

Observation of several new tetra-quark states at the LHCb experiment

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Outline

- **Introduction**
- **A general amplitude analysis tool: TF-PWA**
- **First observation of a double charged tetraquark state and its neutral partner**
- **First observation of a resonant structure near $D_S^+ D_S^-$ threshold**
- **Conclusion**

Composition of nature

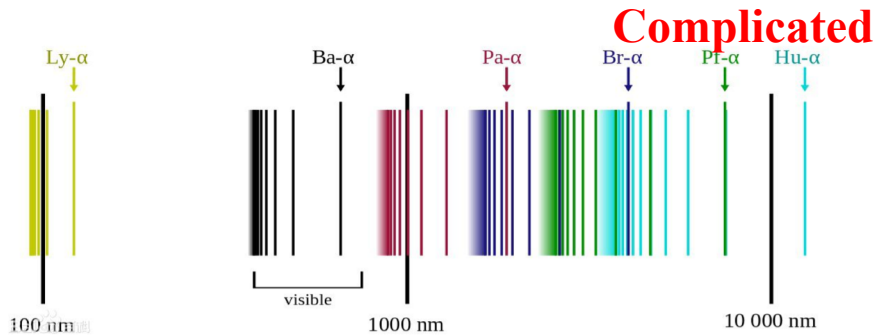
古代哲学



网络图片

Atomic spectrum

赛先生



Measurements



Empirical summary

Balmer's equation:

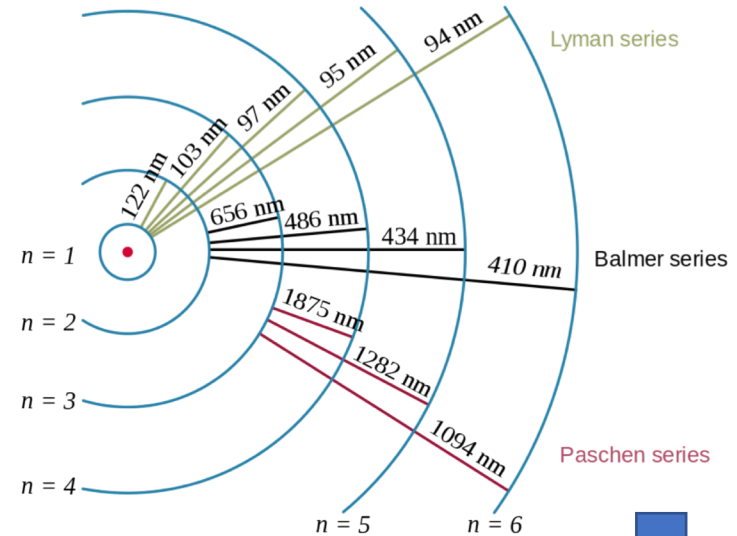
$$\lambda = 365.46 \frac{n^2}{n^2 - 2^2} \text{ nm}, \quad n = 3, 4, 5, \dots$$

Rydberg's equation:

$$\sigma = \frac{1}{\lambda} = R \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right) \quad R = 1.0973731534 \times 10^7 \text{ m}^{-1}$$

$$n_f = 1, 2, 3, 4, \dots, \quad n_i = n_f + 1, n_f + 2, n_f + 3, \dots$$

Bohr model



Surprisingly successful model



介子

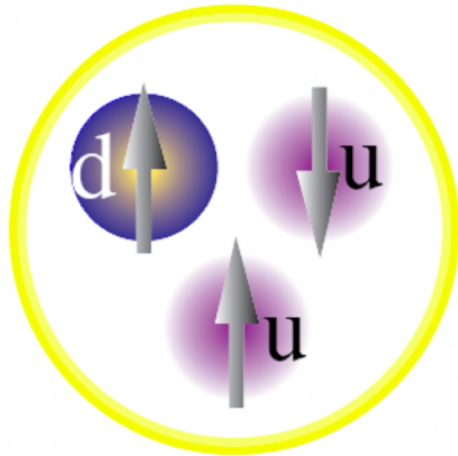


重子

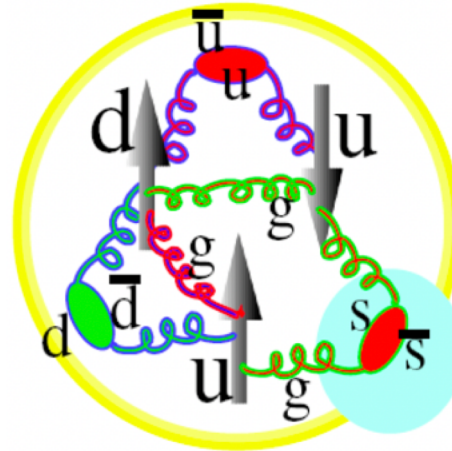
- Most of particles can be explained by a picture of two partons or three partons
- Very simple picture to explain very complicated QCD
- **Not even understand why this picture is successful**

Our understanding of proton

Constituent quarks



Parton distributions



$$\bar{d}(x) = \bar{u}(x)$$

$$\bar{s}(x) = s(x)$$

Garvey & Peng, Prog. Part. Nucl. Phys. 47, 203 (2001)

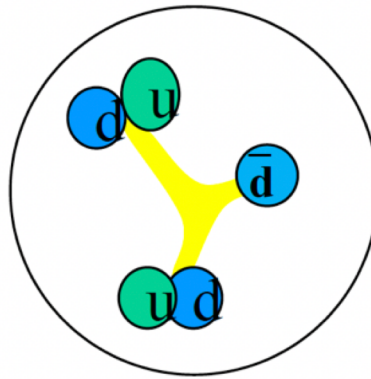
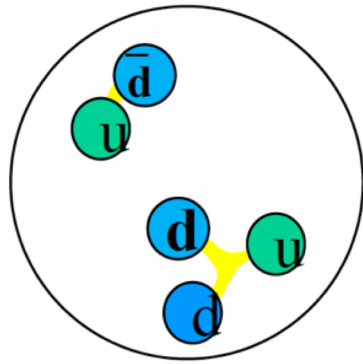
- Deep inelastic scattering and Drell-Yan process tell us: $\int (\bar{d}(x) - \bar{u}(x)) dx \sim 0.12$
- Spin crisis of proton

expt.: $\Delta u \in [0.82, 0.85]$, $\Delta d \in [-0.45, -0.42]$, and $\Delta s \in [-0.11, -0.08]$

$$\Delta q \equiv \int_0^1 [q(x) \uparrow + \bar{q}(x) \uparrow - q(x) \downarrow - \bar{q}(x) \downarrow] dx.$$

A different picture of proton

Current picture



30% of 5-quark
component in proton

Meson cloud picture: Thomas, Speth, Henley, Meissner, Miller, Weise, Oset, Brodsky, Ma, ...

$$|p\rangle \sim |uud\rangle + \varepsilon_1 |n(udd)\pi^+(\bar{d}u)\rangle + \varepsilon_2 |\Delta^{++}(uuu)\pi^-(\bar{u}d)\rangle + \varepsilon' |\Lambda(uds)K^+(\bar{s}u)\rangle + \dots$$

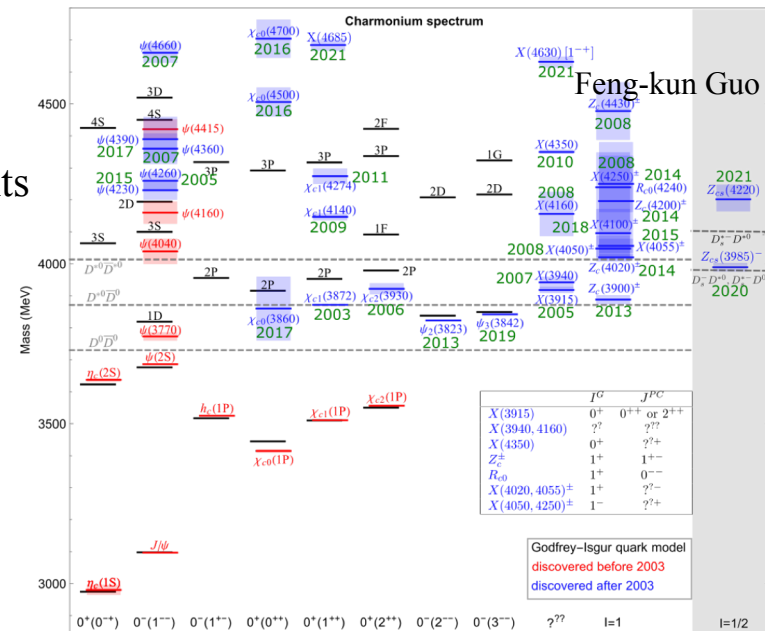
Penta-quark picture: Riska, Zou, Zhu, ...

$$|p\rangle \sim |uud\rangle + \varepsilon_1 |[ud][ud]\bar{d}\rangle + \varepsilon' |[ud][us]\bar{s}\rangle + \dots$$

Slides borrowed from B. Zou

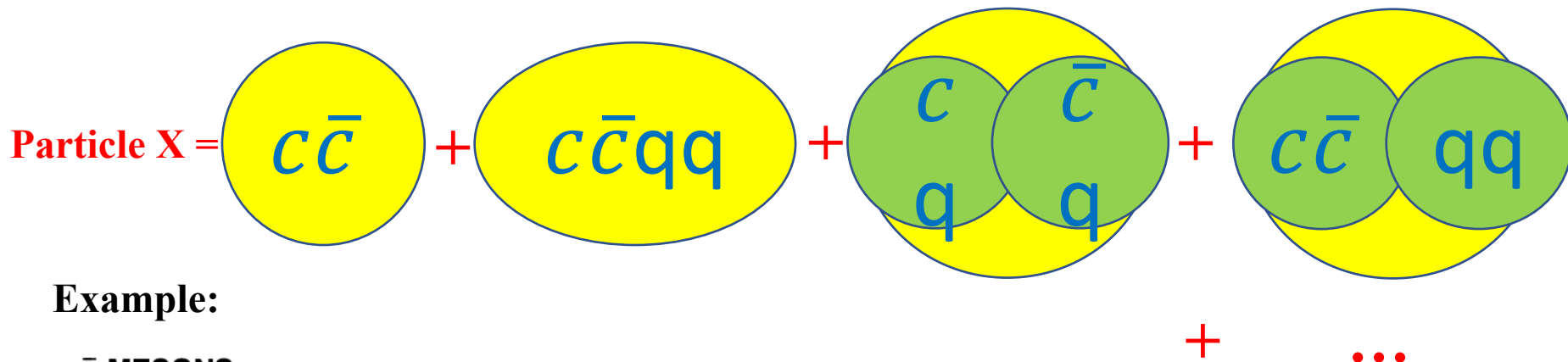
History

- **$X(3872)$: first tetraquark candidates, now called $\chi_{c1}(3872)$**
 - Main motivation for exotic: mass different from prediction
- **$Z_c(3900), Z_c(4200), Z_c(4430)$: charged exotics**
 - Clearly not charmonia, smoking gun; though hidden charm
- **P_c states: pentaquarks!**
- **$X(5568)$: four different flavors!**
 - However, negative conclusions from other experiments
- **$X_{0,1}(2900)$: four different flavors, open charmed**
 - Needs confirmation from other decays
- **T_{cc}^+ : not with hidden charm, but with cc quarks**
- **$X(6900)$: four charm quarks $c\bar{c}c\bar{c}$**



Current task: understanding inner structures of these exotic hadrons

Similar picture as proton



Example:

$c\bar{c}$ MESONS

(including possibly non- $q\bar{q}$ states)

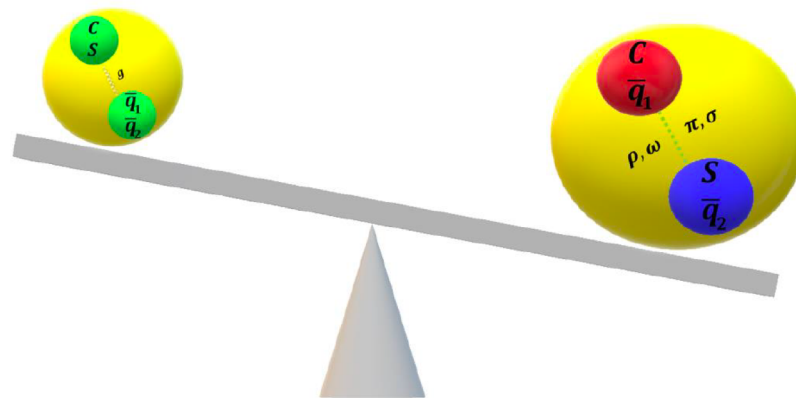
$\chi_{c1}(3872) \quad I^G(J^{PC}) = 0^+(1^{++})$
 also known as X(3872)

Experimental tasks:

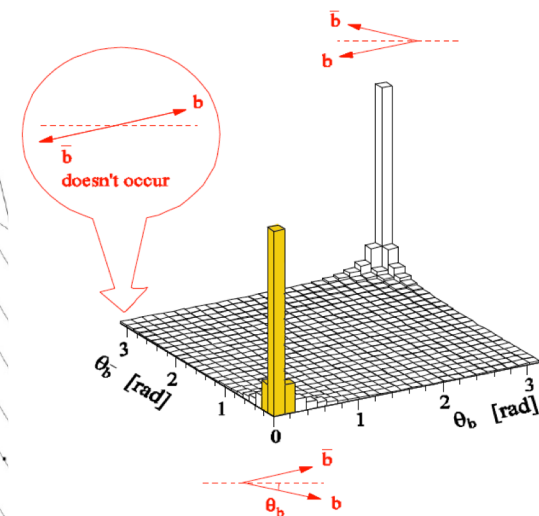
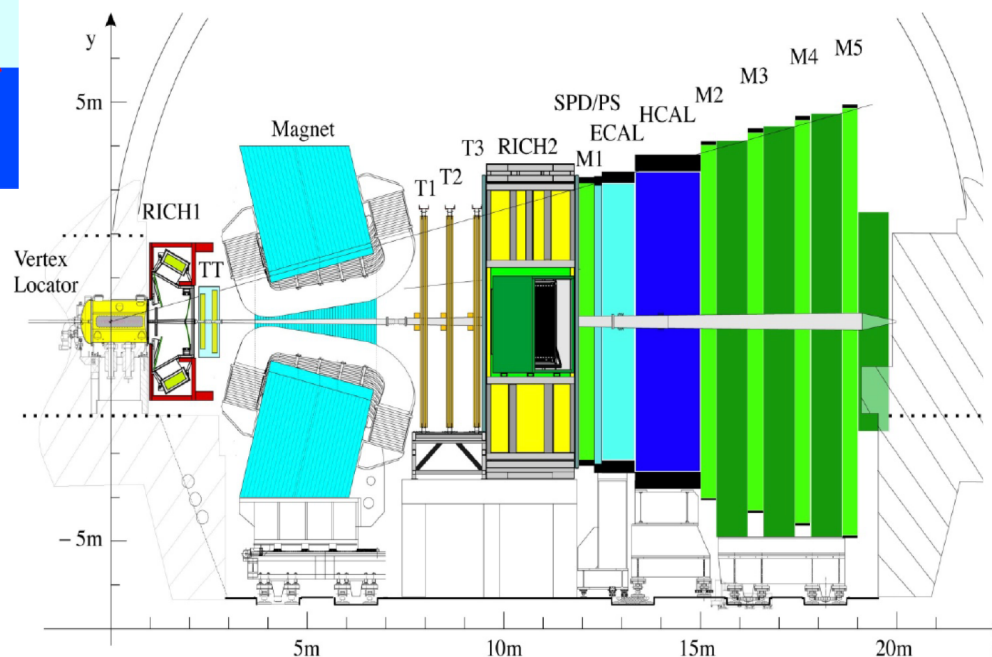
Discover more and understand them through production and decays

$$\frac{\Gamma(X(3872) \rightarrow \bar{D}D^*)}{\Gamma(X(3872) \rightarrow J/\psi\pi^+\pi^-)} = 9.1^{+3.4}_{-2.0}$$

$$\frac{\Gamma(Z_c(3885) \rightarrow \bar{D}D^*)}{\Gamma(Z_c(3885) \rightarrow J/\psi\pi)} = 6.2 \pm 1.1 \pm 2.7$$



The LHCb experiment



Excellent vertex and IP, decay time resolution:

- $\sigma(\text{IP}) \approx 20 \mu\text{m}$ for high- p_T tracks
- $\sigma(\tau) \approx 45 \text{ fs}$ for $B_s^0 \rightarrow J/\psi\phi$ and $B_s^0 \rightarrow D_s^- \pi^+$ decays

Very good momentum resolution:

- $\delta p/p \approx 0.5\% - 1\%$ for $p \in (0, 200) \text{ GeV}$
- $\sigma(m_B) \approx 24 \text{ MeV}$ for two-body decays

Hadron and Muon identification

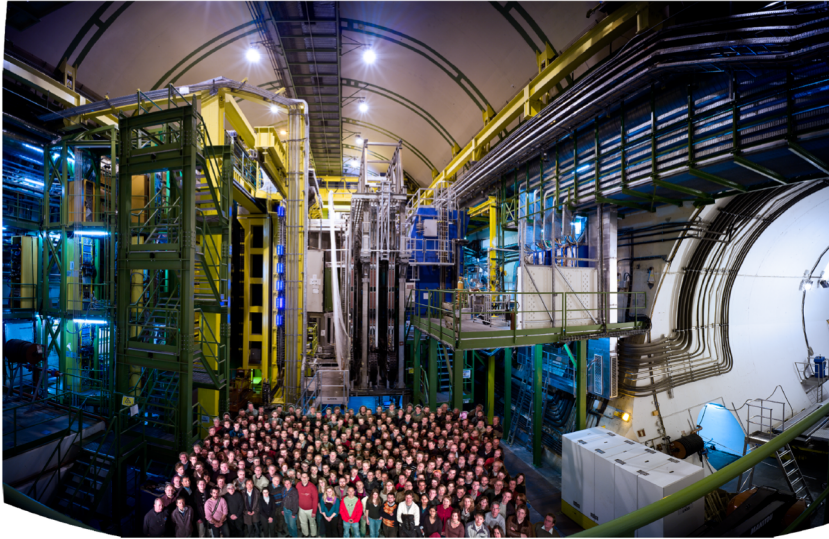
- $\epsilon_{K \rightarrow K} \approx 95\%$ for $\epsilon_{\pi \rightarrow K} \approx 5\%$ up to 100 GeV
- $\epsilon_{\mu \rightarrow \mu} \approx 97\%$ for $\epsilon_{\pi \rightarrow \mu} \approx 1 - 3\%$

Data good for analyses

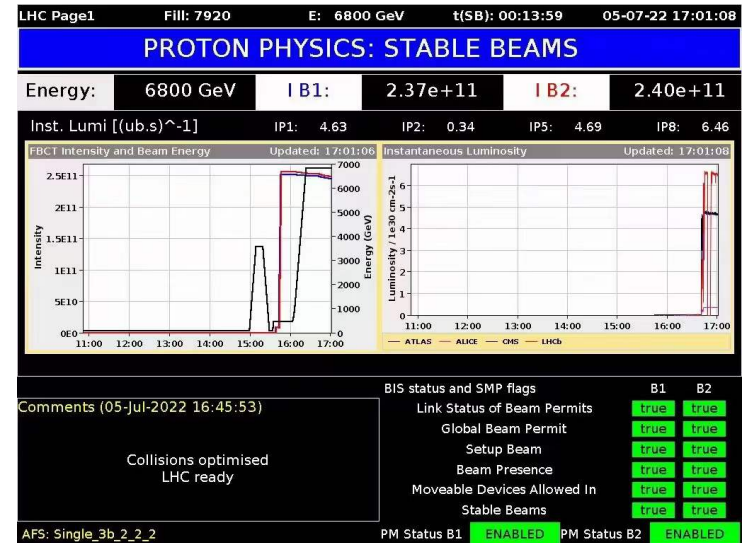
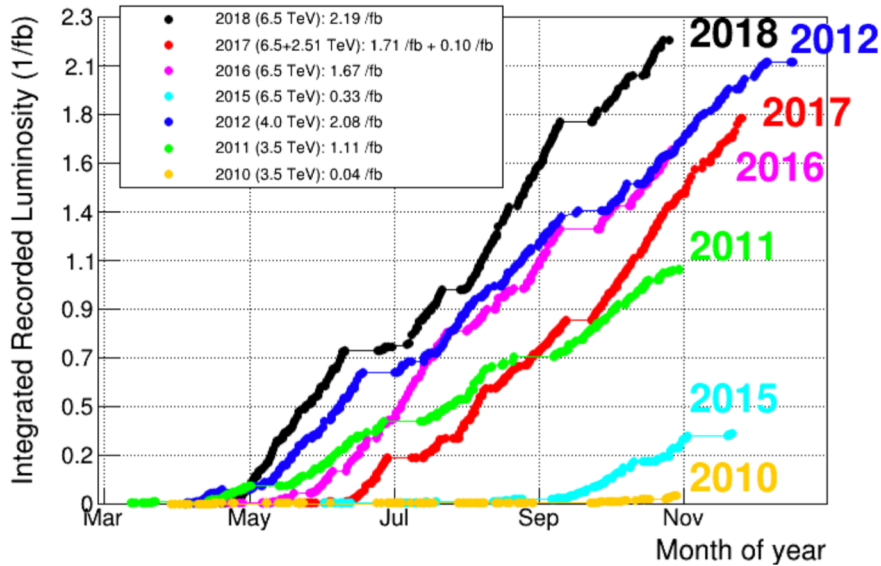
- $> 99\%$

Designed for CP violation and heavy flavor studies

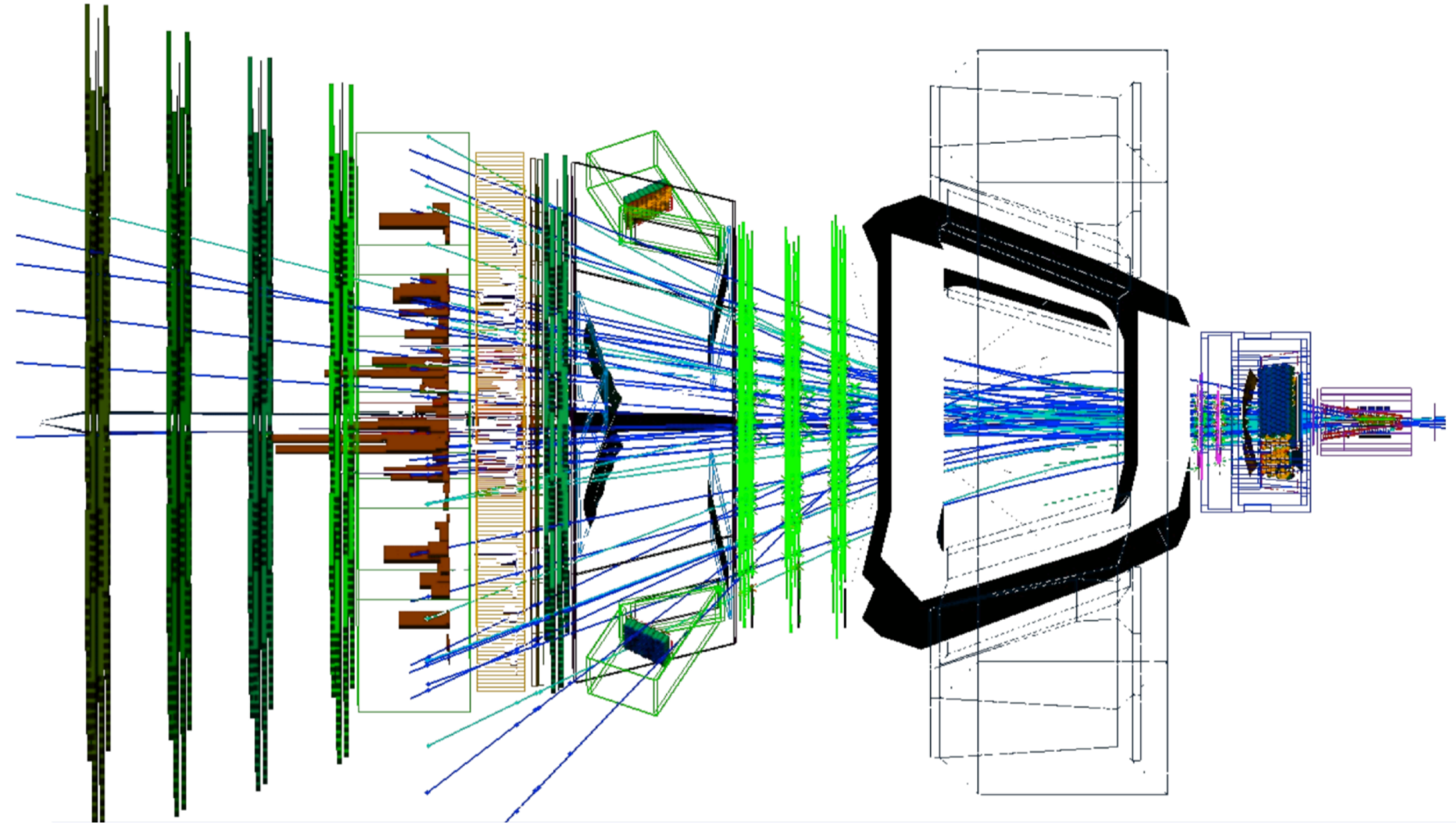
More on LHCb



- Start to take data from 2010
- Run 1:
 - 2011 (7 TeV): 1 fb⁻¹
 - 2012 (8 TeV): 2 fb⁻¹
- Run 2:
 - 2015-2018 (13 TeV): 6 fb⁻¹
- A new LHCb starts this year

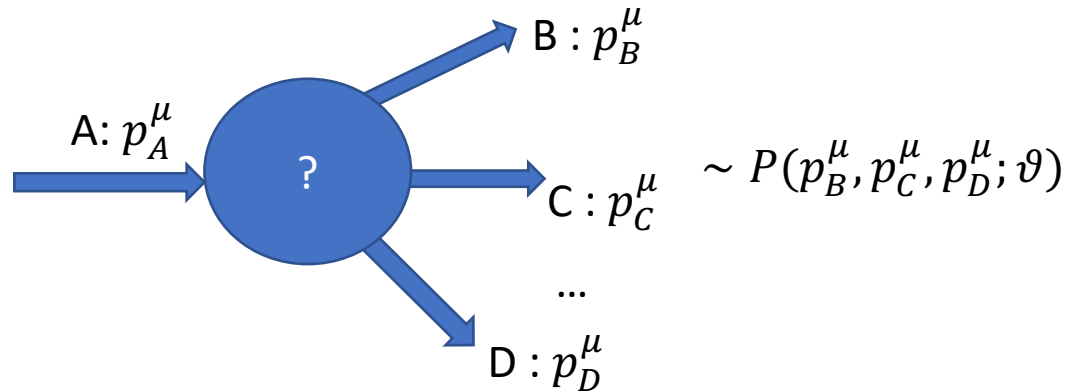


A collision in the LHCb detector



Extract resonant information

- Most exotic states and their properties established in multi-body decays
- Amplitude analyses crucial



- Amplitude analyses **very complicated**: main limitations to start an analysis
- **Enormous data** from BESIII, LHCb and other flavor physics experiments: **massive CPU time** needed to perform analyses
- A general PWA framework using modern acceleration technology (such as GPU, AD,...) eagerly needed
- We have developed a new framework using TensorFlow



A **general** and **user-friendly** partial wave analysis framework

Hao Cai¹, Chen Chen⁵, **Yi Jiang²**, Pei-Rong Li³, **Yin-Rui Liu²**, Xiao-Rui Lyu²,
Rong-Gang Ping⁴, Wenbin Qian², Mengzhen Wang⁵, Zi-Yi Wang²,
Liming Zhang⁵, Yang-Heng Zheng²

¹WHU, ²UCAS, ³LZU, ⁴IHEP, ⁵THU

- **Joint efforts + experience on previous analyses + very good students**
- **Cross-checks performed with several independent fitters developed previously for dedicated analyses: e.g. $Z(4430)^+$ and pentaquark search, $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ analysis etc.**

Features

- **Based on Tensor-Flow v2**

- **Fast**

- **GPU based**
- **Vectorized calculation**
- **Automatic differentiation**

- **General**

- **Custom model available**

- **Easy to use**

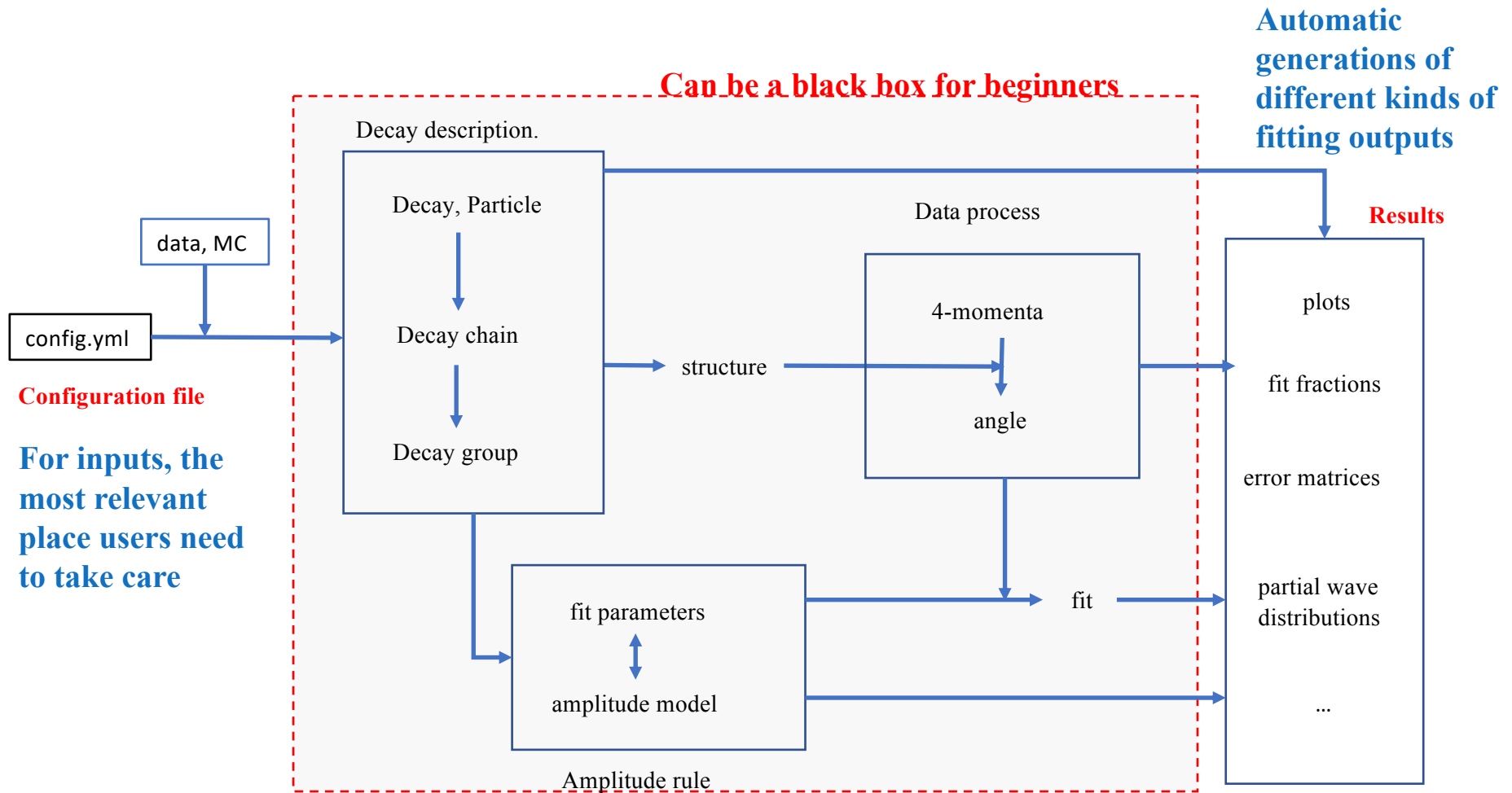
- **Simple configuration file**
- **Automatics process**
- **All necessary functions implemented**

- **Open access and well supported**

<https://gitlab.com/jiangyi15/tf-pwa>

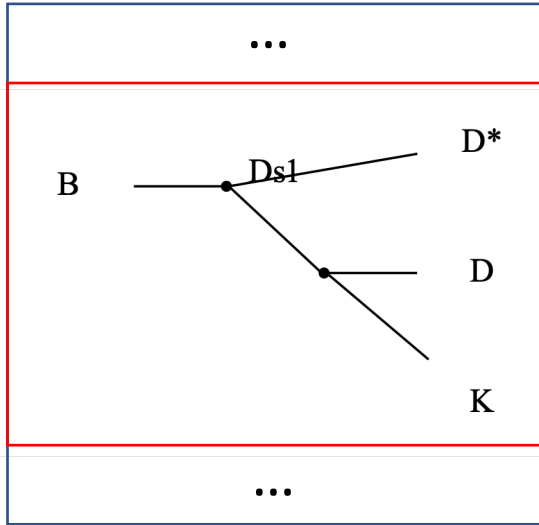


Framework



Topology based algorithm

Decay group



Decay chain

$$\left\{ \begin{array}{l} B^0 \rightarrow R(\rightarrow D^0 K^+) D^{*-} \\ B^0 \rightarrow R(\rightarrow D^0 D^{*-}) K^+ \\ \text{etc.} \end{array} \right.$$

Decays

$$\left\{ \begin{array}{l} B^0 \rightarrow D_{s1}^*(2700)^+ D^{*-} \\ B^0 \rightarrow D_{s1}^*(2860)^+ D^{*-} \\ \text{etc.} \end{array} \right.$$

Wigner D-matrix:
 $A = F D^{*J}(\phi, \theta, 0)$

Particles

initial state (B^0),
 final states (D^{*-}, D^0, K^+)
 propagator ($D_{s1}^*(2700)$)

Breit-Wigner: $R(m)$,
 Other user defined function

$$\tilde{A} = A_1 R A_2 + \dots$$

$$\mathcal{A} = \tilde{A}_1 + \tilde{A}_2 + \dots$$

$$A_{\lambda_A, \lambda_B, \lambda_C, \lambda_D}^R$$

||

$$\sum_{\lambda} F_{\lambda_R \lambda_B} D_{\lambda_A, \lambda_R - \lambda_B}^{j_A^*}(\varphi_1, \theta_1, 0) R(M) F_{\lambda_C \lambda_D} D_{\lambda_R, \lambda_C - \lambda_D}^{j_R^*}(\varphi_2, \theta_2, 0) D_{\lambda_B, \lambda_B'}^{j_B^*}(\alpha_B, \beta_B, \gamma_B) D_{\lambda_C, \lambda_C'}^{j_C^*}(\alpha_C, \beta_C, \gamma_C) D_{\lambda_D, \lambda_D'}^{j_D^*}(\alpha_D, \beta_D, \gamma_D)$$

$$\frac{d\sigma}{d\Phi} \propto \sum_{\lambda_A} \sum_{\lambda_B, \lambda_C, \lambda_D} \left| \sum_R A_{\lambda_A, \lambda_B, \lambda_C, \lambda_D}^R \right|^2$$

Decay



$$F_{\lambda_1, \lambda_2} D_{\lambda_0, \lambda_1 - \lambda_2}^{j_0^*}(\varphi, \theta, 0)$$

Wigner-D matrix

Particle



$$R(M) = \frac{1}{m_0^2 - M^2 - im_0\Gamma}, \dots$$

1

$$D_{\lambda_1, \lambda_1'}^{j_1^*}(\alpha, \beta, \gamma)$$

Benchmarks

CPU: i7-9750H@2.6 Hz with **12** cores

GPU: Nvidia 1660 Ti, a cheap GPU

Test based on simple MC (200000) sample of a simple amplitude model of $e^+e^- \rightarrow R_1(1^+)\pi, R_1 \rightarrow D^*D^*$

Both based on TF-PWA

process	CPU (ms)	GPU (ms)	Ratio
$N = \int A ^2 d\Phi$	573	53	$\sim 11 \times 12 = 132$
N with $\frac{\partial N}{\partial \vartheta}$	1122	117	$\sim 9.5 \times 12 = 114$

Almost a factor of **100 times** faster for GPU than single CPU core.

Automatic differentiation cost the same time as normal evaluation, faster with increase of parameters

Functions implemented

- Toy studies
 - Plotting
 - Fit fractions, interference fractions
 - Simultaneous fit between different datasets
 - Parity conversation
 - Gaussian constraints on parameters
 - 2D chi2 test
 - CP violation fit
 - Final states with identical particles
 - Amplitude factorization
 - Resolution
 - Simple symbolic formula
 - Model independent fit
 - Error propagation
 - ...
- Used in many LHCb/BESIII analyses, including those discussed below**

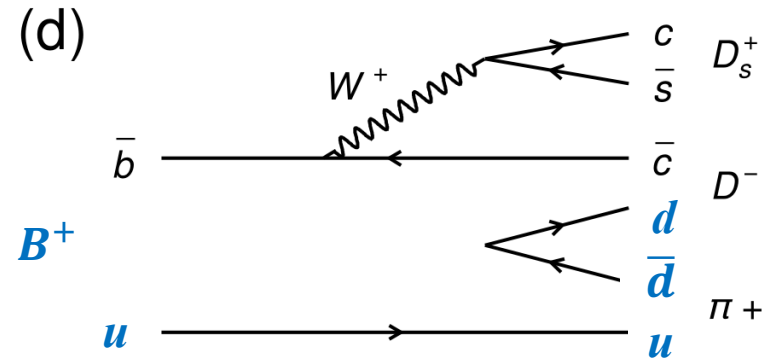
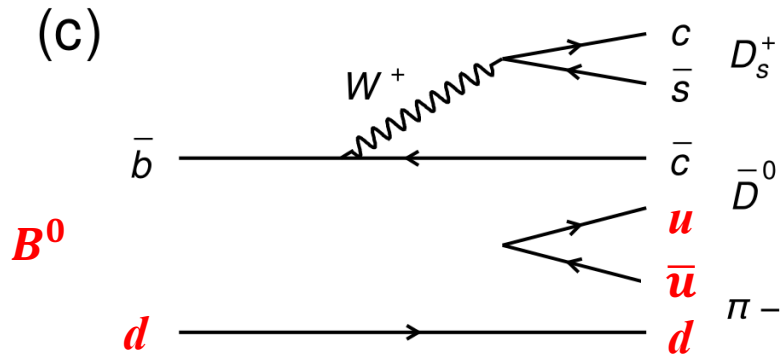
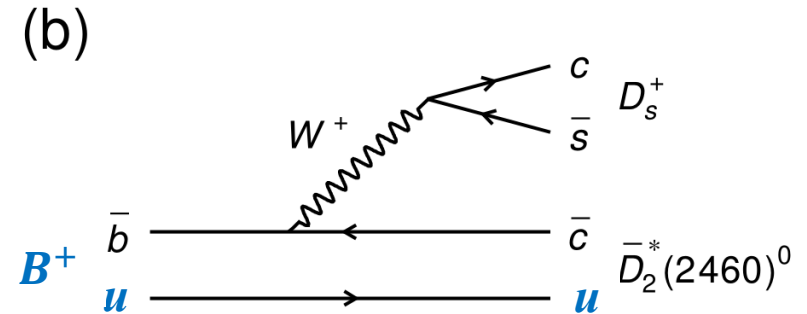
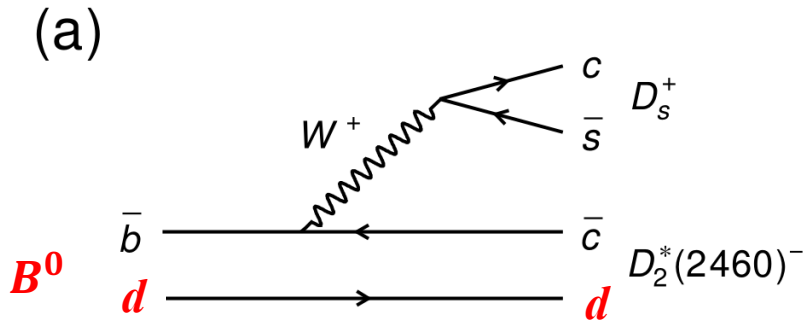
Observation of a double-charged tetra-quark states and its isospin partner

LHCb-PAPER-2022-026

LHCb-PAPER-2022-027

Feynman diagrams

- Two decays considered: $B^0 \rightarrow \bar{D}^0 D_s^+ \pi^-$, $B^+ \rightarrow D^- D_s^+ \pi^+$

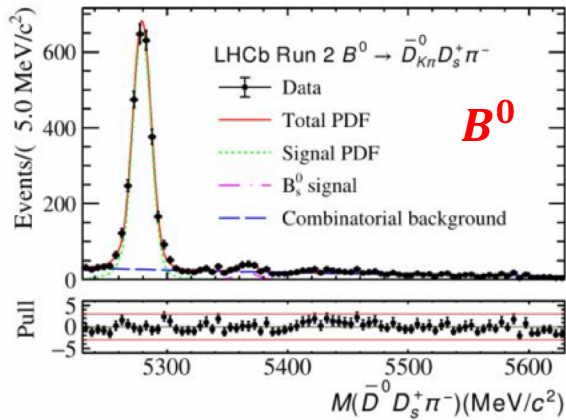


- Connected by isospin relationship in all aspects

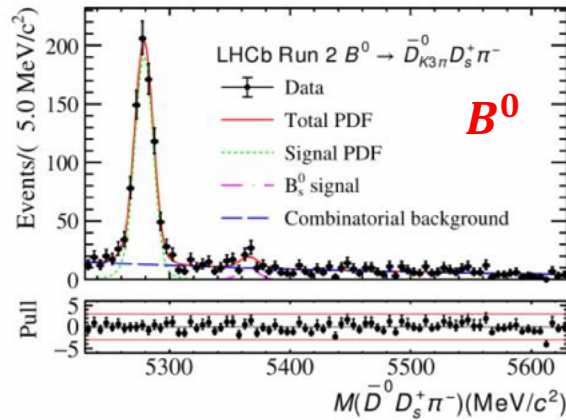
Signal yields

- Two decays considered: $B^0 \rightarrow \bar{D}^0 D_s^+ \pi^-$, $B^+ \rightarrow D^- D_s^+ \pi^+$

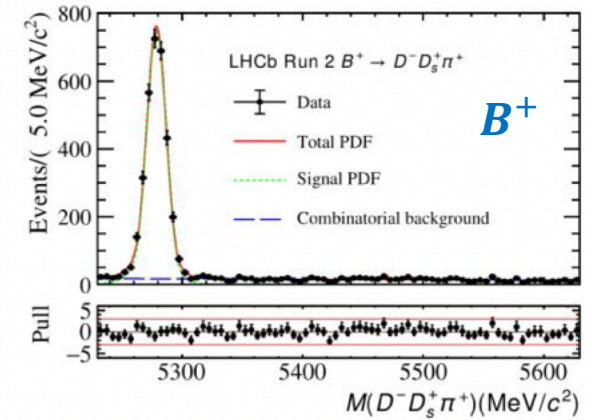
$$D^0 \rightarrow K^- \pi^+$$



$$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$$



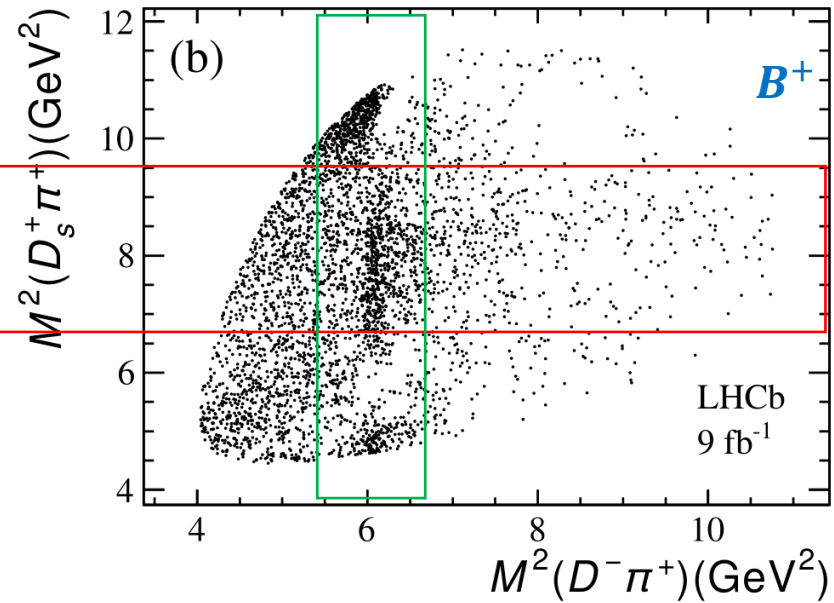
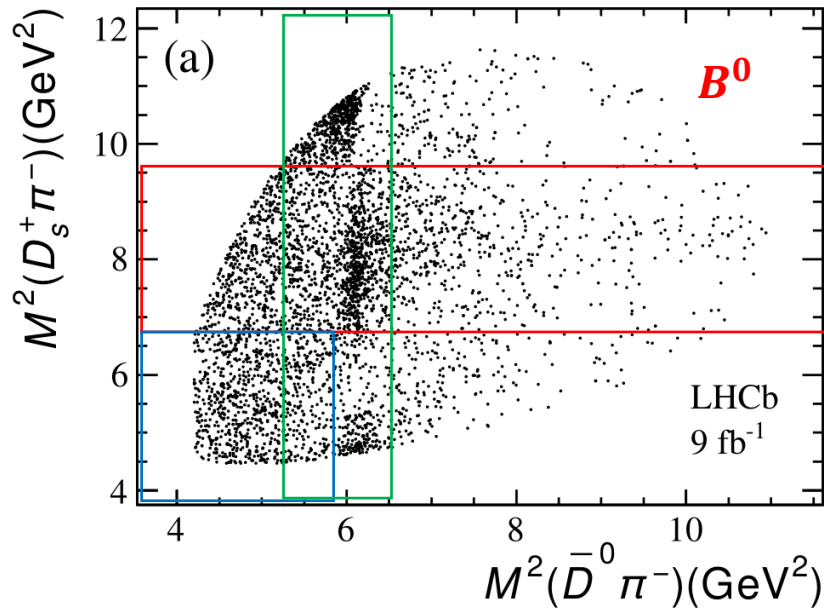
$$D^- \rightarrow K^- \pi^+ \pi^+$$



- Very pure samples, ideal for amplitude analysis
- ~ 4000 B^0 signals with a purity of $\sim 90\%$;
- ~ 3750 B^+ signals with a purity of $\sim 95\%$

Preliminary

First impression on Dalitz plot



Preliminary

- Very similar distributions over Dalitz plot
- Clear accumulation of events on both channels around 2.9 GeV of $m(D_s^+ \pi^-)$ and $m(D_s^+ \pi^+)$
- D^{*-} (2010) cut-off in B^0 channel; small isospin breaking effects at threshold
- Very clear contributions from $D_2(2460)$

Amplitude analysis

- Unbinned maximum likelihood fits performed with TF-PWA

$$P(x; \Theta) = f_{\text{sig}} \cdot P_{\text{sig}}^{\text{norm}}(x; \Theta) + f_{\text{bkg}} \cdot P_{\text{bkg}}^{\text{norm}}(x),$$

Fractions determined from mass fits

- Background modelled from upper sideband with extrapolating into signal regions

- Signal PDF:
$$P_{\text{sig}}^{\text{norm}}(x; \Theta) = \frac{\epsilon(x) |\mathcal{A}(x; \Theta)|^2}{I_{\text{sig}}(\Theta)}.$$
 Normalization factor

- Efficiencies obtained from full simulation with corrections for data-simulation difference

- Amplitude model:
$$\mathcal{A}(x; \Theta) = \sum c_i \cdot \mathcal{A}_i(x; \Theta_i),$$
 Angular distribution + line shape (RBW etc.)

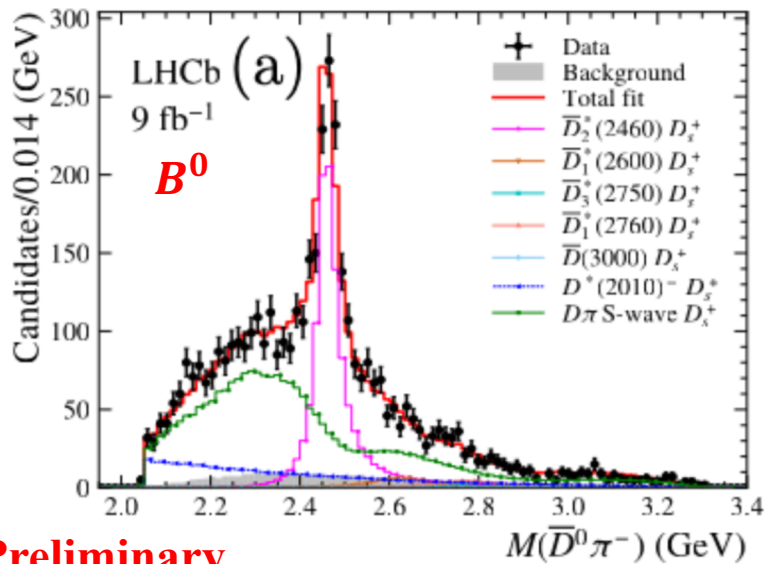
D^* resonances

- D^* main contributors for the Dalitz distribution,;
- Current observed D^* states

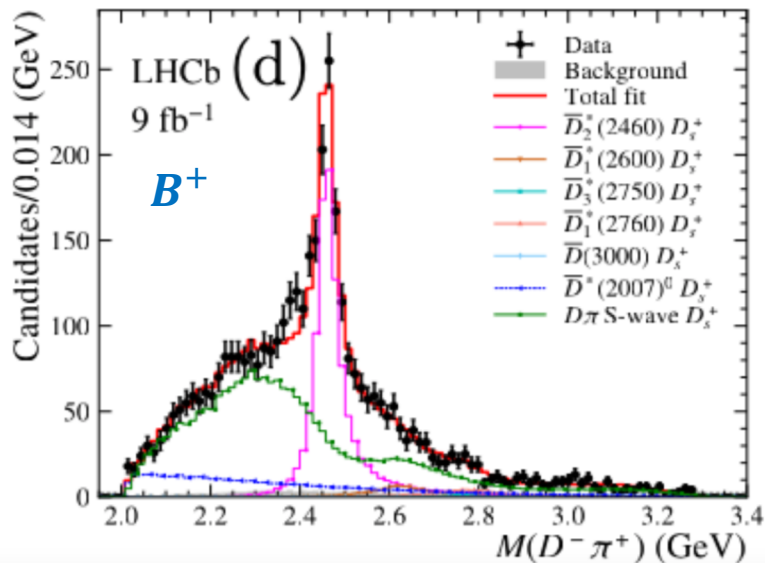
Resonance	J^P	Mass (GeV)	Width (GeV)
$D^*(2007)^0$	1^-	2.00685 ± 0.00005	$< 2.1 \times 10^{-3}$
$D^*(2010)^-$	1^-	2.01026 ± 0.00005	$(8.34 \pm 0.18) \times 10^{-5}$
$D_0^*(2300)$	0^+	2.343 ± 0.010	0.229 ± 0.016
$D_2^*(2460)$	2^+	2.4611 ± 0.0007	0.0473 ± 0.0008
$D_1^*(2600)^0$	1^-	2.627 ± 0.010	0.141 ± 0.023
$D_3^*(2750)$	3^-	2.7631 ± 0.0032	0.066 ± 0.005
$D_1^*(2760)^0$	1^-	2.781 ± 0.022	0.177 ± 0.040
$D(3000)^0$	$??$	3.214 ± 0.060	0.186 ± 0.080

- $D^*(2007)^0$ and $D^*(2010)^-$ close to threshold, small isospin violation effects seen
- PDG currently gives average masses and widths for D^{**} states
- $D_1^*(2600)^-$, $D_1^*(2760)^-$, $D(3000)^-$ not observed yet
- Spin-parity of $D(3000)^0$ not established yet

D^* contributions



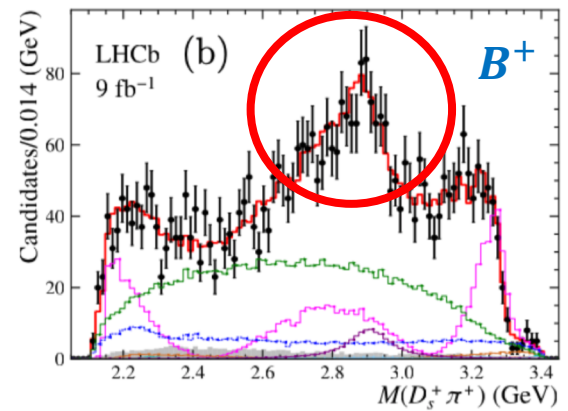
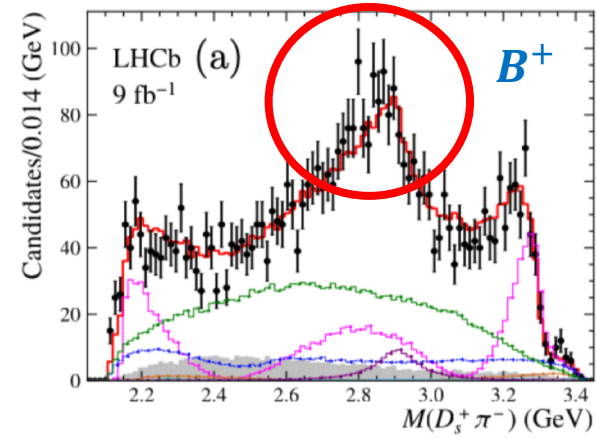
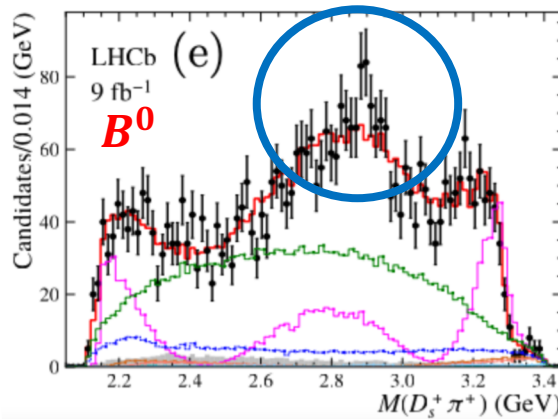
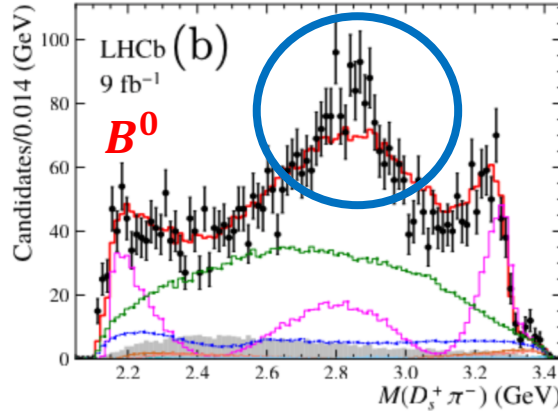
Preliminary



- Different models for $D^*(2007)^0$ and $D^*(2010)^-$, though shapes turn out to be similar
- S-wave can be described by RBW + NR, however, to avoid unitarity problem, a spline function used, offering better and conservative description
- $D_1^*(2600)$, $D_1^*(2760)$, $D(3000)$ not significant, however, still included conservatively
- Generally very good description of $m(D\pi)$ spectrum

Exotics

Without
new
states



Preliminary

With
new
states

- Not very good description on $m(D_s\pi)$ around 2.9 GeV
- Further $m(D\pi)$ or $m(DD_s)$ contributions not help
- Add new states on $m(D_s\pi)$, $T_{c\bar{s}}^a(2900)^0$ and $T_{c\bar{s}}^a(2900)^{++}$ help a lot

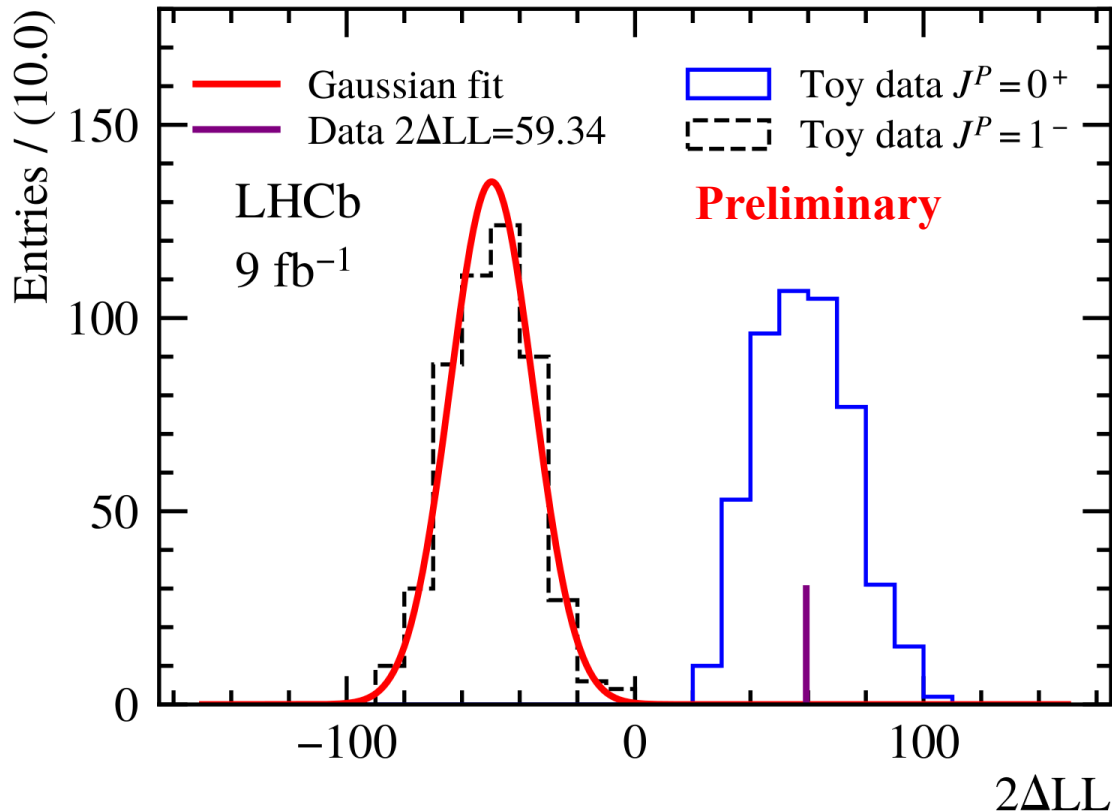
More on exotics

- Isospin relationship imposed on $m(D\pi)$, apart from $D^*(2010)$ and $D^*(2007)$, confirmed by separate fits
- Two scenarios considered for $T_{c\bar{s}}^a(2900)^0$ and $T_{c\bar{s}}^a(2900)^{++}$: with and without isospin relationship

Scenarios	Exotics	Mass (GeV)	Width (GeV)	Significance
No isospin relationship	$T_{c\bar{s}}^a(2900)^0$	$2892 \pm 14 \pm 15$	$119 \pm 26 \pm 12$	8.0σ
	$T_{c\bar{s}}^a(2900)^{++}$	$2921 \pm 17 \pm 19$	$137 \pm 32 \pm 14$	6.5σ
With isospin relationship	Both	$2908 \pm 11 \pm 20$	$136 \pm 23 \pm 11$	9.0σ

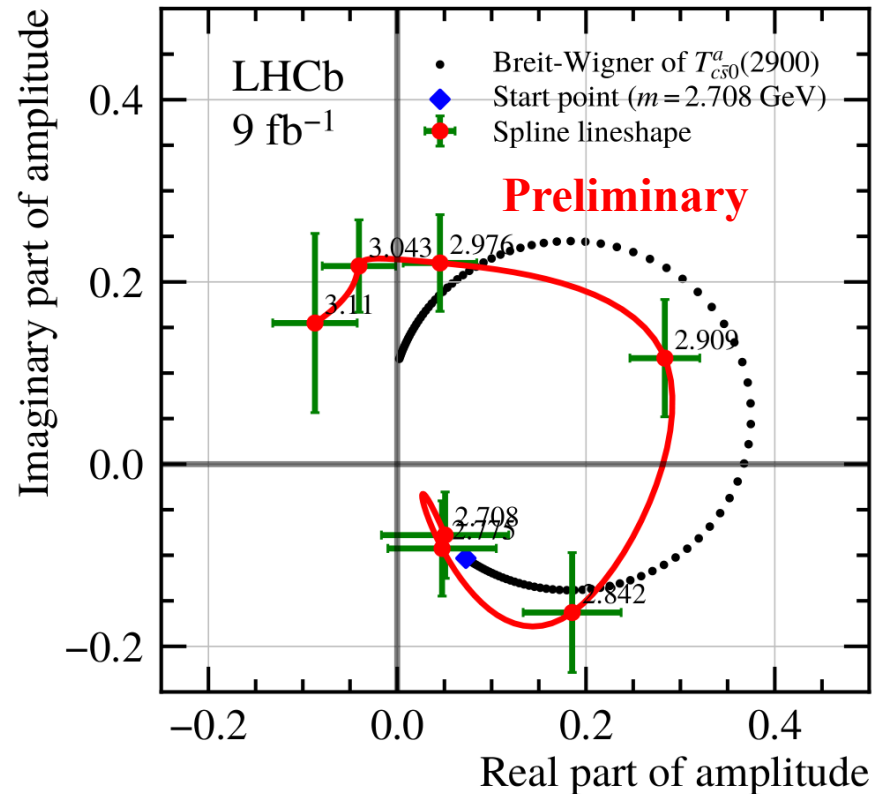
- Significance estimated considering look-else-where effects
- Two states consist with each other: isospin triplet
- $J^P = 0^+$ preferred for both cases

Spin analysis



- Toys generated for spin analysis: 0^+ preferred over 1^- (second best solution) by 7.6σ
- 0^+ is also significantly preferred when exotics not constrained by isospin

Argand diagram



- Replacing RBW description of exotic states with splines (no model assumption)
- Spline description consist with RBW behavior

Discussion

- In $B^+ \rightarrow D^+ D^- K^+$ decays, two states observed with quark content $c\bar{s}\bar{u}\bar{d}$
- $T_{cs}^a(2900)$ have quark content $c\bar{s}\bar{u}d$ and $c\bar{s}u\bar{d}$
- Very similar mass, $T_{cs}^a(2900)$ has larger width
- Only 0^+ $T_{cs}^a(2900)$ states found

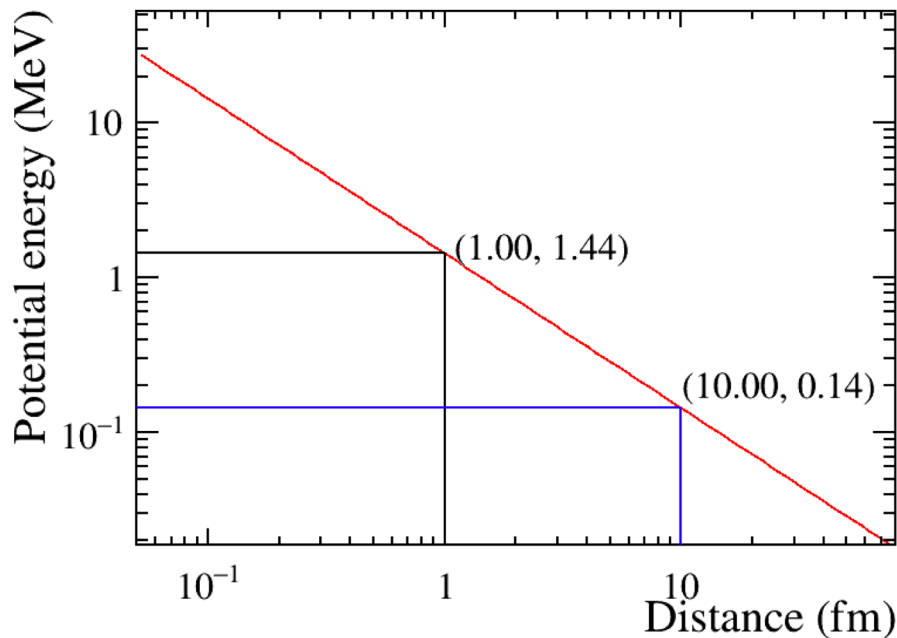
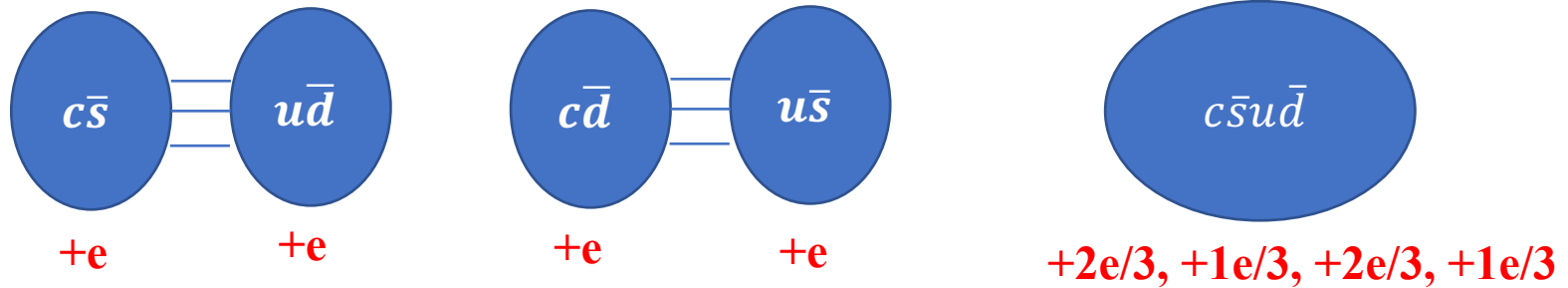
Preliminary

Exotic	Mass (MeV)	Width (MeV)	Spin-parity
$X_0(2900)$	$2866 \pm 7 \pm 2$	$57 \pm 12 \pm 4$	0^+
$X_1(2900)$	$2904 \pm 5 \pm 1$	$110 \pm 11 \pm 4$	1^-
$T_{cs}^a(2900)^0$	$2892 \pm 14 \pm 15$	$119 \pm 26 \pm 12$	0^+
$T_{cs}^a(2900)^{++}$	$2921 \pm 17 \pm 19$	$137 \pm 32 \pm 14$	0^+

- $X(5568)$ claimed by D0 collaboration in $B_s^0 \pi^\pm$ final states, with quark flavor $b\bar{s}\bar{u}d$, however, negative results from other experiments
- Some suggestions for $T_{cs}^a(2900)$ (1705.10088, 2204.02649, 2008.07145, 2008.07340 et al.)

Charge

- For double charged tetraquark candidates, if molecular, repulsion potential around 1.44 MeV @ 1 fm!

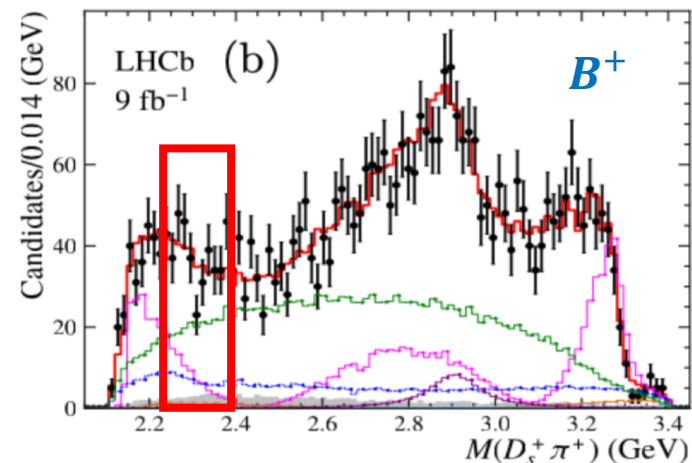
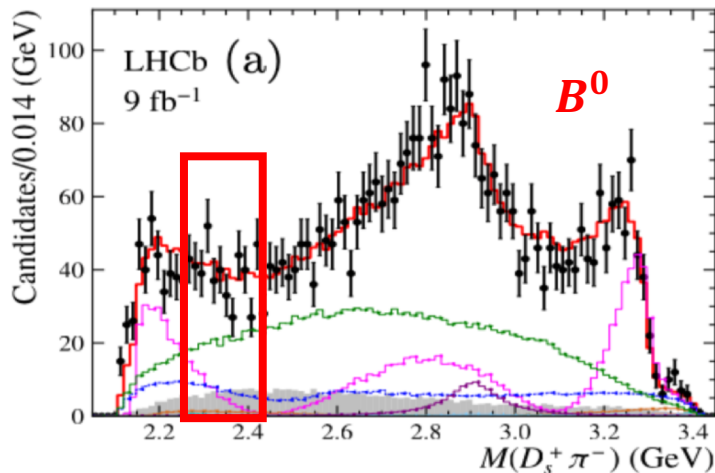


- If compact states, all four quarks have positive charge
- Or may be just cusp

Isospin

- $T_{c\bar{s}}^a(2900)^0$ and $T_{c\bar{s}}^a(2900)^{++}$ are two of the isospin triplet;
- Missing one ($D_s^+ \pi^0$), hard for LHCb, though not entirely impossible;
- Some suggests $D_s^+(2317)$ (decaying into $D_s^+ \pi^0$) to be a tetraquark state; though no clue from current charged pion modes (contamination from $D_2(2460)$)
- $I = 0$ considered to have strong attraction while $I = 1$ to have weak attraction or even repulsion;

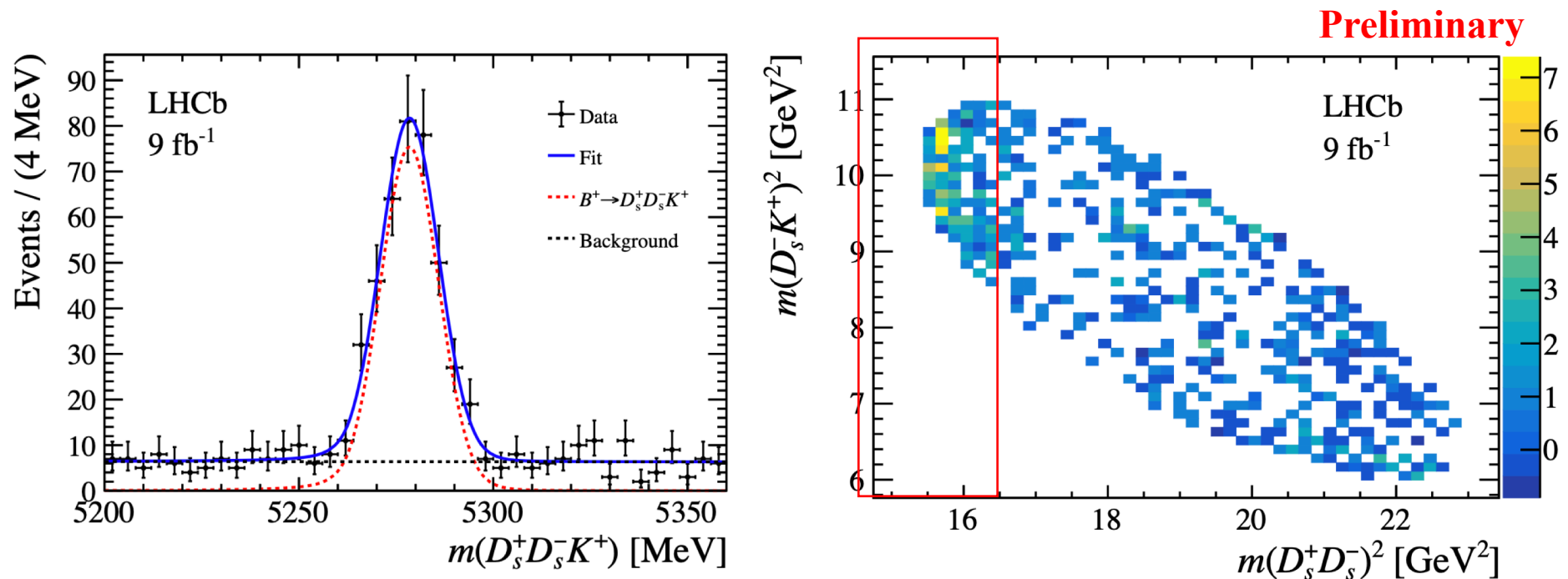
Preliminary



Observation of a resonant structure near the $D_s^+ D_s^-$ threshold

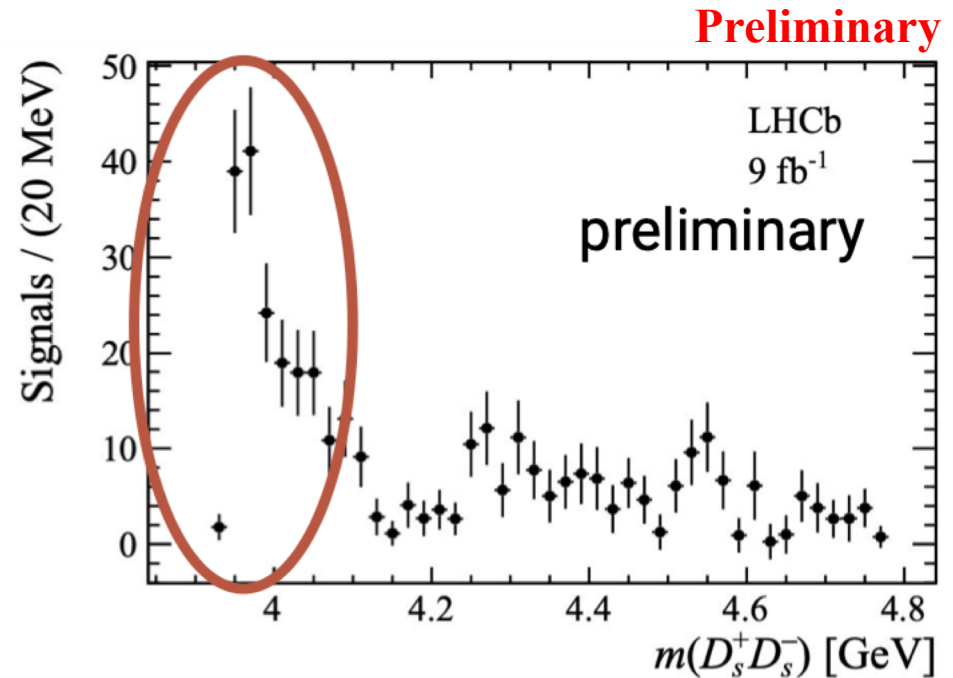
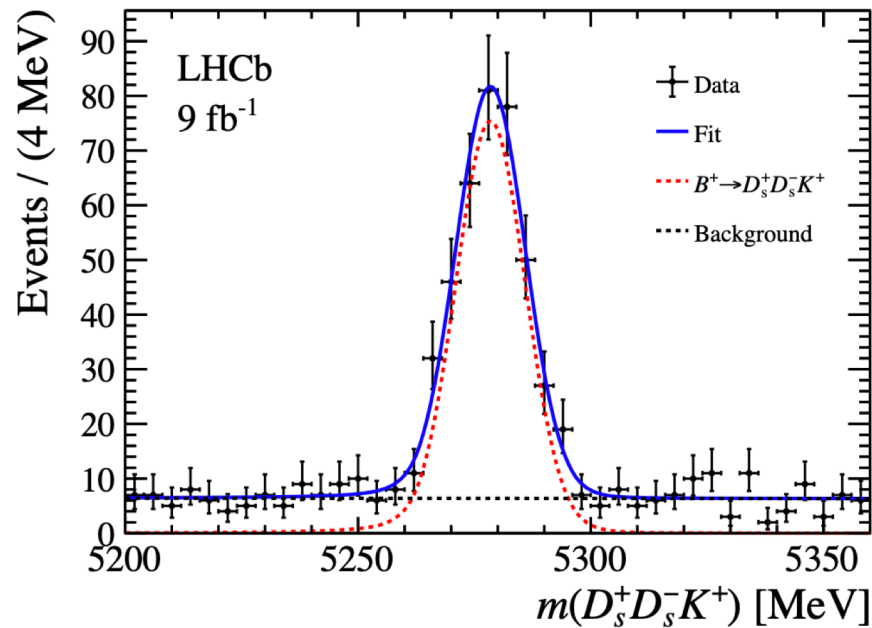
LHCb-PAPER-2022-018
LHCb-PAPER-2022-019

Yields and Dalitz plot distribution



- $B^+ \rightarrow D_s^+ D_s^- K^+$: ~ 360 signal candidates with a purity of $\sim 85\%$
- No clear structures over Dalitz plot except accumulations at the $m(D_s^+ D_s^-)$ threshold around 3.9 GeV

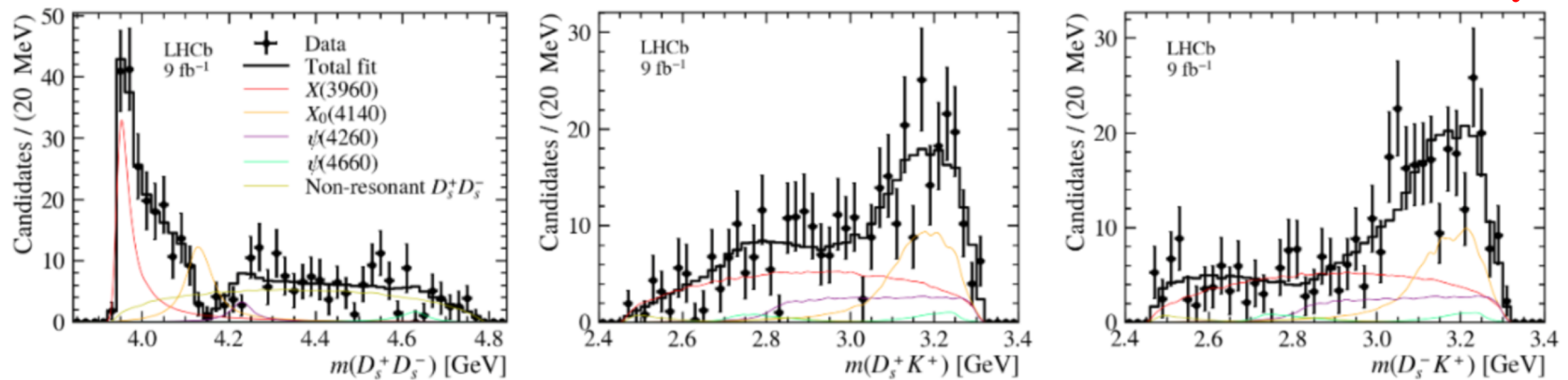
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Amplitude fit results

Preliminary



- Only resonances on $m(D_s^+ D_s^-)$ contribute
- Dominant contribution from NR ($\sim 46.6\%$) and a near threshold state $X(3960)$ ($\sim 24.2\%$, more than 12.6σ)
- Evidence of contributions from $\psi(4260)$, $\psi(4660)$ and $X(4140)$
- Other states ($\chi_{c0}(4500)$, $\chi_{c0}(4700)$, $\psi(4040)$, $\psi(4160)$, $\psi(4415)$ and $\chi_{c2}(3930)$) also tested, though not significant

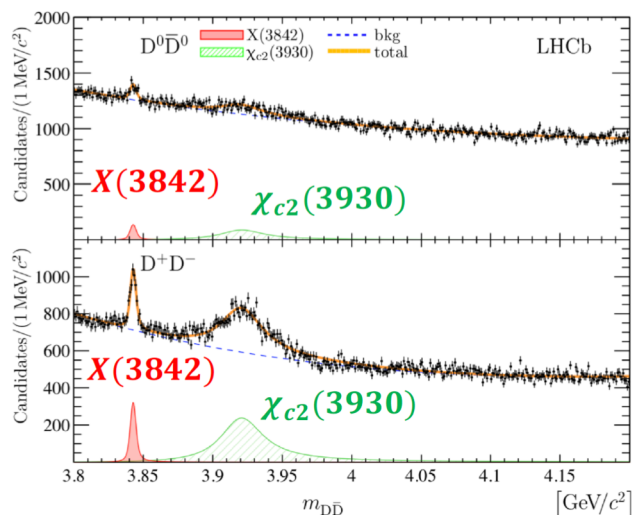
Puzzles around 3930 MeV

Summary of current PDG

$D_s^+ D_s^-$ threshold: 3936.68 MeV

	J^{PC}	Mass(MeV)	Width(MeV)	Decays BaBar, Belle
X(3915)	$0^{++}/2^{++}$	3918.4 ± 1.9	20 ± 5	$J/\psi\omega, \gamma\gamma, ! D\bar{D}$
$\chi_{c2}(3930)$	2^{++}	3922.2 ± 1.0	35.3 ± 2.8	$\gamma\gamma, D\bar{D}$

- X(3915) less likely to be $\chi_{c0}(2P)$ [1208.1134, 1410.6534] due to its small width and mass close to $\chi_{c2}(3930)$, while now $\chi_{c0}(2P)$ is assigned to a state around 3860 MeV (not seen in $B^+ \rightarrow D^+ D^- K^+$).



		$m_{\chi_{c2}(3930)}$ [MeV/c^2]	$\Gamma_{\chi_{c2}(3930)}$ [MeV]
Belle	[17]	$3929 \pm 5 \pm 2$	$29 \pm 10 \pm 2$
BaBar	[18]	$3926.7 \pm 2.7 \pm 1.1$	$21.3 \pm 6.8 \pm 3.6$
This analysis		$3921.9 \pm 0.6 \pm 0.2$	$36.6 \pm 1.9 \pm 0.9$

- LHCb measurements from inclusive DD channels show difference on the mass and width, 2σ lower mass and 2σ larger width
- Current PDG values driven by LHCb inclusive measurements

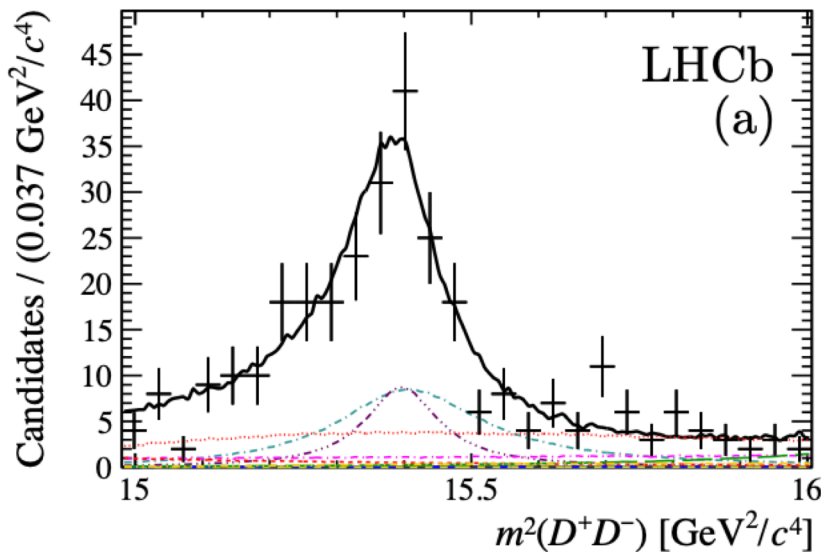
Inputs from $B \rightarrow DDh$

Summary of current PDG

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- Recent LHCb measurements with $B^+ \rightarrow D^+ D^- K^+$ also gives interesting inspection on this area

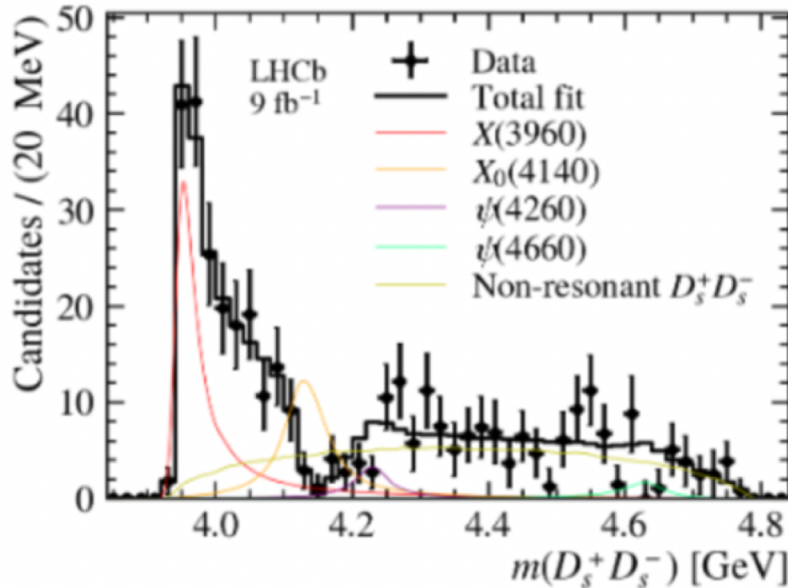


Resonance	Mass (GeV/c^2)	Width (MeV)
$\chi_{c0}(3930)$	$3.9238 \pm 0.0015 \pm 0.0004$	$17.4 \pm 5.1 \pm 0.8$
$\chi_{c2}(3930)$	$3.9268 \pm 0.0024 \pm 0.0008$	$34.2 \pm 6.6 \pm 1.1$

- Two resonances seen in DD decays, with $J=0$ and $J=2$; lead to rethink of previous results
- It also puts the question whether this spin 0 particle = X(3915)?
- Hard to be in 2P triplets, thus may prefer exotic nature;

X(3960)

Preliminary



- J^{PC} of 0^{++} is significantly preferred
- Mass and width determined to be

	M_0 (MeV)	Γ_0 (MeV)
One channel	$3956 \pm 5 \pm 11$	$43 \pm 13 \pm 8$

- $D_s^+ D_s^-$ threshold: ~ 3938 MeV

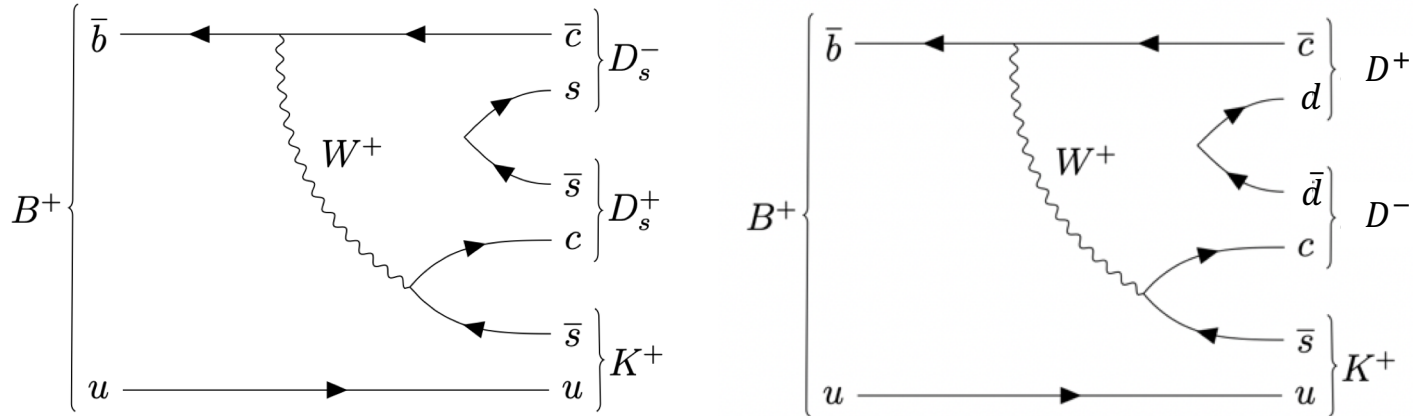
$$R(m | M_0, g_j) = \frac{1}{M_0^2 - m^2 - iM_0 \sum_j \boxed{g_j} \boxed{\rho_j(m)'}}$$

Coupling constant

Phase space factor

- Default: only with one channel = RBW
- Two channels considered: $D_s^+ D_s^-$ ($D^+ D^-$) with couplings: 0.33 ± 1.18 (0.15 ± 0.33) GeV, simultaneous fits with $B^+ \rightarrow D^+ D^- K^+$ decays needed

X(3960)



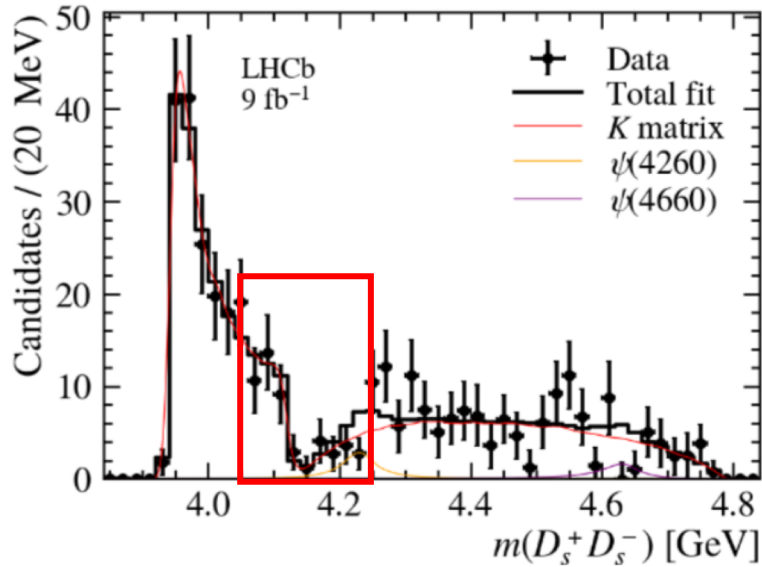
$$\frac{\mathcal{B}(B^+ \rightarrow D_s^+ D_s^- K^+)}{\mathcal{B}(B^+ \rightarrow D^+ D^- K^+)} = \frac{N_{\text{sig}}^{\text{corr}}}{N_{\text{con}}^{\text{corr}}} \left[\frac{\mathcal{B}(D^+ \rightarrow K^- \pi^+ \pi^+)}{\mathcal{B}(D_s^+ \rightarrow K^- K^+ \pi^+)} \right]^2 = 0.525 \pm 0.033,$$

Preliminary

$$\frac{\Gamma(X \rightarrow D^+ D^-)}{\Gamma(X \rightarrow D_s^+ D_s^-)} = \frac{\mathcal{B}^{(1)} \mathcal{F}_X^{(1)}}{\mathcal{B}^{(2)} \mathcal{F}_X^{(2)}} = 0.29 \pm 0.09 \pm 0.10 \pm 0.08,$$

- Phase space of $D_s^+ D_s^-$ smaller than $D^+ D^-$
- Suspiciously smaller branching fraction into $D^+ D^-$ final states: different resonances or a tetraquark with $c\bar{c}s\bar{s}$

X(4140)



- Dip around 4140 MeV can be seen clearly
- Significance around 3.9σ ; mass and width determined to be

	M_0 (MeV)	Γ_0 (MeV)
RBW	$4133 \pm 6 \pm 11$	$67 \pm 17 \pm 7$

- $J/\psi\phi$ threshold: ~ 4116.4 MeV

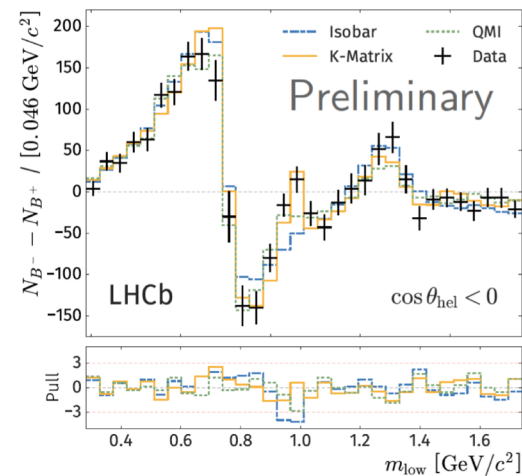
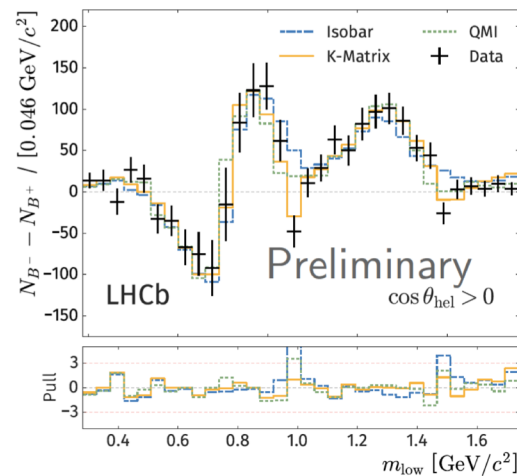
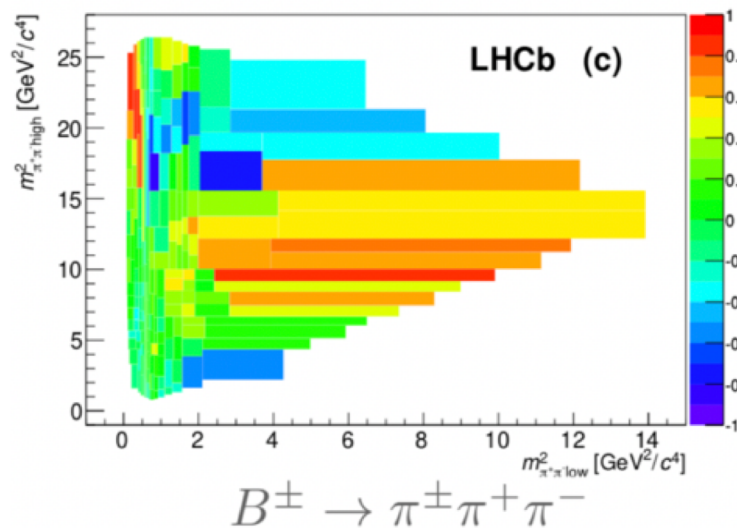
- A KMatrix with single resonance with two decay channels

$$\begin{pmatrix} \mathcal{M}_{D_s^+ D_s^- \rightarrow D_s^+ D_s^-} & \mathcal{M}_{D_s^+ D_s^- \rightarrow J/\psi\phi} \\ \mathcal{M}_{J/\psi\phi \rightarrow D_s^+ D_s^-} & \mathcal{M}_{J/\psi\phi \rightarrow J/\psi\phi} \end{pmatrix} \equiv \begin{pmatrix} \mathcal{K}_{11} & \mathcal{K}_{12} \\ \mathcal{K}_{21} & \mathcal{K}_{22} \end{pmatrix}, \quad \mathcal{K}_{ab}(m) = \sum_R \frac{g_b^R g_a^R}{M_R^2 - m^2} + f_{ab},$$

- Can't conclude whether the dip is due to resonances or due to opening of new decay channel

One slides for CP violation

- Amplitude analysis also important for understanding contributions of CP violation in multi-body decays
- Hadronic dynamic can be described by amplitude mode and thus isolate weak information



- E.g in $B^+ \rightarrow \pi^+\pi^+\pi^-$ decays, one finds several new pattern of CP violation: CP violation due to S-P wave interference, CP violation in tensor particles etc.

Conclusion

- **Understanding fundamental structures of hadrons is one of key topics in particle physics**
- **A general amplitude analysis tool, TF-PWA, has been developed to search for exotic hadrons, to understand their properties and also to study CP violation over phase space**
- **Using TF-PWA, three new tetra-quark states have been observed by the LHCb experiment, one with double charges ($T_{cs}^a(2900)^{++}$) together with its neutral isospin partner, $T_{cs}^a(2900)^0$, and the third $X(3960)$**
- **Stay tuned for more exotic states from LHCb**

Ruiting Ma, Ph. D student from UCAS, will present these results in ICHEP tomorrow

Thank You for Your Attention