

Standard Model Effective Field Theory at Future Lepton Colliders

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Why lepton colliders?

- ▶ **Build large colliders → go to high energy → discover new particles!**

- ▶ Higgs and nothing else?



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— LHC will definitely find new physics!

- ▶ What's next?
 - ▶ Build an even larger collider (~ 100 TeV)?
 - ▶ No guaranteed discovery!

Why lepton colliders?

- ▶ **Build large colliders** → go to high energy → discover new particles!



do precision measurements → discover new physics indirectly!

- ▶ Higgs and nothing else?



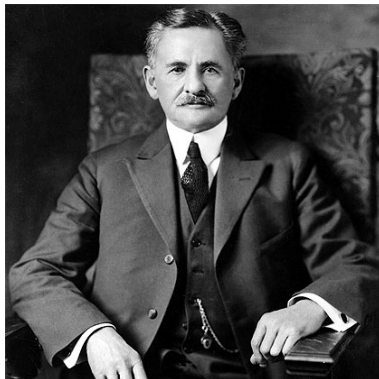
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LHC will definitely find new physics!

- ▶ What's next?

- ▶ Build an even larger collider (~ 100 TeV)?
- ▶ No guaranteed discovery!
- ▶ **Higgs factory!** (A lepton collider at $\sqrt{s} \sim 240$ -250 GeV or above.)
- ▶ **More than just a Higgs factory!** (Z, W, top, ...)
- ▶ **Standard Model Effective Field Theory** (model independent approach)

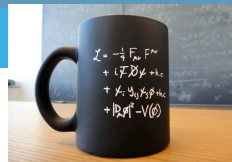
Precision is the key!



“Our future discoveries must be looked for in the sixth place of decimals.”

— Albert A. Michelson

The Standard Model Effective Field Theory

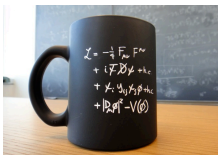


- ▶ $[\mathcal{L}_{\text{SM}}] \leq 4$. Why?
 - ▶ ~~Bad things happen when we have non-renormalizable operators!~~
 - ▶ Everything is fine as long as we are happy with finite precision in perturbative calculation.
- ▶ **d=5:** $\frac{c}{\Lambda} LLHH \sim \frac{c v^2}{\Lambda} \nu\nu$, Majorana neutrino mass.
- ▶ Assuming Baryon and Lepton numbers are conserved,

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_j \frac{c_j^{(8)}}{\Lambda^4} \mathcal{O}_j^{(8)} + \dots$$

- ▶ If $\Lambda \gg v, E$, then **SM + dimension-6 operators** are sufficient to parameterize the physics around the electroweak scale.

The Standard Model Effective Field Theory



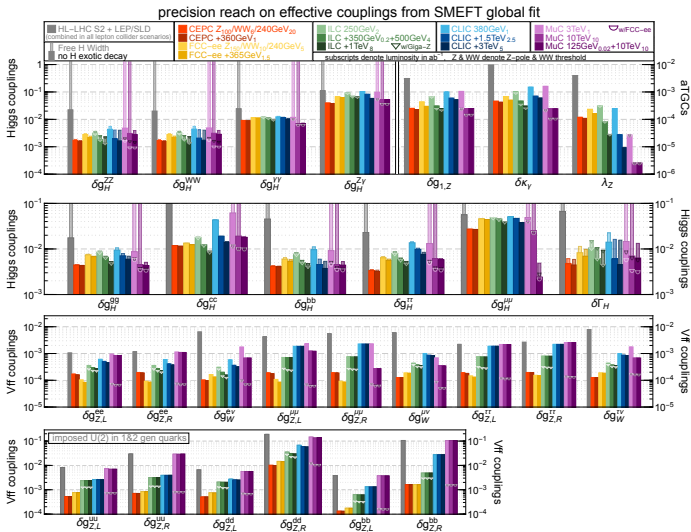
+

X^3			ψ^4 and $\psi^3 D^2$			$\psi^5 \psi^3$			$(LL)(LL)$			$(RR)(RR)$			$(LL)(RR)$		
Q_{G1}	$f^{ABC} G_{\mu\nu}^A G_{\mu\nu}^B G_{\mu\nu}^C$	Q_G	$(\psi^\dagger \psi)^3$	$Q_{\psi\psi}$	$(\psi^\dagger \psi)(\psi_\mu \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi)(\psi_\mu \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi)(\psi_\mu \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi)(\psi_\mu \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi)(\psi_\mu \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi)(\psi_\mu \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi)(\psi_\mu \psi)$
Q_{G2}	$f^{ABC} \tilde{G}_{\mu\nu}^A G_{\mu\nu}^B G_{\mu\nu}^C$	Q_{G3}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{H1}	$\psi^\dagger \psi W_{\mu\nu}^A W^{\mu\nu A}$	Q_{H2}	$(\psi^\dagger D_\mu \psi)^\dagger (\psi^\dagger D_\mu \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{H3}	$\psi^\dagger \psi \tilde{W}_{\mu\nu}^A W^{\mu\nu A}$	Q_{H4}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	$Q_{\psi\psi}$	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
$X^3 \psi^2$			$\psi^5 X \psi$			$\psi^5 \psi^2 D$			$(LL)(LL)$			$(RR)(RR)$			$(LL)(RR)$		
Q_{G1}	$\psi^\dagger \psi G_{\mu\nu}^A G^{\mu\nu A}$	Q_{G2}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G3}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G4}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G5}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G6}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G7}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G8}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G9}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G10}	$\psi^\dagger \psi \tilde{G}_{\mu\nu}^A G^{\mu\nu A}$	Q_{G11}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G12}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G13}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G14}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G15}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G16}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G17}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G18}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G19}	$\psi^\dagger \psi W_{\mu\nu}^A W^{\mu\nu A}$	Q_{G20}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G21}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G22}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G23}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G24}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G25}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G26}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G27}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G28}	$\psi^\dagger \psi \tilde{W}_{\mu\nu}^A W^{\mu\nu A}$	Q_{G29}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G30}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G31}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G32}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G33}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G34}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G35}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G36}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G37}	$\psi^\dagger \psi B_{\mu\nu} B^{\mu\nu}$	Q_{G38}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G39}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G40}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G41}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G42}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G43}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G44}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G45}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G46}	$\psi^\dagger \psi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{G47}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G48}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G49}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G50}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G51}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G52}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G53}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G54}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G55}	$\psi^\dagger \psi W_{\mu\nu}^A W^{\mu\nu A}$	Q_{G56}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G57}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G58}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G59}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G60}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G61}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G62}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G63}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G64}	$\psi^\dagger \psi \tilde{W}_{\mu\nu}^A W^{\mu\nu A}$	Q_{G65}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G66}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G67}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G68}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G69}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G70}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G71}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G72}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G73}	$\psi^\dagger \psi B_{\mu\nu} B^{\mu\nu}$	Q_{G74}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G75}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G76}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G77}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G78}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G79}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G80}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G81}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G82}	$\psi^\dagger \psi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{G83}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G84}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G85}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G86}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G87}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G88}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G89}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G90}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G91}	$\psi^\dagger \psi W_{\mu\nu}^A W^{\mu\nu A}$	Q_{G92}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G93}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G94}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G95}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G96}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G97}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G98}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G99}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G100}	$\psi^\dagger \psi \tilde{W}_{\mu\nu}^A W^{\mu\nu A}$	Q_{G101}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G102}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G103}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G104}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G105}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G106}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G107}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G108}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G109}	$\psi^\dagger \psi B_{\mu\nu} B^{\mu\nu}$	Q_{G110}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G111}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G112}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G113}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G114}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G115}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G116}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G117}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$
Q_{G118}	$\psi^\dagger \psi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{G119}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G120}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G121}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G122}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G123}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G124}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G125}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$	Q_{G126}	$(\psi^\dagger \psi) \Box (\psi^\dagger \psi)$

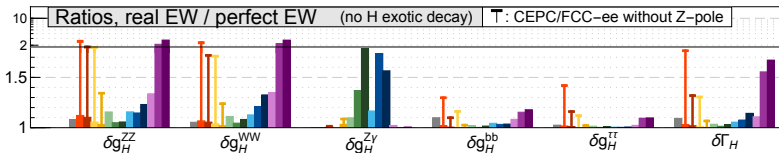
- Write down all possible (non-redundant) dimension-6 operators ...
- 59 operators (76 parameters) for 1 generation, or 2499 parameters for 3 generations. [arXiv:1008.4884] Grzadkowski, Iskrzyński, Misiak, Rosiek, [arXiv:1312.2014] Alonso, Jenkins, Manohar, Trott.
- A full global fit with all measurements to all operator coefficients?
 - We usually only need to deal with a subset of them, e.g. $\sim 20-30$ parameters for Higgs and electroweak measurements.
- Do a global fit and present the results with some fancy bar plots!

Higgs + EW, Results from the Snowmass 2021 (2022) study

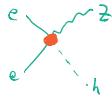
[2206.08326] de Blas, Du, Grojean, JG, Miralles, Peskin, Tian, Vos, Vryonidou



Impacts of (lack of) the Z-pole run



- ▶ Without good Z-pole measurements, the $eeZh$ contact interaction may have a significant impact on the Higgs coupling determination.
- ▶ Current (LEP) Z-pole measurements are not good enough for CEPC/FCC-ee Higgs measurements!
 - ▶ **A future Z-pole run is important!**
- ▶ Linear colliders suffer less from the lack of a Z-pole run. **(Win Win!)**



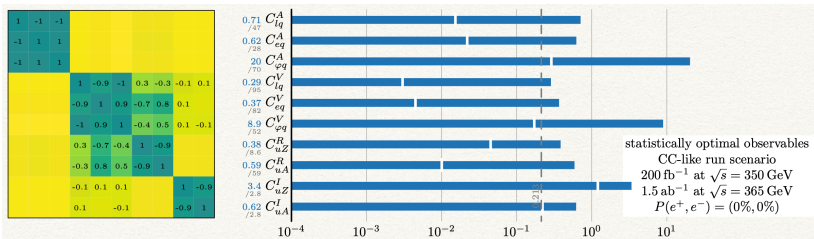
Probing Top operators with $e^-e^+ \rightarrow t\bar{t}$

[arXiv:1807.02121] Durieux, Perelló, Vos, Zhang

$$\begin{aligned}
 O_{\varphi q}^1 &\equiv \frac{y_t^2}{2} \bar{q}\gamma^\mu q \varphi^\dagger i\overleftrightarrow{D}_\mu \varphi, & O_{uG} &\equiv y_t g_s \bar{q} T^A \sigma^{\mu\nu} u \epsilon \varphi^* G_{\mu\nu}^A, \\
 O_{\varphi q}^3 &\equiv \frac{y_t^2}{2} \bar{q}\tau^I \gamma^\mu q \varphi^\dagger i\overleftrightarrow{D}_\mu \varphi, & O_{uW} &\equiv y_t g_W \bar{q}\tau^I \sigma^{\mu\nu} u \epsilon \varphi^* W_{\mu\nu}^I, \\
 O_{\varphi u} &\equiv \frac{y_t^2}{2} \bar{u}\gamma^\mu u \varphi^\dagger i\overleftrightarrow{D}_\mu \varphi, & O_{dW} &\equiv y_t g_W \bar{q}\tau^I \sigma^{\mu\nu} d \epsilon \varphi^* W_{\mu\nu}^I, \\
 O_{\varphi ud} &\equiv \frac{y_t^2}{2} \bar{u}\gamma^\mu d \varphi^T \epsilon i D_\mu \varphi, & O_{uB} &\equiv y_t g_Y \bar{q}\sigma^{\mu\nu} u \epsilon \varphi^* B_{\mu\nu},
 \end{aligned}$$

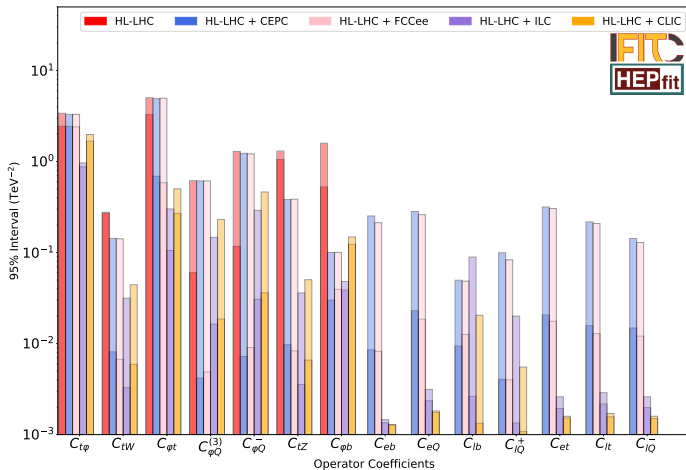
$$\begin{aligned}
 O_{lq}^1 &\equiv \frac{1}{2} \bar{q}\gamma_\mu q \bar{l}\gamma^\mu l, \\
 O_{lq}^3 &\equiv \frac{1}{2} \bar{q}\tau^I \gamma_\mu q \bar{l}\tau^I \gamma^\mu l, \\
 O_{lu} &\equiv \frac{1}{2} \bar{u}\gamma_\mu u \bar{l}\gamma^\mu l, \\
 O_{eq} &\equiv \frac{1}{2} \bar{q}\gamma_\mu q \bar{e}\gamma^\mu e, \\
 O_{eu} &\equiv \frac{1}{2} \bar{u}\gamma_\mu u \bar{e}\gamma^\mu e,
 \end{aligned}$$

- ▶ Also need to include **top dipole** interactions and **eett** contact interactions!
- ▶ Hard to resolve the **top couplings** from **4f** interactions with just the 365 GeV run.
 - ▶ Can't really separate $e^+e^- \rightarrow Z/\gamma \rightarrow t\bar{t}$ from $e^+e^- \rightarrow Z' \rightarrow t\bar{t}$.
 - ▶ Is that a big deal?



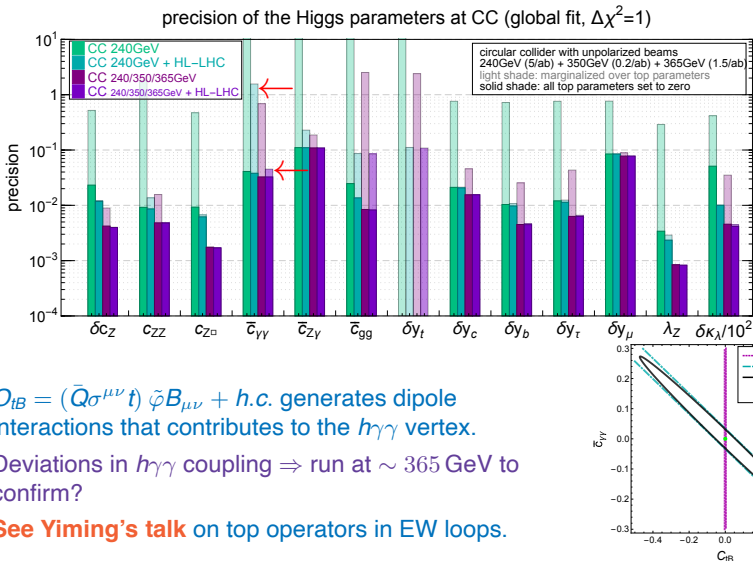
Results from the recent snowmass study

[2206.08326] de Blas, Du, Grojean, JG, Miralles, Peskin, Tian, Vos, Vryonidou



Top operators in loops (Higgs processes)

[1809.03520] G. Durieux, JG, E. Vryonidou, C. Zhang



Machine learning in SMEFT analyses

Machine learning is not physics!



past

真香！

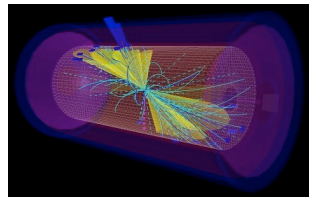
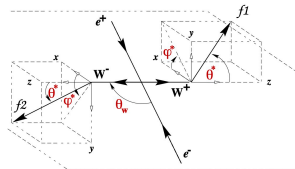


now

- ▶ Current work with Shengdu Chai (柴声都), Lingfeng Li (李凌风) on $e^+e^- \rightarrow WW$.
- ▶ Current work with Yifan Fei (费昶帆), Tong Shen (沈同) and Kerun Yu (余柯润) on $e^+e^- \rightarrow t\bar{t}$.

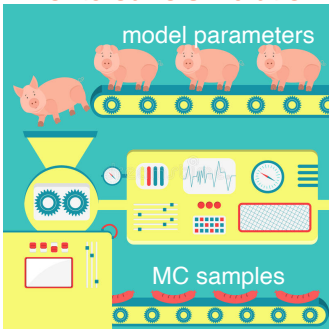
Why Machine learning?

- ▶ In many cases, the new physics contributions are sensitive to the differential distributions.
 - ▶ $e^+e^- \rightarrow WW \rightarrow 4f \Rightarrow 5 \text{ angles}$
 - ▶ $e^+e^- \rightarrow t\bar{t} \rightarrow bW^+ \bar{b}W^- \rightarrow 6f \Rightarrow 9 \text{ angles}$
 - ▶ How to extract information from the differential distribution?
 - ▶ If we have the full knowledge of $\frac{d\sigma}{d\Omega} \Rightarrow$ matrix-element method, optimal observables...
- ▶ The ideal $\frac{d\sigma}{d\Omega}$ we can calculate is not the $\frac{d\sigma}{d\Omega}$ that we actually measure!
 - ▶ detector acceptance, measurement uncertainties, ISR/beamstrahlung ...
 - ▶ In practice we only have **MC samples**, not analytic expressions, for $\frac{d\sigma}{d\Omega}$.

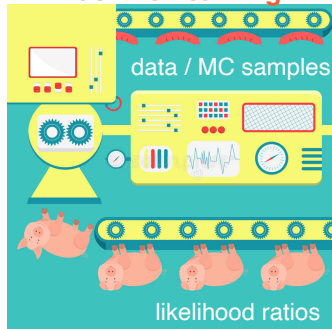


The “inverse problem”

Monte Carlo simulation



Machine Learning

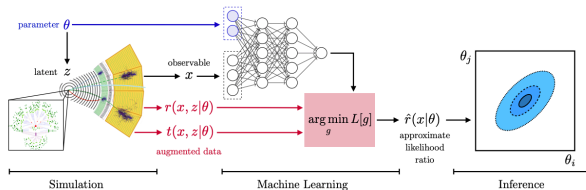


- ▶ **Forward:** From model parameters we can calculate the ideal $\frac{d\sigma}{d\Omega}$, simulate complicated effects and produce MC samples.
- ▶ **Inverse:** From data / MC samples, how do we know the model parameters?
- ▶ With **Neural Network** we can (in principle) reconstruct $\frac{d\sigma}{d\Omega}$ (or likelihood ratios) from MC samples.

Particle physics structure

- One could make use of **latent variable “ z ”** (the parton level analytic result for $\frac{d\sigma}{d\Omega}$) to increase the performance of ML.

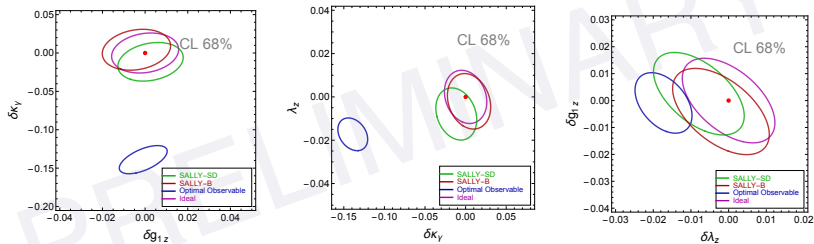
[1805.00013, 1805.00020] Brehmer, Cranmer, Louppe, Pavez



- Assuming linear dependences $\frac{d\sigma}{d\Omega} = S_0 + \sum_i S_{1,i} c_i$, there is a method called **SALLY** (Score approximates likelihood locally).
 - In this case, for each parameter we only need to train once to obtain $\alpha_i \equiv \frac{S_{1,i}}{S_0}$. (It is basically the ML version of Optimal Observables.)
 - We can calculate the “ideal” $\alpha(z)$ which will help us train the actual $\alpha(x)$.

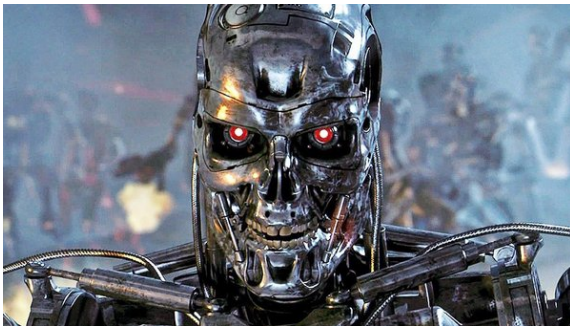
$$L[\hat{\alpha}(x)] = \sum_{x_i, z_i \sim \text{SM}} |\alpha(z_i) - \hat{\alpha}(x_i)|^2.$$

Machine Learning in $e^+e^- \rightarrow WW$ (preliminary results, Shengdu Chai, JG, Lingfeng Li)



- ▶ 3-aTGC fit, scaled to 10^4 events.
 - ▶ OO+classifier: hybrid method that uses a classifier to discriminate background.
- ▶ Naively applying truth-level optimal observables could lead to a large bias!
- ▶ It's easier for machine learning to take care of systematics!

Machine learning



- ▶ **When will Machine take over?**
 - ▶ Before or after a future lepton collider is built?

Conclusion

- ▶ **We have no idea what is the new physics beyond the Standard Model.**
- ▶ **One important direction to move forward is to do precision measurements of the Standard Model processes.**
 - ▶ A future lepton collider is an ideal machine for that.
 - ▶ SMEFT is a good theory framework (but is not everything).
 - ▶ Expanding the theory framework?
 - ▶ Loop contributions, dimension-8 operators, HEFT ...
- ▶ **Machine learning is (likely to be) the future!**

Conclusion



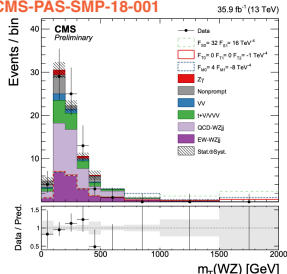
Waiting for a future lepton collider to be built...

backup slides

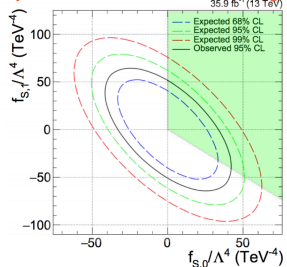
Probing dimension-8 operators?

- ▶ The dimension-8 contribution has a large energy enhancement ($\sim E^4/\Lambda^4$)!
- ▶ It is difficult for LHC to probe these bounds.
 - ▶ Low statistics in the high energy bins.
 - ▶ Example: Vector boson scattering.
 - ▶ $\Lambda \lesssim \sqrt{s}$, the EFT expansion breaks down!
- ▶ Can we separate the dim-8 and dim-6 effects?
 - ▶ Precision measurements at several different \sqrt{s} ?
(A **very** high energy lepton collider?)
 - ▶ Or find some special process where dim-8 gives the leading new physics contribution?

CMS-PAS-SMP-18-001



positivity bounds from 1902.08977 Bi, Zhang, Zhou

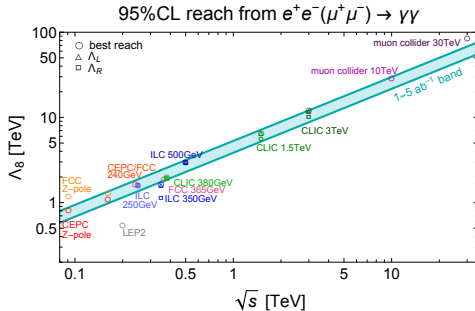
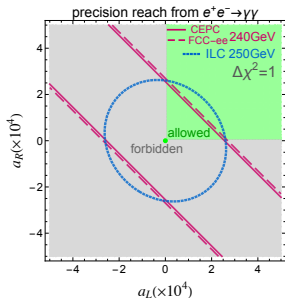


The diphoton channel [arXiv:2011.03055] Phys.Rev.Lett. 129, 011805, JG, Lian-Tao Wang, Cen Zhang

- ▶ $e^+e^- \rightarrow \gamma\gamma$ (or $\mu^+\mu^- \rightarrow \gamma\gamma$), SM, non-resonant.
- ▶ Leading order contribution: **dimension-8 contact interaction**.
($f^+f^- \rightarrow \bar{e}_L e_L$ or $e_R \bar{e}_R$)

$$\mathcal{A}(f^+f^-\gamma^+\gamma^-)_{\text{SM+d8}} = 2e^2 \frac{\langle 24 \rangle^2}{\langle 13 \rangle \langle 23 \rangle} + \frac{a}{v^4} [13][23] \langle 24 \rangle^2.$$

- ▶ Can probe dim-8 operators (and their positivity bounds) at a **Higgs factory** (~ 240 GeV)!



A rough sketch

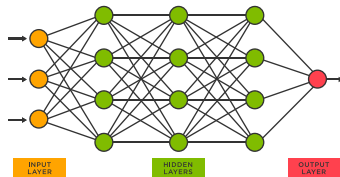
- ▶ We have a theory (SMEFT) that gives a differential cross section $\frac{d\sigma}{d\Omega}$ which is a function of the parameters of interest \mathbf{c} (Wilson coefficients).
 - ▶ For simplicity, let's ignore the total rate and focus on $\frac{1}{\sigma} \frac{d\sigma}{d\Omega} \equiv p(\mathbf{x}|\mathbf{c})$, i.e. it's a probability density function of the observables \mathbf{x} .
 - ▶ Define the likelihood function $\mathcal{L}(\mathbf{c}|\mathbf{x}) \equiv p(\mathbf{x}|\mathbf{c})$. For a sample of N events, maximizing the joint likelihood $\prod_{i=1}^N \mathcal{L}(\mathbf{c}|\mathbf{x}_i)$ (or the log likelihood) gives the best estimator for \mathbf{c} . (matrix-element method)
- ▶ Suppose we have two equal-size samples $\{\mathbf{x}_{i,\mathbf{c}_0}\} \sim p(\mathbf{x}|\mathbf{c}_0)$ and $\{\mathbf{x}_{i,\mathbf{c}_1}\} \sim p(\mathbf{x}|\mathbf{c}_1)$, one could define the cross-entropy loss function(al)

$$L(\hat{s}) = -\sum_{i=1}^N \log \hat{s}(\mathbf{x}_{i,\mathbf{c}_1}) - \sum_{i=1}^N \log (1 - \hat{s}(\mathbf{x}_{i,\mathbf{c}_0})) ,$$

which is minimized by the optimal decision function

$$s(\mathbf{x}|\mathbf{c}_0, \mathbf{c}_1) = \frac{p(\mathbf{x}|\mathbf{c}_1)}{p(\mathbf{x}|\mathbf{c}_0) + p(\mathbf{x}|\mathbf{c}_1)} .$$

A rough sketch



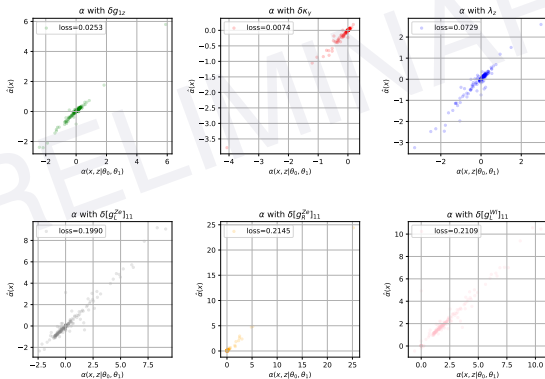
- From **neural network** we can construct a function $\hat{s}(\mathbf{x})$. By minimizing $L(\hat{s})$ with respect to $\hat{s}(\mathbf{x})$ we can obtain an estimator for the likelihood ratio

$$\hat{r}(\mathbf{x}|\mathbf{c}_0, \mathbf{c}_1) = \frac{1 - \hat{s}(\mathbf{x}|\mathbf{c}_0, \mathbf{c}_1)}{\hat{s}(\mathbf{x}|\mathbf{c}_0, \mathbf{c}_1)} = \frac{\hat{p}(\mathbf{x}|\mathbf{c}_0)}{\hat{p}(\mathbf{x}|\mathbf{c}_1)},$$

which is the same as the true likelihood ratio in the ideal limit (large sample, perfect training).

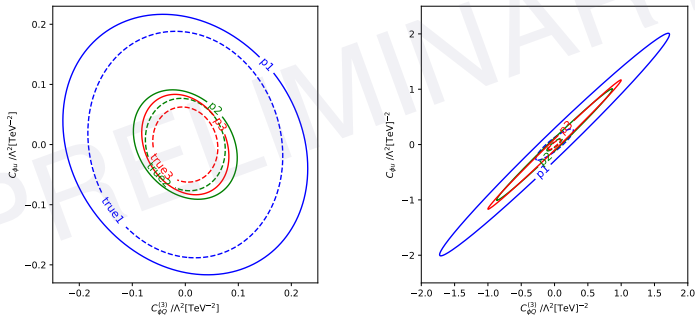
- There are many other ways to construct a loss function(al)....
- With additional assumptions on how $\frac{d\sigma}{d\Omega}$ depends on \mathbf{c} (i.e., a quadratic relation), we only need to train a finite number of times to know how the likelihood ratio depend on \mathbf{c} .

Machine Learning in $e^+e^- \rightarrow WW$ (preliminary results, Shengdu Chai, JG, Lingfeng Li)



- Semileptonic channel, MadGraph/Pythia/Delphes (CEPC detector card), with ZZ backgrounds.

Machine Learning in $e^+e^- \rightarrow t\bar{t}$ (very preliminary results, Yifan Fei, JG, Tong Shen, Kerun Yu)



- ▶ $e^+e^- \rightarrow t\bar{t}$, 3 different channels (no background yet)
- ▶ **Left:** $\sqrt{s} = 1 \text{ TeV}$, **Right:** $\sqrt{s} = 360 \text{ GeV}$

$e^+e^- \rightarrow WW$ with Optimal Observables

- ▶ TGCs (and additional EFT parameters) are sensitive to the differential distributions!

- ▶ One could do a fit to the binned distributions of all angles.
- ▶ Not the most efficient way of extracting information.
- ▶ Correlations among angles are sometimes ignored.

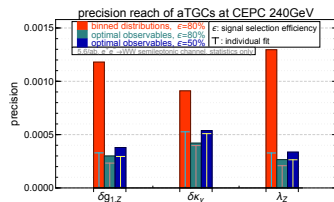
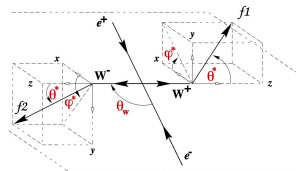
- ▶ What are optimal observables?

(See e.g. Z.Phys. C62 (1994) 397-412 Diehl & Nachtmann)

- ▶ In the limit of large statistics (everything is Gaussian) and small parameters (linear contribution dominates), the **best possible reaches** can be derived analytically!

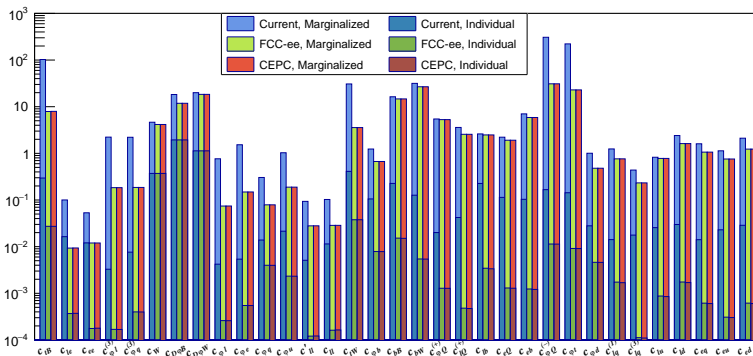
$$\frac{d\sigma}{d\Omega} = S_0 + \sum_i S_{1,i} g_i, \quad c_{ij}^{-1} = \int d\Omega \frac{S_{1,i} S_{1,j}}{S_0} \cdot \mathcal{L},$$

- ▶ The optimal observables are given by $\mathcal{O}_i = \frac{S_{1,i}}{S_0}$, and are functions of the 5 angles.



[arXiv:1907.04311] de Blas, Durieux, Grojean, JG, Paul

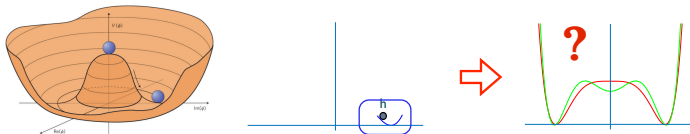
Top operators in loops (EW processes) [2205.05655] Y. Liu, Y. Wang, C. Zhang, L. Zhang, JG



- Top operators (1-loop) + EW operators (tree, including bottom dipole operators)
- Good sensitivities, but too many parameters for a global fit...
- It shows the importance of directly measuring $e^+e^- \rightarrow t\bar{t}$.

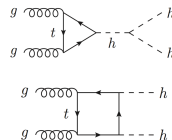
Higgs self-coupling

- ▶ We know very little about the Higgs potential!



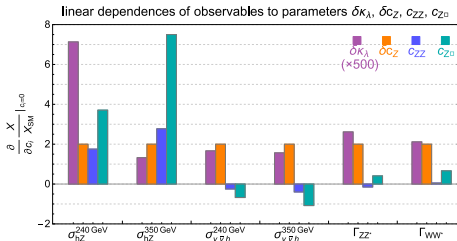
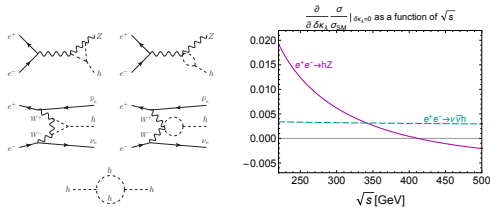
- ▶ To know more about the Higgs potential, we need to measure the Higgs self-couplings (**hhh** and **hhhh** couplings).
- ▶ The $(H^\dagger H)^3$ operator can modify the Higgs self-couplings.
- ▶ Probing the **hhh** coupling at Hadron colliders.

- ▶ $gg \rightarrow hh$
- ▶ $\lesssim 50\%$ at HL-LHC.
- ▶ $\lesssim 5\%$ at a 100 TeV collider.



Triple Higgs coupling at one-loop order

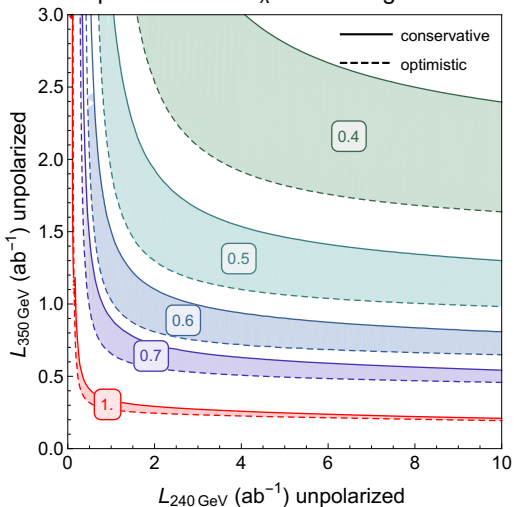
[arXiv:1711.03978] Di Vita, Durieux, Grojean, JG, Liu, Panico, Riembau, Vantalon



- $\kappa_\lambda \equiv \frac{\lambda_{hhh}}{\lambda_{SM}^{hhh}}$,
 $\delta\kappa_\lambda \equiv \kappa_\lambda - 1 = C_6 - \frac{3}{2}C_H$,
 with $\mathcal{L} \supset -\frac{c_6\lambda}{v^2}(H^\dagger H)^3$.
- One loop corrections to all Higgs couplings (production and decay).
- 240 GeV: hZ near threshold (more sensitive to $\delta\kappa_\lambda$)
- at 350-365 GeV:
 - WW fusion
 - hZ at a different energy
- $h \rightarrow WW^*/ZZ^*$ also have some discriminating power (but turned out to be not enough).

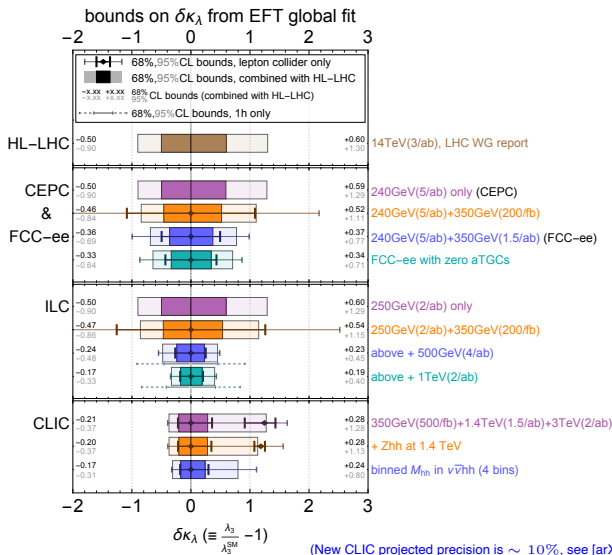
Triple Higgs coupling from EFT global fits

precision on $\delta\kappa_\lambda$ from EFT global fit

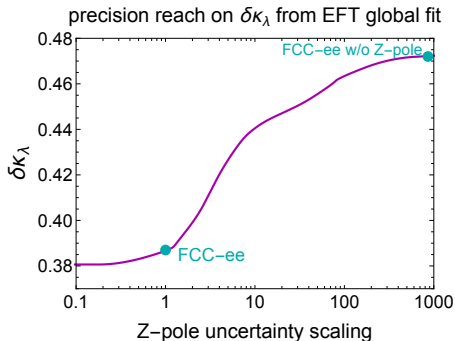
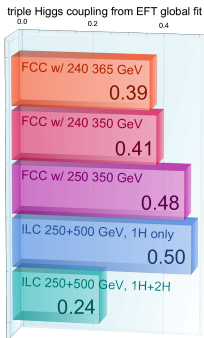


- Runs at two different energies (240 GeV and 350/365 GeV) are needed to obtain good constraints on the triple Higgs coupling in a global fit!

Triple Higgs coupling from global fits [arXiv:1711.03978]



Updates on the triple Higgs coupling determination from EFT global fits

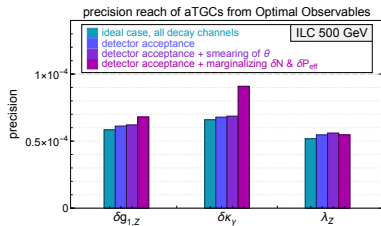
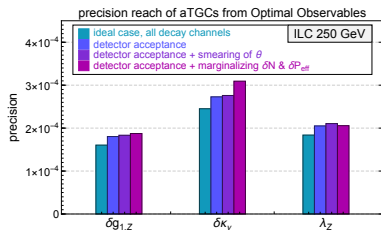


- ▶ 240, 365 GeV are better than 250, 350 GeV.
- ▶ Impacts of Z-pole measurements are not negligible.
($eeZ(h)$ contact interaction enters $e^+e^- \rightarrow hZ$.)



Updates on the WW analysis with Optimal Observables

- ▶ How well can we do it in practice?
 - ▶ detector acceptance, measurement uncertainties, ...
- ▶ What we have done
(current work for the snowmass study)
 - ▶ detector acceptance
($|\cos \theta| < 0.9$ for jets, < 0.95 for leptons)
 - ▶ some smearing
(production polar angle only, $\Delta = 0.1$)
 - ▶ ILC: marginalizing over total rate (δN) and effective beam polarization (δP_{eff})
- ▶ Constructing full EFT likelihood and feed it to the global fit. (For illustration, only showing the 3-aTGC fit results here.)
- ▶ Further verifications (by experimentalists) are needed.

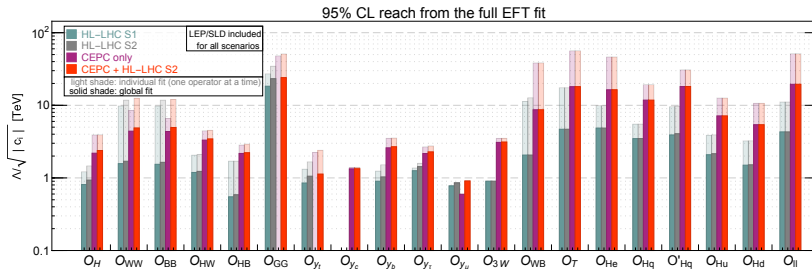


D6 operators

$\mathcal{O}_H = \frac{1}{2}(\partial_\mu H ^2)^2$	$\mathcal{O}_{GG} = g_s^2 H ^2 G_{\mu\nu}^A G^{A,\mu\nu}$
$\mathcal{O}_{WW} = g^2 H ^2 W_{\mu\nu}^a W^{a,\mu\nu}$	$\mathcal{O}_{y_u} = y_u H ^2 \bar{q}_L H u_R + \text{h.c.} \quad (u \rightarrow t, c)$
$\mathcal{O}_{BB} = g'^2 H ^2 B_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_{y_d} = y_d H ^2 \bar{q}_L H d_R + \text{h.c.} \quad (d \rightarrow b)$
$\mathcal{O}_{HW} = ig(D^\mu H)^\dagger \sigma^a (D^\nu H) W_{\mu\nu}^a$	$\mathcal{O}_{y_e} = y_e H ^2 \bar{l}_L H e_R + \text{h.c.} \quad (e \rightarrow \tau, \mu)$
$\mathcal{O}_{HB} = ig'(D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$	$\mathcal{O}_{3W} = \frac{1}{3!} g \epsilon_{abc} W_\mu^{a\nu} W_{\nu\rho}^b W^{c\rho\mu}$
$\mathcal{O}_W = \frac{ig}{2} (H^\dagger \sigma^a \overleftrightarrow{D}_\mu H) D^\nu W_{\mu\nu}^a$	$\mathcal{O}_B = \frac{ig'}{2} (H^\dagger \overleftrightarrow{D}_\mu H) \partial^\nu B_{\mu\nu}$
$\mathcal{O}_{WB} = gg' H^\dagger \sigma^a H W_{\mu\nu}^a B^{\mu\nu}$	$\mathcal{O}_{H\ell} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{\ell}_L \gamma^\mu \ell_L$
$\mathcal{O}_T = \frac{1}{2} (H^\dagger \overleftrightarrow{D}_\mu H)^2$	$\mathcal{O}'_{H\ell} = iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H \bar{\ell}_L \sigma^a \gamma^\mu \ell_L$
$\mathcal{O}_{\ell\ell} = (\bar{\ell}_L \gamma^\mu \ell_L)(\bar{\ell}_L \gamma_\mu \ell_L)$	$\mathcal{O}_{H\bar{e}} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{e}_R \gamma^\mu e_R$
$\mathcal{O}_{Hq} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{q}_L \gamma^\mu q_L$	$\mathcal{O}_{Hu} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{u}_R \gamma^\mu u_R$
$\mathcal{O}'_{Hq} = iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H \bar{q}_L \sigma^a \gamma^\mu q_L$	$\mathcal{O}_{Hd} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{d}_R \gamma^\mu d_R$

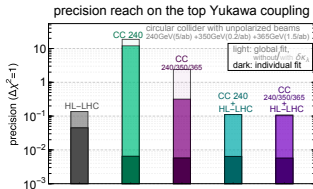
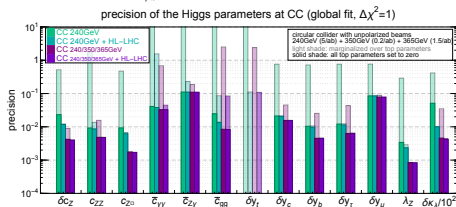
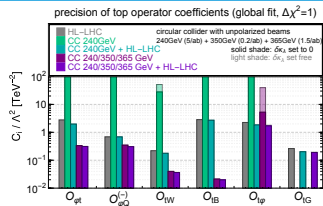
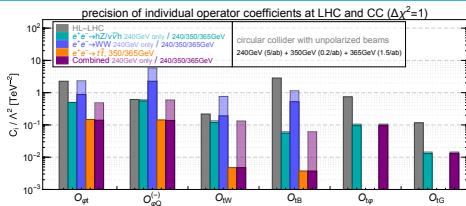
- ▶ SILH' basis (eliminate \mathcal{O}_{WW} , \mathcal{O}_{WB} , $\mathcal{O}_{H\ell}$ and $\mathcal{O}'_{H\ell}$)
- ▶ Modified-SILH' basis (eliminate \mathcal{O}_W , \mathcal{O}_B , $\mathcal{O}_{H\ell}$ and $\mathcal{O}'_{H\ell}$)
- ▶ Warsaw basis (eliminate \mathcal{O}_W , \mathcal{O}_B , \mathcal{O}_{HW} and \mathcal{O}_{HB})

Reach on the scale of new physics



- ▶ Reach on the scale of new physics Λ .
- ▶ Note: reach depends on the couplings c_i !

Top operators in loops [arXiv:1809.03520] G. Durieux, JG, E. Vryonidou, C. Zhang



- ▶ Higgs precision measurements have sensitivity to the top operators in the loops.
 - ▶ But it is challenging to discriminate many parameters in a global fit!
- ▶ HL-LHC helps, but a 360 or 365 GeV run is better.
- ▶ Indirect bounds on the top Yukawa coupling.

You can't really separate Higgs from the EW gauge bosons!

$$\begin{aligned}\mathcal{O}_{H\ell} &= iH^\dagger \overleftrightarrow{D}_\mu H \bar{\ell}_L \gamma^\mu \ell_L, \\ \mathcal{O}'_{H\ell} &= iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H \bar{\ell}_L \sigma^a \gamma^\mu \ell_L, \\ \mathcal{O}_{He} &= iH^\dagger \overleftrightarrow{D}_\mu H \bar{e}_R \gamma^\mu e_R\end{aligned}$$

(or the ones with quarks)

- ▶ modifies gauge couplings of fermions,
- ▶ also generates $hVff$ type contact interaction.



$$\begin{aligned}\mathcal{O}_{HW} &= ig(D^\mu H)^\dagger \sigma^a (D^\nu H) W_{\mu\nu}^a, \\ \mathcal{O}_{HB} &= ig'(D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}\end{aligned}$$

- ▶ generate **aTGCs** $\delta g_{1,Z}$ and $\delta \kappa_\gamma$,
- ▶ also generates **HVV anomalous couplings** such as $hZ_\mu \partial_\nu Z^{\mu\nu}$.



You also have to measure the Higgs!

- ▶ Some operators can only be probed with the **Higgs particle**.
- ▶ $|H|^2 W_{\mu\nu} W^{\mu\nu}$ and $|H|^2 B_{\mu\nu} B^{\mu\nu}$
 - ▶ $H \rightarrow \nu/\sqrt{2}$, corrections to gauge couplings?
 - ▶ **Can be absorbed by field redefinition!** This applies to any operators in the form $|H|^2 \mathcal{O}_{\text{SM}}$.

$$\begin{aligned}
 c_{\text{SM}} \mathcal{O}_{\text{SM}} \quad \text{vs.} \quad & c_{\text{SM}} \mathcal{O}_{\text{SM}} + \frac{c}{\Lambda^2} |H|^2 \mathcal{O}_{\text{SM}} \\
 & = (c_{\text{SM}} + \frac{c v^2}{2 \Lambda^2}) \mathcal{O}_{\text{SM}} + \text{terms with } h \\
 & = c'_{\text{SM}} \mathcal{O}_{\text{SM}} + \text{terms with } h
 \end{aligned}$$

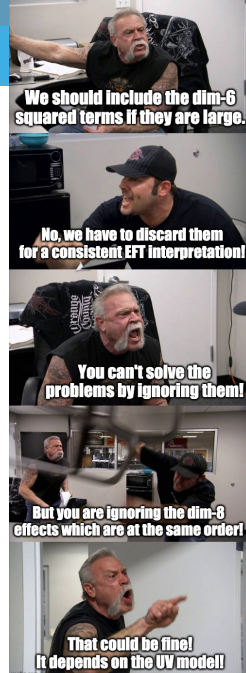
- ▶ probed by measurements of the $h\gamma\gamma$ and $hZ\gamma$ couplings, or the hWW and hZZ **anomalous** couplings.
 - ▶ or Higgs in the loop (different story...)
- ▶ Yukawa couplings, Higgs self couplings, ...

Why lepton colliders?

- ▶ EFT is good for lepton colliders.
 - ▶ A systematic parameterization of Higgs (and other) couplings.
- ▶ Lepton colliders are also good for EFT!
 - ▶ High precision $\Rightarrow E \ll \Lambda$
Ideal for EFT studies!
 - ▶ LHC is built for discovery, but

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 - ▶ LHC is built for discovery, but
- ▶ **Energy vs. Precision**
 - ▶ Poor measurements at the high energy tails lead to problems in the interpretation of EFT...



A lesson from history

- ▶ In 1875, a young Max Planck was told by his advisor Philipp von Jolly not to study physics, since there was nothing left to be discovered.

- ▶ **Planck did not listen.**

- ▶ In 1887, Michelson and Morley tried to find ether, the postulated medium for the propagation of light that was widely believed to exist.

- ▶ **They didn't find it.**

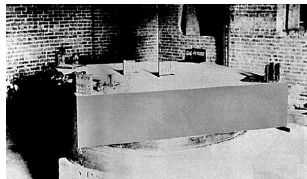
- ▶ **“Our future discoveries must be looked for in the sixth place of decimals.” — Albert A. Michelson**

Max Planck:

Before
quantum physics:



After
quantum physics:



A lesson from Christopher Columbus (哥伦布发现美洲大陆)

- ▶ **You need to have a theory.**
 - ▶ The earth is round, India is in the east...
- ▶ **Your theory can be wrong!**
 - ▶ Columbus did not find India, but found America instead...
- ▶ **You need to ask money from the government!**
 - ▶ Columbus convinced the monarchs of Spain to sponsor him.
- ▶ **Will we discover the new world?**

