

# $W$ mass measurement at LHCb

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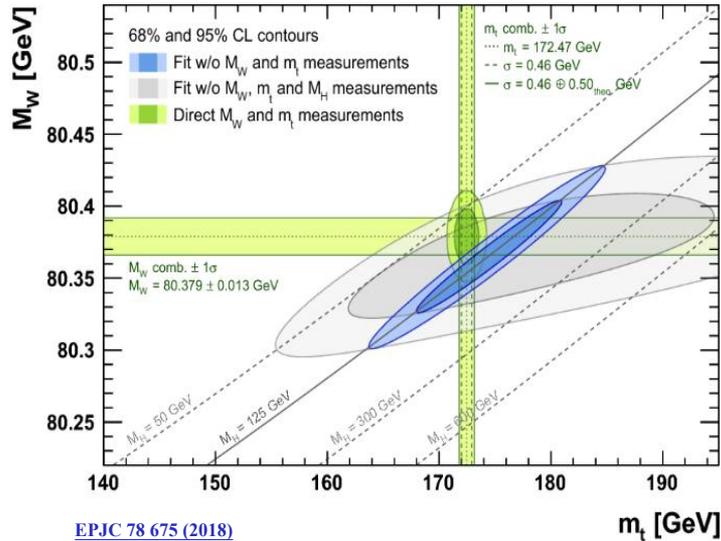
on behalf of the LHCb collaboration

WIN 2023, 07/07



# Motivation

- $m_W$  is directly related to electroweak symmetry breaking in the SM



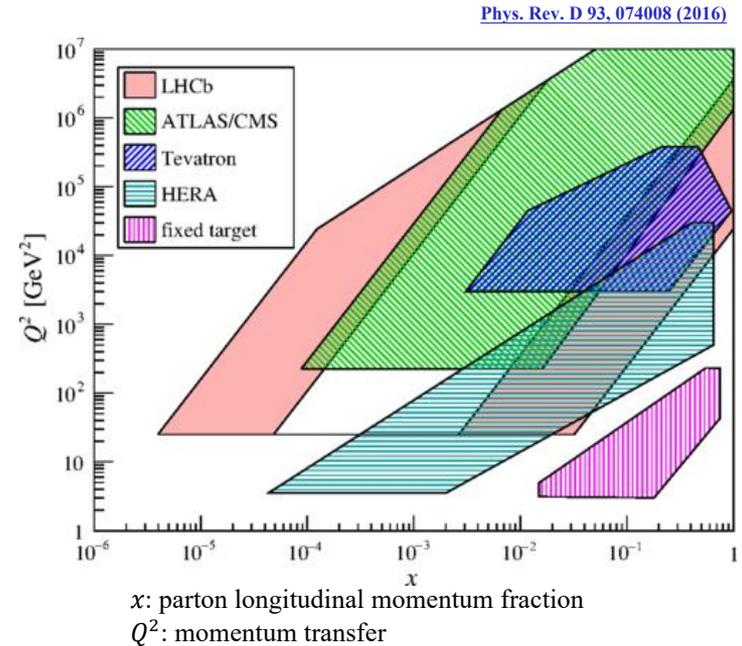
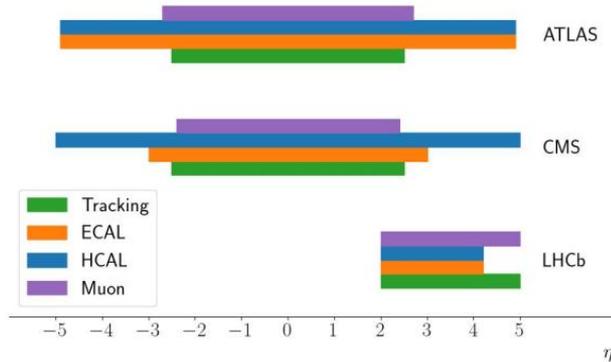
$$m_W^2 = \frac{\pi\alpha}{\sqrt{2}G_F(1 - m_W^2/m_Z^2)(1 - \Delta r)}$$

$\Delta r$ : loop corrections

- Sensitivity to BSM physics is primarily limited by precision of **direct** measurements of  $m_W$

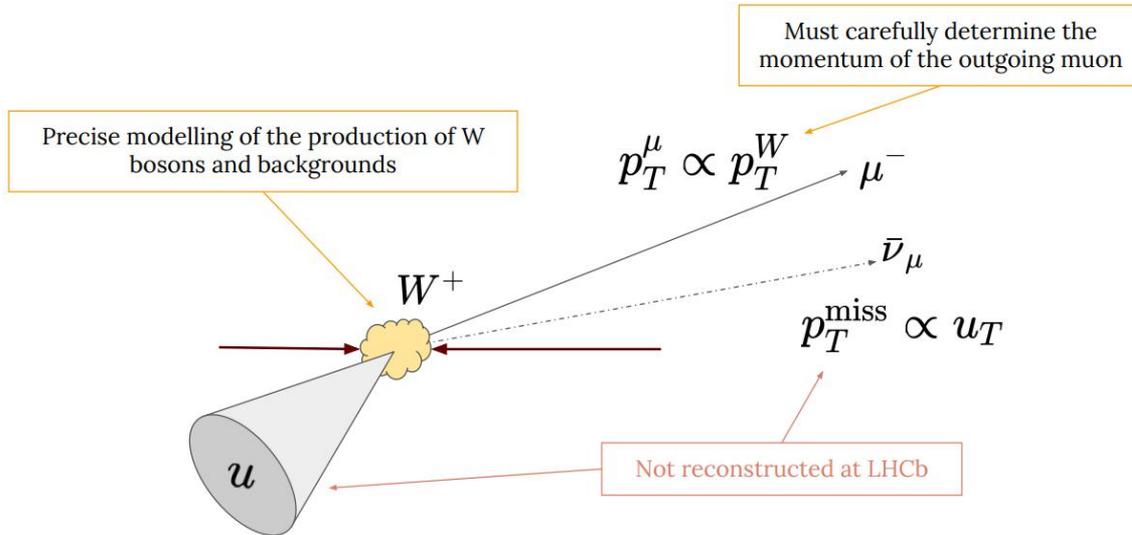
# LHCb forward region

- Low pile-up environment
- Forward region,  $2 < \eta < 5$ : **high/low- $x$**  partons involved



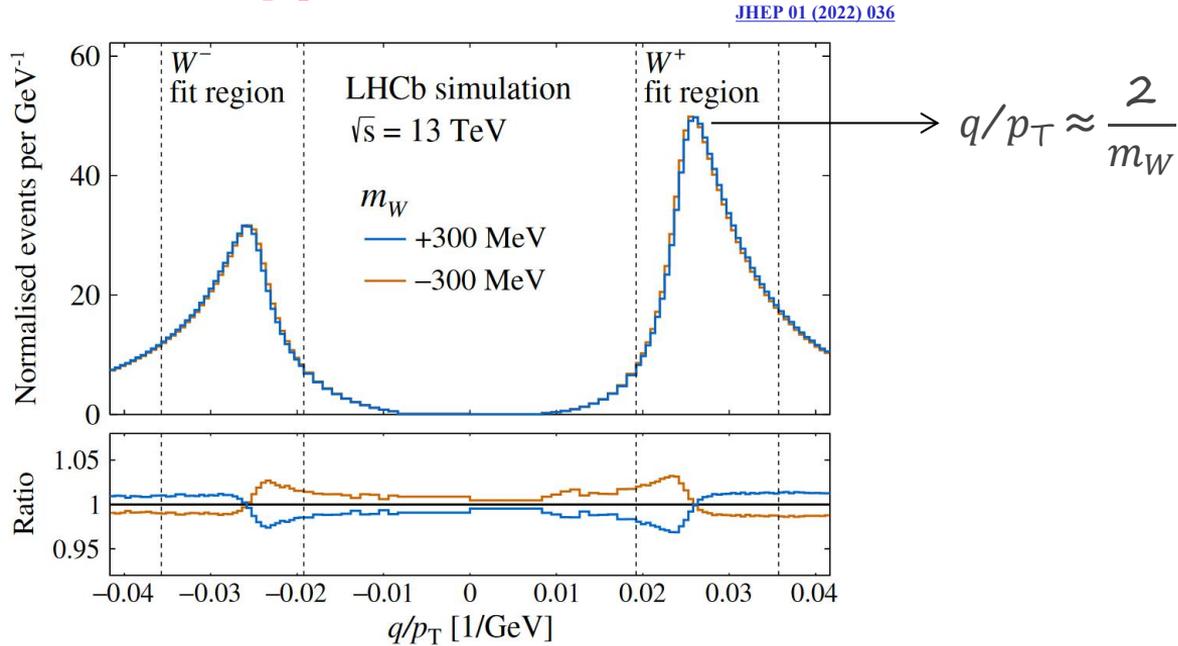
# Signal event signature

- **Identified muon** candidate matched to single muon trigger path
- Hadronic background suppressed to the percent level by an isolation requirement
- Second-muon ( $p_T > 20\text{GeV}$  and  $2.2 < \eta < 4.4$ ) veto suppressed  $Z \rightarrow \mu\mu$  background



# Fitting the muon $q/p_T$ distribution

- Measurements based on muon  $p_T$



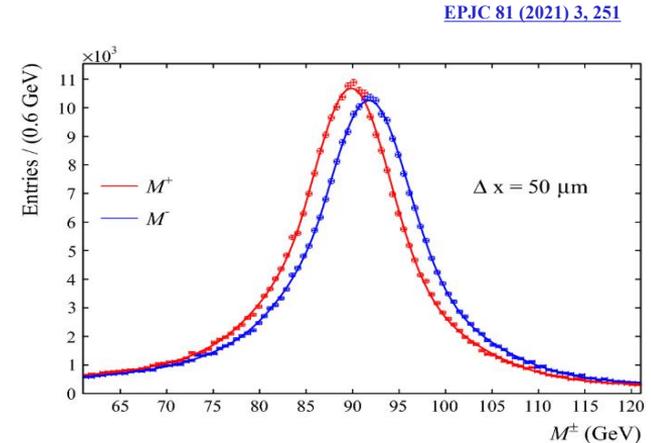
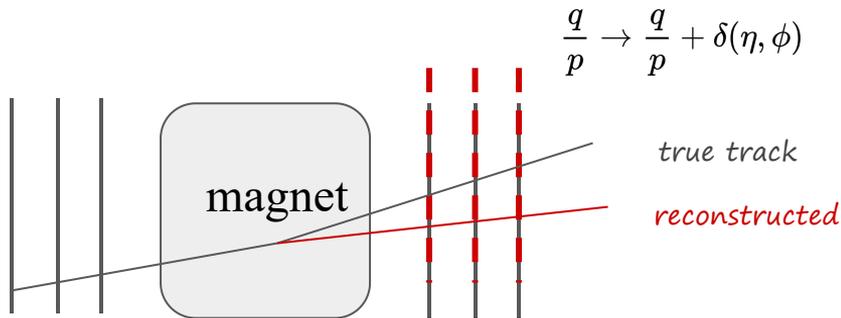
fit region  $\Rightarrow \eta \in [2.2, 4.4], p_T^\mu \in [28, 52] \text{ GeV}$

# Detector and physics modelling

- Detector response
  - Muon momentum, reconstruction and selection efficiency
    - Correct the simulation efficiencies of the different selection steps
- $W$  boson production
  - Modelling of the  $W$   $p_T$  distribution, boson polarisation and electroweak corrections
  - Use plain LHCb Pythia8 simulation
  - A variety of models are used to fully reweight the events to/beyond next-to-leading-order accuracy

# Curvature biases

- $m_W$  determination is highly sensitive to misalignments and miscalibrations of the detector
  - **Misalignment of 10 $\mu\text{m}$  translates into a  $\mathcal{O}$  (50MeV) shift**
- Re-run the alignment and calibration offline using Z events
- Corrected for charge-dependent curvature biases using the pseudomass method

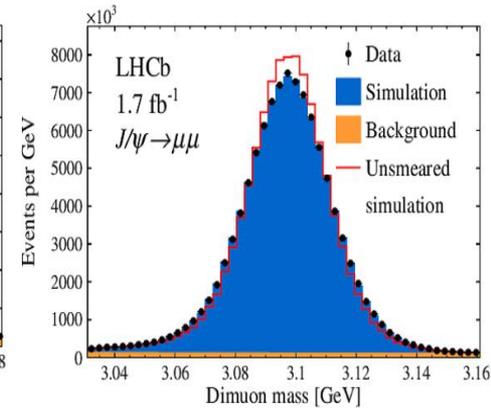
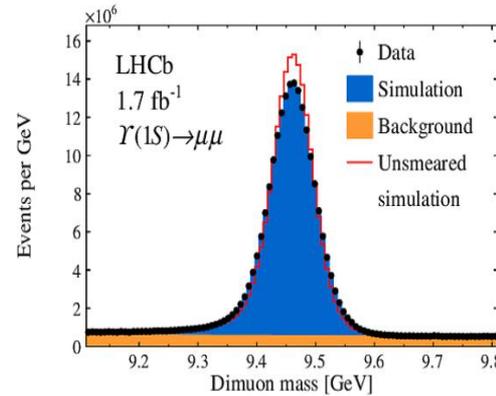
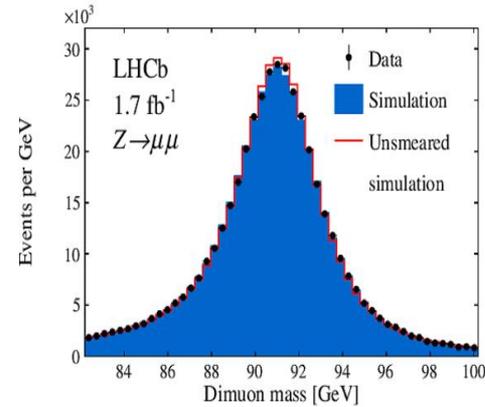


$$M^\pm = \sqrt{2p^\pm p_T^\pm \frac{p^\mp}{p_T^\mp} (1 - \cos \theta)}$$

Phys. Rev. D 91, 072002

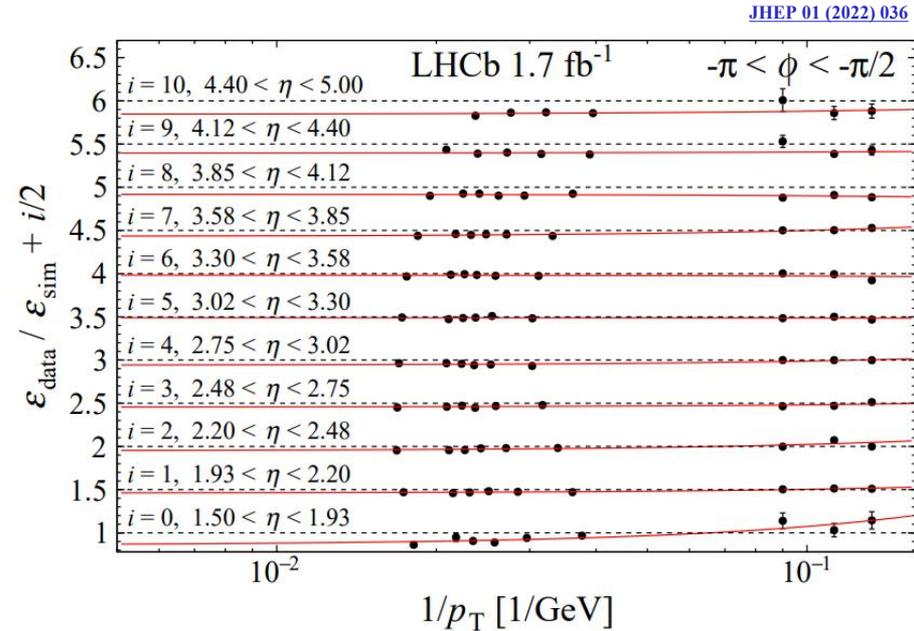
# MC Smearing

- Smearing of the muon momentum in simulation to account for
  - momentum scale
  - multiple scattering
- Simultaneous fit** of  $Z$ ,  $\Upsilon(1S)$  and  $J/\Psi$
- Systematic uncertainties: variations in the PDG resonance masses, detector material budget, final state radiation and the form of the smearing function



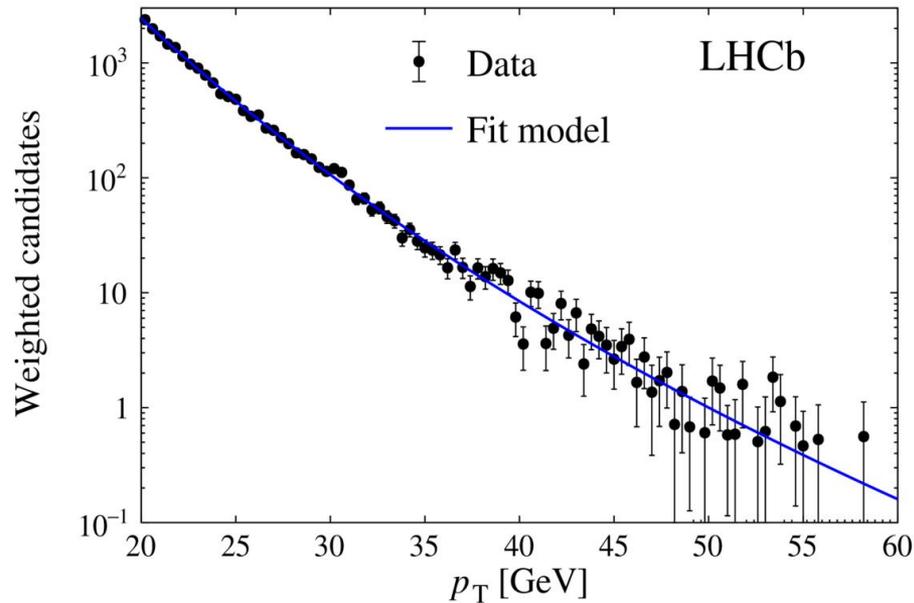
# Selection efficiency modelling

- The selection efficiencies are measured in data and simulation with the same method
- Three main sources of selection biases
  - Trigger efficiencies
  - Muon-identification efficiencies
  - Isolation requirements
- **The simulated events are subsequently corrected with  $\epsilon_{\text{data}}/\epsilon_{\text{mc}}$**



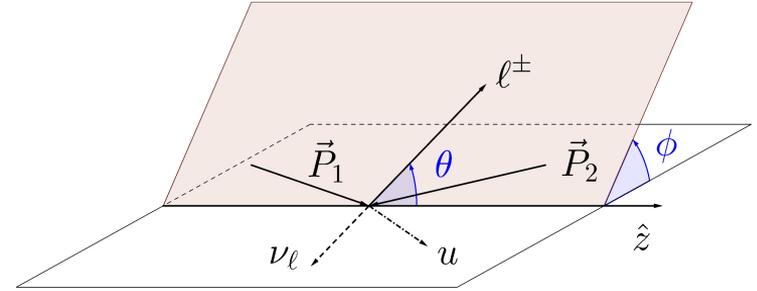
# Backgrounds

- Electroweak backgrounds and heavy flavour hadrons are modelled with the simulation
- Hadronic background (decays-in-flight of pions and kaons)
  - A parametric model is trained on a sample of hadrons with weights to account for the variation of the decay-length acceptance on the Lorentz boost



# Vector boson production model

Collins-Soper frame



Unpolarized part

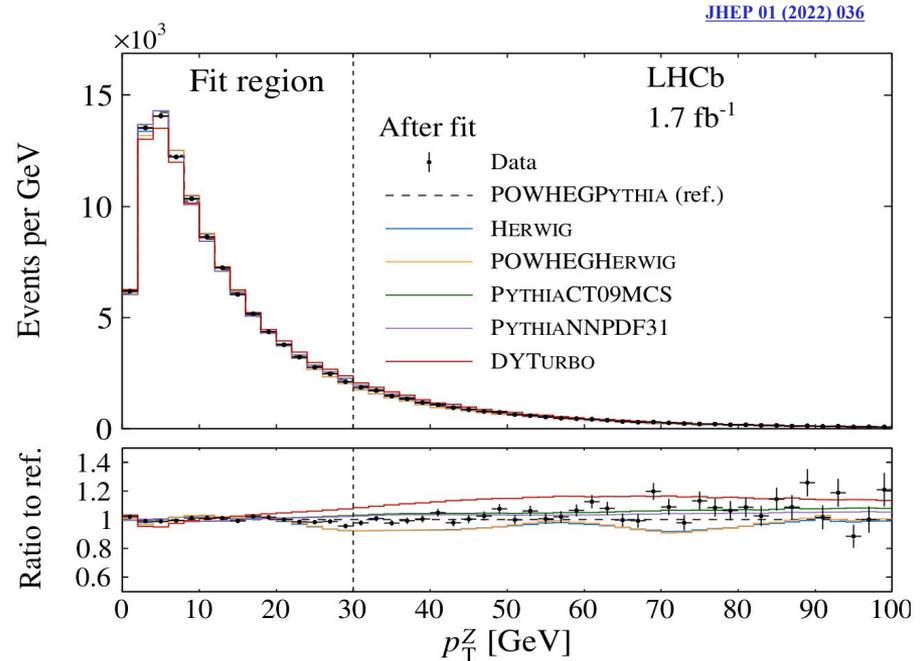
$$\frac{d\sigma}{dp_T^W dy dM d\cos\vartheta d\varphi} = \frac{3}{16\pi} \frac{d\sigma^{\text{unpol.}}}{dp_T^W dy dM}$$

Angular part

$$\left\{ (1 + \cos^2 \vartheta) + A_0 \frac{1}{2} (1 - 3 \cos^2 \vartheta) + A_1 \sin 2\vartheta \cos \varphi \right. \\ \left. + A_2 \frac{1}{2} \sin^2 \vartheta \cos 2\varphi + A_3 \sin \vartheta \cos \varphi + A_4 \cos \vartheta \right. \\ \left. + A_5 \sin^2 \vartheta \sin 2\varphi + A_6 \sin 2\vartheta \sin \varphi + A_7 \sin \vartheta \sin \varphi \right\}$$

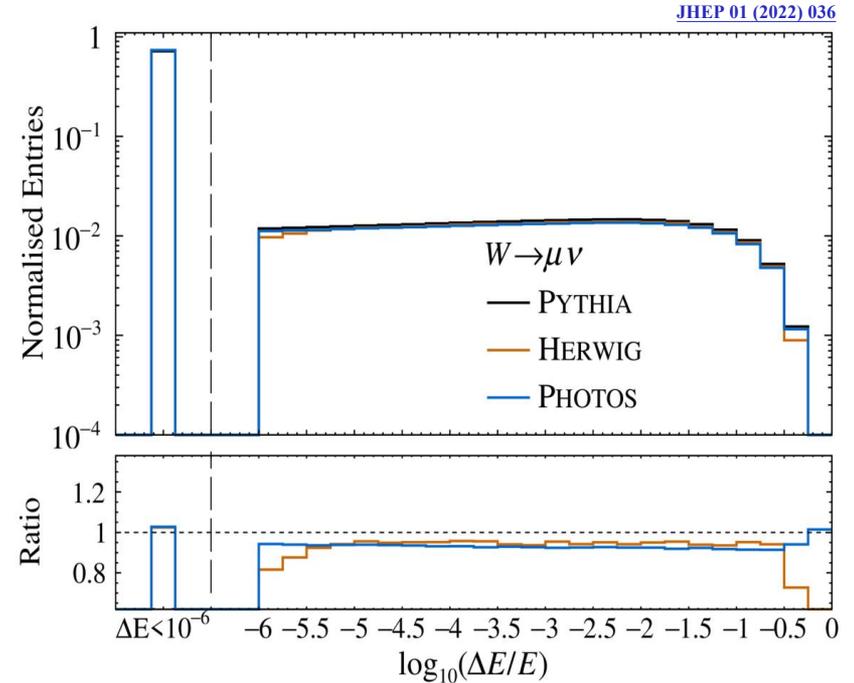
# Physics model

- **POWHEG + Pythia** gives the best description of the **unpolarized** cross-section
  - Varied success with other generators, used to determine systematic uncertainties
- The **angular part** of the cross-section is better described with **DYTurbo**



# Electroweak corrections

- Pythia, Photos and Herwig models of QED final state radiation considered
- Central result based on the **average** of the three, while the uncertainty is based on the envelope over the three individual models



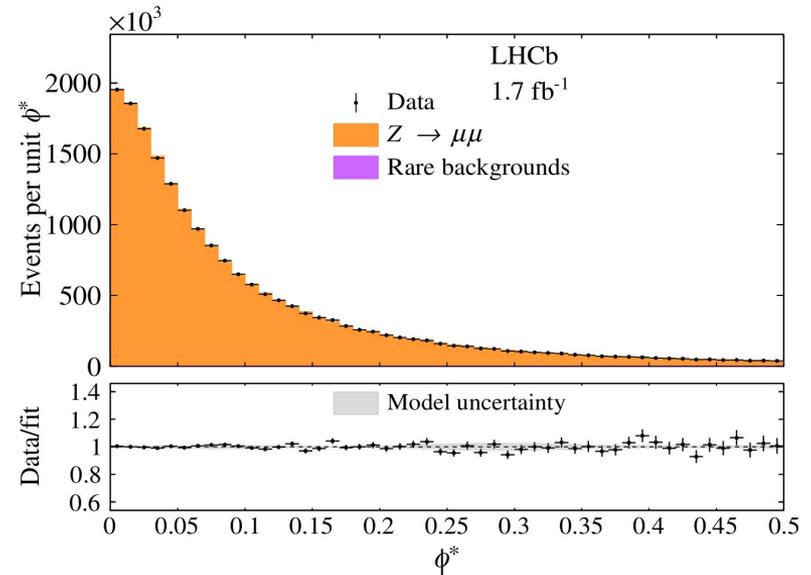
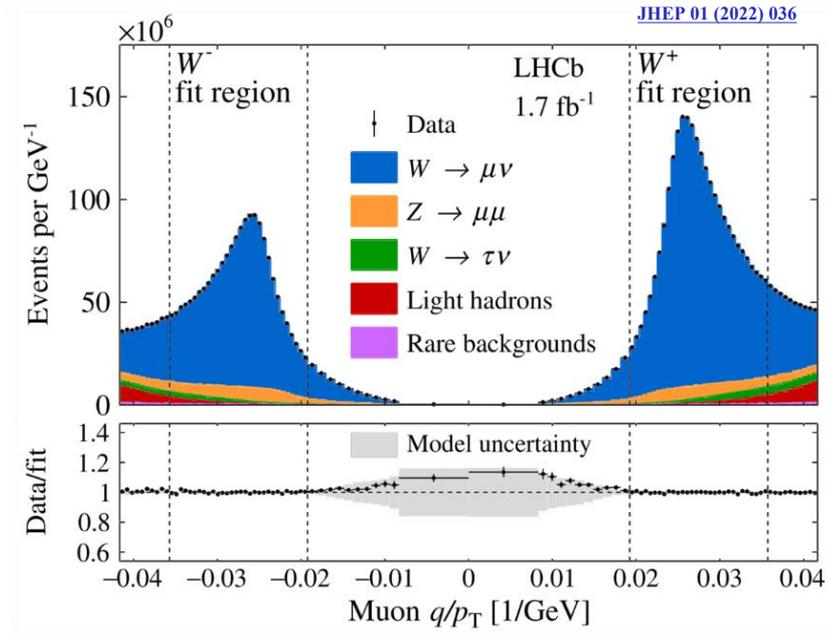
$$\Delta E/E = \frac{E_{\text{boson}} - E_{\text{dilepton}}^{\text{bare}}}{E_{\text{boson}}}$$

# Extract $m_W$

- In a template fit to the  $q/p_T^\mu$  distribution
- In a **simultaneous** fit of  $W$  and  $Z$  data

EPJC 71 1600 (2011)

$$\phi^* \equiv \arctan\left(\frac{\pi - \Delta\phi}{2}\right) / \cosh\left(\frac{\Delta\eta}{2}\right) \sim \frac{p_T}{M}$$



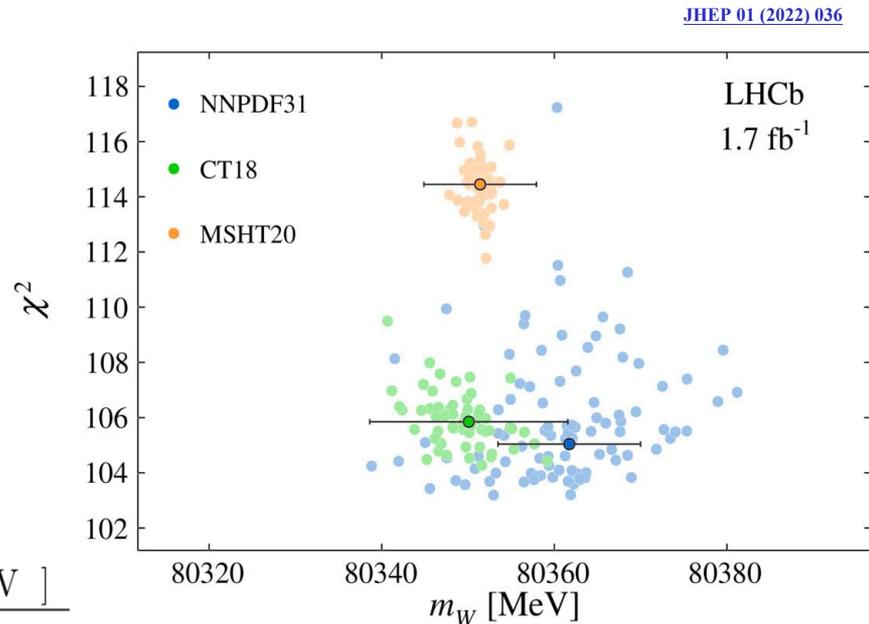
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# PDF uncertainties

- The uncertainties are evaluated with specific prescriptions from each of the three groups
- Central  $m_W$  result is an average of the three results with the individual PDF sets assuming **100%** correlation

Set	$\sigma_{\text{PDF,base}}$ [ MeV ]	$\sigma_{\text{PDF},\alpha_s}$ [ MeV ]	$\sigma_{\text{PDF}}$ [ MeV ]
NNPDF3.1	8.3	2.4	8.6
CT18	11.5	1.4	11.6
MSHT20	6.5	2.1	6.8

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# Measurement uncertainty summary

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Source	Size (MeV)
<b>Parton distribution functions</b>	<b>9</b>
<b>Total theoretical syst. uncertainty (excluding PDFs)</b>	<b>17</b>
Transverse momentum model	11
Angular coefficients	10
QED FSR model	7
Additional electroweak corrections	5
<b>Total experimental syst. uncertainty</b>	<b>10</b>
Momentum scale and resolution modelling	7
Muon ID, tracking and trigger efficiencies	6
Isolation efficiency	4
QCD background	2
<b>Statistical</b>	<b>23</b>
<b>Total uncertainty</b>	<b>32</b>

→ average of NNPDF31, CT18 and MSHT20

→ from five different models

→ scale variation

→ envelope of the QED FSR from PYTHIA8  
Photos and Herweg

→ statistical uncertainties, details of method  
(e.g. binning, smoothing)

# Cross Checks

- Orthogonal splits: differences within  $2\sigma$
- Fit range: the result is stable with the variations in the upper/lower limits
- $W$ -like  $m_Z$  measurement: with  $\mu^+$  and  $\mu^-$  agree to better than  $1\sigma$  and their average agrees with in the PDG value at  $1\sigma$

Subset	$\chi^2_{\text{tot}}/\text{ndf}$	$\delta m_W$ [MeV]
Polarity = $-1$	92.5/102	–
Polarity = $+1$	97.3/102	$-57.5 \pm 45.4$
$\eta > 3.3$	115.4/102	–
$\eta < 3.3$	85.9/102	$+56.9 \pm 45.5$
Polarity $\times q = +1$	95.9/102	–
Polarity $\times q = -1$	98.2/102	$+16.1 \pm 45.4$
$ \phi  > \pi/2$	98.8/102	–
$ \phi  < \pi/2$	115.0/102	$+66.7 \pm 45.5$
$\phi < 0$	91.8/102	–
$\phi > 0$	103.0/102	$-100.5 \pm 45.3$

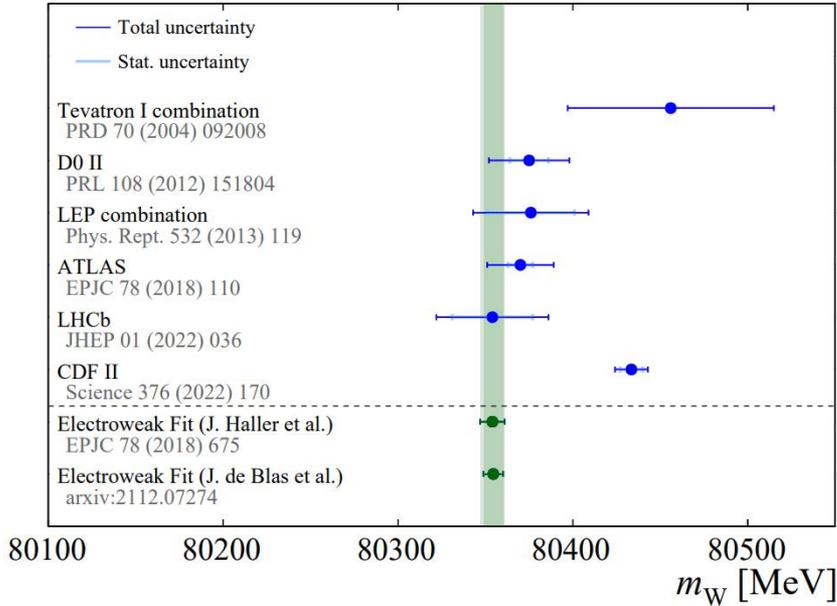
- Alternative fit with the difference between the  $m_{W^+}$  and  $m_{W^-}$  as another floating parameter: this parameter  $\sim 0$  within  $1\sigma$
- Additional tests with NNLO PDFs instead of NLO PDFs, variations in the charm quark mass, etc... affect  $m_W$  at the  $\lesssim 1$  MeV level

# 2016 result

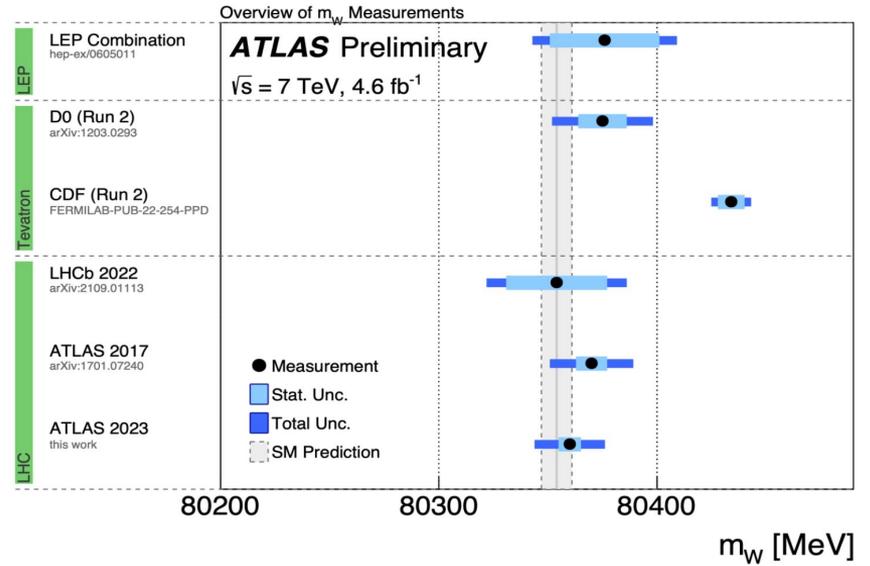
- LHCb achieves a precision of  $\sim 32$  MeV using roughly 1/3 of the Run-II dataset

$$m_W = 80354 \pm 23_{\text{stat.}} \pm 10_{\text{exp.}} \pm 17_{\text{theory}} \pm 9_{\text{PDF}} \text{ MeV}$$

[LHCb-FIGURE-2022-003](#)



[ATLAS-CONF-2023-004](#)

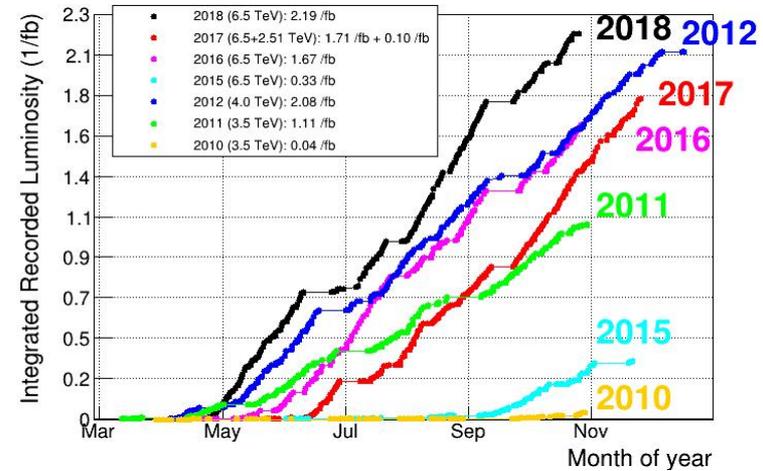


# With the full Run 2 dataset

- Including 2017 and 2018 data is straight-forward
  - More careful treatment of the detector effects
  - Improvements in the physics modelling

Target sensitivity:

$$\sigma_{\text{stat.}}^{\text{Run 2}} \sim 14\text{MeV}$$
$$\sigma_{\text{total}}^{\text{Run 2}} \sim 20\text{MeV}$$



# Conclusions and outlook

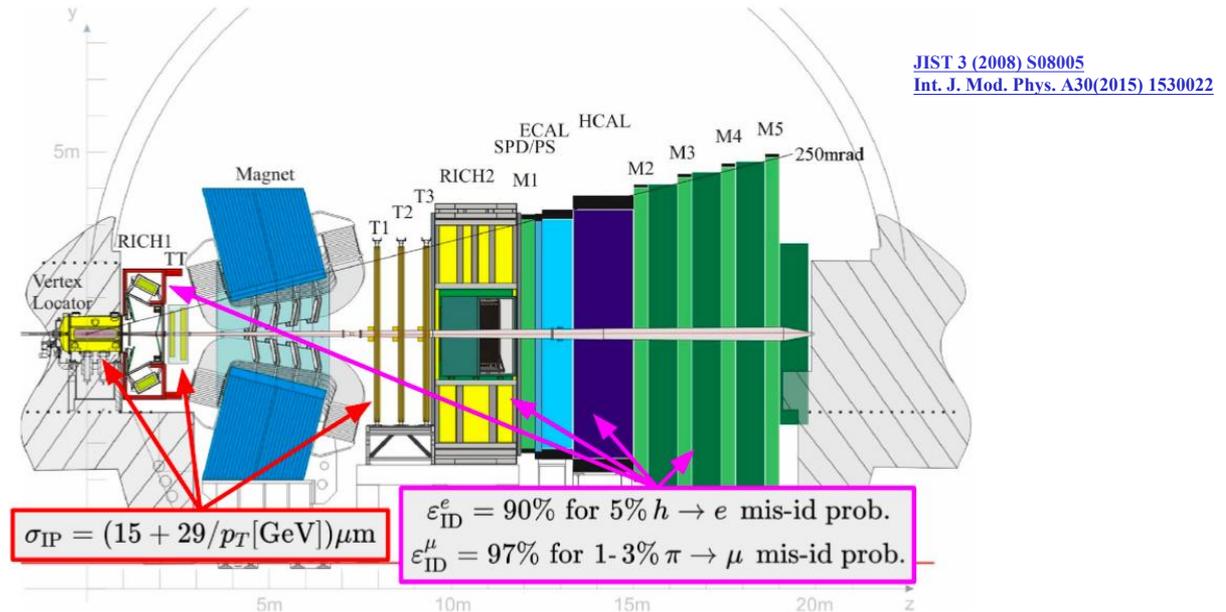
- First measurement of  $m_W$  from LHCb with 32 MeV uncertainty is consistent with the prediction
- A total uncertainty of  $\lesssim 20$  MeV looks achievable with existing LHCb data
- On Run 3, with a similar detector and analysis environment the precision will increase with the square root of the luminosity
- On Run 4 and beyond, an improved electromagnetic calorimeter system might open the door to study the electron mode at LHCb
- Look forward to working with the other LHC experiments, and the theory community, to fully exploit LHCb's unique/complementary rapidity coverage to achieve the ultimate precision on  $m_W$

Back Up



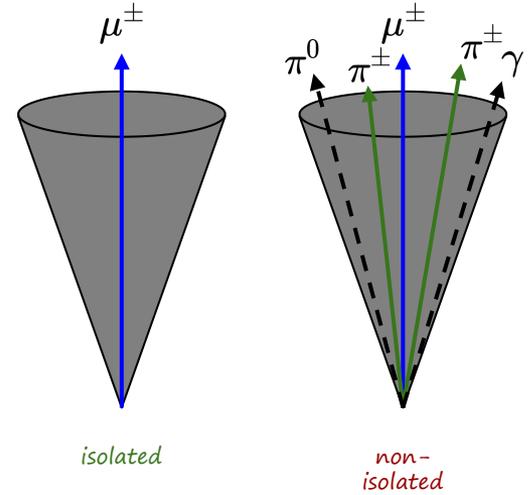
# LHCb Detector

- Single-arm **forward** spectrometer
- Designed for the heavy flavour physics with  $2 < \eta < 5$
- Extended to **EW** measurements: excellent performance of tracking and muon detector



# Selections

- EW physics with leptons in the final state can be done at LHCb with simple selections based on the transverse momentum, impact parameter, isolation and particle identification

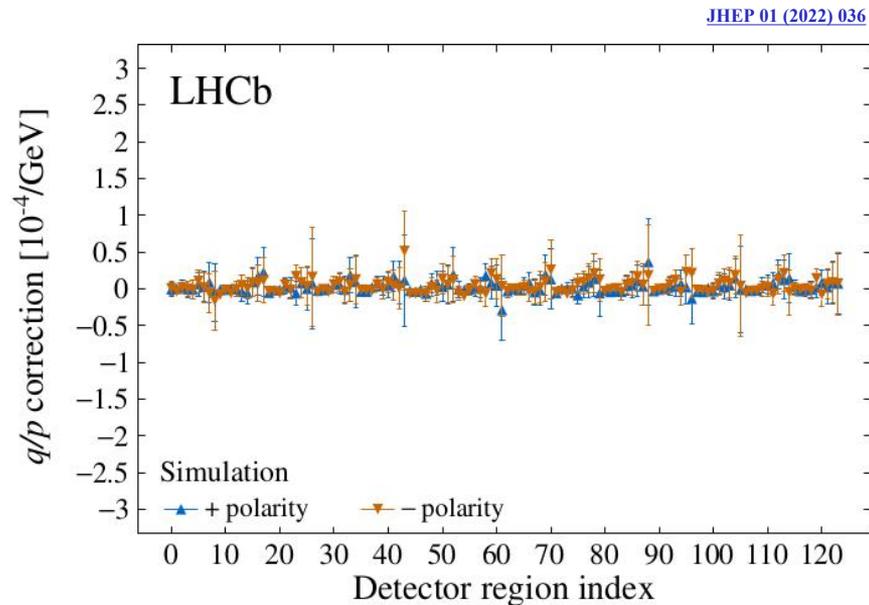
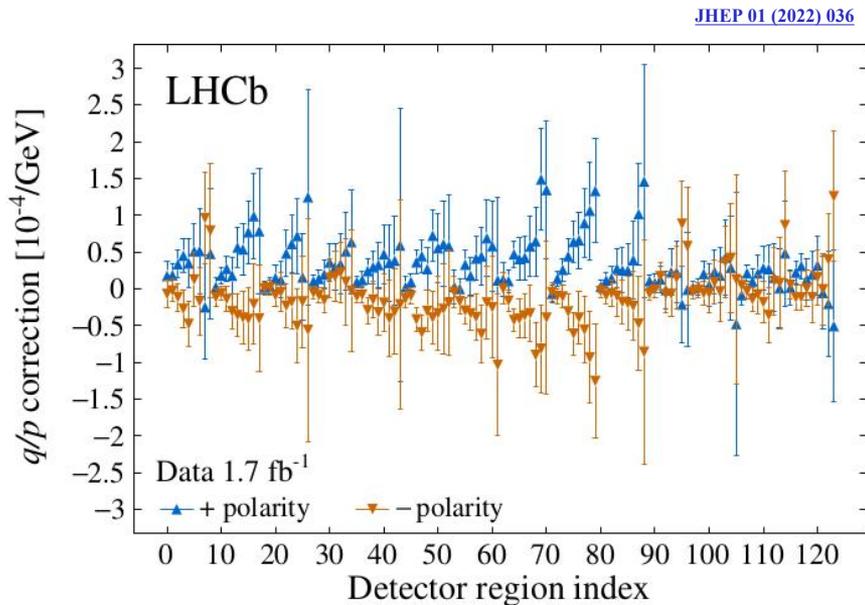


$$I = \sum_i^n p_T^i \in \text{cone}$$

$$\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2 (\text{rad}^{-2})}$$

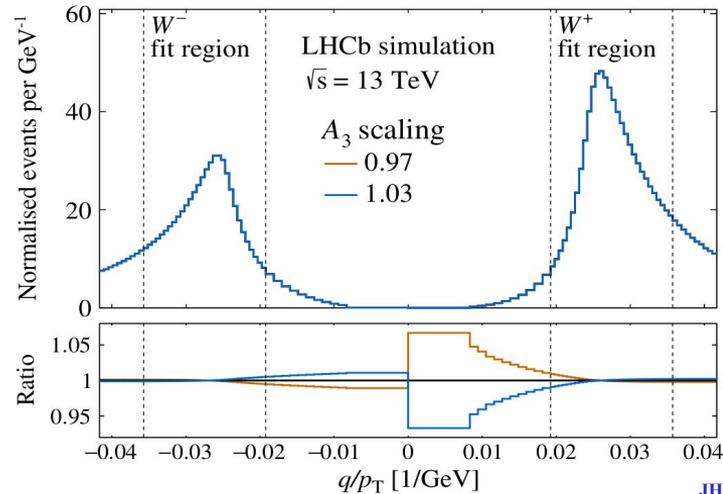
# Curvature corrections

- Fit the pseudomass asymmetries (between  $M^+$  and  $M^-$  peak positions) in fine detector regions (bins in  $\eta$  and  $\phi$ ) and translate these to curvature corrections (shifts in  $q/p$ )



# Polarized cross-section

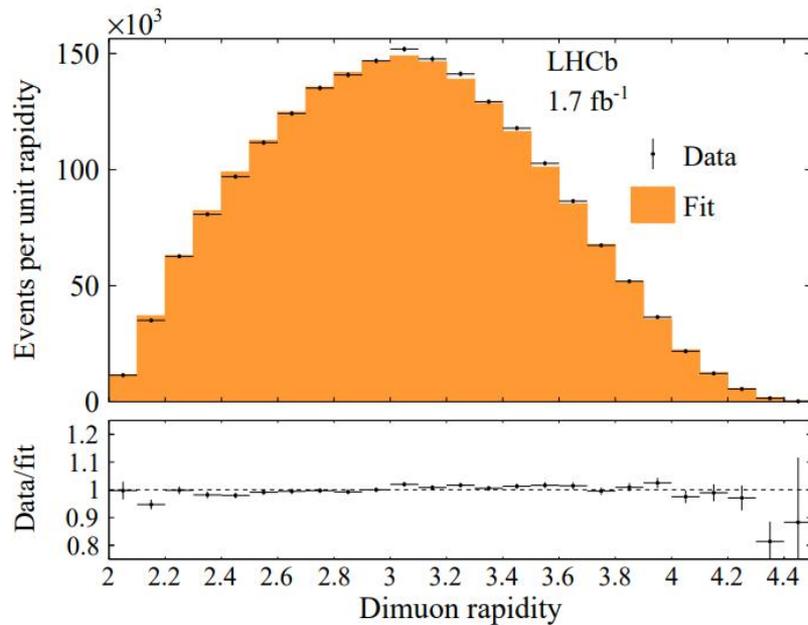
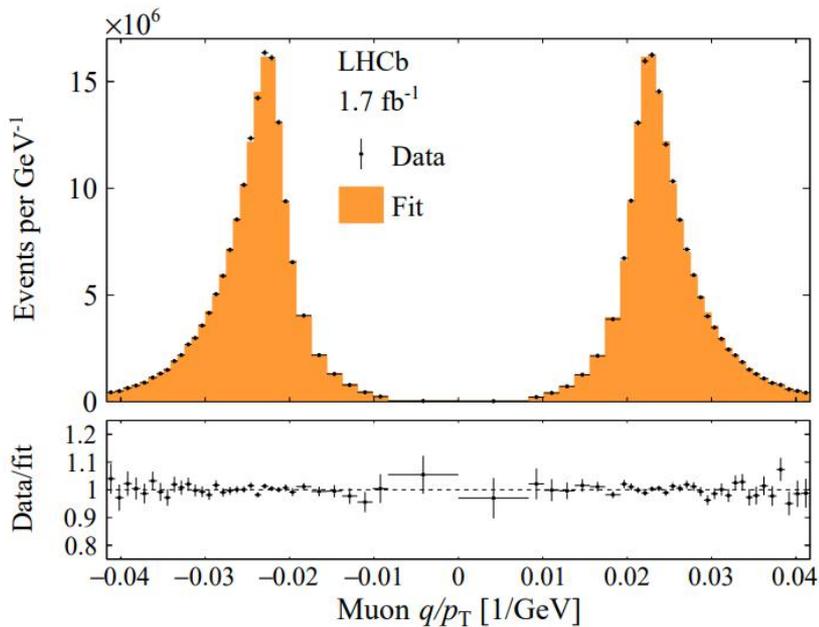
- Uncertainties from DYTurbo mitigated by floating  $A_3$ 
  - Otherwise the uncertainty would be  $O(30 \text{ MeV})$
  - The preferred value in the fit is however consistent with DYTurbo predictions



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# Postfit Plots

- The model is in good agreement with the data, which confirms that the momentum smearing is reliably determined and applied



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# Cross checks

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Change to fit range	$\chi_{\text{tot}}^2/\text{ndf}$	$\delta m_W$ [MeV]	$\sigma(m_W)$ [MeV]
$p_T^{\text{min}} = 24$ GeV	96.5/102	+6.8	19.7
$p_T^{\text{min}} = 26$ GeV	97.7/102	+9.6	20.9
$p_T^{\text{min}} = 30$ GeV	102.7/102	+3.0	25.7
$p_T^{\text{min}} = 32$ GeV	84.9/102	-21.6	30.8
$p_T^{\text{max}} = 48$ GeV	105.3/102	-3.8	23.2
$p_T^{\text{max}} = 50$ GeV	103.0/102	-2.1	23.0
$p_T^{\text{max}} = 54$ GeV	96.3/102	-8.6	22.6
$p_T^{\text{max}} = 56$ GeV	103.7/102	-14.3	22.4

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Configuration change	$\chi_{\text{tot}}^2/\text{ndf}$	$\delta m_W$ [MeV]	$\sigma(m_W)$ [MeV]
$2 \rightarrow 3$ $\alpha_s$ parameters	103.4/101	-6.0	$\pm 23.1$
$2 \rightarrow 1$ $\alpha_s$ and $1 \rightarrow 2$ $k_T^{\text{intr}}$ parameters	116.1/102	+13.9	$\pm 22.4$
$1 \rightarrow 2$ $k_T^{\text{intr}}$ parameters	104.0/101	+0.4	$\pm 22.7$
$1 \rightarrow 3$ $k_T^{\text{intr}}$ parameters	102.8/100	-2.7	$\pm 22.9$
No $A_3$ scaling	106.0/103	+4.4	$\pm 22.2$
Varying QCD background asymmetry	103.8/101	-0.7	$\pm 22.7$