# Type－Il Seesaw Triplet Scalar Effects on Neutrino Trident Scattering 

## 1．Type－II Seesaw model

In addition to the SM Higgs field，the type－II seesaw model contains an additional triplet Higgs field，

$$
\Delta=\left(\begin{array}{cc}
\Delta^{+} / \sqrt{2} & \Delta^{++} \\
\Delta^{0} & -\Delta^{+} / \sqrt{2}
\end{array}\right)
$$

From the Yukawa coupling term，

$$
\begin{array}{r}
-\mathcal{L}_{M_{v}}=Y_{i j} L_{L_{i}}^{T} C i \sigma^{2} \Delta L_{L_{j}}+\text { h.c. } \\
\left(M_{v}\right)_{i j}=\sqrt{2} v_{\Delta} Y_{i j} \rightarrow M_{v}=\frac{\mu v_{d}^{2}}{m_{\Delta}^{2}} Y
\end{array}
$$

## 2．Neutrino Trident Scattering



Neutrino trident scattering（NTS）${ }^{[1]}$ ：a weak process by which a neutrino，scattering off a heavy nucleus， generates a pair of charged leptons．
In type－Il seesaw model，a $\mu^{+} \mu^{-}$pair can be generated by $\Delta^{+}$，


The final modification would be

$$
\frac{\sigma}{\sigma_{S M}}=\frac{\left(1+4 s_{w}^{2}-\frac{2 m_{w}^{2}}{g^{2}} \frac{\left|m_{\mu \mu}\right|^{2}}{m_{\Delta}^{2} v_{\Delta}^{2}}\right)^{2}+\left(1-\frac{2 m_{w}^{2}}{g^{2}} \frac{\left|m_{\mu \mu}\right|^{2}}{m_{\Delta}^{2} v_{\Delta}^{2}}\right)^{2}+2\left(\frac{2 m_{w}^{2}\left|m_{\mu \mu}\right|^{2}}{g^{2} m_{\Delta}^{2} v_{\Delta}^{2}}\right)^{2}\left(\frac{\left|m_{e \mu}\right|^{2}+\left|m_{\tau \mu}\right|^{2}}{\left|m_{\mu \mu}\right|^{2}}\right)}{\left(1+4 s_{w}^{2}\right)^{2}+1}
$$

## 3．Constrains on Trident

Type－II seesaw also induce new processes not exist in the SM，such as $l_{i}^{-} \rightarrow l_{j}^{+} l_{k}^{-} l_{l}^{-}$and $l_{i}^{-} \rightarrow l_{j}^{-} \gamma$ which provide severe constraints to the model parameters．

| Process | Branching | Constraint |
| :--- | :--- | :--- |
| $\mu^{-} \rightarrow e^{+} e^{-} e^{-}$ | $1.0 \times 10^{-12}$ | $m_{\Delta} v_{\Delta}>\left\|\left(M_{\nu}\right)_{\mu e}\left(M_{\nu}\right)_{e e}\right\|^{1 / 2} \times 145 \mathrm{TeV}$ |
| $\mu^{-} \rightarrow e^{-} \gamma$ | $4.2 \times 10^{-13}$ | $m_{\Delta} v_{\Delta}>\sqrt{9\left\|M_{\nu}^{\dagger} M_{\nu}\right\|_{\mu e}} \times 15.3 \mathrm{TeV}$ |


－By taking into account these constraints，$\sigma / \sigma_{\mathrm{SM}}$ can at most reach 0.98 （shown as dashed gray line in the figure）at $3 \sigma$ level．

## 4．Combine the Constrains

Combine these two constrains，

（a）

（b）

The dashed line corresponds to the upper limit from $\mu^{-} \rightarrow$ $\mathrm{e}^{+} \mathrm{e}^{-} \mathrm{e}^{-}$．Points above the dashed line are ruled out．（a）for NO case，and（b）for IO case．
－The deviation of $\sigma / \sigma_{S M}$ from 1 is constrained to less than about $2 \%$ at $3 \sigma$ level．

## 5．Conclusion

From cosmological considerations，the effect of $\Delta$ on $\sigma / \sigma_{\mathrm{SM}}$ is limited to be less than $0.1 \%$ ．This is a challenge to experimental test．
－If a deviation is more than $2 \%$ will be found，the Type－II seesaw is unlikely to be able to explain the data．

