

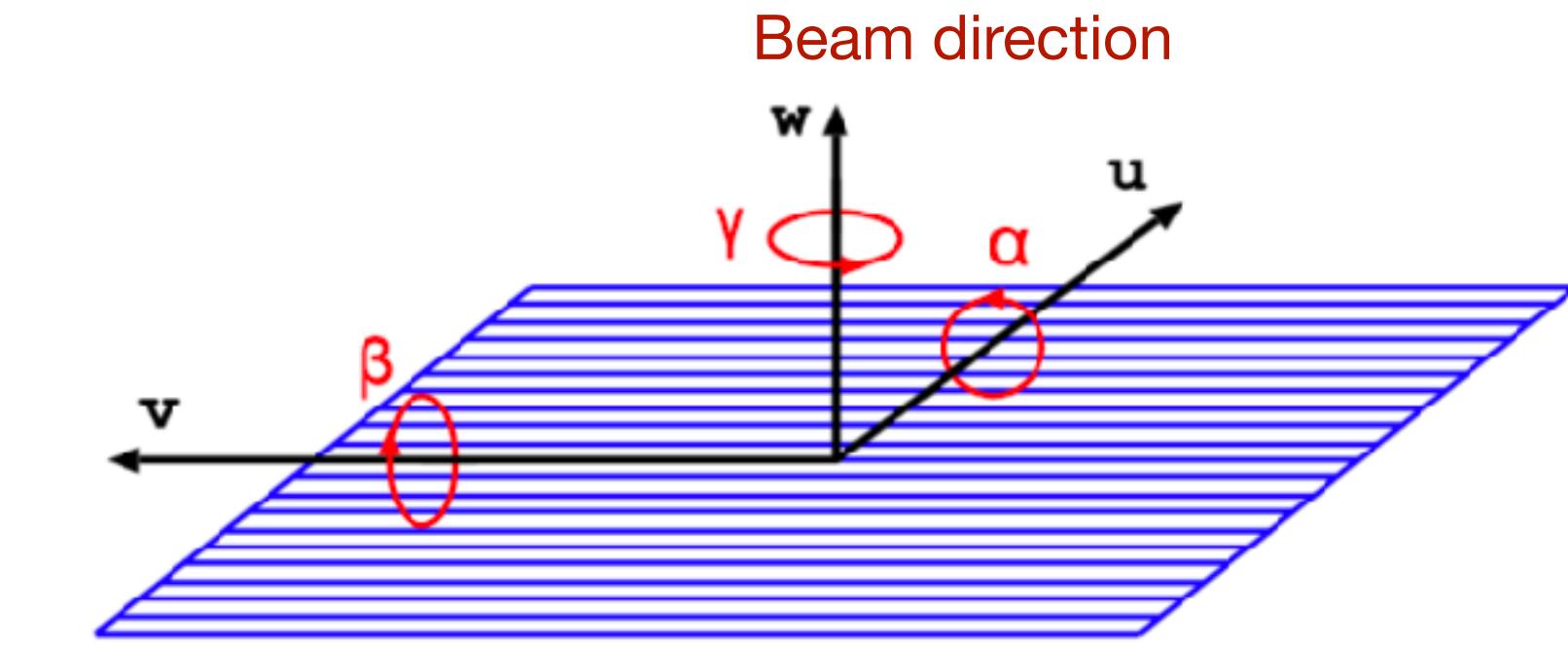
MOST2 offline tracking reconstruction and alignment

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Tue, Sep29, 2022

Interface to Millepede

- using simulated data from G4
- interface to Millepede to solve the matrix, then get the corrected alignment parameters
- digitizing the simulation data, randomly change the ideal geometry



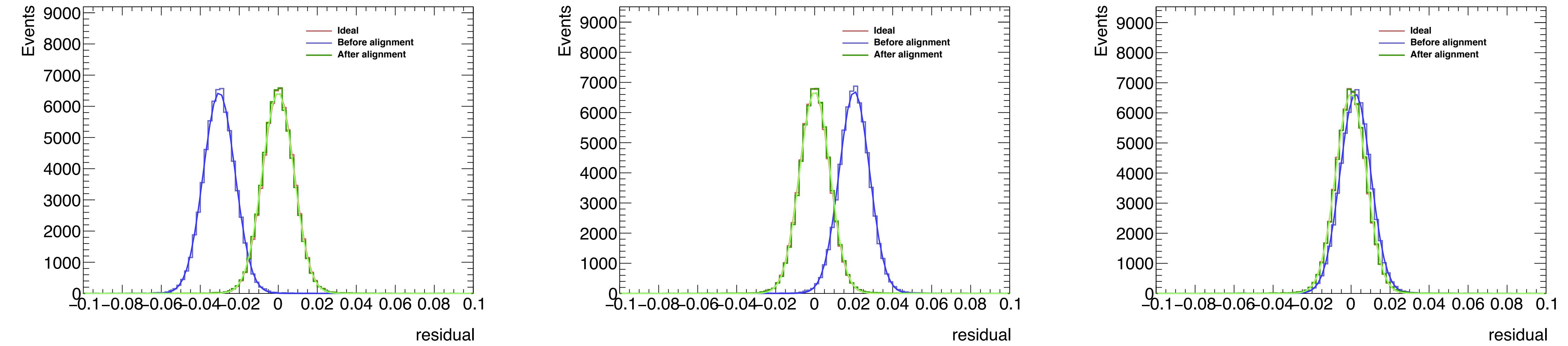
If add Δx , Δy , $\Delta \gamma$ only:

Unit: mm

Unit: rad

| chipID | DeltaX setting | DeltaX fitted | DeltaY setting | DeltaY fitted | DeltaY setting | DeltaY fitted |
|--------|----------------|---------------|----------------|---------------|----------------|---------------|
| 1 | 0.07253 | 0.07250 | -0.02467 | -0.02448 | 0.00046 | 0.00268 |
| 2 | 0.02036 | 0.02024 | 0.02448 | 0.02448 | 0.00493 | 0.00159 |
| 3 | -0.03740 | -0.03747 | 0.02994 | 0.02992 | -0.00189 | -0.00265 |
| 4 | -0.04566 | -0.04552 | -0.01967 | -0.01993 | 0.01671 | 0.00941 |
| 5 | -0.00856 | -0.00853 | 0.04181 | 0.04175 | -0.00823 | -0.00259 |
| 6 | -0.03031 | -0.03015 | -0.03201 | -0.03207 | 0.00435 | 0.00572 |
| 7 | 0.01759 | 0.01763 | -0.03591 | -0.03587 | 0.00090 | 0.00178 |
| 8 | -0.02344 | -0.02362 | -0.01411 | -0.01378 | -0.01306 | -0.01160 |
| 9 | -0.00738 | -0.00738 | 0.03910 | 0.03913 | -0.00168 | -0.00220 |
| 10 | 0.02399 | 0.02401 | -0.02652 | -0.02655 | 0.00099 | 0.00023 |
| 11 | -0.00952 | -0.00955 | 0.00229 | 0.00221 | -0.00016 | 0.00010 |
| 12 | 0.02780 | 0.02782 | 0.01526 | 0.01520 | -0.00332 | -0.00248 |

Residual Plots



- Residual plots Ideal/before alignment/ after alignment
- ~10,000 tracks
- All residual plots can be corrected well, although some mis-alignment parameters can't be corrected well

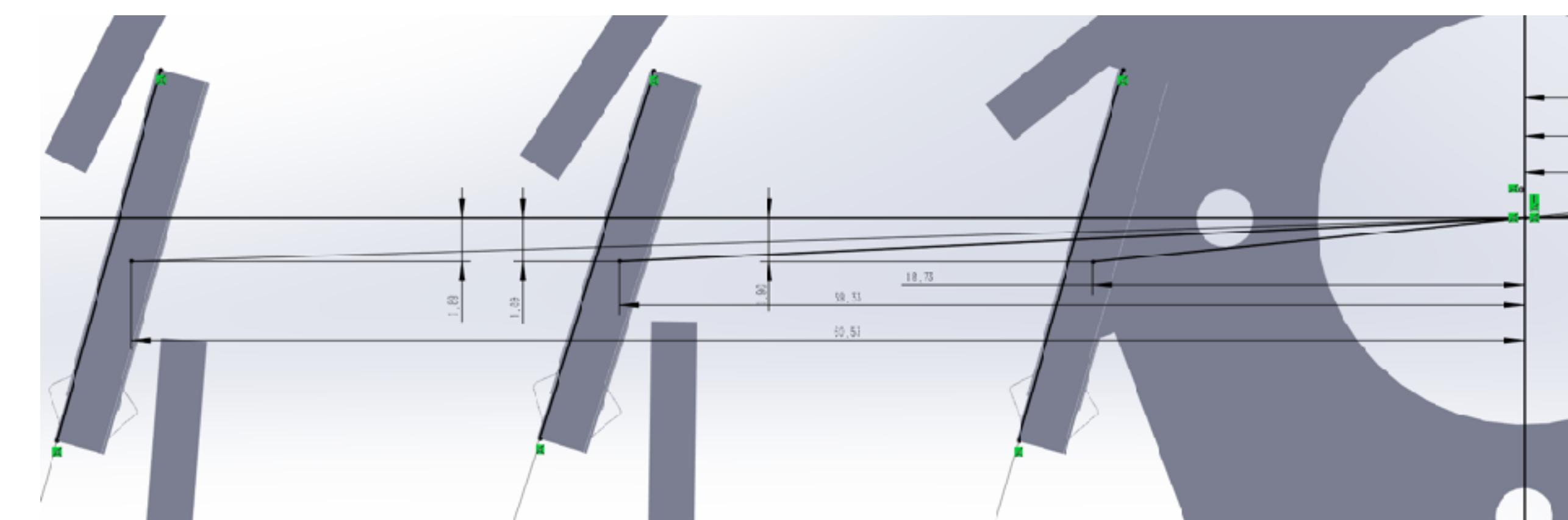
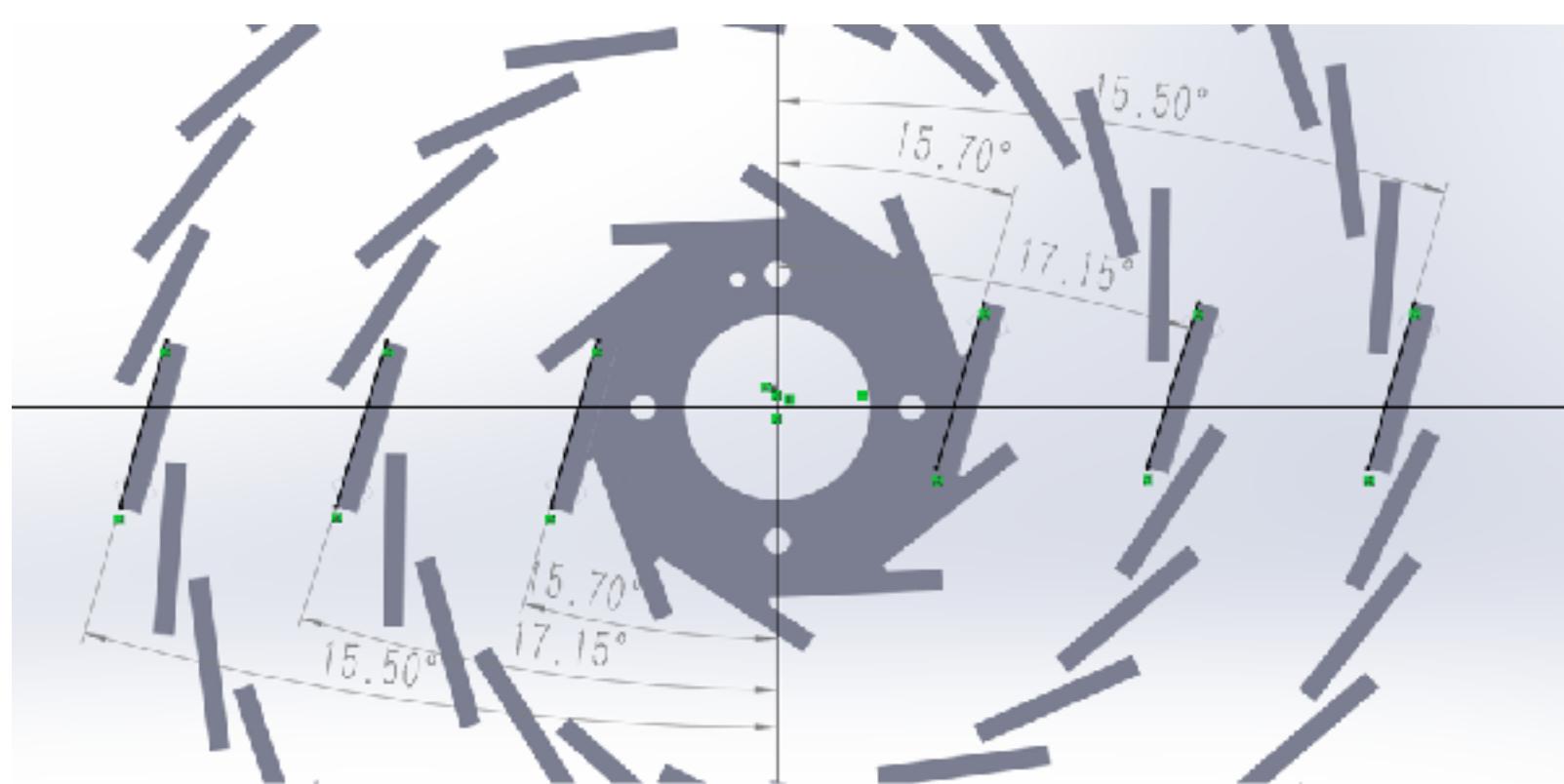
Next Plan

- using actual geometry simulation data

Backup

11 hits position fit, residual calculated from another hit

| | material budget (X/X0 %) | chip0 sigma (um) | chip2 sigma (um) | chip4 sigma (um) | chip6 sigma (um) | chip8 sigma (um) | chip10 sigma (um) |
|--------------|-------------------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|------------------------------|
| 50um | 0.697 | 6.79/6.55 | 3.69/3.75 | 4.56/4.55 | 4.76/4.67 | 3.79/3.72 | 6.74/6.85 |
| 100um | 0.804 | 7.12/6.95 | 3.82/3.84 | 4.91/4.85 | 4.99/4.99 | 3.86/3.79 | 6.91/7.32 |
| 150um | 0.911 | 7.54/7.00 | 3.85/3.96 | 5.11/5.06 | 5.16/5.17 | 3.90/3.92 | 7.25/7.54 |



Alignment

- straight line model: $x = X(z) + x_{res} = az + b + x_{res}; y = Y(z) + y_{res} = cz + d + y_{res}$
- considering misalignment:

local parameters (track parameters): a, b, c, d

global parameters (alignment parameters): $\Delta x, \Delta y, \Delta \gamma, \Delta z, \Delta \alpha, \Delta \beta$

$$X(\vec{p}^{local}, \vec{a}^{global}) = az + b - \Delta x + y\Delta y + a(\Delta z + x\Delta \beta + y\Delta \alpha)$$

$$Y(\vec{p}^{local}, \vec{a}^{global}) = cz + d - \Delta y - x\Delta \gamma + c(\Delta z + x\Delta \beta + y\Delta \alpha)$$

- minimize: $\chi^2 = \sum_{\text{data sets}} \left(\sum_{\text{events}} \left(\sum_{\text{tracks}} \left(\sum_{\text{hits}} w_i r_i^2 \right) \right) \right)$

global parameters that we want to get

- solution:
$$\begin{pmatrix} C & \cdots & H_k & \cdots \\ \vdots & \ddots & 0 & 0 \\ H_k^T & 0 & \Gamma_k & 0 \\ \vdots & 0 & 0 & \ddots \end{pmatrix} \times \begin{pmatrix} \mathbf{a} \\ \vdots \\ \mathbf{p}_k \\ \vdots \end{pmatrix} = \begin{pmatrix} \mathbf{b} \\ \vdots \\ \boldsymbol{\beta}_k \\ \vdots \end{pmatrix}$$

global and local

Loop over all tracks

$$C_k = \sum_i w_{ki} \underline{\mathbf{d}_{ki}^{global}} (\underline{\mathbf{d}_{ki}^{global}})^T,$$

related to global

$$b_k = \sum_i w_{ki} r_{ki} \underline{\mathbf{d}_{ki}^{global}},$$

derivative vectors w.r.t the global parameters

$$C' = \sum_k C_k - \sum_k H_k \Gamma_k^{-1} H_k^T,$$

$$\mathbf{a}' = C'^{-1} \mathbf{b}'$$

$$\mathbf{b}' = \sum_k \mathbf{b}_k - \sum_k H_k \Gamma_k^{-1} \boldsymbol{\beta}_k.$$

Summary

- track alignment using millepede matrix method
- considering Δx , Δy , $\Delta \gamma$ only, most misalignments can be corrected, Δy can be corrected better than Δx , Δz
- Also considering 6 alignment paras, many parameters can't be corrected, except Δy , debugging...
- Plans:
 - using actual geometry simulation data