



Hadron studies using two-photon processes from Belle

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on behalf of the Belle Collaboration

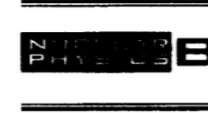
Outlines

- Two-photon interactions
- Charmonium(-like) states
- Accelerator and detector
- Review of two-photon results
- New results of two-photon at Belle
- Summary

Two-photon interactions



Nuclear Physics B 523 (1998) 423–438



Meson–photon transition form factors and resonance cross-sections in e^+e^- collisions

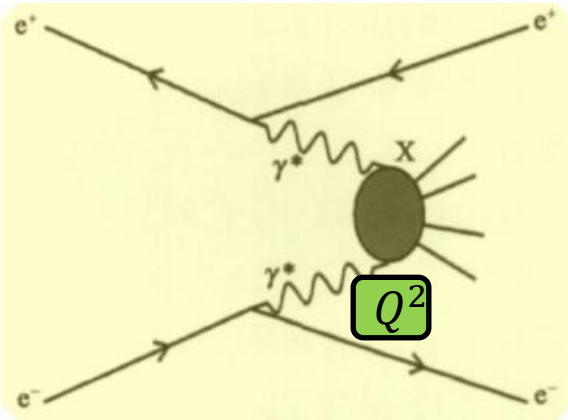
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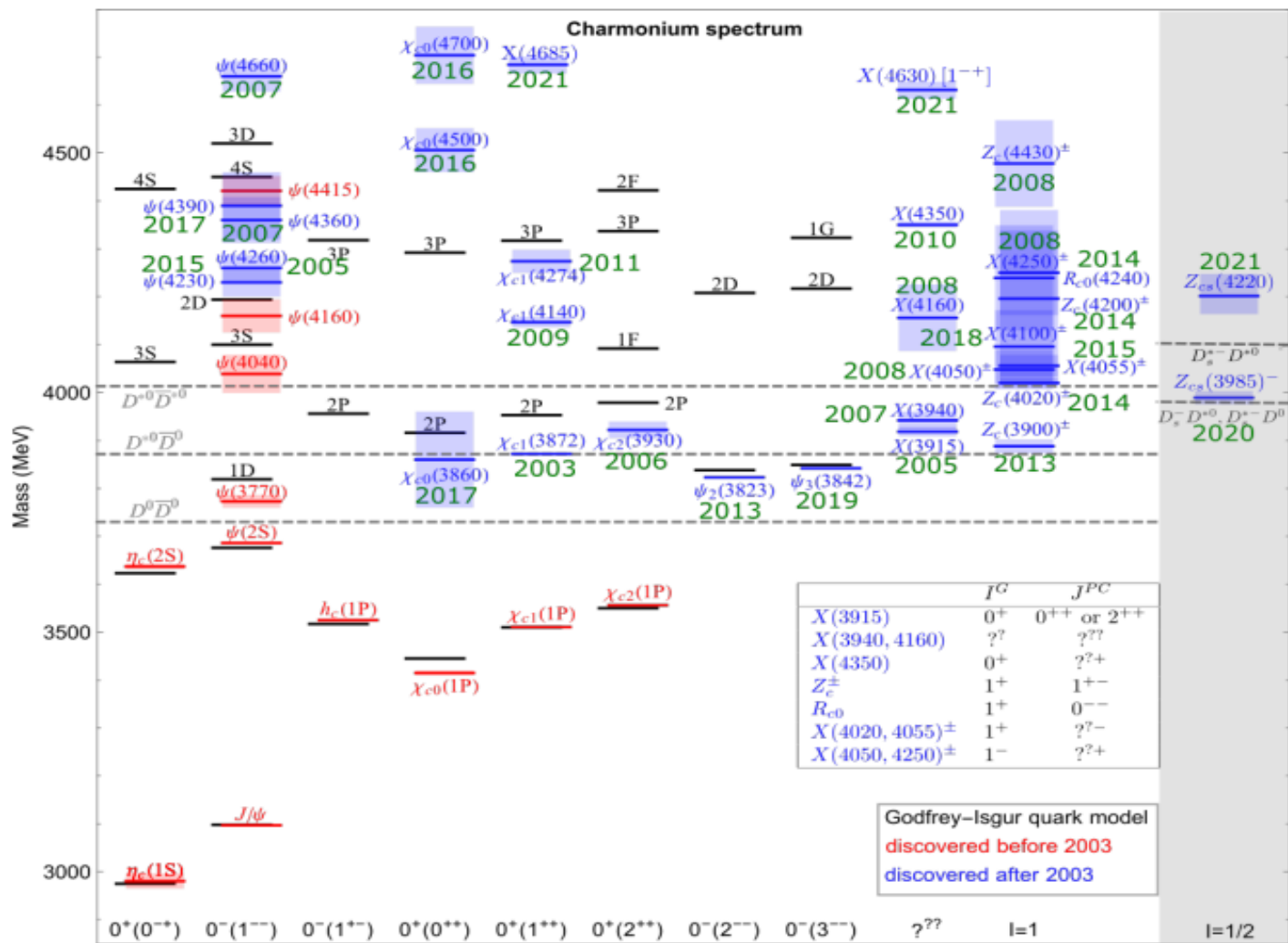
- Meson-photon-photon transition form factors for S -, P -, and D -wave states are calculated.
- Q^2 dependence of the (single) form factor governs the production of mesons.
- e^+e^- cross section for 1^+ states do not vanish at low Q^2



Form factors f_{AB}

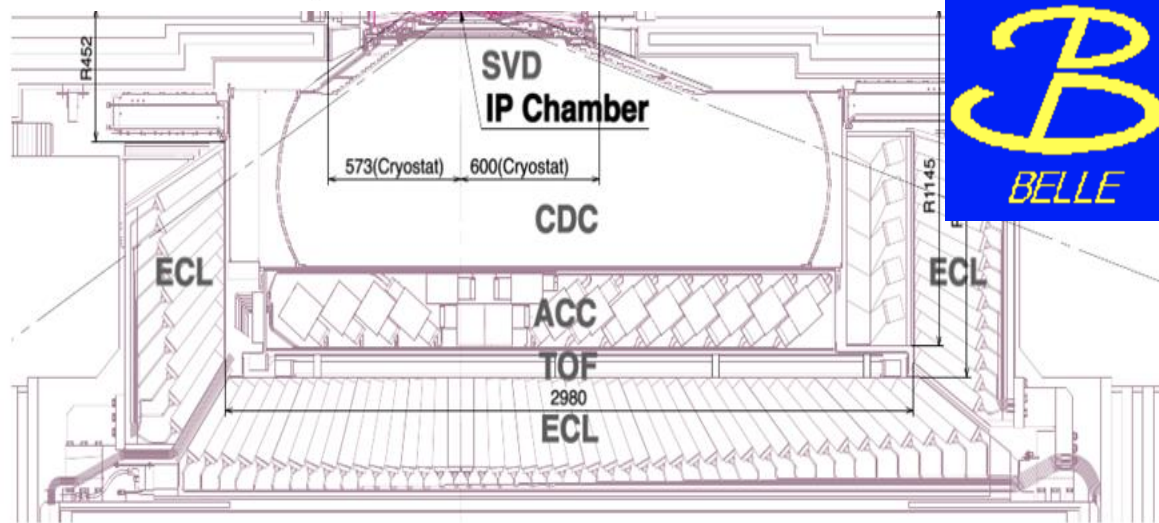
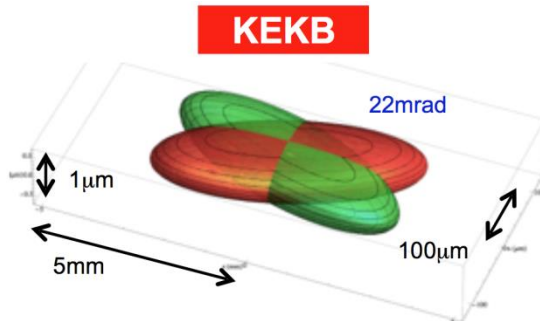
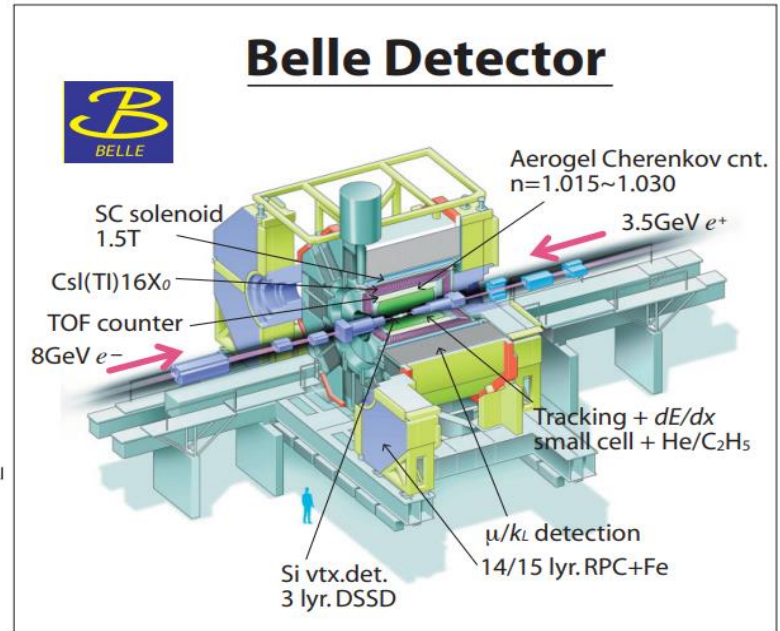
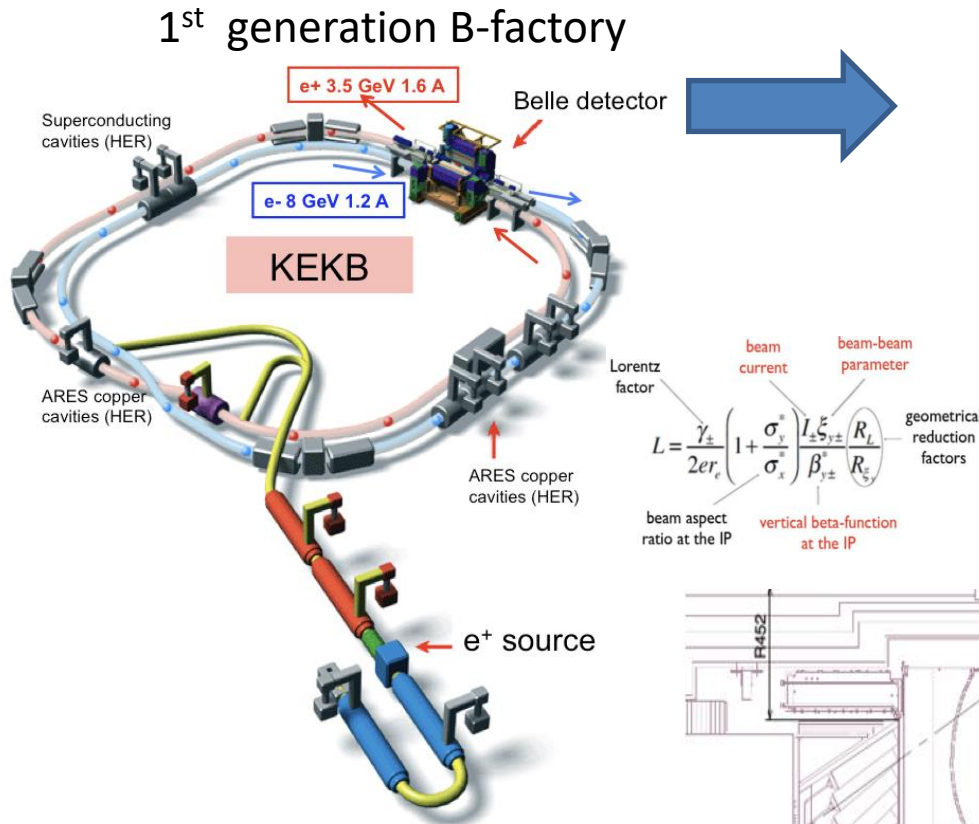
J^P	f_{TT}	f_{TS}	f_{SS}
0^-	$\kappa \frac{X}{\nu^2}$	0	0
0^+	$\kappa \left(\frac{X+\nu M^2}{3\nu^2} \right)^2$	0	$2\kappa \left(\frac{M^2 \sqrt{Q_1^2 Q_2^2}}{3\nu^2} \right)^2$
1^+	$\kappa \left(\frac{Q_2^2 - Q_1^2}{2\nu} \right)^2$	$2\kappa \frac{M^2}{2\nu} \frac{Q_2^2}{2\nu} \left(\frac{\nu + Q_1^2}{\nu} \right)^2$	0
2^+	$\kappa \left(\frac{M^2}{2\nu} \right)^2 \left\{ 1 + \frac{[2Q_1^2 Q_2^2 - \nu(Q_1^2 + Q_2^2)]^2}{6M^4 \nu^2} \right\}$	$\kappa \frac{M^2 Q_2^2 (\nu - Q_1^2)^2}{4\nu^4}$	$\kappa \frac{M^4 Q_1^2 Q_2^2}{3\nu^4}$
2^-	$\kappa \left[\frac{X}{\nu^2} \right]^3$	0	0

Charmonium(-like) states



- ◆ Many puzzles arise from these XYZ states since X(3872) was observed at Belle Experiment in 2003. [Phys. Rev. Lett. 91, 262001(2003)]
- ◆ One of the XYZ puzzles concerns the candidates for P -wave triplet states near 3.9 GeV/c². [Phys. Rev. D 72, 054026 (2005)]

Accelerator and detector



Review of two-photon results

◆ $\gamma\gamma \rightarrow Z(3930) \rightarrow D\bar{D}$

◆ $\gamma\gamma \rightarrow X(3915) \rightarrow \omega J/\psi$

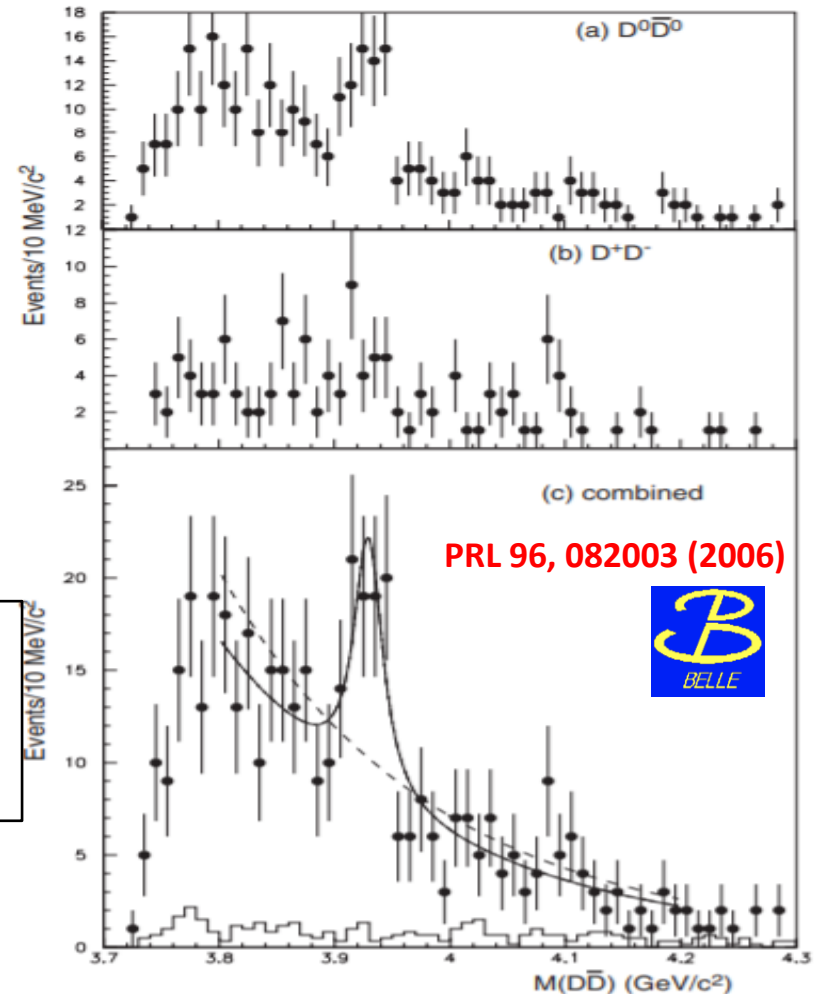
◆ $\gamma\gamma \rightarrow X(4350) \rightarrow \phi J/\psi$

$\gamma\gamma \rightarrow Z(3930) \rightarrow D\bar{D}$

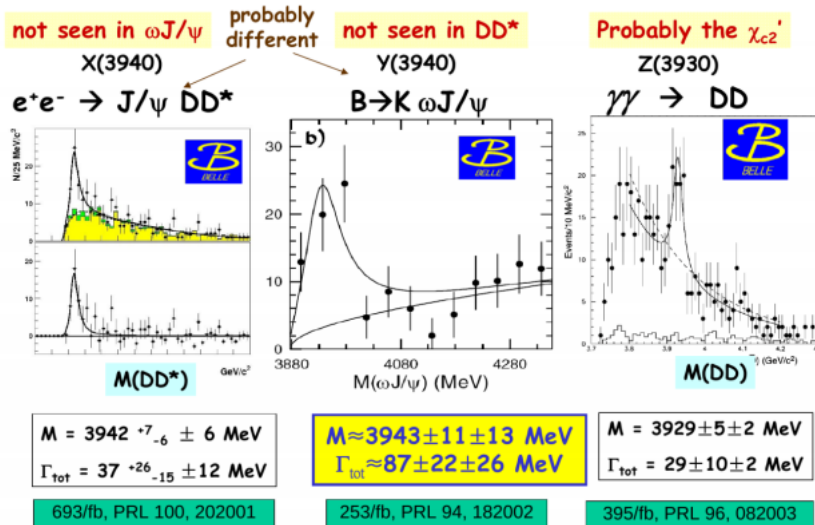
- The first radially excited χ_{cJ} states are predicted to have masses between 3.9 and 4.0 GeV/c^2 , which is considerably above $D\bar{D}$ threshold.
- The results on mass, decay angular distributions and $\Gamma_{\gamma\gamma}(\mathcal{B} \rightarrow D\bar{D})$ are all consistent with expectations for the χ'_{c2} .
- Results for the mass, width, and the product of the two-photon decay width times the branching fraction to $D\bar{D}$:

$$\begin{aligned} M: & 3923 \pm 5 \pm 2 \text{ MeV}/c^2 \\ \Gamma_{tot}: & 29 \pm 10 \pm 2 \text{ MeV} \\ \Gamma_{\gamma\gamma}(\mathcal{B} \rightarrow D\bar{D}) = & 0.18 \pm 0.05 \pm 0.03 \text{ keV} \end{aligned}$$

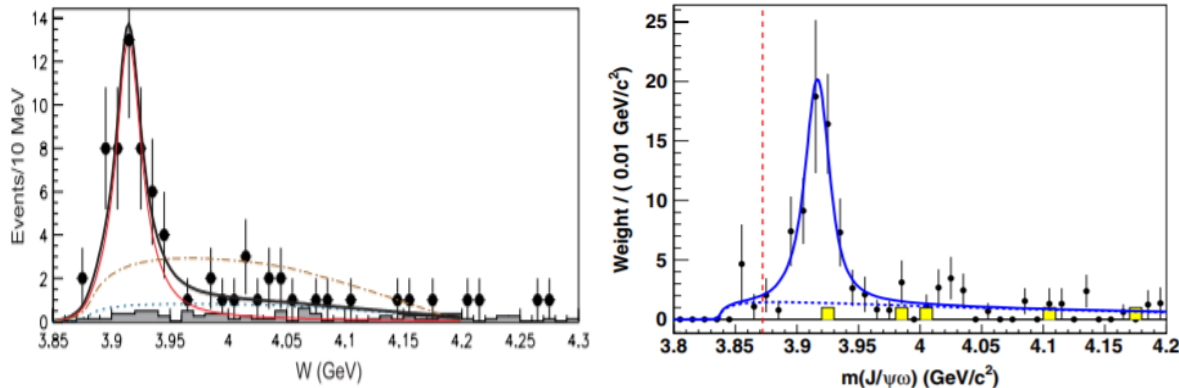
Probably the χ_{c2} : $Z(3930)$



$\gamma\gamma \rightarrow X(3915) \rightarrow \omega J/\psi$



- ◆ Three of the new states were discovered by Belle in the 3.90-3.95 GeV/c^2 .
- ◆ They appear in different production and decay processes, and are usually considered to be distinct particles, however there is no decisive evidence.



X(3915) from Belle:

- $M = (3915 \pm 3 \pm 2)$ MeV;
- $\Gamma = (17 \pm 10 \pm 3)$ MeV
- $N^{\text{sig}} = 49 \pm 14 \pm 4$ events
- Signif. = 7.7σ .

Belle: PRL104, 092001(2010)

X(3915) was expected to be $\chi_{c0}(2P)$ candidate.

X(3915) From BaBar:

- $M = (3919.4 \pm 2.2 \pm 1.6)$ MeV/c^2 ;
- $\Gamma = (13 \pm 6 \pm 3)$ MeV;
- $N^{\text{sig}} = 59 \pm 10$;
- Signif. = 7.6σ .
- Data largely prefer $J^P = 0^\pm$ over 2^+ .

BaBar: PRD86,072002(2012)

- ◆ These values are consistent with those of the Y(3940), and close to those of the Z(3930).
- ◆ Helicity-0 component is allowed, a $J^{PC}=2^{++}$ assignment is possible.

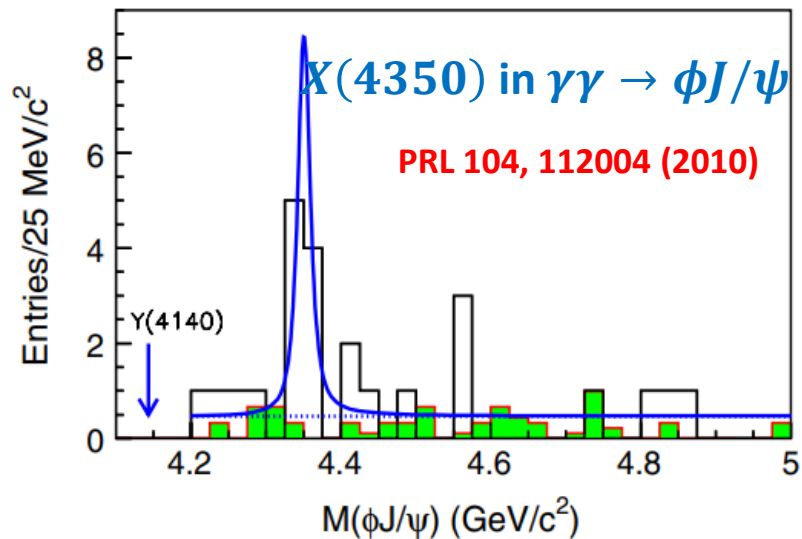
$\gamma\gamma \rightarrow X(4350) \rightarrow \phi J/\psi$

X(4350)

$$J^{PC} = 0^{+}(?^{?+})$$

OMITTED FROM SUMMARY TABLE

Seen by SHEN 10 in the $\gamma\gamma \rightarrow J/\psi\phi$. Needs confirmation.



◆ The first investigation of the $\gamma\gamma \rightarrow \phi J/\psi$ is to search for high mass states with $J^{PC} = 0^{++}$ or 2^{++} , such as the tetraquark states and molecular states that are predicted by various models.

◆ The mass of this structure is consistent with the predicted values of a $c\bar{c}s\bar{s}$ tetraquark state with $J^{PC} = 2^{++}$, and a $D_s^{*+}D_{s0}^{*-}$ molecular state.

◆ The possibility that X(4350) could be an excited P -wave charmonium state(χ''_{c2}).

$$m(X(4350)) = [4350.6^{+4.6}_{-5.1}(stat) \pm 0.7(syst)] \text{ MeV}/c^2$$

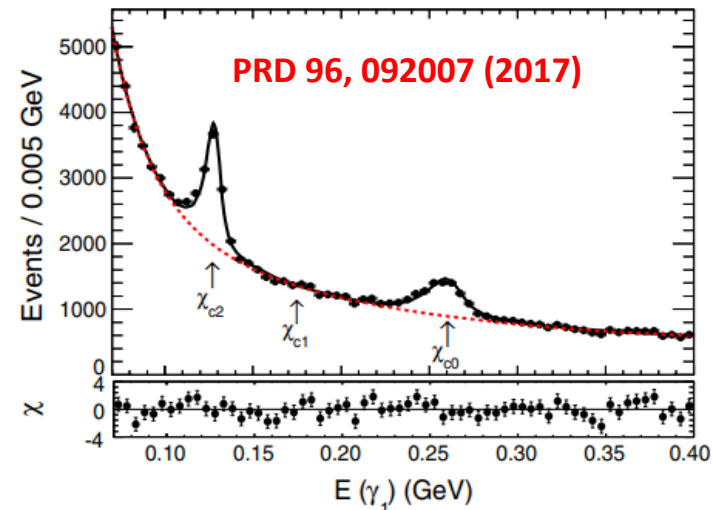
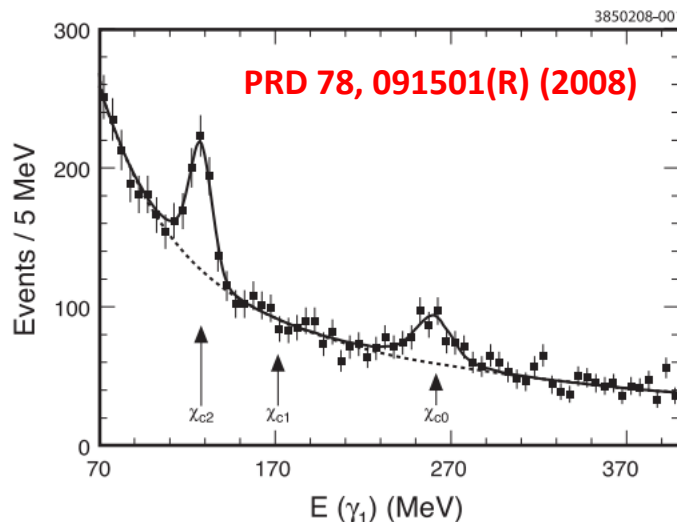
$$\Gamma(X(4350)) = [13^{+18}_{-9}(stat) \pm 4(syst)] \text{ MeV}$$

New results of two-photons at Belle

- $\gamma\gamma \rightarrow \chi_{c2}(1P) \rightarrow J/\psi\gamma$
- $\gamma\gamma \rightarrow Z(3922)/X(4015) \rightarrow \gamma\psi(2S)$
- $\gamma\gamma \rightarrow X(3872) \rightarrow \pi^+\pi^-J/\psi$

$$\gamma\gamma \rightarrow \chi_{c2}(1P) \rightarrow J/\psi\gamma$$

- ◆ The two-photon decay widths ($\Gamma_{\gamma\gamma}$) of mesonic states provide important information for testing models based on quantum chromodynamics(QCD).
- ◆ The predictions of two-photon decay width of $\chi_{c2}(1P)$ have the wide range of values between 280 eV and 930 eV in various theoretical calculations.[[Phys. Rev. D 82, 034021 \(2010\)](#)]
- ◆ Several experiments have reported the measurement of $\Gamma_{\gamma\gamma}(\chi_{c2}(1P))$. The precision of the experimental value of $\Gamma_{\gamma\gamma}(\chi_{c2}(1P))$ using the two-photon process is much less than the value measured in the two-photon decay. Precise measurements will help to improve the understanding of quarkonium states.



$$\gamma\gamma \rightarrow \chi_{c2}(1P) \rightarrow J/\psi\gamma$$

Selection criteria:

- Tracks: $N_{\text{trk}}=2$, $|dz| \leq 3\text{cm}$, $|dr| \leq 1\text{cm}$, $-0.47 \leq \cos\theta \leq 0.82$, $p_T \geq 0.4\text{ GeV}/c$, $|\Delta dz| \leq 1\text{cm}$, $\cos\alpha > -0.997$
- Identify e/μ : $E/p \geq 0.8$ for electron, $E/p \leq 0.4$ for muon
- For photon: $E_\gamma \geq 0.2\text{ GeV}$, the cluster is isolated from the nearest charged track by an angle greater than 18.2° .

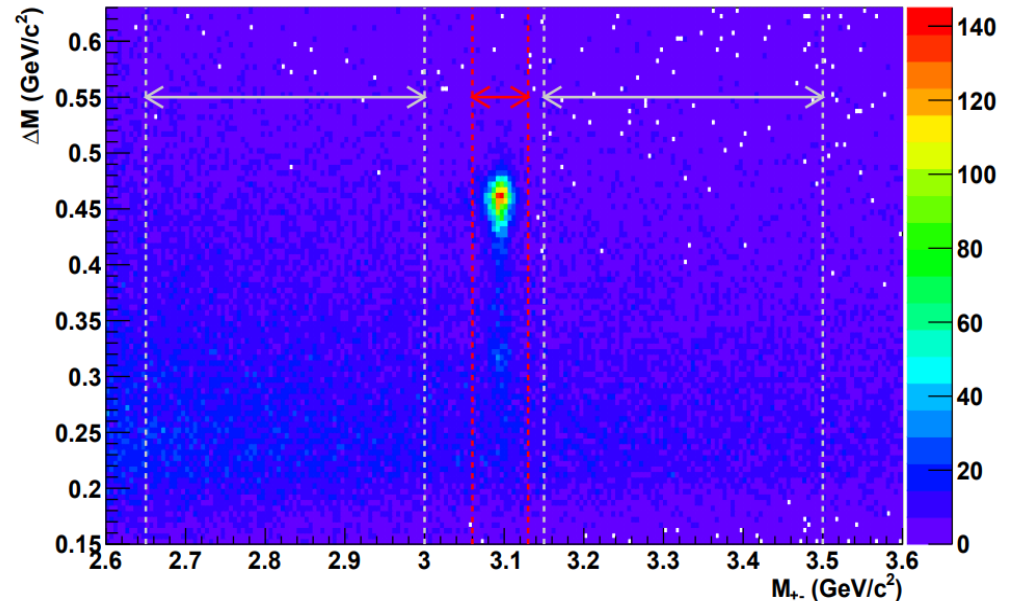
Signal region:

$$3.06\text{ GeV}/c^2 < M_{+-} < 3.13\text{ GeV}/c^2$$

Sideband regions:

$$2.65\text{ GeV}/c^2 < M_{+-} < 3.00\text{ GeV}/c^2$$

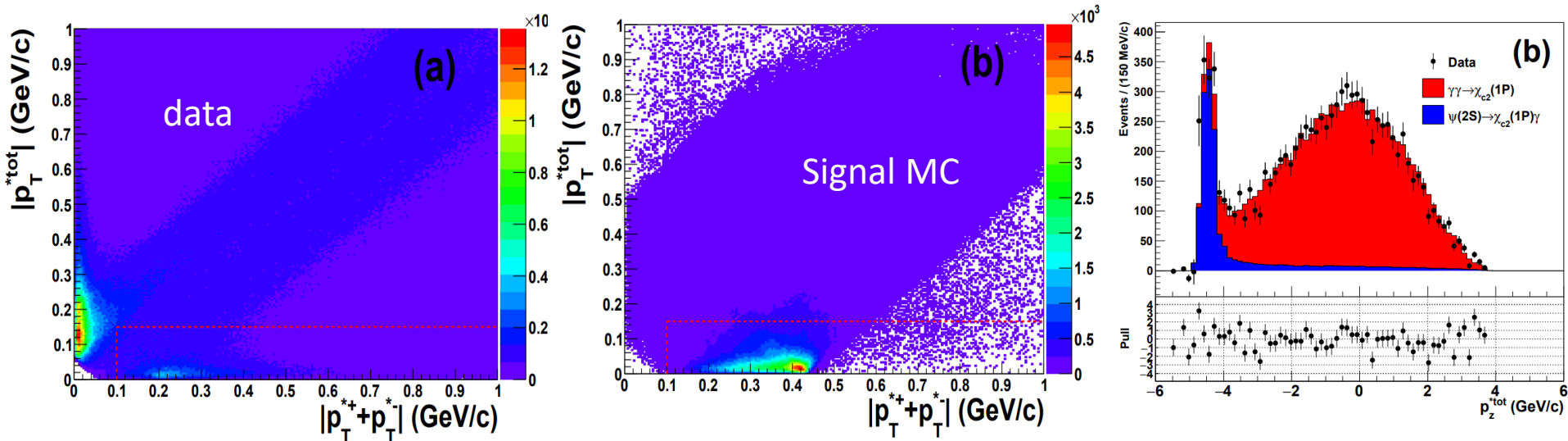
$$3.15\text{ GeV}/c^2 < M_{+-} < 3.50\text{ GeV}/c^2$$



$$\gamma\gamma \rightarrow \chi_{c2}(1P) \rightarrow J/\psi\gamma$$

Background research:

- $M_{rec}^2(\gamma J/\psi) > 5.0 \text{ MeV}^2/c^4$ to reject ISR process
- $|p_T^{*tot}| < 0.15 \text{ GeV}/c$, $|p_T^{*+} + p_T^{*-}| > 0.1 \text{ GeV}/c$ to reject two-photon production with a fake photon
- $p_z^{*tot} < -4.5 \text{ GeV}/c$ to reject the ISR $\psi(2S)$ production



$\gamma\gamma \rightarrow \chi_{c2}(1P) \rightarrow J/\psi\gamma$

- Non- J/ψ background is the dominant background

- Spin-1 meson production is suppressed

$$\Delta M = M_{+-\gamma} - M_{+-}$$

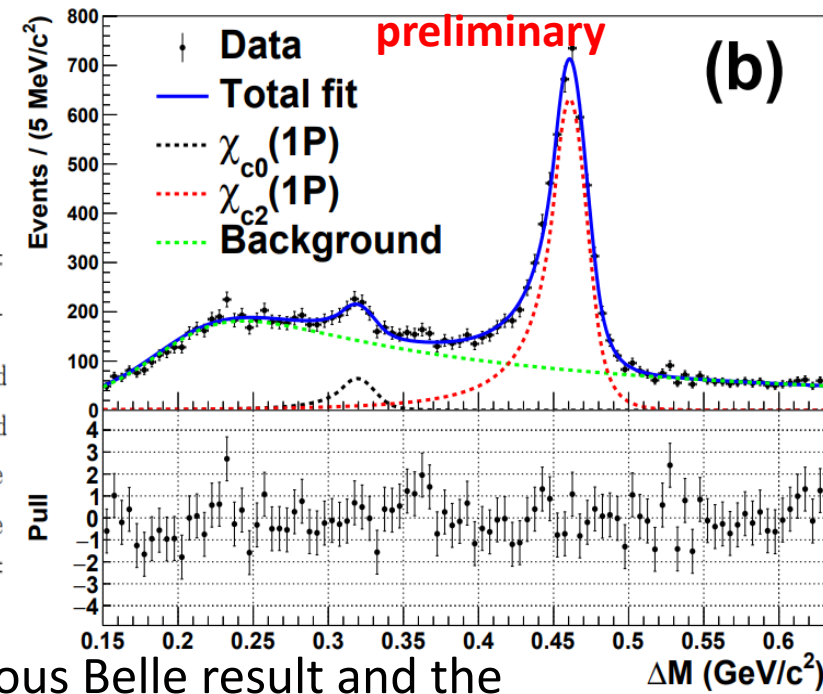
- Fitting functions: $A(\Delta M - a)^{-b} / (1 + e^{-c(\Delta M - d)})$ for background

Double-side Crystal Ball function for $\chi_{c0}(1P)$ and $\chi_{c2}(1P)$

$$\Gamma_{\gamma\gamma}(\chi_{c2}(1P))\mathcal{B}(\chi_{c2}(1P) \rightarrow J/\psi\gamma)\mathcal{B}(J/\psi \rightarrow \ell^+\ell^-) = \frac{m_{\chi_{c2}(1P)}^2 N_{\text{sig}}}{20\pi^2(\int \mathcal{L}dt)\eta L_{\gamma\gamma}(m_{\chi_{c2}(1P)})}$$

$$\Gamma_{\gamma\gamma}(\chi_{c2}(1P)) = 653 \pm 13(\text{stat.}) \pm 31(\text{syst.}) \pm 17(\text{B.R.}) \text{ eV}$$

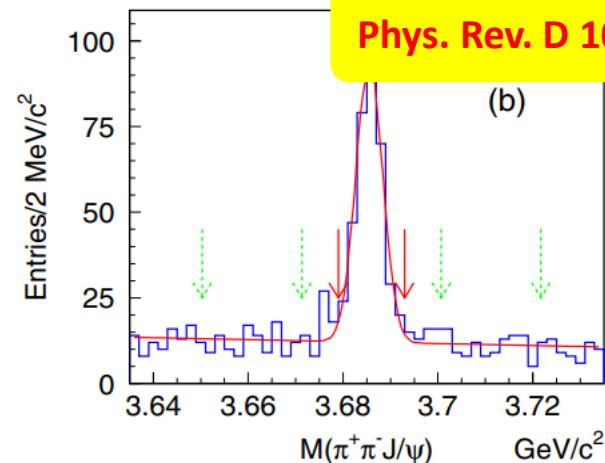
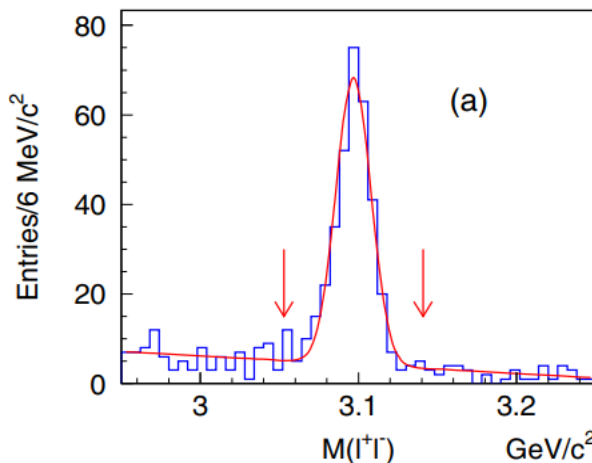
Experiment [Ref.]	Measured value ^a	$\Gamma_{\gamma\gamma}(\chi_{c2}(1P))$ (eV)
This measurement	$\Gamma_{\gamma\gamma}(\chi_{c2}(1P)) \times \mathcal{B}_1 \times \mathcal{B}_2 = 14.8 \pm 0.3 \pm 0.7 \text{ eV}$	$653 \pm 13 \pm 31 \pm 17^b$
Belle [14]	$\Gamma_{\gamma\gamma}(\chi_{c2}(1P)) \times \mathcal{B}_1 \times \mathcal{B}_2 = 13.5 \pm 1.3 \pm 1.1 \text{ eV}$	$596 \pm 58 \pm 48 \pm 16^{b,d}$
CLEOIII [15]	$\Gamma_{\gamma\gamma}(\chi_{c2}(1P)) \times \mathcal{B}_1 \times \mathcal{B}_2 = 13.2 \pm 1.4 \pm 1.1 \text{ eV}$	$582 \pm 59 \pm 50 \pm 15^{b,d}$
CLEO-c [12]	$\mathcal{B}_3 \times \mathcal{B}_4 \times 10^5 = 2.68 \pm 0.28 \pm 0.15$	$555 \pm 58 \pm 32 \pm 28^{c,e}$
BESIII [13]	$\mathcal{B}_3 \times \mathcal{B}_4 \times 10^5 = 2.83 \pm 0.08 \pm 0.06$	$586 \pm 16 \pm 13 \pm 29^{c,e}$



- ✓ This measurement is consistent with the previous Belle result and the other experimental results. The result in this paper achieves the most precise measurement of $\Gamma_{\gamma\gamma}(\chi_{c2}(1P))$.

$\gamma\gamma \rightarrow \gamma\psi(2S)$ at Belle

- Both $\chi_{c0}(2P)$ and $\chi_{c2}(2P)$ can be produced in two-photon collision and decay to $\gamma\psi(2S)$ via E1 transition. [Phys. Rev. D 72, 054026 (2005)]
- The partial widths are expected to be $\Gamma(\chi_{c0}(2P) \rightarrow \gamma\psi(2S)) \approx 135$ keV and $\Gamma(\chi_{c2}(2P) \rightarrow \gamma\psi(2S)) \approx 207$ keV according to Godfrey-Isgur relativized potential model. [Phys. Rev. D 72, 054026 (2005)]
- $\psi(2S)$ reconstructed from $J/\psi\pi^+\pi^-$, and J/ψ reconstructed from e^+e^- or $\mu^+\mu^-$.



Phys. Rev. D 105, 112011(2022)

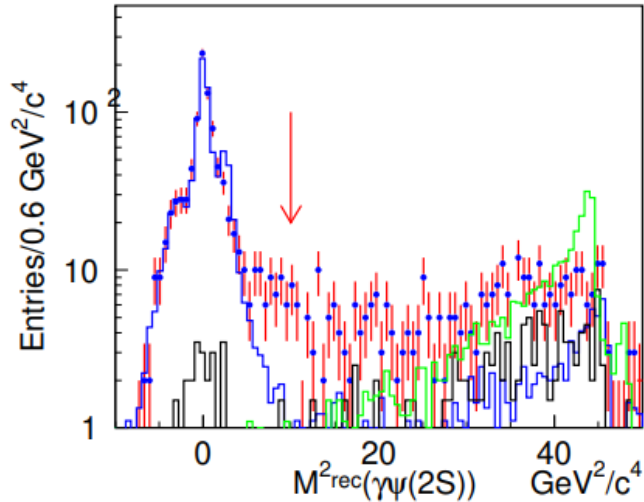
Signal regions : $|M_{l^+l^-} - m_{J/\psi}| < 4\sigma_{J/\psi} (\sigma_{J/\psi} \equiv 11.0 \text{ MeV}/c^2)$

$$|M_{\pi^+\pi^- J/\psi} - m_{\psi(2S)}| < 2.5\sigma_{\psi(2S)} (\sigma_{\psi(2S)} \equiv 2.8 \text{ MeV}/c^2)$$

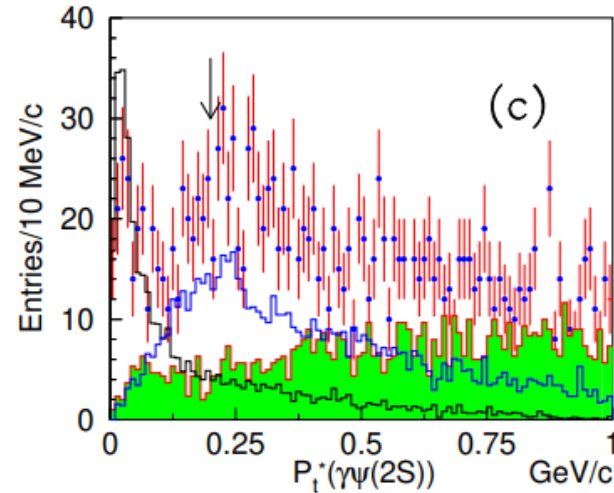
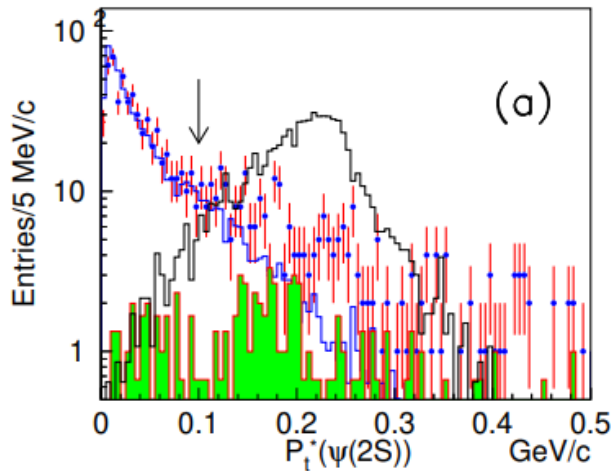
Sideband region : $|M_{\pi^+\pi^- J/\psi} - m_{\psi(2S)}| > 3.75\sigma_{\psi(2S)}$

$\gamma\gamma \rightarrow \gamma\psi(2S)$ at Belle

Phys. Rev. D 105, 112011(2022)



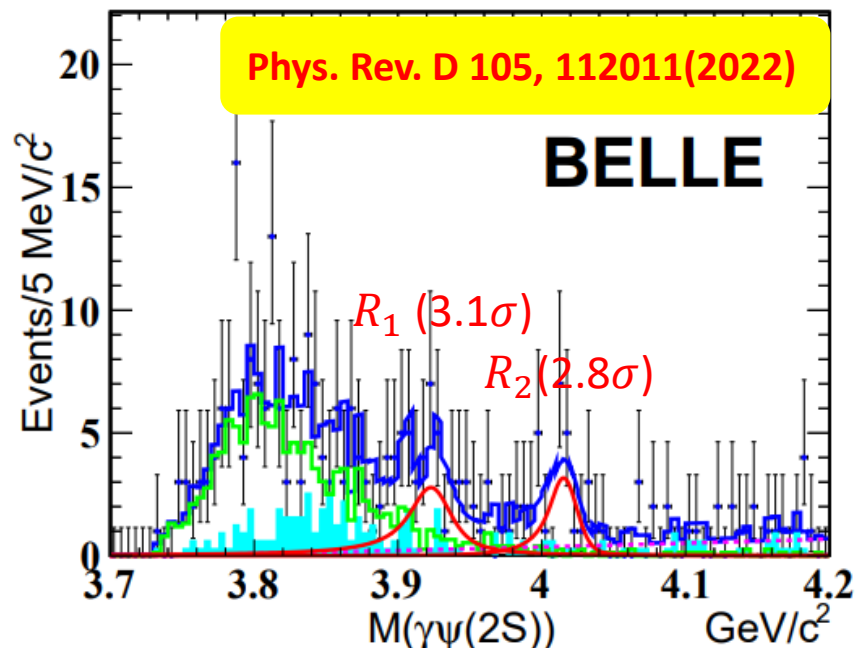
- We apply $M^2_{rec}(\gamma\psi(2S)) > 10(\text{GeV}/c^2)^2$ to remove most ISR events.
- The transverse momenta of $\psi(2S)$ and $\gamma\psi(2S)$ are used to suppress the ISR background further.



- We apply $P_t^*(\psi(2S)) > 0.1\text{GeV}/c$ and $P_t^*(\gamma\psi(2S)) < 0.2\text{GeV}/c$ to suppress the ISR background with selection efficiencies of $(97.1 \pm 0.3)\%$ and $(67.8 \pm 0.7)\%$, respectively.

$\gamma\gamma \rightarrow \gamma\psi(2S)$ at Belle

- Fitting to the $M(\gamma\psi(2S))$ distribution: $f_{PDF} = f_{R_1} + f_{R_2} + f_{ISR} + f_{bkg} + f_{SB}$



- ◆ Two excesses around 3.92 and 4.02 GeV/c^2

- ◆ Fit function: $f_{sum} = f_{R1} + f_{R2} + f_{ISR} + f_{bkg} + f_{SB}$

f_{R1}, f_{R2} : Breit-Wigner $\otimes$ Crystal Ball
(solid red line)

f_{ISR} : for ISR events (green blank histogram)

f_{bkg} : possible addition backgrounds
(pink dashed line)

f_{SB} : the background in $\psi(2S)$ reconstruction
(blue shaded histogram)

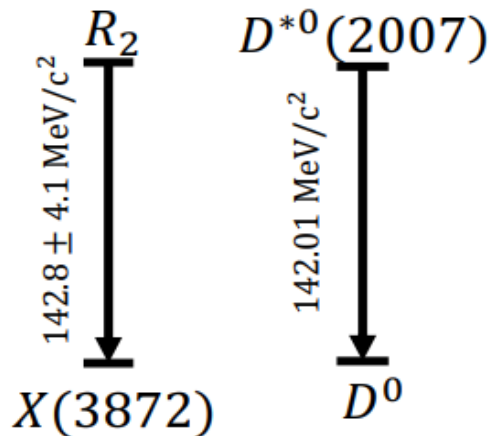
Resonant parameters	$J = 0$	$J = 2$
M_{R_1}	$3922.4 \pm 6.5 \pm 2.0$	
Γ_{R_1}	$22 \pm 17 \pm 4$	
$\Gamma_{\gamma\gamma} \mathcal{B}(R_1 \rightarrow \gamma\psi(2S))$	$9.8 \pm 3.6 \pm 1.2$	$2.0 \pm 0.7 \pm 0.2$
M_{R_2}	$4014.3 \pm 4.0 \pm 1.5$	
Γ_{R_2}	$4 \pm 11 \pm 6$	
$\Gamma_{\gamma\gamma} \mathcal{B}(R_2 \rightarrow \gamma\psi(2S))$	$6.2 \pm 2.2 \pm 0.8$	$1.2 \pm 0.4 \pm 0.2$

- ◆ R_1 near $3.92 \text{ GeV}/c^2$: 3.1σ
including systematic uncertainties

- ◆ R_2 near $4.01 \text{ GeV}/c^2$: study on
look-elsewhere effect show a
global significance of 2.8σ .

$\gamma\gamma \rightarrow \gamma\psi(2S)$ at Belle

- ◆ R_1 may be $X(3915)$, $\chi_{c2}(3930)$, or mix of them. Assuming R_1 is the $\chi_{c2}(3930)$, a rough estimation shows $\Gamma(\chi_{c2}(3930) \rightarrow \gamma\psi(2S)) = 200 \sim 300 \text{ keV}$. [207 keV calculated by GI model in [PRD 72, 054026 \(2005\)](#)]
- ◆ R_2 has the same mass and width with 2^{++} partner of $X(3872)$ predicted in [PRD 88, 054007 \(2013\)](#), [Eur. Phys. J. C 75, 547 \(2015\)](#).
 R_2 corresponds to one new resonance $X(4014)$.



R_2 may be helped for the study of $X(3872)$

- ◆ The hints implies that one state with a mass close to the $D^*\bar{D}^*$ threshold and a narrow width exists. [[arXiv:2207.03930](#)]
- ◆ The newly reported $X(4014)$ state still needs to be studied, and its favored quantum numbers also need to be discussed.

$\gamma\gamma \rightarrow X(3872) \rightarrow \pi^+\pi^-J/\psi$

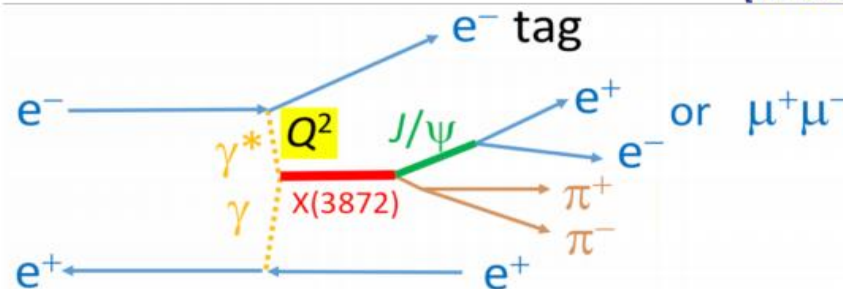
- ◆ The charmonium-like state $X(3872)$ has been observed in various interaction, but not searched for in two-photon interactions
- ◆ Mesons with $J^{PC} = 1^{++}$ can be produced if one or both photons are highly virtual — denoted as γ^*

$X(3872): J^{PC} = 1^{++}$

$\gamma\gamma \rightarrow X(3872) \rightarrow$ Not allowed

But, $\gamma^*\gamma \rightarrow X(3872) \rightarrow$ Allowed

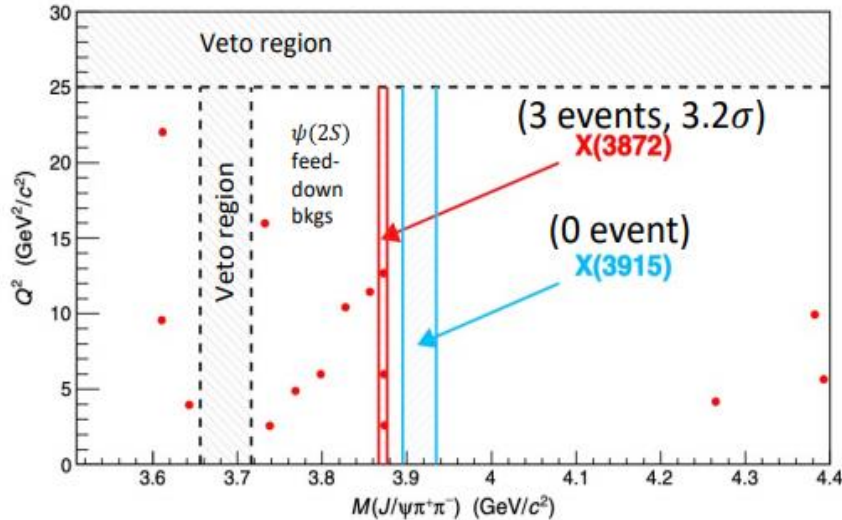
[NPB 523, 423 (1998)]



- ◆ The value of two-photon decay width, obtained from this measurement, is sensitive to the internal structure of the $X(3872)$.

$\gamma\gamma \rightarrow X(3872) \rightarrow \pi^+\pi^-J/\psi$

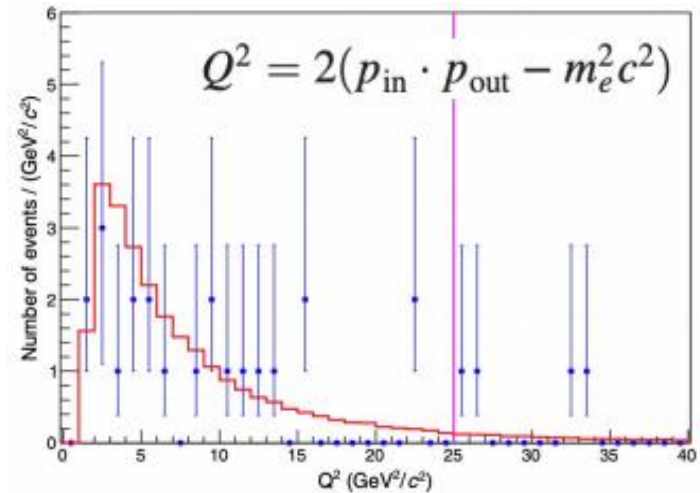
Phys.Rev.Lett.126.122001(2021)



$$\tilde{\Gamma}_{\gamma\gamma} \mathcal{B}(X(3872) \rightarrow J/\psi \pi^+ \pi^-) = 5.5_{-3.8}^{+4.1}(\text{stat}) \pm 0.7(\text{syst}) \text{ eV}.$$

- With future advances in calculations of $\tilde{\Gamma}_{\gamma\gamma}$ for non- $c\bar{c}$ states and higher luminosities accumulated by Belle II, this method will clarify the understanding of the $X(3872)$.

- Assuming the Q^2 dependence of a $c\bar{c}$ meson model



- With $0.032 < \mathcal{B}(X(3872) \rightarrow \pi^+\pi^-J/\psi) < 0.061$ at 90% C.L., $\tilde{\Gamma}_{\gamma\gamma} = 20 - 500 \text{ eV}$, these are consistent with the $c\bar{c}$ model prediction. [NPB 523, 423 (1998), PRD 83, 114015 (2011)]

Summary

- ◆ The two-photon decay width of $\chi_{c2}(1P)$ is determined to be $\Gamma_{\gamma\gamma}(\chi_{c2}(1P)) = 653 \pm 13(stat.) \pm 31(syst.) \pm 17(B.R.)$ eV. The result in BN1501 achieves the precise measurement of $\Gamma_{\gamma\gamma}(\chi_{c2}(1P))$ as of now.
- ◆ The evidence for the R_1 near $3.92 \text{ GeV}/c^2$ may be $X(3915)$, $\chi_{c2}(3930)$ or an admixture of them. A rough estimation shows the partial width $\Gamma(\chi_{c2}(3930) \rightarrow \gamma\psi(2S)) = 200 \sim 300 \text{ keV}$, which is close to the predicted value of 207 keV from GI model. The mass of R_2 agrees with the HQSS-predicted mass ($\approx 4013 \text{ MeV}/c^2$) of the 2^{++} partner of $X(3872)$.
- ◆ The first evidence for $X(3872)$ production was found in two-photon $\gamma^*\gamma$ interactions. Three $X(3872)$ candidates are observed with a significance of 3.2σ , $\Gamma_{\gamma\gamma}\mathcal{B}(X(3872) \rightarrow J/\psi\pi^+\pi^-) = 5.5^{+4.1}_{-3.8}(stat) \pm 0.7(syst)$ eV, assuming the Q^2 dependence of a $c\bar{c}$ meson model.

Thank you!