



中国科学院大学
University of Chinese Academy of Sciences



ICTP-AP
International Centre
for Theoretical Physics Asia-Pacific
国际理论物理中心-亚太地区

Electroweak Phase Transition and Baryogenesis

Huaike Guo (郭怀珂)

UCAS (ICTP-AP)

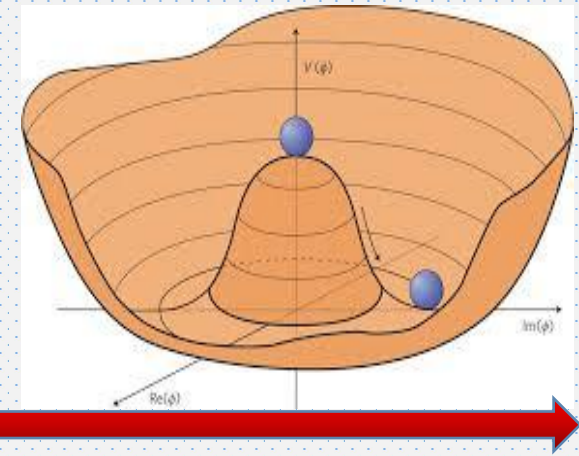
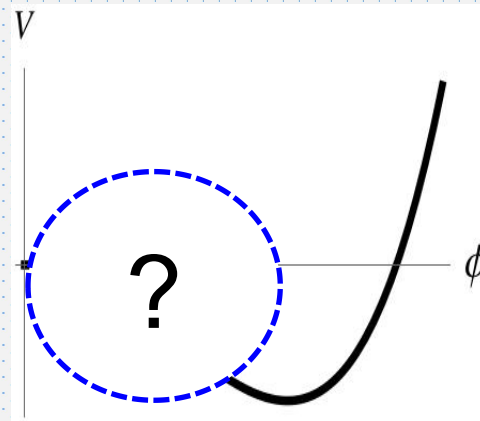
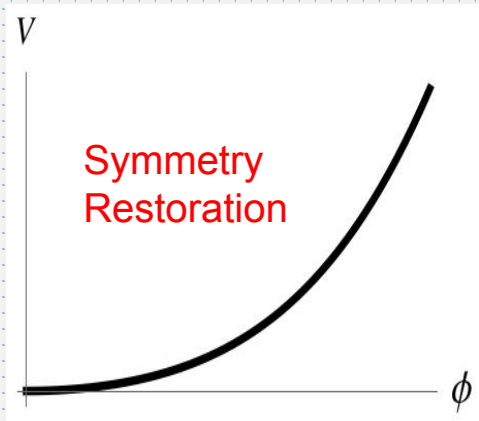
July 7, 2023



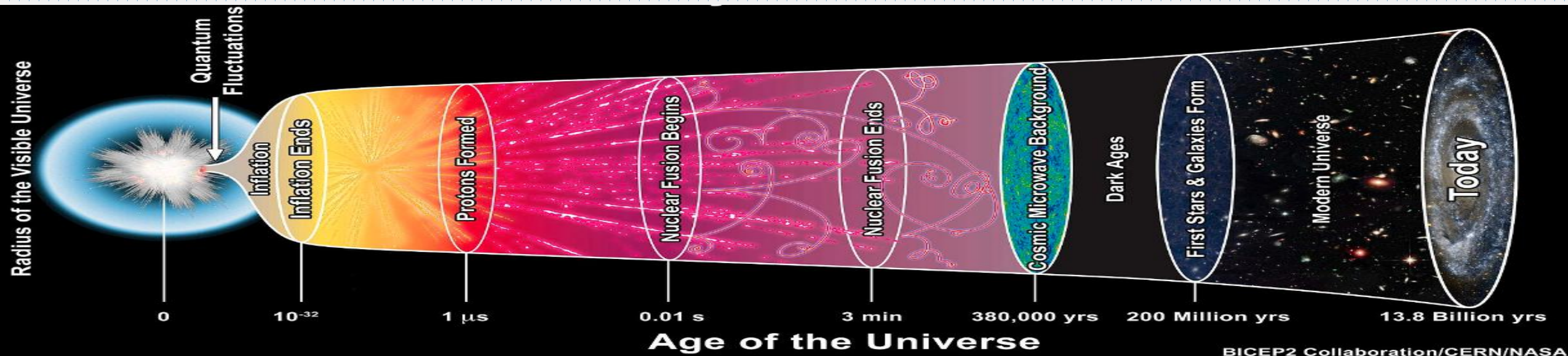
The 29th International Workshop on Weak Interactions and Neutrinos

2023年7月2日至8日
Sun Yat-sen University Zhuhai Campus

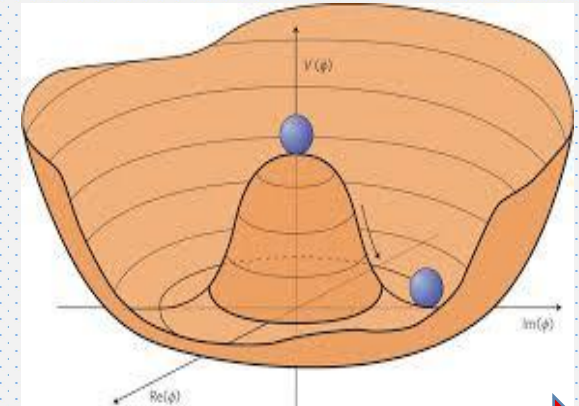
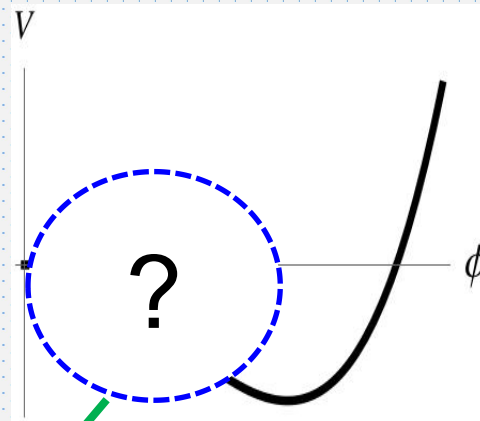
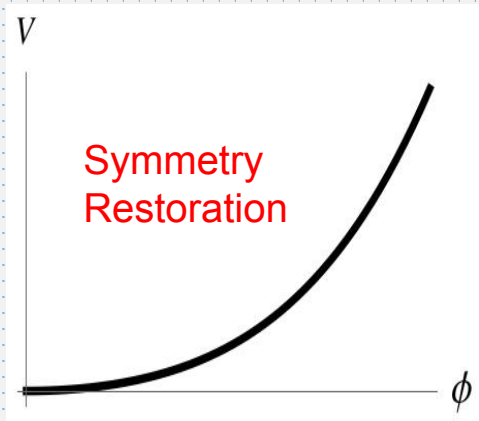
Electroweak Phase Transition



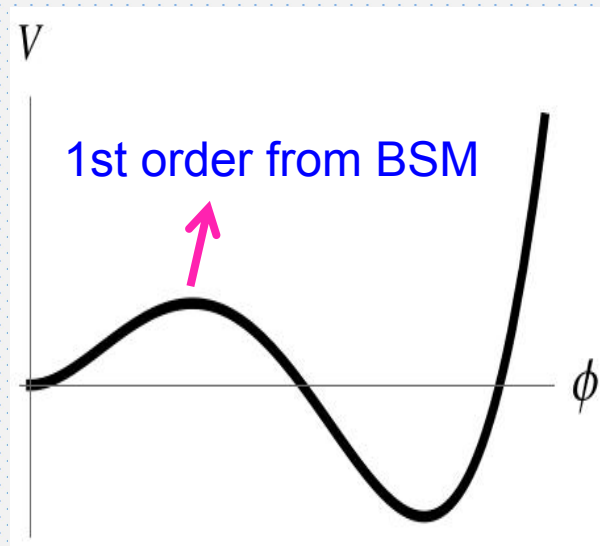
Temperature drops



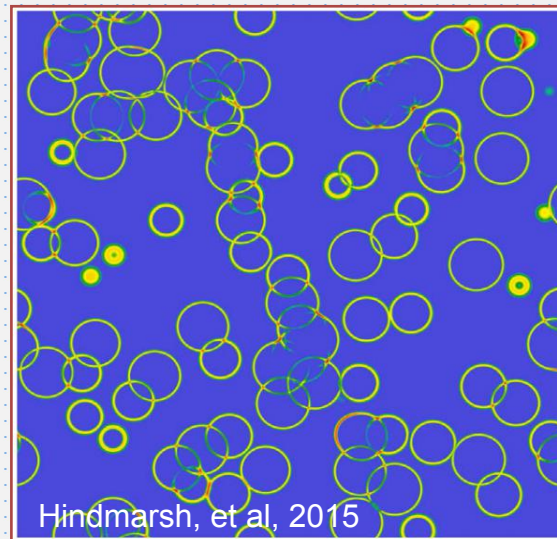
Electroweak Phase Transition



Temperature drops



bubbles, plasma, MHD



Electroweak Baryogenesis

- Modified Higgs potential (Higgs physics, GW)
- Extra CP-violation (EDM, LHC)
- B-violation: Sphaleron process (LHC, GW)

Recent research largely driven by GWs



THE SPECTRUM OF GRAVITATIONAL WAVES

Observatories & experiments

Ground-based experiment



Space-based observatory



Pulsar timing array



Cosmic microwave background polarisation



Timescales

milliseconds

seconds

hours

years

billions of years

Frequency (Hz)

100

1

10^{-2}

10^{-4}

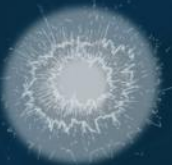
10^{-6}

10^{-8}

10^{-16}

Cosmic fluctuations in the early Universe

Cosmic sources



Supernova



Pulsar



Compact object falling onto a supermassive black hole



Merging supermassive black holes



Merging neutron stars in other galaxies



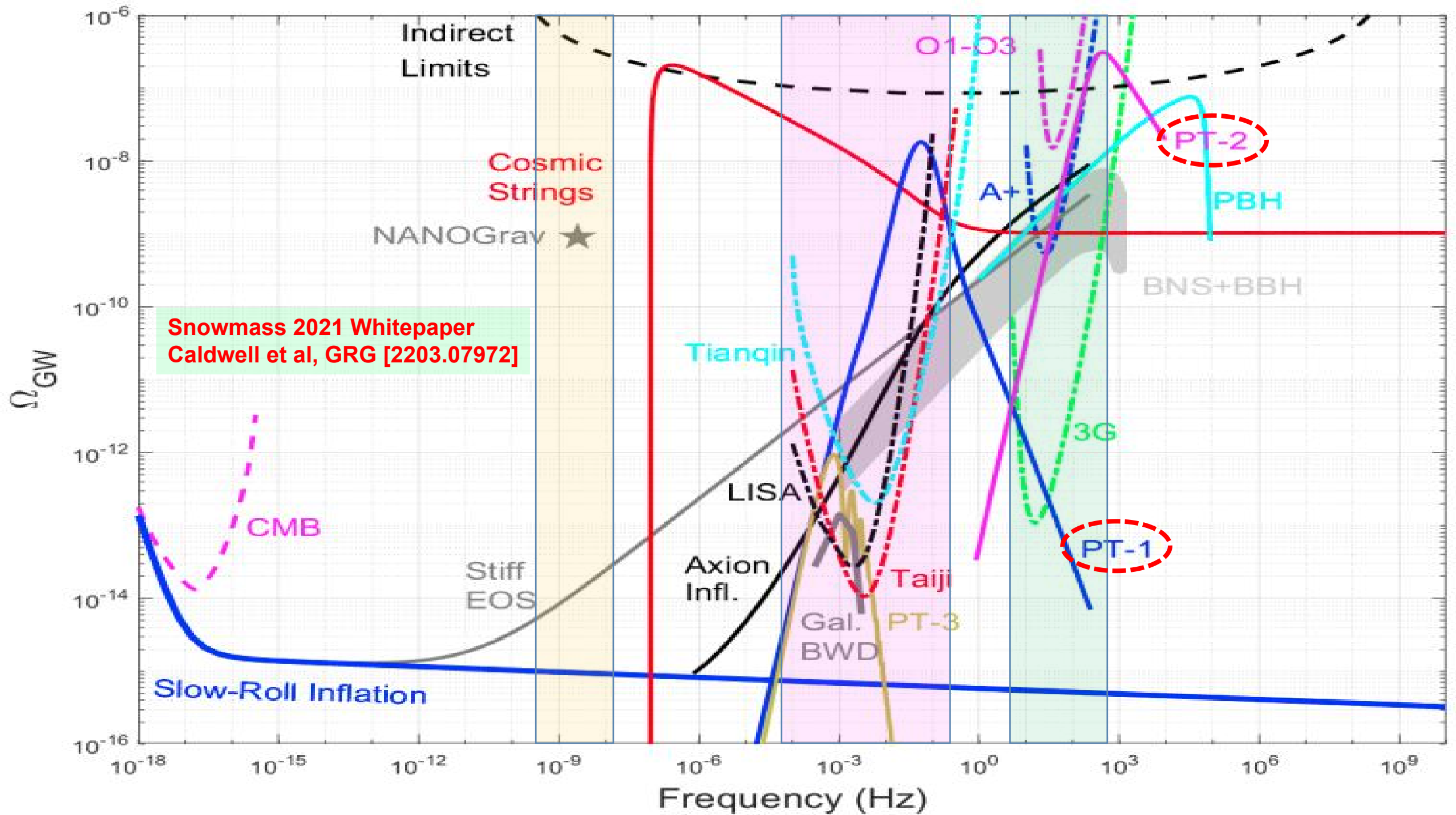
Merging stellar-mass black holes in other galaxies



Merging white dwarfs in our Galaxy

#lisa





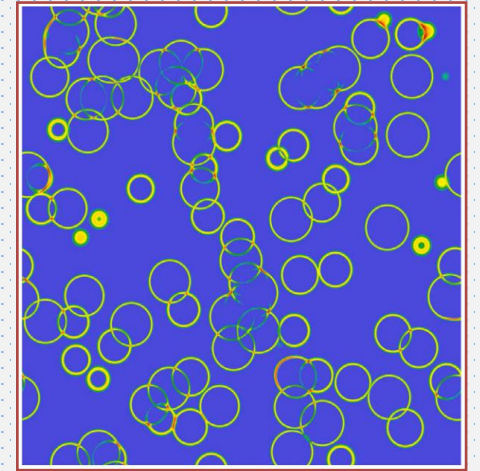
Finite Temperature Effective Potential: Perturbative Method

The commonly adopted approach:

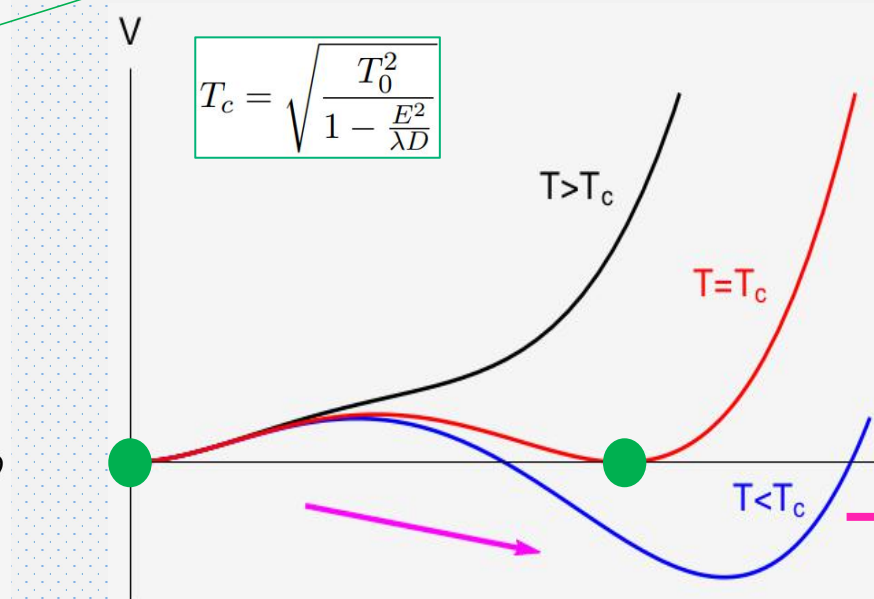
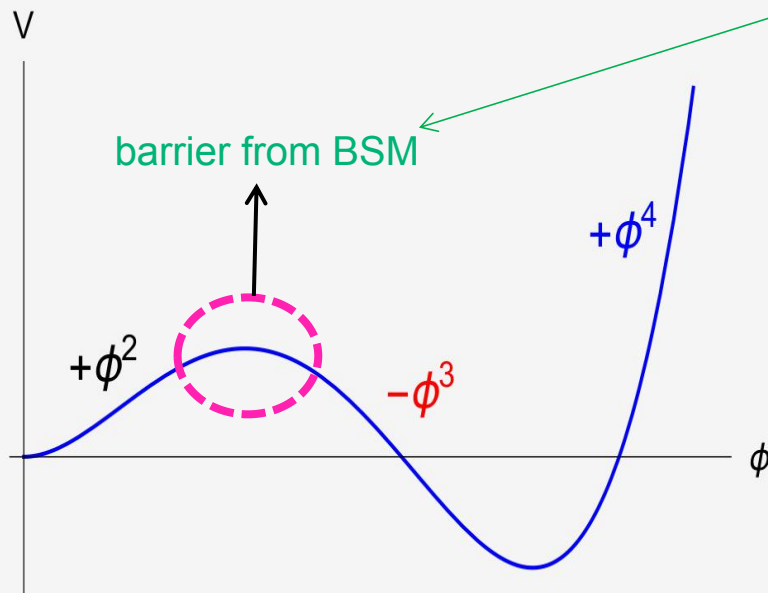
(see, e.g., Morrissey, Ramsey-Musolf, NJP [1206.2942])

$$V_T = V_{\text{tree}} + V_{\text{CW}} + \frac{T^2}{24} \sum_i c_i M_i^2(\phi) - \frac{T}{12\pi} \sum_j d_j [M_j^2(\phi)]^{3/2}$$

$$V(\phi, T) = D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \frac{\lambda}{4}\phi^4$$



Hindmarsh et al, 2015



$$T_c = \sqrt{\frac{T_0^2}{1 - \frac{E^2}{\lambda D}}}$$

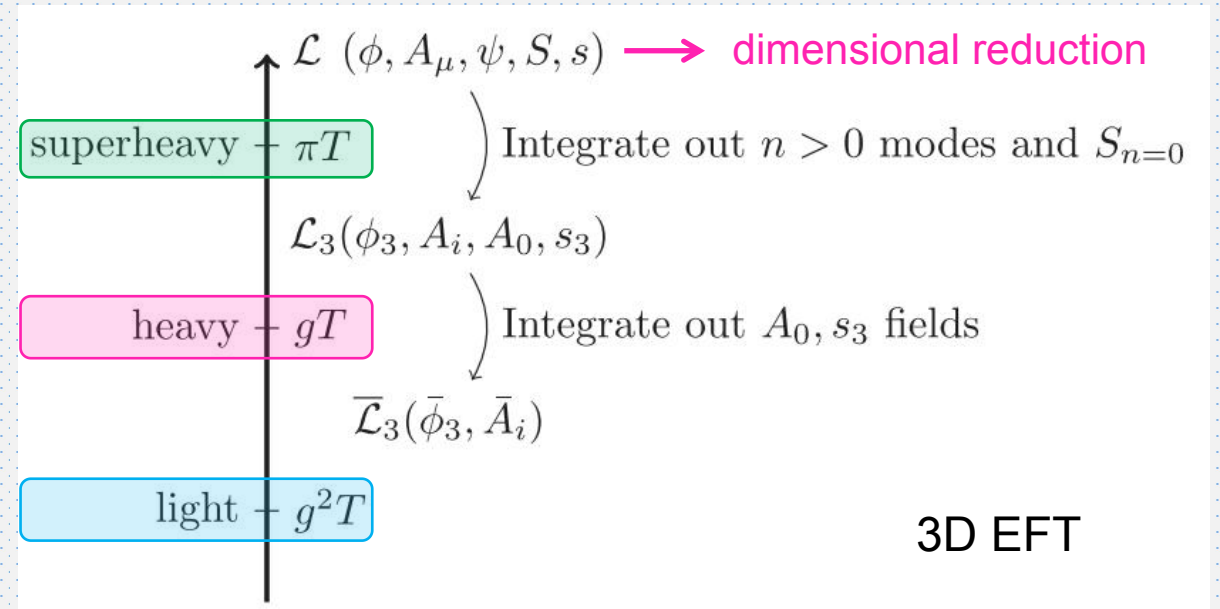
Nucleation rate

$$p = p_0 \exp \left[-\frac{S_{3,b}(T)}{T} \right]$$

fluctuations → critical bubble

Non-Perturbative Method and Applications to BSMs

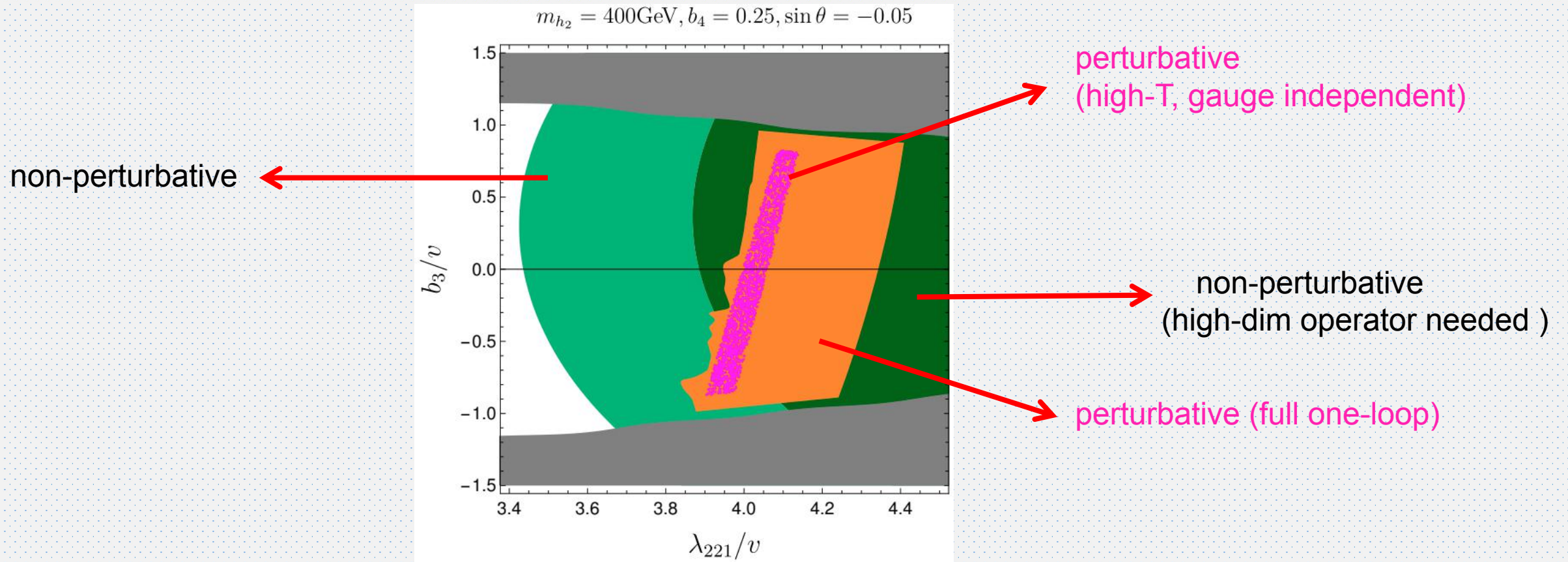
- Infrared problem (Linde, 1980)
- Gauge dependence
(see, e.g., Patel,Ramsey-Musolf, JHEP [1101.4665])
- Non-perturbative method overcomes these problems
- But yet quite limited in BSM studies



Gould,Kozaczuk,Niemi,Ramsey-Musolf,Tenkanen,Weir, PRD [1903.11604]

Dimensional Reduction (Status)		
SM	✓	Farakos,Kajantie,Rummukainen,Shaposhnikov (1994)
MSSM	✓	Cline,Kainulainen(1996), Losada(1996), Laine (1996)
xSM (SM + Singlet)	✓	Brauner,Tenkanen,Tranberg,Vuorinen,Weir, JHEP [1609.06230]
ΣSM (SM + Triplet)	✓	Niemi,Patel,Ramsey-Musolf,Tenkanen,Weir, PRD [1802.10500]
2HDM	✓	Gorda,Helset,Niemi,Tenkanena,Weir, JHEP [1802.05056]

Perturbative vs Non-Perturbative: xSM



Alves, Goncalves, Ghosh, HG, Sinha, JHEP [1909.05268]

Precise Determination of Kinematics

Minkowski spacetime: Hindmarsh, Hijazi, JCAP [1909.10040]

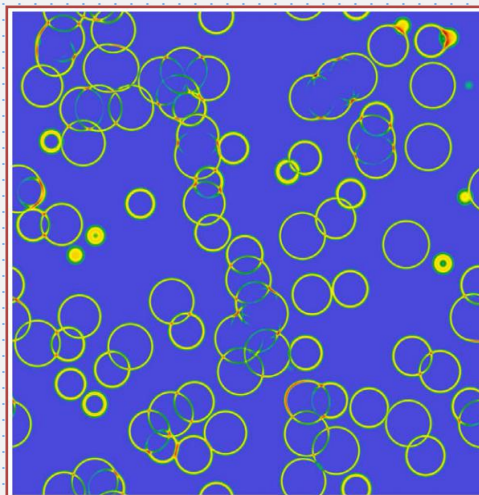
Expanding universe: HG, Sinha, Vagie, White, JCAP [2007.08537]

Statistical properties

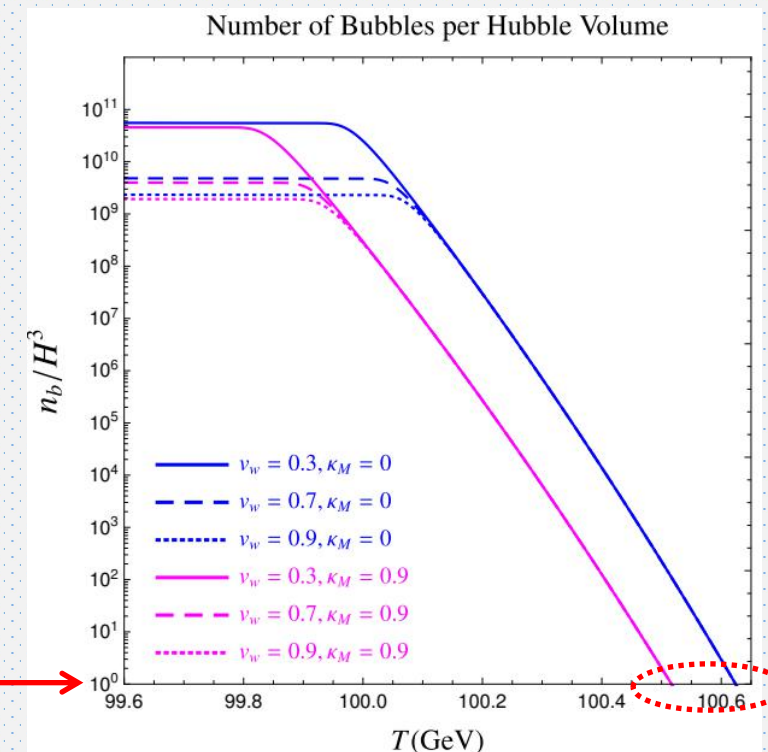
- Bubble Nucleation Rate
- False Vacuum Fraction
- Unbroken Wall Area
- Bubble Lifetime Distribution
- Bubble Number Density and Mean Bubble Separation (R^*)

Useful for modelling of the process

Important inputs for GW (or other observables) calculations



Hindmarsh et al, 2015



Wall Velocity: v_w

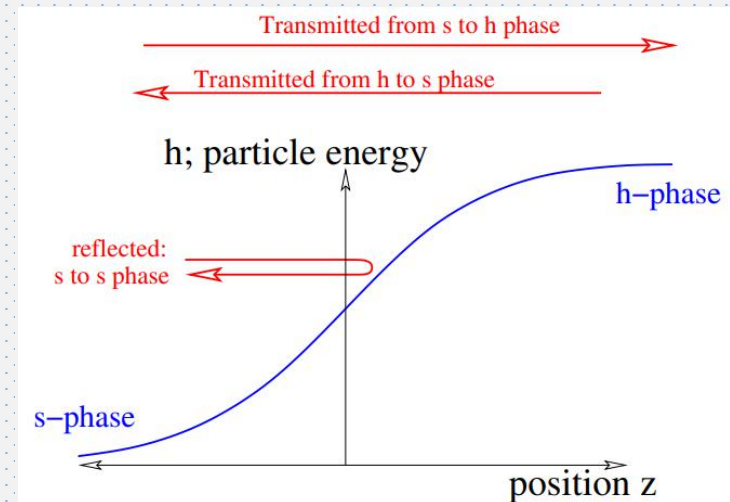
Usually chosen as given fixed value in EWBG and GW studies

But, significant advances in recent years (driven by GW studies)

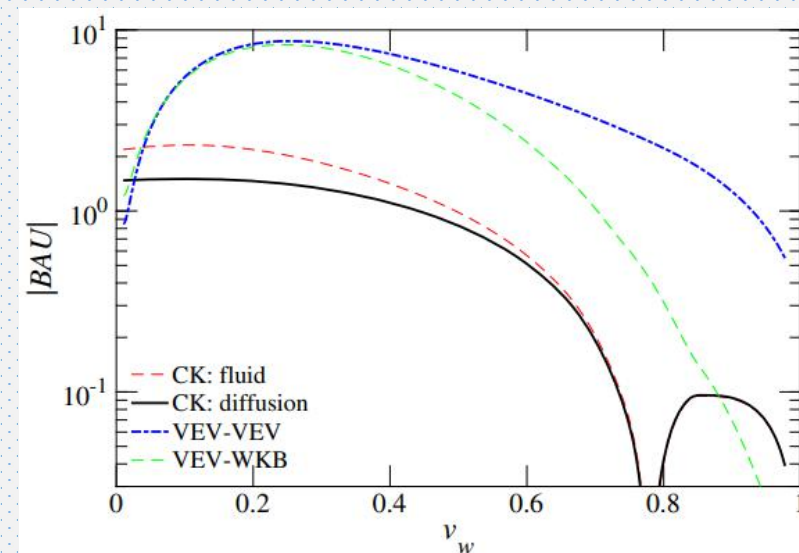
$$\square\phi + V'_T(\phi) + \sum \frac{dm^2}{d\phi} \int \frac{d^3p}{(2\pi)^3 2E} \delta f(p, x) = 0$$

- Friction from out-of-equilibrium (Moore, Prokopec, PRL [9503296]; PRD [9506475])
- Transition radiation (Bodeker, Moore, JCAP [1703.08215])
- All orders resummation (Höche et al, JCAP [2007.10343])
- Lineared distribution or not (Laurent, Cline, PRD [2007.10935]; PRD [2204.13120])
- Singularity or not (Dorsch, Huberb, Konstandin, JCAP [2112.12548], Laurent, Cline)

- EWBG generally requires small v_w
- Might be possible at relatively large v_w , Cline, Kainulainen, PRD [2001.00568]



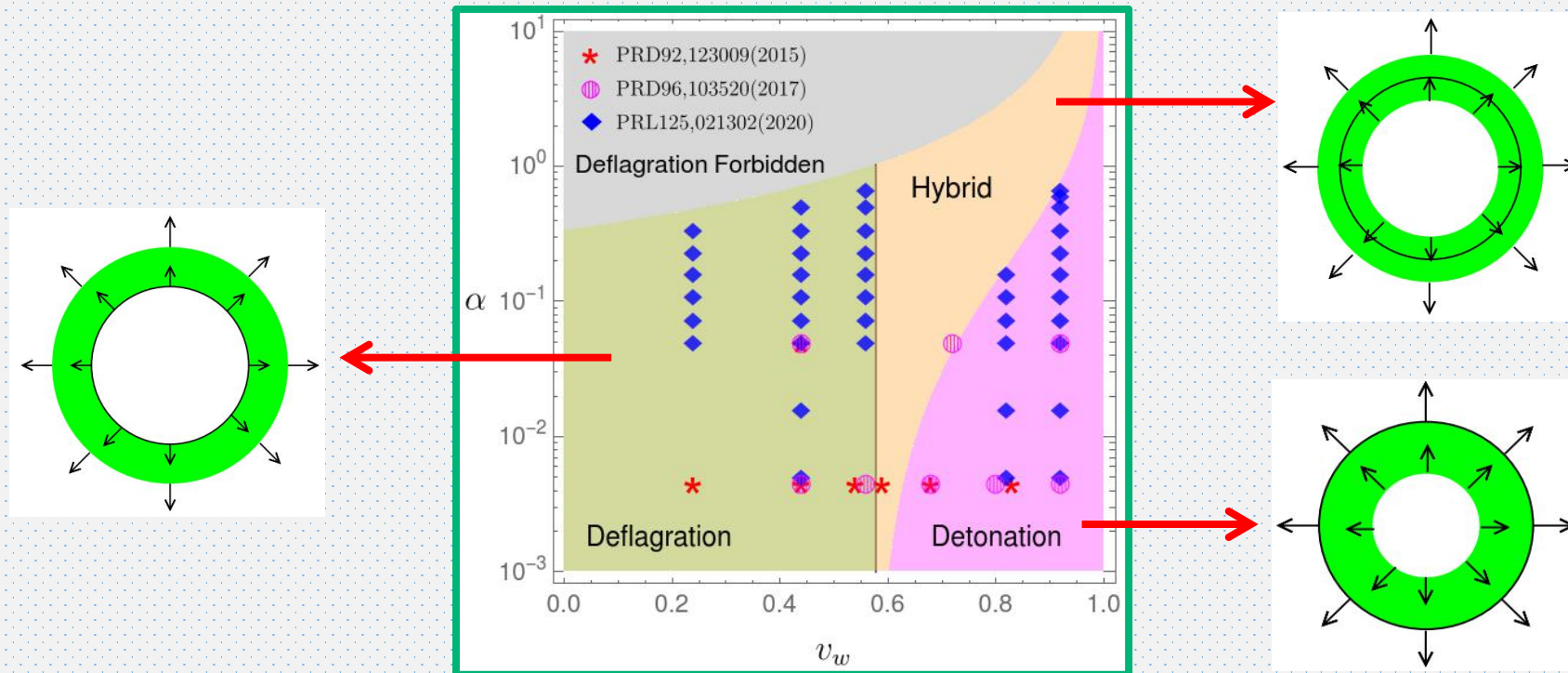
Bodeker, Moore, JCAP [1703.08215]



Cline, Kainulainen, PRD [2001.00568]

Relativistic Combustion and Simulations

Combined analysis: Espinosa,Konstandin,No,Servant JCAP [1004.4187]



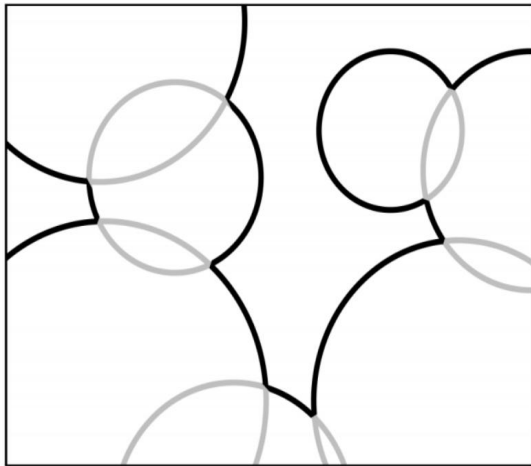
Alves,Goncalves,Ghosh,HG,Sinha, JHEP [1909.05268]

Simulations present clearer picture, and reveal possible new phenomena

Gravitational Wave Sources

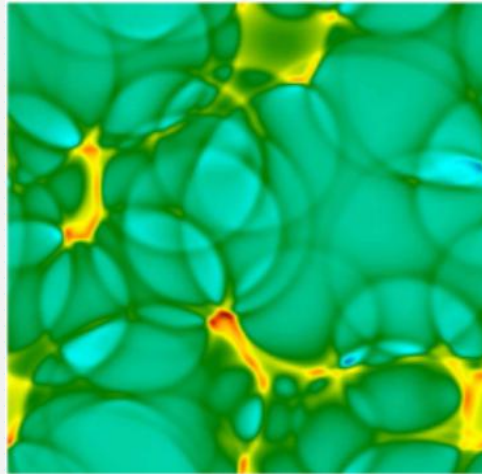
A clearer picture of the PT has been gained from GW studies

Bubble Collisions



energy concentrated at walls

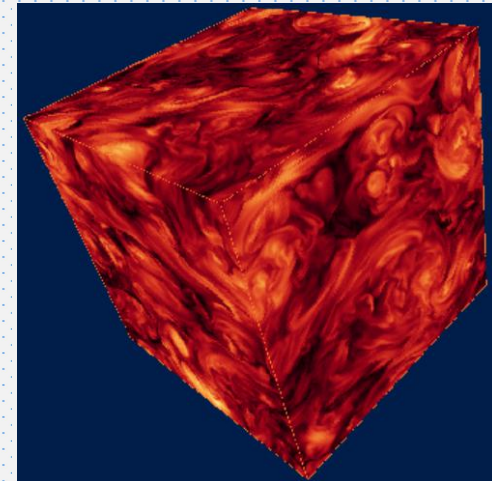
Sound Waves



Hindmarsh, et al, PRL 112, 041301 (2013)

acoustic production

MagnetoHydrodynamic Turbulence



<https://home.mpcdf.mpg.de/~wcm/projects/homog-mhd/mhd.html>

turbulent motion

Bubble Collisions

Envelope Approximation

Simulations:

Kosowsky, Turner, Watkins, Kamionkowski, PRL69,2026(1992), PRD45,4514(1992), PRD47,4372(1993), PRD49,2837(1994), Huber, Konstandin, JCAP09(2008)022

Analytical Modelling:

Jinno, Takimoto, PRD95,024009(2017)

Beyond the Envelope Approximation

Bulk flow model: Konstandin, JCAP03(2018)047, Jinno, Takimoto, JCAP01(2019)060

Direct large scalar lattice simulations: Cutting, Escartin, Hindmarsh, Weir, PRD97,123513(2018), arXiv:2005.13537

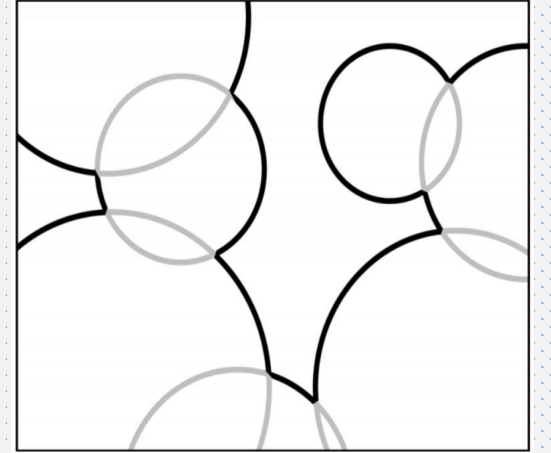
Expanding Universe: Zhong, Gong, Qiu, JHEP02(2022)077

New Phenomena

Di, Wang, Zhou, Bian, Cai, Liu, Phys.Rev.Lett. 126 (2021) 25, 251102

Lewicki, Vaskonen, EPJC 80,1003(2020)

Zhao, Di, Bian, Cai, arxiv:2204.04427



$$\Omega_{\text{coll}}(f)h^2 = 1.67 \times 10^{-5} \Delta \left(\frac{H_{\text{pt}}}{\beta} \right)^2 \left(\frac{\kappa_\phi \alpha}{1 + \alpha} \right)^2 \times \left(\frac{100}{g_*} \right)^{1/3} S_{\text{env}}(f),$$

$$f_{\text{env}} = 16.5 \left(\frac{f_{\text{bc}}}{\beta} \right) \left(\frac{\beta}{H_{\text{pt}}} \right) \left(\frac{T_{\text{pt}}}{100 \text{ GeV}} \right) \left(\frac{g_*}{100} \right)^{1/6} \mu\text{Hz},$$

Sound Waves

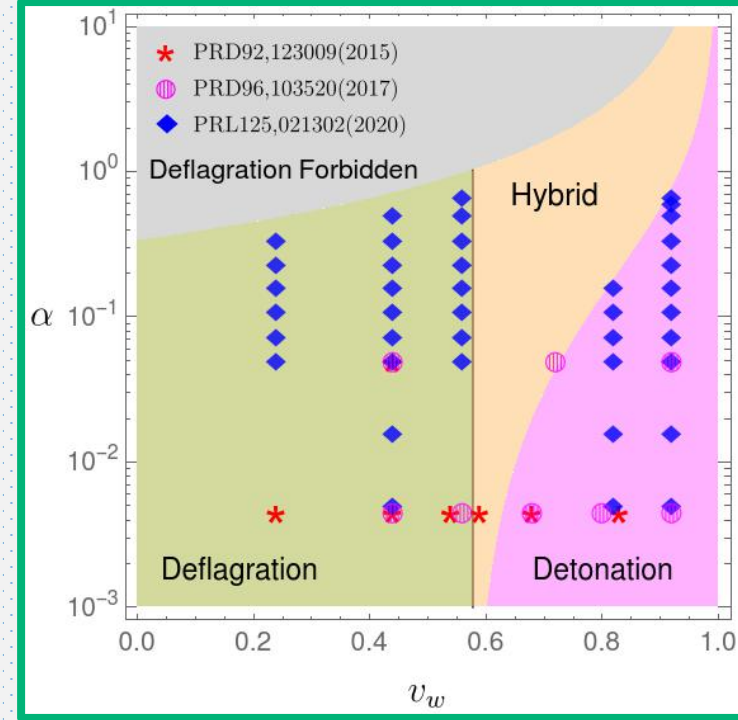
Numerical Simulations:

Hindmarsh, Huber, Rummukainen, Weir,
PRL112, 041301 (2014), PRD92, 123009 (2015), PRD96, 103520 (2017)

Analytical Modelling(sound shell model)

Minkowski: Hindmarsh, 120, 071301 (2018)
Hindmarsh, Hijazi, JCAP12(2019)062

FLRW: [HG](#),Sinha,Vagie,White,JCAP 01 (2021) 001



$$\Omega_{\text{sw}}(f)h^2 = 2.65 \times 10^{-6} \left(\frac{H_{\text{pt}}}{\beta} \right) \left(\frac{\kappa_{\text{sw}}\alpha}{1+\alpha} \right)^2 \left(\frac{100}{g_*} \right)^{1/3} \\ \times v_w \left(\frac{f}{f_{\text{sw}}} \right)^3 \left(\frac{7}{4 + 3(f/f_{\text{sw}})^2} \right)^{7/2} \Upsilon(\tau_{\text{sw}}),$$

Usually the **dominant** source for a thermal plasma.



$$\Upsilon = 1 - (1 + 2\tau_{\text{sw}}H_{\text{pt}})^{-1/2} \quad (\text{RD})$$

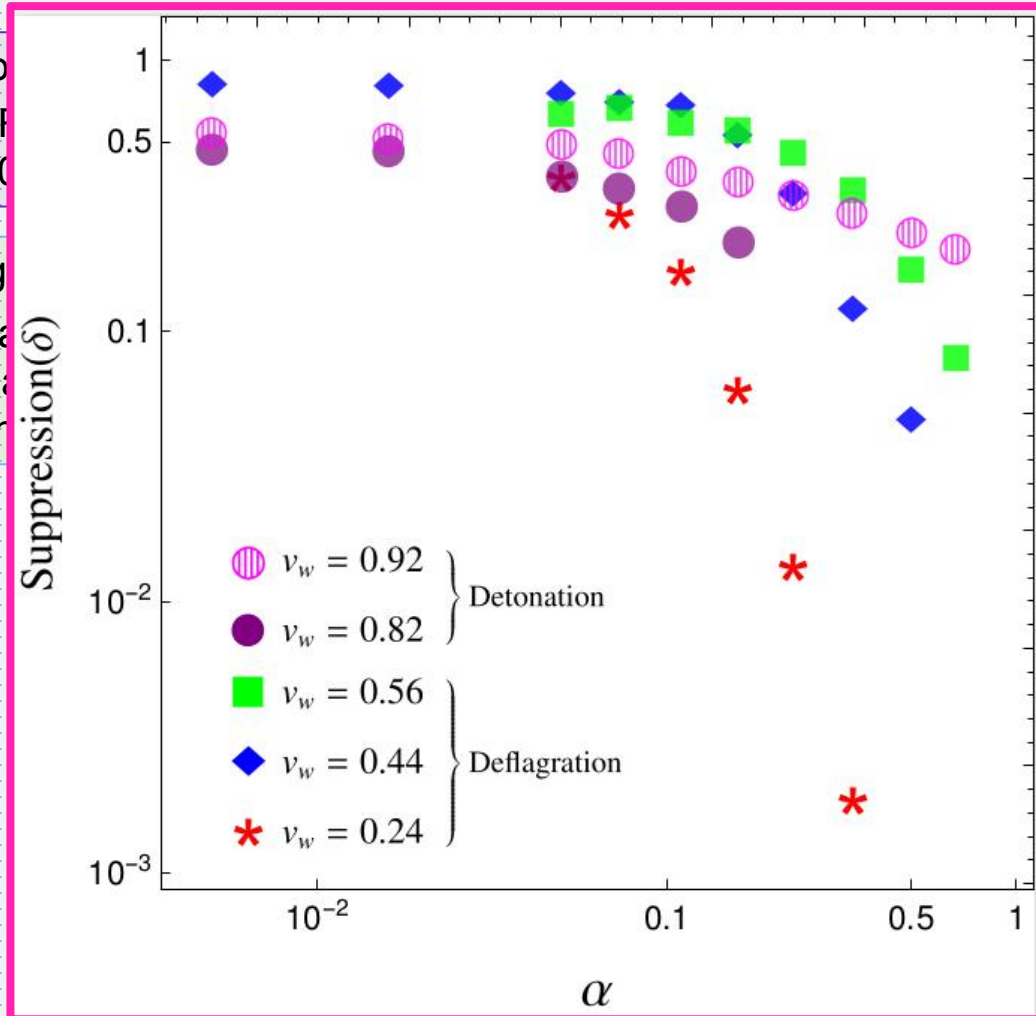
[HG](#),Sinha,Vagie,White,JCAP 01 (2021) 001

Previous formula enforces an infinite lifetime.

Sound Waves

Numerical Simulation
Hindmarsh, Huber, PRL112, 041301 (2004)

Analytical Modelling
Minkowski: Hindmarsh
Hindmarsh
FLRW: HG, Sinha



- Solve the fluid velocity profile modes: detonation, deflagration, hybrid
Espinosa, Konstandin, No, Servant (JCAP06,028)
- Reduction found for $\alpha \sim 1$ and small v_w
Cutting, Hindmarsh, Weir, PRL125, 021302 (2020)

$$\left(\frac{\kappa_{sw} \alpha}{1 + \alpha} \right)^2 \left(\frac{100}{g_*} \right)^{1/3} \left(\frac{7}{f/f_{sw}} \right)^{7/2} \Upsilon(\tau_{sw})$$

$$\Upsilon = 1 - (1 + 2\tau_{sw} H_{pt})^{-1/2} \text{ (RD)}$$

HG, Sinha, Vagie, White, JCAP 01 (2021) 001

Previous formula enforces an infinite lifetime.

The **dominant** source for a FOPT in a thermal plasma.



Magnetohydrodynamic Turbulence

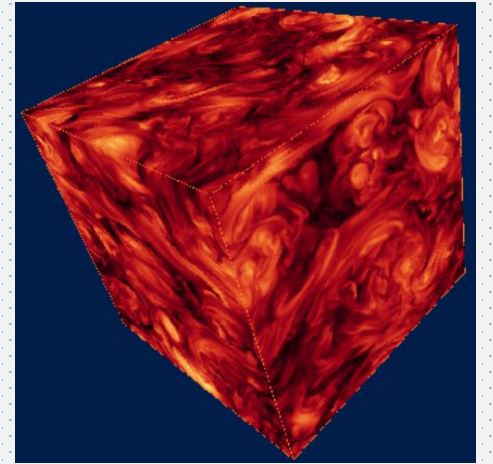
Analytical Modelling

Kolmogorov spectrum:

Kosowsky, Mack, Kahniashvili, PRD66,024030(2002)

Gogoberidze, Kahniashvili, Kosowsky, PRD76,083002(2007)

Caprini, Durrer, Servant, JCAP12(2009)024



<https://home.mpcdf.mpg.de/~wcm/projects/homog-mhd/mhd.html>

5%~10% but uncertain

$$h^2 \Omega_{\text{turb}}(f) = 3.35 \times 10^{-4} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{turb}} \alpha}{1 + \alpha} \right)^{\frac{3}{2}} \left(\frac{100}{g_*} \right)^{1/3} v_w S_{\text{turb}}(f)$$

Caprini, Durrer, Servant, JCAP12(2009)024 (adopted by the LISA Cosmology Working group, JCAP04(2016)001)

$$S_{\text{turb}}(f) = \frac{(f/f_{\text{turb}})^3}{[1 + (f/f_{\text{turb}})]^{\frac{11}{3}} (1 + 8\pi f/h_*)}$$

$$h_* = 16.5 \times 10^{-3} \text{ mHz} \left(\frac{T_*}{100 \text{ GeV}} \right) \left(\frac{g_*}{100} \right)^{\frac{1}{6}}$$

$$f_{\text{turb}} = 2.7 \times 10^{-2} \text{ mHz} \frac{1}{v_w} \left(\frac{\beta}{H_*} \right) \left(\frac{T_*}{100 \text{ GeV}} \right) \left(\frac{g_*}{100} \right)^{\frac{1}{6}}$$

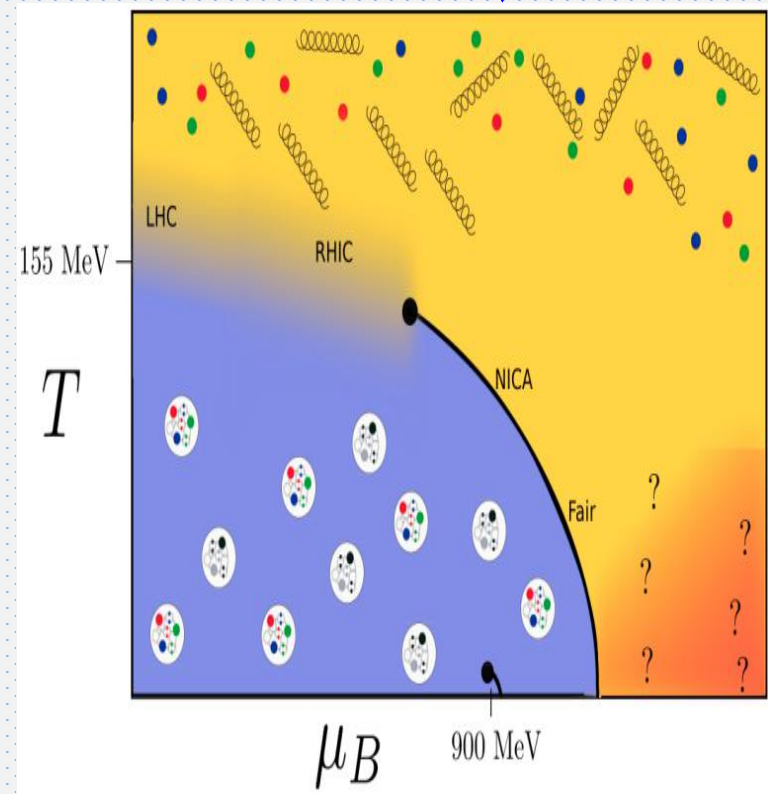
New result: Pol et al, PRD 102, 083512 (2020)

Generic Features

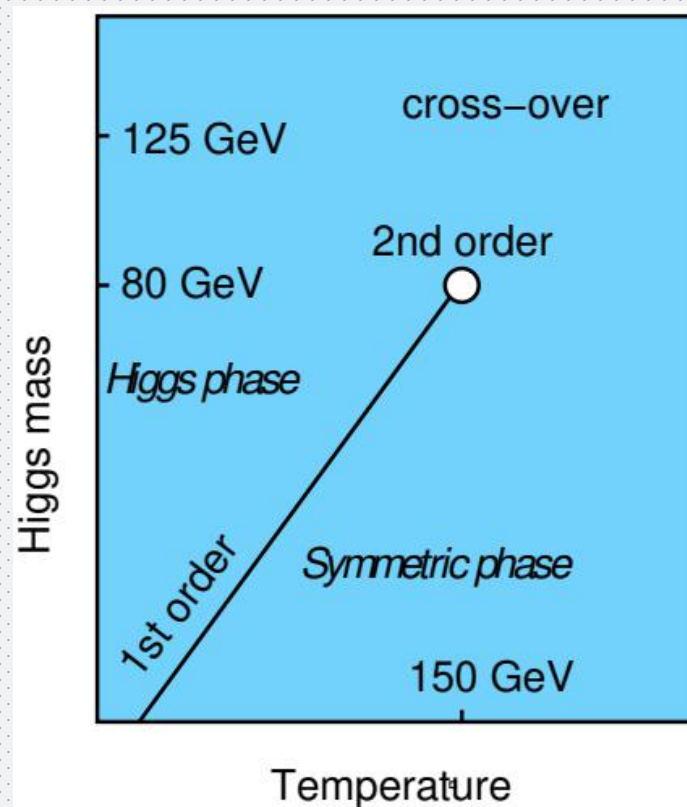
- LIGO (~100Hz) : (~PeV - EeV)
- LISA, Taiji, Tianqin: ~mHz : (~100GeV)
- PTA: nHz (~100MeV)

QCD PT

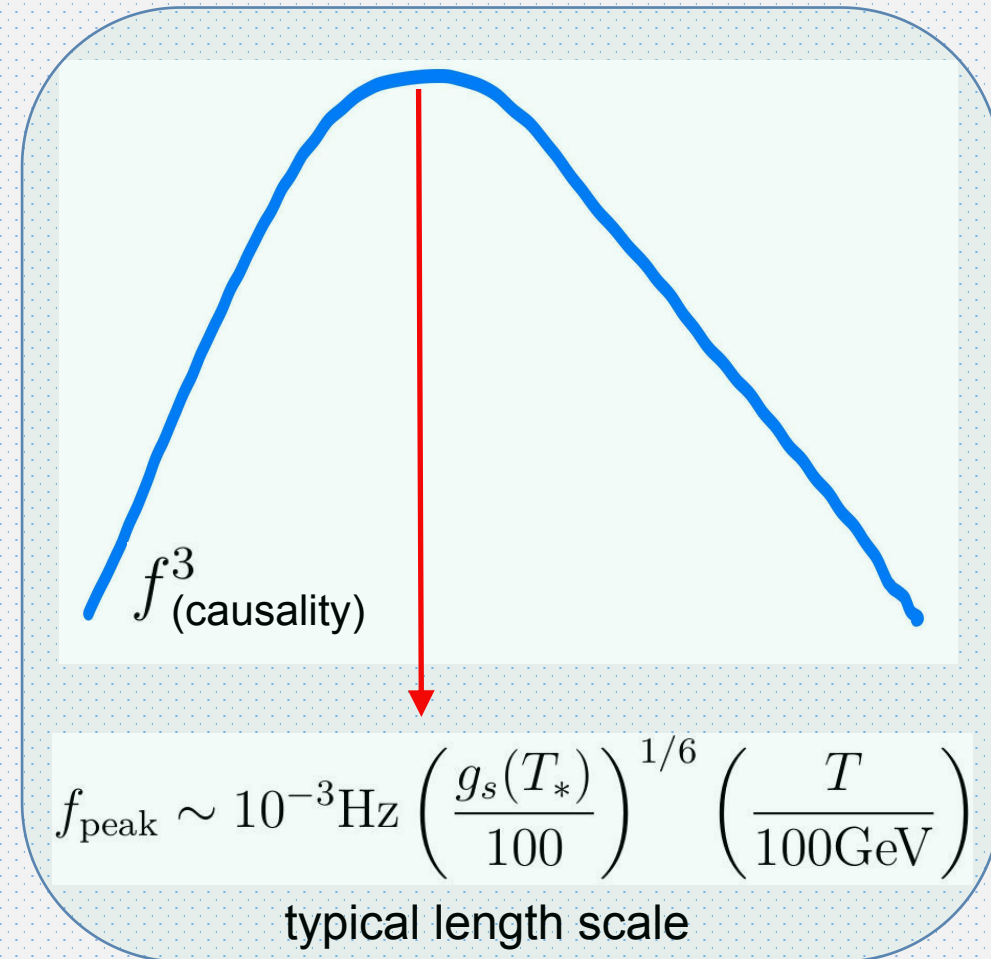
EWPT



Guenther, arxiv: 2010.15503



Hindmarsh et al SciPost Phys.Lect.Notes 24 (2021)



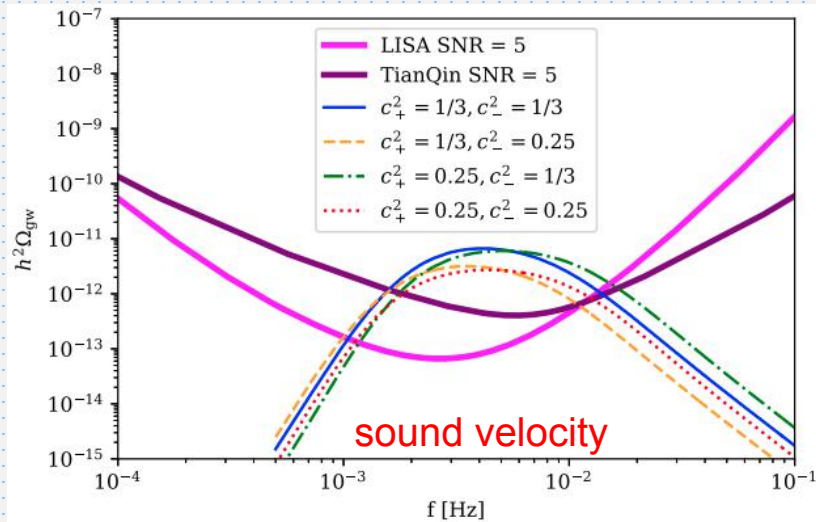
tells PT temperature
(symmetry breaking scale)

Uncertainties

- Finite T effective potential calculations
- Phase transition parameter calculations (vw)
- GW spectra calculations (simulations, modellings)
- Possibly new phenomena

$\Delta\Omega_{\text{GW}}/\Omega_{\text{GW}}$	4d approach	3d approach
RG scale dependence	$\mathcal{O}(10^2 - 10^3)$	$\mathcal{O}(10^0 - 10^1)$
Gauge dependence	$\mathcal{O}(10^1)$	$\mathcal{O}(10^{-3})$
High- T approximation	$\mathcal{O}(10^{-1} - 10^0)$	$\mathcal{O}(10^0 - 10^2)$
Higher loop orders	unknown	$\mathcal{O}(10^0 - 10^1)$
Nucleation corrections	unknown	$\mathcal{O}(10^{-1} - 10^0)$
Nonperturbative corrections	unknown	unknown

Croon, Gould, Schicho, Tenkanen, White, JHEP [2009.10080]



Wang, Huang, Li, PRD [2112.14650]

Effect (fixed wall velocity)	Range of error (medium)	Range of error (low)	Type of error
Transition temperature	$\mathcal{O}(10^{-4} - 10^1)$	$\mathcal{O}(10^{-1} - 10^0)$	Random
Mean bubble separation	$\mathcal{O}(0 - 10^{-1})$	$\mathcal{O}(10^{-1} - 10^0)$	Suppression
Fluid velocity	$\mathcal{O}(10^{-2} - 10^0)$	$\mathcal{O}(10^{-2} - 10^0)$	Random
Finite lifetime	$\mathcal{O}(10^{-3} - 10^{-1})$	$\mathcal{O}(10^1 - 10^3)$	Enhancement
Vorticity effects	$\mathcal{O}(10^{-1} - 10^0)$	—	Random

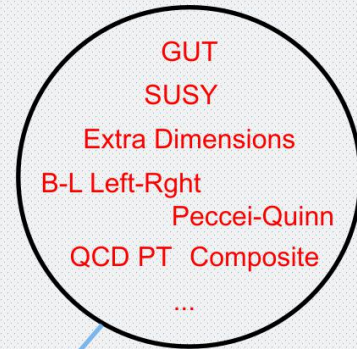
HG, Sinha, Vagie, White, JHEP [2103.06933]

BSM studies

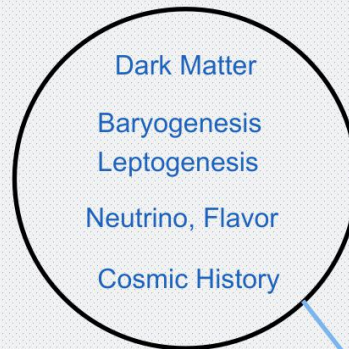
Chung, Long, Wang, PRD [1209.1819]

- Large cubic term from thermal corrections (loop level)
- Add new scalars (tree level)
- Including non-renormalizable operators

More general EFT approach: Cai, Hashino, Wang, Yu [2202.08295]



Classification according to the symmetries



Classification according to the problems

Models	Strong 1 st order phase transition	GW signal	Cold DM	Dark Radiation and small scale structure
SM charged				
Triplet [20–22]	✓	✓	✓	✗
complex and real Triplet [23] (Georgi-Machacek model)	✓	✓	✓	✗
Multiplet [24]	✓	✓	✓	
2HDM [25–30]	✓	✓		✗
MLRSM [31]	✓	✓	✗	✗
NMSSM [32–36]	✓	✓	✓	✗
SM uncharged				
S_ν (xSM) [37–49]	✓	✓	✗	✗
2 S_ν 's [50]	✓	✓	✓	✗
S_c (cxSM) [49, 51–54]	✓	✓	✓	✗
$U(1)_D$ (no interaction with SM) [55]	✓	✓	✓	✗
$U(1)_D$ (Higgs Portal) [56]	✓	✓	✓	
$U(1)_D$ (Kinetic Mixing) [57]	✓	✓	✓	
Composite $SU(7)/SU(6)$ [58]	✓	✓	✓	
$U(1)_L$ [59]	✓	✓	✓	✗
$SU(2)_D \rightarrow$ global $SO(3)$ by a doublet [60–62]			✓	✗
$SU(2)_D \rightarrow U(1)_D$ by a triplet [63–65]			✓	✓
$SU(2)_D \rightarrow Z_2$ by two triplets [66]			✓	✗
$SU(2)_D \rightarrow Z_3$ by a quadruplet [67, 68]			✓	✗
$SU(2)_D \times U(1)_{B-L} \rightarrow Z_2 \times Z_2$ by a quintuplet and a S_c [69]			✓	✗
$SU(2)_D$ with two dark Higgs doublets [70]	✓	✓	✗	✗
$SU(3)_D \rightarrow Z_2 \times Z_2$ by two triplets [62, 71]			✓	✗
$SU(3)_D$ (dark QCD) (Higgs Portal) [72, 73]	✓	✓	✓	
$G_{SM} \times G_{D,SM} \times Z_2$ [74]	✓	✓	✓	
$G_{SM} \times G_{D,SM} \times G_{D,SM} \dots$ [75]	✓	✓	✓	
Current work				
$SU(2)_D \rightarrow U(1)_D$ (see the text)	✓	✓	✓	✓

Ghosh, HG, Han, Liu, JHEP [2012.09758]

EWPT and Related Physics

The electroweak phase transition: a collider target

Michael J. Ramsey-Musolf

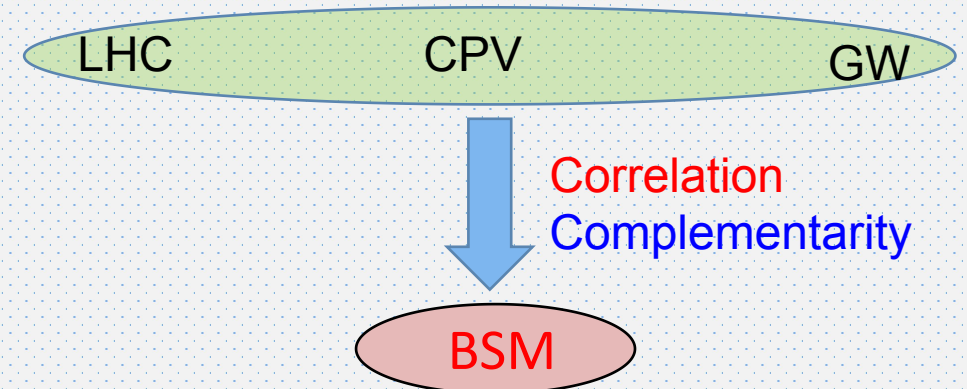
Tsung-Dao Lee Institute, and School of Physics and Astronomy, Shanghai Jiao Tong University, Shanghai 200240, China

Amherst Center for Fundamental Interactions, Department of Physics, University of Massachusetts-Amherst, Amherst, MA 01003, U.S.A.

Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, CA 91125, U.S.A.

E-mail: mjrm@sjtu.edu.cn, mjrm@physics.umass.edu

- Modified Higgs potential (**Higgs physics**, **GW**)
- Extra CP-violation (**EDM**, **LHC**)
- B-violation: Sphaleron process (**LHC**, **GW**)

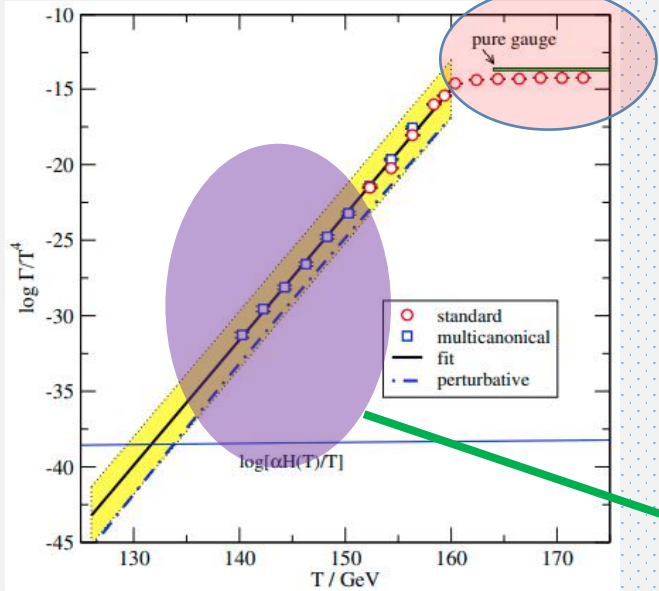


Electroweak Baryogenesis

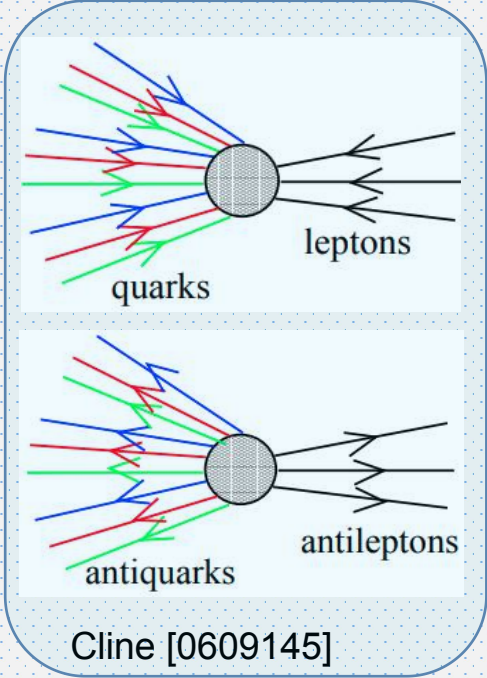
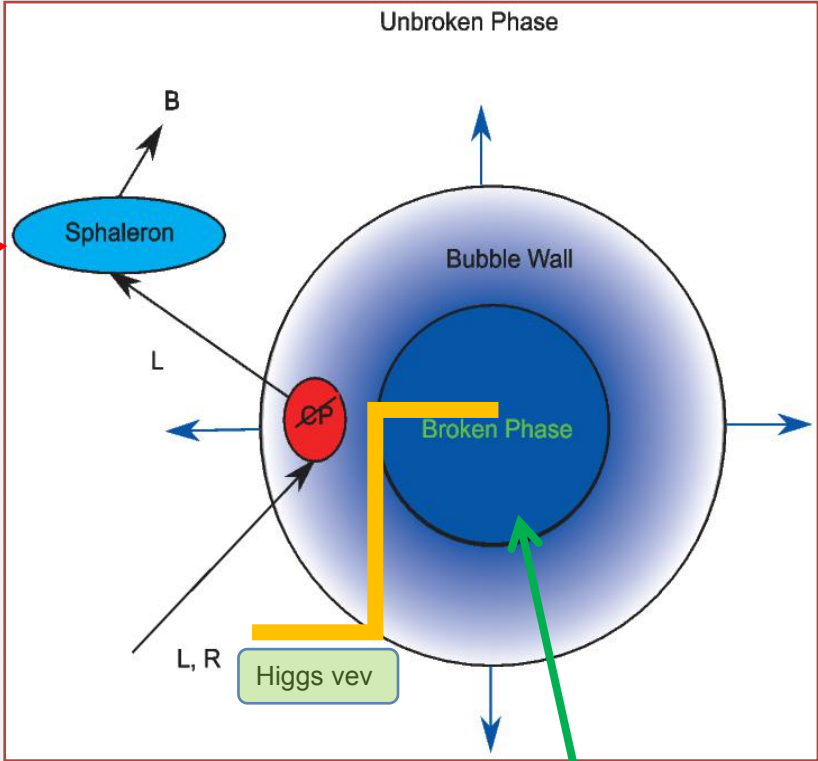
Kuzmin,Rubakov,Shaposhnikov (1985)
 Shaposhnikov (1986)
 Cohen,Kaplan,Nelson (1990, 1991)

symmetric phase

$$\Gamma^{\text{sym}} \approx 6 \times (18 \pm 3) \alpha_W^5 T^4$$



D'Onofrio et al, PRL [1404.3565]



$$\log \frac{\Gamma_{\text{Broken}}}{T^4} = (0.83 \pm 0.01) \frac{T}{\text{GeV}} - (147.7 \pm 1.9)$$

broken phase (should be suppressed)

Lepton-flavored Electroweak Baryogenesis

- CP-violation is generally small, **decoupled** from GW analysis
- Lepton-flavored EWBG is **effective** for baryon asymmetry generation

Many studies since then:

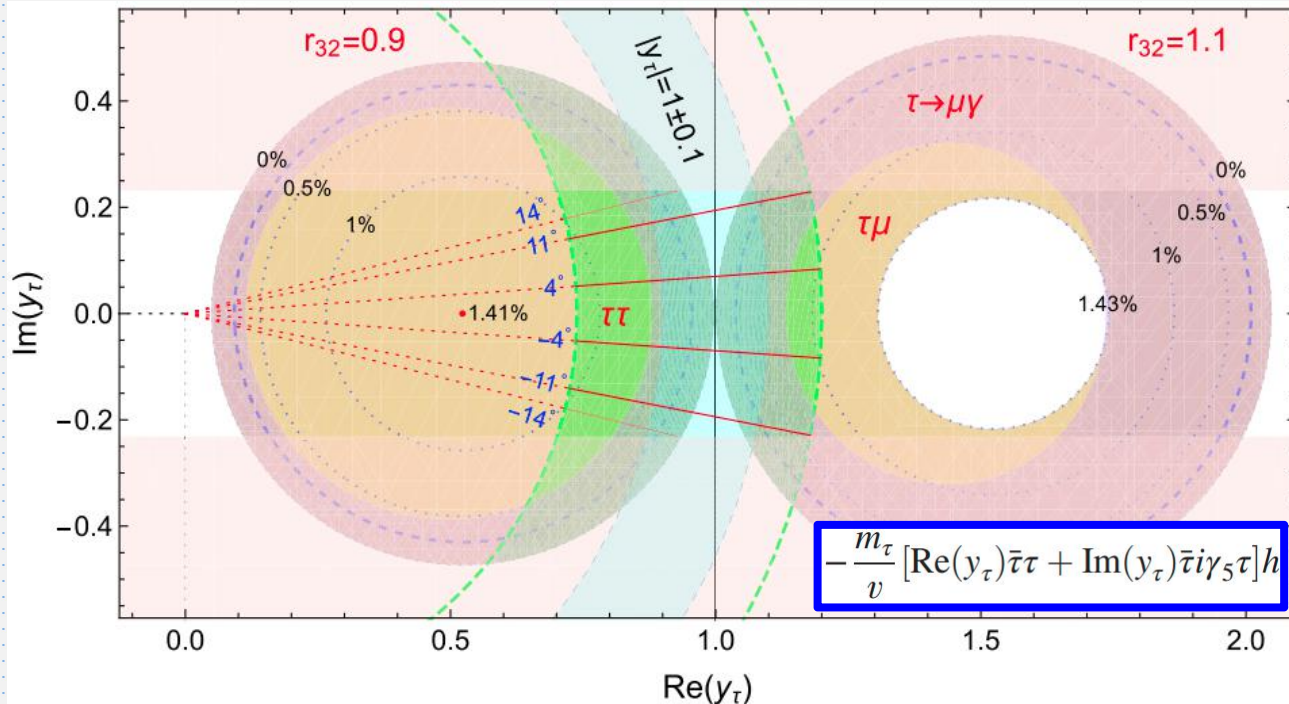
De Vries, Postma, van de Vis, JHEP [1811.11104]

Modak, Senaha, PRD [1811.08088]

Fuyuto, Hou, Senaha, PLB [1705.05034]

and more...

HG, Li, Liu, Ramsey-Musolf, Shu, PRD [1609.09849]



Type III 2HDM

$$\mathcal{L}_{\text{Yukawa}}^{\text{Lepton}} = -\bar{L}^i [Y_{1,ij} \Phi_1 + Y_{2,ij} \Phi_2] e_R^j + \text{H.c.}$$

Jarlskog-like invariant

$$J_A = \frac{1}{v^2 \mu_{12}^{\text{HB}}} \sum_{a,b,c=1}^2 v_a v_b^* \mu_{bc} \text{Tr}[Y_c Y_a^\dagger]$$

$$\text{Im}(J_A) = \begin{cases} \text{Gauge Basis: } -Y_{2,\tau\mu}^E \text{Im} Y_{2,\tau\mu}^E & \Rightarrow \text{Baryon Asymmetry} \\ \text{Mass Basis: } 2m_\tau \text{Im} N_{\tau\tau}^E / v^2 & \Rightarrow \text{CP-violating } h\bar{\tau}\tau \end{cases}$$

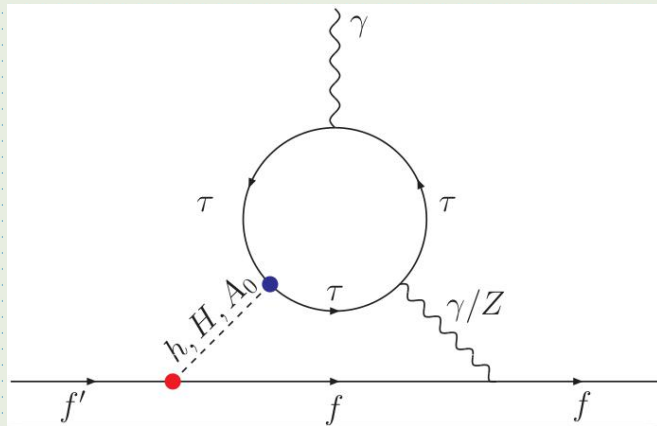
Lepton-flavored Electroweak Baryogenesis: Higgs CPV

$$-\frac{m_\tau}{v} [\text{Re}(y_\tau)\bar{\tau}\tau + \text{Im}(y_\tau)\bar{\tau}i\gamma_5\tau]h$$

OK

discovery or exclusion?

Unconstrained from EDM measurements



$$\left| \frac{d_e}{e} \right| \approx 1.87 \times 10^{-29} |\text{Im}y_\tau|$$

ACME 2014: $\left| \frac{d_e}{e} \right| < 8.7 \times 10^{-29} e \cdot \text{cm}$

Collider Sensitivities

Collider	<i>pp</i>	<i>pp</i>	<i>pp</i>	<i>e⁺e⁻</i>	<i>e⁺e⁻</i>	<i>e⁺e⁻</i>	<i>e⁺e⁻</i>	<i>e⁻p</i>	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	125	125	≥ 500		(theory)
\mathcal{L} (fb ⁻¹)	300	3,000	20,000	250	350	500	1,000	250				
<i>HZZ/HWW</i>	$4 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.4 \cdot 10^{-4}$	$1.1 \cdot 10^{-4}$	$4 \cdot 10^{-5}$	$8 \cdot 10^{-6}$	✓	✓	✓	✓	$< 10^{-5}$
<i>Hγγ</i>	-	0.50	✓	-	-	-	-	-	0.06	-	-	$< 10^{-2}$
<i>HZγ</i>	-	~1	✓	-	-	-	-	-	-	-	-	$< 10^{-2}$
<i>Hgg</i>	0.12	0.011	✓	-	-	-	-	-	-	-	-	$< 10^{-2}$
<i>Ht\bar{t}</i>	0.24	0.05	✓	-	-	0.29	0.08	-	-	-	✓	$< 10^{-2}$
<i>Hττ</i>	0.07	0.008	✓	0.01	0.01	0.02	0.06	-	✓	✓	✓	$< 10^{-2}$
<i>Hμμ</i>	-	-	-	-	-	-	-	-	-	✓	-	$< 10^{-2}$

Snowmass White Paper: Gritsan et al [2205.07715]

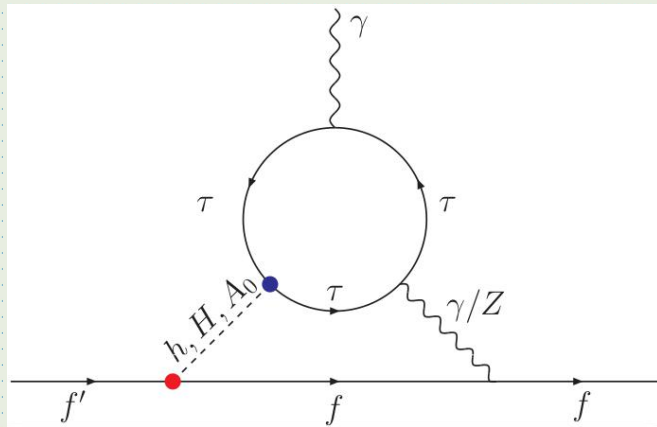
Lepton-flavored Electroweak Baryogenesis: Higgs CPV

$$-\frac{m_\tau}{v} [\text{Re}(y_\tau)\bar{\tau}\tau + \text{Im}(y_\tau)\bar{\tau}i\gamma_5\tau]h$$

OK

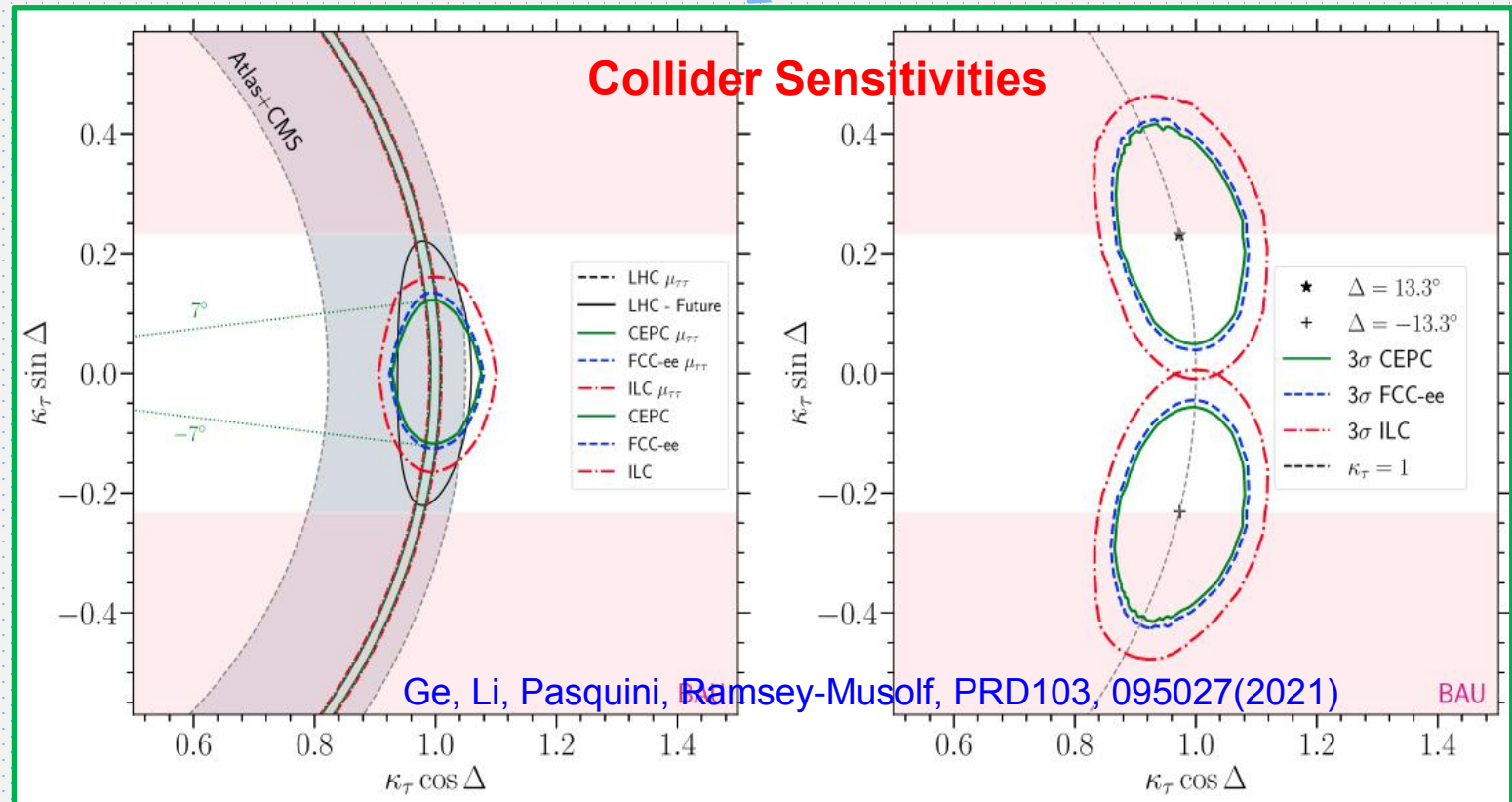
discovery or exclusion?

Unconstrained from EDM measurements



$$\left| \frac{d_e}{e} \right| \approx 1.87 \times 10^{-29} |\text{Im}y_\tau|$$

ACME 2014: $\left| \frac{d_e}{e} \right| < 8.7 \times 10^{-29} e \cdot \text{cm}$

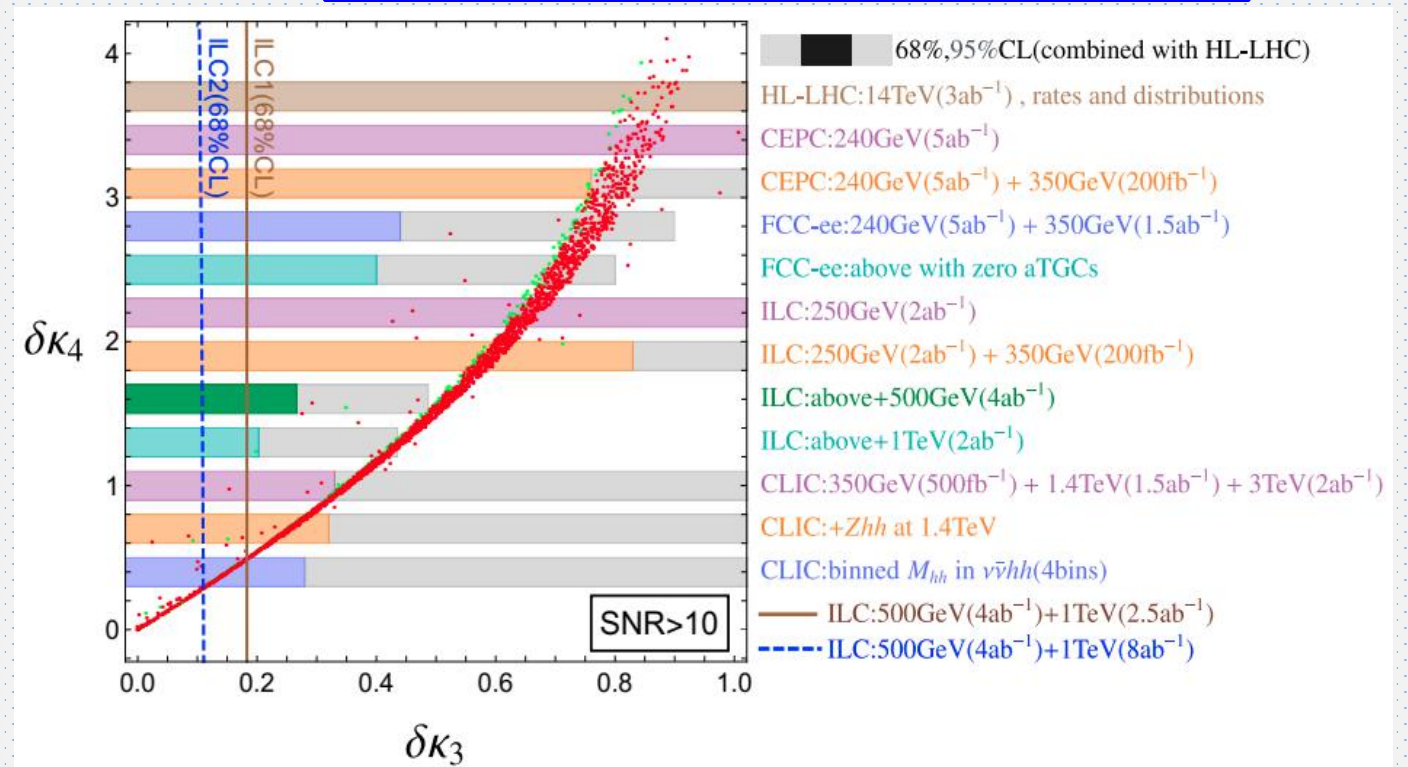
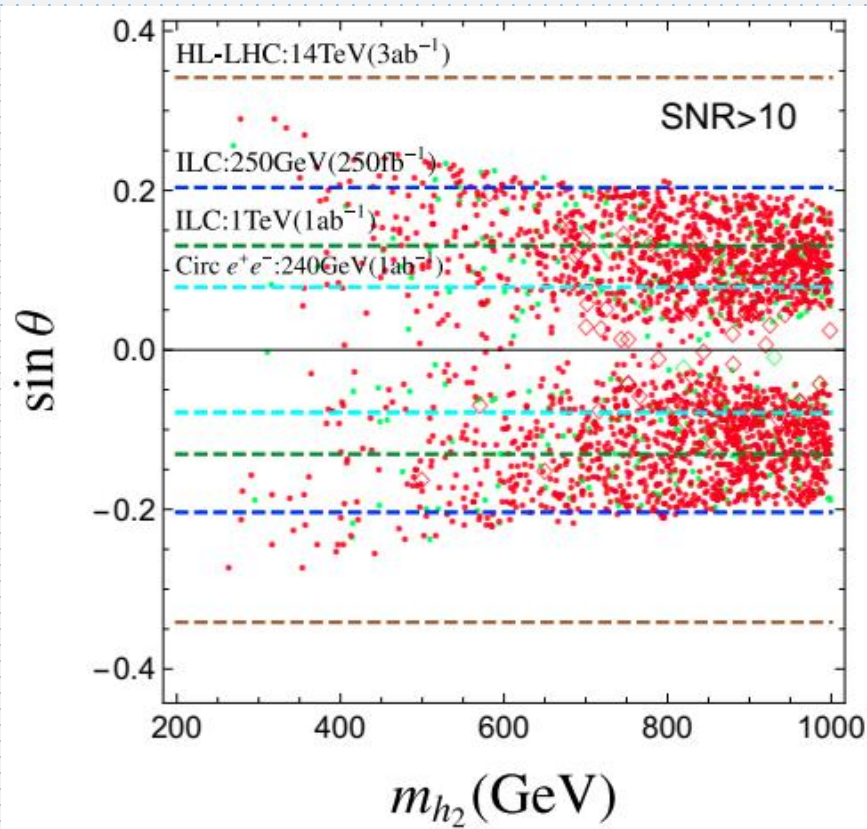


Higgs Precision Measurements

- First order EWPT achievable in simplest **SM+Singlet** model
- **Correlation** and **complementarity** between collider and GW probes

h1: the Higgs
h2: heavier scalar

$$\Delta\mathcal{L} = -\frac{1}{2} \frac{m_{h_1}^2}{v} (1 + \delta\kappa_3) h_1^3 - \frac{1}{8} \frac{m_{h_1}^2}{v^2} (1 + \delta\kappa_4) h_1^4$$



Di-Higgs Production

- Enhanced (resonant) di-Higgs production

See also:

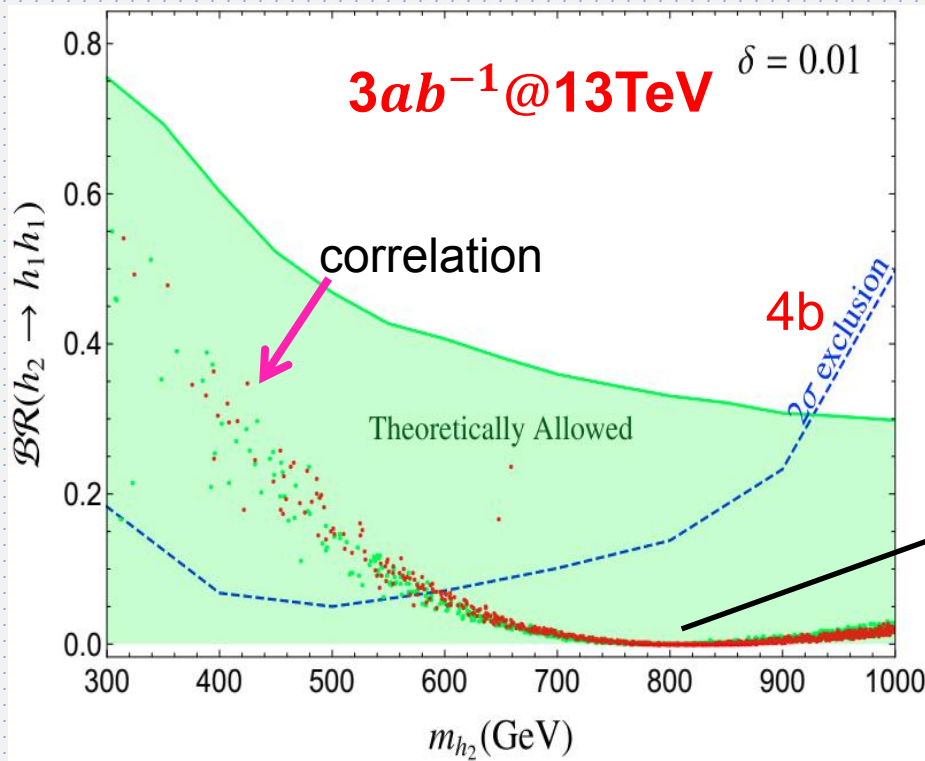
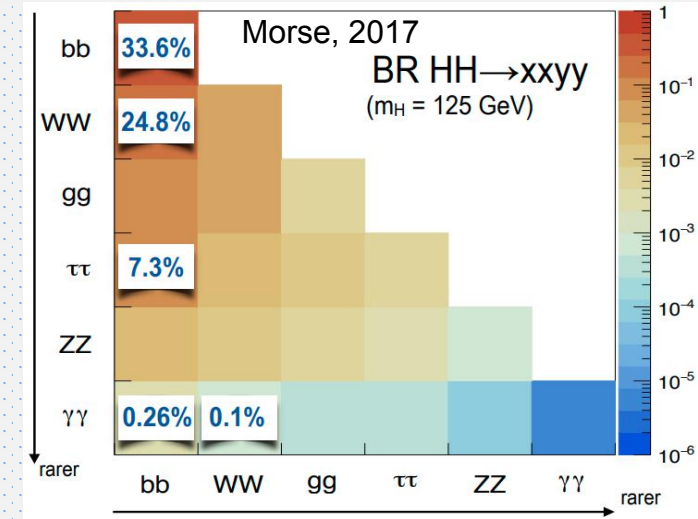
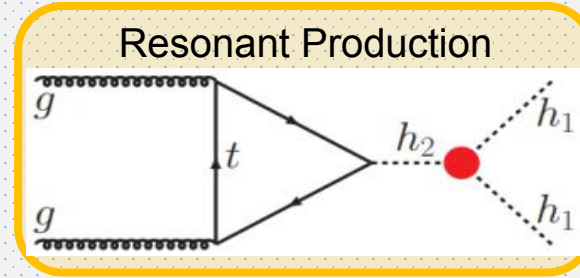
No, Ramsey-Musolf, PRD [1310.6035]

Li, Ramsey-Musolf, Willcoq, JHEP [1906.05289]

Huang, No, Pernie, Ramsey-Musolf, Safonov, PRD [1701.04442]

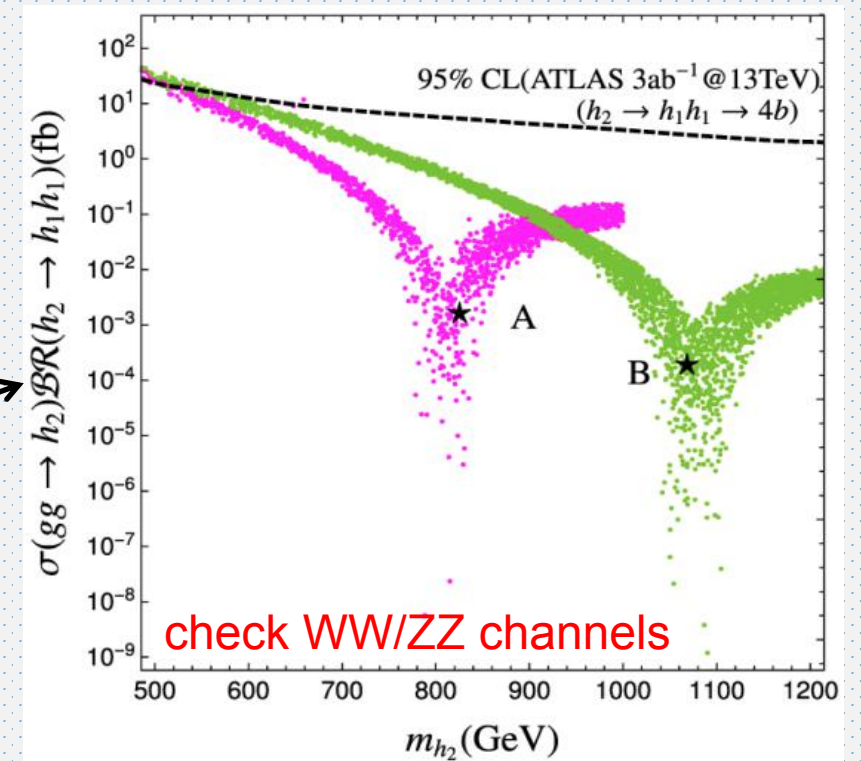
Zhang, Li, Liu, Ramsey-Musolf, Zeng, Arunasalam [2303.03612]

and more...



Alves, Gonçalves, Ghosh, HG, Sinha, JHEP [1909.05268]

di-Higgs blindspot
complementarity



Alves, Gonçalves, Ghosh, HG, Sinha, PLB [2007.15654]

WIMP affecting EWPT

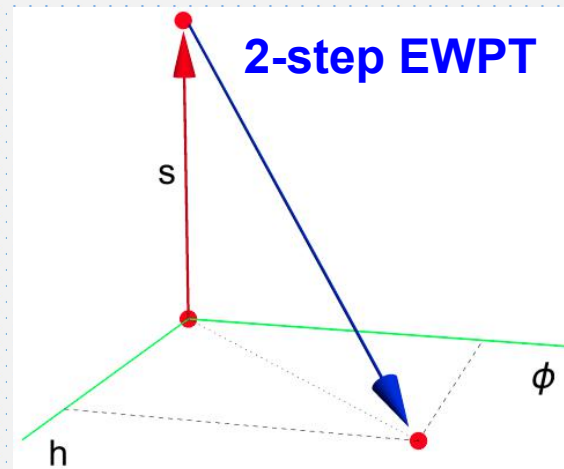
- WIMP naturally plays a role during EWPT

$$V_0 = -\frac{1}{2}\mu_\Phi^2\Phi^2 + \frac{1}{4}\lambda_\Phi\Phi^4 - \frac{1}{2}\mu_S^2S^2 + \frac{1}{4}\lambda_S S^4$$

$$-\mu^2 H^\dagger H + \lambda(H^\dagger H)^2 + \lambda_1 S^2 H^\dagger H + \lambda_2 \Phi^2 H^\dagger H$$

$$+\lambda_3 S^2 \Phi^2,$$

Chao, HG, Shu, JCAP [1702.02698]

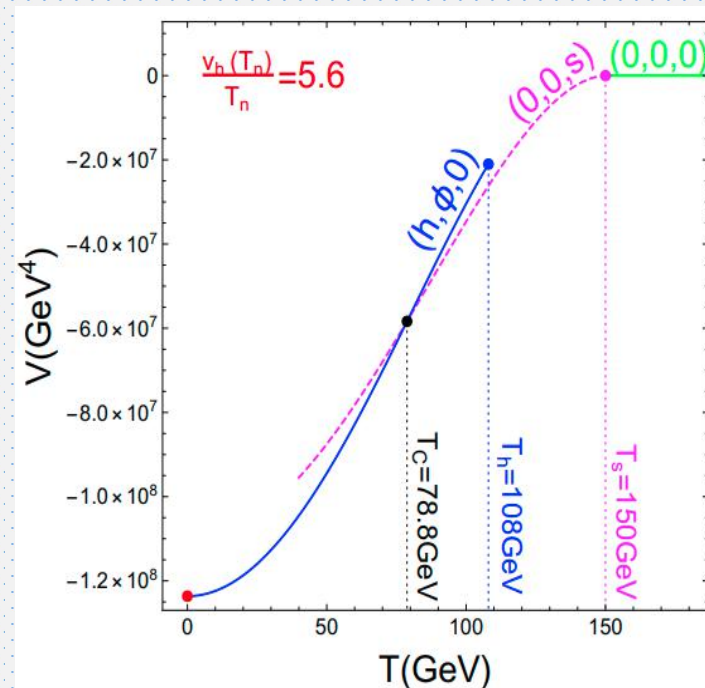
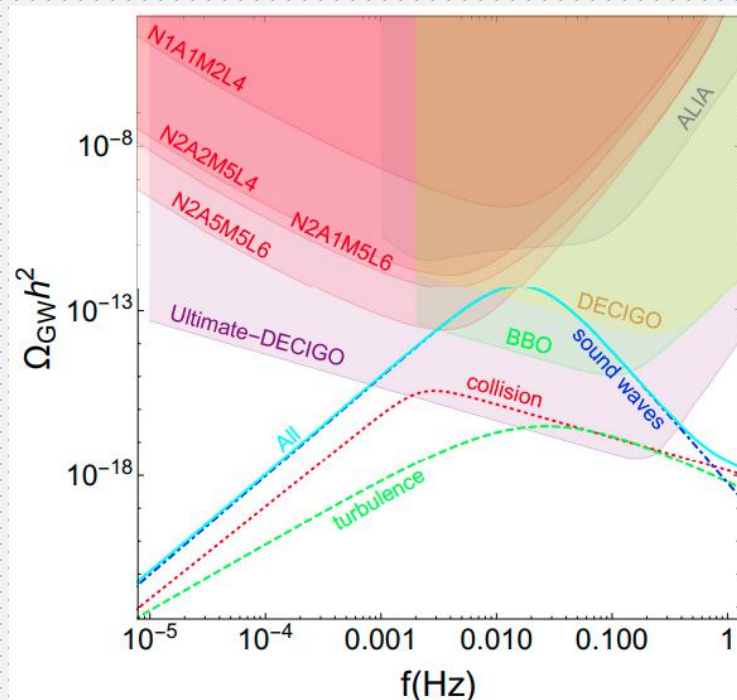


Direct detection limits

$$\sigma_n = \frac{\mu^2 m_n^2}{\pi v_{EW}^2 m_S^2} \left[\frac{c_\theta a_{\hat{h}}}{m_{\hat{h}}^2} - \frac{s_\theta a_{\hat{\phi}}}{m_{\hat{\phi}}^2} \right]^2 \left(\frac{2}{9} + \frac{7}{9} \sum_{q=u,d,s} f_{T_q}^n \right)^2$$

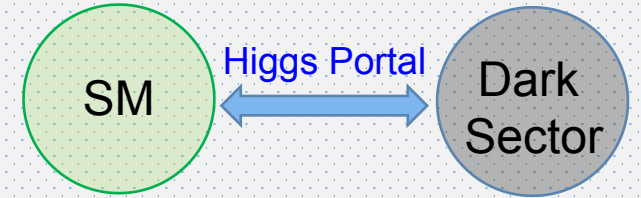
vanishes

$$\lambda_3 = \frac{v_{EW} \lambda_1 (m_{\hat{h}}^2 \tan \theta + m_{\hat{\phi}}^2 \cot \theta)}{2v_\Phi (m_{\hat{h}}^2 - m_{\hat{\phi}}^2)}$$



Dark Sector affecting EWPT

- Dark sector with a Higgs portal interaction with the SM sector

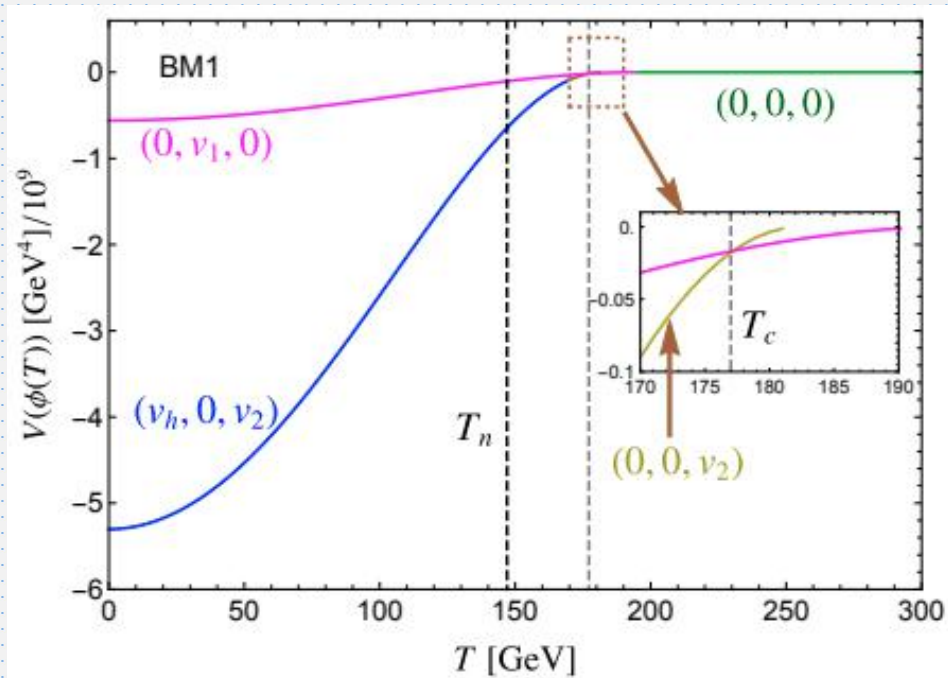


$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{portal}} + \mathcal{L}_{\text{DS}},$$

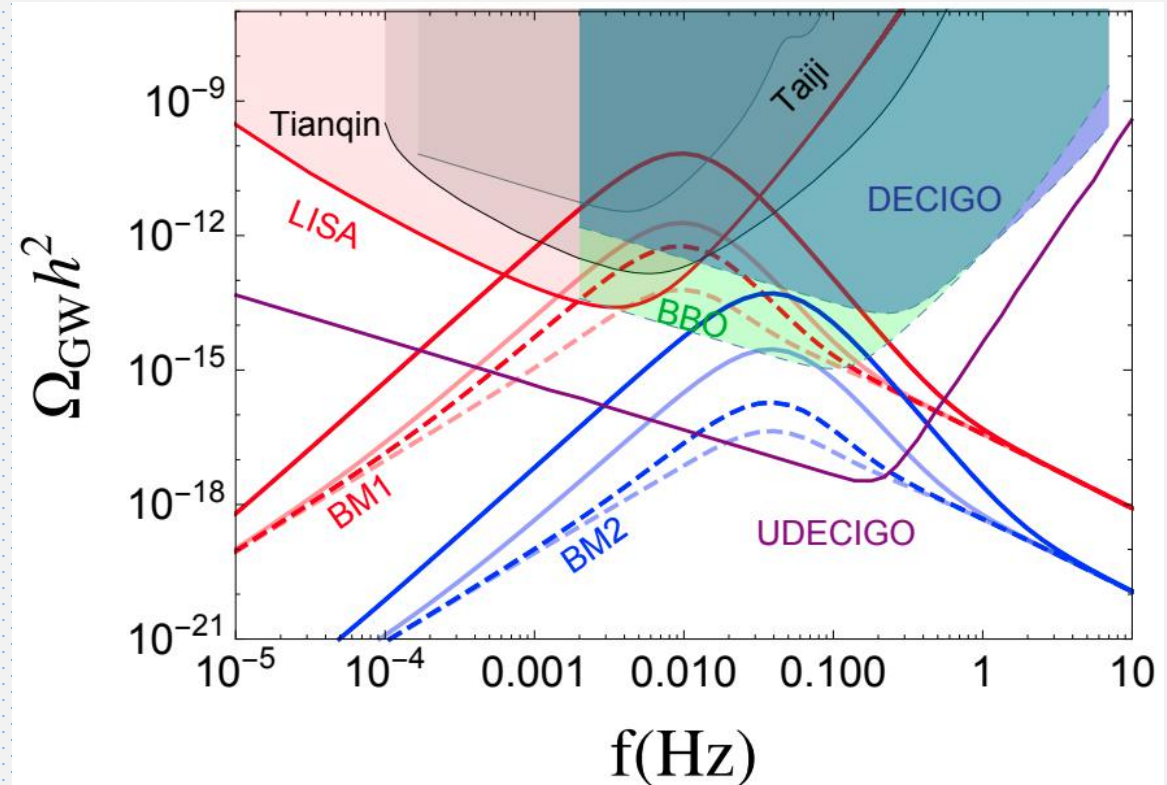
$$-\mathcal{L}_{\text{SM}} \supset V_{\text{SM}} = m_H^2 |H|^2 + \frac{\lambda_H}{2} |H|^4,$$

$$-\mathcal{L}_{\text{portal}} \supset V_{\text{portal}} = \lambda_{H11} |H|^2 |\Phi_1|^2 + \lambda_{H22} |H|^2 |\Phi_2|^2,$$

$$\mathcal{L}_{\text{DS}} = -\frac{1}{4} \tilde{W}_{\mu\nu}^a \tilde{W}^{a\mu\nu} + |D_\mu \Phi_1|^2 + |D_\mu \Phi_2|^2 - V_{\text{DS}}$$



Ghosh, [HG](#), Han, Liu, JHEP [2012.09758]



THE SPECTRUM OF GRAVITATIONAL WAVES

Observatories & experiments

Ground-based experiment



Space-based observatory



Pulsar timing array



Cosmic microwave background polarisation



Timescales

milliseconds

seconds

hours

years

billions of years

Frequency (Hz)

100

1

10^{-2}

10^{-4}

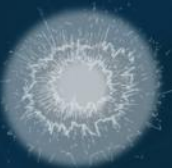
10^{-6}

10^{-8}

10^{-16}

Cosmic fluctuations in the early Universe

Cosmic sources



Supernova



Pulsar



Compact object falling onto a supermassive black hole



Merging supermassive black holes



Merging neutron stars in other galaxies



Merging stellar-mass black holes in other galaxies



Merging white dwarfs in our Galaxy

#lisa



LIGO Search Result

O1+O2+O3@LIGO (H1, L1), Virgo

- No Evidence for Broken Power Law Signal
- No Evidence for Bubble Collision Domination Signal
- No Evidence for Sound Waves Domination Signal

Broken Power Law

95% CL UL (CBC+BPL)

$$\Omega_{\text{ref}} = 6.1 \times 10^{-9}$$

$$\Omega_* = 5.6 \times 10^{-7}$$

$$\Omega_{\text{BPL}}(25 \text{ Hz}) = 4.4 \times 10^{-9}$$

Bubble Collision

95% CL UL with fixed T_{pt} and β/H_{pt}

Phenomenological model (bubble collisions)

$\Omega_{\text{coll}}^{95\%}(25 \text{ Hz})$

$\beta/H_{\text{pt}} \setminus T_{\text{pt}}$	10^7 GeV	10^8 GeV	10^9 GeV	10^{10} GeV
0.1	9.2×10^{-9}	8.8×10^{-9}	1.0×10^{-8}	7.2×10^{-9}
1	1.0×10^{-8}	8.4×10^{-9}	5.0×10^{-9}	...
10	4.0×10^{-9}	6.3×10^{-9}

no sensitivity

Sound Waves

95% CL UL

$$\Omega_{\text{sw}}(25 \text{ Hz}) = 5.9 \times 10^{-9}$$

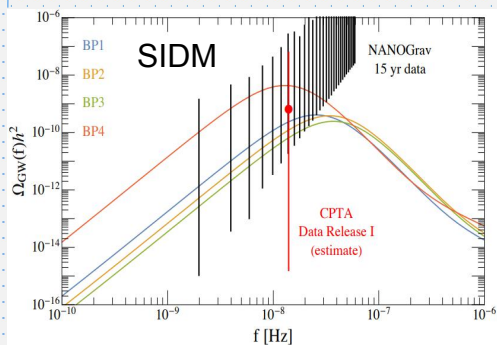
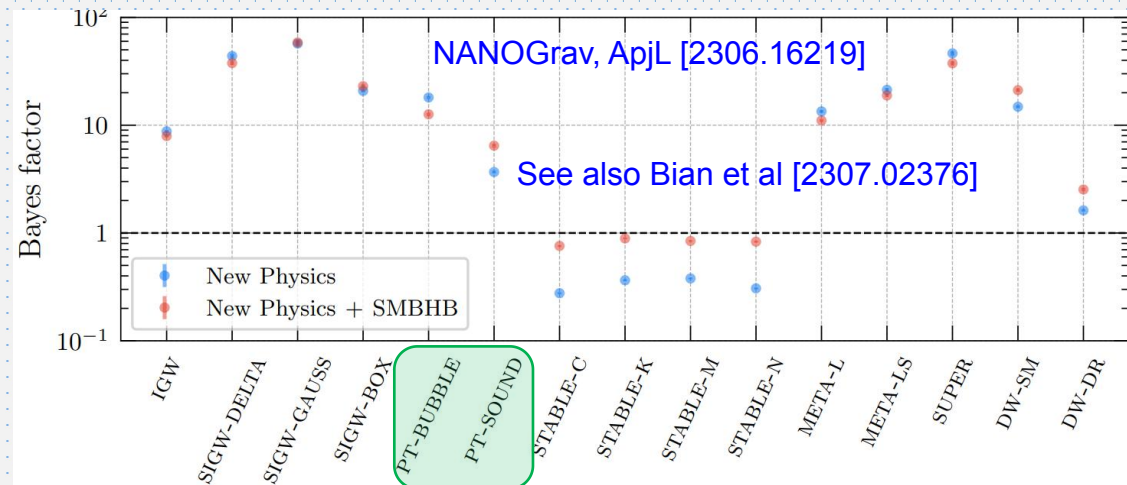
$$\beta/H_{\text{pt}} < 1 \text{ and } T_{\text{pt}} > 10^8 \text{ GeV}$$

First result from gravitational wave data!

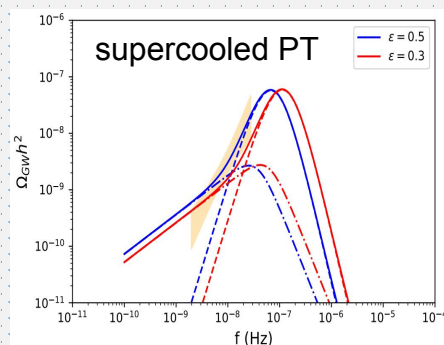
What possible PTA discovery implies?

- Once discovered, firstly needs to know its origin
- Can be the next “CMB” (spectral shape, anisotropy, etc)
- Can be from first order QCD-scale PT

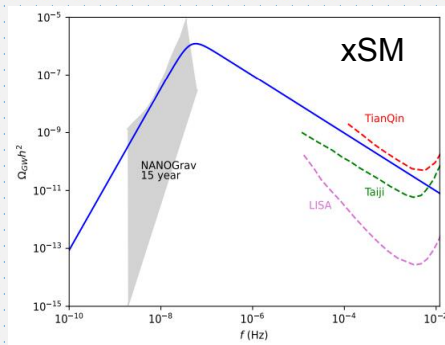
PPTA: Xue et al, PRL [2110.03096]
 NANOGrav (12.5-year): Arzoumanian et al, PRL [2104.13930]
 ...



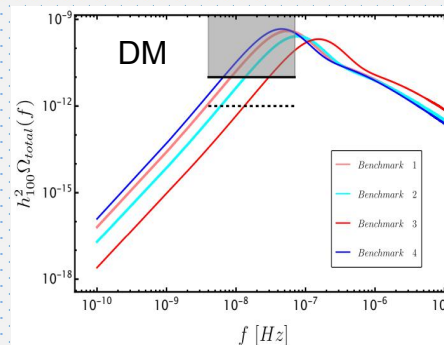
Han,Xie,Yang,Zhang [2306.16966]



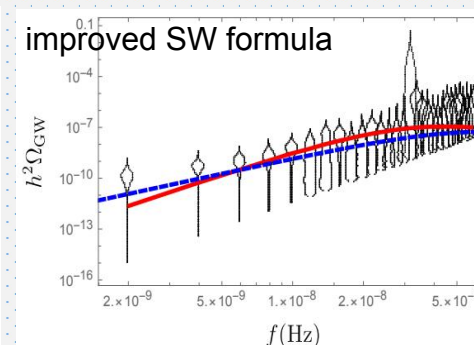
Zu,Zhang,Li,Gu,Tsai,Fan [2306.17239]



Xiao,Yang,Zhang [2307.01072]



Yang,Ma,Jiang,Huang [2306.17827]

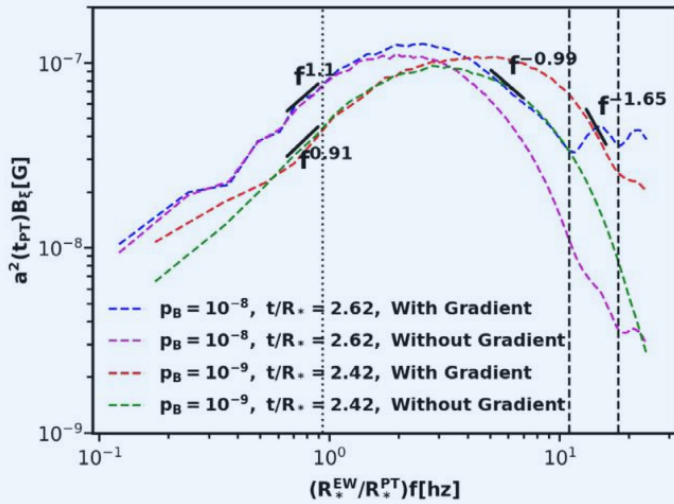


Ghosh et al [2307.02259]

and more...

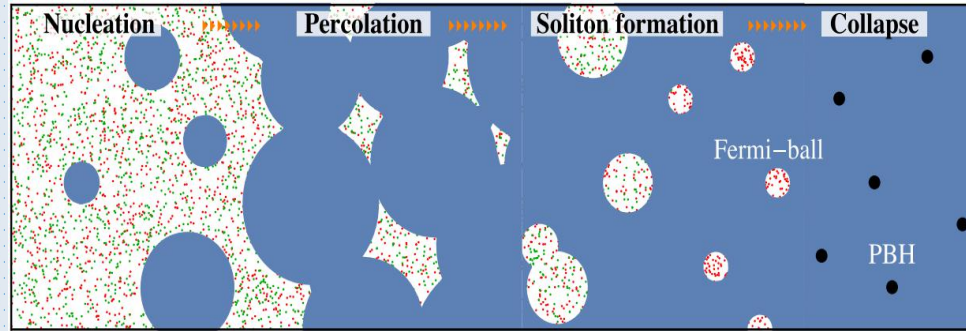
New Observables

Primordial magnetic field



Di, Wang, Zhou, Bian, Cai, PRL [2012.15625]
 Yang, Bian, PRD [2102.01398]

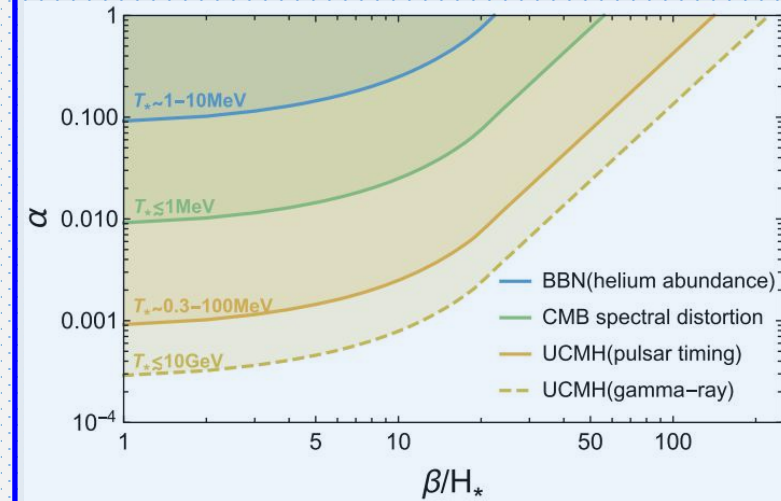
Primordial black holes



Kawana, Xie, PLB [2106.00111]

and more...

Curvature perturbations



Liu, Bian, Cai, Guo, Wang, PRL [2208.14086]

Summary

- Rapid experimental progresses (LIGO-Virgo-KAGRA, LISA/Taiji/Tianqin, PTA)
- A much clearer picture of a first order EWPT (simulations, analytical insights)
- More robust calculations (dimensional reduction, non-perturbative methods)
- More accurate predictions for GWs
- New observables (PBHs, curvature perturbations, magnetic fields, etc)
- Extensive phenomenological studies

Since LIGO's first direct detection of GWs (announced in 2016)

The 2023 Shanghai Symposium on Particle Physics and Cosmology: Phase Transitions, Gravitational Waves, and Colliders (SPCS 2023)



Organizing Committee

- Michael Ramsey-Musolf 任穆 (Shanghai Jiao Tong University, Tsung-Dao Lee Institute)
- Huaike Guo (University of Chinese Academy of Sciences, ICTP-AP)
- Fa Peng Huang (Sun Yat-Sen University)
- Shu Li (Shanghai Jiao Tong University, Tsung-Dao Lee Institute)
- Kun Liu (Shanghai Jiao Tong University, Tsung-Dao Lee Institute)
- Lei Zhang (Nanjing University)

Website: <https://indico-tdli.sjtu.edu.cn/event/1741/>