

# **Probing top Yukawa coupling at the LHC via associated production of single top and Higgs**

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Higgs 2023

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Based on

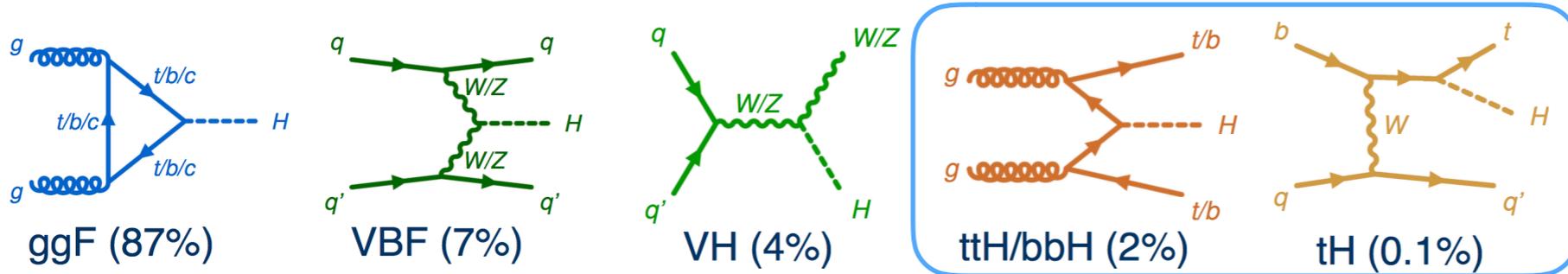
- [1] Vernon Barger, Kaoru Hagiwara, and YJZ, PRD99(2019)031701 [arXiv:1807.00281]
- [2] Vernon Barger, Kaoru Hagiwara, and YJZ, JHEP09(2020)101 [arXiv:1912.11795].
- [3] YJZ, work in progress

# Outline

- Top Higgs Yukawa couplings with CP violation
- Helicity amplitudes:  $ub > dth$  and  $\bar{d}b > \bar{u}th$  for  $pp > t+h+j$   
 $d\bar{b} > u\bar{t}h$  and  $\bar{u}\bar{b} > \bar{d}\bar{t}h$  for  $pp > \bar{t}+h+j$
- Single top/anti-top + Higgs event distributions
- Azimuthal asymmetry  $A_\varphi$  ( $\bar{A}_\varphi$ ) in  $pp > t+h+j$  ( $\bar{t}+h+j$ ) events
- Top (anti-top) polarisation  $P_2$  ( $\bar{P}_2$ ) in  $pp > t+h+j$  ( $\bar{t}+h+j$ ) events
- Summary

# LHC searches and Constraints

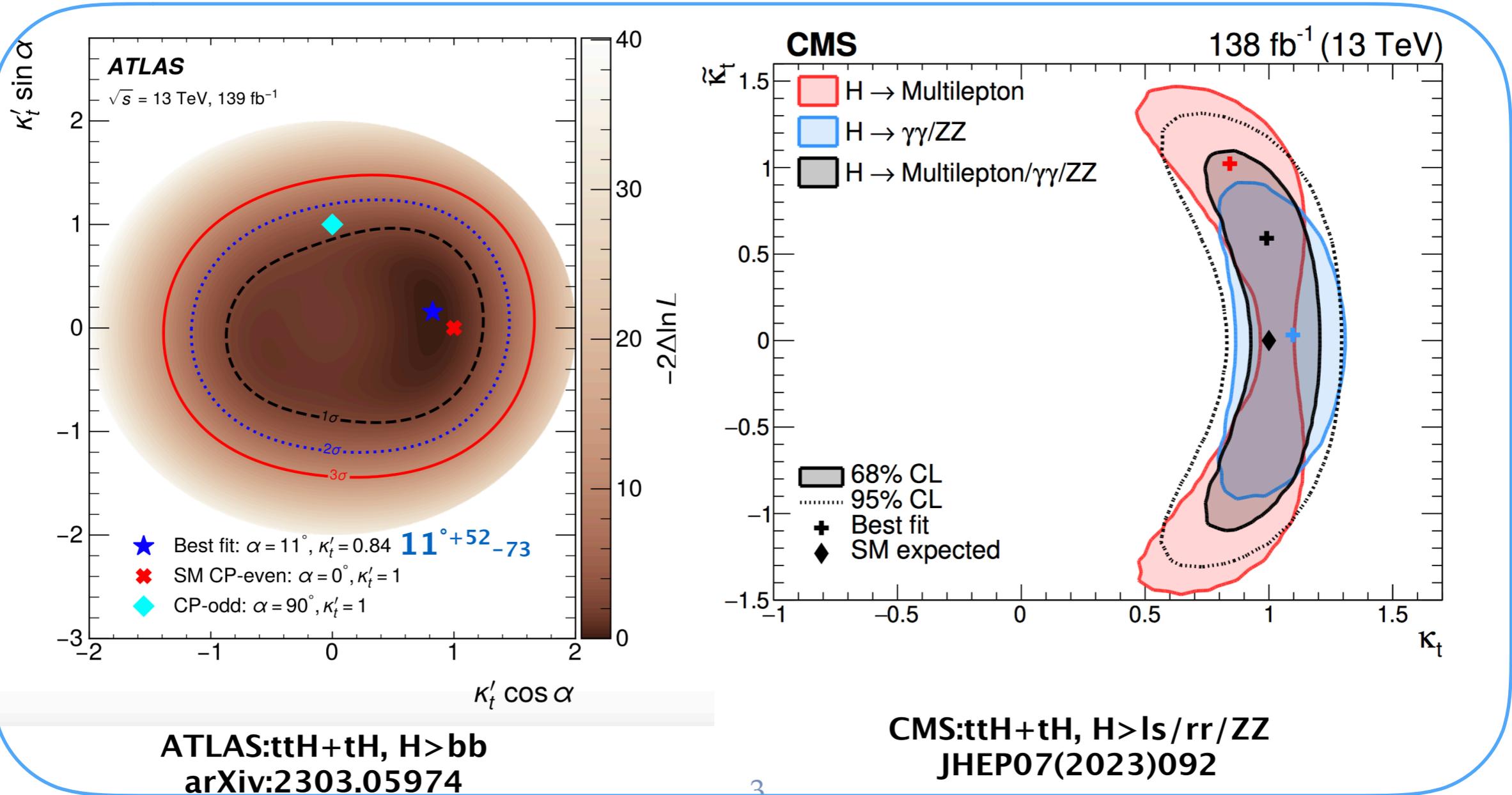
$$\mathcal{L}_{t\bar{t}H} = -\kappa'_t y_t \phi \bar{\psi}_t (\cos \alpha + i\gamma_5 \sin \alpha) \psi_t$$



Process	Cross section [fb]
$t\bar{t}H$	507 [53]
$tHq$	74.3 [53]
$tHW$	15.2 [87]
$ggH$	$4.86 \times 10^4$ [53]
$qqH$	$3.78 \times 10^3$ [53]
$WH$	$1.37 \times 10^3$ [53]
$ZH$	884 [53]

Hongtao Yang (USTC)

CMS:JHEP07(2023)092



ATLAS:ttH+tH, H>bb  
arXiv:2303.05974

CMS:ttH+tH, H>ls/rr/ZZ  
JHEP07(2023)092

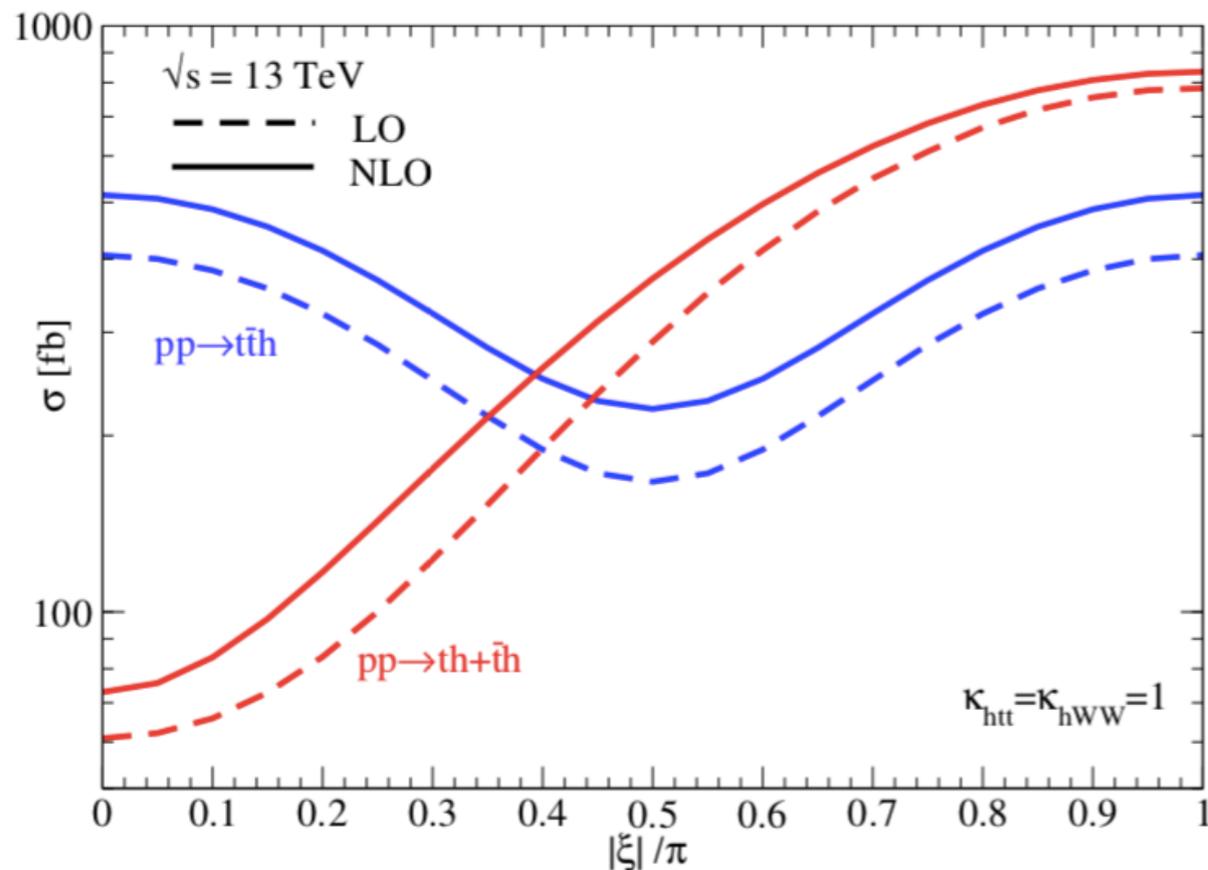
# Top Yukawa coupling

kappa framework

$$\begin{aligned} \mathcal{L} &= -g_{htt} h \bar{t} (\cos \xi_{htt} + i \sin \xi_{htt} \gamma_5) t \\ &= -g_{htt} h (t_R^\dagger, t_L^\dagger) \begin{pmatrix} e^{-i\xi_{htt}} & 0 \\ 0 & e^{i\xi_{htt}} \end{pmatrix} \begin{pmatrix} t_L \\ t_R \end{pmatrix} \\ &= -g_{htt} h (e^{-i\xi_{htt}} t_R^\dagger t_L + e^{i\xi_{htt}} t_L^\dagger t_R) \\ g_{htt} &= \frac{m_t}{v} \kappa_{htt}, \quad \kappa_{htt} > 0, \quad -\pi < \xi_{htt} \leq \pi \end{aligned}$$

Gauge invariant Lagrangian with dimension six operator in SMEFT:

$$\begin{aligned} \mathcal{L} &= -y_{SM} Q^\dagger \phi t_R + \frac{\lambda}{\Lambda^2} Q^\dagger \phi t_R \left( \phi^\dagger \phi - \frac{v^2}{2} \right) + \text{h.c.} \\ Q &= (t_L, b_L)^T \\ \phi &= ((v + H + i\pi^0)/\sqrt{2}, i\pi^-)^T \\ g_{SM} &= \frac{y_{SM}}{\sqrt{2}} = \frac{m_t}{v} \quad g_{SM} - g e^{i\xi} = \frac{\lambda v^2}{\sqrt{2} \Lambda^2} \end{aligned}$$



$$pp \rightarrow th + \bar{t}h + \text{anything}$$

$$\sigma_{tot}(|\xi_{htt}| = \pi) \sim \mathbf{13} \sigma_{tot}^{SM}(\xi_{htt} = 0)$$

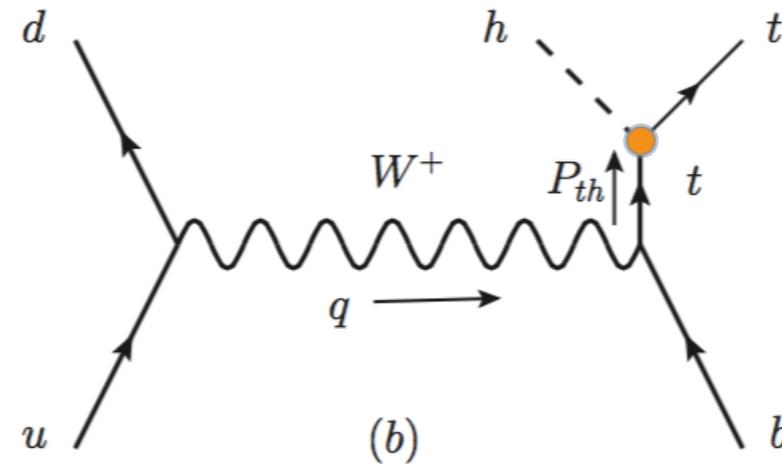
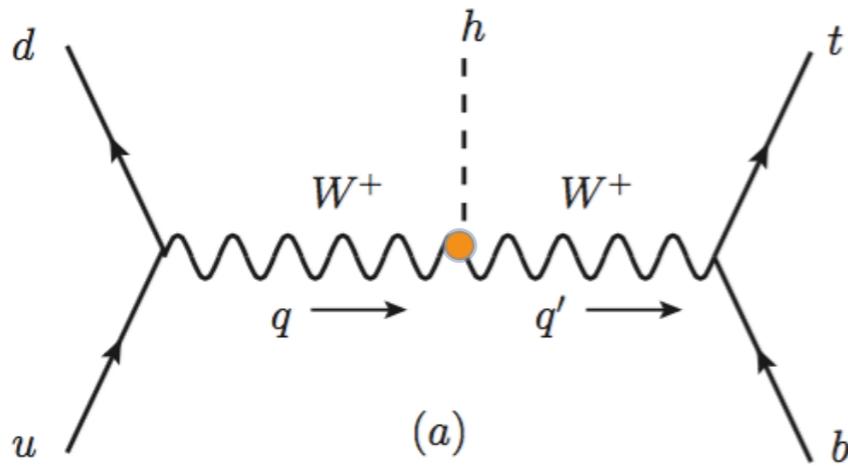
↑ change the sign of Yukawa coupling

In the SM, strong destructive interference between the htt and hWW amplitudes.

Preserving unitarity

W.Stirling, D.Summers, Phys.Lett.B283(1992)411-415  
 G.Bordes, B.van Eijk, Phys.Lett.B299(1993)315-320

# ub > dth amplitudes



$$M_\sigma \sim \boxed{u_L(p_d)^\dagger \sigma_-^\mu u_L(p_u) \frac{-g_{\mu\nu} + q_\mu q_\nu / m_W^2}{q^2 - m_W^2}}$$

common to both diagrams

$\bar{u}(p_t, \sigma)$

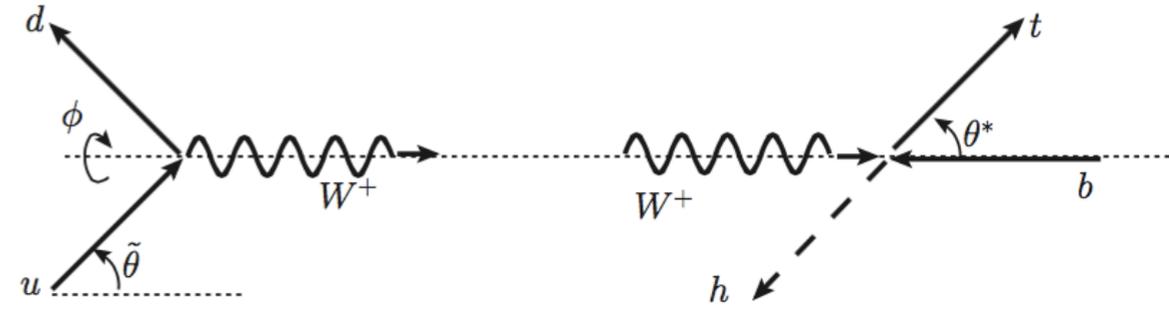
$$\left( \bar{u}_R^\dagger(p_t, \sigma), \bar{u}_L^\dagger(p_t, \sigma) \right) \left\{ \boxed{g_{hWW}} \frac{-g_\rho^\nu + q'^\nu q'_\rho / m_W^2}{q'^2 - m_W^2} \right. \\ \left. + \frac{\boxed{g_{htt}} \delta_\rho^\nu}{P_{th}^2 - m_t^2} \begin{pmatrix} e^{-i\xi} & 0 \\ 0 & e^{i\xi} \end{pmatrix} \begin{pmatrix} m & P_{th} \cdot \sigma_+ \\ P_{th} \cdot \sigma_- & m \end{pmatrix} \right\} \begin{pmatrix} 0 & \sigma_+^\rho \\ \sigma_-^\rho & 0 \end{pmatrix} \begin{pmatrix} u_L(p_b) \\ 0 \end{pmatrix}$$

$$\begin{matrix} \uparrow & \uparrow & \uparrow & \uparrow \\ \boxed{\cos \xi + i \sin \xi \gamma_5} & \boxed{P_{th} \cdot \gamma + m} & \boxed{\gamma^\rho} & \boxed{\frac{1 - \gamma_5}{2} u(p_b)} \end{matrix}$$

$$g_{hWW} = \frac{2m_W^2}{v} \kappa_{hWW} \quad (\kappa_{hWW} = 1)$$

# Amplitudes (full process $u b \rightarrow d t h$ )

$$M_\sigma = \sum_{\lambda=\pm 1,0} j(u \rightarrow dW_\lambda^+) \hat{M}(W_\lambda^+ b \rightarrow t_\sigma h)$$



$$M_+ = \frac{1 - \tilde{c}}{2} e^{i\phi} \sin \frac{\theta^*}{2} A \frac{1 + \cos \theta^*}{2}$$

$$+ \frac{1 + \tilde{c}}{2} e^{-i\phi} \sin \frac{\theta^*}{2} \left[ A \left( \frac{1 + \cos \theta^*}{2} + \epsilon_1 \right) - B (e^{-i\xi} + \delta\delta' e^{i\xi}) \right]$$

$$+ \frac{\tilde{s}}{2} \cos \frac{\theta^*}{2} \frac{W}{Q} \left[ A \left( \frac{q^* E_h^* + q^{0*} p^* \cos \theta^*}{W p^*} + \epsilon_1 \right) - B (e^{-i\xi} + \delta\delta' e^{i\xi}) \right]$$

$$M_- = - \frac{1 - \tilde{c}}{2} e^{i\phi} \cos \frac{\theta^*}{2} A \delta \frac{1 - \cos \theta^*}{2}$$

$$- \frac{1 + \tilde{c}}{2} e^{-i\phi} \cos \frac{\theta^*}{2} \left[ A \left( \delta \frac{1 - \cos \theta^*}{2} - \epsilon_2 \right) + B (\delta e^{-i\xi} + \delta' e^{i\xi}) \right]$$

$$- \frac{\tilde{s}}{2} \sin \frac{\theta^*}{2} \frac{W}{Q} \left[ A \left( \delta \frac{q^* E_h^* + q^{0*} p^* \cos \theta^*}{W p^*} + \epsilon_2 \right) - B (\delta e^{-i\xi} + \delta' e^{i\xi}) \right]$$

←  $\lambda=+1$   
 $J_z=3/2$

←  $\lambda=-1$   
 $J_z=-1/2$

←  $\lambda=0$   
 $J_z=1/2$

←  $\lambda=+1$   
 $J_z=3/2$

←  $\lambda=-1$   
 $J_z=-1/2$

←  $\lambda=0$   
 $J_z=1/2$

$$A = 2g^2 \underline{D_W}(q) \tilde{\omega} \sqrt{2q^*(E^* + p^*)} \frac{mp^*}{m_W^2} \underline{g_{hWW}} \underline{D_W}(q'), > 0$$

$$B = -2g^2 \underline{D_W}(q) \tilde{\omega} \sqrt{2q^*(E^* + p^*)} W \underline{g_{htt}} \underline{D_t}(P_{th}), > 0$$

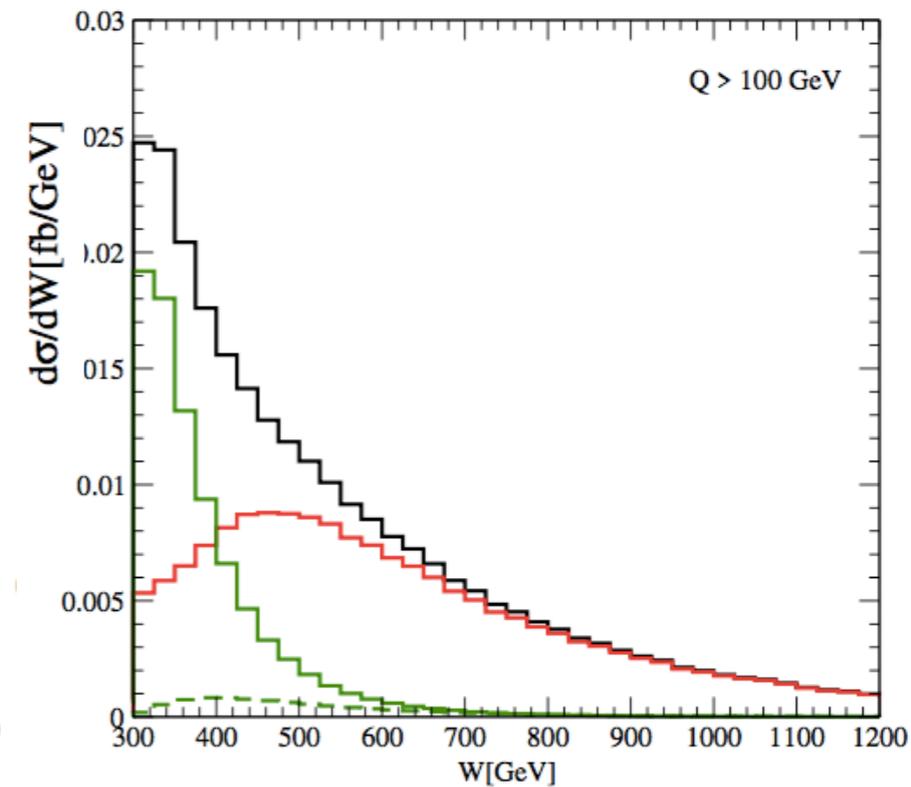
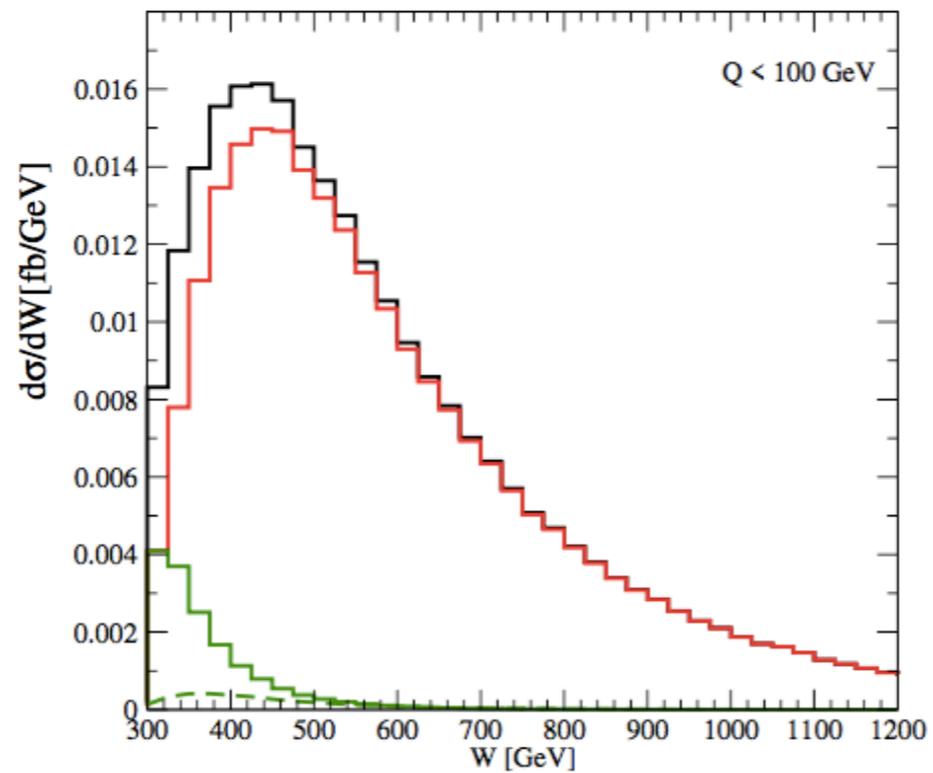
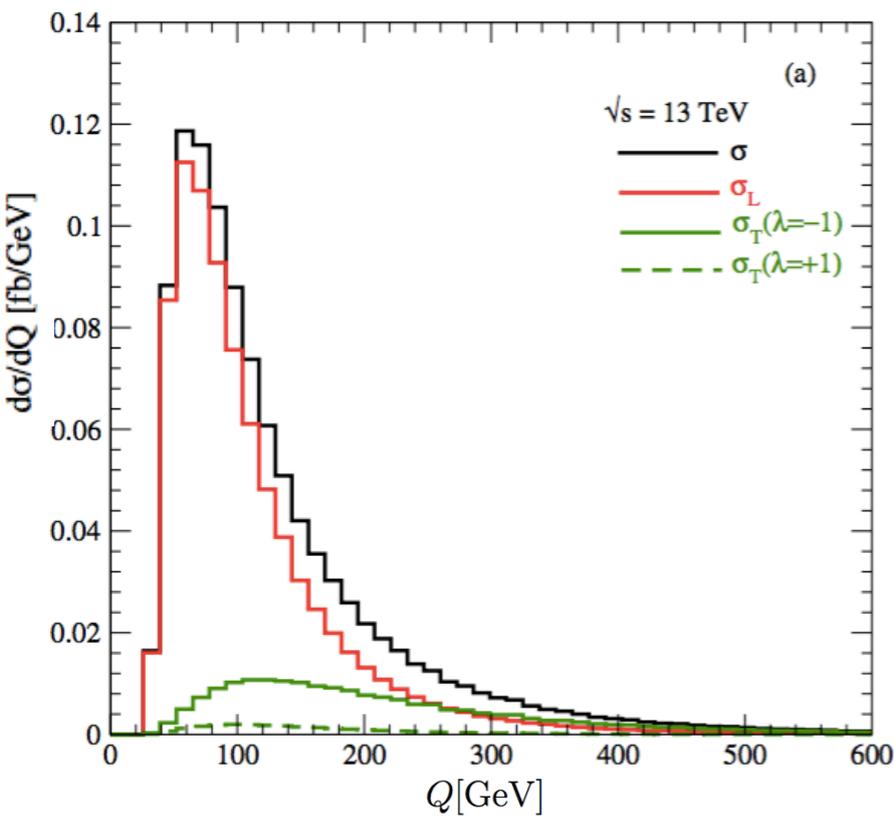
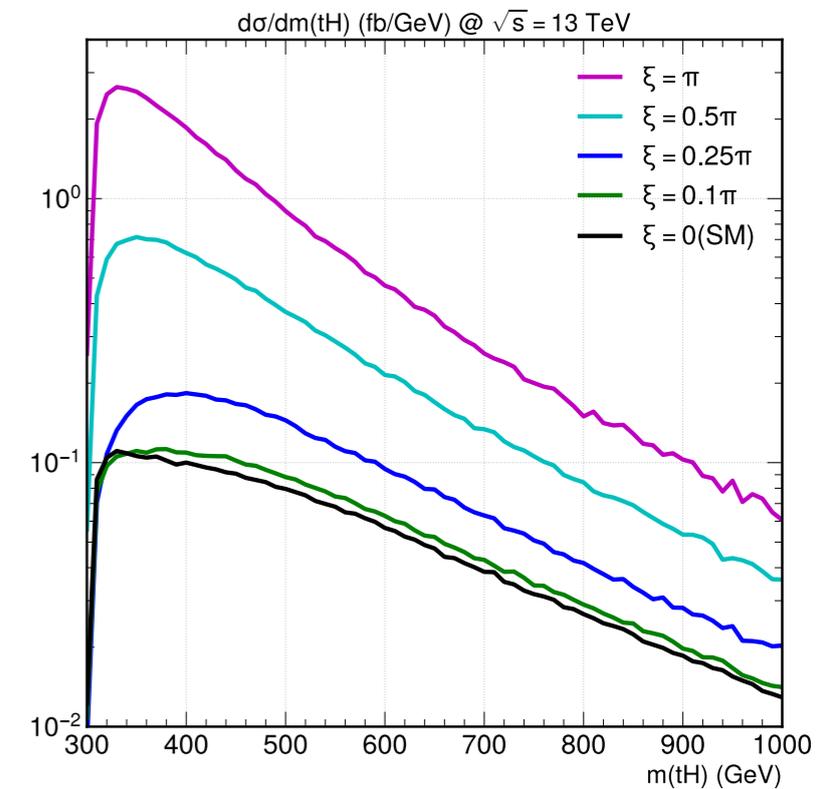
$$\delta = m_t / (E^* + p^*)$$

$$\delta' = m_t / W$$

→  $\delta \sim \delta'$   
at high energy  
high W ( $W=m_{th}$ )

# Q and W distribution

$Q = \sqrt{-q^2}$  invariant momentum transfer of the virtual  $W^+$   
 $W = \sqrt{P_{th}^2} = m(th)$  the invariant mass of the  $th$  system



$W_L$  is dominant in low  $Q$  ( $Q < 100$  GeV) and large  $W$  ( $W > 400$  GeV)

$W_T$  is significant in large  $Q$  ( $Q > 100$  GeV) and small  $W$  ( $W < 400$  GeV)

# Azimuthal angle distribution

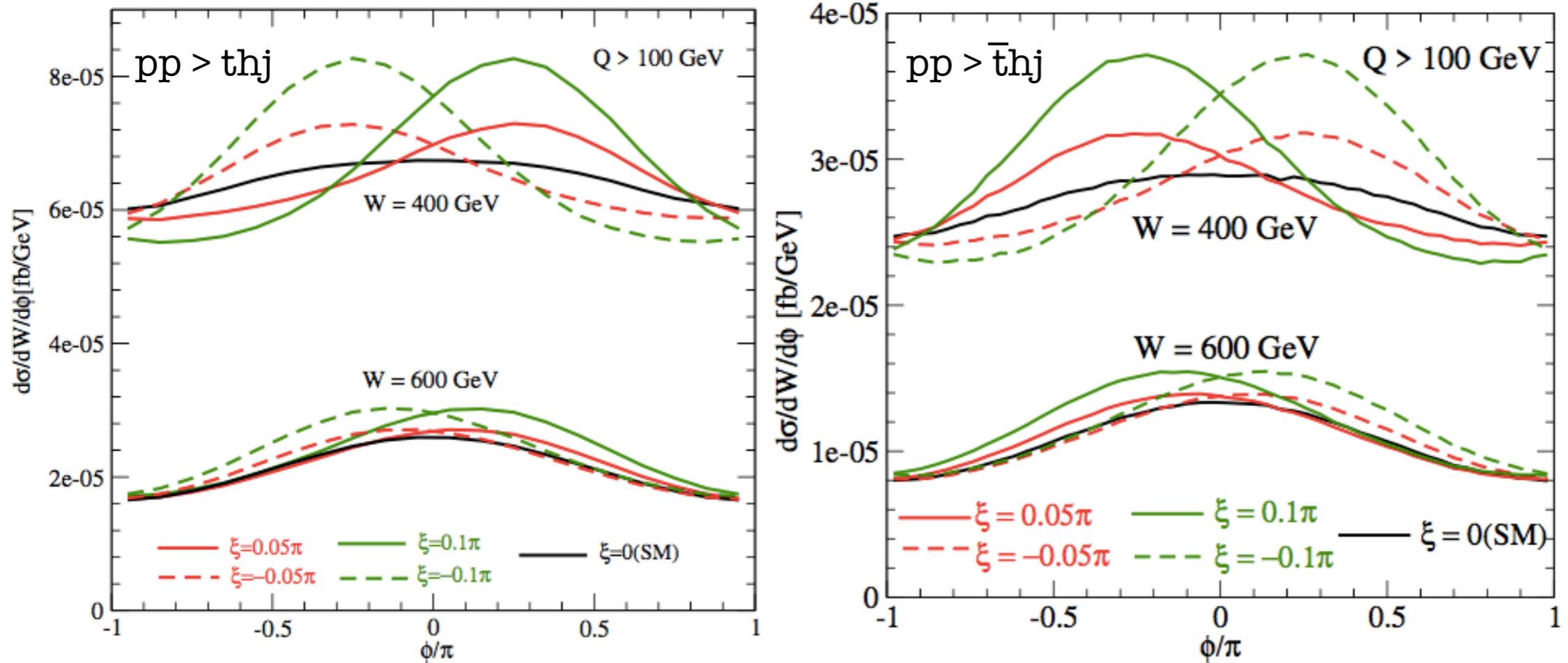
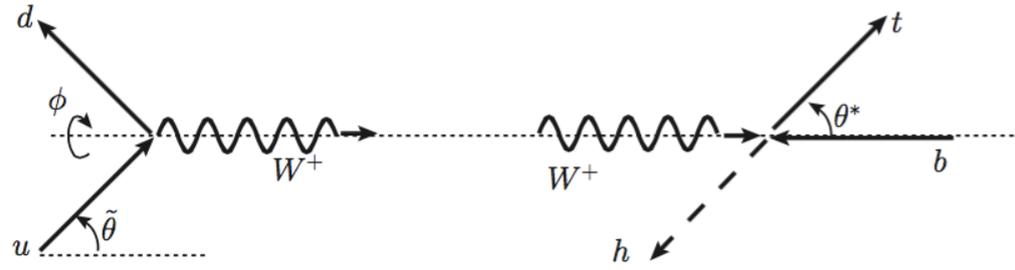


FIG. 8: Left panel:  $t$ . Right panel:  $\bar{t}$ .  $d\sigma/dW/d\phi$  v.s.  $\phi$  at  $W = 400$  and  $600$  GeV for  $Q > 100$  GeV. Black, red and green curves are for the SM ( $\xi = 0$ ),  $\xi = \pm 0.1\pi$ , and  $\pm 0.2\pi$ . The solid curves are for  $\xi \geq 0$ , while the dashed curves are for  $\xi < 0$ .

asymmetry

$$A_\phi(W) = \frac{\int_{-\pi}^{\pi} d\phi \operatorname{sgn}(\phi) d\sigma/dW/d\phi}{d\sigma/dW}$$

$> 0$  ( $th$ ) and  $< 0$  ( $\bar{t}h$ ) for  $\xi > 0$   
 $< 0$  ( $th$ ) and  $> 0$  ( $\bar{t}h$ ) for  $\xi < 0$

Asymmetry is large at small  $W$  & large  $Q$  ( $W_T$  is comparable to  $W_L$ )  
 small at large  $W$  & small  $Q$  ( $W_L$  dominates over  $W_T$ )

# Azimuthal asymmetry $A_\phi$

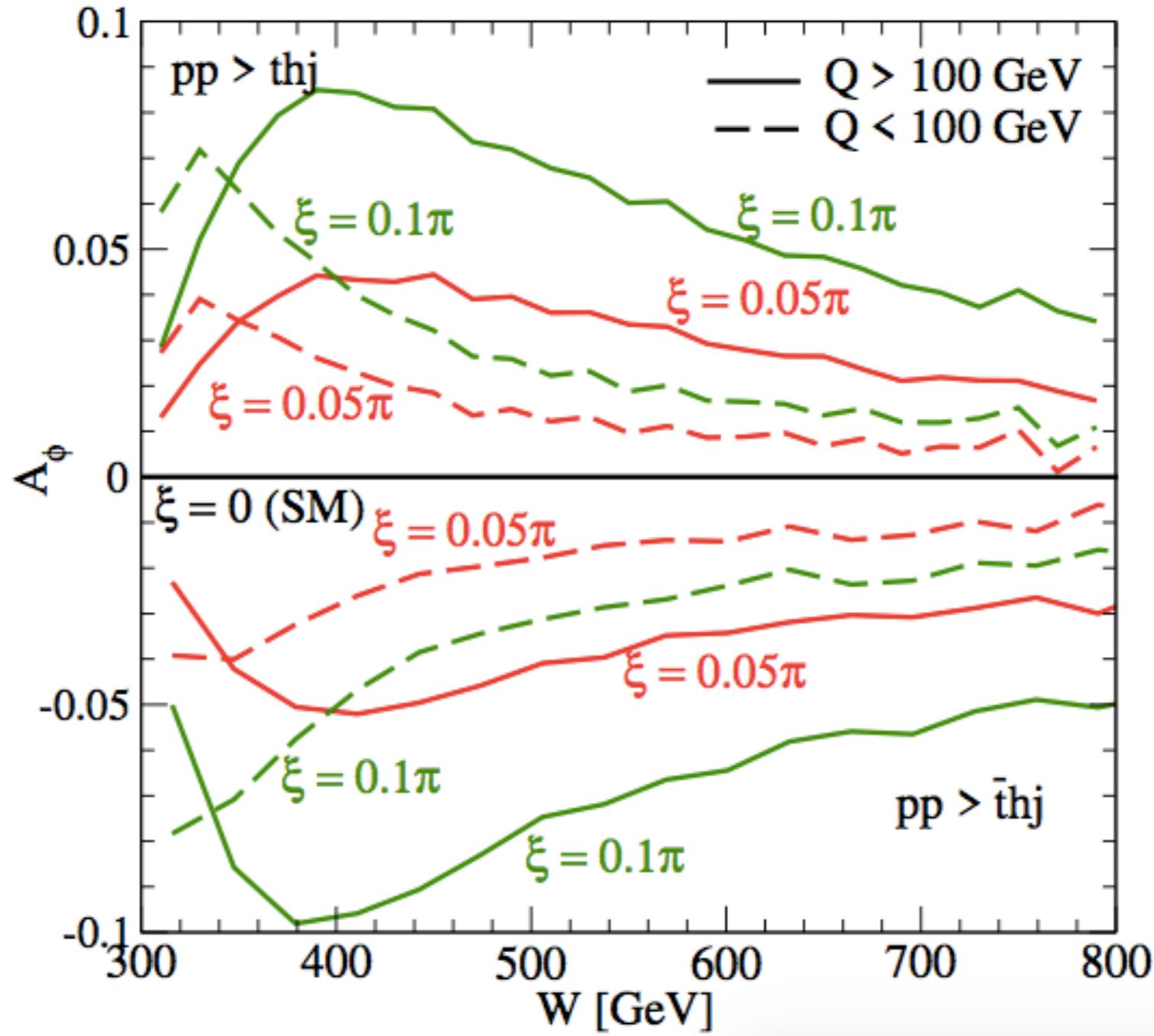


FIG. 11: Asymmetry  $A_\phi(W)$  for  $pp \rightarrow thj$  and  $pp \rightarrow \bar{t}hj$  as functions of  $W$ , the invariant mass of  $th$  or  $\bar{t}h$  system. Large  $Q$  ( $Q > 100$  GeV) events are shown by solid lines, while small  $Q$  ( $Q < 100$ ) GeV, events are shown by dashed curves. Results are shown for  $\xi = 0$  (SM),  $\xi = 0.05\pi$  (red) and  $0.1\pi$  (green).  $A_\phi > 0$  for  $th$  and  $A_\phi < 0$  for  $\bar{t}h$ , when  $\xi > 0$ .

# $|\mathcal{M}_+(\text{ub} \rightarrow \text{dth})|^2$ v.s. $|\overline{\mathcal{M}}_-(\text{d}\overline{\text{b}} \rightarrow \text{u}\overline{\text{t}}\text{h})|^2$

$$\begin{aligned}
 \mathcal{M}_+ &= \frac{1 - \tilde{c}}{2} e^{i\phi} \sin \frac{\theta^*}{2} \left[ \frac{1 + \cos \theta^*}{4} \bar{\beta} A \right] && J_z=3/2 \\
 &&& \lambda=+1 \\
 &+ \frac{1 + \tilde{c}}{2} e^{-i\phi} \sin \frac{\theta^*}{2} \left[ \left( \frac{1 + \cos \theta^*}{4} \bar{\beta} + \epsilon \delta \delta' \right) A - (e^{-i\xi} + \delta \delta' e^{i\xi}) B \right] && J_z=-1/2 \\
 &&& \lambda=-1 \\
 &+ \frac{\tilde{s}}{2} \frac{W}{Q} \cos \frac{\theta^*}{2} \left[ \left( \frac{q^* E_h^* + q^{0*} p^* \cos \theta^*}{W^2} + \epsilon \delta \delta' \right) A - (e^{-i\xi} + \delta \delta' e^{i\xi}) B \right] && J_z=1/2 \\
 &&& \lambda=0
 \end{aligned}$$

$$\begin{aligned}
 \overline{\mathcal{M}}_- &= \frac{1 - \tilde{c}}{2} e^{i\phi} \sin \frac{\theta^*}{2} \left[ \left( \frac{1 + \cos \theta^*}{4} \bar{\beta} + \epsilon \delta \delta' \right) A - (e^{i\xi} + \delta \delta' e^{-i\xi}) B \right] && J_z=1/2 \\
 &&& \lambda=+1 \\
 &+ \frac{1 + \tilde{c}}{2} e^{-i\phi} \sin \frac{\theta^*}{2} \frac{1 + \cos \theta^*}{4} \bar{\beta} A && J_z=-3/2 \\
 &&& \lambda=-1 \\
 &+ \frac{\tilde{s}}{2} \frac{W}{Q} \cos \frac{\theta^*}{2} \left[ \left( \frac{q^* E_h^* + q^{0*} p^* \cos \theta^*}{W^2} + \epsilon \delta \delta' \right) A - (e^{i\xi} + \delta \delta' e^{-i\xi}) B \right] && J_z=1/2 \\
 &&& \lambda=0
 \end{aligned}$$

# Top Polarization (mixed state)

For general mixed state, we introduce differential cross section matrix

$$d\sigma_{\lambda\lambda'} = \int dx_1 \int dx_2 D_{u/p}(x_1) D_{b/p}(x_2) \frac{1}{2\hat{s}} \overline{\sum} M_{\lambda} M_{\lambda'}^* d\Phi_{dth}$$

where the phase space integration can be restricted. For an arbitrary kinematical distributions,  $d\sigma = d\sigma_{++} + d\sigma_{--}$ , the polarisation density matrix is defined as

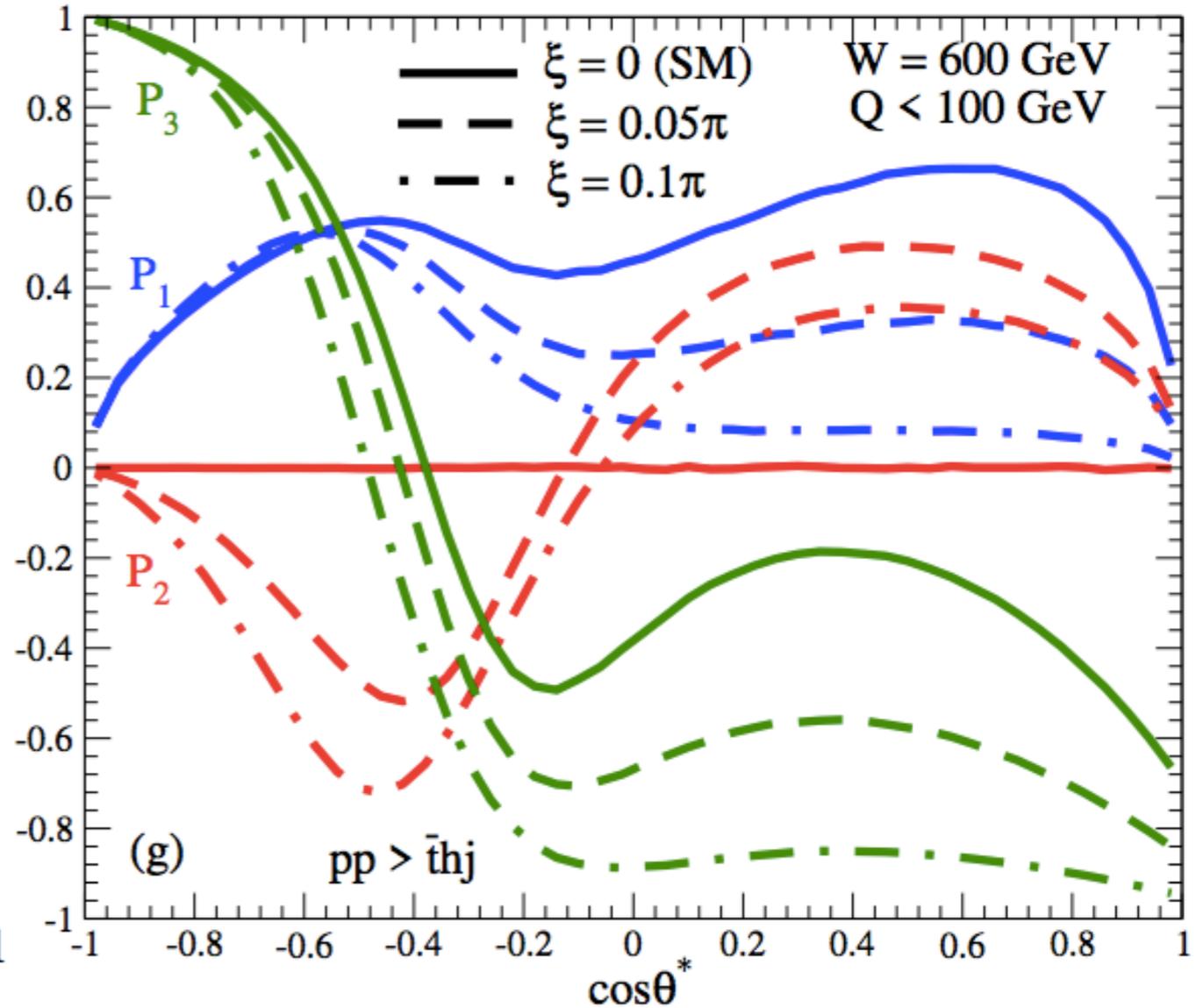
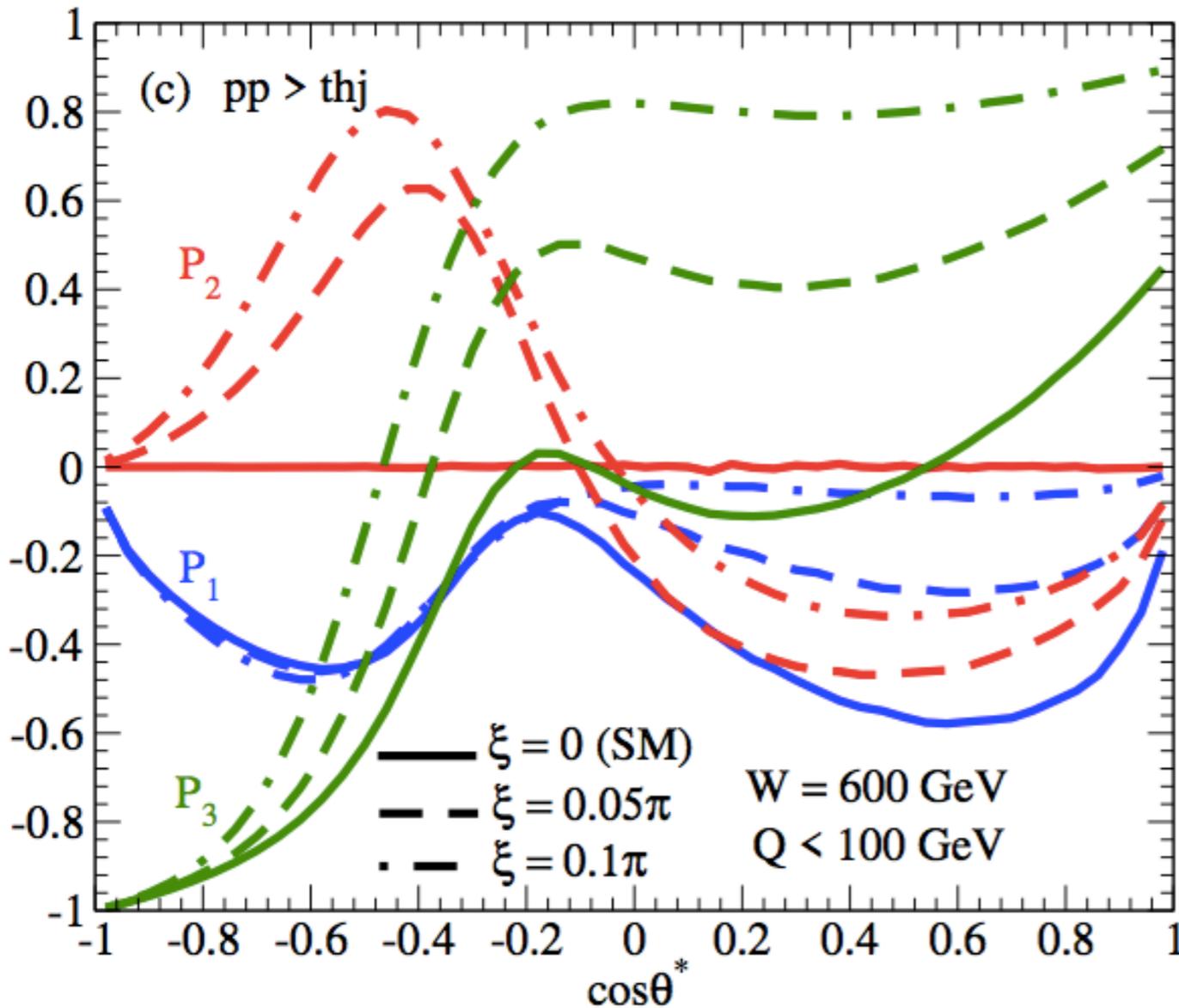
$$\rho_{\lambda\lambda'} = \frac{d\sigma_{\lambda\lambda'}}{d\sigma_{++} + d\sigma_{--}} = \frac{1}{2} \left[ \delta_{\lambda\lambda'} + \sum_{k=1}^3 P_k \sigma_{\lambda\lambda'}^k \right]$$

The 3-vector  $\mathbf{P} = (P_1, P_2, P_3)$  gives the general polarisation of the top quark. The magnitude  $P = |\mathbf{P}|$  gives the degree of polarisation ( $P=1$  for 100% polarization,  $P=0$  for no polarisation). The orientation gives the direction of the top quark spin in the top rest frame.

$$P_2 = -2\text{Im}(M_+ M_-^*) / (|M_+|^2 + |M_-|^2)$$

We find  $\mathbf{P}$  lies in the  $W+b \rightarrow th$  scattering plane in the SM ( $\xi_i=0$ ). Polarisation orthogonal to the production plane  $P_2$  appears for nonzero  $\xi_i$ . The sign of  $P_2$  determines the sign of  $\xi_i$ .

# Top Polarization and anti-top polarisation $\mathbf{P} = (P_1, P_2, P_3)$



We find large  $|P_2|$  when  $\cos\theta^* < 0$ , positive for  $t$  and negative for  $tbar$ . We therefore examine  $P_2$  for events with  $\cos\theta^* < 0$  in the next slides.

# Polarization $P_2$ of top and anti-top

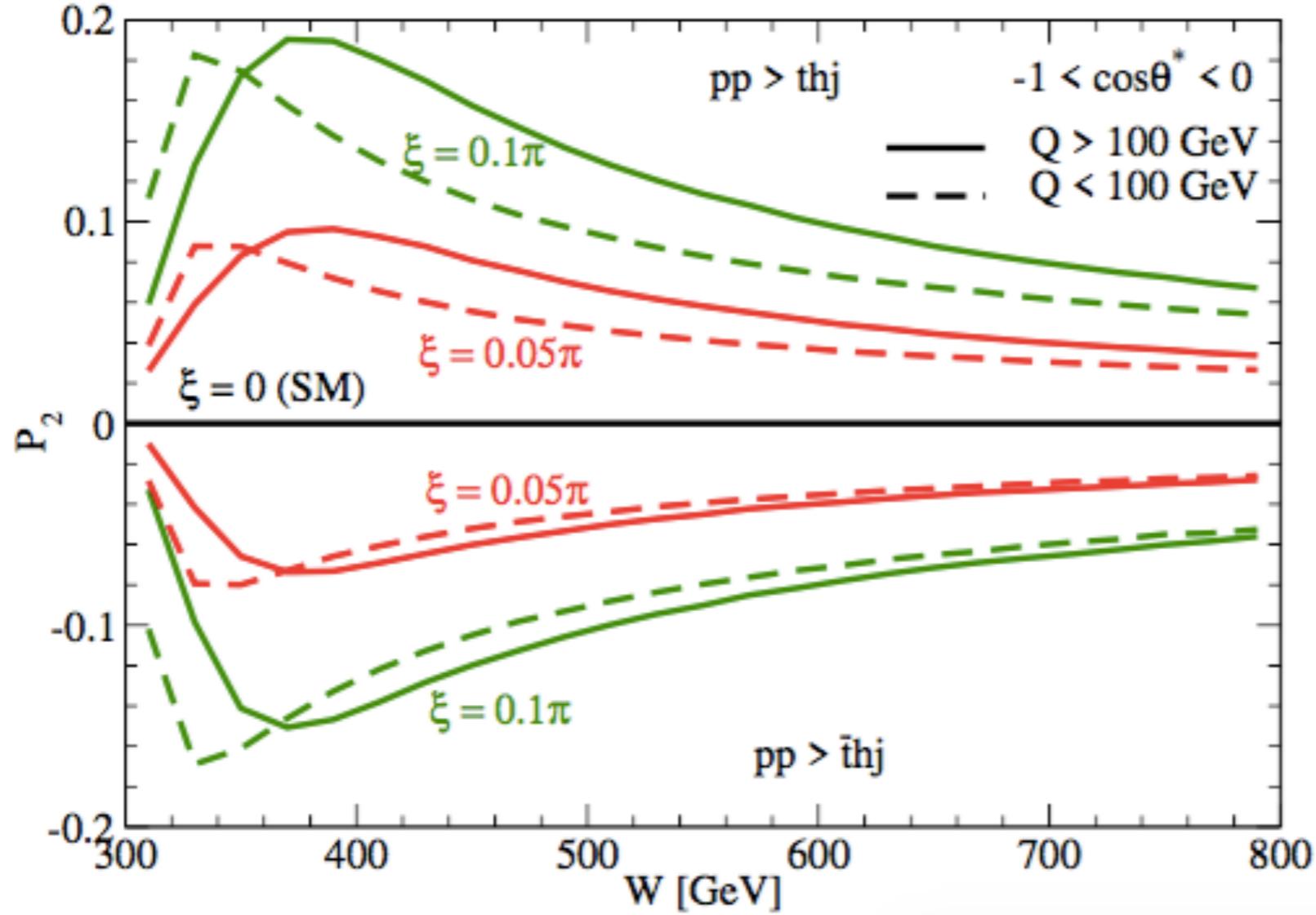
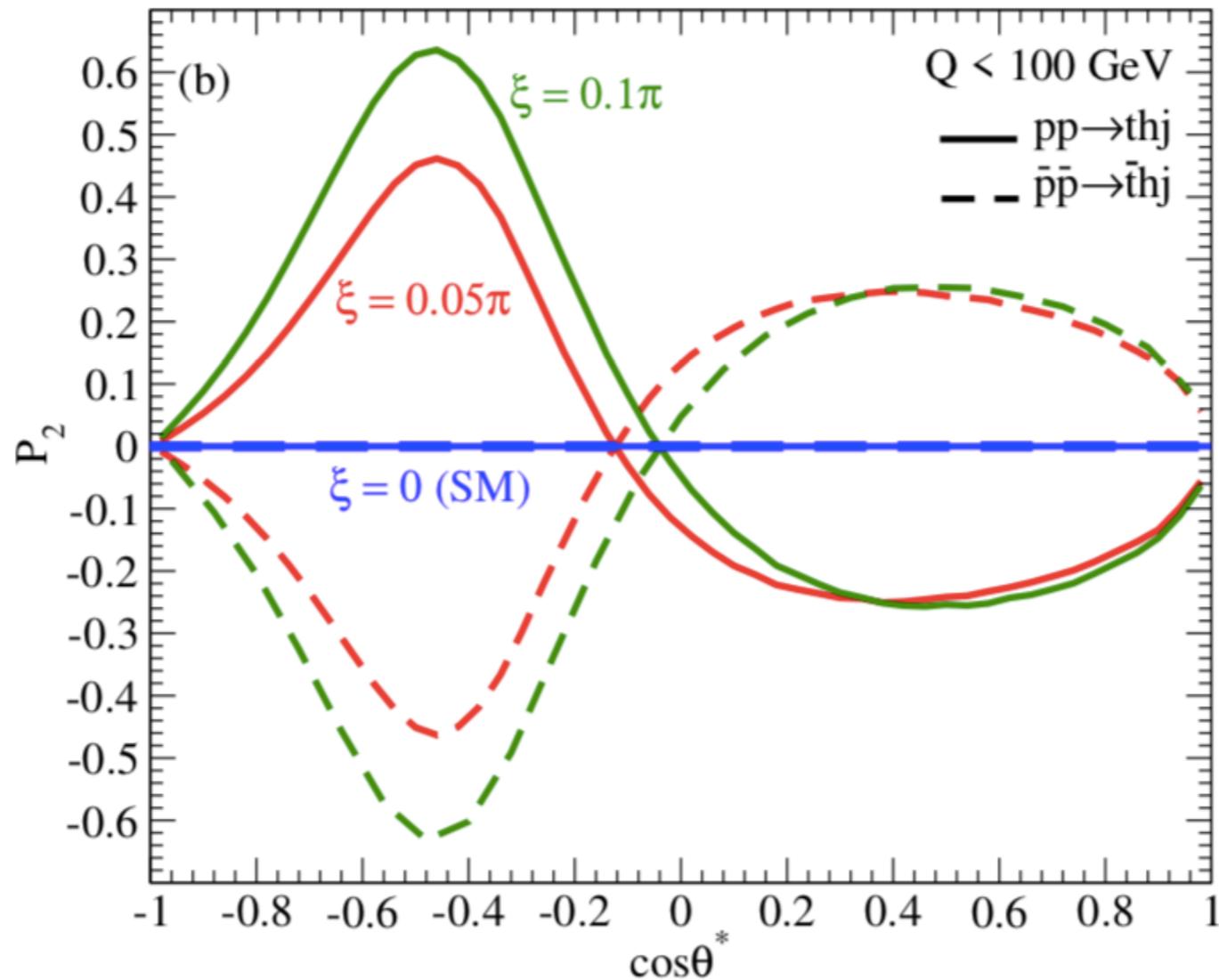


FIG. 15:  $P_2$  v.s.  $W$  for  $pp \rightarrow thj$  (a) and  $pp \rightarrow \bar{t}hj$  (b) in the region  $-1 < \cos\theta^* < 0$ . The green curves are for  $\xi = 0.1\pi$ , while the red curves are for  $\xi = 0.05\pi$ . The solid curves are for  $Q > 100$  GeV, while the dashed curves are for  $Q < 100$  GeV.



$$pp \rightarrow thj \quad (ub \rightarrow dth) \quad \longleftrightarrow \text{CP} \quad \longleftrightarrow \quad \bar{p}\bar{p} \rightarrow \bar{t}h j \quad (\bar{u}\bar{b} \rightarrow \bar{d}\bar{t}h)$$

In  $thj$  and  $\bar{t}h j$  production at the LHC, longitudinal contributions ( $W^\pm(\lambda=0)$ ) dominate.

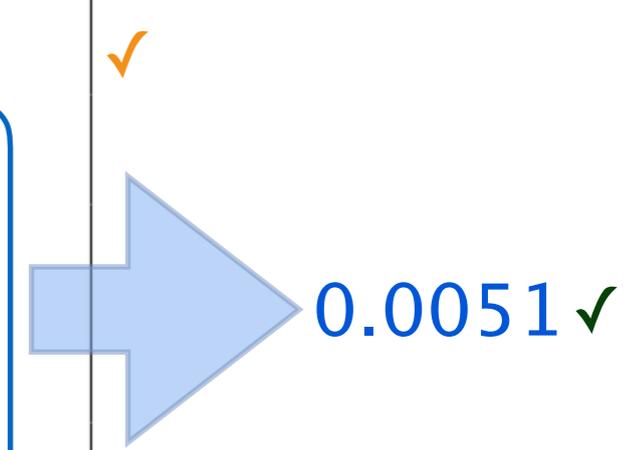
$$W^+(\lambda = 0) + b \rightarrow t + h \quad \longleftrightarrow \text{CP} \quad \longleftrightarrow \quad W^-(\lambda = 0) + \bar{b} \rightarrow \bar{t} + h$$

# Expected number of events @ HL-LHC

	$\sqrt{s}$ 14 TeV	Number of events @ $3ab^{-1}$	Decay channel	Branching Ratio	Number of events	
$\sigma(th)+\sigma(\bar{t}h)$	90 fb	270,000	$(bl\nu)(b\bar{b})$	0.13	34,000	✓✓
			$(bl\nu)(\gamma\gamma, \ell\ell jj, \mu\mu, 4\ell)$	0.0011	300	✓✓
$\sigma(t\bar{t}h)$	613 fb	1,840,000	$(bl\nu)(bjj)(b\bar{b})$	0.17	310,000	✓✓✓
			$(bl\nu)^2(b\bar{b})$	0.028	52,000	✓✓✓
			$(bl\nu)(bjj)(\gamma\gamma, \ell\ell jj, \mu\mu, 4\ell)$	0.0015	2,800	✓✓✓
			$(bl\nu)^2(\gamma\gamma, \ell\ell jj, \mu\mu, 4\ell)$	0.00025	460	✓✓✓

- $t > bl\nu$  mode for CP sensitivity (t vs.  $\bar{t}$ )
- h decay should not have neutrinos to determine  $t(\bar{t})$  frame.

	Decay channel	Branching ratio		Decay channel	Branching Ratio
$t \rightarrow$	$bjj$	0.67	$h \rightarrow$	$b\bar{b}$	0.58
	$bl\nu(\ell = e, \mu)$ ✓	0.22		$\ell\bar{\ell}jj$	0.0025
	$b\tau\nu$ ✓	0.11		$\gamma\gamma$	0.0023
				$\mu\bar{\mu}$	0.00022
				$4\ell$	0.00012



- For a few percent asymmetry measurement,  $h > bb$  is necessary

# Summary

- Single top+Higgs production is an ideal probe of the top Yukawa coupling because the htt and hWW amplitudes interfere strongly.

- Azimuthal asymmetry between the  $u \rightarrow dW^+$  emission and the  $W^+b \rightarrow th$  production planes probes the sign of CP violating phase.

$$A_\phi \sim \int_0^\pi (|M_+|^2 + |M_-|^2) d\phi - \int_{-\pi}^0 (|M_+|^2 + |M_-|^2) d\phi \propto \sin \xi_{htt}$$

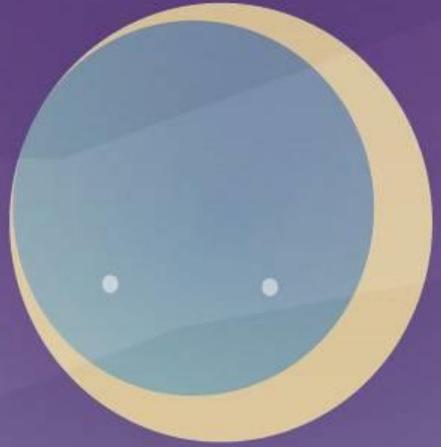
- Polarization can be measured by using the density matrix.

$$\rho_{\lambda\lambda'} = \frac{1}{\int (|M_+|^2 + |M_-|^2) d\Phi} \int \begin{pmatrix} |M_+|^2 & M_+ M_-^* \\ M_- M_+^* & |M_-|^2 \end{pmatrix} d\Phi = \frac{1}{2} \left[ \delta_{\lambda\lambda'} + \sum_{k=1}^3 P_k \sigma_{\lambda\lambda'}^k \right]$$

- Polarization perpendicular to the scattering plane measures the relative phase between the two helicity amplitudes

$$P_2 = \frac{-2\text{Im}(M_+ M_-^*)}{|M_+|^2 + |M_-|^2} \propto \sin \xi_{htt}$$

- We find significant asymmetry reaching  $A_\phi \sim +8\%$ (th),  $-10\%$ ( $\bar{\text{th}}$ ), whereas  $P_2 \sim +18\%$  (th),  $-15\%$  (th) for  $\xi = 0.1\pi$ . All the asymmetries change sign if  $\xi$  is negative.



**IWATE COLLIDER SCHOOL**  
**2024**

**26 FEBRUARY - 2 MARCH, 2024**

Appi highland, Iwate, Japan

## Registration fee

FREE and local expenses will be supported.  
(No support for travel fees.)

## Eligibility

Mainly for graduate students and postdoc fellows  
(Max. 25 participants in person )

## Venue

ANA Crowne Plaza Resort Appi Kogen

## Application submission deadline

8 December, 2023

## Website

<https://ics.sgk.iwate-u.ac.jp/>



## Contact

ics2024@iwate-u.ac.jp

## Overview

Students will learn a variety of topics in collider physics via lectures and tutorials. Long lunch break for skiing and discussions are planned.

### Lecturers:

Celine Degrande (Louvain, Belgium)  
Rikkert Frederix (Lund, Sweden)  
Fabio Maltoni (Louvain, Belgium)  
Olivier Mattelaer (Louvain, Belgium)  
Marco Zaro (Milan, Italy) etc.

### Organizers:

Kaoru Hagiwara (KEK)  
Daniel Jeans (KEK)  
Fabio Maltoni (UC Louvain / Bologna)  
Kentarou Mawatari (Chair, Iwate U.)  
Shinya Narita (Iwate U.)  
Yajuan Zheng (Iwate U.)