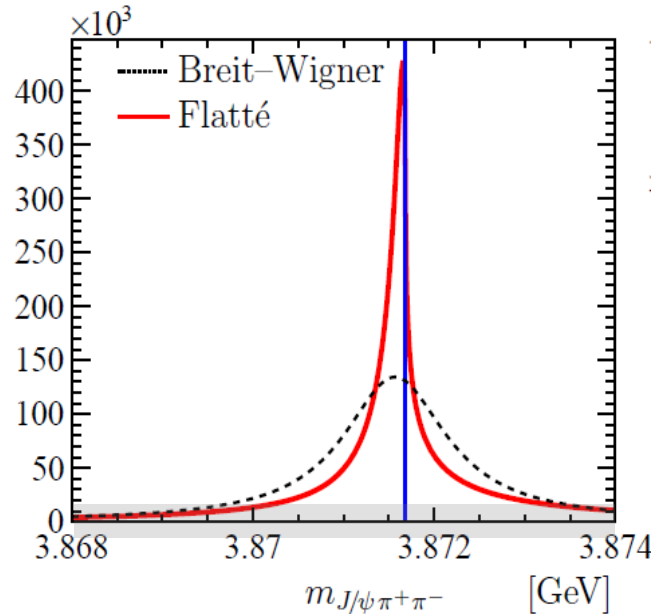
$E_f = -5.7$  MeV



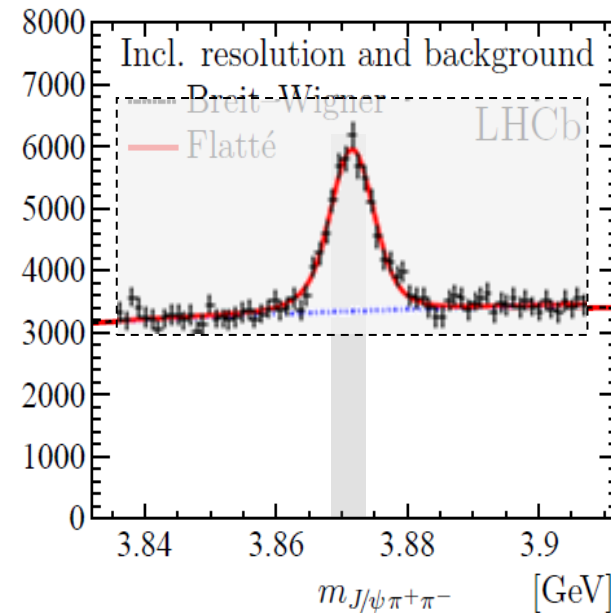
[Hanhart et al, PRD 76 (2007) 034007]

# LHCb Lineshapes (incl Resolution)

Original lineshapes



Lineshapes with resolution ( $\sim 2.6$  MeV)



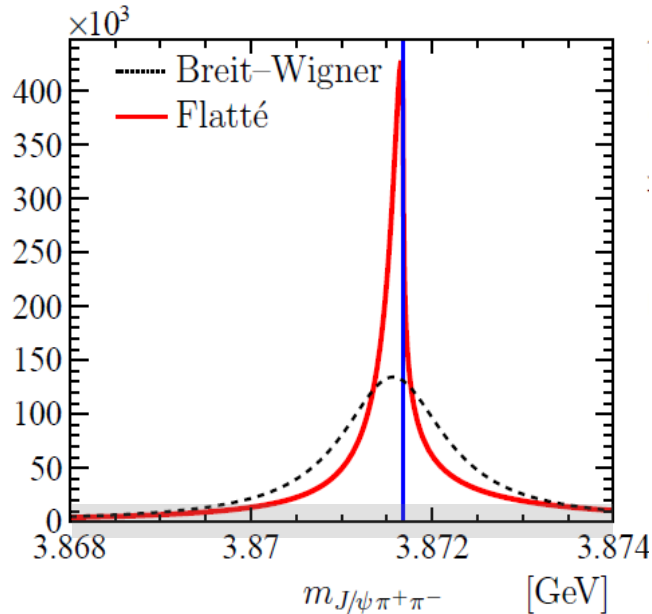
- Quote LHCb:

## 7.3 Comparison between Breit-Wigner and Flatté lineshapes

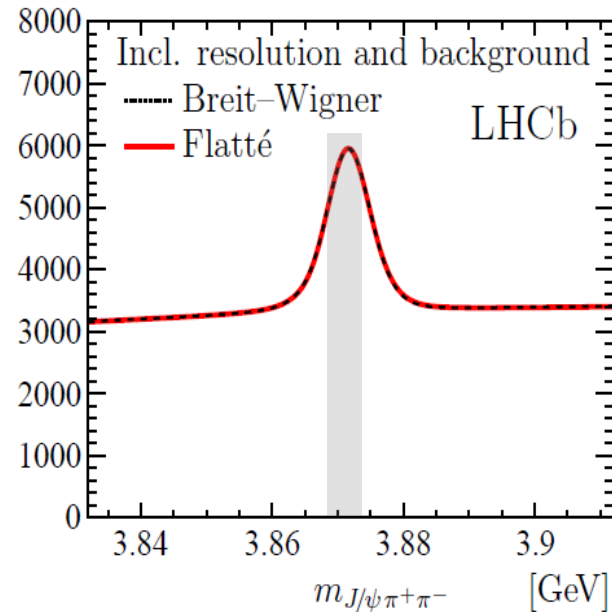
Figure 4 shows the comparison between the Breit-Wigner and the Flatté lineshapes. While in both cases the signal peaks at the same mass, the Flatté model results in a significantly narrower lineshape. However, after folding with the resolution function and adding the background, the observable distributions are indistinguishable.

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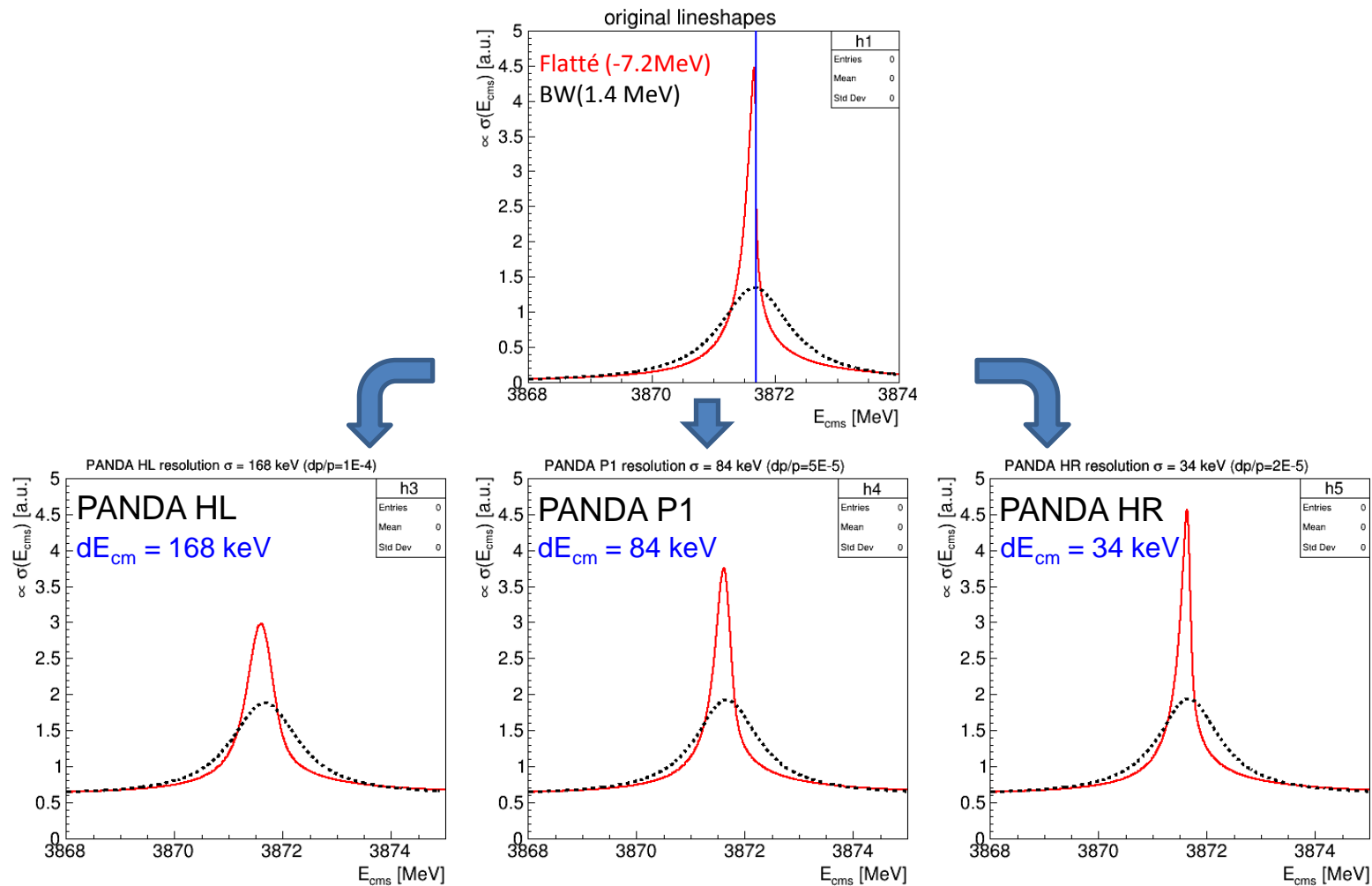
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# PANDA@HESR Beam Resolution

Due to precise beam resolution

→ Breit-Wigner and Flatté-model are distinguishable



# Distinguish Breit-Wigner from Flatté

- Extension of our previous study:  
**Investigate separation power between Flatté & BW lineshapes**
- Take  $(\varepsilon_{reco}, \mathcal{B}, \sigma, L, \dots)$  to estimate **expected yields** from study

$$N_{\text{exp}}(E_{\text{cms}}) = \sigma^*(E_{\text{cms}}) \cdot L \cdot t \cdot \text{BR}_\chi \cdot \text{BR}_{J/\psi} \cdot \varepsilon_{\text{reco}}$$

- Adapted Parameters:

Total beam time:  $T = 40 \times 2d = 80 d$

Cross section assumption:  $\sigma_{\text{peak}}(\bar{p}p \rightarrow \chi_{c1}) = 50 \text{ nb}$

BW Width:  $\Gamma = [100, 150, 200, 250, 300, \dots, 550] \text{ keV}$

Flatté energy:  $E_f = [-8.7, -8.2, -7.7, -7.2, -6.7, -6.2, -5.7, -5.2] \text{ MeV}$



# Procedure

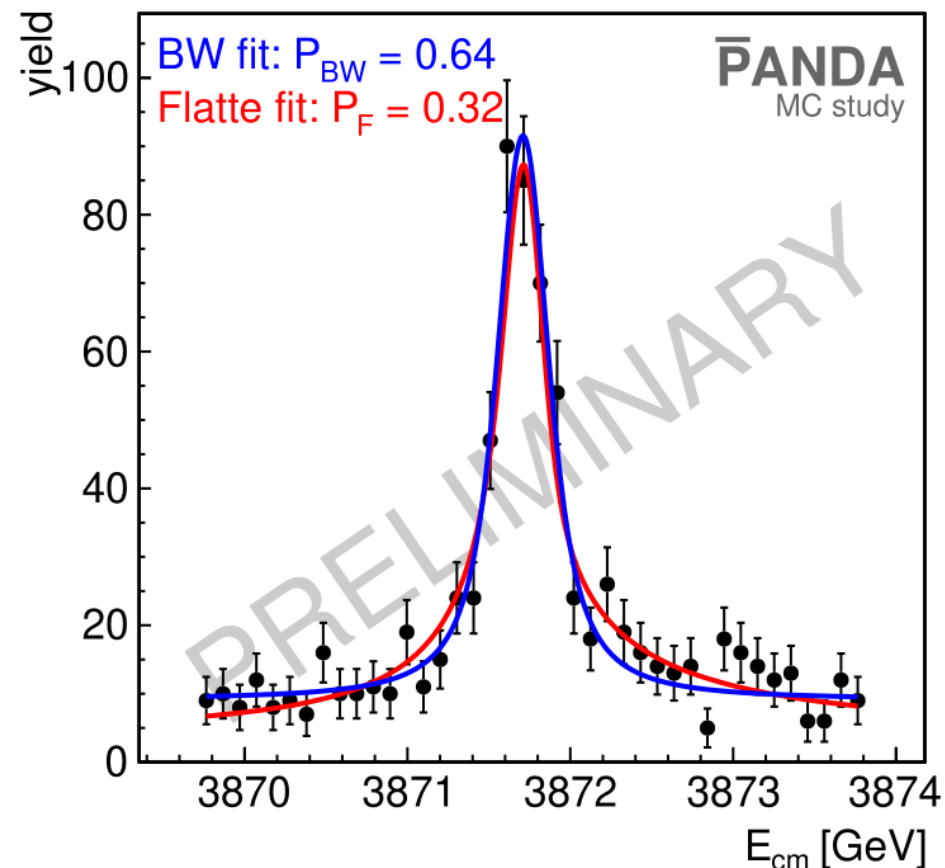
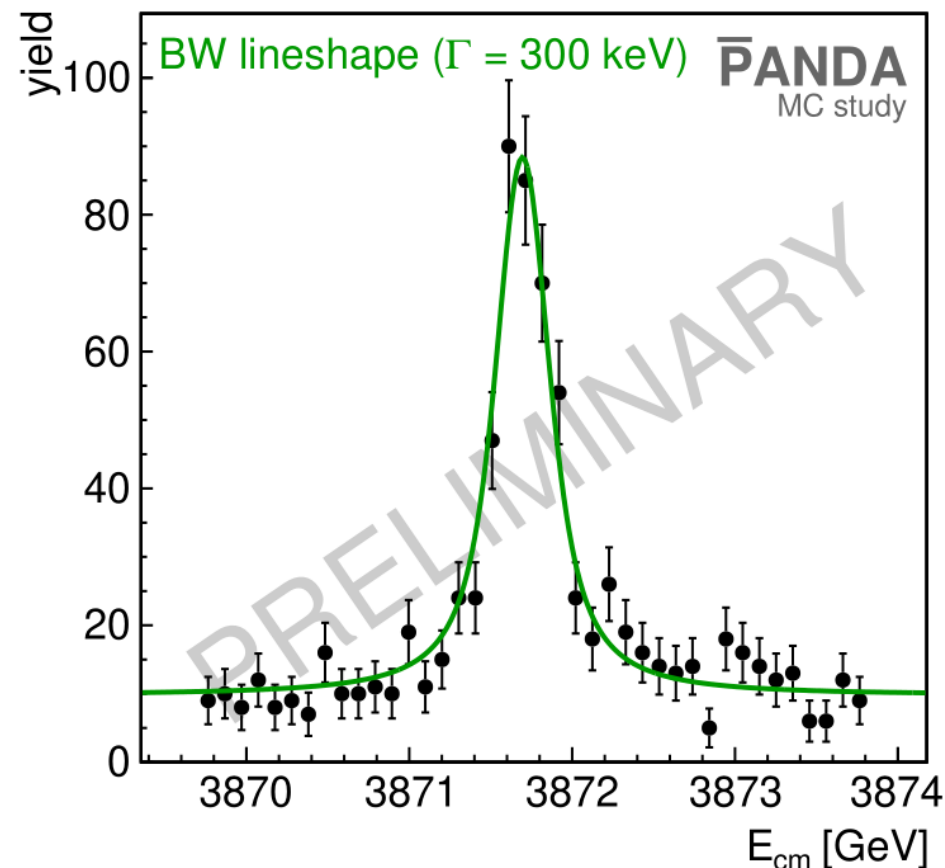
We use the following approach:

1. Use **key parameters** from EPJ A 55 (2019) 42
2. **Generate** many (toy) **spectra** for Flatté (**BW**) model
3. **Fit both BW and Flatté** to each generated distribution and determine **fit probabilities**  $P_{BW}$  and  $P_F$
4. Identification considered **correct**, if  $P_F > P_{BW}$  ( $P_{BW} > P_F$ )
5. **Count fraction** of incorrect assignments  $\rightarrow P_{mis}$
6.  $P_{mis}$  measure for **separation power**
7.  $P_{mis} = 50\%$  means: models **indistinguishable**

# Scan Procedure Principle (Example)

Example: Breit-Wigner,  $\Gamma = 300$  keV (P1 mode)

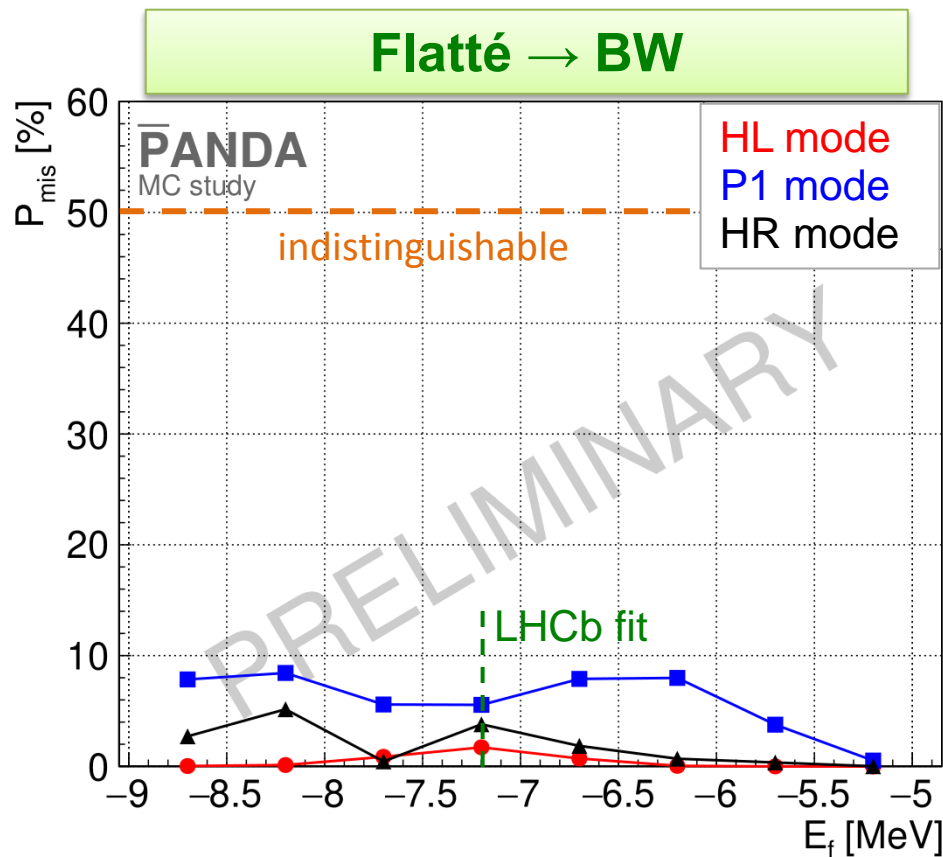
1. Compute **true lineshape** reflecting the **expected yields**
2. **Fit lineshapes** to extract fit probabilities  $P_{BW}$  and  $P_F$



# RESULTS

# Parameter Dependent Performance

- Performance across **Flatté energy  $E_f$**  range

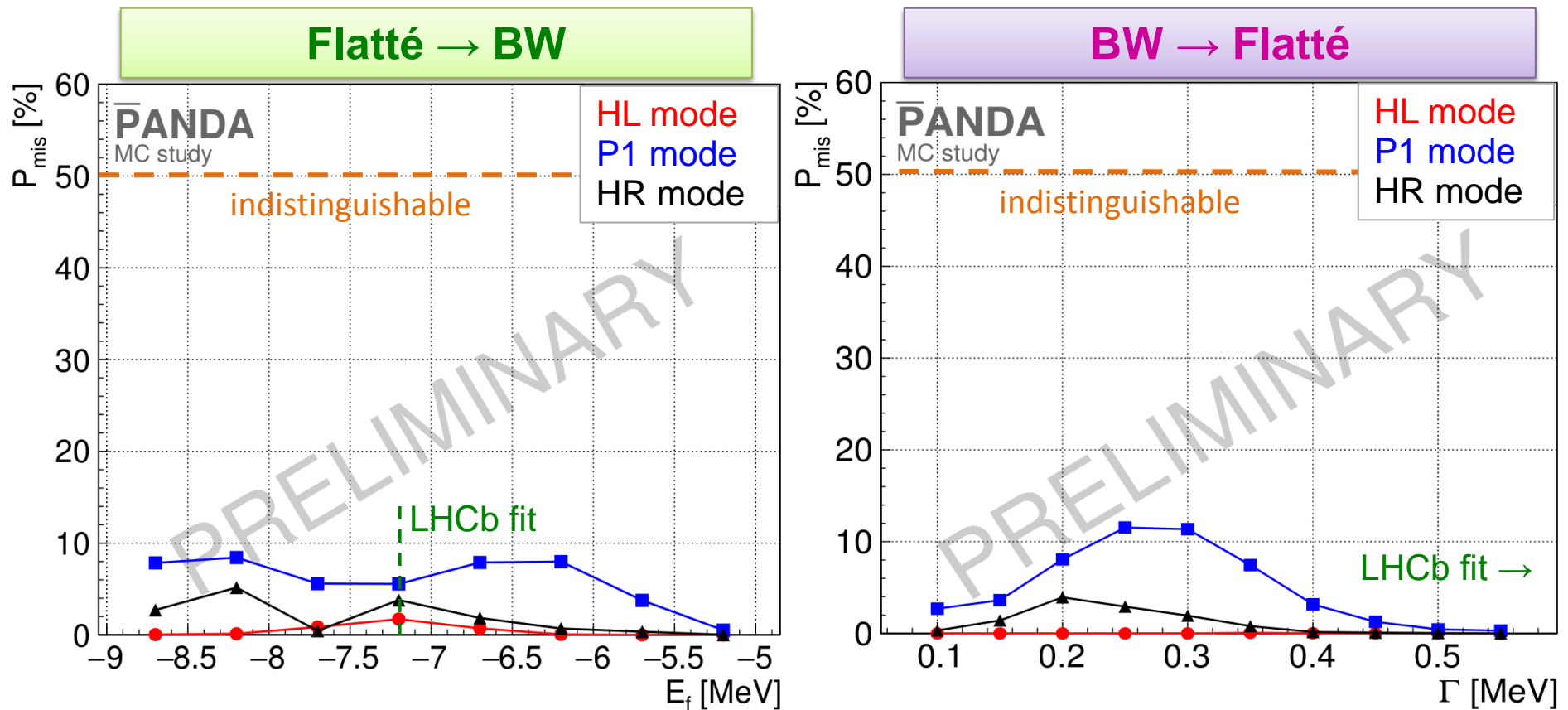


For **Mis-match** of **Flatté as BW** we see

- for the three **beam modes** **HL**, **HR**, **P1**
- the mis-identification probability  **$P_{\text{mis}}$**
- across **range** of input parameters  **$E_f$**
- with **LHCb** best fit  **$E_f = -7.2 \text{ MeV}$**
- and  **$P_{\text{mis}} = 50\%$**  for "indistinguishable"

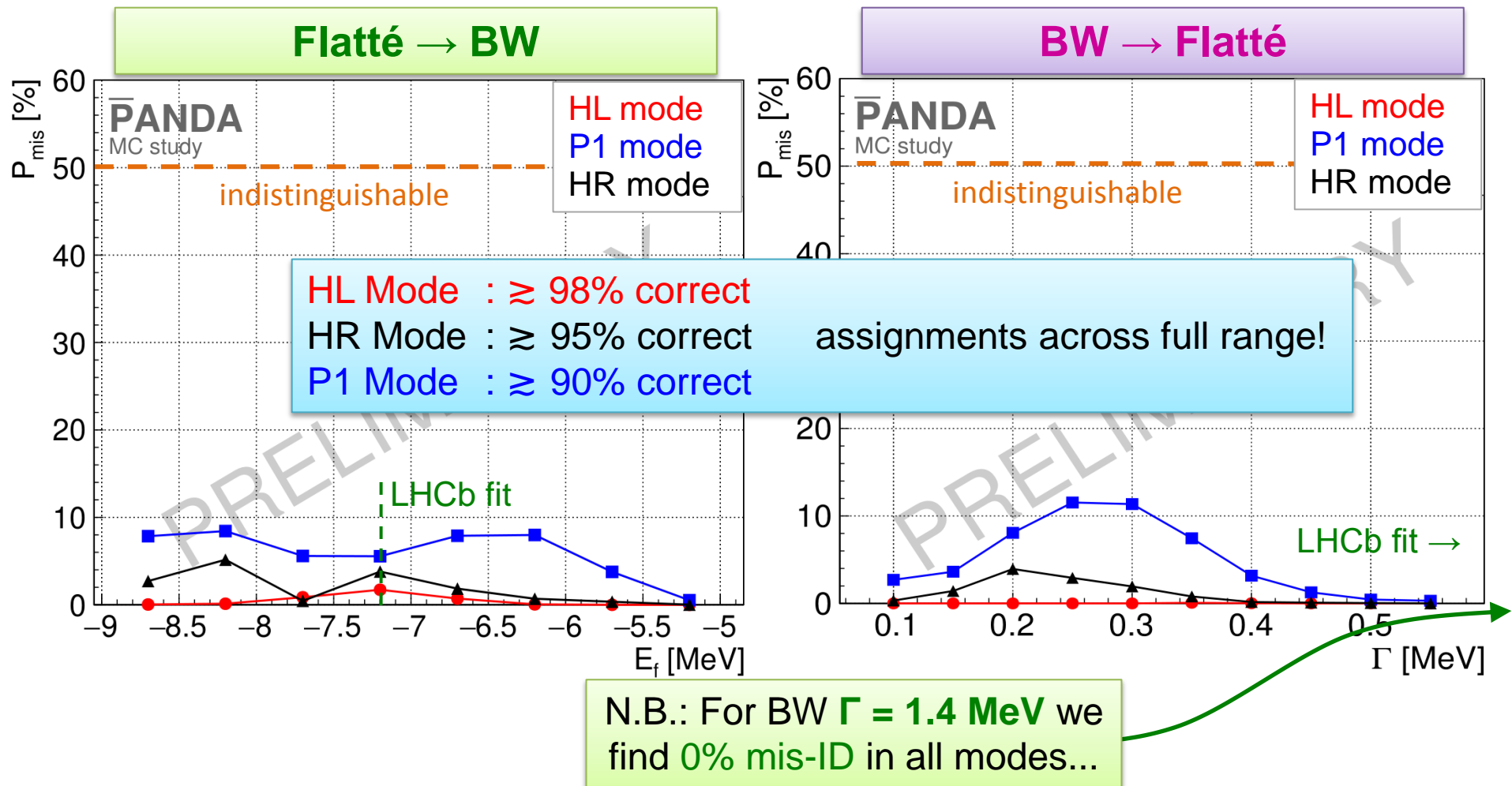
# Parameter Dependent Performance

- Performance across **Flatté energy  $E_f$**  / **Breit-Wigner  $\Gamma$**  range



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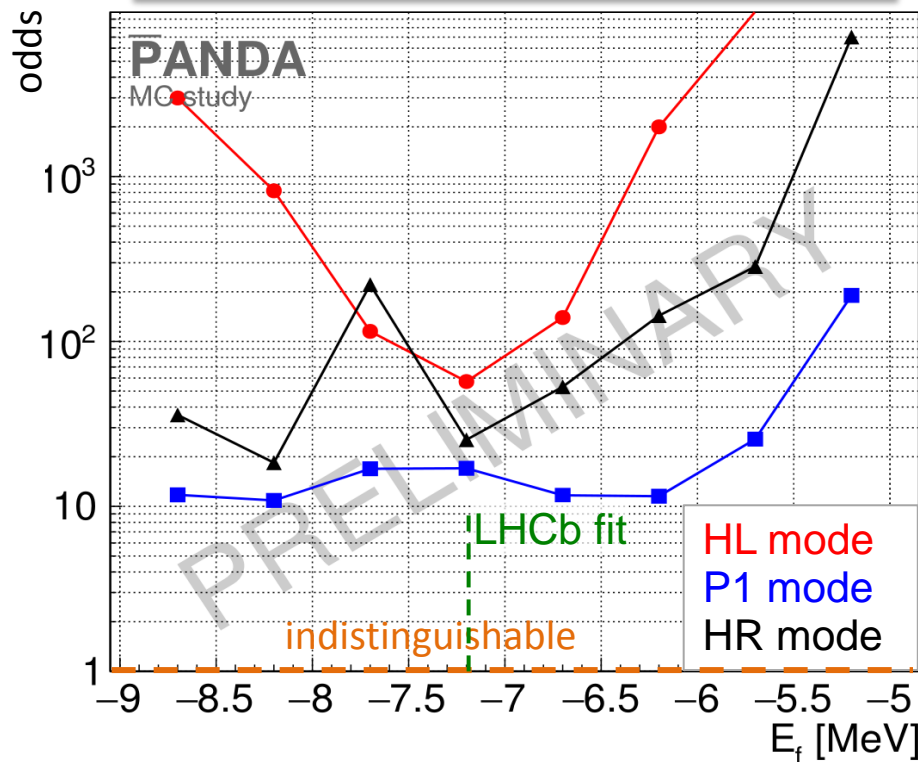


# Performance - Alternative Representation

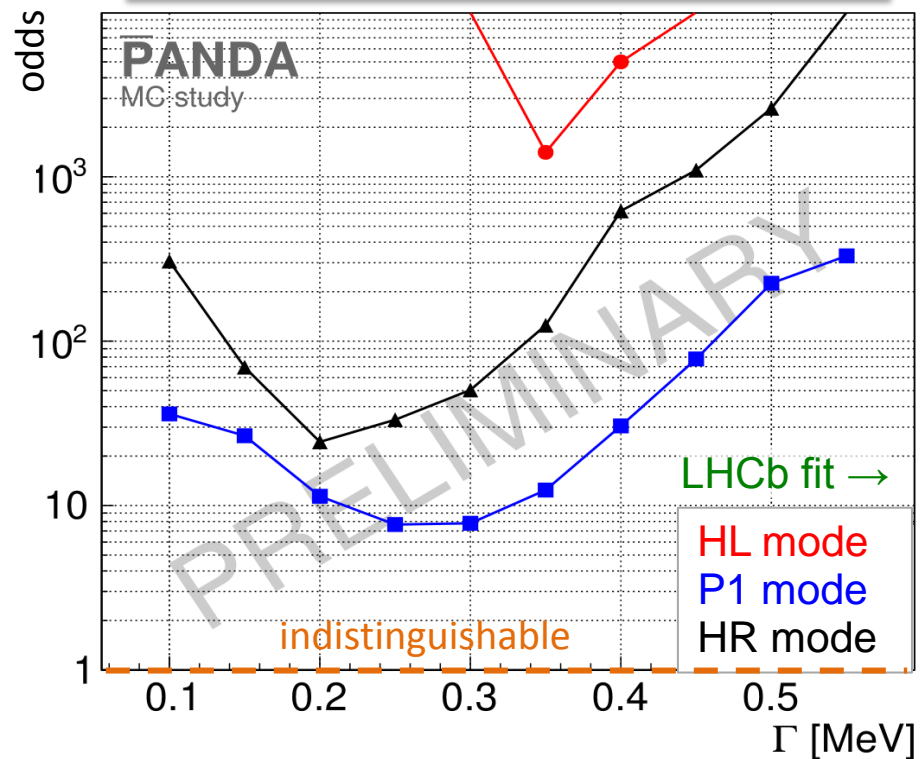
- How much better than "indistinguishable" is it?
- Idea: Consider so-called **odds** = correct identifications per wrong one

$$\text{odds} = (1 - P_{\text{mis}}) / P_{\text{mis}}$$

Flatté → BW



BW → Flatté



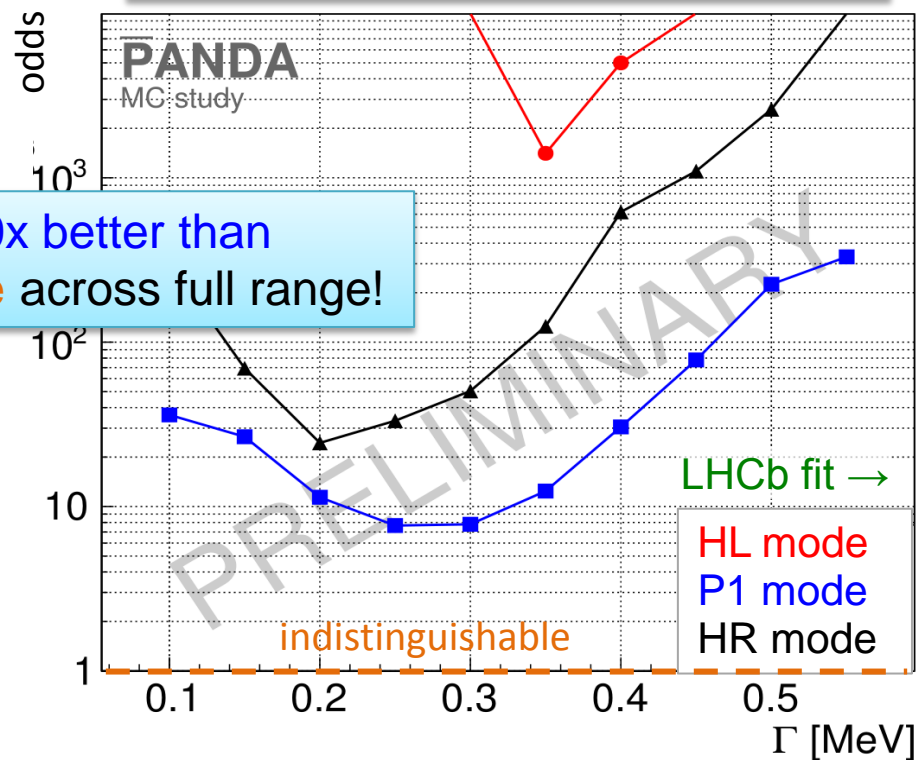
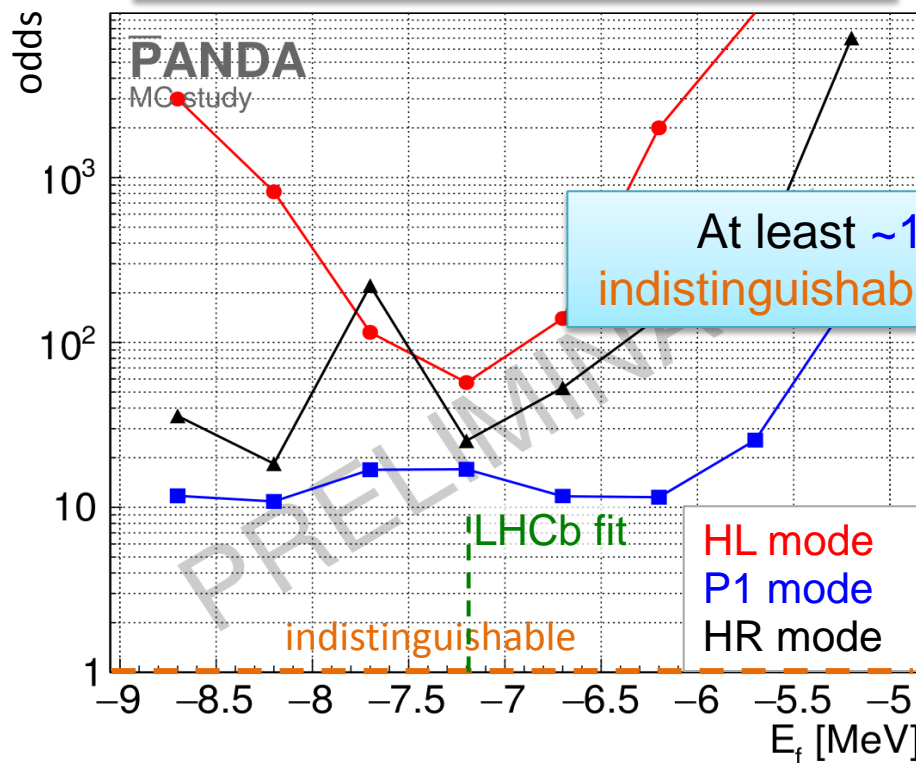
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Flatté  $\rightarrow$  BW

BW  $\rightarrow$  Flatté





# Summary and Conclusion

- Line shape measurement of  $\chi_{c1}(3872)$  at **PANDA**  
⇒ Different models can be **well distinguished**
- **Correct assignment** of fit model over full range between **≥90% (P1)** and **≥98% (HL)** depending on beam mode
- At least **~10x higher odds** to identify correct model than LHCb

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**Thank you very much  
for your attention!**