

第十六届TeV物理工作组学术研讨会

16th TeV Workshop

Heavy long-lived coannihilation partner from
inelastic Dark Matter model and its signatures
at the LHC

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Date: Nov 9, 2022

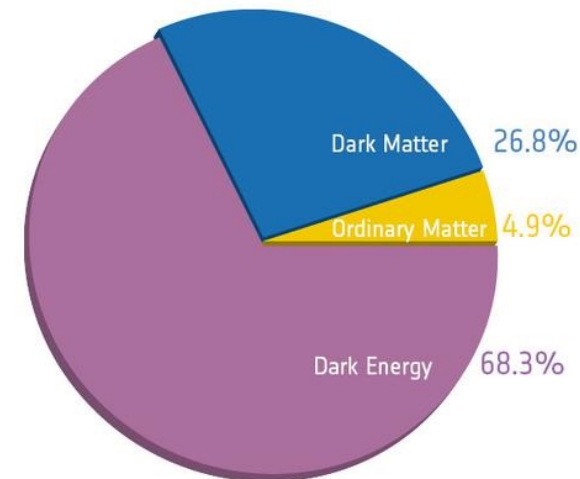
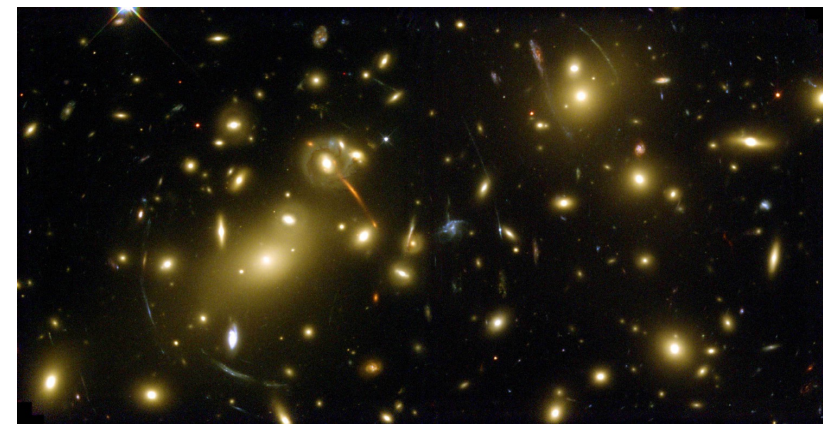
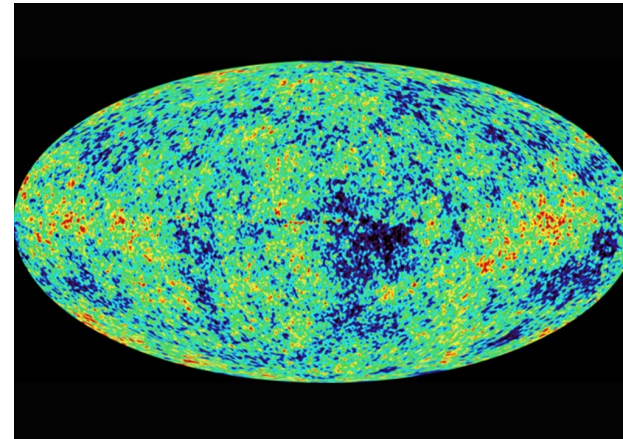
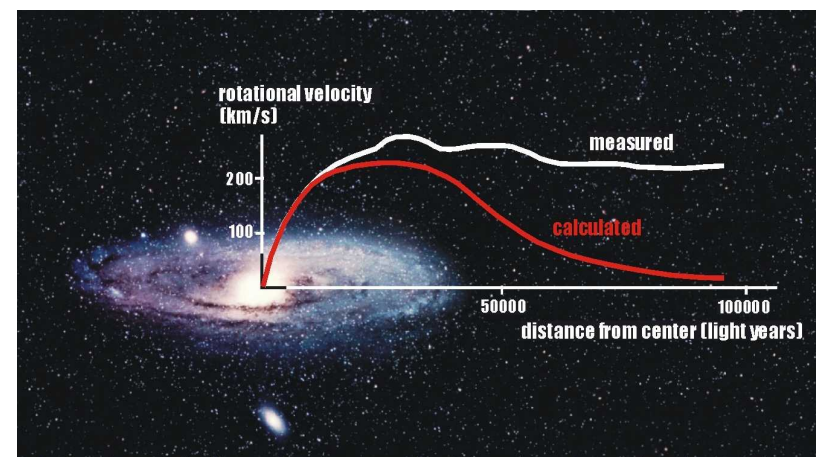
1. Introduction
2. Coannihilation inelastic DM Models and Constraints
3. LLPs's phenomenology in collider
4. Conclusions

- 1. Introduction**
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1. Introduction

Does dark matter (DM) exist?

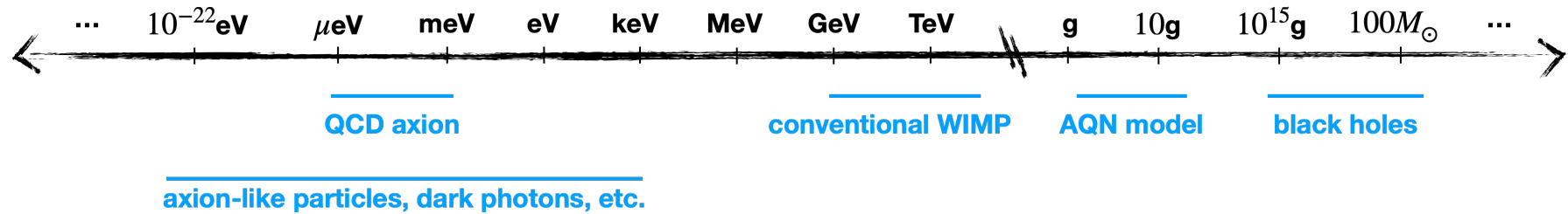
Ref: [Rubin, V.C., Ford, W.K. & Thonnard, N. 1978, Astrophys. J. 225, L107](#)



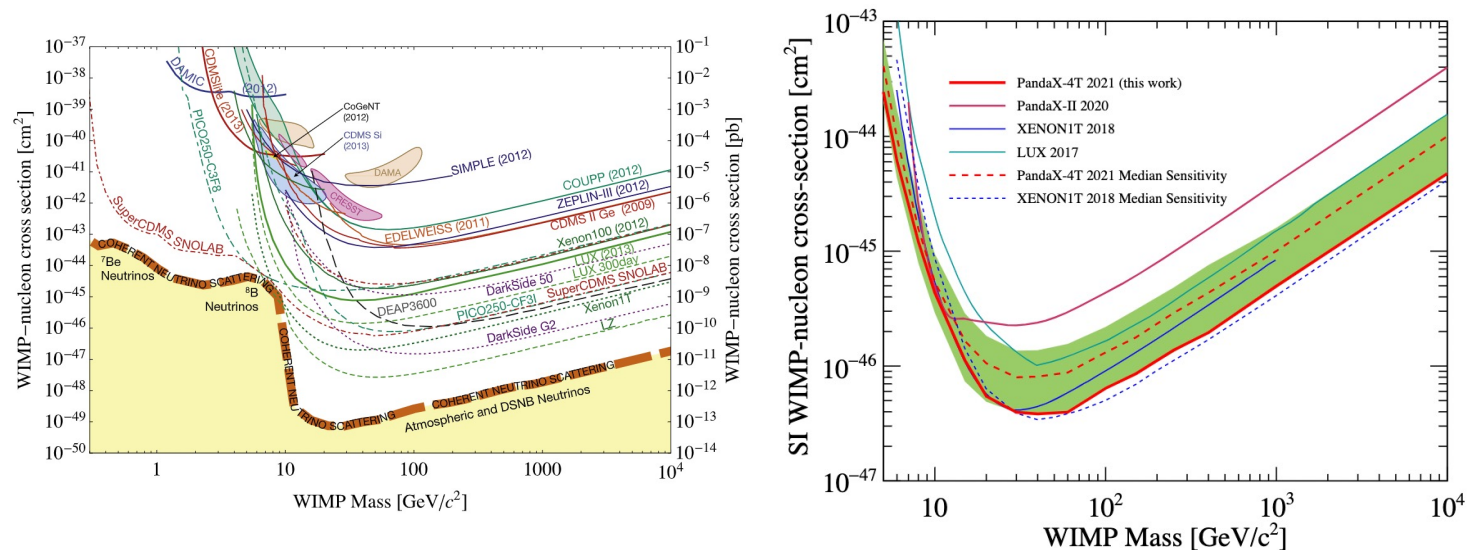
Ref: [ESA and the Planck Collaboration](#)

1. Introduction

Searching for Dark Matter



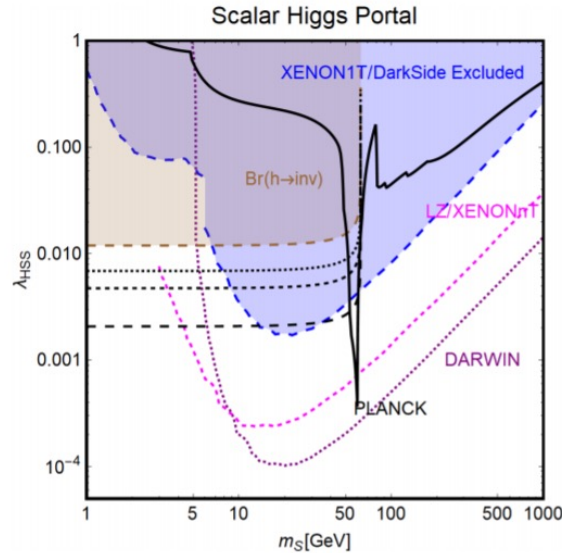
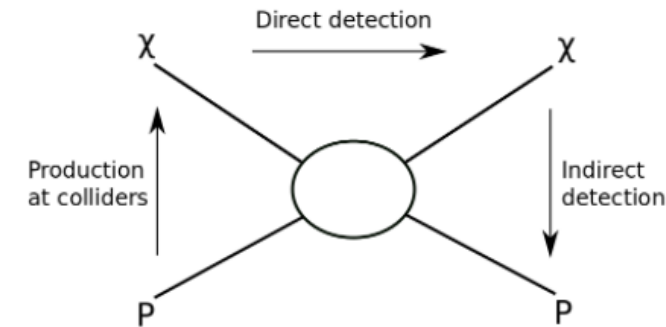
For the WIMP DM:



Ref: PHYSICAL REVIEW LETTERS 127, 261802 (2021) by PandaX-4T, J.Cooley

1. Introduction

Dark matter **(in)direct detection** constrains many of WIMP models:



Ref: G. Arcadi, et. al.
Phys.Rept. 842 (2020) 1-180

$$\Delta\mathcal{L}_S = -\frac{1}{2}M_S^2 S^2 - \frac{1}{4}\lambda_S S^4 - \frac{1}{4}\lambda_{HSS}\Phi^\dagger\Phi S^2$$

DM: enough cross section

DD: small cross section

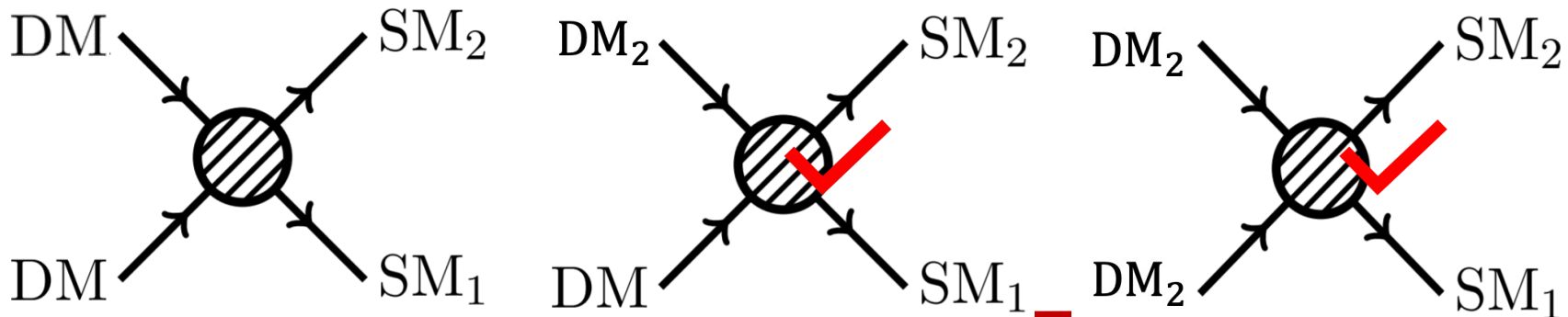


Inelastic DM

$$\Delta \equiv \frac{m_2 - m_1}{m_1}$$

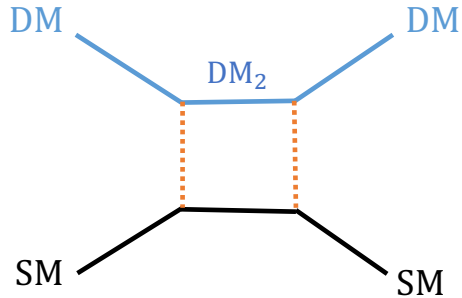
Coannihilation mechanism:

$$\sigma_{eff} = \frac{g_{s1}^2}{g_{eff}^2}(\sigma_{11} + 2\sigma_{12}\frac{g_{s2}}{g_{s1}}(1 + \Delta)^{3/2}e^{-x_f\Delta} + \sigma_{22}\frac{g_{s2}^2}{g_{s1}^2}(1 + \Delta)^3e^{-2x_f\Delta}).$$

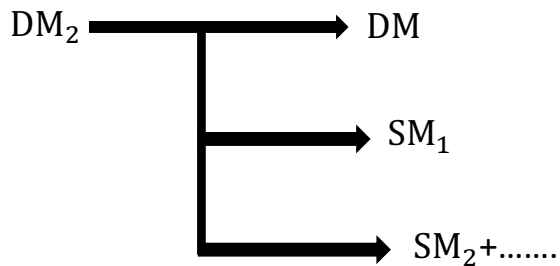


1. Introduction

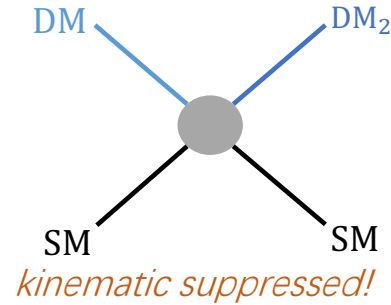
- Elastic scatterings $\sigma(\text{SM} + \text{DM})$



- The DM_2 may be long-lived



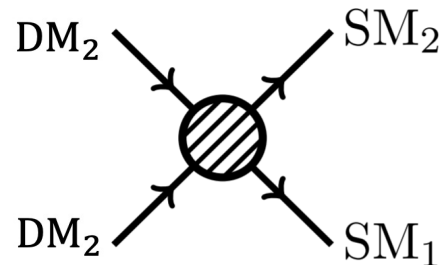
- Inelastic scatterings $\sigma(\text{SM} + \text{DM})$



- Previous studies: coannihilation dominated by σ_{12} and LLP search for light DM.

We focus on the case:

- $\sigma_{22} \gg \sigma_{12} \gg \sigma_{11} \sim 0$ and $m_{\text{DM}} > 100 \text{ GeV}$
- Searching for the DM_2 's long-lived signature.



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- 2. Coannihilation inelastic DM Models and Constraints**
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2. Coannihilation inelastic DM Models and Constraints

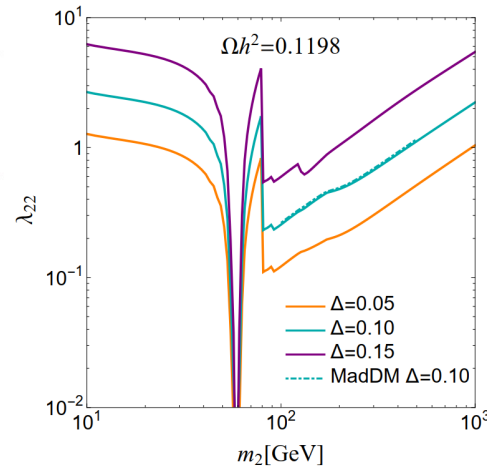
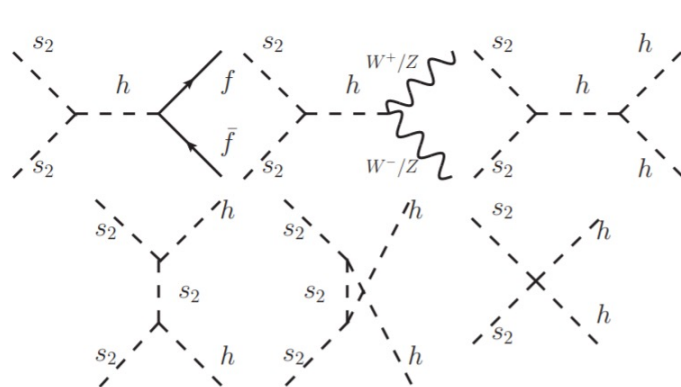
- The effective Lagrangian is

$$\mathcal{L} \supset (D_\mu S)^\dagger (D^\mu S) - \frac{m_1^2}{2} s_1^2 - \frac{m_2^2}{2} s_2^2 - \lambda_{22} s_2^2 \left(H^\dagger H - \frac{v^2}{2} \right) - \frac{1}{4} F'^{\mu\nu} F'_{\mu\nu} - \frac{\epsilon}{2 \cos \theta_W} F'^{\mu\nu} B_{\mu\nu} + \frac{m_{A'}^2}{2} A'^\mu A'_\mu.$$

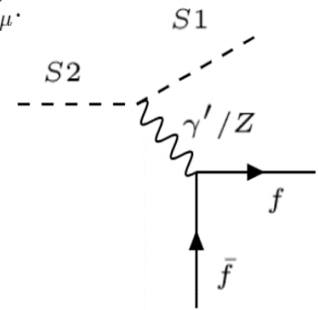
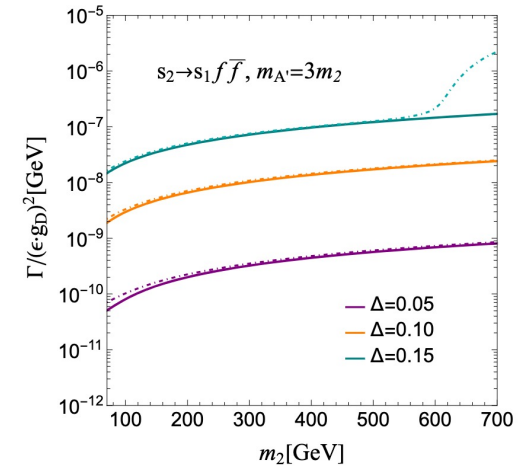
We have $\sigma_{11} = 0, \sigma_{12} \ll \sigma_{22}$. And $\Gamma(s_2)$ is suppressed by $m_{A'} = 3m_2$, ϵ and Δm , which can be a LLP.

With $g_D = 0.1, m_{A'} = 3m_2$, the free parameters: $\{\epsilon, m_2, \Delta\}$

- Dark Matter Relic abundance



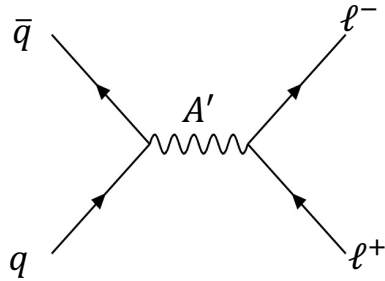
- The decay width of s_2



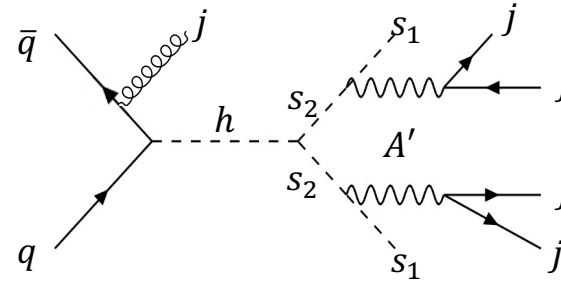
2. Coannihilation inelastic DM Models and Constraints

Constraints on our model:

1. Constraints from LHC



Dilepton resonance search



Monojet plus missing energy

The soft final jets may be not detectable

2. Electroweak precision measurement: heavy massive A' leads to ignorable contribution.

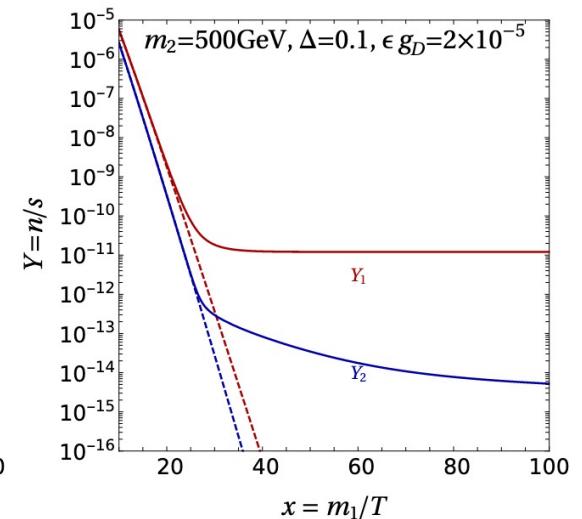
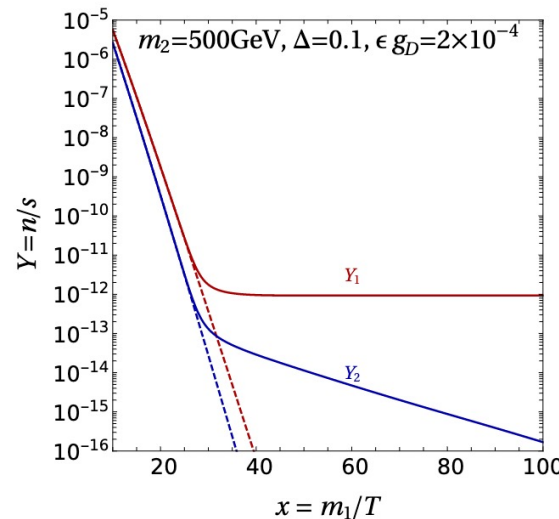
3. Constraints from thermalization requirement

$$s_1 + f \leftrightarrow s_2 + f$$

$$\Gamma(T) = \sum_f n_f^{eq} \langle \sigma_f v \rangle \gtrsim H$$

$$\begin{cases} \frac{dY_1}{dx} = -\frac{\lambda_f}{x^2} Y_f (Y_1 - \frac{Y_1^{eq}}{Y_2^{eq}} Y_2) + \gamma x (Y_2 - \frac{Y_2^{eq}}{Y_1^{eq}} Y_1), \\ \frac{dY_2}{dx} = -\frac{\lambda_{22}}{x^2} (Y_2^2 - Y_2^{eq2}) + \frac{\lambda_f}{x^2} Y_f (Y_1 - \frac{Y_1^{eq}}{Y_2^{eq}} Y_2) - \gamma x (Y_2 - \frac{Y_2^{eq}}{Y_1^{eq}} Y_1) \end{cases}$$

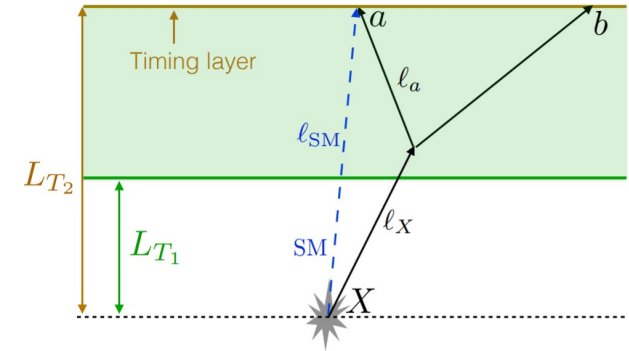
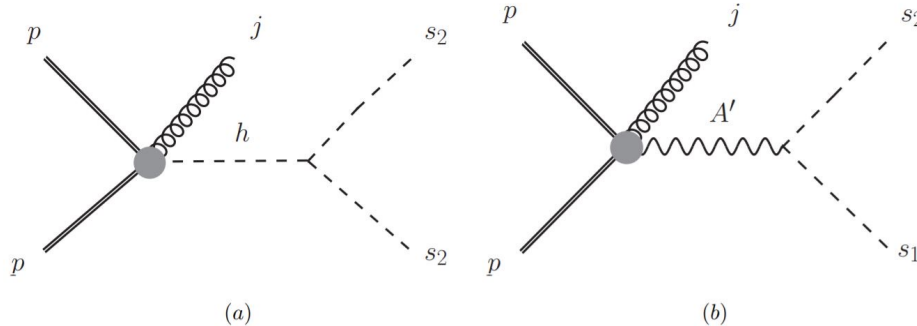
$$\lambda = \frac{s(m_1)}{H(m_1)} \langle \sigma v \rangle, \quad \gamma = \frac{\langle \Gamma_2 \rangle}{H(m_1)}$$



1. Introduction
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3. LLPs phenomenology in collider

- The generation of LLPs s_2



[Ref: J.Liu Z. Liu L.T.Wang PRL 122.13\(2019\)](#)

- Time delayed signature in LHC

$$\Delta t = L_{s_2}/\beta_{s_2} + L_f/\beta_f - L_{SM}/\beta_{SM}$$

- Basic cuts on signal

- Displaced muon-jet cuts (DMJ):

$$p_{T,j} > 120 \text{ GeV}, p_{T,\mu} > 5 \text{ GeV}, r_{s_2} < 30 \text{ cm}, d_0^\mu > 1 \text{ mm}$$

- LLPs cuts:

$$p_{T,j} > 120 \text{ (30) GeV}, p_{T,\ell} > 3 \text{ GeV}, |\eta| < 2.4, \Delta t_\ell > 0.3 \text{ ns}, 5 \text{ cm} < r_{s_2} < 30 \text{ cm}, z_{s_2} < 3.04 \text{ m}$$

[Ref: E. Izaguirre et.al. PRD93.6\(2016\)063523](#)

[Ref: J.Liu Z. Liu L.T.Wang PRL 122.13 \(2019\)](#)

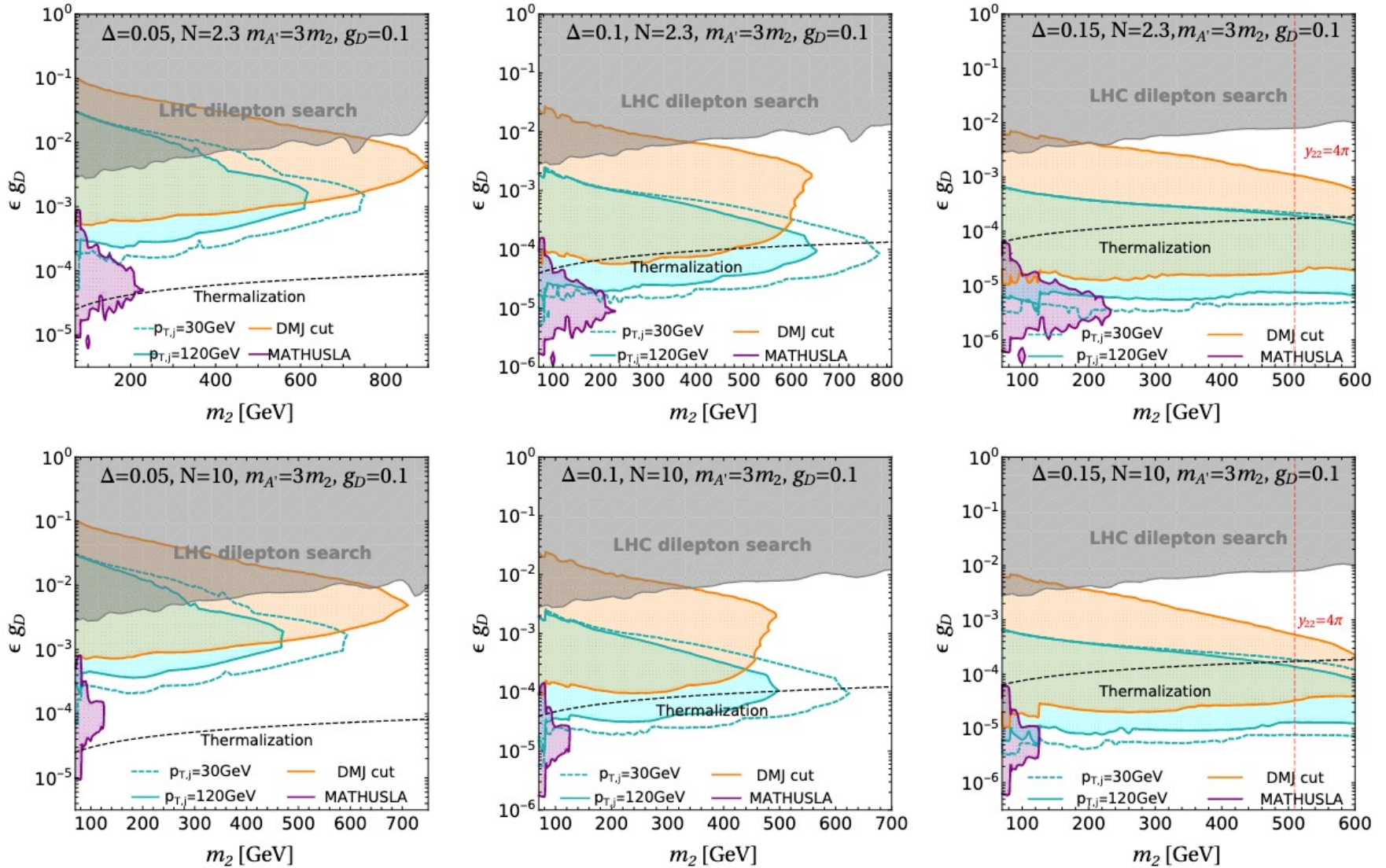
[A. Berlin F. Kling PRD99.1\(2019\)015021](#)

- MATHUSLA

$$100 \text{ m} < x_{s_2} < 120 \text{ m}, -100 \text{ m} < y_{s_2} < 100 \text{ m}, 100 \text{ m} < z_{s_2} < 300 \text{ m}$$

[Ref: ATLAS PLB 796 \(2019\) 68-87](#)

3. LLPs phenomenology in collider



The expected sensitivity at HL-LHC to the scalar-vector model in the $\epsilon g_D, m_2$ plane for $L = 3 \text{ ab}^{-1}$ and $\sqrt{s} = 13 \text{ TeV}$

1. Introduction
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3. LLPs's phenomenology in collider
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4. Conclusions

- We explore a coannihilation scenario that annihilation between coannihilation partner is the dominant contribution.
- We illustrate this mechanism with simplified scalar DM model.
- And we explore the long-lived signature of partner in HL-LHC.

Thanks!

Backup

Backup

- Derivation of co-annihilation effective cross section

$$\frac{dn_i}{dt} = -3Hn_i - \sum_{j,X} [\langle \sigma_{ij} v \rangle (n_i n_j - n_i^{\text{eq}} n_j^{\text{eq}}) - (\langle \sigma'_{ij} v \rangle n_i n_X - \langle \sigma'_{ji} v \rangle n_j n_X) - \Gamma_{ij} (n_i - n_i^{\text{eq}})] , \quad ($$

$$\frac{dn}{dt} = -3Hn - \sum_{i,j=1}^N \langle \sigma_{ij} v \rangle (n_i n_j - n_i^{\text{eq}} n_j^{\text{eq}}) \\ n_i n_j \sigma_{ij} \sim T^3 m_i^{3/2} m_j^{3/2} \sigma_{ij} \exp[-(m_i + m_j)/T] ,$$

while the rate for a reaction of type (6b) is

$$n_i n_X \sigma'_{ij} \sim T^{9/2} m_i^{3/2} \sigma'_{ij} \exp(-m_i/T) .$$

So the latter rates are larger by a factor of roughly

$$n_X/n_j \sim (T/m_j)^{3/2} \exp(m_j/T) \sim 10^9 ,$$

$$r_i \equiv n_i^{\text{eq}}/n^{\text{eq}} = \frac{g_i (1 + \Delta_i)^{3/2} \exp(-x \Delta_i)}{g_{\text{eff}}}$$

$$g_{\text{eff}} = \sum_{i=1}^N g_i (1 + \Delta_i)^{3/2} \exp(-x \Delta_i)$$

$$\frac{dn}{dt} = -3Hn - \langle \sigma_{\text{eff}} v \rangle (n^2 - n_{\text{eq}}^2) ,$$

where

$$\sigma_{\text{eff}} = \sum_{ij}^N \sigma_{ij} r_i r_j \\ = \sum_{ij}^N \sigma_{ij} \frac{g_i g_j}{g_{\text{eff}}^2} (1 + \Delta_i)^{3/2} (1 + \Delta_j)^{3/2} \\ \times \exp[-x(\Delta_i + \Delta_j)] .$$

K. Griest and D. Seckel PRD 43 (1991)3191-3203

Coannihilation inelastic DM Models

- Consider Lagrangian with **complex scalar** $\hat{S} = (\hat{s}_1 + i\hat{s}_2) / \sqrt{2}$

$$\mathcal{L} \supset (\partial_\mu \hat{S})^* (\partial^\mu \hat{S}) - m_S^2 \hat{S}^* \hat{S} - \delta \hat{m}_{ij}^2 \hat{s}_i \hat{s}_j - \hat{\lambda}_{ij} \hat{s}_i \hat{s}_j \left(H^\dagger H - \frac{v^2}{2} \right)$$

Where **U(1) violation** terms $\delta \hat{m}_{ij}^2$ and $\hat{\lambda}_{ij}$ are 2×2 **rank 1** matrices and $\hat{\lambda}_{ij}$ is proportional to $\delta \hat{m}_{ij}^2$. After diagonalizing the mass terms:

$$\mathcal{L} \supset (\partial_\mu S)^\dagger (\partial^\mu S) - \frac{m_1^2}{2} s_1^2 - \frac{m_2^2}{2} s_2^2 - \lambda_{22} s_2^2 \left(H^\dagger H - \frac{v^2}{2} \right)$$

We have $\sigma_{11} = 0$, $\sigma_{12} = 0$

Only s_2 couple with SM particles, s_1 can not be DM candidate

Backup

- Pure scalar model

Simply assume δm_{ij}^2 and λ_{ij} can not be simultaneously diagonalized but have a **misalignment angle** $\delta\theta$, After diagonalizing mass term:

$$\lambda_{12} \approx -\delta\theta \times \lambda_{22}, \quad \lambda_{11} \approx \delta\theta^2 \times \lambda_{22}$$

And then $\sigma_{11} \approx 0, \quad \sigma_{12} \ll \sigma_{22}$

Since λ_{11} is strongly constrained in direct detection, we simply set it to 0. and we have $\lambda_{12} \ll \lambda_{22}$:

$$\mathcal{L} \supset \frac{1}{2}(\partial S_1)^2 + \frac{1}{2}(\partial S_2)^2 - \frac{m^2}{2}S_1^2 - \frac{M^2}{2}S_2^2 - \lambda_{12}S_1S_2(|H|^2 - \frac{v^2}{2}) - \frac{\lambda_{22}S_2S_2}{2}(|H|^2 - \frac{v^2}{2})$$

Where the heavier state S_2 can potentially be LLP due to **small coupling** and **mass splitting**

Coannihilation inelastic DM Models

- Scalar-vector model

Gauging the U(1) Symmetry, introducing dark photon A' , which have kinematic mixing with SM B field:

$$\mathcal{L} \supset (D_\mu S)^\dagger (D^\mu S) - \frac{m_1^2}{2} s_1^2 - \frac{m_2^2}{2} s_2^2 - \lambda_{22} s_2^2 \left(H^\dagger H - \frac{v^2}{2} \right) - \frac{1}{4} F'^{\mu\nu} F'_{\mu\nu} - \frac{\epsilon}{2 \cos \theta_W} F'^{\mu\nu} B_{\mu\nu} + \frac{m_{A'}^2}{2} A'^\mu A'_\mu.$$

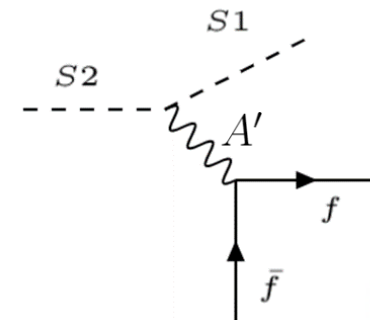
Where $D_\mu S = \partial_\mu S + i g_D A'_\mu S$ introducing coupling between 2 scalars.

Diagonalizing mass terms we have:

$$\mathcal{L}_{\text{int}} = \tilde{Z}_\mu (g J_Z^\mu - g_D \frac{m_Z^2 \tan \theta_W}{m_Z^2 - m_{A'}^2} \epsilon J_D^\mu) + \tilde{A}'_\mu (g_D J_D^\mu + g \frac{m_{A'}^2 \tan \theta_W}{m_Z^2 - m_{A'}^2} \epsilon J_Z^\mu + e \epsilon J_{\text{em}}^\mu) + \tilde{A}_\mu e J_{\text{em}}^\mu.$$

s_2 decay mainly mediated by dark photon,

its width is suppressed by **dark photon mass**,
small coupling and **mass splitting**.



Backup

- Scalar-vector model details

realized in UV models with dark Higgs. For instance we consider dark Higgs Φ carrying a opposite charge comparing to S . Terms like $y\text{Im}(S\Phi^*)^2$ can be added to the Lagrangian and generating mass splitting yv_Φ^2 . The kinetic mixing between SM Higgs and dark Higgs generates appropriate terms like $\frac{\lambda_{22}S_2S_2}{2}(|H|^2 - \frac{v^2}{2})$ after integrating out Φ field.

$$\begin{pmatrix} Z_\mu \\ A_\mu \\ A'_\mu \end{pmatrix} = \begin{pmatrix} 1 & 0 & \frac{m_{A'}^2 \tan \theta_W}{m_Z^2 - m_{A'}^2} \epsilon \\ 0 & 1 & \epsilon \\ \frac{m_Z^2 \tan \theta_W}{m_{A'}^2 - m_Z^2} \epsilon & 0 & 1 \end{pmatrix} \begin{pmatrix} \tilde{Z}_\mu \\ \tilde{A}_\mu \\ \tilde{A}'_\mu \end{pmatrix} \quad \frac{g_D^2}{2}(S_1^2 + S_2^2) \left(\tilde{A}'_\mu + \epsilon \frac{m_Z^2 \tan \theta_W}{m_Z^2 - m_{A'}^2} \tilde{Z}_\mu \right)^2$$

Existing constraints from Cosmology and LHC

- Direct detection:
 - elastic scatterings : very small E. Izaguirre et.al. PRD93.6(2016)063523
A. Berlin F. Kling PRD99.1(2019)015021
 - inelastic scatterings : suppressed by **non-relativistic** velocity.
- Indirect detection:
 - s_1 : tiny pair annihilation cross-section.
 - s_2 : already decayed in early universe. E. Izaguirre et.al. PRD93.6(2016)063523
- LHC search: **MET+mono jet, dilepton resonance** search in LHC constrains some of parameter space.
- Electroweak precision measurement (EWPM) is not sensitive to parameter region in our model since A' is very heavy.

Backup

- Co-annihilation calculation

$$\langle\sigma v\rangle_s = \langle\sigma v\rangle_{f\bar{f}} + \langle\sigma v\rangle_{WW} + \langle\sigma v\rangle_{ZZ} + \langle\sigma v\rangle_{hh},$$

$$\langle\sigma v\rangle_{f\bar{f}} = \frac{\lambda_{22}^2 m_f^2 (m_2^2 - m_f^2)^{3/2}}{4\pi m_2^3 (4m_2^2 - m_h^2)^2},$$

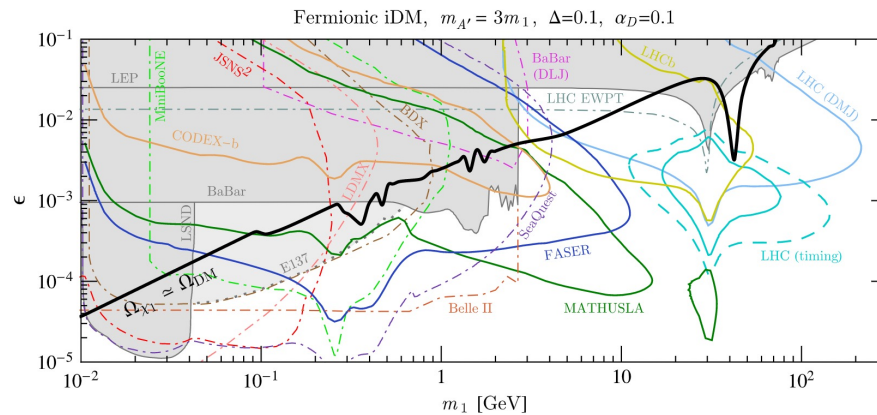
$$\langle\sigma v\rangle_{WW} = \frac{\lambda_{22}^2 (4m_2^2 - 4m_W^2 m_2^2 + 3m_W^4) \sqrt{m_2^2 - m_W^2}}{8\pi m_2^3 (4m_2^2 - m_h^2)^2},$$

$$\langle\sigma v\rangle_{ZZ} = \frac{\lambda_{22}^2 (4m_2^2 - 4m_Z^2 m_2^2 + 3m_Z^4) \sqrt{m_2^2 - m_Z^2}}{16\pi m_2^3 (4m_2^2 - m_h^2)^2},$$

$$\langle\sigma v\rangle_{hh} = \frac{\lambda_{22}^2 (\lambda_{22} v_h^2 (4m_2^2 - m_h^2) - 4m_2^4 + m_h^4)^2 \sqrt{m_2^2 - m_h^2}}{16\pi m_2^3 (8m_2^4 - 6m_2^2 m_h^2 + m_h^4)^2}.$$

- Previous studies: coannihilation dominated by σ_{12} and LLP search for light DM.

$$\mathcal{L} \supset \frac{e}{2 \cos \theta_w} A'_{\mu\nu} B^{\mu\nu} \quad ie_D A'_\mu \bar{\chi}_1 \gamma^\mu \chi_2$$



Ref: *PHYSICAL REVIEW D* 99, 015021 (2019) by Felix Kling