

# (Semi-)leptonic charmed meson decays at BESIII

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# Outline

## 1 Introduction

## 2 Leptonic Decays of $D_s^+$

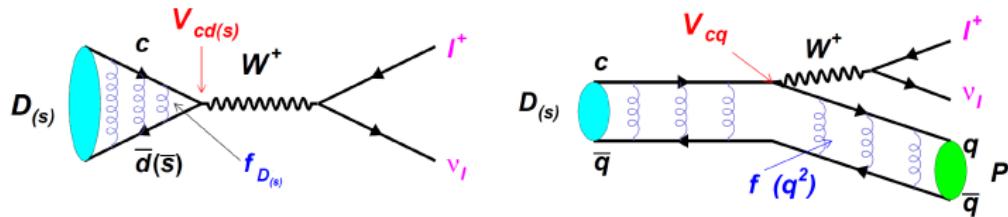
- $D_s^+ \rightarrow \tau^+ (\tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau) \nu_\tau$
- $D_s^+ \rightarrow \tau^+ (\tau^+ \rightarrow \pi^+ \pi^0 \bar{\nu}_\tau) \nu_\tau$
- $D_s^+ \rightarrow \tau^+ (\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau) \nu_\tau$

## 3 Semileptonic Decays of $D^{0(+)}$ and $D_s^+$

- $D^0 \rightarrow K_1(1270)^- e^+ \nu_e$
- $D^{0(+)} \rightarrow \bar{K} e^+ \nu_e$
- $D^0 \rightarrow \rho^- \mu^+ \nu_\mu$
- $D_s^+ \rightarrow X e^+ \nu_e$
- $D_s^+ \rightarrow f_0 e^+ \nu_e$
- $D_s^+ \rightarrow a_0(980) e^+ \nu_e$
- $D_s^+ \rightarrow \pi^0 e^+ \nu_e$

## 4 Conclusions

# Introduction



$$\Gamma(D_{(s)} \rightarrow l^+ \nu_l) = \frac{G_F^2 f_{D_{(s)}}^2}{8\pi} |V_{cd(s)}|^2 m_l^2 m_{D_{(s)}} (1 - \frac{m_l^2}{m_{D_{(s)}}^2})^2$$

$$\frac{d\Gamma(D_{(s)} \rightarrow P l^+ \nu_l)}{dq} = \frac{G_F^2 p^3}{24\pi^3} |f(q^2)|^2 |V_{cq}|^2$$

- 测量衰变常数  $f_{D_s^+}$  和形状因子  $f_+(0)$ , 检验理论格点 QCD 的计算
- 测量 CKM 矩阵元  $|V_{cs(d)}|$ , 检验 CKM 矩阵的幺正性
- 精确检验  $\mu - e, \tau - \mu$  轻子普适性

# Double-tag method for $D^0\bar{D}^0$ and $D^+D^-$

The yields of tag modes can be written as

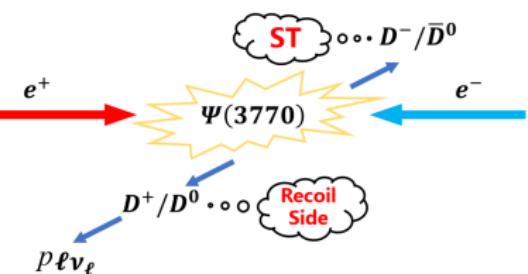
$$N_{\text{tag}} = 2 \cdot N_{D\bar{D}} \cdot \mathcal{B}_{\text{tag}} \cdot \varepsilon_{\text{ST}} \quad (1)$$

The signal yields can be written as

$$N_{\text{sig}} = 2 \cdot N_{D\bar{D}} \cdot \mathcal{B}_{\text{tag}} \cdot \mathcal{B}_{\text{sig}} \cdot \varepsilon_{\text{DT}} \quad (2)$$

The branching fractions of semi-leptonic  $D_s$  decays are determined by

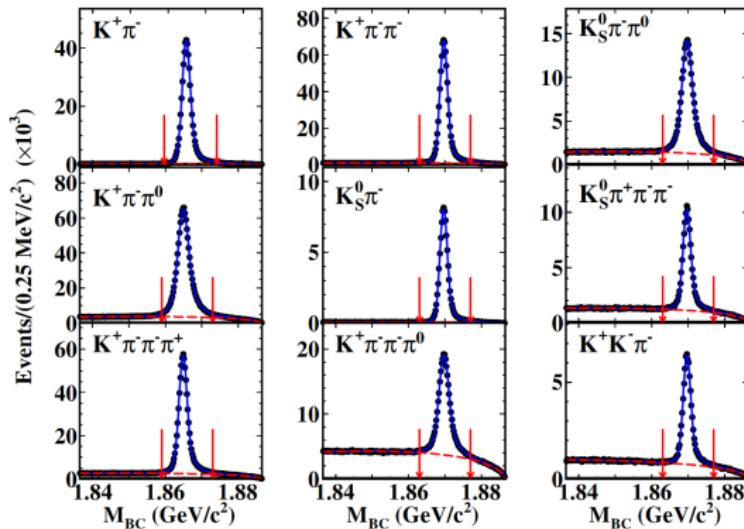
$$\mathcal{B}_{\text{sig}} = \frac{N_{\text{sig}} / (\varepsilon_{\text{DT}} / \varepsilon_{\text{ST}})}{N_{\text{tag}}} \quad (3)$$



# Double-tag method for $D^0\bar{D}^0$ and $D^+D^-$

9 possible single tags at BESIII

$N_{ST(D^0\bar{D}^0)} \sim 2.3M$  and  $N_{ST(D^+D^-)} \sim 1.5M$  with 9 tags @3.773 GeV  $\sim 2.93\text{fb}^{-1}$



signal side:  $X$  ( $X = e, \mu$ , hadron) is reconstructed, the missing neutrinos are determined by

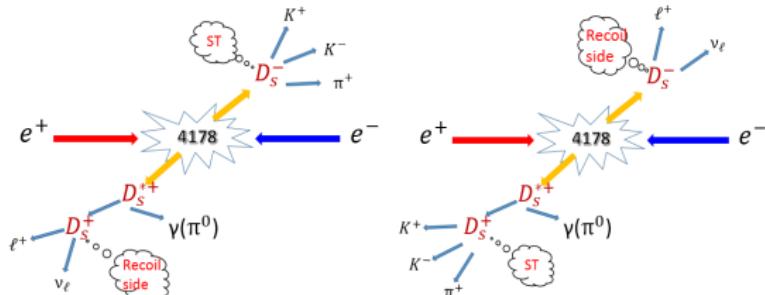
$$M_{\text{miss}}^2 = E_{\text{miss}}^2 - |\vec{p}_{\text{miss}}|^2$$

$$E_{\text{miss}} = E_{\text{cm}} - \sqrt{|\vec{p}_{\text{tag}}|^2 + m_D^2} - E_X$$

$$\vec{p}_{\text{miss}} = -\vec{p}_{\text{tag}} - \vec{p}_X$$

# Double-tag method for $D_s^* \pm D_s^\mp$

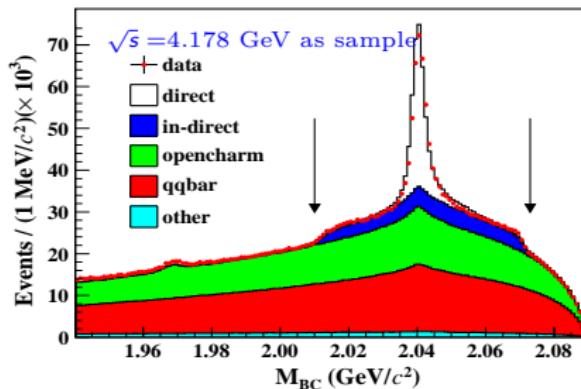
direct: Tag  $D_s$  from  $e^+ e^-$     in-direct: Tag  $D_s$  from  $D_s^*$



Tag mode:  $K^+ K^- \pi^-$ , ...

$$M_{BC} = \sqrt{E_{beam}^2 - |\vec{p}_{tag}|^2},$$

suppress non- $D_s D_s^*$  background



$$N_{ST} = 2N_{D_s^- D_s^+} \mathcal{B}_{tag} \epsilon_{tag}$$

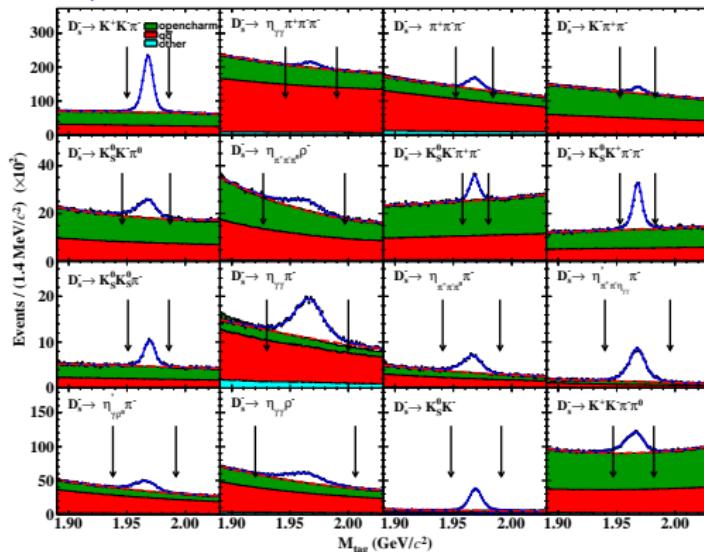
$$N_{DT} = 2N_{D_s^- D_s^+} \mathcal{B}_{tag} \mathcal{B}_{sig} \epsilon_{tag,sig}$$

$$\mathcal{B}(sig) = \frac{N_{DT}}{N_{ST} \epsilon_{DT} / \epsilon_{ST}}$$

# Double-tag method for $D_s^{*\pm} D_s^{\mp}$

16 possible single tags at BESIII

$N_{ST} \sim 0.78M$  with 16 tags @4.178-4.226 GeV  $\sim 3.19\text{fb}^{-1} + 3.13\text{fb}^{-1}$   
 $\sqrt{s} = 4.178 \text{ GeV}$  as sample

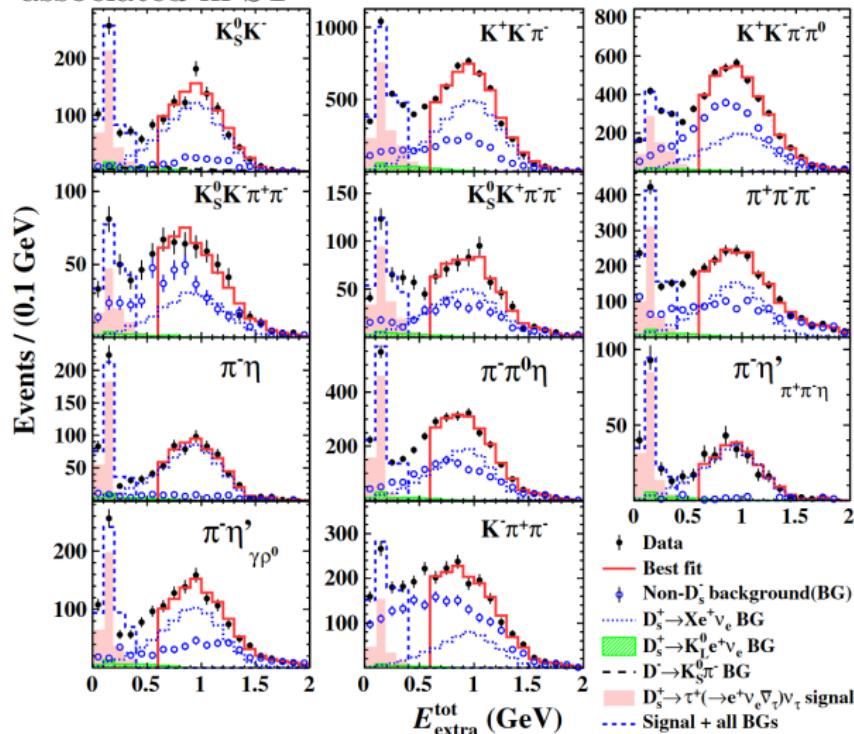


signal side:  $X$  ( $X = \pi, e, \mu$ ) is reconstructed, the missing neutrinos are determined by

$$\begin{aligned} M_{\text{miss}}^2 &= E_{\text{miss}}^2 - |\vec{p}_{\text{miss}}|^2 \\ E_{\text{miss}} &= E_{\text{cm}} - \sqrt{|\vec{p}_{\text{tag}}|^2 + m_{D_s}^2} - E_{\gamma(\pi^0)} - E_X \\ \vec{p}_{\text{miss}} &= -\vec{p}_{\text{tag}} - \vec{p}_{\gamma(\pi^0)} - \vec{p}_X \end{aligned}$$

$D_s^+ \rightarrow \tau^+\nu_\tau$  via  $\tau^+ \rightarrow e^+\nu_e\bar{\nu}_\tau$ 

$E_{\text{extra}}^{\text{tot}}$ : the total energy of the good EMC showers, excluding FSR and those associated in ST



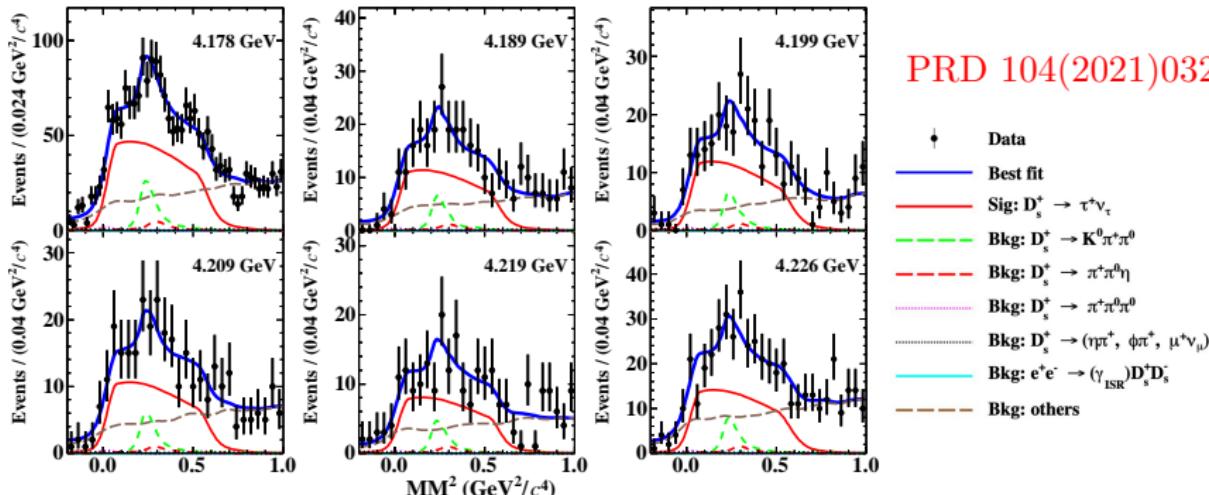
PRL127(2021)171801

- $N_{\text{DT}}^{\text{tot}} = 4940 \pm 94$
- $\mathcal{B}(D_s^+ \rightarrow \tau^+\nu_\tau) = (5.27 \pm 0.10 \pm 0.12)\%$
- $f_{D_s^+} |V_{cs}| = (244.4 \pm 2.3 \pm 2.9) \text{ MeV}$

The most precise result to date~ $\sim 1.5\%$

$$D_s^+ \rightarrow \tau^+\nu_\tau \text{ via } \tau^+ \rightarrow \pi^+\pi^0\bar{\nu}_\tau$$

Simultaneous fit to  $M_{\text{miss}}^2$  @  $\sqrt{s} = 4.178\text{-}4.226$  GeV



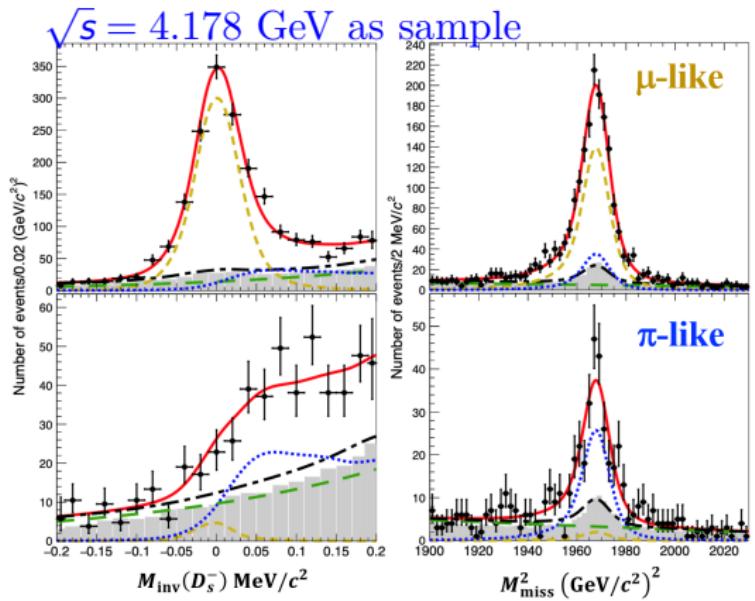
$$N_{\text{DT}} = 1745 \pm 84 \quad \mathcal{B}(D_s^+ \rightarrow \tau^+\nu_\tau) = (5.29 \pm 0.25 \pm 0.20)\%$$

$$f_{D_s^+}|V_{cs}| = (244.8 \pm 5.8 \pm 4.8) \text{ MeV} \quad \text{Precision: 3.1\%}$$

PRD 104(2021)032001

$$D_s^+ \rightarrow \tau^+\nu_\tau \text{ via } \tau^+ \rightarrow \pi^+\bar{\nu}_\tau$$

An unbinned simultaneous maximum likelihood fit to two dimensional distributions



PRD 104(2021)052009

- $\mu\text{-like}$  (upper):  $E_{\text{EMC}} \leq 300$  MeV, mixture of  $D_s^+ \rightarrow \tau^+(\rightarrow \pi^+\bar{\nu}_\tau)\nu_\tau$  and  $D_s^+ \rightarrow \mu^+\nu_\mu$
- $\pi\text{-like}$  (lower):  $E_{\text{EMC}} > 300$  MeV, dominated of  $D_s^+ \rightarrow \tau^+(\rightarrow \pi^+\bar{\nu}_\tau)\nu_\tau$

$$N(D_s^+ \rightarrow \mu^+\nu_\mu) = 2198 \pm 55 \quad N(D_s^+ \rightarrow \tau^+\nu_\tau) = 946^{+46}_{-45}$$

$$\mathcal{B}(D_s^+ \rightarrow \mu^+\nu_\mu) = (0.535 \pm 0.013 \pm 0.016)\% \quad \mathcal{B}(D_s^+ \rightarrow \tau^+\nu_\tau) = (5.21 \pm 0.25 \pm 0.17)\%$$

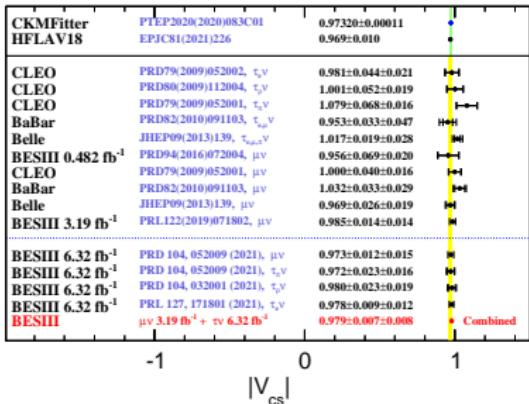
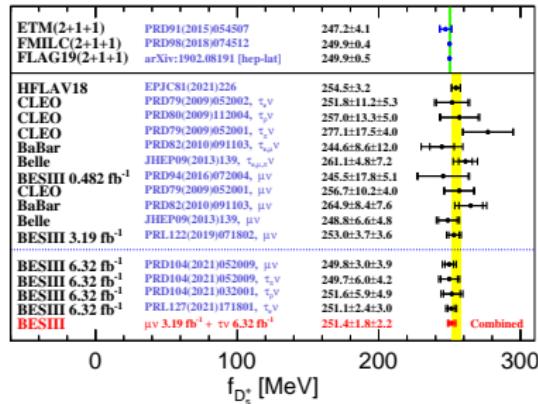
$$f_{D_s^+}|V_{cs}|_\mu = (243.1 \pm 3.0 \pm 3.8) \text{ MeV}$$

$$f_{D_s^+}|V_{cs}|_\tau = (243.0 \pm 5.8 \pm 4.1) \text{ MeV}$$

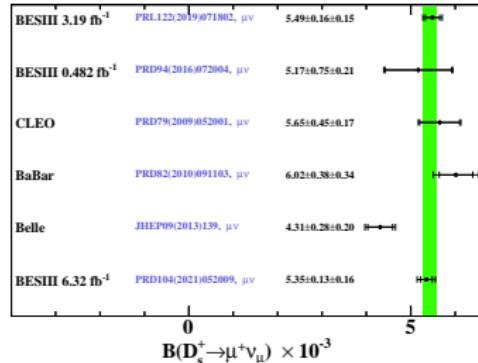
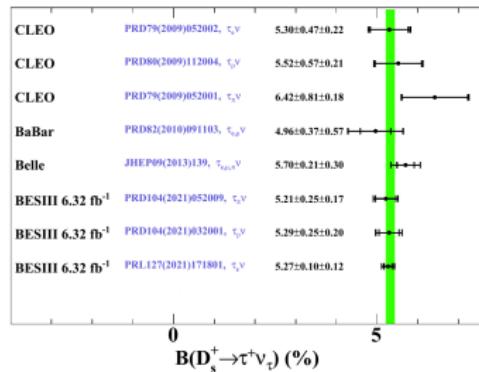
# Comparison of $f_{D_s^+}$ and $|V_{cs}|$

With the values of  $G_F$ ,  $m_{D_s}$ ,  $m_\tau$ , and  $\tau_{D_s}$  [PDG 2022].

Input  $|V_{cs}|_{\text{CKMFitter}} = 0.97349 \pm 0.00016$    Input  $f_{D_s^+}_{LQCD} = (249.9 \pm 0.5) \text{ MeV}$



# Test of Lepton flavor universality



Combined results:

$$\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu) = (5.43 \pm 0.15) \times 10^{-3}$$

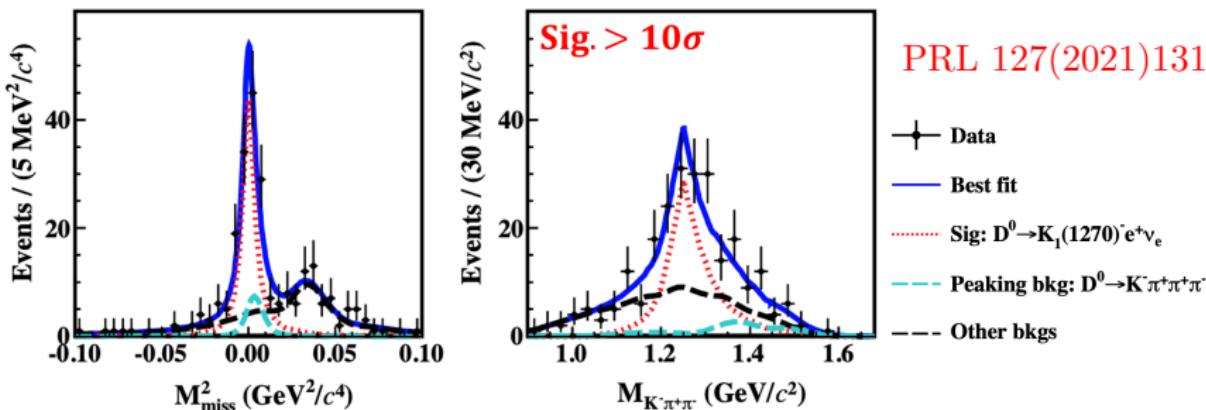
$$\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau) = (5.32 \pm 0.11)\%$$

$$R_{D_s} = \frac{\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu)}{\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau)} = 9.82 \pm 0.36 \quad \text{SM prediction: } 9.75$$

No LFU violation in  $\tau - \mu$  flavors with the current precision.

# Observation of $D^0 \rightarrow K_1(1270)^- e^+ \nu_e$

Two dimensional unbinned extended maximum likelihood simultaneous fits ( $K_1(1270)^- \rightarrow K^- \pi^+ \pi^-$ ).



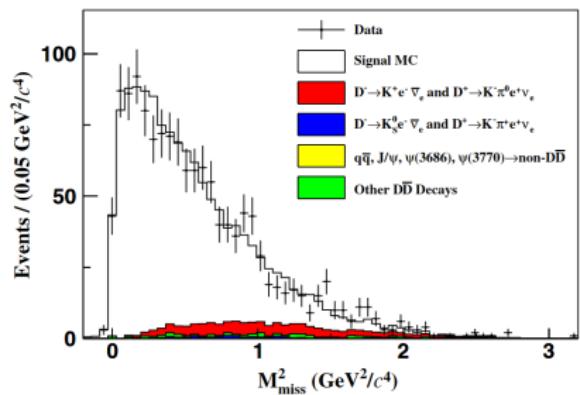
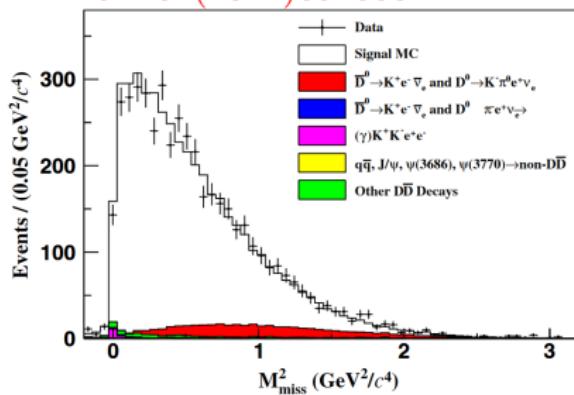
- $N_{DT} = 109.0 \pm 12.5$
- $\mathcal{B}(D^0 \rightarrow K_1(1270)^- e^+ \nu_e) = (1.09 \pm 0.13^{+0.09}_{-0.13} \pm 0.12_{ex.})\%$
- $\frac{\Gamma_{D^0 \rightarrow K_1(1270)^- e^+ \nu_e}}{\Gamma_{D^+ \rightarrow \bar{K}_1(1270)^0 e^+ \nu_e}} = 1.20 \pm 0.02_{stat.} \pm 0.14_{syst.} \pm 0.04_{ex.}$  (Isospin conservation test)

# Measurement of branching fractions of $D^0(+) \rightarrow \bar{K}e^+\nu_e$

Independent measurement with new method at BESIII.

$$N_{\text{sig}} = N_{D\bar{D}} \mathcal{B}^2(D \rightarrow \bar{K}e\nu_e) \epsilon_{\text{sig}} \Rightarrow \mathcal{B}(D \rightarrow \bar{K}e\nu_e) = \sqrt{\frac{N_{\text{sig}}}{N_{D\bar{D}} \epsilon_{\text{sig}}}}$$

PRD104(2021)052008



$$\mathcal{B}(D^0 \rightarrow K^- e^+ \nu_e) = (3.567 \pm 0.031 \pm 0.021)\%$$

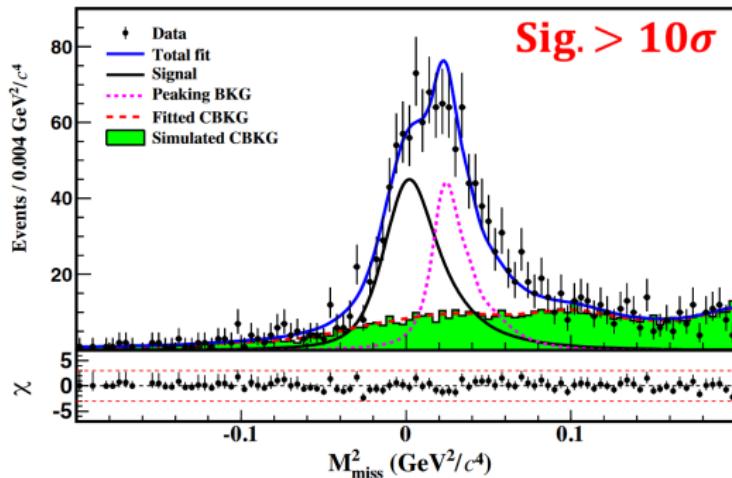
$$\mathcal{B}(D^+ \rightarrow \bar{K}e^+\nu_e) = (8.68 \pm 0.14 \pm 0.16)\%$$

$$\frac{\Gamma_{(D^0 \rightarrow K^- e^+ \nu_e)}}{\Gamma_{(D^+ \rightarrow \bar{K}e^+\nu_e)}} = 1.039 \pm 0.021 \text{ (Support isospin symmetry within } 1.9\sigma\text{)}$$

# Observation of $D^0 \rightarrow \rho^- \mu^+ \nu_\mu$

First measurement of  $D^0 \rightarrow \rho^- \mu^+ \nu_\mu (\rho^- \rightarrow \pi^- \pi^0)$

PRD104(2021)L091103



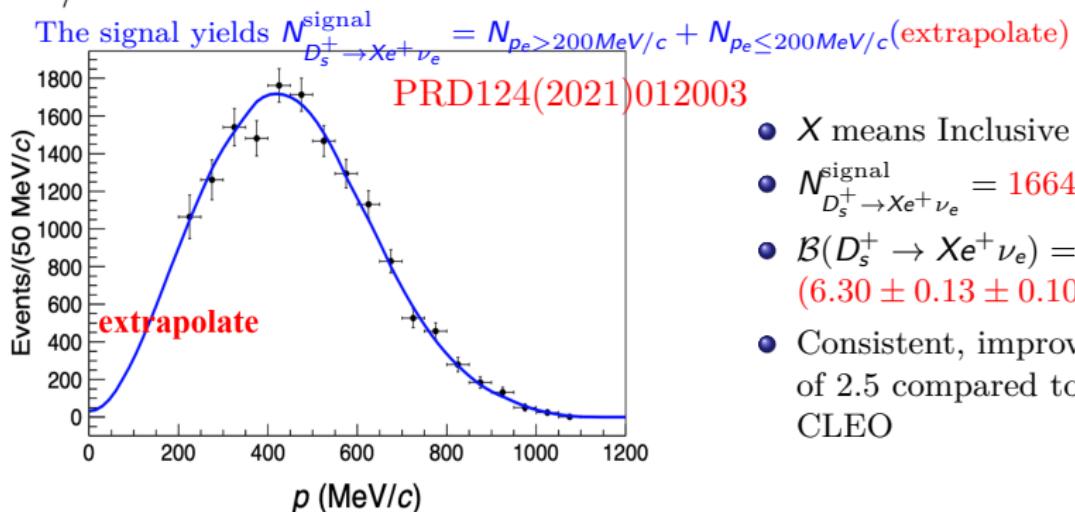
- $N_{DT} = 570 \pm 40$
- $\mathcal{B}(D^0 \rightarrow \rho^- \mu^+ \nu_\mu) = (1.35 \pm 0.09 \pm 0.09) \times 10^{-3}$

$$R_{\mu/e} = \frac{\mathcal{B}(D^0 \rightarrow \rho^- \mu^+ \nu_\mu)}{\mathcal{B}(D^0 \rightarrow \rho^- e^+ \nu_e)} = 0.90 \pm 0.11 \quad \text{SM}(0.93-0.96)$$

$$\frac{\Gamma_{(D^0 \rightarrow \rho^- \mu^+ \nu_\mu)}}{2\Gamma_{(D^+ \rightarrow \rho^0 \mu^+ \nu_\mu)}} = 0.71 \pm 0.14 \quad (\text{Support isospin symmetry within } 2.1\sigma)$$

# Precision measurement of $D_s^+ \rightarrow X e^+ \nu_e$

Sort recoil side selected tracks into eighteen momentum ( $p_e$ ) bins for  $p_e > 200$  MeV/c



- $X$  means Inclusive MC
- $N_{D_s^+ \rightarrow X e^+ \nu_e}^{\text{signal}} = 16648 \pm 326$
- $\mathcal{B}(D_s^+ \rightarrow X e^+ \nu_e) = (6.30 \pm 0.13 \pm 0.10) \times 10^{-2}$
- Consistent, improved by a factor of 2.5 compared to that from CLEO

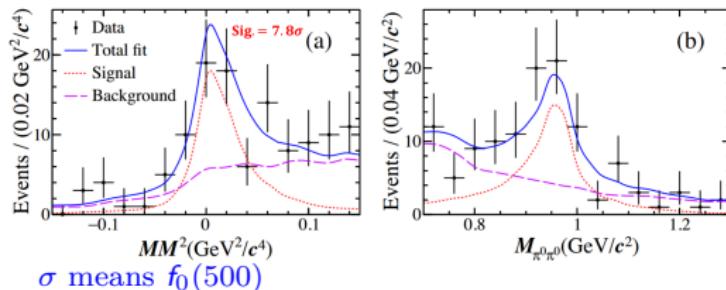
$$\mathcal{B}(D_s^+ \rightarrow X e^+ \nu_e) - \sum_i \mathcal{B}(D_s^+ \rightarrow X_i e^+ \nu_e)_{\text{known}} = (-0.04 \pm 0.13 \pm 0.20) \times 10^{-2}$$

No evidence for the existence of unobserved  $D_s^+$  semileptonic decay modes

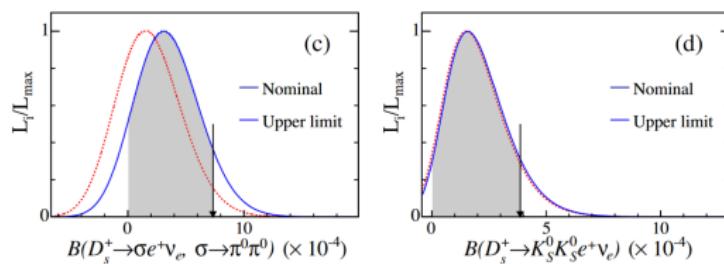
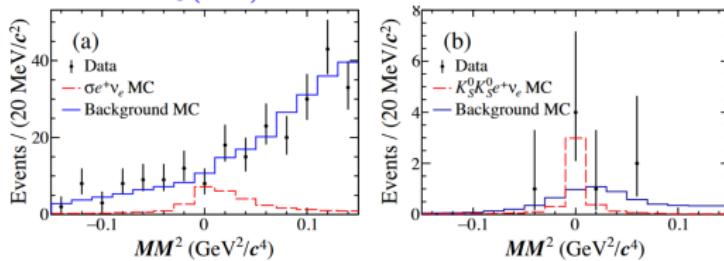
$$\frac{\Gamma_{D_s^+ \rightarrow X e^+ \nu_e}}{\Gamma_{D^0 \rightarrow X e^+ \nu_e}} = 0.790 \pm 0.016 \pm 0.020 \quad (\text{consistent with prediction} \sim 0.813)$$

# Measurement of branching fraction of $D_s^+ \rightarrow f_0 e^+ \nu_e$

Two dimensional unbinned extended maximum likelihood fit( $f_0 \rightarrow \pi^0 \pi^0$ ).



$\sigma$  means  $f_0(500)$



PRD105(2022)L031101

$$N_{DT} = 54.8 \pm 10.1$$

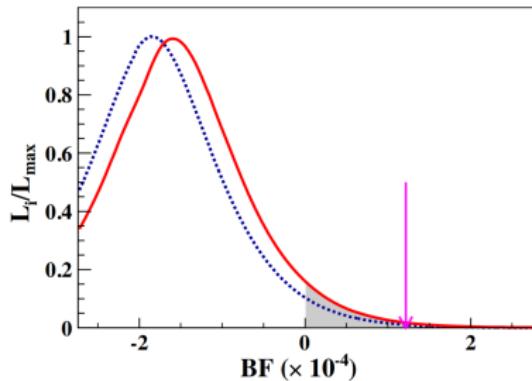
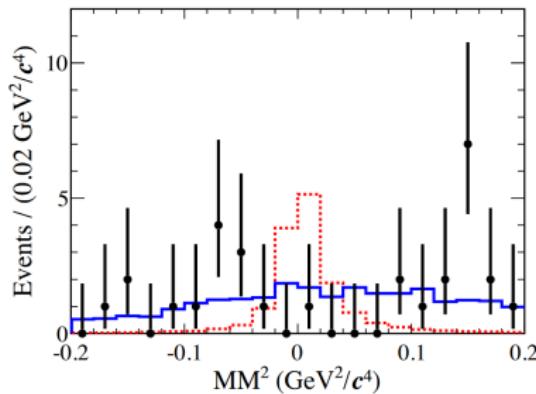
$$\mathcal{B}(D_s^+ \rightarrow f_0(980)e^+\nu_e) = (7.9 \pm 1.4 \pm 0.4) \times 10^{-4}$$

$$\mathcal{B}(D_s^+ \rightarrow f_0(500)e^+\nu_e) < 7.3 \times 10^{-4}$$

$$\mathcal{B}(D_s^+ \rightarrow K_s^0 K_s^0 e^+\nu_e) < 3.8 \times 10^{-4}$$

Search for  $D_s^+ \rightarrow a_0(980)e^+\nu_e$ 

PRD103(2021)092004

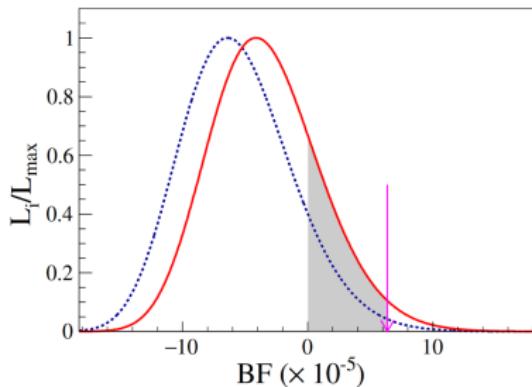
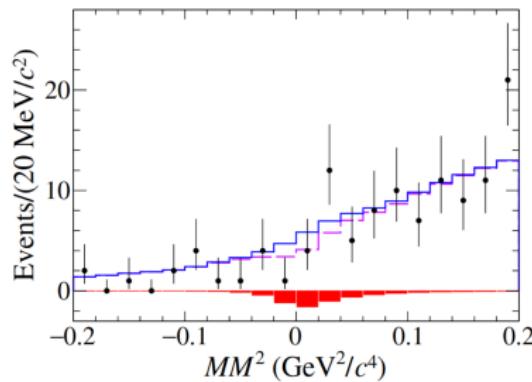


No significant signal is observed

$$\mathcal{B}(D_s^+ \rightarrow a_0(980)e^+\nu_e) \times \mathcal{B}(a_0(980) \rightarrow \pi^0\eta) < 1.2 \times 10^{-4}$$

Search for  $D_s^+ \rightarrow \pi^0 e^+ \nu_e$ 

arXiv:2206.13870



No significant signal is observed

$$\mathcal{B}(D_s^+ \rightarrow \pi^0 e^+ \nu_e) < 6.4 \times 10^{-5}$$

consistent with the predicted BF of  $D_s^+ \rightarrow \pi^0 e^+ \nu_e$ ,  $(2.65 \pm 0.38) \times 10^{-5}$

# Prospects

- More analyses of  $D_s \rightarrow \mu\nu_\mu$  and  $D_s \rightarrow \tau\nu_\tau$
- Improved analyses of  $D_s \rightarrow \eta^{(\prime)}\ell\nu$
- Improved analyses of  $D_s \rightarrow K^0\ell\nu$
- Improved analyses of  $D_s \rightarrow KK\ell\nu$
- Improved analyses of  $D_s \rightarrow \pi\pi\ell\nu$
- Improved measurements of  $D \rightarrow \mu\nu_\mu$  and  $D \rightarrow \tau\nu_\tau$
- Improved measurements of  $D^{0(+)} \rightarrow (\text{P}, \text{V}, \text{S}, \text{ and A})\ell\nu$

# Conclusions

In recent two years, with  $2.93\text{fb}^{-1}$  at  $3.773\text{ GeV}$  and  $6.32\text{ fb}^{-1}$  from  $4.178\text{-}4.226\text{ GeV}$  data samples, BESIII have studied leptonic and semi-leptonic decays.

- Precisely measured
  - $D_s^+ \rightarrow \tau^+ \nu_\tau$
  - $\tau^+ \rightarrow e \nu_e \bar{\nu}_\tau$
  - $\tau \rightarrow \pi^+ \pi^0 \bar{\nu}_\tau$
  - $\tau \rightarrow \pi \bar{\nu}_\tau$
  - $D_s^+ \rightarrow \mu^+ \nu_\mu$
  - $D_s^+ \rightarrow X e^+ \nu_e$
- First observation for
  - $D^0 \rightarrow K_1(1270)^- e^+ \nu_e$
  - $D^0 \rightarrow \rho^- \mu^+ \nu_\mu$
- Searches for
  - $D_s^+ \rightarrow a_0(980) e^+ \nu_e$
  - $D_s^+ \rightarrow \pi^0 e^+ \nu_e$
- New method
  - $D^{0(+)} \rightarrow \bar{K} e^+ \nu_e$

In the near future, BESIII will collect  $20\text{ fb}^{-1}$  @  $3.773\text{ GeV}$  data sample, and another  $3\text{fb}^{-1}$  @  $4.178\text{ GeV}$ , the precisions will be further improved.

Thank you!