

Questions on Higgs Physics

Andrea Wulzer



References:

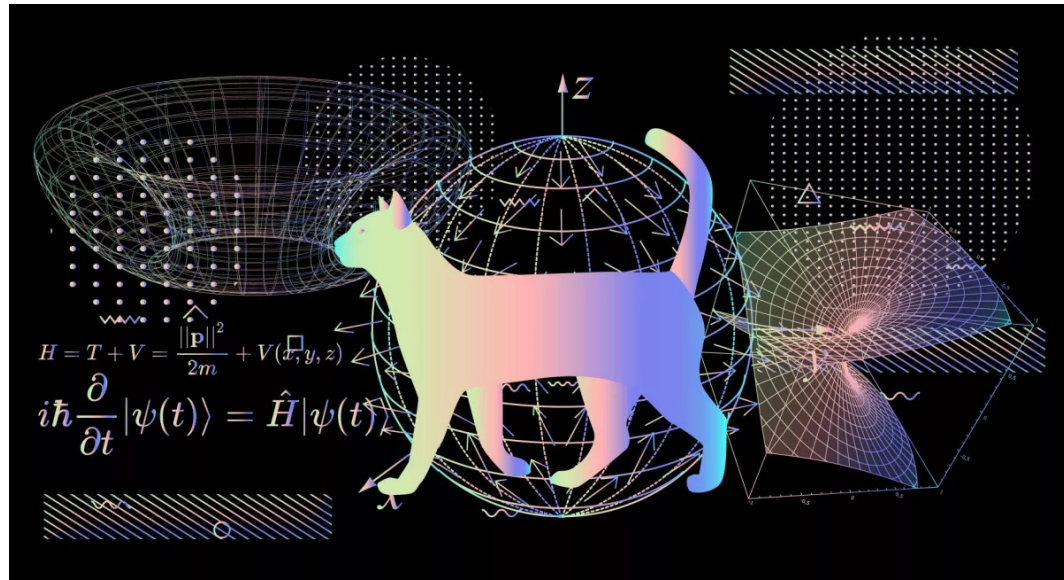
Physics Briefing Book: *Input for the European Strategy for Particle Physics Update 2020*

ECFA: *Higgs Boson Studies at Future Particle Colliders*

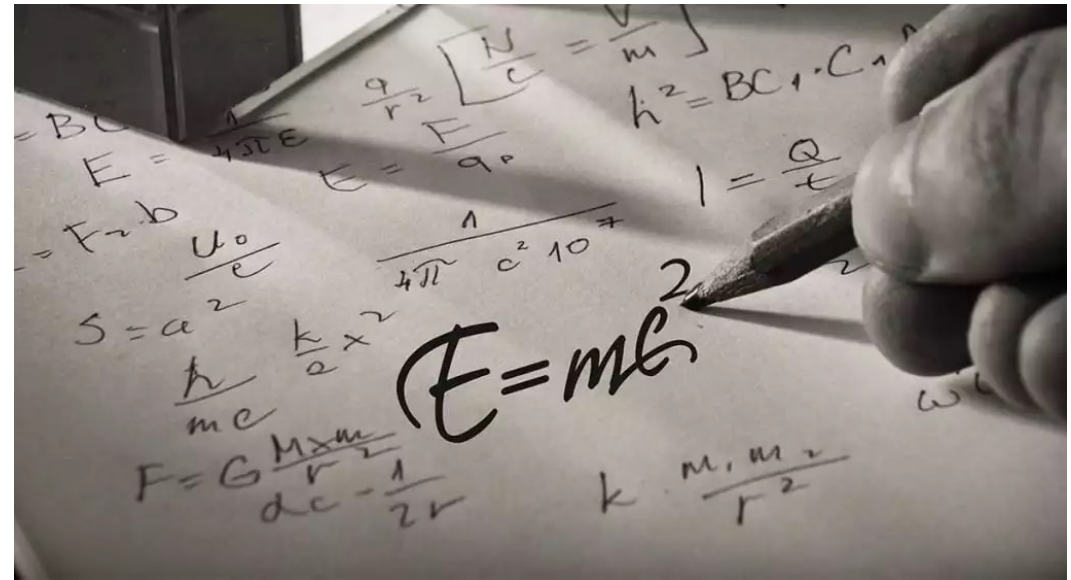
Muon Collider: *Towards a Muon Collider*

Introduction

Quantum Mechanics



+ Special Relativity

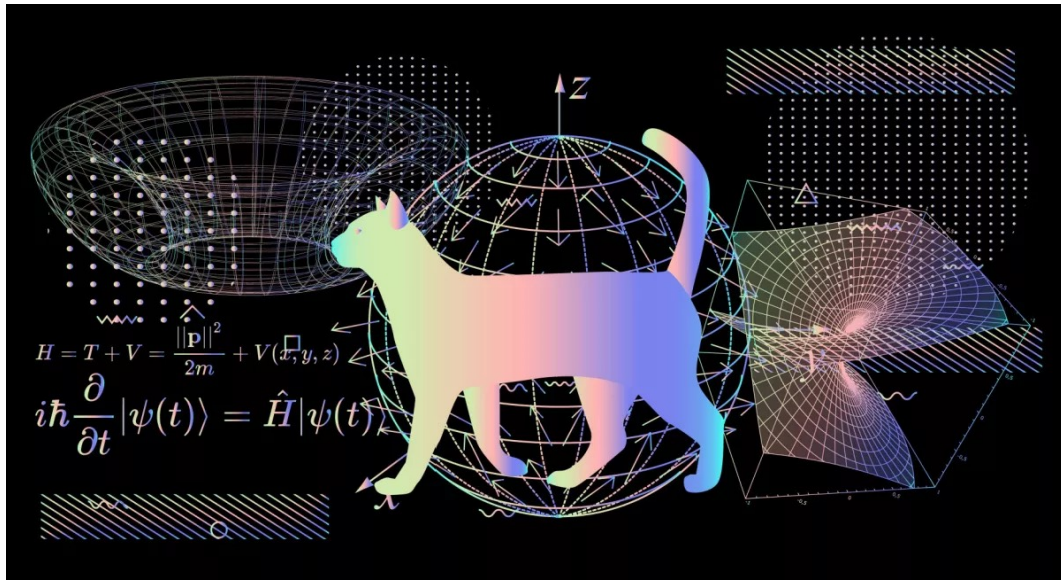


! = ? Quantum Field Theory

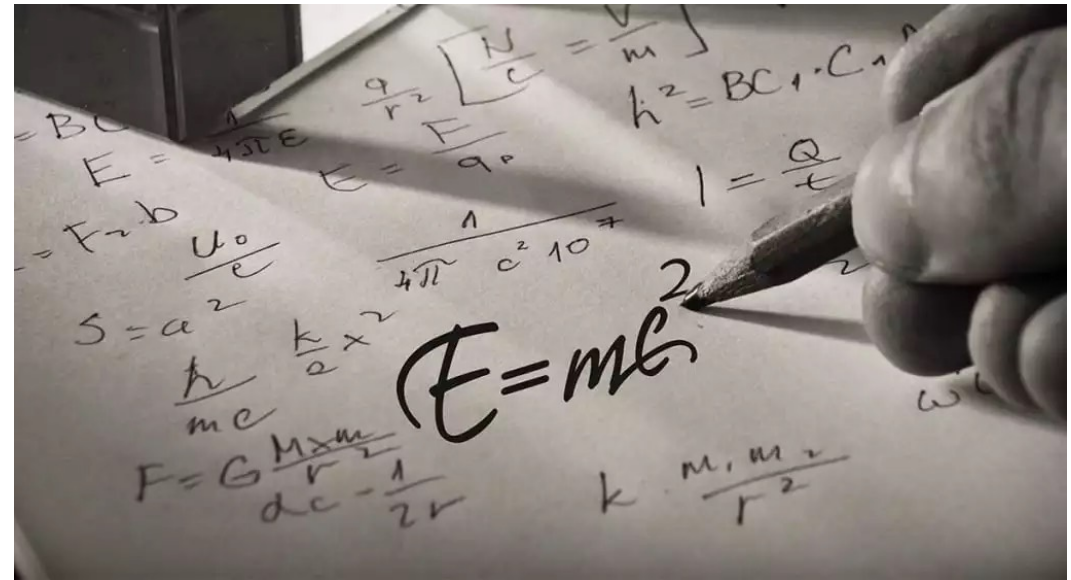
! = ? The Standard Model

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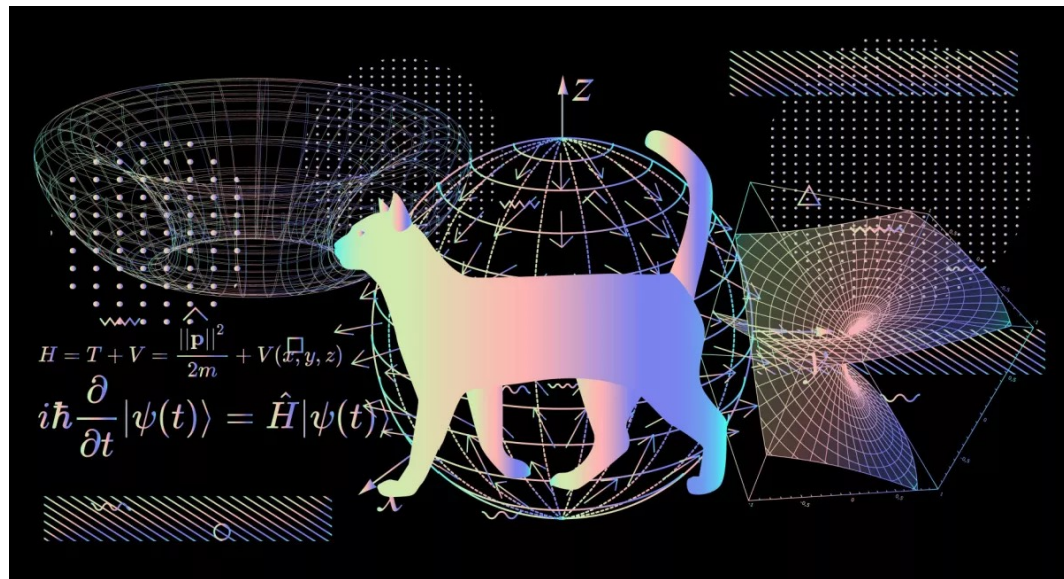
No, of course. The SM merely **accommodates** all fields we have



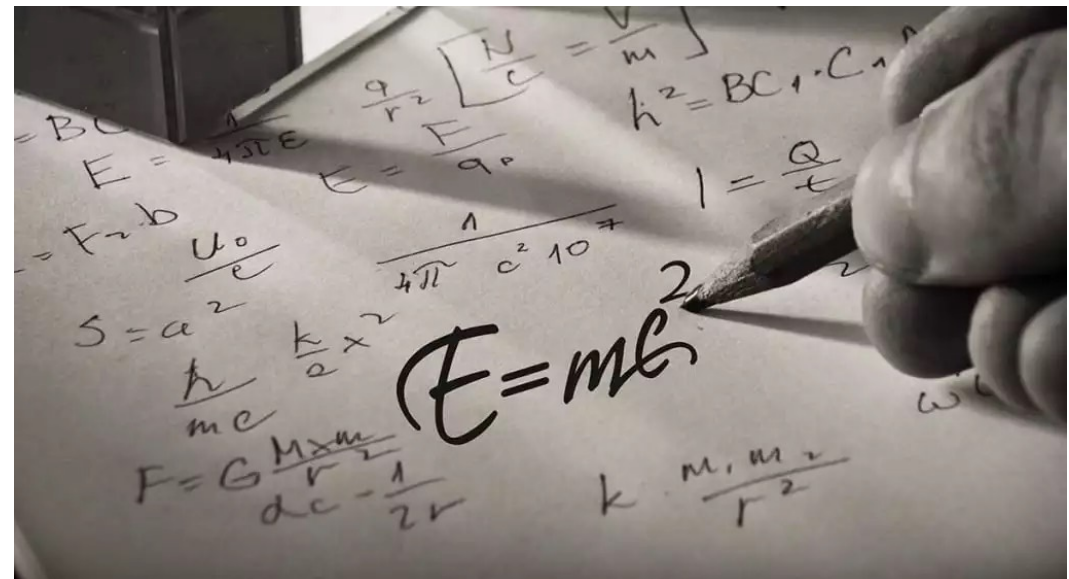
observed and the corresponding particles. And, it seems, not all of them, like Dark Matter.

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+ Special Relativity



¿ = ? Quantum Field Theory

No! Quantum fields with local Lagrangian and gauge theories are **one implementation** of QM+SR principles (the only one found so far). Its extra ingredients surely stem from an even deeper unknown underlying principle.

¿ = ? The Standard Model

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Introduction

The Higgs is revolutionary!

One more direct experimental confirmation of the QFT implementation of QM+SR principles (and indirectly of the principles).

The **first manifestation** of a new class of theories: **massive gauge theories**

The Standard Higgs model is not unique, not even within the QFT machinery:
We could “**theoretically predict**” it only **because we knew all other particles experimentally and we relied on a field and particle “economy” principle.**

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Higgs Physics questions in this talk:

Is it the Standard Model Higgs Particle?

- Single-Higgs couplings
- Trilinear Higgs coupling

What is it made of?

- Composite Higgs

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Is it the Standard Model Higgs Theory?

- High-energy EW (with Higgs) Physics

Single-Higgs couplings

Coupling modifiers “ κ ” in front of SM interaction vertices

Most basic **stress test of the SM**, where all $\kappa = 1$. SM couplings prediction is intricate manifestation of massive gauge theory machinery.

$\kappa_g, \kappa_\gamma, \kappa_{Z\gamma}$ are not vertices of SM Feynman rules, but are also left floating

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From ECFA 2019 report
[1905.03764]

kappa-0	HL-LHC	LHeC	HE-LHC		ILC			CLIC			CEPC	FCC-ee		FCC-ee/eh/hh
			S2	S2'	250	500	1000	380	15000	3000		240	365	
κ_W [%]	1.7	0.75	1.4	0.98	1.8	0.29	0.24	0.86	0.16	0.11	1.3	1.3	0.43	0.14
κ_Z [%]	1.5	1.2	1.3	0.9	0.29	0.23	0.22	0.5	0.26	0.23	0.14	0.20	0.17	0.12
κ_g [%]	2.3	3.6	1.9	1.2	2.3	0.97	0.66	2.5	1.3	0.9	1.5	1.7	1.0	0.49
κ_γ [%]	1.9	7.6	1.6	1.2	6.7	3.4	1.9	98*	5.0	2.2	3.7	4.7	3.9	0.29
$\kappa_{Z\gamma}$ [%]	10.	—	5.7	3.8	99*	86*	85*	120*	15	6.9	8.2	81*	75*	0.69
κ_c [%]	—	4.1	—	—	2.5	1.3	0.9	4.3	1.8	1.4	2.2	1.8	1.3	0.95
κ_t [%]	3.3	—	2.8	1.7	—	6.9	1.6	—	—	2.7	—	—	—	1.0
κ_b [%]	3.6	2.1	3.2	2.3	1.8	0.58	0.48	1.9	0.46	0.37	1.2	1.3	0.67	0.43
κ_μ [%]	4.6	—	2.5	1.7	15	9.4	6.2	320*	13	5.8	8.9	10	8.9	0.41
κ_τ [%]	1.9	3.3	1.5	1.1	1.9	0.70	0.57	3.0	1.3	0.88	1.3	1.4	0.73	0.44

Adding muon collider
[2303.08533]

	HL-LHC	HL-LHC +10 TeV	HL-LHC +10 TeV + ee
κ_W	1.7	0.1	0.1
κ_Z	1.5	0.4	0.1
κ_g	2.3	0.7	0.6
κ_γ	1.9	0.8	0.8
$\kappa_{Z\gamma}$	10	7.2	7.1
κ_c	—	2.3	1.1
κ_b	3.6	0.4	0.4
κ_μ	4.6	3.4	3.2
κ_τ	1.9	0.6	0.4
κ_t^*	3.3	3.1	3.1

* No input used for the MuC

In short:

percent-level from HL-LHC

permille-level with several future collider options

Single-Higgs couplings

BSM Interpretations:

Not only a (fundamental) SM stress test. Higgs couplings are effective BSM probes

A new sector with mass M_* , mixed with Higgs, typically gives:

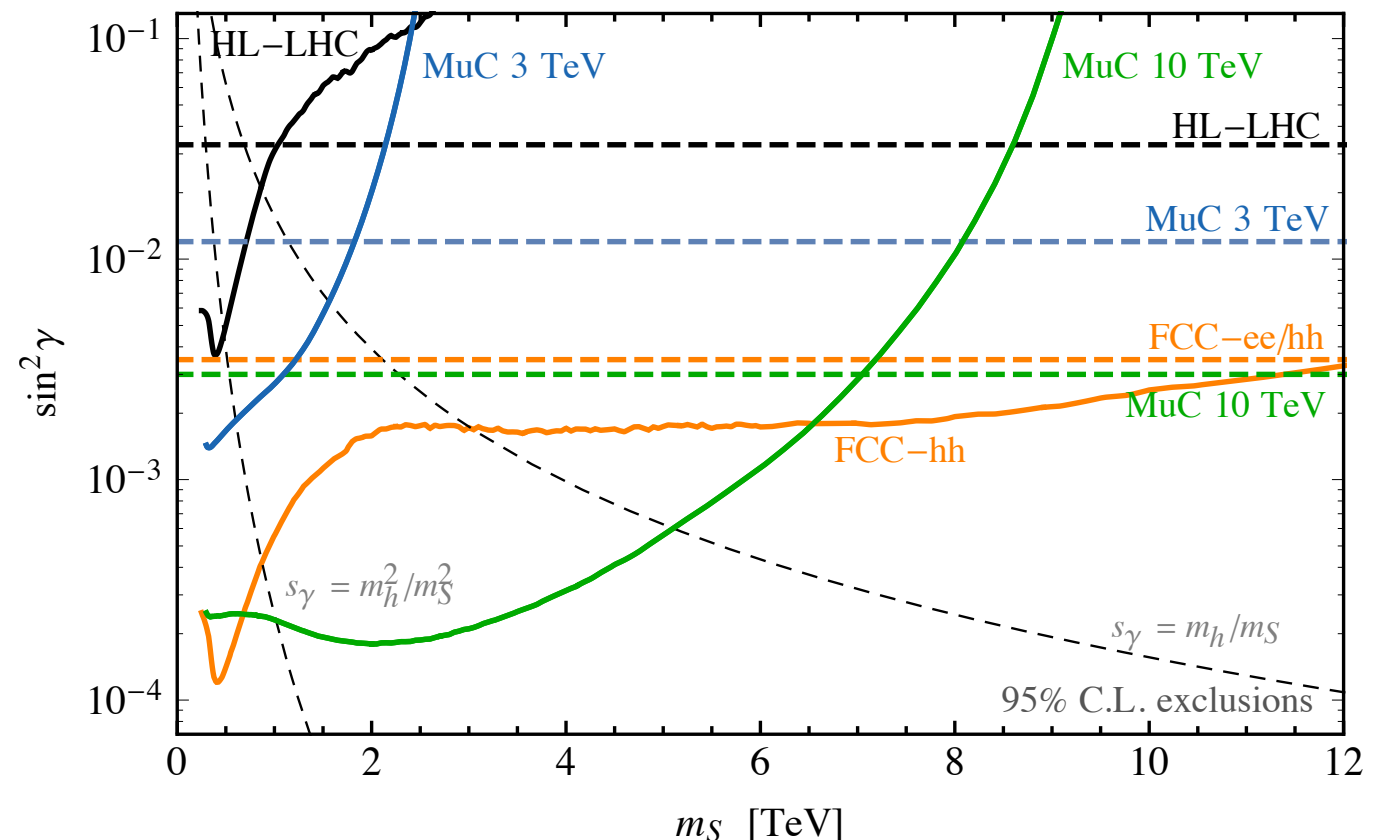
A Feynman diagram representing a scalar field h interacting with a fermion S through a loop involving a vector field v . The diagram shows a horizontal line for h entering a shaded circular loop from the left. A dashed line labeled v exits the loop upwards. A horizontal line for S enters the loop from the right. The diagram is equated to the expression $\sim \frac{g_* v}{M_*}$.

$$\sin \gamma \simeq \frac{g_x v}{M_*}$$

$$K = \cos \gamma \simeq 1 - \frac{g_x^2 v^2}{2M_*^2}$$

$$\frac{\delta\kappa}{[1\%]} \simeq \left(\frac{g_*}{g_w}\right)^2 \left(\frac{M_*}{[\text{TeV}]}\right)^2$$

Need $< 1\%$ to start testing well
above LHC direct reach for
EW-like g_* coupling



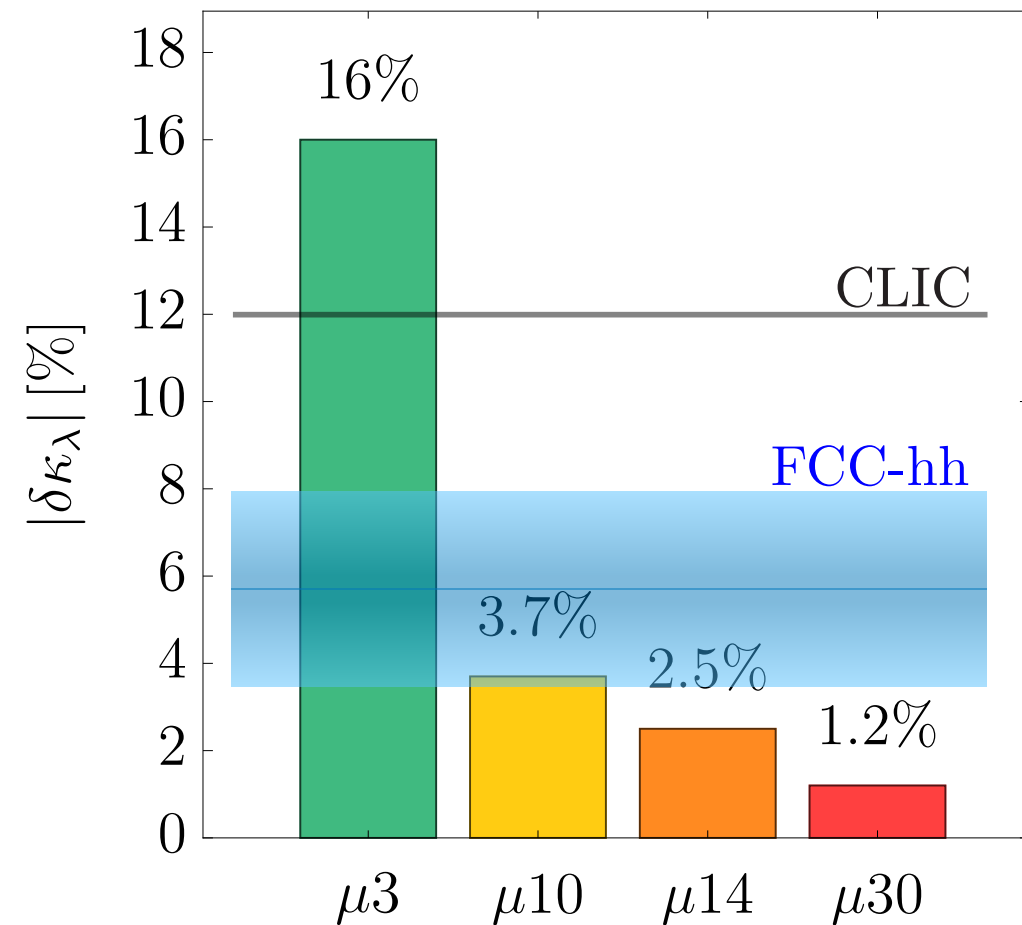
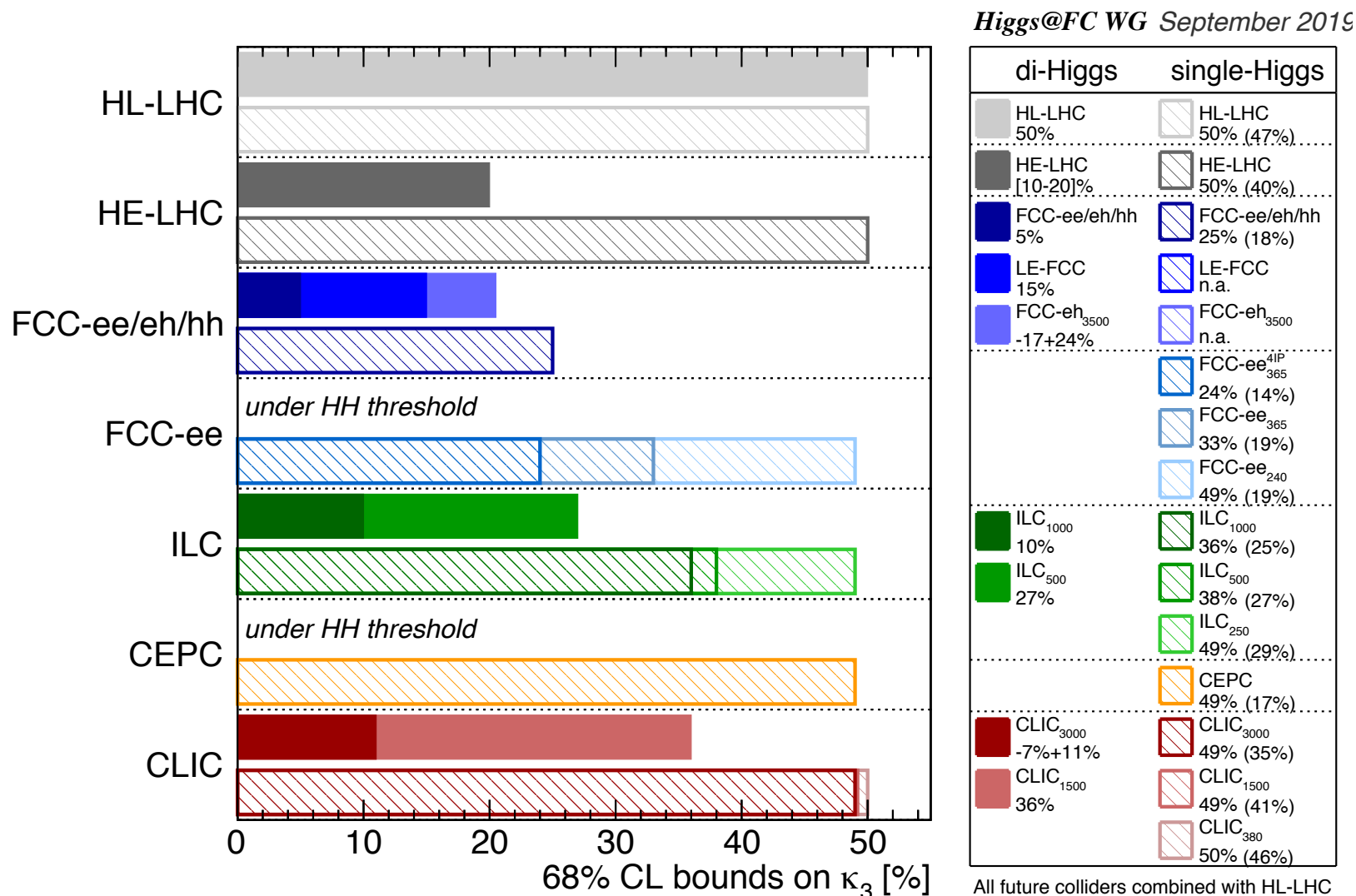
The Higgs self-coupling

The first (Scalar)³ vertex to be ever seen at work

HL-LHC will perhaps demonstrate its existence

Low-energy e^+e^- could see its indirect effect through loops

A direct measurement requires high energy: FCC-hh, CLIC-3, MuC



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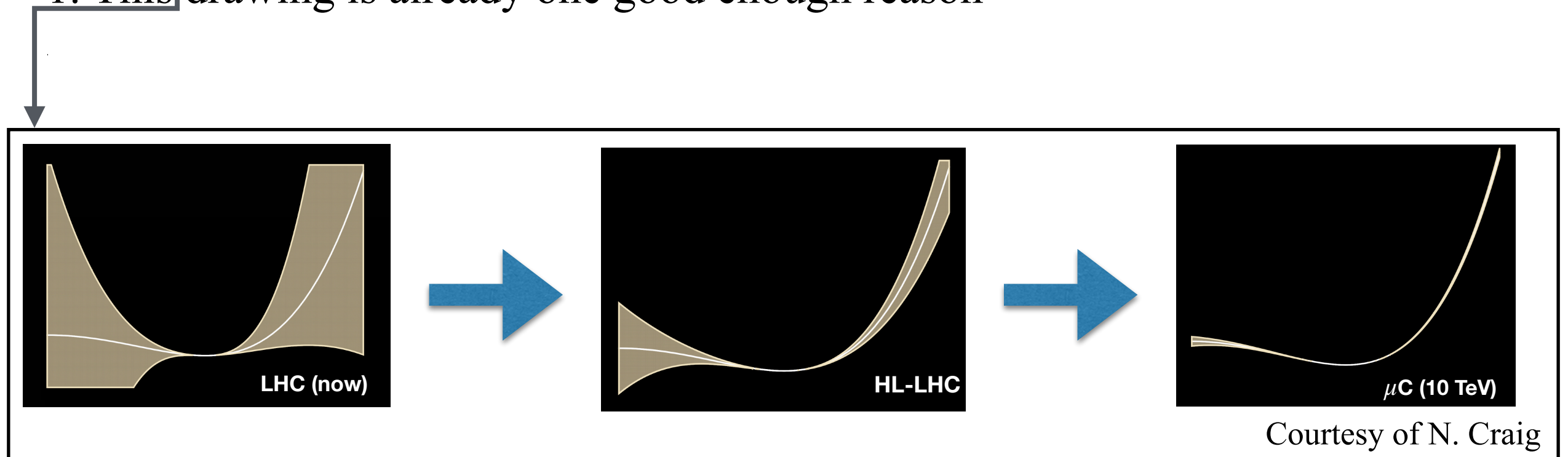
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Why measuring it **precisely**?

1. This drawing is already one good enough reason

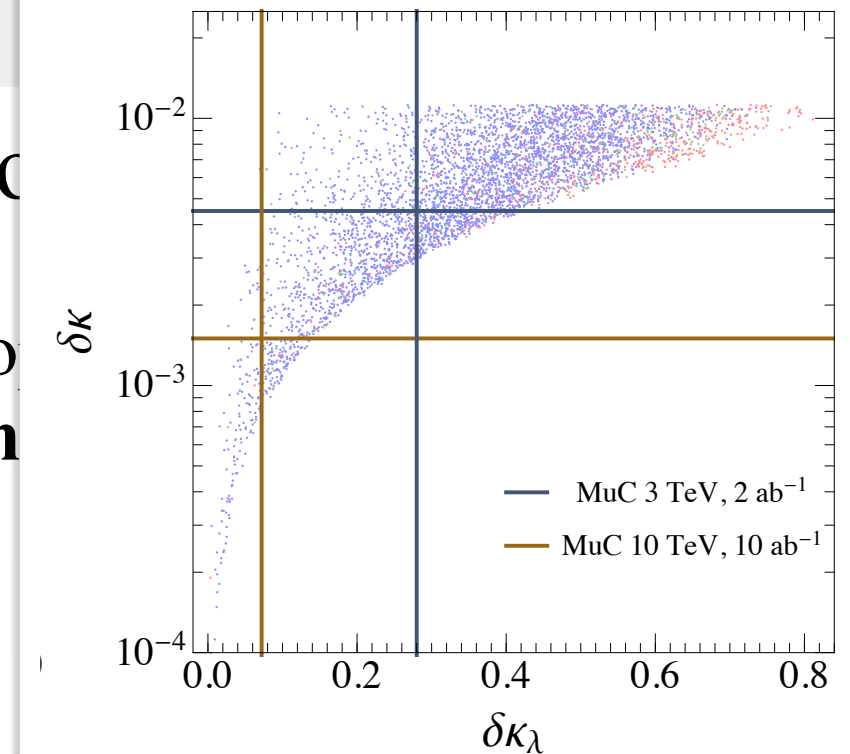


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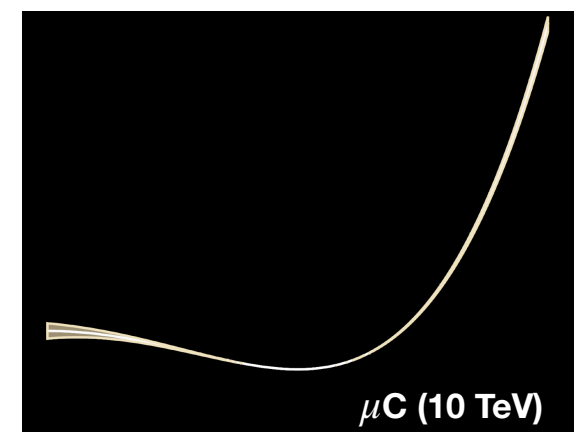
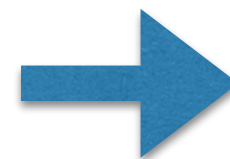
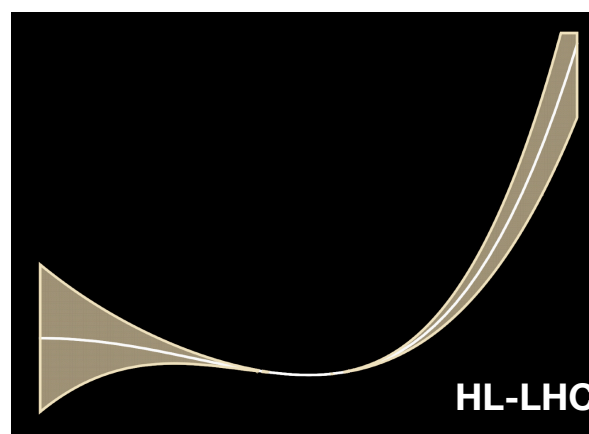
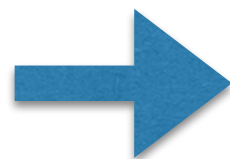
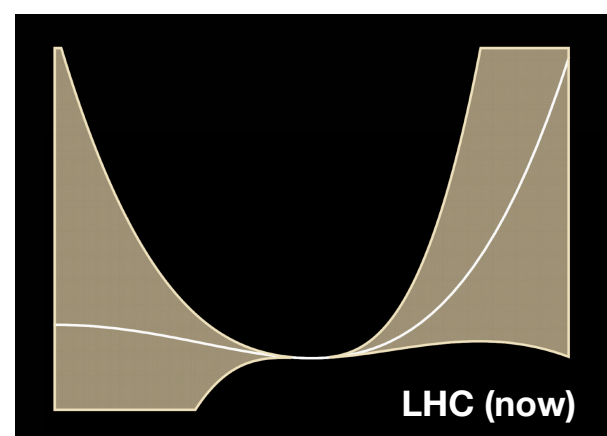
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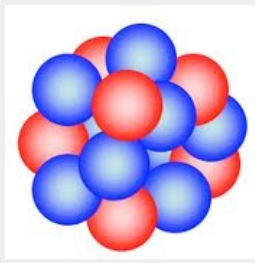


Why measuring it **precisely**?

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2. Additionally, below-10% sensitivity starts probing models with 1st order EW phase transition in the Early Universe better than 0.1% single -Higgs couplings

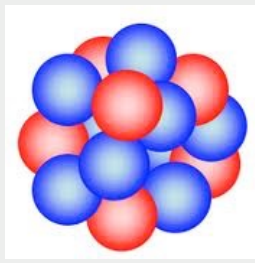


Courtesy of N. Craig



Composite Higgs

We must check if the Higgs is elementary.
If so, it is the first spin-zero elementary particle

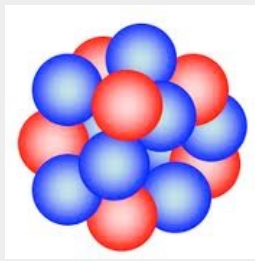


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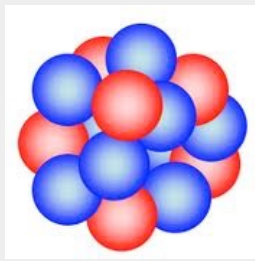
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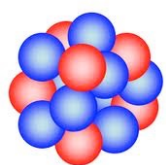
Rich phenomenology: Composite sector resonances; Higgs couplings modifications; new EFT interactions of $d > 4$. All this, broadly controlled only by:

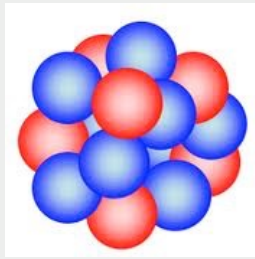
$$m_* = 1/r_H$$

The Higgs inverse size

$$g_* = m_*/f$$

The coupling-strength of resonances

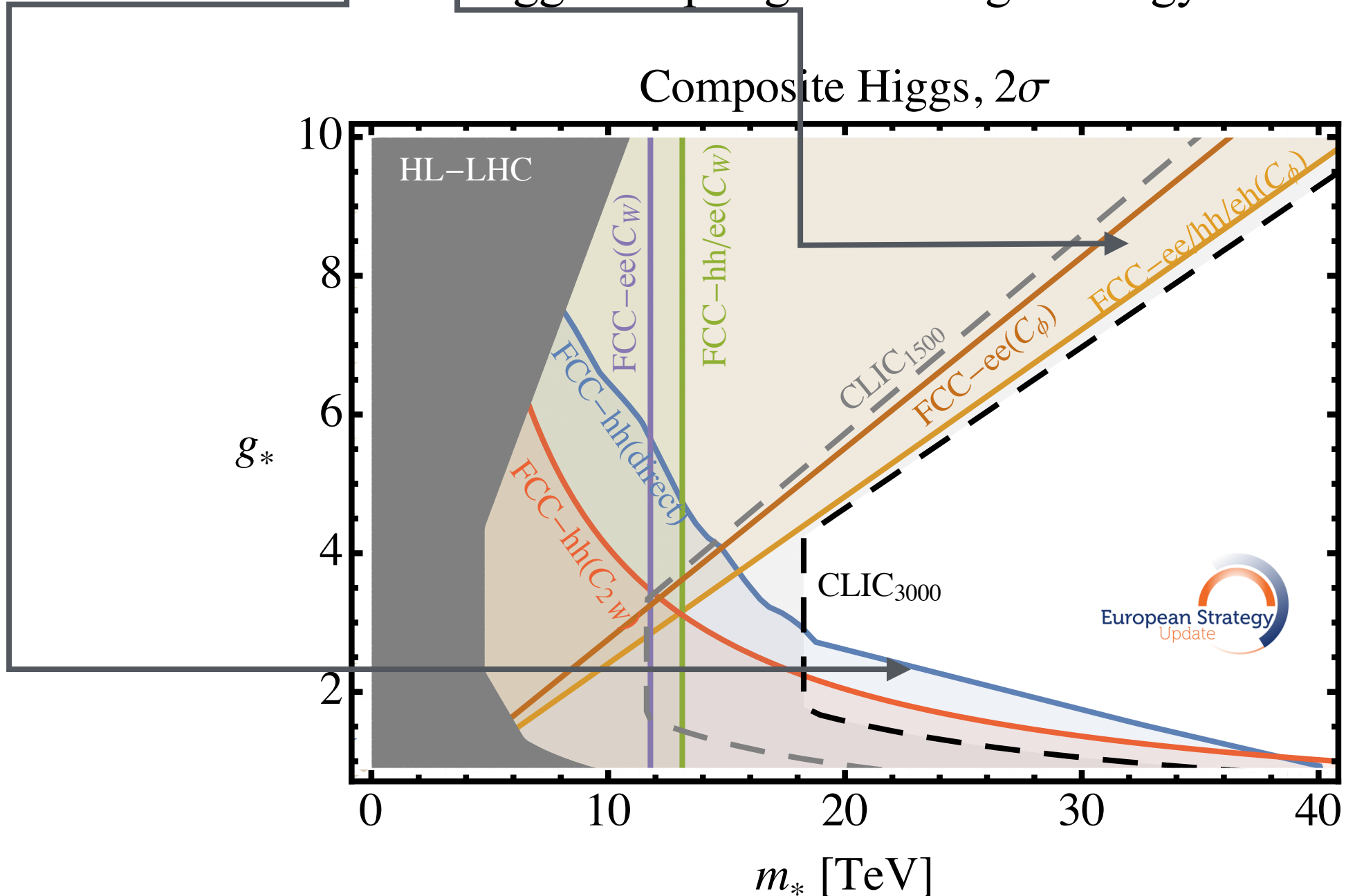

$$r_H = 1/m_*$$

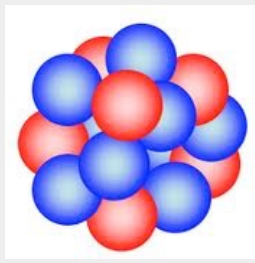


Composite Higgs

Complementary role of precision and energy

Direct Searches vs Higgs Couplings vs High-Energy Probes

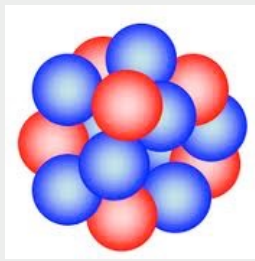




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What is the “Direct” test of Higgs compositeness ?

Obviously, a one that displays that is not point-like (i.e., not elementary).



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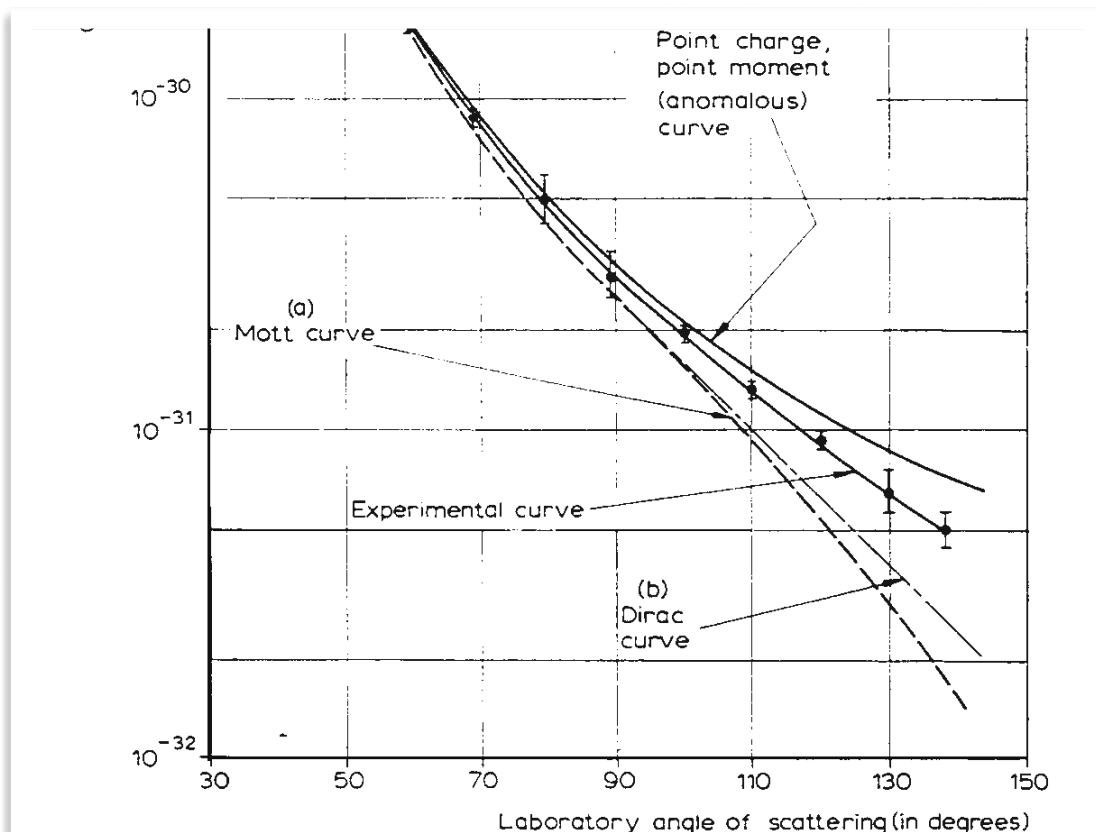
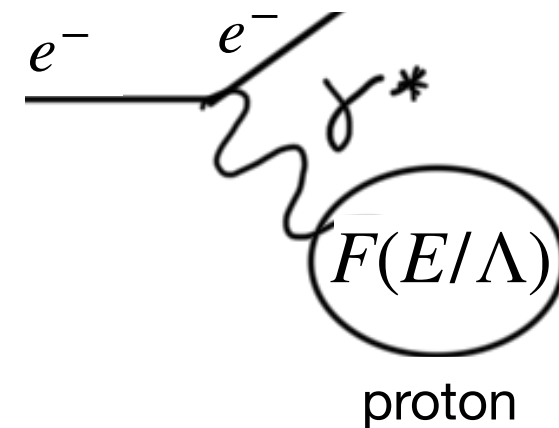
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Proton compositeness discovery:

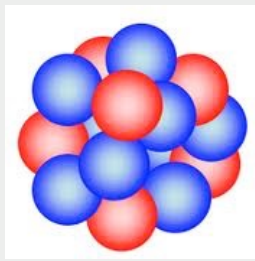
Order 10% departure from point-like prediction.

Visible form-factor effects required **large energy**

$$E \nearrow \Lambda \sim 1/r_p$$



Electron scattering from the proton at an incident energy of 188 MeV.



Composite Higgs

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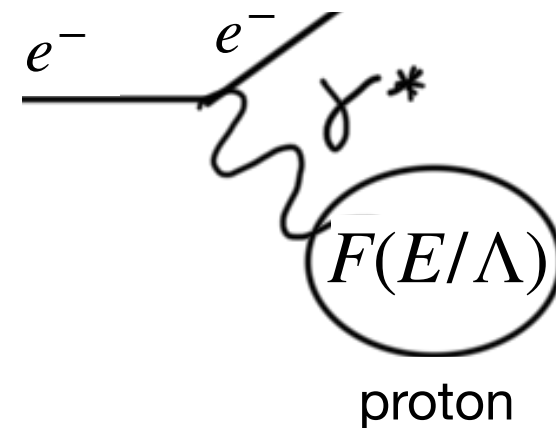
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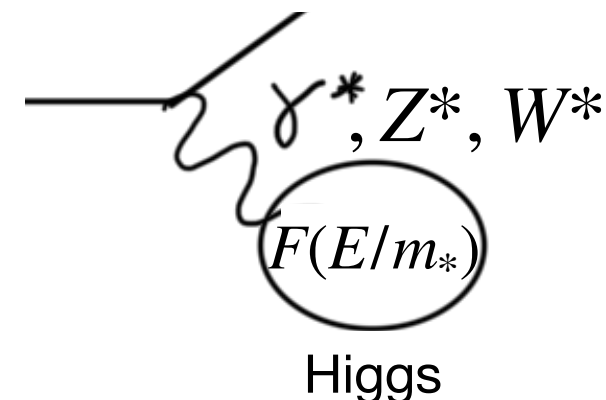


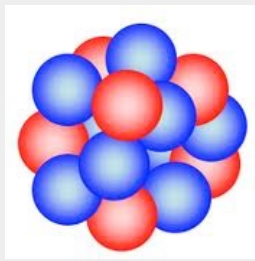
We can probe Higgs form-factors by virtual s-channel EW bosons

Same as proton, with **larger energy**

$$E \nearrow m_* \sim 1/r_H$$

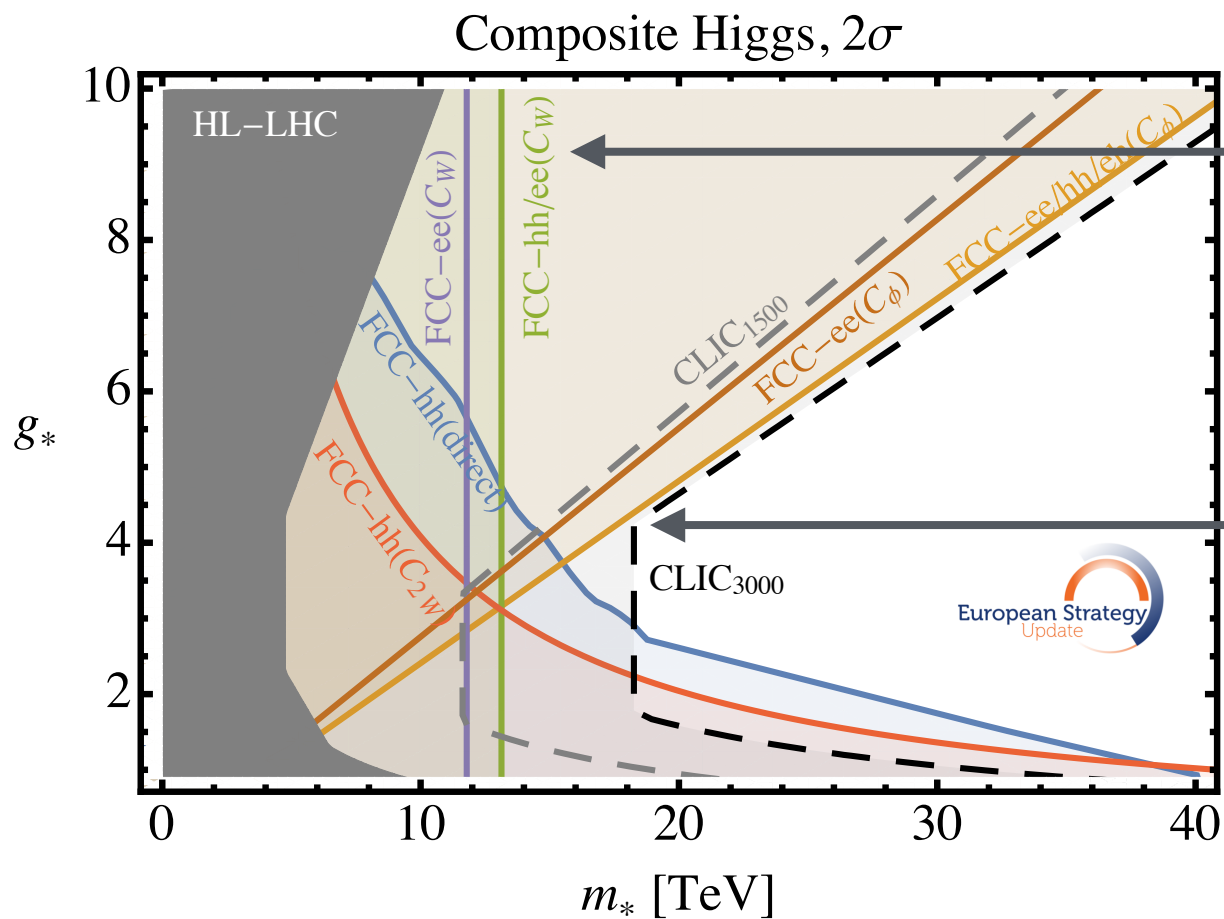
HZ and HW at cross-section measurement
at a very high energy collider

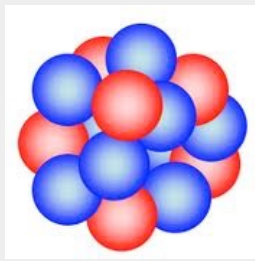




Composite Higgs

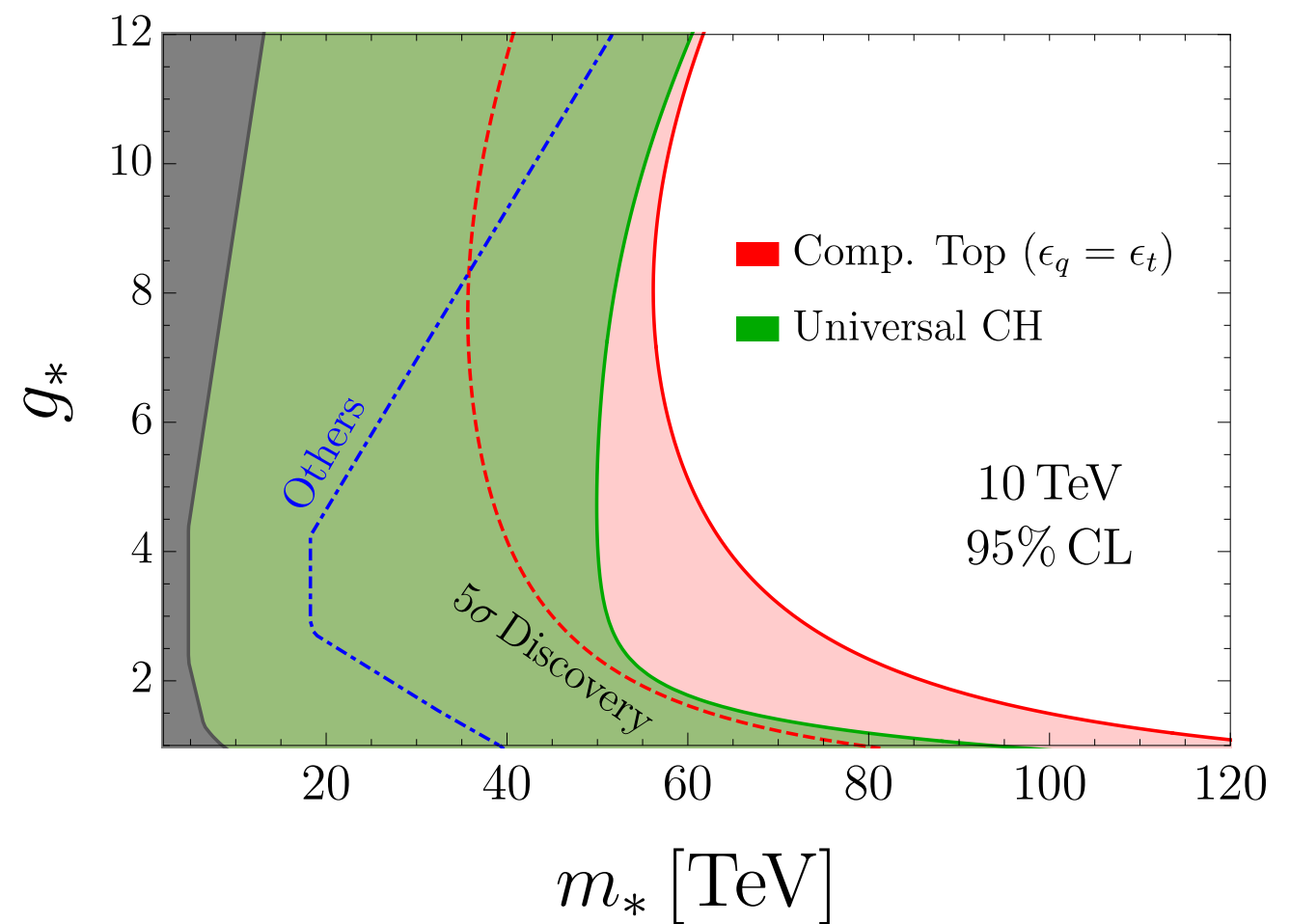
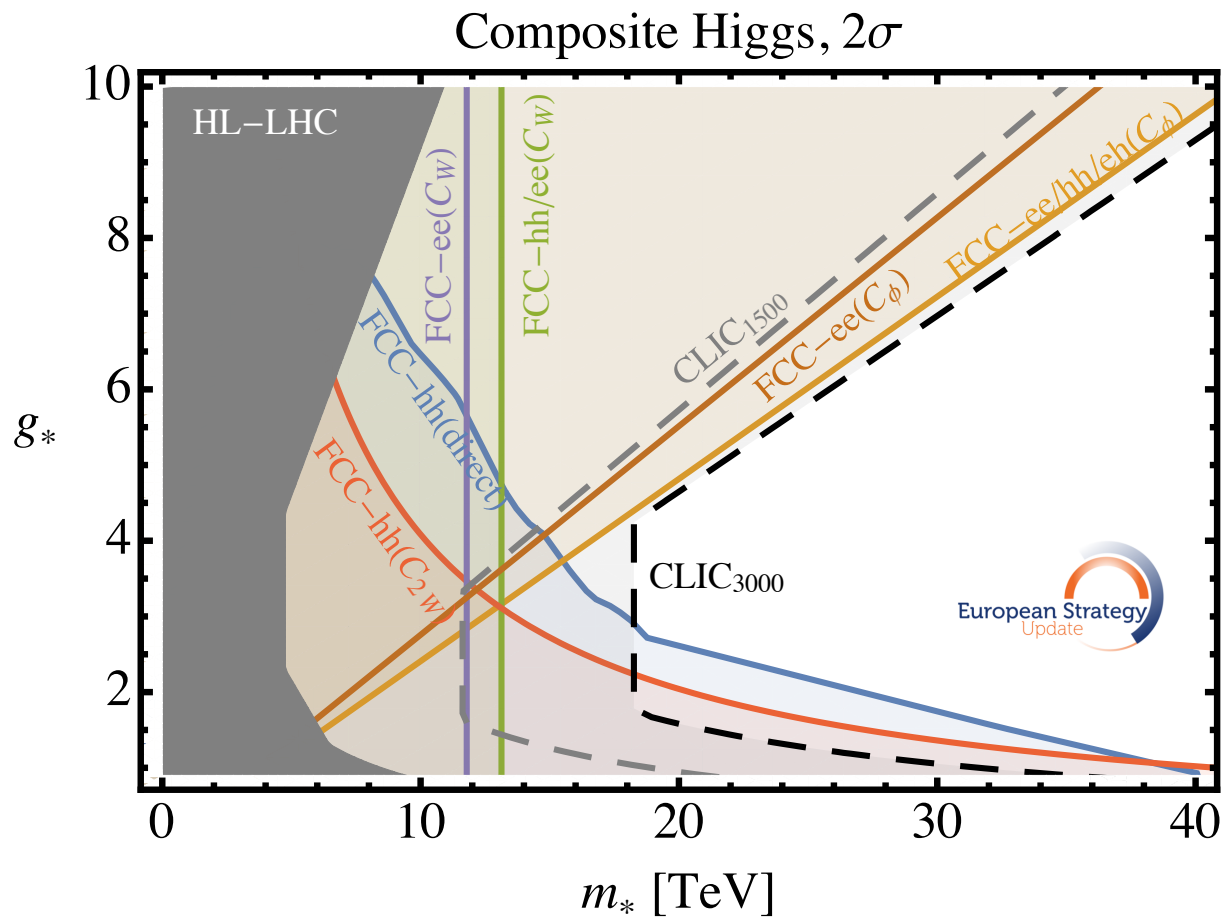
Direct test of Higgs Compositeness at FCC-hh, CLIC, and MuC



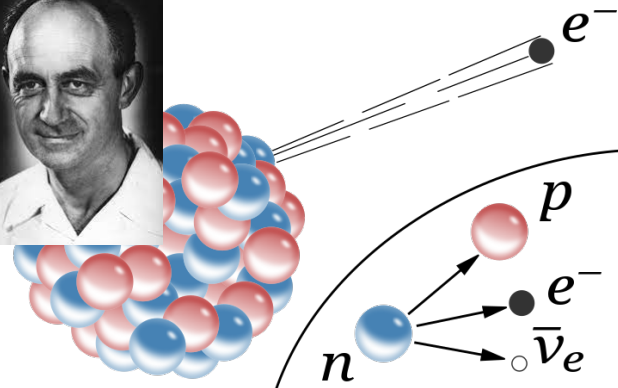
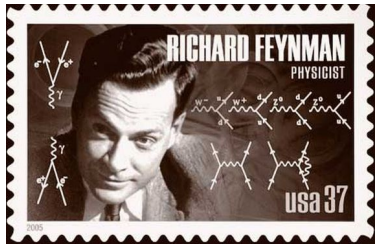


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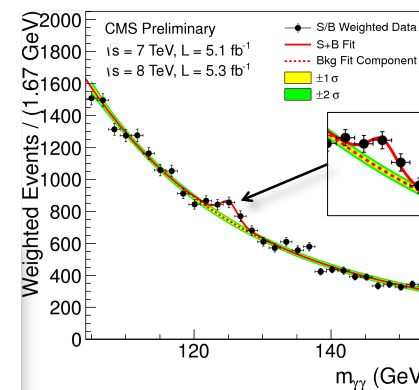
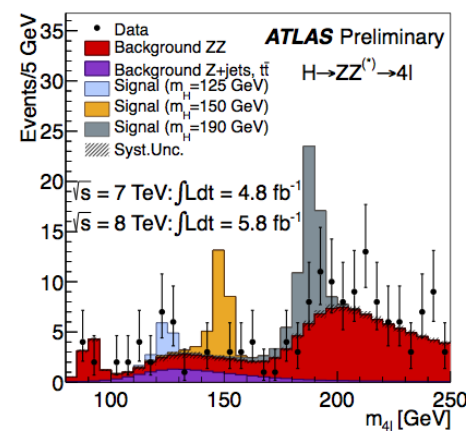
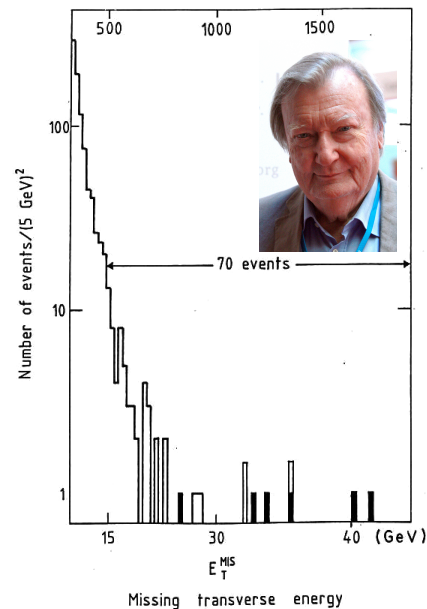
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The Standard Model Higgs Theory ?



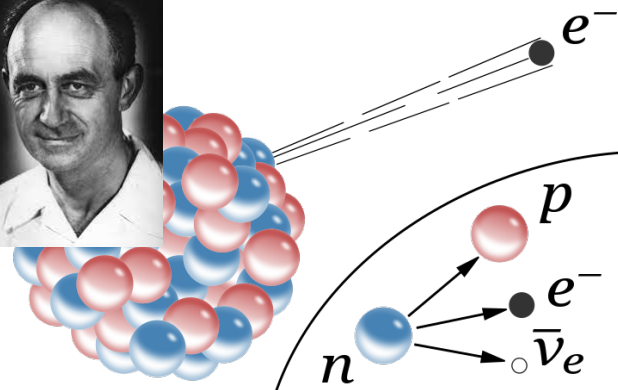
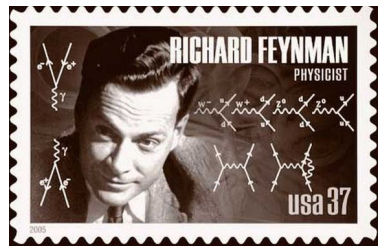
$$E \ll m_W$$



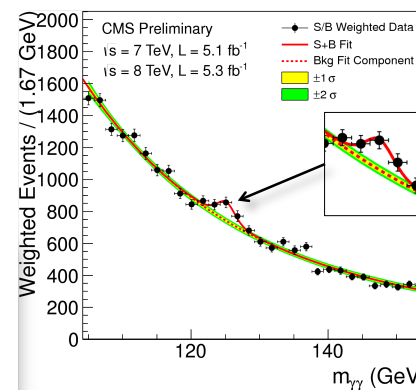
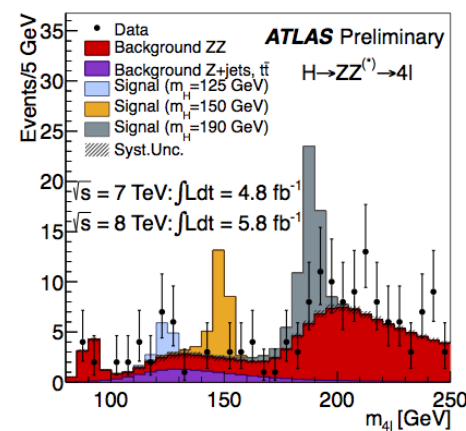
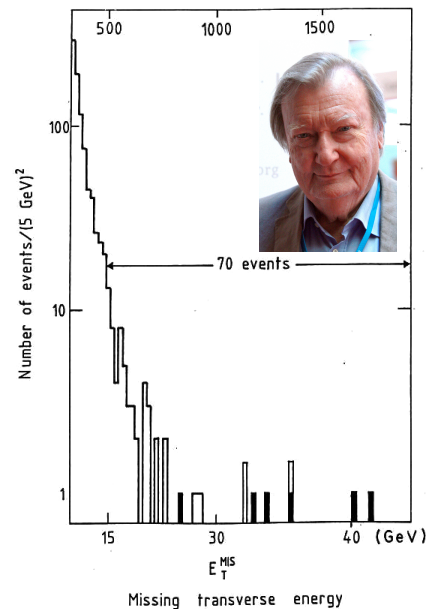
$$E \gtrsim m_W$$

$$E \gg m_W$$

The Standard Model Higgs Theory ?



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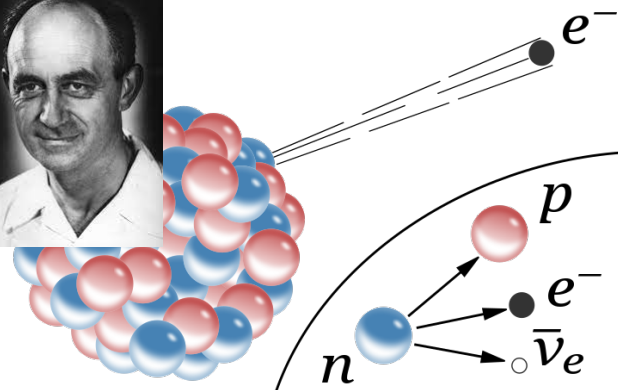
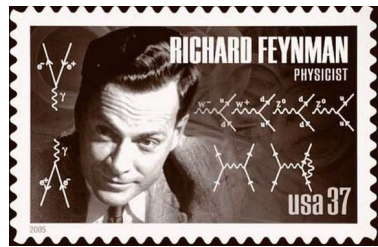


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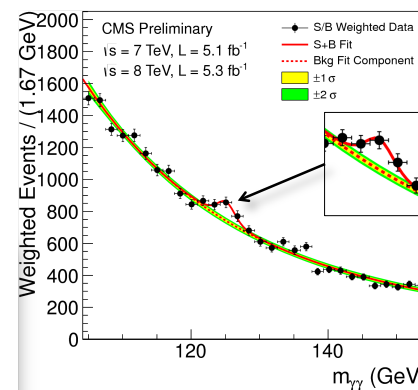
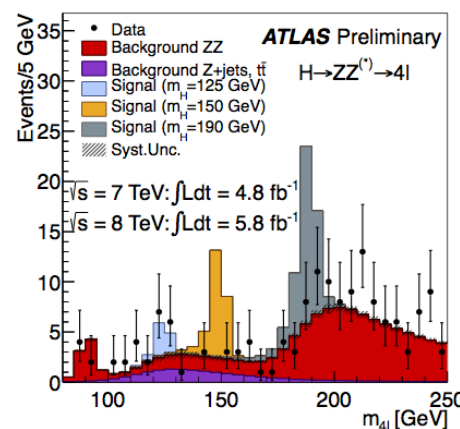
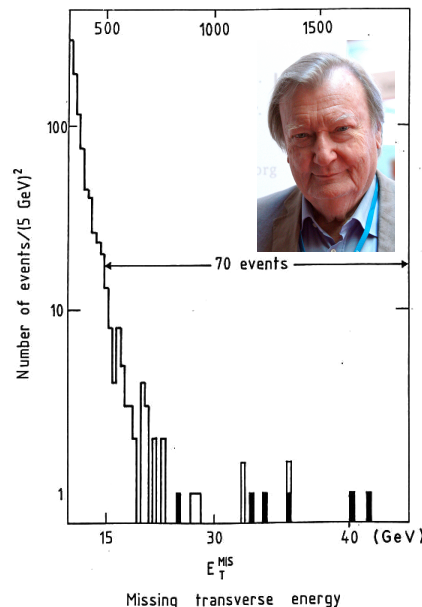
The Higgs particle shows up **here**
but theory needs it in order to go **there**

$$E \gg m_W$$

The Standard Model Higgs Theory ?



$$E \ll m_W$$



$$E \gtrsim m_W$$

The Higgs particle shows up **here**
but theory needs it in order to go **there**

Most direct theory implications are at high En.

The role of the Higgs as part of the microscopic description of the EW force must be verified by **high energy** experiments

$$E \gg m_W$$

Higgs questions at increasing energy

Is the Higgs alone? (100 GeV — TeV energy)

No prior theoretical reason for the Higgs to be minimal. Extended Higgs sectors must be investigated, also in connection with broader BSM questions, e.g. SUSY
Relevant mass-range not much above order TeV. LHC can do quite a lot. Progress requires high-energy collider like CLIC-3, FCC-hh, or MuC

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Is the EW symmetry restored? ($>$ TeV energy) 

Restoration is direct prediction of the massive gauge theory formalism. A vastly non-trivial one that we can verify directly by high-energy measurements.

Higgs should be part of a doublet: symmetry relations between H and V_L amplitudes.

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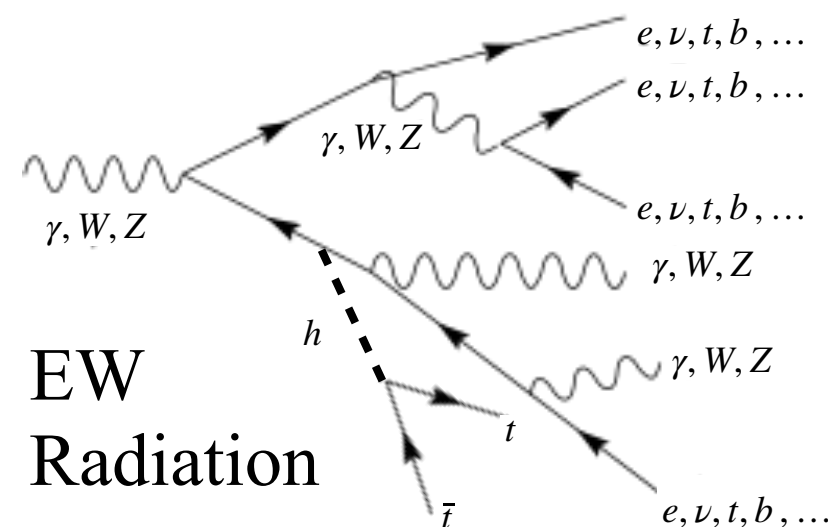
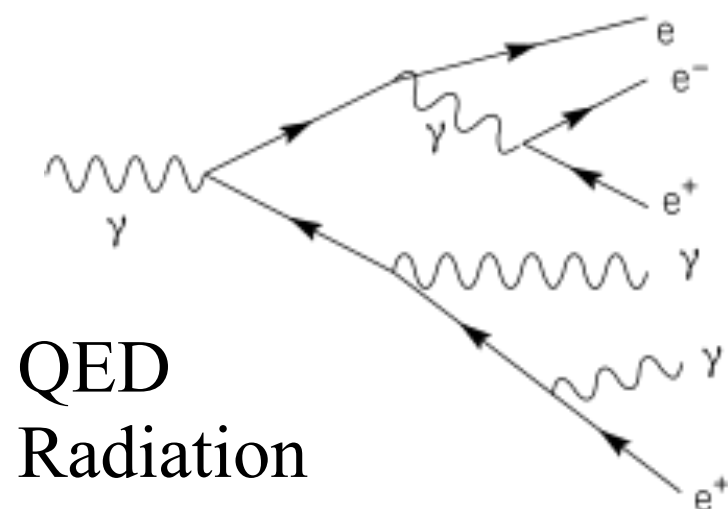
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EW Radiation (10 TeV energy):

Transition to massless vector bosons regime: $-g^2/16\pi^2 \log^2(E_{\text{cm}}^2/m_W^2) \times \text{Casimir} \approx 1$



Conclusions

The Standard Model Higgs Particle is very new!

- First direct manifestation of massive gauge theory formalism
- First elementary scalar particle
- We must test if it has SM properties, or not, as precisely as we can

Per-mille level Single-Higgs couplings:

- Possible at several future facilities, including a 10 TeV MuC
- Inform us on Extended Higgs sectors, Composite Higgs, and many other BSM

Learning more requires access to order 10 TeV energies

- The direct (and most effective) probe of Higgs compositeness
- The Higgs trilinear (and possibly 4-linear) coupling
- Searching for other Higgses/composite resonances
- Observing the restoration of the EW symmetry
- **Directly probe the SM description of short-distance EW force!**

Thank You

Backup

Single-Higgs couplings + Width

Could the Higgs decay to invisible or untagged BSM states?

Signal-strength measurements **do answer** this question:

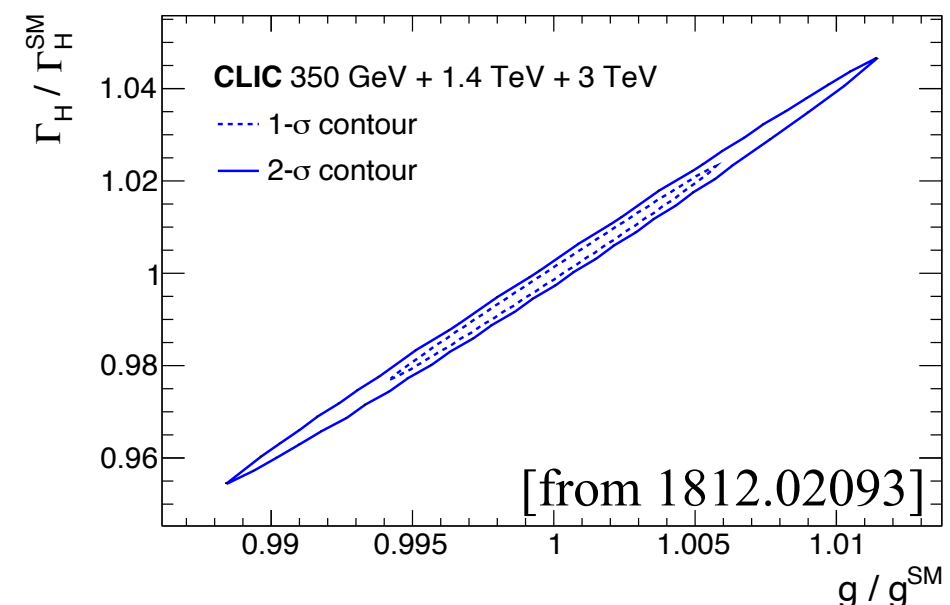
$$\sigma(i \rightarrow H \rightarrow j) \sim \frac{g_i^2 g_j^2}{\Gamma_H} \quad \rightarrow \quad \text{We probe } BR_{BSM} = \Gamma_{BSM}/\Gamma_H \text{ just as precisely as we probe } \delta\kappa, \text{ with the same measurements}$$

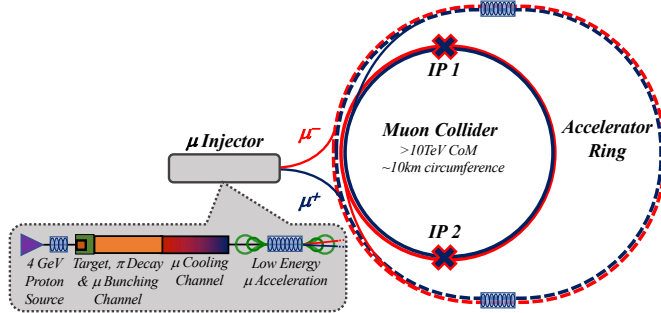
“Direct” searches for exotic or invisible Higgs decay, at e.g. FCC-hh are also possible and worthy.

There is a flat direction in the global fit to couplings+width

In a very tuned configuration
where all couplings conspire with Γ_{BSM}
Is not really very important to resolve
this degeneracy.

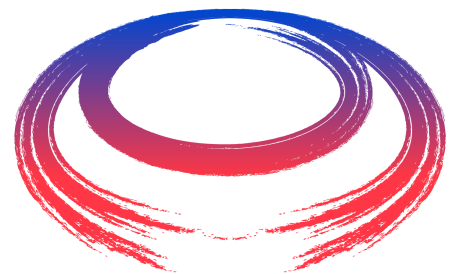
So, don't use the coupling+width fit
to rank Higgs factories.





Muon Colliders

muoncollider.web.cern.ch
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International
Muon Collider
Collaboration

MuC now part of European Roadmap for Accelerator R&D

International Muon Collider Collaboration working full steam

Also financed by European Union

Aim is establish maturity for CDR/Demonstrator program
after 2026 ESPPU

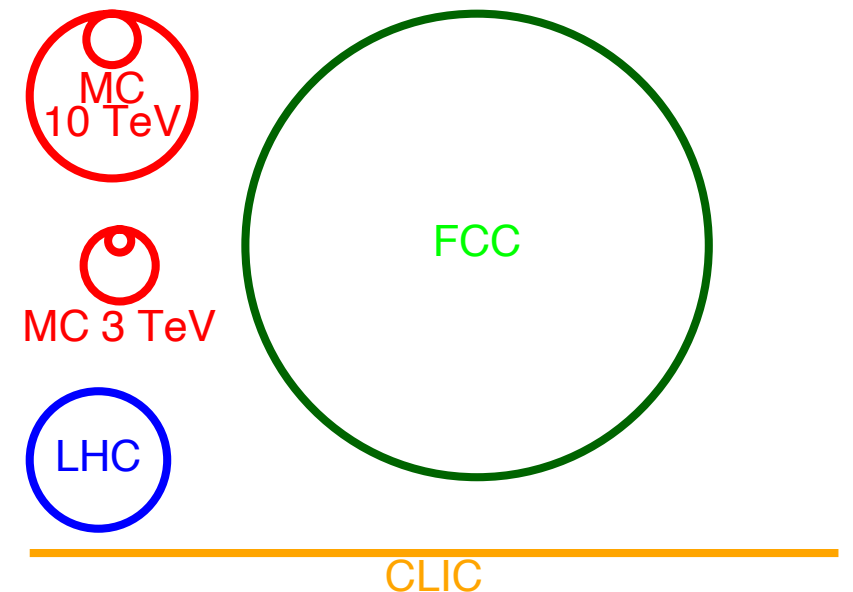
No showstopper identified

Might have technology ready in '30s and operation in '40s

Parameter	Symbol	Unit	Target value		
Centre-of-mass energy	E_{cm}	TeV	3	10	14
Luminosity	\mathcal{L}	$1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	1.8	20	40
Collider circumference	C_{coll}	km	4.5	10	14

$$5 \text{ yrs run, 1 IP: } \mathcal{L}_{\text{int}} = 10 \text{ ab}^{-1} \left(\frac{E_{\text{cm}}}{10 \text{ TeV}} \right)^2$$

Natural quadratic lumi scaling at MuC



The status of muon collider facility design, physics and detector, in this EPJC Review:

Towards a Muon Collider