



# Determination of CPV Higgs mixing angle in ZZ-fusion at 1 TeV ILC

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*on behalf of the ILD Detector Concept Group*



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## OPENING QUESTIONS/OUTLINE

1. Could 125 GeV Higgs mass eigenstate be a CPV mixture of CP-odd and CP-even states via mixing angle  $\Psi_{\text{CP}}$ ?
2. If so, with what precision  $\Psi_{\text{CP}}$  can be measured at 1 TeV ILC ?
3. What is the interpretation of the measurement sensitivity (in the context of Snowmass CPV White paper [\[arXiv:2205.07715v3\]](https://arxiv.org/abs/2205.07715v3))?

## SENSITIVE OBSERVABLE

- Generic model of CPV mixing:  $h_{125} = H \cdot \cos \Psi_{CP} + A \cdot \sin \Psi_{CP}$
- CP-sensitive observable: angle between production planes  $\Delta\phi$
- As shown in [\[arXiv:2203.11707v3\]](https://arxiv.org/abs/2203.11707v3)  $\Delta\Phi$  carries the most information on the Higgs CP state

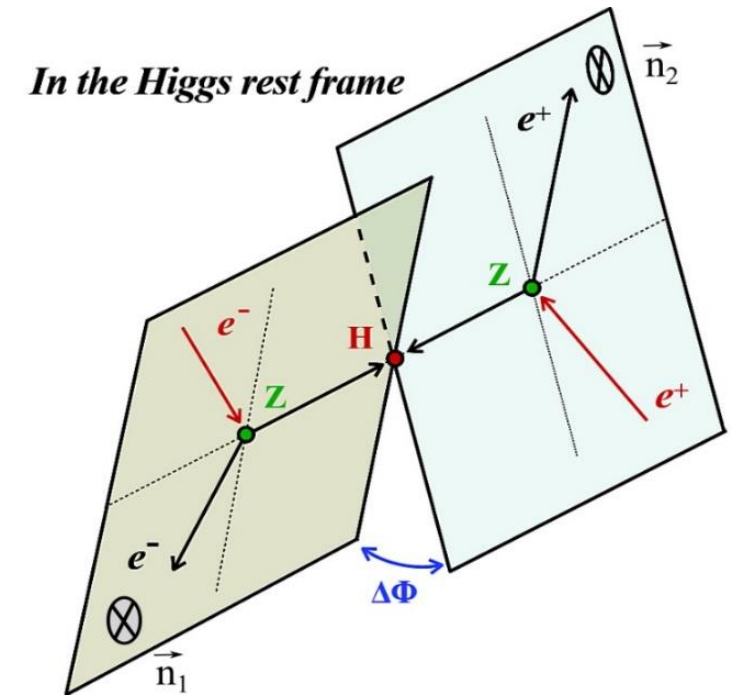
$$\Delta\Phi = \begin{cases} \arccos(\cos \Delta\Phi), & \text{sgn}(\sin \Phi) \geq 0 \\ 2\pi - \arccos(\cos \Delta\Phi), & \text{sgn}(\sin \Phi) < 0 \end{cases}$$

$$\cos \Phi = (\hat{n}_1 \cdot \hat{n}_2)$$

$$\text{sgn}(\sin \Phi) = \frac{q_1 \cdot (\hat{n}_1 \times \hat{n}_2)}{|q_1 \cdot (\hat{n}_1 \times \hat{n}_2)|}$$

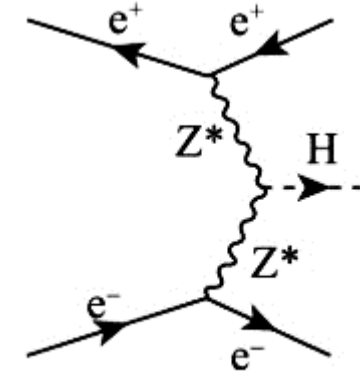
$$\hat{n}_1 = \frac{q_{e_i^-} \times q_{e_f^-}}{|q_{e_i^-} \times q_{e_f^-}|}$$

$$\hat{n}_2 = \frac{q_{e_i^+} \times q_{e_f^+}}{|q_{e_i^+} \times q_{e_f^+}|}$$



# SIGNAL AND BACKGROUND

1 TeV	$\sigma$ (fb)	Expected in 8 ab <sup>-1</sup> full range	Reconstructed with ILD
<b>Signal:</b>			
$e^+e^- \rightarrow H e e, H \rightarrow b\bar{b}$	13	104000	2·10 <sup>5</sup> DELPHES~36.6 ab <sup>-1</sup> 3495 full sim. ~0.22 ab <sup>-1</sup>
$e^+e^- \rightarrow q\bar{q}l^+l^-$	255	2·10 <sup>6</sup>	1·10 <sup>6</sup> DELPHES 5886 full sim.
$e^+e^- \rightarrow q\bar{q}$	9375	75·10 <sup>6</sup>	120343 full sim.
$e^+e^- \rightarrow q\bar{q}lv$	4116	32.9·10 <sup>6</sup>	955058 full sim.



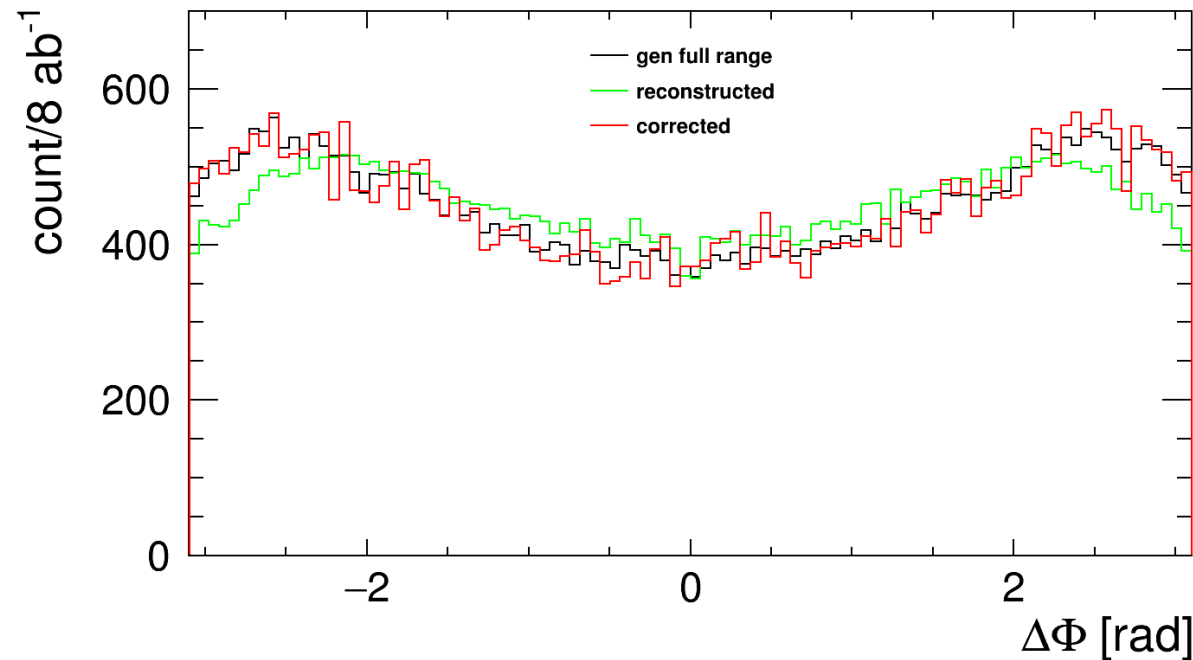
~ 1 TeV energies are optimal due to interplay of x-section and centrality

	$\sqrt{s}$	beam polarisation	$\int L dt$ (baseline)
<b>ILC</b>	0.1 - 1 TeV	e-: 80% e+: 30% (20%)	2 ab <sup>-1</sup> @ 250 GeV 0.2 ab <sup>-1</sup> @ 350 GeV 4 ab <sup>-1</sup> @ 500 GeV <u>8 ab<sup>-1</sup> @ 1 TeV</u>

- Generator level WHIZARD V2.8.3/UFO/Higgs characterization model signal and WHIZARD 1.95/SM background
- Unpolarized beams

# GENERATED AND RECONSTRUCTED SIGNAL

**Corrected** reconstructed signal for pure scalar  $\Psi_{\text{CP}}=0$ , **generated** information (WHIZARD) and **uncorrected** reconstructed signal



- Acceptance correction needed to retrieve full physical information
- Generated information is reasonably well reproduced with corrected reconstructed data

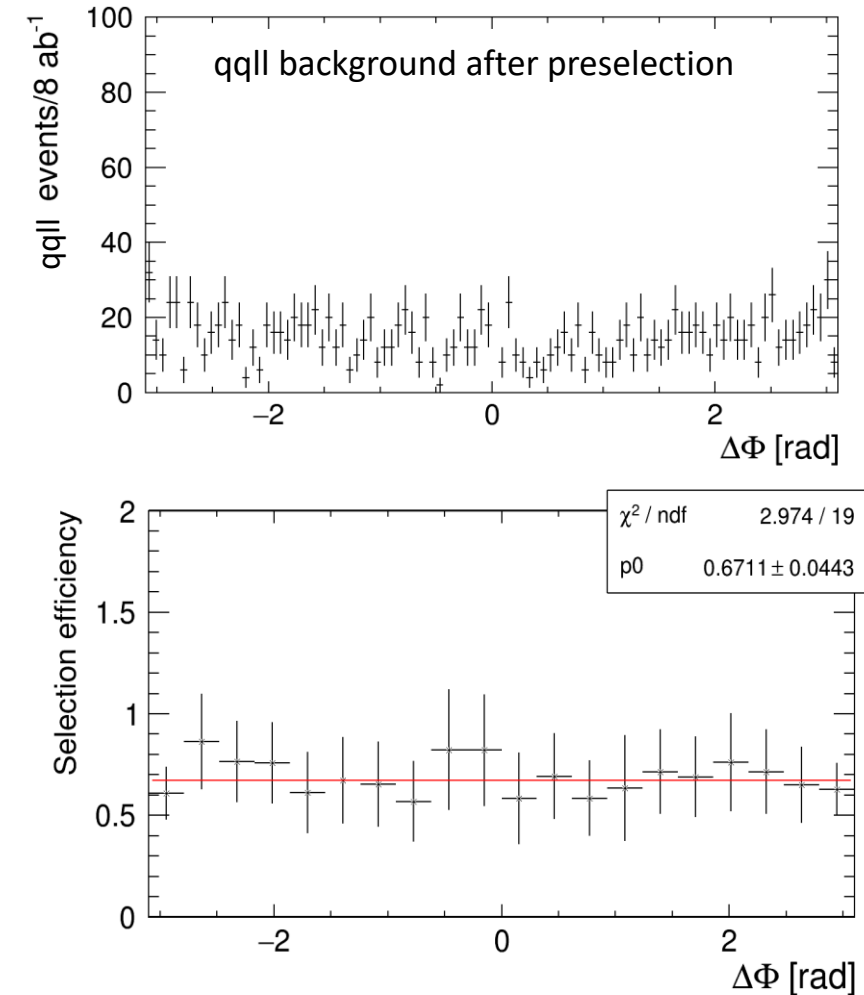
# EVENT SELECTION

## ○ Preselection – electron isolation:

- $m_{e^+e^-} > 200 \text{ GeV}$  (veto HZ)
- $E_{e^\pm} > 60 \text{ GeV}$
- DELPHES electron isolation
  - $\Delta R_{\text{max}} = 0.5$
  - $p_{T\text{min}} = 0.5 \text{ GeV}$
  - $I = \frac{\sum_{i \neq P}^{p_{T(i)} > p_{T\text{min}}} p_{T(i)}}{p_{T(P)}} < 0.12$
- Signal preselection efficiency: **~71%**

## ○ Selection cuts:

- $80 \text{ GeV} < m_{q\bar{q}} < 160 \text{ GeV}$
- $m_{Z_1, Z_2} > 30 \text{ GeV}$
- $p_{Tee} > 15 \text{ GeV}$ ,
- $p_{T\text{miss}} > 150 \text{ GeV}$
- Selection efficiency: **96%**
- **Total signal efficiency: ~ 68%**

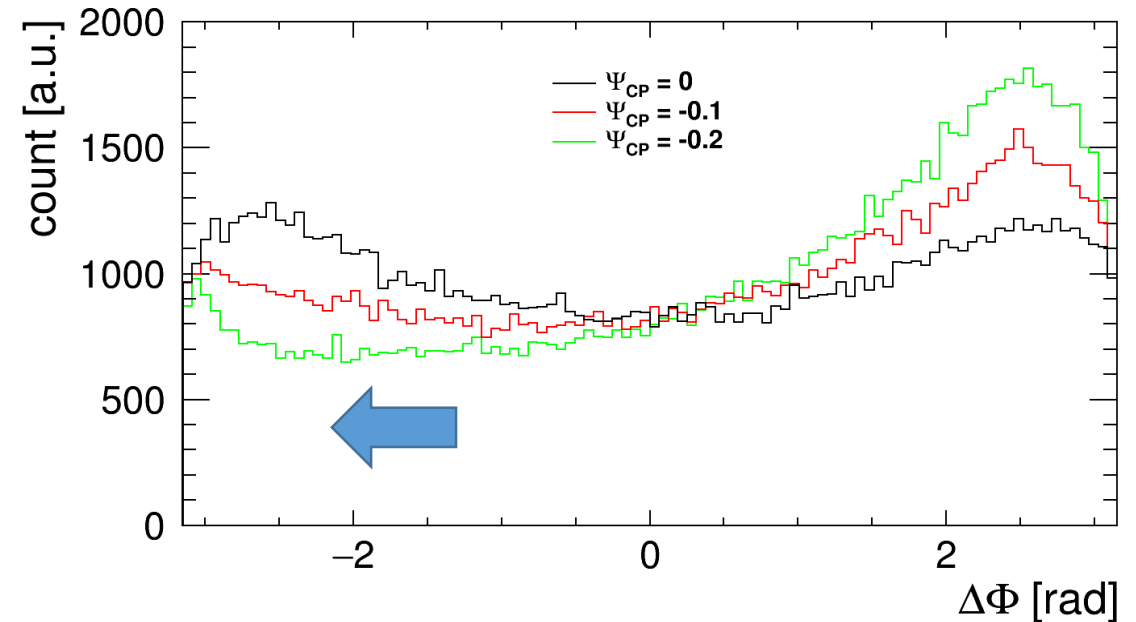
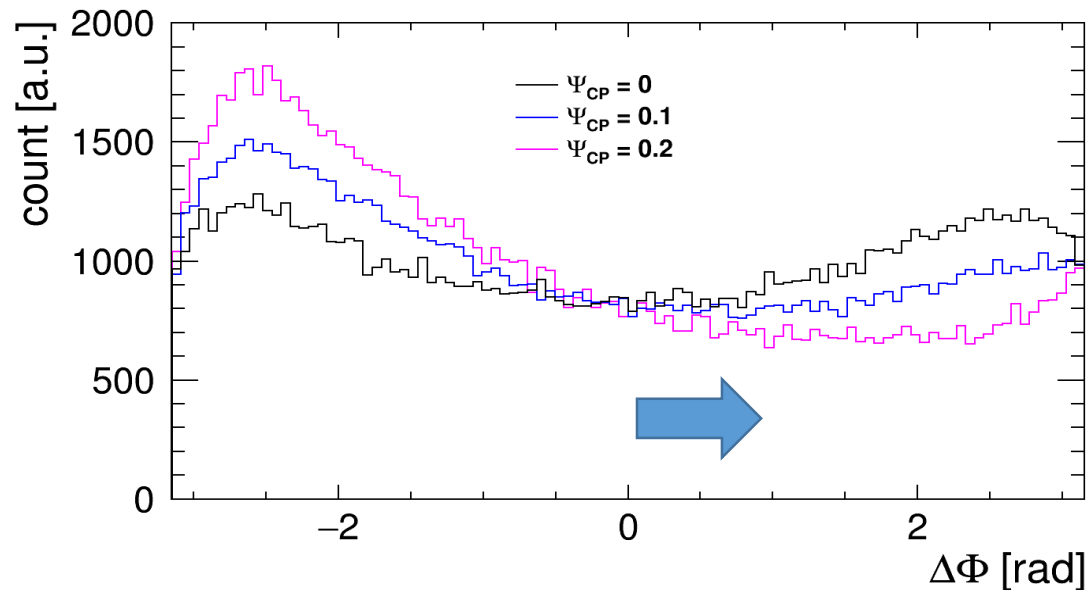


- **Unbiased selection w.r.t.  $\Delta\Phi$**
- Background is CP insensitive, fully suppressed (preselection efficiency < 1‰)

# ANGULAR OBSERVABLE $\Delta\Phi$ AND MIXING ANGLE $\Psi_{CP}$

○ Minimum of  $\Delta\Phi$  shifts for non-zero  $\Psi_{CP}$

- Differently from the  $H \rightarrow \tau\tau$  angular observable whose dependence on  $\Psi_{CP}$  can be derived from the differential x-section, here  $\Psi_{CP}$  has to be extracted **empirically**



## HOW TO EXTRACT $\Psi_{CP}$ ?

✓ Minimum of  $\Delta\Phi$  is sensitive to  $\Psi_{CP}$ ;

1. Determine position of the local minimum  
(b/a) from experimental (pseudo) data:

$$f(\Delta\Phi, \Psi_{CP}) = A + B \cdot \cos(a \cdot \Delta\Phi - b)$$

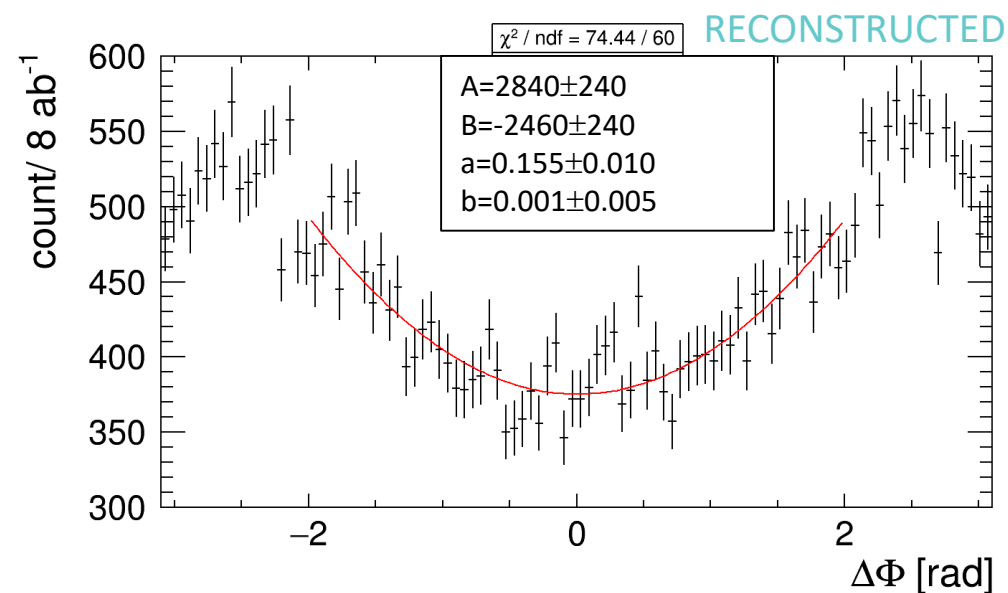
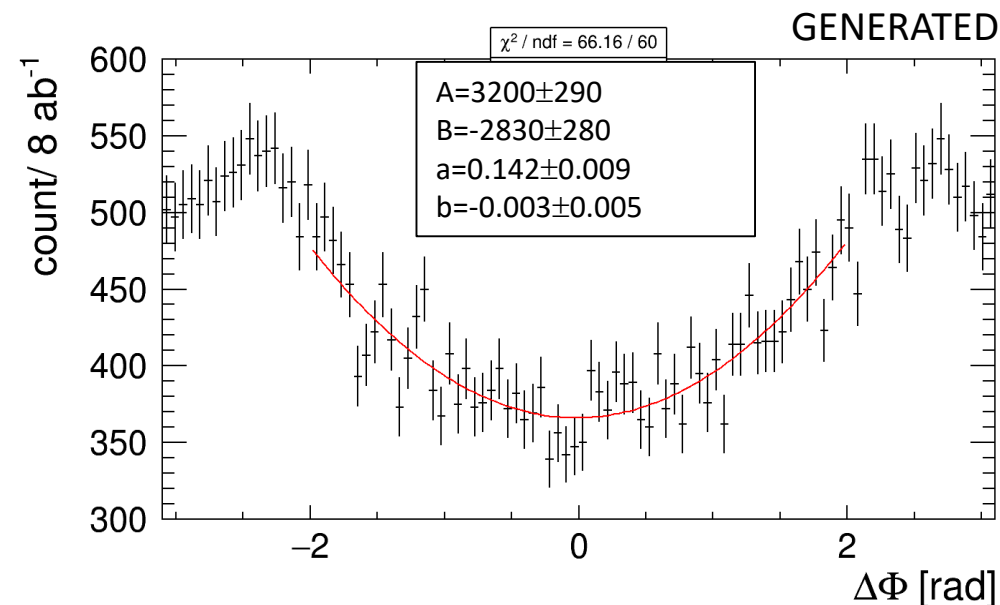
2. Position (b/a)/  $\Psi_{CP}$  is a linear function of  $\Psi_{CP}$ :

$$(b/a) / \Psi_{CP} = k \cdot \Psi_{CP} + m$$

3. Determine from simulation coefficients  $k, m$

4.  $\Psi_{CP}$  can be retrieved from quadratic equation:

$$k \cdot \Psi_{CP}^2 + m \cdot \Psi_{CP} - (b/a) = 0$$





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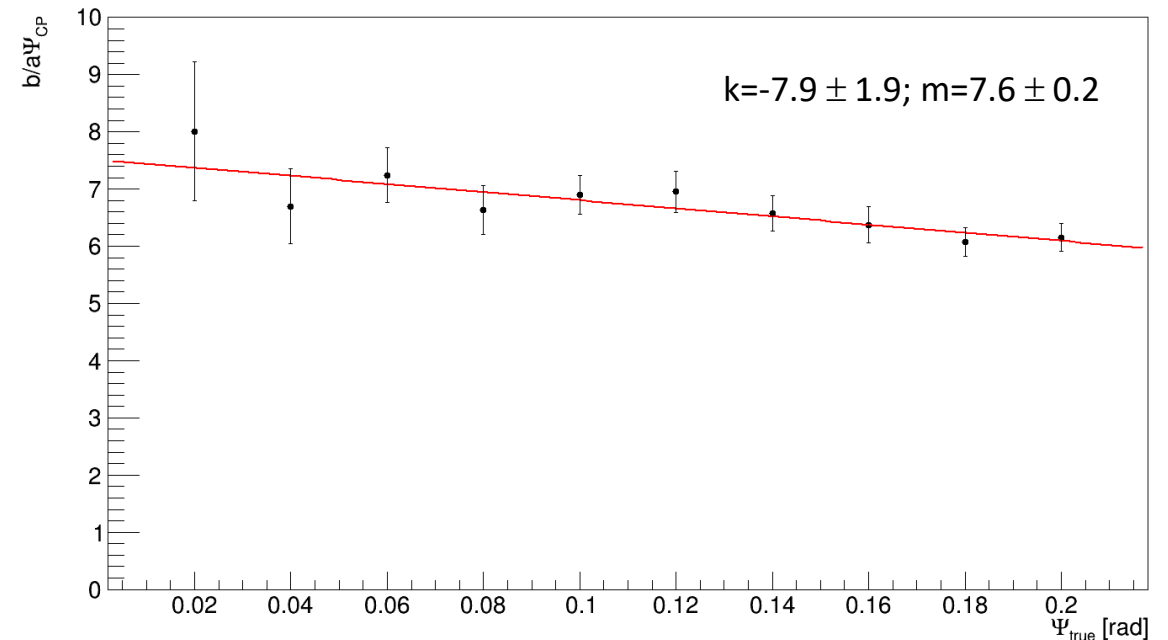
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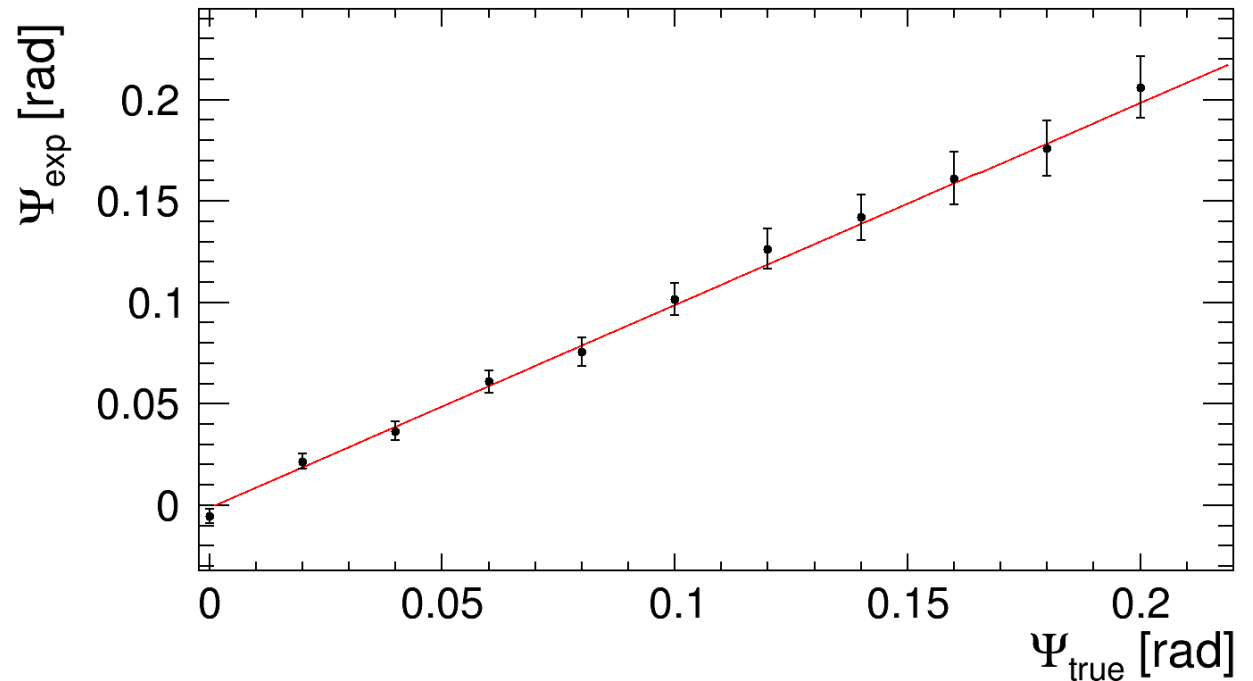
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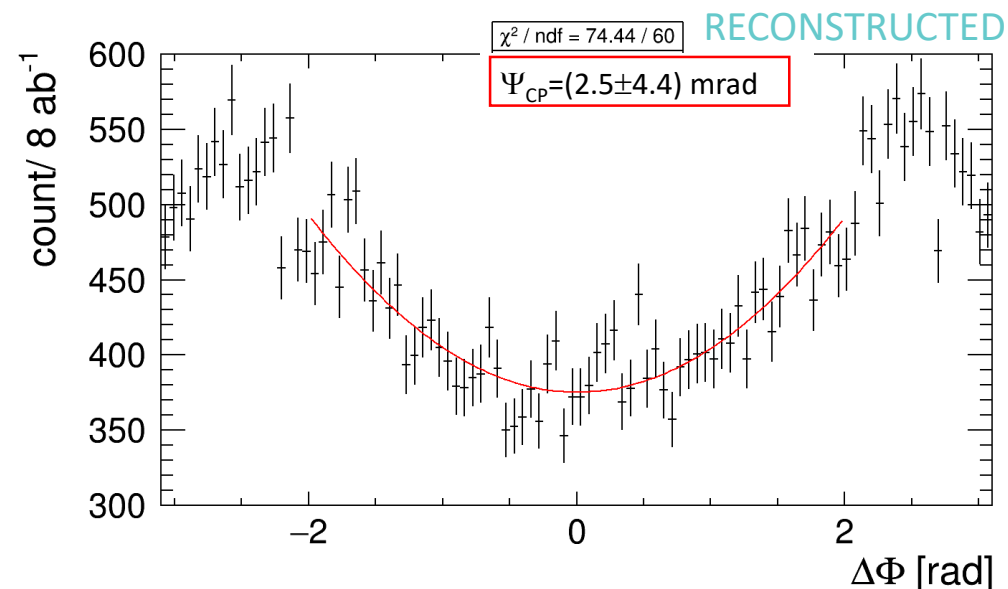
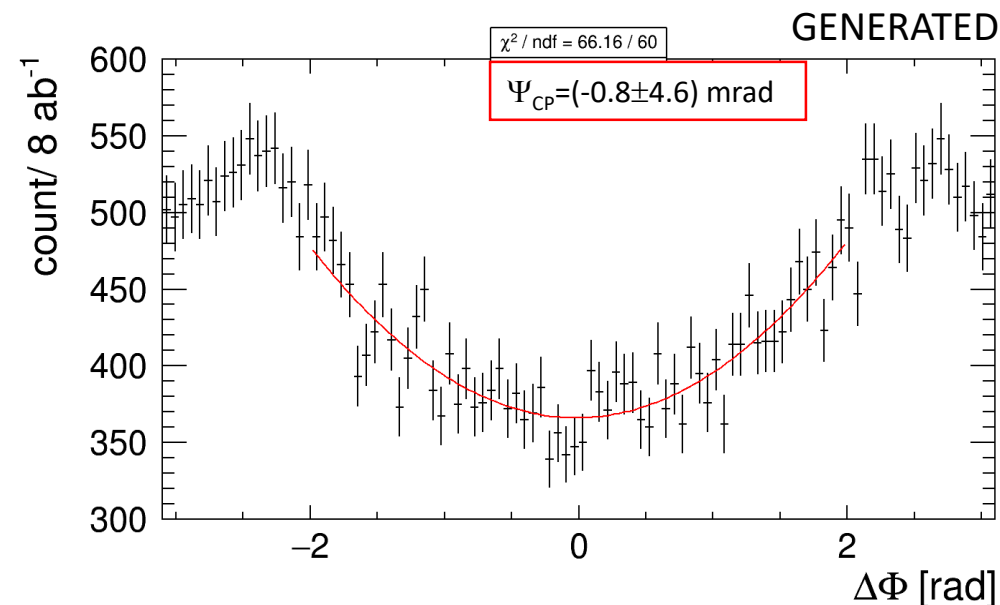
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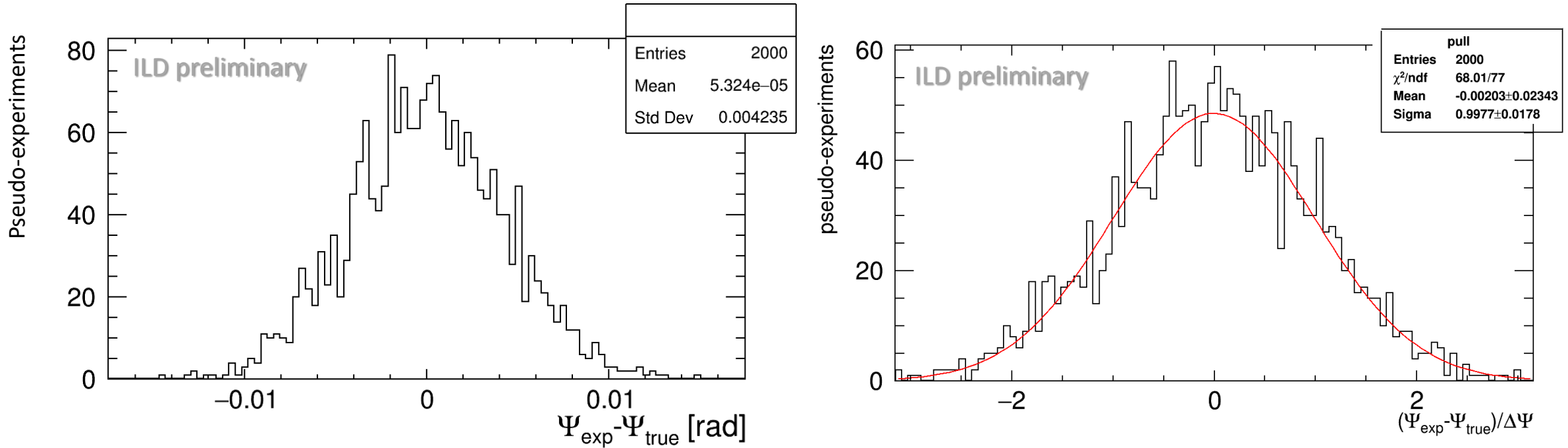
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# PSEUDO-EXPERIMENTS

$$\Delta\Psi_{\text{(stat.)}}^{\text{CP}} = 4 \text{ mrad}$$



- 2000 pseudo-experiments give 4 mrad for statistical dissipation of the mean
- Pull distribution indicates that uncertainties are correctly estimated
- Systematic error from the fit parameters uncertainties gives ~1 mrad

# INTERPRETATION

- Common framework is defined in the Snowmass CPV White paper: benchmark parameter  $f_{CP} \sim \sin^2(\Delta\Psi_{CP})$  quantifying relative contribution from CP-odd amplitude
- Interpretation for LHC/HL-LHC and future Higgs factories, for EFT and CP-sensitive observable based measurements

(68% CL, pure scalar)

[arXiv:2205.07715v3]

Collider	$pp$	$pp$	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^+e^-$	$e^-p$	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
$\mathcal{L}$ (fb $^{-1}$ )	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
$HZZ/HWW$	$4.0 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.9 \cdot 10^{-5}$	$2.9 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	$3.0 \cdot 10^{-6}$ (10 ab $^{-1}$ )	✓	✓	✓	✓	$< 10^{-5}$
$H\gamma\gamma$	–	0.50	✓	–	–	–	–	–	0.06	–	–	$< 10^{-2}$
$HZ\gamma$	–	$\sim 1$	✓	–	–	–	$\sim 1$	–	–	–	–	$< 10^{-2}$
$Hgg$	0.12	0.011	✓	–	–	–	–	–	–	–	–	$< 10^{-2}$
$Ht\bar{t}$	0.24	0.05	✓	–	–	0.29	0.08	✓	–	–	✓	$< 10^{-2}$
$H\tau\tau$	0.07	0.008	✓	0.01	0.01	0.02	0.06	–	✓	✓	✓	$< 10^{-2}$
$H\mu\mu$	–	–	–	–	–	–	–	–	–	✓	–	$< 10^{-2}$

## 1 TeV ILC

- ✓ First measurement in VBF
- ✓ First measurement in HZZ vertex based on angular observable
- ✓ Full background simulation of ILD detector and fast simulation of the signal
- ✓ Realistic ILC running scenario

## INTERPRETATION

(68% CL, pure scalar)

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E (GeV)	14,000	14,000	100,000	250	350	500	<b>1 TeV</b>	1,300	125	125	3,000	(theory)
$\mathcal{L}$ (fb $^{-1}$ )	300	3,000	30,000	250	350	500	<b>8 ab<math>^{-1}</math></b>	1,000	250	20	1,000	
$HZZ/HWW$	$4.0 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.9 \cdot 10^{-5}$	$2.9 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	<b><math>1.6 \cdot 10^{-5}</math></b>	✓	✓	✓	✓	$< 10^{-5}$
$H\gamma\gamma$	–	0.50	✓	–	–	–	–	–	0.06	–	–	$< 10^{-2}$
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$H\mu\mu$	–	–	–	–	–	–	–	–	–	✓	–	$< 10^{-2}$

# SUMMARY

- ✓ Complete simulation of CPV Higgs mixing angle ( $\Psi_{\text{CP}}$ ) measurement is performed at 1 TeV ILC with the ILD detector
- ✓ This is the first result in VBF fusion based on angular observable ( $\Delta\Phi$ );
- ✓ Knowing the dependence of  $\Delta\Phi$  minimum to  $\Psi_{\text{CP}}$  from simulation,  $\Psi_{\text{CP}}$  can be determined from (experimental) data;
- ✓ From  $8 \text{ ab}^{-1}$  of 1 TeV ILC data, pure scalar state should be measured with 4 mrad statistical uncertainty of  $\Psi_{\text{CP}}$  at 68% CL; Systematic uncertainty from the fit is found to be smaller ( $< 1 \text{ mrad}$ );
- ✓ The above uncertainty corresponds to  $f_{\text{CP}} \approx 1.6 \cdot 10^{-5}$  approaching theoretical target;
- ✓ The precision can be improved in combination with other Higgs decay channels (i.e.  $\text{H} \rightarrow \text{WW} \rightarrow 4\text{-jets}$ ).