

Recent results of the exotic hadron studies at CMS



WiV2023
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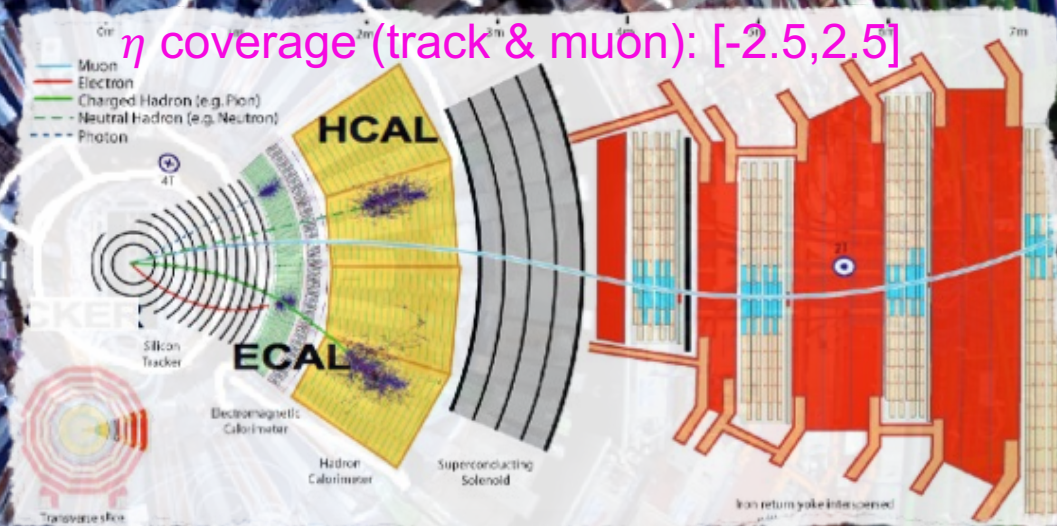
the Compact Muon Solenoid detector

3.8T Superconducting Solenoid

Hermetic ($|\eta| < 5.2$)
Hadron Calorimeter (HCAL)
[scintillators & brass]

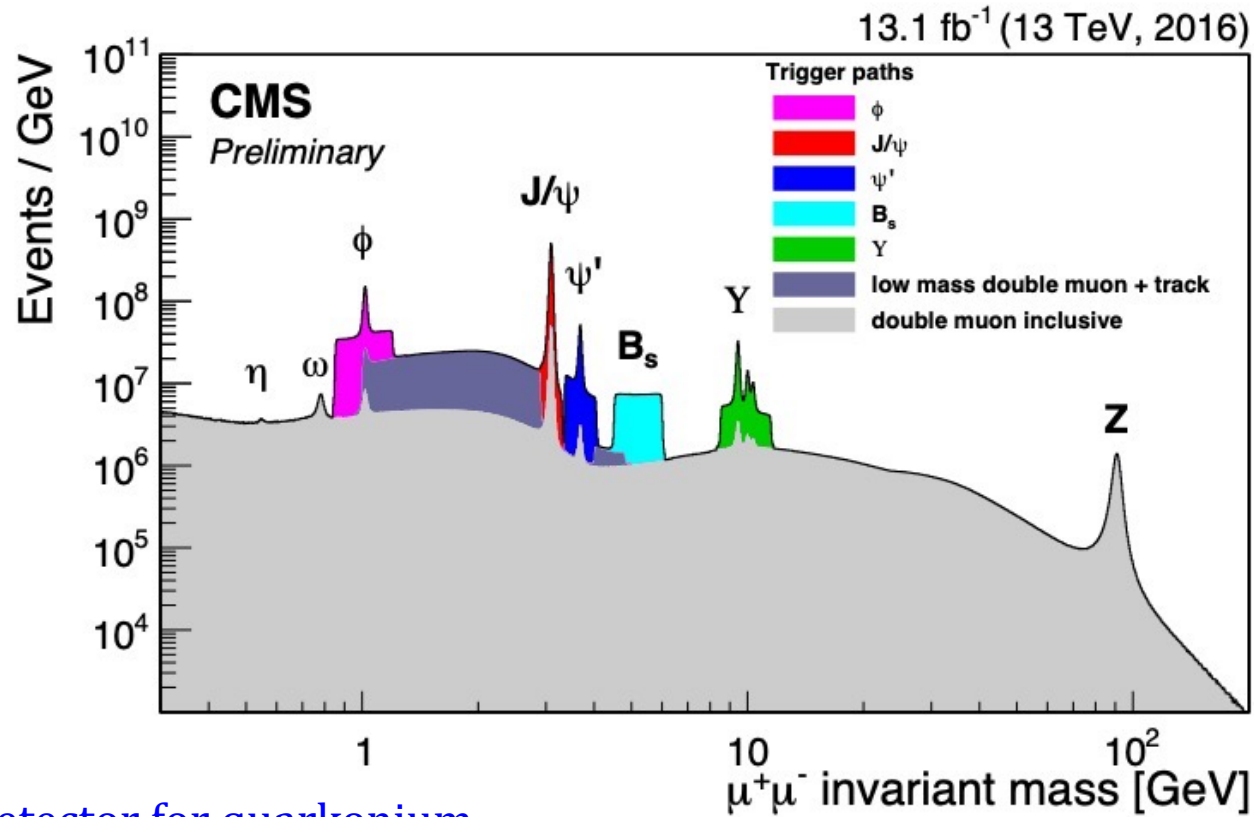
Lead tungstate
E/M Calorimeter (ECAL)

η coverage (track & muon): $[-2.5, 2.5]$



All Silicon Tracker
(Pixels and Microstrips)

Redundant Muon System
(RPCs, Drift Tubes,
Cathode Strip Chambers)

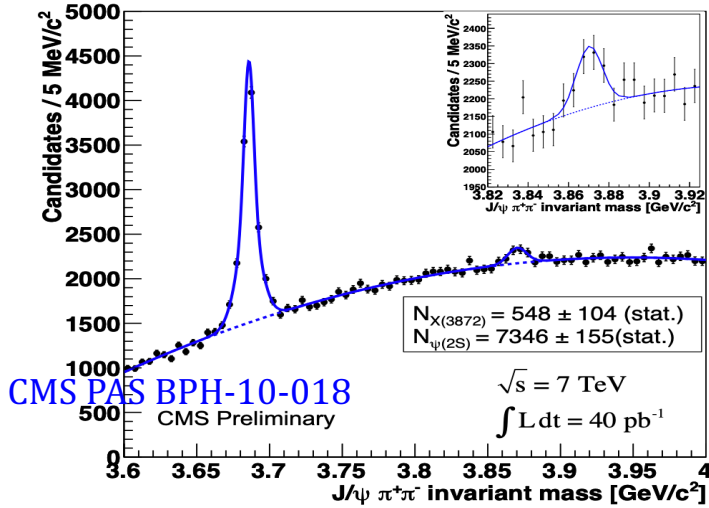


Excellent detector for quarkonium

- Muon system
 - High-purity muon ID, $\Delta m/m \sim 0.6\%$ for J/ψ
- Silicon Tracking detector, $B=3.8T$
 - $\Delta p_T/p_T \sim 1\%$ & excellent vertex resolution
- Special triggers for different analyses at increasing Inst. Lumi.
 - μp_T , $(\mu\mu) p_T$, $(\mu\mu)$ mass, $(\mu\mu)$ vertex, and additional μ

CMS played the following leading roles

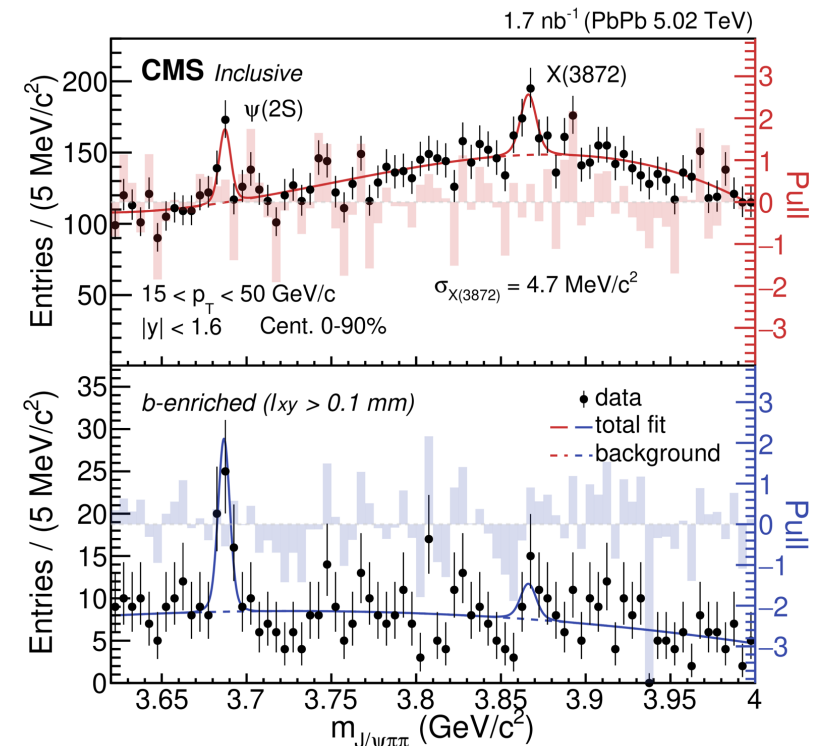
First LHC experiment re-discovered X(3872)



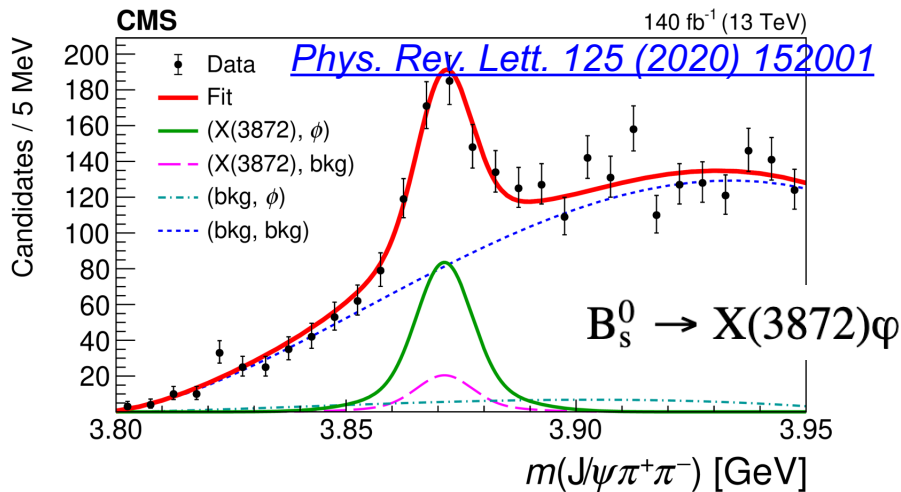
First experiment to see X(3872) signal in PbPb

$$X(3872) \rightarrow J/\psi \pi^+ \pi^- \rightarrow \mu^+ \mu^- \pi^+ \pi^-$$

4.2σ



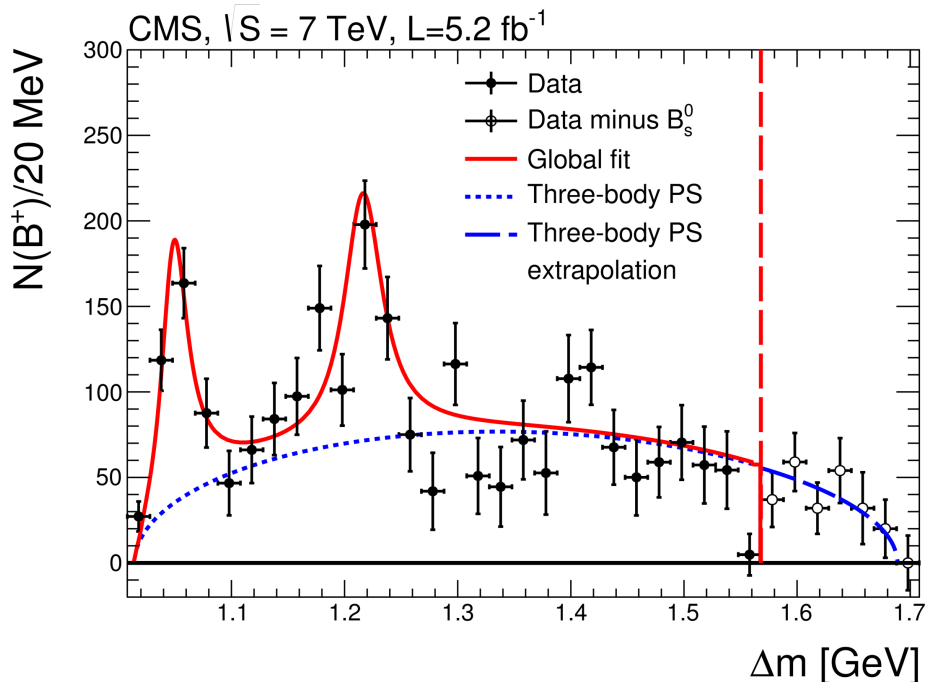
First experiment to observe X(3872) in B_s^0 decay



[Phys. Rev. Lett. 128 \(2022\) 032001](#)

CMS played the following leading roles

- First LHC experiment to see new exotic hadrons (Y(4140))



The fitted mass and width

$$M = 4148.0 \pm 2.4 \text{ (stat.)} \pm 6.3 \text{ (syst.) MeV}$$

$$\Gamma = 28^{+15}_{-11} \text{ (stat.)} \pm 19 \text{ (syst.) MeV}$$

First confirmation of Y(4140)

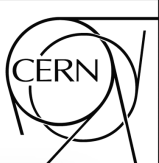
Evidence for an additional peaking structure at higher mass also reported

[Phys. Lett. B 734 \(2014\) 261-281](https://arxiv.org/abs/1405.3802)

<https://www.nikhef.nl/~pkoppenb/particles.html>

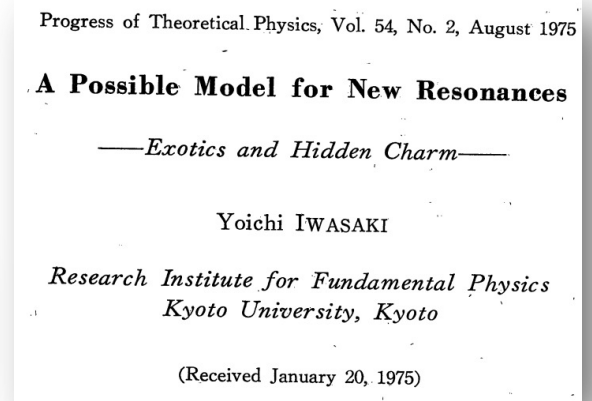


New domain of exotics: all-heavy tetra-quarks



- First mention of 4c states at 6.2 GeV (1975)
 - Just one year after the discovery of J/ψ

We expect at least three exotic mesons with hidden charm, $c\bar{c}(p\bar{p}-n\bar{n})$ [between 3.7~4.1 GeV], $c\bar{c}\lambda\bar{\lambda}$ [~ 4.1 GeV] and $c\bar{c}c\bar{c}$ [~ 6.2 GeV] to which we refer as ψ_c , ψ_c' and ψ_c'' respectively. [Weinberg, Phys. Rev. Lett. 37:662 (1976)]



- First calculation of 4c states (1981): Z. Phys. C 7 (1981) 317

| L | S | J^{PC} | Mass (GeV) |
|-----|-----|--|------------|
| 1 | 0 | 1^{--} | 6.55 |
| | 1 | $0^{-+}, 1^{-+}, 2^{-+}$ | |
| | 2 | $1^{--}, 2^{--}, 3^{--}$ | |
| 2 | 0 | 2^{++} | 6.78 |
| | 1 | $1^{+-}, 2^{+-}, 3^{+-}$ | |
| | 2 | $0^{++}, 1^{++}, 2^{++}, 3^{++}, 4^{++}$ | |
| 3 | 0 | 3^{--} | 6.98 |
| | 1 | $2^{-+}, 3^{-+}, 4^{-+}$ | |
| | 2 | $1^{--}, 2^{--}, 3^{--}, 4^{--}, 5^{--}$ | |

$$\left| (cc)_3^* - (\bar{c}\bar{c})_3 \right|$$

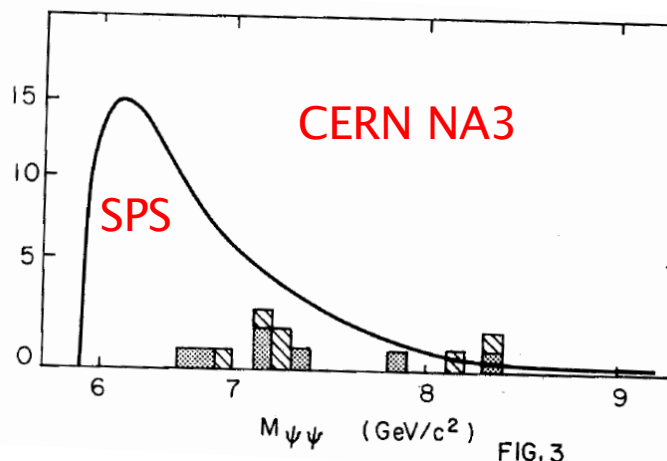
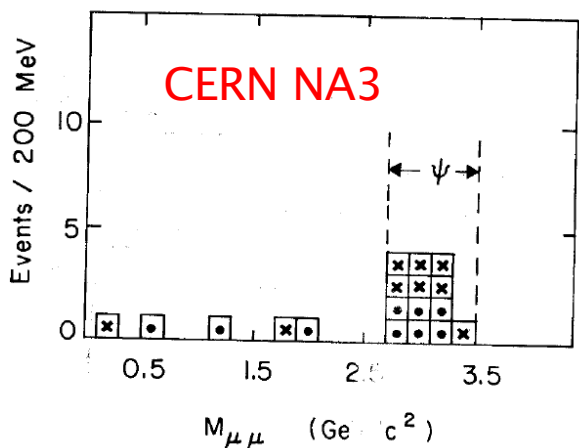
$$(cc)_6 - (\bar{c}\bar{c})_6^*$$

| L | S | J^{PC} | Mass (GeV) |
|-----|-----|----------|------------|
| 1 | 0 | 1^{--} | 6.82 |
| 2 | 0 | 2^{++} | 7.15 |
| 3 | 0 | 3^{--} | 7.41 |

- A different exotic system compared to exotics with light quarks

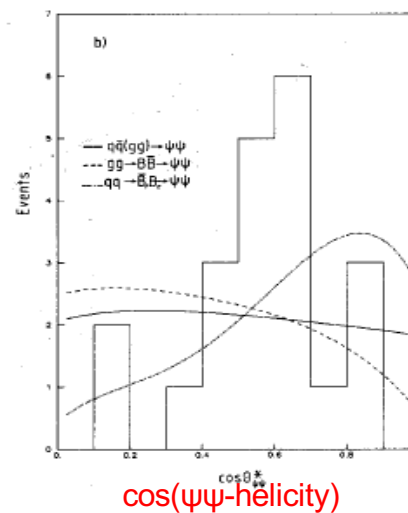
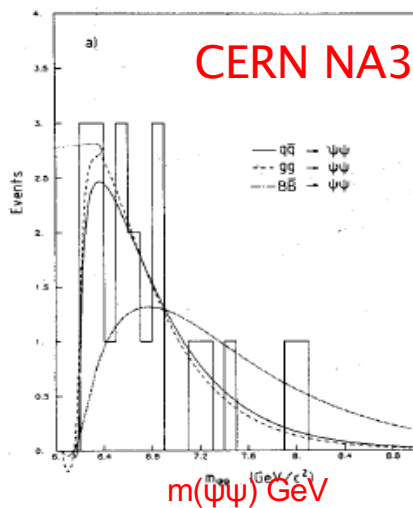
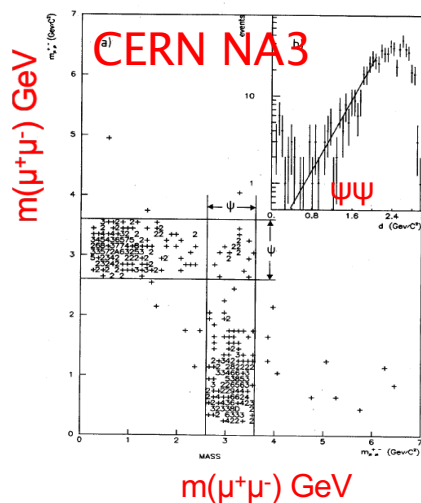


J/ψ events—first evidence (1982)



PLB114 (1982) 457

Was interpreted as 2^{++} 4-quark state



PLB158 (1985) 85

2^{++} four-quark states, PRD29 (1984) 426

TABLE I. Parameters used in Eq. (8) to calculate the cross sections for vector-meson pair production. (+) and (-) denote two degenerate $2^{++} Q^2 \bar{Q}^2$ states. Except in the case of JJ , we take $4\pi/f_L^2=0.03$, due to the fact that the $2^{++} Q^2 \bar{Q}^2$ are expected to lie not far above the threshold. α_s is determined from Eq. (11).

| $V_1 V_2$ | $a \psi_{V_1} \psi_{V_2} / a$ | $b_{\alpha\beta}^l / \alpha_s \frac{a}{\sqrt{8}} \delta_{\alpha\beta}$ | M_J (GeV) | α_s | m_1 |
|--------------------------|-------------------------------|--|----------------|------------|-------|
| JJ | $1/\sqrt{3}$ | $\left[\frac{2}{3}\right]^{1/2} \frac{4\pi}{f_L^2}$ | 7.0 | 0.18 | 3.10 |
| $J\omega^{(+)}$ | $1/\sqrt{6}$ | $\frac{-1}{\sqrt{3}} \frac{4\pi}{f_L f_\omega}$ | 4.05 | 0.2 | |
| $J\omega^{(-)}$ | $1/\sqrt{12}$ | $\left[\frac{2}{3}\right]^{1/2} \frac{4\pi}{f_L f_\omega}$ | 4.05 | 0.2 | |
| $\Upsilon J^{(+)}$ | $1/\sqrt{6}$ | $\frac{-1}{\sqrt{3}} \frac{4\pi}{f_\Upsilon f_L}$ | 13.5 | 0.167 | |
| $\Upsilon J^{(-)}$ | $1/\sqrt{12}$ | $\left[\frac{2}{3}\right]^{1/2} \frac{4\pi}{f_\Upsilon f_L}$ | 13.5 | 0.167 | |
| $B_c^* \bar{B}_c^{*(+)}$ | $-1/\sqrt{6}$ | $\frac{-1}{\sqrt{3}} \frac{4\pi}{f_\Upsilon f_L}$ | 13.5 | 0.167 | 6.60 |
| $B_c^* \bar{B}_c^{*(-)}$ | $1/\sqrt{12}$ | $\left[\frac{2}{3}\right]^{1/2} \frac{4\pi}{f_\Upsilon f_L}$ | 13.5 | 0.167 | |

There were other attempts

(cccc) *Phys. Rev. D 86, 034004 (2012)*

| | | | |
|-----------|--------------------------|--|--|
| $0^{++'}$ | $M = 5.966 \text{ GeV},$ | $M - M_{\text{th}} = -228. \text{ MeV},$ | } <i>Below double J/ψ threshold</i> <i>Search via $J/\psi\mu^+\mu^-, J/\psi^*$</i> |
| $1^{+-'}$ | $M = 6.051 \text{ GeV},$ | $M - M_{\text{th}} = -142. \text{ MeV},$ | |
| 2^{++} | $M = 6.223 \text{ GeV},$ | $M - M_{\text{th}} = 29.5 \text{ MeV}.$ | |

Above double J/ψ threshold
Search via $J/\psi J/\psi$

(bbcc)

| | | | |
|-----------|---------------------------|--|--|
| 0^{++a} | $M = 12.359 \text{ GeV},$ | $M - M_{\text{th}} = -191. \text{ MeV}$ | } <i>Below double B_c threshold</i> <i>$J/\psi Y(1S)$ threshold</i> <i>? ...</i> |
| 0^{++b} | $M = 12.471 \text{ GeV},$ | $M - M_{\text{th}} = -78.7 \text{ MeV},$ | |
| 1^{+-a} | $M = 12.424 \text{ GeV},$ | $M - M_{\text{th}} = -126. \text{ MeV}$ | |
| 1^{+-b} | $M = 12.488 \text{ GeV},$ | $M - M_{\text{th}} = -62.5 \text{ MeV},$ | |
| 1^{++} | $M = 12.485 \text{ GeV},$ | $M - M_{\text{th}} = -64.9 \text{ MeV},$ | |
| 2^{++} | $M = 12.566 \text{ GeV},$ | $M - M_{\text{th}} = 16.1 \text{ MeV}.$ | |

Above double B_c threshold
 $J/\psi Y(1S)$ threshold
Search via the above two channels

(bbbb)

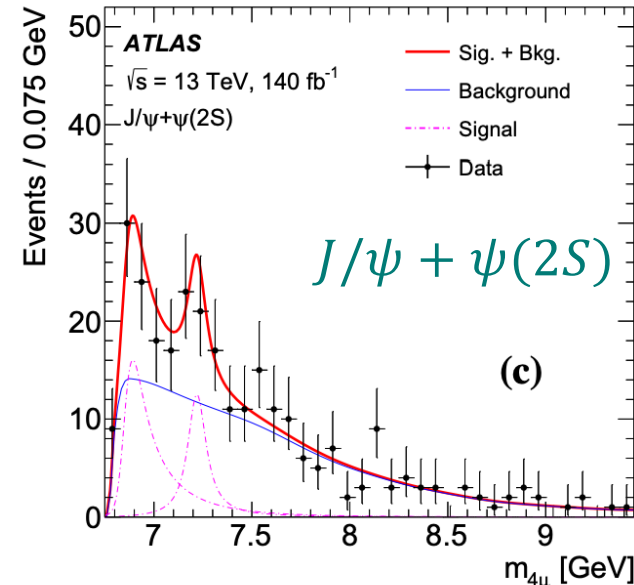
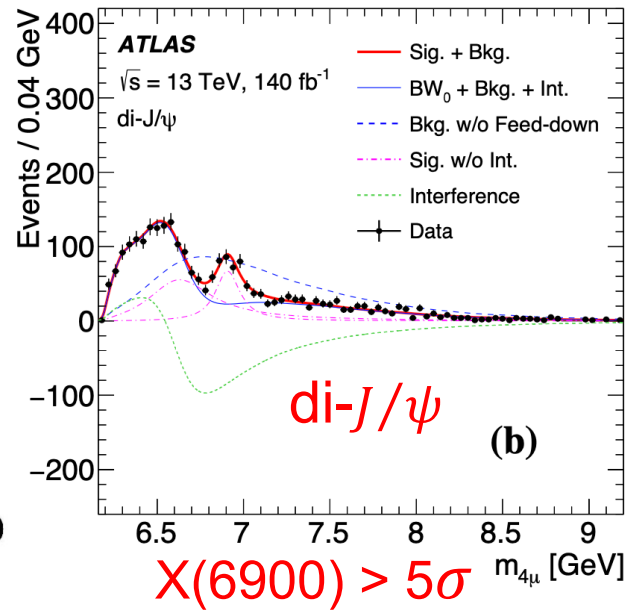
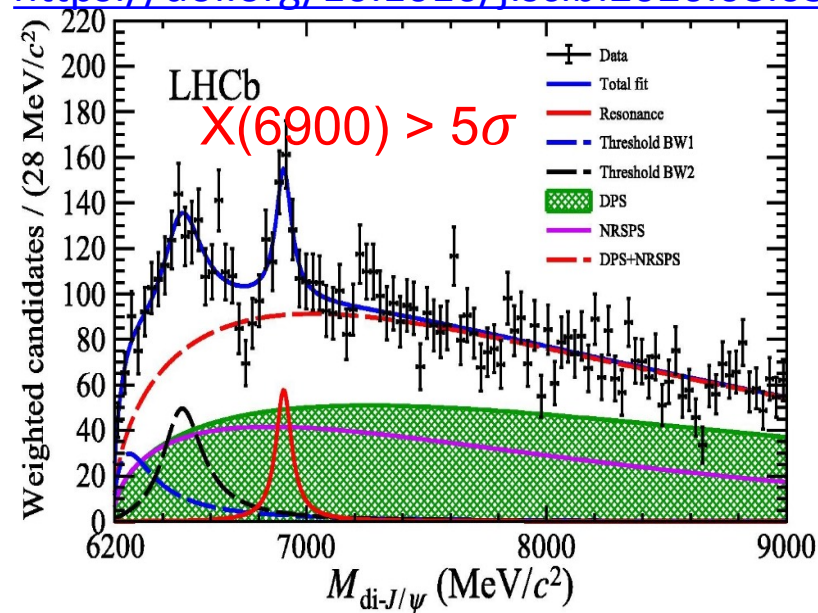
| | | | |
|-----------|---------------------------|--|--|
| $0^{++'}$ | $M = 18.754 \text{ GeV},$ | $M - M_{\text{th}} = -544. \text{ MeV},$ | } <i>Below double $Y(1S)$ threshold</i> <i>Search via $Y(1S)\mu^+\mu^-$</i> |
| $1^{+-'}$ | $M = 18.808 \text{ GeV},$ | $M - M_{\text{th}} = -490. \text{ MeV},$ | |
| 2^{++} | $M = 18.916 \text{ GeV},$ | $M - M_{\text{th}} = -382. \text{ MeV}.$ | |

- Many recent theoretical studies on $(c\bar{c}c\bar{c}), (b\bar{b}b\bar{b}), (b\bar{b}c\bar{c})$:
 - controversial on existence of bound states below $\eta_b\eta_b$ (or $\eta_c\eta_c$) threshold;
 - consistent on existence of resonant states above $\eta_b\eta_b$ (or $\eta_c\eta_c$) threshold.

- LHCb observed X(6900) in J/ψJ/ψ

<https://doi.org/10.1016/j.scib.2020.08.032>

<https://arxiv.org/abs/2304.08962>

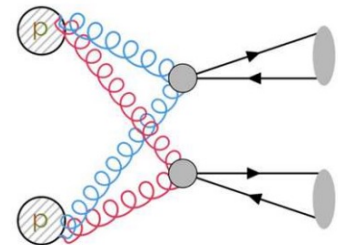
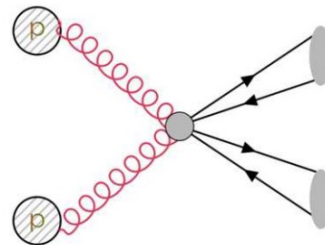


Two bumps together: 4.7σ

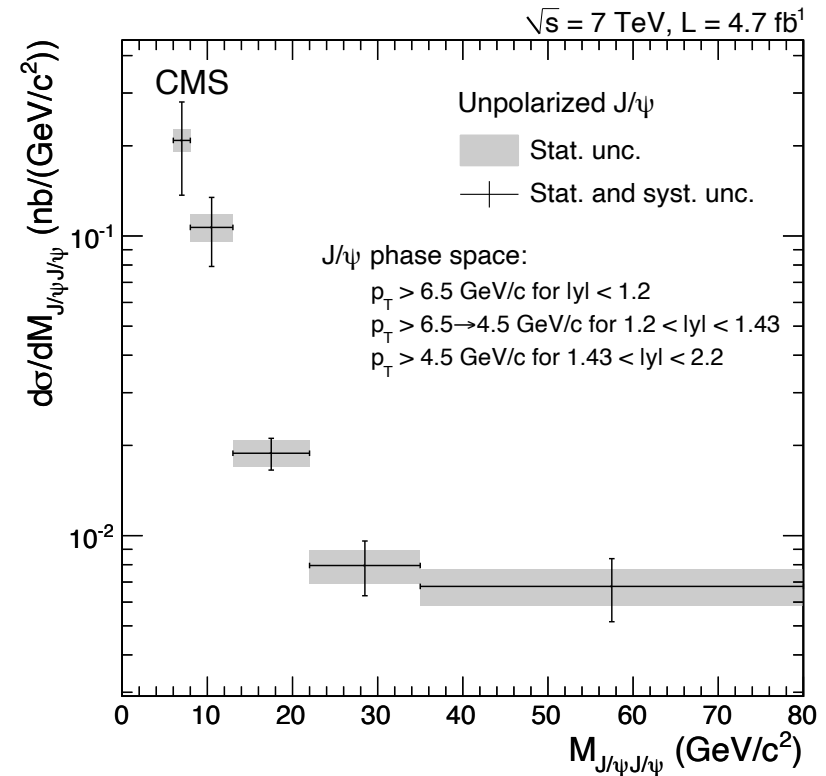
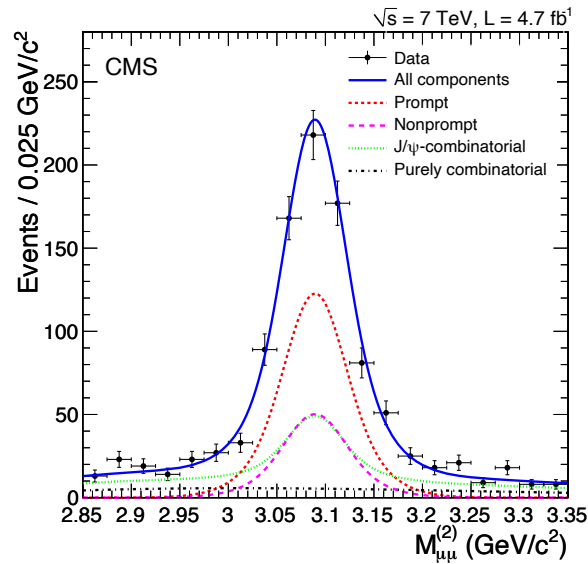
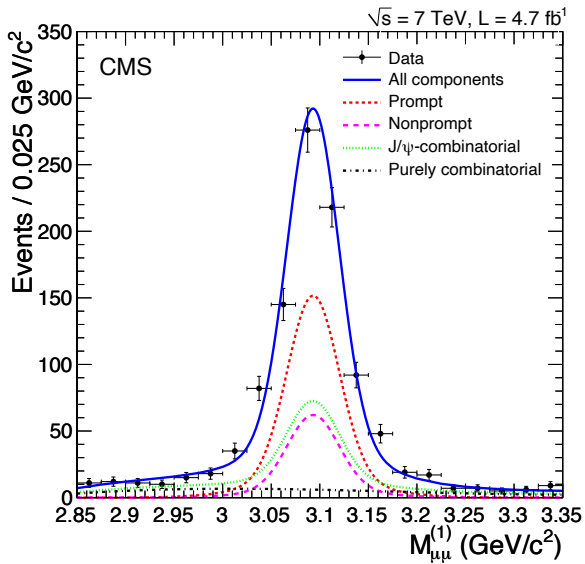
2nd bump alone: 3σ

- ATLAS fully-charmed exotic states
 - Confirmation of X(6900) in J/ψJ/ψ
 - Evidence of structures in J/ψψ(2S)

- Signal: $X \rightarrow J/\psi J/\psi \rightarrow \mu^+ \mu^- \mu^+ \mu^-$
- Signal MC samples:
 - $J^P = 0^+$ resonance
Generator: Pythia8, JHUGen
- Main background:
 - Nonresonant single-parton scattering (NRSPS)
Generator: Pythia8, HelacOnia (next-to-next-to-leading order), Cascade (next-to-leading order)
 - Nonresonant double-parton scattering (NRDPS)
Generator: Pythia8
 - Combinatorial background



[J. High Energy Phys. 09 \(2014\) 094](#)



Total cross section, assuming unpolarized prompt $J/\psi J/\psi$ pair production
 1.49 ± 0.07 (stat.) ± 0.13 (syst.) nb

Different assumptions about the $J/\psi J/\psi$ polarization imply modifications to the cross section ranging from -31% to +27%.

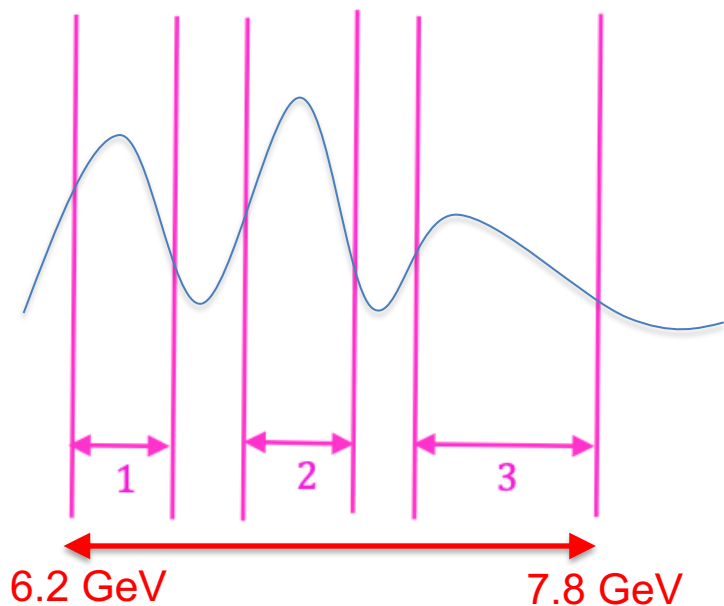


CMS blind mass window for 13 TeV



We saw hints at Run I data (7 TeV & 8 TeV)
Proposed **three** signal regions for Run II data

Signal: $X \rightarrow J/\psi J/\psi \rightarrow \mu^+ \mu^- \mu^+ \mu^-$



Blinded mass windows for Run II:

1. [6.3,6.6] GeV
2. [6.8,7.1] GeV
3. [7.2,7.8] GeV
(for potential wide structure)

These mass windows will be windows for LEE for potential structures

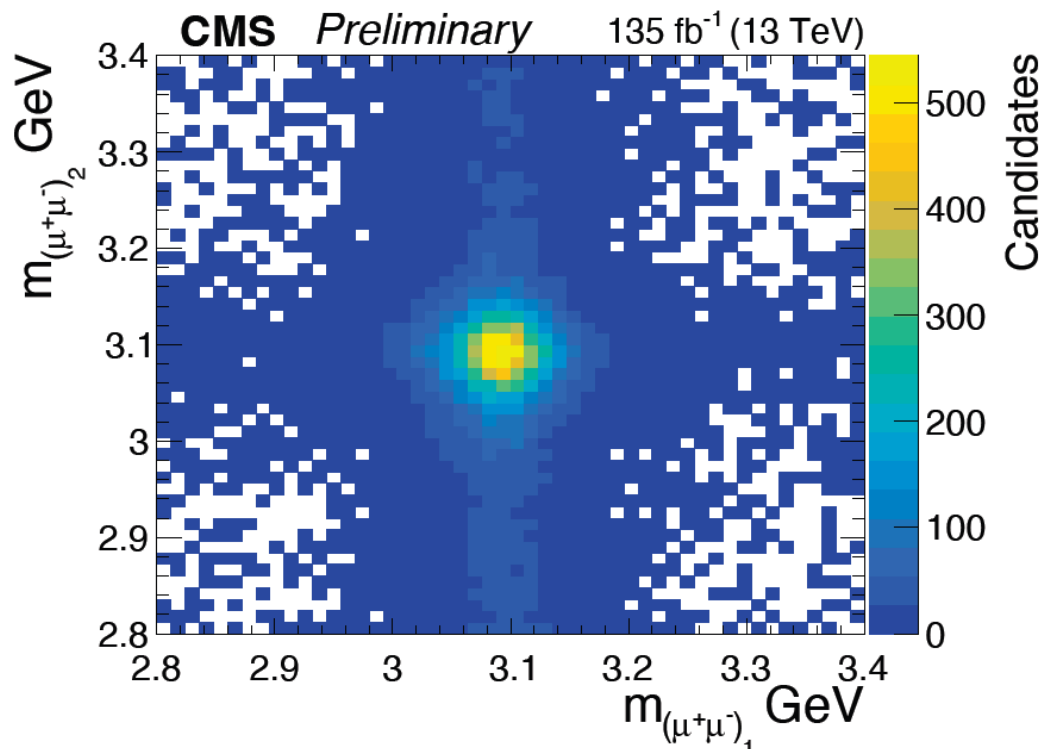
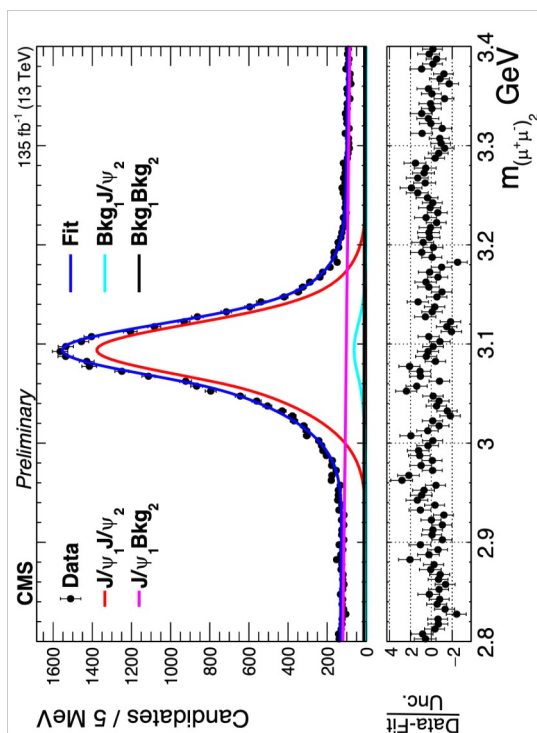
Run I data will be ignored for significance calculation

CMS eventually decide to blind the whole region: [6.2, 7.8] GeV after LHCb released their result (13 TeV, 2020)

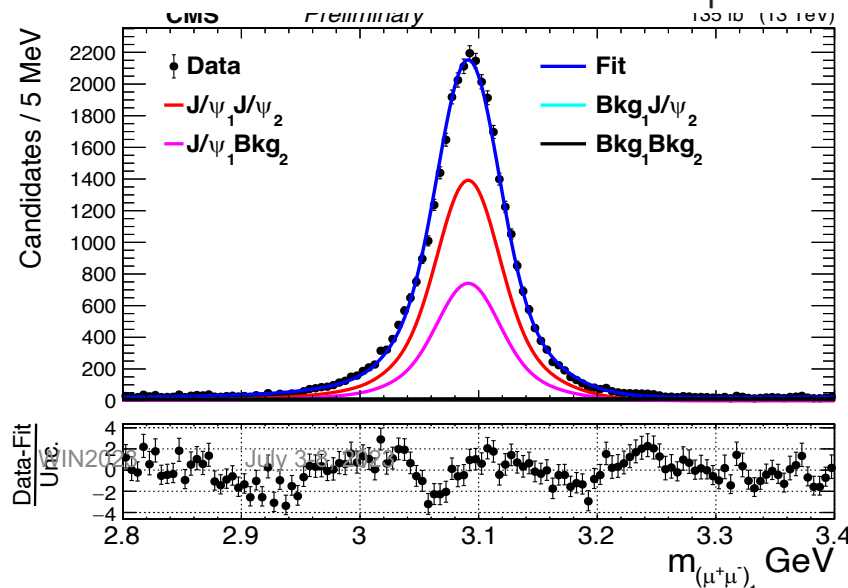




CMS $J/\psi J/\psi$ candidates at 13 TeV



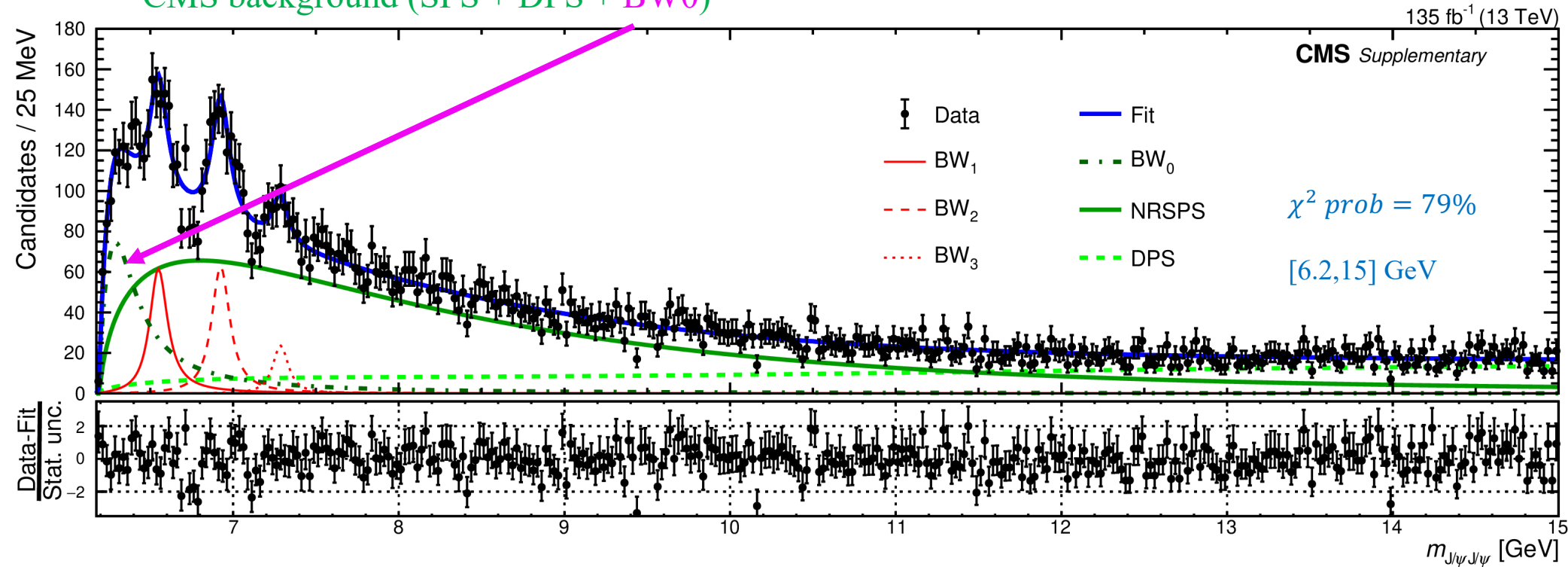
- CMS data: 135 fb^{-1} , taken in 2016, 2017 and 2018 LHC runs
- J/ψ mass and vertex related cuts removed
- Clean J/ψ signals are seen



<https://cms-results.web.cern.ch/cms-results/public-results/superseded/BPH-21-003/index.html>

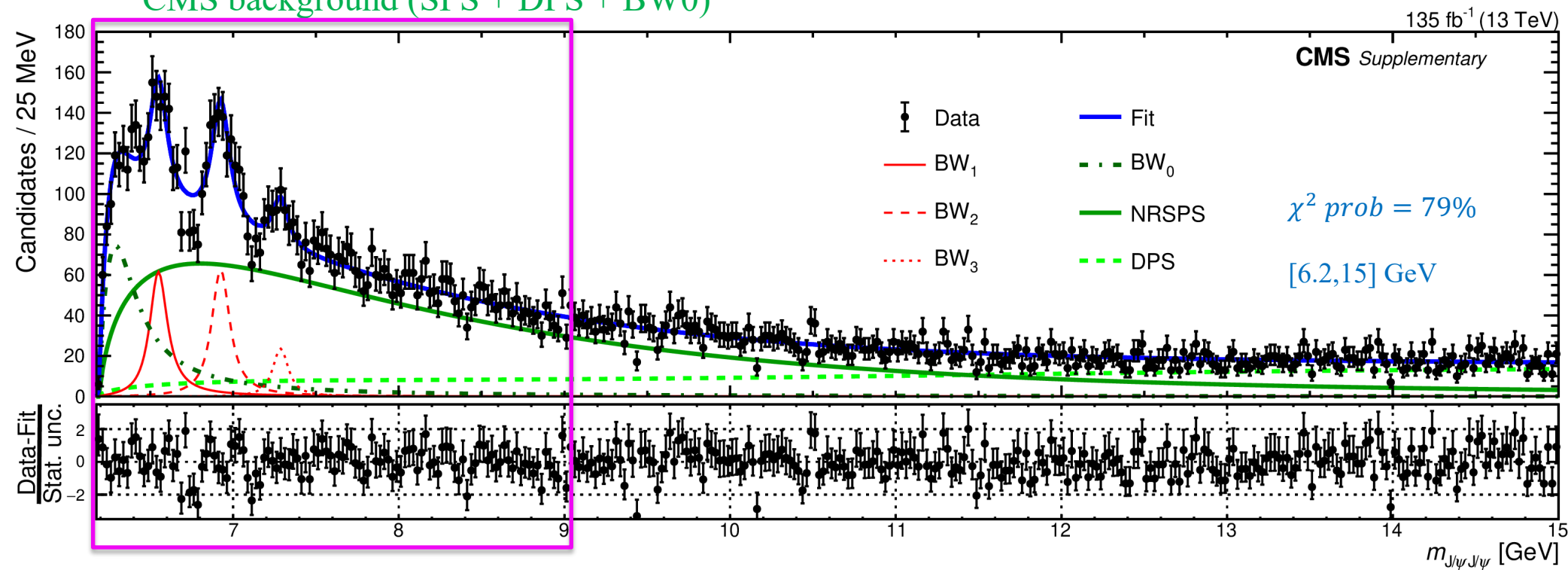


CMS background (SPS + DPS + BW0)



- Most significant structure is a BW at threshold, **BW0**--what is its meaning?
- **Treat BW0 as part of background** due to:
 - **BW0 parameters very sensitive to SPS and DPS model assumptions**
 - A region populated by feed-down from possible higher mass states
 - Possible coupled-channel interactions, pomeron exchange processes...

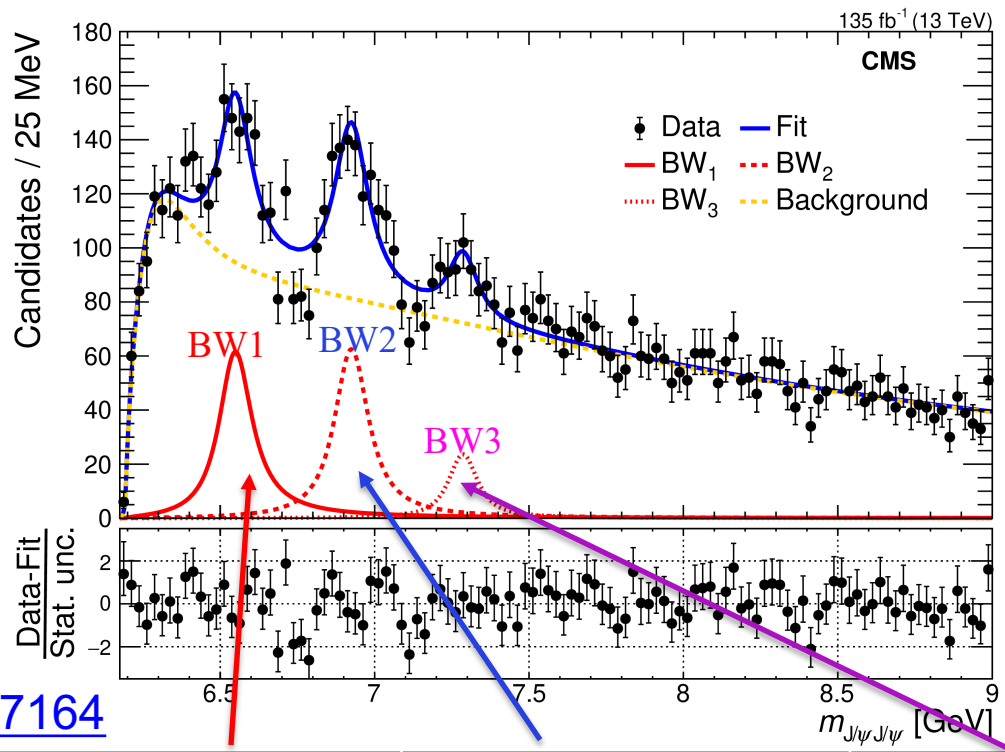
CMS background (SPS + DPS + BW0)



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- **Treat BW0 as part of background** due to:
 - **BW0 parameters very sensitive to SPS and DPS model assumptions**
 - A region populated by feed-down from possible higher mass states
 - Possible coupled-channel interactions, pomeron exchange processes...
- **SPS+DPS+BW0 as our background**



CMS model: 3 BWs + Background



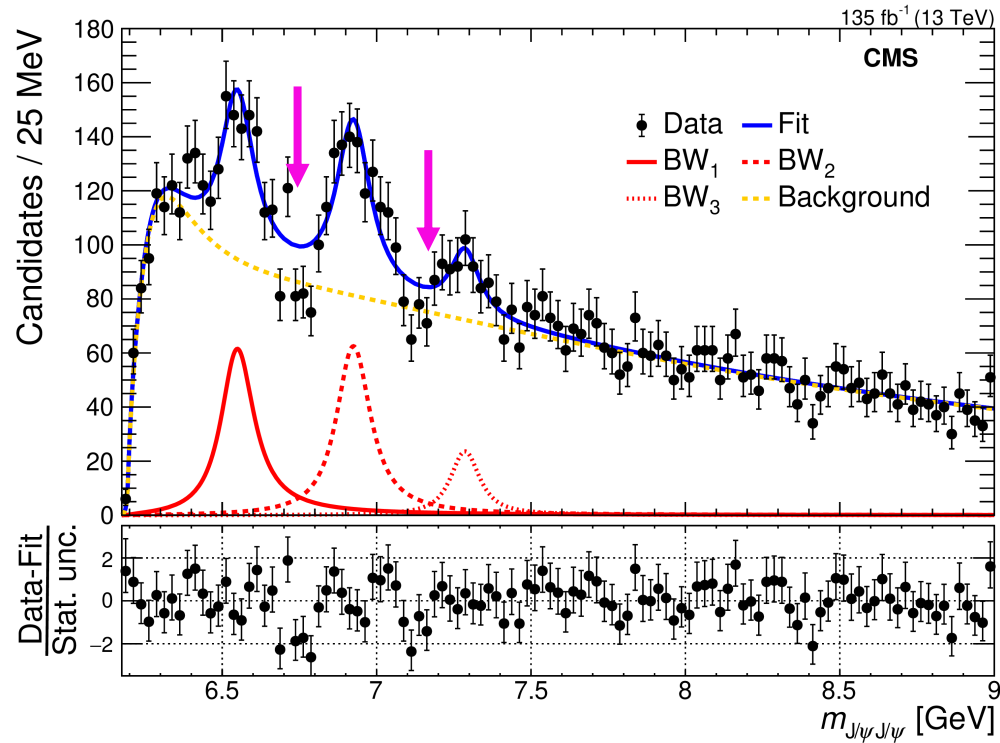
Statistical significance based on:
 $2 \ln(L_0/L_{\max})$

χ^2 Prob. = 1%
 [6.2,7.8] GeV

<https://arxiv.org/abs/2306.07164>

| | BW1 (MeV) | BW2 (MeV) | BW3 (MeV) |
|---------------------------------------|--------------------------|-----------------------------------|--------------------------|
| m | $6552 \pm 10 \pm 12$ | $6927 \pm 9 \pm 4$ | $7287^{+20}_{-18} \pm 5$ |
| Γ | $124^{+32}_{-26} \pm 33$ | $122^{+24}_{-21} \pm 18$ | $95^{+59}_{-40} \pm 19$ |
| N | 470^{+120}_{-110} | 492^{+78}_{-73} | 156^{+64}_{-51} |
| $\sigma(\text{stat.})$ | 6.5 | 9.4 | 4.1 |
| $\sigma(\text{stat.} + \text{syst.})$ | 5.7 | 9.4 | 4.1 |
| | Observation | Confirmation of X(6900) from LHCb | Evidence |





➤ Possibility #1:

- Interference among structures?

➤ Possibility #2:

- Multiple fine structures to reproduce the dips?
- Mentioned in PAS

- More secrets to dig out

- We explored possibility #1 in detail

- Explored fit with interference among various combinations of BWs
- Pdf for three BW interference

$$Pdf(m) = N_{X_0} \cdot |BW_0|^2 \otimes R(M_0)$$

$$+ N_{X \text{ and interf}} \cdot |r_1 \cdot \exp(i\phi_1) \cdot BW_1 + BW_2 + r_3 \cdot \exp(i\phi_3) \cdot BW_3|^2$$

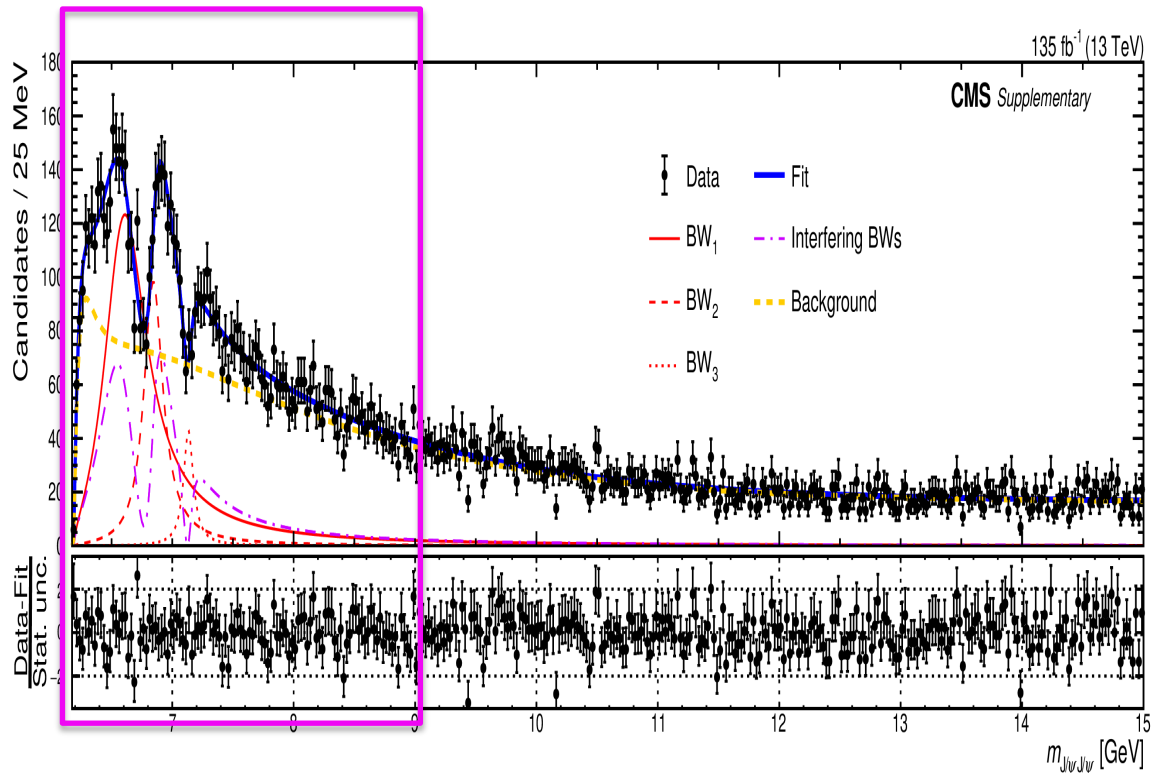
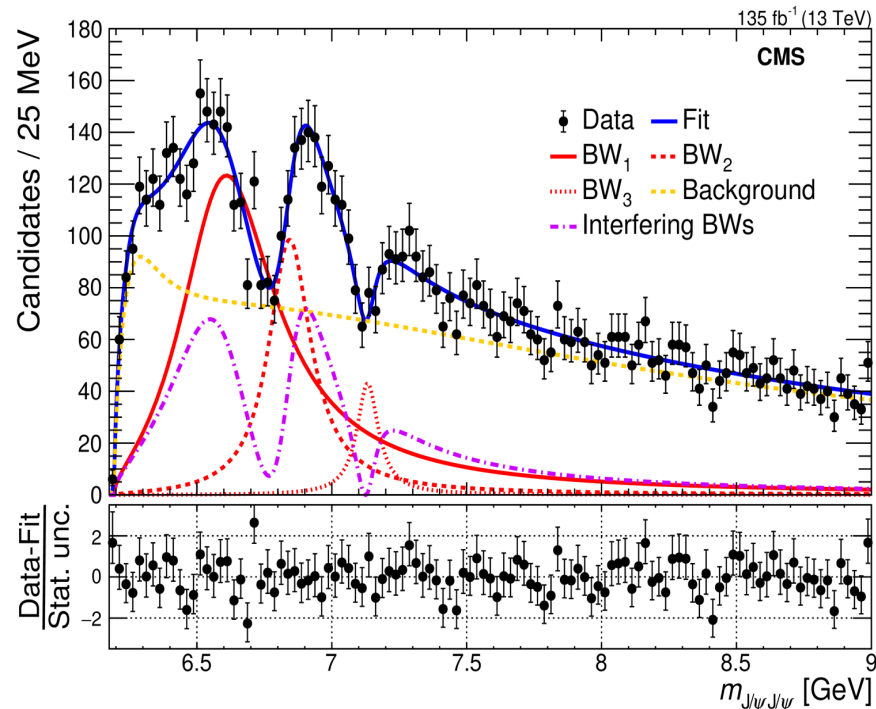
$$+ N_{NRSPS} \cdot f_{SPS}(m) + N_{NRDPS} \cdot f_{DPS}(m)$$

Interf. term

- Studied many ways interference due to possible J^{PC} and quantum coherence
 - 2-object-interference among BW0, BW1, BW2, BW3
 - 3-object-interference among BW0, BW1, BW2, BW3
 - 4-object-interference among BW0, BW1, BW2, BW3

Final CMS choice: interference among BW1, BW2, BW3

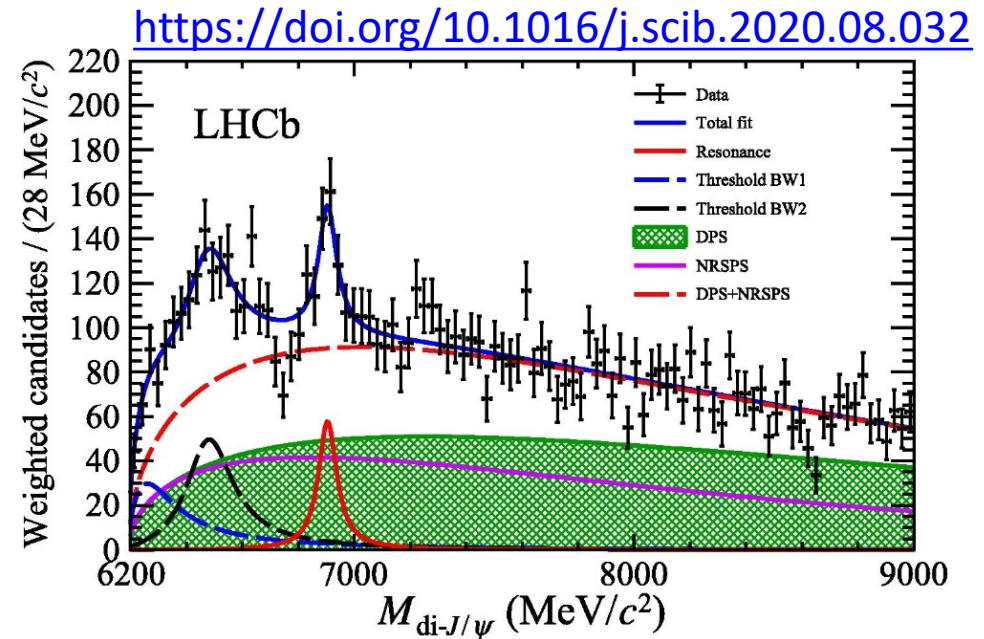
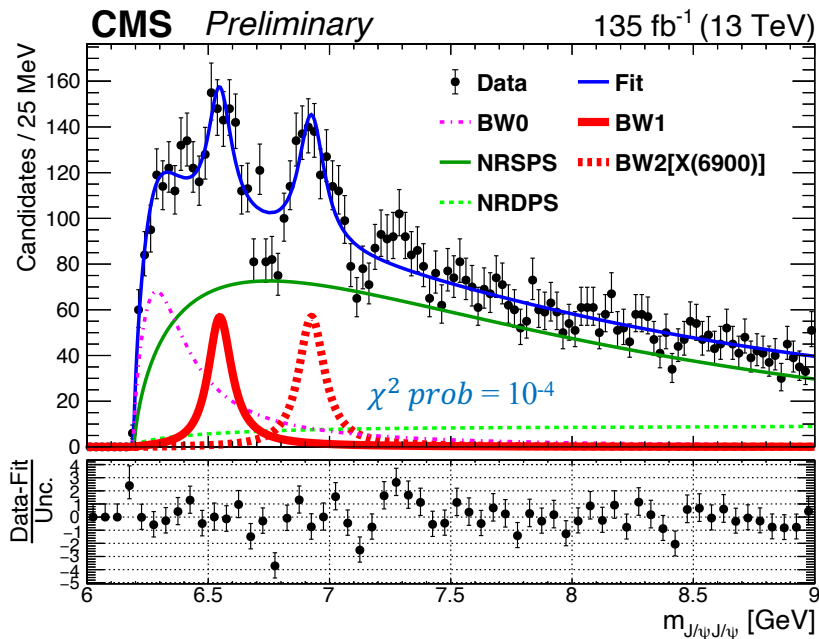
<https://arxiv.org/abs/2306.07164>



- Fit with interf. among BW1, BW2, and BW3 describes data well
- Measured mass and width in the interference fit

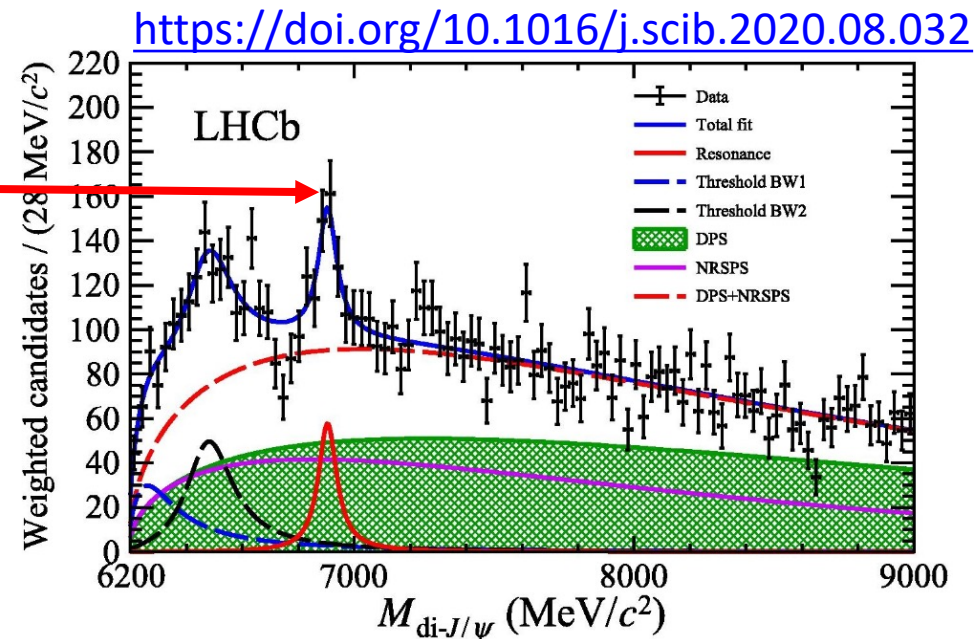
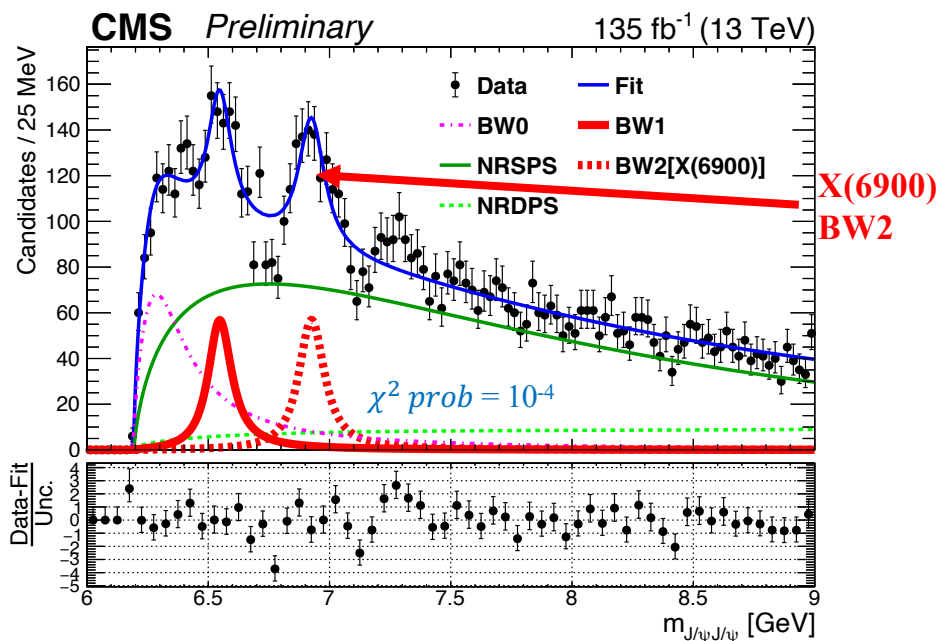
| | | BW ₁ | BW ₂ | BW ₃ |
|--------------|----------------|-----------------------------|--------------------------|--------------------------|
| Interference | m [MeV] | 6638^{+43+16}_{-38-31} | 6847^{+44+48}_{-28-20} | 7134^{+48+41}_{-25-15} |
| | Γ [MeV] | $440^{+230+110}_{-200-240}$ | 191^{+66+25}_{-49-17} | 97^{+40+29}_{-29-26} |

Fit CMS data with LHCb model I : 2 auxiliary BWs + X(6900) + bkg



| Exp. | Fit | $m(\text{BW1})$ | $\Gamma(\text{BW1})$ | $m(6900)$ | $\Gamma(6900)$ |
|-----------|---------|-----------------|----------------------|---------------------|--------------------|
| LHCb [15] | Model I | unrep. | unrep. | $6905 \pm 11 \pm 7$ | $80 \pm 19 \pm 33$ |
| CMS | Model I | 6550 ± 10 | 112 ± 27 | 6927 ± 10 | 117 ± 24 |

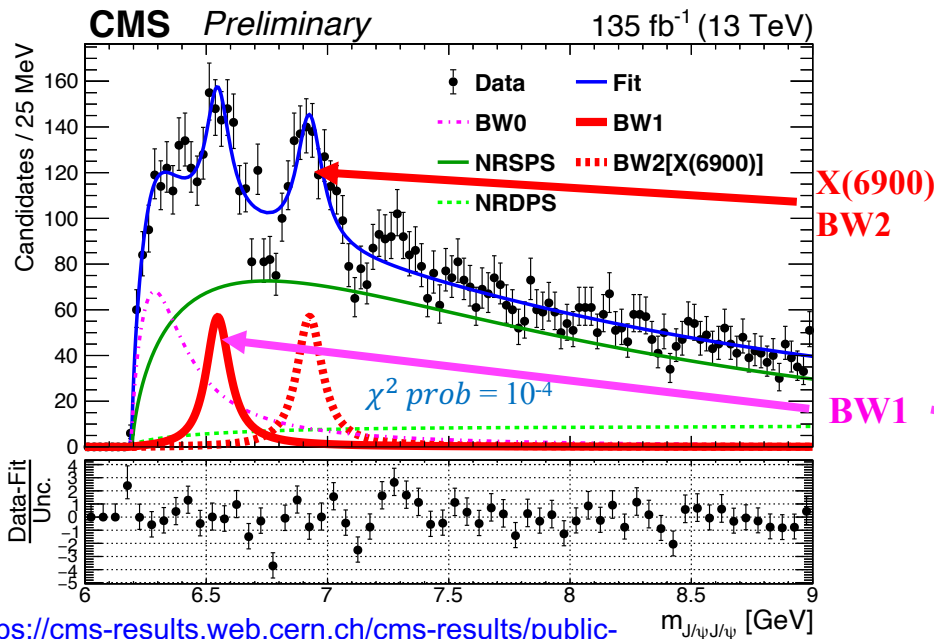
Fit CMS data with LHCb model I : 2 auxiliary BWs + X(6900) + bkg



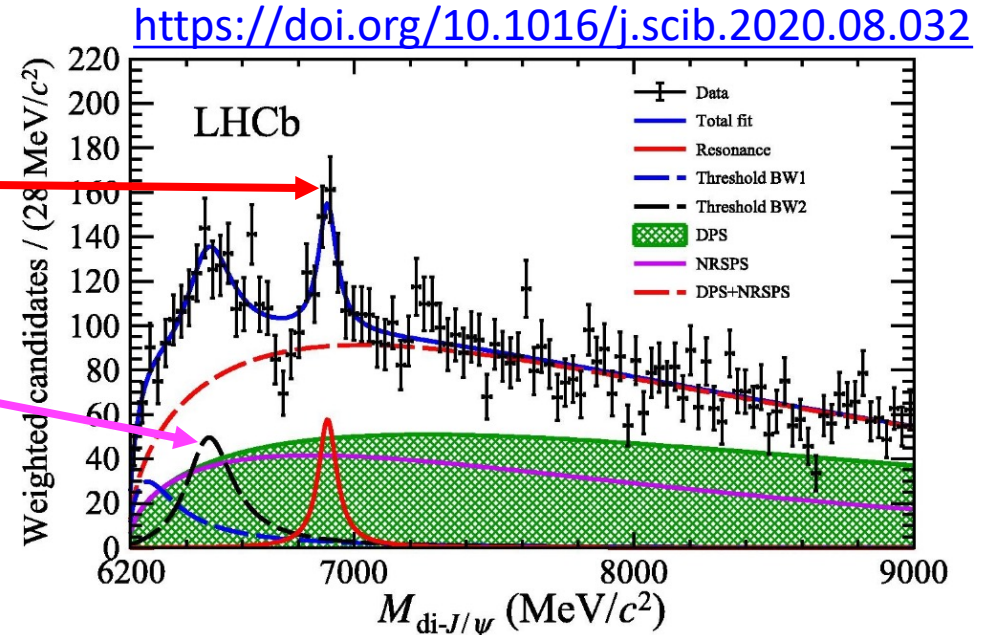
BW2 are in good agreement with LHCb X(6900)

| Exp. | Fit | $m(\text{BW1})$ | $\Gamma(\text{BW1})$ | $m(6900)$ | $\Gamma(6900)$ |
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Fit CMS data with LHCb model I : 2 auxiliary BWs + X(6900) + bkg



<https://cms-results.web.cern.ch/cms-results/public-results/superseded/BPH-21-003/index.html>



<https://doi.org/10.1016/j.scib.2020.08.032>

BW2 are in good agreement with LHCb X(6900)

| Exp. | Fit | $m(\text{BW1})$ | $\Gamma(\text{BW1})$ | $m(6900)$ | $\Gamma(6900)$ |
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| CMS | Model I | 6550 ± 10 | 112 ± 27 | 6927 ± 10 | 117 ± 24 |

- LHCb did not give parameters for BW1
 - CMS has a shoulder before BW1
 - helps make BW1 distinct
- Does not describe 2 dips well

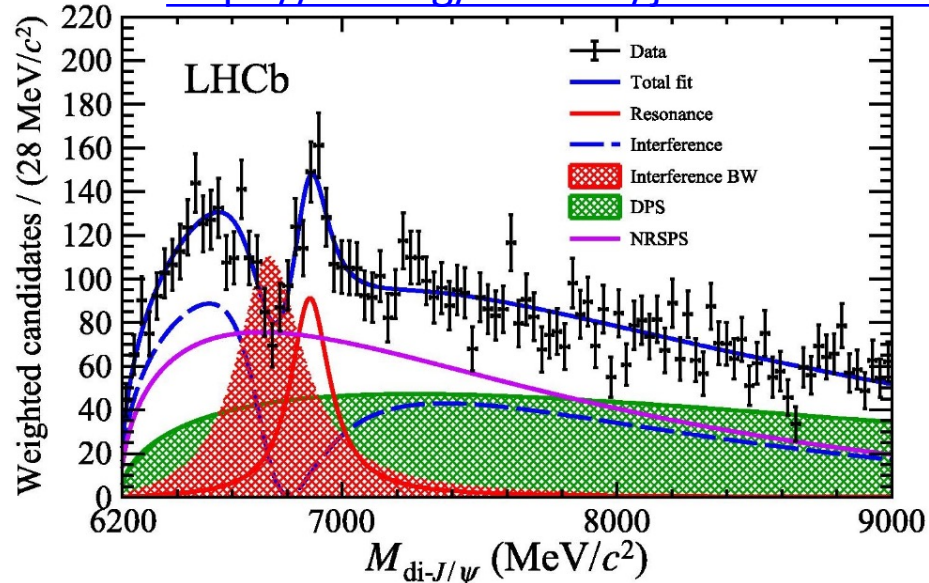
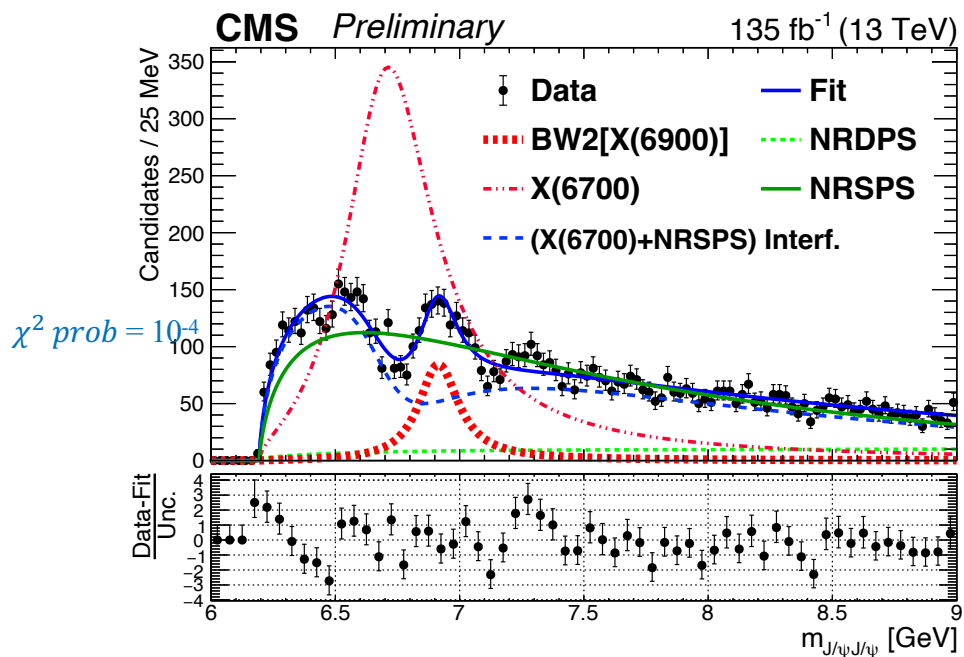


CMS and LHCb Fit Comparison - 2



Fit CMS data with LHCb model II : "X(6700)" interferes with NRSPS + X(6900) + Bkg

<https://doi.org/10.1016/j.scib.2020.08.032>

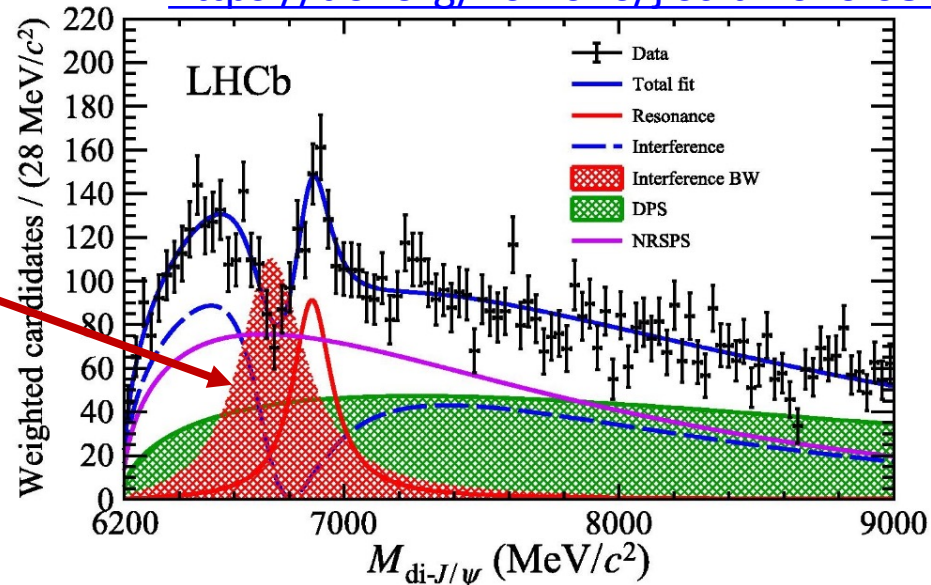
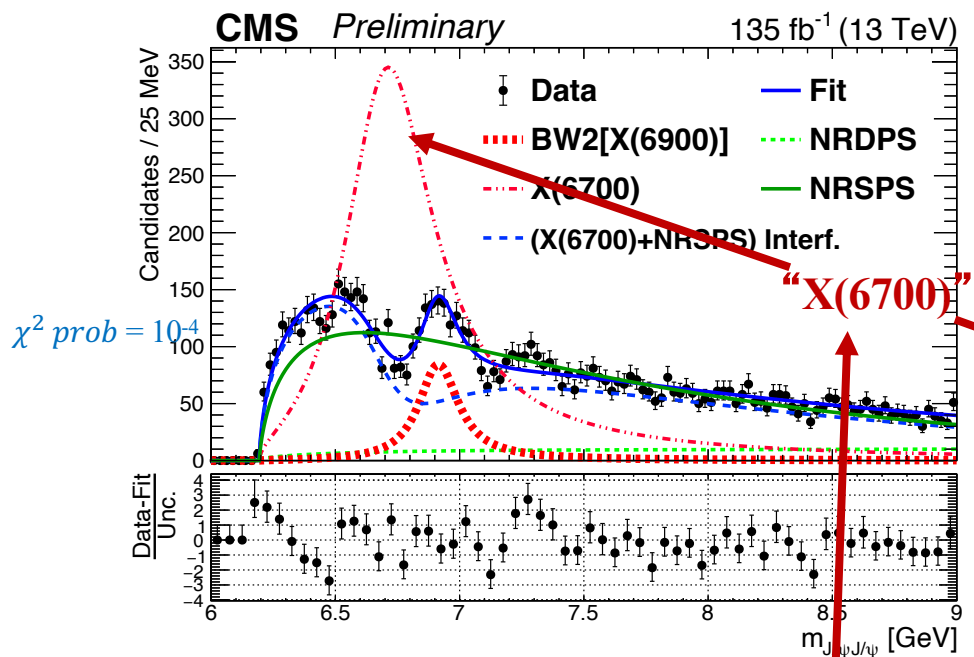


| Exp. | Fit | $m(\text{BW1})$ | $\Gamma(\text{BW1})$ | $m(6900)$ | $\Gamma(6900)$ |
|-----------|----------|-----------------|----------------------|----------------------|---------------------|
| LHCb [15] | Model II | 6741 ± 6 | 288 ± 16 | $6886 \pm 11 \pm 11$ | $168 \pm 33 \pm 69$ |
| CMS | Model II | 6736 ± 38 | 439 ± 65 | 6918 ± 10 | 187 ± 40 |



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- CMS obtained larger amplitude and wider width for X(6700)

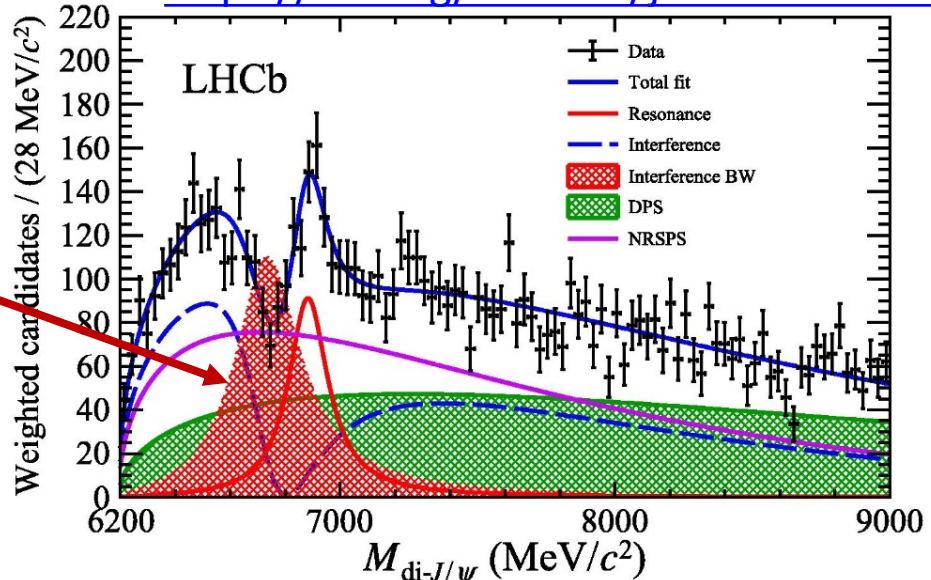
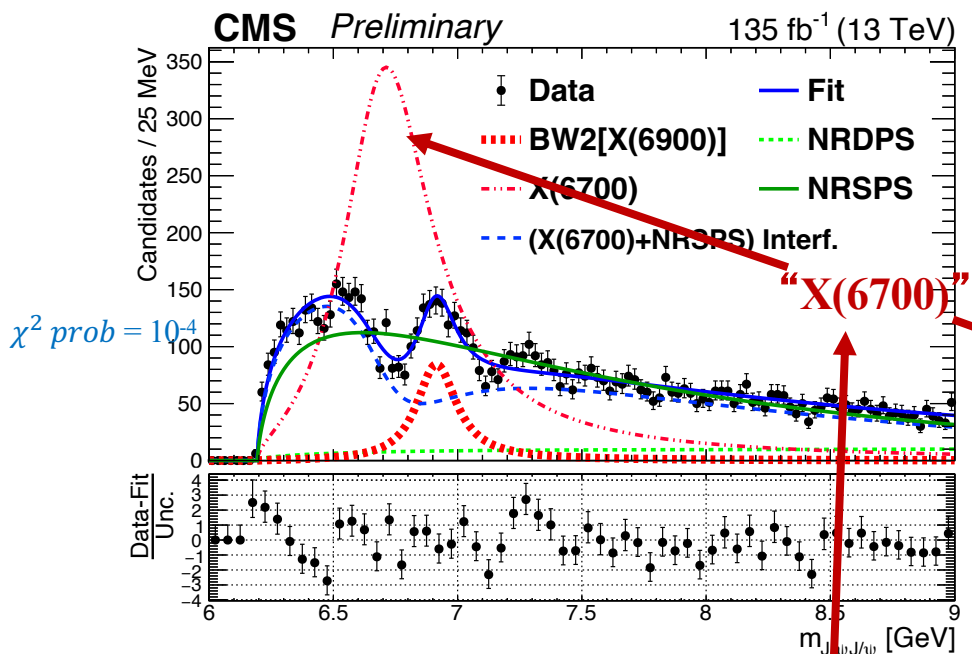


CMS and LHCb Fit Comparison - 2



Fit CMS data with LHCb model II : "X(6700)" interferes with NRSPS + X(6900) + Bkg

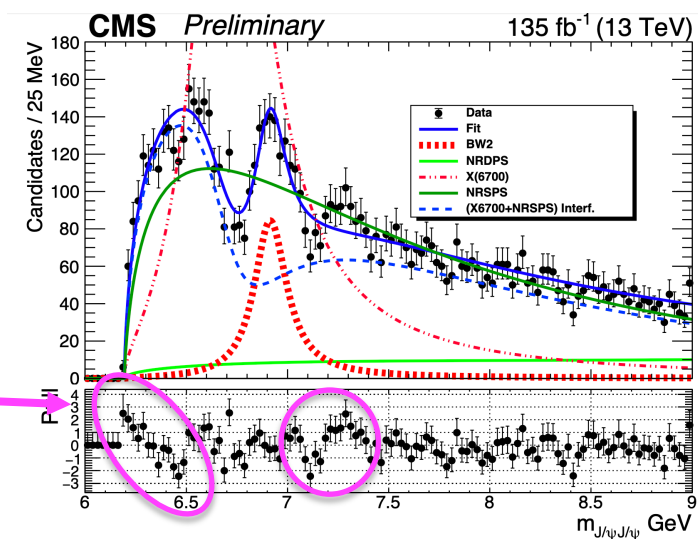
<https://doi.org/10.1016/j.scib.2020.08.032>



<https://cms-results.web.cern.ch/cms-results/public-results/superseded/BPH-21-003/index.html>

| Exp. | Fit | $m(\text{BW1})$ | $\Gamma(\text{BW1})$ | $m(6900)$ | $\Gamma(6900)$ |
|-----------|----------|-----------------|----------------------|----------------------|---------------------|
| LHCb [15] | Model II | 6741 ± 6 | 288 ± 16 | $6886 \pm 11 \pm 11$ | $168 \pm 33 \pm 69$ |
| CMS | Model II | 6736 ± 38 | 439 ± 65 | 6918 ± 10 | 187 ± 40 |

- CMS obtained larger amplitude and wider width for X(6700)
- Does not describe X(6600) and below
- Does not describe X(7200) region

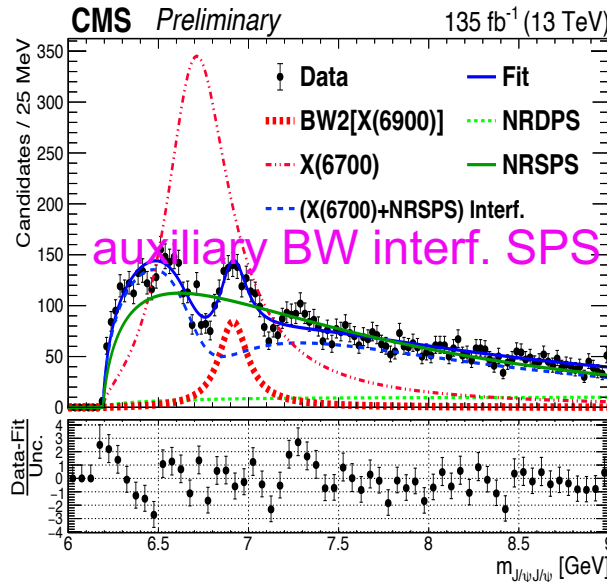
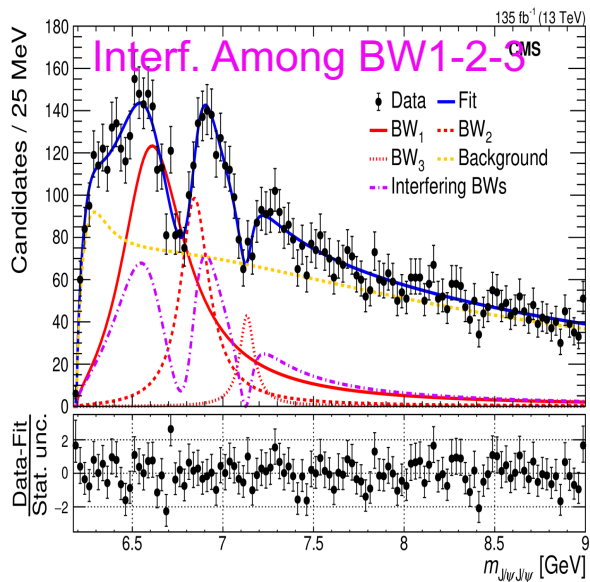
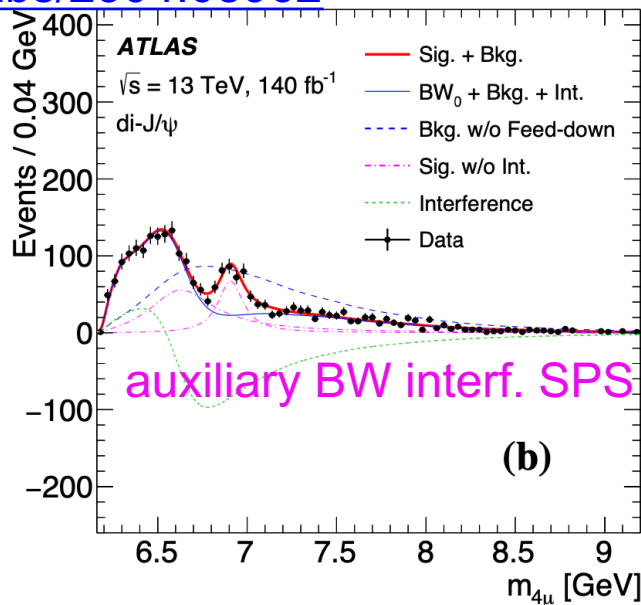
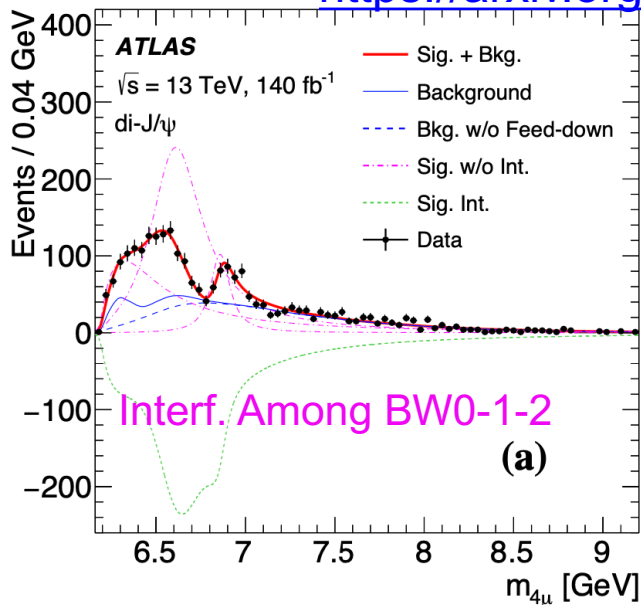




CMS and ATLAS Fit Comparison



<https://arxiv.org/abs/2304.08962>



- **ATLAS model A**: analogous to LHCb model I, but **2 auxiliary BWs** interfere with **X(6900)**
- **ATLAS Model B**: analogous to LHCb model II, **one auxiliary BW** interferes with NRSPS
- Both models describe the data well
- the broad structure at the lower mass could result from other physical effects, such as the feed-down
- The 3rd peak mass is consistent with the LHCb observed X(6900), with significance $> 5\sigma$

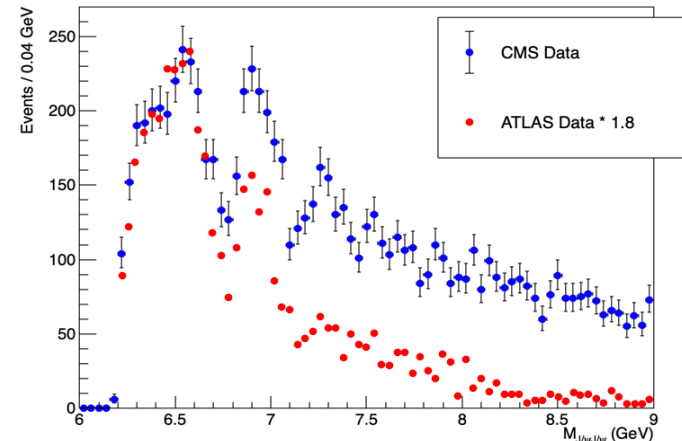
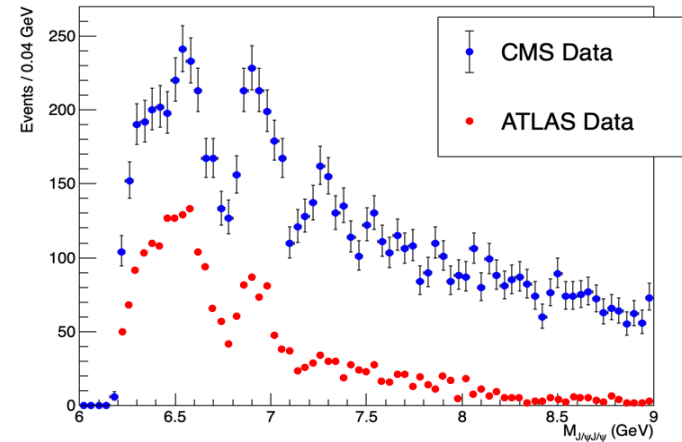
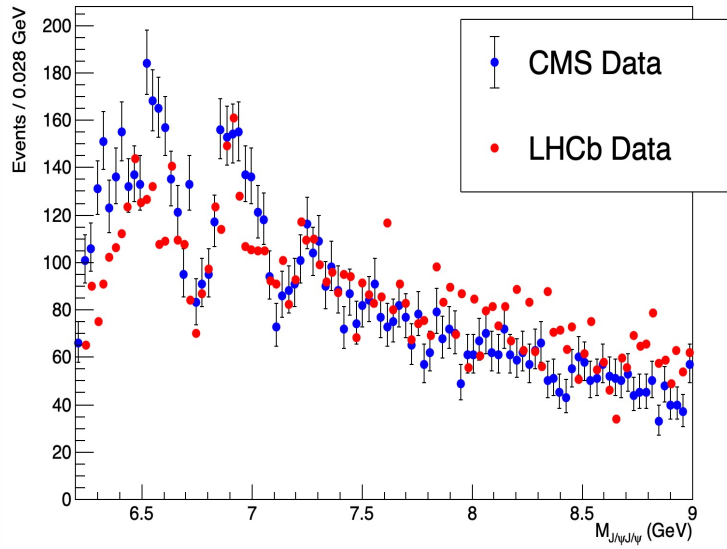




ATLAS-CMS-LHCb data comparison



Disclaimer: comparison plots in this page are not made by ATLAS/CMS/LHCb (taken from <https://indico.cern.ch/event/1158681/contributions/5162594/>)



- Comparing with LHCb, CMS has:
 - $135/(3+6) \approx 15X$ int. lum.
 - $(5/3)^4 \approx 8X$ muon acceptance
 - Higher muon p_T (>3.5 or 2.0 GeV vs >0.6 GeV)
 - Similar number of final events, but much less DPS
 - $2X$ yield @CMS for X(6900)

- Comparing with CMS, ATLAS has:
 - $1/3 - 1/2$ of CMS data (trigger?)
 - dR cut—remove high mass events



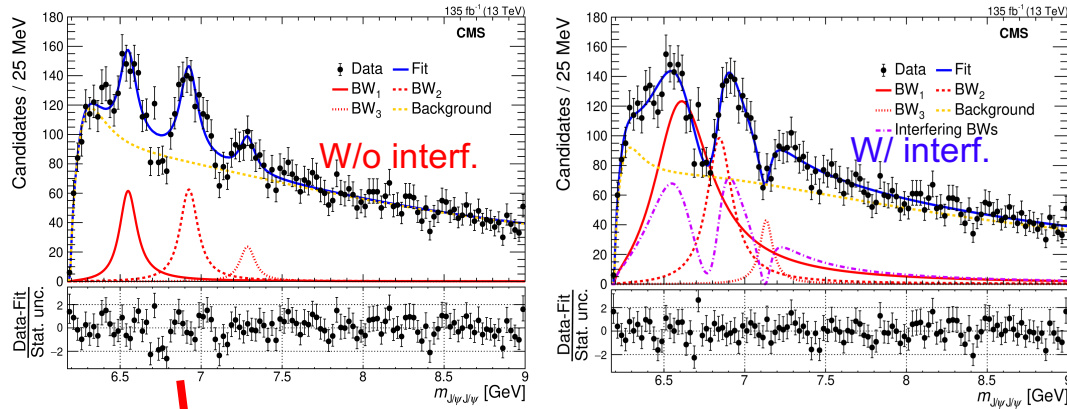


Table 1. Predictions of the masses (MeV) of S-wave fully heavy $T_{4Q}(nS)$ tetraquarks. Only 0^{++} and 2^{++} are considered for $T_{bc\bar{b}\bar{c}}$. The uncertainty is from the coupling constant $\alpha_s = 0.35 \pm 0.05$.

Nucl. Phys. B 966 (2021) 115393

| $T_{4Q}(nS)$ states | J^P | Mass(n=1) | Mass(n=2) | Mass(n=2) | Mass(n=3) |
|-------------------------|----------|-----------------------|---------------------|---------------------|---------------------|
| $T_{cc\bar{c}\bar{c}}$ | 0^{++} | 6055^{+69}_{-74} | 6555^{+36}_{-37} | 6883^{+27}_{-27} | 7154^{+22}_{-22} |
| $T_{cc\bar{c}\bar{c}}$ | 2^{++} | 6090^{+62}_{-66} | 6638^{+34}_{-35} | 6888^{+27}_{-26} | 7160^{+22}_{-22} |
| $T'_{cc\bar{c}\bar{c}}$ | 0^{++} | 5984^{+64}_{-67} | 6468^{+28}_{-28} | 6745^{+26}_{-26} | 7066^{+21}_{-21} |
| $T_{bc\bar{b}\bar{c}}$ | 0^{++} | 12387^{+109}_{-120} | 12911^{+68}_{-68} | 13200^{+35}_{-36} | 13429^{+29}_{-30} |
| $T_{bc\bar{b}\bar{c}}$ | 2^{++} | 12401^{+117}_{-106} | 12914^{+49}_{-49} | 13202^{+35}_{-36} | 13430^{+29}_{-29} |
| $T'_{bc\bar{b}\bar{c}}$ | 0^{++} | 12300^{+106}_{-117} | 12816^{+48}_{-50} | 13104^{+35}_{-35} | 13333^{+29}_{-29} |
| $T_{bb\bar{b}\bar{b}}$ | 0^{++} | 18475^{+151}_{-169} | 19073^{+59}_{-63} | 19533^{+42}_{-42} | 19566^{+33}_{-35} |
| $T_{bb\bar{b}\bar{b}}$ | 2^{++} | 18483^{+149}_{-168} | 19075^{+59}_{-62} | 19555^{+41}_{-43} | 19567^{+33}_{-35} |
| $T'_{bb\bar{b}\bar{b}}$ | 0^{++} | 18383^{+149}_{-167} | 18976^{+59}_{-62} | 19566^{+43}_{-42} | 19468^{+34}_{-34} |

S-wave

$$M[\text{BW1}] = 6638 \pm 10 \pm 12 \text{ MeV}$$

$$M[\text{BW2}] = 6847 \pm 9 \pm 5 \text{ MeV}$$

$$M[\text{BW3}] = 7134 \pm 19 \pm 5 \text{ MeV}$$

| | | | | | | | | | | | | |
|-----------|----------|-------|-------|--------|-------|-------|-------|-------|------|------|--------|---------------------------|
| $1^1 P_1$ | 1^{--} | 363.9 | 320.3 | -366.7 | 337.5 | -14.4 | 0 | 0 | -2.6 | 6553 | - | - |
| $1^3 P_0$ | 0^{--} | 356.7 | 320.2 | -366.7 | 337.5 | -7.2 | -36.9 | -43.1 | -2.6 | 6460 | 6398.1 | $\eta_c(1S)\chi_{c0}(1P)$ |
| $1^3 P_1$ | 1^{--} | 356.6 | 320.3 | -366.7 | 337.5 | -7.2 | -28.4 | 21.5 | -2.7 | 6554 | 6494.1 | $\eta_c(1S)\chi_{c1}(1P)$ |
| $1^3 P_2$ | 2^{--} | 356.6 | 320.2 | -366.7 | 337.5 | -7.2 | 28.4 | -2.1 | -2.4 | 6587 | 6539.6 | $\eta_c(1S)\chi_{c2}(1P)$ |
| $1^5 P_1$ | 1^{--} | 342.4 | 320.4 | -366.7 | 337.5 | 7.2 | -85.3 | -30.2 | -2.7 | 6439 | 6508.8 | $\eta_c(1S)h_{c1}(1P)$ |
| $1^5 P_2$ | 2^{--} | 342.2 | 320.2 | -366.7 | 337.5 | 7.2 | -28.4 | 30.2 | -2.5 | 6571 | 6607.6 | $J/\psi(1S)\chi_{c1}(1P)$ |
| $1^5 P_3$ | 3^{--} | 342.3 | 320.3 | -366.7 | 337.5 | 7.2 | 56.9 | -8.6 | -2.5 | 6623 | 6653.1 | $J/\psi(1S)\chi_{c2}(1P)$ |
| $2^1 P_1$ | 1^{--} | 414.7 | 688.7 | -263.4 | 548.6 | -11.2 | 0 | 0 | -1.6 | 6925 | - | - |
| $2^3 P_0$ | 0^{--} | 410.0 | 689.6 | -263.4 | 548.6 | -5.6 | -46.2 | -34.5 | -1.7 | 6851 | - | - |
| $2^3 P_1$ | 1^{--} | 410.0 | 689.6 | -263.4 | 548.6 | -5.6 | -23.1 | 17.2 | -1.6 | 6926 | - | - |
| $2^3 P_2$ | 2^{--} | 410.0 | 689.6 | -263.4 | 548.6 | -5.6 | 23.1 | -3.4 | -1.7 | 6951 | - | - |
| $2^5 P_1$ | 1^{--} | 398.7 | 689.5 | -263.4 | 548.6 | -5.6 | -69.3 | -24.2 | -1.7 | 6841 | - | - |
| $2^5 P_2$ | 2^{--} | 398.7 | 689.5 | -263.4 | 548.6 | 5.6 | -23.1 | 24.2 | -1.5 | 6944 | - | - |
| $2^5 P_3$ | 3^{--} | 398.8 | 689.7 | -263.4 | 548.6 | 5.6 | 46.2 | -6.9 | -1.6 | 6982 | - | - |
| $3^1 P_1$ | 1^{--} | 479.8 | 982.2 | -215.5 | 727.8 | -9.3 | 0 | 0 | -1.1 | 7221 | - | - |
| $3^3 P_0$ | 0^{--} | 475.2 | 982.7 | -215.5 | 727.7 | -4.6 | -41.9 | -31.0 | -1.2 | 7153 | - | - |
| $3^3 P_1$ | 1^{--} | 475.1 | 982.6 | -215.5 | 727.7 | -4.6 | -20.9 | 15.5 | -1.2 | 7220 | - | - |
| $3^3 P_2$ | 2^{--} | 475.1 | 982.6 | -215.5 | 727.8 | -4.6 | 20.9 | -3.1 | -1.0 | 7243 | - | - |
| $3^5 P_1$ | 1^{--} | 465.9 | 982.8 | -215.5 | 727.7 | 4.6 | -62.8 | -21.7 | -1.2 | 7150 | - | - |
| $3^5 P_2$ | 2^{--} | 465.7 | 982.6 | -215.5 | 727.8 | -4.6 | -20.9 | 21.7 | -1.1 | 7236 | - | - |
| $3^5 P_3$ | 3^{--} | 465.8 | 982.6 | -215.5 | 727.8 | 4.6 | 41.9 | -6.2 | -1.1 | 7271 | - | - |

arXiv:2108.04017 [hep-ph]

P-wave

$$M[\text{BW1}] = 6552 \pm 10 \pm 12 \text{ MeV}$$

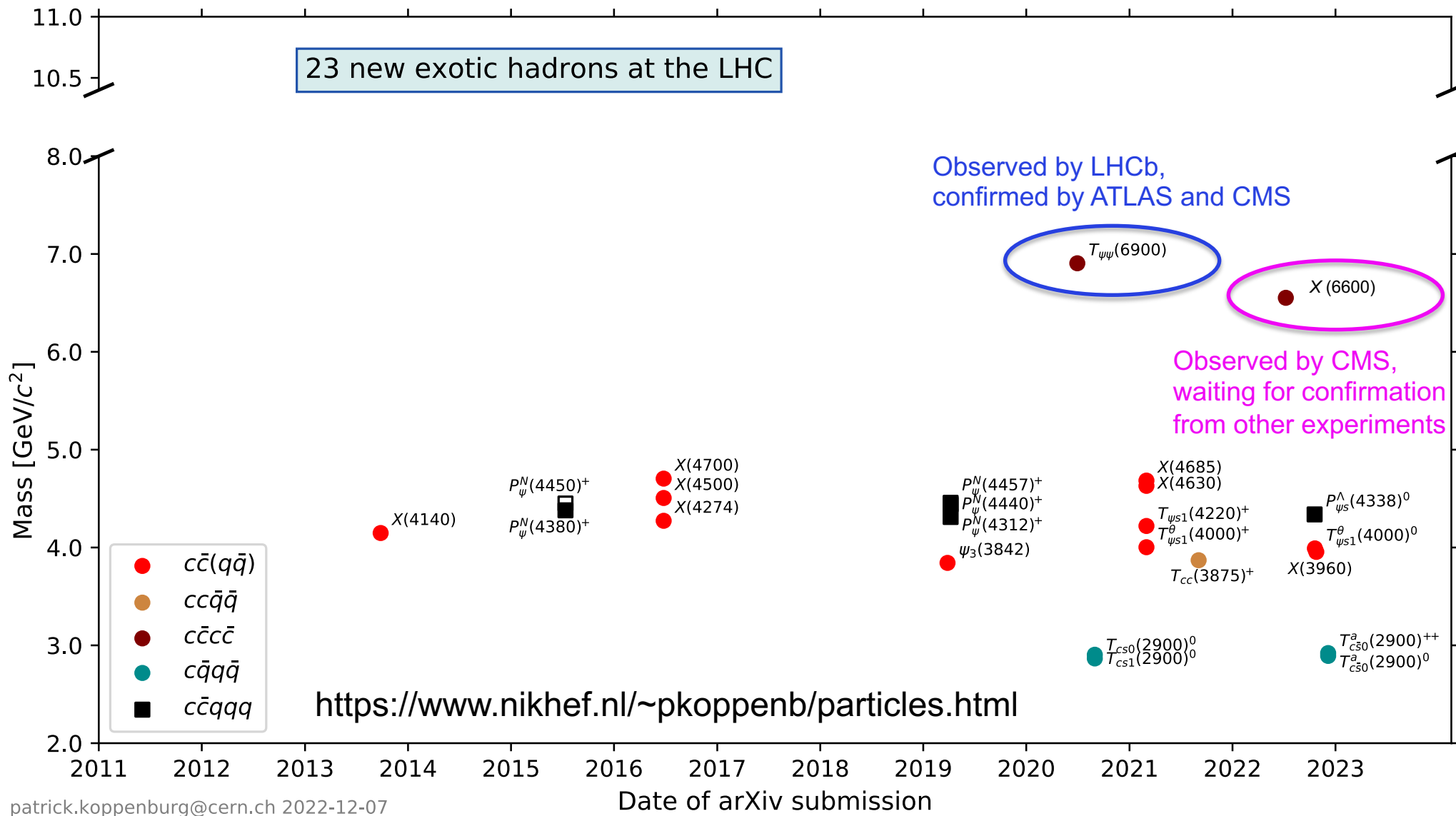
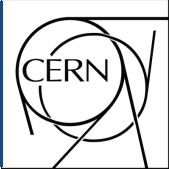
$$M[\text{BW2}] = 6927 \pm 9 \pm 5 \text{ MeV}$$

$$M[\text{BW3}] = 7287 \pm 19 \pm 5 \text{ MeV}$$

- Radial excited p-wave states (like J/ψ series)?
- Or Radial excited S-wave states?
- Theoretical situation difficulty & confusing
 - Important next step: measure J^{PC} to clarify
- Natural question: what about YY final state?



New exotic hadrons at LHC

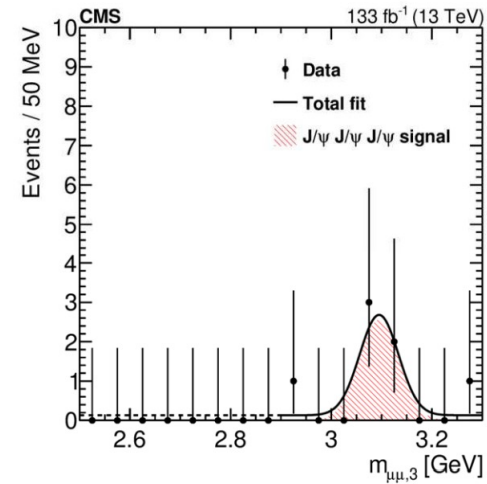
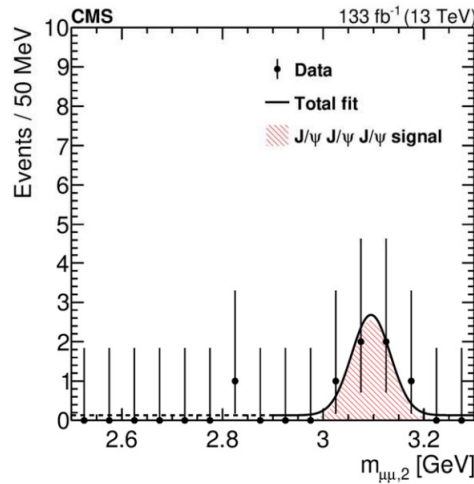
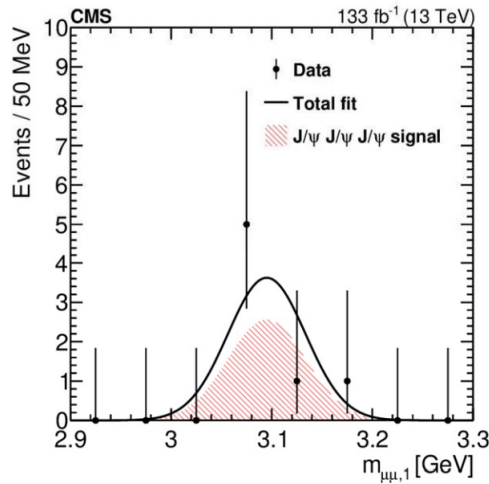
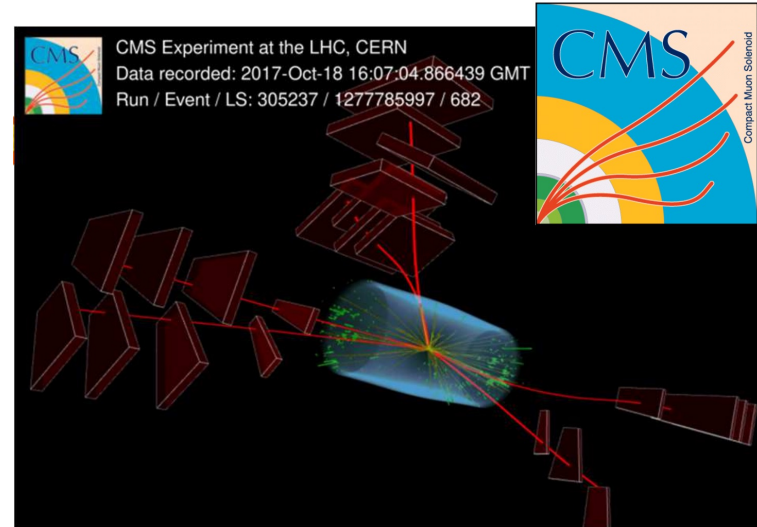


Signal yield: $5_{-1.9}^{+2.6}$ events

Significance $> 5\sigma$

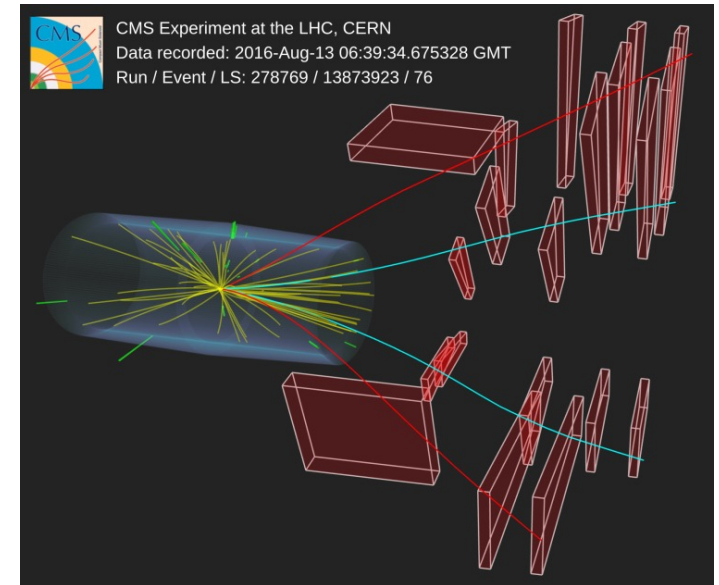
$$\sigma(pp \rightarrow J/\psi J/\psi J/\psi X) = 272 +141-104 \text{ (stat)} \pm 17 \text{ (syst)} \text{ fb}$$

Nature Physics 19 (2023) 338



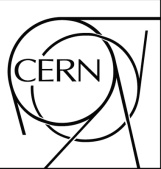
“6c” search in future?

- CMS played leading roles in some exotic hadron studies
- All-heavy quark exotic structures offer a system easier to understand
 - A new window to understand strong interaction
- CMS found 3 significant structures in di- J/ψ mass spectrum
 - X(6900) consistent with LHCb
 - **First observation of X(6600)** and evidence of X(7300) in di- J/ψ
 - Dips in data show possible interference effects
 - **A family of structures which are candidates for all-charm tetra-quarks!**
 - <https://arxiv.org/abs/2306.07164> (Submitted to PRL)



X(6600) event display

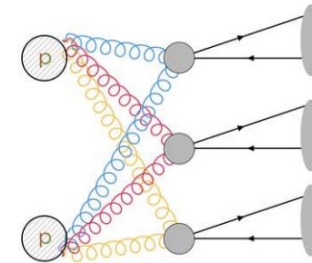
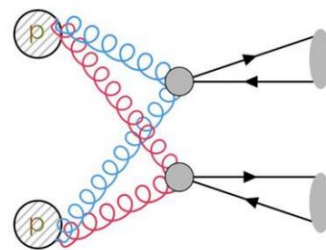
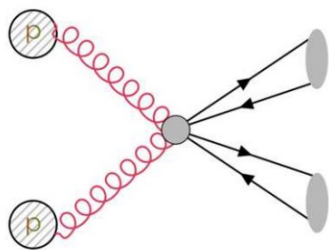
- Triple J/ψ production has also been observed for the first time



Backup



- Study interplay of soft QCD with (semi)hard QCD and EW physics
- Sensitivity to perturbative heavy flavor generation and nonperturbative initial and final state effects
 - Initial state: e.g. sensitivity to the concepts of single (SPS), double (DPS) and triple (TPS) parton scattering



parameterized by σ_{eff}

$$\sigma_{\text{DPS}}^{AB} = \frac{1}{1 + \delta_{AB}} \frac{\sigma^A \sigma^B}{\sigma_{\text{eff}}}$$

- Final state: e.g. sensitivity to heavy flavour hadron formation (colour singlet vs. colour octet), sensitivity to resonant multi-heavy-flavor states

Muon selection

- $p_T(\mu^\pm) > 2.0 \text{ GeV}/c$
- $|\eta(\mu^\pm)| < 2.4$
- All muons are soft
- For 2017-18 years: $p_T(\mu^\pm) > 3.5 \text{ GeV}/c$ for at least one $\mu^+\mu^-$ pair, which has $vtxprob(\mu^+\mu^-) > 0.5\%$ and $2.95 < m_{\mu^+\mu^-} < 3.25 \text{ GeV}$

J/ψ selection

- $2.95 < m_{J/\psi} < 3.25 \text{ GeV}$
- $p_T(J/\psi) > 3.5 \text{ GeV}/c$
- $vtxprob(J/\psi) > 0.5\%$
- Constrained $vtxprob(J/\psi) > 0.1\%$

J/ψJ/ψ selection

- $vtxprob(4\mu) > 0.5\%$
- $vtxprob(J/\psi J/\psi) > 0.1\%$
- Proper HLT is fired in event

Multiple candidates

- Choose the best candidate with minimum $\left(\frac{M(J/\psi_1) - M(J/\psi_{PDG})}{\sigma(M(J/\psi_1))}\right)^2 + \left(\frac{M(J/\psi_2) - M(J/\psi_{PDG})}{\sigma(M(J/\psi_2))}\right)^2$ value if there are 4 muons in event, but more than one candidate ($\sim 0.2\%$)
- Keep all candidates if there are more than 4 muons in event ($\sim 0.2\%$)

Baseline mass variable – invariant mass of two constrained J/ψ candidates

- To include systematics, alternative resonance/background shapes applied in the fit.
- Calculate signal- and null-hypothesis NLL_{syst} including systematic using:

$$NLL_{(syst-sig)} = \text{Min}\{NLL_{(nom-sig)}, NLL_{(alt-i-sig)}+0.5+0.5\cdot\Delta dof\}$$
 - $NLL_{(nom-sig)}$: the NLL of nominal 'signal hypothesis' fit.
 - $NLL_{(alt-i-sig)}$: the NLL of i-th alternative fit of 'signal hypothesis'
 - Δdof : the additional free parameters comparing to the nominal 'signal hypothesis' fit.
- $NLL_{(syst-null)} = \text{Min}\{NLL_{(nom-null)}, NLL_{(alt-j-null)}+0.5+0.5\cdot\Delta dof\}$
- Significance including systematics as usual from $NLL_{(syst-null)} - NLL_{(syst-sig)}$

| | Significance with syst. |
|-----|----------------------------|
| BW1 | 5.7σ |
| BW2 | <i>no sensible changes</i> |
| BW3 | <i>no sensible changes</i> |

- S-wave relativistic Breit-Wigner (used in default fit):

$$BW(m; m_0, \Gamma_0) = \frac{\sqrt{m\Gamma(m)}}{m_0^2 - m^2 - im\Gamma(m)}, \text{ where } \Gamma(m) = \Gamma_0 \frac{qm_0}{q_0m},$$

q is the momentum of a daughter in the mother particle rest frame; q_0 means the value at peak position ($m = m_0$).

- NRSPS and NRDPS:

$$f_{NRSPS}(x, x_0, \alpha, p_1, p_2, p_3)$$

$$= (x - x_0)^\alpha \cdot \left(1 - \left(\frac{1}{(15 - x_0)^2} - \frac{p_1}{10} \right) \cdot (15 - x)^2 \right) \cdot \exp\left(-\frac{(x - x_0)^{p_3}}{2 \cdot p_2^{p_3}} \right),$$

$$f_{NRDPS}(x, a, p_0, p_1, p_2) = \sqrt{x_t} \cdot \exp(-a \cdot x_t) \cdot (p_0 + p_1 \cdot x_t + p_2 \cdot x_t^2),$$

where $x_0 = 2m_{J/\psi}$, $x_t = x - x_0$

| Source | ΔM_{BW1} | ΔM_{BW2} | ΔM_{BW3} | $\Delta \Gamma_{BW1}$ | $\Delta \Gamma_{BW2}$ | $\Delta \Gamma_{BW3}$ |
|--------------------------|------------------|------------------|------------------|-----------------------|-----------------------|-----------------------|
| signal shape | 3 | 4 | 3 | 14 | 7 | 7 |
| NRDPS | 1 | < 1 | < 1 | 3 | 3 | 4 |
| NRSPS | 3 | 1 | 1 | 18 | 15 | 17 |
| momentum scaling | 1 | 3 | 4 | - | - | - |
| mass resolution | < 1 | < 1 | < 1 | < 1 | < 1 | 1 |
| combinatorial background | < 1 | < 1 | < 1 | 2 | 3 | 3 |
| efficiency | < 1 | < 1 | < 1 | 1 | < 1 | 1 |
| feeddown shape | 11 | 1 | 1 | 25 | 8 | 6 |
| total | 12 | 5 | 5 | 34 | 19 | 20 |

- Investigated effects of systematics on local significance by a profiling procedure
- A discrete set of individual alternative signal and background hypotheses tested in minimization
 - Significant change: BW1 significance changed from 6.5σ to $>5.7\sigma$
 - No relative significance changes for BW2 and BW3

$$M[BW1] = 6552 \pm 10 \pm 12 \text{ MeV} \quad \Gamma[BW1] = 124 \pm 29 \pm 34 \text{ MeV} \quad >5.7\sigma$$

$$M[BW2] = 6927 \pm 9 \pm 5 \text{ MeV} \quad \Gamma[BW2] = 122 \pm 22 \pm 19 \text{ MeV} \quad >9.4\sigma$$

$$M[BW3] = 7287 \pm 19 \pm 5 \text{ MeV} \quad \Gamma[BW3] = 95 \pm 46 \pm 20 \text{ MeV} \quad >4.1\sigma$$

| Fit | Dominant sources | ΔM_{BW1} | ΔM_{BW2} | ΔM_{BW3} | $\Delta \Gamma_{BW1}$ | $\Delta \Gamma_{BW2}$ | $\Delta \Gamma_{BW3}$ |
|------------------|--------------------|------------------|------------------|------------------|-----------------------|-----------------------|-----------------------|
| Interference | Signal shape | 7 | 12 | 7 | 56 | 8 | 7 |
| | NRDPS | 1 | 3 | 2 | 18 | 6 | 2 |
| | NRSPS | 9 | 14 | 13 | 85 | 9 | 20 |
| | Resolution | 8 | 4 | 1 | 24 | 7 | 13 |
| | Combinatorial bkg. | 7 | 2 | < 1 | 5 | 3 | 2 |
| | Feeddown shape | -27 | +44 | +38 | -208 | +19 | +12 |
| Full uncertainty | | +16 | +48 | +41 | +109 | +25 | +29 |
| | | -31 | -20 | -15 | -235 | -17 | -26 |

- Total systematic uncertainty is quadrature sum of each source
- Systematic uncertainties from feeddown contribution are asymmetric
- Systematic uncertainties from other sources are symmetric

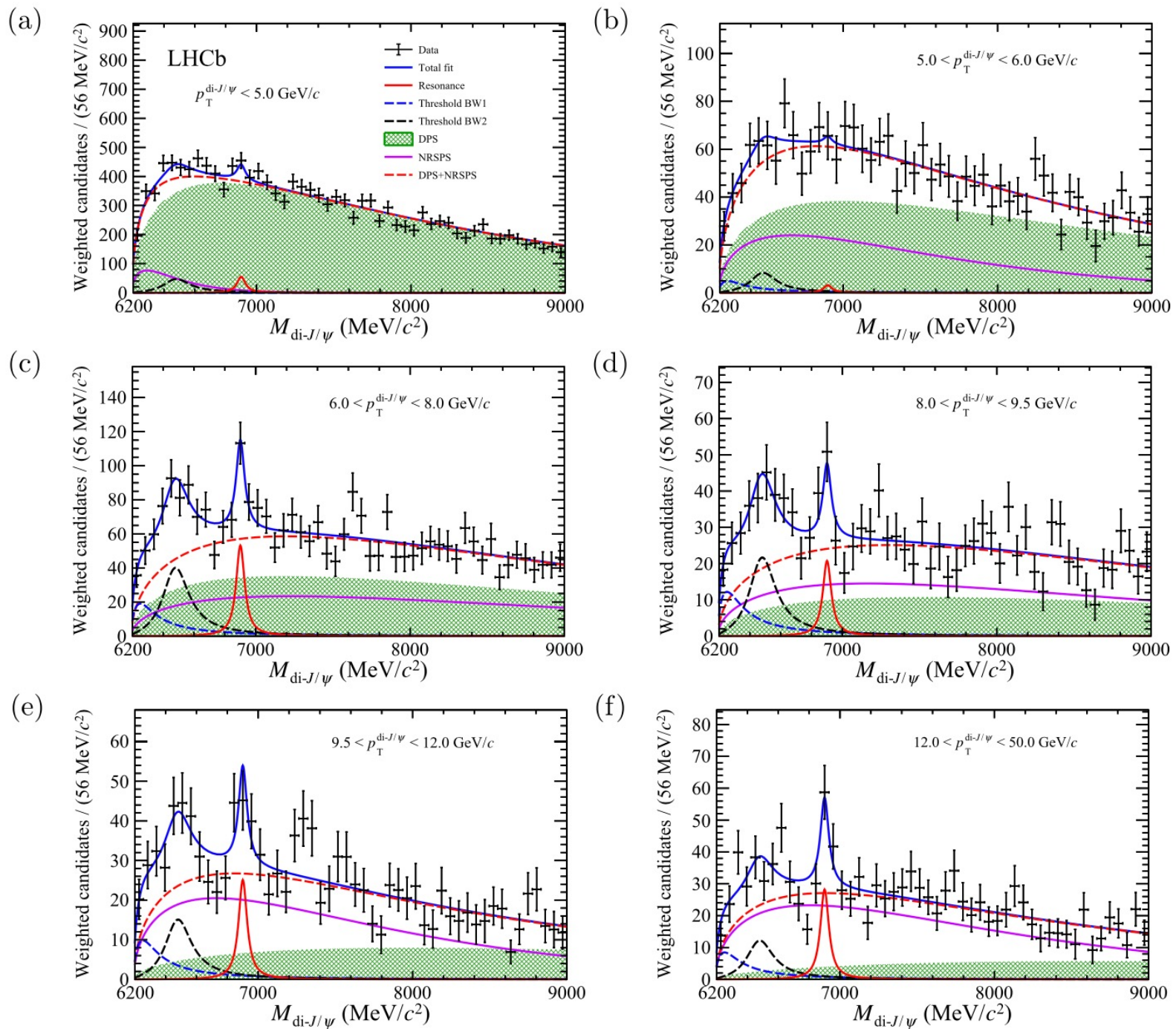


Fig. 4. Invariant mass spectra of weighted di- J/ψ candidates in bins of $p_T^{\text{di-}J/\psi}$ and overlaid projections of the $p_T^{\text{di-}J/\psi}$ -binned fit with model I.