# Singlino DM in General Next-to-Miminmal Supersymmetric Standard Model

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① Why is the attractiveness of Bino-dominated DM fading?

2 Why doesn't  $Z_3$ -NMSSM explain DM experiments naturally?

3 Advantages of Singlino-dominated DM in GNMSSM

4 Conclusions

### Why Does Bino-dominated DM Become Less Favored?

• Take the MSSM as an example:

$$\begin{split} &\sigma_{\tilde{\chi}_{1}^{0}-N}^{\rm SI} \simeq 5 \times 10^{-45}~{\rm cm}^{2} \left(\frac{{\rm C}_{\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0}{\rm h}}}{0.1}\right)^{2} \left(\frac{m_{\rm h}}{125 {\rm GeV}}\right)^{2} \\ &\sigma_{\tilde{\chi}_{1}^{0}-N}^{\rm SD} \simeq 10^{-39}~{\rm cm}^{2} \left(\frac{{\rm C}_{\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0}{\rm Z}}}{0.1}\right)^{2} \\ &C_{\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0}h}^{2} \simeq e \tan \theta_{W} \frac{m_{Z}}{\mu \left(1-m_{\tilde{\chi}_{1}^{0}}^{2}/\mu^{2}\right)} \left(\sin 2\beta + \frac{m_{\tilde{\chi}_{1}^{0}}}{\mu}\right) \\ &C_{\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0}Z}^{2} \simeq \frac{e \tan \theta_{W} \cos 2\beta}{2} \frac{m_{Z}^{2}}{\mu^{2}-m_{\tilde{\chi}_{1}^{0}}^{2}} \end{split}$$

Conservative bounds on Higgsino mass:

LZ Experiment: 
$$\mu \gtrsim 380 \text{ GeV}$$
,

LZ Experiment: 
$$\mu \gtrsim 380 \text{ GeV}$$
, LZ + LHC +  $a_{\mu}$ :  $\mu \gtrsim 500 \text{ GeV}$ .

Higgsino mass is related with electroweak symmetry breaking!

$$m_Z^2 = 2(m_{H_d}^2 - m_{H_u}^2 \tan^2 \beta)/(\tan^2 \beta - 1) - 2\mu^2.$$

A tuning of 1% in EWSB. The situation will become worse if no DM is found.

### Why Does Bino-dominated DM Become Less Favored?

### Solutions: Go beyond minimal realizations of WIMP miracle.

DM EFTs	Examples	Annihilation	$\tilde{\chi} - N$ Scattering	Remarks
SM+DM	$\mathrm{SM}{+}S_{real}$	Weak/contact interactions	$\sigma_{\rm SI} \gtrsim 10^{-45} {\rm cm}^2$ and/or $\sigma_{\rm SD} \gtrsim 10^{-39} {\rm cm}^2$	Experimentally excluded.
			Suppressed by cancellation	Symmetry!
		Feeble interaction:	Suppressed	Increasingly Fine-tuned:
		h/Z funnels		$\Delta > 150$ .
SM+DM+X	MSSM with Light Gauginos	Coannihilation	Suppressed	Fine-tuning: $\Delta > 30$ ;
				Tight LHC constraitns.
SM+DM+XY	GNMSSM	May form	Suppressed	No tuning;
	ISS-NMSSM	secluded DM sector	Suppressed	three portals to SM.

Why is the dark matter still called WIMP? Weak interactions in the DM sector to predict proper  $\Omega h^2$ , feeble connections between SM and DM sectors to suppress ...

#### At least two directions to build models:

- Realize naturally EWSB:  $MSSM \rightarrow Z_3$ - $NMSSM \rightarrow General NMSSM$ .
- Generate neutrino mass: Type-I NMSSM  $\rightarrow$  ISS-NMSSM  $\rightarrow$  B-L NMSSM.

# Why Doesn't $Z_3$ -NMSSM Explain DM Exp. Naturally?

• Field content and gauge group

SF	Spin 0	Spin $\frac{1}{2}$	Generations	$   (\mathrm{U}(1) \otimes \mathrm{SU}(2) \otimes \mathrm{SU}(3)   $
$\hat{q}$	$ ilde{ ilde{q}}$	q	3	$\left(\frac{1}{6},2,3\right)$
î	$\tilde{l}$	l	3	$(-\frac{1}{2}, 2, 1)$
$\hat{H}_d$	$H_d$	$\tilde{H}_d$	1	$\left(-rac{1}{2},2,1 ight)$
$\hat{H}_u$	$H_u$	$\tilde{H}_u$	1	$(\frac{1}{2}, 2, 1)$
$\hat{d}$	$\tilde{d}_R^*$	$d_R^*$	3	$(\frac{1}{3}, 1, \overline{3})$
$\hat{u}$	$\tilde{u}_R^*$	$u_R^*$	3	$\left(-\frac{2}{3},1,\overline{3}\right)$
$\hat{e}$	$\tilde{u}_R^*$ $\tilde{e}_R^*$	$\begin{array}{c} d_R^* \\ u_R^* \\ e_R^* \end{array}$	3	(1, 1, 1)
ŝ	S	$ ilde{S}$	1	(0, 1, 1)

• Superpotential — an ad hoc  $Z_3$  discrete symmetry

$$W_{\text{NMSSM}} = W_{\text{Yukawa}} + \lambda \hat{S} \hat{H}_u \hat{H}_d + \frac{1}{3} \kappa \hat{S}^3$$

Try to solve  $\mu$ -problem and little hierarchy problem.

• DM may be Bino- or Singlino-dominated. For Bino-dom. case: DM physics is the same as that of MSSM since  $\lambda \lesssim 0.3$ . LZ Experiment:  $\mu \gtrsim 380$  GeV, Higgs Data:  $\lambda \mu \lesssim 100$  GeV.

## $Z_3$ -NMSSM: Neutralino Sector

### Singlino-dominated DM:

ullet Neutralino mass matrix — diagonalized by a rotation matrix N

$$\mathcal{M} = \left( \begin{array}{cccc} M_1 & 0 & -\frac{g_1 v_d}{\sqrt{2}} & \frac{g_1 v_u}{\sqrt{2}} & 0 \\ & M_2 & \frac{g_2 v_d}{\sqrt{2}} & -\frac{g_2 v_u}{\sqrt{2}} & 0 \\ & 0 & -\mu & -\lambda v_u \\ & & 0 & -\lambda v_d \\ & & & \frac{2\kappa}{\lambda} \mu \end{array} \right)$$

• DM mass and its couplings are approximated by:  $\mu \equiv \frac{\lambda}{\sqrt{2}} v_s$ 

$$\begin{split} & m_{\tilde{\chi}_{1}^{0}} \approx \frac{2\kappa}{\lambda} \mu + \frac{\lambda^{2} v^{2}}{\mu^{2}} (\mu \sin 2\beta - \frac{2\kappa}{\lambda} \mu) \simeq \frac{2\kappa}{\lambda} \mu, \qquad N_{15} \simeq 1, \\ & \frac{N_{13}}{N_{15}} = \frac{\lambda v}{\sqrt{2} \mu} \frac{(m_{\tilde{\chi}_{1}^{0}}/\mu) \sin \beta - \cos \beta}{1 - \left(m_{\tilde{\chi}_{1}^{0}}/\mu\right)^{2}}, \qquad \frac{N_{14}}{N_{15}} = \frac{\lambda v}{\sqrt{2} \mu} \frac{(m_{\tilde{\chi}_{1}^{0}}/\mu) \cos \beta - \sin \beta}{1 - \left(m_{\tilde{\chi}_{1}^{0}}/\mu\right)^{2}}, \\ & C_{\tilde{\chi}_{1}^{0} \tilde{\chi}_{1}^{0} h_{i}} \simeq \frac{\sqrt{2} \mu}{v} \left(\frac{\lambda v}{\mu}\right)^{2} \frac{V_{h_{i}}^{\text{SM}} (m_{\tilde{\chi}_{1}^{0}}/\mu - \sin 2\beta)}{1 - (m_{\tilde{\chi}_{1}^{0}}/\mu)^{2}} + \dots, \\ & C_{\tilde{\chi}_{1}^{0} \tilde{\chi}_{1}^{0} Z} \simeq \frac{m_{Z}}{\sqrt{2} v} \left(\frac{\lambda v}{\mu}\right)^{2} \frac{\cos 2\beta}{1 - (m_{\tilde{\chi}_{1}^{0}}/\mu)^{2}}, \end{split}$$

## $Z_3$ -NMSSM: DM Properties

### Singlino-dominated DM:

• DM properties are described by **four** independent parameters:

$$\tan \beta$$
,  $\lambda$ ,  $\mu$ ,  $m_{\tilde{\chi}^0_1}$  or  $\kappa$ , and  $2\kappa/\lambda < 1$ .

• DM-Nucleon Scattering in the alignment limit:

$$\begin{split} \sigma_{\tilde{\chi}_{1}^{0}-N}^{\rm SI} & \simeq & 5 \times 10^{-45} {\rm cm}^{2} \times \left(\frac{\mathcal{A}}{0.1}\right)^{2}, \quad \sigma_{\tilde{\chi}_{1}^{0}-N}^{\rm SD} \simeq 10^{-39} \ {\rm cm}^{2} \left(\frac{C_{\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0}Z}}{0.1}\right)^{2}, \\ \mathcal{A} & \simeq & \left(\frac{125 {\rm GeV}}{m_{h}}\right)^{2} V_{h}^{\rm SM} C_{\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0}h} + \left(\frac{125 {\rm GeV}}{m_{h_{s}}}\right)^{2} V_{h_{s}}^{\rm SM} C_{\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0}h_{s}} \\ & \simeq & \sqrt{2} \left(\frac{125 {\rm GeV}}{m_{h}}\right)^{2} \lambda \frac{\lambda v}{\mu} \frac{(m_{\tilde{\chi}_{1}^{0}}/\mu - \sin 2\beta)}{1 - (m_{\tilde{\chi}_{1}^{0}}/\mu)^{2}}, \\ C_{\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0}Z} & \simeq & \frac{m_{Z}}{\sqrt{2}v} (\frac{\lambda v}{\mu})^{2} \frac{\cos 2\beta}{1 - (m_{\tilde{\chi}_{1}^{0}}/\mu)^{2}}. \end{split}$$

LZ Experiment:  $\lambda \lesssim 0.1$ , DM- $\tilde{H}$  coannihilation to obtain proper abudance. Bayesian evidence is heavily suppressed  $\to$  A fine-tuning theory!

## Advantages of Singlino-dominated DM in GNMSSM

• Chiral Superfields

SF	Spin 0	Spin $\frac{1}{2}$	Generations	$(\mathrm{U}(1)\otimes\mathrm{SU}(2)\otimes\mathrm{SU}(3)$
$\hat{q}$	$ ilde{ ilde{q}}$	q	3	$\left(rac{1}{6},2,3 ight)$
Î	$\tilde{l}$	l	3	$\left(-rac{1}{2},2,1 ight)$
$\hat{H}_d$	$H_d$	$\tilde{H}_d$	1	$\left(-rac{1}{2},2,1 ight)$
$\hat{H}_u$	$H_u$	$\tilde{H}_u$	1	$(\frac{1}{2}, 2, 1)$
$\hat{d}$	$\begin{array}{c} \tilde{d}_R^* \\ \tilde{u}_R^* \\ \tilde{e}_R^* \end{array}$	$d_R^*$	3	$(\overline{\frac{1}{3}}, 1, \overline{3})$
$\hat{u}$	$\tilde{u}_R^*$	$u_R^*$	3	$\left(-\frac{2}{3},1,\overline{3}\right)$
$\hat{e}$	$\tilde{e}_R^*$	$egin{array}{c} d_R^* \ u_R^* \ e_R^* \  ilde{m{S}} \end{array}$	3	(1, 1, 1)
$\hat{s}$	S	$ ilde{S}$	1	(0, 1, 1)

• Superpotential — no ad hoc symmetry!

$$W_{\rm GNMSSM} = W_{\rm Y} + \lambda \hat{S} \hat{H}_u \cdot \hat{H}_d + \frac{1}{3} \kappa \hat{S}^3 + \mu \hat{H}_u \cdot \hat{H}_d + \frac{1}{2} \mu' \hat{S}^2 + \xi \hat{S}$$

- lacktriangle Free from domain wall and tadpole problems in  $Z_3$ -NMSSM.
- ②  $Z_3$ -violating terms originate from unified theories with a  $Z_4^n$  or  $Z_8^n$  sym..
- 3 The  $\xi \hat{S}$  term can be eliminated by field redefinitions.

# GNMSSM: DM Mass and Couplings

### Singlino-dominated DM:

• Neutralino mass matrix:  $\mu_{eff} \equiv \frac{\lambda}{\sqrt{2}} v_s$ ,  $\mu_{tot} \equiv \mu + \mu_{eff}$ .

$$m_{\tilde{\chi}_i^0} = \begin{pmatrix} M_1 & 0 & -\frac{1}{2}g_1v_d & \frac{1}{2}g_1v_u & 0 \\ 0 & M_2 & \frac{1}{2}g_2v_d & -\frac{1}{2}g_2v_u & 0 \\ -\frac{1}{2}g_1v_d & \frac{1}{2}g_2v_d & 0 & -\mu_{\textbf{tot}} & -\frac{1}{\sqrt{2}}v_u\lambda \\ \frac{1}{2}g_1v_u & -\frac{1}{2}g_2v_u & -\mu_{\textbf{tot}} & 0 & -\frac{1}{\sqrt{2}}v_d\lambda \\ 0 & 0 & -\frac{1}{\sqrt{2}}v_u\lambda & -\frac{1}{\sqrt{2}}v_d\lambda & \mathbf{m_N} \end{pmatrix}$$

Mass and couplings of the singlino-dominated DM are given by:

$$\begin{split} m_{\tilde{\chi}_1^0} & \simeq & m_N + \frac{1}{2} \frac{\lambda^2 v^2 (m_{\tilde{\chi}_1^0} - \mu_{tot} \sin 2\beta)}{m_{\tilde{\chi}_1^0}^2 - \mu_{tot}^2} \\ \simeq \mathbf{m_N}, \quad \mathbf{m_N} \equiv \frac{2\kappa}{\lambda} \mu_{\text{eff}} + \mu', \\ C_{\tilde{\chi}_1^0 \tilde{\chi}_1^0 h_i} & = & C_{\tilde{\chi}_1^0 \tilde{\chi}_1^0 h_i}^{\text{Z}_3 - \text{NMSSM}} |_{\mu \to \mu_{tot}}, \qquad C_{\tilde{\chi}_1^0 \tilde{\chi}_1^0 Z} = C_{\tilde{\chi}_1^0 \tilde{\chi}_1^0 Z}^{\text{Z}_3 - \text{NMSSM}} |_{\mu \to \mu_{tot}}. \end{split}$$

• DM properties are described by **five** independent parameters:

 $\tan \beta$ ,  $\lambda$ ,  $\kappa$ ,  $\mu_{\text{tot}}$ , and  $m_{\tilde{\chi}_1^0}$ .  $\mu_{\text{tot}}$ : Higgsino mass.

Different from  $Z_3$ -NMSSM,  $m_{\tilde{\chi}_1^0}$ ,  $\lambda$ , and  $\kappa$  are not correlated!

• In the limit  $\lambda \to 0$ , matrix decomposition:  $5 \times 5 = 4 \oplus 1$ , decoupled!

## GNMSSM: Higgs Sector

#### Soft-breaking terms:

$$-\mathcal{L}_{soft} = \left[ \lambda A_{\lambda} S H_{u} \cdot H_{d} + \frac{1}{3} A_{\kappa} \kappa S^{3} + m_{3}^{2} H_{u} \cdot H_{d} + \frac{1}{2} m_{S}^{\prime 2} S^{2} + h.c. \right] + m_{H_{u}}^{2} |H_{u}|^{2} + m_{H_{d}}^{2} |H_{d}|^{2} + m_{S}^{2} |S|^{2}.$$

CP-odd Higgs mass matrix in bases  $(A_{NSM}, Im(S))$ :

$$\mathcal{M}_{P,11}^2 = \frac{2\left[\mu_{eff}(\lambda A_\lambda + \kappa \mu_{eff} + \lambda \mu') + \lambda m_3^2\right]}{\lambda \sin 2\beta} \equiv \mathbf{m_A^2},$$

$$\mathcal{M}_{P,22}^2 = \frac{(\lambda A_\lambda + 4\kappa \mu_{eff} + \lambda \mu')\sin 2\beta}{4\mu_{eff}} \lambda v^2 - \frac{\kappa \mu_{eff}}{\lambda} (3A_\kappa + \mu') - \frac{\mu}{2\mu_{eff}} \lambda^2 v^2 - 2m_S'^2$$

$$\mathcal{M}_{P,12}^2 = \frac{v}{\sqrt{2}} (\lambda A_{\lambda} - 2\kappa \mu_{eff} - \lambda \mu') \equiv \frac{\lambda \mathbf{v}}{\sqrt{2}} (\mathbf{A}_{\lambda} - \mathbf{m}_{\mathbf{N}}).$$

- In the limit  $\lambda \to 0$ , matrix decomposition:  $2 \times 2 = 1 \oplus 1$ , singlet decoupled!
- $m_A$ : hevay doublet mass scale,  $m_B \equiv \sqrt{M_{P,22}^2}$ : CP-odd singlet Higgs mass.

$$m_{3}^{2} = \frac{\lambda \mathbf{m_{A}^{2}} \sin 2\beta - 2\kappa \mu_{\text{eff}}^{2} - 2\lambda \mu_{\text{eff}} \mu' - 2\lambda \mu_{\text{eff}} A_{\lambda}}{2\lambda}$$

$$m_{S}^{\prime 2} = -\frac{1}{2} \left[ \mathbf{m_{B}^{2}} + \frac{\mu}{2\mu_{\text{eff}}} \lambda^{2} v^{2} + \frac{\kappa \mu_{\text{eff}}}{\lambda} \left( 3A_{\kappa} + \mu' \right) - \frac{(\lambda A_{\lambda} + 4\kappa \mu_{\text{eff}} + \lambda \mu') \sin 2\beta}{4\mu_{\text{eff}}} \lambda v^{2} \right]$$

## GNMSSM: Higgs Sector

CP-even Higgs mass matrix in bases  $(H_{NSM}, H_{SM}, Re[S])$ :

$$\begin{split} \mathcal{M}_{S,11}^2 &= m_A^2 + \frac{1}{2} (2m_Z^2 - \lambda^2 v^2) \sin^2 2\beta, \\ \mathcal{M}_{S,12}^2 &= -\frac{1}{4} (2m_Z^2 - \lambda^2 v^2) \sin 4\beta, \\ \mathcal{M}_{S,13}^2 &= -\frac{1}{\sqrt{2}} (\lambda A_{\lambda} + 2\kappa \mu_{eff} + \lambda \mu') v \cos 2\beta \equiv -\frac{\lambda}{\sqrt{2}} (A_{\lambda} + m_N) v \cos 2\beta, \\ \mathcal{M}_{S,22}^2 &= m_Z^2 \cos^2 2\beta + \frac{1}{2} \lambda^2 v^2 \sin^2 2\beta, \\ \mathcal{M}_{S,23}^2 &= \frac{v}{\sqrt{2}} \left[ 2\lambda (\mu_{eff} + \mu) - (\lambda A_{\lambda} + 2\kappa \mu_{eff} + \lambda \mu') \sin 2\beta \right], \\ &\equiv \frac{\lambda \mathbf{v}}{\sqrt{2}} \left[ 2\mu_{\mathbf{tot}} - (\mathbf{A}_{\lambda} + \mathbf{m}_{\mathbf{N}}) \sin 2\beta \right], \\ \mathcal{M}_{S,33}^2 &= \frac{\lambda (A_{\lambda} + \mu') \sin 2\beta}{4\mu_{eff}} \lambda v^2 + \frac{\mu_{eff}}{\lambda} (\kappa A_{\kappa} + \frac{4\kappa^2 \mu_{eff}}{\lambda} + 3\kappa \mu') - \frac{\mu}{2\mu_{eff}} \lambda^2 v^2, \end{split}$$

• In the limit 
$$\lambda \to 0$$
, matrix decomposition:  $3 \times 3 = 2 \oplus 1$ , singlet decoupled!

•  $m_C \equiv \sqrt{\mathcal{M}_{S,33}^2}$ : CP-even singlet Higgs mass.

$$A_{\kappa} \quad = \quad \frac{\mathbf{m_{C}^2} + \frac{\mu}{2\mu_{\mathrm{eff}}}\lambda^2 v^2 - \frac{\lambda(A_{\lambda} + \mu') sin2\beta}{4\mu_{\mathrm{eff}}}\lambda v^2 - \frac{4\kappa^2}{\lambda^2}\mu_{\mathrm{eff}}^2 - \frac{3\kappa}{\lambda}\mu_{\mathrm{eff}}\mu'}{\frac{\mu_{\mathrm{eff}}}{\lambda}\kappa}$$

## GNMSSM: Input Parameters

### Input parameters in the original Lagrangian:

- Soft-breaking masses:  $m_{H_u}^2$ ,  $m_{H_d}^2$ , and  $m_S^2$ ;
- Yukawa couplings in Higgs sector:  $\lambda$  and  $\kappa$ ;
- Soft-breaking trilinear coefficients  $A_{\lambda}$  and  $A_{\kappa}$ ;
- Bilinear mass parameters  $\mu$  and  $\mu'$ , and their soft-breaking parameters  $m_3^2$  and  $m_S'^2$ .

## Physical inputs: $\lambda$ , $\kappa$ , $\tan \beta$ , $v_s$ , $m_{H^{\pm}}$ , $m_{h_s}$ , $m_{A_s}$ , $m_{\tilde{\chi}_1^0}$ , and $\mu_{tot}$ .

- Vacuum expectation values:  $v_u$ ,  $v_d$ ,  $v_s$ ;
- Yukawa couplings in Higgs sector:  $\lambda$  and  $\kappa$ ;
- Electroweakino masses:  $m_{\tilde{\chi}_1^0} \simeq m_N$ , and Higgsino mass  $\mu_{tot}$ ;
- Higgs boson masses:  $m_{H^{\pm}}^2 \simeq m_A^2$ ,  $m_{A_s} \simeq m_B$ , and  $m_{h_s} \simeq m_C$ ;
- Soft-breaking trilinear coefficients  $A_{\lambda}$ , which is an insensitive parameter for all observables.

## GNMSSM: Key Features

### Important applications of the Singlino-dominated DM:

- Singlet-dominated particles form a secluded DM sector: proper abundance is generated by
  - s-wave process  $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \to h_s A_s$ , occuring by s-channel exchange of Higgs bosons and t-channel exchange of neutralinos:

$$|C_{\tilde{\chi}_1^0 \tilde{\chi}_1^0 h_s}| = |C_{\tilde{\chi}_1^0 \tilde{\chi}_1^0 A_s}| = \sqrt{2}\kappa \simeq 0.2 \times \left(\frac{m_{\tilde{\chi}_1^0}}{300 \text{ GeV}}\right)^{1/2};$$

- p-wave process  $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \to h_s h_s, A_s A_s$ , via adjusting  $\kappa$ ;
- $h_s/A_s$ -funnels, via adjusting  $m_{h_s}/m_{A_s}$ .
- DM-nucleon scatterings suppressed by  $\lambda^4$ : Current LZ experiment requires  $\lambda \lesssim 0.1$ . Future DD expt. will further suppress  $\lambda$ , but not affect GNMSSM phenomenology.
- Bayesian analyses:
   DM is primarily preferred to be Singlino-dominated.

### GNMSSM: Other Distinct Features

#### Characteristics:

- Free from the domain wall and tadpole problems;
- More stable vacuum than the MSSM;

$$V_{\min}^{\text{des}} = \dots - \frac{\kappa^2}{\lambda^4} \mu_{eff}^4 - \frac{1}{3} \frac{\kappa A_{\kappa}}{\lambda^3} \mu_{eff}^3.$$

- Significant alleviation of the LHC constraints. Heavy sparticles prefer to decay into NLSP or NNLSP first. Their decay chains are thus lengthened and their decay products become more complex.
- **1** Every EW parameter takes natural values. Considering LZ + LHC +  $a_{\mu}$ ,  $Z_3$ -NMSSM:  $m_{\tilde{\chi}_1^0} \gtrsim 260 {\rm GeV}, \; \mu \gtrsim 550 {\rm GeV}, \; v_s \gtrsim 2 \; {\rm TeV};$  GNMSSM:  $m_{\tilde{\chi}_1^0} \gtrsim 100 {\rm GeV}, \; \mu_{tot} \gtrsim 200 {\rm GeV}, \; v_s < 1 \; {\rm TeV}.$
- **3** Bayesian evidence is much larger than that of  $Z_3$ -NMSSM.

## Technical Support

### Results are based on global fits of supersymmetric theories.

- Specially designed clusters.
- SARAH suite for calculation.
  - Model building: SARAH-4.14.3;
  - Spectrum generator: SPheno-4.0.4;
  - DM physics calculator: MicrOMEGAs-5.0.4;
  - Higgs physics calculator: HiggsSingal-2.2.3, HiggsBounds-5.3.2;
  - Flavor physics calculator: FlavorKit;
  - MC simulation: MadGraph\_aMC@NLO, PYTHIA8, and Delphes;
  - LHC SUSY search: SModelS-2.1.1, CheckMATE-2.0.29.
- Scan strategy: parallel MultiNest algorithm.
  - High performance:
  - Simultaneous computation of more than 10<sup>6</sup> programes.
- Members of the developers for the package CheckMATE. Reproduce more than 40 experimental analyses.

# Technical Support

Table 1: Experimental analyses of the electroweakino production processes.

Scenario	Final State	Name
$\tilde{\chi}^0_2 \tilde{\chi}^\pm_1 \to W Z \tilde{\chi}^0_1 \tilde{\chi}^0_1$	$n\ell(n\geq 2) + nj(n\geq 0) + \mathcal{E}_{\mathcal{T}}^{\text{miss}}$	$\begin{array}{l} \text{CMS-SUS-20-001} \left(137fb^{-1}\right) \\ \text{ATLAS-2106-01676} \left(139fb^{-1}\right) \\ \text{CMS-SUS-17-004} \left(35.9fb^{-1}\right) \\ \text{CMS-SUS-16-039} \left(35.9fb^{-1}\right) \\ \text{ATLAS-1803-02762} \left(36.1fb^{-1}\right) \\ \text{ATLAS-1806-02293} \left(36.1fb^{-1}\right) \end{array}$
$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm \to \ell \tilde{\nu} \ell \tilde{\ell}$	$n\ell(n=3) + \mathrm{E_T^{miss}}$	$\begin{array}{l} {\rm CMS-SUS-16-039}(35.9fb^{-1}) \\ {\rm ATLAS-1803-02762}(36.1fb^{-1}) \end{array}$
$\tilde{\chi}^0_2 \tilde{\chi}^\pm_1 \to \tilde{\tau} \nu \ell \tilde{\ell}$	$2\ell + 1\tau + E_T^{miss}$	${\tt CMS-SUS-16-039}(35.9fb^{-1})$
$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm \to \tilde{\tau} \nu \tilde{\tau} \tau$	$3\tau + E_T^{miss}$	${\tt CMS-SUS-16-039}(35.9fb^{-1})$
$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm \to W h \tilde{\chi}_1^0 \tilde{\chi}_1^0$	$n\ell(n\geq 1) + nb(n\geq 0) + nj(n\geq 0) + \mathbf{E}_{\mathrm{T}}^{\mathrm{mins}}$	$\begin{array}{l} {\rm ATLAS-1909-09226(139fb^{-1})} \\ {\rm CMS-SUS-17-004(35.9fb^{-1})} \\ {\rm CMS-SUS-16-093(35.9fb^{-1})} \\ {\rm CMS-SUS-16-0943(36.1fb^{-1})} \\ {\rm CMS-SUS-16-034(35.9fb^{-1})} \\ {\rm CMS-SUS-16-045(35.9fb^{-1})} \\ \end{array}$
$\tilde{\chi}_1^{\mp}\tilde{\chi}_1^{\pm} \rightarrow WW\tilde{\chi}_1^0\tilde{\chi}_1^0$	$2\ell + E_T^{\rm miss}$	$\begin{array}{c} \mathtt{ATLAS-1908-08215}(139fb^{-1}) \\ \mathtt{CMS-SUS-17-010}(35.9fb^{-1}) \end{array}$
$\tilde{\chi}_1^{\mp} \tilde{\chi}_1^{\pm} \rightarrow 2 \tilde{\ell} \nu (\tilde{\nu} \ell)$	$2\ell + E_T^{\rm miss}$	$\begin{array}{l} {\tt ATLAS-1908-08215(139}fb^{-1}) \\ {\tt CMS-SUS-17-010(35.9}fb^{-1}) \end{array}$
$\begin{array}{l} \tilde{\chi}^0_2\tilde{\chi}^\mp_1 \rightarrow h/ZW\tilde{\chi}^0_1\tilde{\chi}^0_1,\tilde{\chi}^0_1 \rightarrow \gamma/Z\tilde{G} \\ \tilde{\chi}^\pm_1\tilde{\chi}^\mp_1 \rightarrow WW\tilde{\chi}^0_1\tilde{\chi}^0_1,\tilde{\chi}^0_1 \rightarrow \gamma/Z\tilde{G} \end{array}$	$2\gamma + n\ell(n \geq 0) + nb(n \geq 0) + nj(n \geq 0) + \mathbf{E}_{\mathrm{T}}^{\mathrm{miss}}$	${\tt ATLAS-1802-03158} (36.1 fb^{-1})$
$\begin{array}{l} \tilde{\chi}_{0}^{0}\tilde{\chi}_{1}^{\pm}\rightarrow ZW\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0},\tilde{\chi}_{1}^{0}\rightarrow h/Z\tilde{G}\\ \tilde{\chi}_{1}^{\pm}\tilde{\chi}_{1}^{\mp}\rightarrow WW\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0},\tilde{\chi}_{1}^{0}\rightarrow h/Z\tilde{G}\\ \tilde{\chi}_{0}^{0}\tilde{\chi}_{1}^{0}\rightarrow Z\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0},\tilde{\chi}_{1}^{0}\rightarrow h/Z\tilde{G}\\ \tilde{\chi}_{1}^{\mp}\tilde{\chi}_{1}^{0}\rightarrow W\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0},\tilde{\chi}_{1}^{0}\rightarrow h/Z\tilde{G}\\ \end{array}$	$n\ell(n \geq 4) + \mathrm{E}_{\mathrm{T}}^{\mathrm{miss}}$	${\tt ATLAS-2103-11684(139} fb^{-1})$
z0,±z0,∓ → z0z0 + v → ZZ/HČ	$\tilde{G} = n\ell(n \ge 2) + nb(n \ge 0) + nj(n \ge 0) + \text{Emiss}$	CMS-SUS-16-039(35.9fb <sup>-1</sup> ) CMS-SUS-17-004(35.9fb <sup>-1</sup> )

Status of SUSY

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### Conclusion

- WIMP crisis just means that the simplest realizations of the WIMP miracle are facing challenges —— More elaborate theories are encouraged.
- **Q** Occam razor was incorrectly applied to the NMSSM. Specifically, the  $Z_3$ -NMSSM is too restricted to exhibit all the essential characteristics of the NMSSM.
- **1** It is time to explore the phenomenology of GNMSSM, which is one of the simplest supersymmetric theories to explain naturally current experiments.
  - Signlino DM is primarily preferred by Bayesian statistics!
  - The GNMSSM has many distinct theoretical advantages!
- Seemingly independent problems may have common physical origins!
  - Go forward to explore them with creative ideas and more sophisticated techniques.

