

# Introduction to Heavy Ion Collisions – Experimental

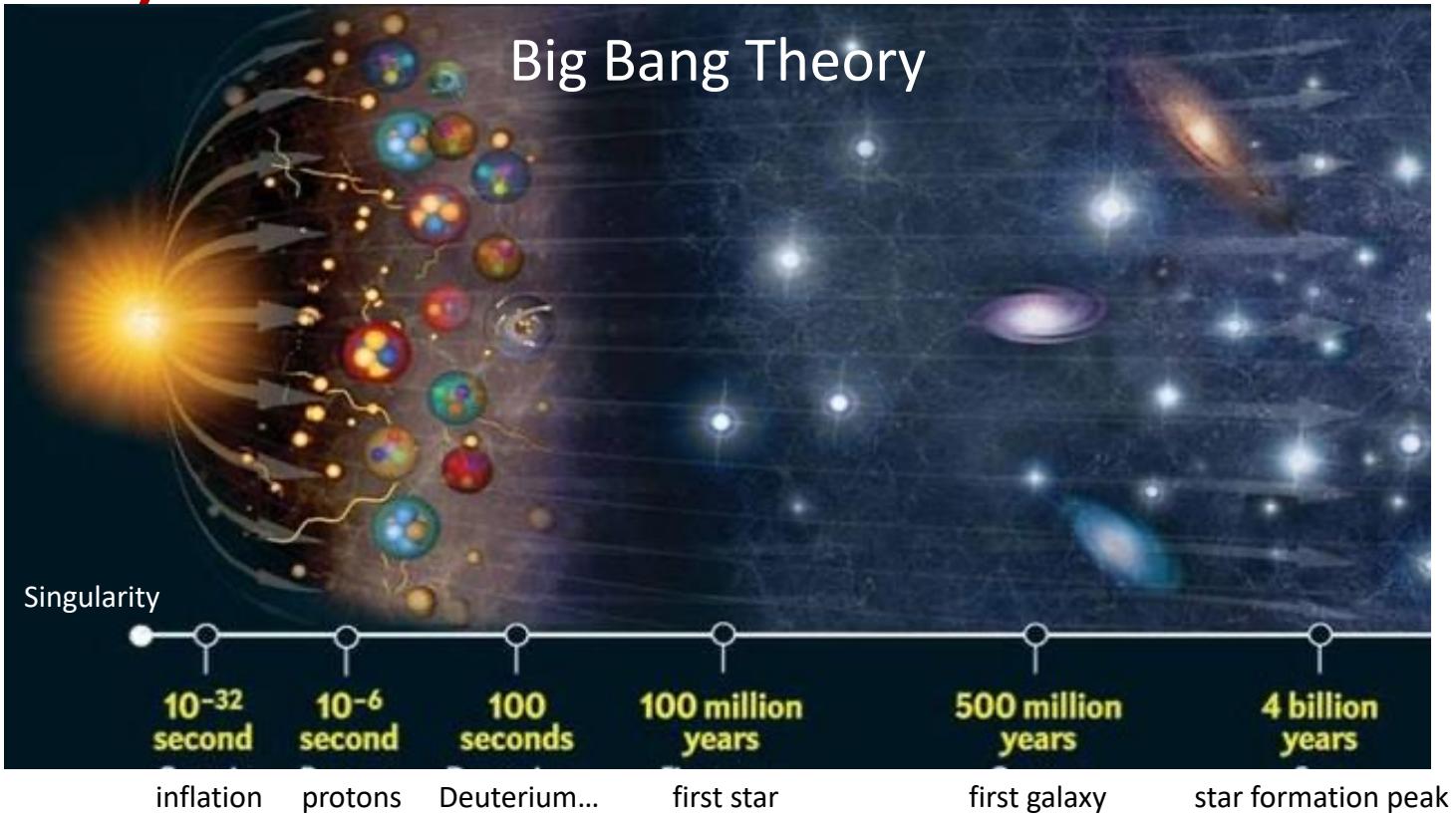
## Part1 Collective Flow

陈震宇  
山东大学

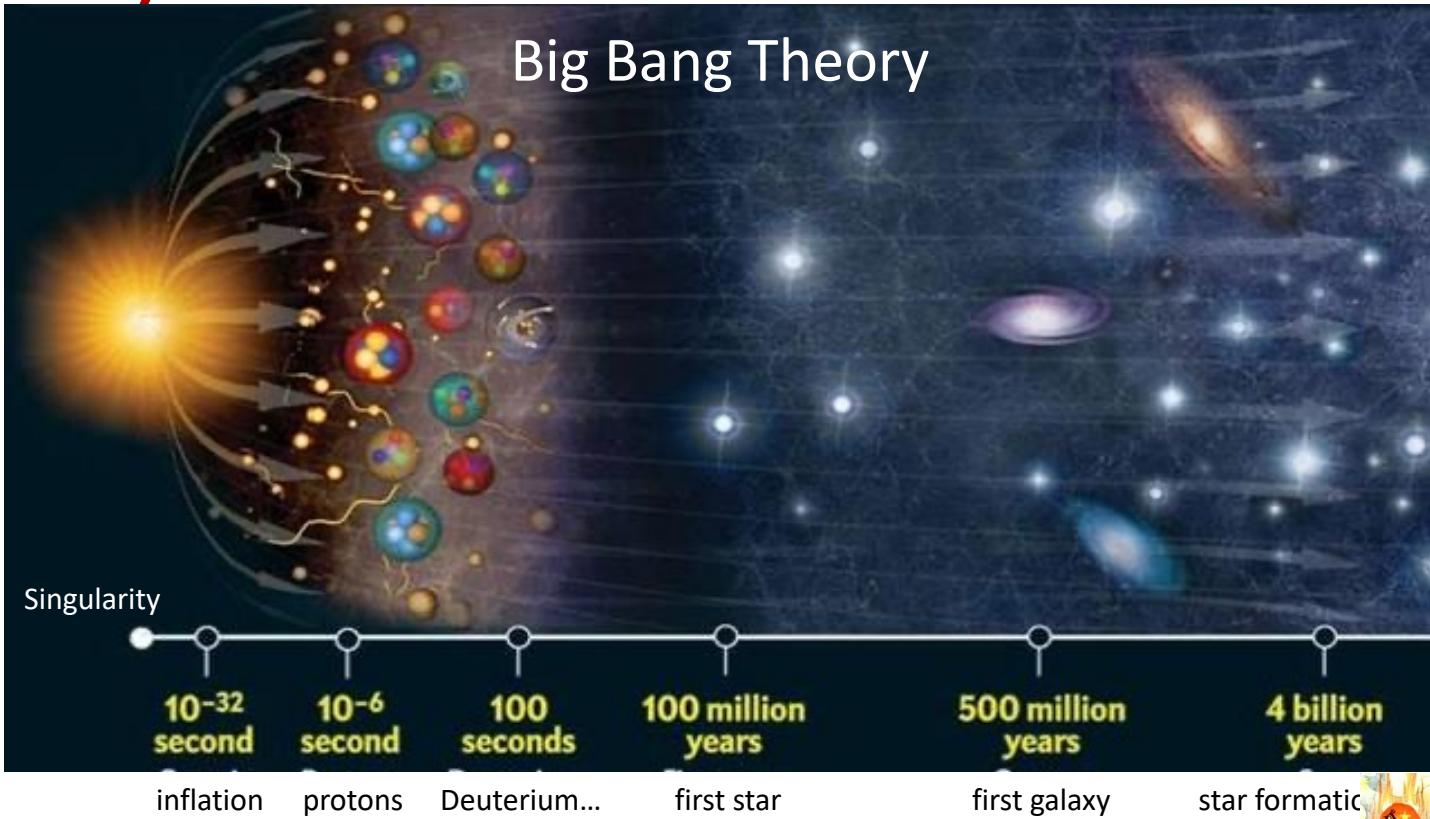


山东大学  
SHANDONG UNIVERSITY

# The early universe



# The early universe



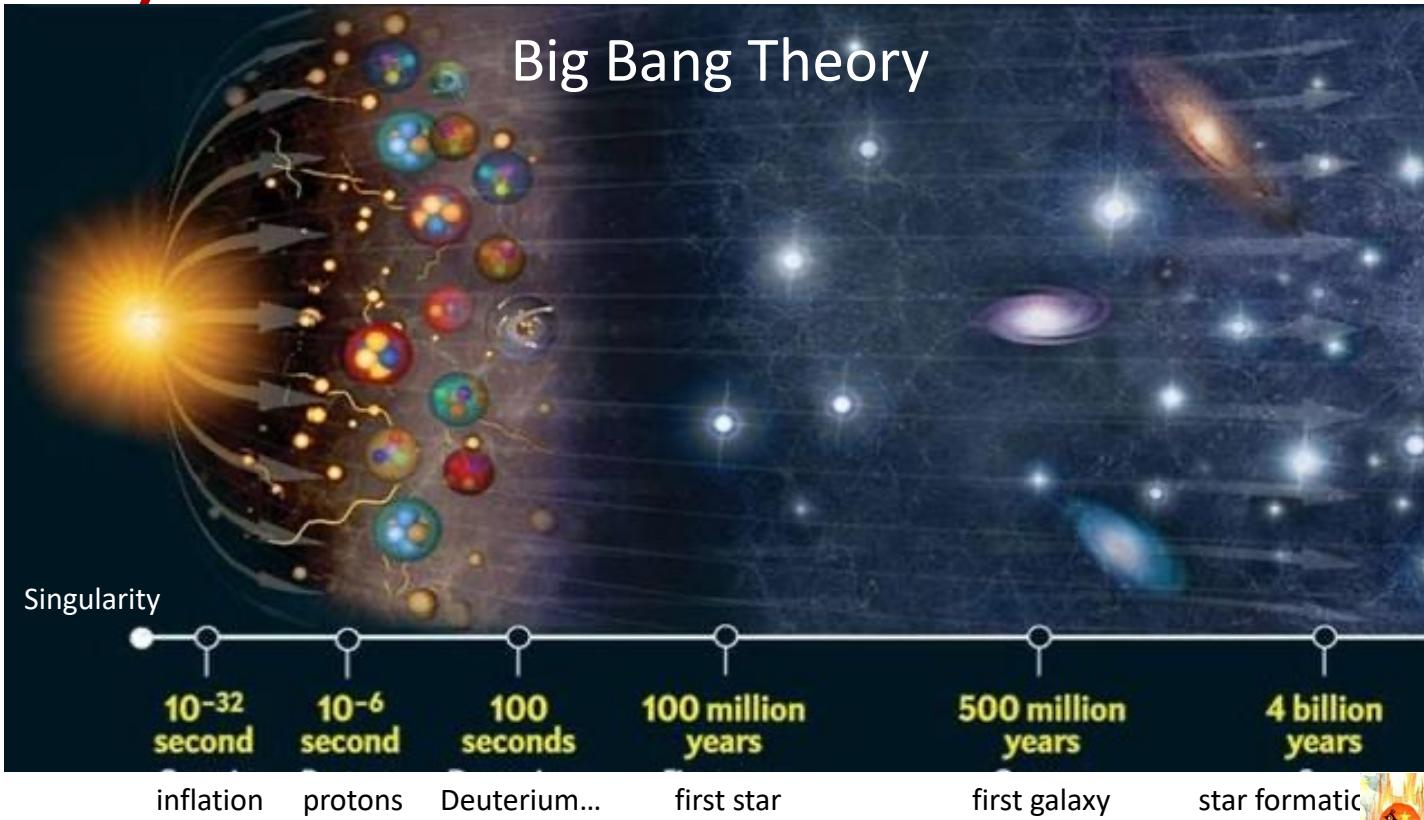
天地混沌如鸡子（奇点），盘古生其中（暴胀）

盘古在其中，一日九变（质子-轻核元素产生）

天日高一丈，地日厚一丈，盘古日长一丈。如此万八千岁，  
天数极高，地数极深，盘古极长（现今宇宙）



# The early universe



天地混沌如鸡子（奇点），盘古生其中（暴胀）

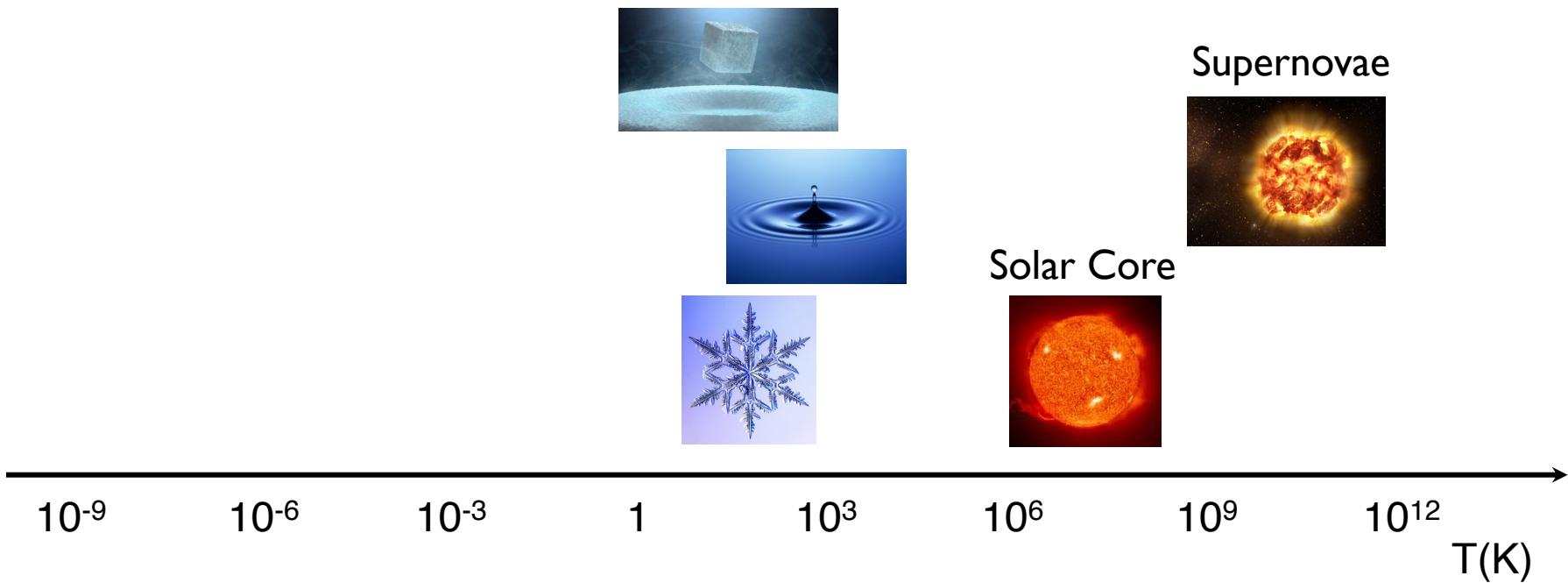
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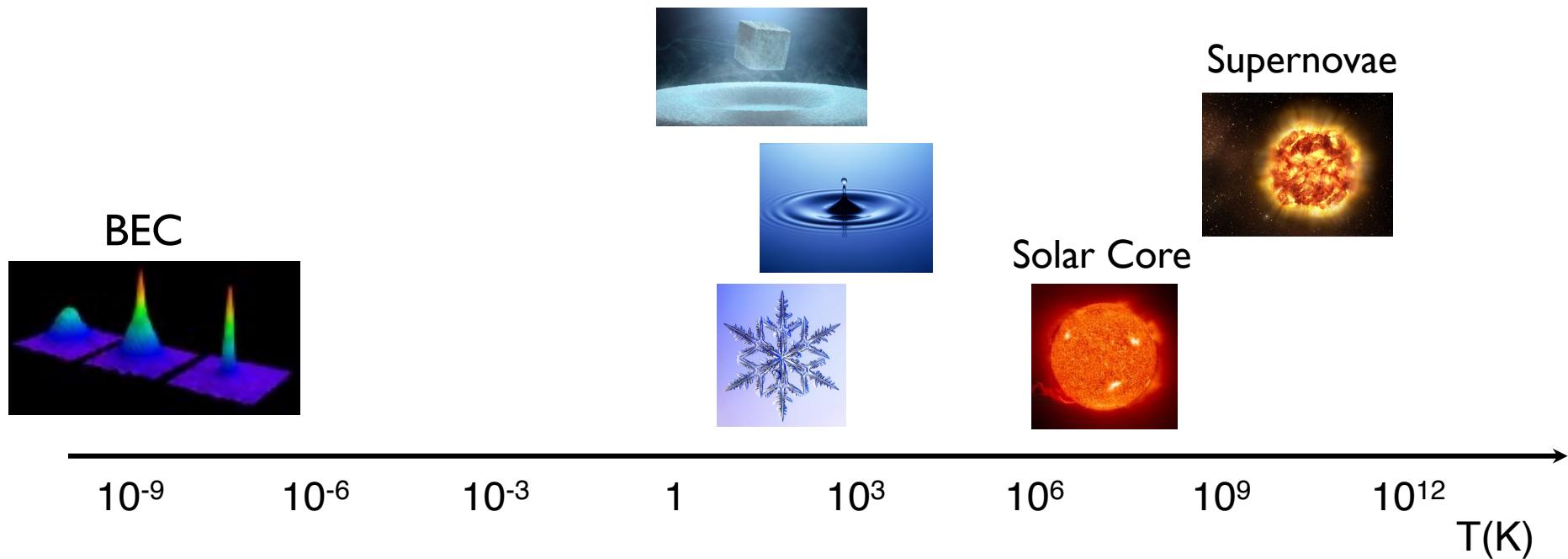
The early universe has high temperature/density



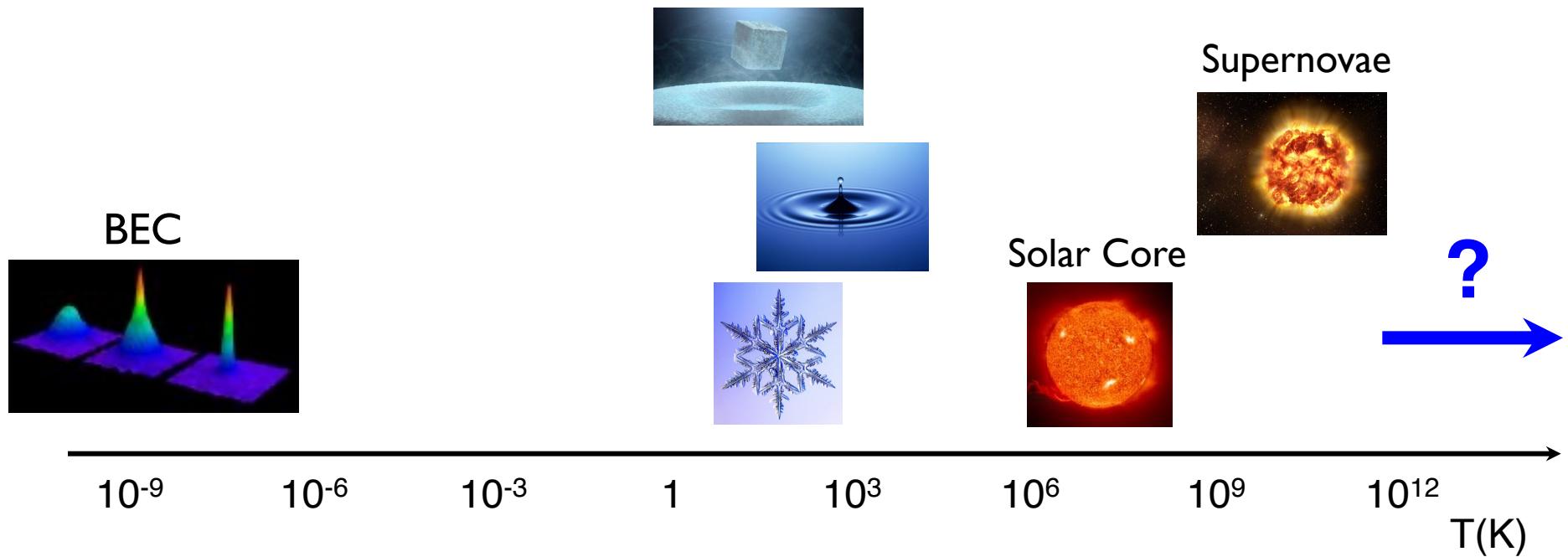
# Phases of matter



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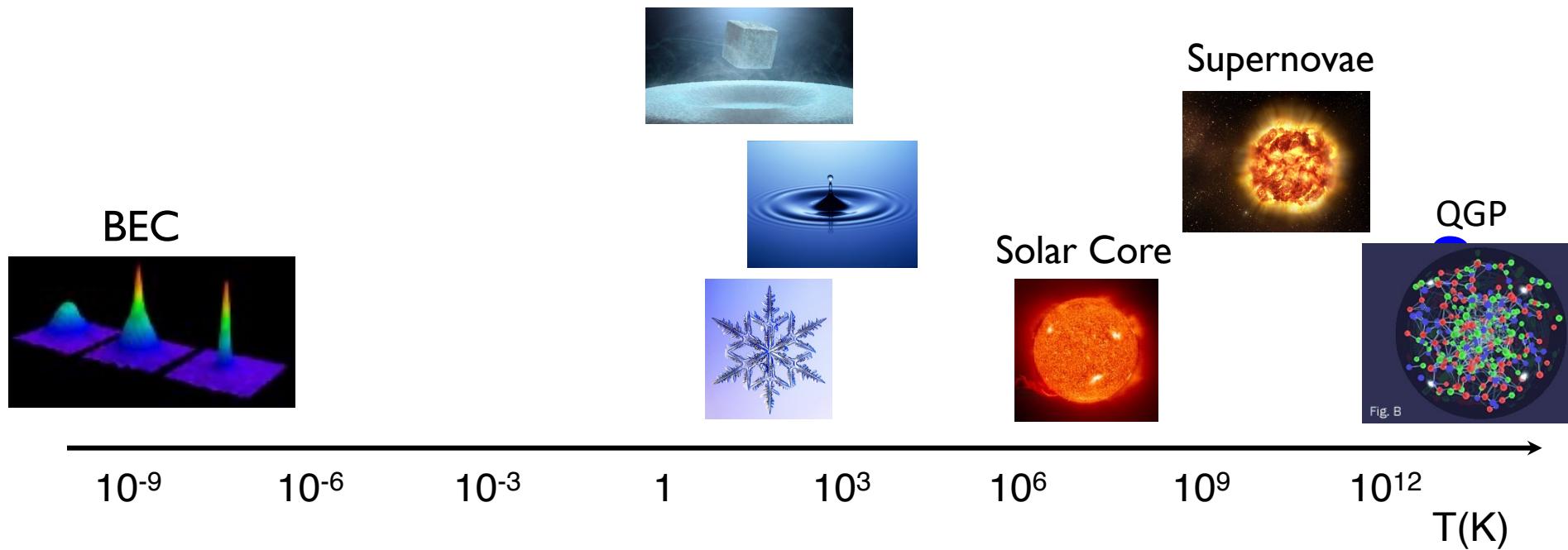


# Phases of matter



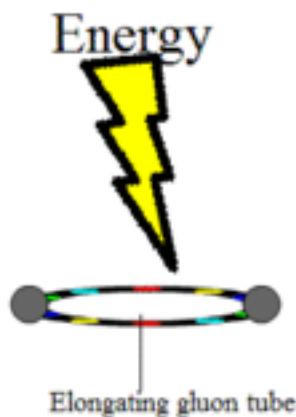
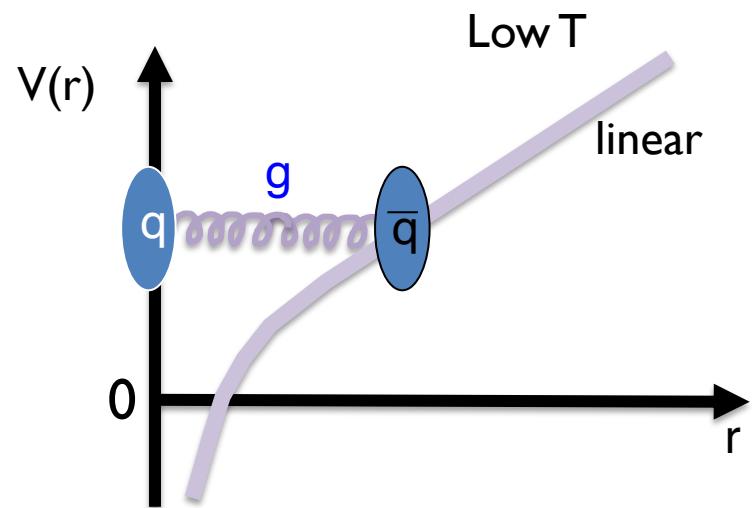
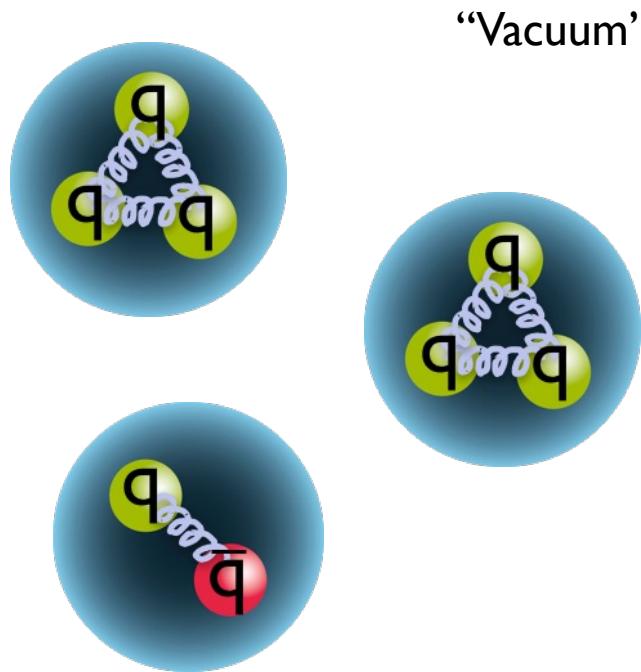
What are the properties of matter at extremely high temperatures ( $> 10^{12}$  K)?

# Phases of matter

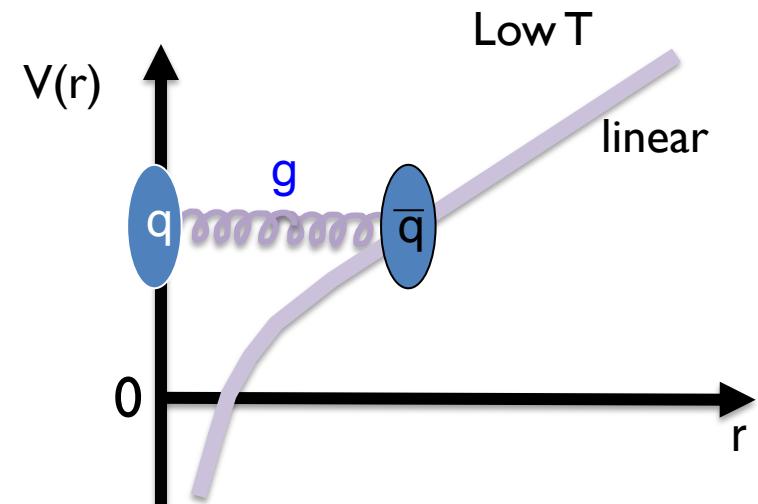


What are the properties of matter at extremely high temperatures ( $> 10^{12}$  K)?

# Confinement → De-confinement



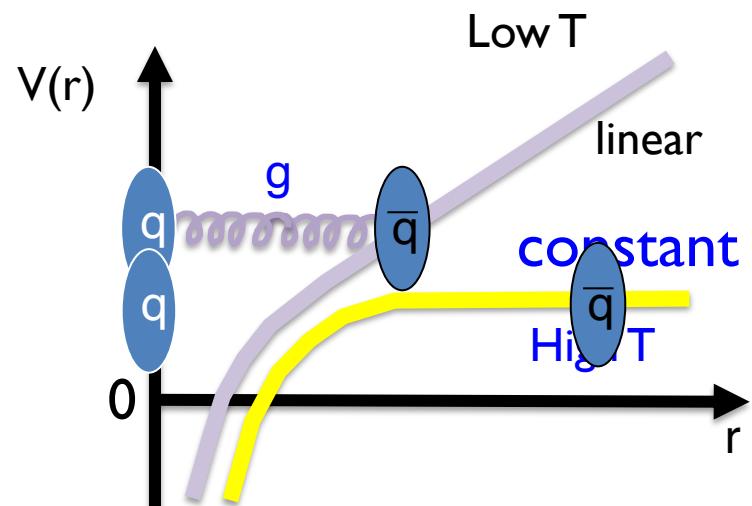
# Confinement → De-confinement



# Confinement → De-confinement



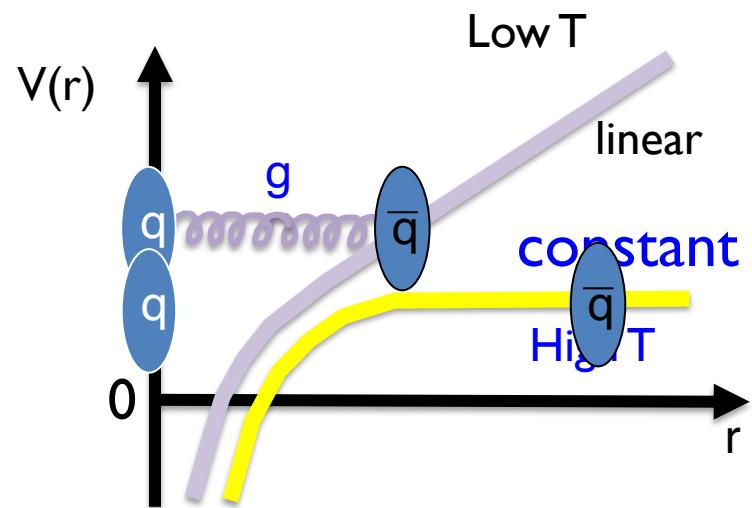
Taken from "Cooking Master Boy"



# Confinement → De-confinement



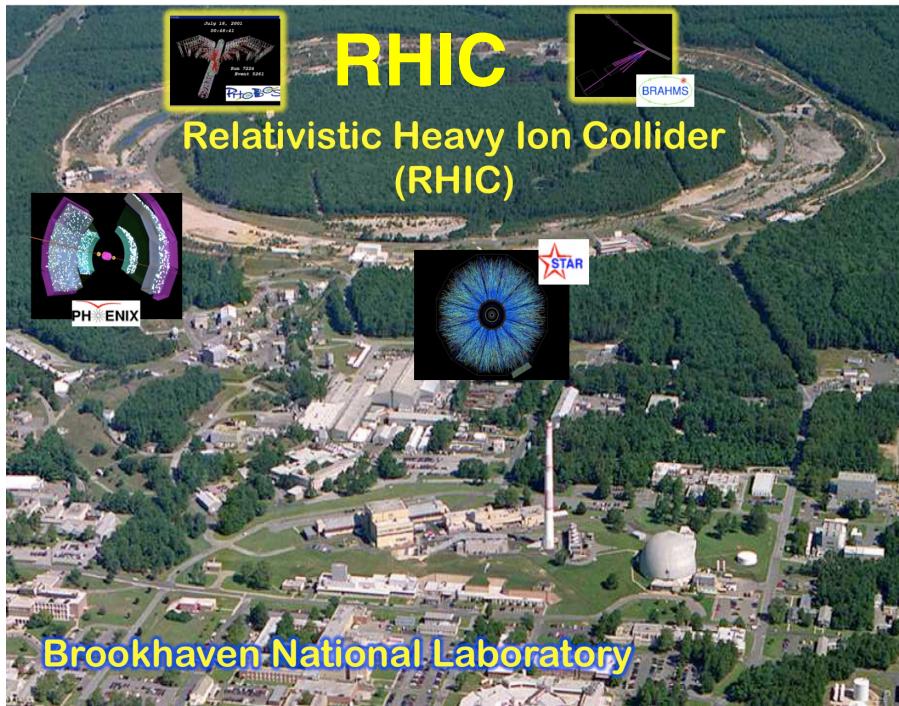
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**"Quark-Gluon Plasma"  
(QGP)**

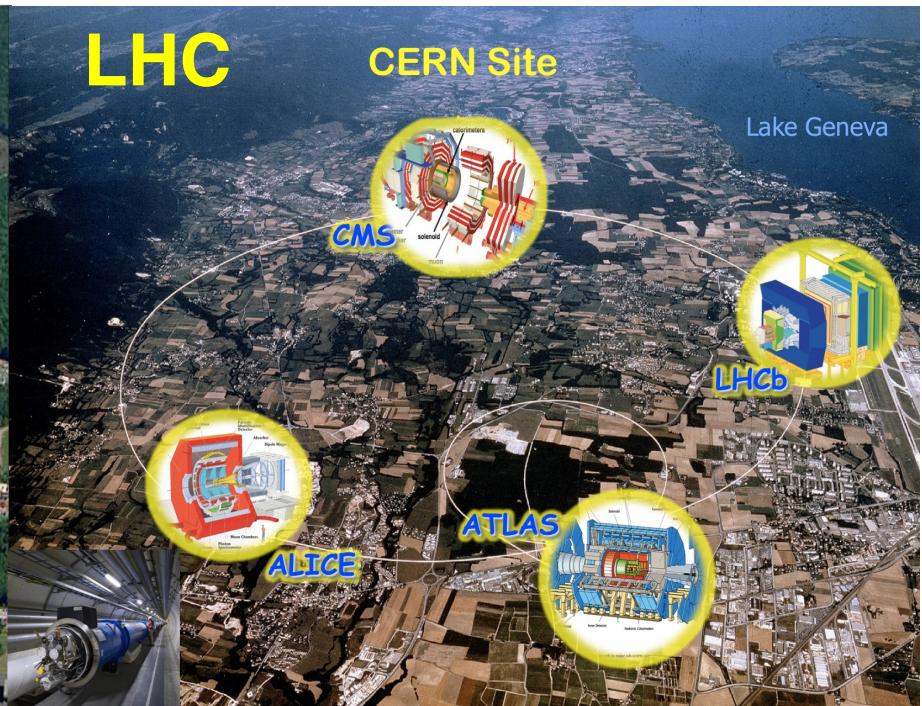
$$T_C \sim 154 \text{ MeV} \sim 2 \times 10^{12} \text{ K}$$

# Creating QGP in lab



# First collisions in 2000

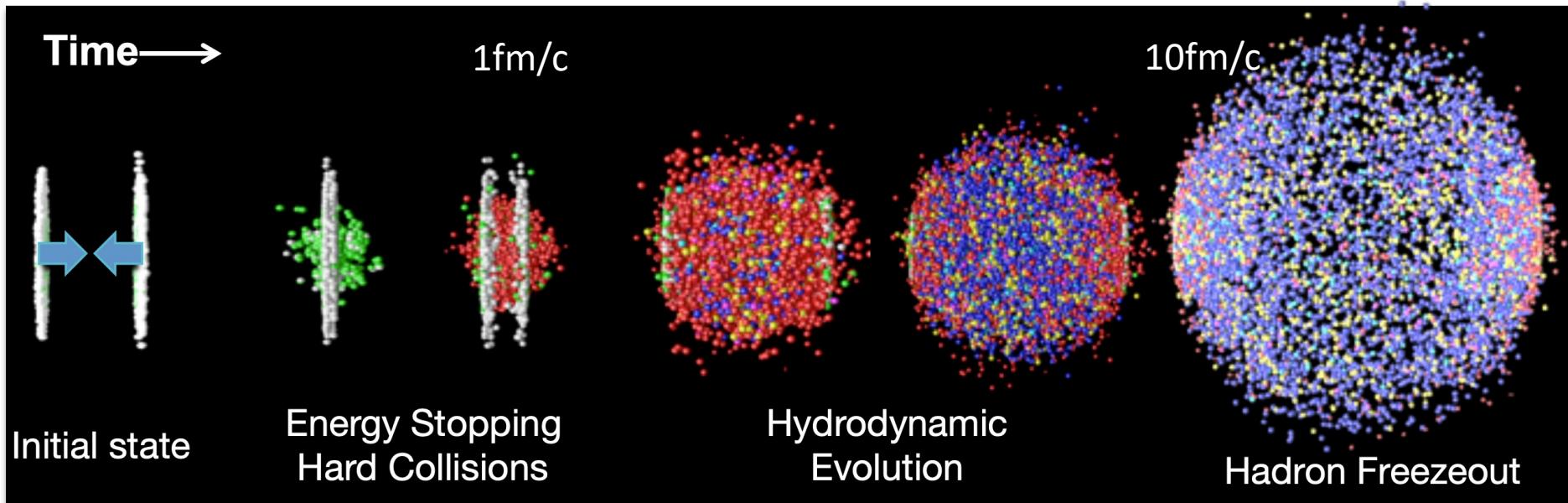
- Diameter 1.2 km
  - pp, dAu, CuCu, AuAu, UU, OO, ...
  - $\sqrt{s}_{\text{NN}} \sim \mathbf{0.007 - 0.2 \text{ TeV}}$
  - 99.995% speed of light



# First collisions in 2010

- Diameter 8.6 km
  - pp, PbPb, pPb, XeXe
  - $\sqrt{s}_{\text{NN}} \sim \mathbf{5 - 8 \, TeV}$
  - 99.9999991% speed of light

# QGP evolution



Extremely short-lived matter

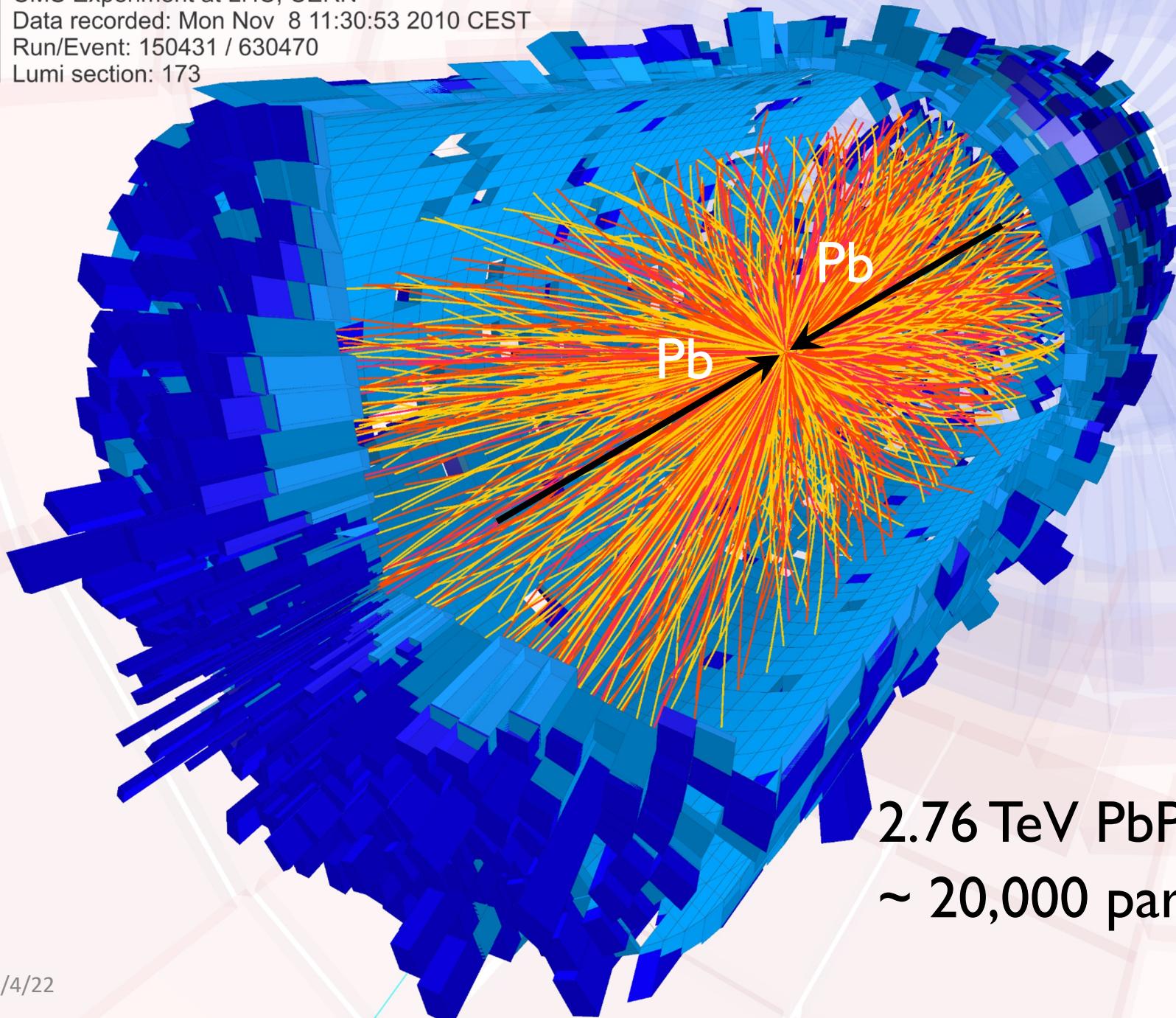


CMS Experiment at LHC, CERN

Data recorded: Mon Nov 8 11:30:53 2010 CEST

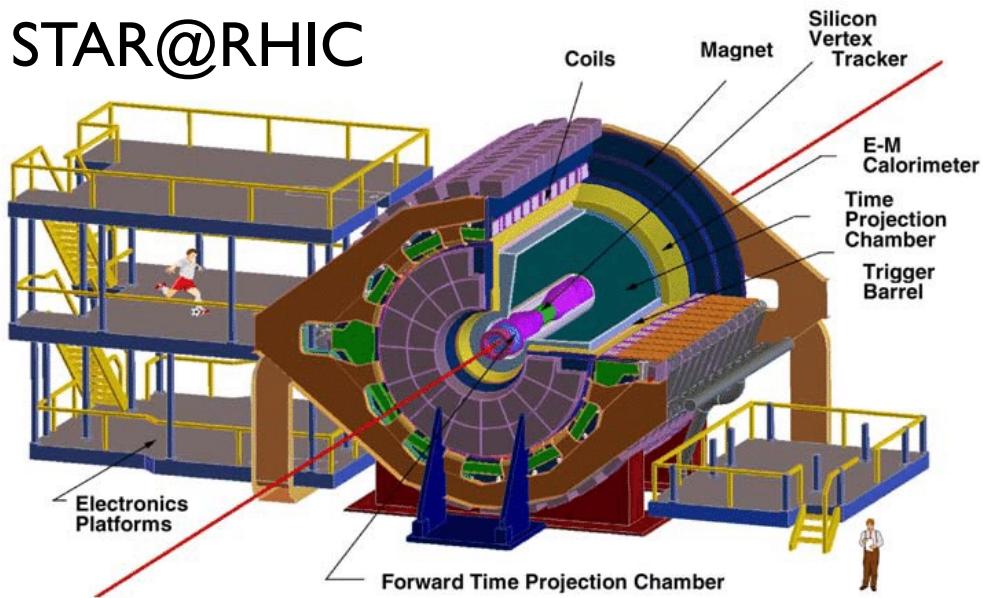
Run/Event: 150431 / 630470

Lumi section: 173

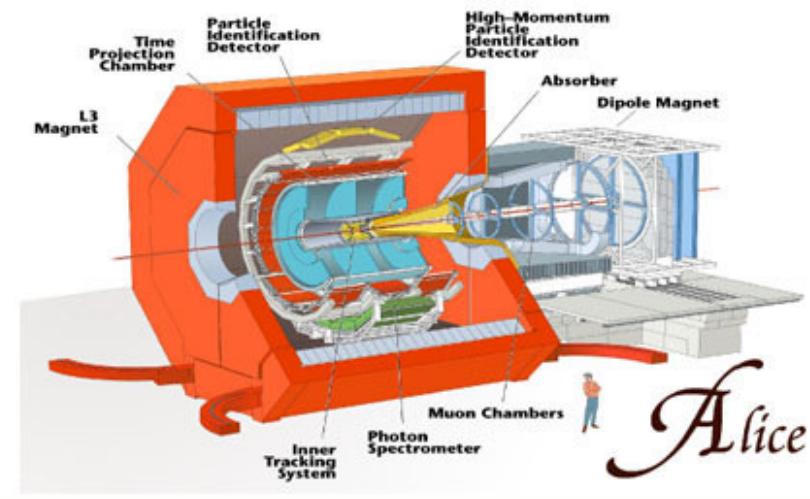
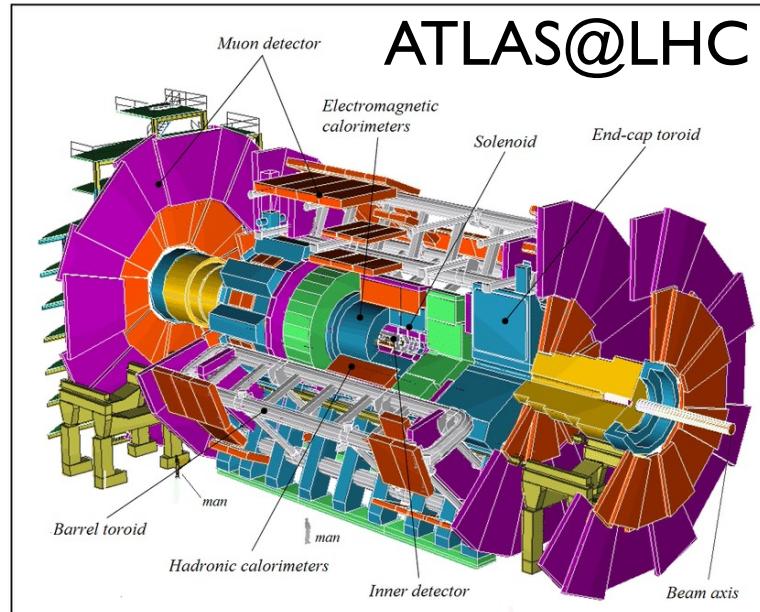
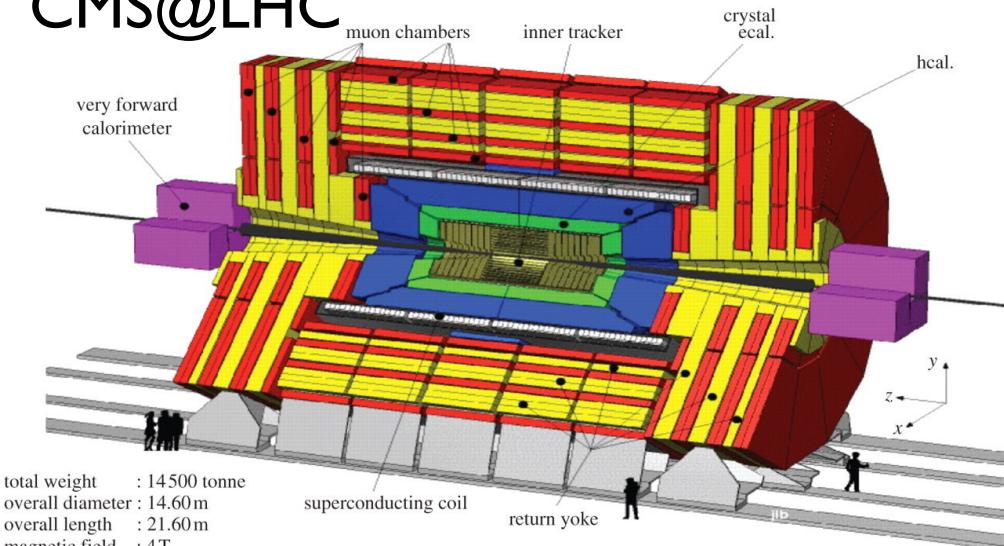


# Detectors

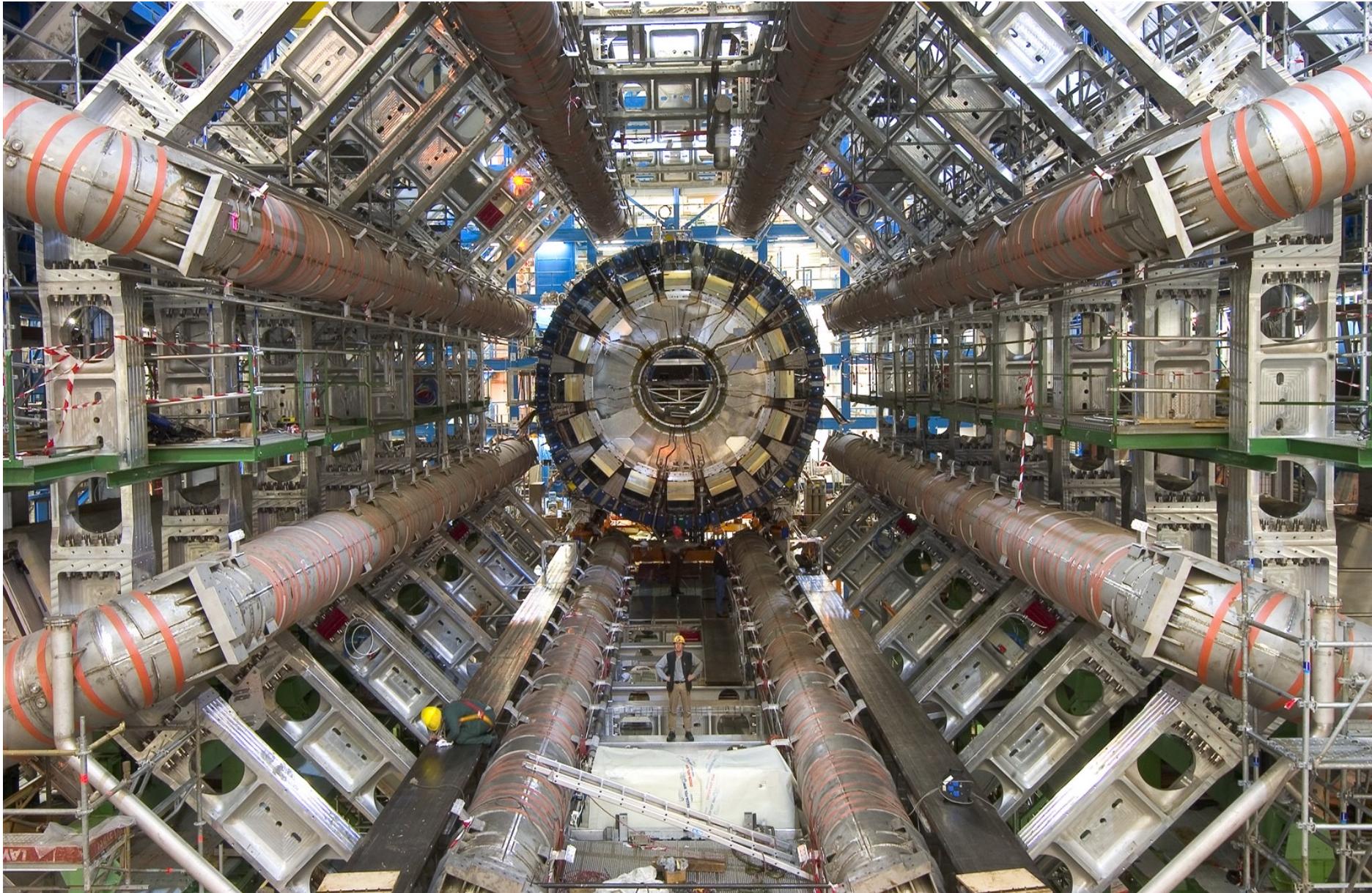
## STAR@RHIC



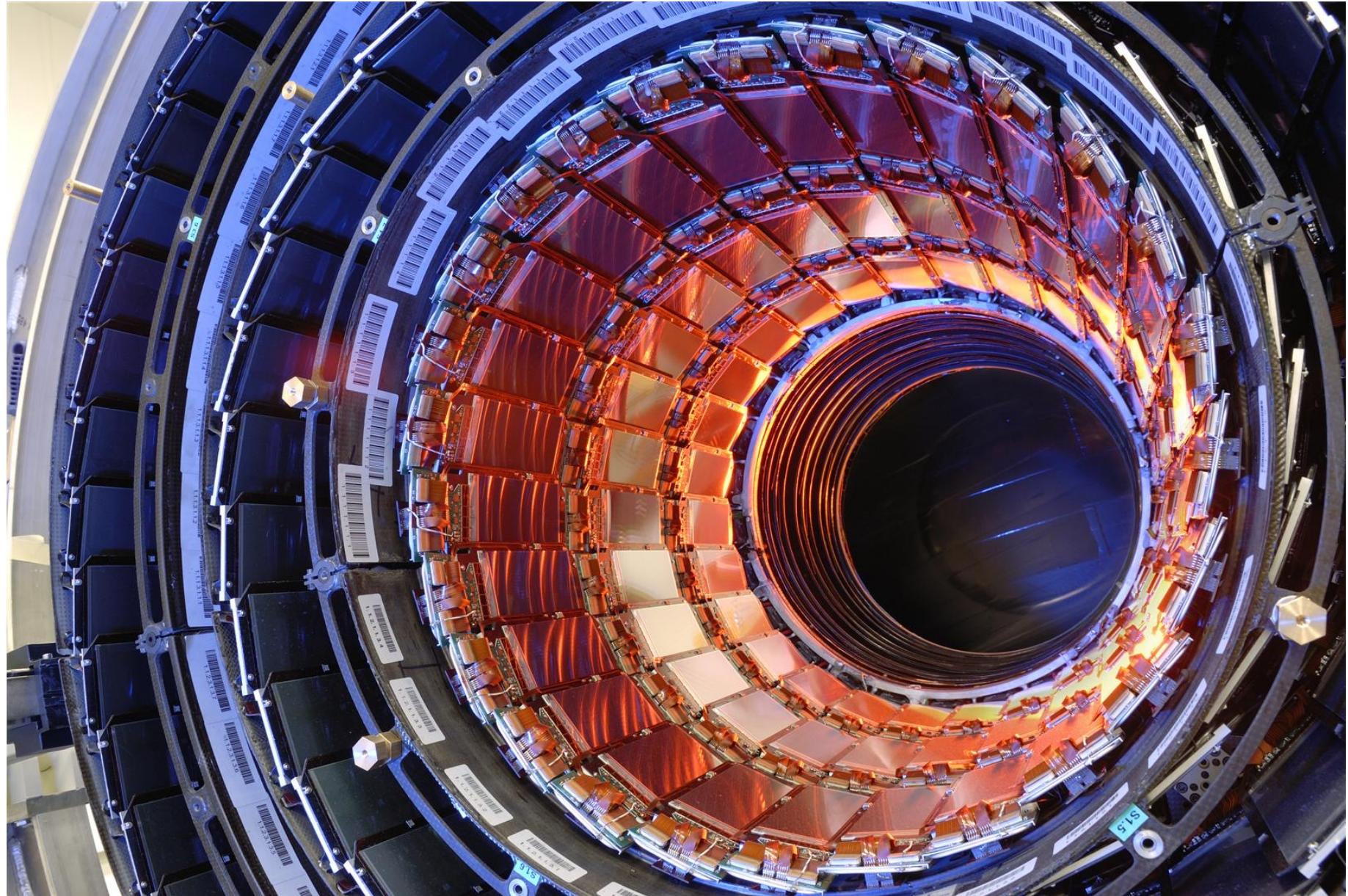
## CMS@LHC



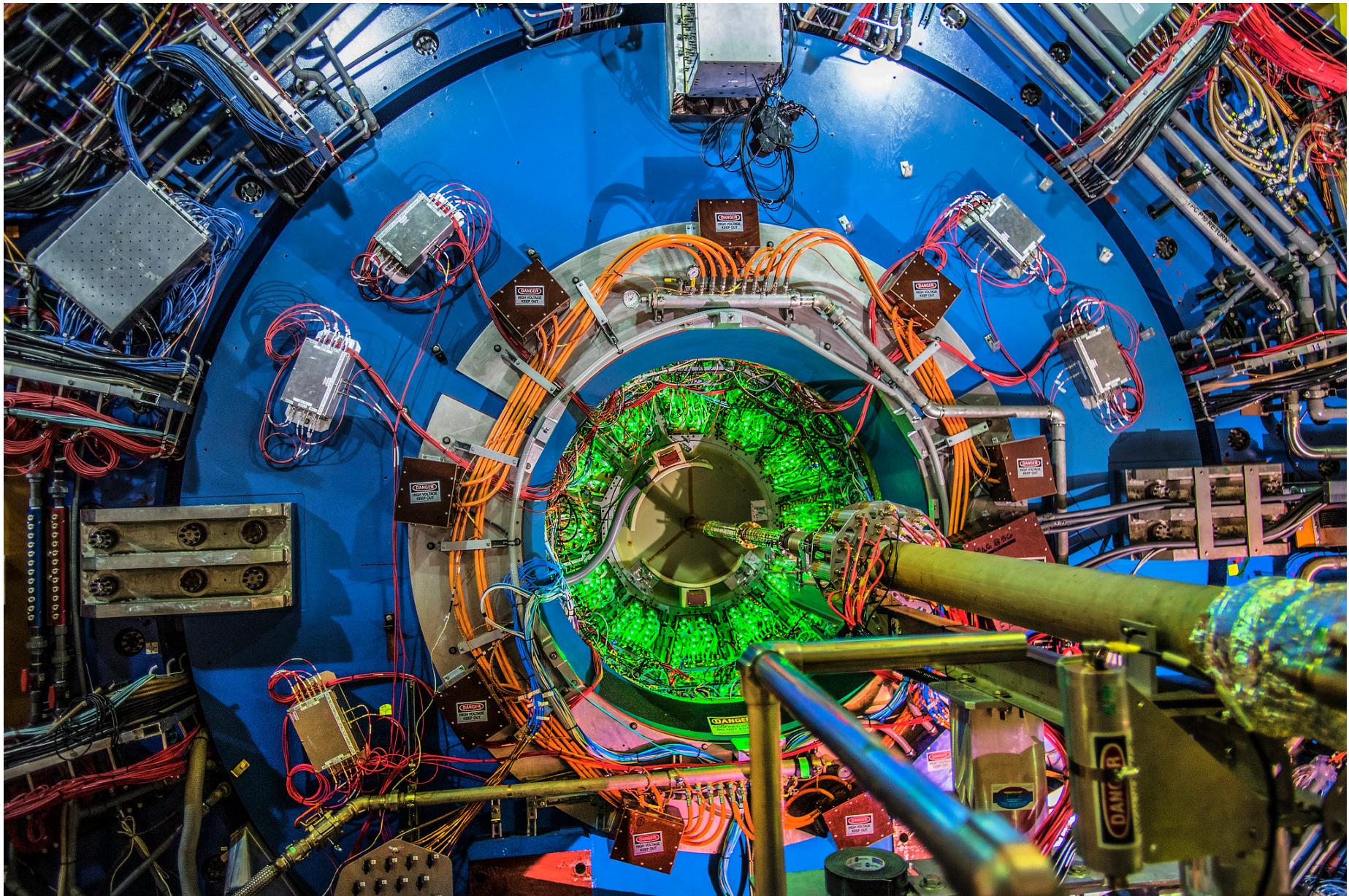
# Detectors



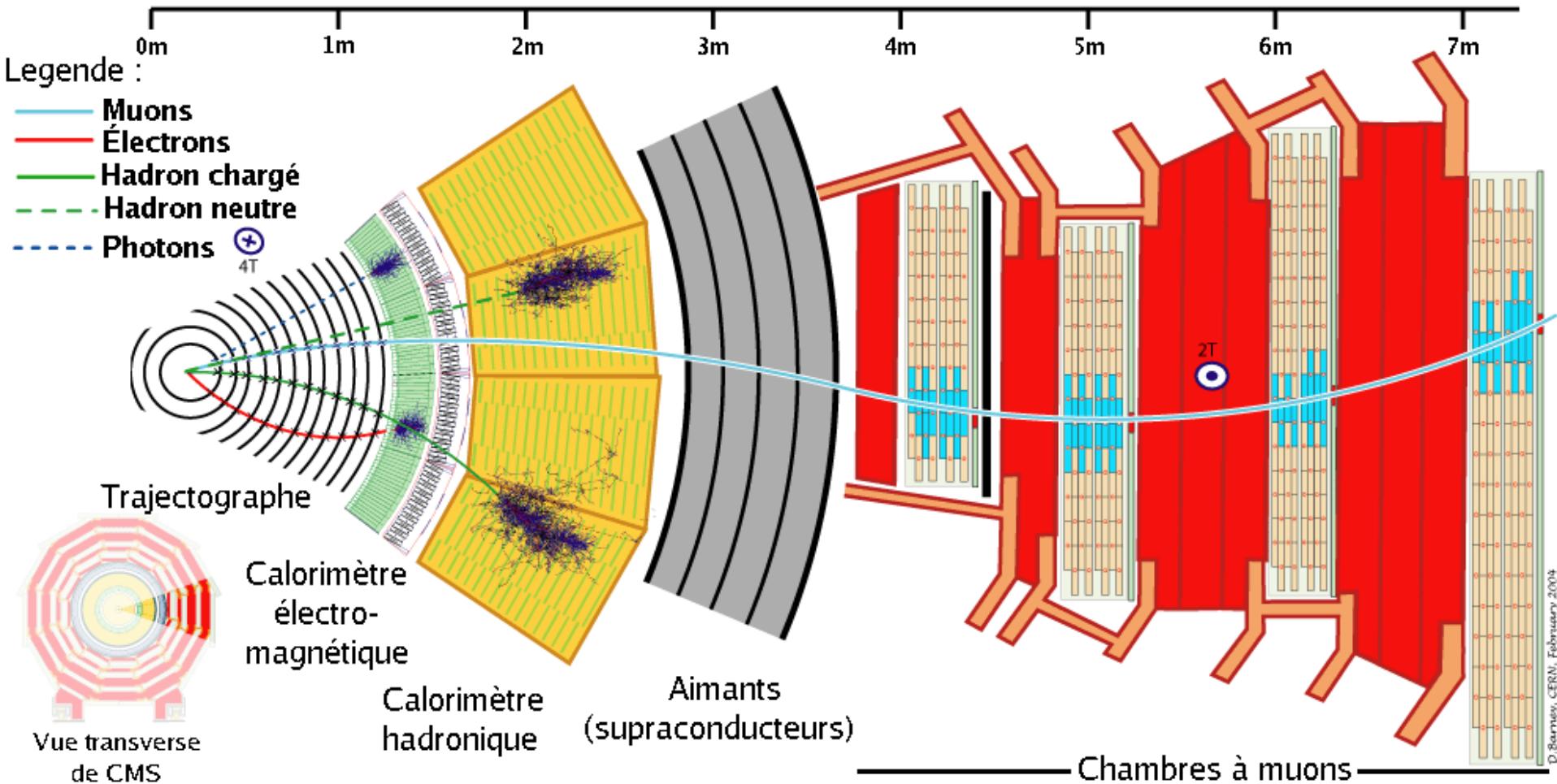
# Detectors



# Detectors



# Particle journey



# Discovery of a strongly coupled QGP



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## RHIC Scientists Serve Up "Perfect" Liquid (2005)

New state of matter more remarkable than predicted -- raising many new questions

Monday, April 18, 2005

TAMPA, FL -- The four detector groups conducting research at the [Relativistic Heavy Ion Collider](#) (RHIC) -- a giant atom "smasher" located at the U.S. Department of Energy's Brookhaven National Laboratory -- say they've created a new state of hot, dense matter out of the quarks and gluons that are the basic particles of atomic nuclei, but it is a state quite different and even more remarkable than had been predicted. In [peer-reviewed papers](#) summarizing the first three years of RHIC findings, the scientists say that instead of behaving like a gas of free quarks and gluons, as was expected, the matter created in RHIC's heavy ion collisions appears to be more like a *liquid*.

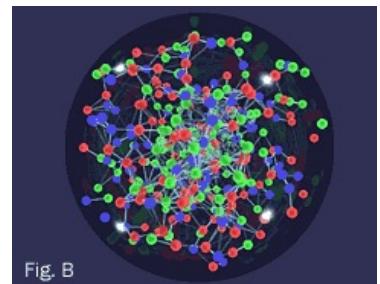


Fig. B

# Discovery of a strongly coupled QGP



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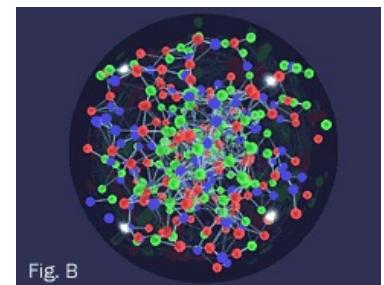
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Strongly coupled like a *liquid*, instead of gas



# Discovery of a strongly coupled QGP



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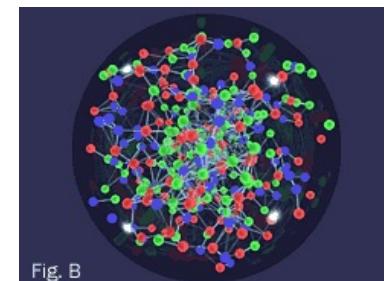
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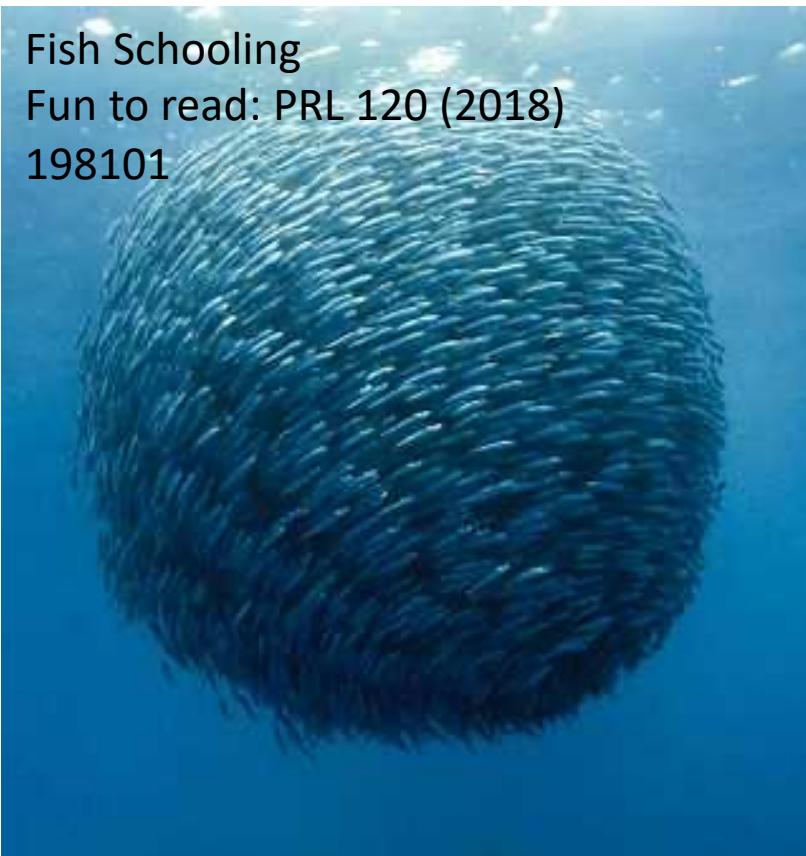
*Important evidence from collectivity*



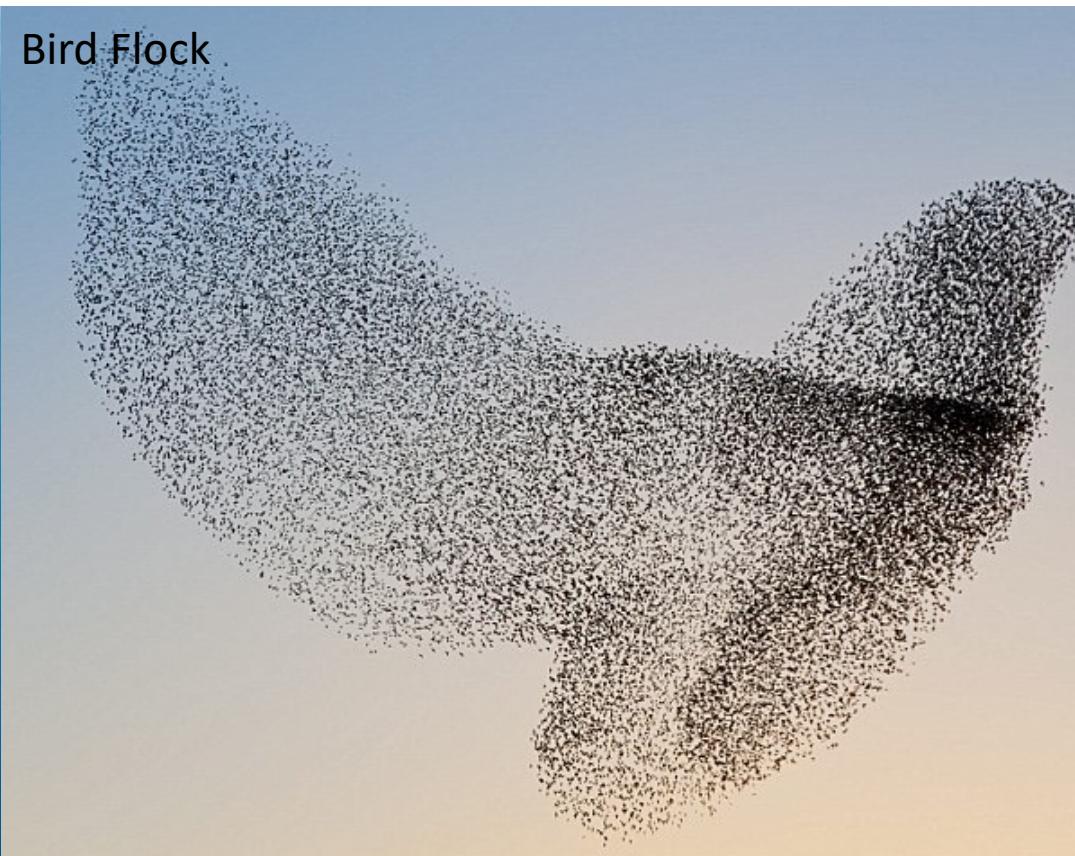
# Collectivity

Fish Schooling

Fun to read: PRL 120 (2018)  
198101



Bird Flock

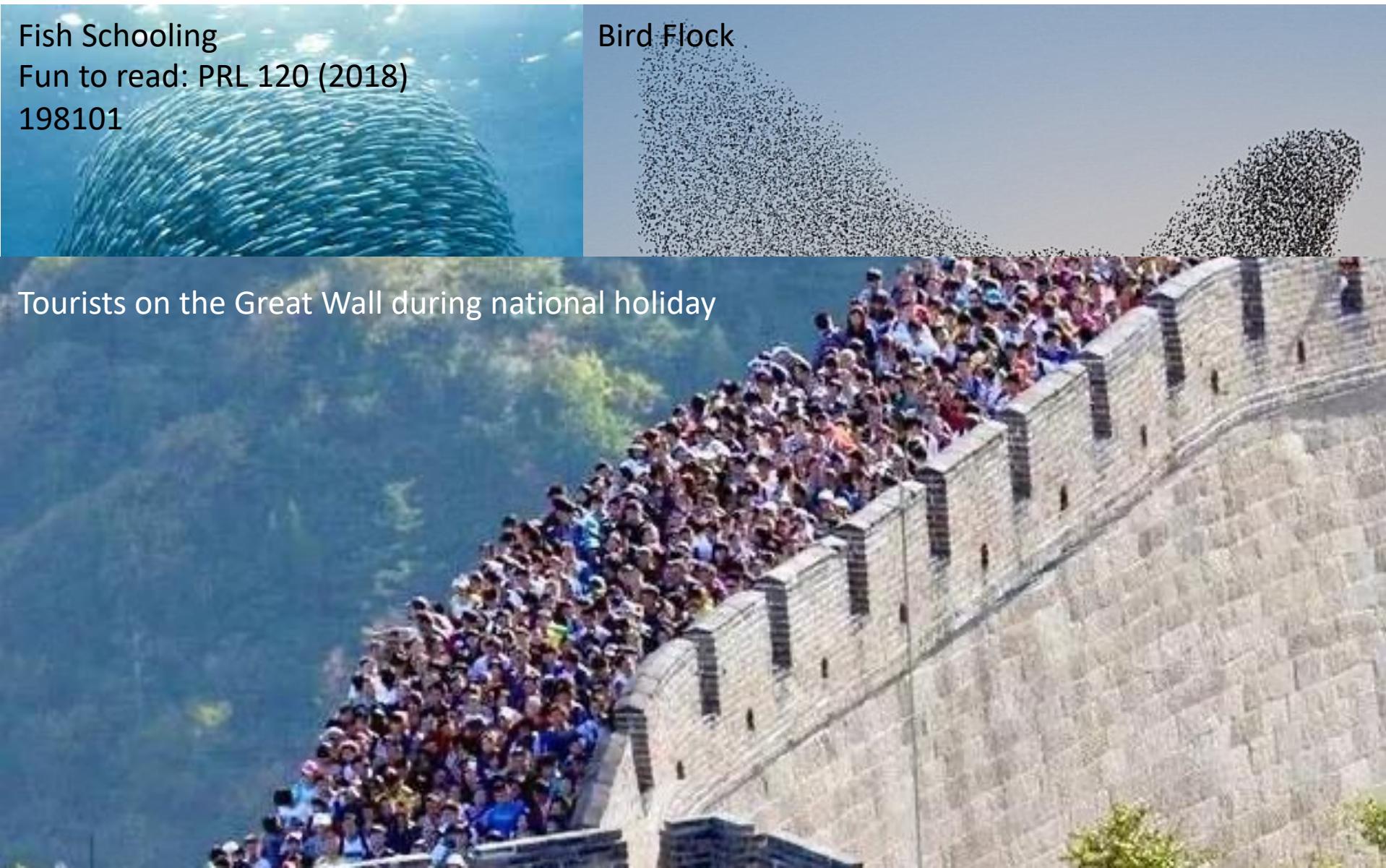


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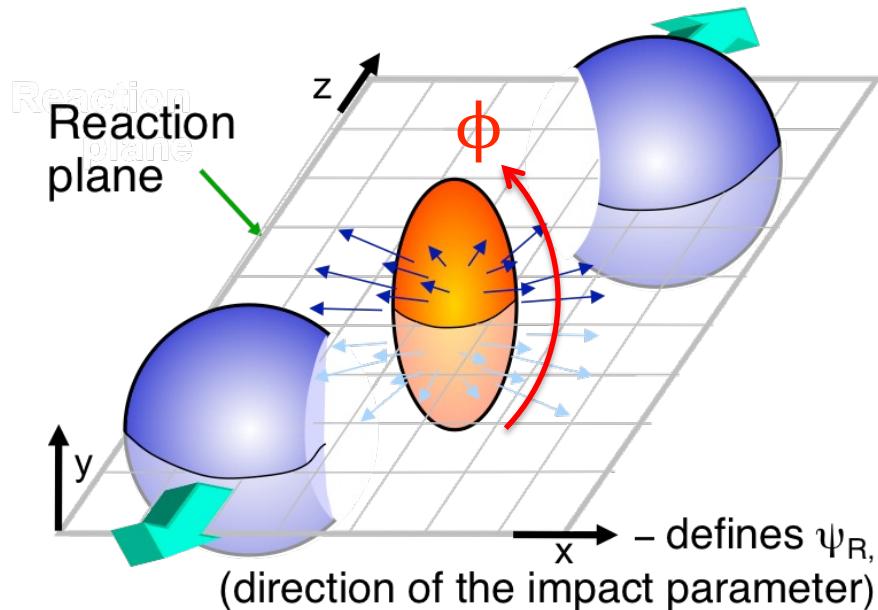
Bird Flock

Tourists on the Great Wall during national holiday

**Group of objects interact with each other frequently and move as a whole**

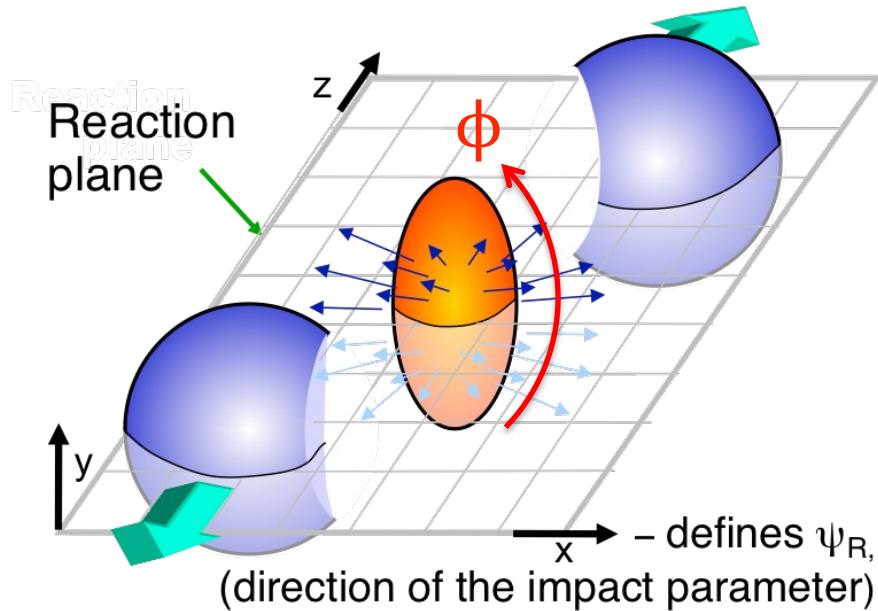
# Collectivity – Evidence of fluidity

## Off-center AA collision



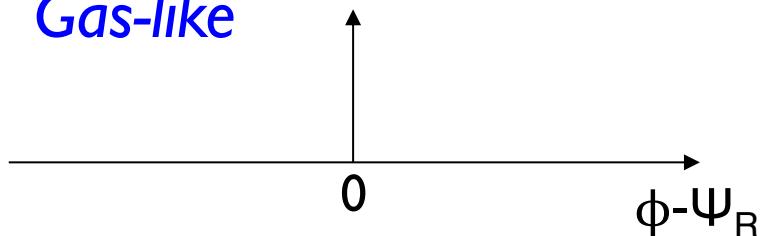
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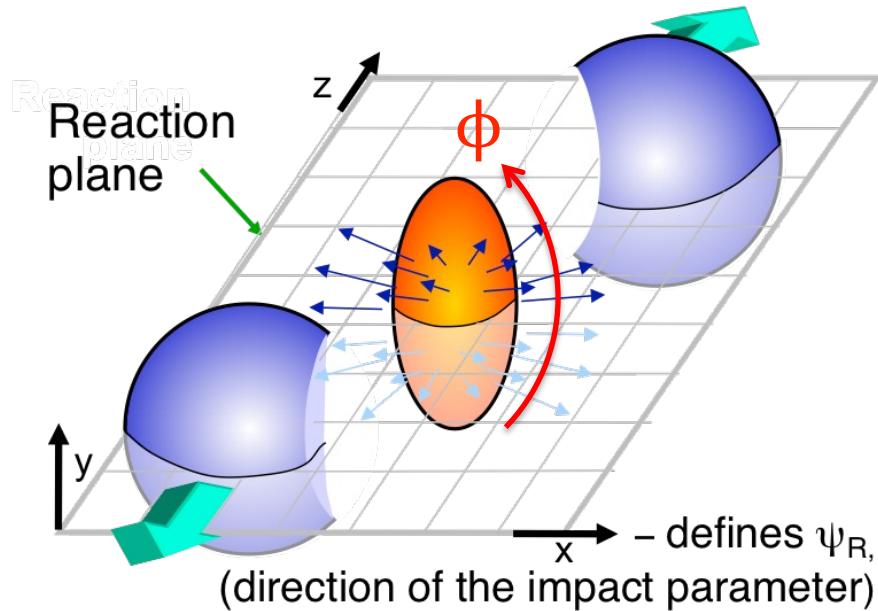
## Momentum anisotropy

*Gas-like*

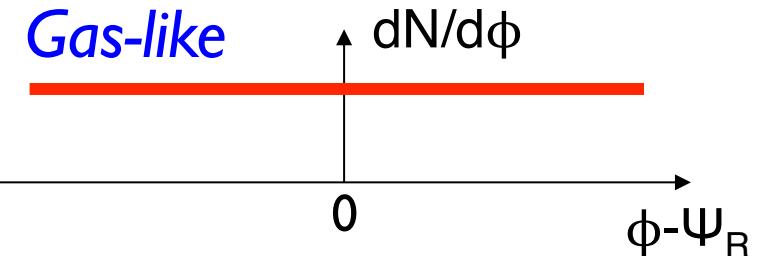


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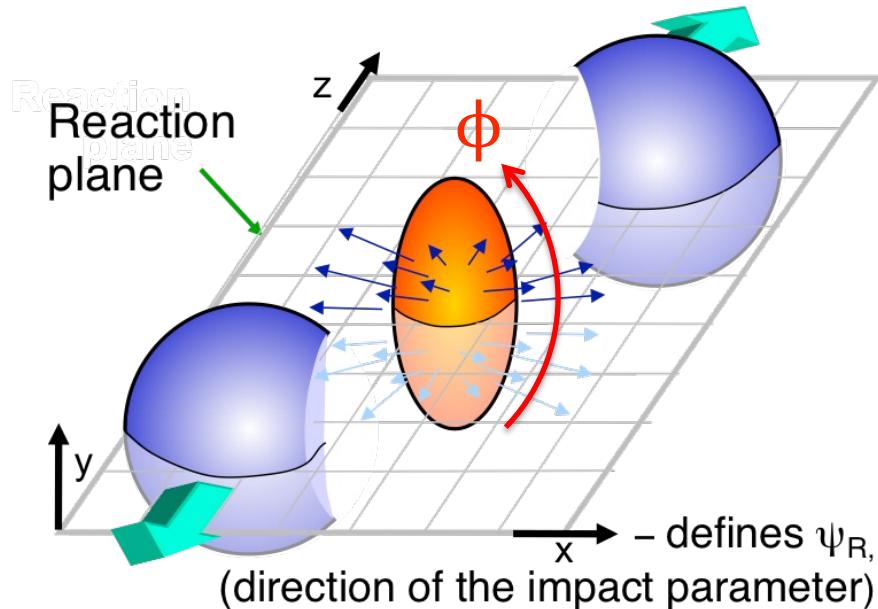


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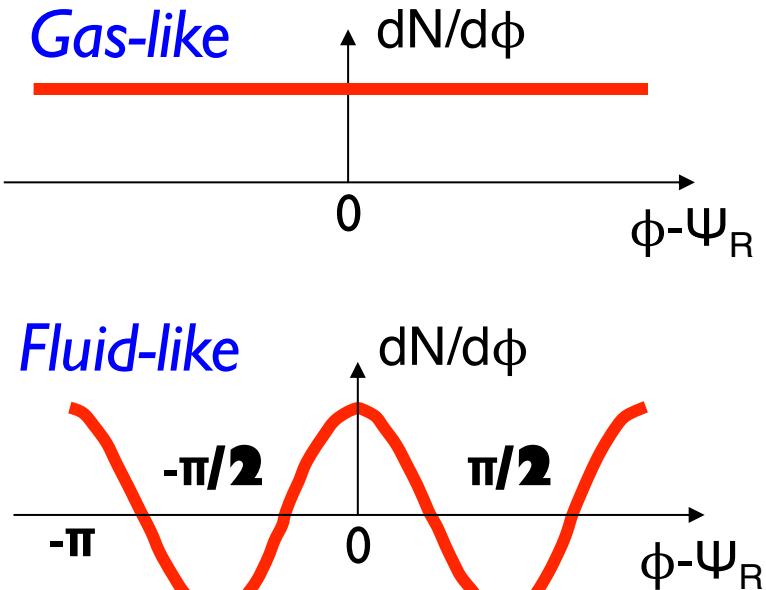


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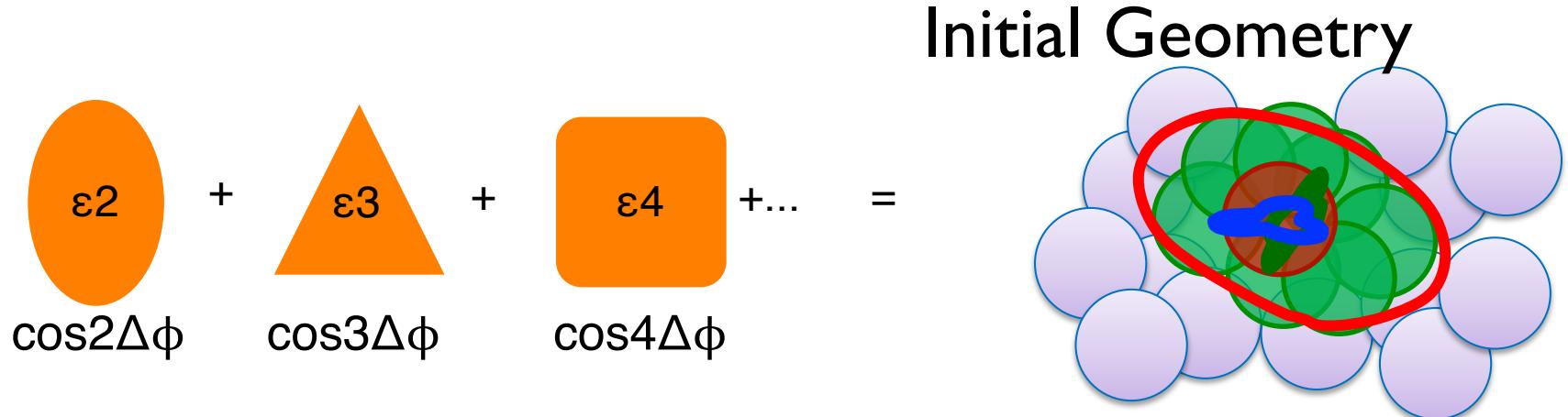
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## Momentum anisotropy



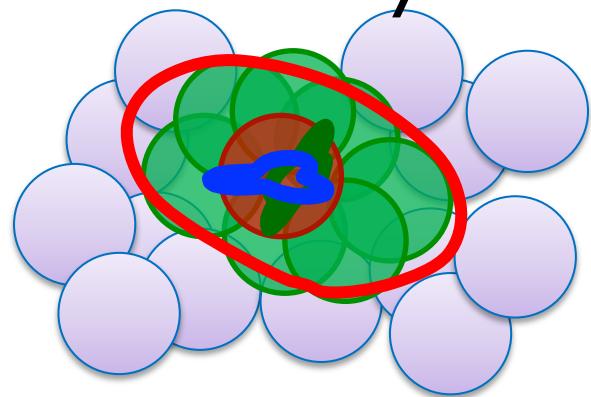
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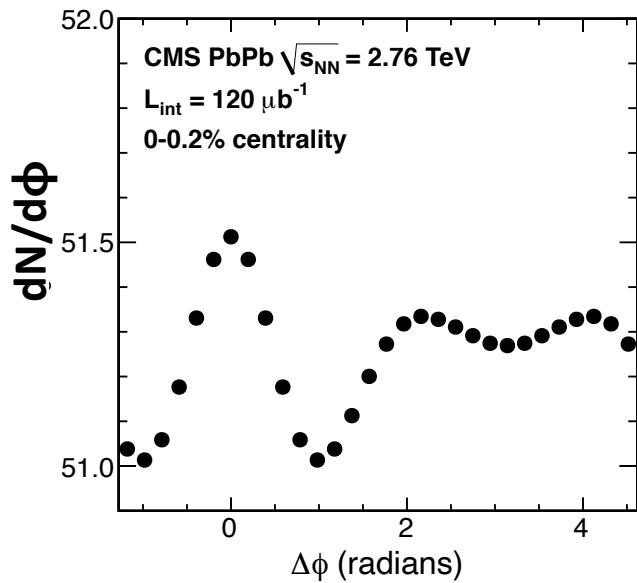
# Collectivity – Evidence of fluidity

$$\varepsilon_2 + \varepsilon_3 + \varepsilon_4 + \dots = \cos 2\Delta\phi + \cos 3\Delta\phi + \cos 4\Delta\phi$$

Initial Geometry



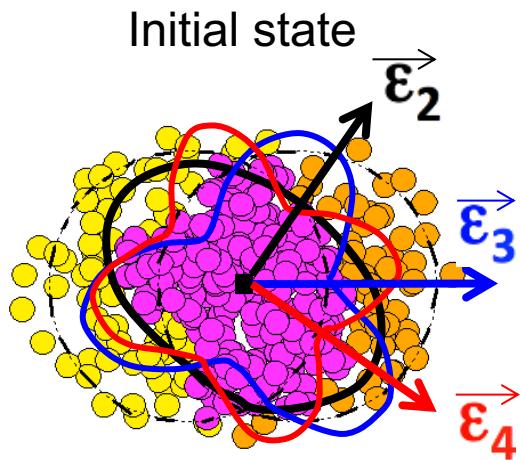
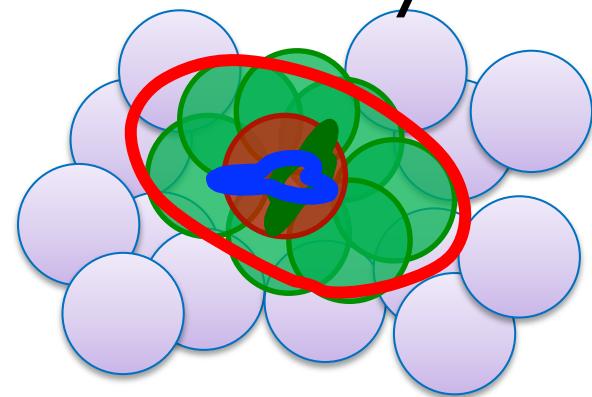
Particle distribution



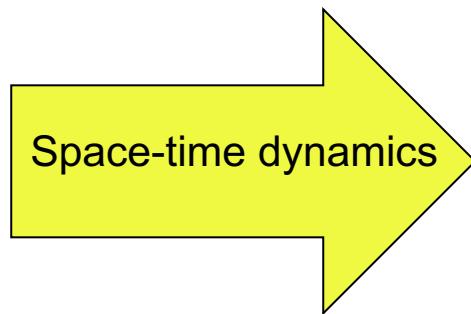
# Collectivity – Initial to final

$$\varepsilon_2 + \varepsilon_3 + \varepsilon_4 + \dots = \cos 2\Delta\phi + \cos 3\Delta\phi + \cos 4\Delta\phi$$

## Initial Geometry

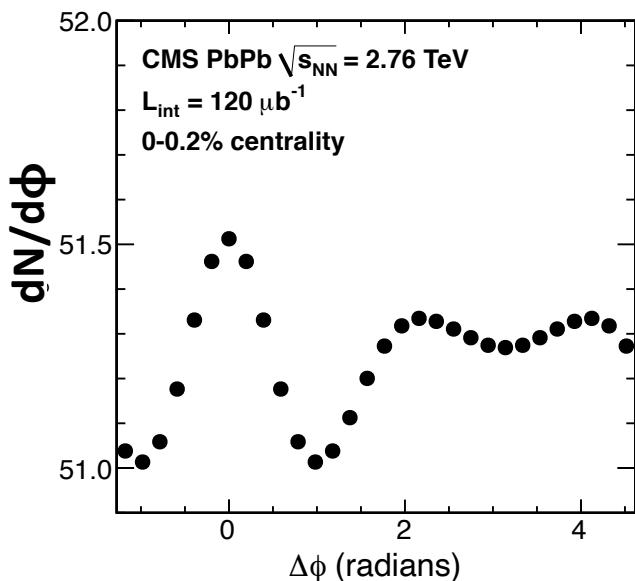


## Hydro-response



$$\vec{\epsilon}_n \equiv \epsilon_n e^{in\Phi_n^*} \equiv -\frac{\langle r^n e^{in\phi} \rangle}{\langle r^n \rangle}$$

## Particle distribution



# Brief intro to hydrodynamics

ISBN: 9781108483681

arXiv: 1712.05815

Energy-momentum conservation

$$\partial_\mu T^{\mu\nu} = 0$$

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Energy-momentum conservation

$$\partial_\mu T^{\mu\nu} = 0$$

Ideal hydro: System always in local equilibrium

$$T^{\mu\nu} = (\epsilon + P)u^\mu u^\nu - P g^{\mu\nu}$$

Hydro response controlled by QCD Equation of State  $P(\epsilon)$

# Brief intro to hydrodynamics

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Energy-momentum conservation

$$\partial_\mu T^{\mu\nu} = 0$$

Viscous hydro: Including near-equilibrium corrections

$$T^{\mu\nu} = \epsilon u^\mu u^\nu - (P + \Pi)\Delta^{\mu\nu} + \pi^{\mu\nu}$$

↗ Bulk Pressure      ↗ Shear Tensor

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Bulk Pressure      Shear Tensor

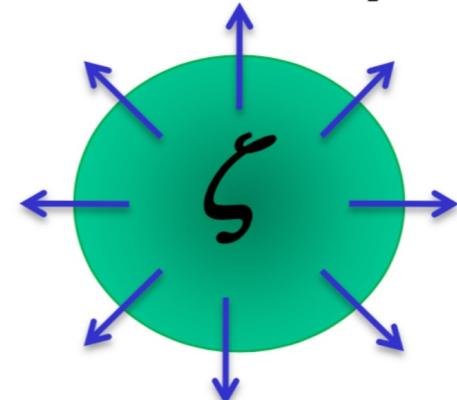
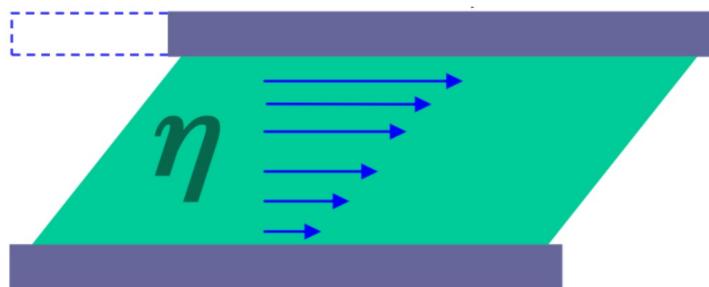
With 1<sup>st</sup> order gradient expansion

$$\pi^{\mu\nu} = -\eta \sigma^{\mu\nu}$$

$\eta$ : Shear viscosity

$$\Pi = -\zeta \nabla \frac{1}{\lambda} u^\lambda$$

$\zeta$ : Bulk viscosity



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Bulk Pressure      Shear Tensor

With 2<sup>nd</sup> order gradient expansion

$$\begin{aligned} \pi^{\mu\nu} &= -\eta \sigma^{\mu\nu} + \eta \tau_\pi \left[ \langle D\sigma^{\mu\nu} \rangle + \frac{\nabla_\lambda^\perp u^\lambda}{3} \sigma^{\mu\nu} \right] + \kappa [R^{\langle\mu\nu\rangle} - 2u_\lambda u_\rho R^{\lambda\langle\mu\nu\rangle\rho}] + \lambda_1 \sigma^{\langle\mu}_\lambda \sigma^{\nu\rangle\lambda} \\ &\quad + \lambda_2 \sigma^{\langle\mu}_\lambda \Omega^{\nu\rangle\lambda} + \lambda_3 \Omega^{\langle\mu}_\lambda \Omega^{\nu\rangle\lambda} + \kappa^* 2u_\lambda u_\rho R^{\lambda\langle\mu\nu\rangle\rho} + \eta \tau_\pi^* \frac{\nabla_\lambda^\perp u^\lambda}{3} \sigma^{\mu\nu} + \bar{\lambda}_4 \nabla_\perp^{\langle\mu} \ln \epsilon \nabla_\perp^{\nu\rangle} \ln \epsilon \\ \Pi &= -\zeta (\nabla_\lambda^\perp u^\lambda) + \zeta \tau_\Pi D (\nabla_\lambda^\perp u^\lambda) + \xi_1 \sigma^{\mu\nu} \sigma_{\mu\nu} + \xi_2 (\nabla_\lambda^\perp u^\lambda)^2 \\ &\quad + \xi_3 \Omega^{\mu\nu} \Omega_{\mu\nu} + \bar{\xi}_4 \nabla_\mu^\perp \ln \epsilon \nabla_\perp^\mu \ln \epsilon + \xi_5 R + \xi_6 u^\lambda u^\rho R_{\lambda\rho}. \end{aligned}$$

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ab.initio calc. for QGP not easy, relies on **model/data** comparison

# Collectivity – how to measure

- Single particle distribution

$$\frac{dN}{d\phi} = \frac{N}{2\pi} \left[ 1 + 2 \sum_n v_n \cos n(\phi - \Phi_n) \right]$$

Event Plane  
Anisotropic Flow

# Collectivity – how to measure

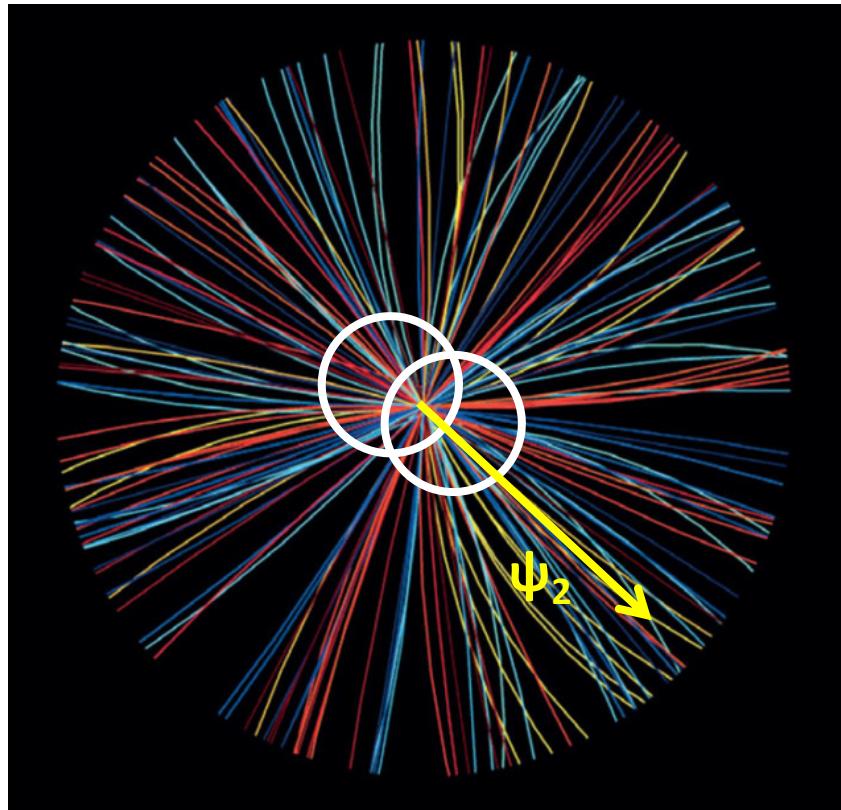
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Event Plane

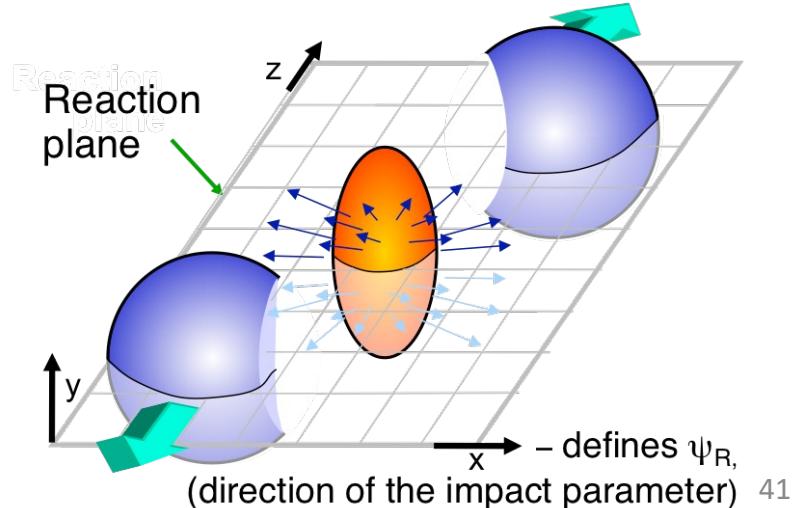
Anisotropic Flow

- Event Plane method



Event Plane from emitted particles

$$\psi_n = \frac{1}{n} \tan^{-1} \frac{\sum_i \sin(n\phi_i)}{\sum_i \cos(n\phi_i)}$$



– defines  $\psi_R$ ,  
(direction of the impact parameter) 41

# Collectivity – how to measure

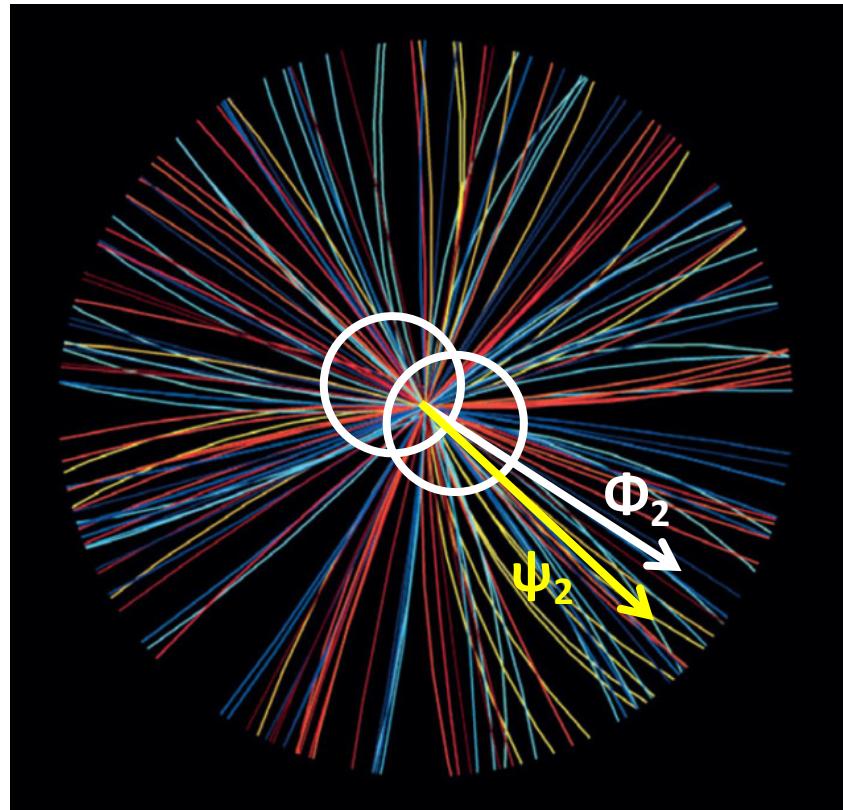
- Single particle distribution

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Event Plane

Anisotropic Flow

- Event Plane method



Event Plane from emitted particles

$$\psi_n = \frac{1}{n} \tan^{-1} \frac{\sum_i \sin(n\phi_i)}{\sum_i \cos(n\phi_i)}$$

Event Plane Resolution

$$\mathcal{R}_n \propto \cos n(\Phi_n - \psi_n)$$

$$v_n = v_n^{obs} / \mathcal{R}_n$$

$\mathcal{R}_n$  cannot be perfectly determined!

# Collectivity – how to measure

- Particle pair distribution

$$V_{n\Delta,ab} = v_{n,a}v_{n,b} \text{ when } \Phi_n^a = \Phi_n^b$$

$$\frac{dN^{pair}}{d\Delta\phi} = \frac{N^{pair}}{2\pi} \left[ 1 + 2 \sum_n V_{n\Delta,ab} \cos n(\phi_a - \phi_b) \right]$$

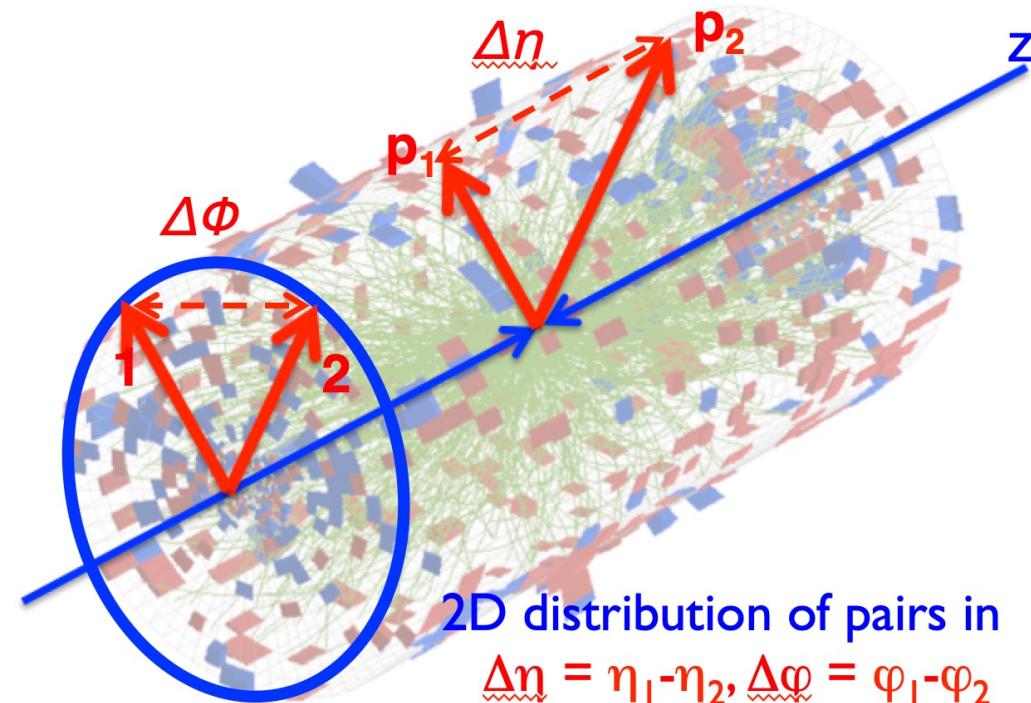
# Collectivity – how to measure

- Particle pair distribution

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- Two particle correlation method



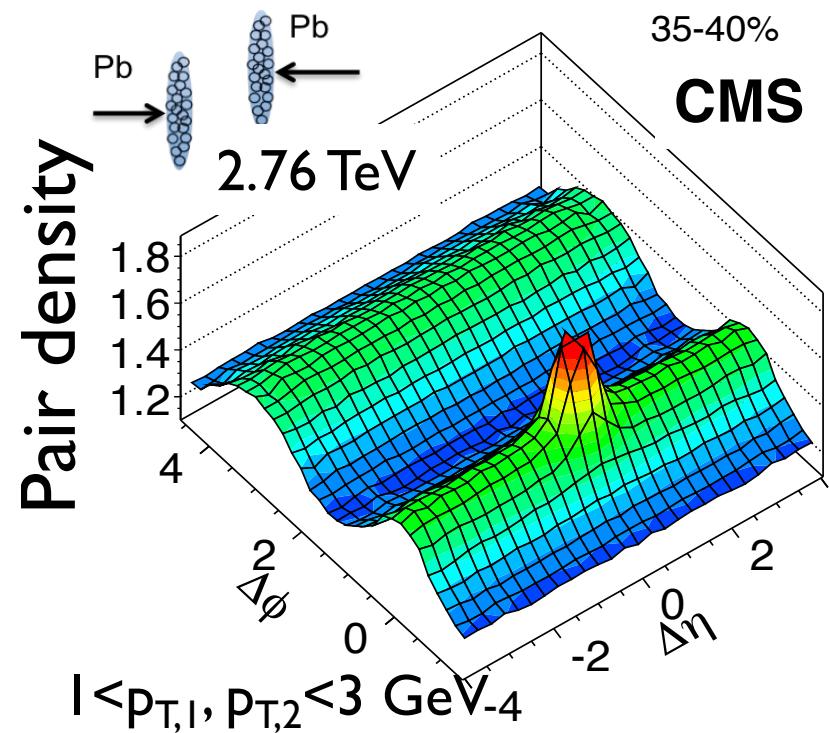
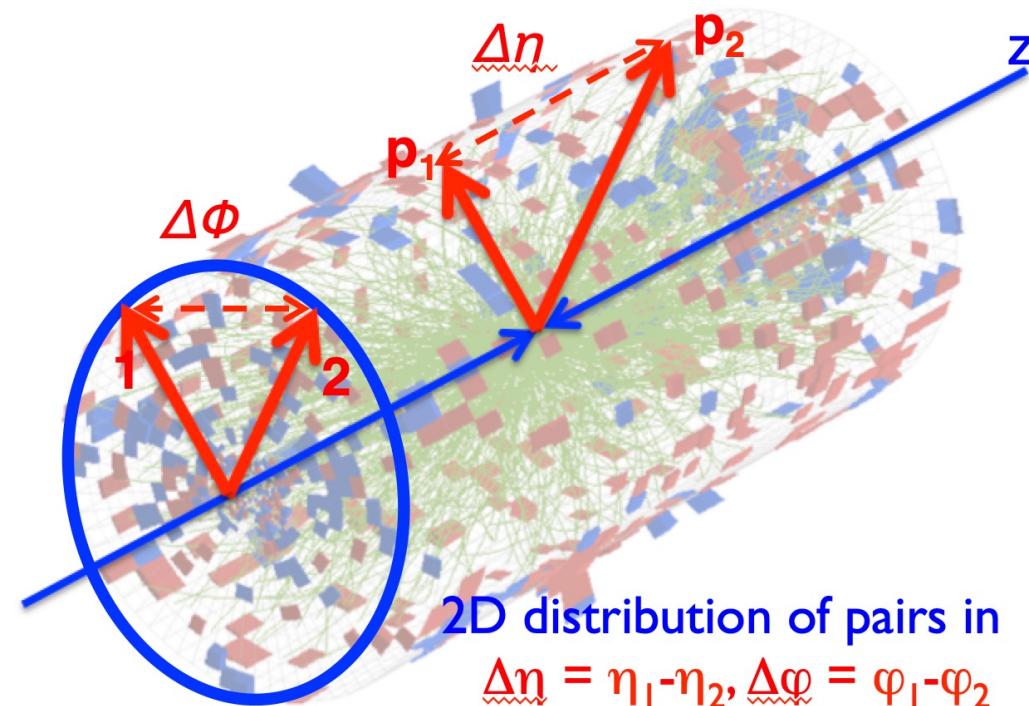
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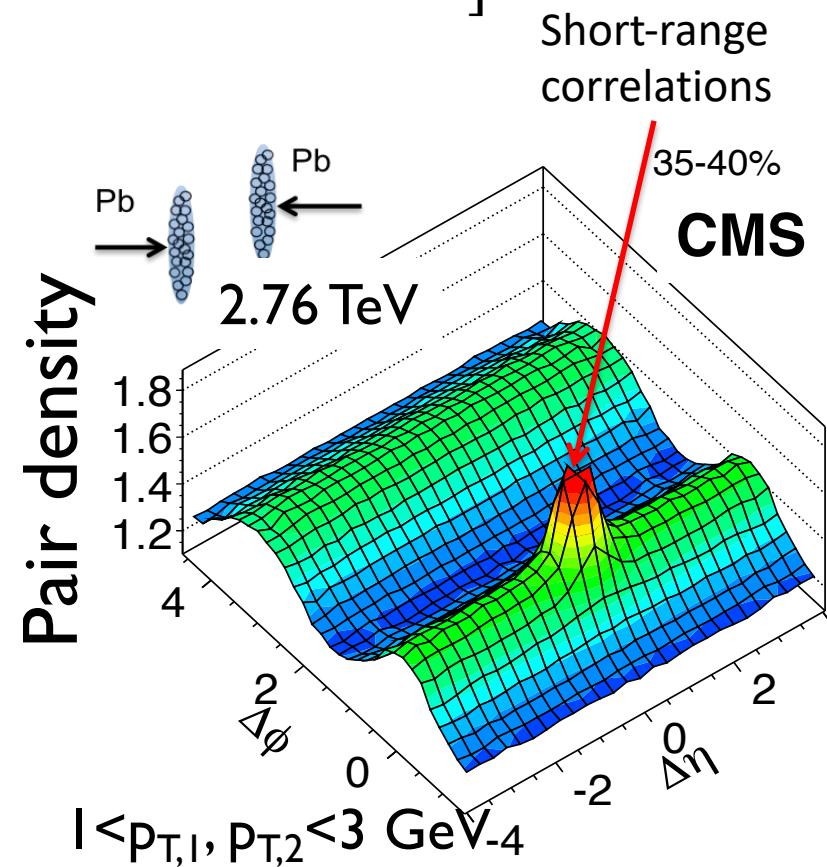
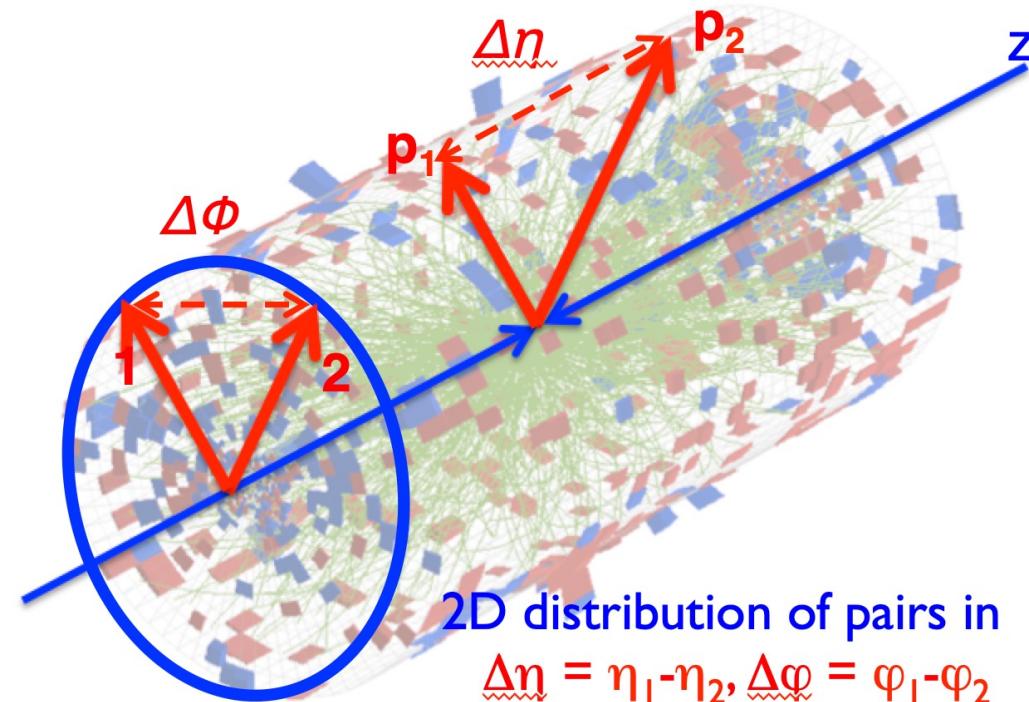
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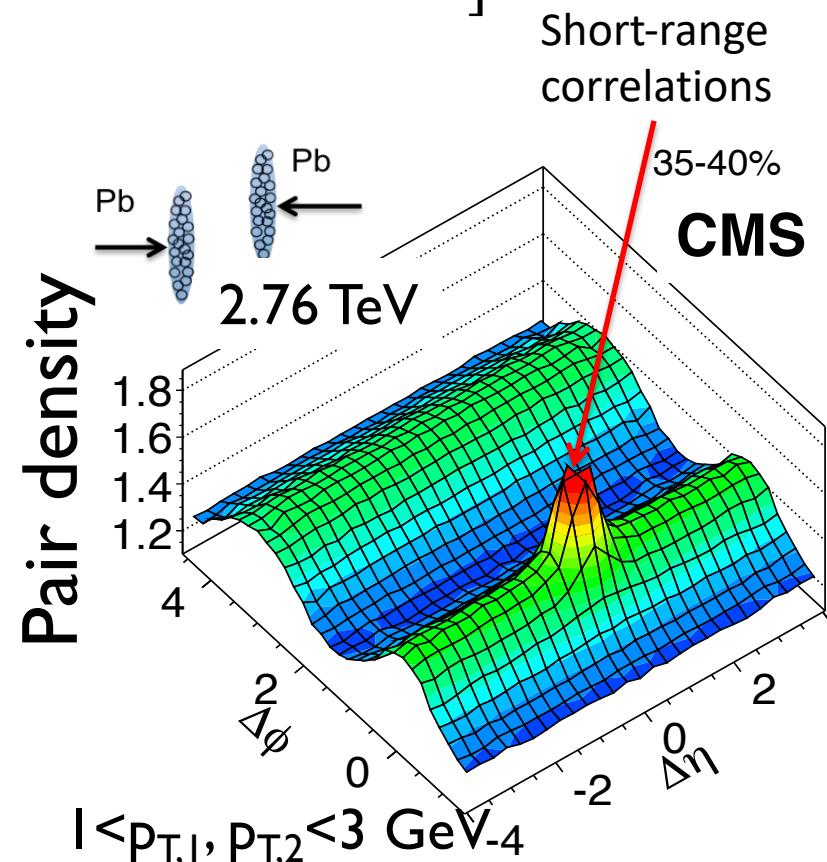
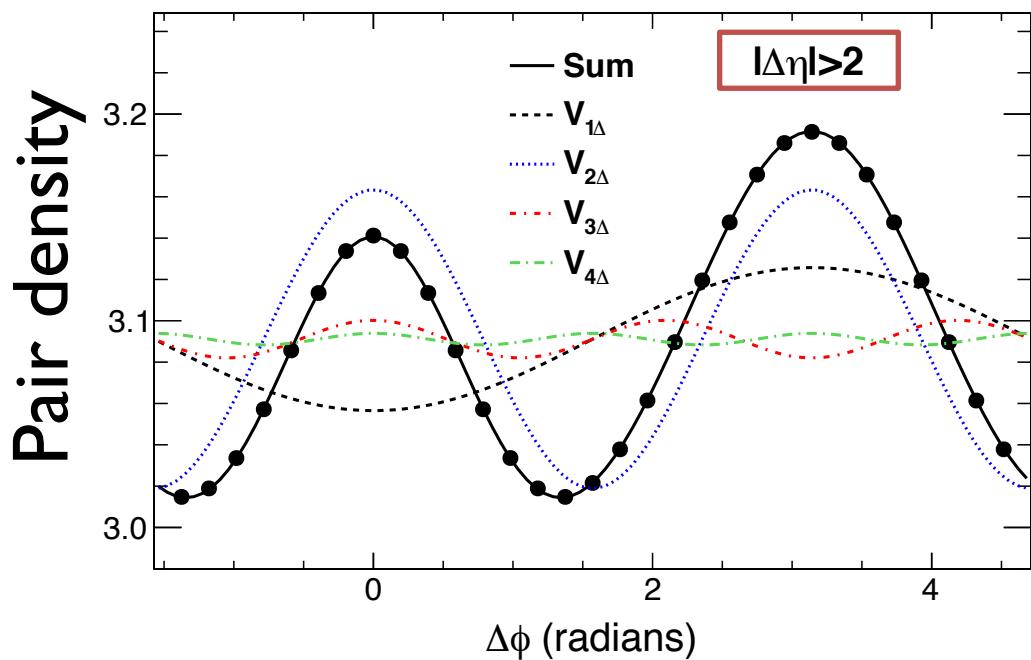
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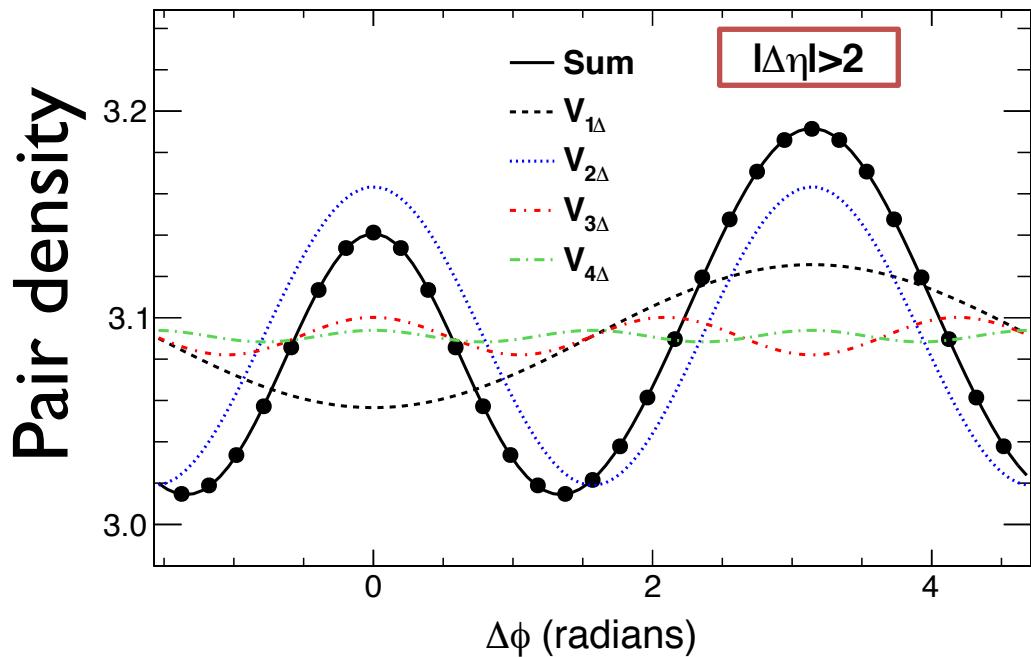
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- Two particle correlation method



Fourier analysis:

$$\frac{dN^{pair}}{d\Delta\phi} \sim 1 + 2V_{1\Delta} \cos(\Delta\phi) + 2V_{2\Delta} \cos(2\Delta\phi) + 2V_{3\Delta} \cos(3\Delta\phi) + 2V_{4\Delta} \cos(4\Delta\phi) + \dots$$

$$V_{n\Delta} = v_{n,a}v_{n,b}$$

# Collectivity – how to measure

- Multi-particle distribution

$$\frac{dN_1}{d\phi_1} \dots \frac{dN_m}{d\phi_m} \Rightarrow v_{n_1} v_{n_2} \dots v_{n_m} \cos(n_1\phi_1 + n_2\phi_2 + \dots + n_m\phi_m)$$

# Collectivity – how to measure

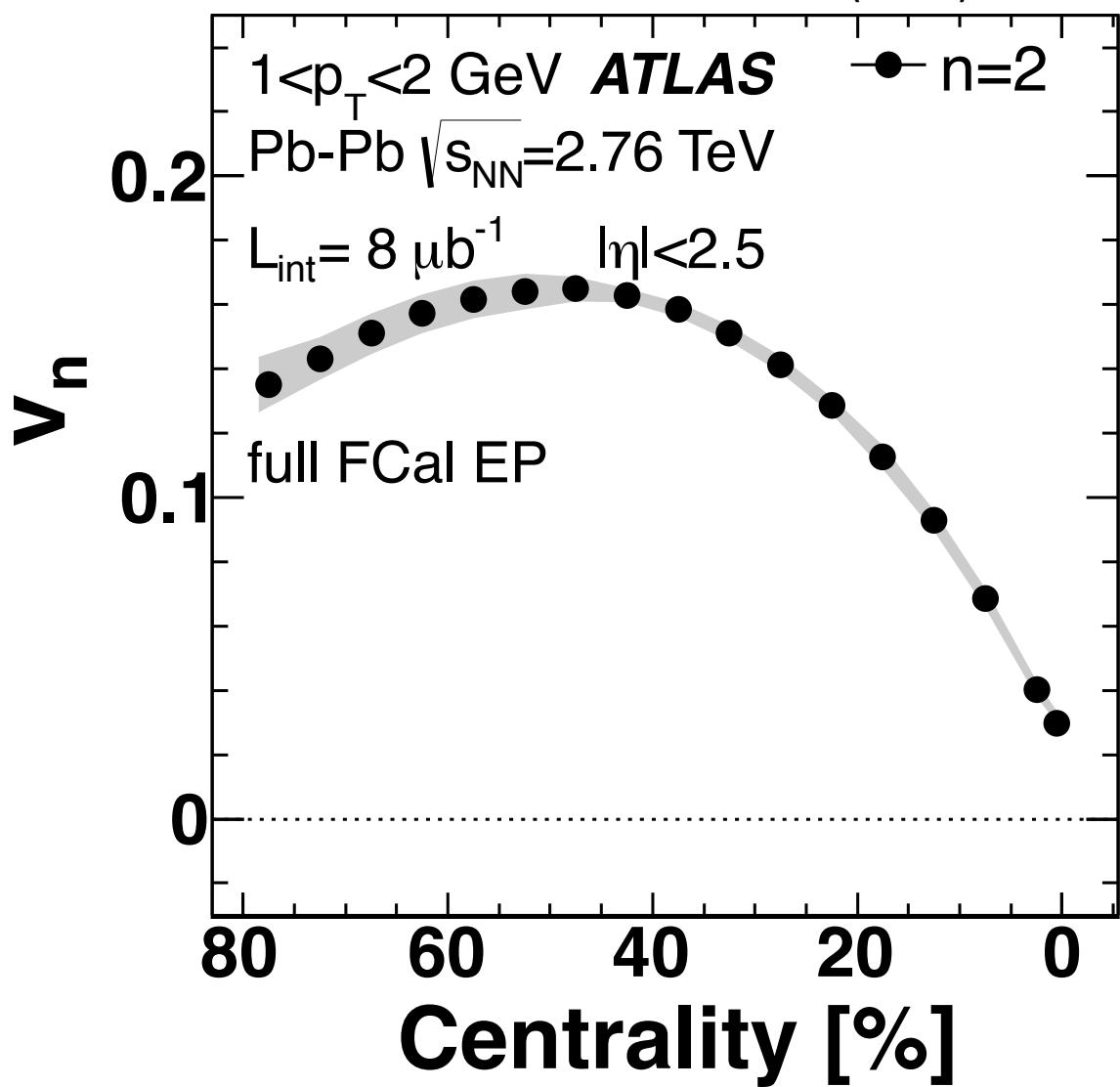
- Multi-particle distribution

$$\frac{dN_1}{d\phi_1} \dots \frac{dN_m}{d\phi_m} \Rightarrow v_{n_1} v_{n_2} \dots v_{n_m} \cos(n_1\phi_1 + n_2\phi_2 + \dots + n_m\phi_m)$$

- Cumulant method
  - PRC 83 (2011) 044913,  $v_n\{m\}$  with multi-particle correlation
  - PRC 89 (2014) 064904, Symmetric Cumulant (*Standard Candles*)
  - PRC 90 (2014) 024905, Asymmetric Cumulant
- $v_n\{m\}$  – Less sensitive to few particle correlation
- SC – Event-by-event correlation between  $v_n$  and  $v_m$
- AC – Initial geometry fluctuation & non-linear mixing between  $v_n, v_m$

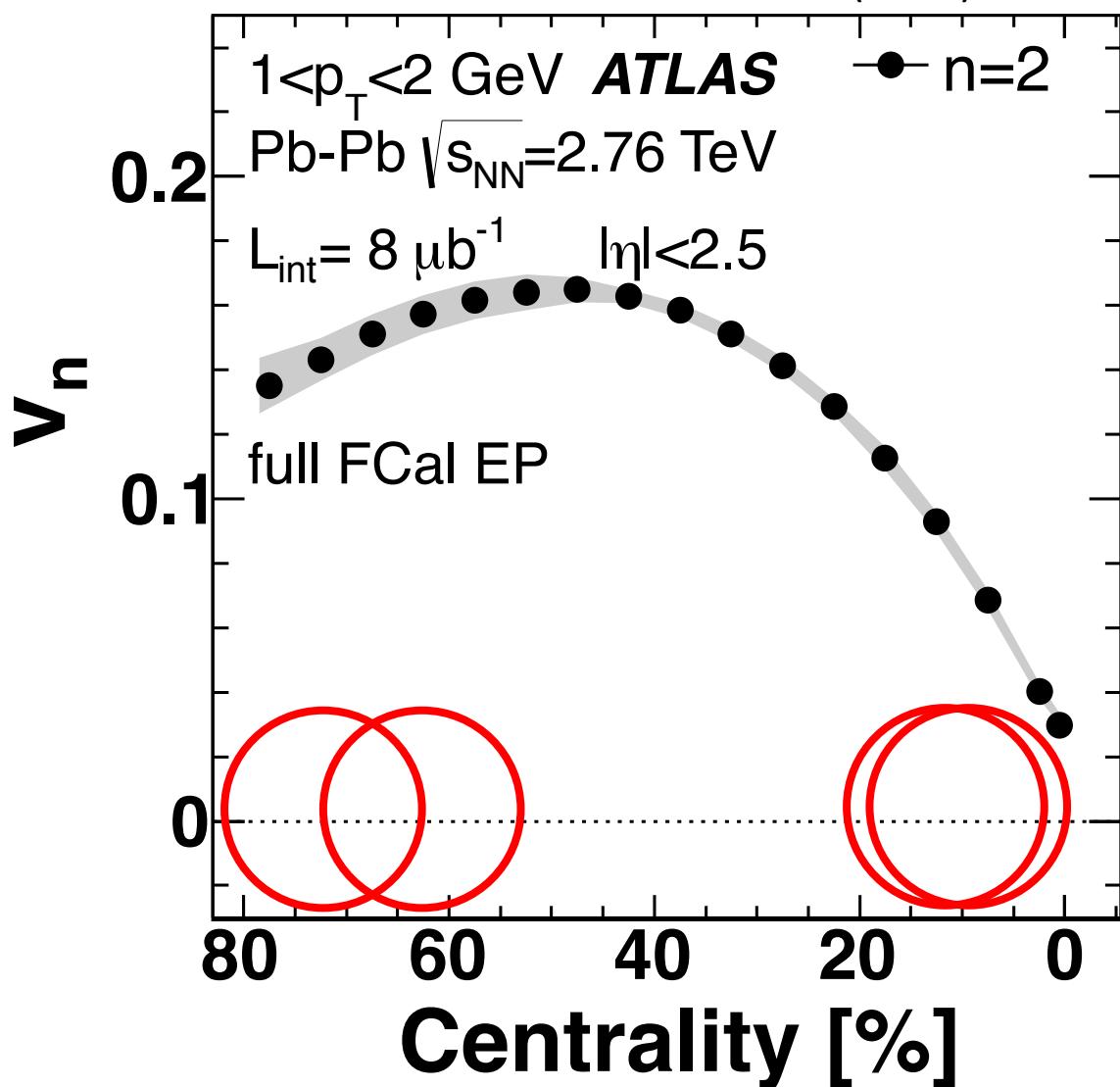
# $v_2$ vs centrality

PRC 86 (2012) 014907



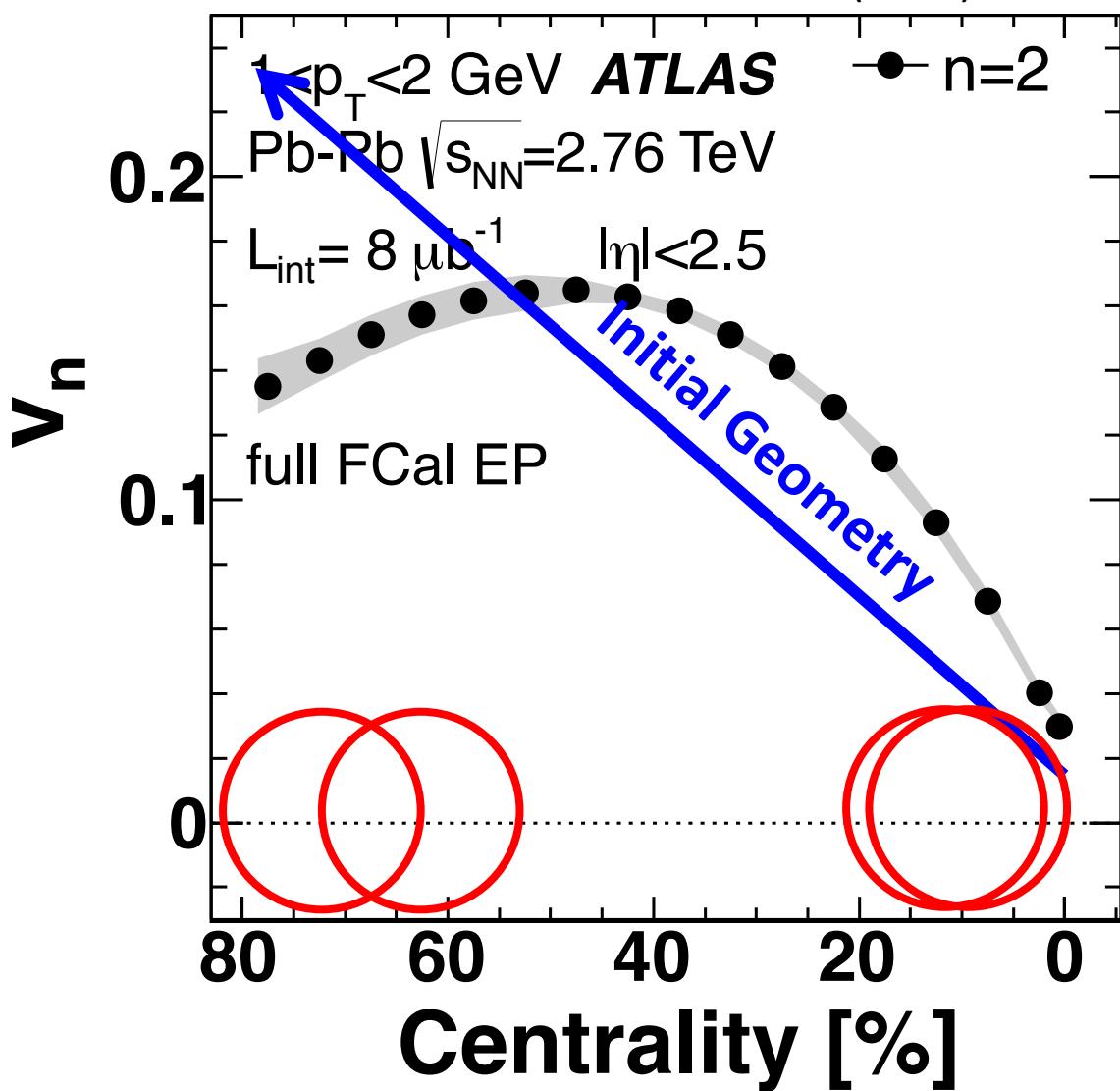
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PRC 86 (2012) 014907



# $v_2$ vs centrality

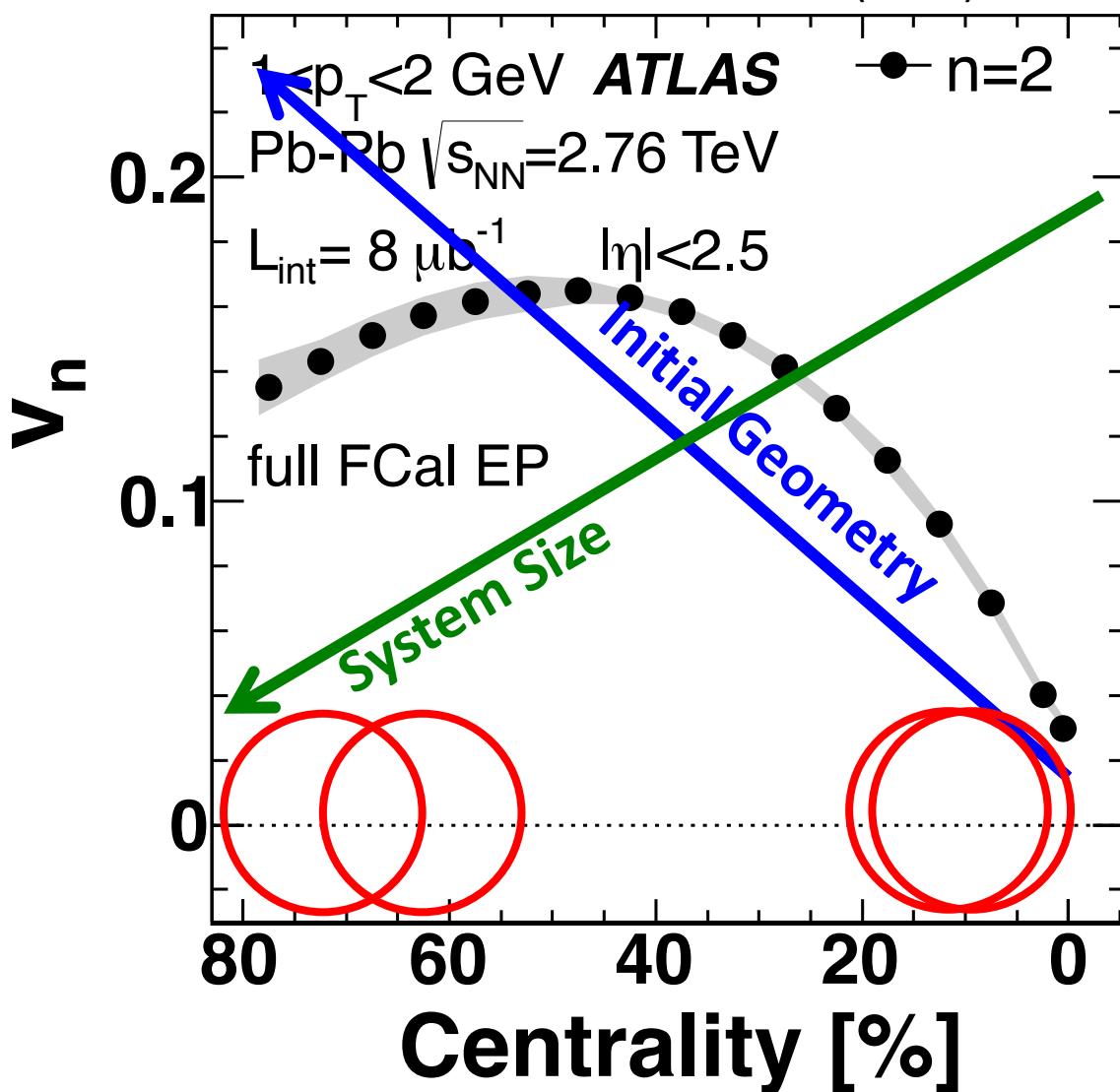
PRC 86 (2012) 014907



Geometry response:  
 $v_n \propto A \varepsilon_n$

# $v_2$ vs centrality

PRC 86 (2012) 014907



Geometry response:

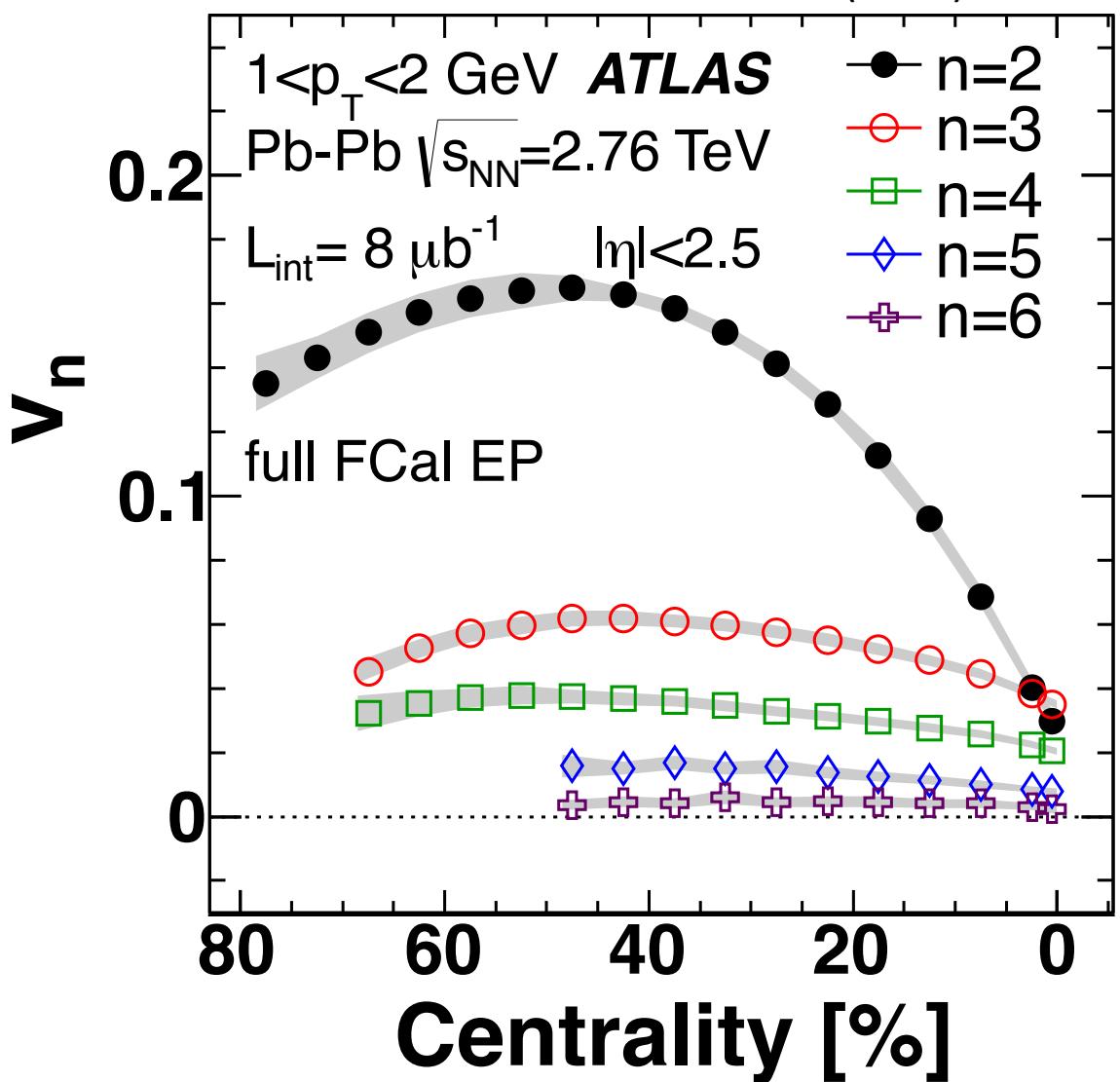
$$v_n \propto A \epsilon_n$$

System Size:

Less interactions  
develop less flow

# $v_n$ vs centrality

PRC 86 (2012) 014907



Geometry response:

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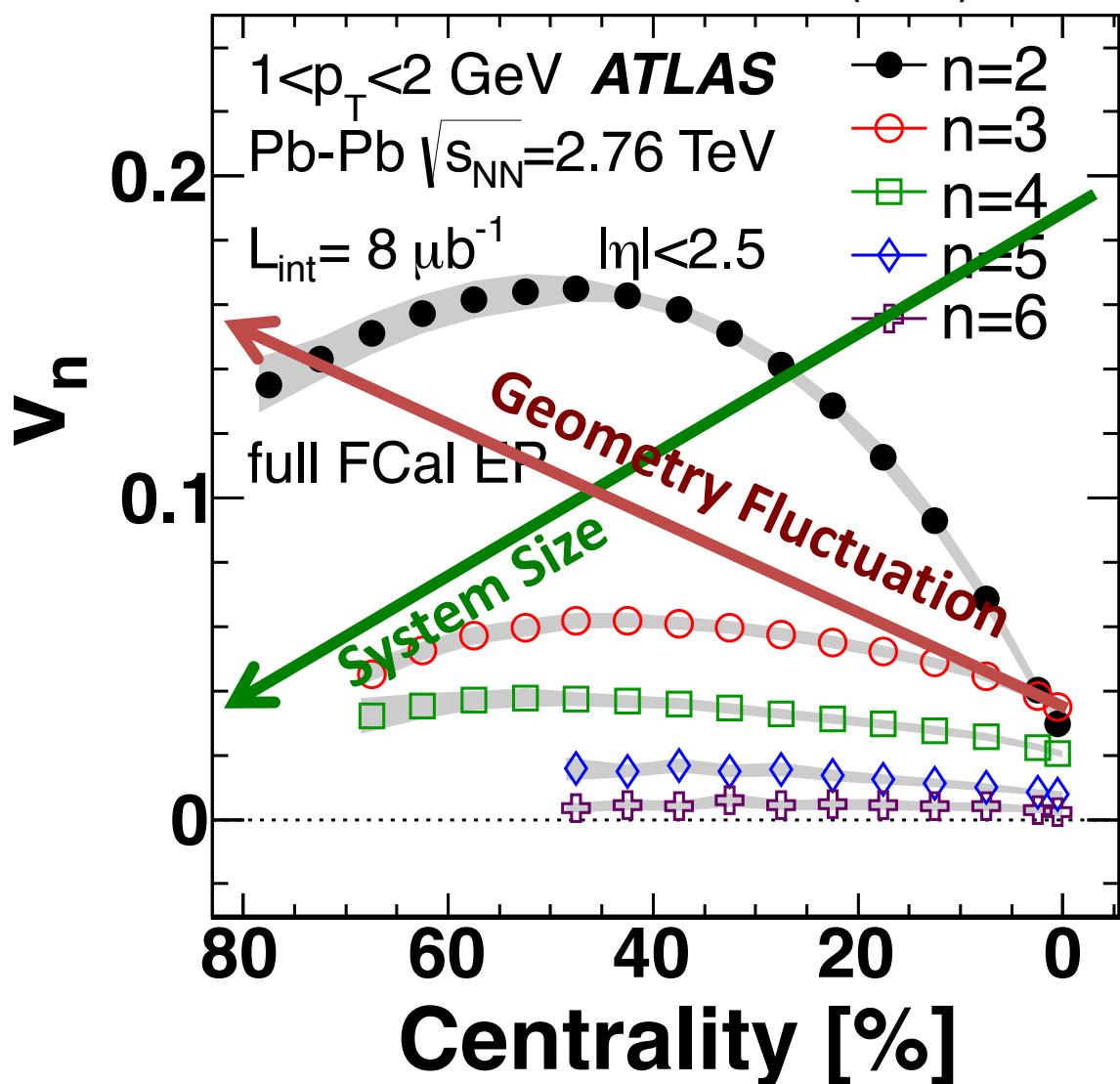
System Size:

Less interactions  
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Eccentricity from  
Geometry Fluctuation

# $v_n$ vs centrality

PRC 86 (2012) 014907



Geometry response:

$$v_n \propto A \epsilon_n$$

System Size:

Less interactions  
develop less flow

Eccentricity from

Geometry Fluctuation:

$$GF \propto 1/N_{par}$$

# $v_n$ vs centrality across systems

PRC 98 (2018) 021902

Constrain on viscosity from acoustic model: viscous attenuation

$$\ln(v_n/\varepsilon_n) \propto -n^2 \left\langle \frac{\eta}{s}(T) \right\rangle \langle N_{ch} \rangle^{-1/3},$$

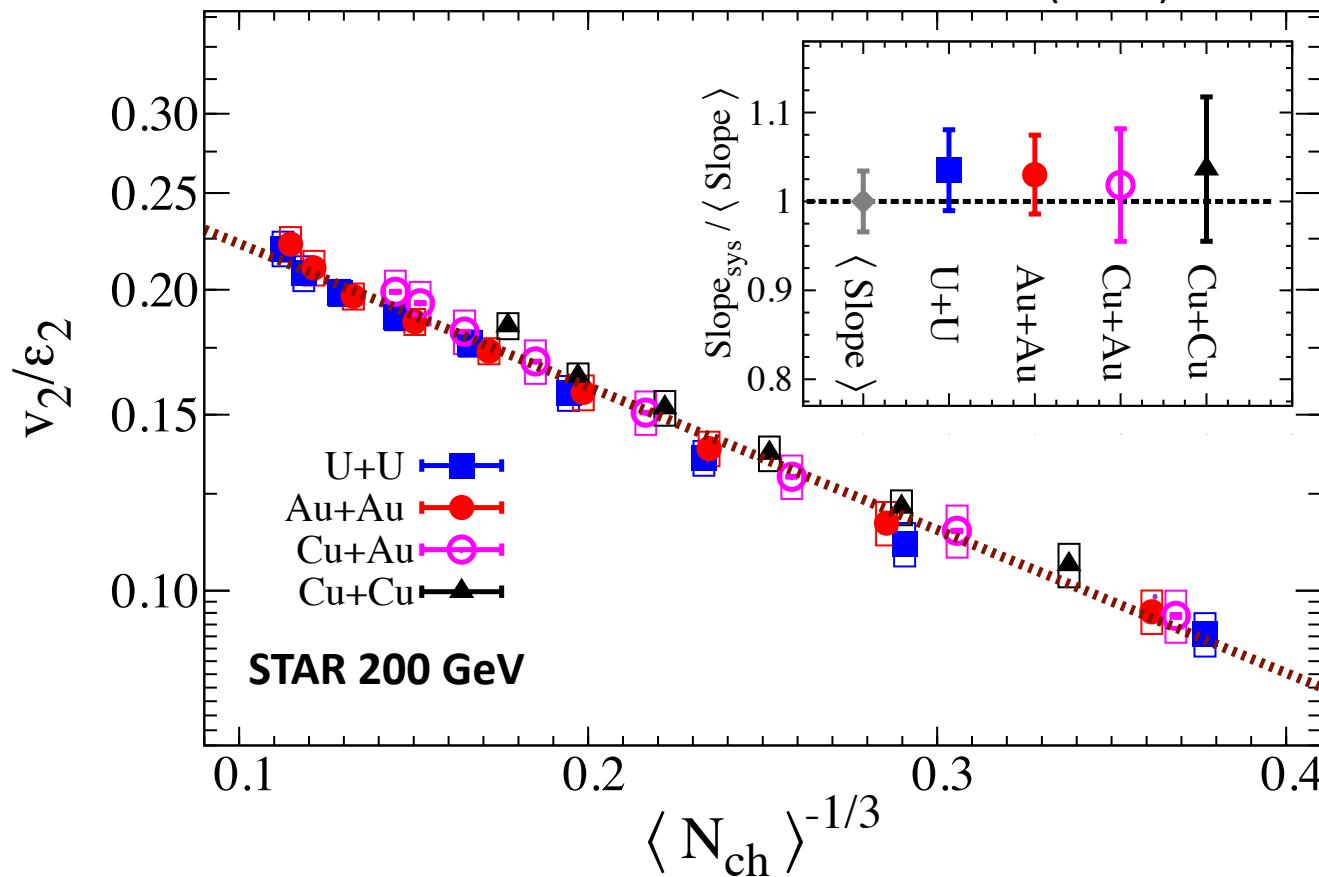
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PRC 98 (2018) 021902

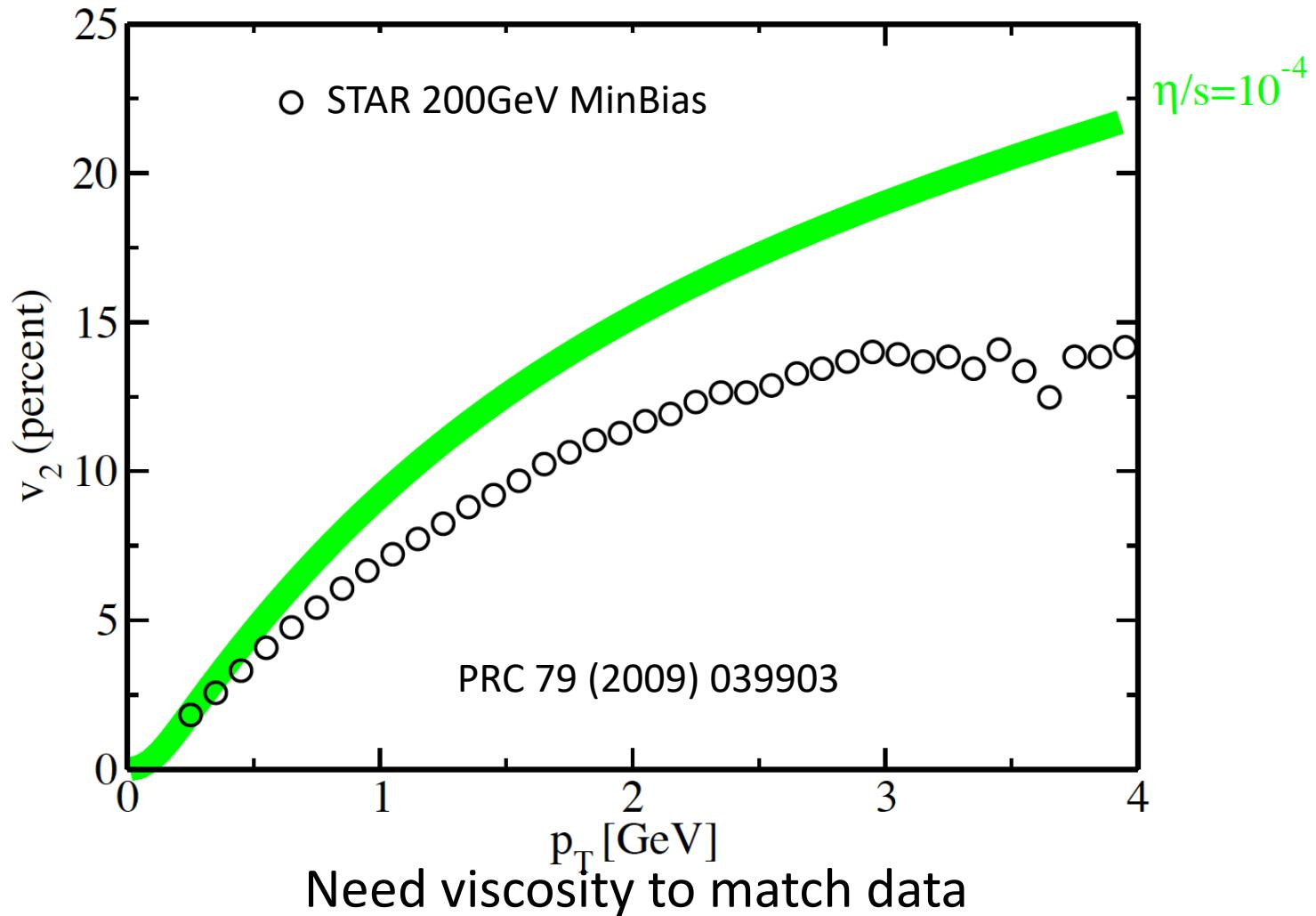
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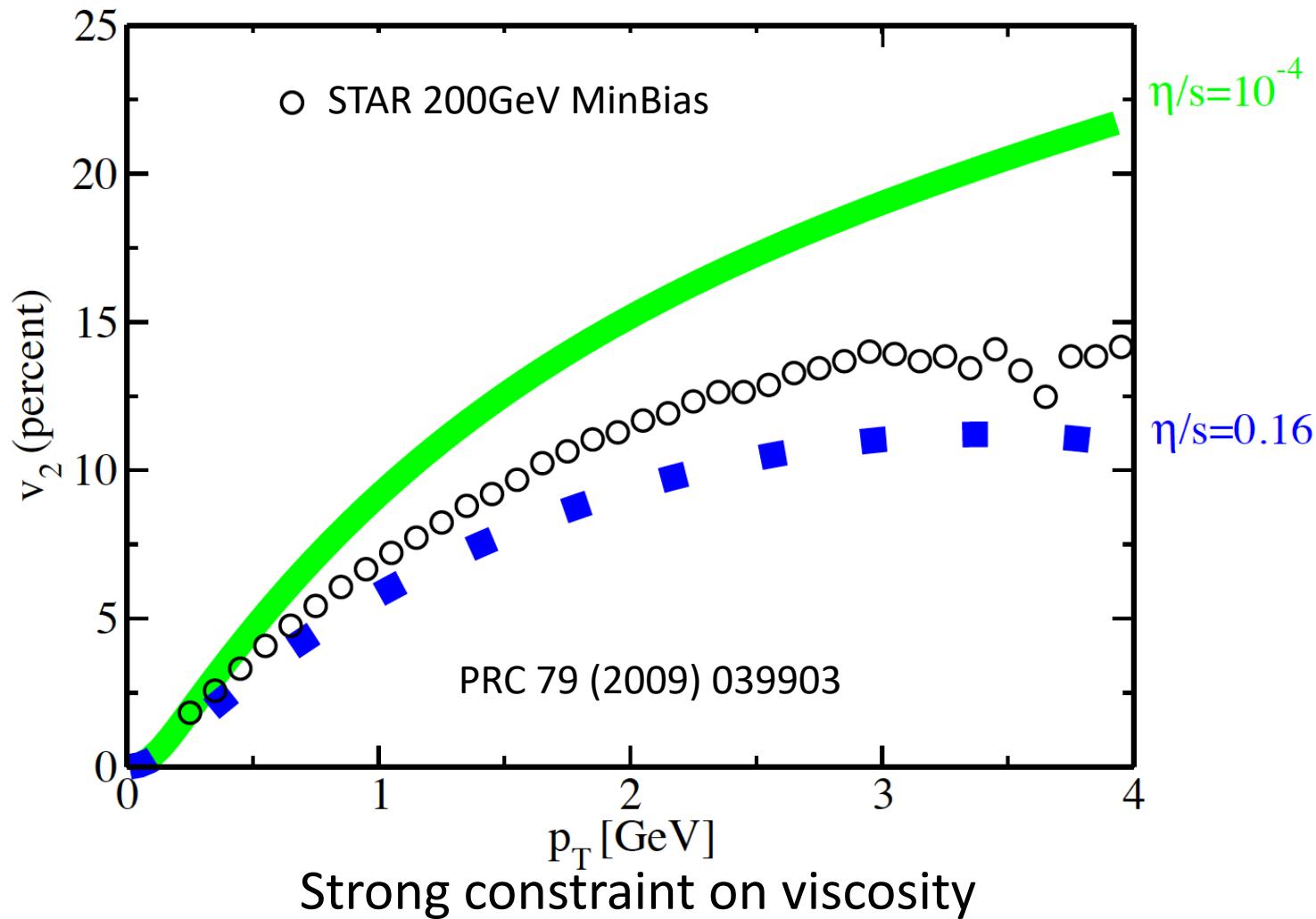
PRL 122 (2019) 172301



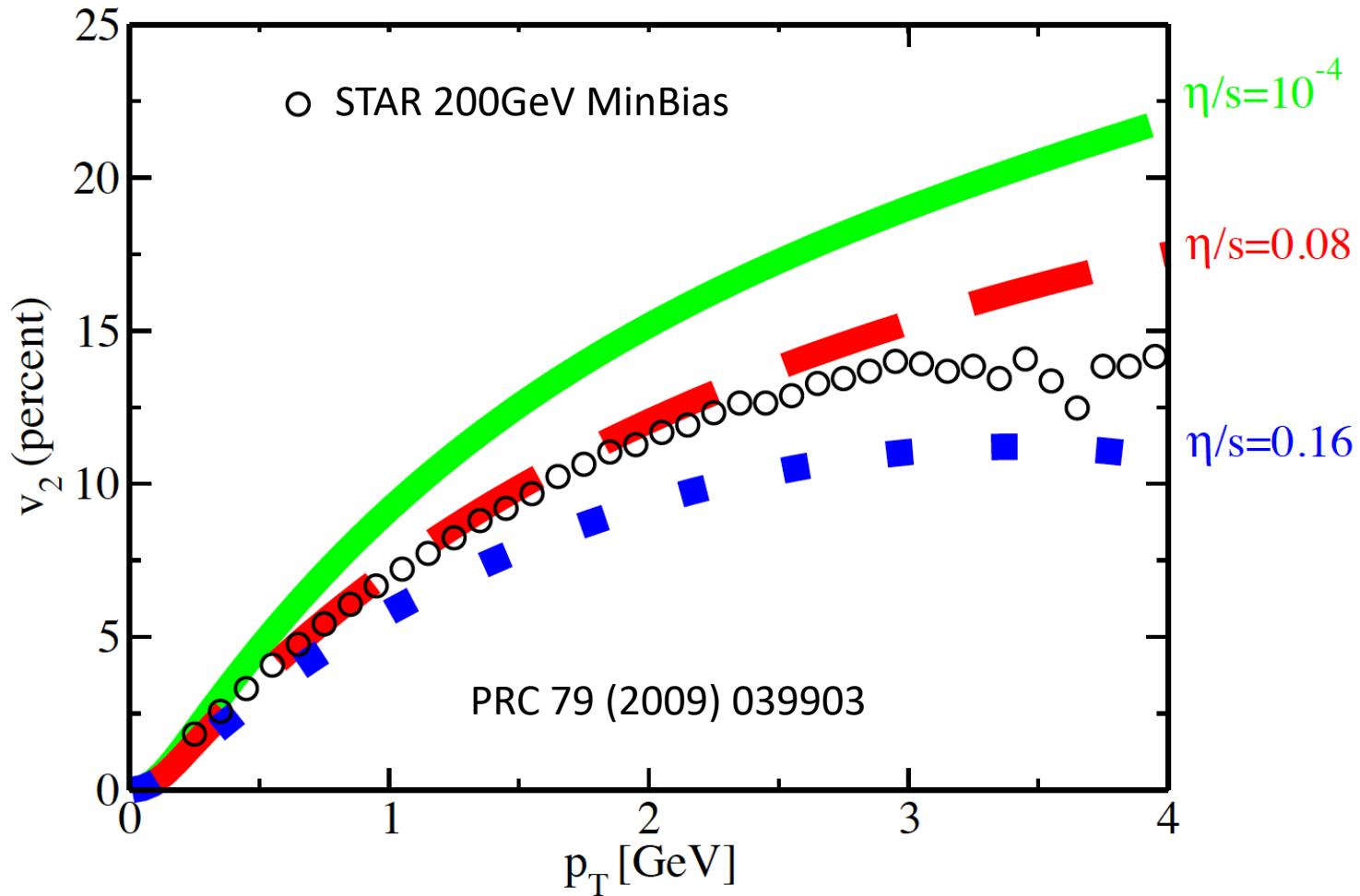
## $v_2$ vs $p_T$ – constrain viscosity



# $v_2$ vs $p_T$ – constrain viscosity



# $v_2$ vs $p_T$ – constrain viscosity

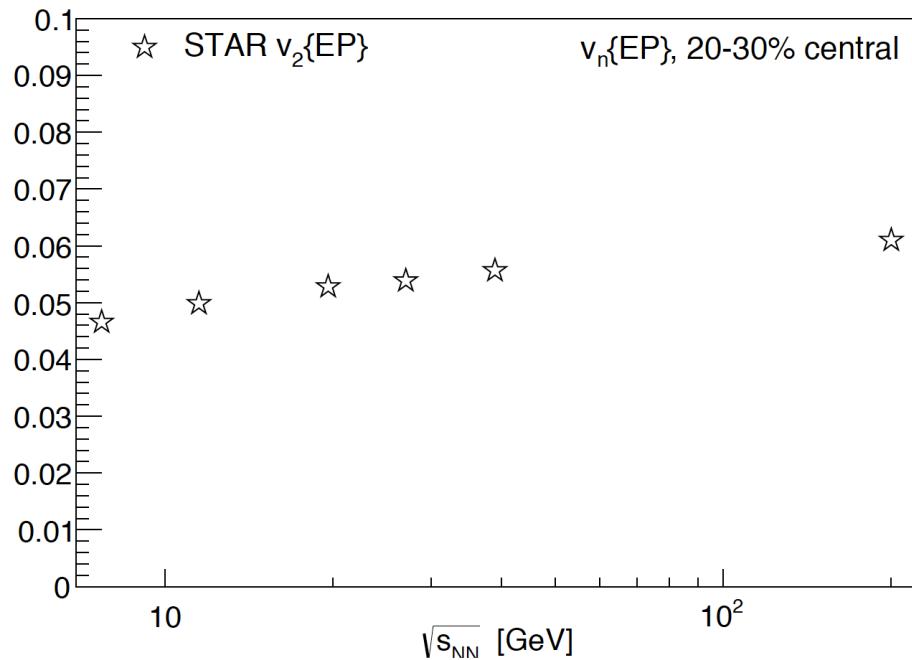


Strong constraint on viscosity

Reveal the nature of “perfect” fluid

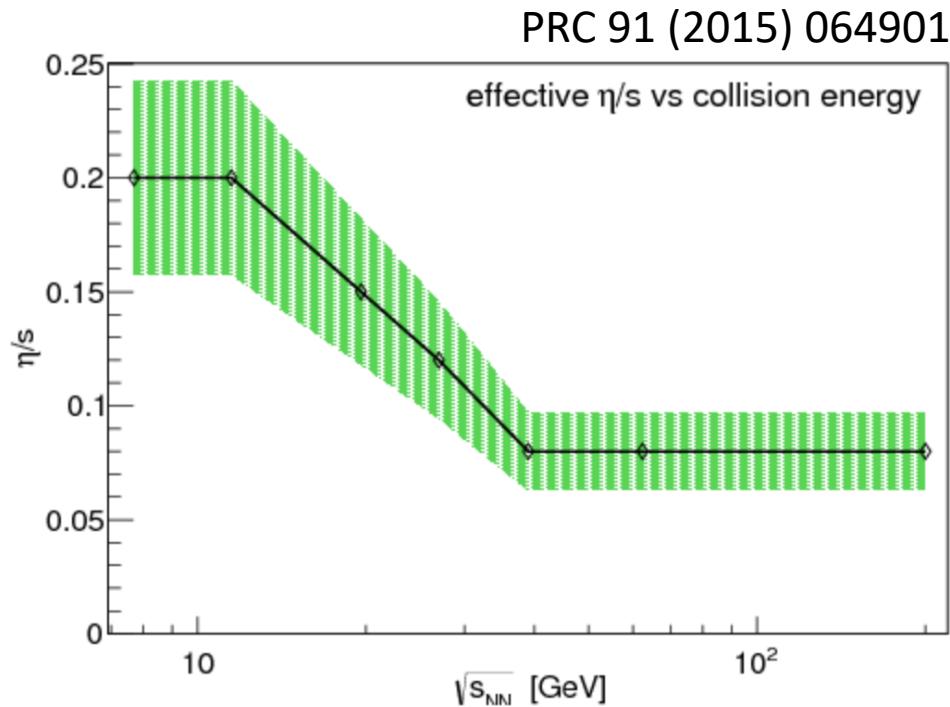
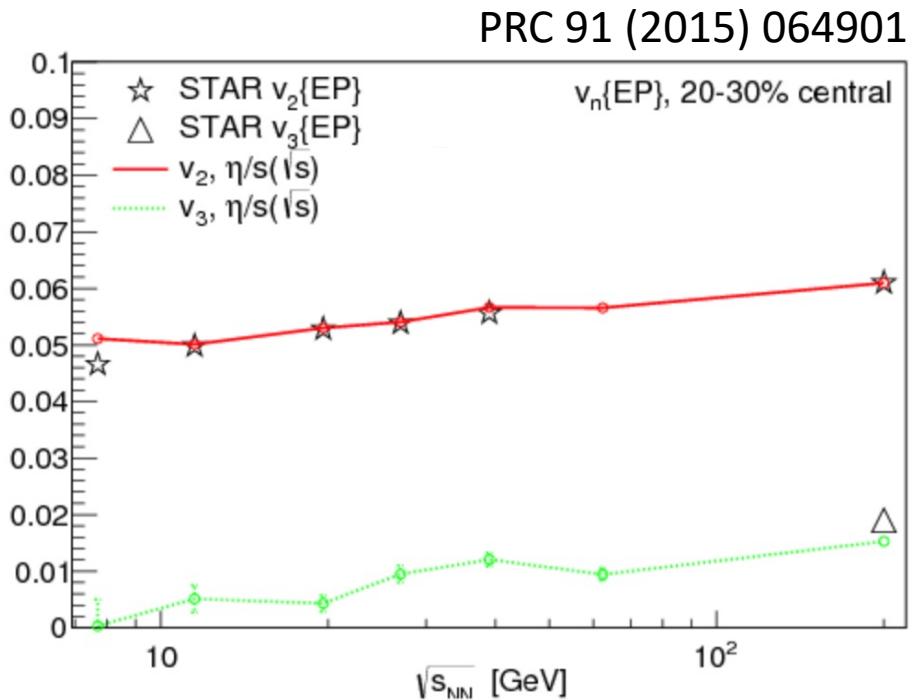
Ads/CFT lower limit  $\eta/s = 1/4\pi \approx 0.078$ , PRL 94 (2005) 11601

# $v_n$ vs. energy – viscosity vs. energy



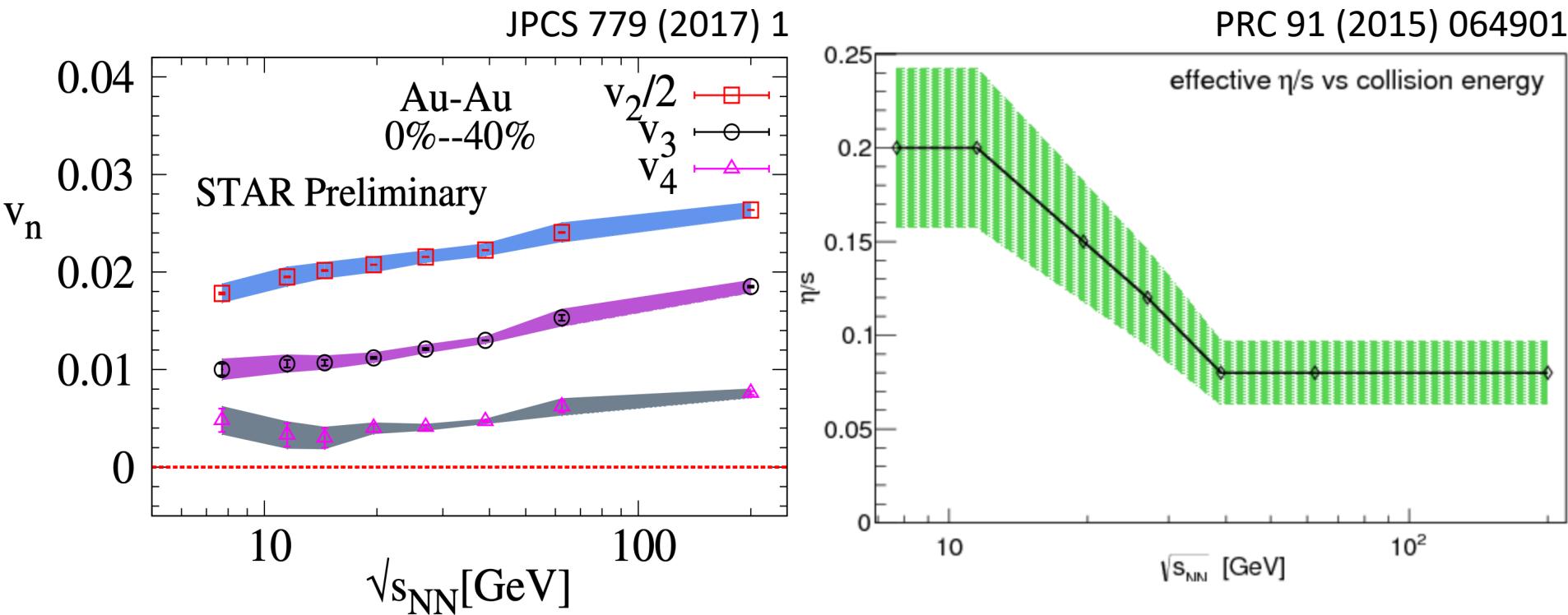
$v_2$  increases with collision energy

# $v_n$ vs. energy – viscosity vs. energy



$v_2$  increases with collision energy  
Indication of collision energy dependent viscosity

# $v_n$ vs. energy – viscosity vs. energy

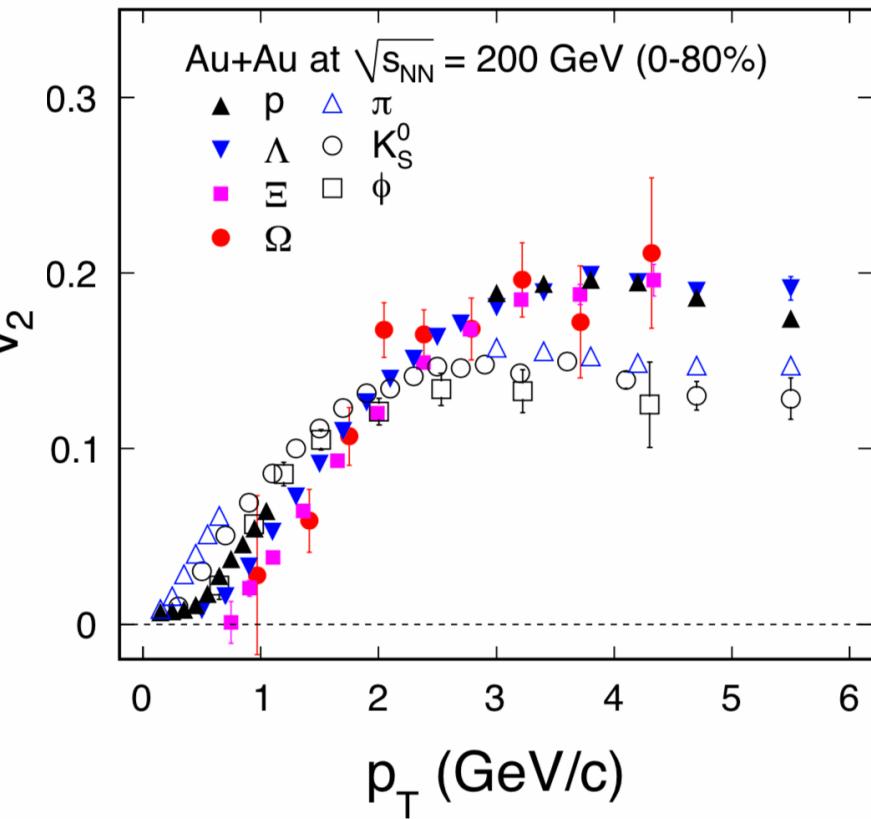
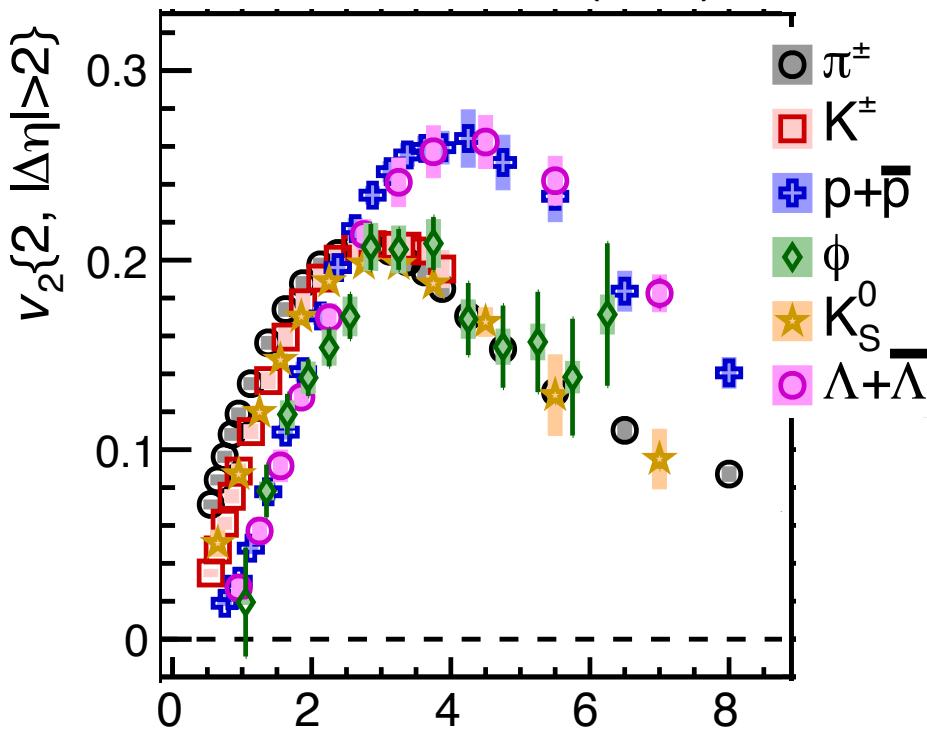


$v_2$  increases with collision energy  
Indication of collision energy dependent viscosity  
New results available for further investigation

# $v_n$ vs PID

# $v_n$ vs PID – mass ordering

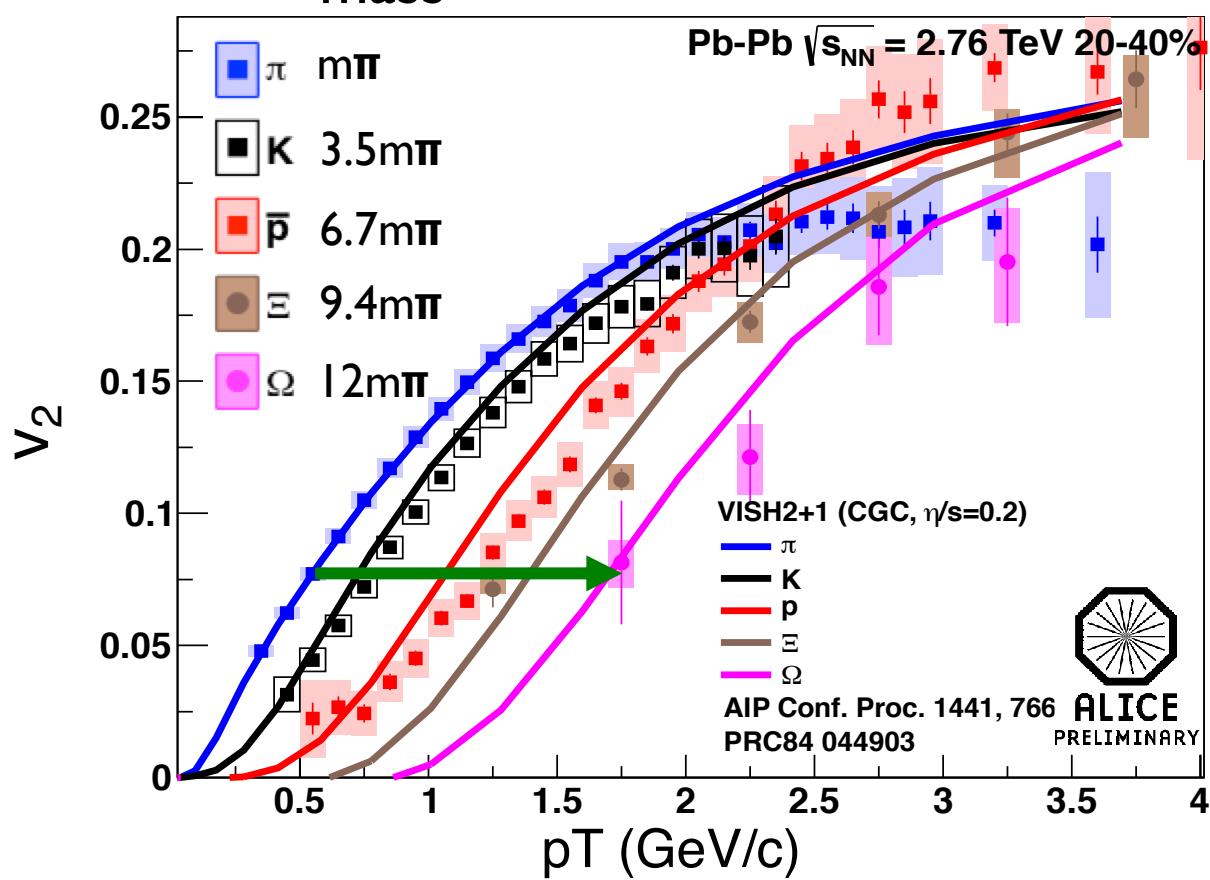
JHEP 09 (2018) 006



Mass ordering at low  $p_T < \approx 3$  GeV

Heavier particle has smaller  $v_n$  at same  $p_T$

# $v_n$ vs PID – mass ordering



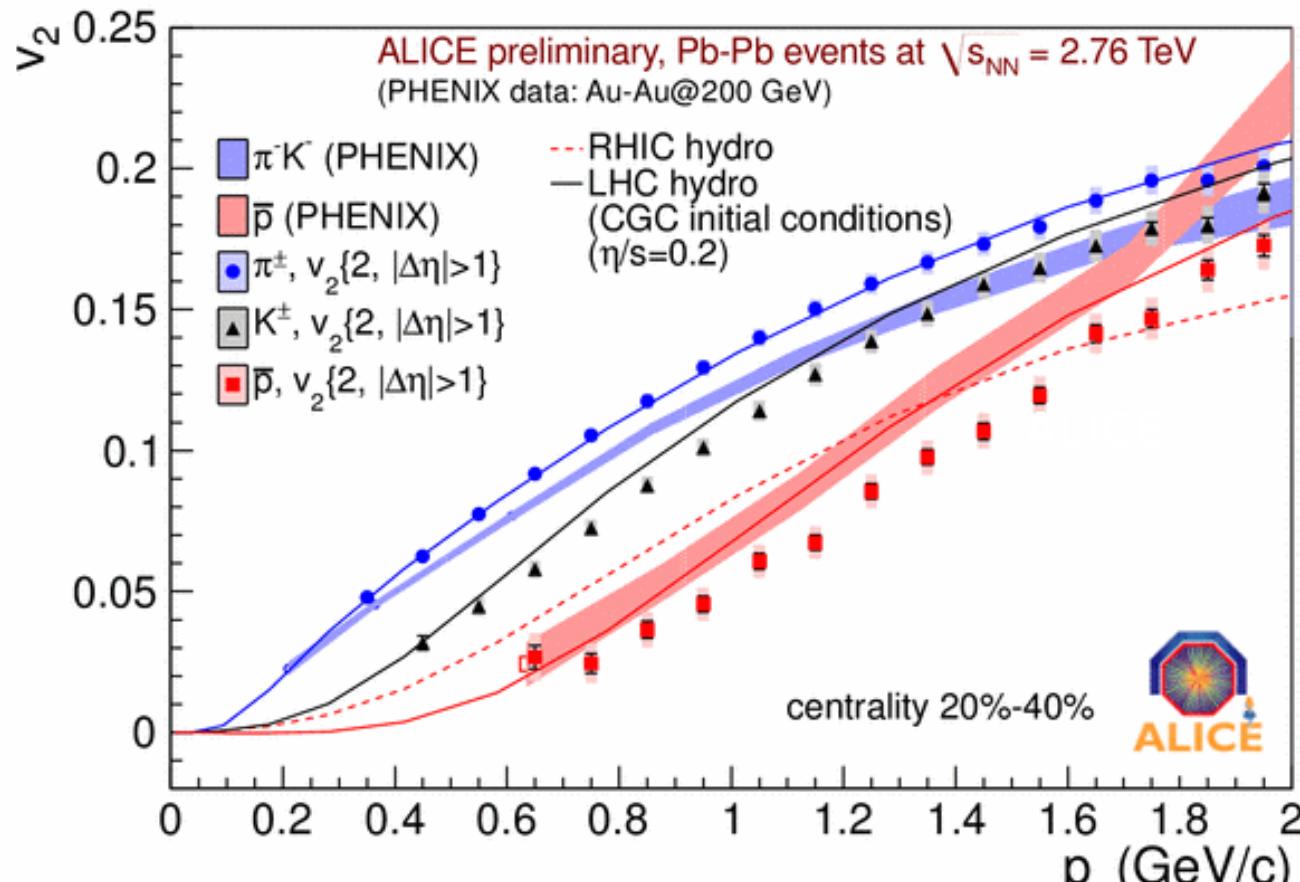
Boost:  
 $\Delta p_T \sim m\beta_T$

Mass ordering at low  $p_T < \approx 3\text{GeV}$

Heavier particle has smaller  $v_n$  at same  $p_T$

Predicted by hydro: common boost from pressure gradient

# $v_n$ vs PID – mass ordering



Mass ordering at low  $p_T \approx 3$  GeV

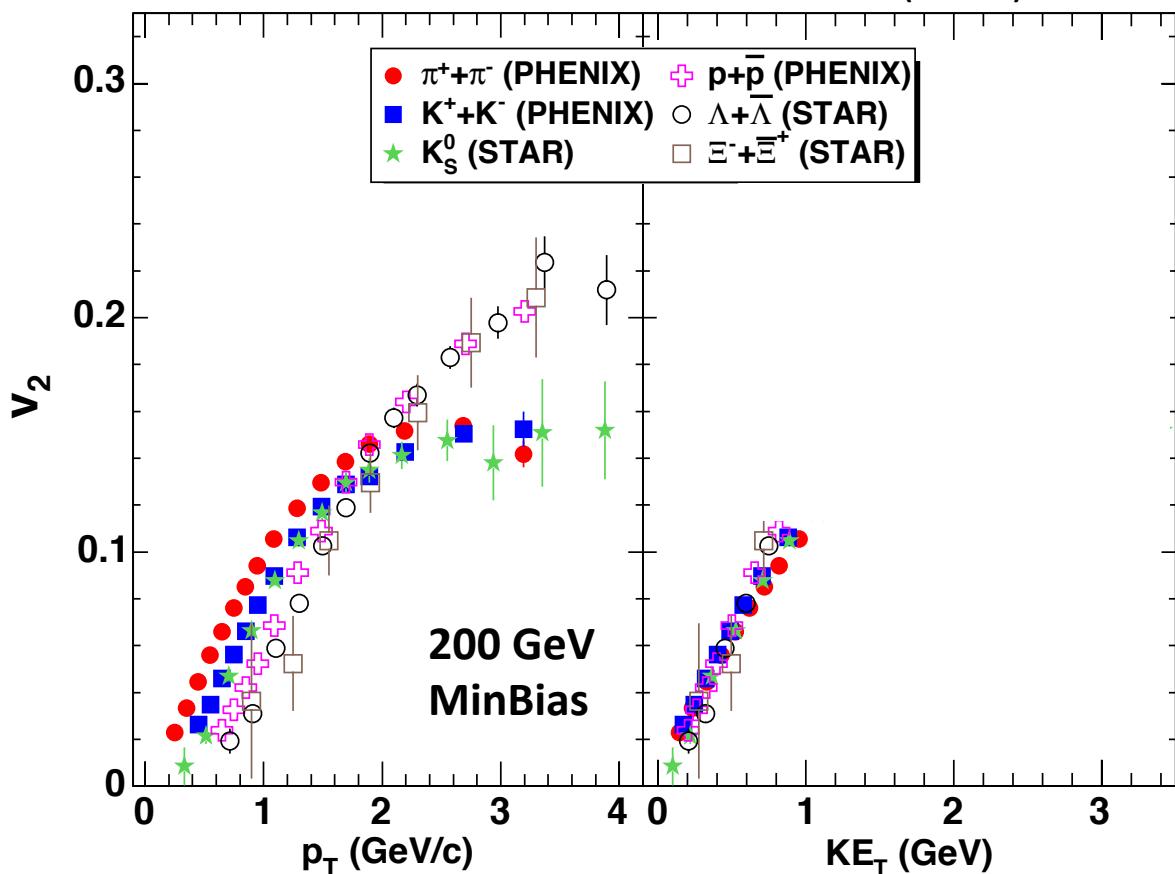
Heavier particle has smaller  $v_n$  at same  $p_T$

Predicted by hydro: common boost from pressure gradient

Indicate larger boost @ LHC energies

# $v_n$ vs PID – $KE_T$ scaling

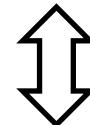
PRL 98 (2007) 162301



$KE_T$  scaling @  $KE_T \approx 1$  GeV: Hydro pressure gradient

$$KE_T = \sqrt{m^2 + p_T^2} - m$$

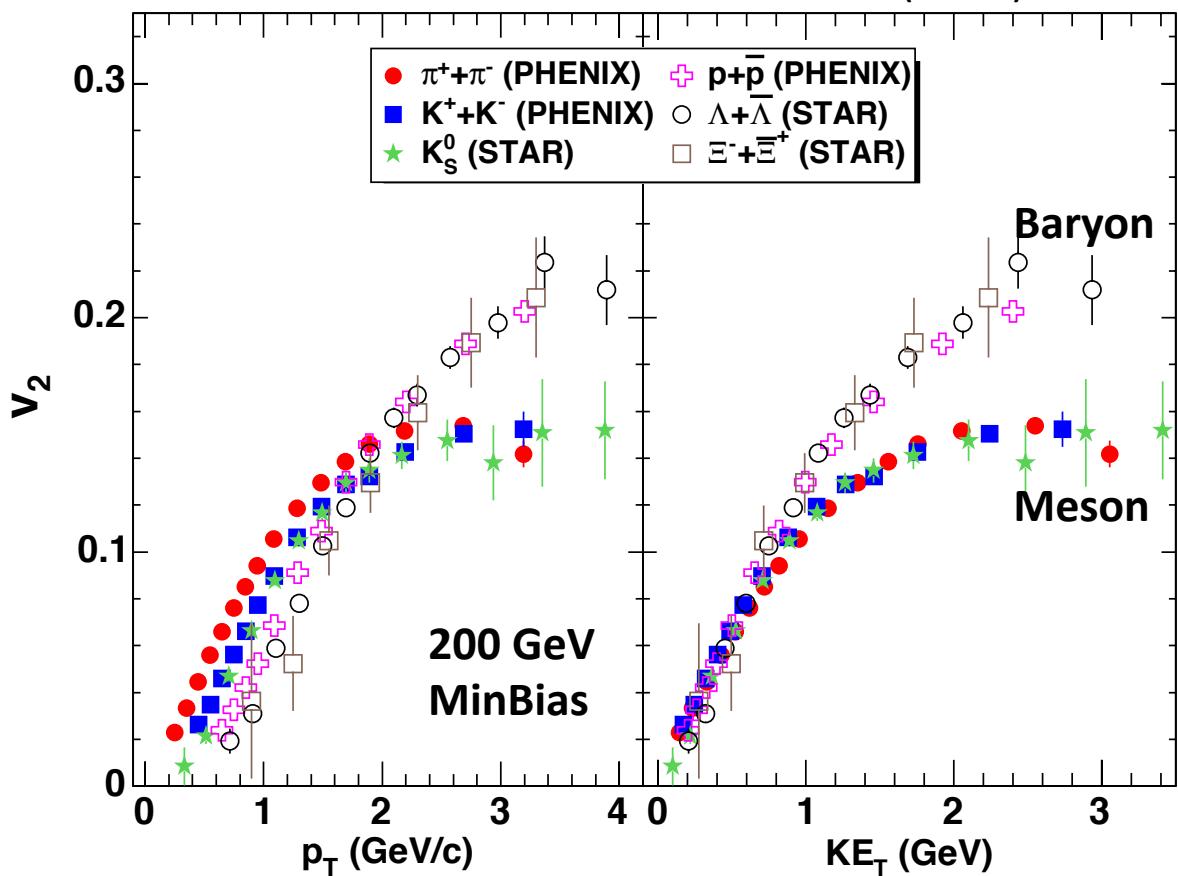
Pressure gradient



collective kinetic energy

# $v_n$ vs PID – Quark Coalescence

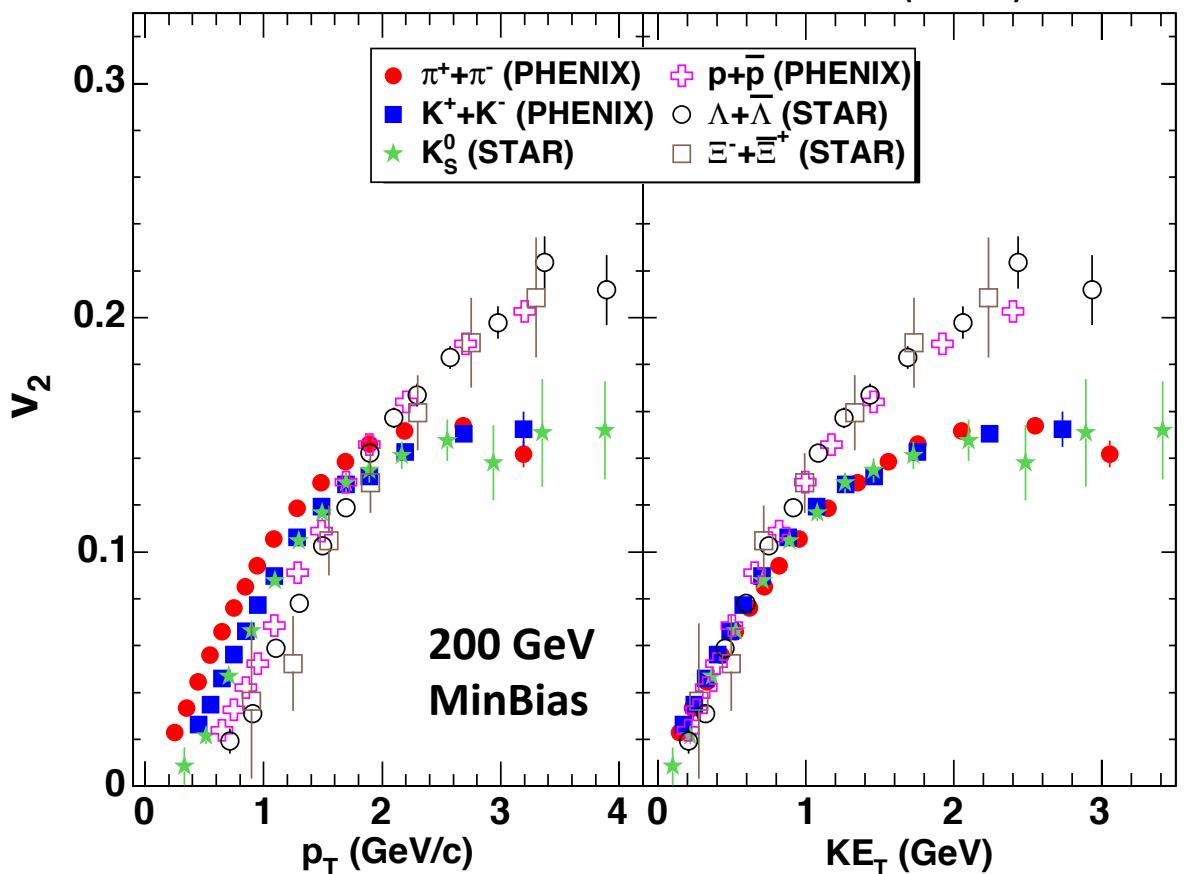
PRL 98 (2007) 162301



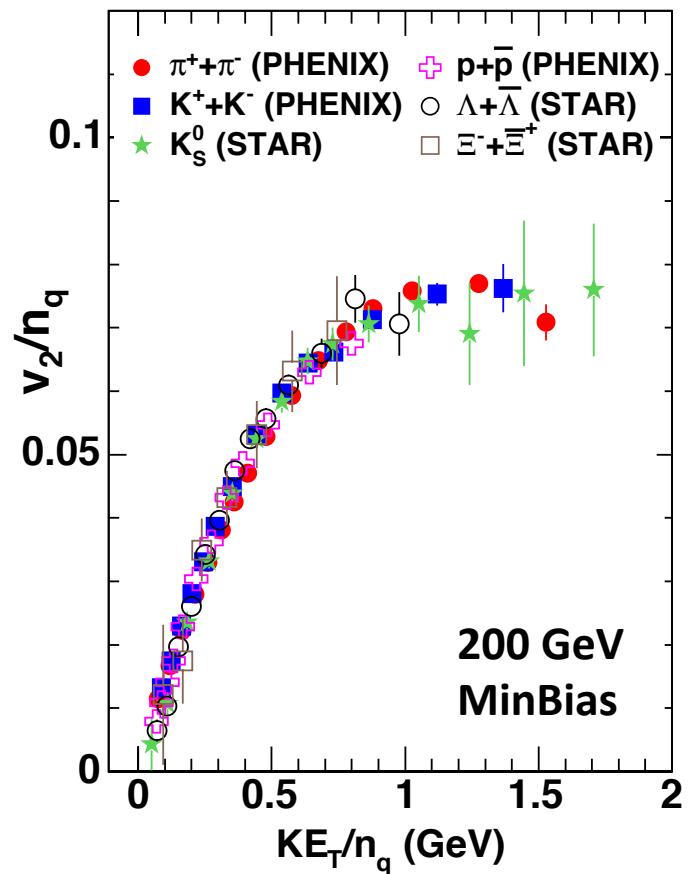
$KE_T$  scaling @  $KE_T \approx 1\text{GeV}$ : Hydro pressure gradient  
Meson/Baryon splitting: Quark coalescence

# $v_n$ vs PID – NCQ scaling

PRL 98 (2007) 162301



PRL 98 (2007) 162301



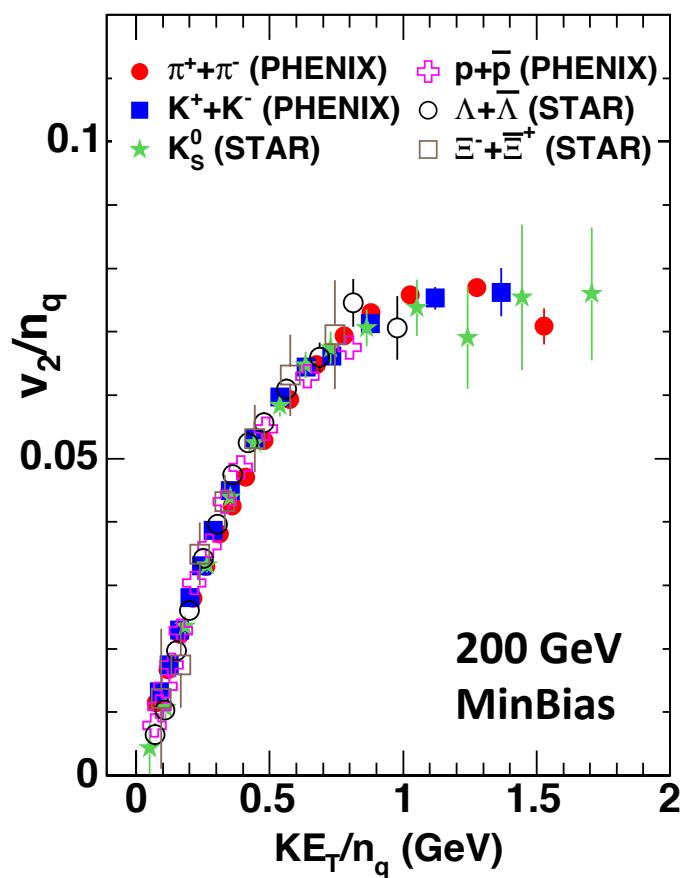
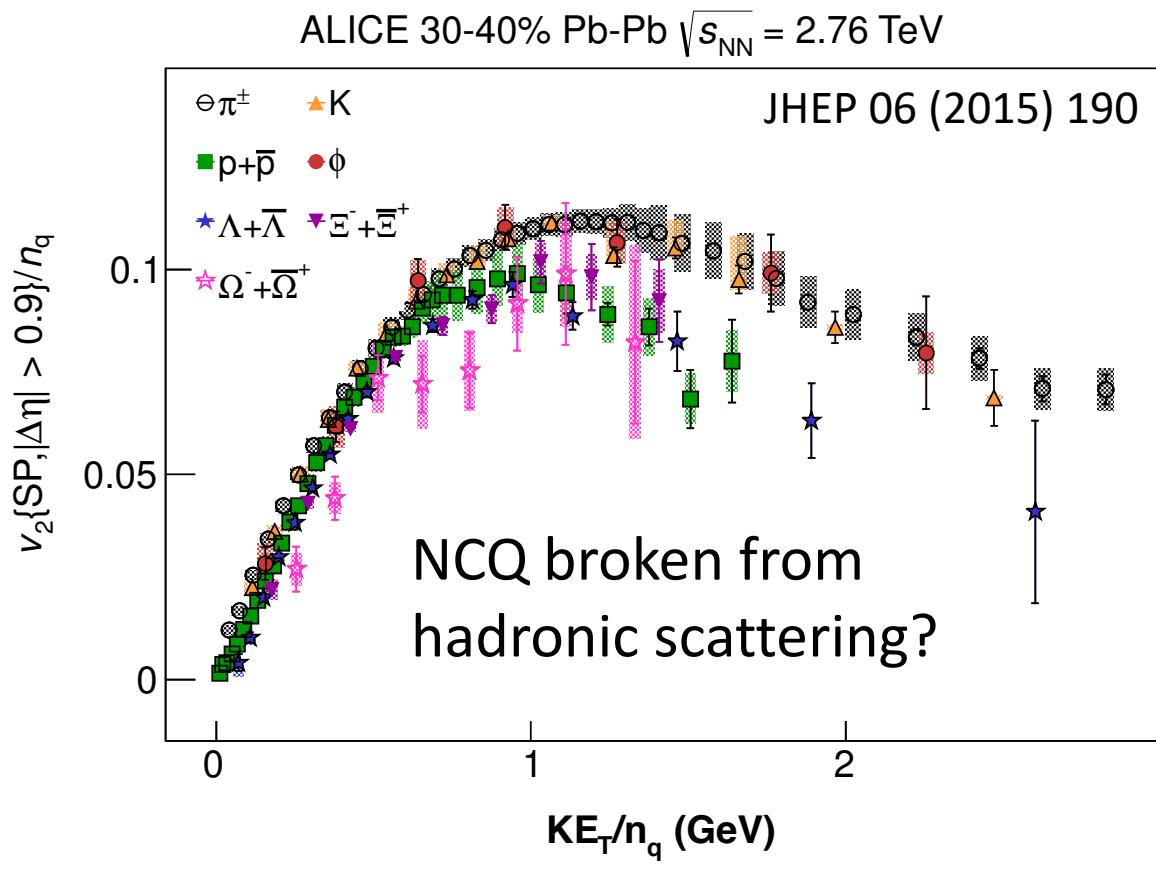
$KE_T$  scaling @  $KE_T \approx 1$  GeV: Hydro pressure gradient

Meson/Baryon splitting: Quark coalescence

Number of Constituent Quark scaling: Parton degree of freedom

# $v_n$ vs PID – NCQ scaling

PRL 98 (2007) 162301

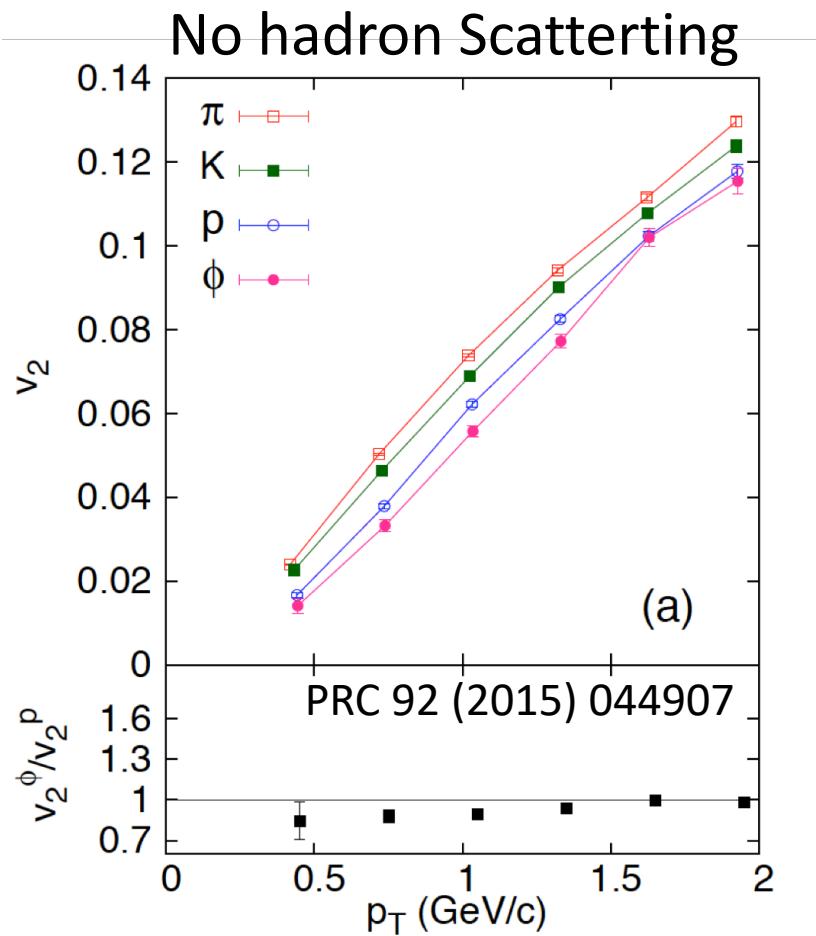


$KE_T$  scaling @  $KE_T \approx 1$  GeV: Hydro pressure gradient

Meson/Baryon splitting: Quark coalescence

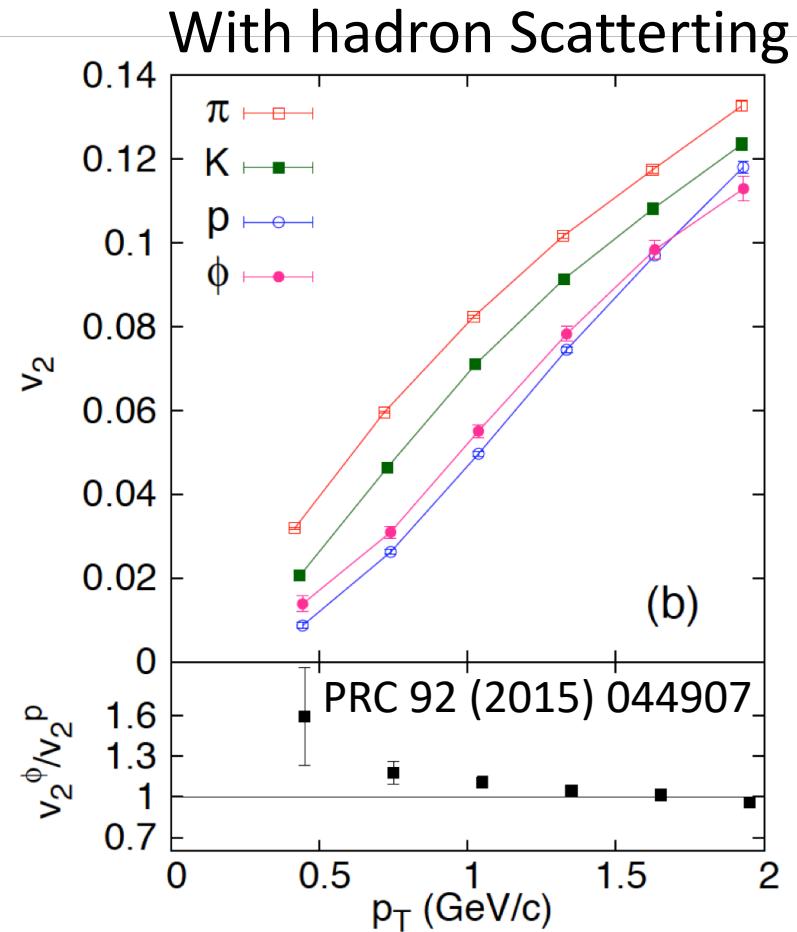
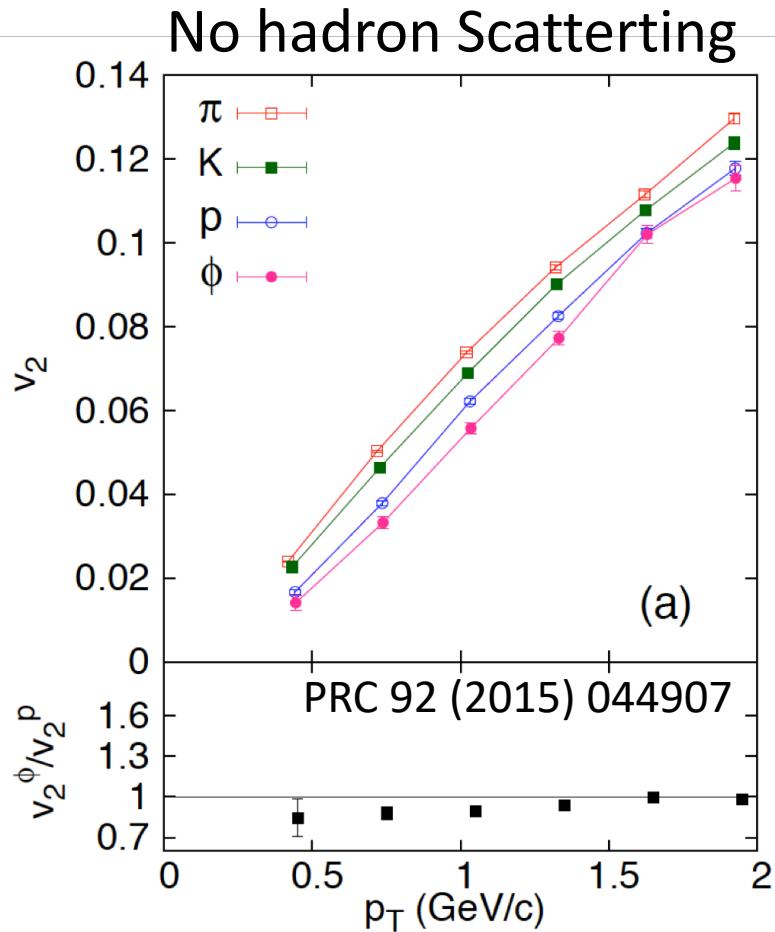
Number of Constituent Quark scaling: Parton degree of freedom

# $v_n$ vs PID – impact of hadronic phase



Ideal hydro + hadron cascade (JAM)

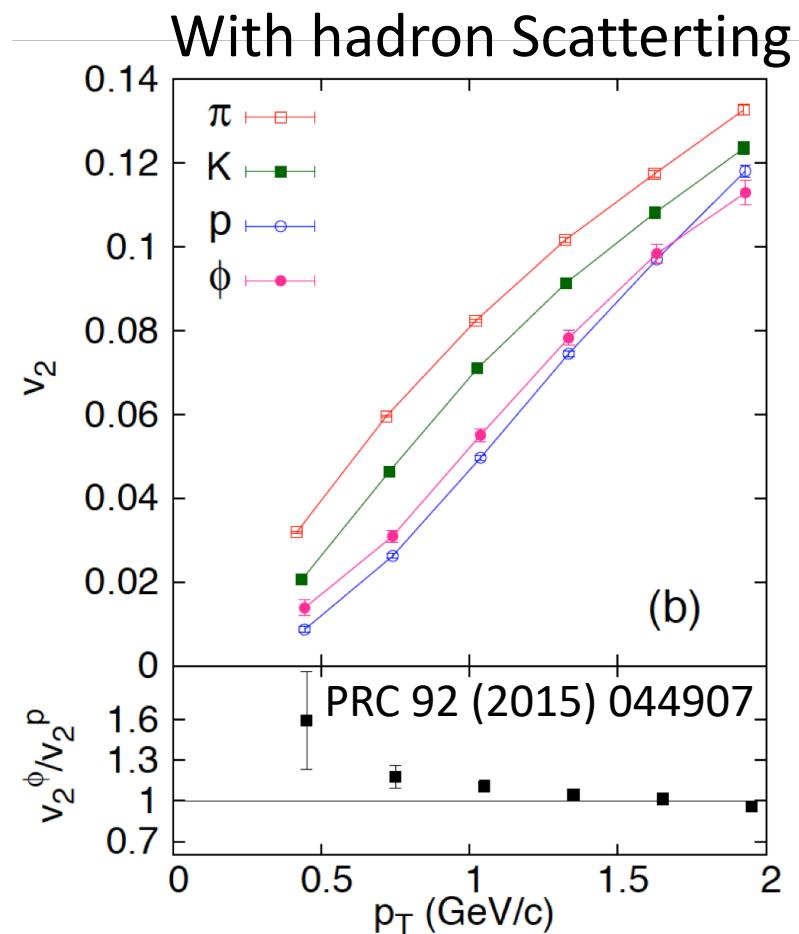
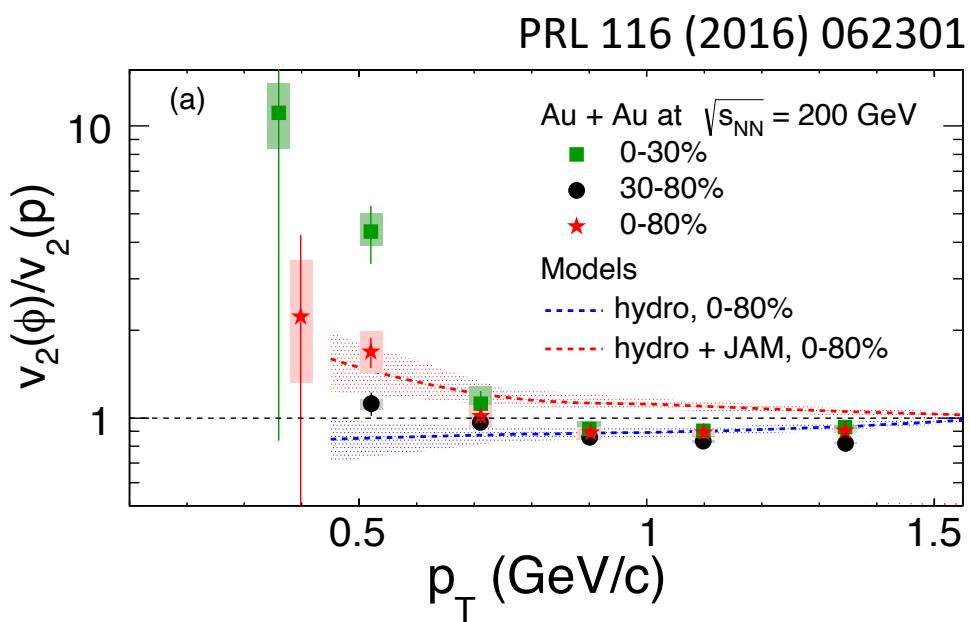
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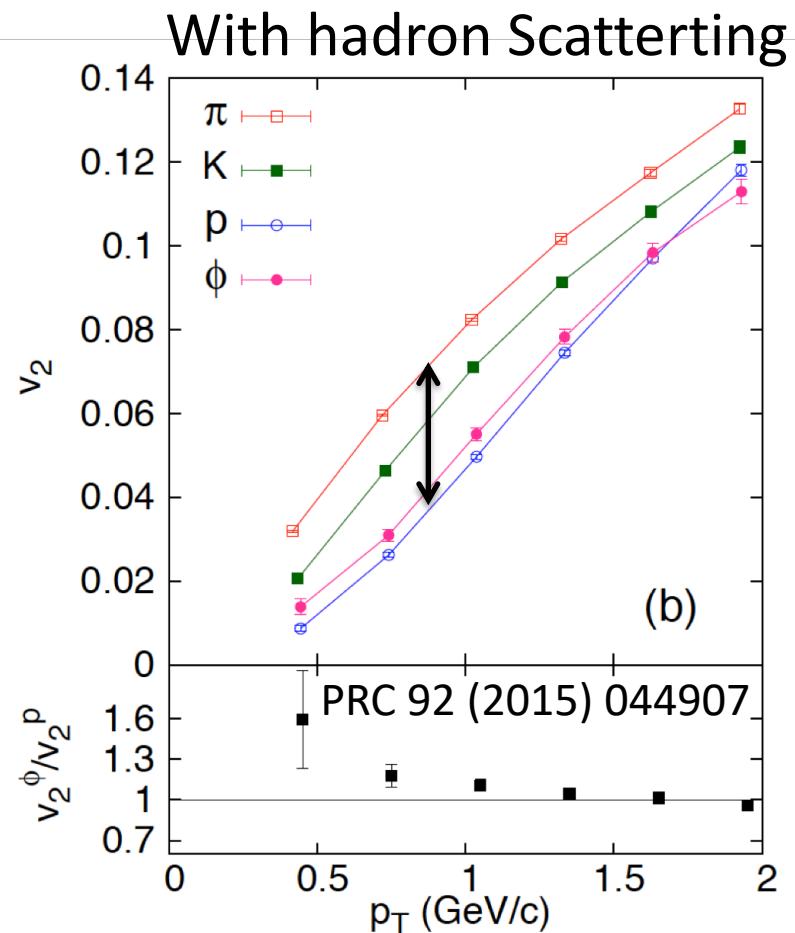
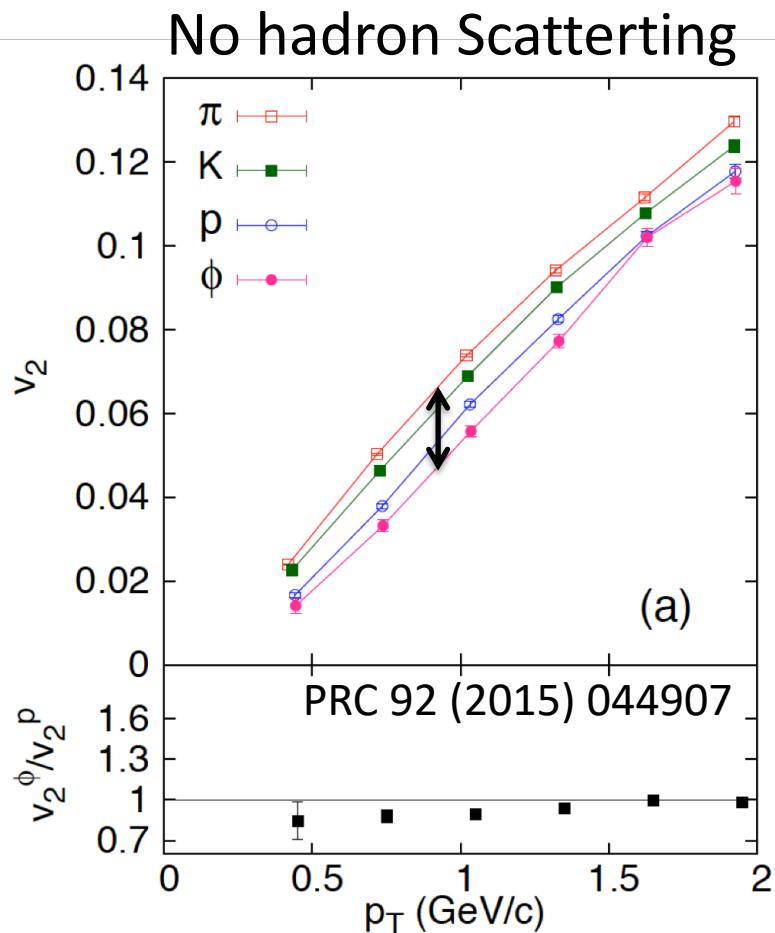
Small hadron cross section breaks mass ordering for  $\phi$

# $v_n$ vs PID – impact of hadronic phase



Ideal hydro + hadron cascade (JAM)  
 Small hadron cross section breaks mass ordering for  $\phi$   
 Confirmed by data

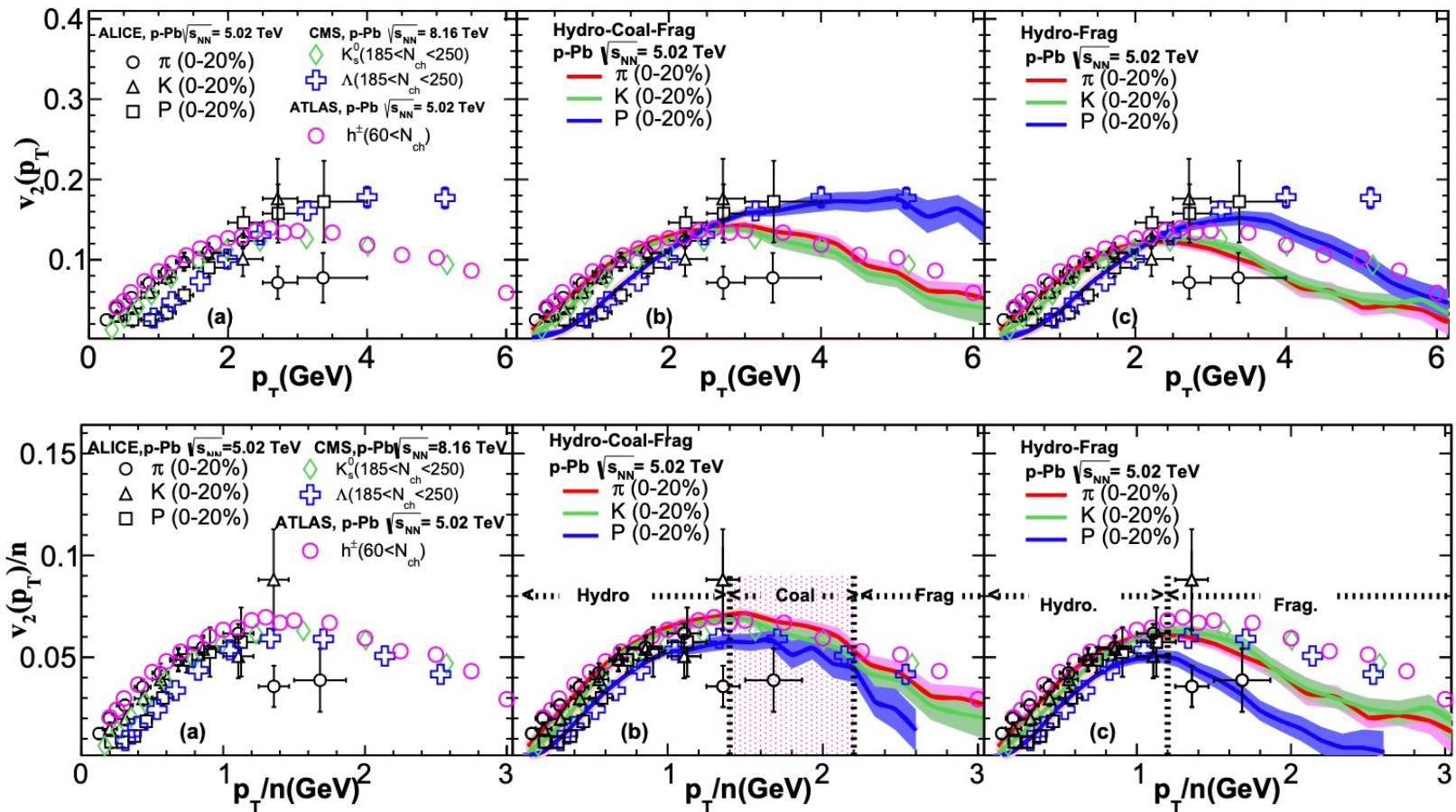
# $v_n$ vs PID – impact of hadronic phase



Ideal hydro + hadron cascade (JAM)

Small hadron cross section breaks mass ordering for phi  
Confirmed by data; **implication on NCQ scaling?**

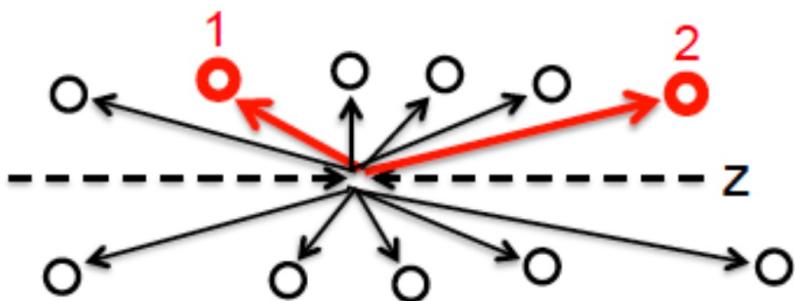
# $v_n$ vs PID – impact from coalescence?



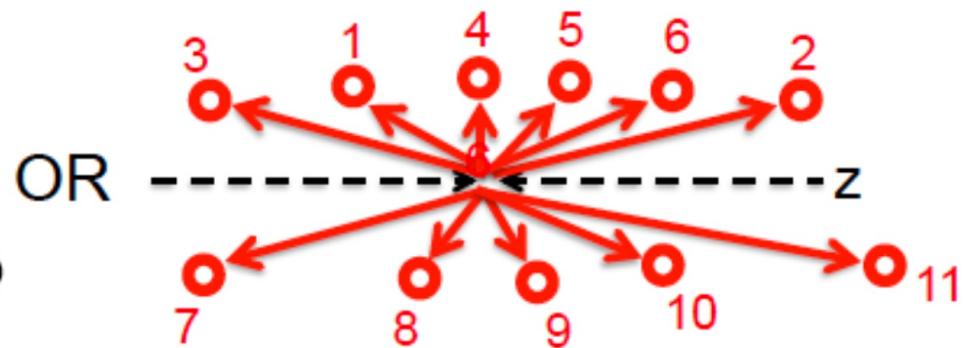
Coalescence of  
quenched jet particle and bulk particle  
can break the scaling

# $v_n$ from multi-particle correlation

Two-particle correlation



Multi-particle correlation



Multi-particle ( $>2$ ) cumulants:

$$\langle\langle 6 \rangle\rangle = \langle\langle e^{in(\phi_1+\phi_2+\phi_3-\phi_4-\phi_5-\phi_6)} \rangle\rangle$$

$$c_n\{6\} = \langle\langle 6 \rangle\rangle - 9 \cdot \langle\langle 4 \rangle\rangle \langle\langle 2 \rangle\rangle + 12 \cdot \langle\langle 2 \rangle\rangle^3$$



$$v_n\{4\} = \sqrt[4]{-c_n\{4\}}$$

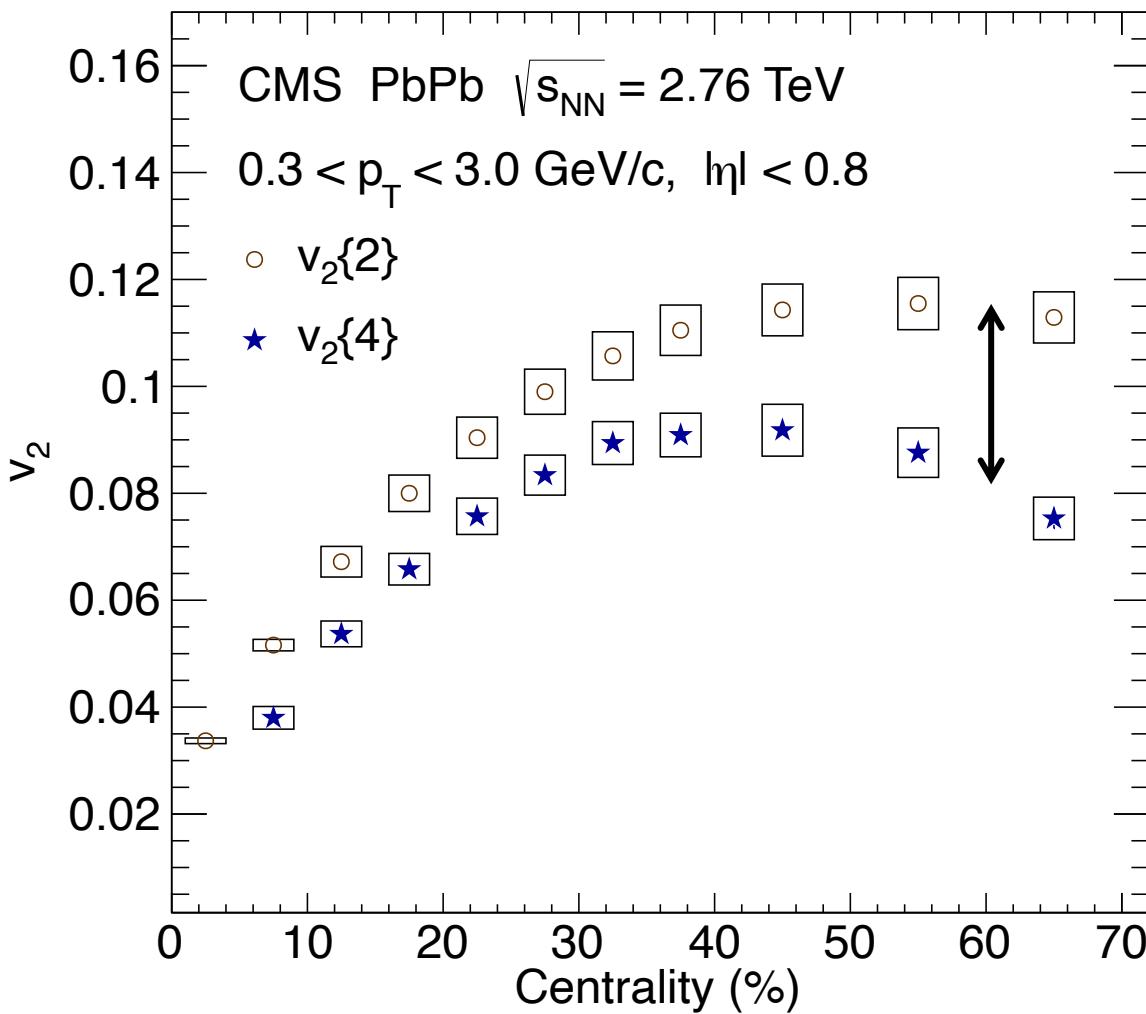
$$v_n\{6\} = \sqrt[4]{\frac{1}{4}c_n\{6\}}$$

Q-cumulant, PRC 83 (2011) 044913

$v_n\{4\} \approx v_n\{6\} \approx \dots \rightarrow$  system is collective

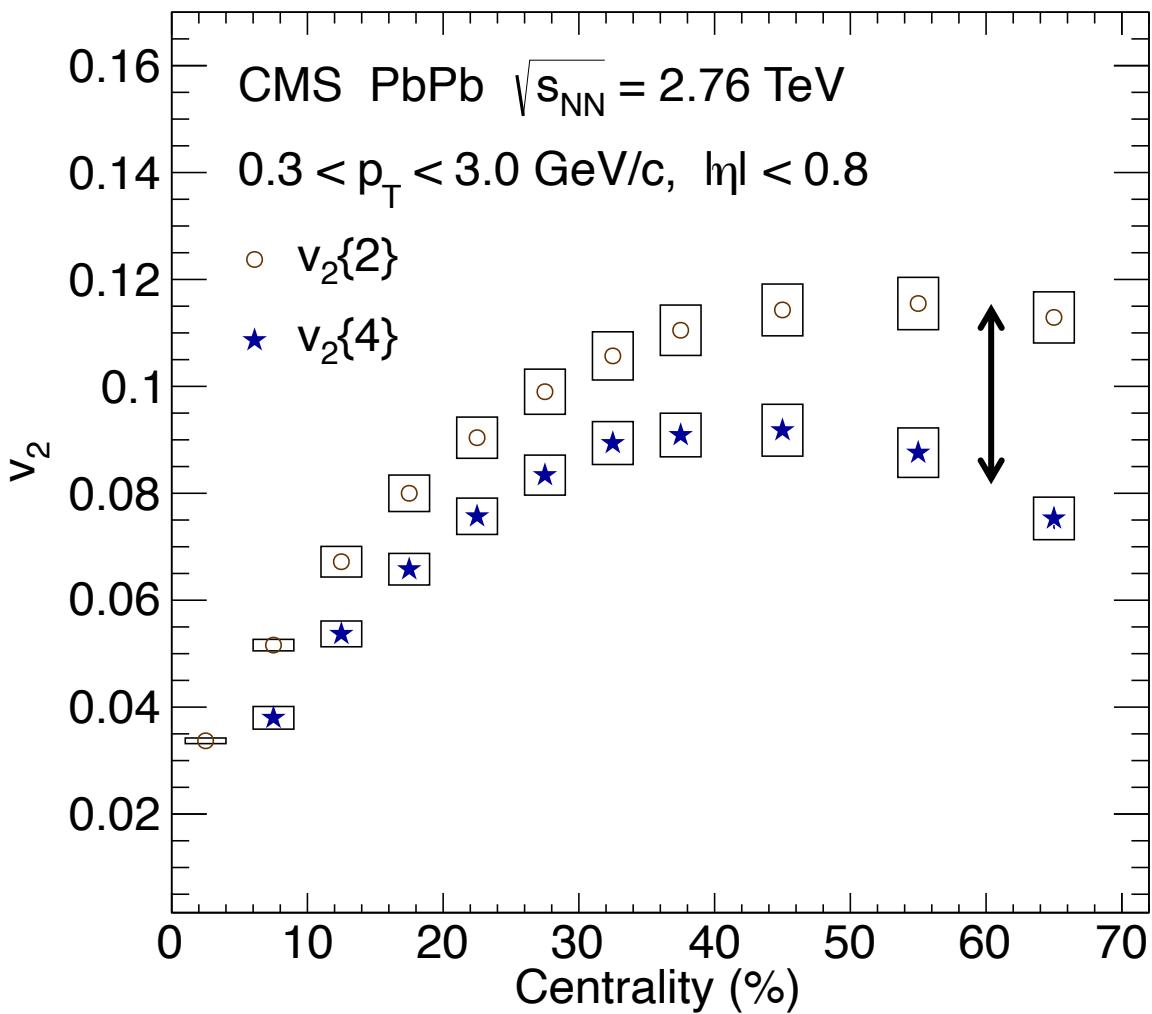
# $v_n$ from multi-particle correlation

PRC 87 (2013) 014902

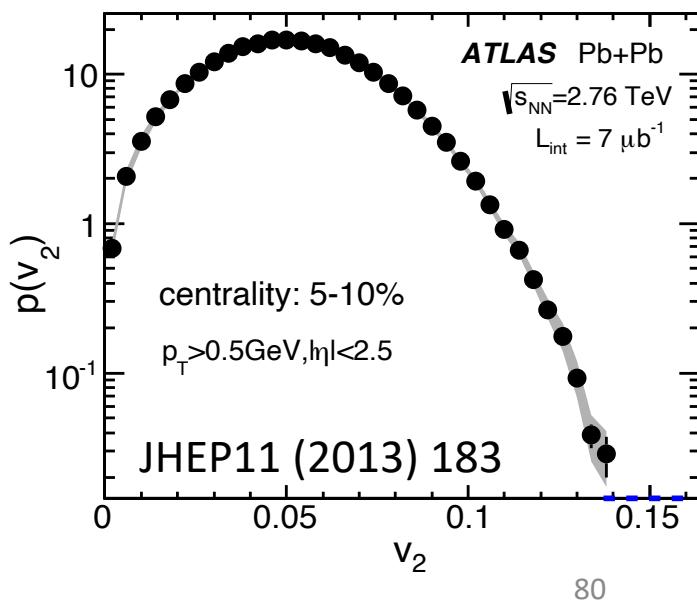


# $v_n$ from multi-particle – flow fluctuation

PRC 87 (2013) 014902

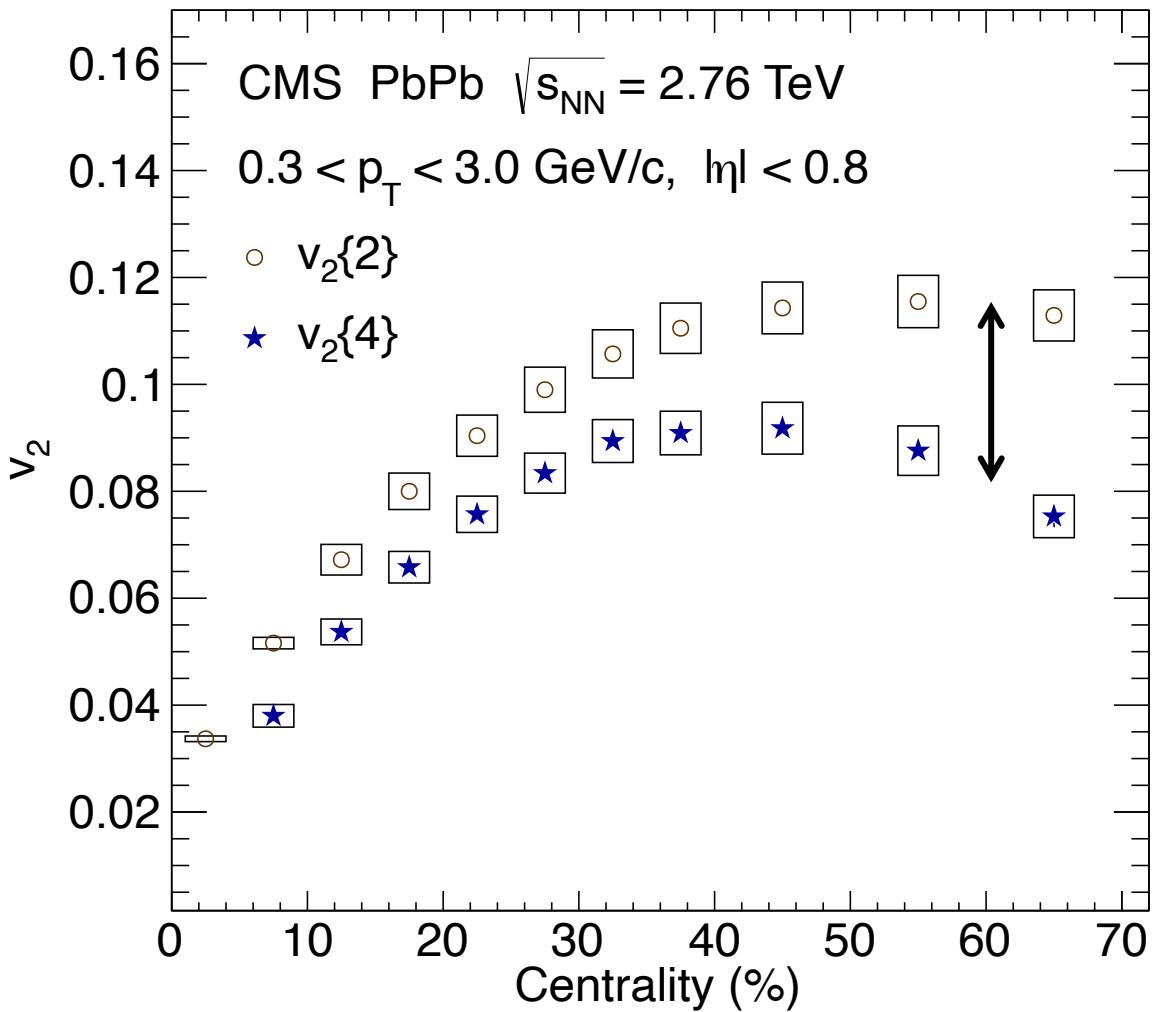


Event-by-Event  
Flow Fluctuation



# $v_n$ from multi-particle – flow fluctuation

PRC 87 (2013) 014902



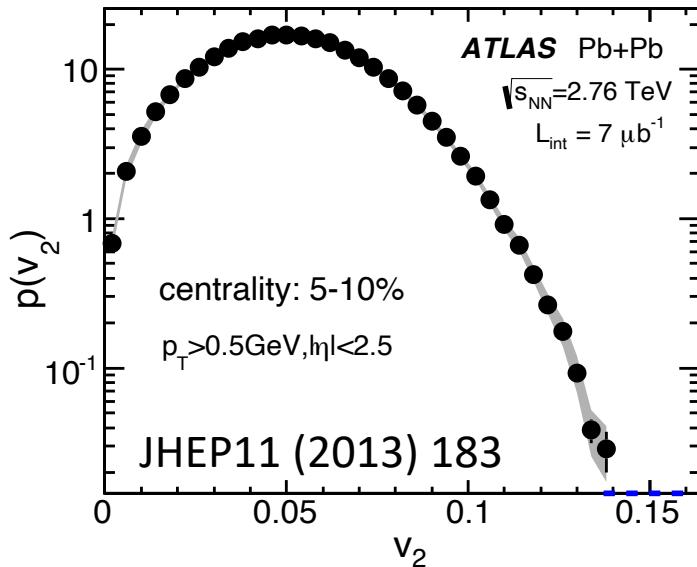
Event-by-Event  
Flow Fluctuation

$$v_n\{2\}^2 = \langle v_n^2 \rangle = \langle v_n \rangle^2 + \sigma_{v_n}^2$$

$$v_n\{4\}^2 = (2\langle v_n^2 \rangle^2 - \langle v_n^4 \rangle)^{\frac{1}{2}}$$

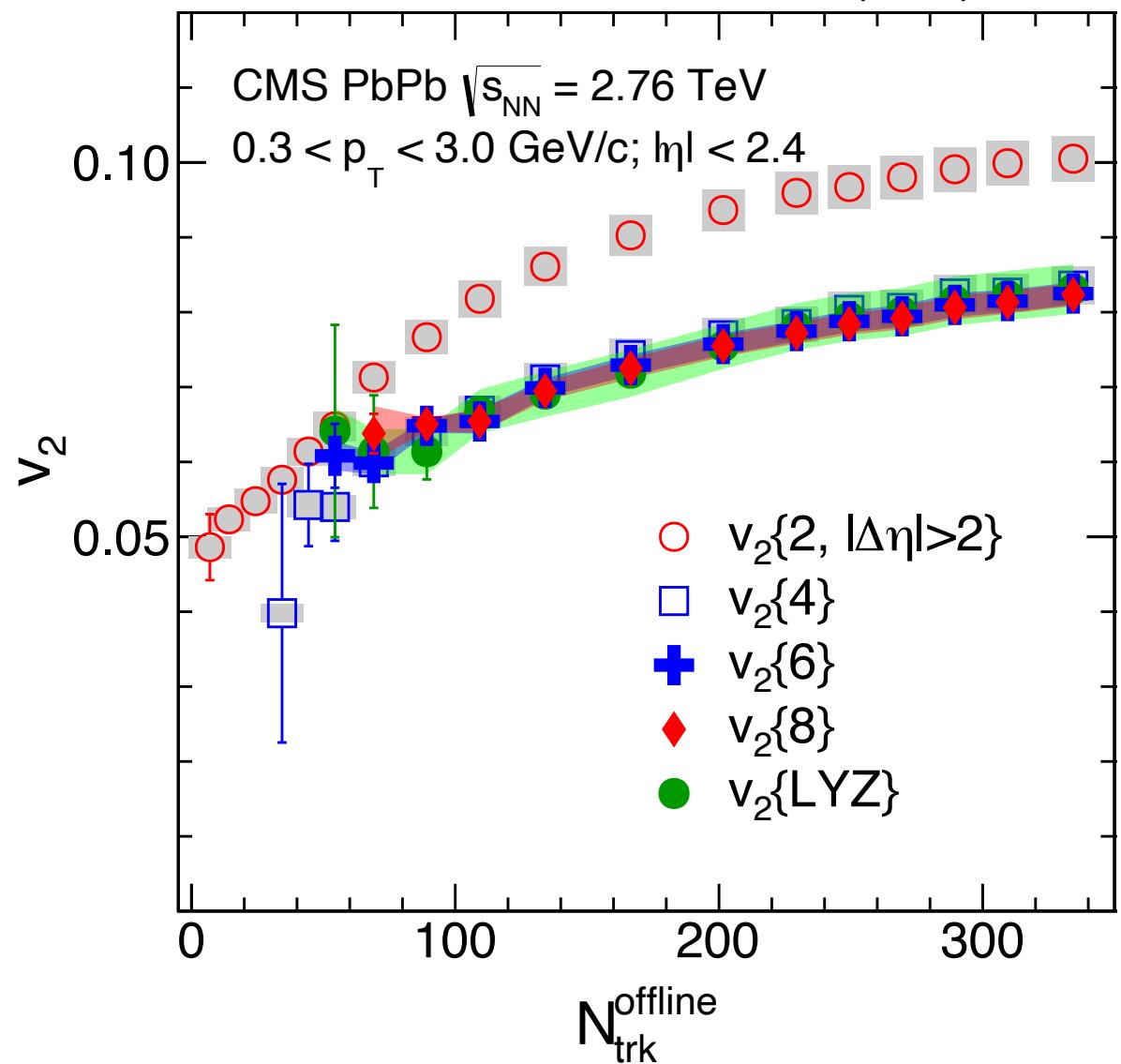
$$\approx \langle v_n \rangle^2 - \sigma_{v_n}^2$$

PRC 80 (2009) 014904



# $v_n$ from multi-particle – flow fluctuation

PRL 115 (2015) 012301



Event-by-Event  
Flow Fluctuation

$$v_n\{2\}^2 = \langle v_n^2 \rangle = \langle v_n \rangle^2 + \sigma_{v_n}^2$$

$$v_n\{4\}^2 = (2\langle v_n^2 \rangle^2 - \langle v_n^4 \rangle)^{\frac{1}{2}}$$

$$\approx \langle v_n \rangle^2 - \sigma_{v_n}^2$$

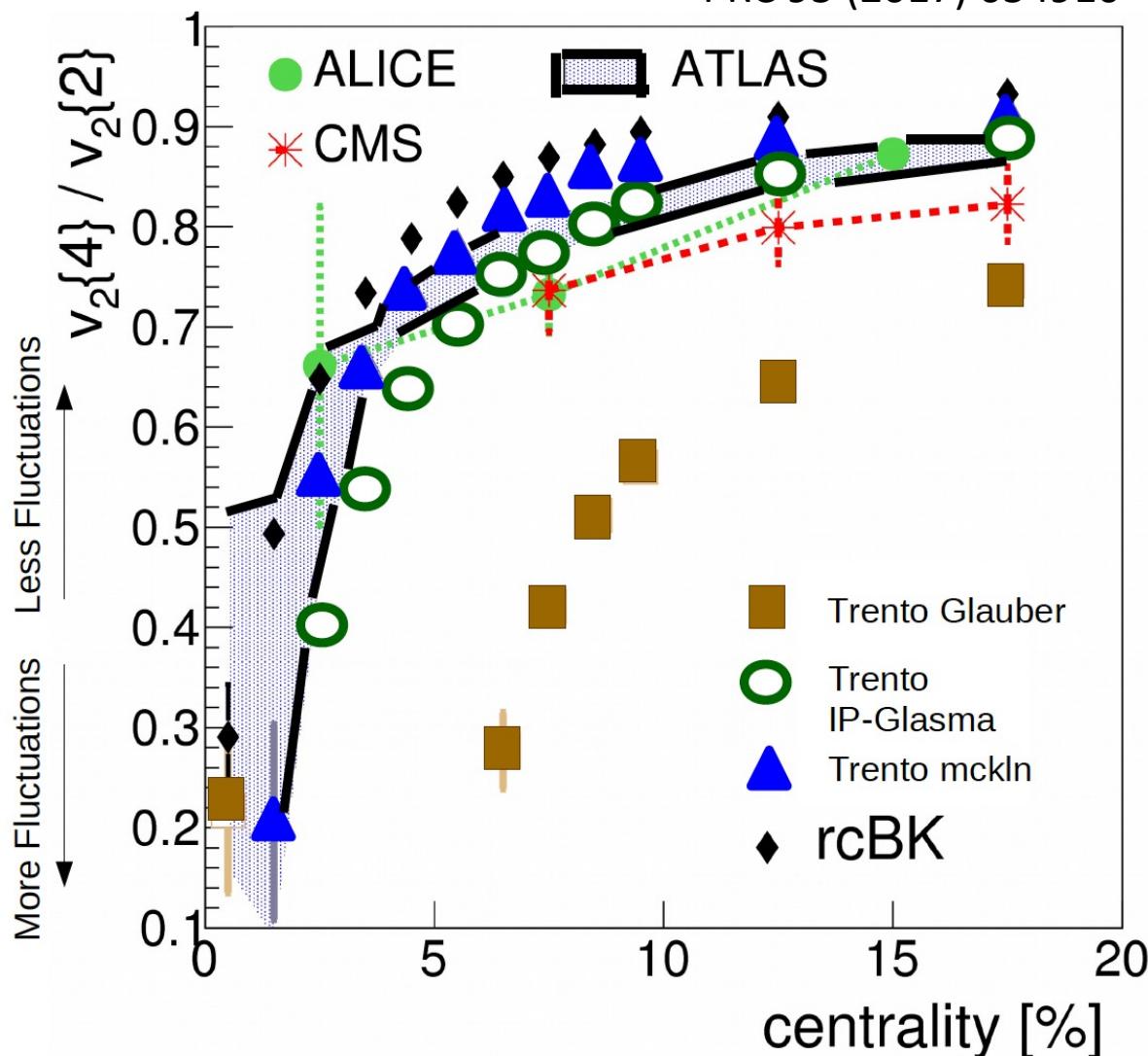
PRC 80 (2009) 014904

$v_2\{4,6,8,\text{LYZ}\}$   
indicate multi-particle  
nature of correlation

More implications  
on flow fluctuation  
see EPJC 74 (2014) 3157

# $v_n$ from multi-particle – constrain initial-state

PRC 95 (2017) 054910



Event-by-Event  
Flow Fluctuation

$$v_n\{2\}^2 = \langle v_n^2 \rangle = \langle v_n \rangle^2 + \sigma_{v_n}^2$$

$$v_n\{4\}^2 = (2\langle v_n^2 \rangle^2 - \langle v_n^4 \rangle)^{\frac{1}{2}}$$
$$\approx \langle v_n \rangle^2 - \sigma_{v_n}^2$$

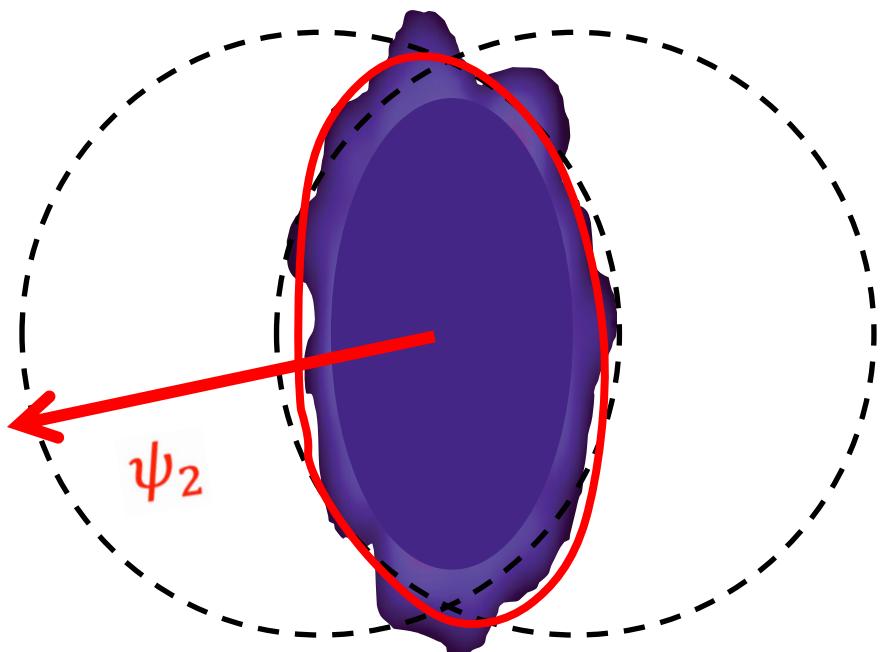
PRC 80 (2009) 014904

Strong constraints on  
initial state models  
MC Glauber fails!

TRENTO: PRC 92(2015) 011901

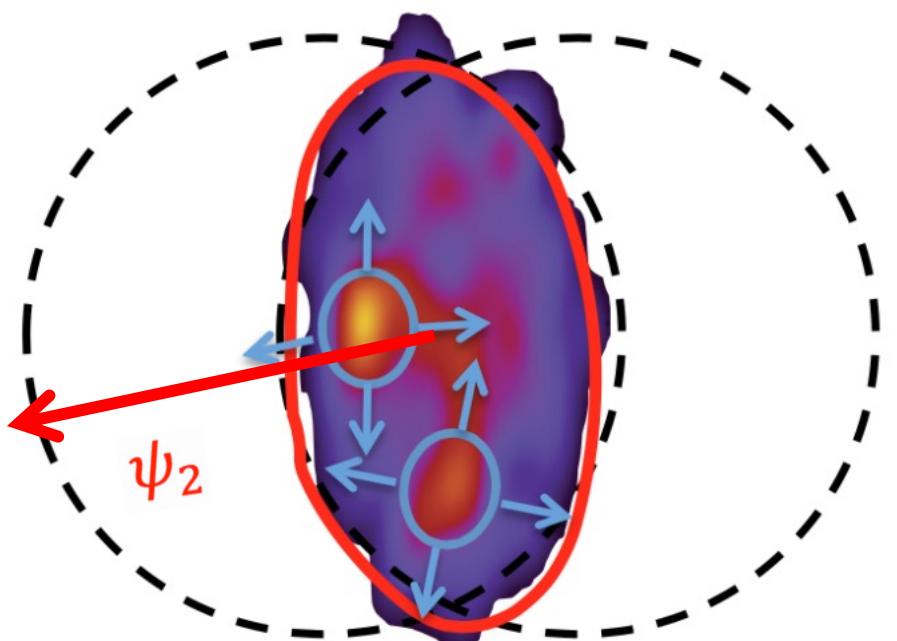
rcBK: arXiv:1011.5161

# Decorrelation – Transeverse



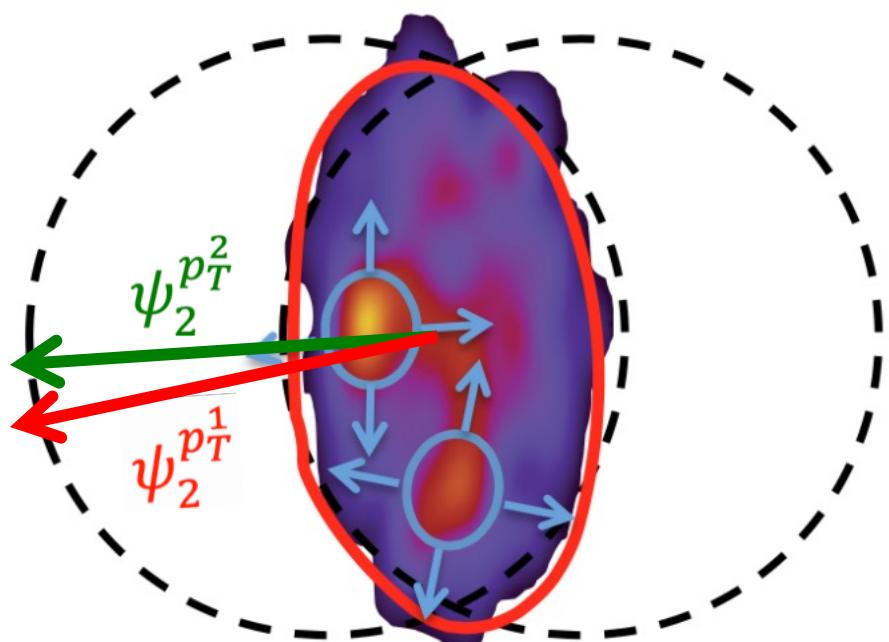
All particle share the same event plane

# Decorrelation – Transeverse



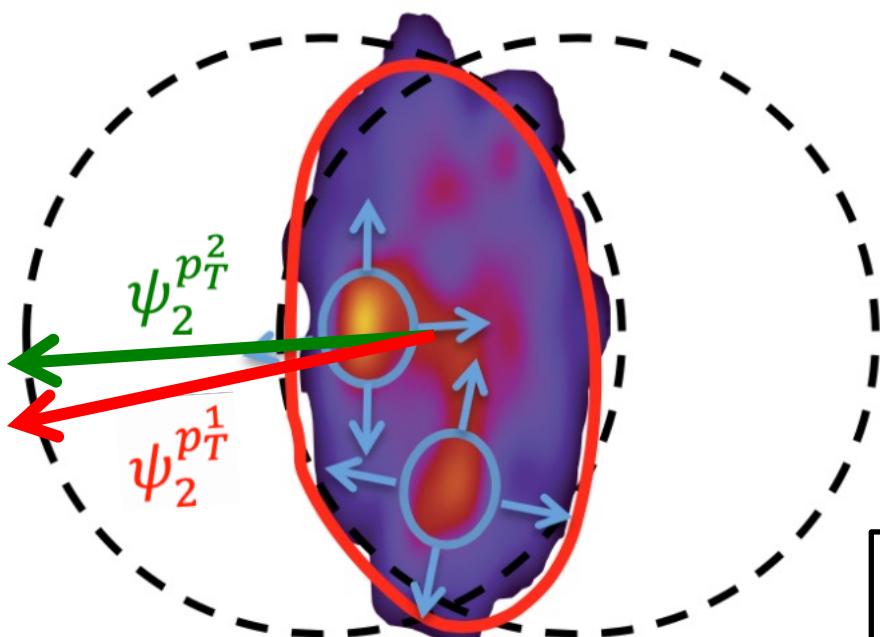
Local hot spots push particles to higher  $p_T$

# Decorrelation – Transeverse



Local hot spots push particles to higher  $p_T$   
AND  
result in different event planes  
for different  $p_T$  range

# Decorrelation – Transverse



Local hot spots push particles to higher  $p_T$   
AND  
result in different event planes for different  $p_T$  range

Factorization breaking

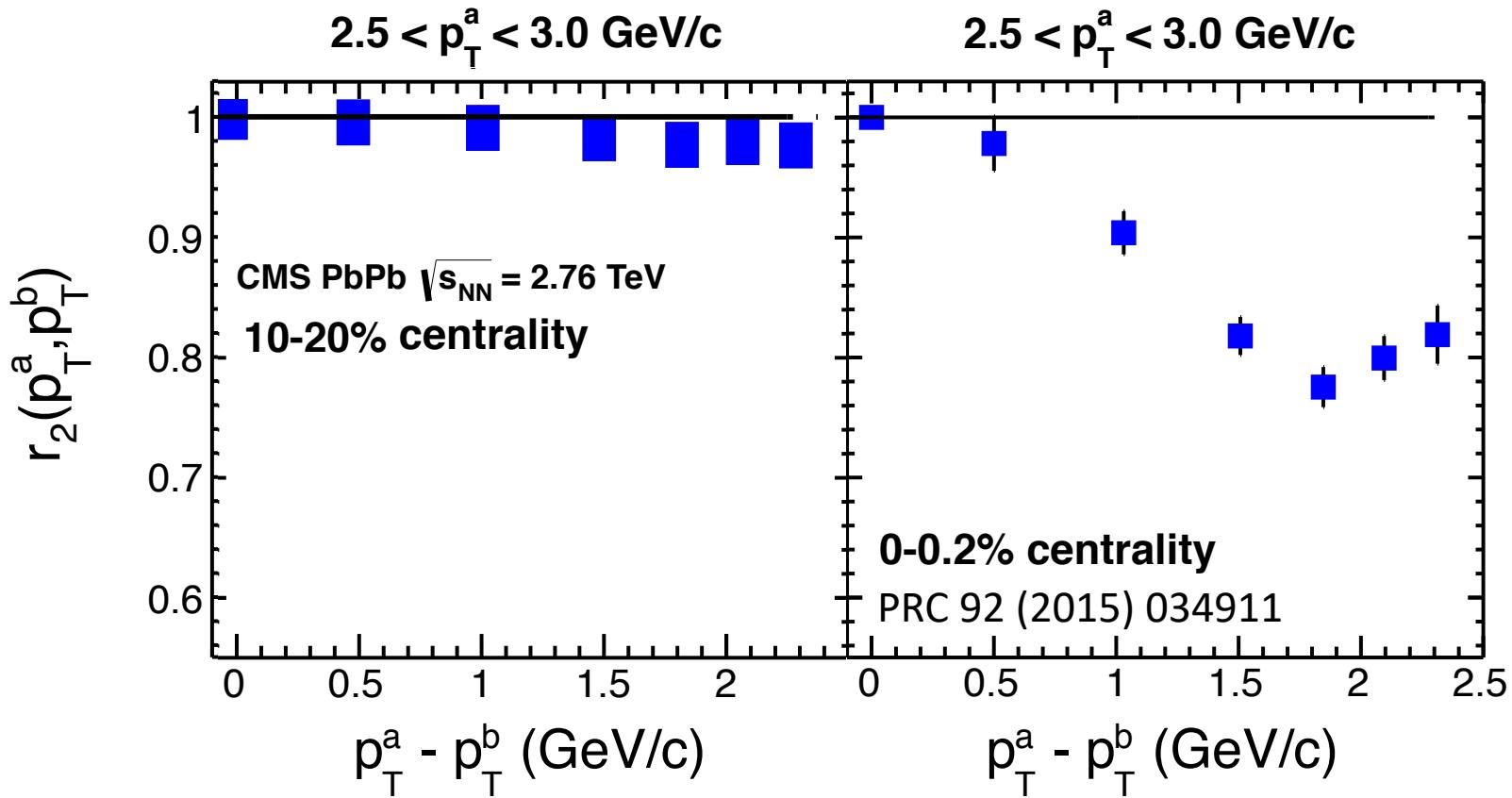
$$V_{n\Delta}(p_T^a, p_T^b) \neq v_n(p_T^a) \times v_n(p_T^b)$$

Effects measurable by

$$r_n(p_T^a, p_T^b) \equiv \frac{V_{n\Delta}(p_T^a, p_T^b)}{\sqrt{V_{n\Delta}(p_T^a, p_T^a)} \sqrt{V_{n\Delta}(p_T^b, p_T^b)}} \sim \langle \cos [n(\Psi_n(p_T^a) - \Psi_n(p_T^b))] \rangle$$

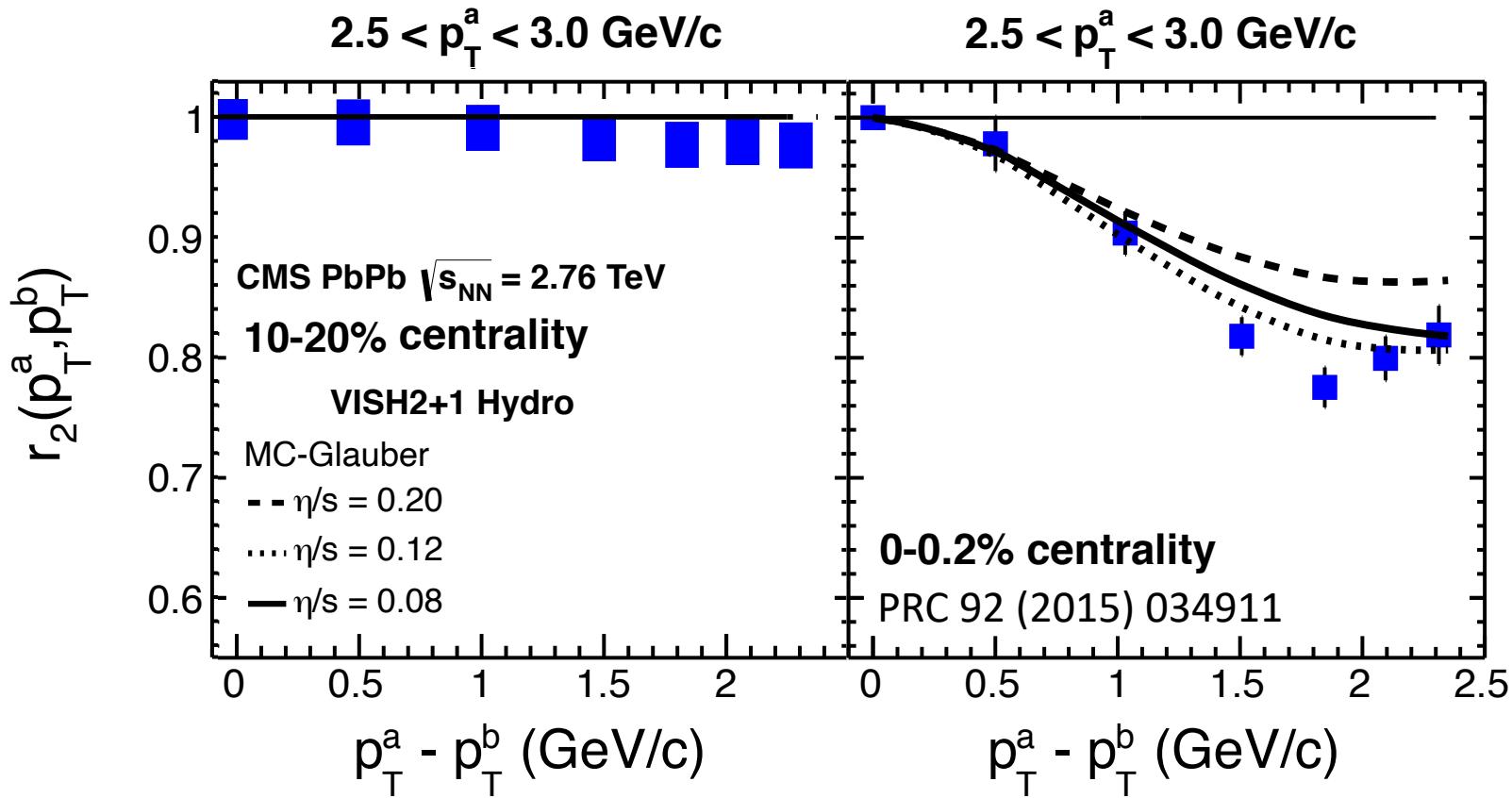
PRC 92 (2015) 034911

# Decorrelation – $p_T$



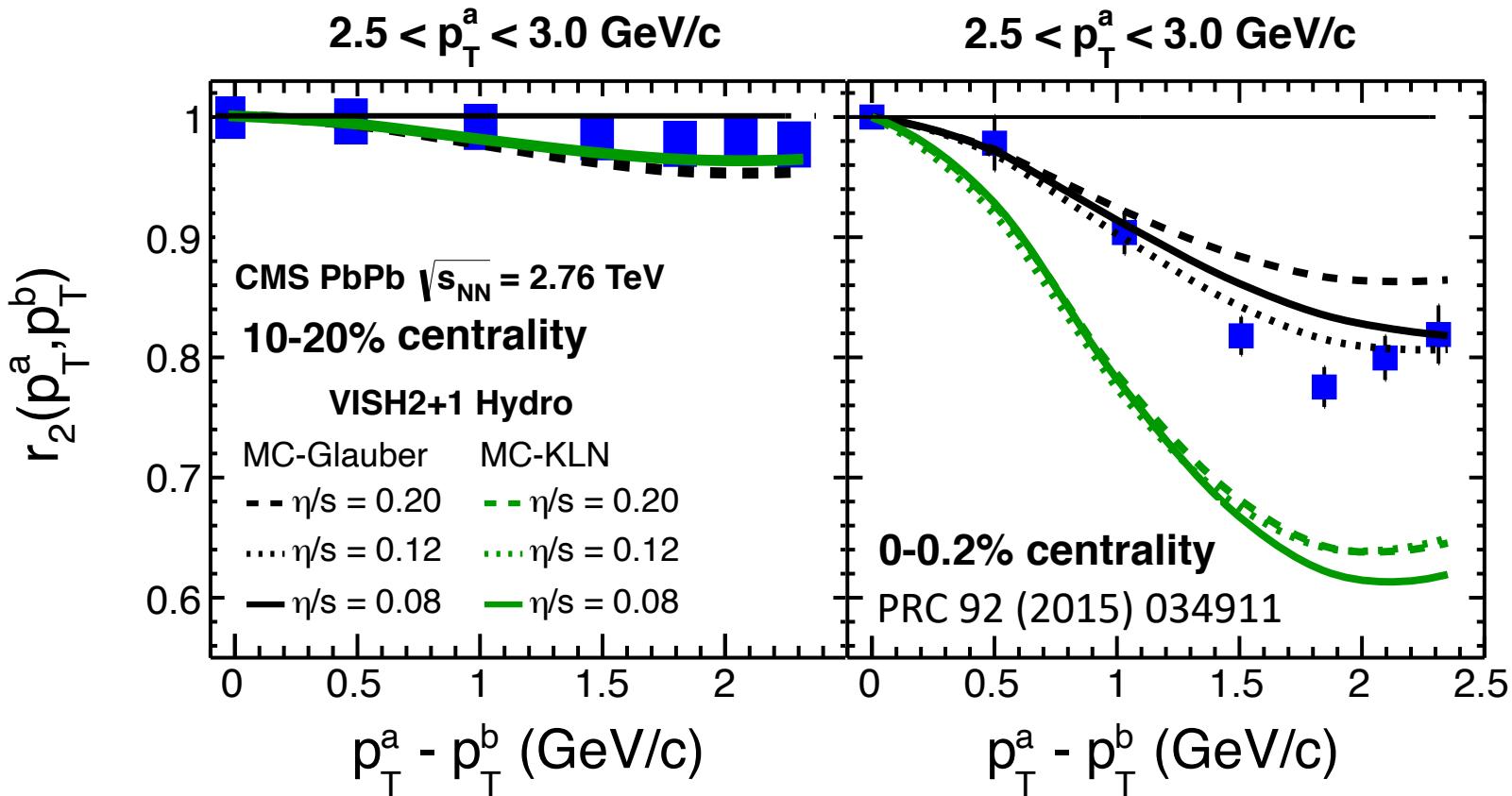
Most prominent at central collisions where fluctuation dominates

# Decorrelation – $p_T$



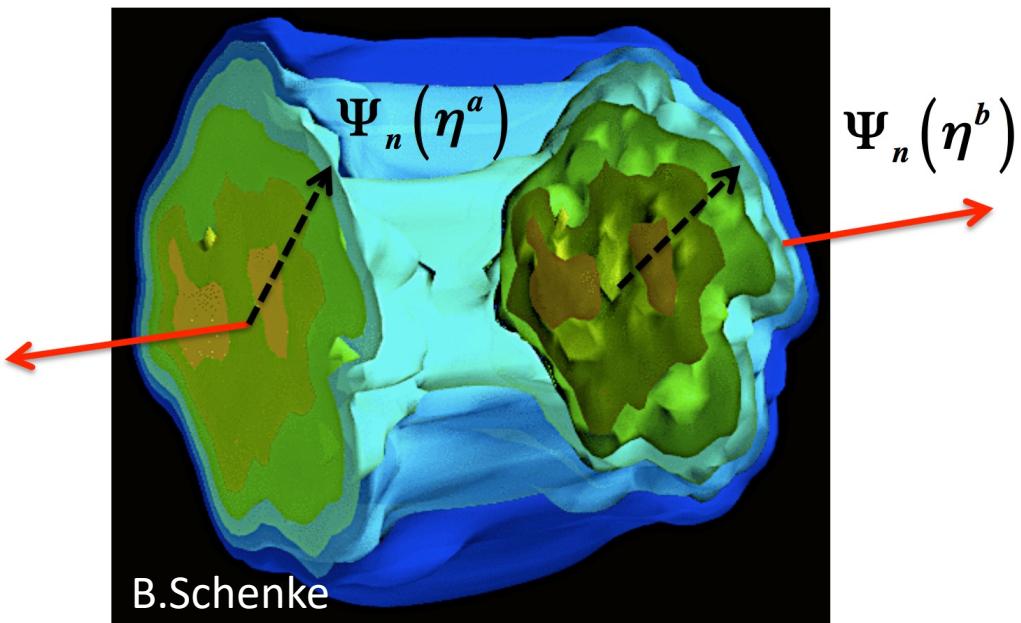
Most prominent at central collisions where fluctuation dominates  
Some dependence on  $\eta/s$

# Decorrelation – $p_T$

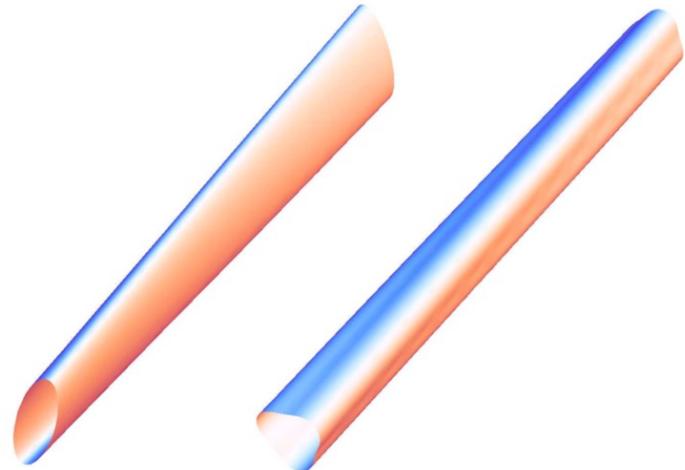


Most prominent at central collisions where fluctuation dominates  
Some dependence on  $\eta/s$   
Very sensitive to initial state geometry

# Decorrelation – Longitudinal



Torqued fireball



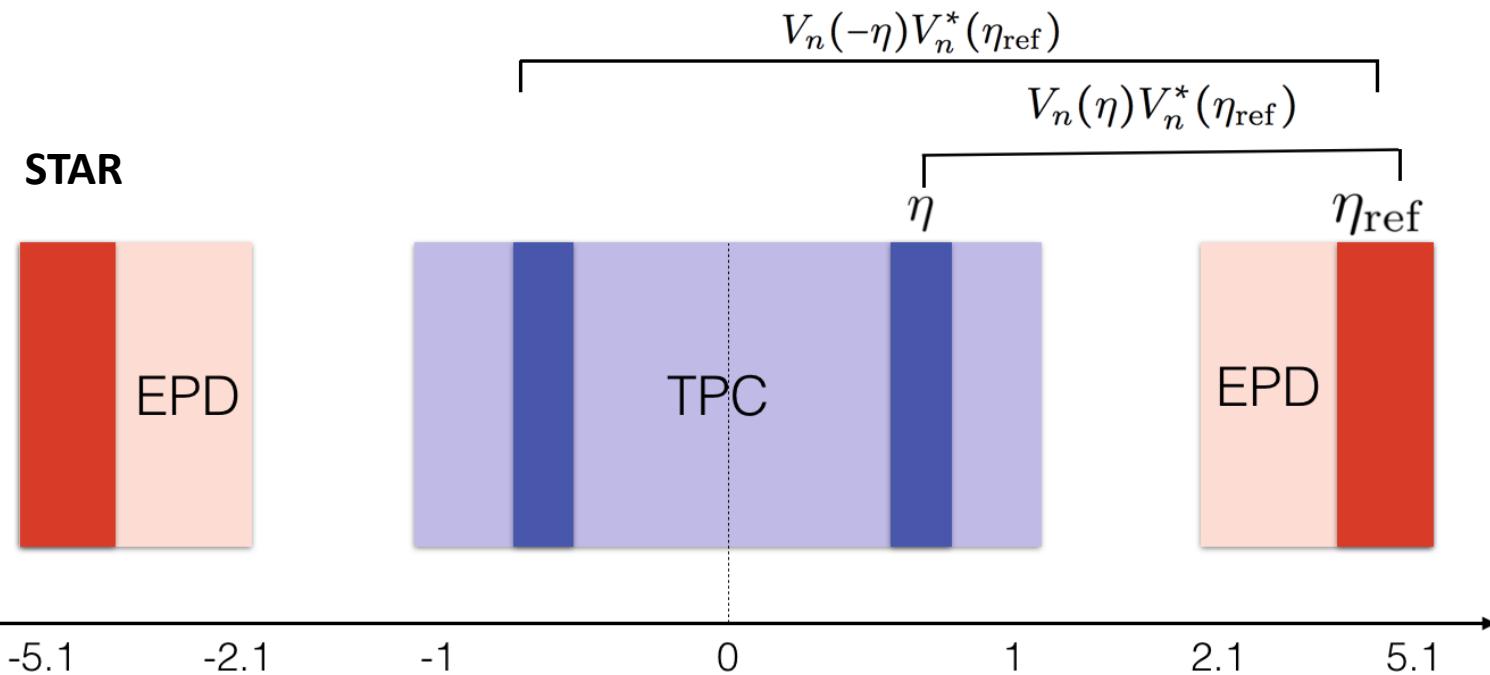
PRC 83 (2011) 034911

Event Plane decorrelation along longitudinal direction  
Provide constraints on how system evolves in 3D

# Decorrelation – Longitudinal

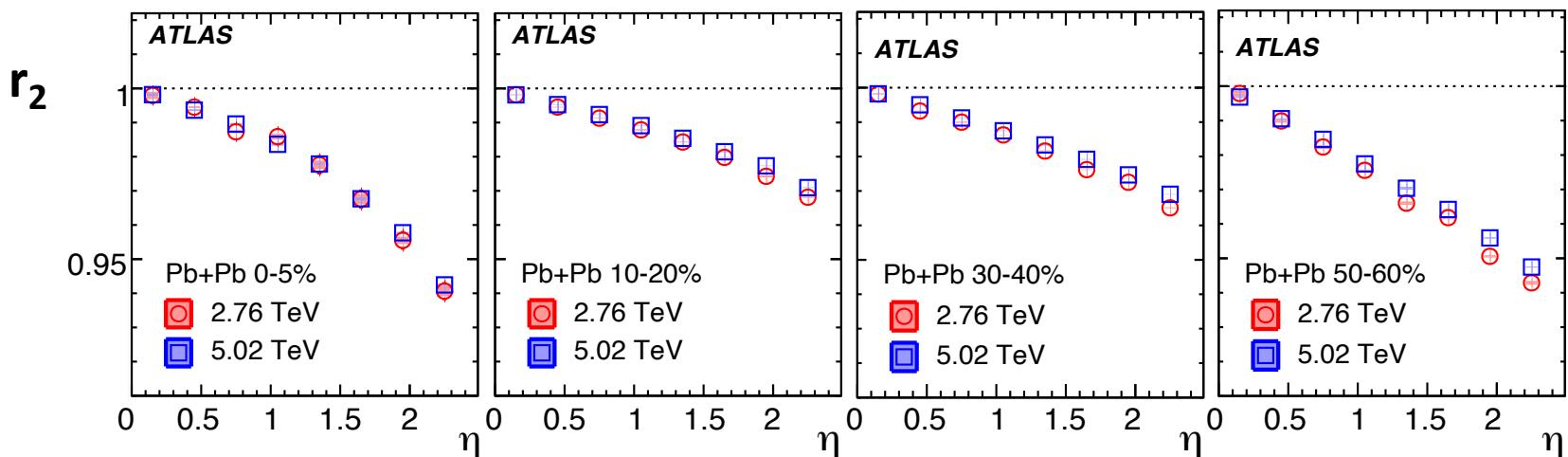
Effects measurable by

$$\begin{aligned} r_n(\eta) &= \frac{\langle V_n(-\eta) V_n^*(\eta_{\text{ref}}) \rangle}{\langle V_n(\eta) V_n^*(\eta_{\text{ref}}) \rangle} \\ &= \frac{\langle v_n(-\eta) v_n(\eta_{\text{ref}}) \cos n(\Psi_n(-\eta) - \Psi_n(\eta_{\text{ref}})) \rangle}{\langle v_n(\eta) v_n(\eta_{\text{ref}}) \cos n(\Psi_n(\eta) - \Psi_n(\eta_{\text{ref}})) \rangle} \end{aligned}$$



# Decorrelation – Longitudinal

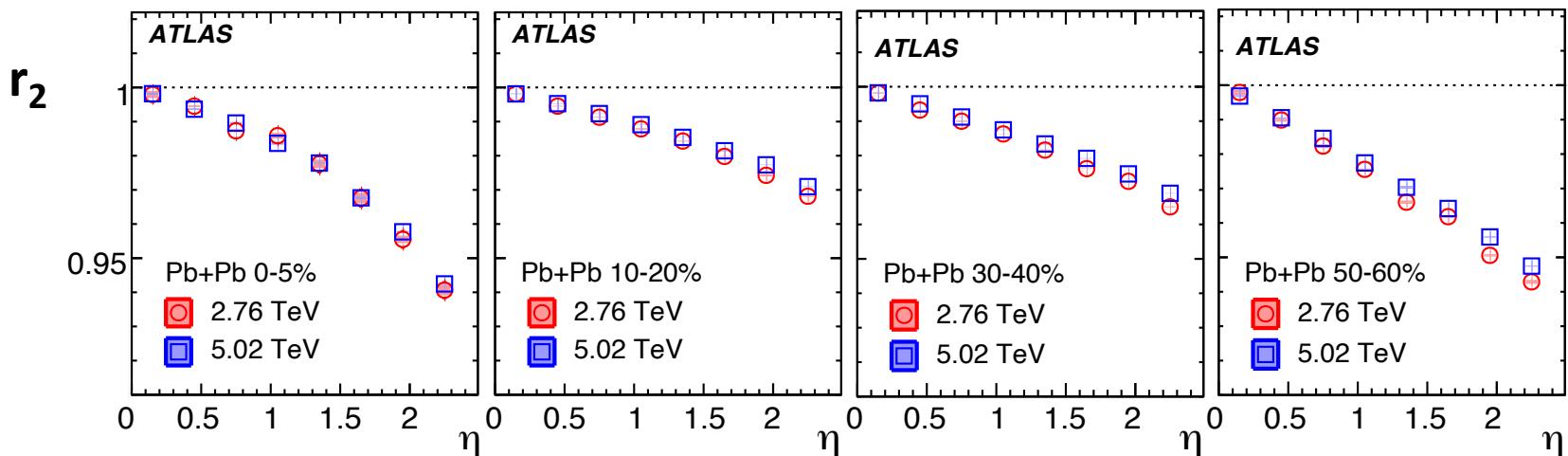
EPJC 76 (2018) 142



$r_2$ : Centrality dependence; Initial geometry + fluctuation

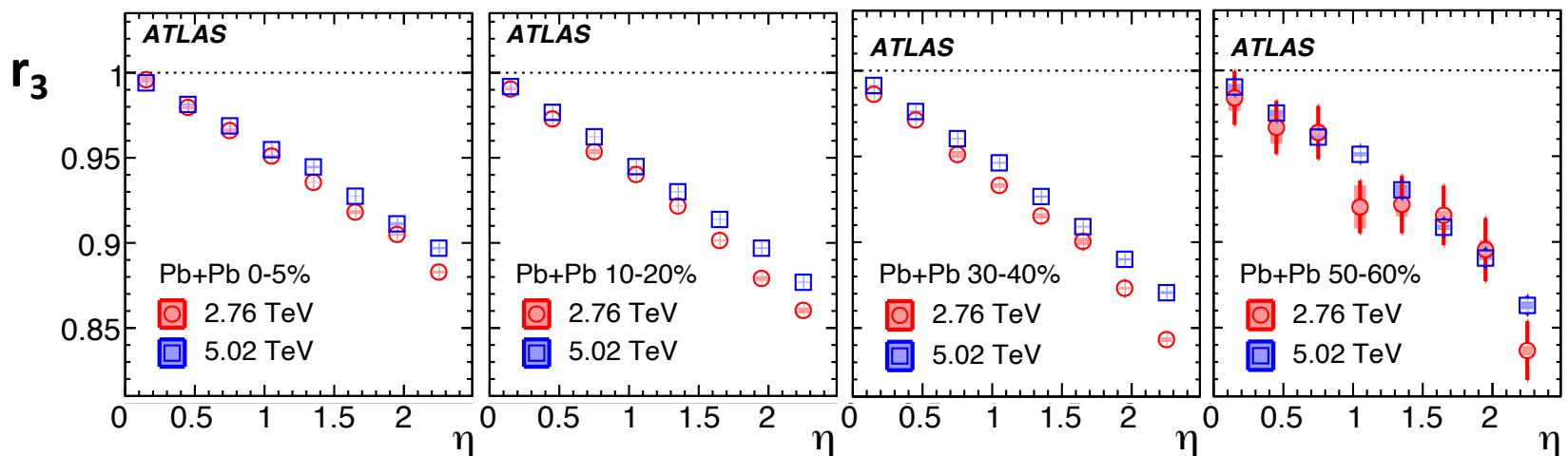
# Decorrelation – Longitudinal

EPJC 76 (2018) 142

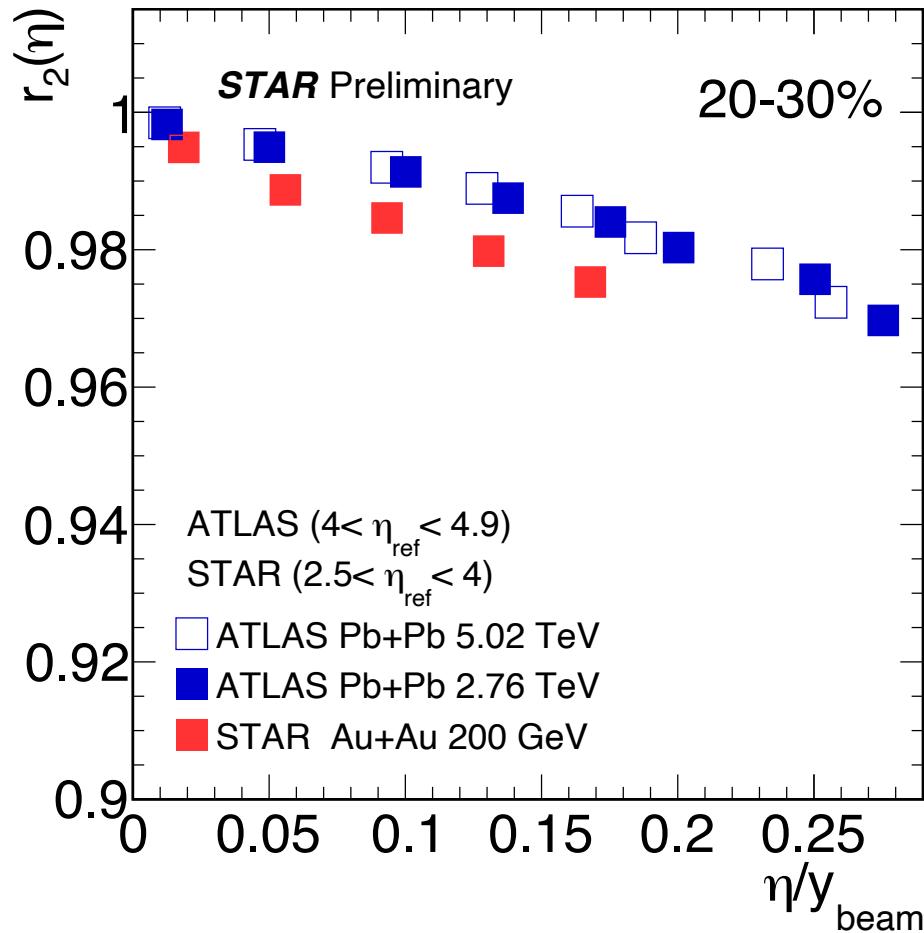


$r_2$ : Centrality dependence; Initial geometry + fluctuation

$r_3$ : No centrality dependence; Pure fluctuation

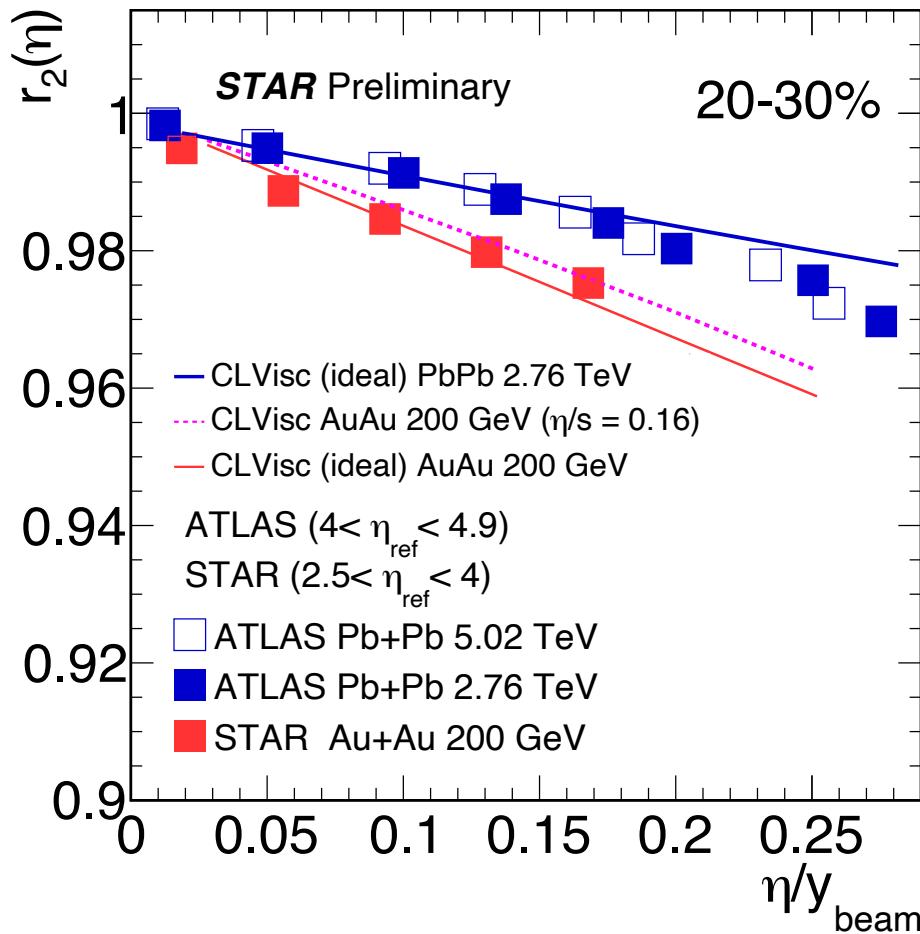


# Decorrelation – Longitudinal



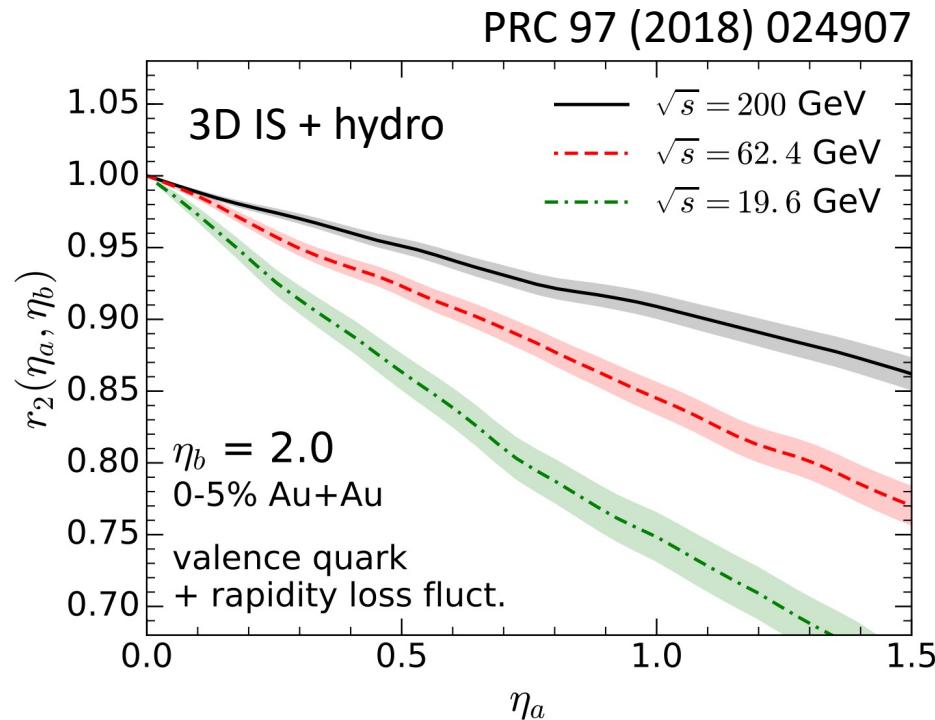
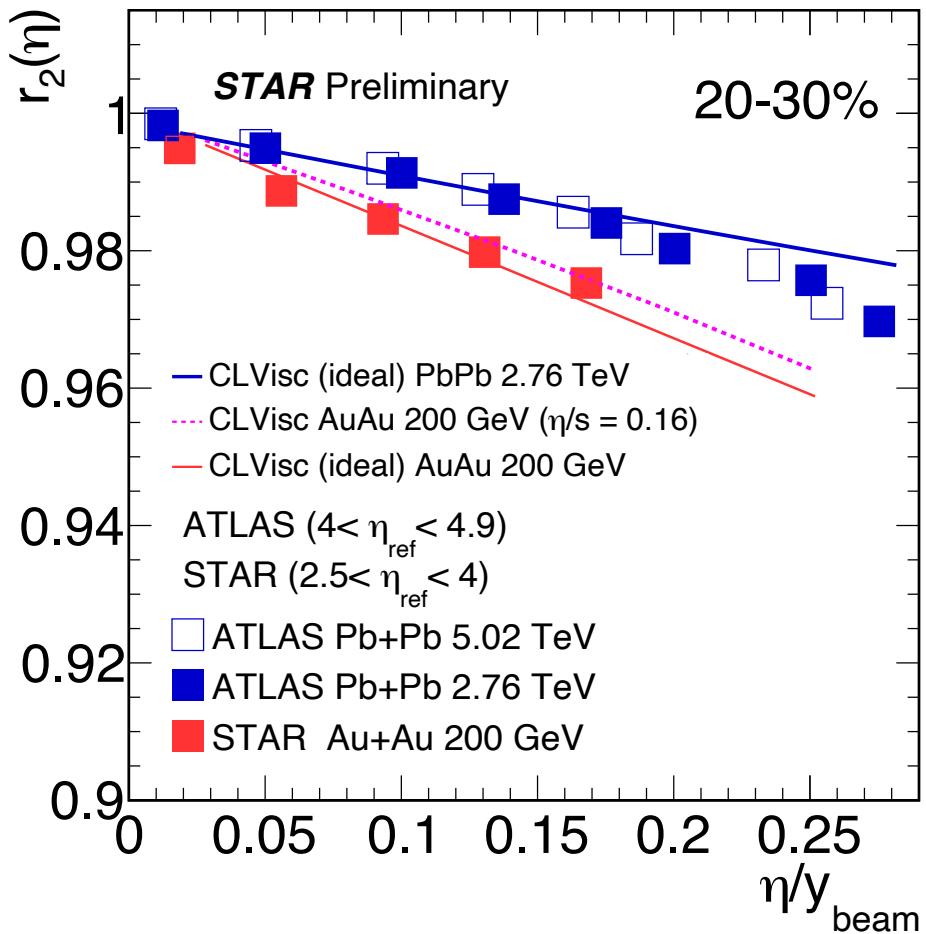
Larger effect seen at RHIC than LHC

# Decorrelation – Longitudinal



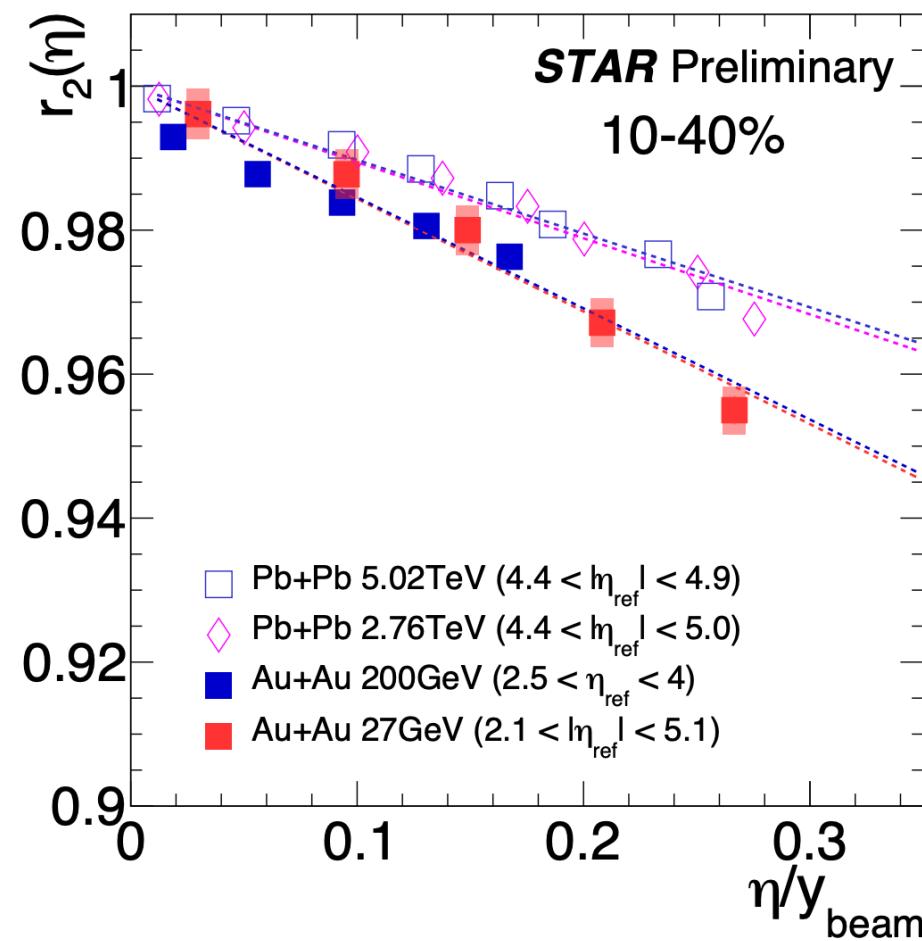
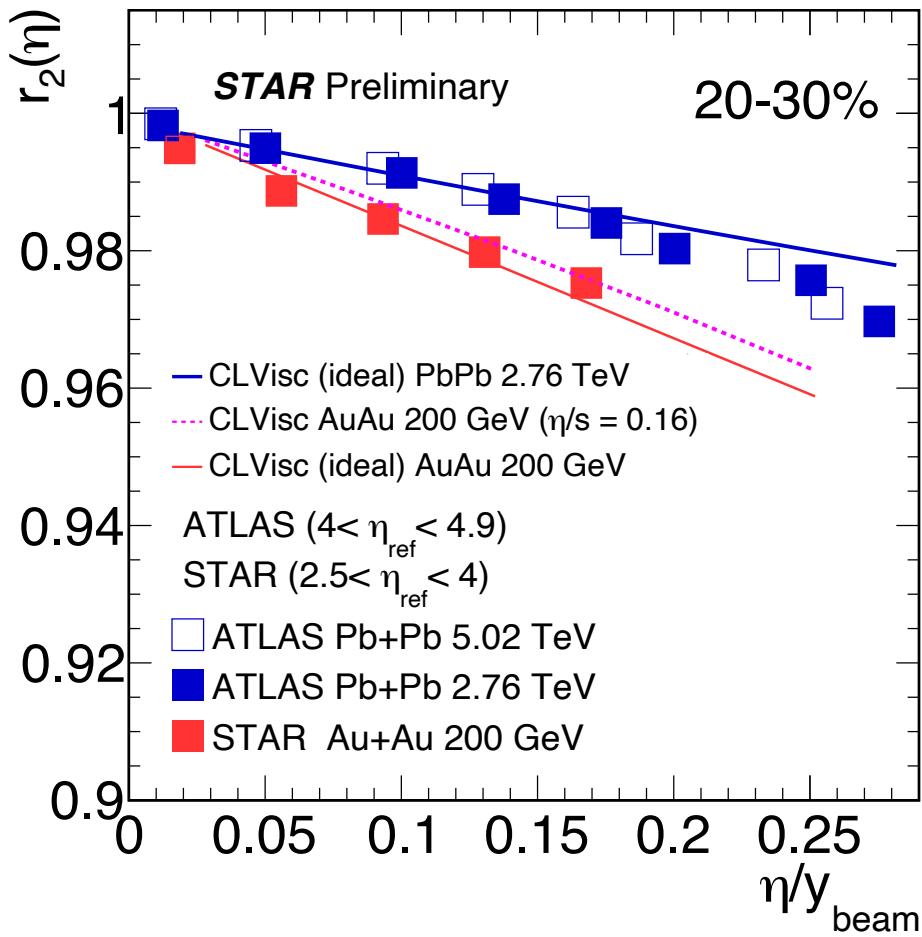
Larger effect seen at RHIC than LHC

# Decorrelation – Longitudinal



Larger effect seen at RHIC than LHC  
3D IS + Hydro predicts larger decorrelation at lower energies

# Decorrelation – Longitudinal



Larger effect seen at RHIC than LHC

3D IS + Hydro predicts larger decorrelation at lower energies

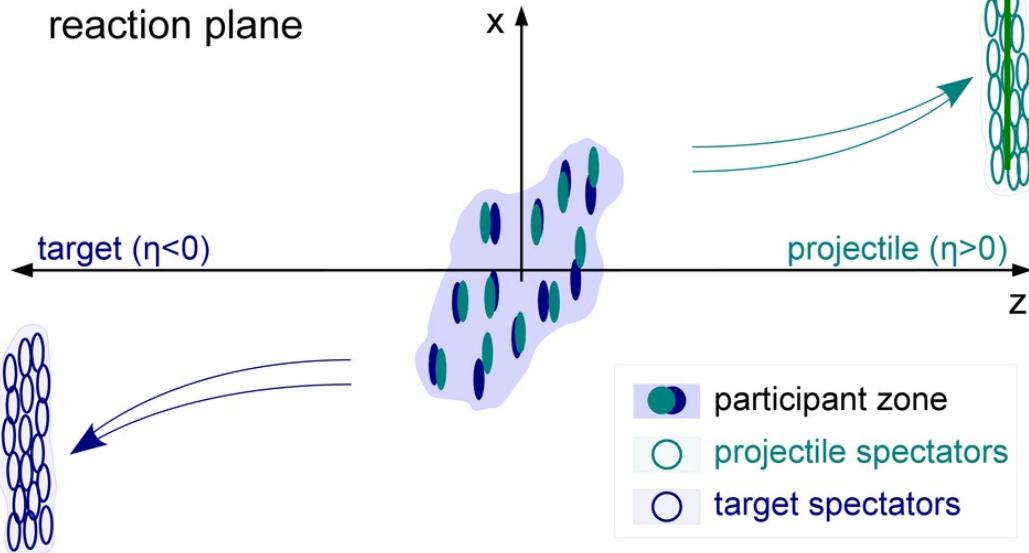
Data suggest same decorrelation at lower RHIC energy?

# Directed flow $v_1$

$$v_1 = \langle \cos(\phi - \psi_{sp}) \rangle$$

Preferred moving direction  
at different rapidity

Collision symmetry  
 $v_1(\eta) = -v_1(-\eta)$



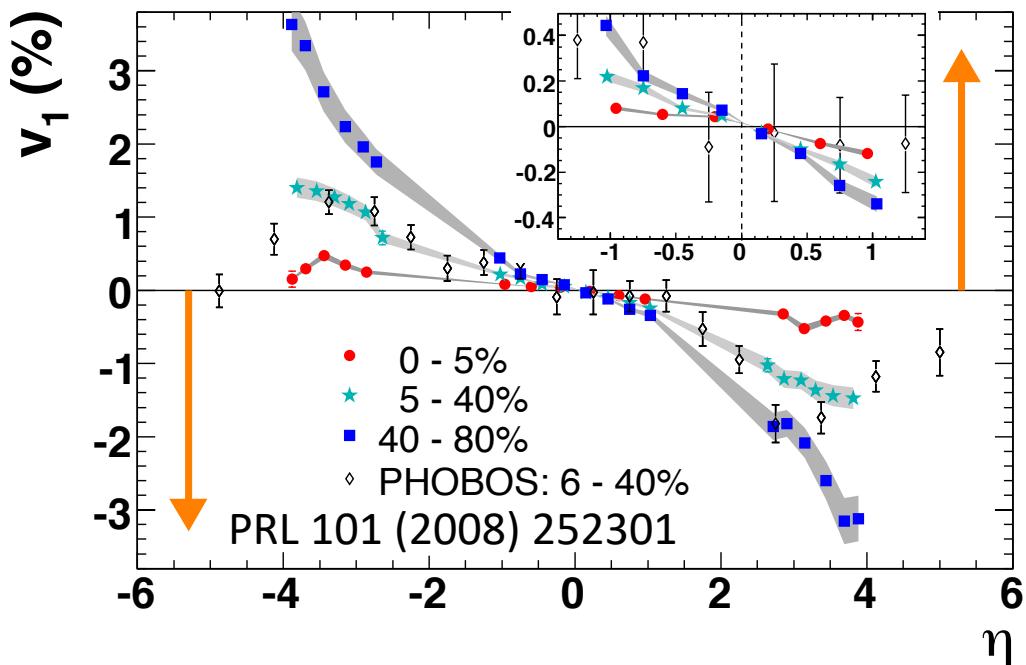
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$$v_1 = \langle \cos(\phi - \psi_{sp}) \rangle$$

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Collision symmetry

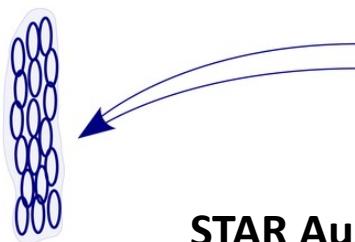
$$v_1(\eta) = -v_1(-\eta)$$



reaction plane

target ( $\eta < 0$ )

projectile ( $\eta > 0$ )

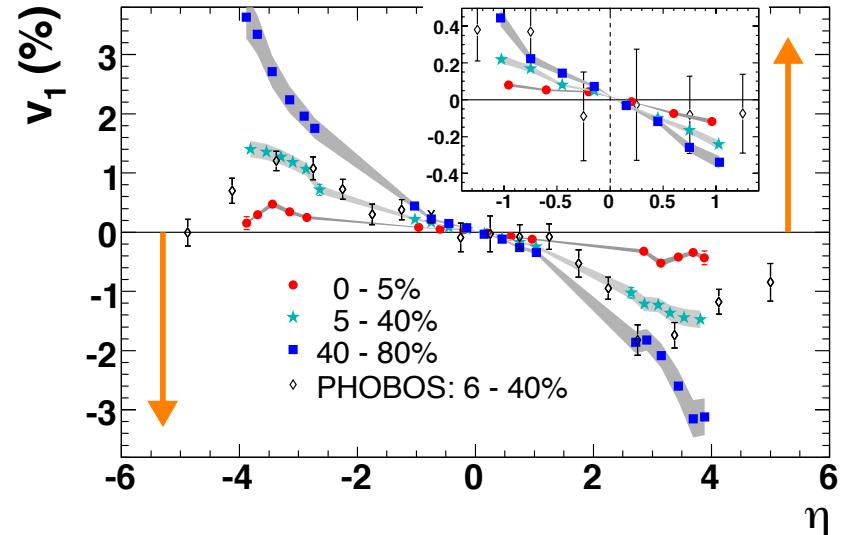


x

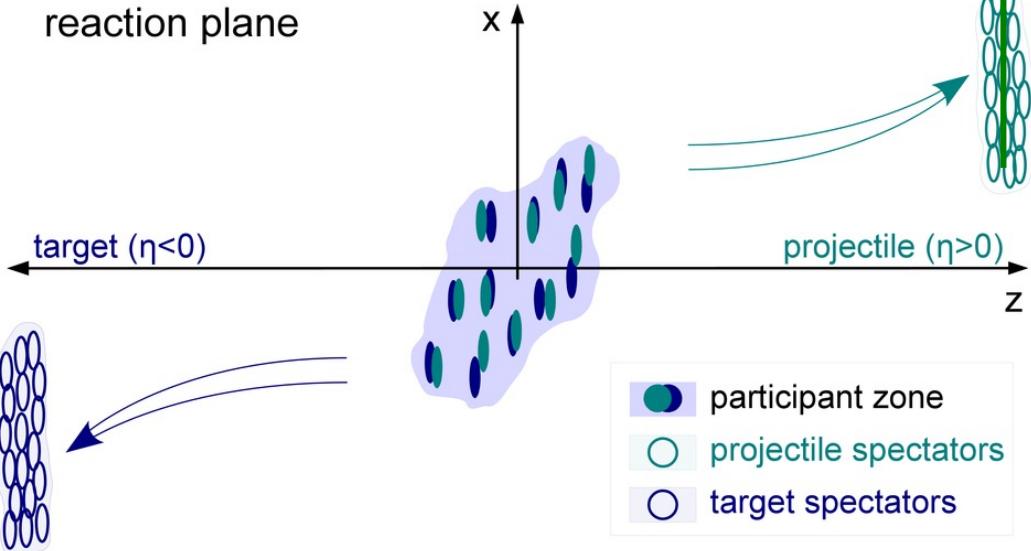
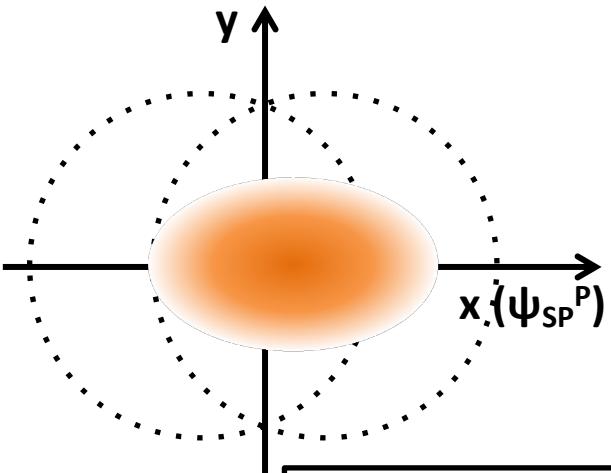
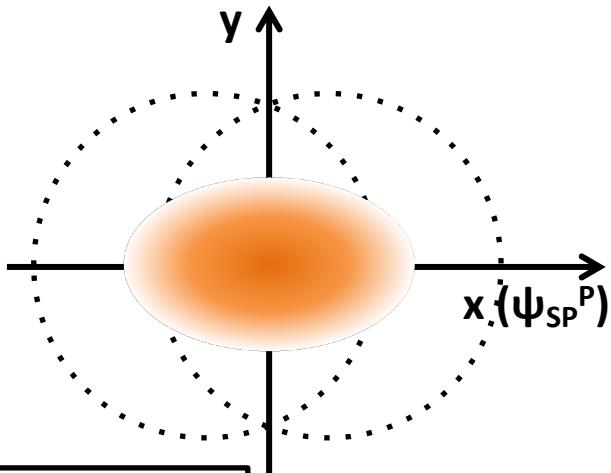
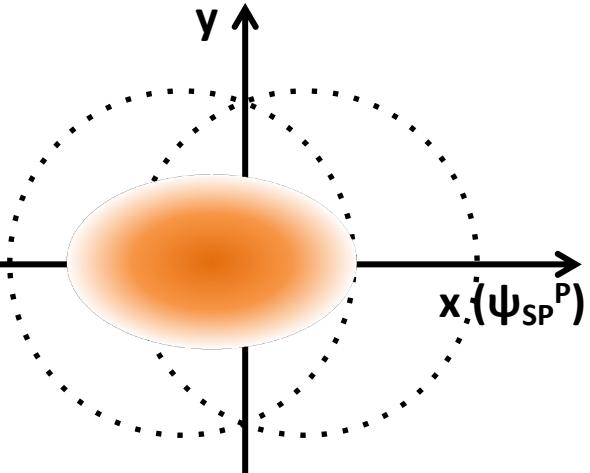
z

- participant zone
- projectile spectators
- target spectators

# Directed flow $v_1$

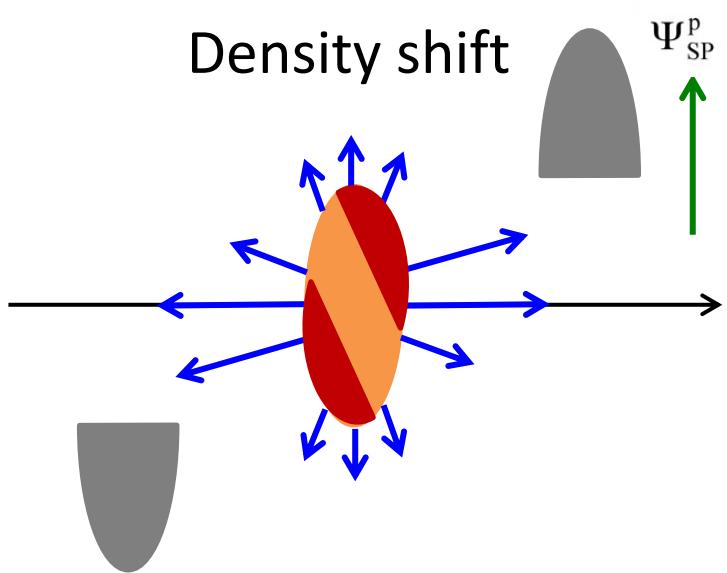


reaction plane

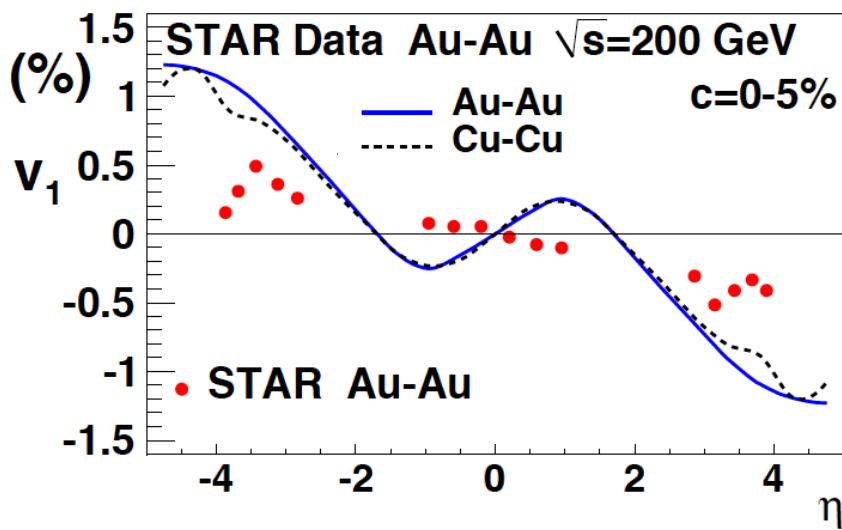
 $\eta < 0, v_1 > 0$  $\eta = 0, v_1 = 0$  $\eta > 0, v_1 < 0$ 

Momentum distribution

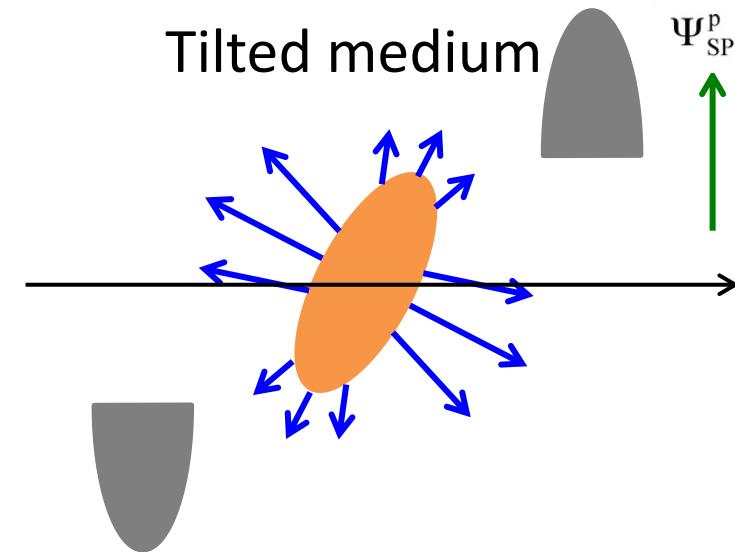
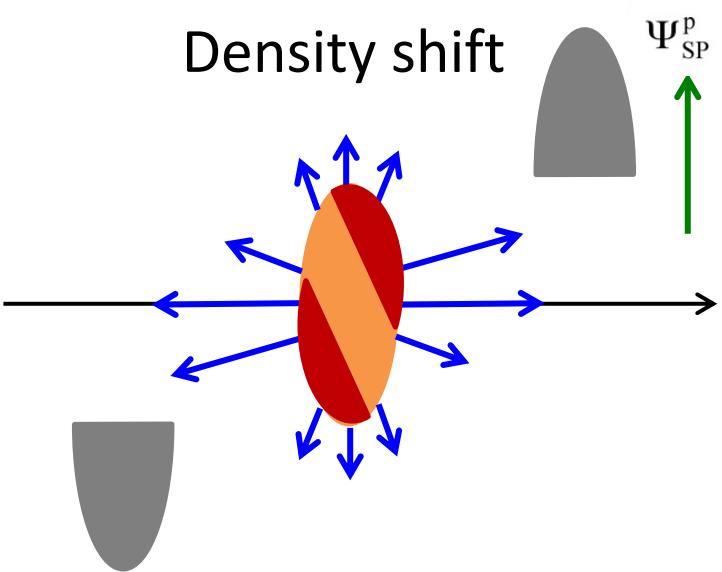
# Directed flow $v_1$



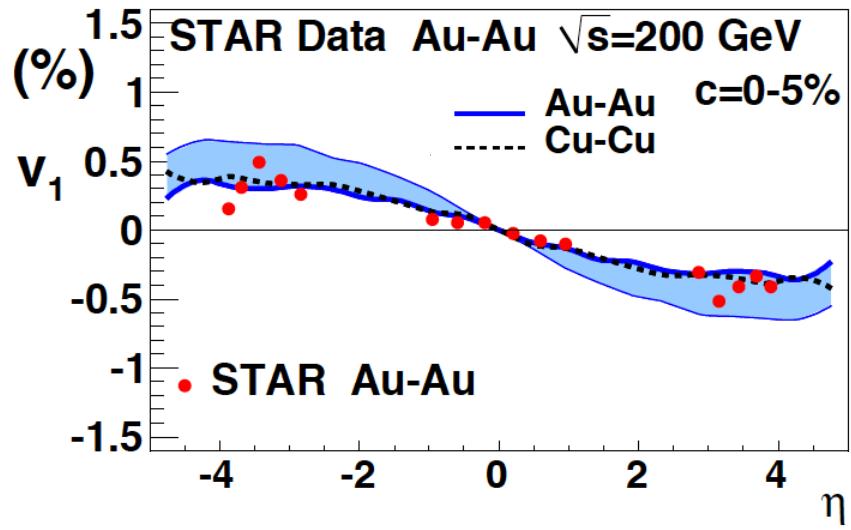
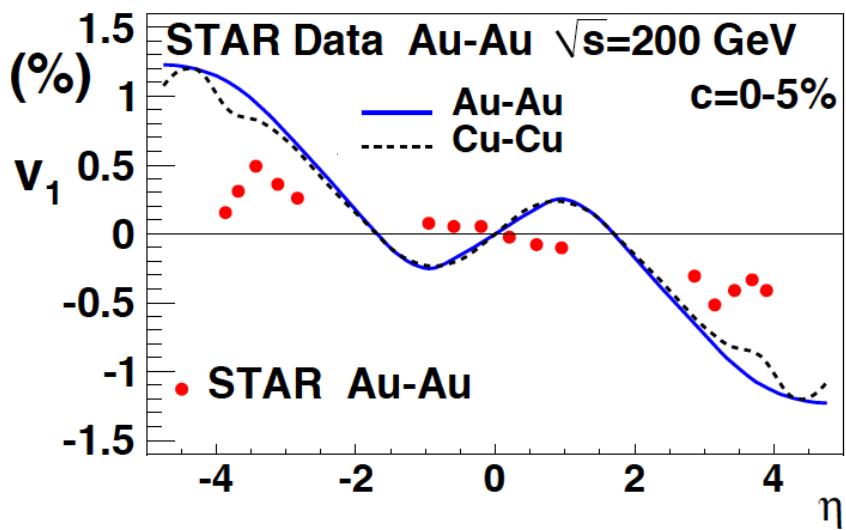
PRC 81 (2010) 054902



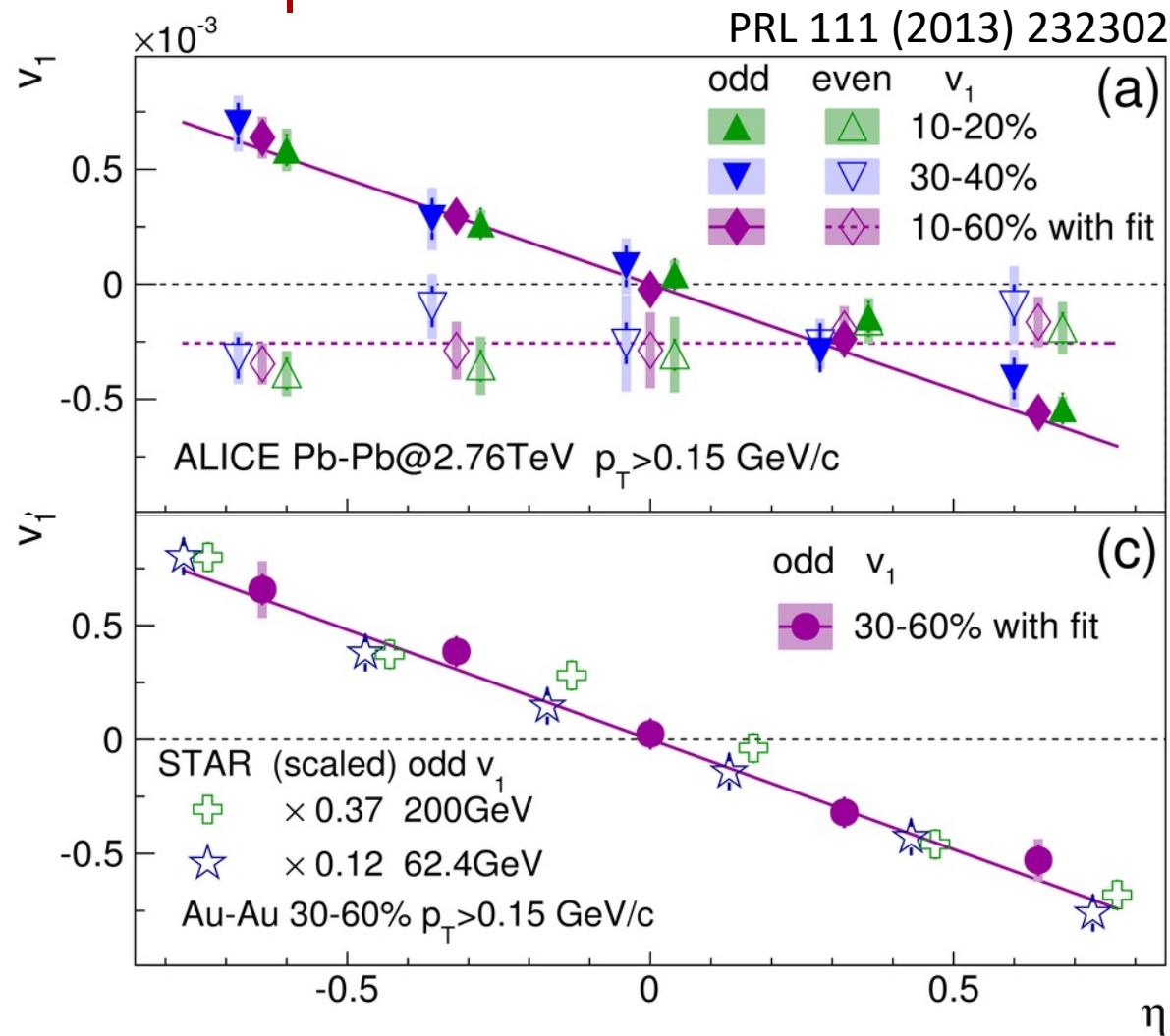
# Directed flow $v_1$



PRC 81 (2010) 054902



# Directed flow $v_1$



Larger slope of  $v_1^{\text{odd}}$  at RHIC energies: smaller tilt at LHC

# Directed flow $v_1$

$$v_1 = \langle \cos(\phi - \psi_{sp}) \rangle$$

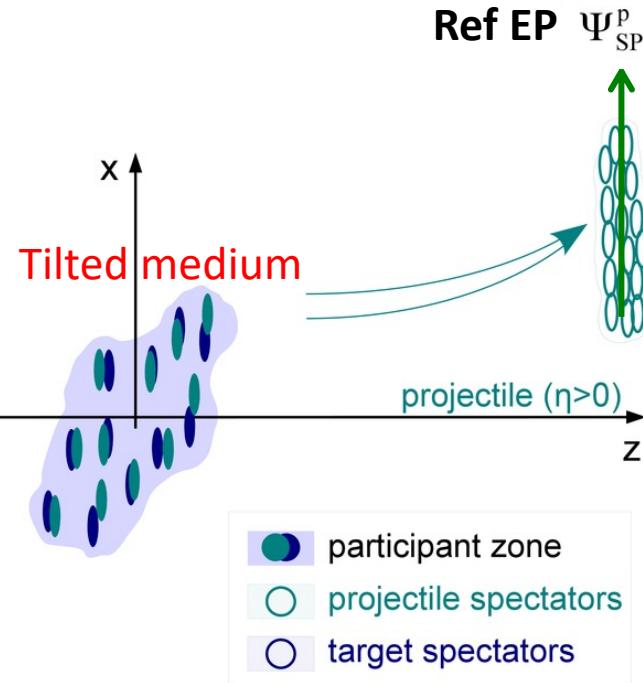
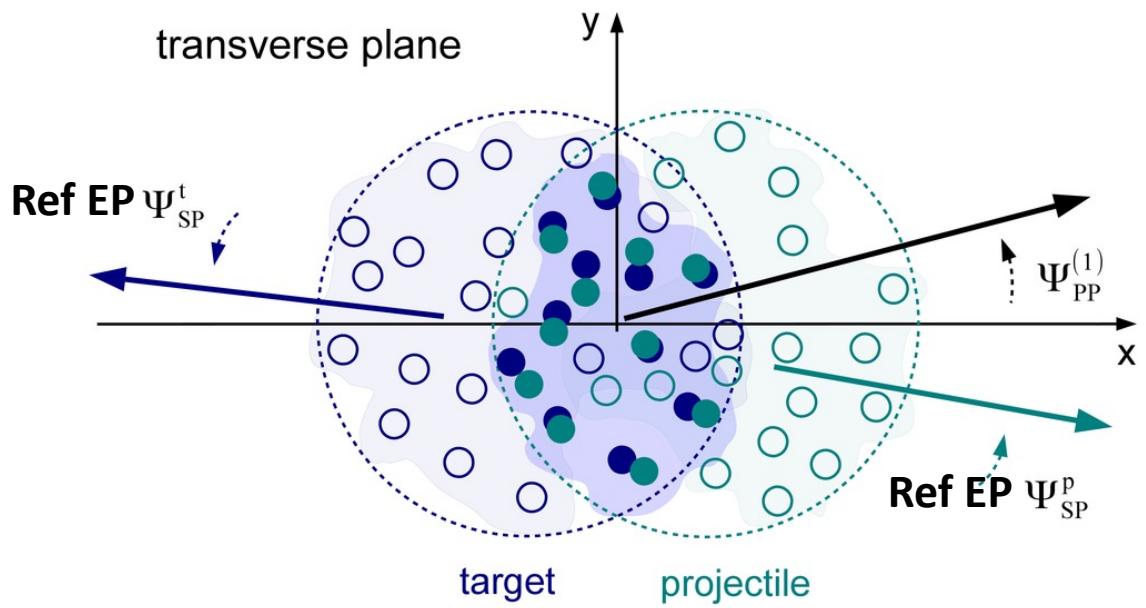
Preferred moving direction  
at different rapidity

Collision symmetry

$$v_1(\eta) = -v_1(-\eta)$$

$$v_1^{\text{odd}}$$

transverse plane

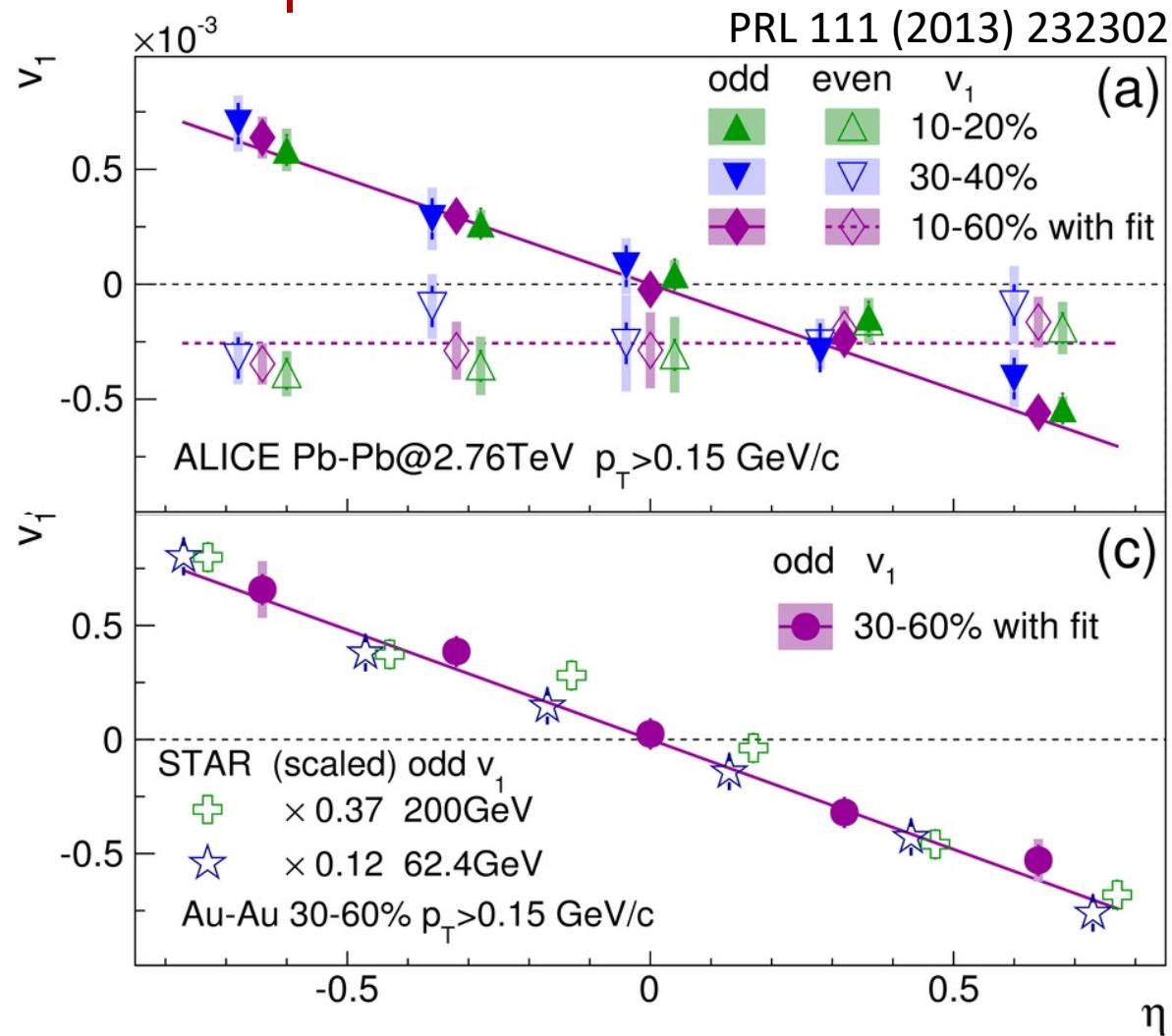


Transverse plane  
geometry fluctuation

$$v_1(\eta) = v_1(-\eta)$$

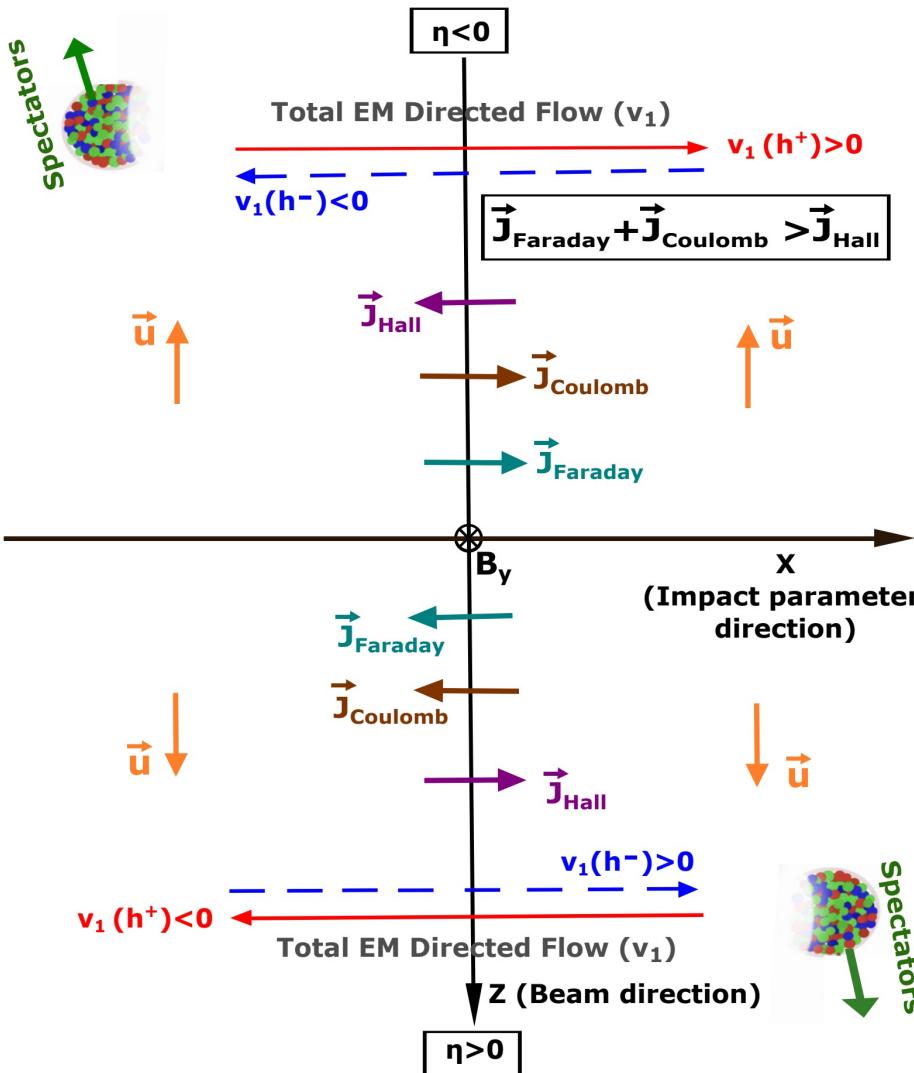
$$v_1^{\text{even}}$$

# Directed flow $v_1$



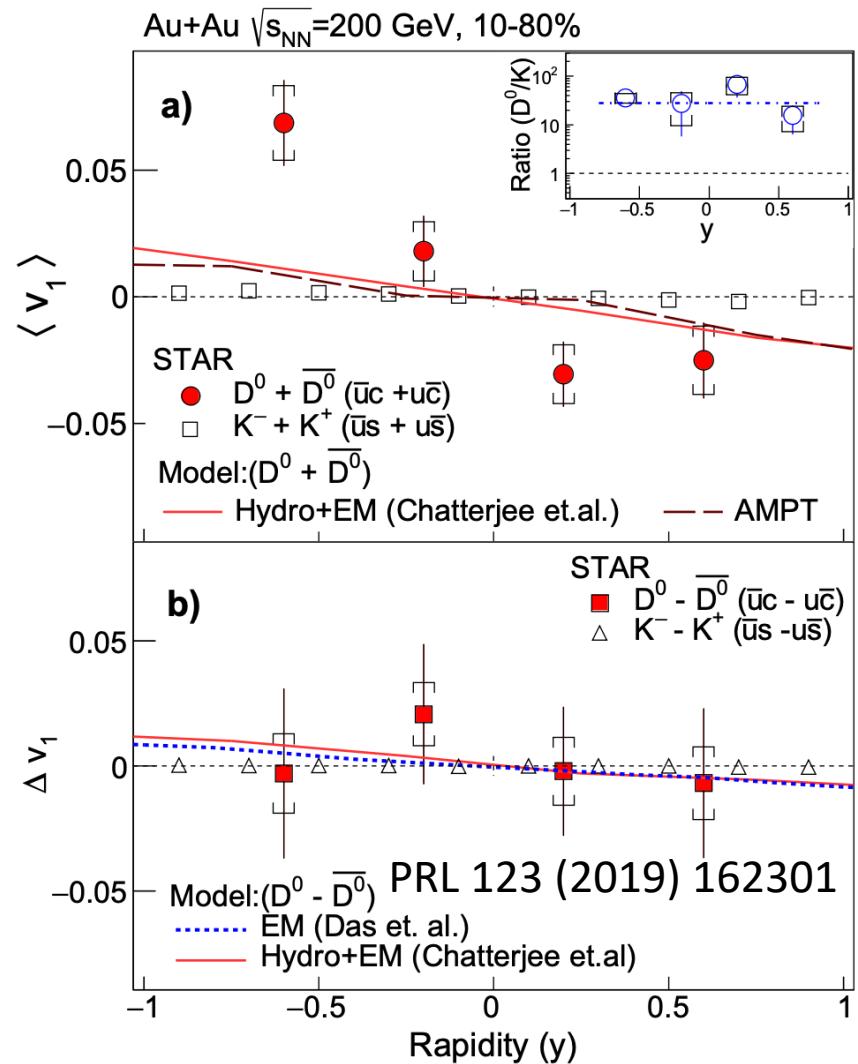
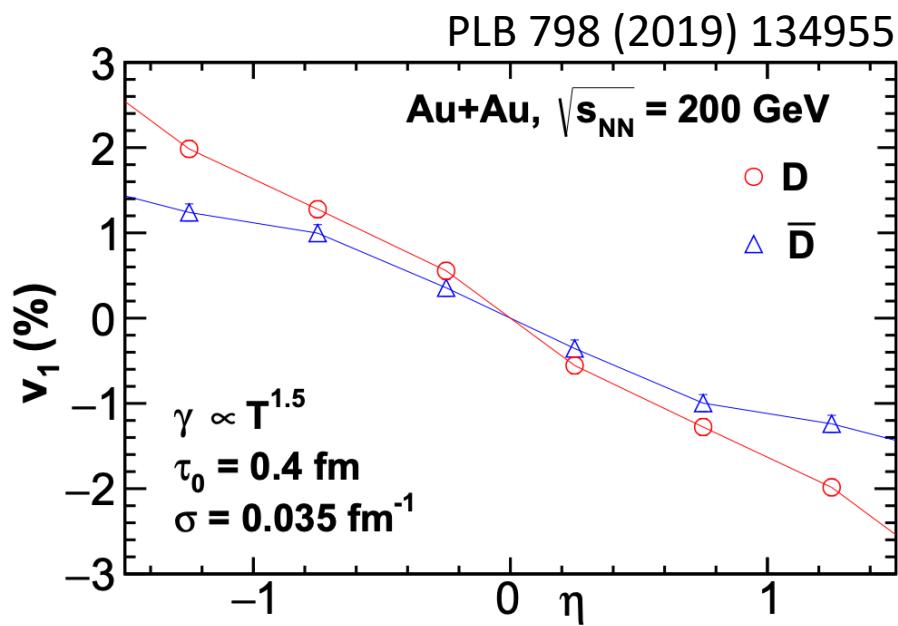
Larger slope of  $v_1^{\text{odd}}$  at RHIC energies: smaller tilt at LHC  
 Non-zero  $v_1^{\text{even}}$ : sizable geometry fluctuation

# Directed flow $v_1$ – B & E field effects



Main electro-magnetic effects on  $v_1$

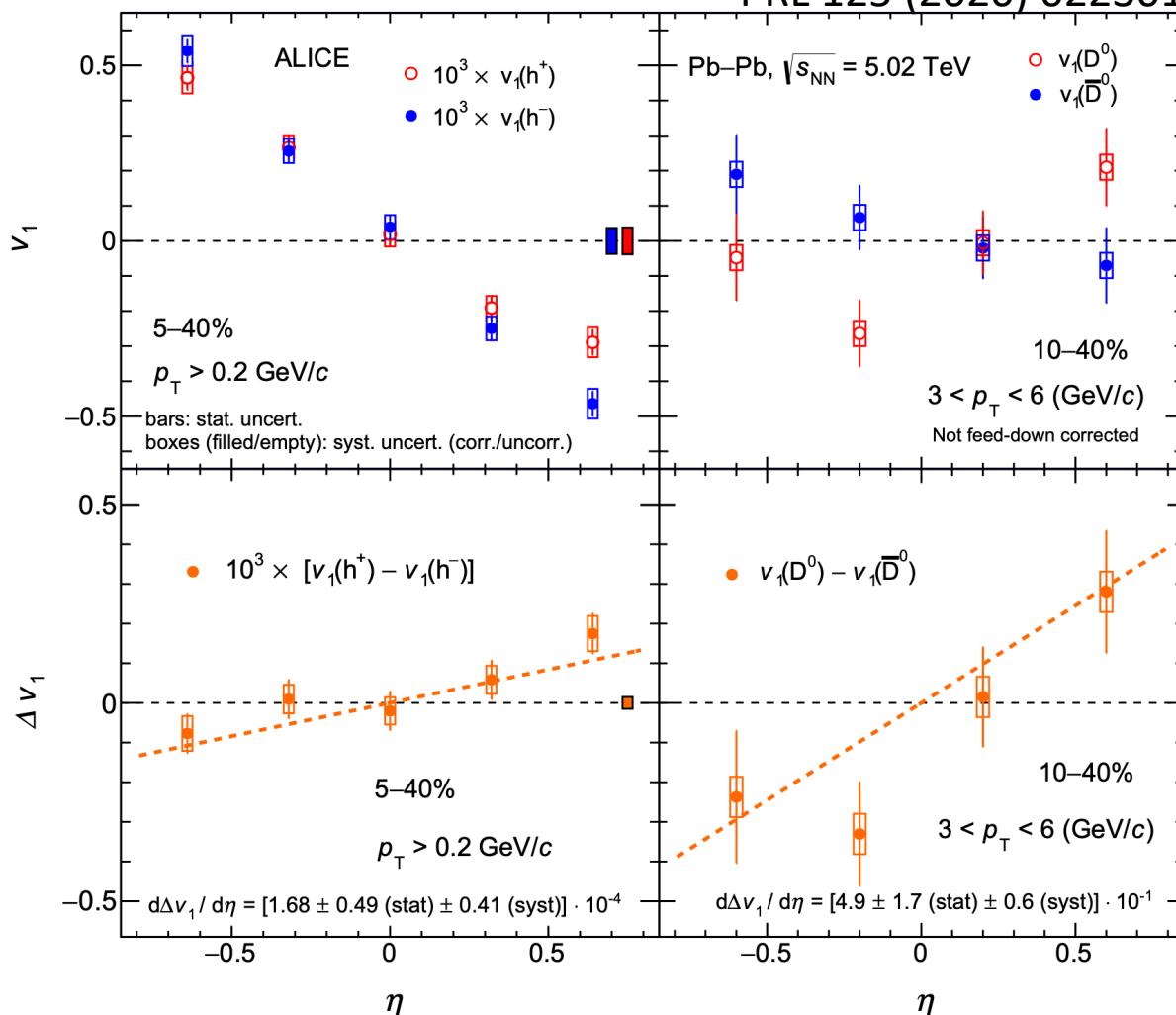
# Directed flow $v_1$ – B & E field effects



Models predict negative slope of  $\Delta v_1$  @ RHIC  
Faraday + Coulomb > Hall

# Directed flow $v_1$ – B & E field effects

PRL 125 (2020) 022301

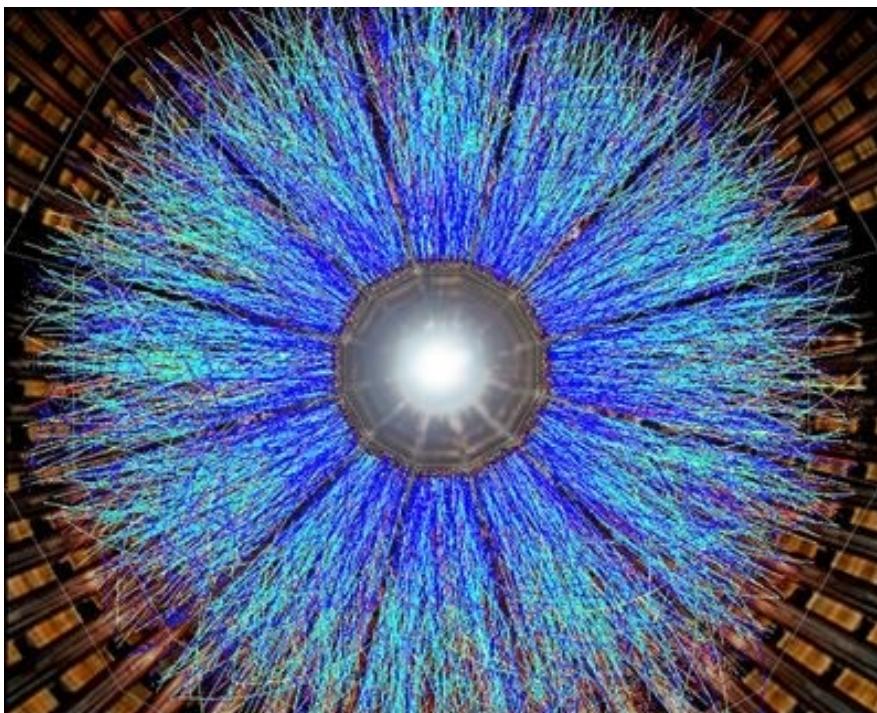


Hint of positive slope of  $\Delta v_1$  @ LHC  
Faraday + Coulomb < Hall

# Summary

Collective flow measurements are versatile tools to study all stages of heavy ion collision

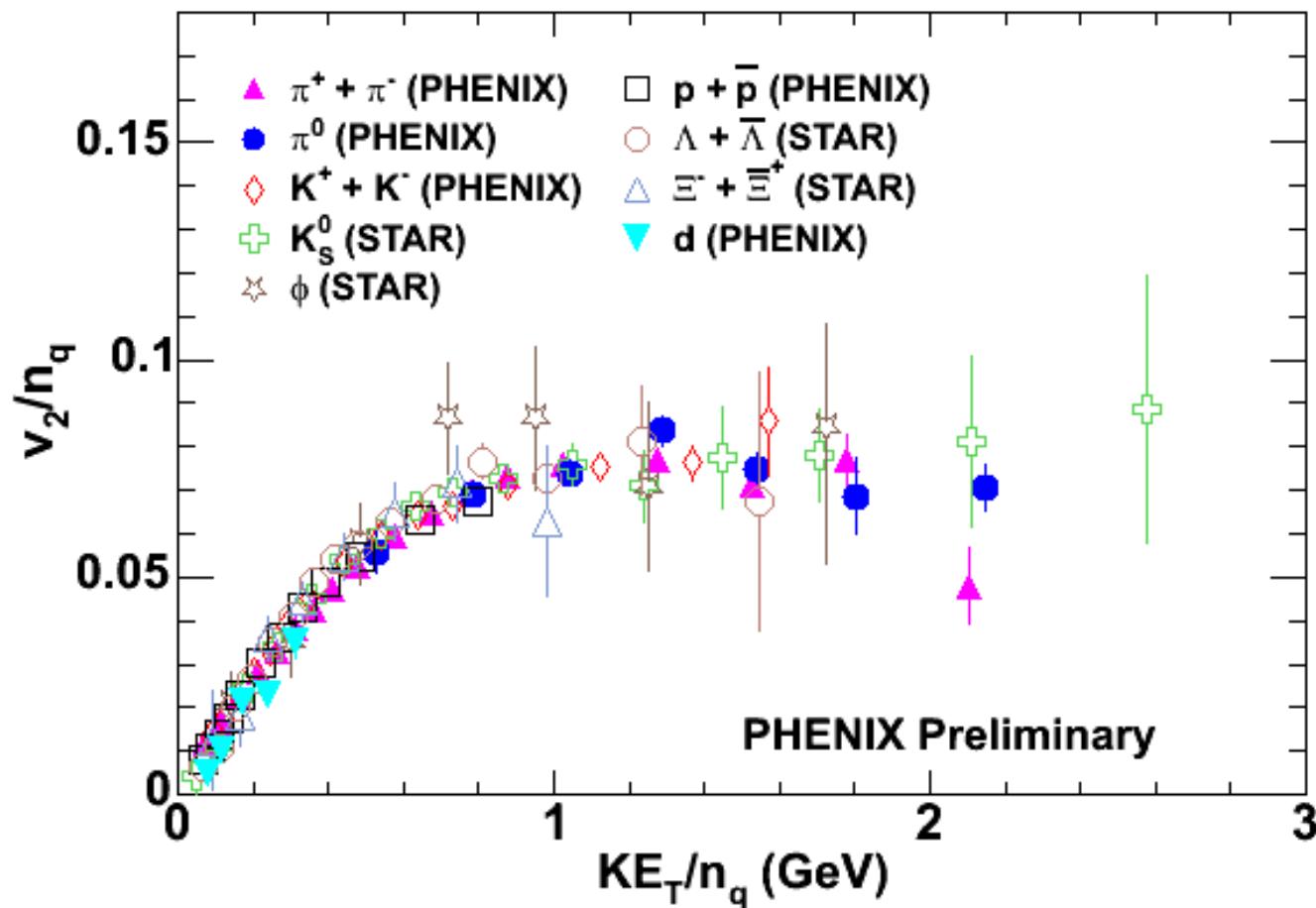
- QGP viscosity  $\Leftrightarrow v_n$  vs centrality;  $v_n$  vs energy;  $v_n$  vs  $p_T$ ; ...
- Initial state  $\Leftrightarrow$  multi-particle  $v_n$ ; decorrelation;  $v_1$ ; ...
- Hadronic phase  $\Leftrightarrow$  PID  $v_n$ ; ...
- ...



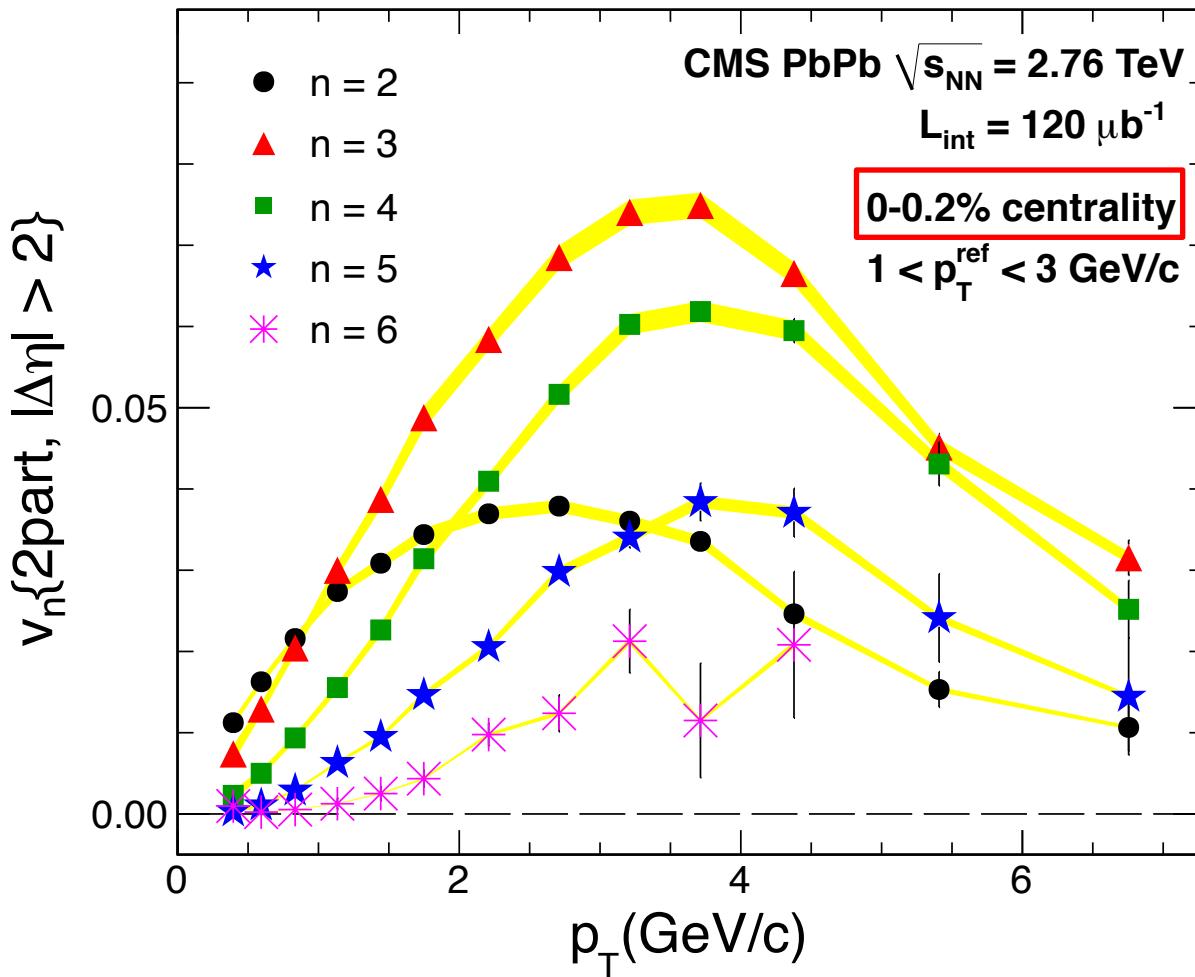
Questions to  
[zhenyuchen@sdu.edu.cn](mailto:zhenyuchen@sdu.edu.cn)



# Back up



# $v_n$ vs centrality



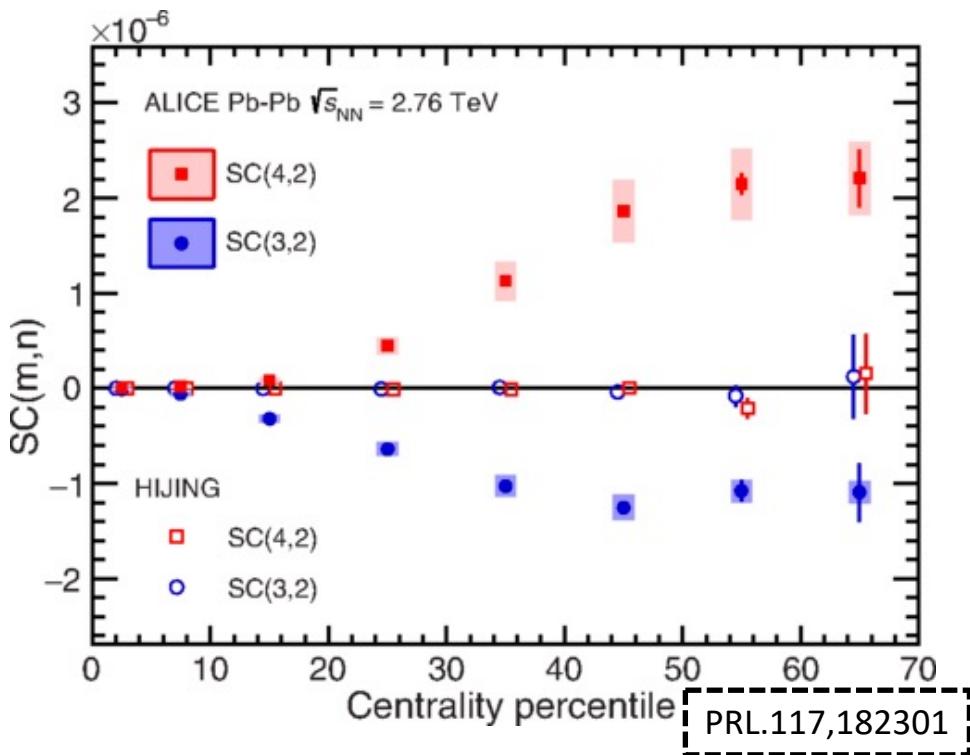
Probe geometry fluctuation with Ultra-Central-Collision

# Symmetric cumulants

- Correlation between harmonics:

$$SC(n,m) = \left\langle v_n^2 v_m^2 \right\rangle - \left\langle v_n^2 \right\rangle \left\langle v_m^2 \right\rangle$$

- Symmetric Cumulant (SC)  
developed by ALICE
  - Based on 4-particle cumulant technique
  - Non-flow highly suppressed at high multiplicity



$SC(2,3) < 0 \rightarrow v_2$  and  $v_3$  are **anti-correlated**  
 $SC(2,4) > 0 \rightarrow v_2$  and  $v_4$  are **correlated**

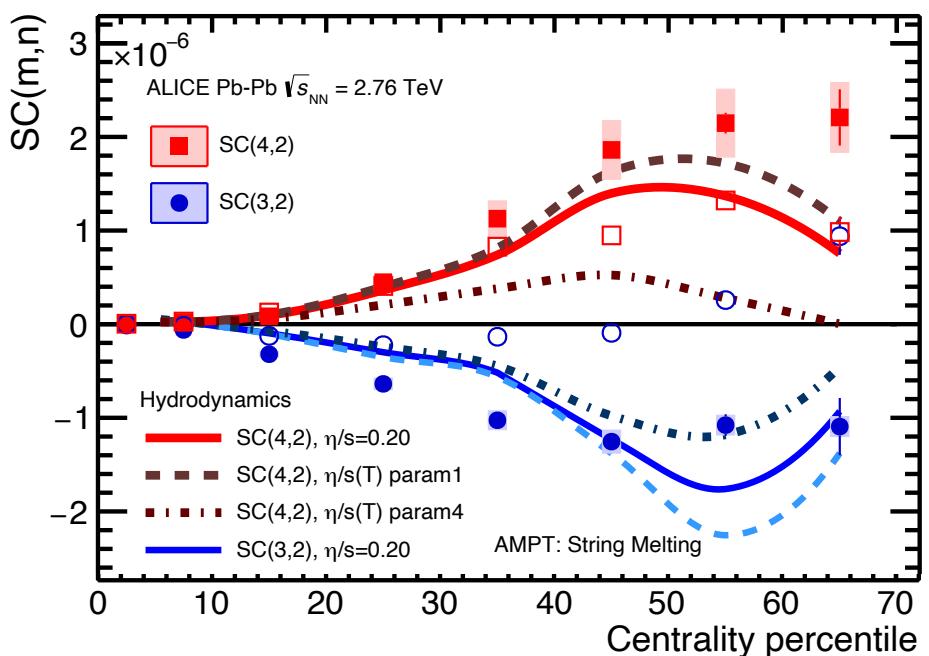
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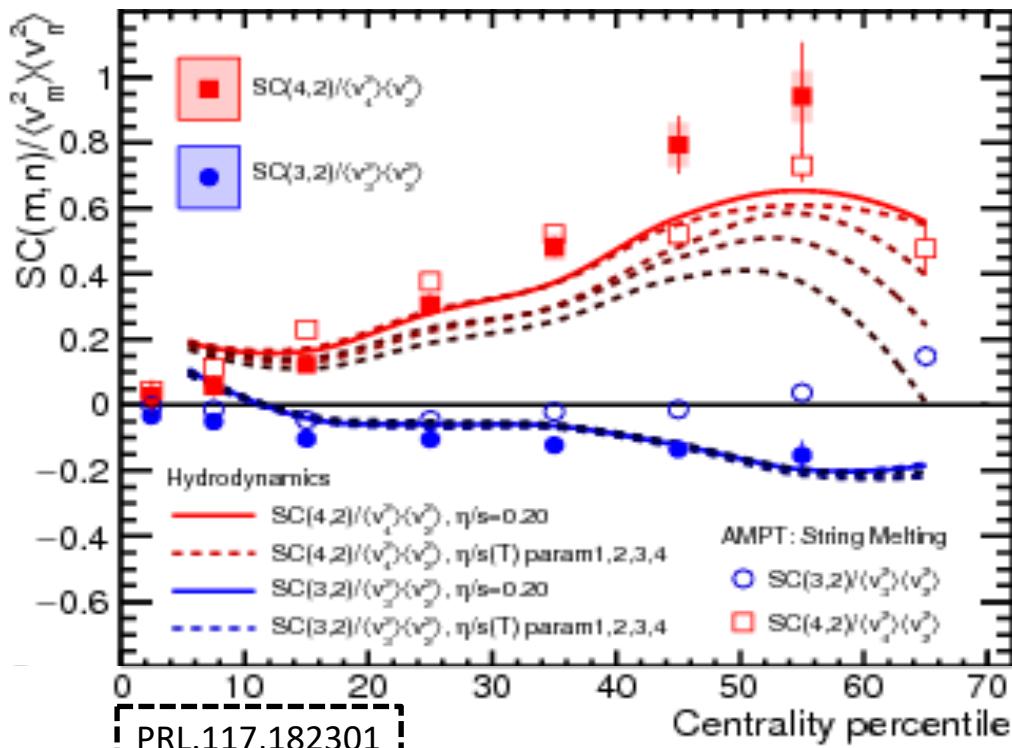


PRL.117,182301

$SC(2,3) < 0 \rightarrow v_2$  and  $v_3$  are **anti-correlated**  
 $SC(2,4) > 0 \rightarrow v_2$  and  $v_4$  are **correlated**

# Symmetric cumulants

- SC normalized by  $\langle v_n^2 \rangle \langle v_m^2 \rangle$
- Normalized SC(2,4)
  - Probe Initial State fluctuation
  - Sensitive to medium response
- Normalized SC(2,3)
  - Probe Initial State fluctuation
  - **Inensitive** to medium response
- Constraints on models
  - Giacalone et al. [arxiv 1605.08303](#)
  - Gardim et al. [arxiv 1608.02982](#)
  - Norhona-Holster et al. [arxiv 1609.05171](#)
  - Welsh et al. [arxiv 1609.09418](#)
  - Zhu et al. [arxiv 1608.05305](#)



# Mass ordering broken for phi

