# QCD phases under rotation

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#### **Introduction**

#### **Where rotating QCD matter: Neutron stars**





Isolated pulsars can have  $\omega \sim 10^3 s^{-1}$ 



#### Where rotating QCD matter: Rotating nuclei







(M A Riley et al 2016 Phys. Scr. 91 123002)

#### Where rotating QCD matter: Quark-gluon plasma



#### Where rotating QCD matter: Quark-gluon plasma

• From global angular momentum to vorticity to hyperon spin polarization



First measurement of Λ polarization by STAR@RHIC \*



(\* First theoretical proposal: Liang and Wang 2004)

#### parity-violating decay of hyperons

In case of  $\Lambda$ 's decay, daughter proton preferentially decays in the direction of  $\Lambda$ 's spin (opposite for anti- $\Lambda$ )

$$\frac{dN}{d\Omega^*} = \frac{1}{4\pi} (1 + \alpha \mathbf{P}_{\mathbf{\Lambda}} \cdot \mathbf{p}_{\mathbf{p}}^*)$$

 $\alpha$ :  $\Lambda$  decay parameter ( $\alpha_{\Lambda}$ =0.732) P\_{\Lambda}:  $\Lambda$  polarization p<sub>p</sub><sup>\*</sup>: proton momentum in  $\Lambda$  rest frame



#### Where rotating QCD matter: Quark-gluon plasma

• More recent measurements:  $\Xi^-$ ,  $\Omega^-$  by STAR@RHIC,  $\Lambda$  by ALICE@LHC



hyperon	decay mode	ah	magnetic moment µ <sub>H</sub>	spin
Λ (uds)	Λ→pπ⁻ (BR: 63.9%)	0.732	-0.613	1/2
∃- (dss)	Ξ-→Λπ- (BR: 99.9%)	-0.401	-0.6507	1/2
Ω- (sss)	Ω-→ΛK- (BR: 67.8%)	0.0157	-2.02	3/2

•  $\Lambda$  at low energy by STAR@RHIC 2021, HADES@GSI 2021





 "The most vortical fluid": ω ~ 10<sup>20</sup> - 10<sup>21</sup>s<sup>-1</sup>

 Relativistic suppression
 at high energies

(Deng-XGH 2016, Deng-XGH-Ma-Zhang 2020)

## **Effects of rotation: Comparison with magnetic field**

• Hints for possible rotation effect: comparison with B field





#### **Rotation field**







In rotating frame, Coriolis force:  $F = 2m(\dot{x} \times \omega) + O(\omega^2)$ 

#### **Orbital:**

Larmor theorem:  $eB \sim 2m\omega$ 

## **Effects of rotation: Comparison with chemical potential**

• Hints for possible rotation effect: comparison with chemical potential



#### (At rotating axis, for unbounded system)

(Ambrus and Winstanley 2019; Palermo etal 2021)

>>> Both have sign problem on lattice

### **QCD** phase diagram



- Rotation affects chiral condensate and confinement?
- Rotation effects combined with finite temperature, densities, B field?

#### **Can rotation affect chiral condensate?**

## **Angular momentum polarization**

• Consider a scalar (or pseudoscalar) pair of fermions



- Thus in general, rotation tends to suppress  $\sigma, \Delta, \pi, \dots$
- Compare with magnetic catalysis (dimensional reduction)





#### **Rotating fermions**

• Consider a rotating frame



• Fermion field

$$S = \int d^4x \sqrt{-g} \bar{\psi} \left( i\gamma^{\mu} \nabla_{\mu} - m_0 \right) \psi \qquad \nabla_{\mu} = \partial_{\mu} + i \hat{Q} A_{\mu} + \Gamma_{\mu}$$
$$\downarrow$$
$$H = \hat{Q} A_0 + m_0 \beta + \boldsymbol{\alpha} \cdot \boldsymbol{\pi} - \boldsymbol{\Omega} \cdot \left( \mathbf{r} \times \boldsymbol{\pi} + \boldsymbol{\Sigma} \right)$$

#### **Rotating fermions**

• Uniformly rotating system must be finite



- Boundary conditions for Dirac fermions in a cylinder
  - Dirichlet B.C. (No)
  - MIT B.C. (Yes)

$$[i\gamma^{\mu}n_{\mu}(\theta) - 1]\psi\Big|_{r=R} = 0$$
  $i = 0$   $j^{\mu}n_{\mu} = 0$  at  $r = R$ 

• No-flux B.C. (Yes)

### **Rotating fermions**

• Consider no-flux B.C.



- $p_t = p_{l,k}$  discretized by  $J_l(p_{l,k}R) = 0$
- $E = (p_{l,k}^2 + p_z^2 + m^2)^{1/2} > \Omega |l + \frac{1}{2}|$
- Vacuum does not rotate

(Vilenkin 1979, Ebihara-Fukushima-Mameda 2016)

• To see uniform rotation effect, we need **T**, **μ**, **B**, .....

Figures drawn by K.Mameda



*B*: Chen-XGH etal 2015, Liu-Zahed 2017, Chen-Mameda-XGH 2019, Cao-He 2019, Tabatabaee etal 2021, ...





μ: XGH-Nishimura-Yamamoto 2017,
Zhang-Hou-Liao 2018, Huang etal
2018, Nishimura etal 2020,2021,
Hou etal 2022,2023...

T: Jiang-Liao 2016, Chernodub-Gongyo 2017, Wang etal 2019, Luo etal 2020, Jiang 2021, Huang etal 2020-2023, ...

• Take a four-fermion model

$$Z = \int \mathcal{D}[\bar{\psi}, \psi] \exp\left(i \int d^4 x \sqrt{-g} \mathcal{L}_{\text{NJL}}\right)$$
$$\mathcal{L}_{\text{NJL}} = \bar{\psi}(i\gamma^{\mu}\nabla_{\mu} - m_0)\psi + \frac{G}{2}[(\bar{\psi}\psi)^2 + (\bar{\psi}i\gamma^5\tau\psi)^2]$$
$$\nabla_{\mu} = \partial_{\mu} + i\hat{Q}A_{\mu} + \Gamma_{\mu}$$

• Mean-field approximation

$$V_{\rm eff} = \frac{1}{\beta V} \int d^4 x_E \left\{ \frac{\sigma^2 + \pi^2}{2G} - \sum_{\{\xi\}} \left[ \frac{\varepsilon_{\{\xi\}}}{2} + \frac{1}{\beta} \ln(1 + e^{-\beta \varepsilon_{\{\xi\}}}) \right] \Psi_{\{\xi\}}^{\dagger} \Psi_{\{\xi\}} \right\}$$

 $\{ \mathcal{E}_{\{\xi\}} \}$  and  $\{ \Psi_{\{\xi\}} \}$  : Eigen-energy and eigen-wavefunction with quantum numbers  $\{ \xi \}$ 

• Consider a simple case: massless, no pion modes, homogeneous

$$\varepsilon_{l,\pm} = \pm \sqrt{p_z^2 + p_t^2 + \sigma^2} - \Omega \left( l + \frac{1}{2} \right) \qquad \qquad \varepsilon_{n,\pm} = \pm \sqrt{p_z^2 + \sigma^2 + 2nqB}$$

Ration

Magnetic field

• Chiral condensate vs rotation and/or magnetic field



• Consider a simple case: massless, no pion modes, homogeneous

$$\varepsilon_{l,\pm} = \pm \sqrt{p_z^2 + p_t^2 + \sigma^2} - \Omega\left(l + \frac{1}{2}\right)$$
Ration
$$\mu$$

$$\varepsilon_{n,\pm} = \pm \sqrt{p_z^2 + \sigma^2 + 2nqB}$$

Magnetic field

• Compare with finite-density case:



Sakai-Sugimoto model

(Freis-Rebhan-Schmitt 2010)



Quark-meson model

(Andersen-Tranberg 2012)

• Chiral condensate with rotation: finite temperature



#### **Can rotation affect confinement?**

### **Confinement under rotation**

- It is not easy to intuitively imagine the rotational effect on confinement
- Results based on holography



(Chen-Zhang-Li-Hou-Huang 2020)

#### Rotation favors deconfinement

### **Confinement under rotation**

- It is not easy to intuitively imagine the rotational effect on confinement
- Argument based on hadron resonance gas (HRG) model



(Fujimoto-Fukushima-Hidaka 2021)

Rotation favors deconfinement

### **Confinement under rotation**

- It is not easy to intuitively imagine the rotational effect on confinement
- Argument based on Tolman-Ehrenfest temperature



(Chernodub 2020)

#### Rotation favors deconfinement

### Lattice calculation of rotating QCD

(Yang-XGH 2023)

### **Formulate rotating lattice**

- Gluons and Wilson fermions (Angular momentum) (Yamamoto-Hirono 2013)
- Pure gluons (Polyakov loop) (Braguta etal 2021)
- We consider gluons and 2+1 flavor staggered fermions



• We measure: (imaginary) angular momentum

Ji decomposition

$$\mathbf{J} = \mathbf{J}_G + \mathbf{s}_q + \mathbf{L}_q$$

#### **Formulate rotating lattice**

- Gluons and Wilson fermions (Angular momentum) (Yamamoto-Hirono 2013)
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• We measure: chiral condensate and Polyakov loop

$$\Delta_{l,s}(T,\Omega) = \frac{\langle \bar{\psi}_l \psi_l \rangle_{T,\Omega} - \frac{m_l}{m_s} \langle \bar{\psi}_s \psi_s \rangle_{T,0}}{\langle \bar{\psi}_l \psi_l \rangle_{0,0} - \frac{m_l}{m_s} \langle \bar{\psi}_s \psi_s \rangle_{0,0}}$$

$$L_{ren} = \exp(-N_{\tau}c(\beta)a/2)L_{bare}$$
$$L_{bare} = \operatorname{tr}\left[\sum_{\mathbf{n}}\prod_{\tau}U_{\tau}(\mathbf{n},\tau)\right]/3N_{x}^{3}$$

#### Angular momentum

- Angular momentum
- $J_G$  and  $L_q$  approximately  $\propto r^2$ , and  $s_q$  approximately independent of r, thus



## **Chiral condensate and Polyakov loop**



#### Chiral condensate and Polyakov loop

• Chiral and Polyakov loop susceptibilities



- Imaginary rotation tends to melt chiral condensate and deconfine the system
- The phase transition lines on  $T \Omega$  plane coincide
- Since they are even function of rotation, if we naively shift to real rotation, this implies rotational catalysis of chiral breaking and confinement
- Opposite to effective models



#### **Imaginary rotation to real rotation**



• Can we make the analytical continuation to real rotation?



> Lattice QCD with Taylor expansion at small rotation



#### **Summary and outlooks**

### **Summary and outlooks**

- It is NOT understood how rotation modifies chiral and deconfinement phase transitions of QCD.
- Outlooks:

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... ...

- More lattice simulations for imaginary rotation
- Cross check torsion effect on chiral condensate and confinement on lattice (Yamamoto 2020)

#### • More model studies

(Chen-Fukushima-Shimada 2022; Sun-Xu-Huang 2023)



# Thank you!

#### **Rotating QCD matter: Quark-gluon plasma**



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#### No rigid rotation\*, but local fluid vorticity

\* At low energy, there is a possibility that two colliding nuclei fuse into a compound high-spin nucleus

### **Rotating QCD matter: Quark-gluon plasma**

Angular momentum conservation



#### No rigid rotation\*, but local fluid vorticity

$$\boldsymbol{\omega} = \frac{1}{2} \boldsymbol{\nabla} \times \boldsymbol{v}$$

(Angular velocity of fluid cell)



- Estimation at low energy  $\sqrt{s} \gtrsim 2m_N$
- Estimation at high energy  $\sqrt{s} \gg 2m_N$ part of  $J_0 \sim Ab \sqrt{s}$  retained in the produced matter:

$$J \approx \int d^3 x \gamma^2(x) \varepsilon(x) x_{\perp}^2 \overline{\omega} \sim s A \sqrt{s} R_A^2 \overline{\omega} / (2m_N)^2$$
 for  $b < 2R_A$ 

 $\overline{\omega} \sim \frac{b}{R_A^2} \left(\frac{2m_N}{\sqrt{s}}\right)^2 \sim 10^{19} s^{-1}$  $(b = R_A, \sqrt{s} = 200 \text{ GeV})$ 

\* At low energy, there is a possibility that two colliding nuclei fuse into a compound high-spin nucleus