



PRECISION SM HIGGS PREDICTIONS AND FUTURE PROSPECTS

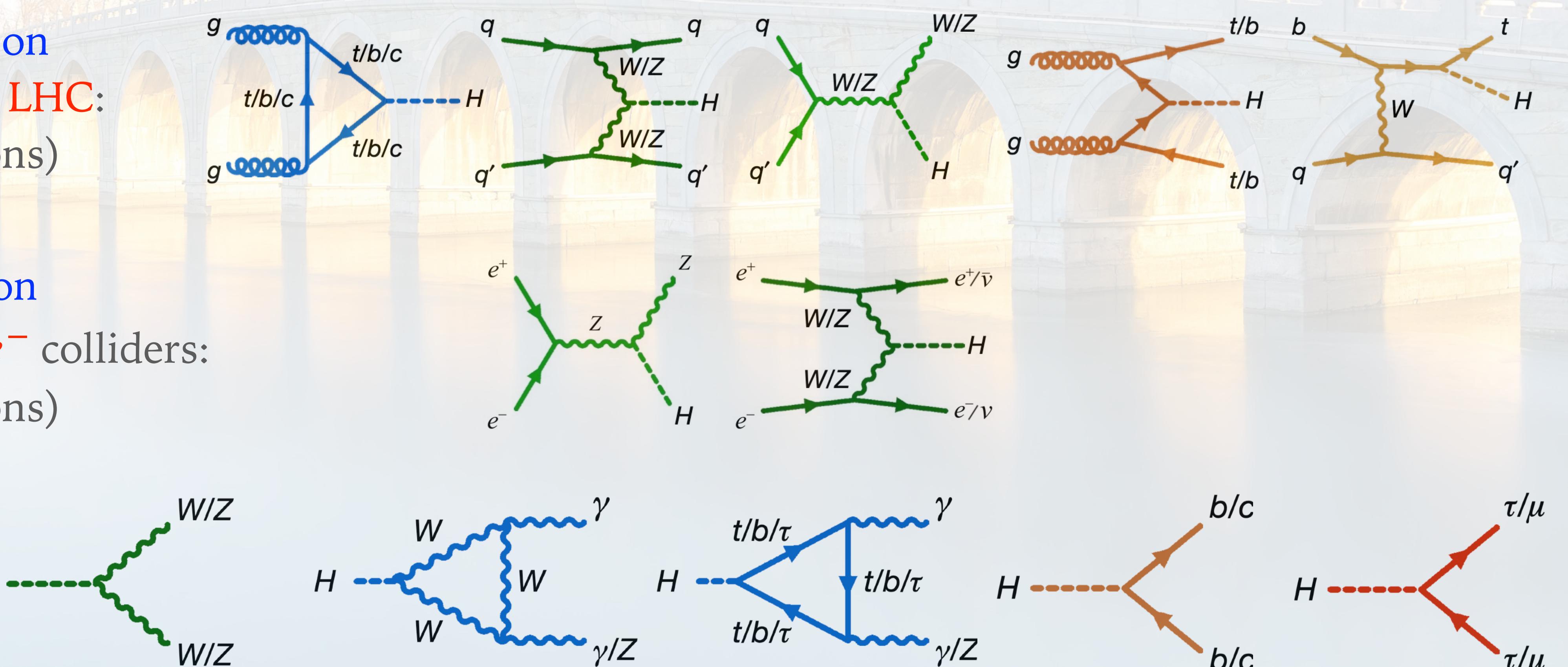


Xuan Chen

Beijing, China
27 November, 2023

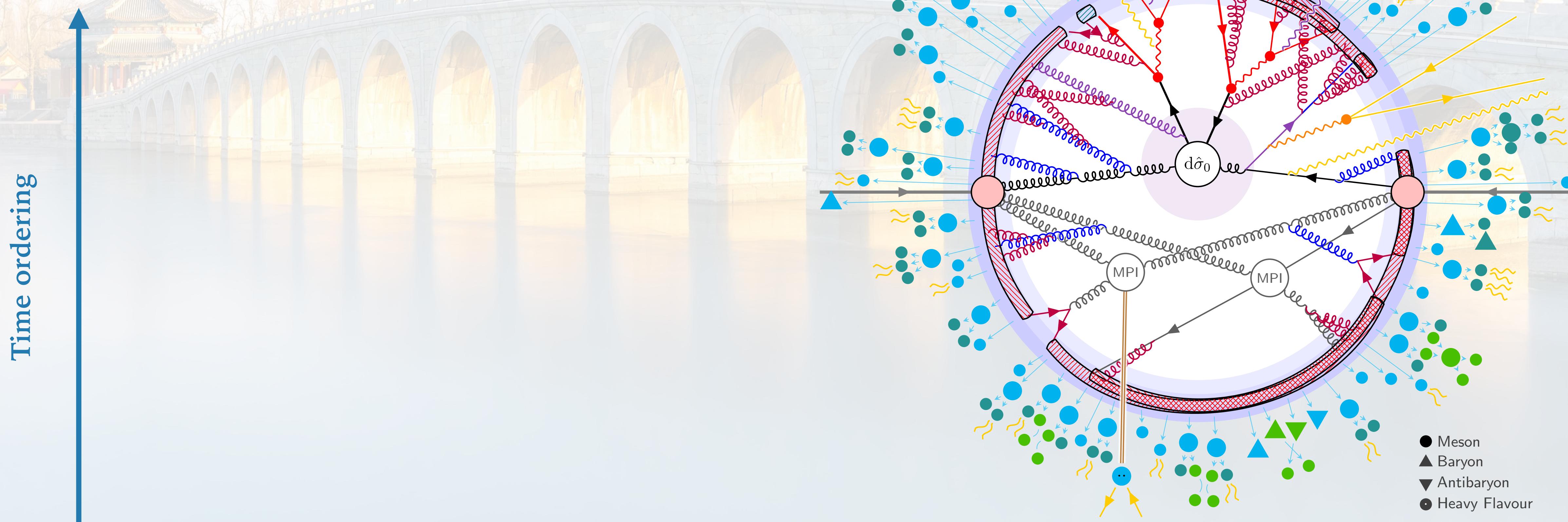


Standard Model Higgs Boson

- SM Higgs properties
 - A fundamental scalar boson with spin zero, CP even, giving mass to SM massive particles (SSB)
 - $m_H \sim 125$ GeV leads metastable EW vacuum but all current data compatible with SM predictions
 - Higgs production channels at the LHC:
(by cross sections)
 - Higgs production channels at e^+e^- colliders:
(by cross sections)
 - Higgs decay channels:
- 

Collider Event in Theorist's Eye

- For a scale of 100 GeV, the idea of factorisation in Quantum Field Theory plays important role to help understanding complex high energy processes:



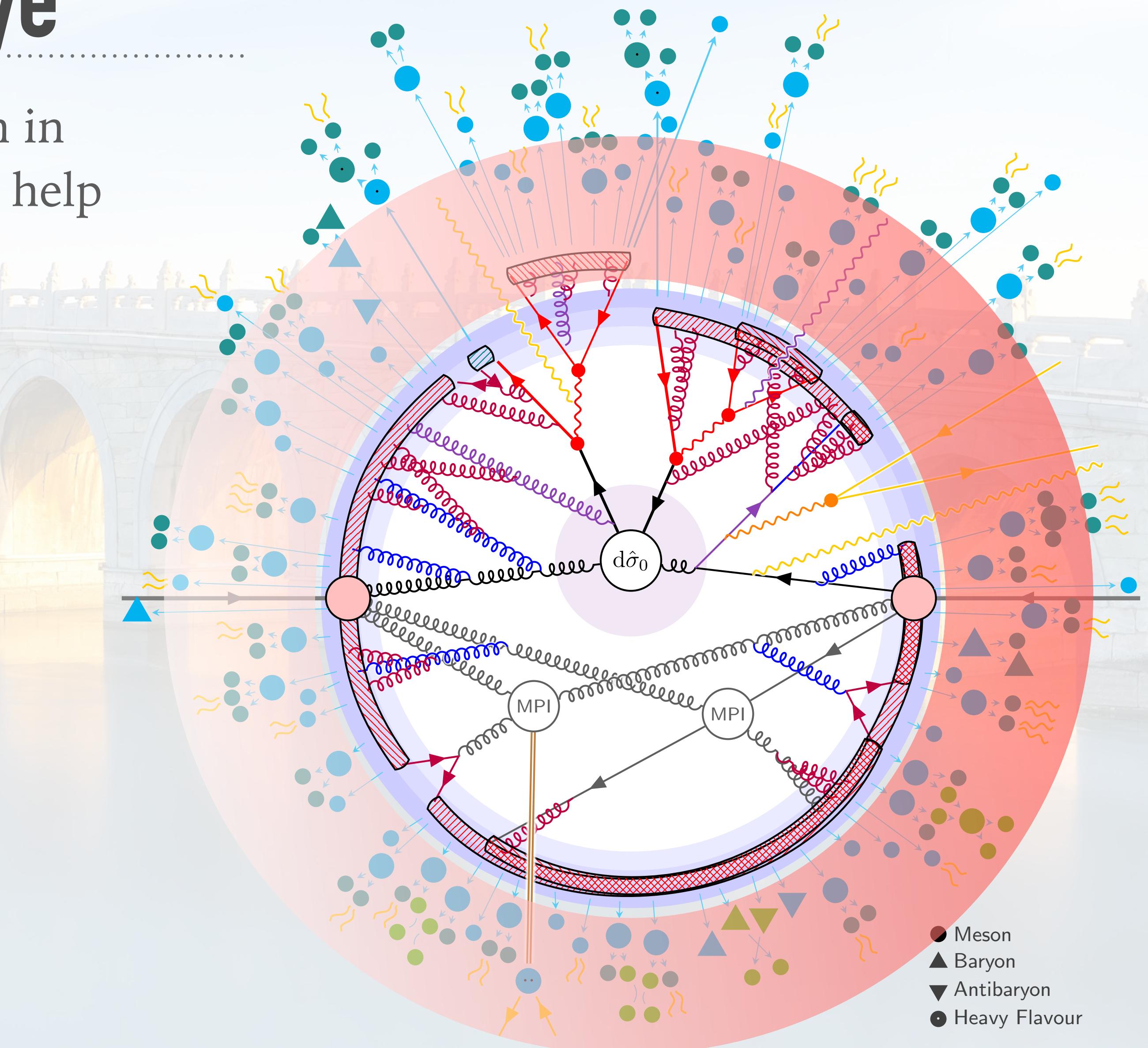
PYTHIA 8.3

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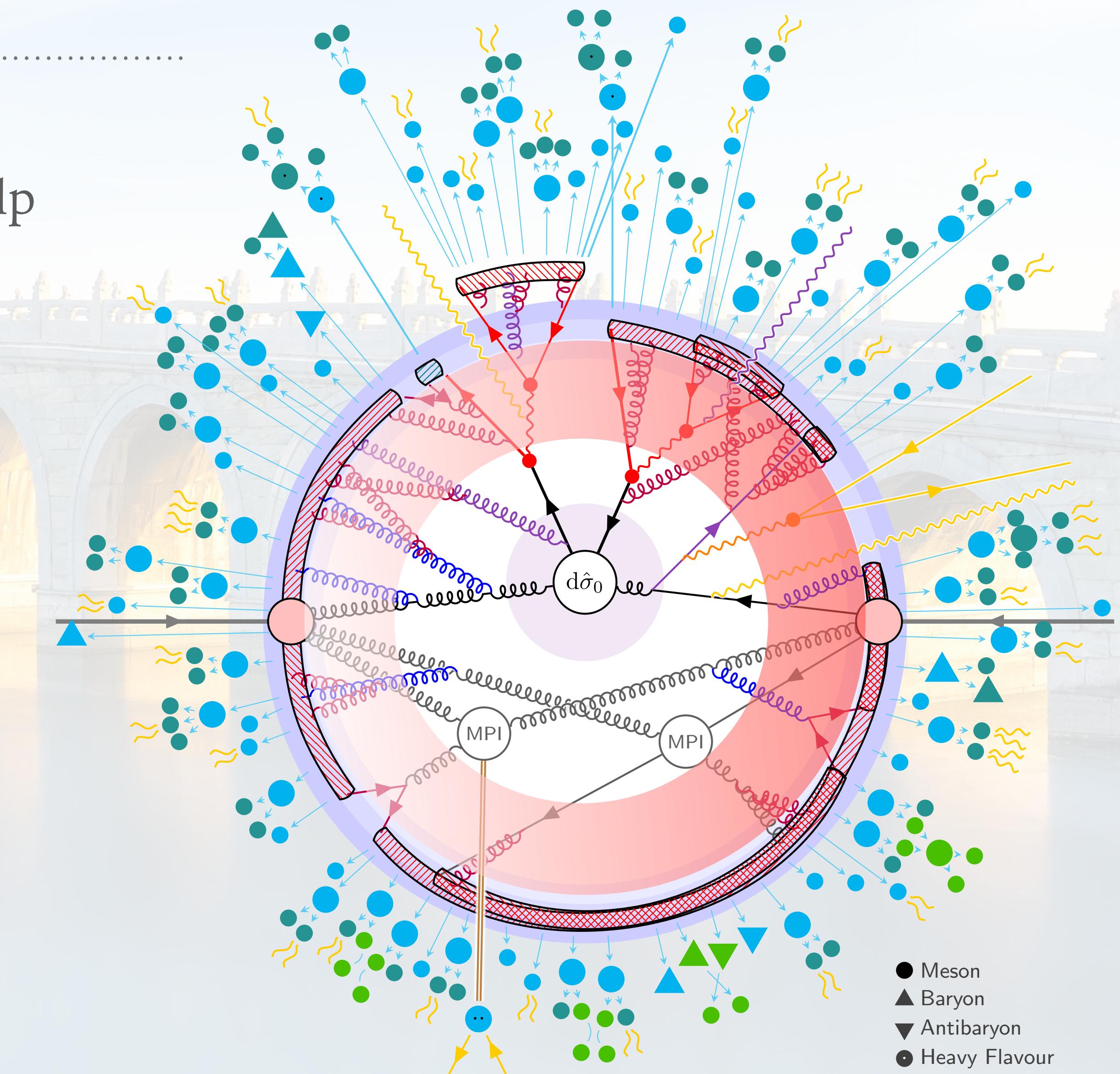
Hadronisation



PYTHIA 8.3

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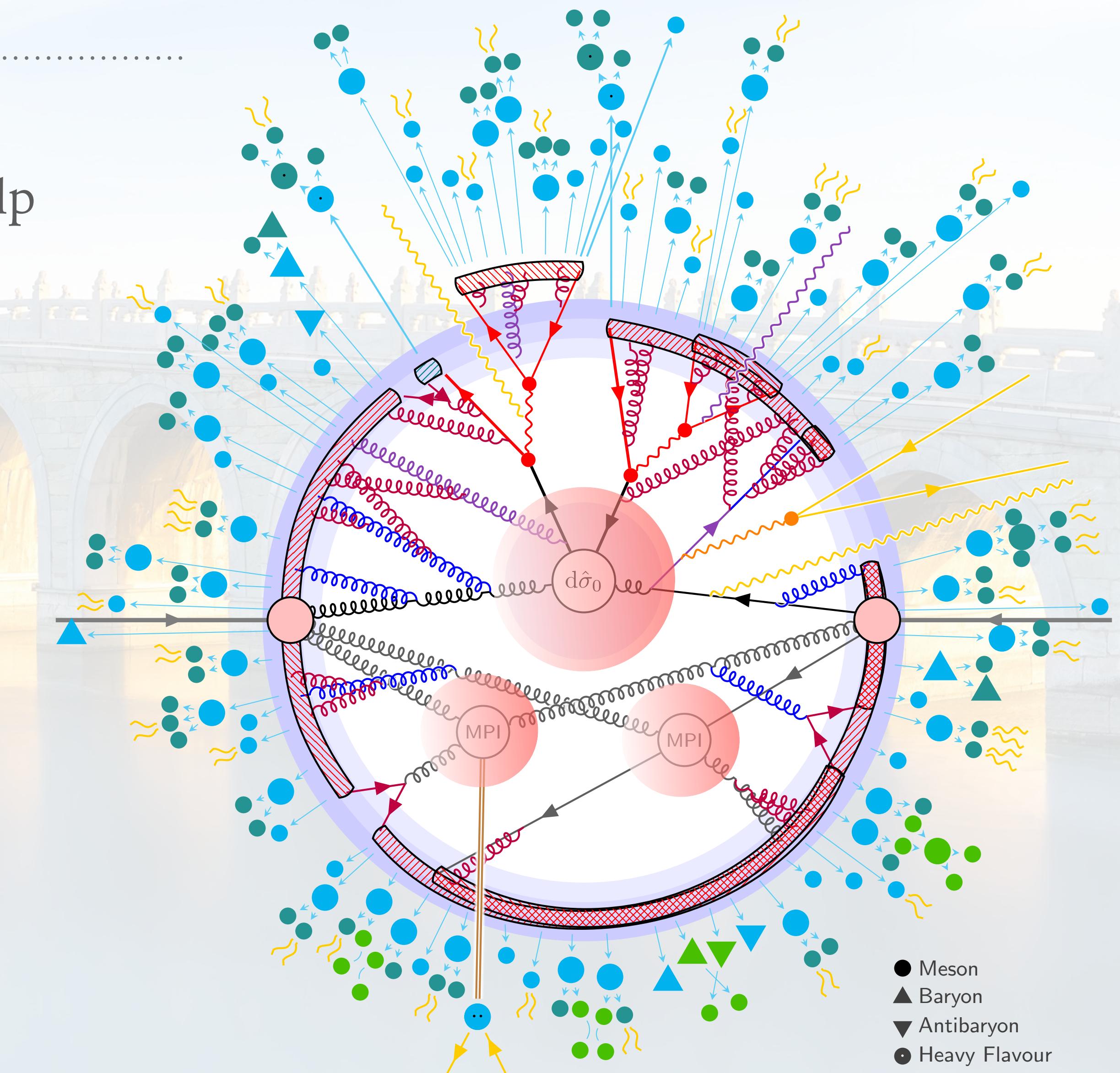
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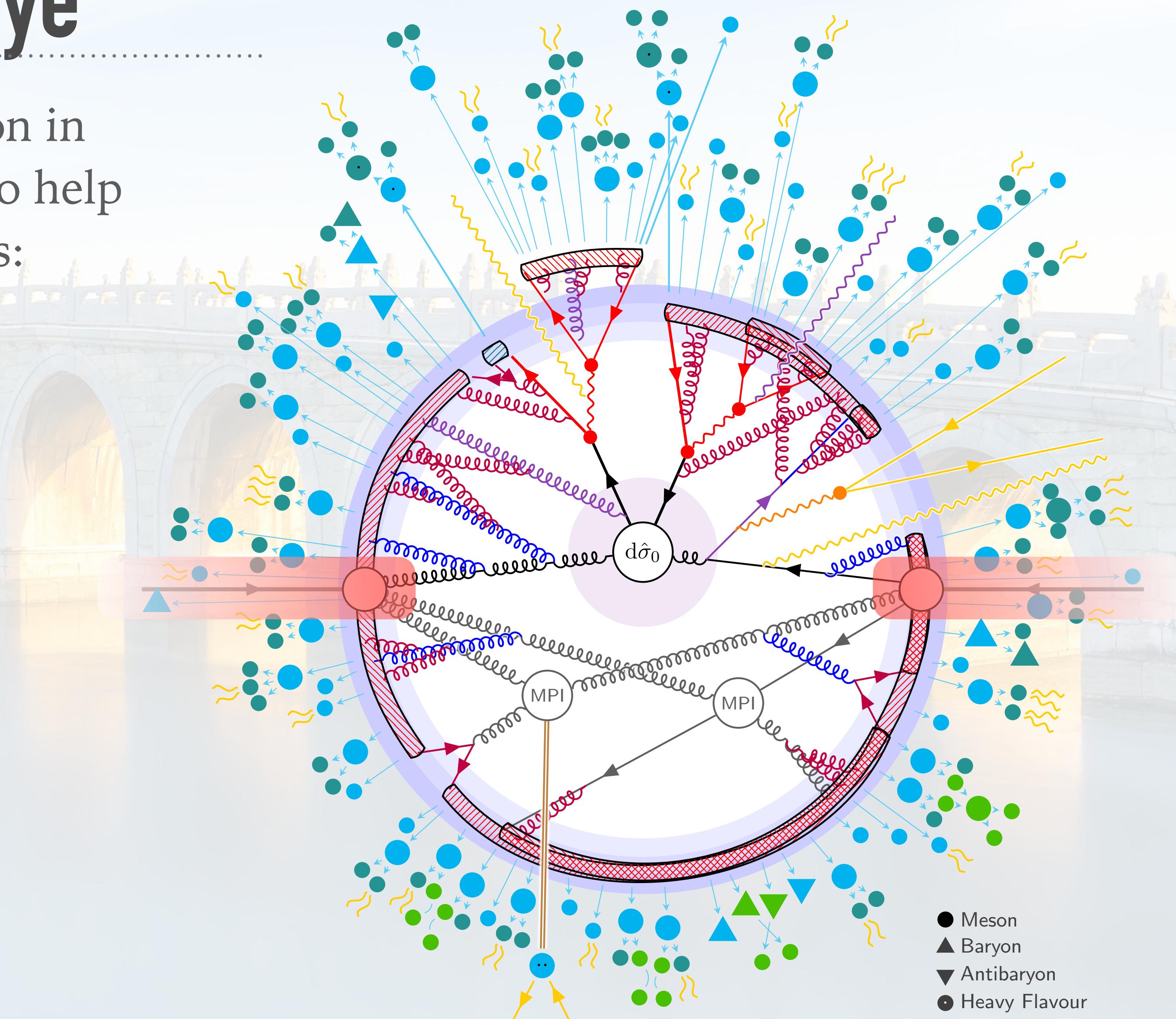
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PYTHIA 8.3

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PYTHIA 8.3

The Bucket Effect in Precision Predictions



The Bucket Effect in Precision Predictions

Which is the
shortest panel?

Hadronisation

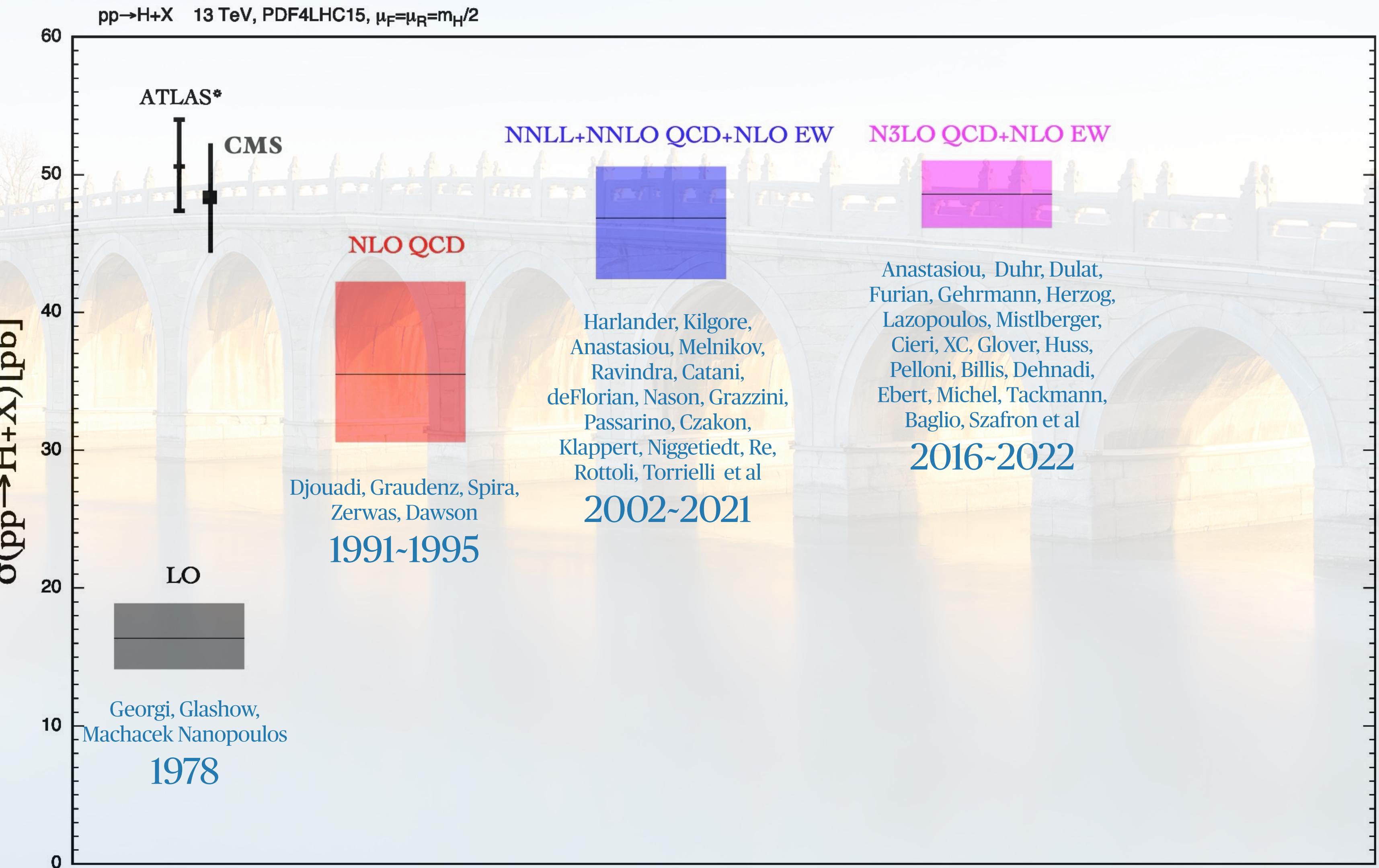
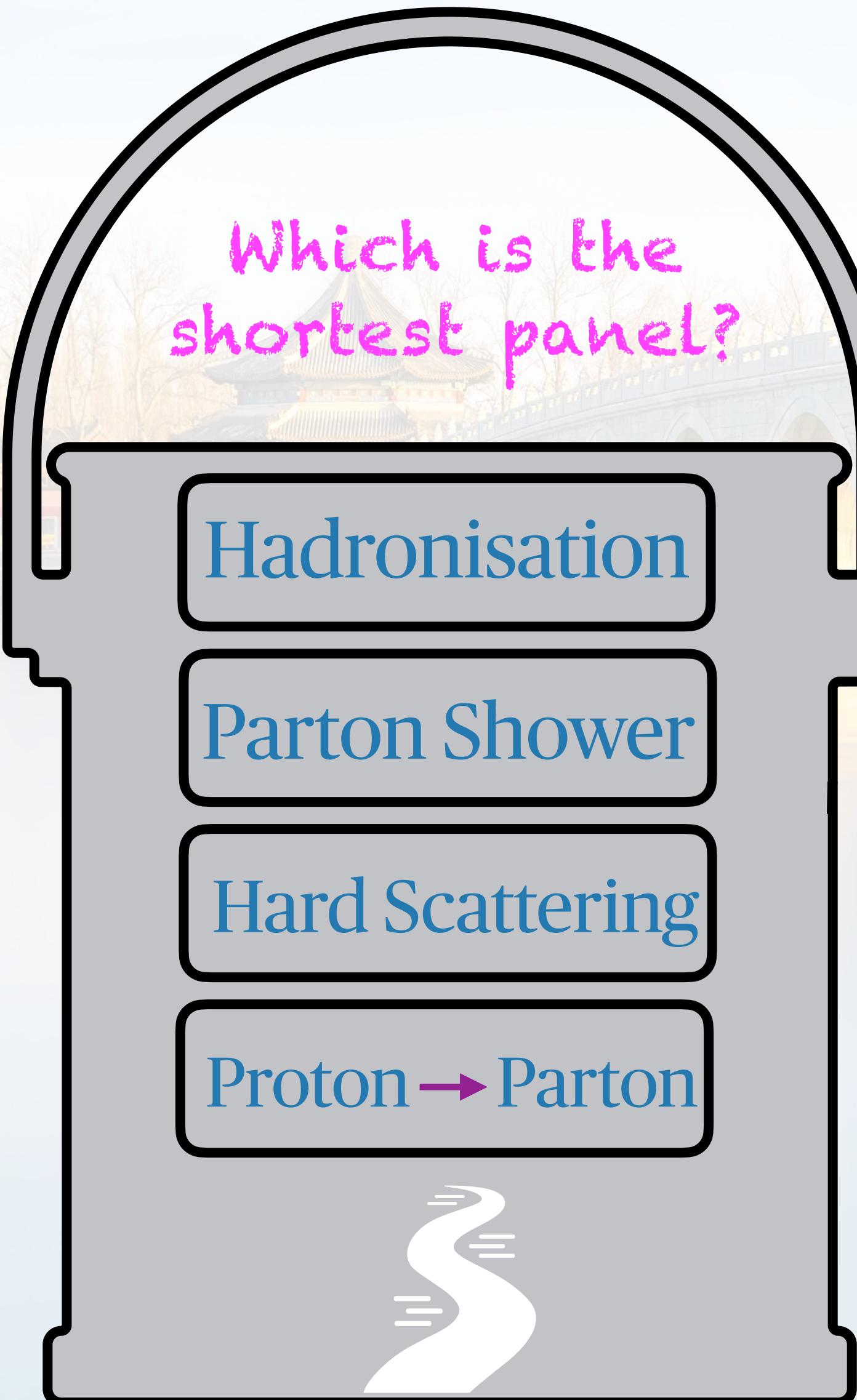
Parton Shower

Hard Scattering

Proton → Parton

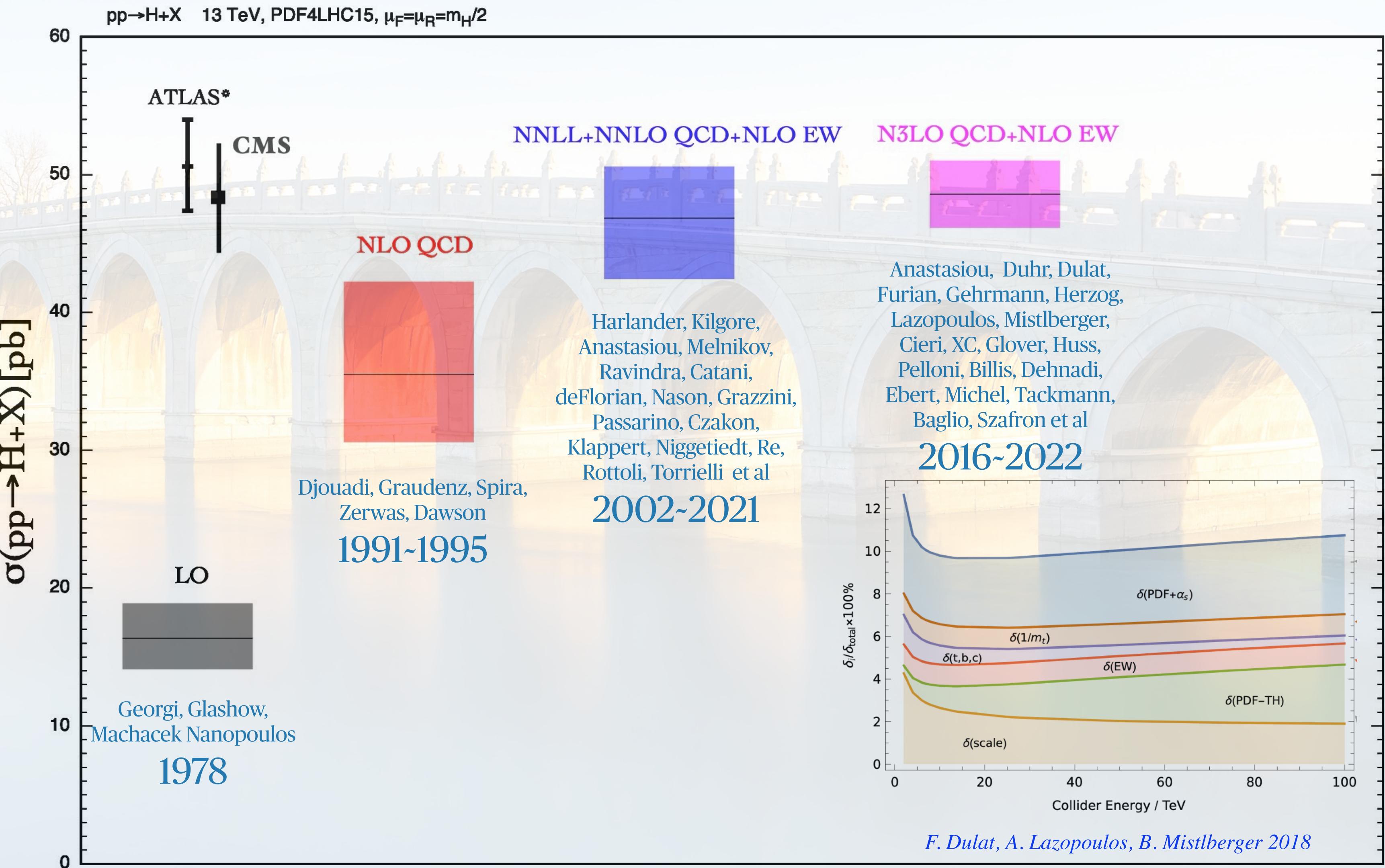
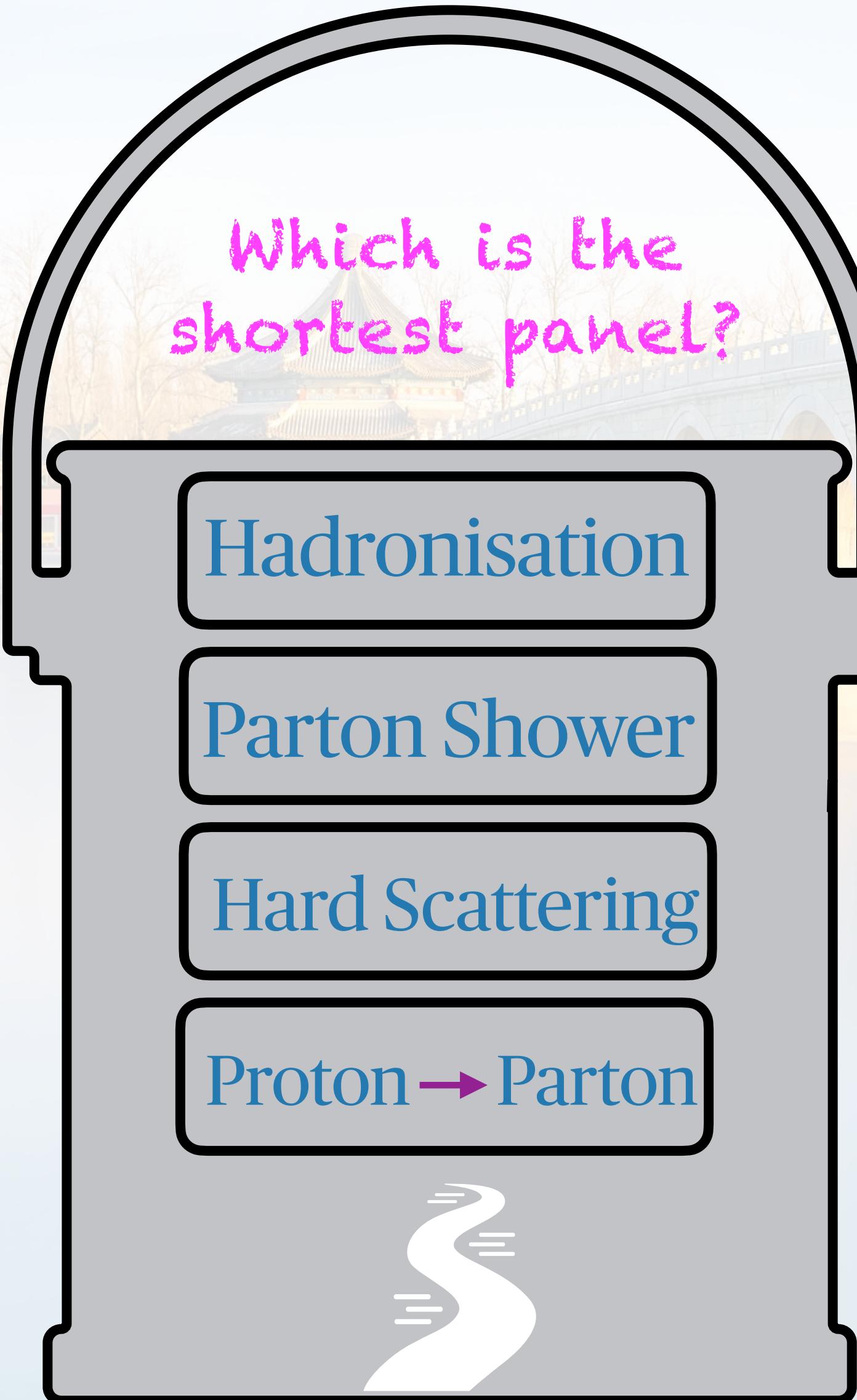


The Bucket Effect in $pp \rightarrow H + X$



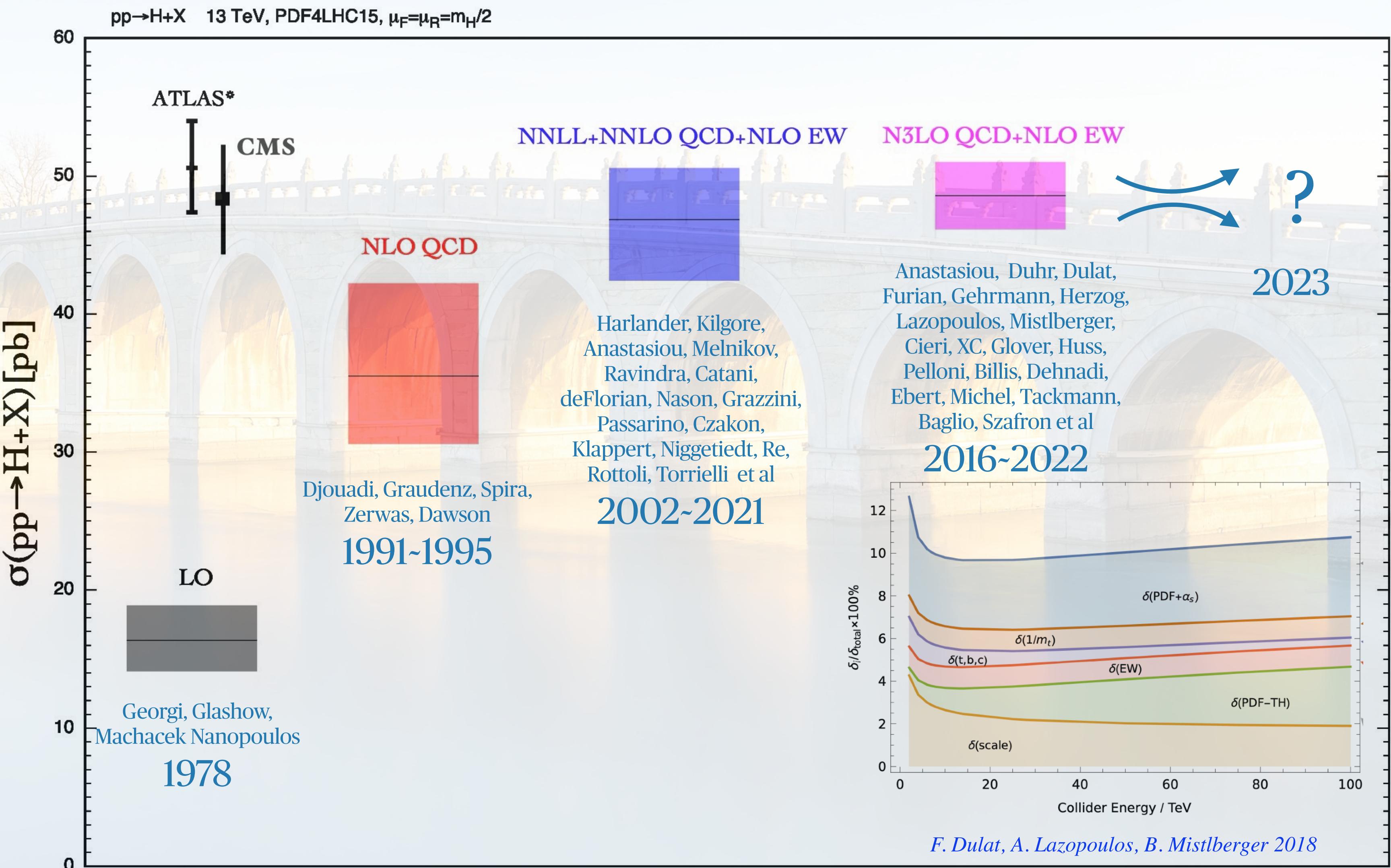
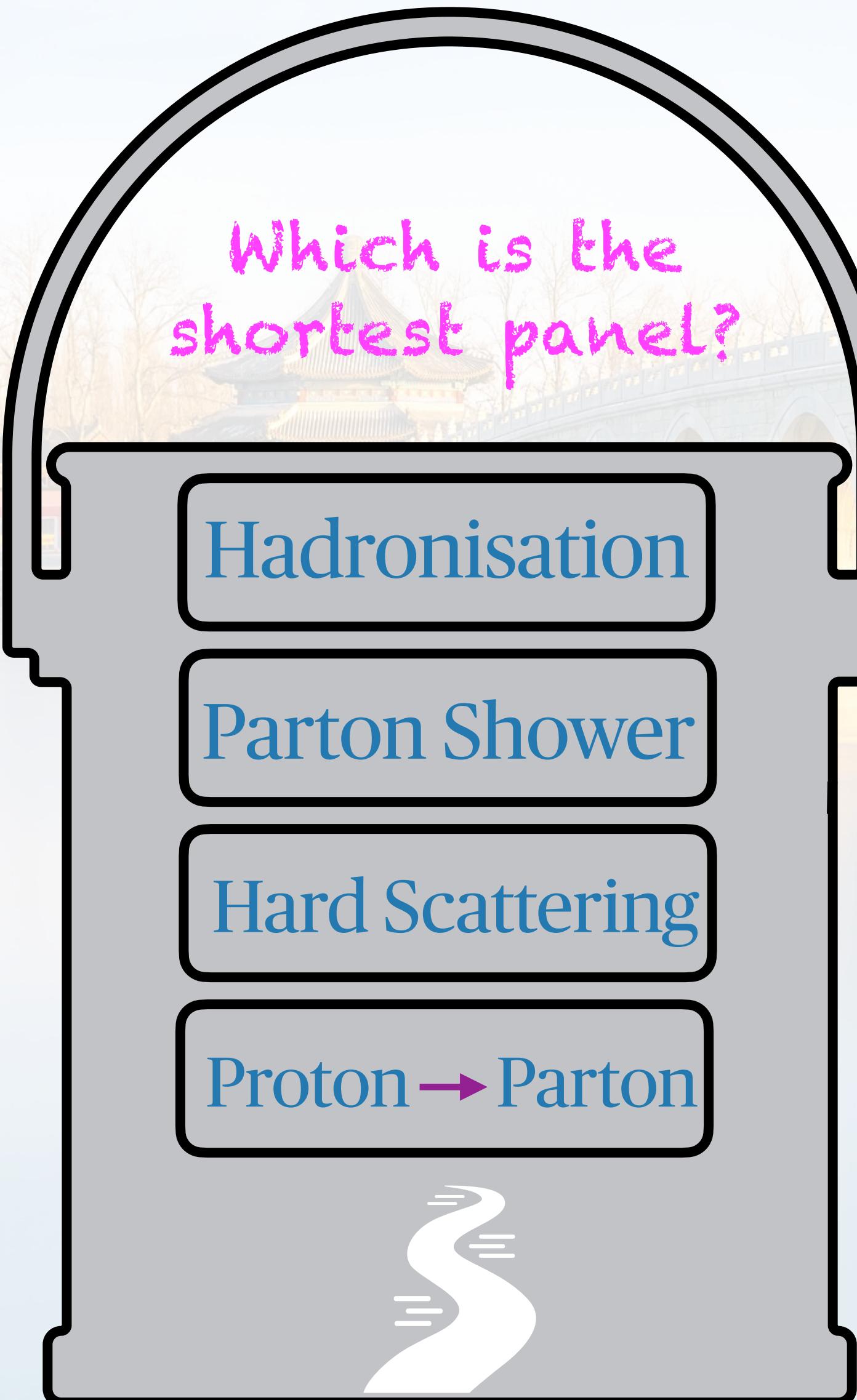
Slide based on M. Grazzini's talk @ Higgs10

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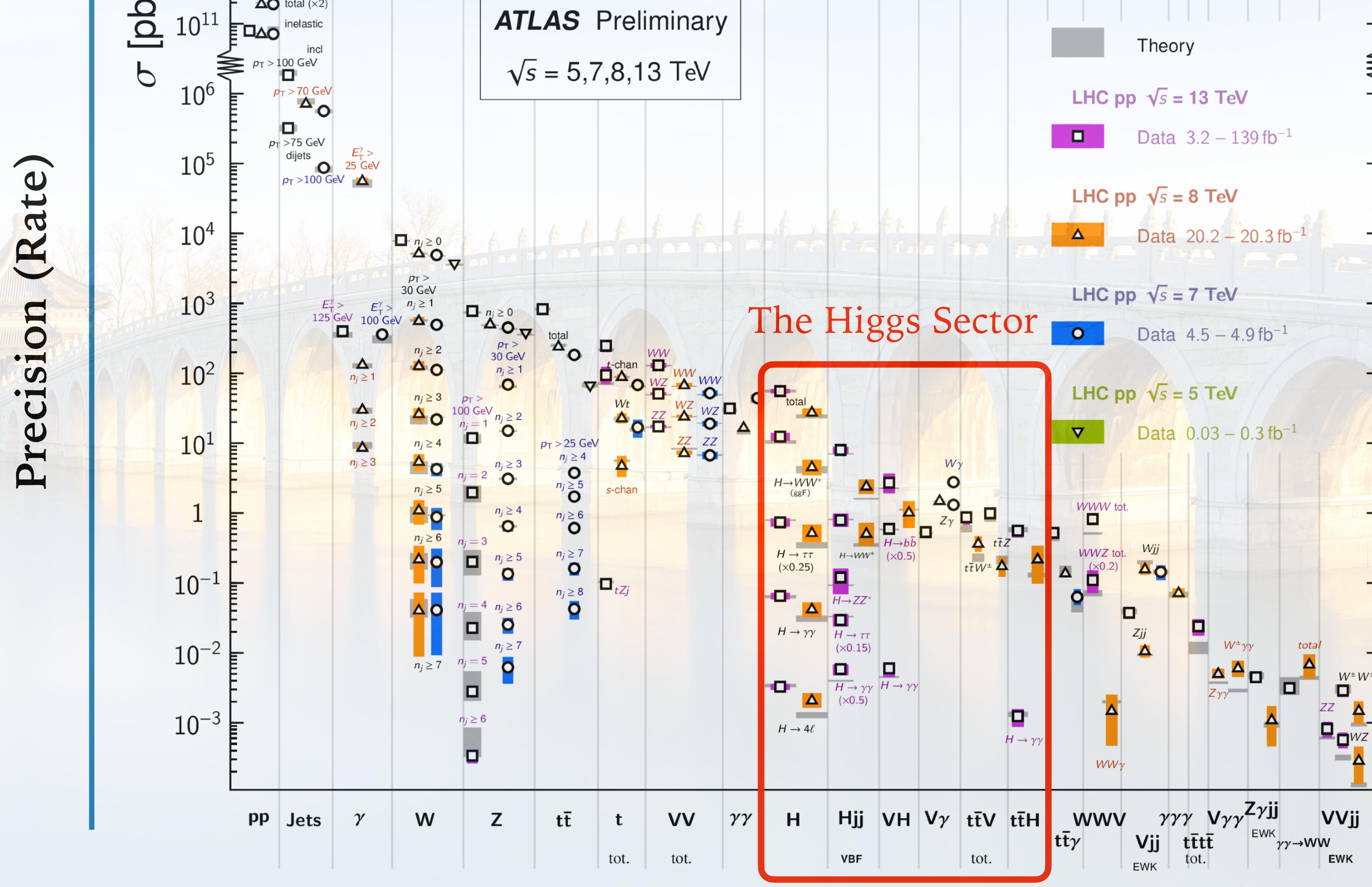
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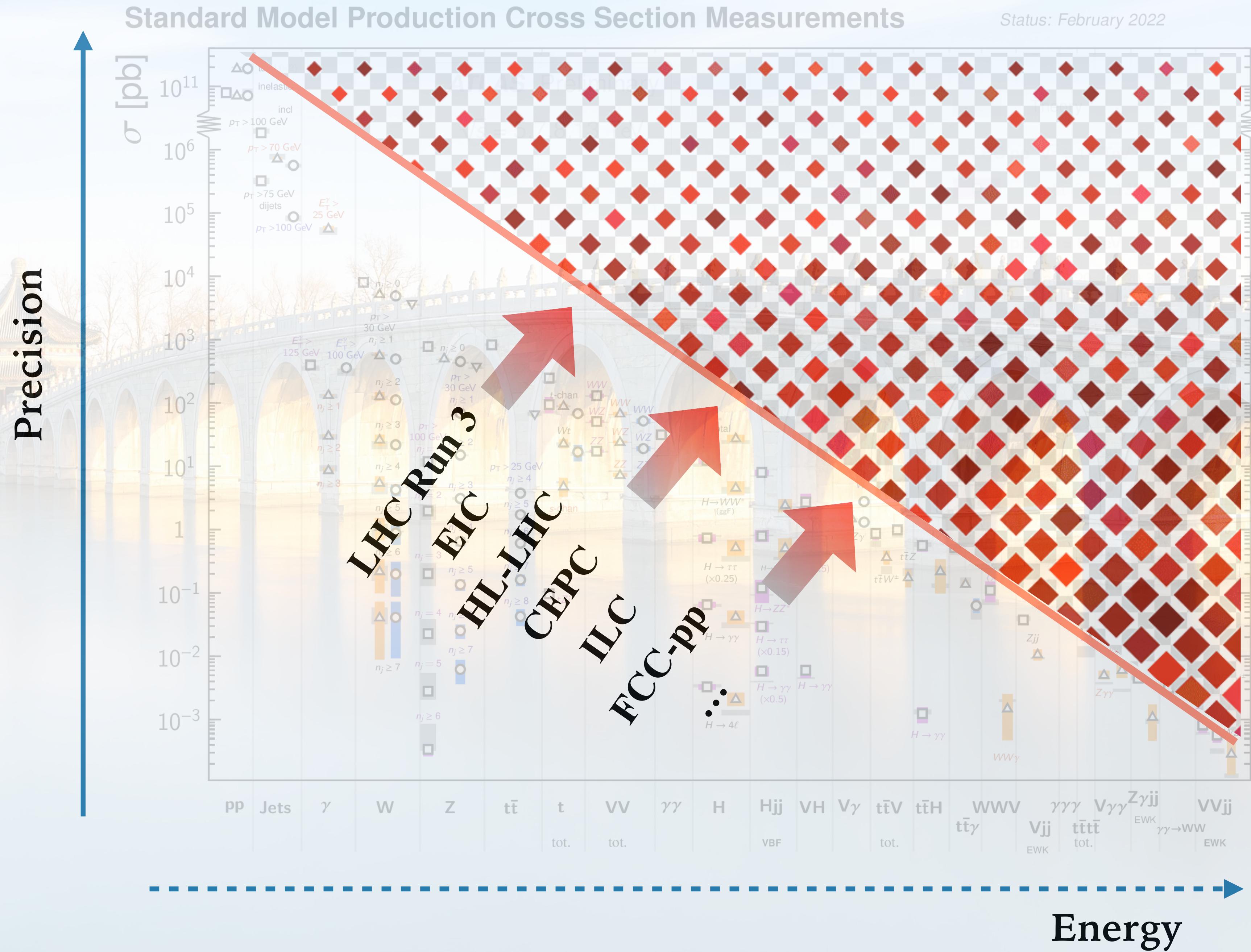
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Standard Model Production Cross Section Measurements

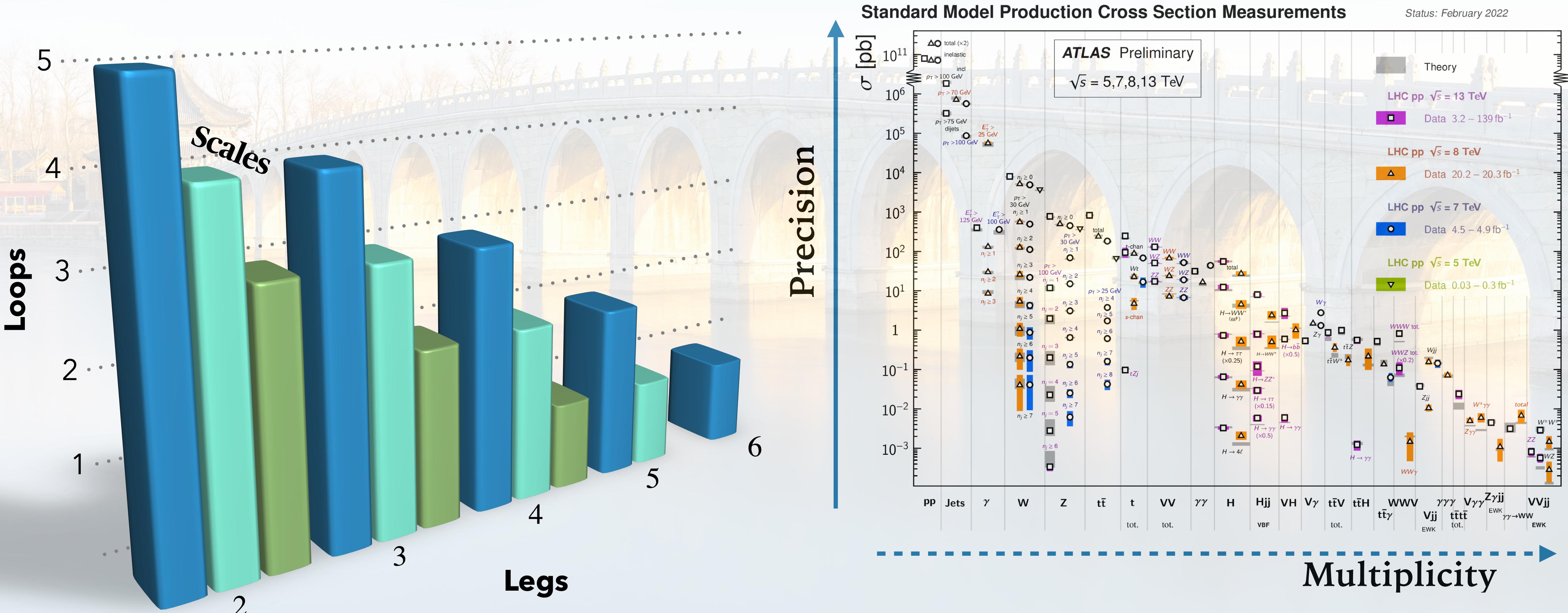
Status: February 2022



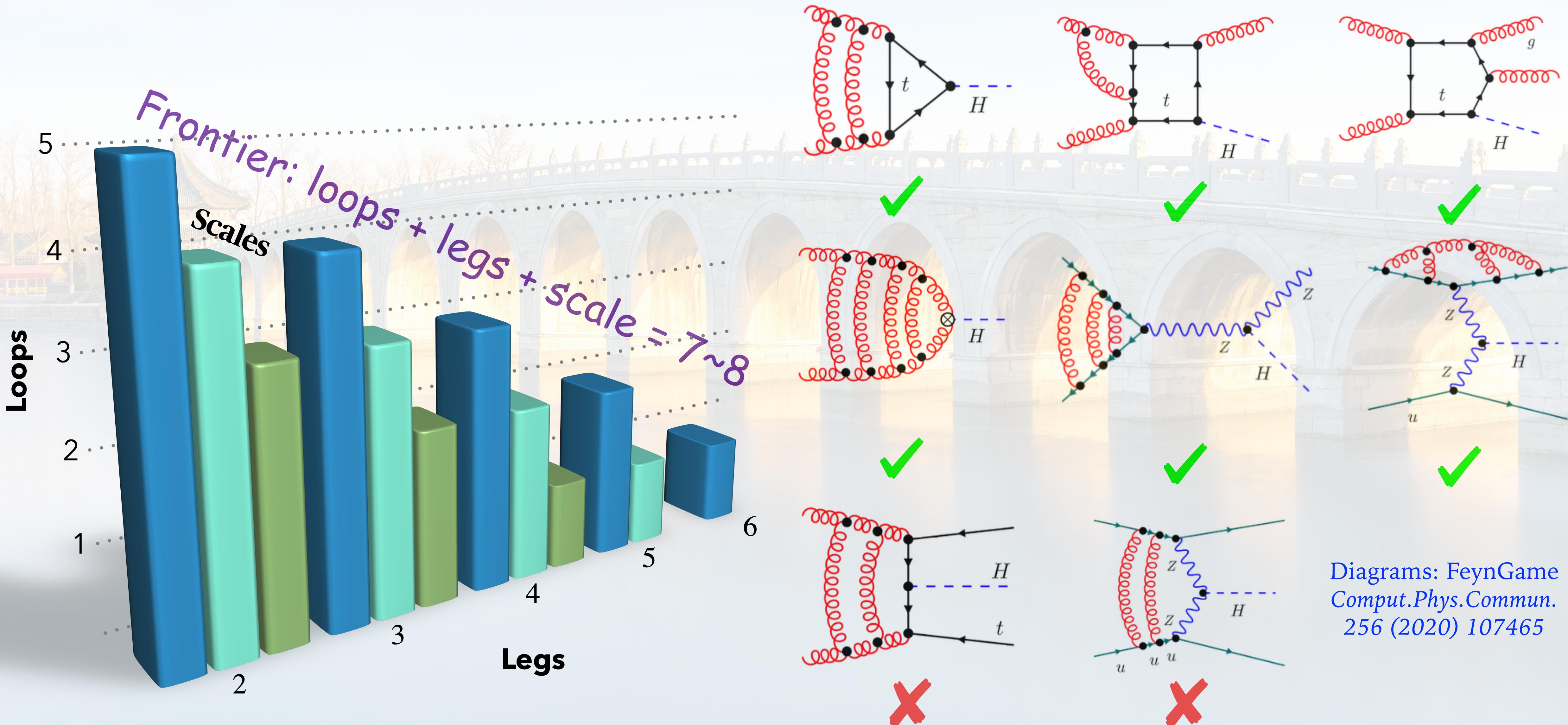
Energy (Multiplicity)



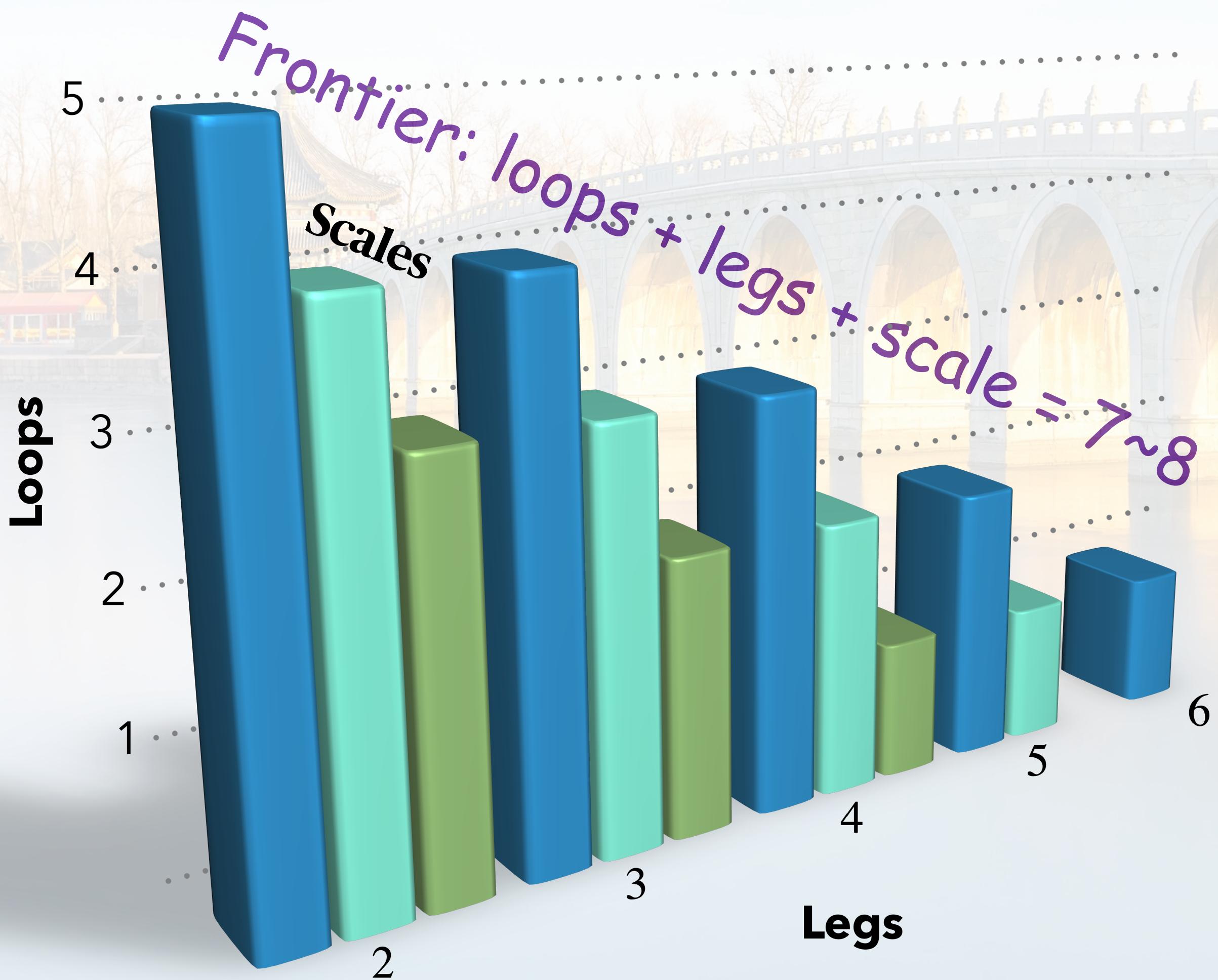
Perturbative QFT for Precision Predictions



Perturbative QFT for Precision Predictions



Perturbative QFT for Precision Predictions



Generalised polylogarithms
Riemann zeta values
Elliptic functions
...
Unitarity
Generalised Unitarity
Recursion
Twistors
Differential equations
Integrand/Integral
Sector decomposition
Numerical unitarity
Finite field
Auxiliary mass flow
Neural network amplitude
...

Parton Distributions @ approximated N3LO

State-of-the-art Parton Distribution Functions

- Theory input
 - Option A: solve proton wave function with Lattice QCD *Recent progress in D. Chakrabarti, P. Choudhary et. al. 2304.09908*
 - Option B: collinear factorisation $f_a \rightarrow f_a(x, \mu)$ with p-QCD evolution of factorisation scale
- Experiment input
 - All past and current measurements of DIS, DY, jets etc. provide fitting targets of $f_a(x, Q)$
 - Differential and total cross sections provide sensitivity in different regions of $x \in [0, 1]$
 - Various technology for fitting: functional form, neural network, fast evaluation grids etc.

$$\frac{d}{d \ln \mu^2} \begin{pmatrix} f_q \\ f_g \end{pmatrix} = \begin{pmatrix} P_{q \leftarrow q} & P_{q \leftarrow g} \\ P_{g \leftarrow q} & P_{g \leftarrow g} \end{pmatrix} \otimes \begin{pmatrix} f_q \\ f_g \end{pmatrix}$$

DGLAP evolution with

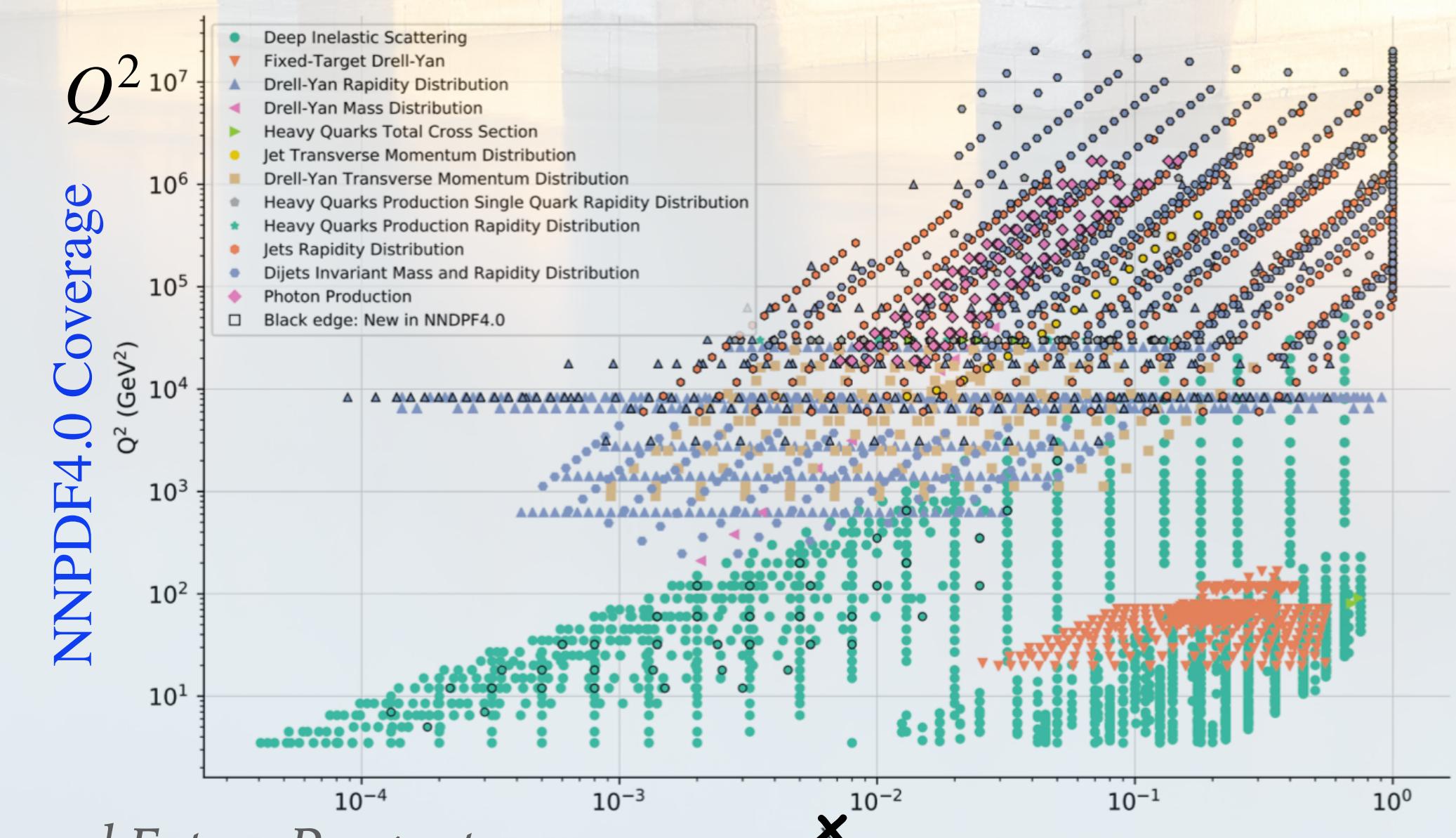
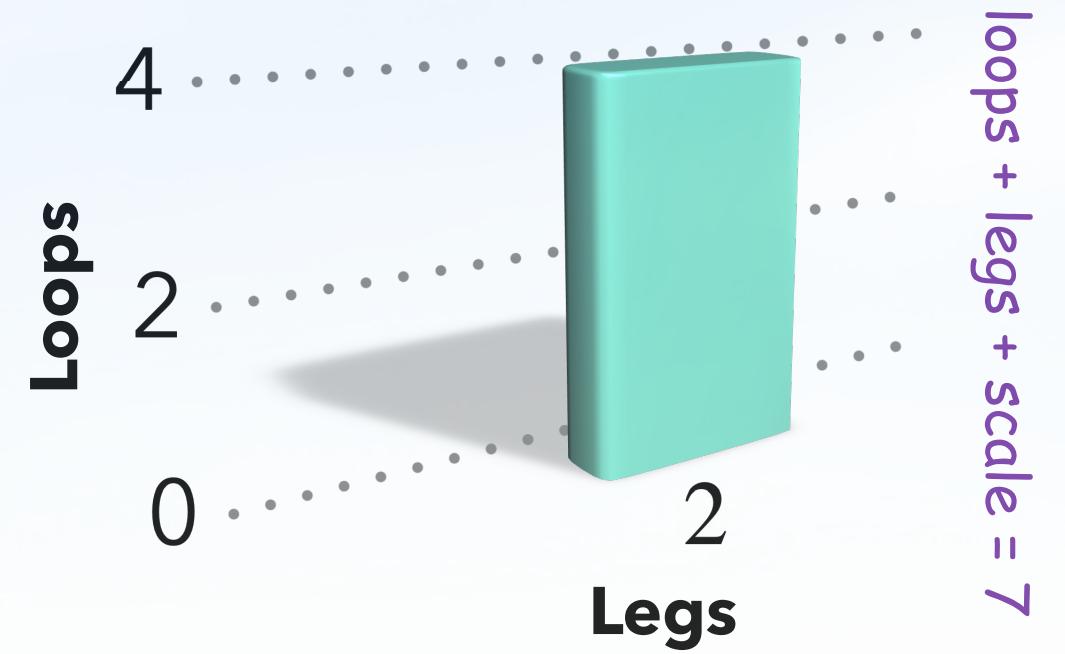
$$P_{a \leftarrow b} = \frac{\alpha_s}{\pi} P_{a \leftarrow b}^{(0)} + \frac{\alpha_s^2}{\pi^2} P_{a \leftarrow b}^{(1)} + \frac{\alpha_s^3}{\pi^3} P_{a \leftarrow b}^{(2)} + \dots$$

1970's 1980 2004

$$\gamma_{q \leftarrow q}^{(3)}(N) = - \int_0^1 dx x^{N-1} P_{q \leftarrow q}^{(3)}(x) \quad G. Falcioni, F. Herzog et. al. Phys.Lett.B 842 (2023)$$

$$\gamma_{q \leftarrow g}^{(3)}(N) = - \int_0^1 dx x^{N-1} P_{q \leftarrow g}^{(3)}(x) \quad G. Falcioni, F. Herzog, S. Moch, A. Vogt 2307.04158$$

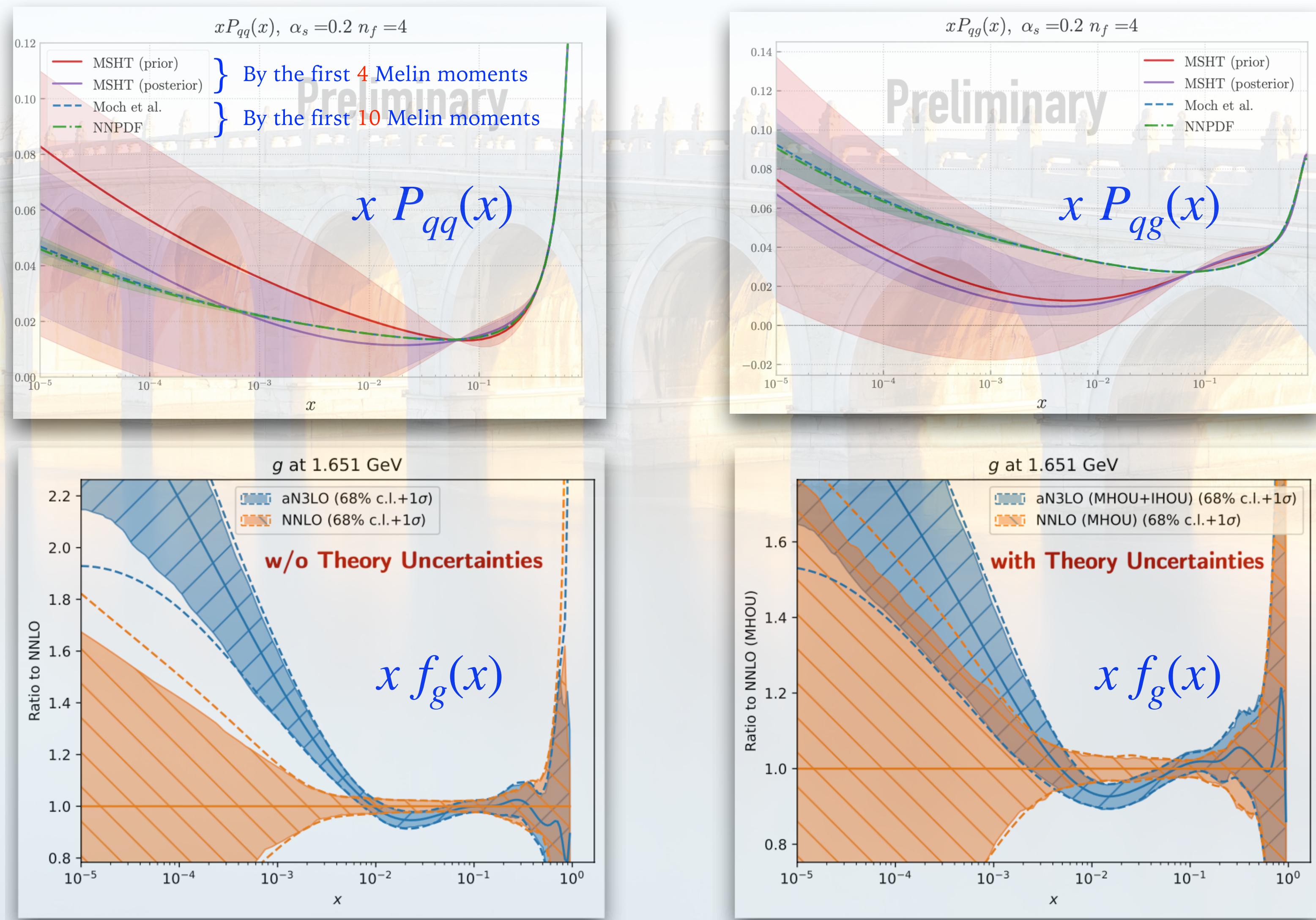
For $N = 2, 4, \dots, 20$



Parton Distributions @ approximated N3LO

State-of-the-art Parton Distribution Functions

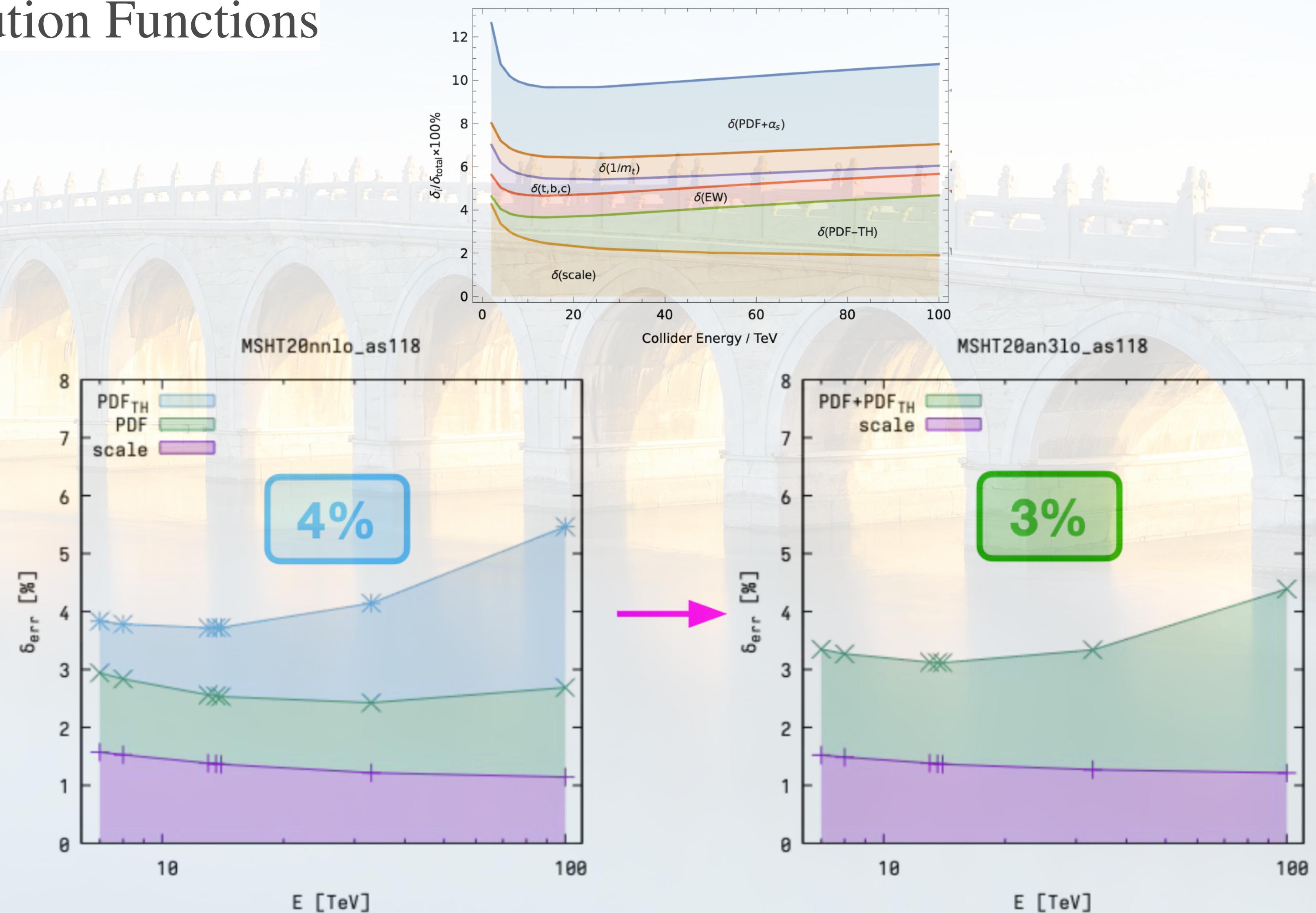
- Approximated N3LO PDF available:
MSHT20aN3LO *Eur.Phys.J.C 83 (2023) 4*
NNPDFaN3LO *NNPDF preliminary*
- More precise 4-loop splitting functions affect small x region.
- Large correction at aN3LO at small x region outside 68% c.l. region.
- Missing Higher Order Uncertainty (MHOU) not included in standard NNLO PDF.
- Crucial to consider MHOU and IHOU to understand consistency between NNLO and N3LO PDF.



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Parton Distributions @ approximated N3LO

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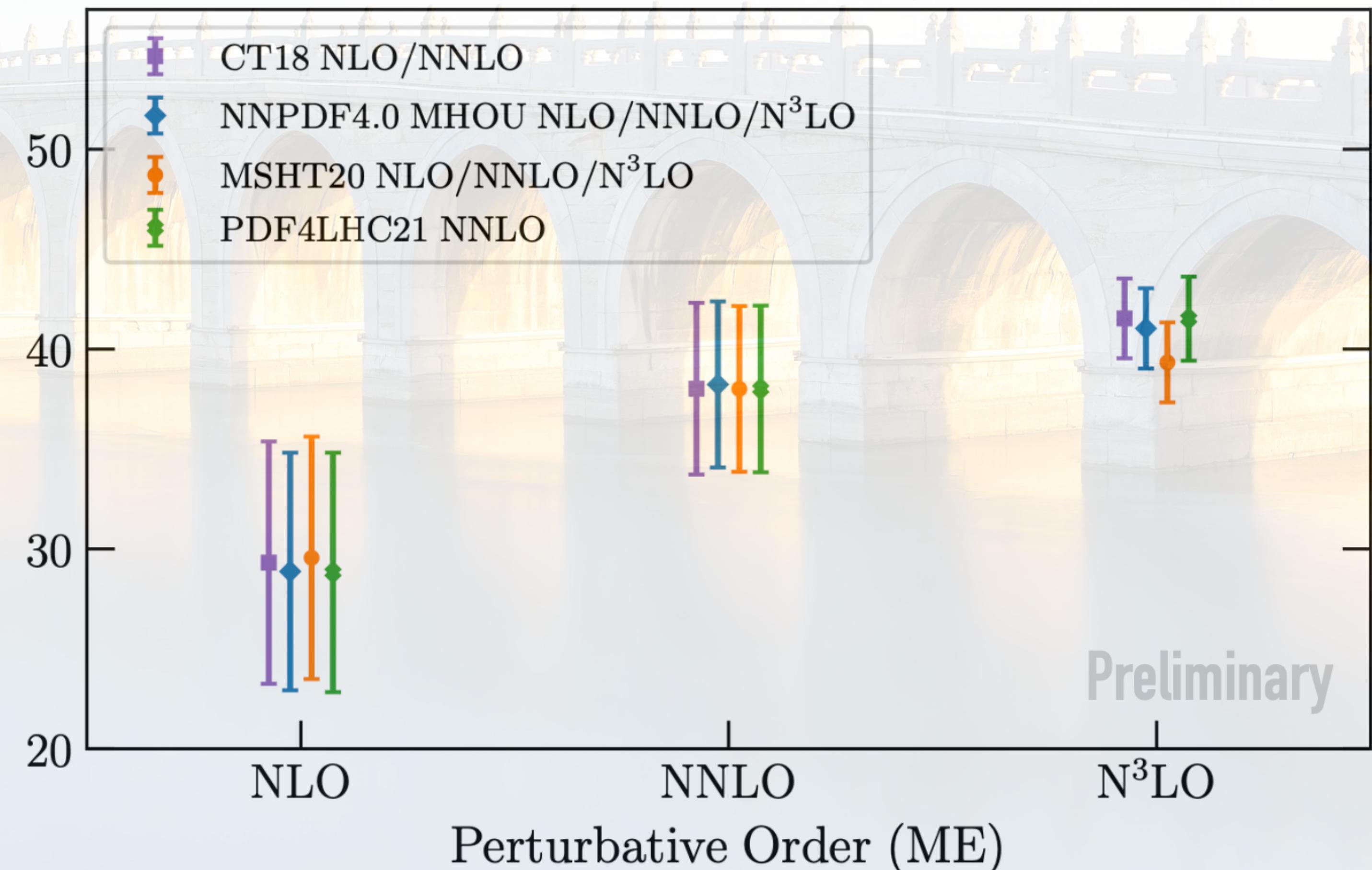
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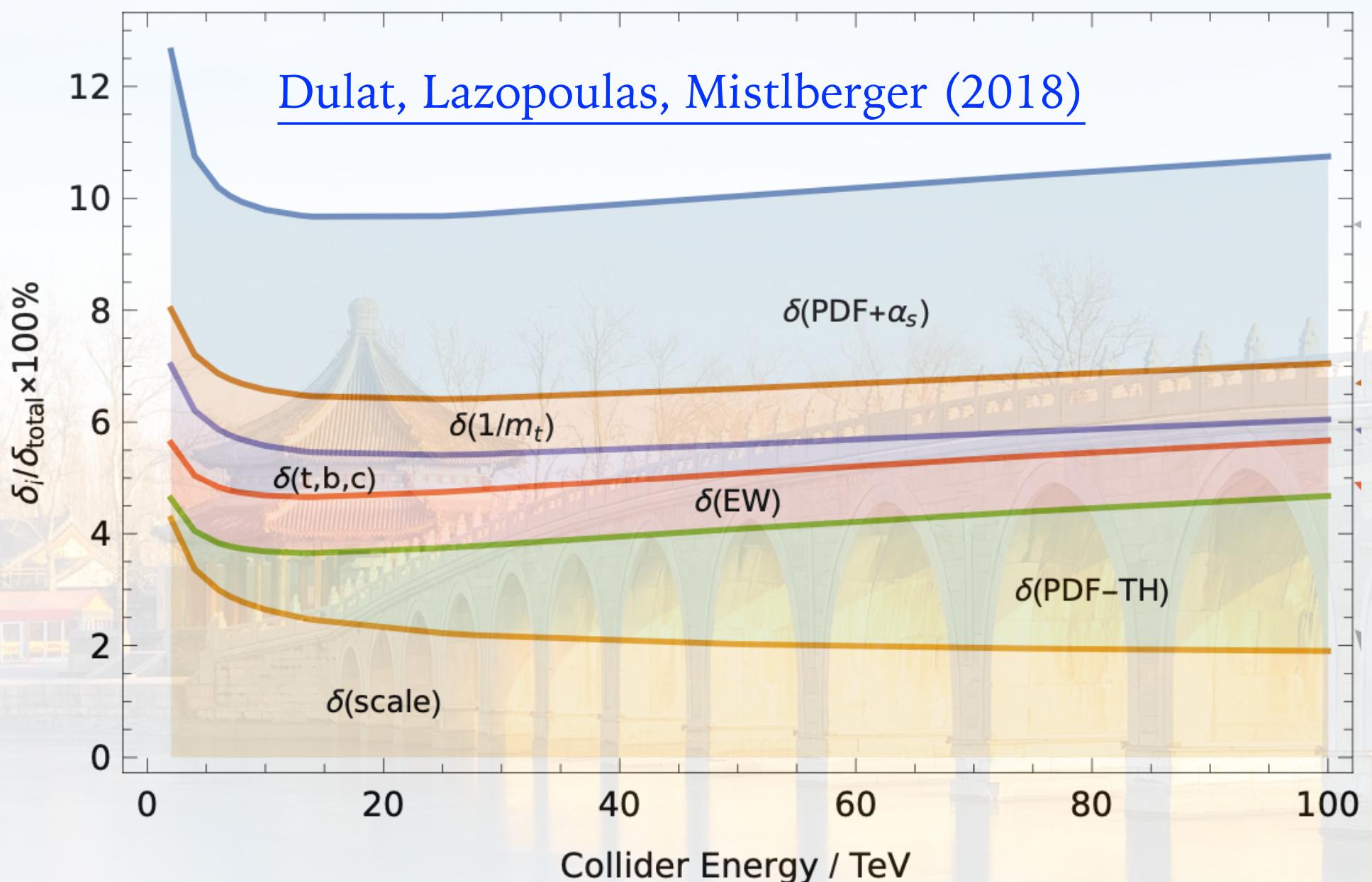
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Higgs production in gluon fusion (PDF + MHOUs)



Gluon Fusion Channel Uncertainties



- $\delta(\text{Scale})$: 4-loop QCD form factors
von Manteuffel, Schabinger (2019), Das, Moch, Vogt (2020), Lee, von Manteuffel, Schabinger et al (2022)
- $\delta(\text{Scale})$: Diff. N3LO(+N3LL) QCD
Cieri, XC et al (2018), XC, Gehrmann et al (2021), Billis, Dehnadi et al (2021),
- $\delta(\text{EW})$: NLO mixed QCD-EW $\sim 0.5\%$
Bonetti, Panzer et al (2020), Becchetti, Bonciani et al (2020), Becchetti, Moriello, Schweitzer (2021), Bonetti, Panzer, Tancredi (2022)

- $\delta(1/m_t)$: 3 and 4-loop QCD form factors

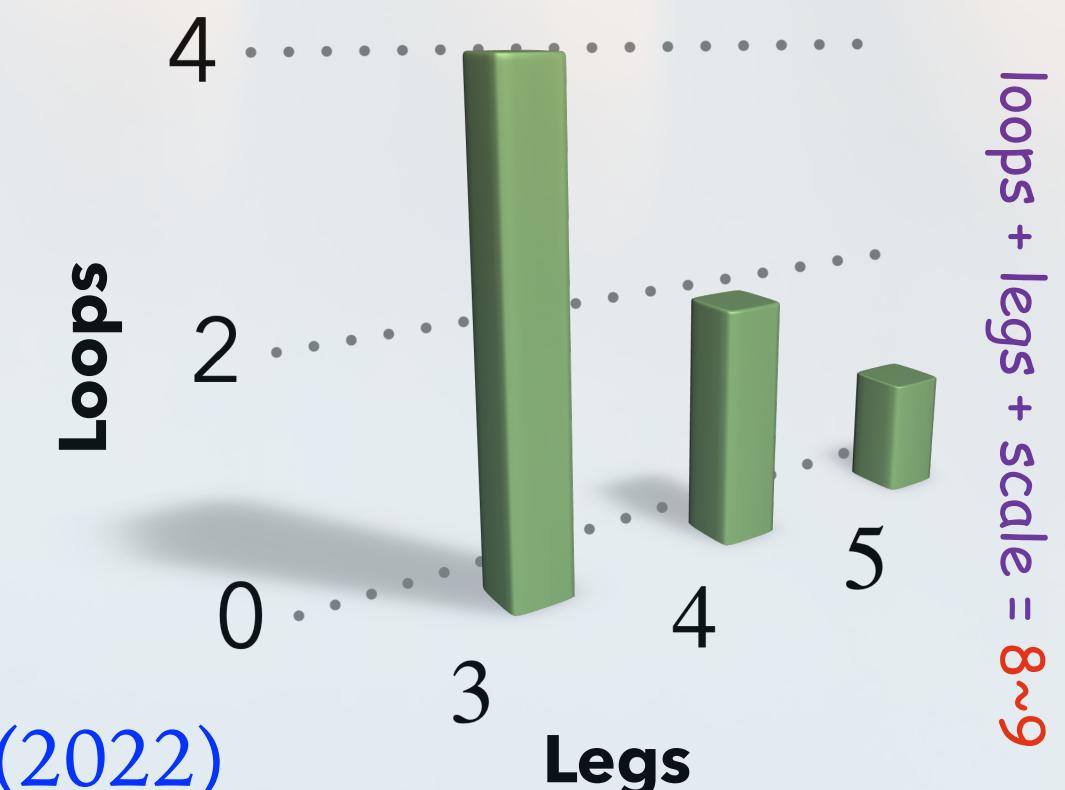
[Davies, Gröber et al \(2019\)](#), [Davies, Herren, Steinhauser \(2019\)](#)

- $\delta(1/m_t)$: H@NNLO QCD $\sim 0.3\%$

[Czakon, Niggetiedt \(2020\)](#), [Czakon, Harlander et al \(2021\)](#)

- $\delta(1/m_t)$: H+J(J)@NLO QCD

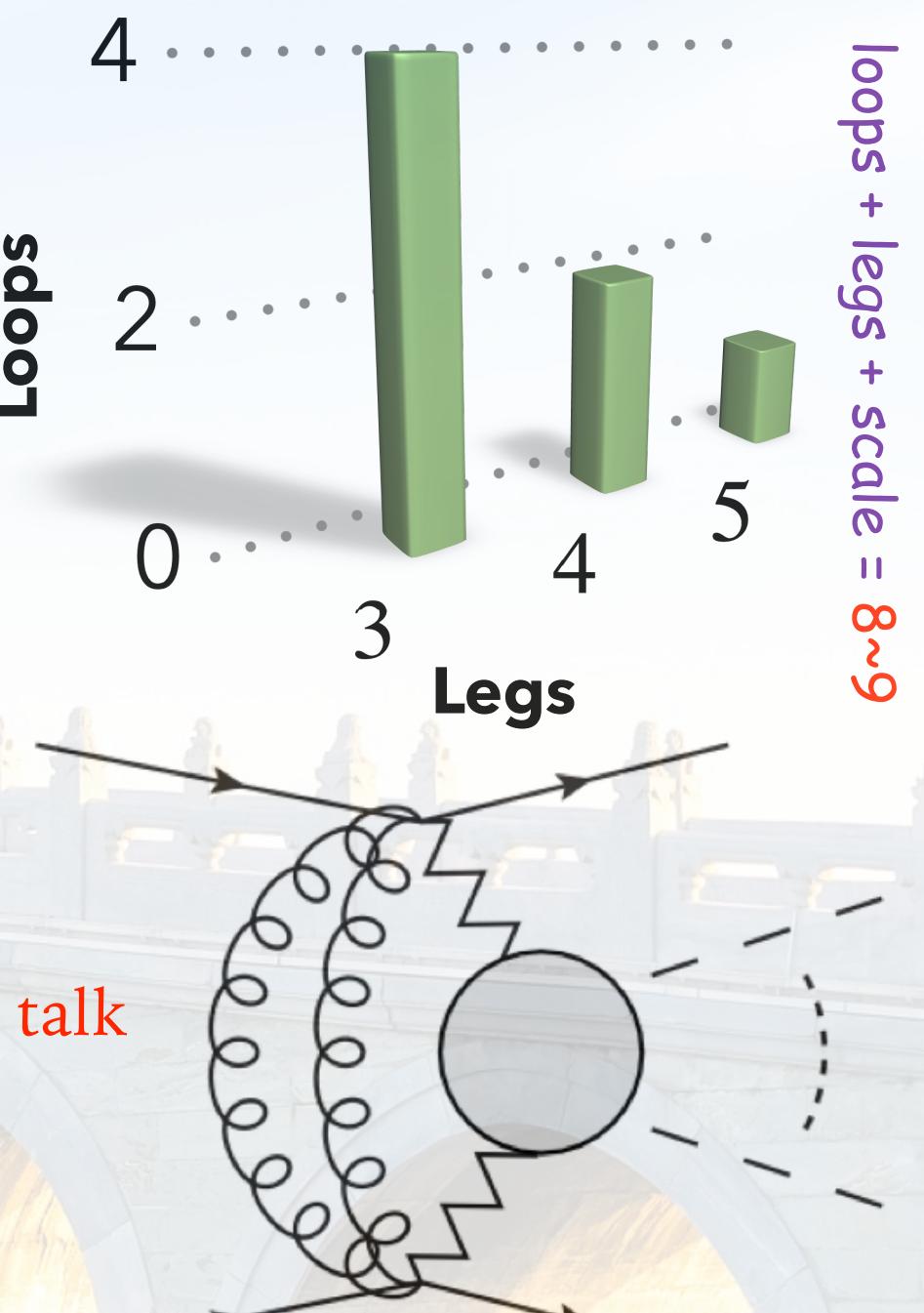
[XC, Huss, Jones et al \(2020\)](#), [Bonciani, Del Duca, Frellesvig et al \(2022\)](#)



- $\delta(t, b, c)$: NLO+NNLL QCD
[Caola, Lindert, Melnikov et al \(2018\)](#), [Anastasiou, Penin \(2020\)](#),
- $\delta(t, b, c)$: 3-loop form factor
[Harlander, Prausa Usovitsch \(2019\)](#)

Vector Boson Fusion to Higgs

- Double DIS approx. @ inclusive N3LO with $\sim \pm 0.2\%$ scale uncertainty [Dreyer, Karlberg \(2016\)](#)
- Fully differential predictions @ NNLO (DDIS approx.) with $\sim \pm 1\%$ scale uncertainty:
[Cacciari, Dreyer, Salam, Zanderighi \(2015\)](#), [Cruz-Martinez, Gehrmann et al \(2018\)](#), [Asteriadis, Caola et al \(2021\)](#)
- Non-factorizable corrections @ NNLO (eikonal approx.) $\sim 0.4\%$:
[Liu, Melnikov, Penin \(2019\)](#), [Dreyer, Karlberg, Tancredi \(2020\)](#), [Long, Melnikov, Quarroz \(2023\)](#) More details in M.M. Long's talk
Partial N3LO ($\beta_0 \alpha_s^3$) corrections $\sim 0.2\%$: [Brønnum-Hansen, Long, Melnikov \(2023\)](#)
- EW and QCD showers @ NLOPS (Powheg): [Jäger, Scheller \(2022\)](#)

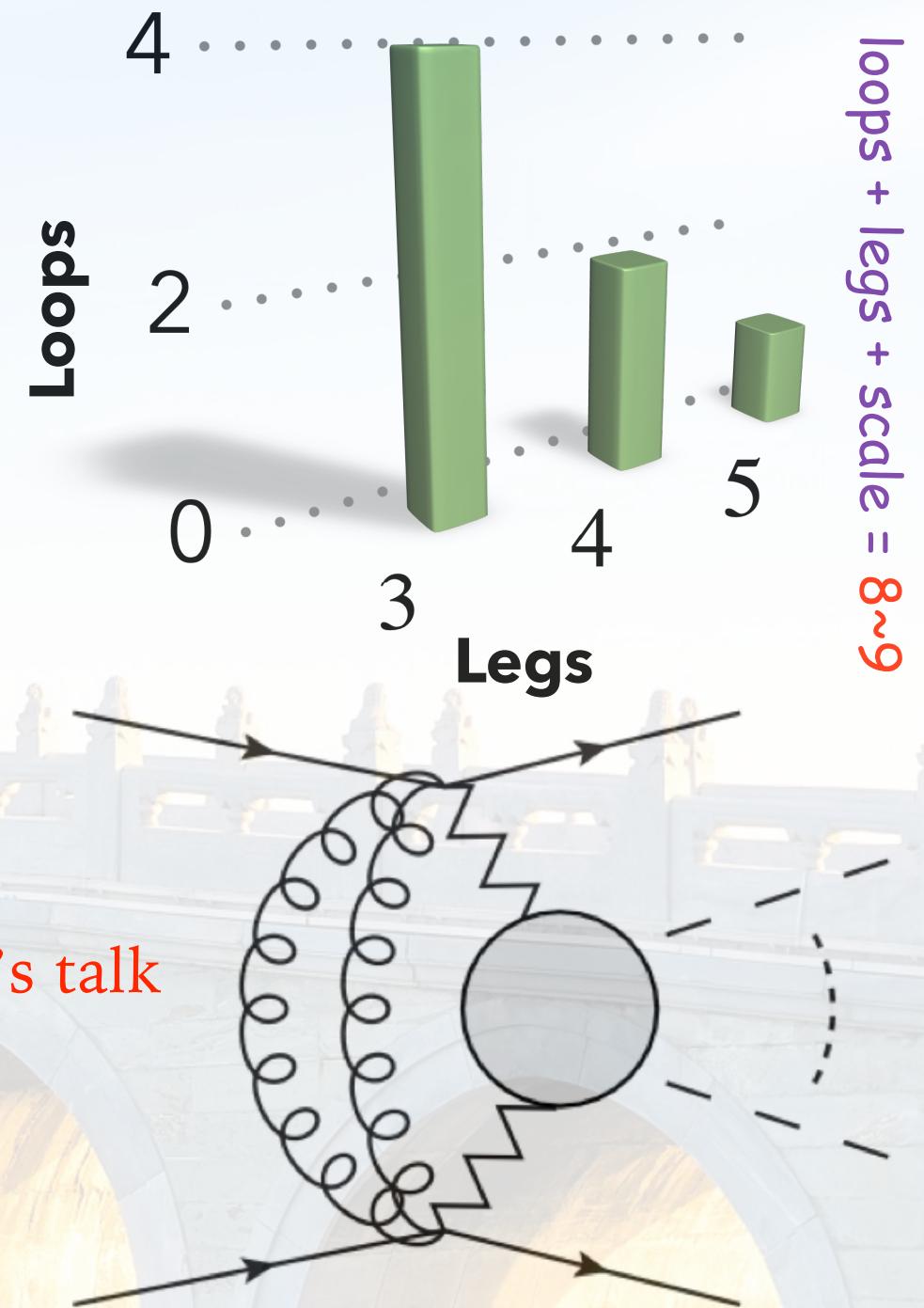


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Source of systematic uncertainty	Impact on signal strength [%]
VBF parton shower	13.0
Jet energy scale	7.7
Trigger efficiency	6.7
Parton shower (final-state radiation)	5.6
b jet regression smearing	3.3
b tagging efficiency	3.0
Pileup modeling	2.3
b jet regression scale	2.0
Jet energy resolution	1.5

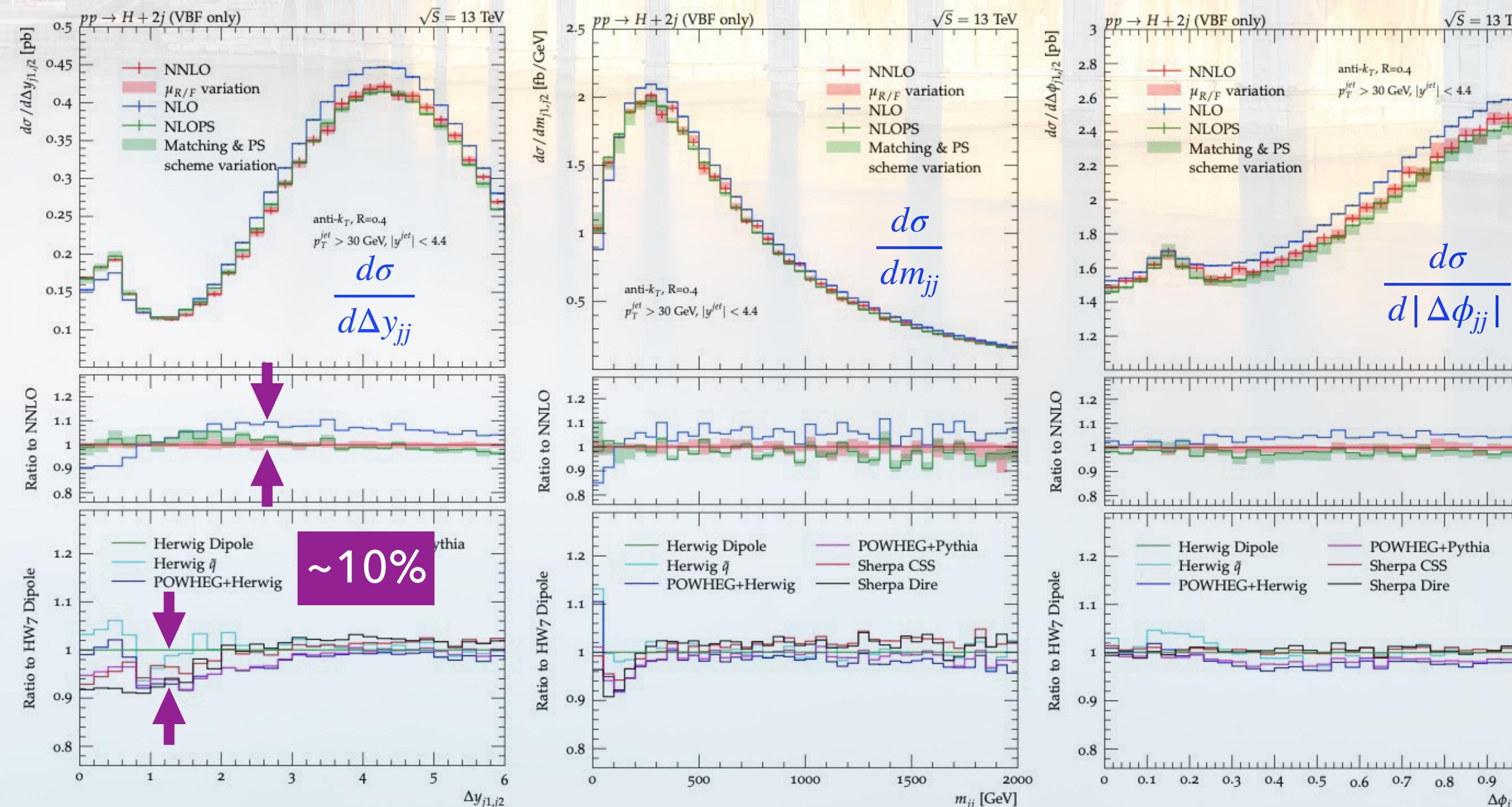
- What is the shortest panel of the bucket?
- CMS and ATLAS measurement in 2023 indicates parton shower uncertainties.



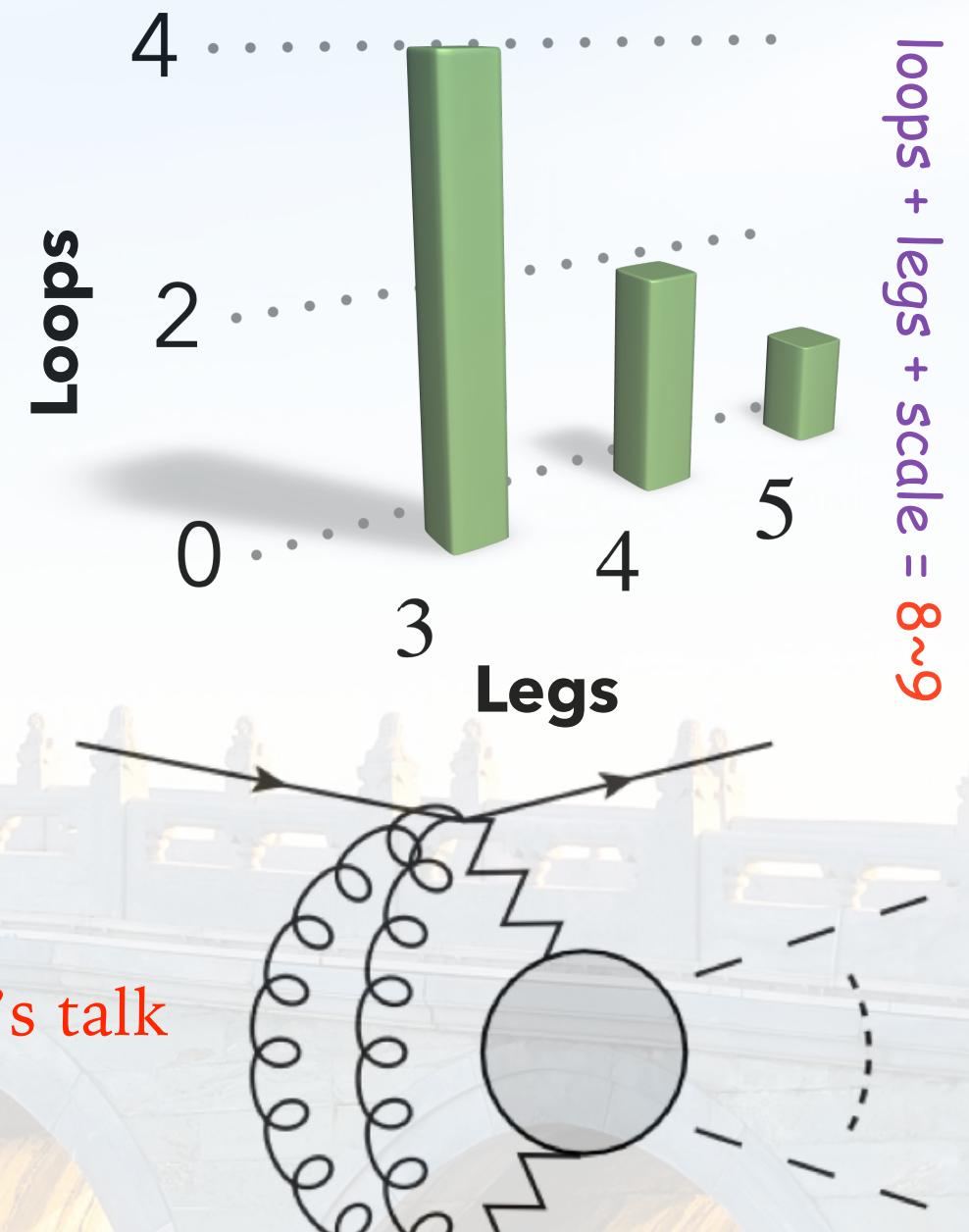
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Partial N3LO ($\beta_0 \alpha_s^3$) corrections $\sim 0.2\%$: [Brønnum-Hansen, Long, Melnikov \(2023\)](#)



- What is the shortest panel of the bucket?
- CMS and ATLAS measurement in 2023 indicates parton shower uncertainties.
- Comparative study of VBF with different parton showers (NLO+LL accuracy):
[Jäger, Karlberg, Plätzer, Scheller, Zaro \(2022\)](#)
[Buckley, XC, Cruz-Martinez et al \(2021\)](#)
- Can we Improve the PS accuracy?
More details in Simone Alioli's talk



Vector Boson Fusion to Higgs

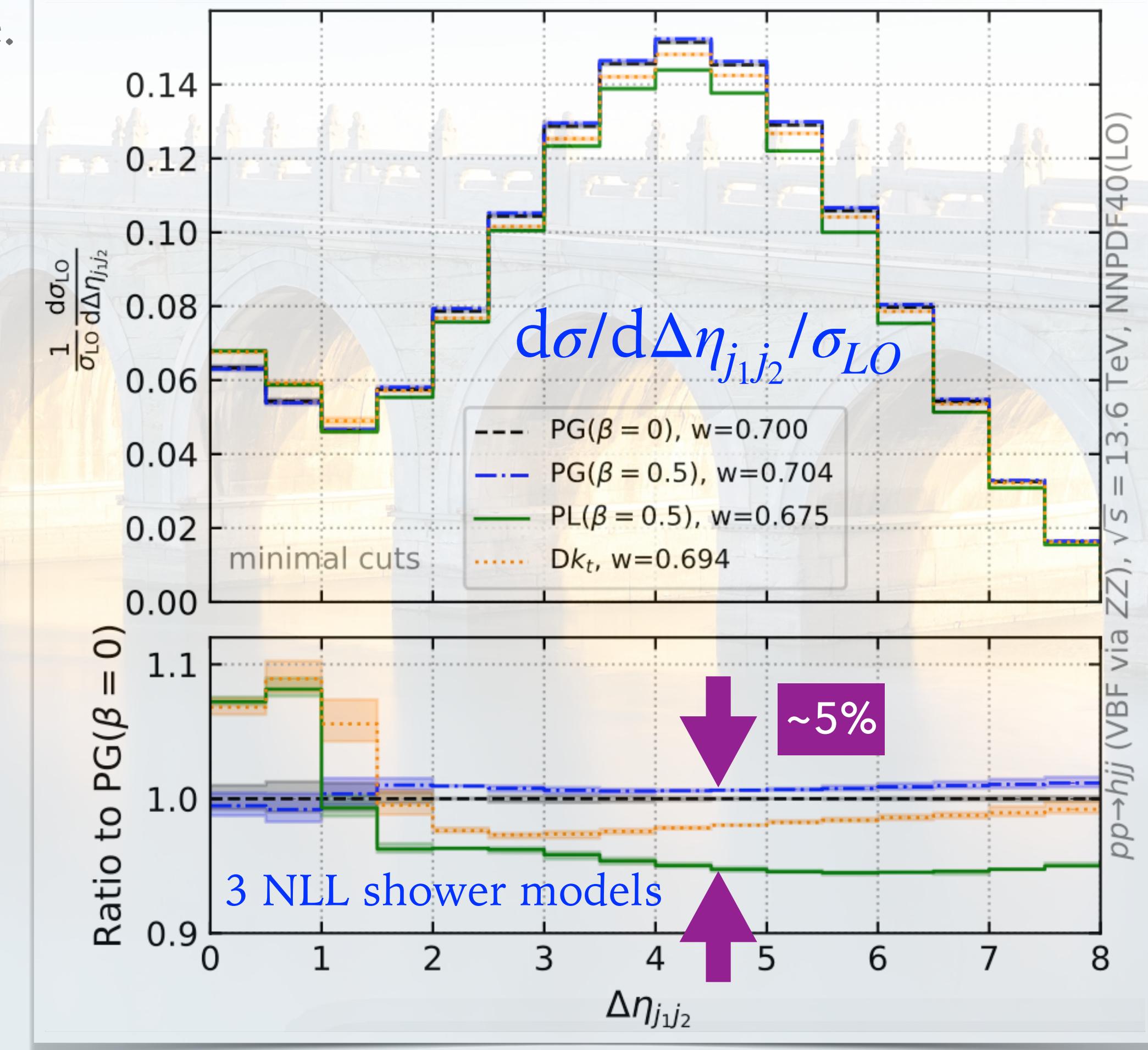
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State-of-the-art Parton Shower accuracy

- Standard parton showers are Leading Logarithmic (LL) accurate. (**SHERPA**, **PYTHIA**, **DIRE**, **GENEVA**, **HERWIG**, **VINCIA** etc.)
- NNLO + LL PS established for $2 \rightarrow 2$ colour singlet and $t\bar{t}$.
- $pp \rightarrow W^\pm Z \rightarrow l^+ l^- l'^+ \nu_l' + [\text{QCD}, \text{QED}]$ shower
[J. M. Lindert, D. Lombardi, M. Wiesemann et al \(2022\)](#)
- Several groups working on new PS framework aiming for NLL:
 - **CVOLVER**: Forshaw, Holguin, Plätzer **DEDUCTOR**: Nagy, Soper
 - ALARIC**: Assi, Herren, Höche, Krauss, Reichelt, Schönherr
 - PANSCALES**: van Beekveld, Ferrario Ravasio, Hamilton, Salam, Soto-Ontoso, Soyez, Verheyen, Halliwell, Medves, Dreyer, Scyboz, Karlberg, Monni, El-Menoufi
- Test of shower accuracy (**PANSCALES**):

$$\lim_{\alpha_s \rightarrow 0} \frac{\Sigma_{\text{PS}}(\lambda) - \Sigma_{\text{NLL}}(\lambda)}{\Sigma_{\text{NLL}}(\lambda)}, \quad \lambda = \alpha_s L$$
- **PANSCALES**: VBFH (initial and final NLL shower)
 - First NLL shower uncertainty estimation at $\sim 10\%$
- **ALARIC**: massive shower (final NLL shower)
[Alaric Collaboration \(2022\), B. Assi, S. Höche \(2023\)](#)

$pp \rightarrow H (\text{VBF}) + PS$

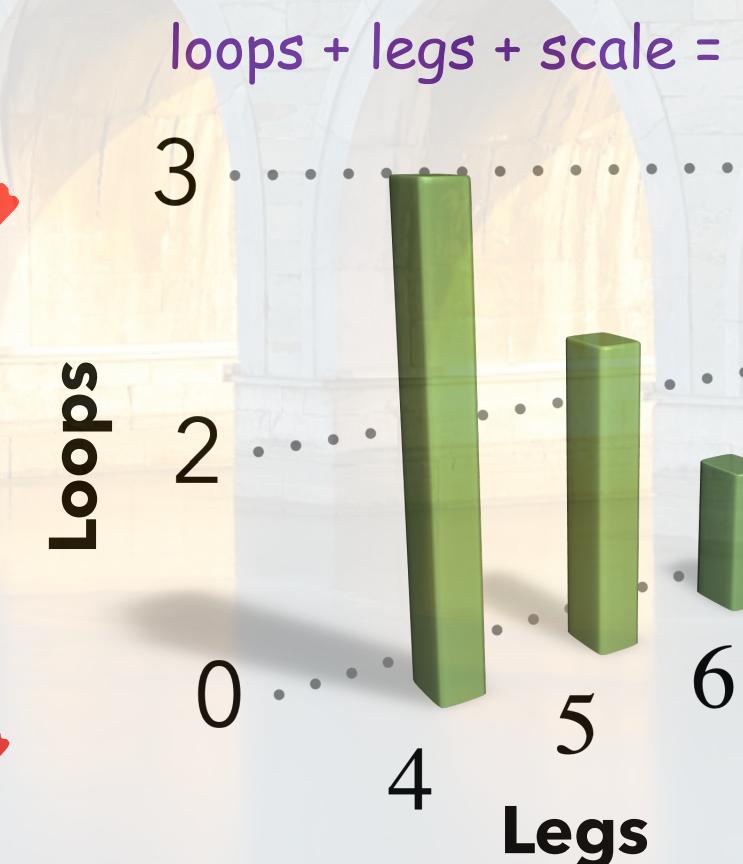
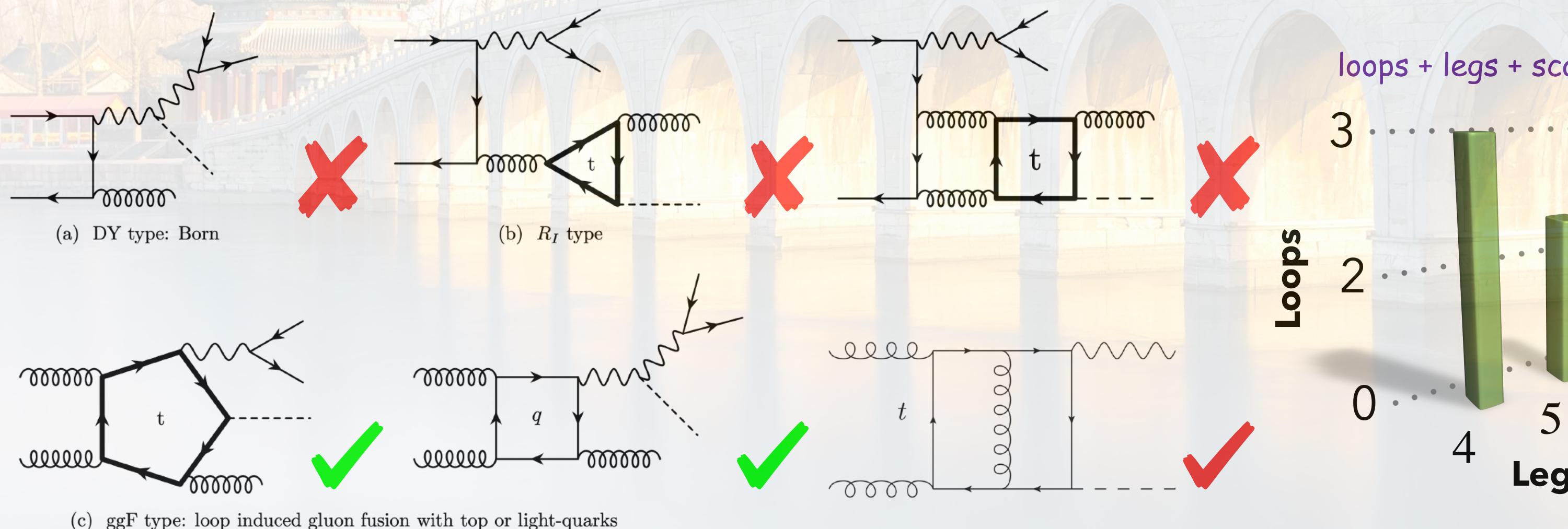


Beekveld, Ferrario Ravasio (2023)

VH Production

- $q\bar{q} \rightarrow VH$ @ NNLO contribute $\sim 4\%$ to Higgs XS with $\pm 5\%$ error
- $gg \rightarrow VH$ @ NLO contribute $\sim 0.5\%$ to Higgs XS:

[Wang, Xu et al \(2021\)](#), [Chen, Davies et al \(2022\)](#), [Degrassi, Gröber, et al \(2022\)](#)



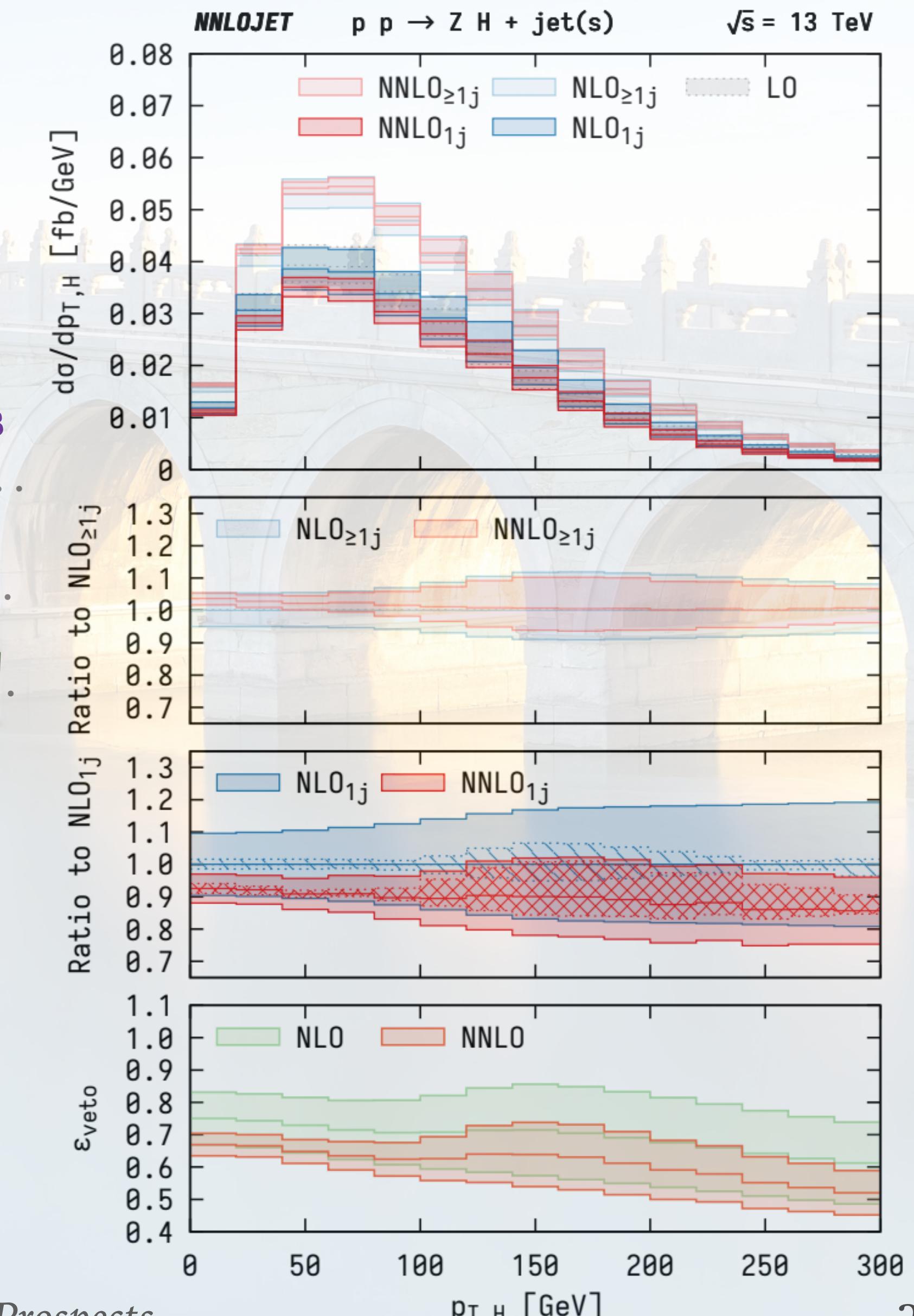
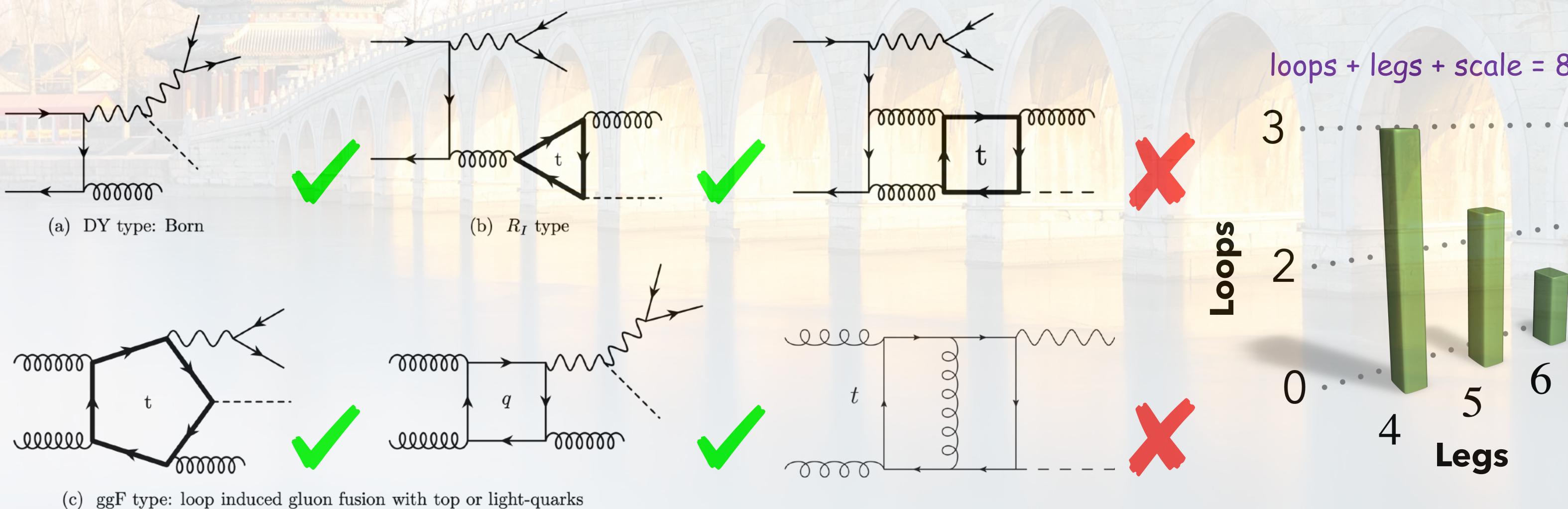
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► VH + jet @ NNLO $\pm 5\%$ scale error: [Gauld, Gehrmann-De Ridder et al \(2021\)](#)

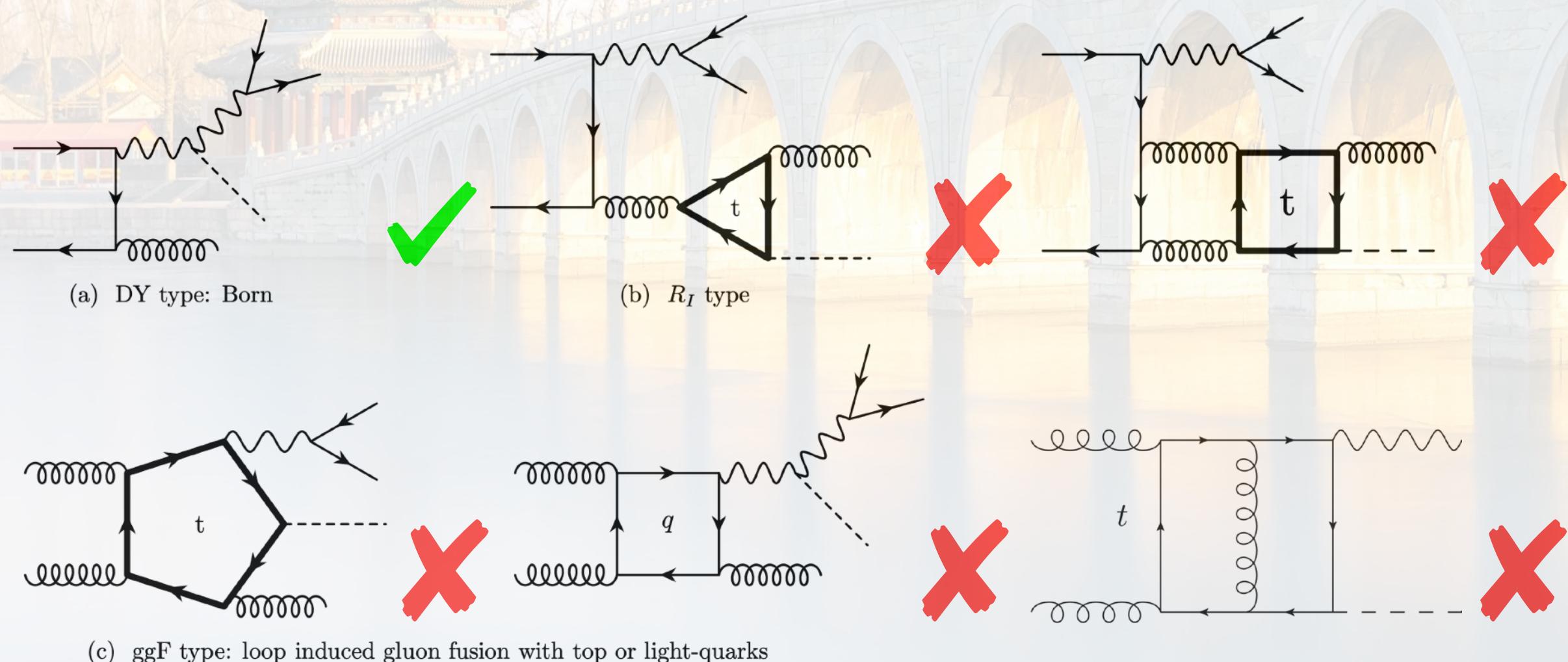


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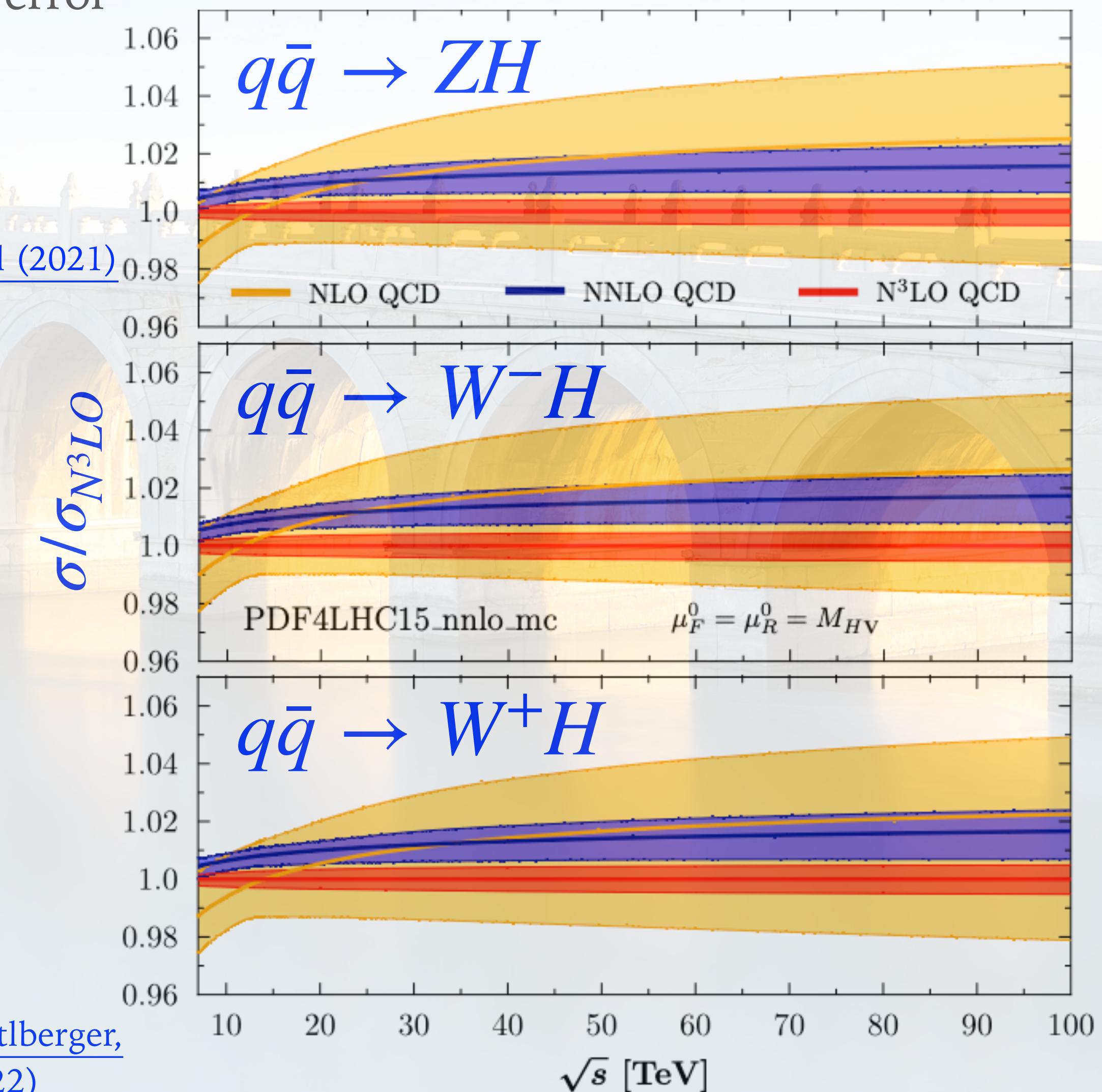
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- VH @ N3LO (DY type contribution) $\pm 0.5\%$ error
- ME from $2 \rightarrow 3$ @ NNLO + ME @ 3-loop.
- Use reverse unitarity for IR pole cancellation.
- Different perturbative-series convergent behaviour

[Baglio, Duhr, Mistlberger,
Szafron \(2022\)](#)

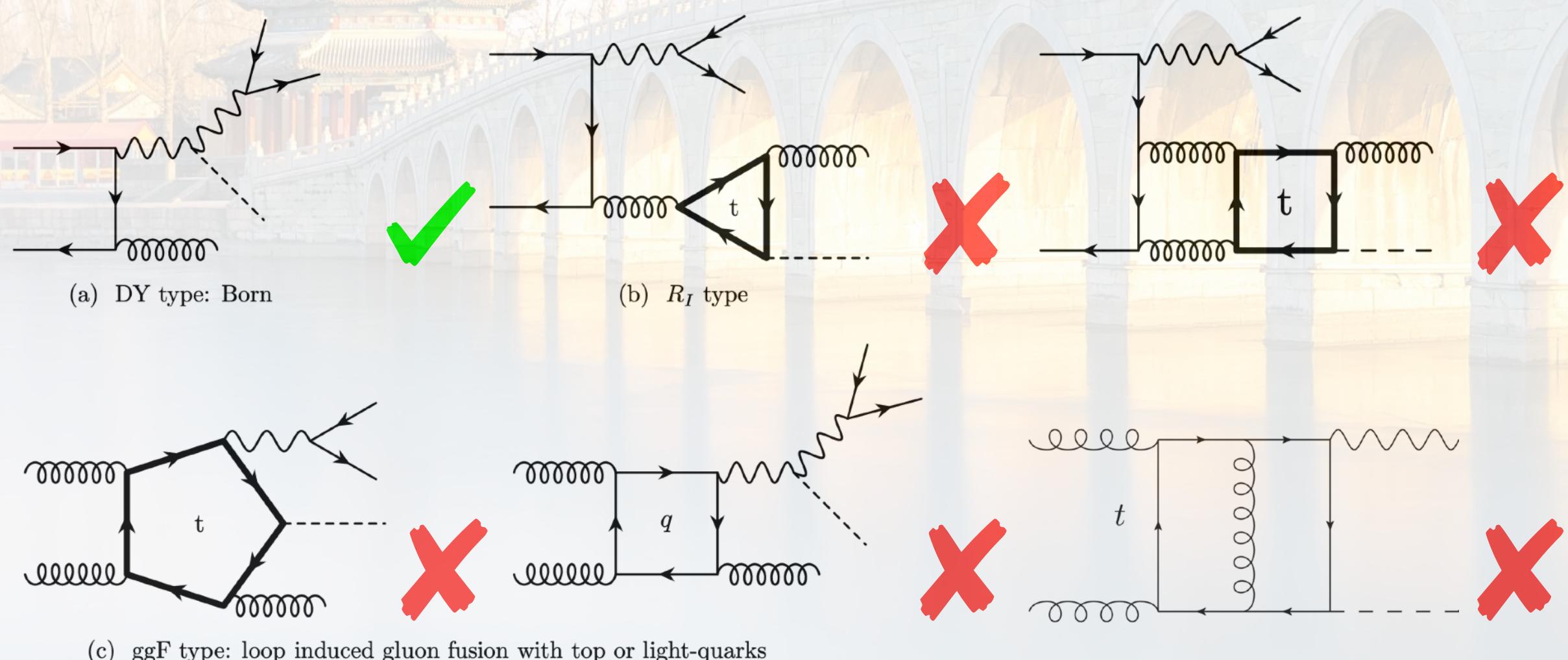


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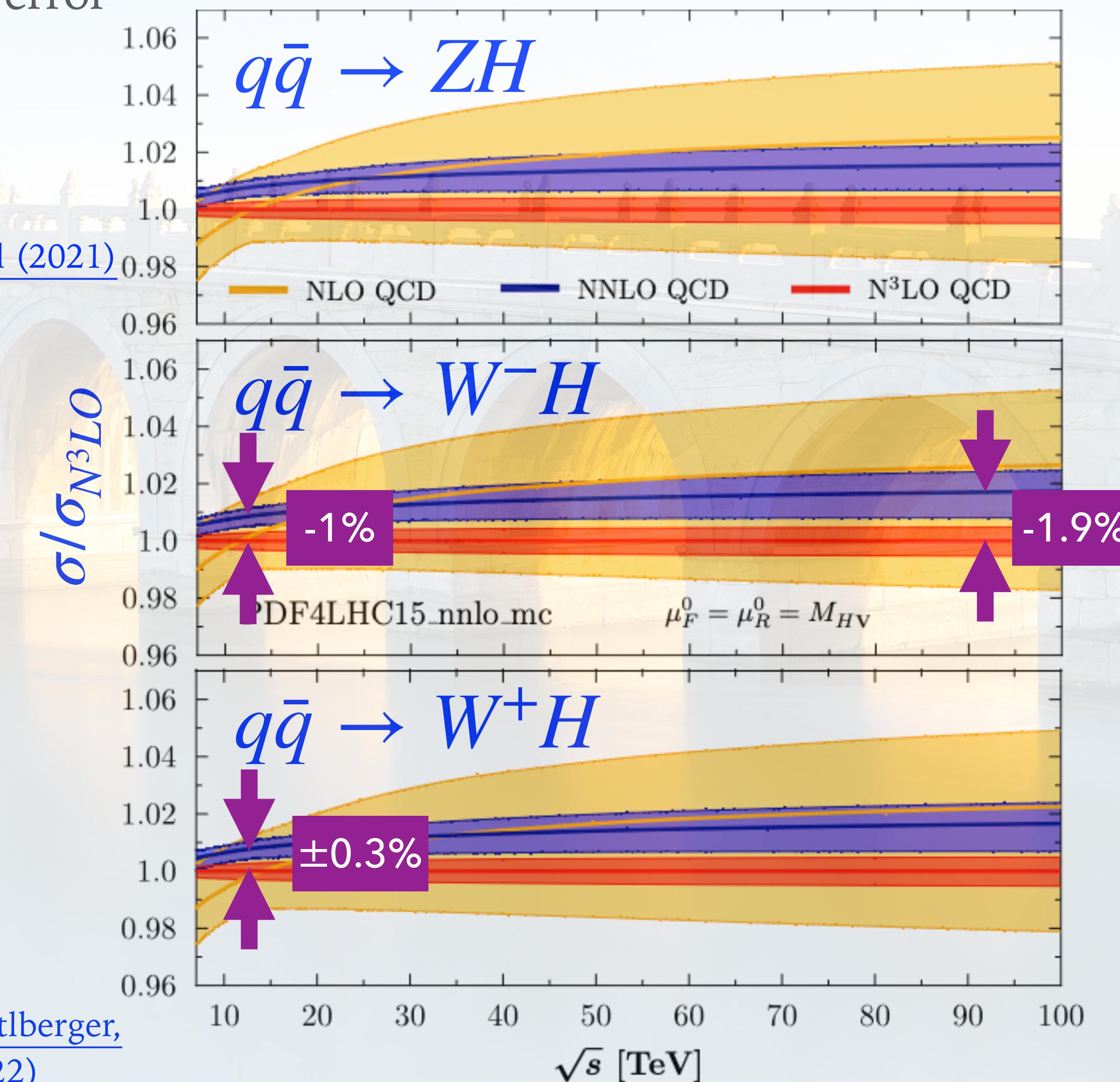
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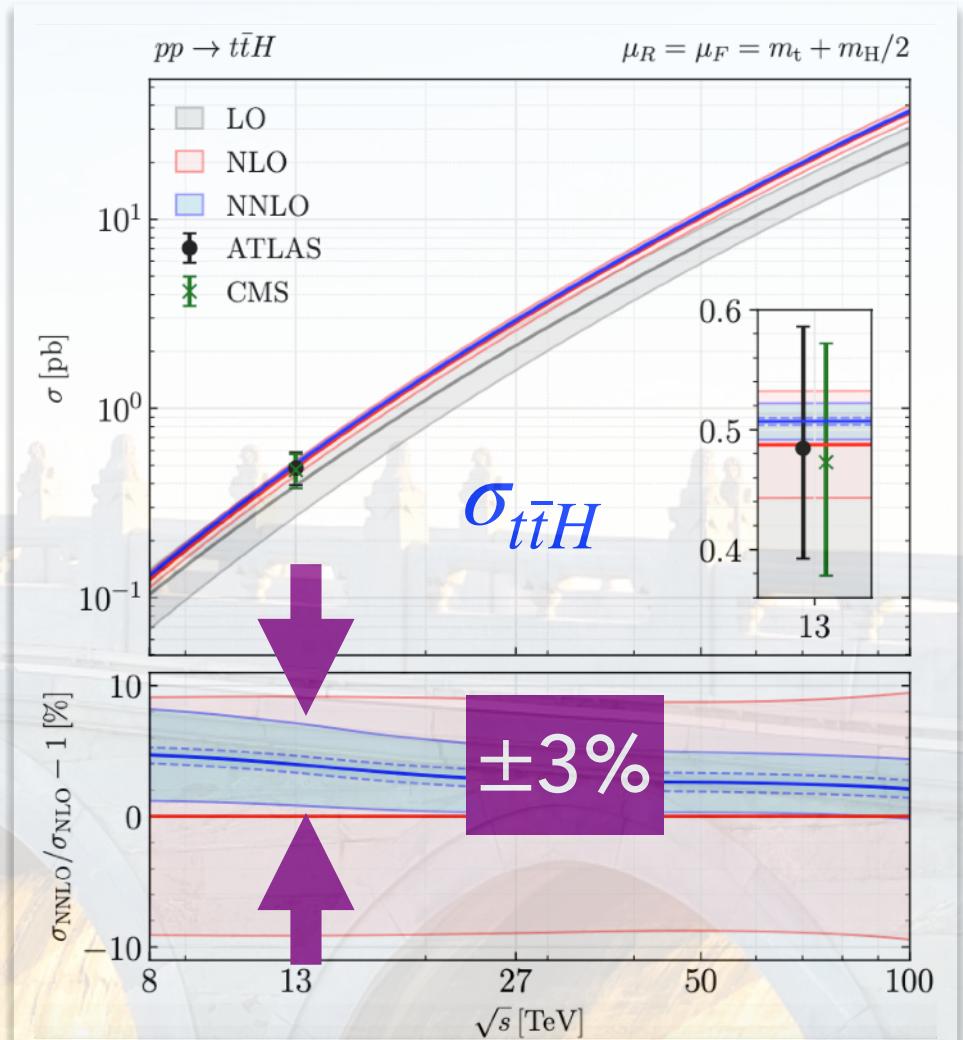
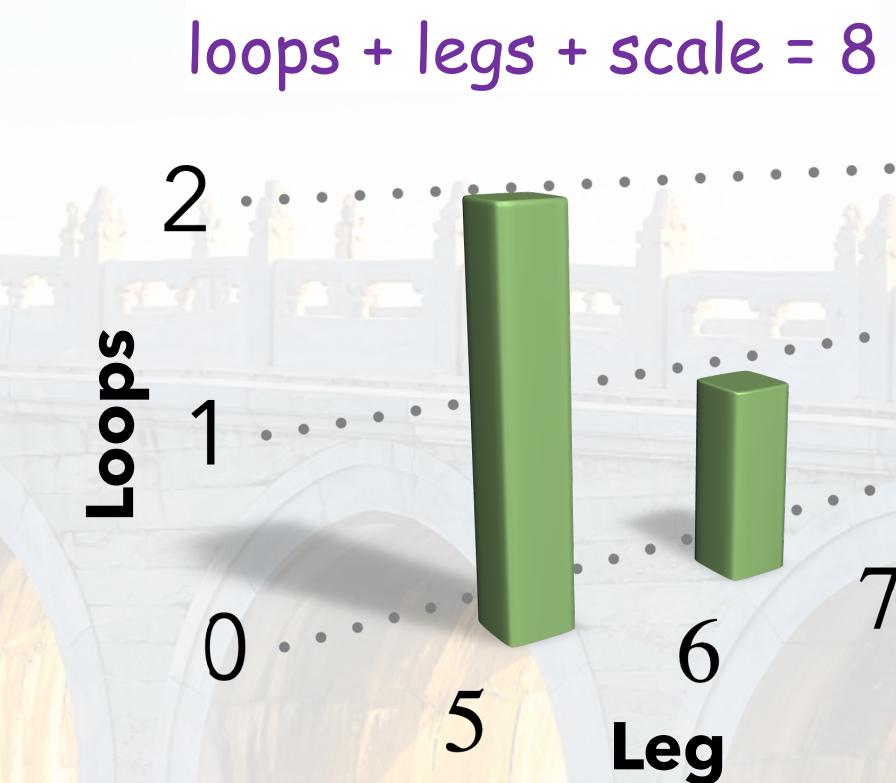


tH Production

$pp \rightarrow t\bar{t}H$ @NNLO + NNLL QCD + NLO EW

More details in Simone Devoto's talk

- Rapid progress of NNLO QCD corrections to $2 \rightarrow 3$ scattering at the LHC
 - Automation of tree and 1-loop scattering ME with [OpenLoops](#).
 - IR pole structure at 2-loop: [Chen, Ma, Wang, Yang, Ye \(2022\)](#)
 - Processes dependent approximation for 2-loop-5-leg ME with 1 mass scale:
 - Soft approximation to estimate $Ht\bar{t}gg$, $Ht\bar{t}q\bar{q}$ @ 2-loop
 - Mature machinery of NNLO qT-slicing in MATRIX [Catani, Devoto et al \(2023\)](#)



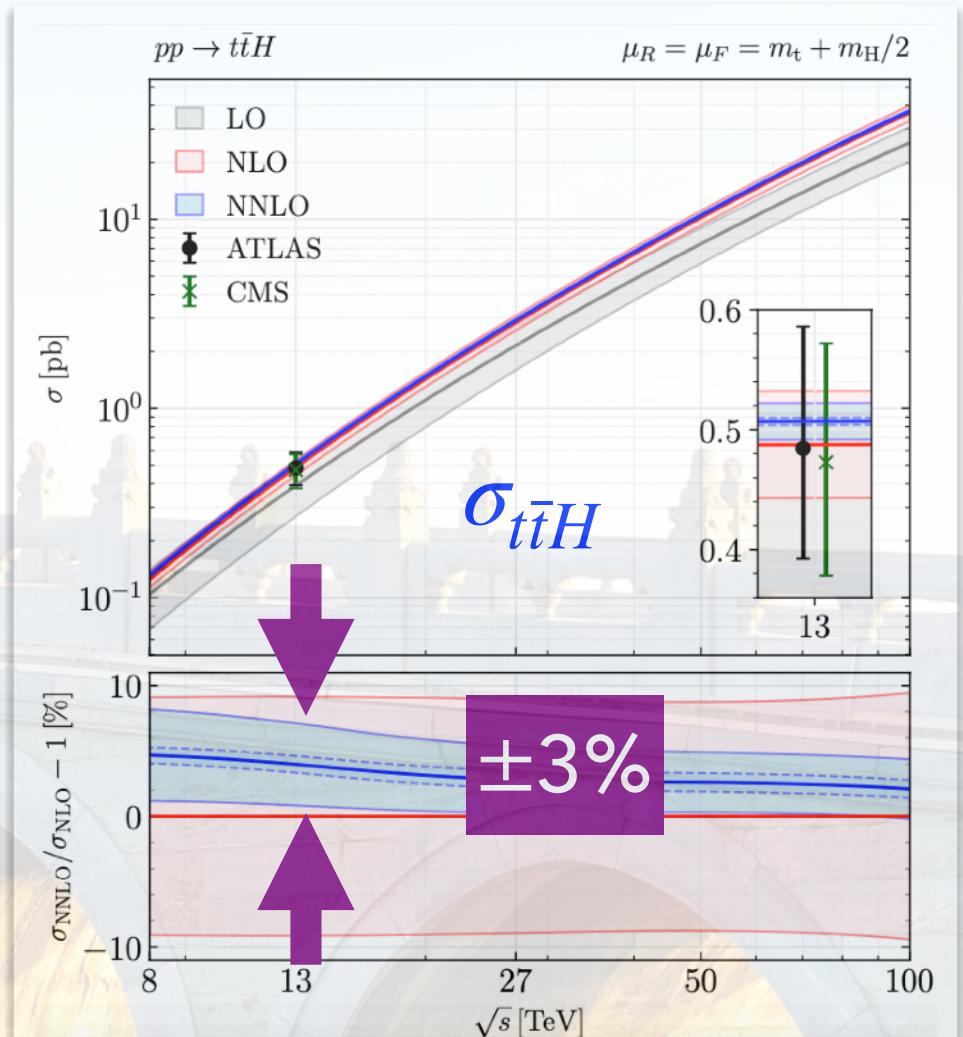
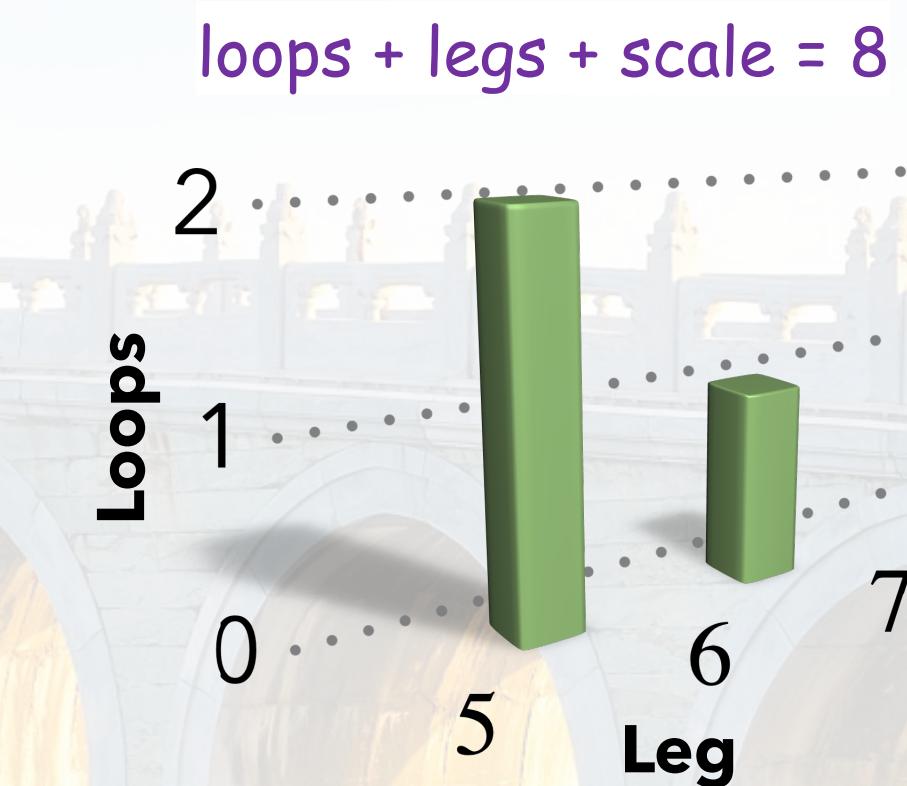
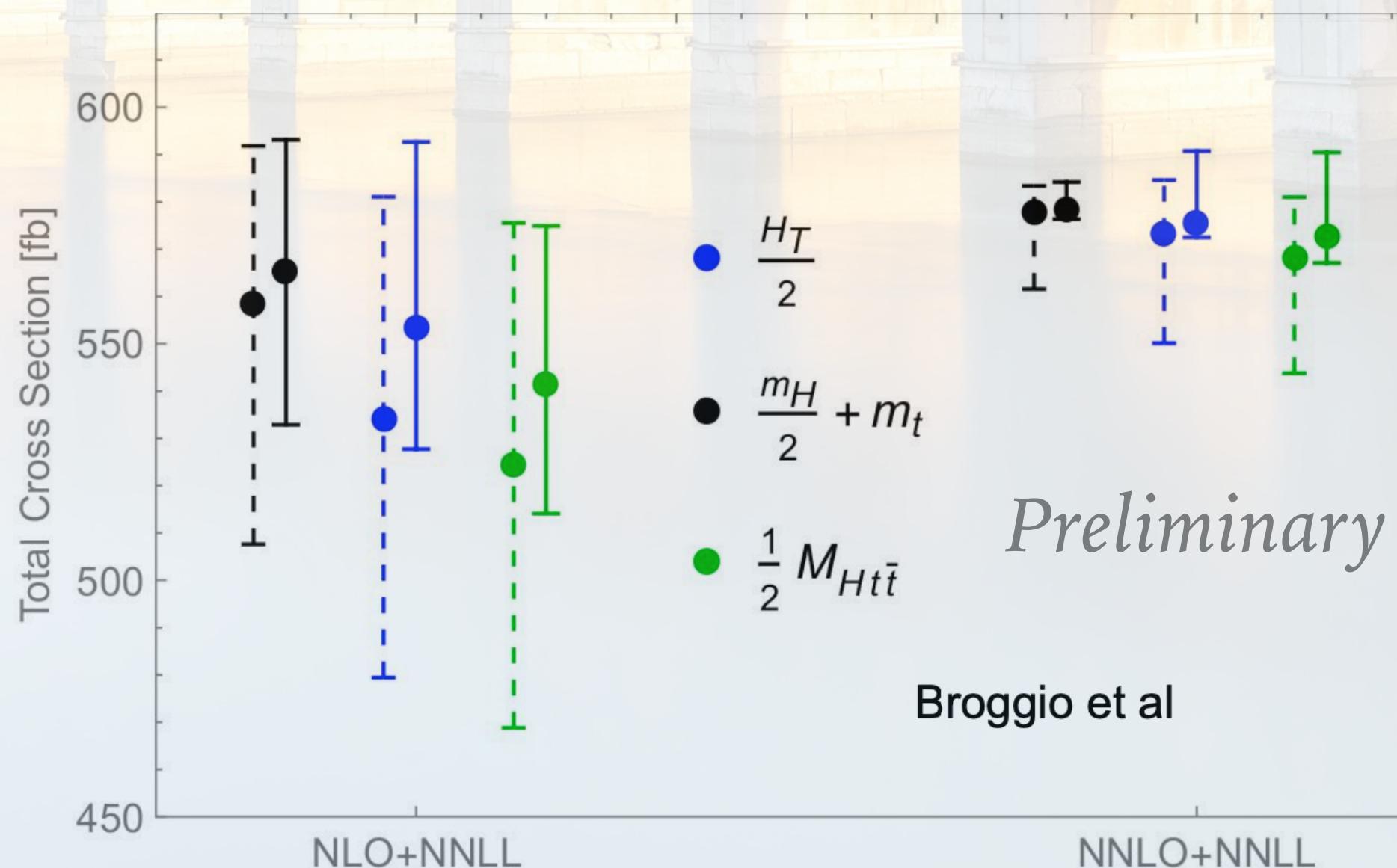
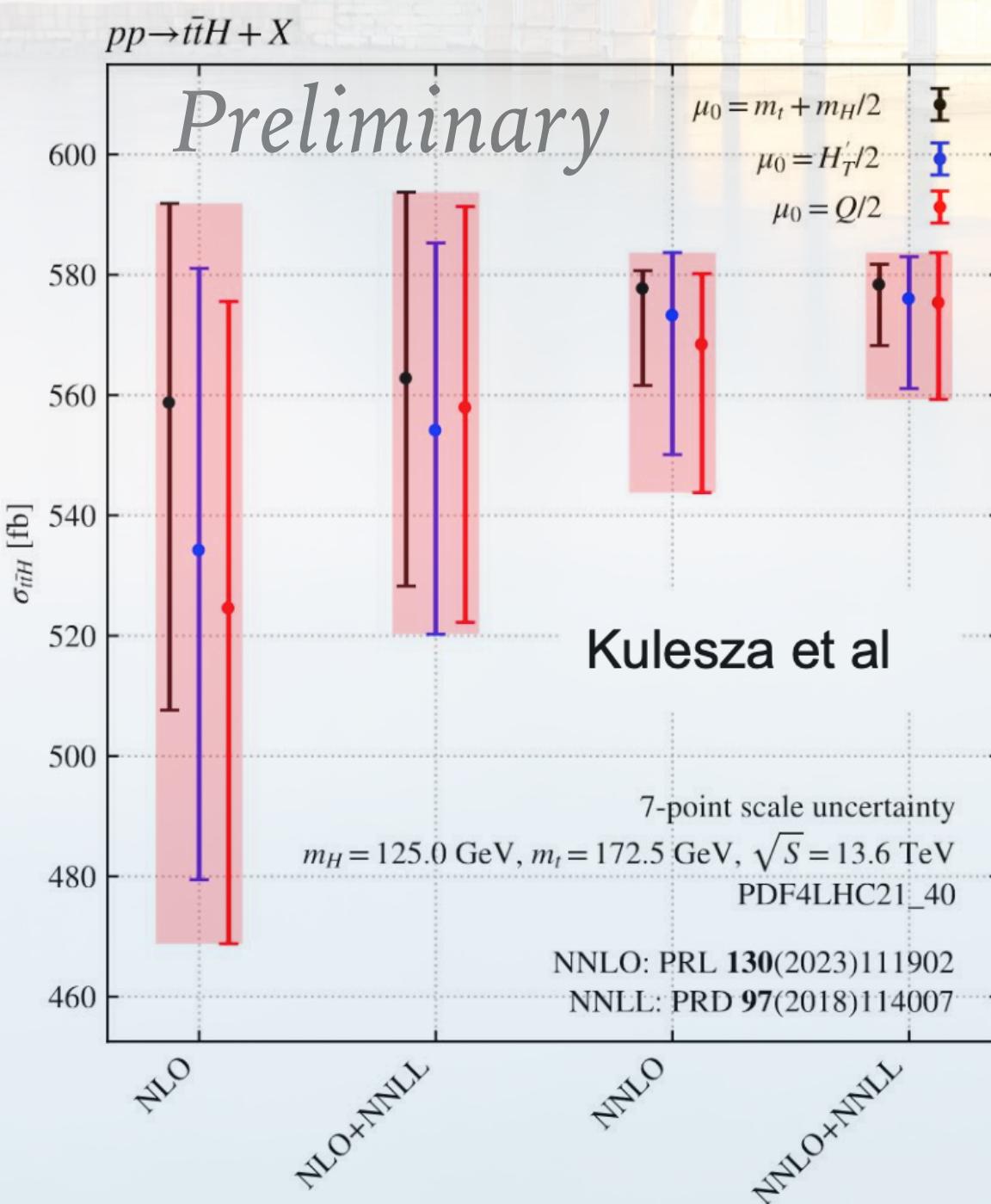
Catani, Devoto et al (2023)

tH Production

$pp \rightarrow t\bar{t}H @\text{NNLO + NNLL QCD + NLO EW}$

More details in Simone Devoto's talk

- Rapid progress of NNLO QCD corrections to $2 \rightarrow 3$ scattering at the LHC
 - Automation of tree and 1-loop scattering ME with [OpenLoops](#).
 - IR pole structure at 2-loop: [Chen, Ma, Wang, Yang, Ye \(2022\)](#)
 - Processes dependent approximation for 2-loop-5-leg ME with 1 mass scale:
 - Soft approximation to estimate $Ht\bar{t}gg, Ht\bar{t}q\bar{q}$ @ 2-loop
 - Mature machinery of NNLO qT-slicing in MATRIX [Catani, Devoto et al \(2023\)](#)



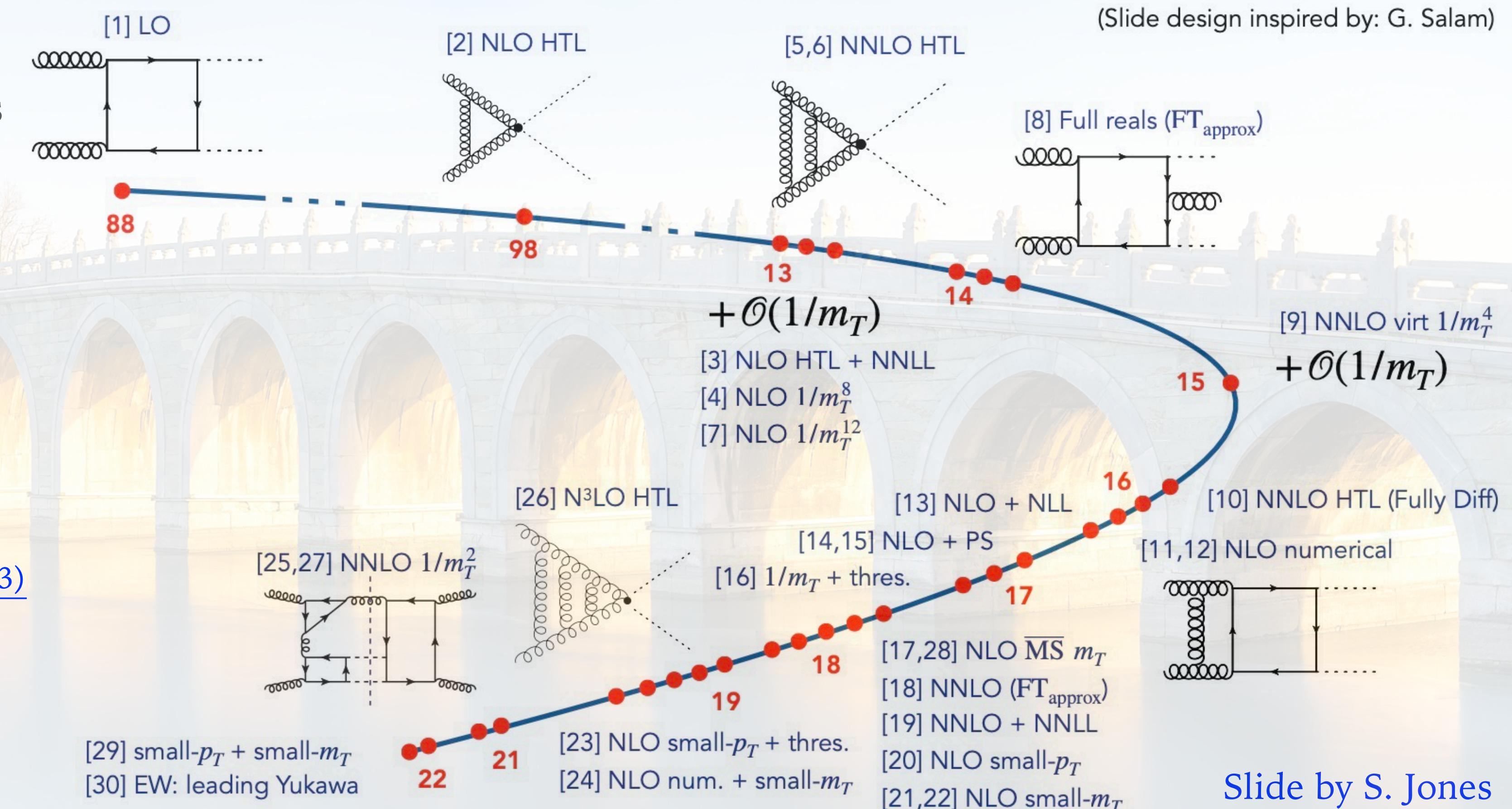
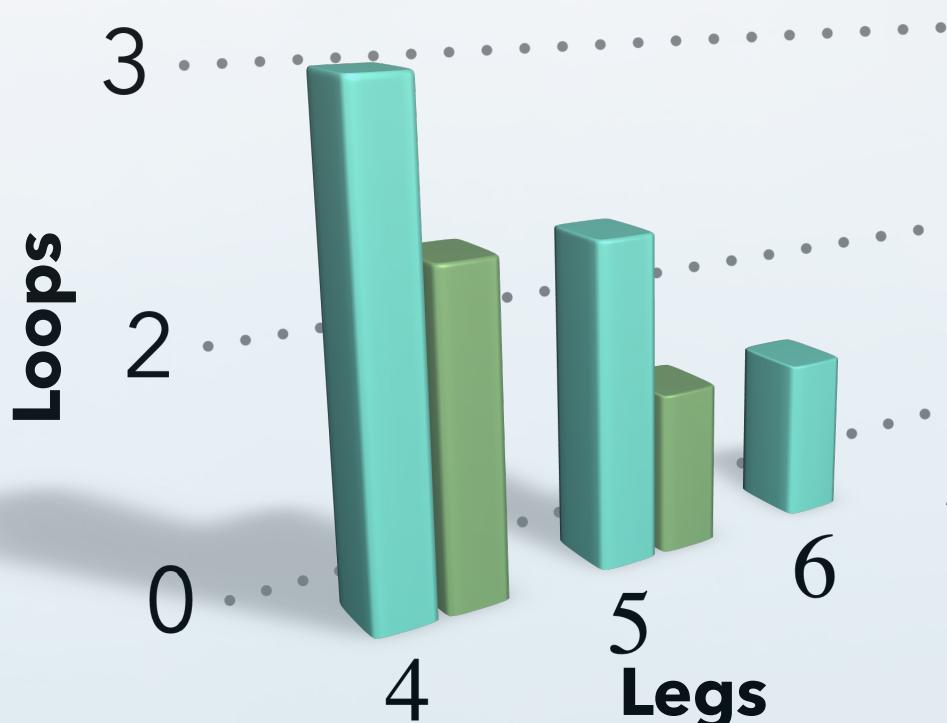
- Combined with NNLL QCD + NLO EW:
[Broggio, Ferroglio et al \(2019\)](#),
[Kulesza, Motyka et al \(2020\)](#)
- see also high energy EW correction in
[Pagani et al \(2023\)](#)
- Combined effort at 13.6 TeV in HWG:
 - Two resummation collaborations
 - Three different central scales
 - Contribute 0.58 pb $\sim 1\%$ to Higgs XS

HH Production

- $pp \rightarrow HH$ theory history in 35 years
- LLS complexity from 6 to 9
- State-of-the-art accuracy at 13 TeV:
 - NNLO QCD $\text{FT}_{\text{approx.}}$ fiducial $\sim 5\%$
 - N3LO QCD HTL total $\sim 3\%$
 - Large NLO m_T scheme dependence
 - Partial NNLO QCD ME know:
[Davies, Schönwald, Steinhauser \(2023\)](#)
 - NLO EW corrections:
[Davies, Schönwald, Steinhauser, Zhang \(2023\)](#)

More details in H.T. Zhang's talk

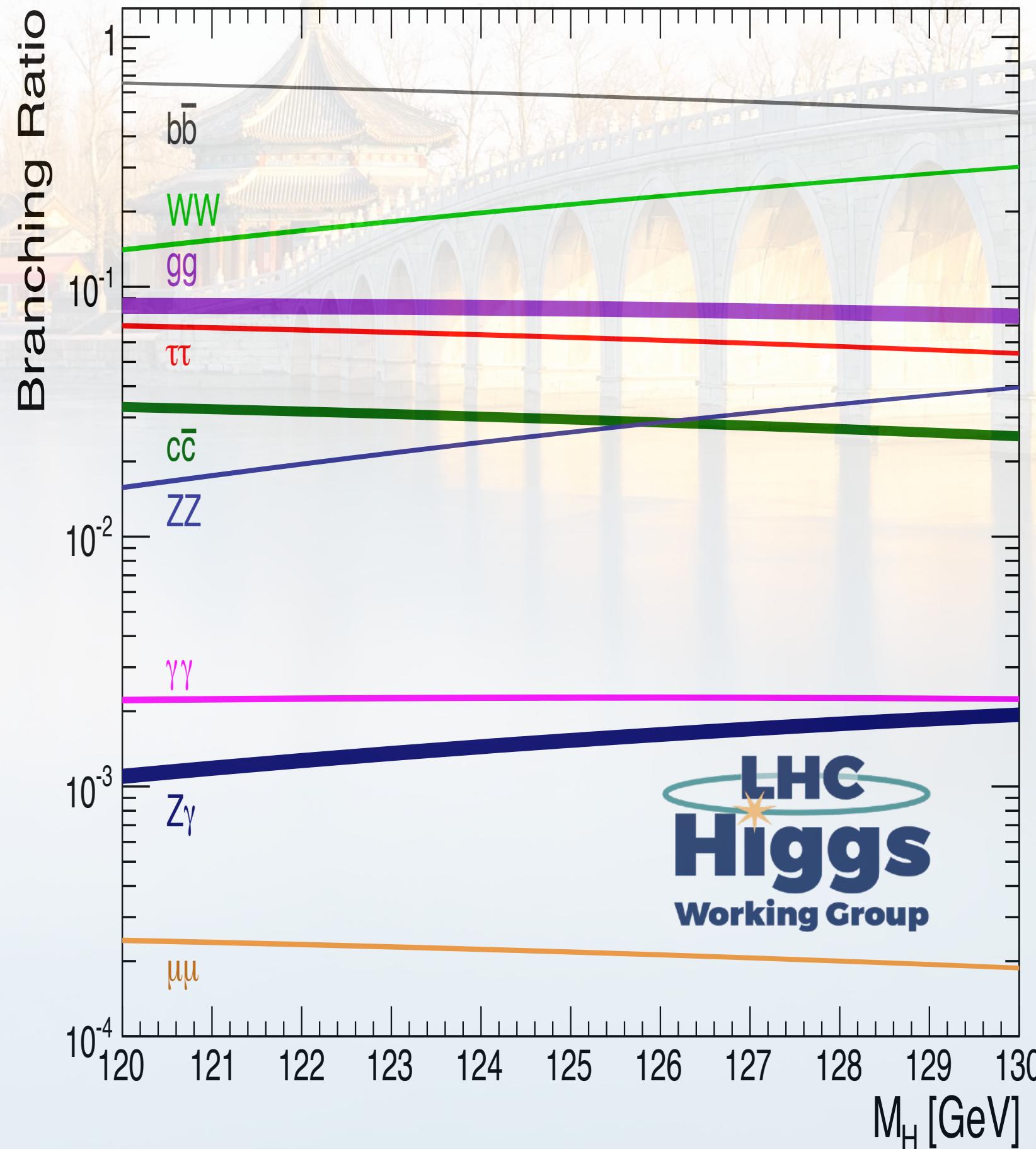
loops + legs + scale = 8-9



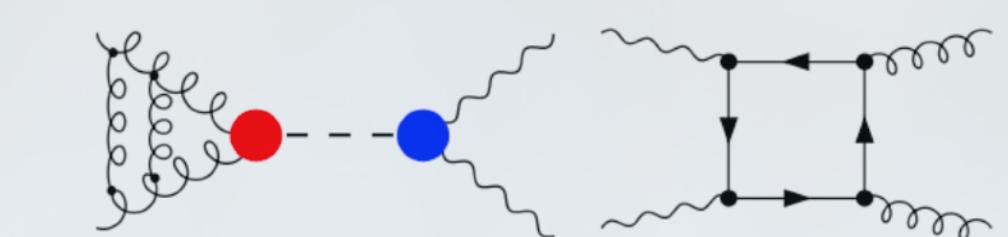
[1] Glover, van der Bij 88; [2] Dawson, Dittmaier, Spira 98; [3] Shao, Li, Li, Wang 13; [4] Grigo, Hoff, Melnikov, Steinhauser 13; [5] de Florian, Mazzitelli 13; [6] Grigo, Melnikov, Steinhauser 14; [7] Grigo, Hoff 14; [8] Maltoni, Vryonidou, Zaro 14; [9] Grigo, Hoff, Steinhauser 15; [10] de Florian, Grazzini, Hanga, Kallweit, Lindert, Maierhöfer, Mazzitelli, Rathlev 16; [11] Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Schubert, Zirke 16; [12] Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Zirke 16; [13] Ferrera, Pires 16; [14] Heinrich, SPJ, Kerner, Luisoni, Vryonidou 17; [15] SPJ, Kuttimalai 17; [16] Gröber, Maier, Rauh 17; [17] Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher 18; [18] Grazzini, Heinrich, SPJ, Kallweit, Kerner, Lindert, Mazzitelli 18; [19] de Florian, Mazzitelli 18; [20] Bonciani, Degrassi, Giardino, Gröber 18; [21] Davies, Mishima, Steinhauser, Wellmann 18, 18; [22] Mishima 18; [23] Gröber, Maier, Rauh 19; [24] Davies, Heinrich, SPJ, Kerner, Mishima, Steinhauser, David Wellmann 19; [25] Davies, Steinhauser 19; [26] Chen, Li, Shao, Wang 19, 19; [27] Davies, Herren, Mishima, Steinhauser 19, 21; [28] Baglio, Campanario, Glaus, Mühlleitner, Ronca, Spira 21; [29] Bellafronte, Degrassi, Giardino, Gröber, Vitti 22; [30] Davies, Mishima, Schönwald, Steinhauser, Zhang 22;

Higgs Boson Decay

- Higgs decay branch ratio (YR4):
- $\Gamma_H^{tot} \sim 4 \text{ MeV}$ for all Higgs Factories



- Dominant $H \rightarrow b\bar{b}$
- Inclusive BR known at N4LO: [Baikov, Chetykin, Kuhn \(2005\)](#), [Herzog et al \(2017\)](#), [Davies et al \(2017\)](#)
 $\sim \pm 0.15\%$ scale error for $\mu \in [0.1, 10] \times m_H$
- Differential BR known at N3LO $\sim \pm 0.7\%$: [Mondini, Schiavi, Williams \(2019\)](#)
- Additional 1% (15%) contribution for top induced $b\bar{b}$ ($c\bar{c}$) decay at N3LO: [Mondini, Schubert, Williams \(2020\)](#)
- Need IR safe flavour tagging (anti-kT is **NOT**)
- $H \rightarrow gg$ BR known at N4LO $\sim \pm 3\%$: [Davies et al \(2017\)](#), [Herzog et al \(2017\)](#)
- More details in L. Chen's talk
- $H \rightarrow W^+W^-$
- Mixed QCD-EW at 2-loop contribute $0.2 \sim 1\%$ depending on EW schemes: [Ma, Wang, Xu, Yang, Zhou \(2021\)](#)
- $H \rightarrow Z\gamma, ZZ$
- Mixed QCD-EW correction (2-loop triangle) [Wang, Xu, Yang \(2019\)](#)
- $H \rightarrow \gamma\gamma$ interference at NNLO_{SV}
- $gg \rightarrow H \rightarrow \gamma\gamma \times gg \rightarrow \gamma\gamma$ background
- -2% destructive contribution to $\sigma_{H \rightarrow \gamma\gamma}$



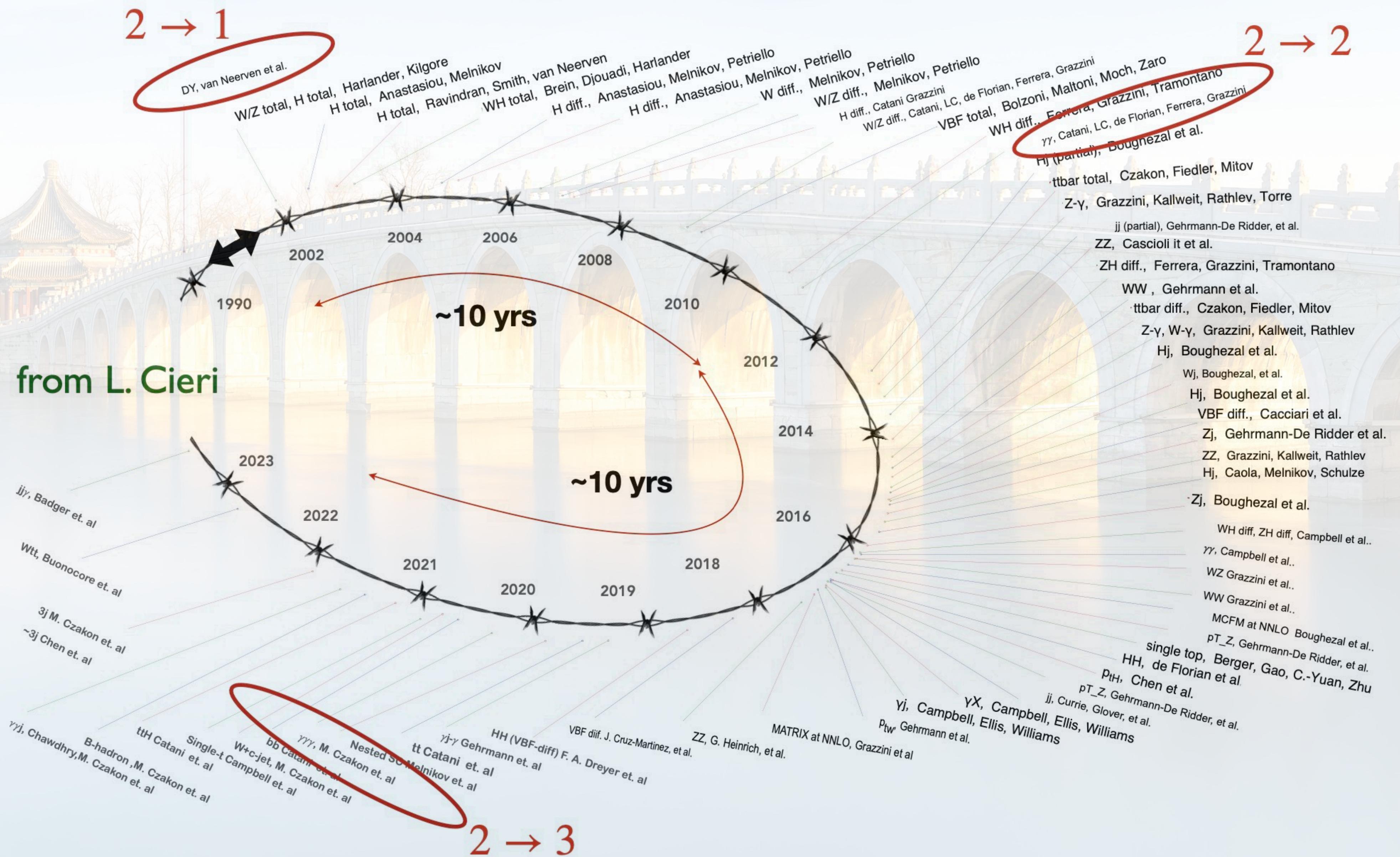
[Bargiela, Buccioni et al \(2022\)](#)

Future Prospects

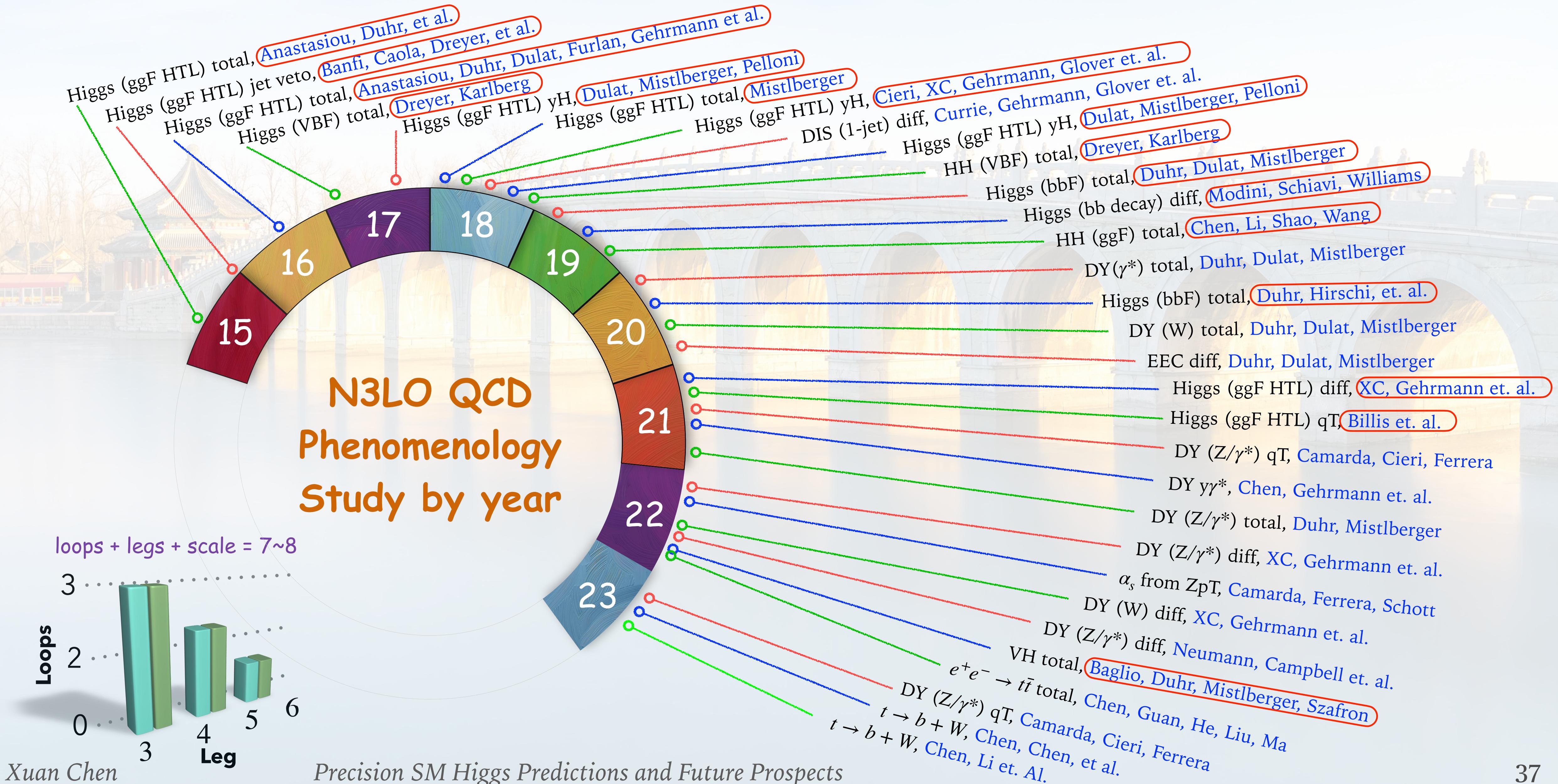
Reflections from History



Perturbative QCD @ NNLO



Perturbative QCD @ N3LO



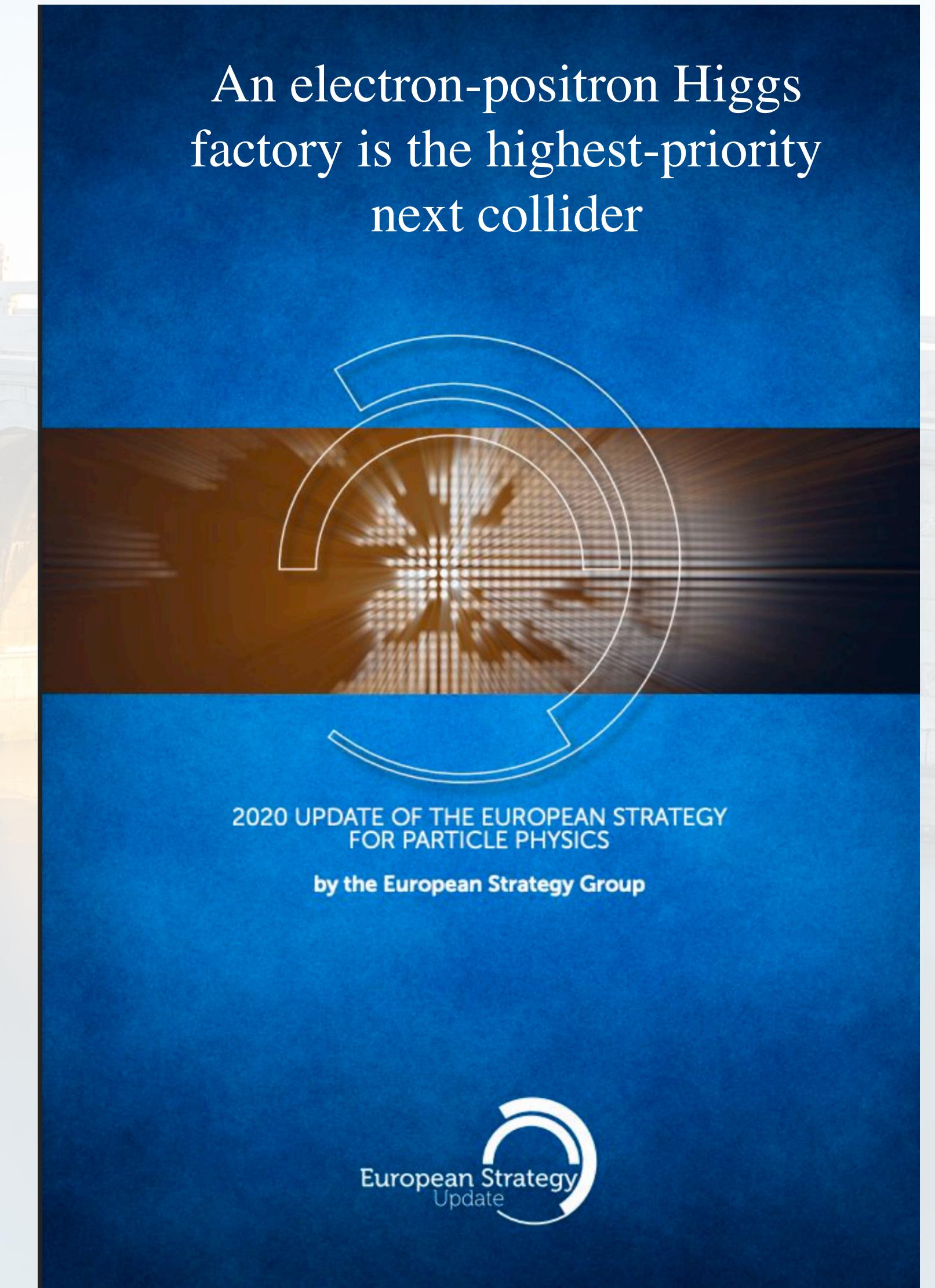
FUTURE PROSPECTS

- Precision is not the ultimate goal → identify anomaly then understand
- The most famous **failed experiment**: Michelson–Morley in **1887**,
foundation of special relativity. → 1907 Nobel Prize to **Albert A. Michelson** .
- “... it seems probable that **most of the grand underlying principles have been firmly established** and that further advances are to be sought chiefly in the rigorous application of these principles to all the phenomena which come under our notice. ... An eminent physicist remarked that **the future truths of physical science are to be looked for in the sixth place of decimals.**” — **Albert A. Michelson**, **1894** University of Chicago
- Mass origin, Higgs potential, EW vacuum metastability etc.

An electron-positron Higgs factory is the highest energy particle accelerator ever proposed.

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- Higgs Yellow Report 5 planned at 2025, publication style, not monolithic



Yellow Report 5

- Four Yellow Reports produced by the LHC Higgs WG over its lifetime:
 - “*Inclusive Observables*” [\[CERN-2011- 002\]](#)
 - “*Differential Distributions*” [\[CERN-2012-002\]](#)
 - “*Higgs Properties*” [\[CERN-2013-004\]](#)
 - “*Deciphering the Nature of the Higgs Sector*” [\[CERN-2017-002\]](#)
- HL-LHC data-taking will start in 2029. Aim to collect 1000 fb^{-1} data during Run 4 (2029–2032).
 - What can we achieve with this dataset?
 - What recommendations are needed for analyses?
 - **Plan to collect this information in a new Yellow Report 5.**



Towards Yellow Report 5

- YR5 preferably not monolithic, rather many separate reports; could be published in a dedicated *SciPost Physics Community Reports Volume*
- Time scale ~2025, focus on Run 4 of HL-LHC (1000 fb^{-1}) and include Run 3 results as far as available
- Predictions should be reproducible (ideally provide runcards)
- Initial brainstorming for experimental wishlist with ATLAS and CMS Higgs/HDBS convenors in July 2023

G. Heinrich @ HWG 23

A traditional Chinese garden scene featuring a long, blue-tiled arch bridge spanning a body of water. The bridge is lined with small figures and topped with decorative stone railings. In the background, there are several traditional buildings with dark blue roofs and intricate architectural details. The sky is a vibrant yellow and orange, suggesting either sunrise or sunset. The overall atmosphere is serene and classical.

Thank You for Your Attention



Thank You for Your Attention

[Apologies for the personal selection of topics, and
for the many interesting results not covered here]

STATE-OF-THE-ART PREDICTIONS FOR $d\sigma_{N^3LO+N^3(4)LL}$

FO	α_s^n	$P_{ab}^{(n)}(x)$	$\ln W(x_a, x_b, m_V, \vec{b}, \mu = b_0/b) \sim \int_{\mu_h}^{\mu} d\bar{\mu}/\bar{\mu} \left(A(\alpha_s(\bar{\mu})) \ln \frac{m_V^2}{\bar{\mu}^2} + B(\alpha_s(\bar{\mu})) \right)$							
$\frac{d\hat{\sigma}_{NLO}^V}{dq_T}$	1		$\ln^2(b^2 m_V^2)$	$\ln(b^2 m_V^2)$	1		1		1	
$\frac{d\hat{\sigma}_{NNLO}^V}{dq_T}$	2		$\ln^3(b^2 m_V^2)$	$\ln^2(b^2 m_V^2)$	$\ln(b^2 m_V^2)$	1		1		
$\frac{d\hat{\sigma}_{N^3LO}^V}{dq_T}$	3		$\ln^4(b^2 m_V^2)$	$\ln^3(b^2 m_V^2)$	$\ln^2(b^2 m_V^2)$	$\ln(b^2 m_V^2)$	1		1	
$\frac{d\hat{\sigma}_{N^4LO}^V}{dq_T}$	4		$\ln^5(b^2 m_V^2)$	$\ln^4(b^2 m_V^2)$	$\ln^3(b^2 m_V^2)$	$\ln^2(b^2 m_V^2)$	$\ln(b^2 m_V^2)$	1		1
...
$\frac{d\hat{\sigma}_{N^kLO}^V}{dq_T}$	K		$\ln^{k+1}(b^2 m_V^2)$	$\ln^k(b^2 m_V^2)$	$\ln^{k-1}(b^2 m_V^2)$	$\ln^{k-2}(b^2 m_V^2)$	$\ln^{k-3}(b^2 m_V^2)$
...
	Resum		LL	NLL	NNLL	N3LL	N4LL	...	$N^{k+1}LL$	
	A		A1	A2	A3	A4	A5	...	A_{k+2}	
	B			B1	B2	B3	B4	...	B_{k+1}	

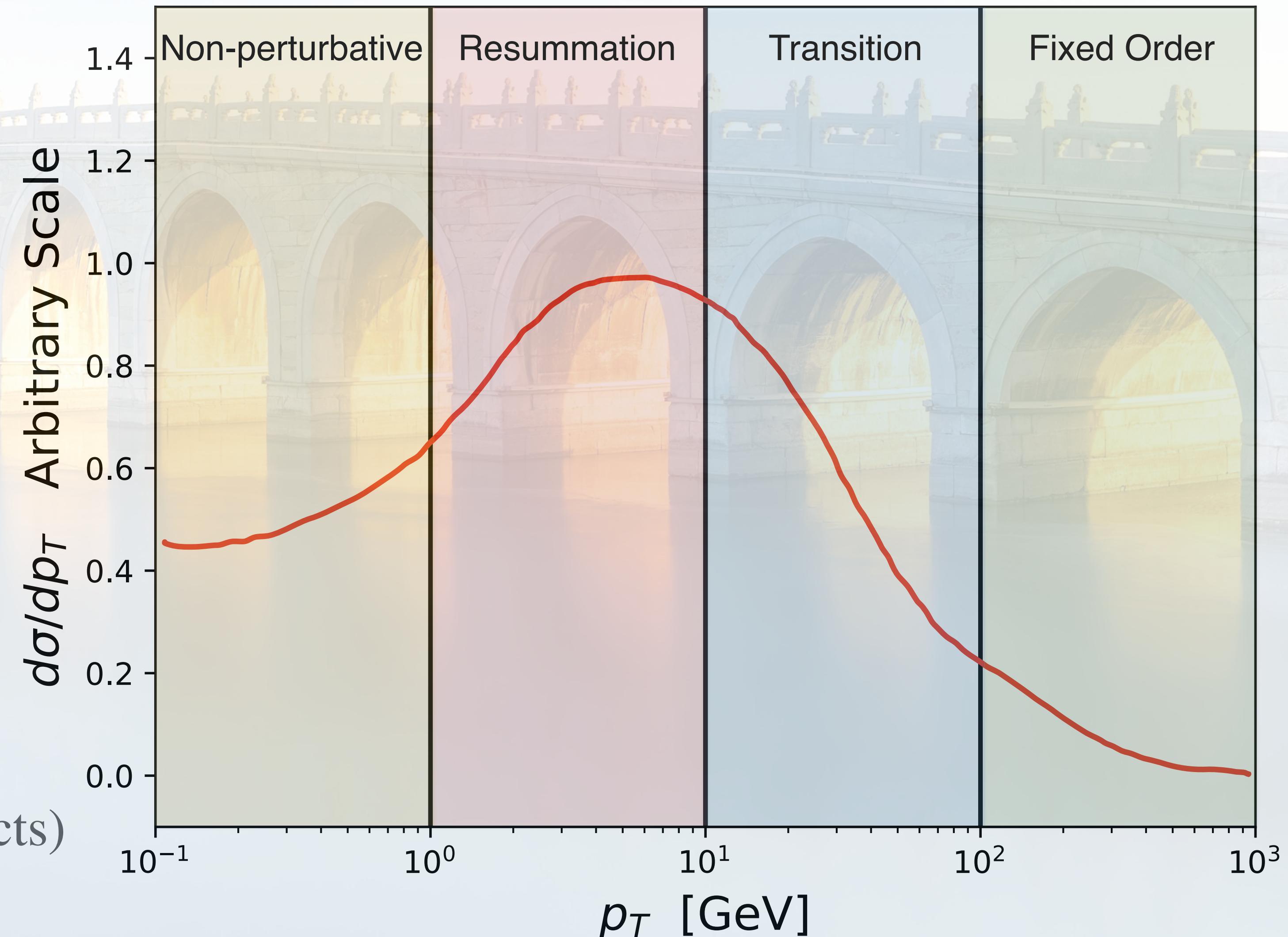
Predictions of Colourless pT at Hadron Collider

p_T Spectrum = multi-scale problem

- Beyond QCD improved parton model
- pQCD describes the tail of spectrum
- Large logarithmic divergence

$$\ln \frac{p_T}{Q} \text{ as } p_T \rightarrow 1 \text{ GeV}$$

- Various LP resummation schemes
- Multiple solutions in transition region
- Non-perturbative effects ~ 1 GeV
(Short distance and long distance effects)



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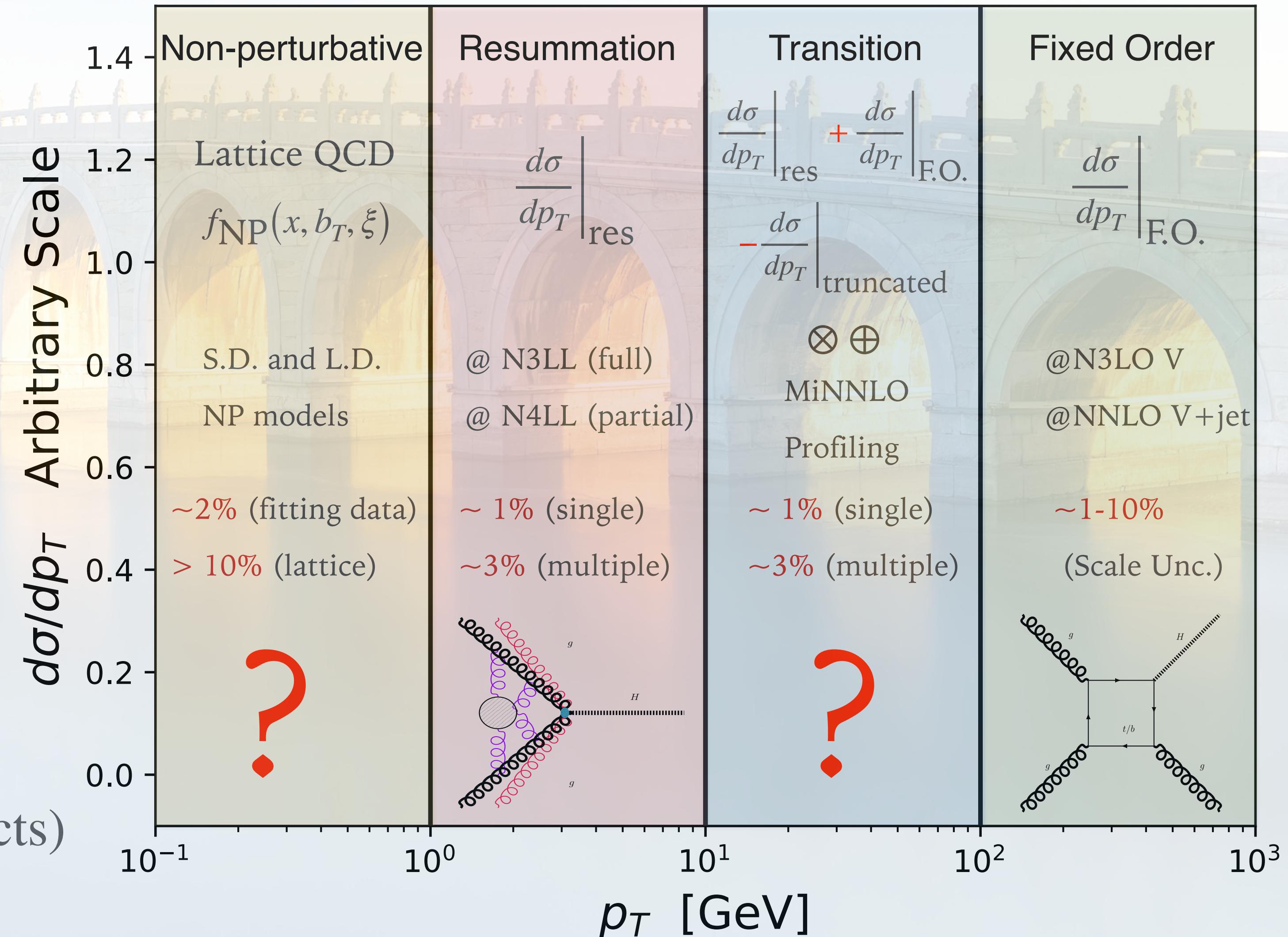
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Anatomy of differential cross sections $d\hat{\sigma}_{ab}$

► State-of-the-art differential N3LO predictions

- Fully differential N3LO Drell-Yan production (via γ^*) (XC, T. Gehrmann, N. Glover, A. Huss, T.-Z. Yang, H. X. Zhu 2021)
- Apply qt-slicing at N3LO with **SCET factorisation** and expand to N3LO:

$$\frac{d^3\sigma}{dQ^2 d^2\vec{q}_T dy} = \int \frac{d^2 b_\perp}{(2\pi)^2} e^{-iq_\perp \cdot b_\perp} \sum_q \sigma_{\text{LO}}^{\gamma^*} H_{q\bar{q}} \left[\sum_k \int_{x_1}^1 \frac{dz_1}{z_1} \mathcal{I}_{qk}(z_1, b_T^2, \mu) f_{k/h_1}(x_1/z_1, \mu) \right. \\ \times \left. \sum_j \int_{x_2}^1 \frac{dz_2}{x_2} \mathcal{I}_{\bar{q}j}(z_2, b_T^2, \mu) f_{j/h_2}(x_2/z_2, \mu) \mathcal{S}(b_\perp, \mu) + (q \leftrightarrow \bar{q}) \right] + \mathcal{O}\left(\frac{q_T^2}{Q^2}\right)$$

- All factorised functions are recently known up to N3LO:

- 1) 3-loop hard function $H_{q\bar{q}}^{(3)}$ (T. Gehrmann, E.W.N. Glover, T. Huber, N. Ikizlerli, C. Studerus 2010)
- 2) Transverse-momentum-dependent (TMD) soft function $S(b_\perp, \mu)$ at α_s^3 (Y. Li, H.X. Zhu 2016)
- 3) Matching kernel of TMD beam function I_{qk} at α_s^3 (M.-X. Luo, T.-Z. Yang, H. X. Zhu, Y. J. Zhu 2019, M. A. Ebert, B. Mistlberger, G. Vita 2020)

- Apply qt cut to factorise N3LO contribution into two parts:

$$d\sigma_{N^3LO}^{\gamma^*} = [\mathcal{H}^{\gamma^*} \otimes d\sigma^{\gamma^*}]_{N^3LO} \Big|_{\delta(p_{T,\gamma^*})} + [d\sigma_{NNLO}^{\gamma^*+jet} - d\sigma_{N^3LO}^{\gamma^* CT}]_{p_{T,\gamma^*} > \textcolor{red}{qt}_{cut}} + \mathcal{O}(qt_{cut}^2/Q^2)$$