

# Multiple boson production at high-energy muon colliders to probe the Higgs-muon coupling

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# A multi-TeV lepton collider is amazing



- ▶  $\ell^+ \ell^-$  annihilation **probes TeV scale directly**
- ▶ VBF **scans the new physics hints in the full spectrum**  
From the threshold to up to 2 orders of magnitude above EW scale.
- ▶ It produces a lot of  $H$ , top quarks,  $W/Z$ , ... as a **“factory” for SM precision test**
- ▶ **An “EW jet factory”**

In addition to QCD jets, there are  $W/Z$  jet,  $H$  jet,  $t$  jet, neutrino jet, . . .

Even neutrino collision is not impossible!

## Challenges:

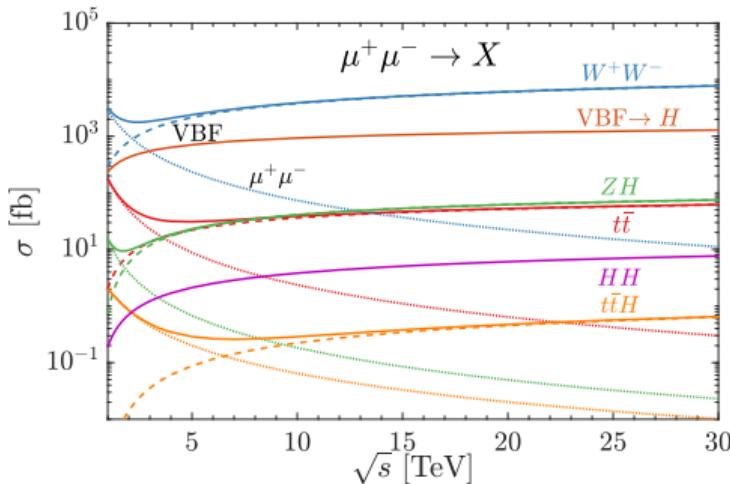
**Be careful about the radiations!**

EW NLO shall be necessary, just like the NLO QCD at LHC.

# The full picture: An electroweak version of Tevatron

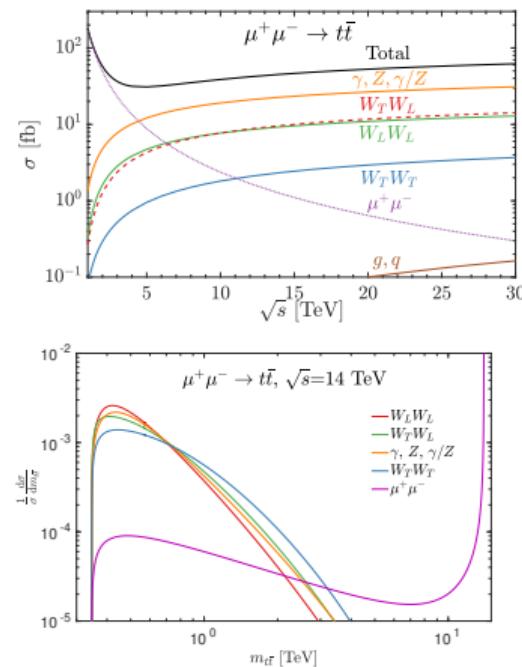
**Just like in hadronic collisions:**

$\mu^+\mu^- \rightarrow$  exclusive particles + remnants



[T. Han, Y. Ma, K.Xie 2007.14300]

**One example:  $\mu^+\mu^- \rightarrow t\bar{t} + X$**



Compare the “EW Tevatron” with LHC

**The lepton collider is better in studying EW physics**

$$\mathcal{L}_{W_{\lambda_1}^+ W_{\lambda_2}^-} = \int_{\tau}^1 \frac{d\xi}{\xi} f_{W_{\lambda_1}}(\xi, \mu_f) f_{W_{\lambda_2}}\left(\frac{\tau}{\xi}, \mu_f\right)$$

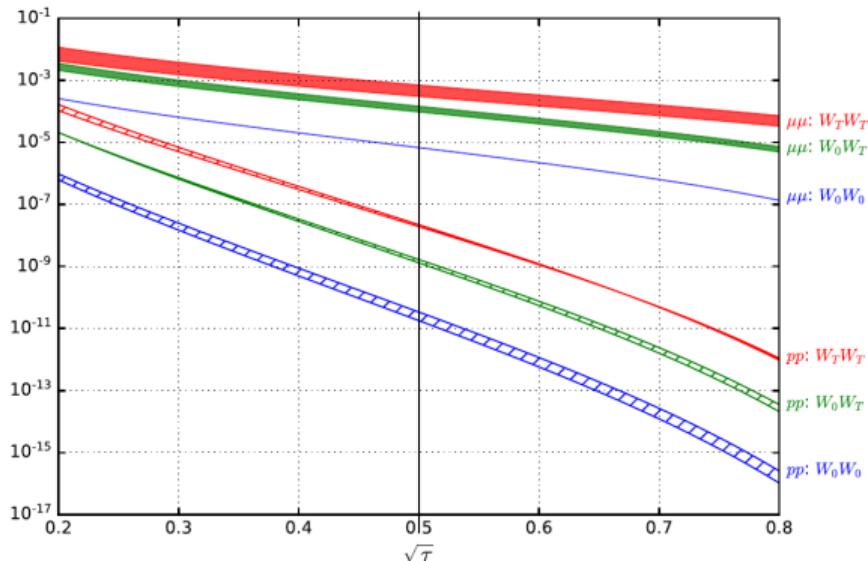
Consider the two colliders in the same ring

$$\sqrt{s}_{\mu\mu} = \sqrt{s}_{pp}$$

For  $2 \rightarrow 1$  processes, take a benchmark

$$\sqrt{\tau} = \frac{M}{\sqrt{s}} = \frac{1}{2}$$

**The ratio  $\mu\mu/pp$  is larger than  $10^4$ !**



[2005.10289]

# Muon collider: Our first time to play with beams in another flavor

## One example in precision physics: The Muon-Higgs Coupling

[T. Han, W. Kilian, N. Kreher, YM, T. Striegl, J. Reuter, and K. Xie, 2108.05362]

[E. Celada, T. Han, W. Kilian, N. Kreher, YM, F. Maltoni, D. Pagani, T. Striegl, J. Reuter, and K. Xie, in progress]

- ▶ Physics: We actually do not know whether the SM mass-generation mechanism applies just to the heavy particles, or also to the 1st/2nd generations.
- ▶ Logical possibility: Muon mass not (only) generated by SM Higgs.  
⇒ **Why not have an arbitrary Yukawa coupling?**

## EFT parameterizations

- Nonlinear HEFT gives  $\kappa_\mu = \frac{v}{\sqrt{2}m_\mu} y_1$  [Coleman et al., PR1969, Weinberg, PLB1980, · · ·]

$$\begin{aligned}\mathcal{L}_{UH} = & \frac{v^2}{4} \text{Tr} \left[ D_\mu U^\dagger D^\mu U \right] F_U(H) + \frac{1}{2} \partial_\mu H \partial^\mu H - V(H) \\ & - \frac{v}{2\sqrt{2}} \left[ \bar{\ell}_L^i \tilde{Y}_\ell^{ij}(H) U (1 - \tau_3) \ell_R^j + \text{h.c.} \right]\end{aligned}$$

with  $F_U, V, \tilde{Y}$  expanded as

$$F_U(H) = 1 + \sum_{n \geq 1} f_{U,n} \left( \frac{H}{v} \right)^n, V(H) = v^4 \sum_{n \geq 2} f_{V,n} \left( \frac{H}{v} \right)^n, \tilde{Y}_\ell^{ij}(H) = \sum_{n \geq 0} \tilde{Y}_{\ell,n} \left( \frac{H}{v} \right)^n$$

- Linear SMEFT [Weinberg PRL1979, Abbott & Wise PRD1980, · · ·]

$$\mathcal{L} \supset - \sum_{n=1}^{\infty} \frac{c_\varphi^{(2n+4)}}{\Lambda^{2n}} \left( \varphi^\dagger \varphi - \frac{v^2}{2} \right)^{n+2} - \sum_{n=1}^{\infty} \frac{c_{\ell\varphi}^{(2n+4)}}{\Lambda^{2n}} \left( \varphi^\dagger \varphi - \frac{v^2}{2} \right)^n (\bar{\ell}_L \varphi e_R + \text{h.c.})$$

# HEFT in the unitary gauge: the extended $\kappa$ framework

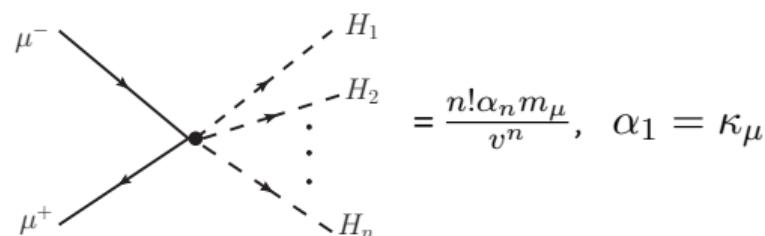
Introduce the form factors  $\alpha_n, \beta_n$

$$y_{\mu,n} = \frac{\sqrt{2}m_\mu}{v}\alpha_n, \quad f_{V,n} = \beta_n\lambda$$

In the unitary gauge, the HEFT formalism can be simplified to

$$\mathcal{L} \supset -\frac{m_H^2}{2}H^2 - m_\mu \bar{\mu}\mu - \sum_{n=3}^{\infty} \beta_n \frac{\lambda}{v^{n-4}} H^n - \sum_{n=1}^{\infty} \alpha_n \frac{m_\mu}{v^n} H^n \bar{\mu}\mu$$

The regular “ $\kappa$  framework” is extended to include more vertices



## Relate the two EFTs

$$\alpha_1 = \frac{v}{\sqrt{2}m_\mu} y_{\ell,1} = 1 + \frac{v^3}{\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(6)}}{\Lambda^2} + \frac{v^5}{\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(8)}}{\Lambda^4} + \frac{3v^7}{4\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(10)}}{\Lambda^6},$$

$$\alpha_2 = \frac{v}{\sqrt{2}m_\mu} y_{\ell,2} = \frac{3v^3}{2\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(6)}}{\Lambda^2} + \frac{5v^5}{2\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(8)}}{\Lambda^4} + \frac{21v^7}{8\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(10)}}{\Lambda^6},$$

$$\alpha_3 = \frac{v}{\sqrt{2}m_\mu} y_{\ell,3} = \frac{v^3}{2\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(6)}}{\Lambda^2} + \frac{5v^5}{2\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(8)}}{\Lambda^4} + \frac{35v^7}{8\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(10)}}{\Lambda^6},$$

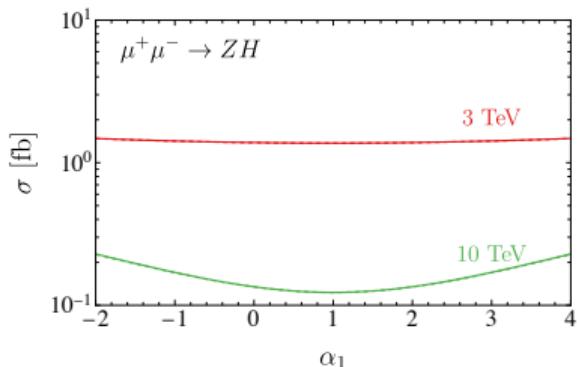
$$\alpha_4 = \frac{v}{\sqrt{2}m_\mu} y_{\ell,4} = \frac{5v^5}{4\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(8)}}{\Lambda^4} + \frac{35v^7}{8\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(10)}}{\Lambda^6},$$

$$\alpha_5 = \frac{v}{\sqrt{2}m_\mu} y_{\ell,5} = \frac{v^5}{4\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(8)}}{\Lambda^4} + \frac{21v^7}{8\sqrt{2}m_\mu} \frac{c_{\ell\phi}^{(10)}}{\Lambda^6},$$

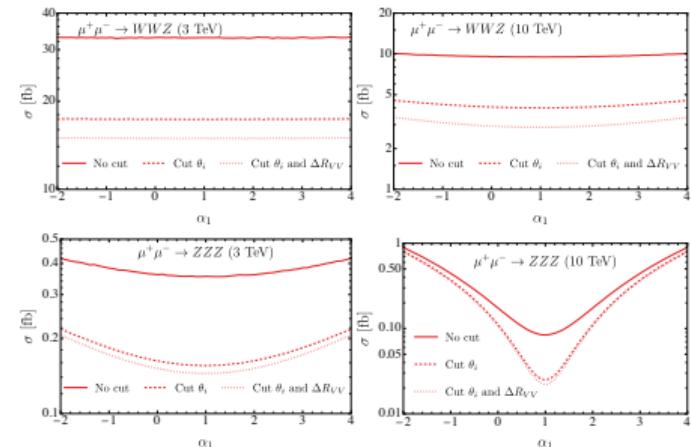
# Measure the $\mu\mu H$ vertex

There are processes that depend on only  $\alpha_1$ :  $\mu^+\mu^- \rightarrow ZH$  and  $\mu^+\mu^- \rightarrow V^3$

## ► $ZH$ production



## ► $V^3$ production



## ► Sign of Yukawa: $\alpha_1 = 1$ VS $\alpha_1 = -1$

$$\begin{aligned} S_{3\text{ TeV}}^\pm &= 1.23, & S_{10\text{ TeV}}^\pm &= 11.8 \\ S_{10\text{ TeV}} &= 2.09, & |\Delta\alpha_1| &\leq 0.8 \end{aligned}$$

## ► Measure $\alpha_1$ more precisely

$$\begin{aligned} S_{10\text{ TeV}}^{WWZ} &= 2.1, & |\Delta\alpha_1| &\leq 0.8 \\ S_{10\text{ TeV}}^{ZZZ} &= 2.2, & |\Delta\alpha_1| &\leq 0.2. \end{aligned}$$

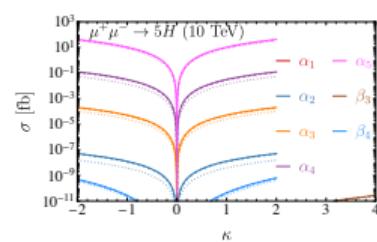
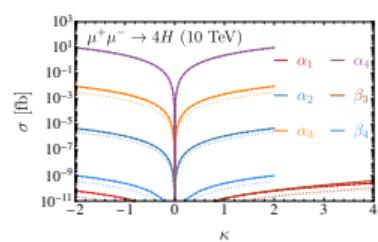
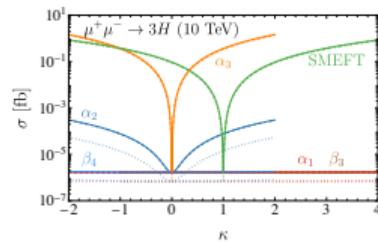
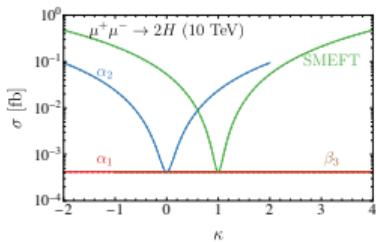
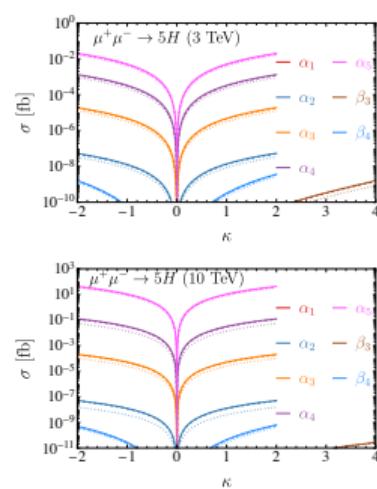
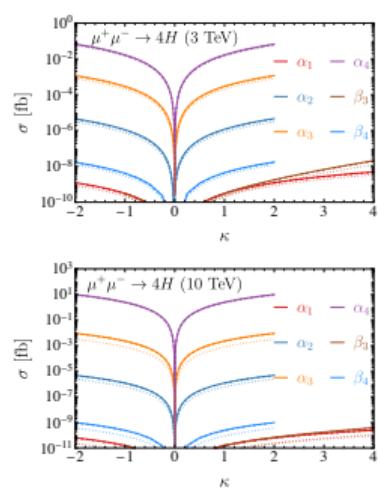
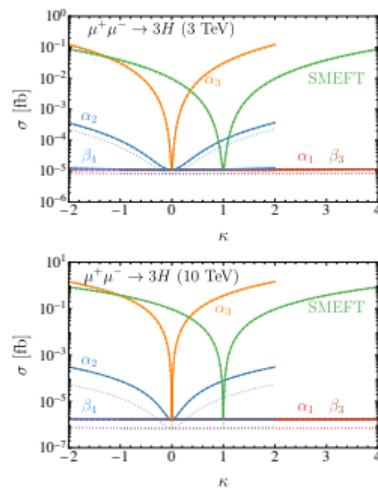
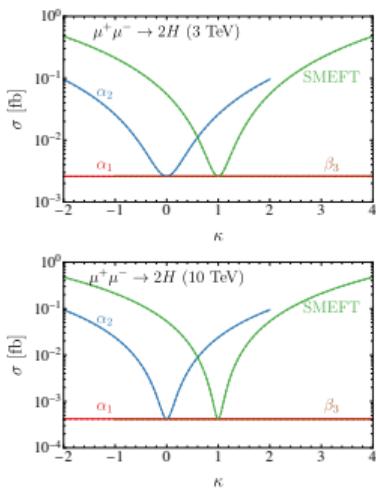
# Processes in consideration

H \ V	0	1	2	3	4	5
0	-	Z	$Z^2, W^2$	$Z^3$ $W^2 Z$	$Z^4, W^4$ $W^2 Z^2$	$Z^5, W^2 Z^3$ $W^4 Z$
1	$H$	$ZH$	$W^2 H$ $Z^2 H$	$W^2 ZH$ $Z^3 H$	$W^4 H, Z^4 H$ $W^2 Z^2 H$	-
2	$H^2$	$ZH^2$	$W^2 H^2$ $Z^2 H^2$	$W^2 ZH^2$ $Z^3 H^2$	-	-
3	$H^3$	$ZH^3$	$W^2 H^3$ $Z^2 H^3$	-	-	-
4	$H^4$	$ZH^4$	-	-	-	-
5	$H^5$	-	-	-	-	-

[E. Celada, T.Han, W.Kilian, N. Kreher, YM, F. Maltoni, D. Pagani, J. Reuter, T. Striegl, and K.Xie, coming out soon ]

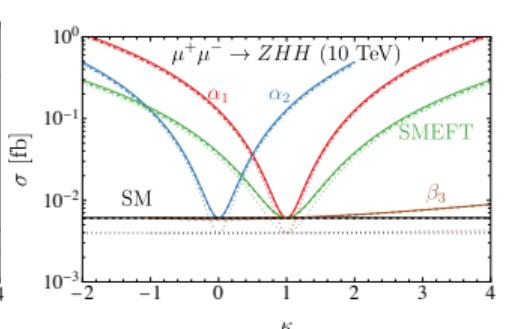
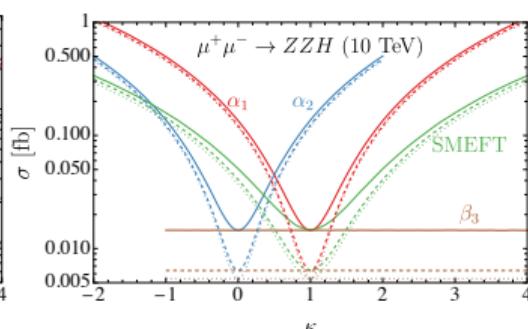
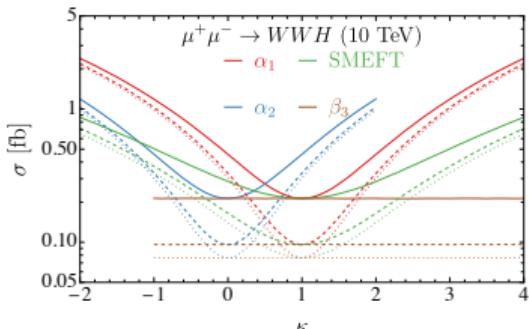
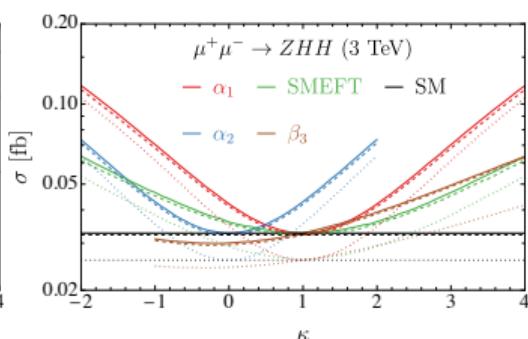
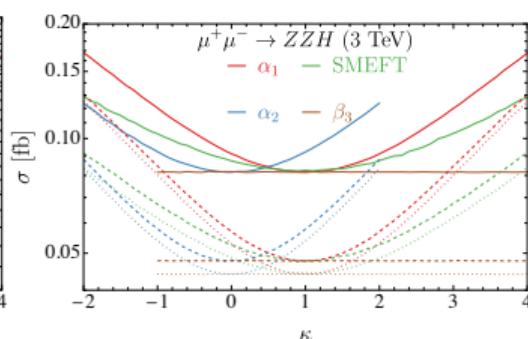
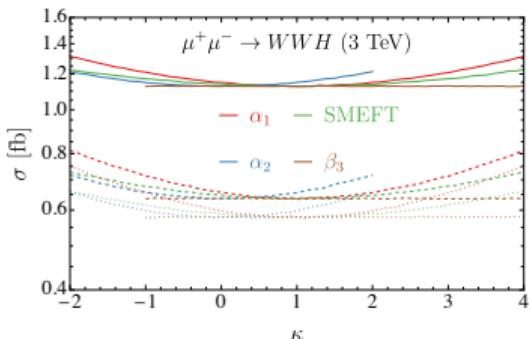
# Multi-Higgs production processes: $\mu^+ \mu^- \rightarrow H^n$

The cross section is solely dependent on  $\alpha_n \Rightarrow$  Measure  $\alpha_n$  directly

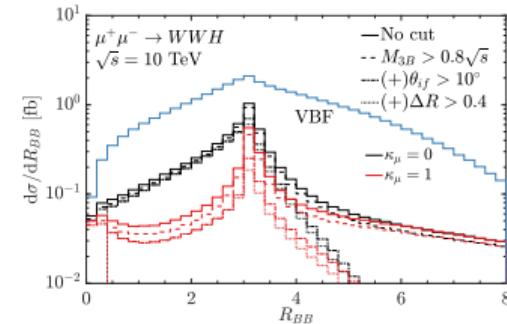
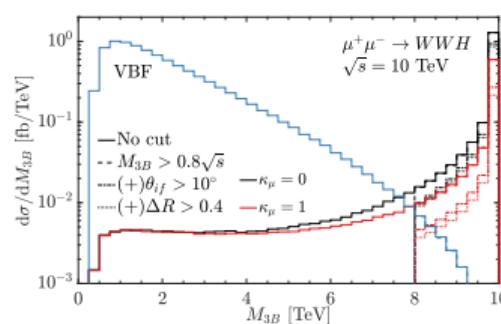
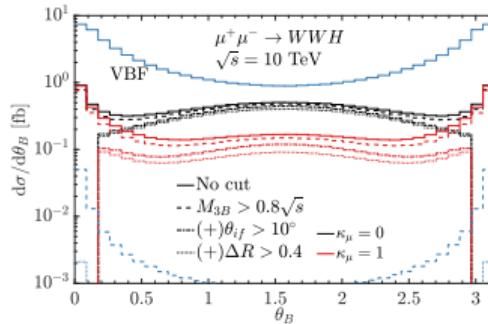


# Other processes: constrain $(\alpha_1, \alpha_2)$ simultaneously

Example:  $WWH, ZZH, ZHH$



# Kinematics: $WWH$ at a 10 TeV muon collider



- ▶ Background (VBF) is much larger than signal (annihilation)
- ▶ VBF events accumulate around threshold, and mostly forward
- ▶ Annihilation in the rest frame (central, and  $M \sim \sqrt{s}$  spread by ISR)
- ▶ Annihilation also has forward dominance, due to the gauge splitting  $W \rightarrow WH$

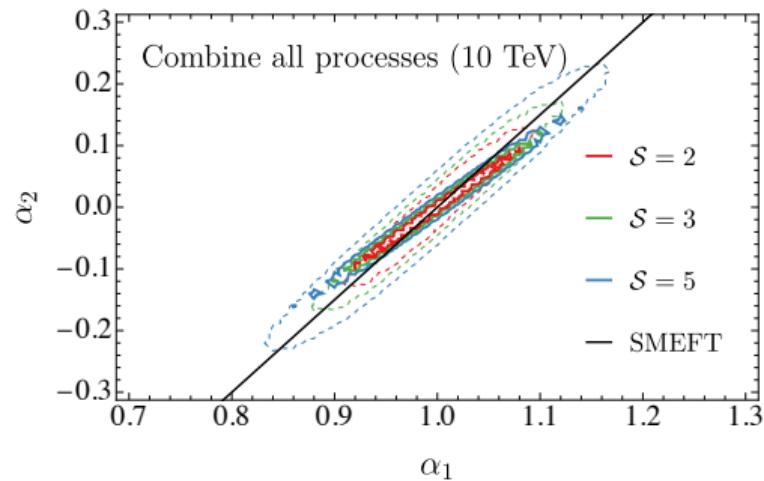
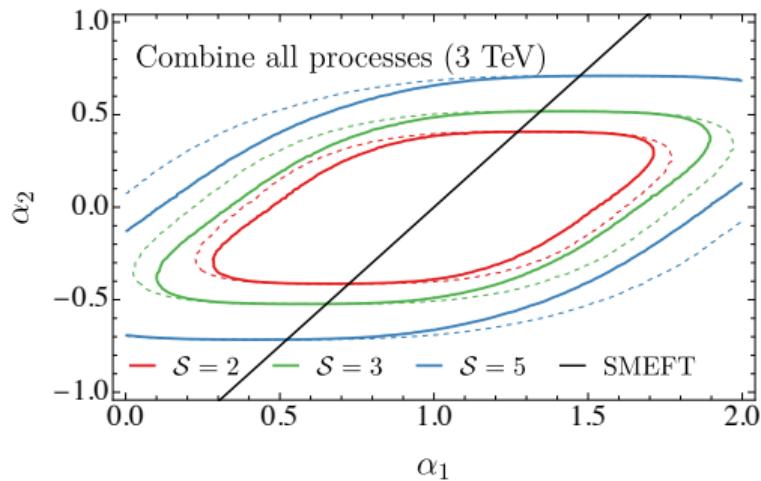
[T.Han, W.Kilian, N. Kreher, YM.J. Reuter, and K.Xie, JHEP 12 (2021) 162, 2108.05362 ]

# Cuts: $WWH$ at a 10 TeV muon collider

Cut flow	$\kappa_\mu = 1$	w/o ISR	$\kappa_\mu = 0$ (2)	CVBF	NVBF
$\sigma$ [fb]	$WWH$				
No cut	0.24	0.21	0.47	2.3	7.2
$M_{3B} > 0.8\sqrt{s}$	0.20	0.21	0.42	$5.5 \cdot 10^{-3}$	$3.7 \cdot 10^{-2}$
$10^\circ < \theta_B < 170^\circ$	0.092	0.096	0.30	$2.5 \cdot 10^{-4}$	$2.7 \cdot 10^{-4}$
$\Delta R_{BB} > 0.4$	0.074	0.077	0.28	$2.1 \cdot 10^{-4}$	$2.4 \cdot 10^{-4}$
# of events	740	770	2800	2.1	2.4
$S/B$	2.8				

- ▶ Integrated luminosity  $\mathcal{L} = (\sqrt{s}/10 \text{ TeV})^2 \cdot 10 \text{ ab}^{-1}$  [\[1901.06150\]](#)
- ▶  $S = N_{\kappa_\mu} - N_{\kappa_\mu=1}$ ,  $B = N_{\kappa_\mu=1} + N_{\text{VBF}}$ .
- ▶ VBF and ISR are mostly excluded by invariant mass cut.
- ▶ Angular cut also weaken VBF further.

# Constrains on $(\alpha_1, \alpha_2)$



# Summary and prospects

## Higgs is special and important

- ▶ The Higgs sector is the portal to new physics beyond SM.
  - ▶ Testing the SM mass generation mechanism indirectly helps BSM physics searches.
  - ▶ Measuring the vertices that do not exist in SM directly aim at BSM physics
  - ▶ The Yukawa couplings of the 3rd generation fermions are precisely measured  
⇒ The 2nd generation is the next target.

## Multi-TeV muon collider is cool

- ▶ A dream machine with many physics opportunities
- ▶ Two mechanisms with different kinematic features: lepton collision and VBF
- ▶ The main background is from VBF: Introduce kinematic cuts  $M_F > 80\% \sqrt{s}$
- ▶ The sign of  $\mu\mu H$  can be determined via  $\mu^+ \mu^- \rightarrow ZH$
- ▶ The  $\mu\mu H^n$  couplings can be determined via multi-boson production processes directly
- ▶ The  $\mu\mu H$  and  $\mu\mu H^2$  can be constrained simultaneously in the  $(\alpha_1, \alpha_2)$  contour plots