



湖南大学
HUNAN UNIVERSITY

BESIII

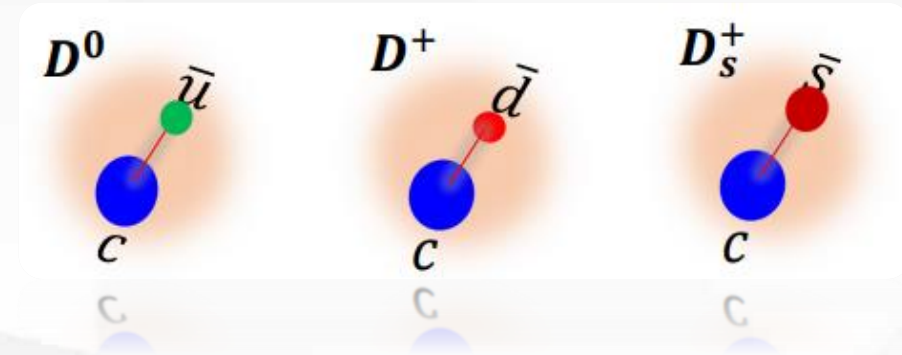
(Semi-)leptonic D decays at BESIII

Qiu-tian Tao
Hunan University
On behalf of the BESIII Collaboration

The 13th International Workshop on e^+e^- collisions from Phi to Psi
August 17, 2022

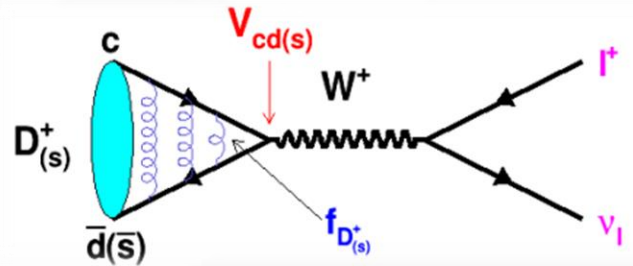


- Motivation
- BESIII experiment
- Pure leptonic decays of D
- Semi-leptonic decays of D
- Summary and prospect





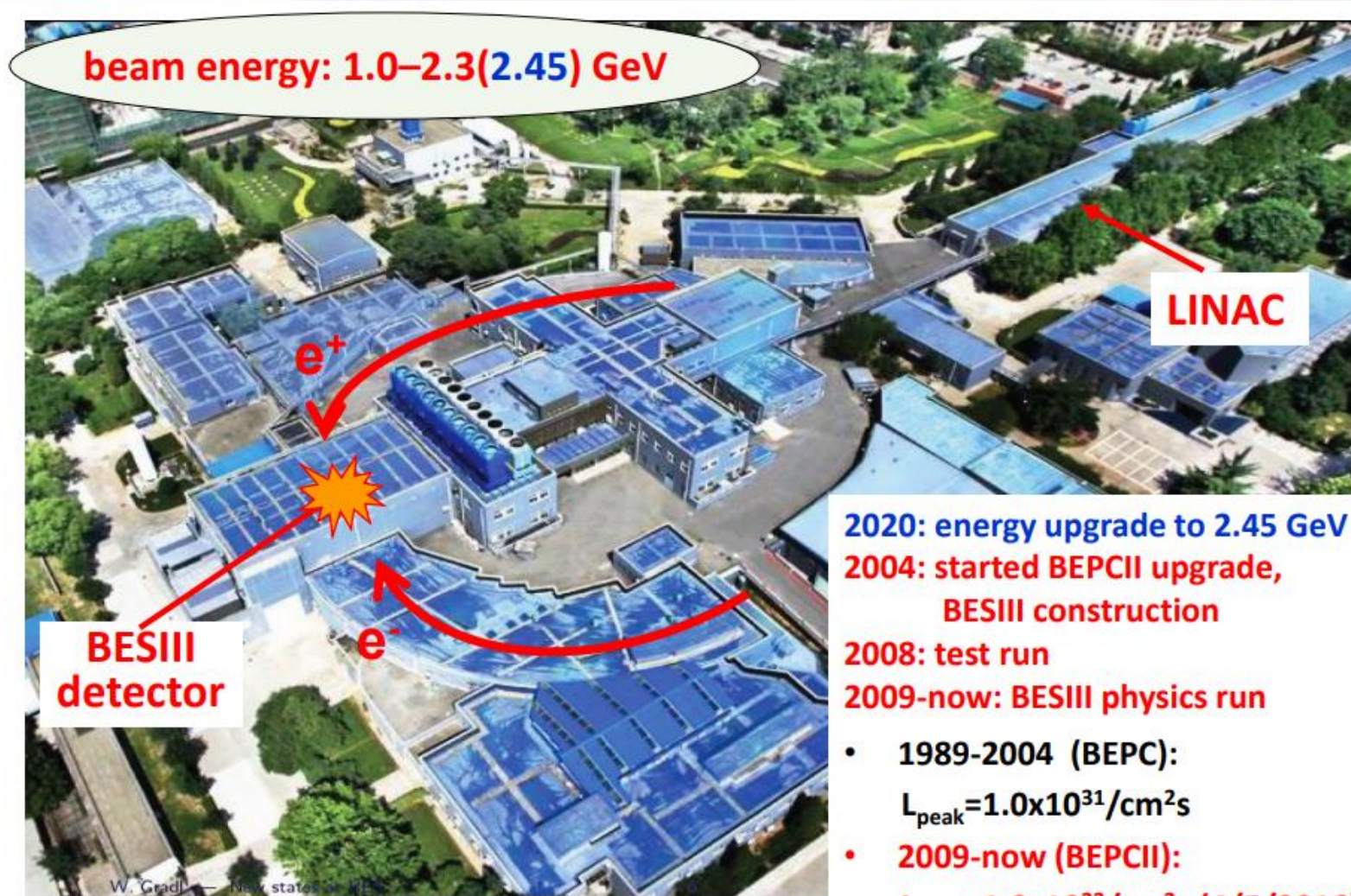
- Measure decay constant and semi-leptonic decay form factor → **Test and Calibrate Lattice QCD**
- Measure CKM matrix element ($|V_{cs}|$, $|V_{cd}|$) → **Test the unitarity of CKM matrix**
- Measure $R = \frac{\mathcal{B}(D_{(s)} \rightarrow \tau^+ \nu_\tau)}{\mathcal{B}(D_{(s)} \rightarrow \mu^+ \nu_\mu)}$ → **Test the lepton flavor universality**



$$\Gamma(D_{(s)}^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_\ell^2 m_{D_{(s)}^+} \left(1 - \frac{m_\ell^2}{m_{D_{(s)}^+}^2}\right)^2$$

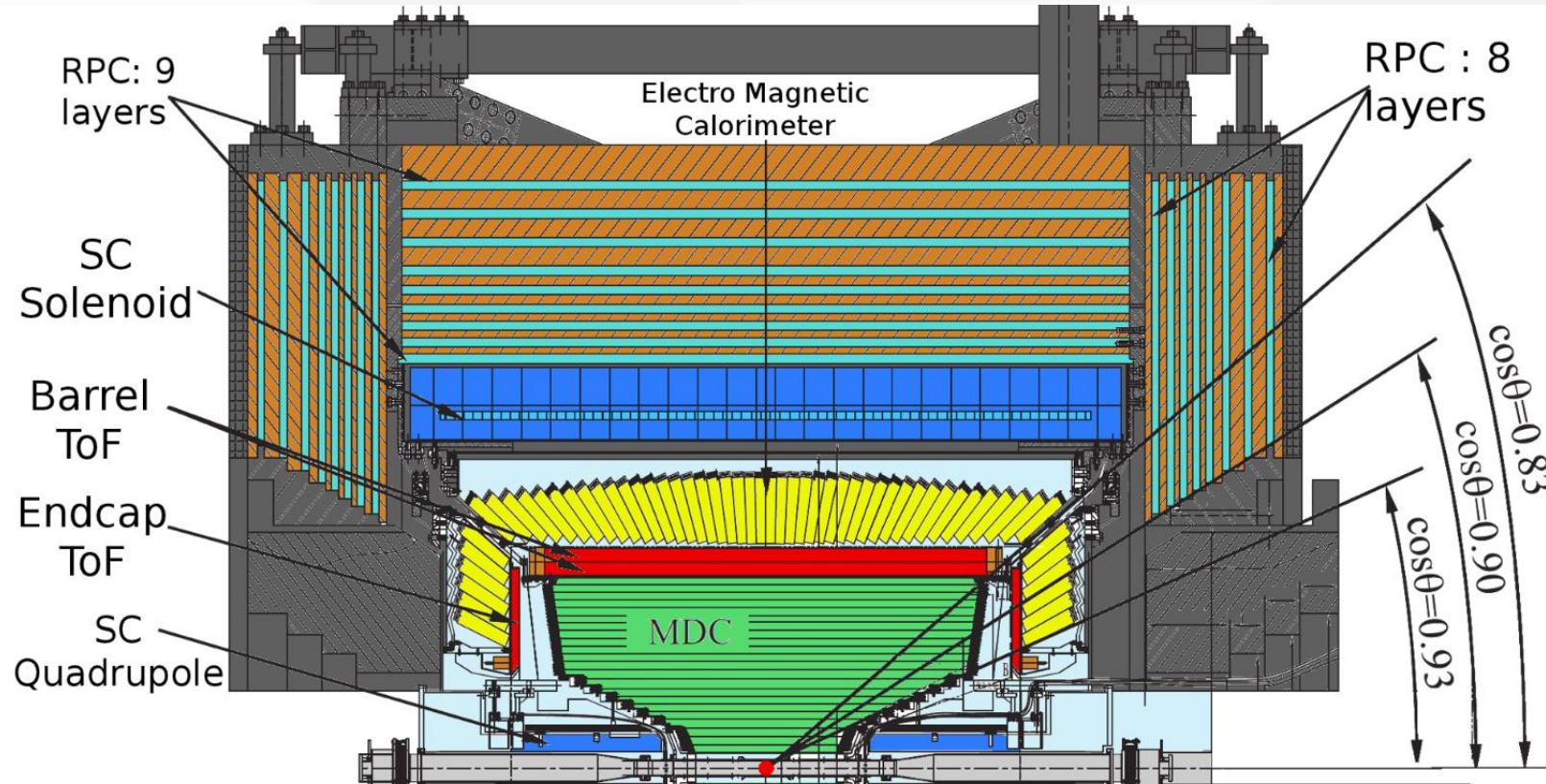


Beijing Electron Positron Collider (BEPCII)





BESIII detector



MDC

$$\frac{\delta p}{p} < 0.5\% \text{ @1 GeV}$$
$$\frac{\delta(dE/dx)}{dE/dx} < 6\%$$

TOF

$$\delta t \text{ 80 ps Barrel}$$
$$\delta t \text{ 110 ps Endcap}$$

EMC

$$\frac{\delta E}{E} < 2.5\% \text{ @1 GeV}$$
$$\delta z = 0.6/\sqrt{E}$$

MUC

$$\delta(xy) < 2 \text{ cm}$$



Data samples at BESIII

TECN	Luminosity (fb^{-1})	E_{cm} (GeV)	Year
BESIII	$D^{+(0)}$: 2.93 (8) D_s^+ : 7.33	3.773 4.128-4.223	2010-2011(+2022) 2013-2019
CLEO-c	$D^{+(0)}$: 0.82 D_s^+ : 0.6	3.770 4.170	— 2008

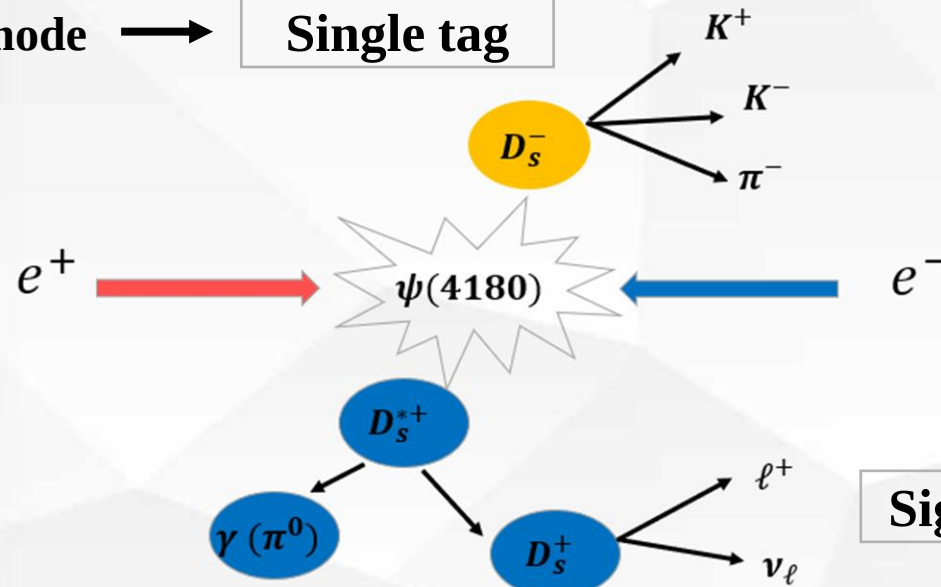
2023—2024 : $8 \rightarrow 20 \text{ fb}^{-1} \psi(3770)$ (for $D^{+(0)}$) at BESIII.



Pure leptonic D decay

Well known mode $\longrightarrow$

Single tag



➤ Single tag (ST)

$$N_{tag}^{ST} = 2N_{D_s^* D_s} \mathcal{B}_{tag} \epsilon_{tag}$$

➤ Double tag (DT)

$$N_{tag,sig}^{DT} = 2N_{D_s^* D_s} \mathcal{B}_{tag} \mathcal{B}_{sig} \mathcal{B}_{\gamma(\pi^0)} \epsilon_{sig}$$

$$\mathcal{B}_{sig} = \frac{N_{tag,sig}^{DT}}{\mathcal{B}_{\gamma(\pi^0)} \sum_{\alpha} N_{tag}^{ST,\alpha} \epsilon_{sig}^{\alpha} / \epsilon_{tag}^{\alpha}}$$

$$\mathcal{B}_{\gamma(\pi^0)} = \mathcal{B}(D_s^* \rightarrow \gamma(\pi^0) D_s)$$

Signal side

$\longleftarrow$ Aim to study

$$M_{miss}^2 = E_{miss}^2 - |\vec{p}_{miss}|^2$$



Studies of $D_s^+ \rightarrow \ell^+ \nu_\ell$

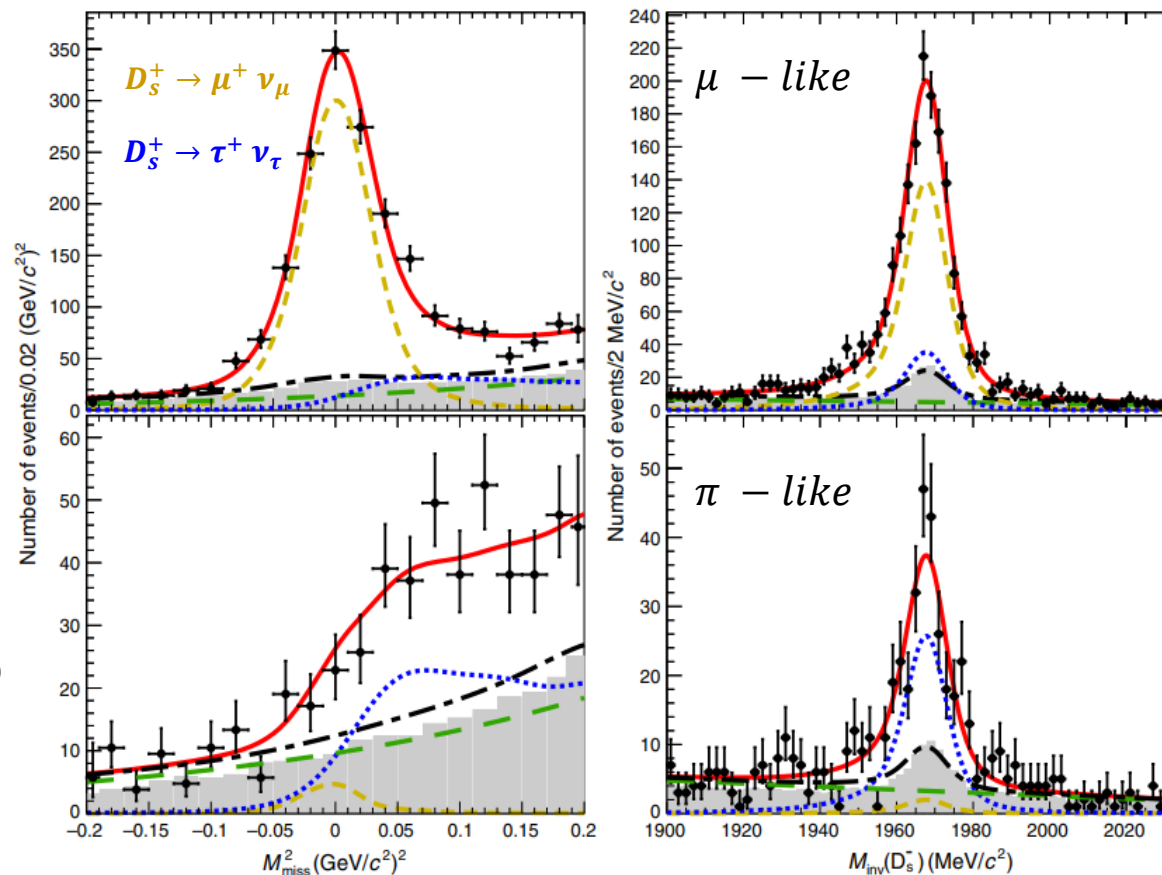
Phys. Rev. D 104, 052009 (2021)

- **Data:** 6.3 fb^{-1} @4.18 – 4.23 GeV
- $N_{sig} = 2198 \pm 55$, $N_{sig} = 946 \pm 46$
- $\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu) = (5.35 \pm 0.13 \pm 0.16) \times 10^{-3}$
- $f_{D_s^+} |V_{cs}| = (243.1 \pm 3.0 \pm 3.7) \text{ MeV } [\mu] \text{ precision} \sim 2.0\%$
- $\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau) = (5.21 \pm 0.25 \pm 0.17)\%$
- $f_{D_s^+} |V_{cs}| = (243.0 \pm 5.8 \pm 4.0) \text{ MeV } [\tau] \text{ precision} \sim 2.9\%$

$$R = \frac{\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau)}{\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu)} = 9.73_{-0.58}^{+0.61} \pm 0.37$$

SM prediction: 9.75 ± 0.01

$D_s^+ \rightarrow \mu^+ \nu_\mu$ and $D_s^+ \rightarrow \tau^+ (\pi^+ \bar{\nu}_\tau) \nu_\tau$





Studies of $D_s^+ \rightarrow \ell^+ \nu_\ell$

Phys. Rev. D 104, 032001 (2021)

$D_s^+ \rightarrow \tau^+ (\rho^+ \bar{\nu}_\tau) \nu_\tau$

➤ **Data:** 6.3 fb^{-1} @4.18 – 4.23 GeV

➤ $N_{sig} = 1745 \pm 84$

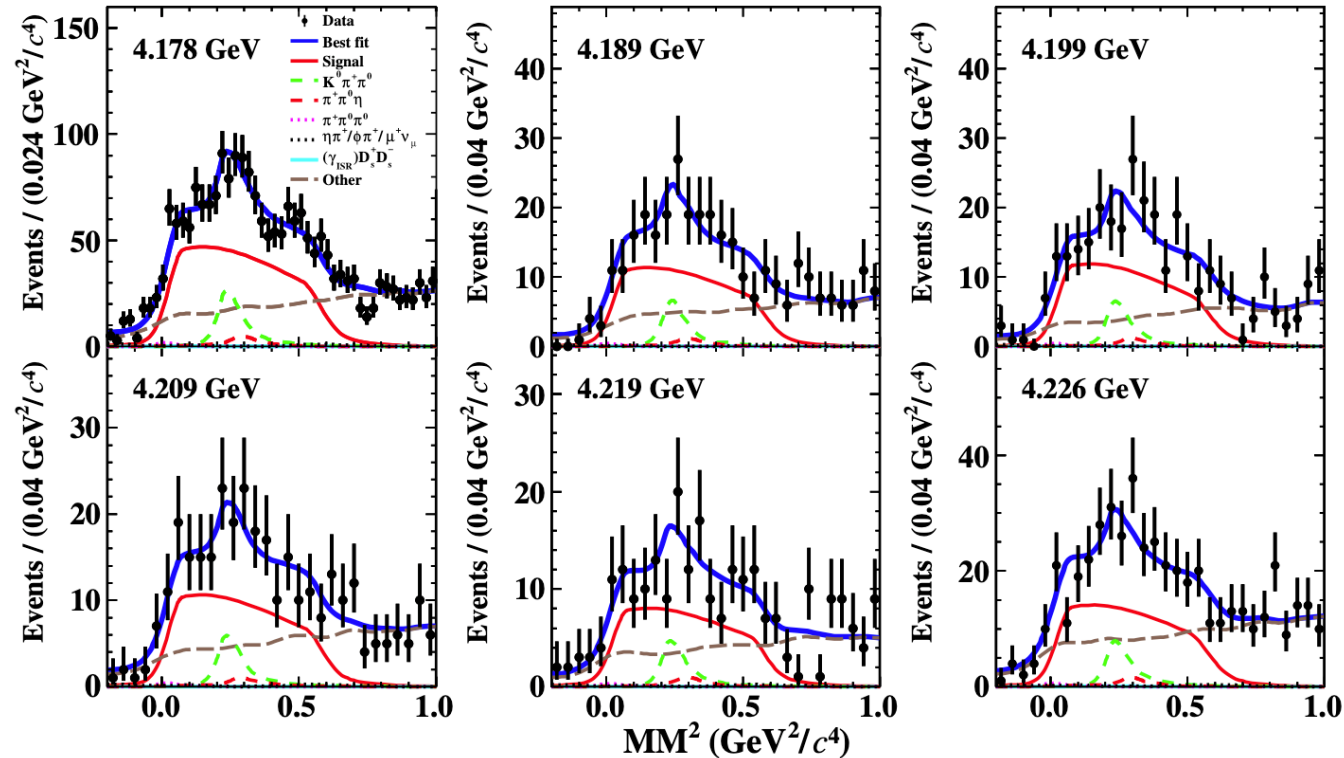
➤ $\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau) = (5.29 \pm 0.25 \pm 0.20)\%$

$f_{D_s^+} |V_{cs}| = (244.8 \pm 5.8 \pm 4.8) \text{ MeV}$ **precision~3.1%**

$$R = \frac{\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau)}{\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu)_{\text{BESIII}}} = 9.89 \pm 0.71$$

SM prediction: 9.75 ± 0.01

BESIII: Phys. Rev. D 104, 052009 (2021)





Studies of $D_s^+ \rightarrow \ell^+ \nu_\ell$

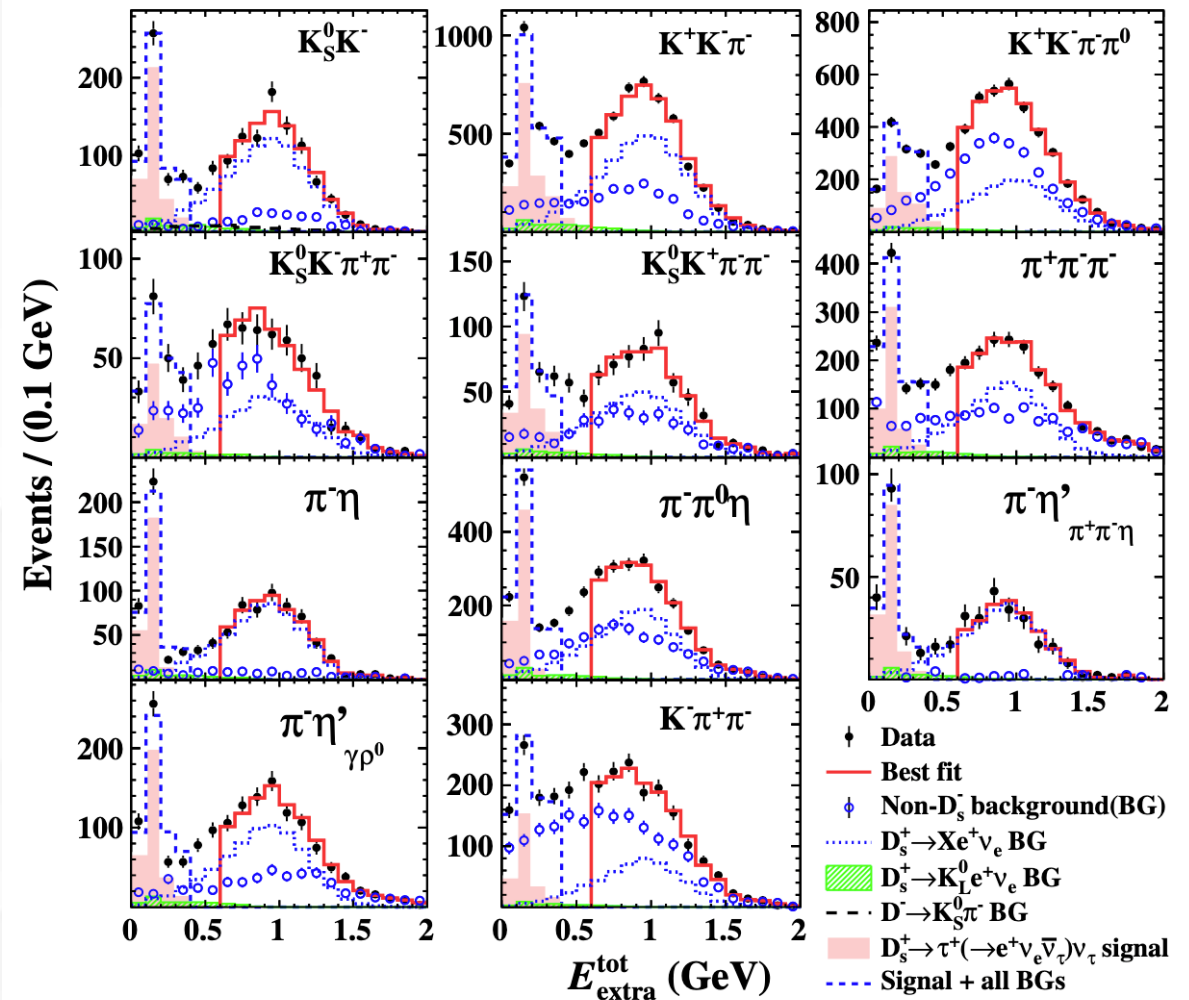
Phys. Rev. Lett. 127, 171801 (2021)

- Data: 6.3 fb^{-1} @ 4.18 – 4.23 GeV
- $N_{sig} = 4940 \pm 97$
- $\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau) = (5.27 \pm 0.10 \pm 0.12)\%$
- $f_{D_s^+} |V_{cs}| = (244.4 \pm 2.3 \pm 2.9) \text{ MeV}$ precision~1.5%

$$R = \frac{\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau)}{\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu)_{PDG}} = 9.72 \pm 0.37$$

SM prediction: 9.75 ± 0.01

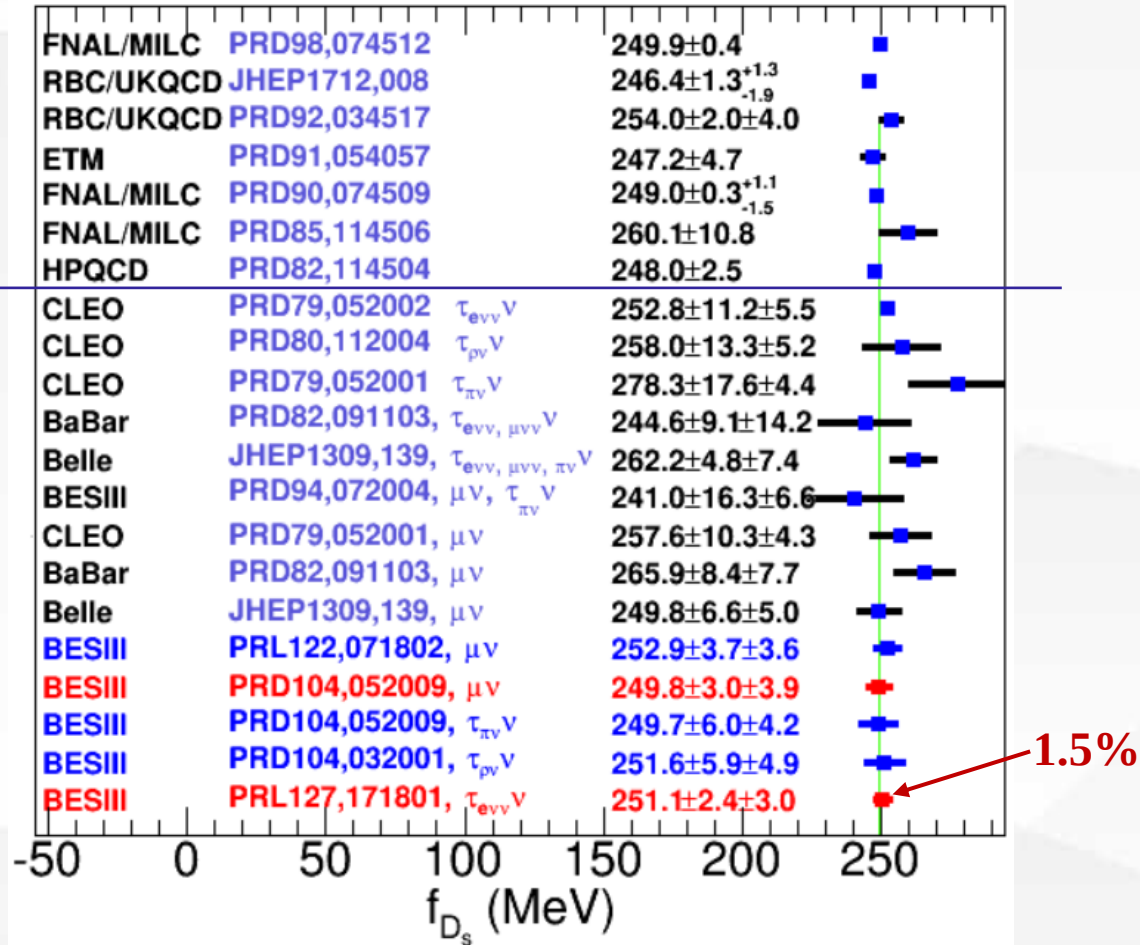
$$D_s^+ \rightarrow \tau^+ (e^+ \nu_e \bar{\nu}_\tau) \nu_\tau$$



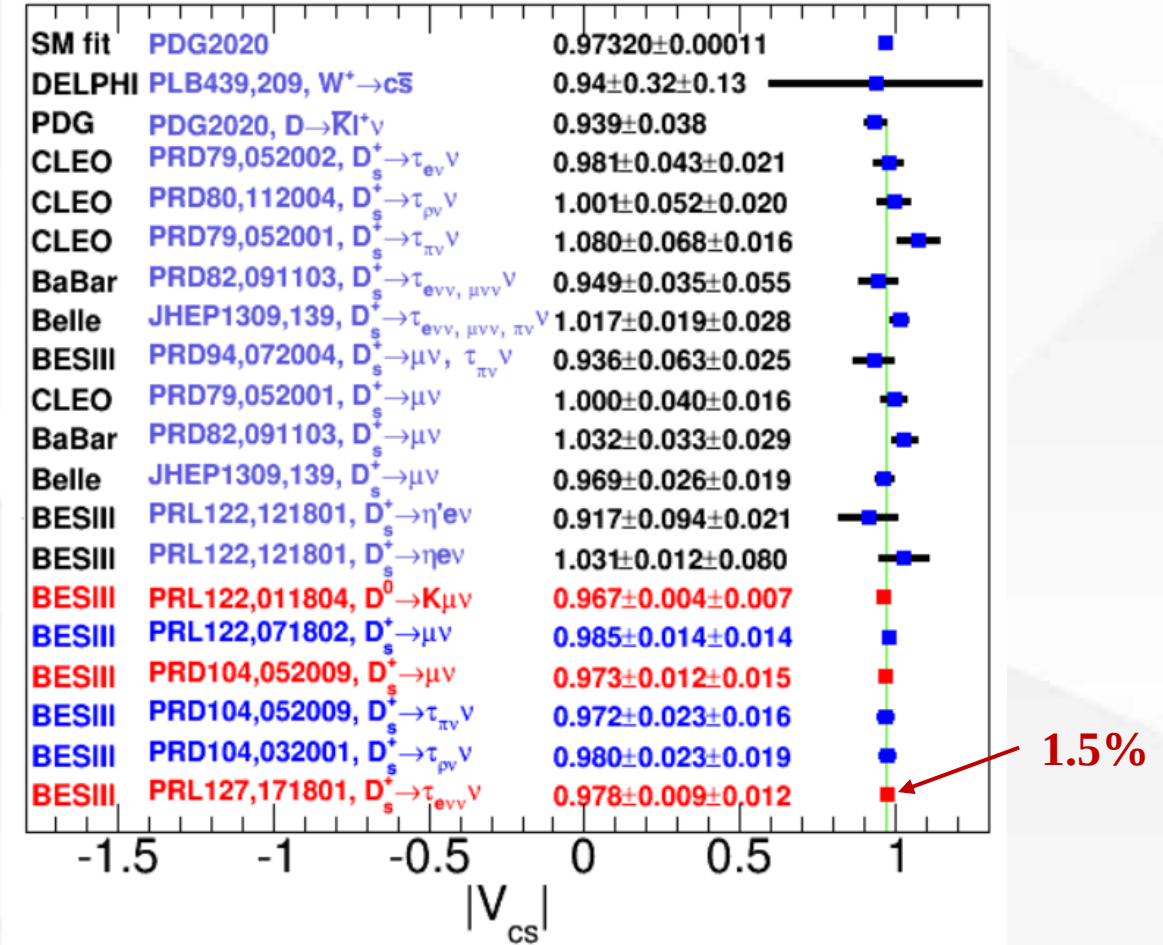


Comparisons of $f_{D_s^+}$ and $|V_{cs}|$

$f_{D_s^+}$

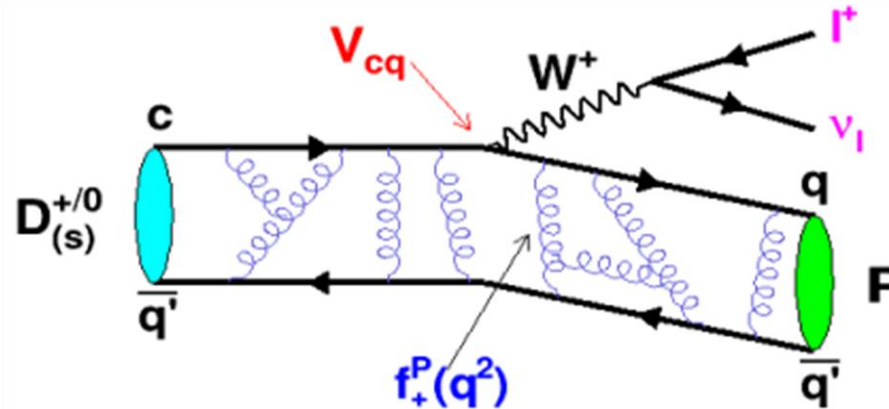


$|V_{cs}|$





Semi-leptonic $D \rightarrow P(S) e^+ \nu_e$



$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2$$

$(X = 1 \text{ for } K^-, \pi^-, \bar{K}^0, \eta^{(\prime)}; X = \frac{1}{2} \text{ for } \pi^0)$

Dynamics study

$$f_+^{D \rightarrow P(S)}(0) |V_{cd(s)}|$$

★ Very helpful for us to study:

- light meson spectrum
- Nonperturbative QCD by measuring the form factor

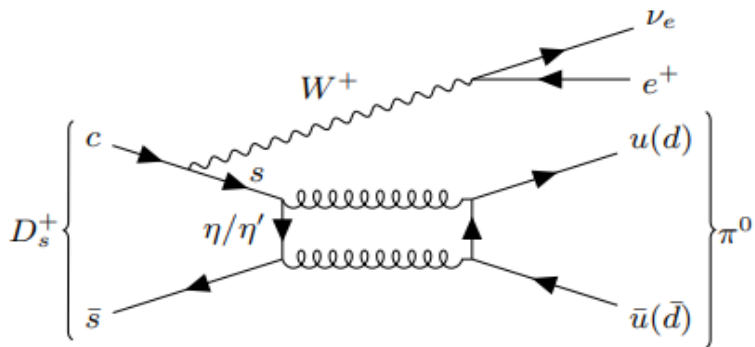
Parametric form of form factor:

(1) Single pole form (2) Modified pole model (3) ISGW2 model (4) Series expansion model



Study of $D_s^+ \rightarrow \pi^0 e^+ \nu_e$

arXiv:2206.13870(2022)

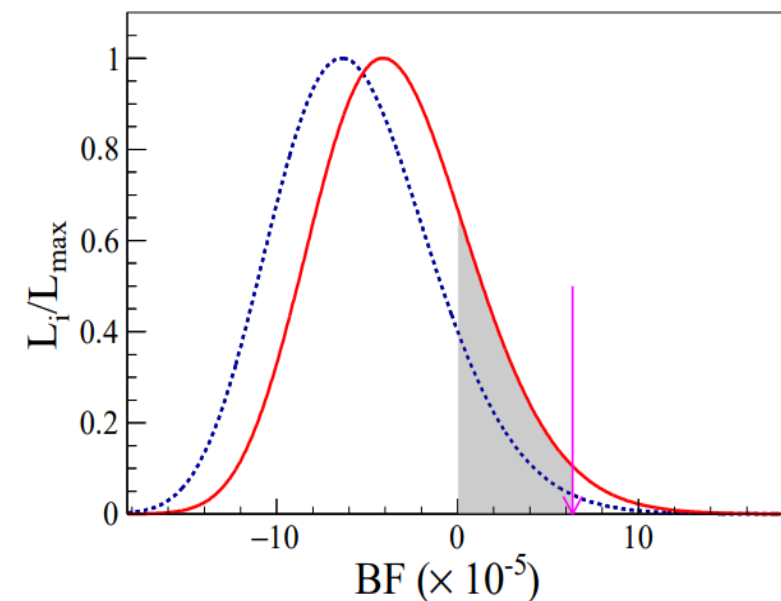
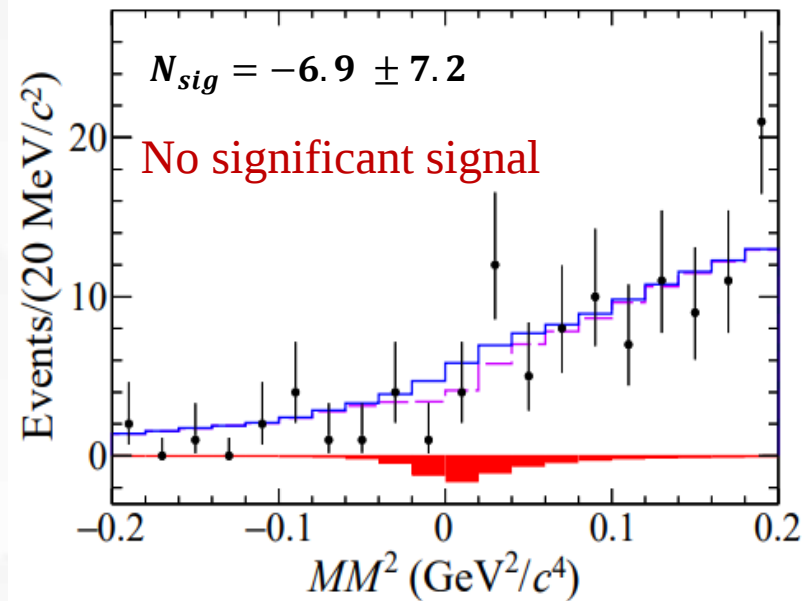


To study $\pi^0 - \eta$ mixing effect

➤ **Data:** 6.3 fb^{-1} @4.18 – 4.23 GeV

➤ $\mathcal{B}(D_s^+ \rightarrow \pi^0 e^+ \nu_e) < 6.4 \times 10^{-5} @90\% \text{CL}$

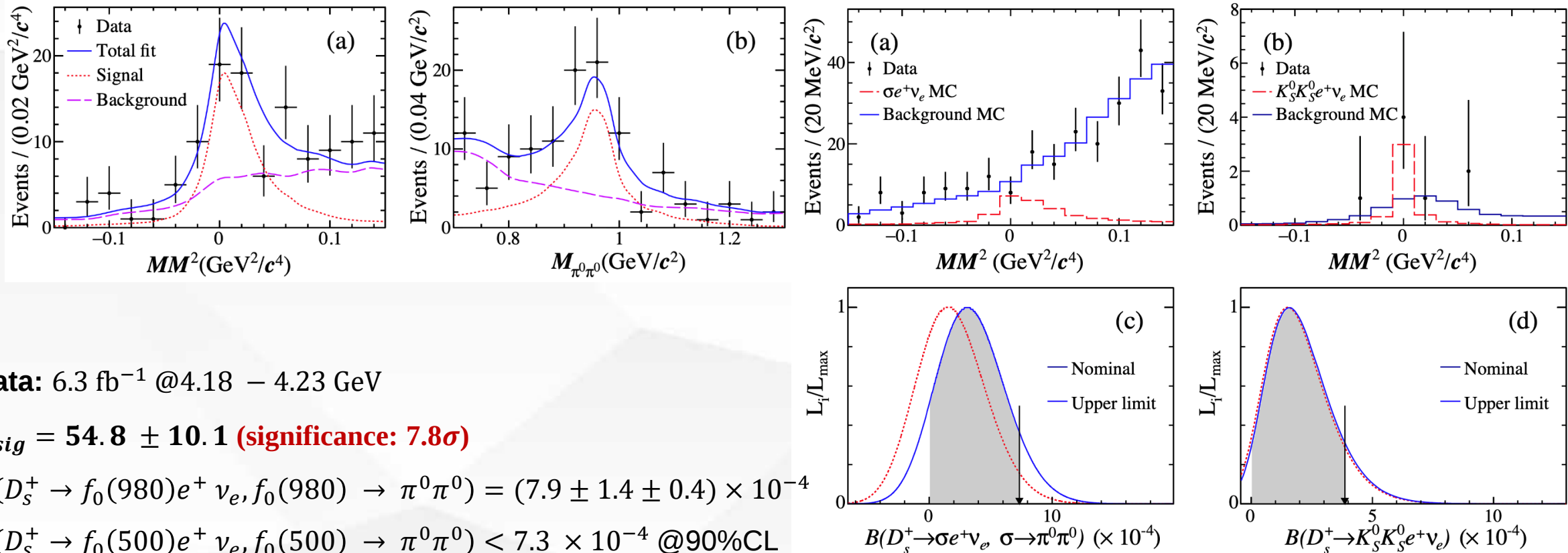
Theory: $(2.65 \pm 0.38) \times 10^{-5}$ [PLB811,135879(2020)]





Phys. Rev. D(L) 105, L031101 (2022)

No significant signal



- **Data:** 6.3 fb^{-1} @ $4.18 - 4.23 \text{ GeV}$
- $N_{\text{sig}} = 54.8 \pm 10.1$ (**significance: 7.8σ**)
- $B(D_s^+ \rightarrow f_0(980)e^+ \nu_e, f_0(980) \rightarrow \pi^0 \pi^0) = (7.9 \pm 1.4 \pm 0.4) \times 10^{-4}$
- $B(D_s^+ \rightarrow f_0(500)e^+ \nu_e, f_0(500) \rightarrow \pi^0 \pi^0) < 7.3 \times 10^{-4}$ @90%CL
- $B(D_s^+ \rightarrow K_S^0 K_S^0 e^+ \nu_e) < 3.8 \times 10^{-4}$ @90%CL



Inclusive D_s semi-leptonic decay

Phys. Rev. D 104, 012003 (2021)

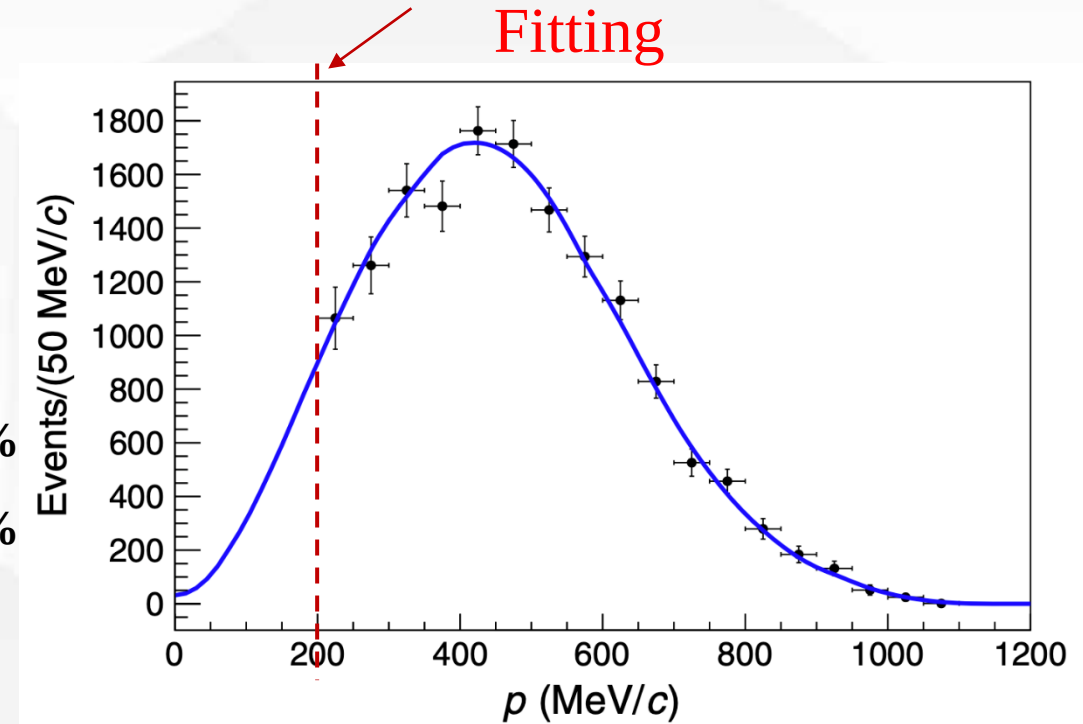
- **Data:** 6.3 fb^{-1} @4.18 – 4.23 GeV
- $N_{\text{tag}}(D_s^- \rightarrow K^+ K^- \pi^-) = \mathbf{262660 \pm 1137}$
- $N_{\text{sig}} = \mathbf{16648 \pm 326}$

$$\mathcal{B}(D_s^+ \rightarrow X e^+ \nu_e) = (6.30 \pm 0.13 \pm 0.09 \pm 0.04)\% \quad \text{Precision} \sim 2.6\%$$

$$\mathcal{B}(D_s^+ \rightarrow X e^+ \nu_e)_{\text{CLEO}} = (6.52 \pm 0.39 \pm 0.15)\% \quad \text{Precision} \sim 6.4\%$$

$$\begin{aligned} & \mathcal{B}(D_s^+ \rightarrow X e^+ \nu_e) - \sum_i \mathcal{B}(D_s^+ \rightarrow X_i e^+ \nu_e) \\ &= (-0.04 \pm 0.13 \pm 0.09 \pm 0.17)\% \end{aligned}$$

No evidence for unobserved
exclusive semi-electronic modes



Extract $D_s^+ \rightarrow X e^+ \nu_e$ signal yields from e^+
momentum spectrum



New method for $D \rightarrow K e \nu_e$

Phys. Rev. D 104, 052008 (2021)

Independent sample of previous measurement
with hadronic tags

➤ **Data:** 2.93 fb^{-1} @3.773 GeV

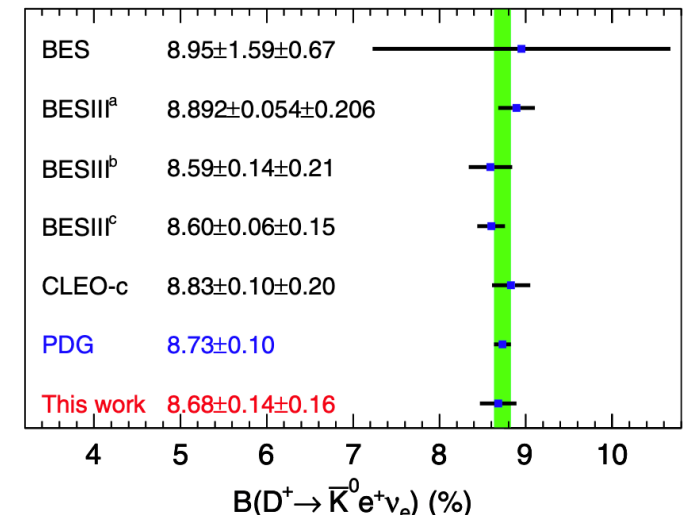
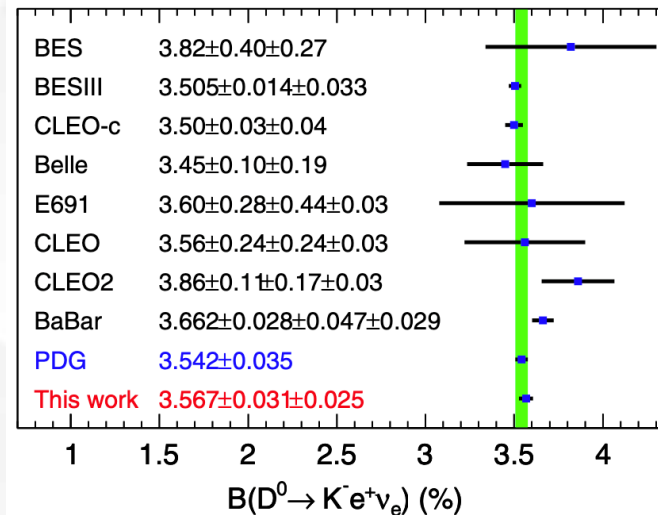
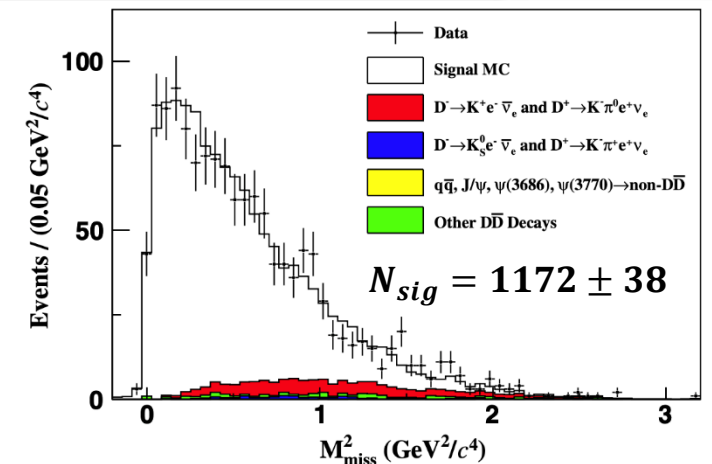
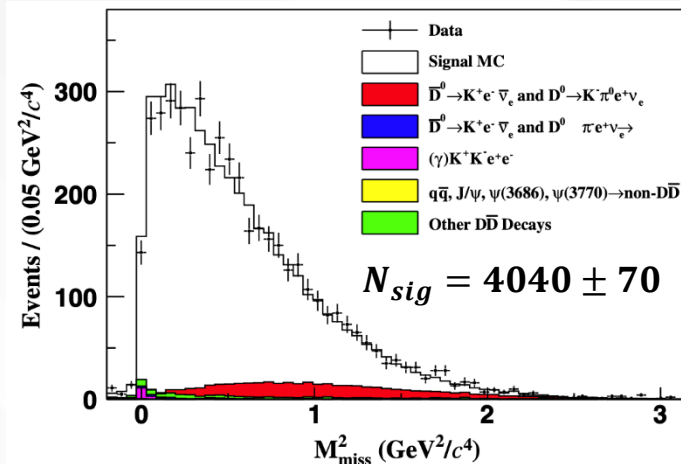
➤ $\mathcal{B}_{SL} = \sqrt{N_{DT}/(N_{D\bar{D}} \cdot \epsilon_{DT})}$

$$\mathcal{B}(D^0 \rightarrow K^- e^+ \nu_e) = (3.567 \pm 0.031 \pm 0.025)\%$$

$$\mathcal{B}(D^+ \rightarrow \bar{K}^0 e^+ \nu_e) = (8.68 \pm 0.14 \pm 0.16)\%$$

$$D^0 \rightarrow K^- e^+ \nu_e$$

$$D^+ \rightarrow \bar{K}^0 e^+ \nu_e$$





New decay mode $D^{*0} \rightarrow D^0 e^+ e^-$

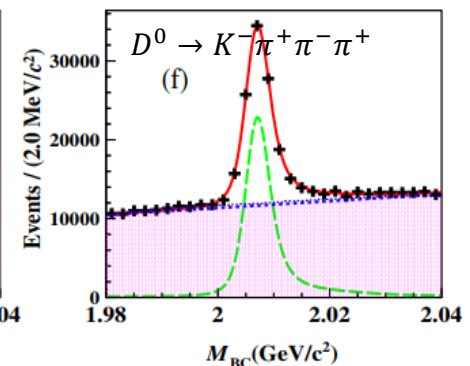
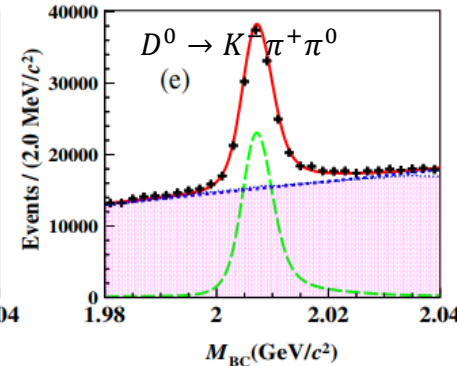
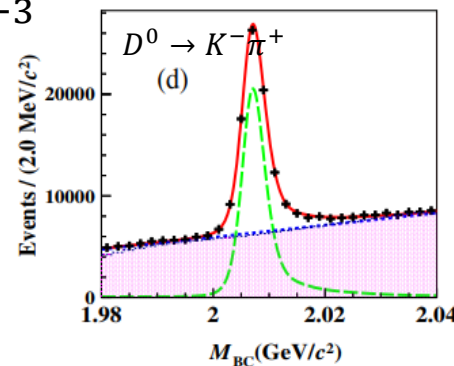
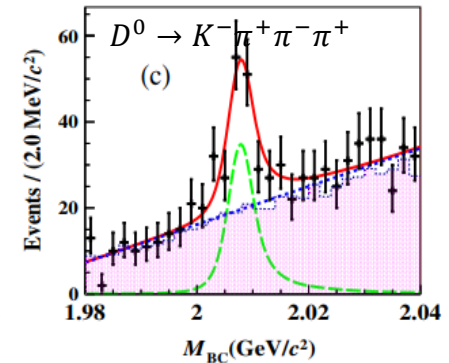
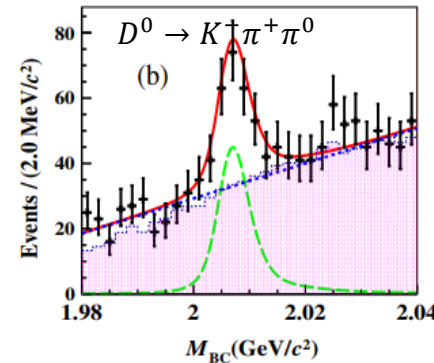
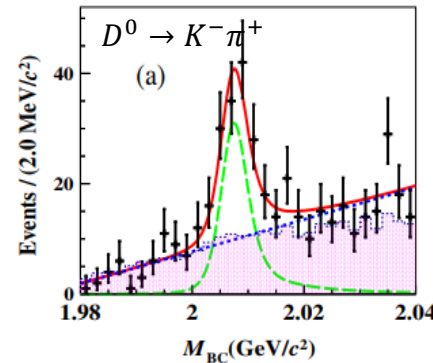
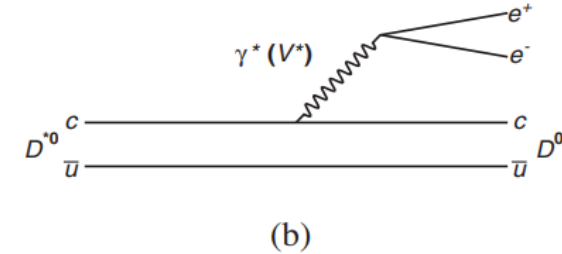
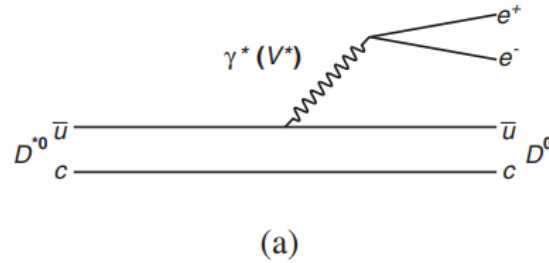
Phys. Rev. D 104, 112012 (2021)

➤ **Data:** 3.19 fb^{-1} @4.18

➤ $N_{sig} = 420.9 \pm 16.9$

➤ $N_{ref} = 238151 \pm 468$

$$\begin{aligned} \mathcal{B}(D^{*0} \rightarrow D^0 e^+ e^-) &= \frac{N_{sig} \cdot \epsilon_{ref}}{N_{ref} \cdot \epsilon_{sig}} \cdot \mathcal{B}_{ref} \\ &= (3.91 \pm 0.27 \pm 0.17 \pm 0.10) \times 10^{-3} \end{aligned}$$



$D^{*0} \rightarrow D^0 e^+ e^-$

$D^{*0} \rightarrow D^0 \gamma$



➤ Summary

- (1) We have reported precision measurements of $f_{D_s^+}$, $|V_{cs}|$ and test of lepton flavor universality by studying the leptonic decays of $D_s^+ \rightarrow \tau^+ \nu_\tau$.
- (2) We have reported the studies of $D_s^+ \rightarrow \pi^0 e^+ \nu_e$, $D_s^+ \rightarrow \pi^0 \pi^0 e^+ \nu_e$, $D_s^+ \rightarrow K_S^0 K_S^0 e^+ \nu_e$ and inclusive D_s semi-leptonic decay.
- (3) We have also reported the new method for $D \rightarrow K e \nu_e$ and the new decay mode $D^{*0} \rightarrow D^0 e^+ e^-$.

➤ Prospect @3.773 GeV --From White Paper (Chin. Phys. C 44, 040001 (2020))

- (1) 20 fb⁻¹ of data set at 3.773 GeV is on the way.
- (2) BESIII is expected to provide unique data to improve the statistical uncertainty of f_{D^+} and $|V_{cd}|$ from about 2.6% to about 1.0% and test LFU in $D^+ \rightarrow \ell^+ \nu_\ell$ decays.
- (3) All form factor measurements which are currently statistically limited will be improved by a factor of up to 2.6.

Thanks for your attention

Backup



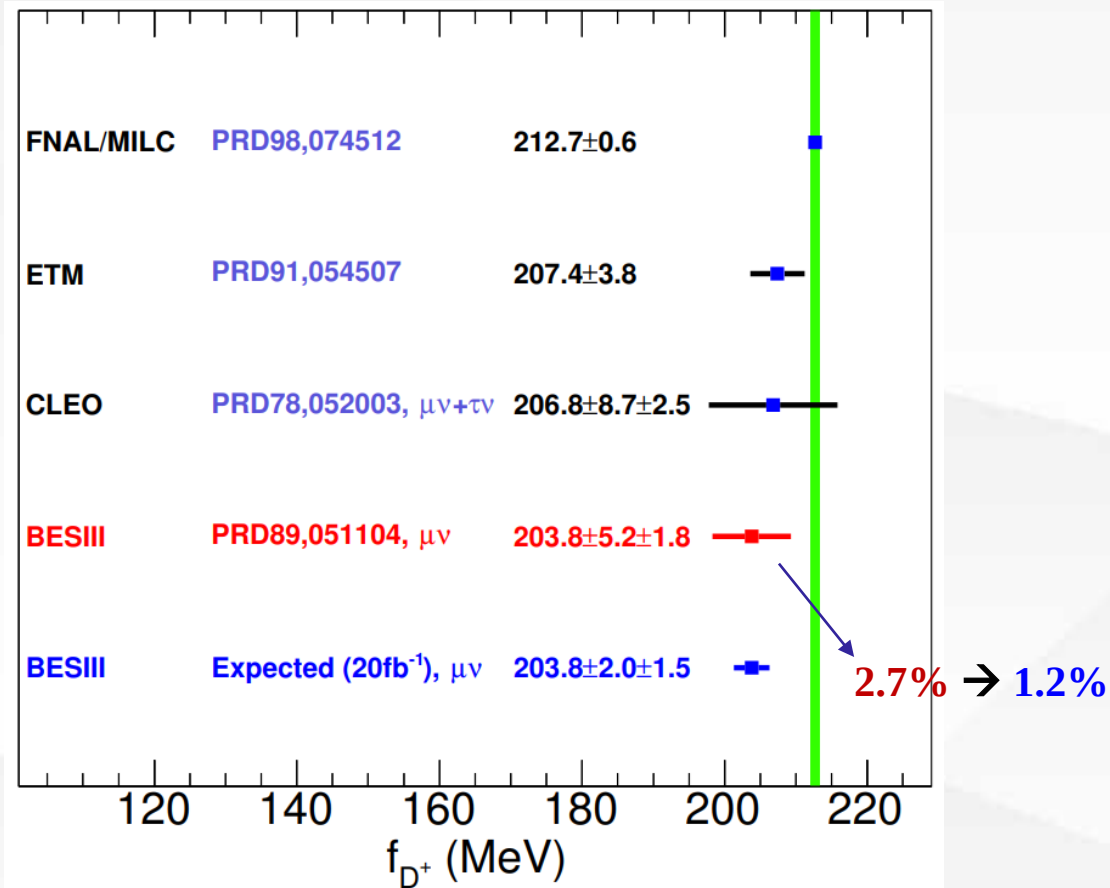
Other semi-leptonic D decays

✓ $D^0 \rightarrow K_1(1270)^- e^+ \nu_e$	PRL127,131801(2021)
✓ $D^0 \rightarrow \rho(770)^- \mu^+ \nu_\mu$	PRD104,L091103(2021)
✓ $D^{0(+)} \rightarrow b_1(1235)^{-(0)} e^+ \nu_e$	PRD102,112005(2020)
✓ $D^+ \rightarrow \eta \mu^+ \nu_\mu$	PRL124,231801(2020)
✓ $D^+ \rightarrow \omega \mu^+ \nu_\mu$	PRD101,072005(2020)
✓ $D^+ \rightarrow K_1(1270)^0 e^+ \nu_e$	PRL123,231801(2019)
✓ $D^{0(+)} \rightarrow \pi^- \pi^{0(+)} e^+ \nu_e$	PRL122,062001(2019)
✓ $D_s^+ \rightarrow K^{(*)0} e^+ \nu$	PRL122,061801(2019)
✓ $D^0 \rightarrow \bar{K}^0 \pi^- e^+ \nu_e$	PRD99,011103R(2019)
✓ $D_s^+ \rightarrow p \bar{p} e^+ \nu_e$	PRD100,112008(2019)
✓ $D_s^+ \rightarrow \gamma e^+ \nu_e$	PRD99,072002(2019)
✓ $D^0 \rightarrow K^- \mu^+ \nu_\mu$	PRL122,011804(2019)
✓ $D^+ \rightarrow \tau^+ \nu_\tau$	PRL123,211802(2019)
✓ $D^{0(+)} \rightarrow a_0(980)^{-(0)} e^+ \nu$	PRL121,081802(2018)
✓ $D_s^+ \rightarrow \eta^{(\prime)} \mu^+ \nu$ and $\phi \mu^+ \nu$	PRD97,012006(2018)
✓ $D^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$	PRD97,092009(2018)
✓ $D^{0(+)} \rightarrow \pi^{-(0)} \mu^+ \nu_\mu$	PRL121,171803(2018)

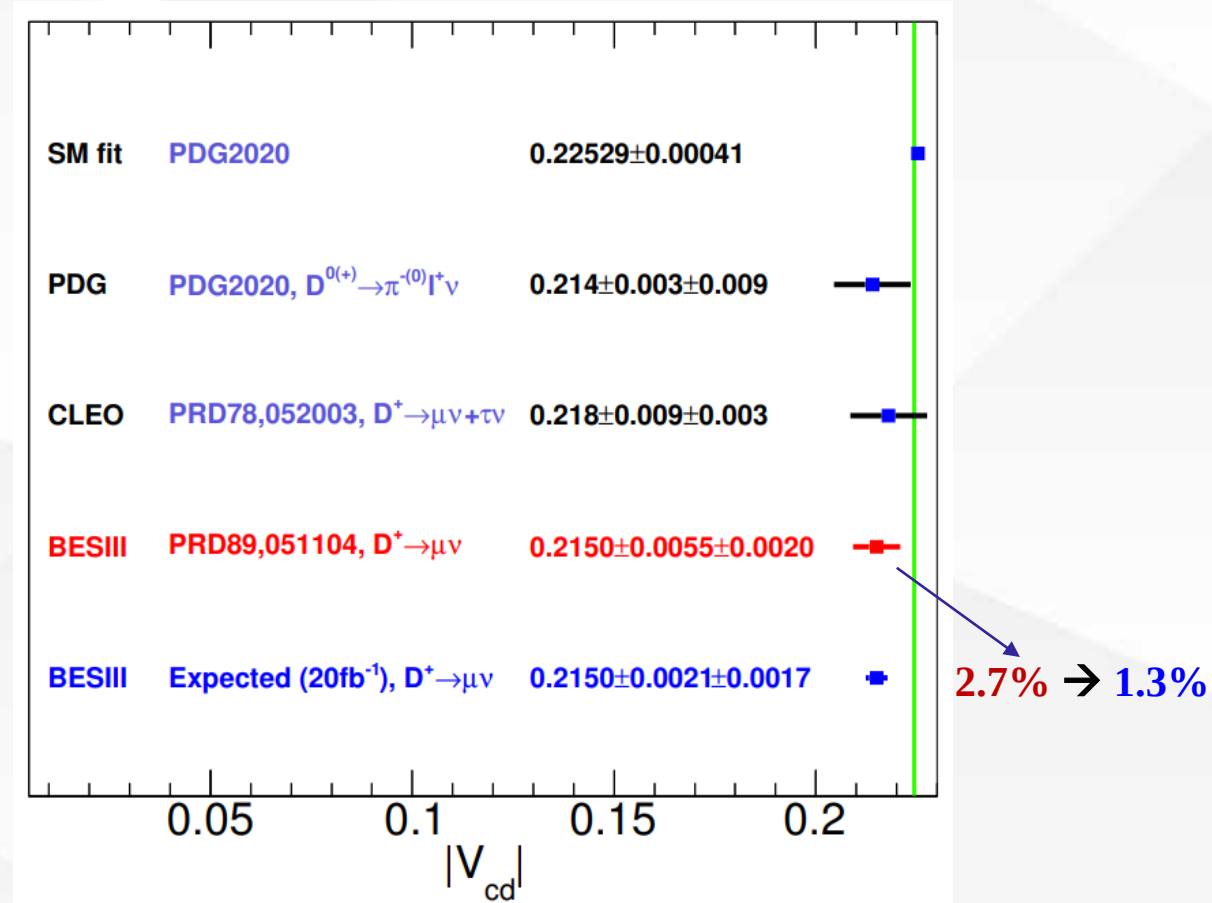


Comparisons of f_{D^+} and $|V_{cd}|$

f_{D^+}



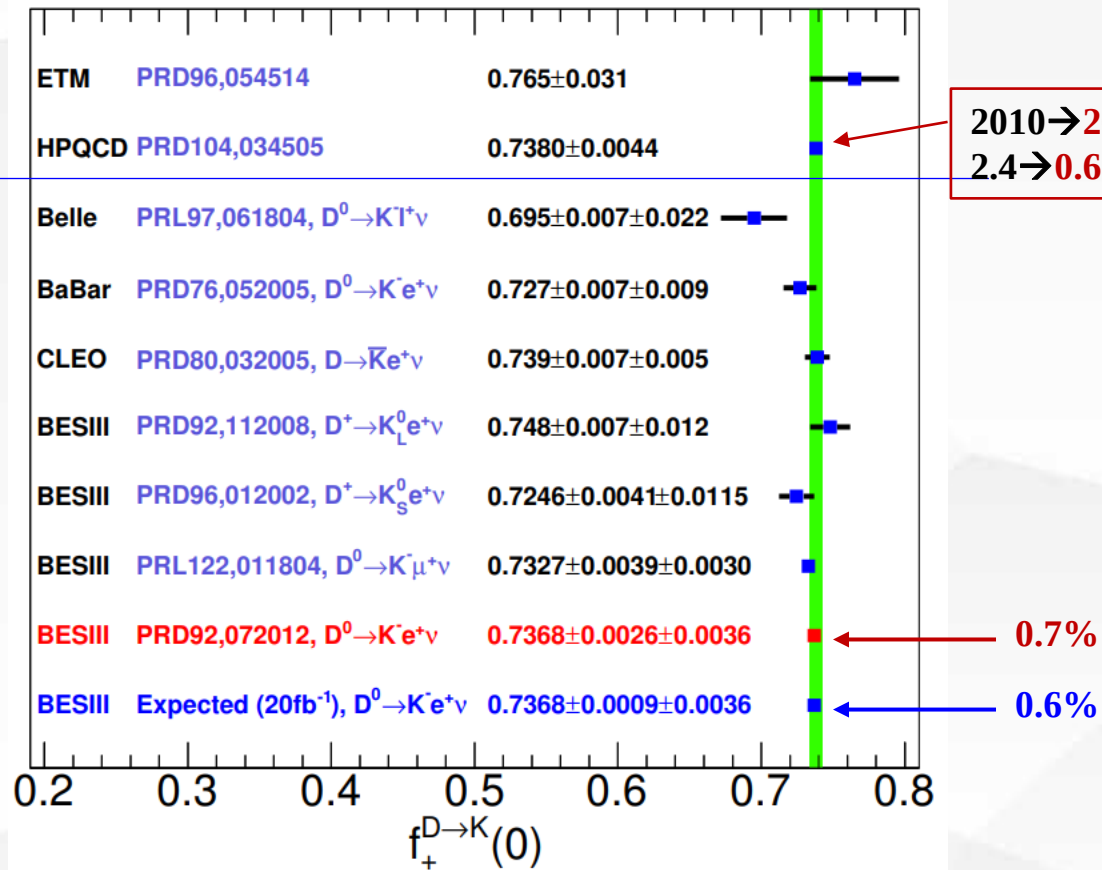
$|V_{cd}|$





Comparisons of $f_+^{D \rightarrow K}(0)$ and $f_+^{D \rightarrow \pi}(0)$

$$f_+^{D \rightarrow K}(0)$$

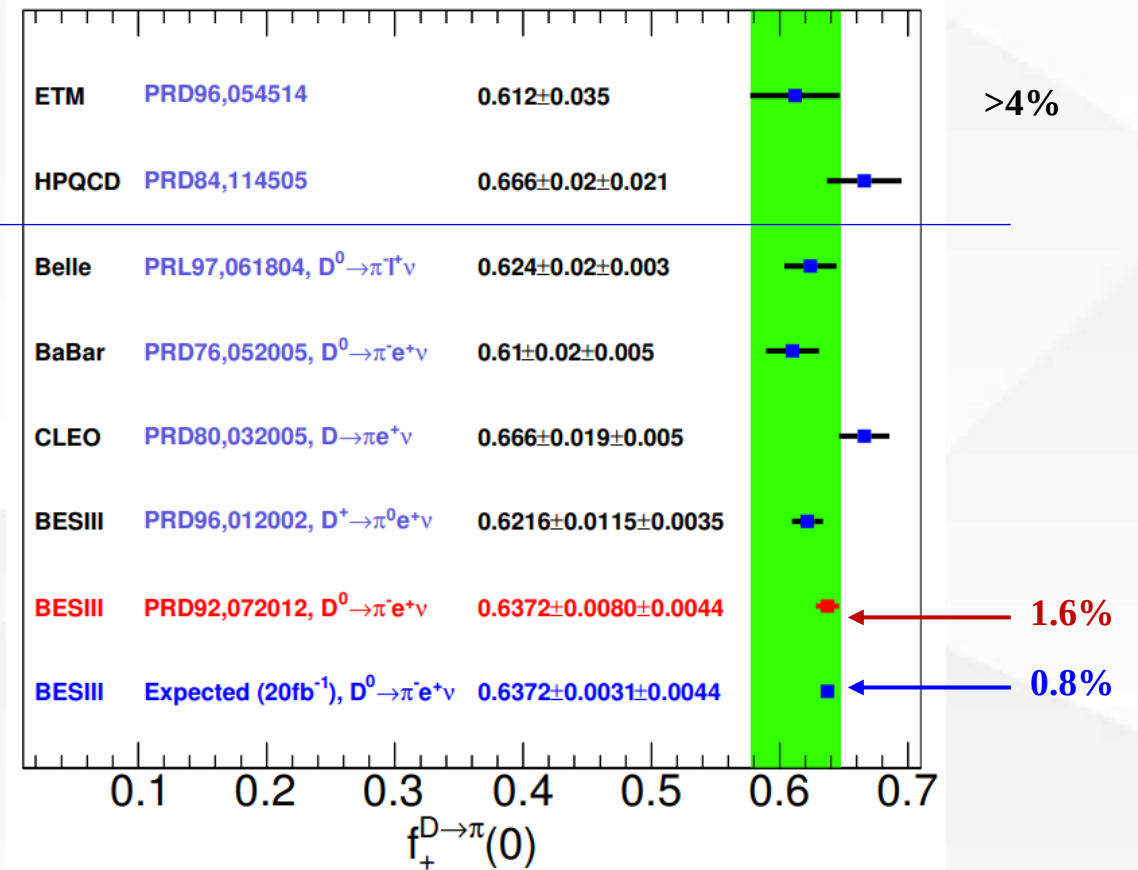


2010 → 2021
2.4 → 0.6%

0.7%

0.6%

$$f_+^{D \rightarrow \pi}(0)$$



>4%

1.6%

0.8%