

MOST2 offline tracking reconstruction and alignment

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Tue, Sep29, 2022

Alignment

- straight line model: $x = X(z) + x_{res} = az + b + x_{res}; y = Y(z) + y_{res} = cz + d + y_{res}$
- considering misalignment:

local parameters (track parameters): a, b, c, d

global parameters (alignment parameters): $\Delta x, \Delta y, \Delta \gamma, \Delta z, \Delta \alpha, \Delta \beta$

$$X(\vec{p}^{local}, \vec{a}^{global}) = az + b - \Delta x + y\Delta y + a(\Delta z + x\Delta \beta + y\Delta \alpha)$$

$$Y(\vec{p}^{local}, \vec{a}^{global}) = cz + d - \Delta y - x\Delta \gamma + c(\Delta z + x\Delta \beta + y\Delta \alpha)$$

- minimize: $\chi^2 = \sum_{\text{data sets}} \left(\sum_{\text{events}} \left(\sum_{\text{tracks}} \left(\sum_{\text{hits}} w_i r_i^2 \right) \right) \right)$

global parameters that we want to get

- solution:
$$\begin{pmatrix} C & \cdots & H_k & \cdots \\ \vdots & \ddots & 0 & 0 \\ H_k^T & 0 & \Gamma_k & 0 \\ \vdots & 0 & 0 & \ddots \end{pmatrix} \times \begin{pmatrix} \mathbf{a} \\ \vdots \\ \mathbf{p}_k \\ \vdots \end{pmatrix} = \begin{pmatrix} \mathbf{b} \\ \vdots \\ \boldsymbol{\beta}_k \\ \vdots \end{pmatrix}$$

global and local

Loop over all tracks

$$C_k = \sum_i w_{ki} \underline{\mathbf{d}_{ki}^{global}} (\underline{\mathbf{d}_{ki}^{global}})^T,$$

related to global

$$b_k = \sum_i w_{ki} r_{ki} \underline{\mathbf{d}_{ki}^{global}},$$

derivative vectors w.r.t the global parameters

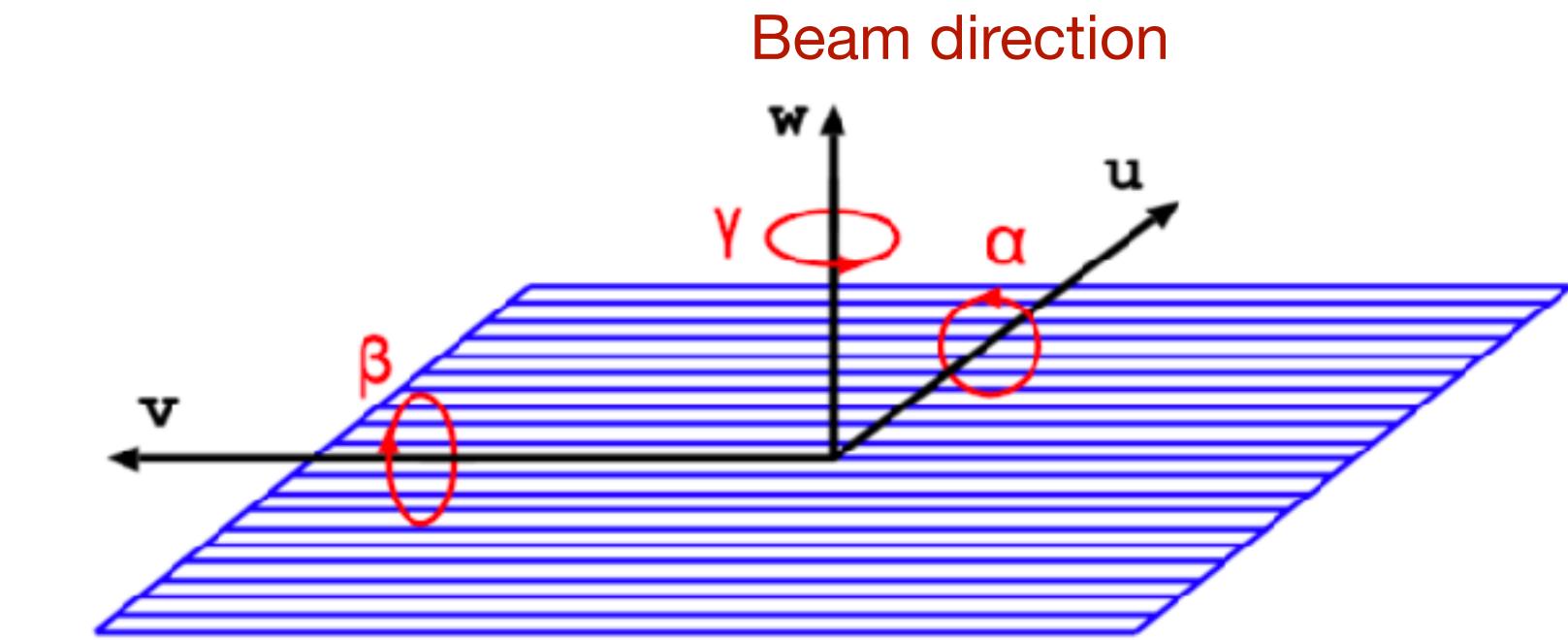
$$C' = \sum_k C_k - \sum_k H_k \Gamma_k^{-1} H_k^T,$$

$$\mathbf{a}' = C'^{-1} \mathbf{b}'$$

$$\mathbf{b}' = \sum_k \mathbf{b}_k - \sum_k H_k \Gamma_k^{-1} \boldsymbol{\beta}_k.$$

Interface to Millepede

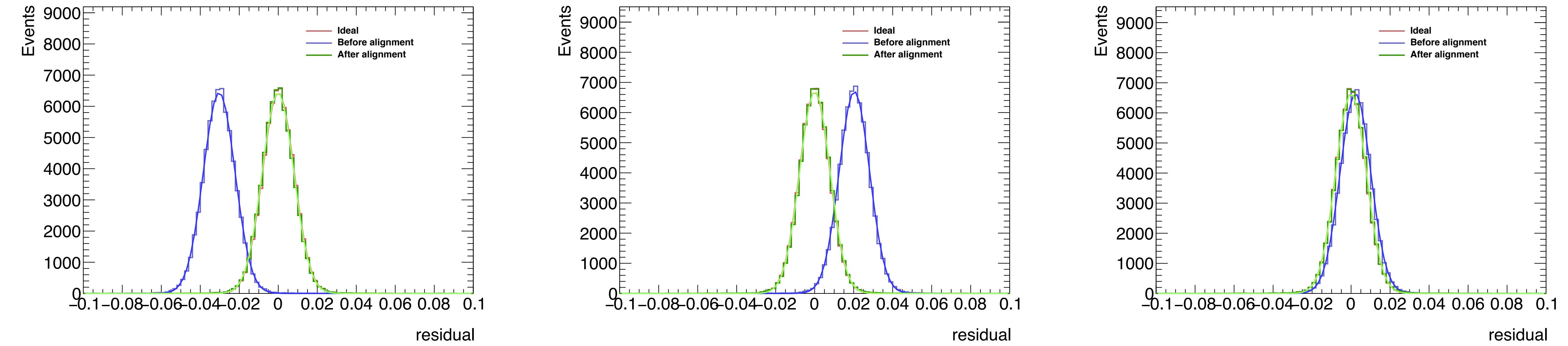
- using simulated data from G4
- interface to Millepede to solve the matrix, then get the corrected alignment parameters
- digitizing the simulation data, randomly change the ideal geometry



If add Δx , Δy , $\Delta \gamma$ only:

chipID	DeltaX setting	DeltaX fitted	Unit: mm	DeltaY fitted	Unit: rad	Deltay setting	Deltay fitted
			DeltaY setting		Deltay setting		
1	0.07253	0.07250	-0.02467	-0.02448	0.00046	0.00268	
2	0.02036	0.02024	0.02448	0.02448	0.00493	0.00159	
3	-0.03740	-0.03747	0.02994	0.02992	-0.00189	-0.00265	
4	-0.04566	-0.04552	-0.01967	-0.01993	0.01671	0.00941	
5	-0.00856	-0.00853	0.04181	0.04175	-0.00823	-0.00259	
6	-0.03031	-0.03015	-0.03201	-0.03207	0.00435	0.00572	
7	0.01759	0.01763	-0.03591	-0.03587	0.00090	0.00178	
8	-0.02344	-0.02362	-0.01411	-0.01378	-0.01306	-0.01160	
9	-0.00738	-0.00738	0.03910	0.03913	-0.00168	-0.00220	
10	0.02399	0.02401	-0.02652	-0.02655	0.00099	0.00023	
11	-0.00952	-0.00955	0.00229	0.00221	-0.00016	0.00010	
12	0.02780	0.02782	0.01526	0.01520	-0.00332	-0.00248	

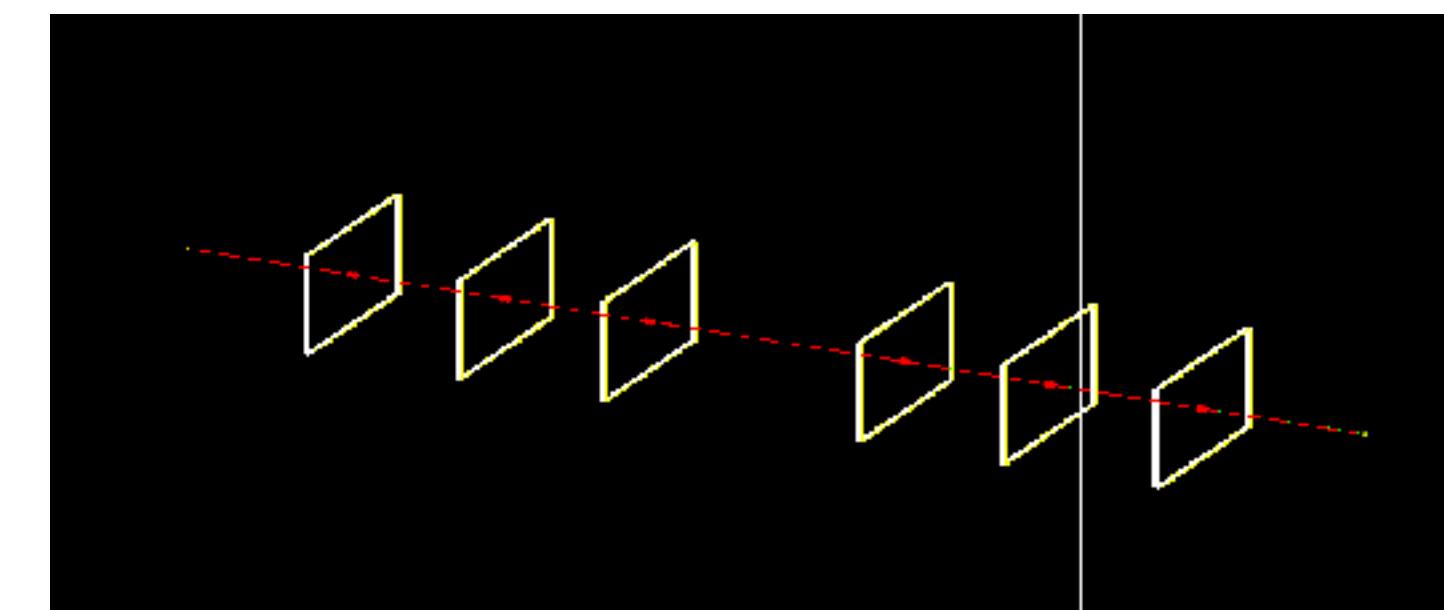
Residual Plots

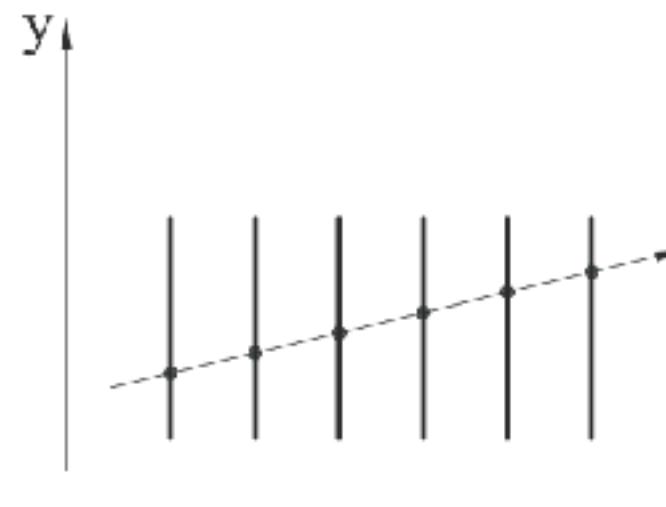


- Residual plots Ideal/before alignment/ after alignment
- ~100,000 tracks
- All residual plots can be corrected well, although some mis-alignment parameters can't be corrected well

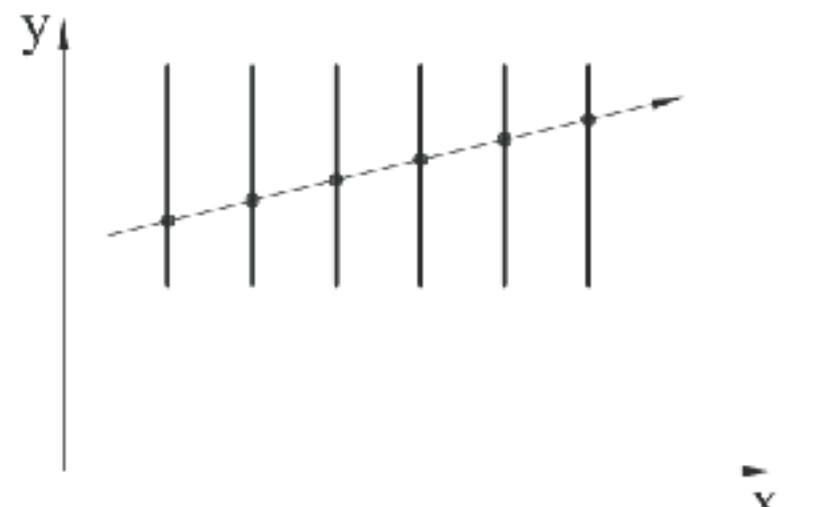
Next Plan

- using actual geometry simulation data
- constrains
- official Millepede2

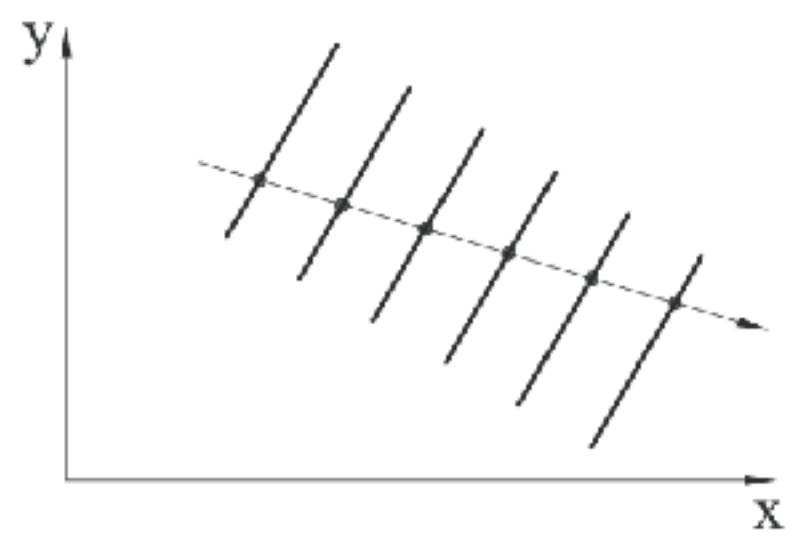




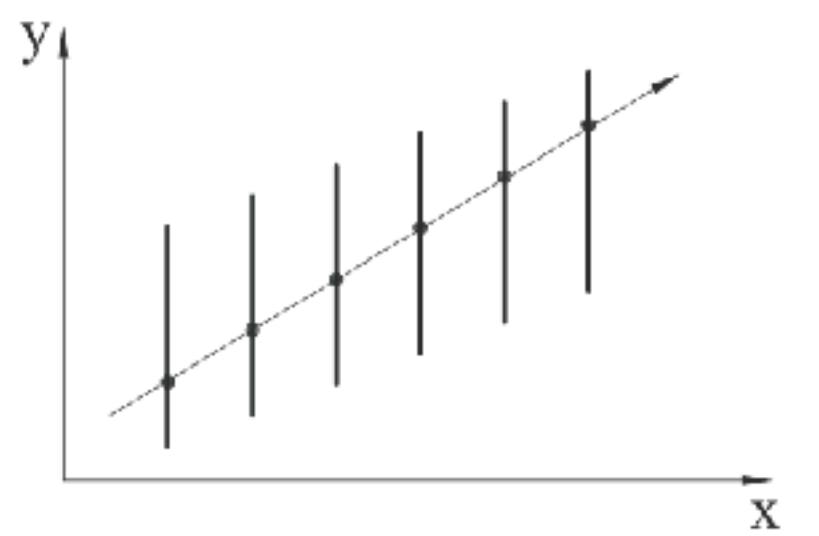
(a) 实际状态



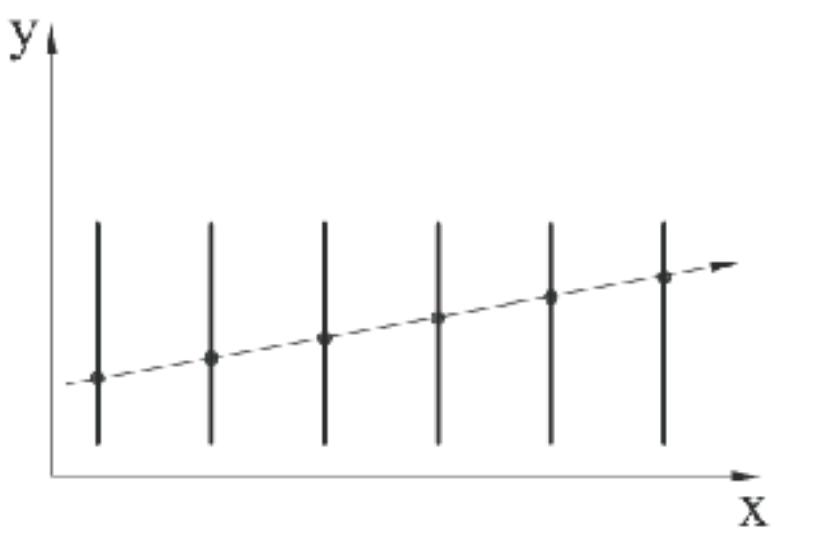
(b) 平移变换 (Translation)



(c) 旋转变换 (Rotation)



(d) Shearing 变换

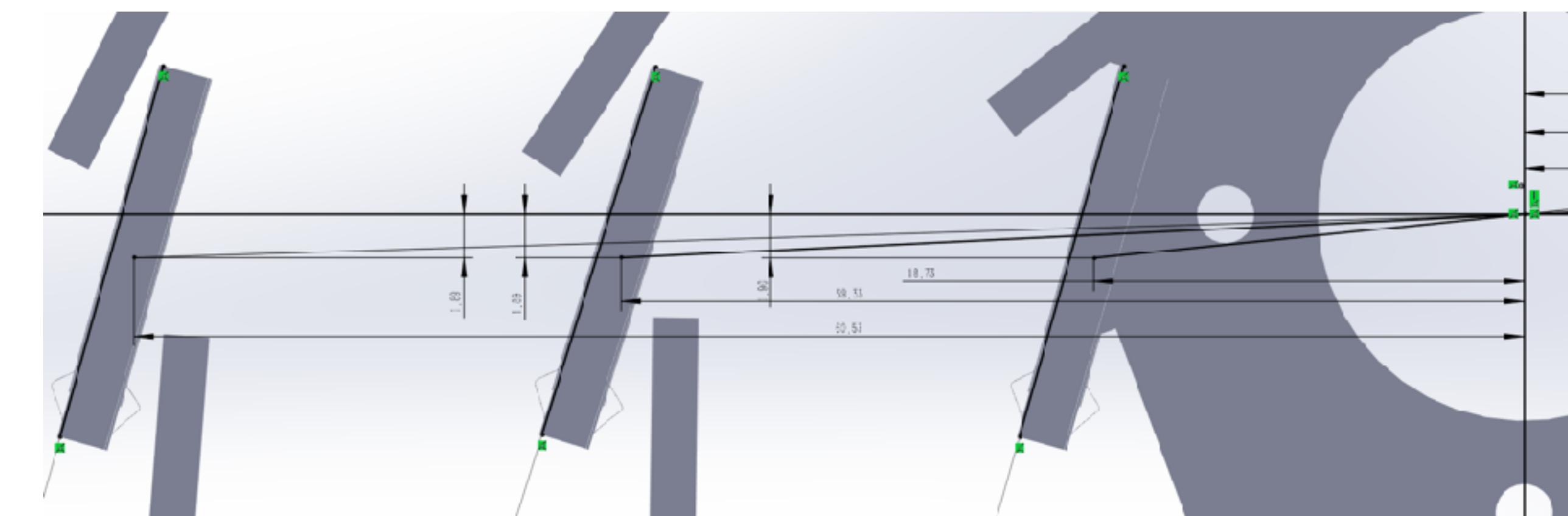
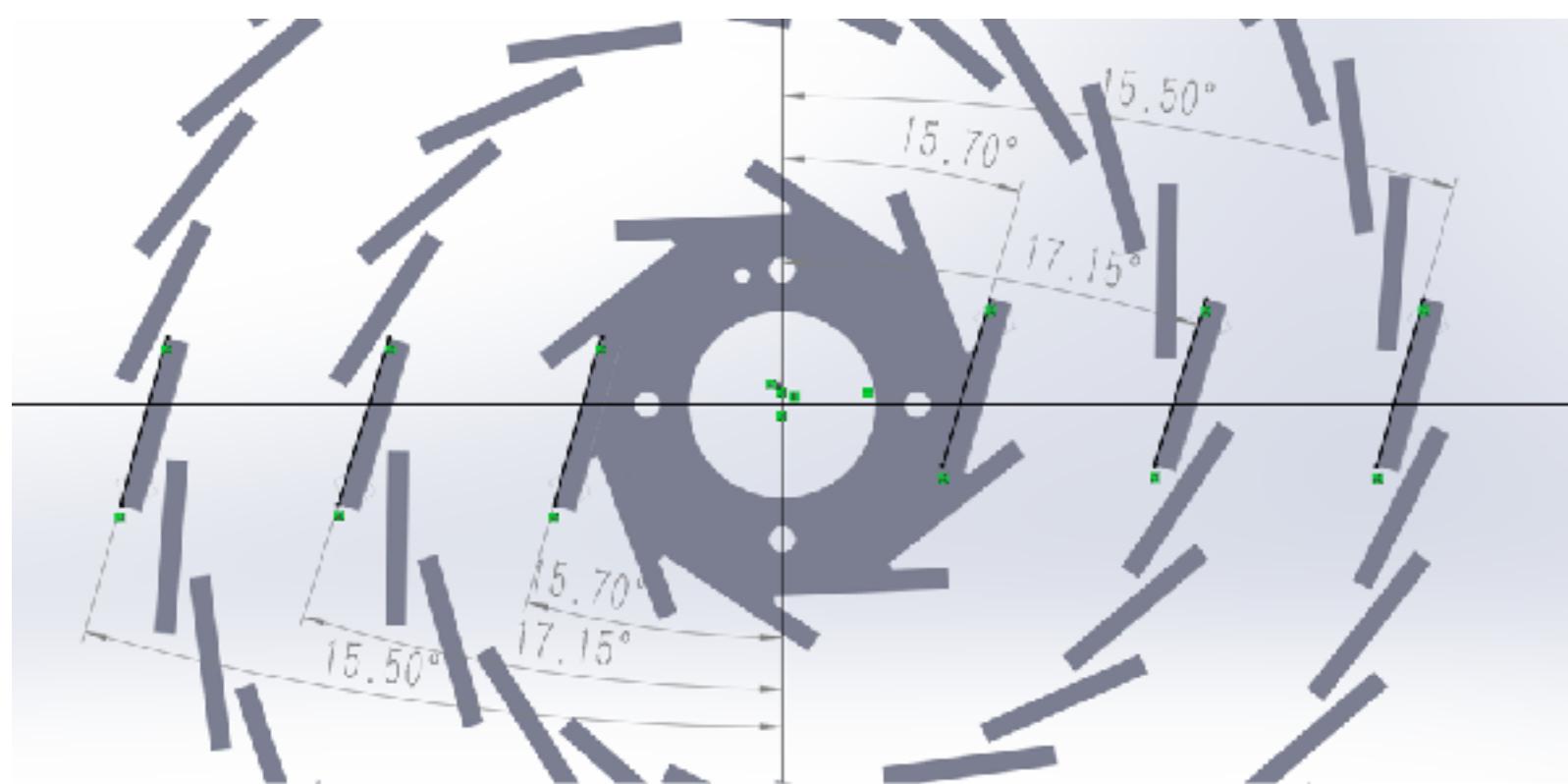


(e) Scaling 变换

图 7.4: 径迹探测器校准中的4 种线性变换效应

11 hits position fit, residual calculated from another hit

	material budget (X/X0 %)	chip0 sigma (um)	chip2 sigma (um)	chip4 sigma (um)	chip6 sigma (um)	chip8 sigma (um)	chip10 sigma (um)
50um	0.697	6.79/6.55	3.69/3.75	4.56/4.55	4.76/4.67	3.79/3.72	6.74/6.85
100um	0.804	7.12/6.95	3.82/3.84	4.91/4.85	4.99/4.99	3.86/3.79	6.91/7.32
150um	0.911	7.54/7.00	3.85/3.96	5.11/5.06	5.16/5.17	3.90/3.92	7.25/7.54



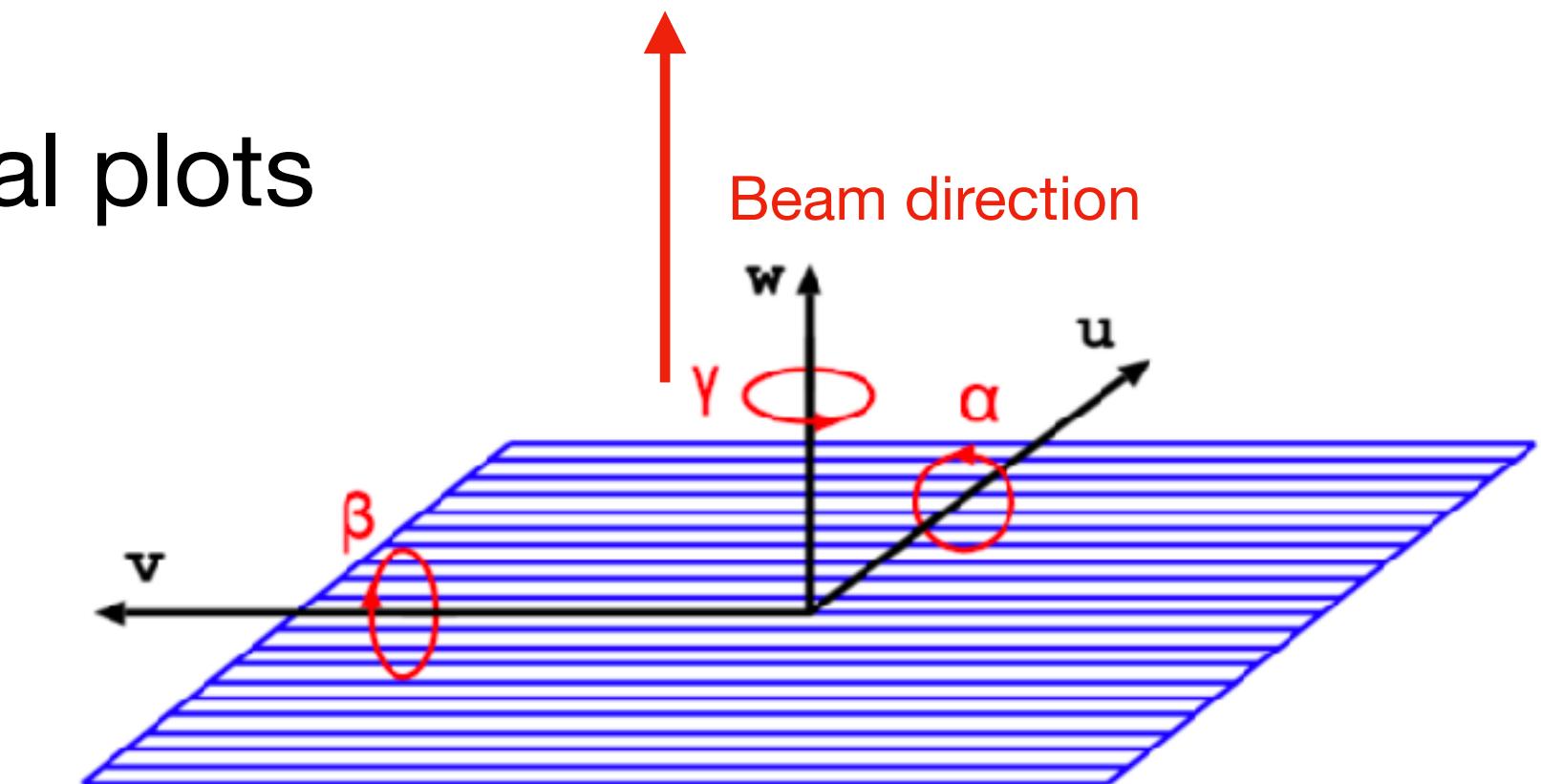
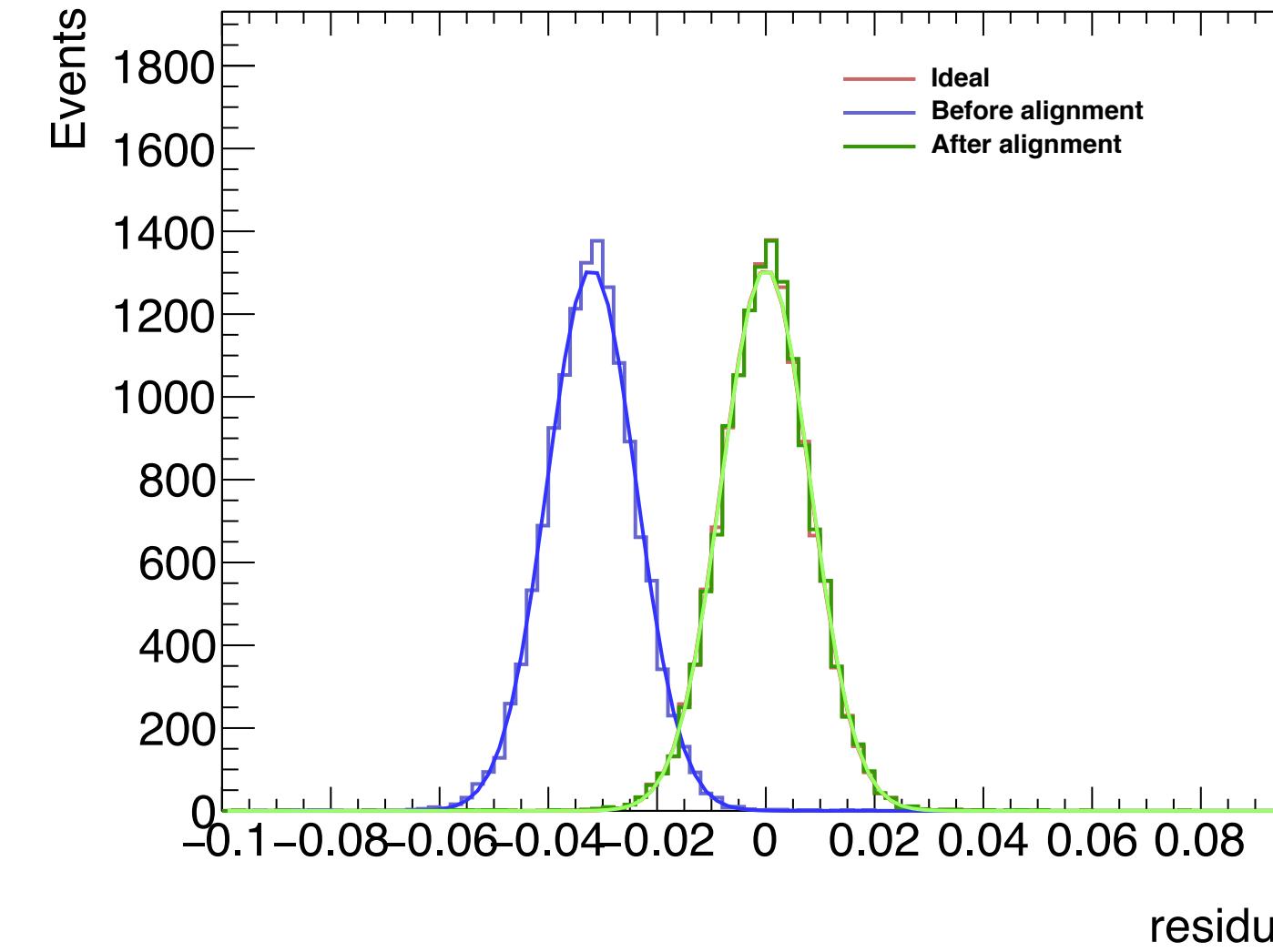
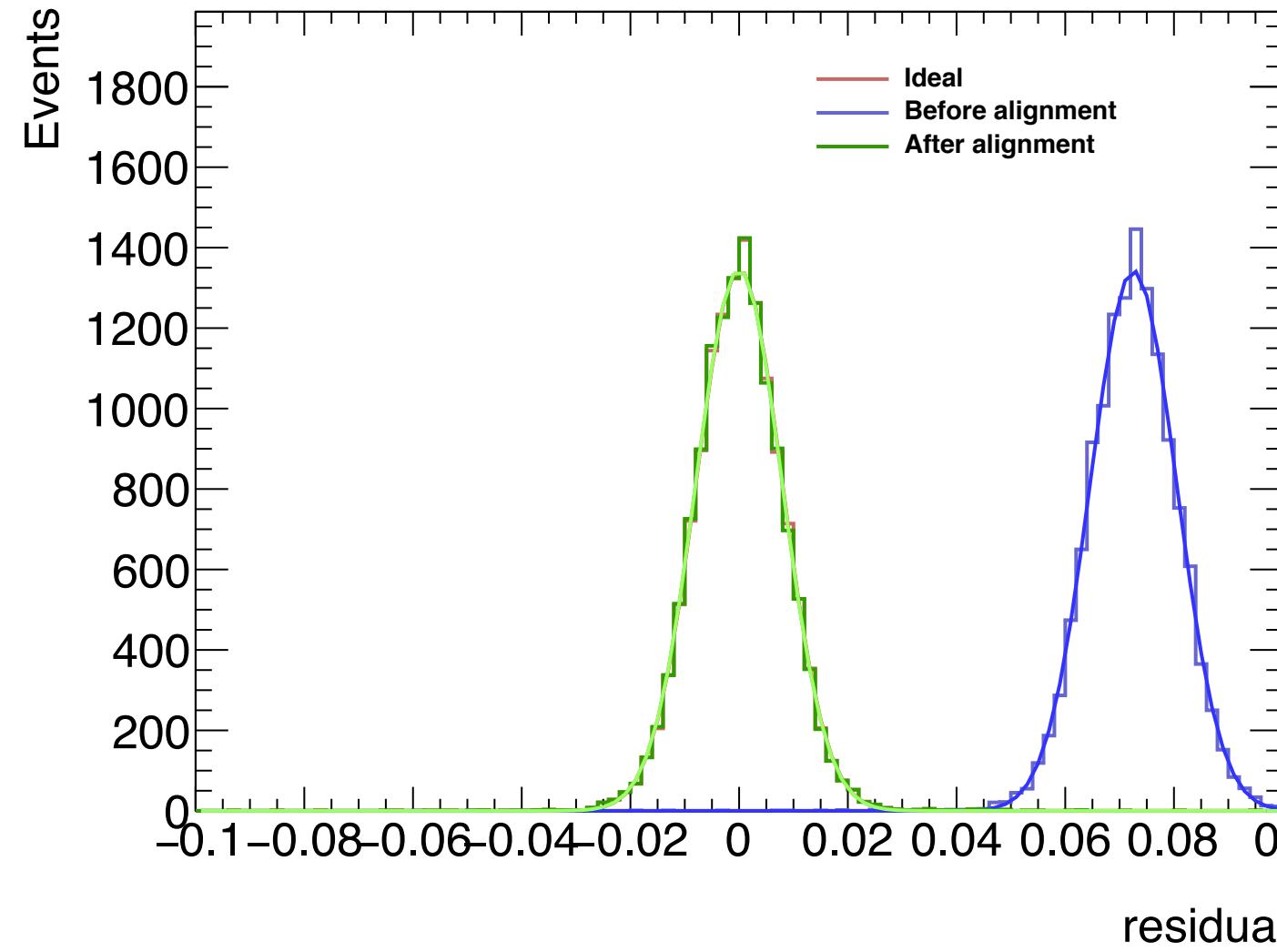
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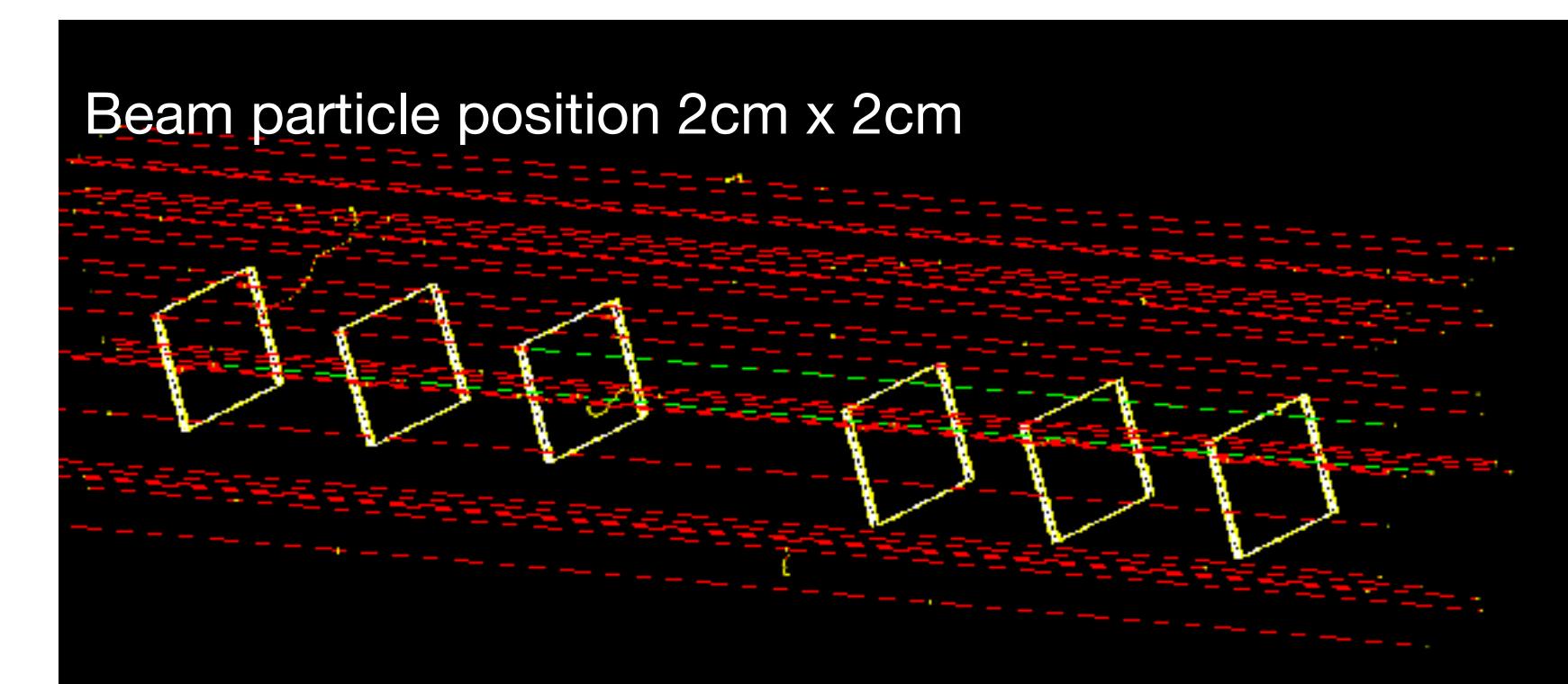
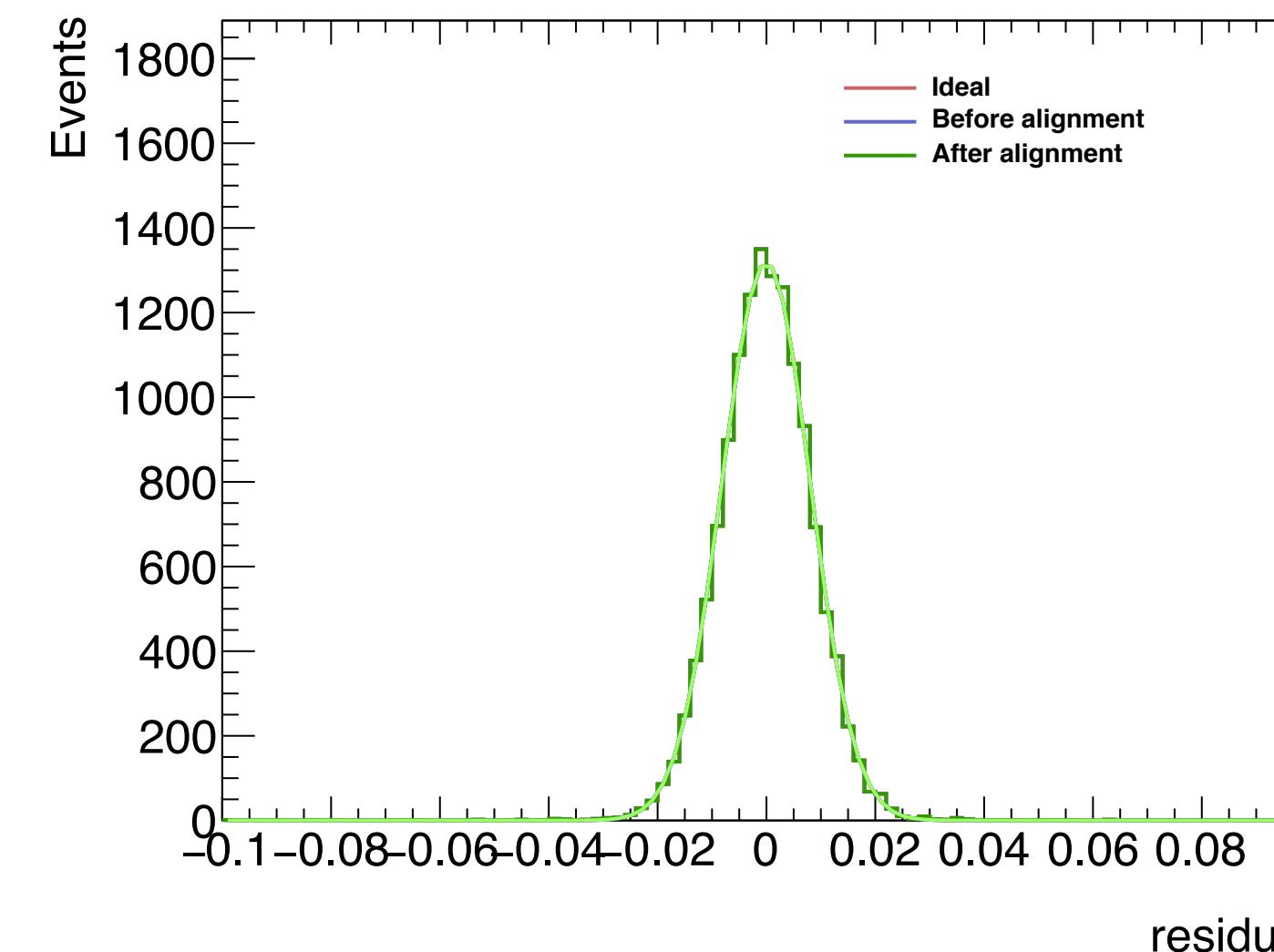
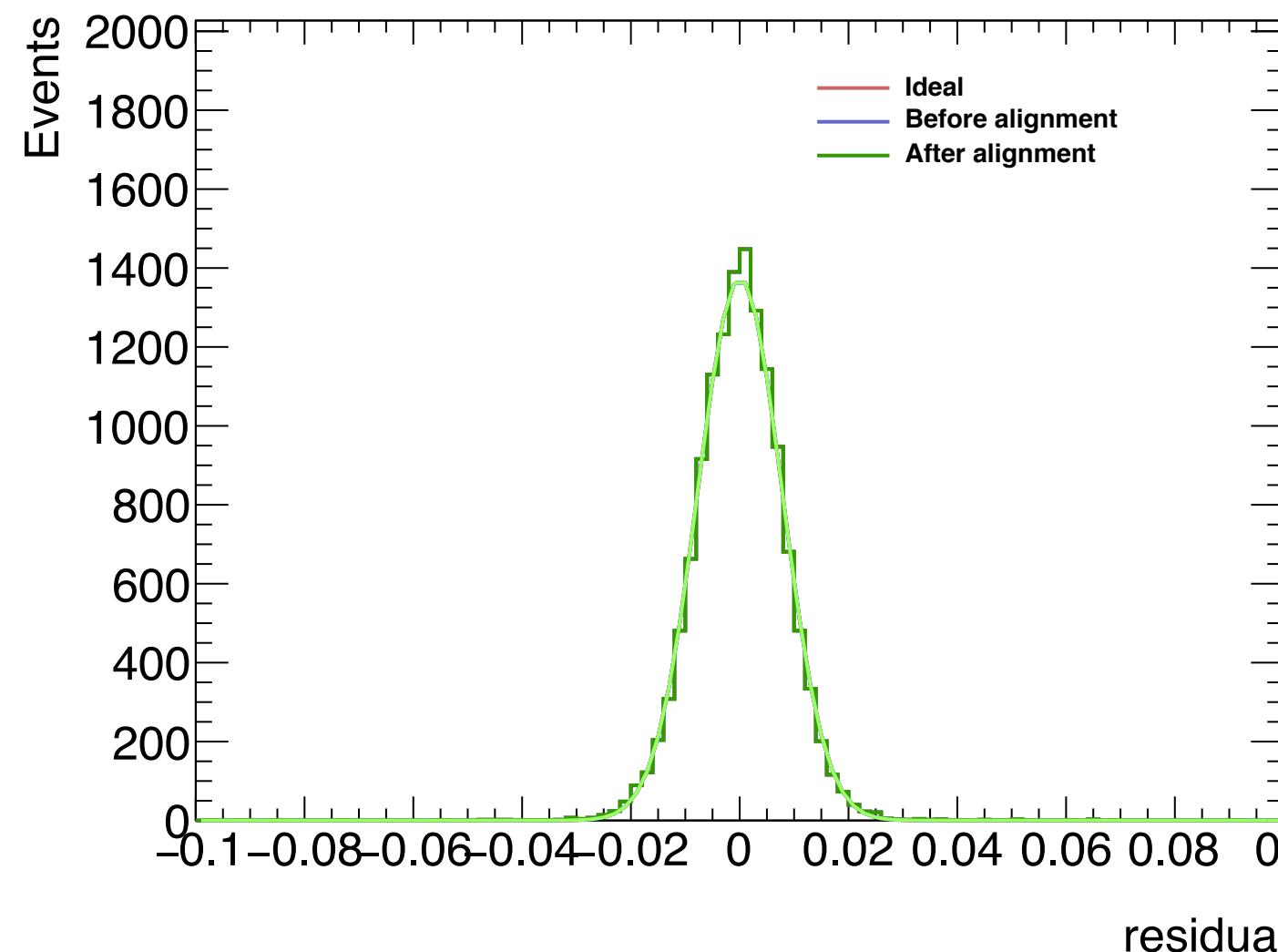
Tue, Oct13, 2022

Influence of alignment parameters on spatial resolution

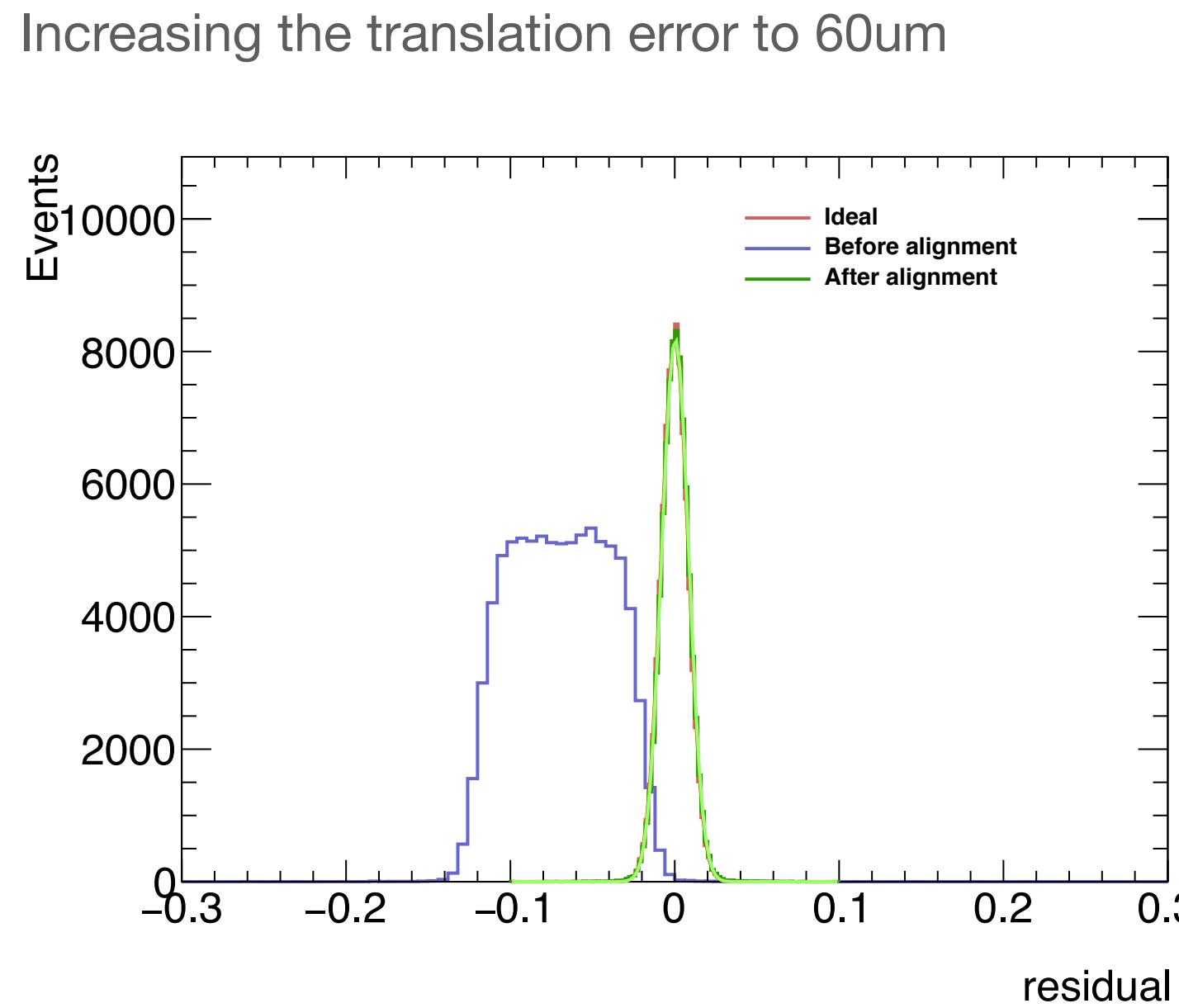
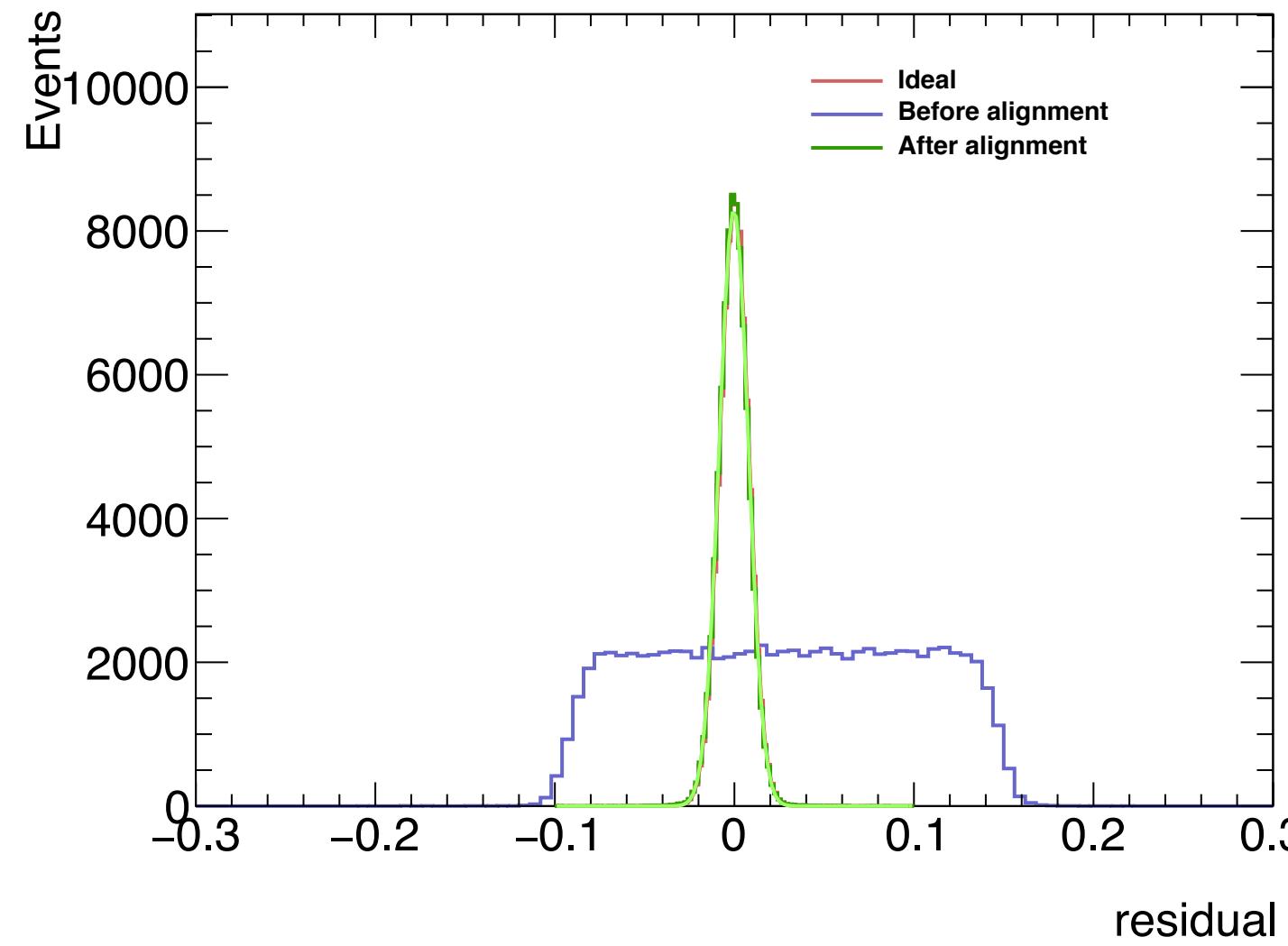
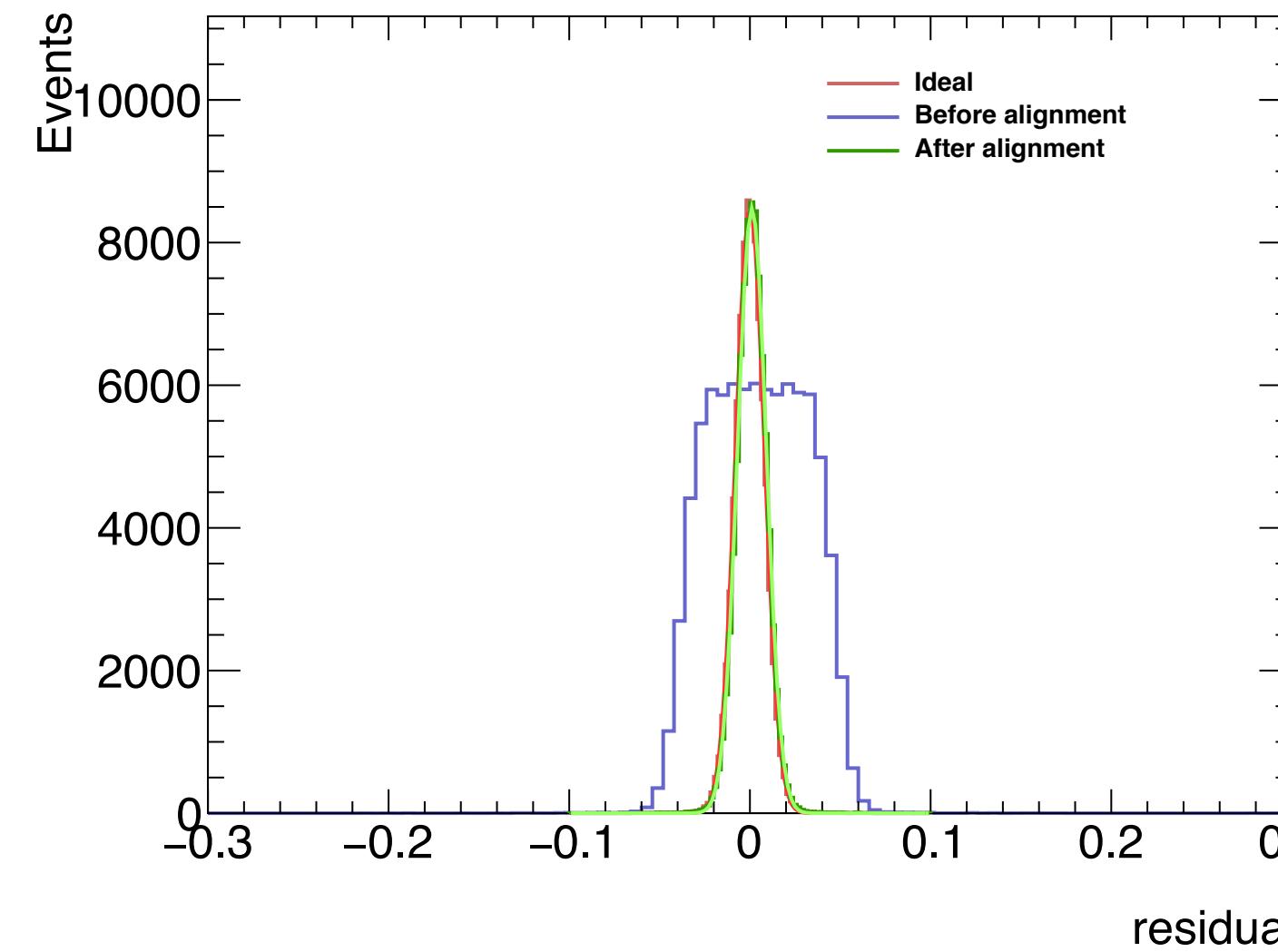
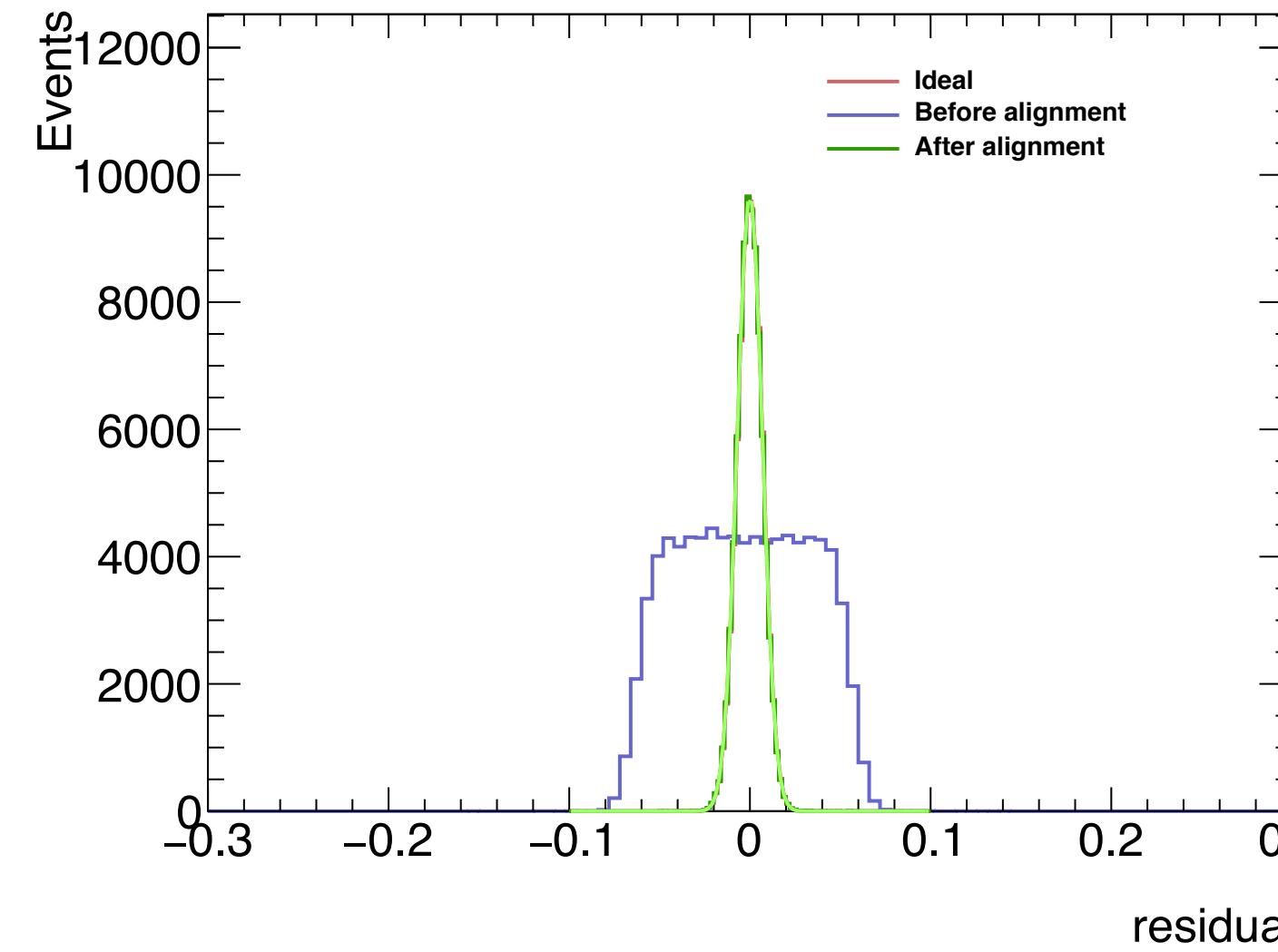
- Translation on X and Y only influence the mean value of residual plots



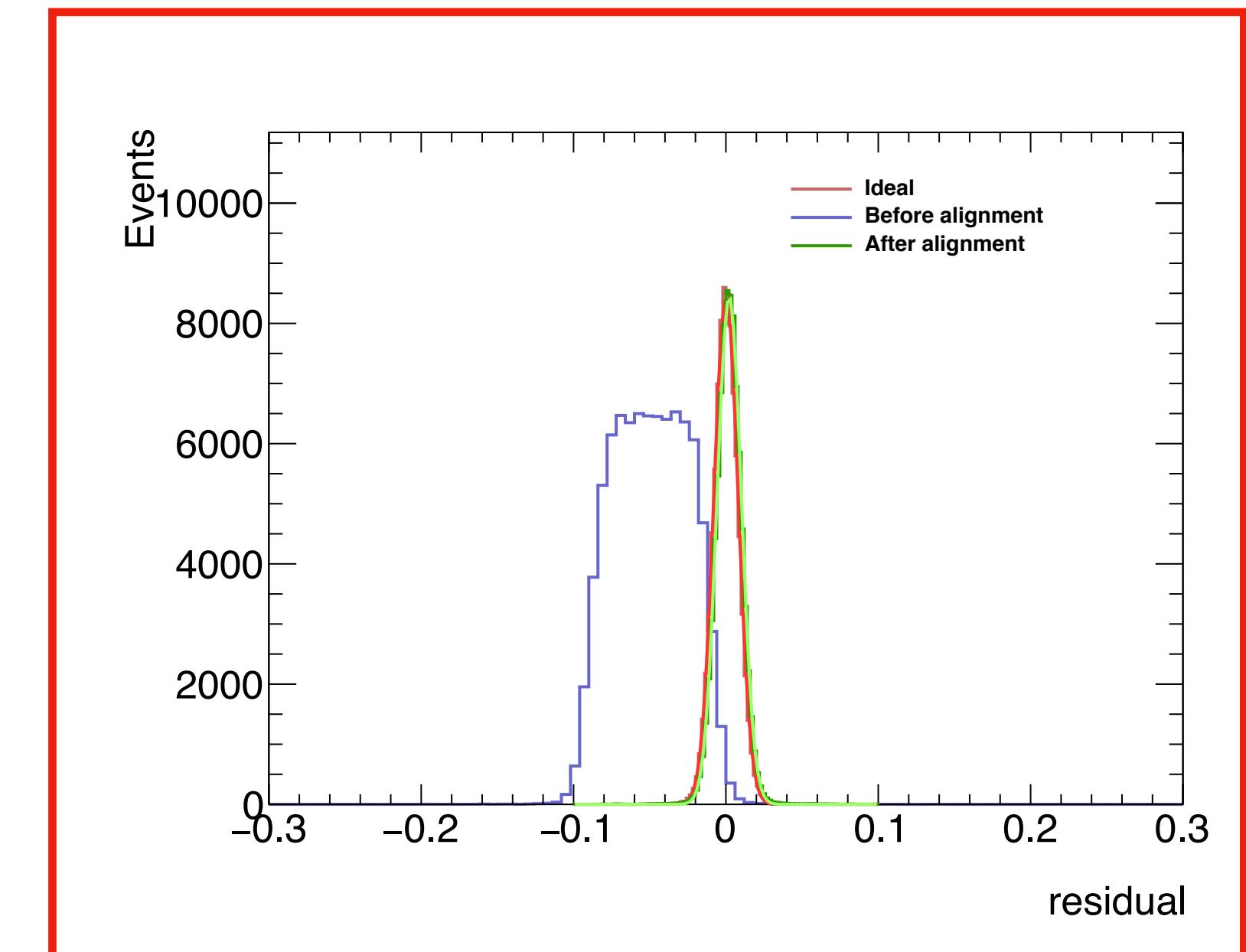
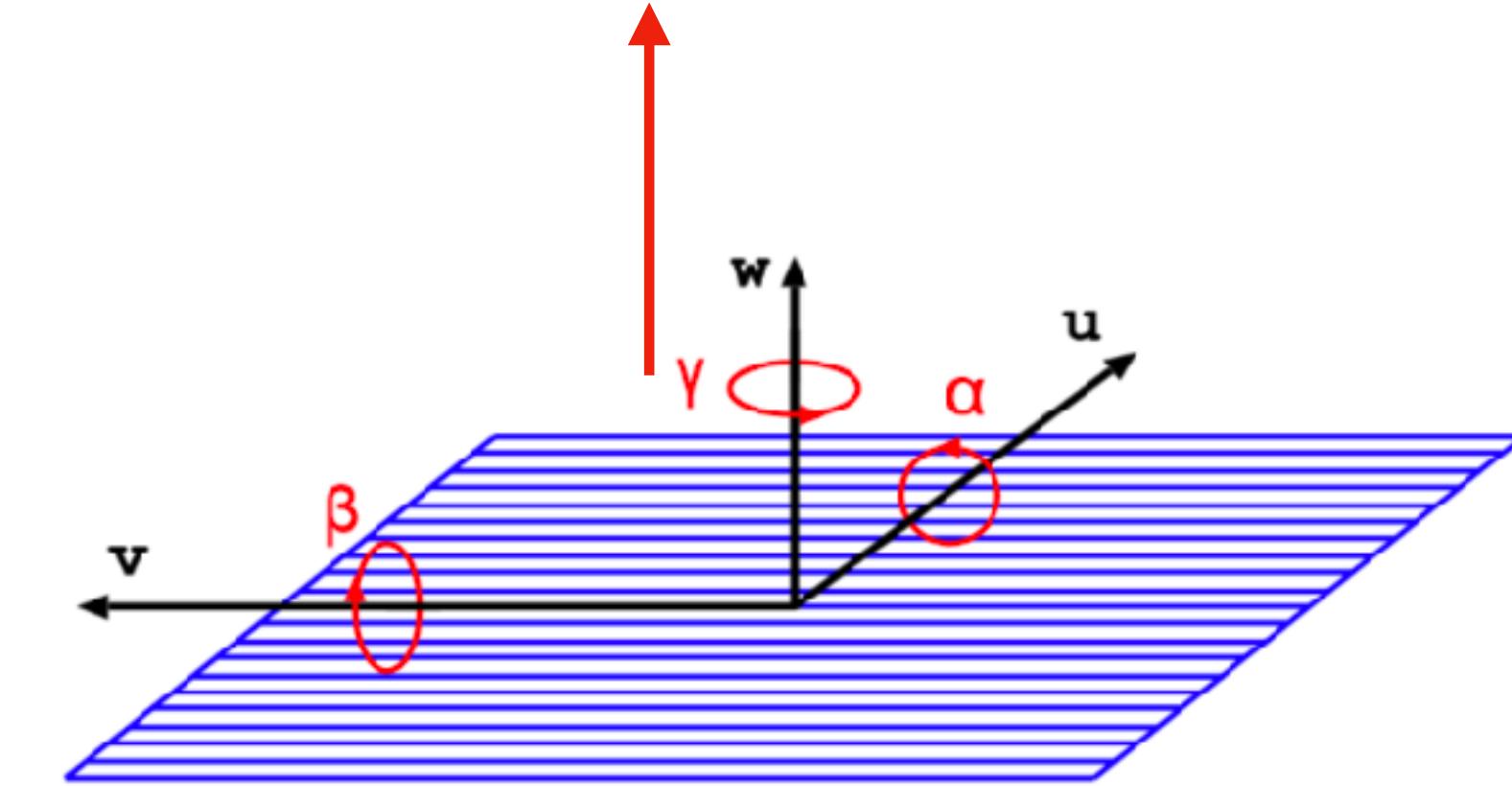
- Translation on Z and Rotation around X Y have little effect on residual plots



- Rotation around Z(beam direction) have great effect on spatial resolution



Increasing the translation error to 60um



- The horizontal assembly error is preferably within 60 microns
- The error of rotation around the beam direction is best controlled within 0.5 degrees

Summary

- I will don't consider Translation on Z and Rotation around XY alignment , only considering Translation on XY and Rotation around Z (beam direction) alignment
- I will perform 100 run Geant4 simulation and misalignment randomly, test the stability of alignment by residual plots.

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Alignment

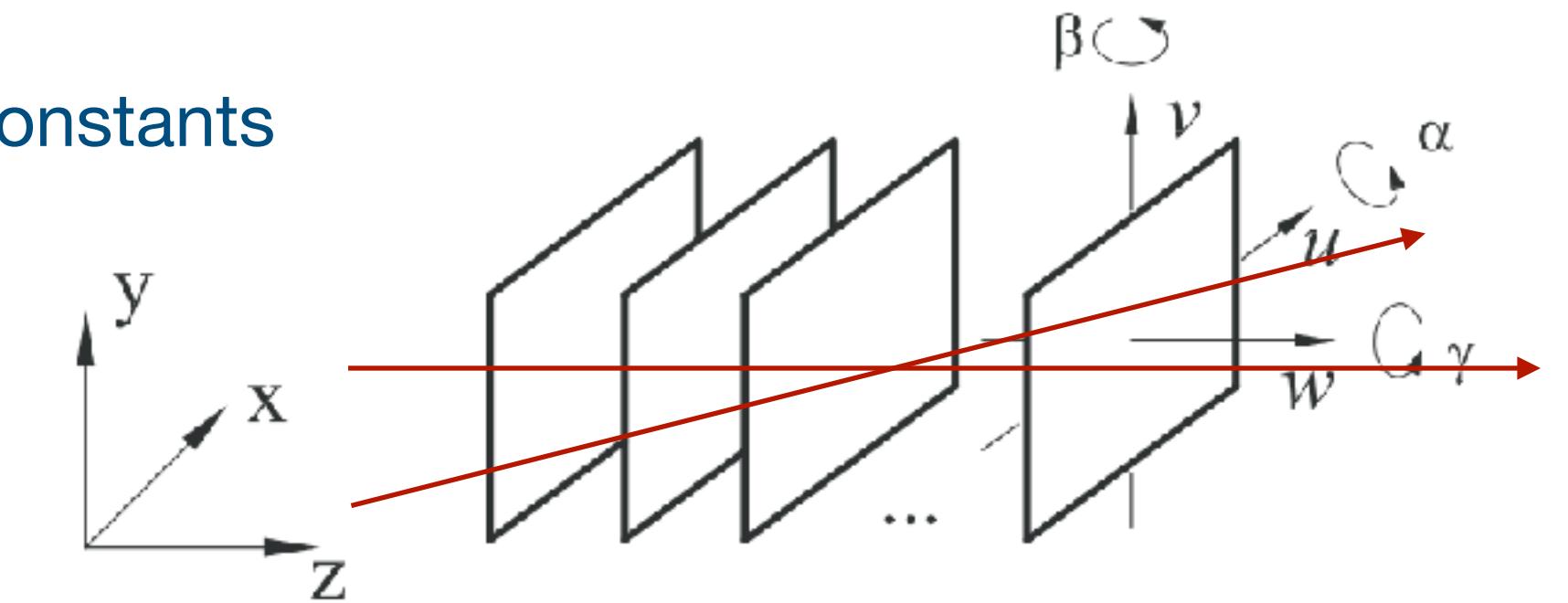
- straight line model: $x = X(z) + x_{res} = \boxed{az} + b + x_{res}; y = Y(z) + y_{res} = \boxed{cz} + d + y_{res}$
- considering misalignment

Building the linear relationship between the track parameters and the alignment constants

Simple situation (Discard the second-order miniature):

$$x_{corr}^{local} - x_{meas}^{local} = -\Delta u + y_{meas}^{local} \Delta \gamma + \boxed{a} (\Delta w + x_{meas}^{local} \Delta \beta + y_{meas}^{local} \Delta \alpha)$$

$$y_{corr}^{local} - y_{meas}^{local} = -\Delta v - x_{meas}^{local} \Delta \gamma + \boxed{c} (\Delta w + x_{meas}^{local} \Delta \beta + y_{meas}^{local} \Delta \alpha)$$



Actual situation (Discard the second-order miniature): $r_{corr} = \Delta RR(r^{global} - r_0) - \Delta r$

$$x_{corr}^{local} - x_{meas}^{local} = -\Delta u + y_{meas}^{local} \Delta \gamma + \boxed{ah}$$

$$y_{corr}^{local} - y_{meas}^{local} = -\Delta v + y_{meas}^{local} \Delta \gamma + \boxed{ch}$$

$$h = \frac{\Delta \beta x_{meas}^{local} + \Delta \alpha y_{meas}^{local} + \Delta w \cos \alpha - \Delta v \sin \alpha}{-\Delta \beta - c(\Delta \alpha + \sin \alpha) - (\Delta \alpha \sin \alpha - \cos \alpha)}$$

- minimize: $\chi^2 = \sum_{\text{data sets}} \left(\sum_{\text{events}} \left(\sum_{\text{tracks}} \left(\sum_{\text{hits}} w_i r_i^2 \right) \right) \right)$

