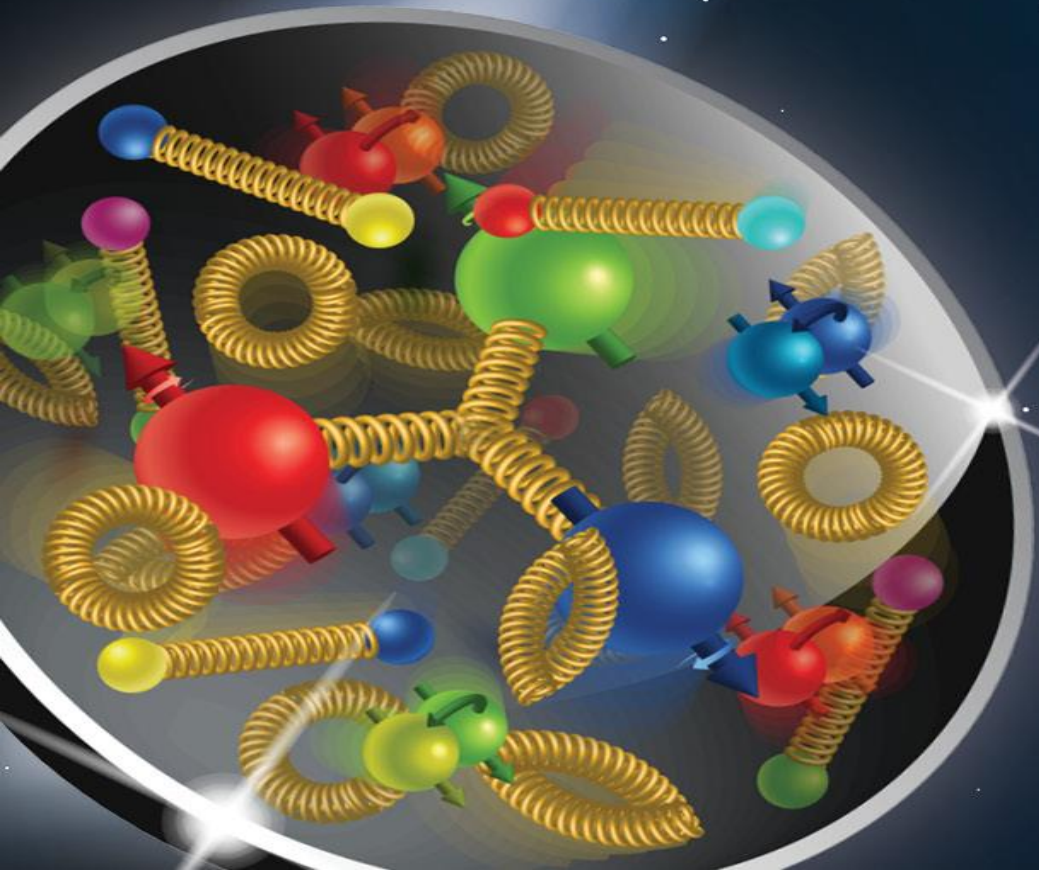


Exclusive quarkonia photoproduction simulation and physics at EICs



Xinbai Li, xinbai@mail.ustc.edu.cn

X. Li et al., NIMA 1048 (2023) 167956



Electron-Ion Collider

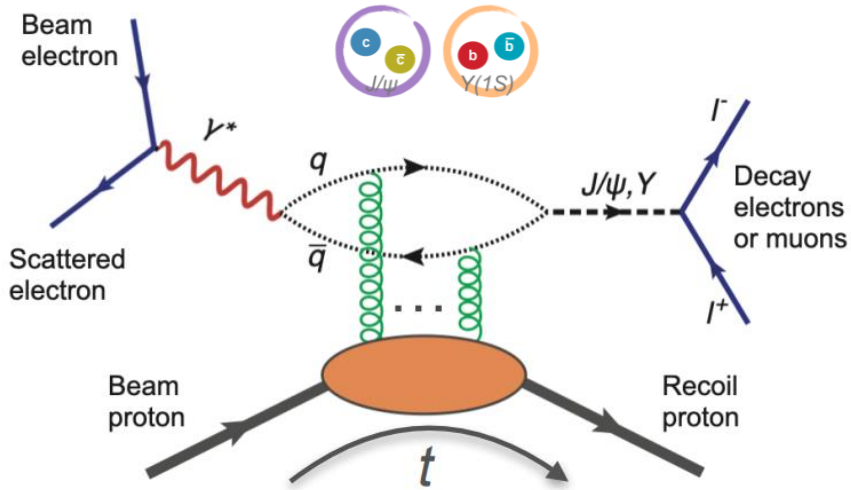
BROOKHAVEN
NATIONAL LABORATORY

Jefferson Lab



U.S. DEPARTMENT OF
ENERGY | Office of
Science

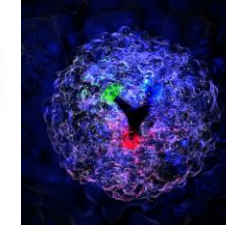
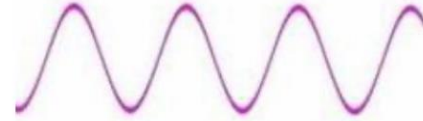
Process of interest



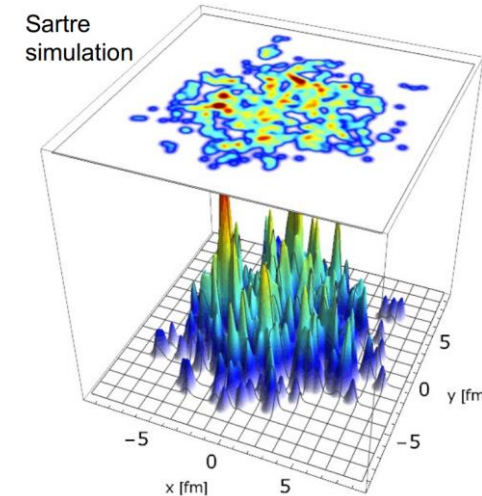
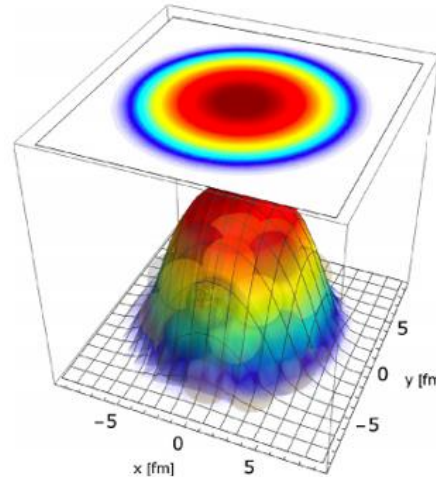
- ❑ The energy of photon decided the wave length and is related to the momentum fraction x of the detected partons (down to 5×10^{-4}).
- ❑ EIC will benefit from the large detector rapidity acceptance $(-3.5-3.5)$ so that the maximum energy of photon could be close to the electron beam energy (5-18 GeV).

$$E_\gamma = \frac{M_p}{2} e^{-y}$$

between RHIC ~ 4 GeV and LHC $\sim 75-100$ GeV



Diffraction pattern is like a CT scan for spatial and momentum distributions of gluons in nucleon/nuclei.



Gold nuclear gluon density profile (from Kong's slide)
[made by A. Kumar (IIT, Delhi)]

Coherent: photons interact with the whole nucleon/nucleus.

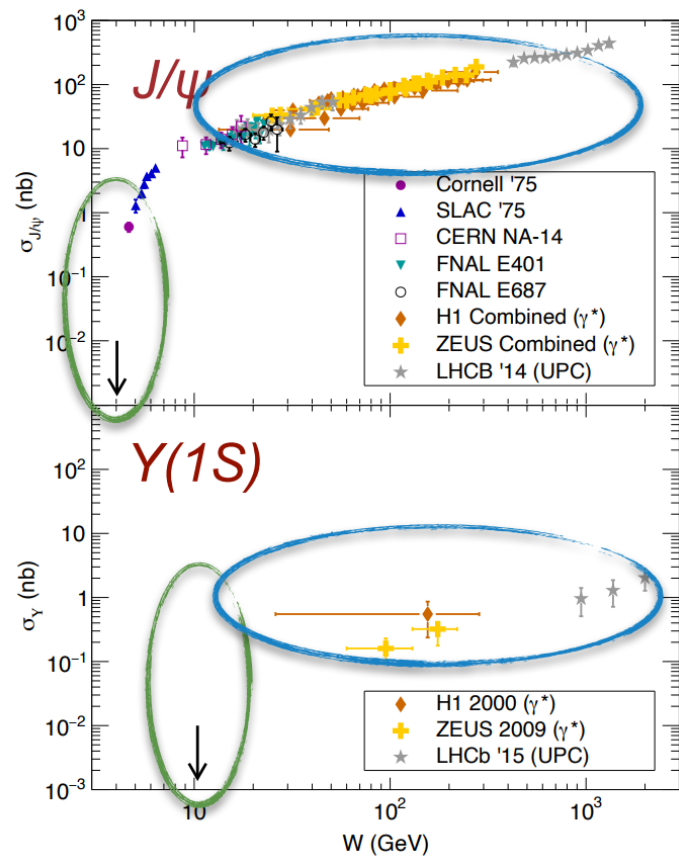
Incoherent: vector meson production with nucleon/nucleus excited.

What do we know?

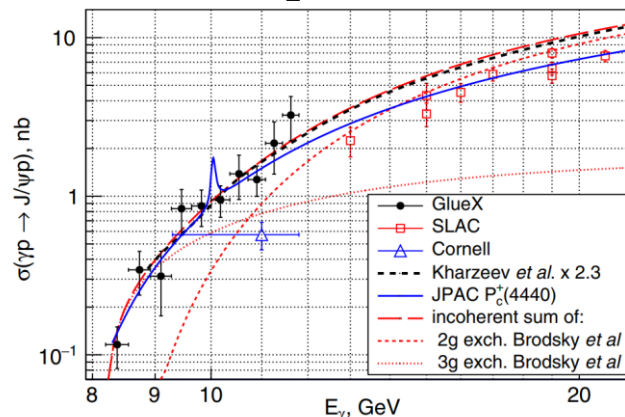
- Low momentum transfer ($t=P_T^2$) is dominated by **coherent photoproduction**.
- Strong proton shape fluctuations in **incoherent diffraction**...
- The ratio of the incoherent to coherent cross-section drops with **increasing photon energy**.
-

H. Mantysaari and B. Schenke PRL 117 (2016) 052301

H. Mantysaari and B. Schenke PRD 98 (2018) 034013

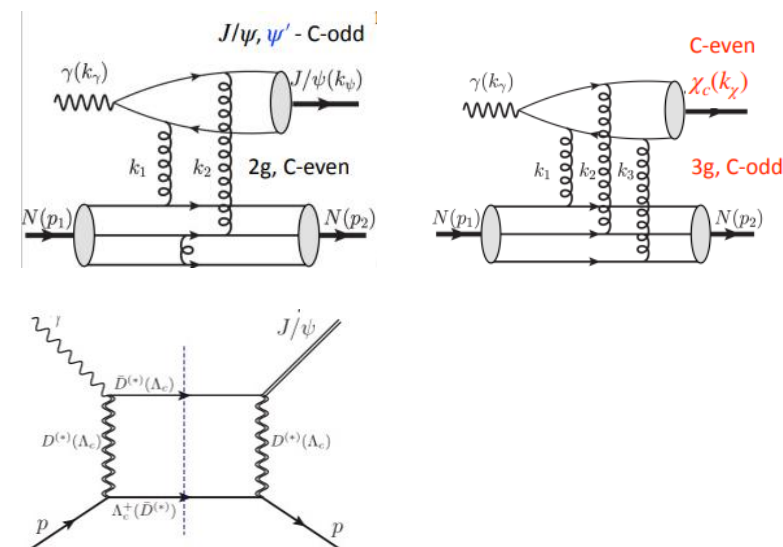
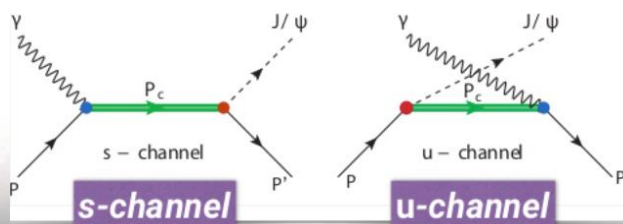


Near threshold production at JLab



Ali et al., PRL 123 (2019) 072001;
Brodsky et al., PLB 498 (2001) 23

□ Set upper limits for P_c^+ channels



□ Recent GlueX measurements have observed the higher mass C-even χ_c and possible evidence for production from open charm channel. (DIS 2023)

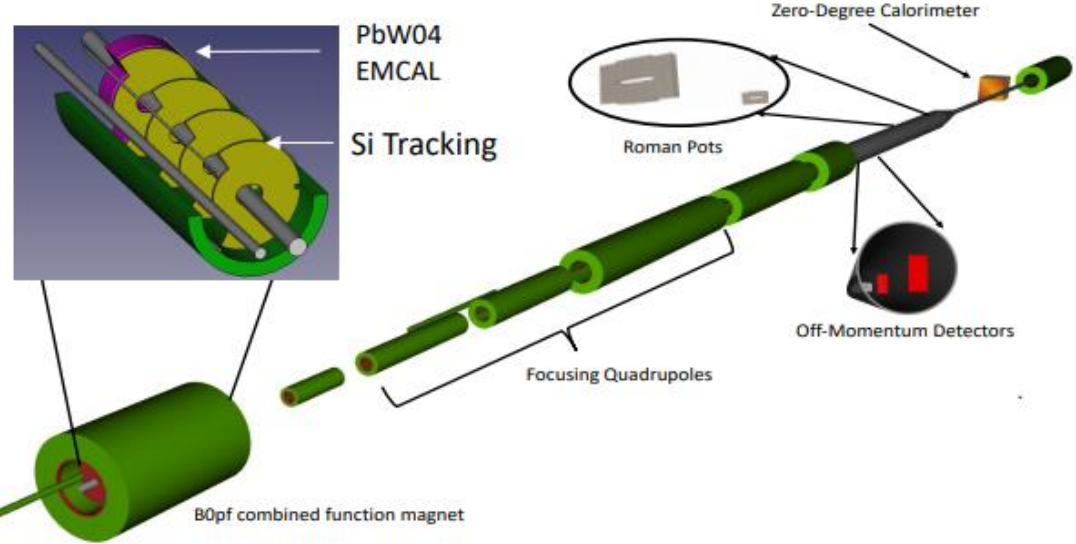
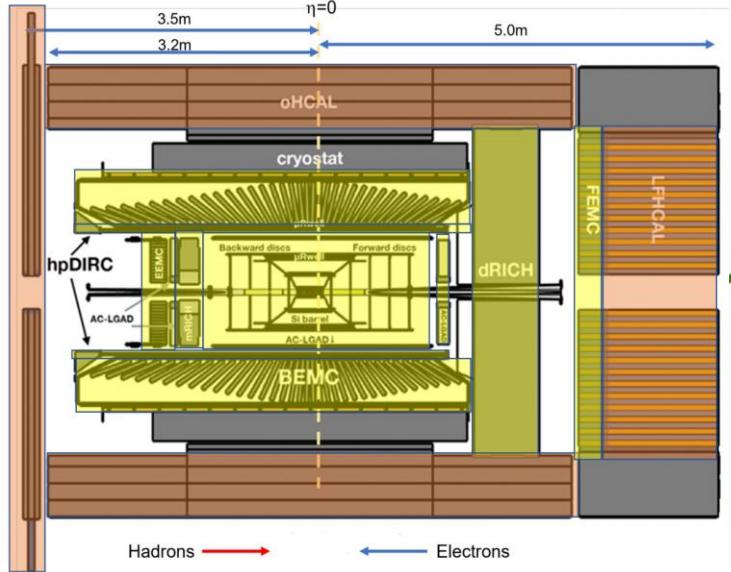
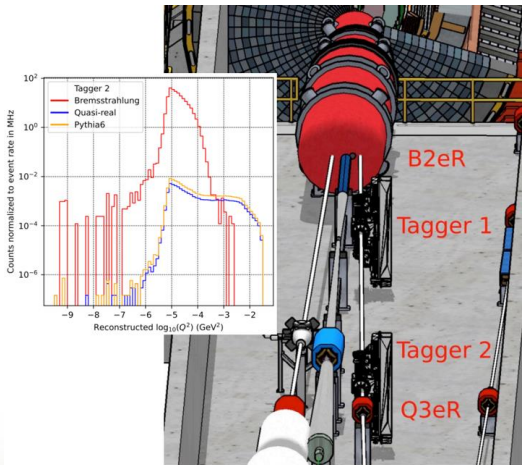
EIC detector overview

Exclusive measurements — all final state particles could be detected (e', daughters of V, (p'))
 [better t resolution; large Q² lever arm to reduce model dependence; allow to analyze photon flux and gluon density separately.]

ePIC Detector Design (Current)

Far-Backward Detectors

- Luminosity monitor
- Low-Q² Tagging Detectors



Detector	Acceptance
Zero-Degree Calorimeter (ZDC)	$\theta < 5.5$ mrad ($\eta > 6$)
Roman Pots (2 stations)	$0.0^* < \theta < 5.0$ mrad ($\eta > 6$)
Off-Momentum Detectors (2 stations)	$0.0^* < \theta < 5.0$ mrad ($\eta > 6$)
B0 Detector	$5.5 < \theta < 20.0$ mrad ($4.6 < \eta < 5.9$)

Clean photoproduction signal for $10^{-3} < Q^2 < 10^{-1}$

Reference: ePIC wiki page: [Electron-Proton/Ion Collider Experiment](#)

Theoretical framework to estimate the yield

Equivalent photon approximation vector meson dominate model (EPA-VPD) with several modifications.

$$\sigma(eA \rightarrow eAV) = \int \frac{dW}{W} \int dk \int dQ^2 \frac{d^2 N_\gamma}{dkdQ^2} \sigma_{\gamma^* A \rightarrow VA}(W, Q^2),$$

$$\frac{d^2 N_\gamma}{dkdQ^2} = \frac{\alpha}{\pi k Q^2} \left[1 - \frac{k}{Ee} + \frac{k^2}{2E_e^2} - \left(1 - \frac{k}{Ee} \right) \left| \frac{Q_{\min}^2}{Q^2} \right| \right].$$

$$\sigma_{\gamma^* A \rightarrow VA}(W, Q^2) = f(M_V) \sigma(W, Q^2 = 0) \left(\frac{M_V^2}{M_V^2 + Q^2} \right)^n$$

$$n = c_1 + c_2(Q^2 + M_V^2),$$

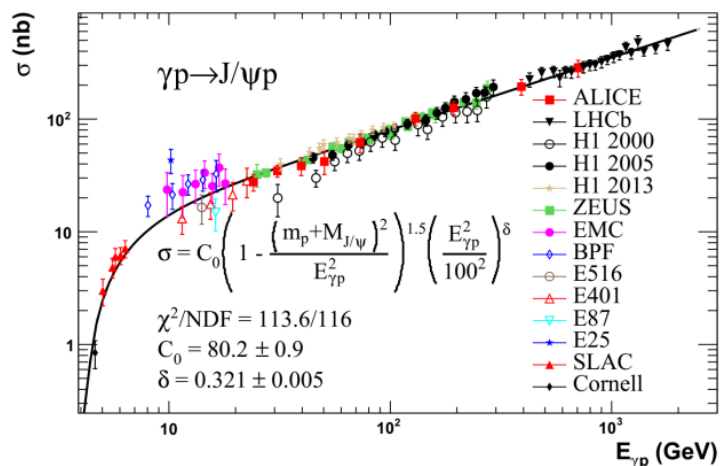
$$\sigma(W, Q^2 = 0) = \int_{t_{\min}}^{\infty} dt \frac{d\sigma(\gamma A \rightarrow VA)}{dt} \Big|_{t=0} |F(t)|^2,$$

event observable reconstruction

$$W_{\gamma p} = \sqrt{m_p^2 + 2m_p E_\gamma}, \quad E_\gamma = \frac{M_V}{2} e^{-y}, \quad x = \frac{M_V e^y}{2E_N},$$

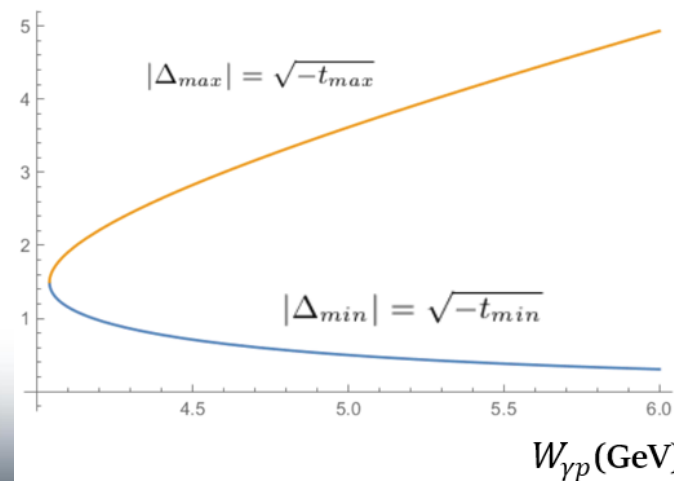
$$Q^2 = -q^2 = -(l - l')^2, \quad t = -(p' - p)^2$$

All of them could be precisely measured!



pQCD motivated expression fitting of exist experimental data for $\sigma_{\gamma p \rightarrow J/\psi p}$

Z. Cao et al., CPC 43 (2019) 064103

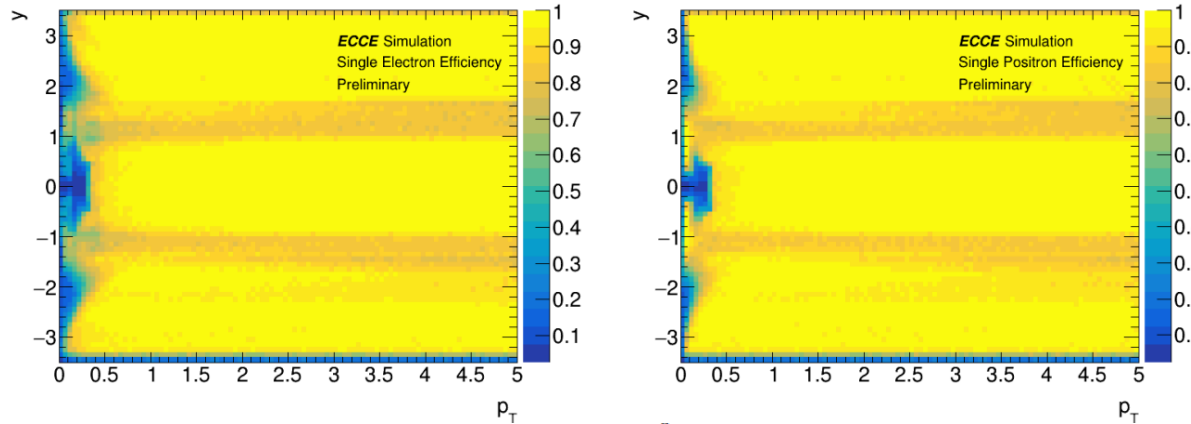


t limitation when center of γp mass is close to J/ψ threshold

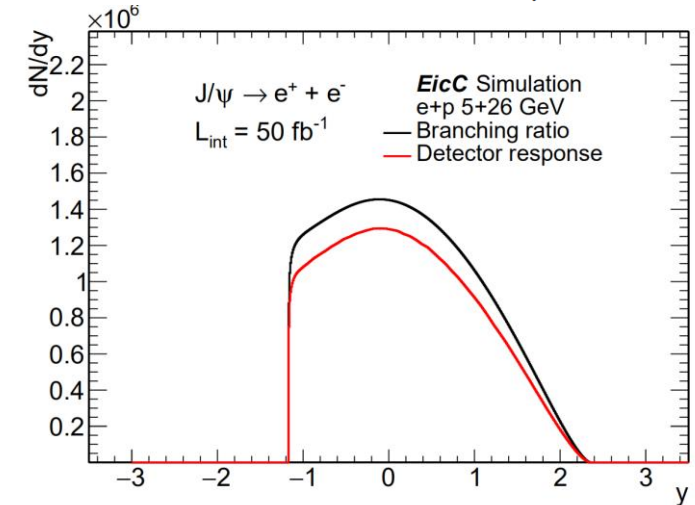
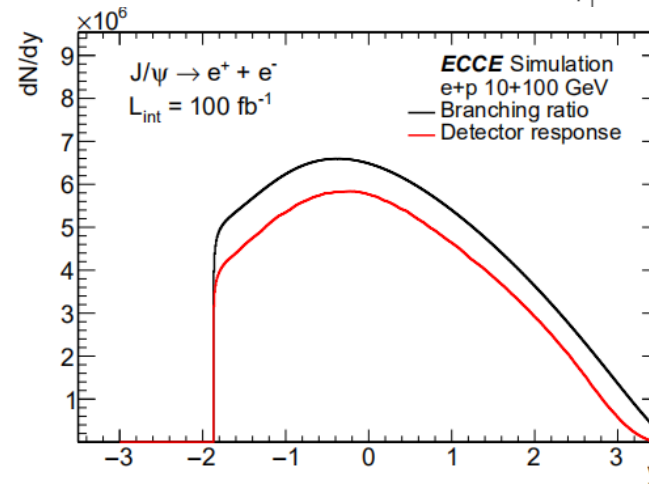
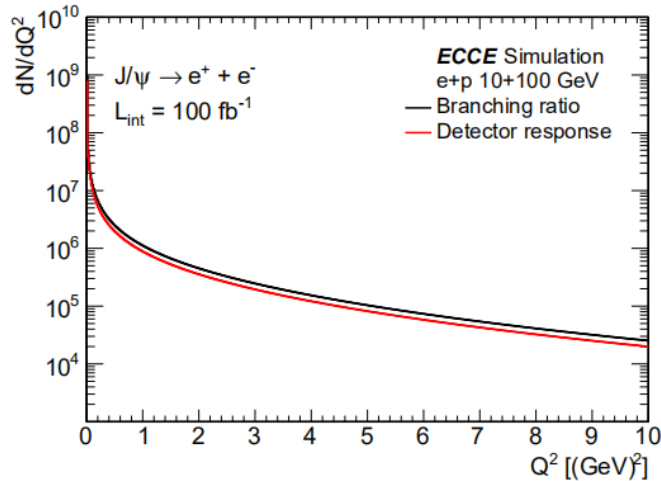
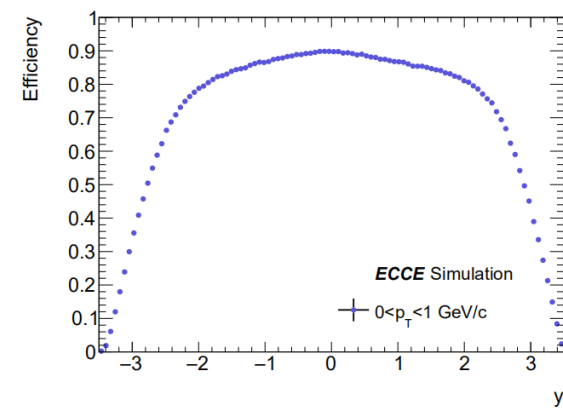
Differential yield prediction

A prediction for the yield of J/ψ photoproduction at EIC (EicC) with fast efficiency correction.

Single track efficiency. Left Panel: e^- efficiency. Right Panel: e^+ efficiency



J/ψ tagging efficiency



- ❑ Results for more beam energy sets could be found in Backup.
- ❑ Amounts of photo-produced J/ψ would be measured at EIC and EicC.
- ❑ Anticipated $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ luminosity on HIAF.

[X. Li et al., NIMA 1048 \(2023\) 167956](#)

Probe nuclear gluon profile

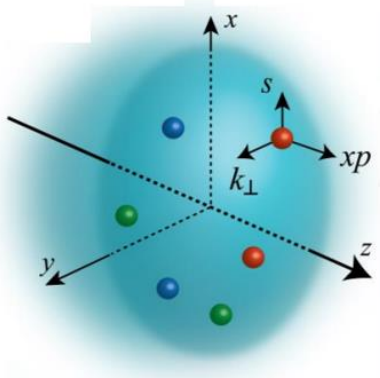
The powerful probe of nuclear gluon multi-dimensional distributions:

Generalized transverse momentum dependent parton distributions (GTMDs) / Wigner Function

5D Dist.

Generalized Parton Dist. (GPDs)

Transverse Momentum Dep.
Dist. (TMDs)

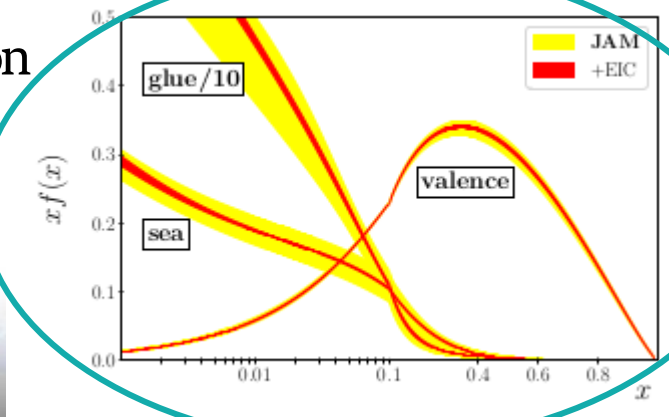


$$f_1^u(x, k_T)$$

$$h_1^u(x, k_T)$$

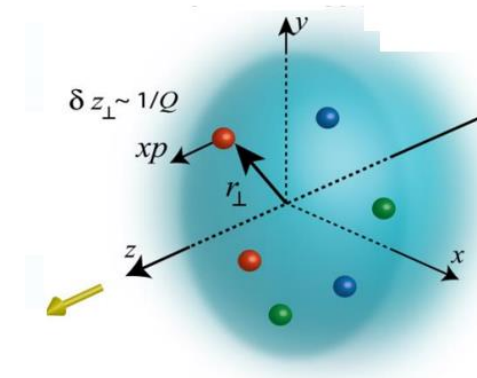
"3D" imagining

Parton Distribution
Functions (PDFs)
x is available.



$$d^2k_T$$

GPD



Fourier transform

$$f(x, b, Q^2) \equiv \int \frac{d^2\Delta}{(2\pi)^2} e^{-i(\Delta b)} \text{GPD}(x, t = -\Delta^2, Q^2)$$

Imaging in position space

Probe nuclear gluon profile — PDF

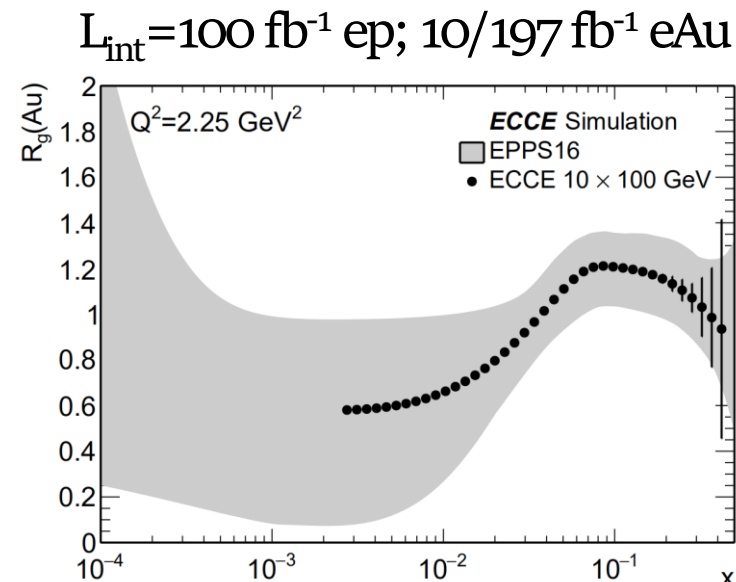
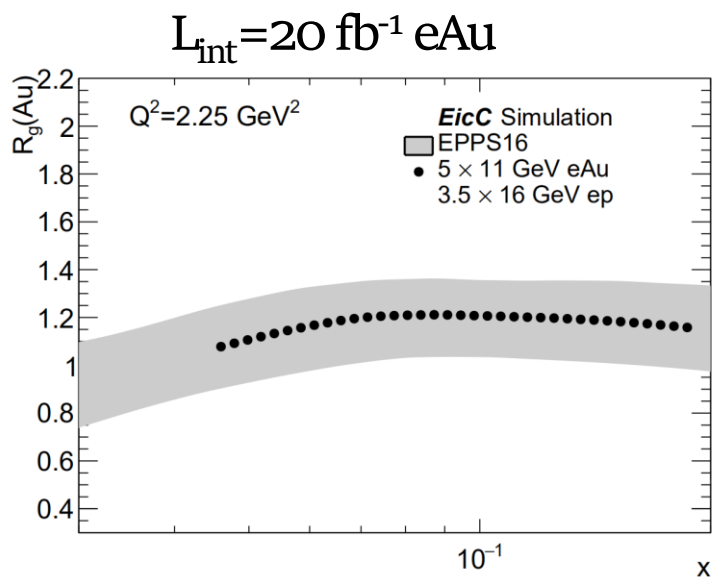
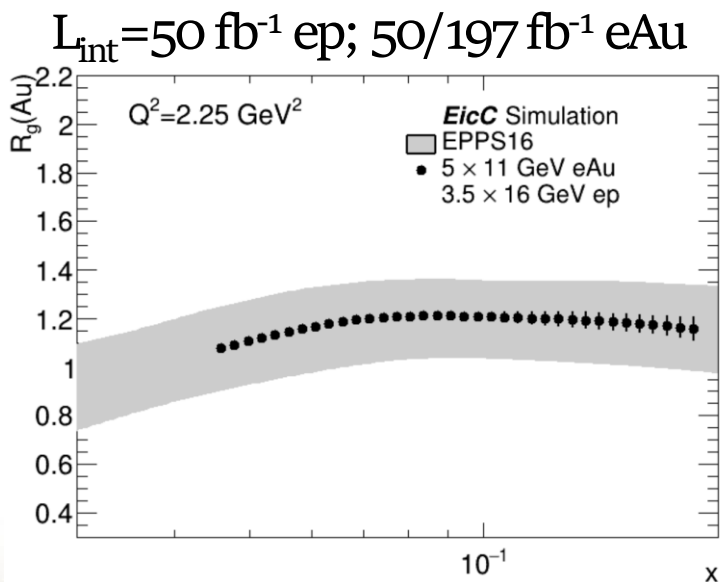
Nuclear parton distribution functions (**nPDF**) describe the behavior of bound partons in the nucleus. (Recently gluon shadowing exhibited by **J/ψ photoproduction** data from LHC have little impact on it.)

B. Abelev, et al., PLB 718 (4) (2013) 355 1273–1283.

V. Khachatryan, et al., PLB 772 (2017) 489–511

$$\left. \frac{d\sigma(\gamma A \rightarrow VA)}{dt} \right|_{t=0} = \frac{\alpha_s^2 \Gamma_{ee}}{3\alpha M_V^\xi} 16\pi^3 [xg_A(x, \mu^2)]^2$$

$$R_g = \sqrt{\frac{\left. \frac{d\sigma(\gamma A \rightarrow VA)}{dt} \right|_{t=0}}{\left. \frac{d\sigma(\gamma p \rightarrow Vp)}{dt} \right|_{t=0}}}$$



- One of the advantages of photon gluon fusion to extract PDF is that low x is dominated by gluons (significant constrain power)

X. Li et al., NIMA 1048 (2023) 167956

- Little is known about anti-shadowing at $x \sim 0.1$. x could down to 5×10^{-4} for ep 18+275

Probe nuclear gluon profile — GPD

unpolarized gluon GPD

$$q(x, b_T) = \int \frac{d^2\Delta_T}{(2\pi)^2} H_q(x, \xi = 0, \Delta_T^2) e^{-i\Delta_T \cdot b_T},$$

$$F(b) = \frac{1}{2\pi} \int_0^\infty d\Delta \cdot \Delta J_0(\Delta b) \sqrt{\left. \frac{d\sigma_{\text{coherent}}}{d|t|}(\Delta) \right|_{\text{mod}}}$$

t-spectra

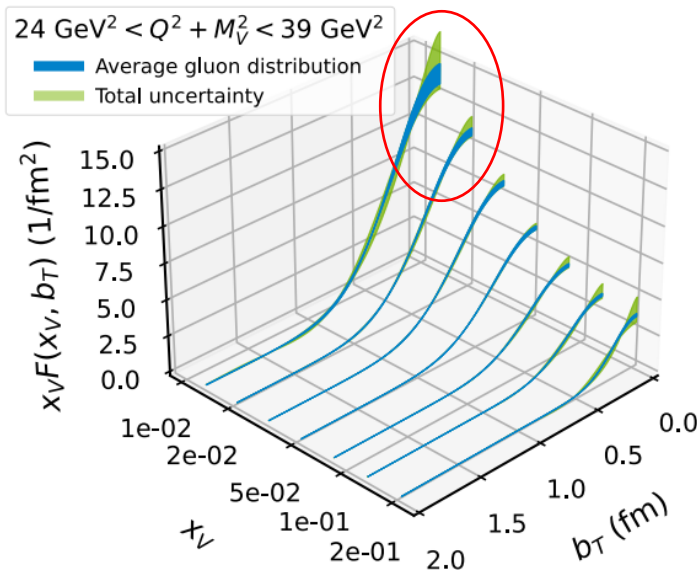
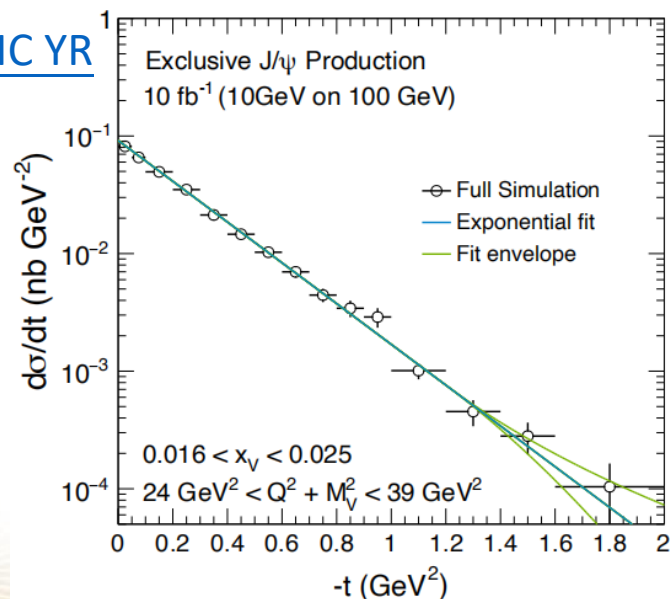
Only possible at an EIC:
from the valence region
deep into the sea!

Normalized
average gluon
density

Hard scale: $Q^2 + M_V^2$

Modified Bjorken-x: $x_V = \frac{Q^2 + M_V^2}{2p \cdot q}$

From EIC YR



- ★ **Remarks:**
- ★ Simplest possible GPD extraction
 - ★ Intrinsic systematic uncertainty due to **extrapolation** outside of measured *t*-range
 - ★ **NLO effects** could be significant
 - ★ Corrections expected to be smaller for *Y*(1*s*) than for *J/ψ*

Slide from S. Joosten

High suppression ratio of coherent to incoherent should be guaranteed for measurements of coherent process to probe nuclear shape or structure! (coherent/incoherent > 500)

Probe nuclear gluon profile — t distribution

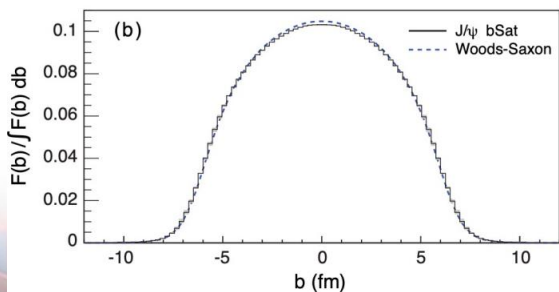
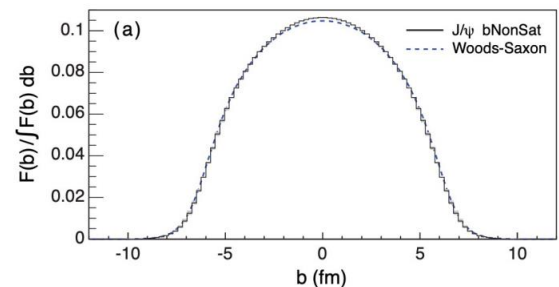
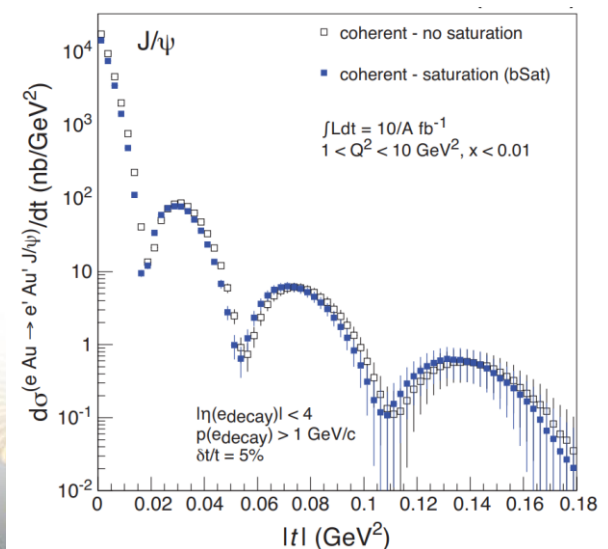
- ❑ Exclusive and diffractive vector meson production as a golden channel to precisely probe t
- ❑ Several methods have been investigated to reconstruct t when scattered ion beam is invisible

Exact (E):	$-t = -(\mathbf{p}_e - \mathbf{p}_{e'} - \mathbf{p}_{VM})^2 = -(\mathbf{p}_A' - \mathbf{p}_A)^2$
Approximate (A):	$-t = (p_{T,e'} + p_{T,VM})^2$
Exclusivity corrected (L):	$-t = -(\mathbf{p}_{A',corr} - \mathbf{p}_A)^2,$

where $\mathbf{p}_{A',corr}$ is constrained by exclusive reaction.

Besides the slope for t distributions, the shape is also sensitive to gluon spatial distributions.

EIC YR, Toll & Ullrich (2012)



From EIC Yellow Report (YR), the best method is **method L**:

- t resolution is sensitive to momentum spread beam effect at low t close to t_{min} .
- More precise than Method A for electroproduction.

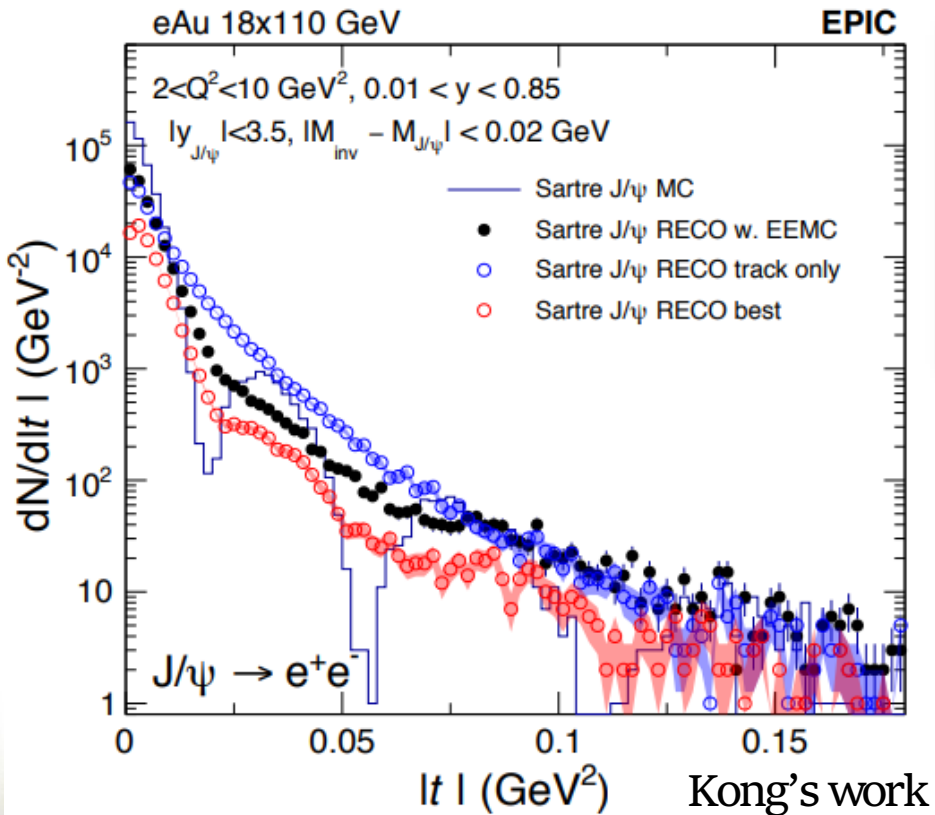
[EIC YR](#)

From Kong's slide in DIS 2023

Probe nuclear gluon profile — t distribution

- First full ePIC simulation (current ePIC detector) in an unified and modern software framework (2023).
- Bottle neck is scattered electron detection.
- State of the art theoretical study from EIC theory group for the smearing of the dips (**Coulomb interaction**).

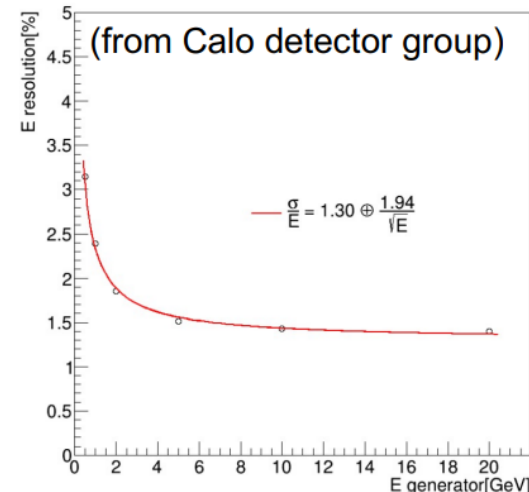
X. Roca-Maza et al., PRC 78 (2018) 044332



Legend details:

- w. EEMC, electron energy from EEMC, angle from tracking
- Track only: all from tracking
- Best: average of the above 2 E-by-E

~ 1.5% energy resolution for EEMC

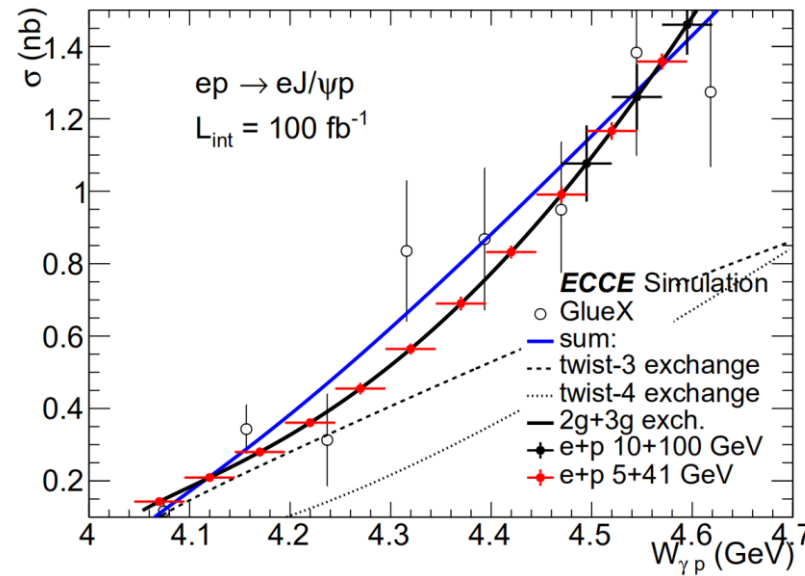
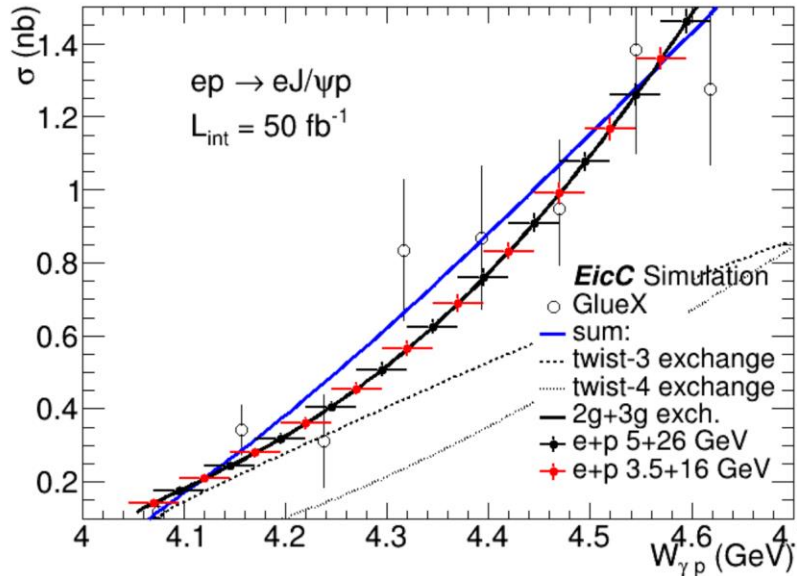


- For lower electron energy, there will be longer transit time through the nucleus for the coulomb interaction.
- Generally we thought the **lifetime** of the dipole is longer than the **transit time** (fixed configuration).

Near-Threshold Production Mechanism

- 2g+3g is still used to describe the GlueX data in YR.
- Higher-mass charmonium states C-even χ_c with 3g exchange.
- EIC, EicC and (JLab) can dramatically improve the statistics near threshold to optimize models

[X. Li et al., NIMA 1048 \(2023\) 167956](#)



- ❑ The uncertainty of the prediction (red and black points) is obviously smaller than the discrepancy between models. (more beam configuration choices for EicC)
- ❑ Further study should focus on the problem: find a kinematic region to separate the gluon exchange, open-charm exchange, or any other contribution.

New power law twist 3+4 form factor, 5?

$$\frac{d\sigma}{dt} \Big|_{(-t) \gg \Lambda_{QCD}^2} = \frac{1}{16\pi (W_{\gamma p}^2 - M_p^2)^2} (|\overline{\mathcal{A}}_3|^2 + |\overline{\mathcal{A}}_4|^2)$$

$$\approx \frac{1}{(-t)^4} \left[(1 - \chi) \mathcal{N}_3 + \tilde{m}_t^2 \mathcal{N}_4 \right],$$

[P. Sun et al., PLB 822 \(2021\) 136655](#)

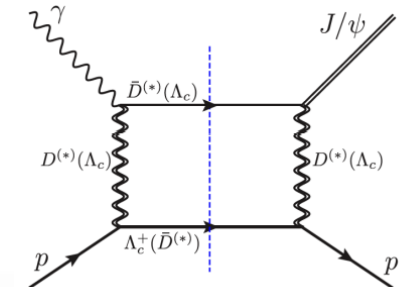
2g+3g C-odd and C-even

$$\frac{d\sigma}{dt} = \mathcal{N}_{2g} v \frac{(1-x)^2}{R^2 \mathcal{M}^2} F_{2g}^2(t) (W_{\gamma p}^2 - m_p^2)^2$$

$$\frac{d\sigma}{dt} = \mathcal{N}_{3g} v \frac{(1-x)^0}{R^4 \mathcal{M}^4} F_{3g}^2(t) (W_{\gamma p}^2 - m_p^2)^2$$

[S.J. Brodsky, et al., PLB 498 \(2001\) 23–28](#)

alternative production mechanism!



Open charm exchanges.

Possible pentaquark state?

Proton shape and mass structure

- The latest measurements of this process carried out by JLab to answer the fundamental questions of proton mass radius and mass structure. *Z.-E. Meziani et al., Nature 615 (2023) 813–816*
- EIC, EicC and JLab (CLAS 12 with upgrade and SoLID) are promising to further address on them.
- Although no direct relationship with gravitational form factor (GFF), theorists insist the forward amplitude is an important observable to understand mass decomposition.

$$\frac{d\sigma}{dt} = \frac{1}{64\pi s} \frac{1}{|p_{\gamma cm}|^2} (Q_e c_2)^2 \left(\frac{16\pi^2 M}{b}\right)^2 G(t)^2, \quad \langle r_m^2 \rangle = \frac{6}{M} \frac{dG}{dt} \Big|_{t=0} = \frac{12}{m_s^2}$$

$$M_N = M_m + M_q + M_g + M_a$$

Ji, PRD 52 (1995) 271; Hatta and Yang, PRD 98 (2018) 074003

$$T_\mu^\mu = \underbrace{\frac{\tilde{\beta}(g)}{2g} G^2}_{\text{Trace Anomaly}} + \underbrace{\sum_{q=u,d,s} m_q (1 + \gamma_m) \bar{\psi}_q \psi_q}_{\text{Light Quark Mass}}$$

$$M_m = \frac{4 + \gamma_m}{4(1 + \gamma_m)} b m_p$$

$$M_q = \frac{3}{4} \left(a - \frac{b}{1 + \gamma_m} \right) m_p$$

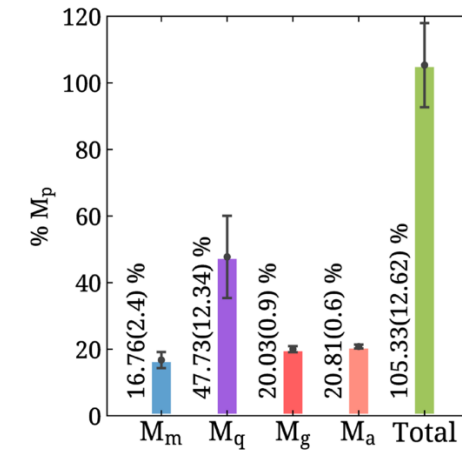
$$M_g = \frac{3}{4} (1 - a) m_p$$

$$M_a = \frac{1}{4} (1 - b) m_p$$

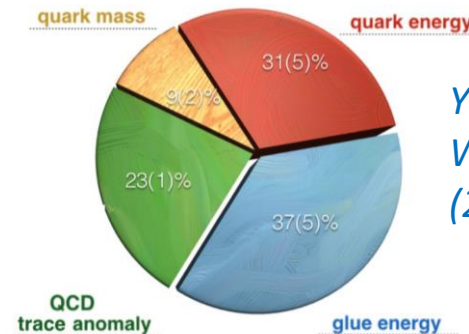
$$\left. \frac{d\sigma_{\gamma N \rightarrow J/\psi N}}{dt} \right|_{t=0} = \frac{3\Gamma(J/\psi \rightarrow e^+ e^-)}{\alpha m_{J/\psi}} \left(\frac{k_{J/\psi N}}{k_{\gamma N}} \right)^2 \left. \frac{d\sigma_{J/\psi N \rightarrow J/\psi N}}{dt} \right|_{t=0}$$

$$\begin{aligned} F_{J/\psi N} &\approx r_0^3 d_2 \frac{2\pi^2}{27} \left(2M_N^2 - \left\langle N \left| \sum_{i=u,d,s} m_i \bar{q}_i q_i \right| N \right\rangle \right) \\ &\approx r_0^3 d_2 \frac{2\pi^2}{27} (2M_N^2 - 2bM_N^2) \\ &\approx r_0^3 d_2 \frac{2\pi^2}{27} 2M_N^2 \boxed{(1 - b)}, \end{aligned}$$

$$\left. \frac{d\sigma_{J/\psi N \rightarrow J/\psi N}}{dt} \right|_{t=0} = \frac{1}{64\pi} \frac{1}{m_{J/\psi}^2 (\lambda^2 - m_N^2)} |F_{J/\psi N}|^2.$$



C. Alexandrou et al., (ETMC), PRL 116, 252001 (2016)



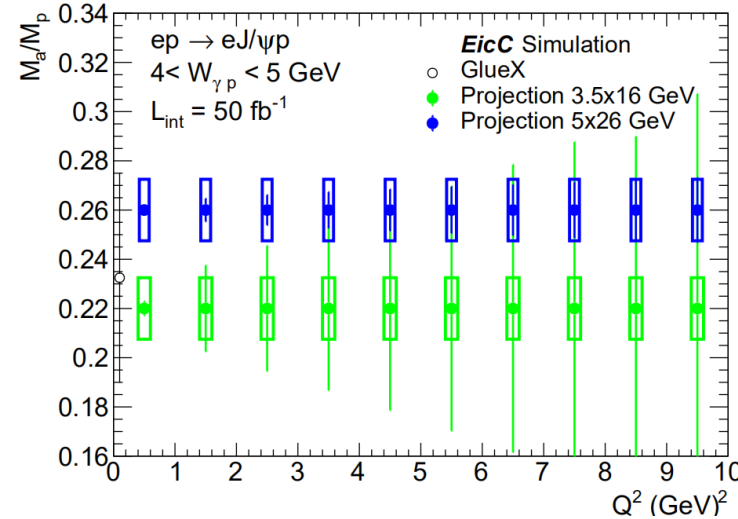
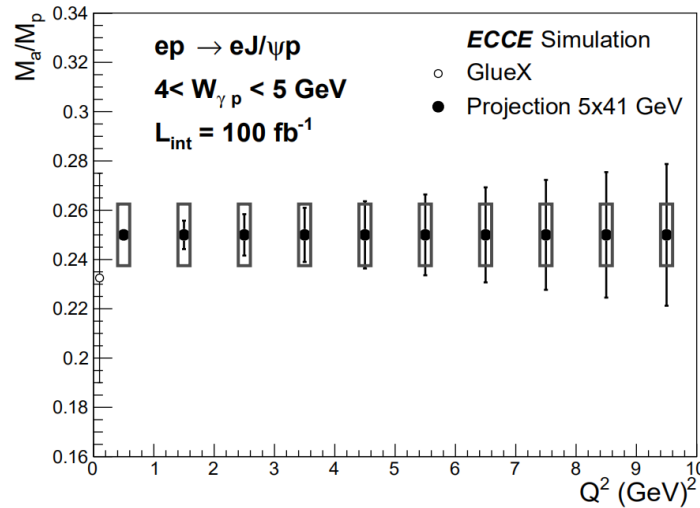
Yi-Bo Yang et al, EPJ Web of Conferences 175, (2018) 14002

Trace anomaly prediction at EIC/EicC

New HMS+SHMS results with dipole GFF fit at JLab (W in 4.36-4.55 GeV) have comparable uncertainty with prediction at W in 4.04-4.29 GeV.

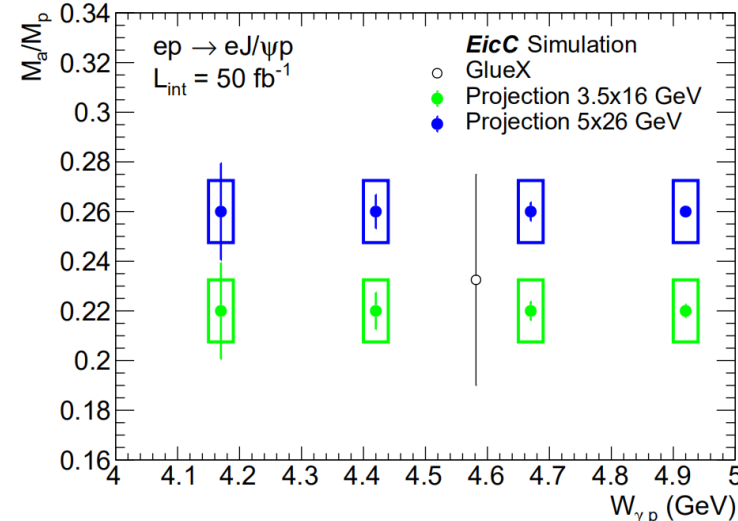
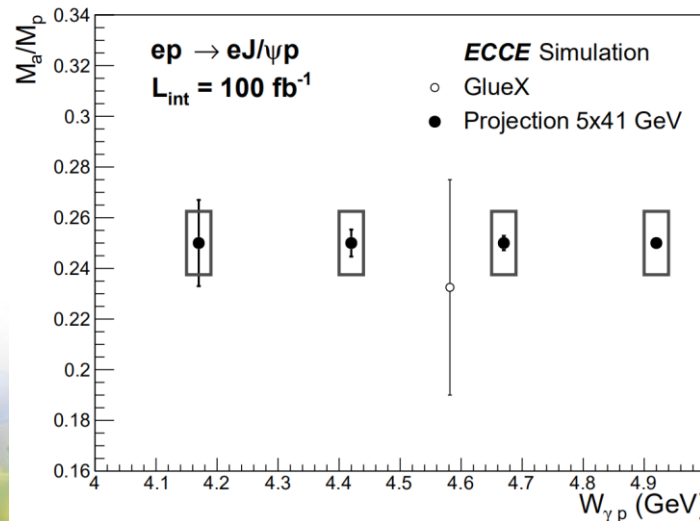
Z.-E. Meziani et al., Nature 615 (2023) 813–816

Q^2 distribution



GlueX data from R. Wang et al., EPJC 80 (2020) 507

W distribution



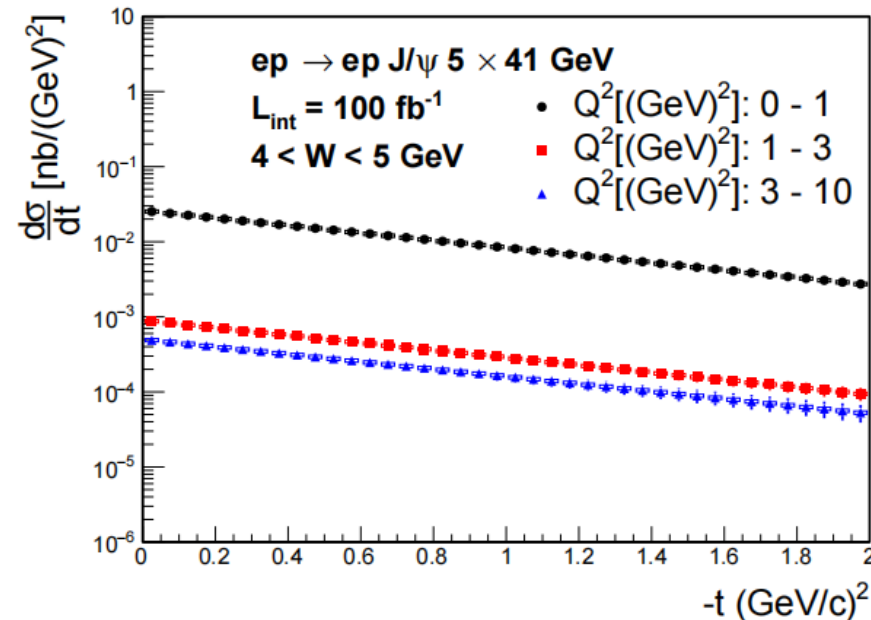
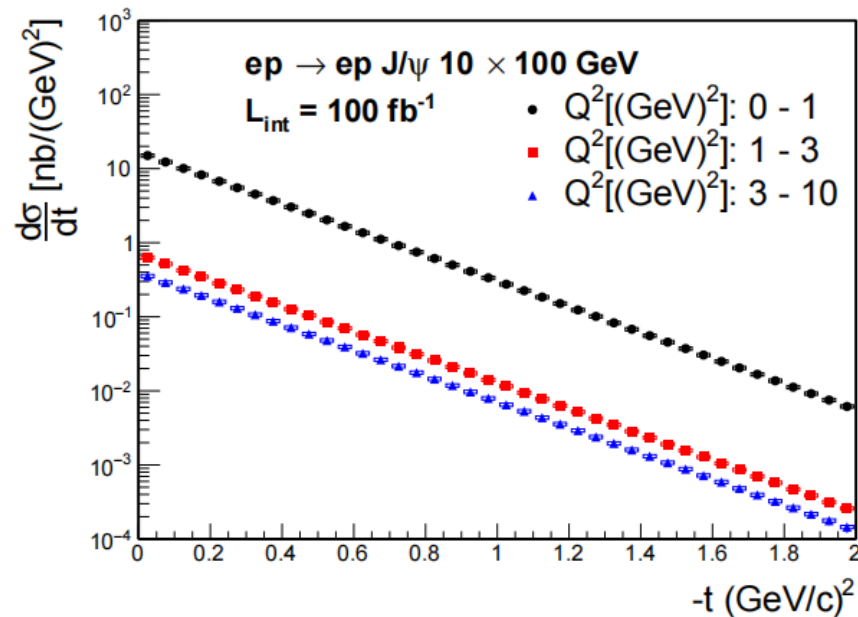
Colliders will cover a wider kinematic region (Q^2 and W) to reduce the model dependence compared with fixed target experiments.

—see next slide

X. Li et al., NIMA 1048 (2023) 167956

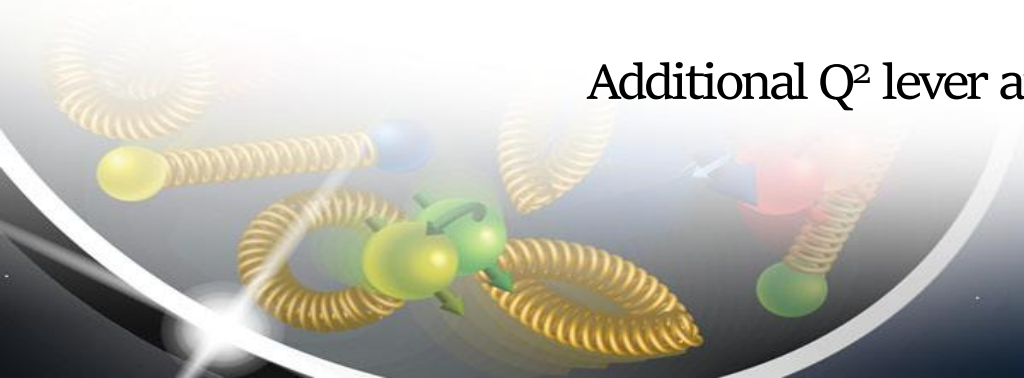
Trace anomaly prediction at EIC/EicC

- ❑ JLab took advantage of two dimensional (t-W) near threshold J/ψ photoproduction measurements.
- ❑ It is possible to do for another two dimensional distribution (t-Q²) at EIC. (parameter a and b in P12 are sensitive to Q²!)
- ❑ Three dimensions ? (W in 4-5 GeV)



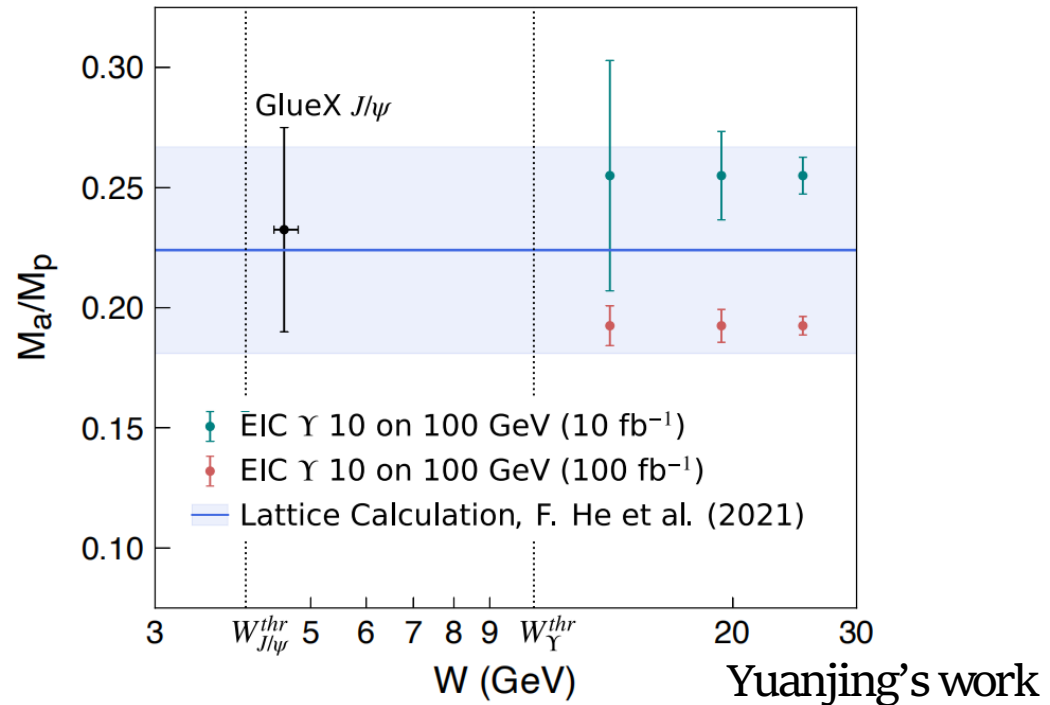
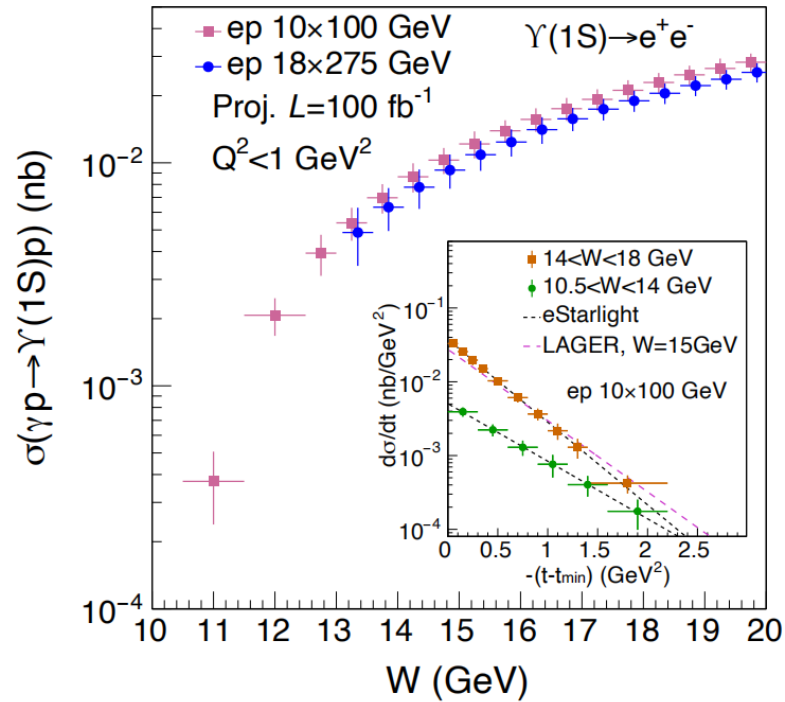
[X. Li et al., NIMA 1048 \(2023\) 167956](#)

Additional Q² lever arm could help further check the models.



Trace anomaly prediction at EIC/EicC

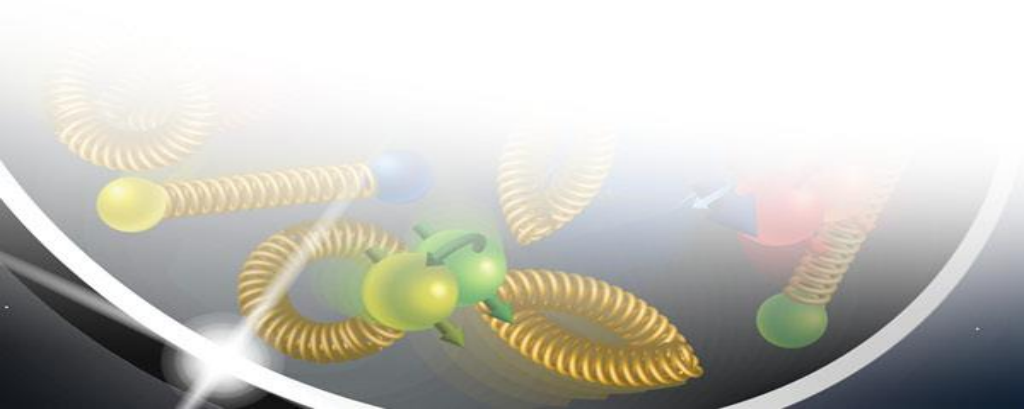
- The measurements of Υ threshold photoproduction will be a strong complementarity for J/ψ programs.
- The larger bottomonium mass leads to negligible uncertainty from higher order corrections.



Uncertainty from Υ near threshold one-year yield at EIC seems comparable to GlueX J/ψ .

Summary

- Quarkonia photoproduction is a powerful probe for the gluonic physics.
- ePIC detector at EIC will cover a wide kinematic region to detect this process with precise measurements of event variables.
- The measurements of this process at EIC have the ability to significantly reduce the model uncertainty on nuclear gluon PDF, GPD, spatial distributions and near-threshold production mechanism and nuclear mass structure.
- EIC will be a bridge between physics related to photoproduction at RHIC/LHC and JLab.

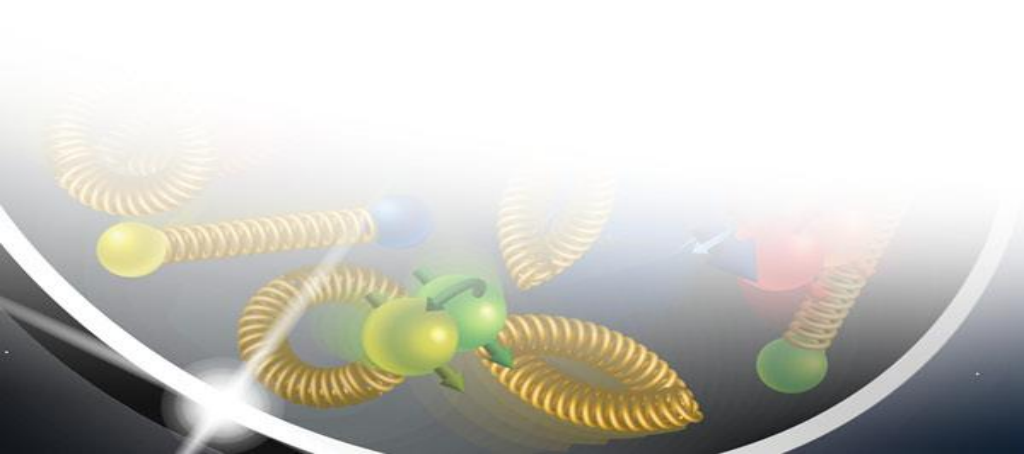


QUESTIONS?

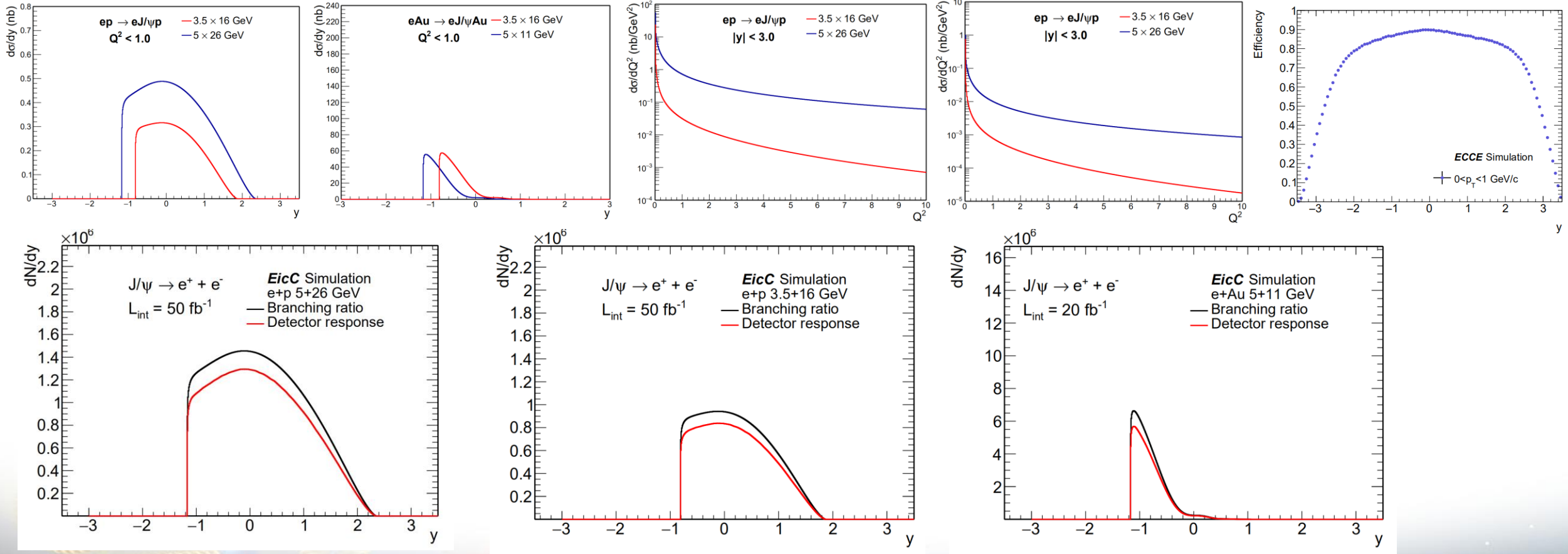




BACK UP



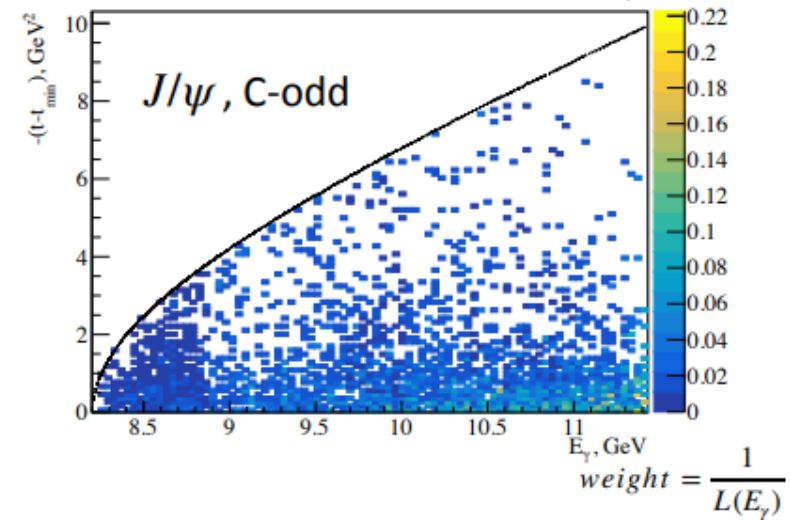
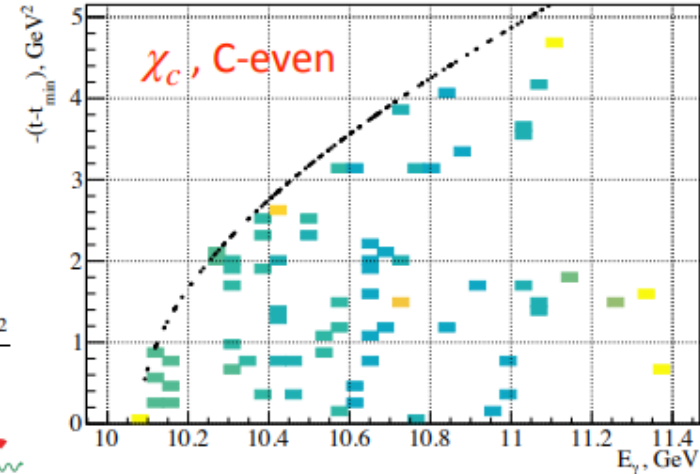
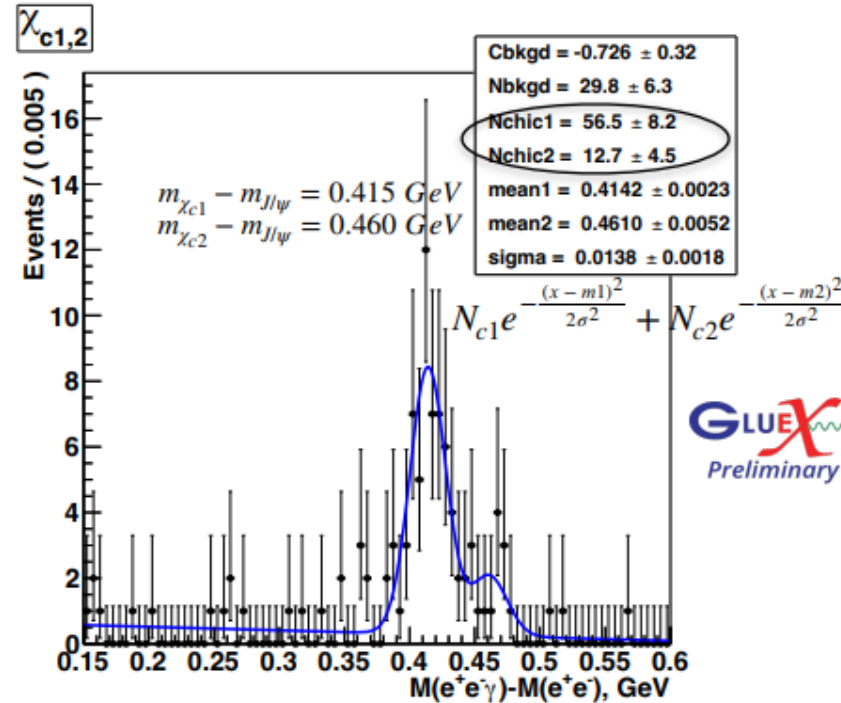
γ and Q^2 dependence



Higher-mass charmonium states with GlueX

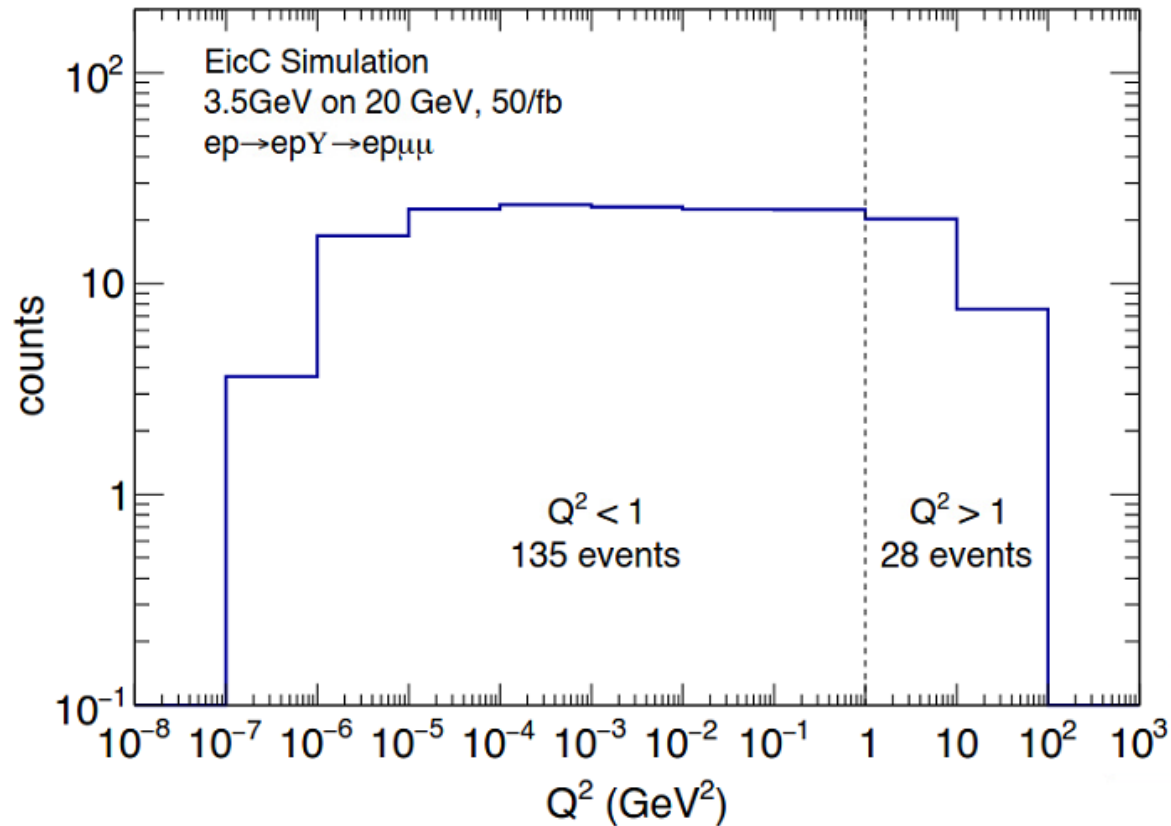
C-odd ($J/\psi, \psi'$) vs C-even (χ_c) production

$$\gamma p \rightarrow \chi_c p \rightarrow (J/\psi \gamma) p \rightarrow (e^+ e^- \gamma) p$$



- $\chi_{c1}(3511)$ and $\chi_{c2}(3556)$, 1^{++} and 2^{++} ($1P$),
 $E_\gamma^{thr} = 10.1 \text{ GeV}$
- C-even charmonium states require 3g-exchange
- Dramatic difference in (E_γ, t) distribution w.r.t J/ψ

Υ experiments at EicC compared



ep 3.5+20 GeV seems perfect for $\Upsilon(1S)$ near threshold due to the center of mass.

Photo-production dominants.

Low statistics.

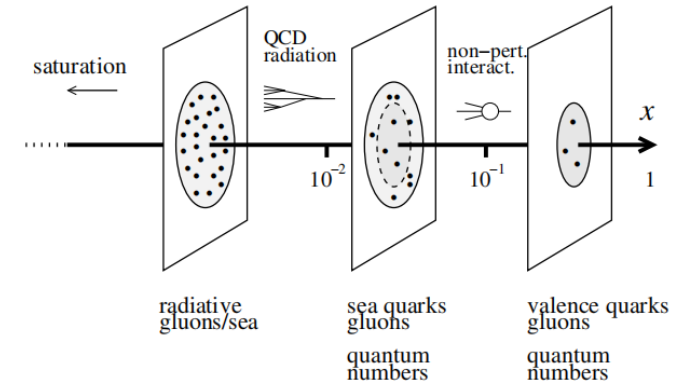
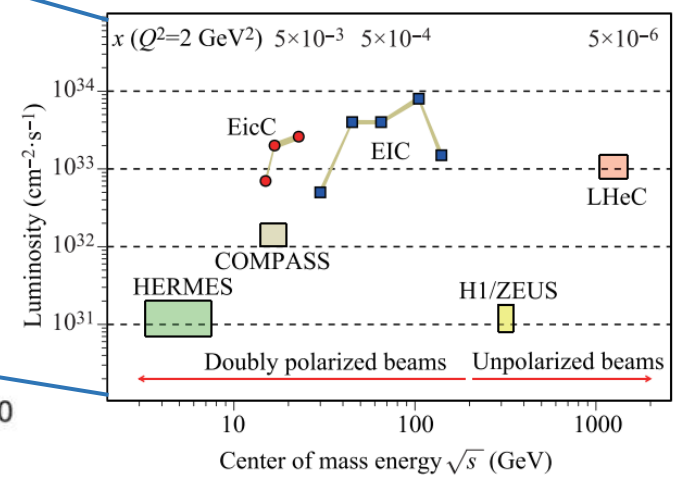
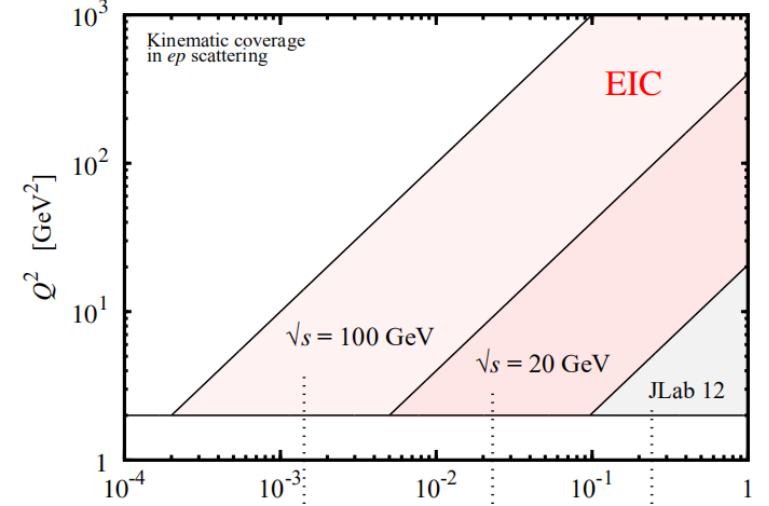
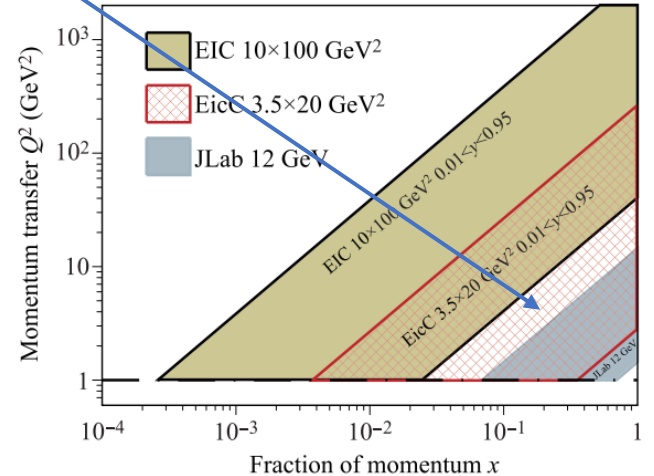
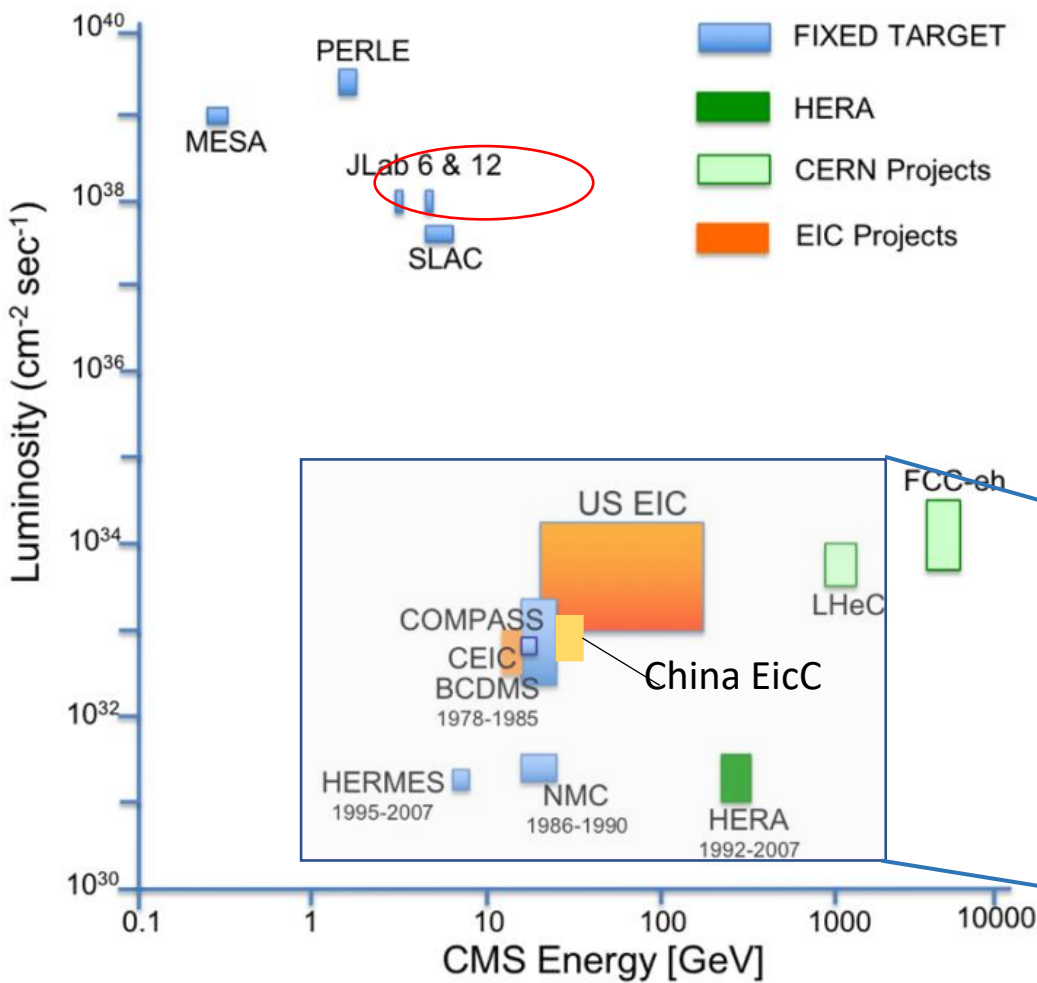
Allow to search beautiful pentaquark!

Figure from S. Jooster's slide ([meeting](#))

Kinematic coverage and nucleon's partonic structure

What physics should be important here?

$\sqrt{s}_{sep} = 28 - 140$ GeV at EIC 15-20 GeV at EicC



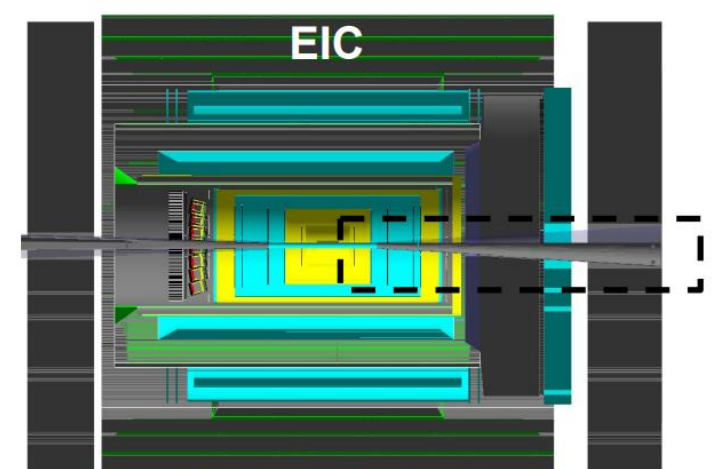
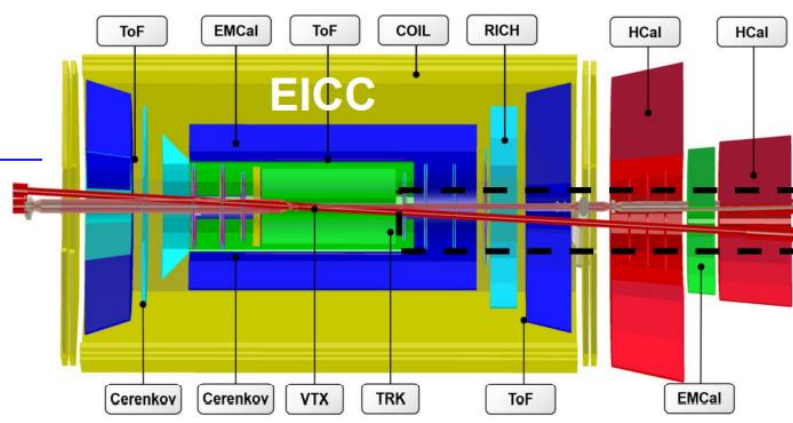
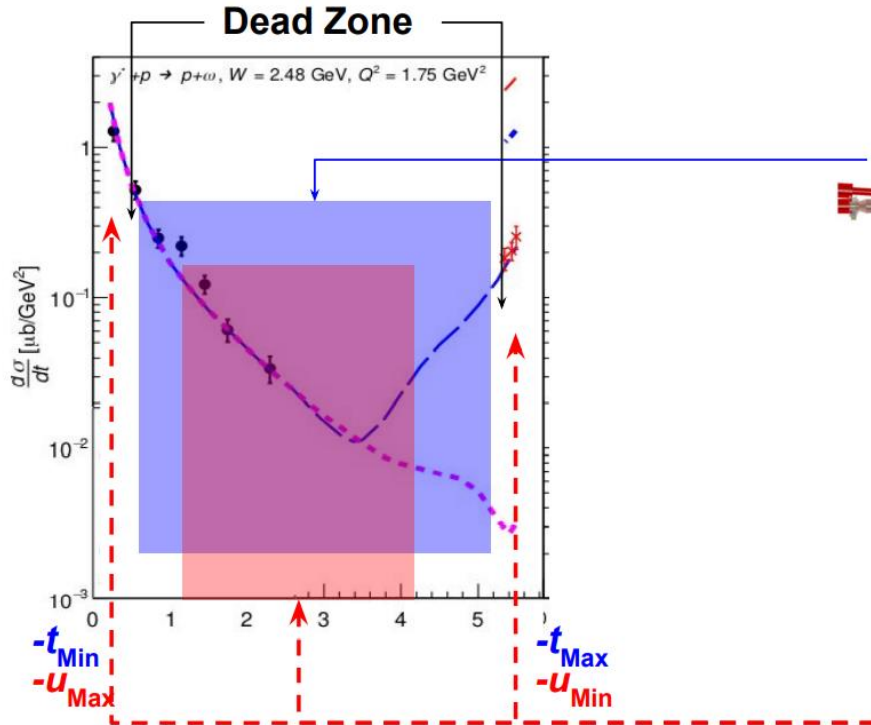
Special physics – Backup angle u-channel

See in Bill Li's presentation: [link](#)

History and physics of this channel: [link](#)

Adv: Larger acceptance of ZDC, 15mrad and kinematic coverage

EIC and EicC Complementarity



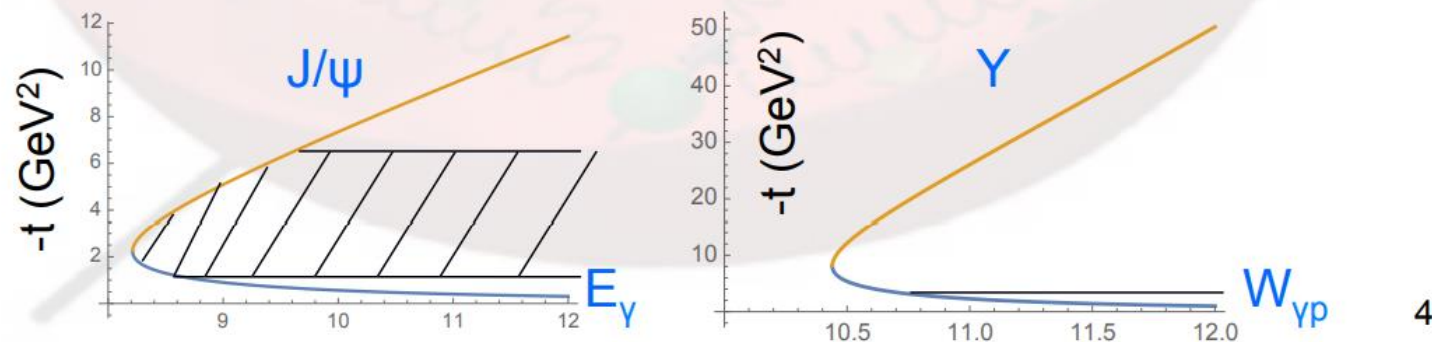
- EIC and EIC should be designed to avoid common dead zone overlap in phasespace. **Studies needed**
- **Angular dependence asymmetry study is possible (needed to extract TDAs)**

Slide from Bill

Materials – gravitational FF (form factor)

This talk focuses on the special kinematics:
large momentum transfer

- We can compute both the cross section and the form factors separately in **perturbative QCD**, then we can check that if there is/not direct connection between the near threshold production and the gluonic gravitational form factors

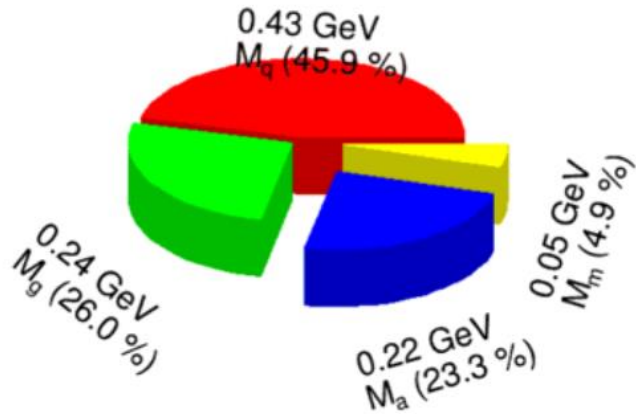


Direct connection?

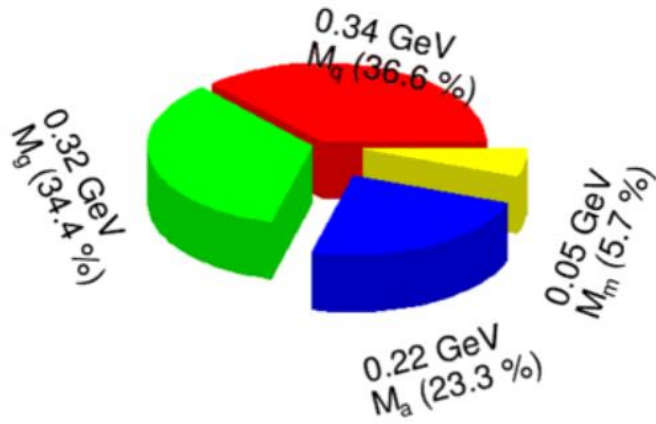
Slide from Feng Yuan

Materials – mass decom. & Q2 limitation

$$\mu^2 = 0.41 \text{ GeV}^2$$



$$\mu^2 = 4.0 \text{ GeV}^2$$



Input interpretation

$$\sqrt{((w + 26)^2 - ((5 - w) \sin(t))^2 - (26 - ((5 - w) \cos(t) + 5))^2)} = 4.04$$

solve

$$2 \times 5 w - 2 \times 5^2 + Q = 2 \times 5 (5 - w) \cos(t)$$

$$Q \geq 0$$

$$w \geq 0$$

$$t \geq 0$$

$$t \leq \pi$$

for

w

Results

Approximate form

$$w = \frac{10201}{65000} \text{ and } Q = 0 \text{ and } t = \pi$$

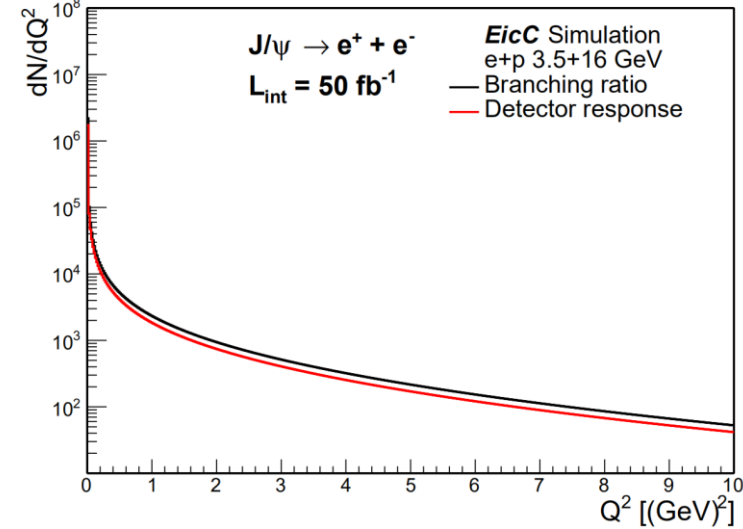
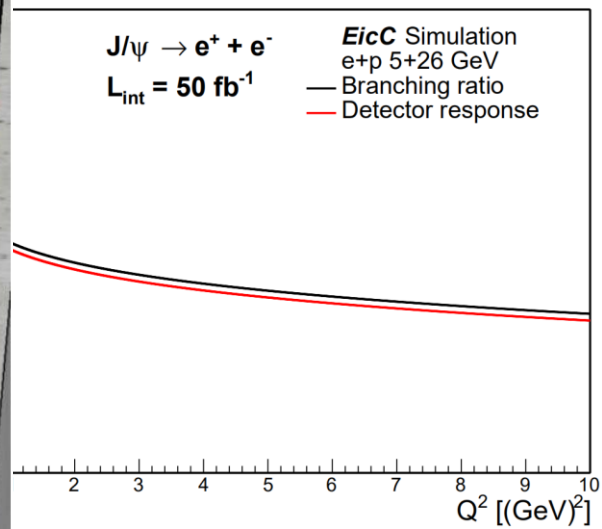
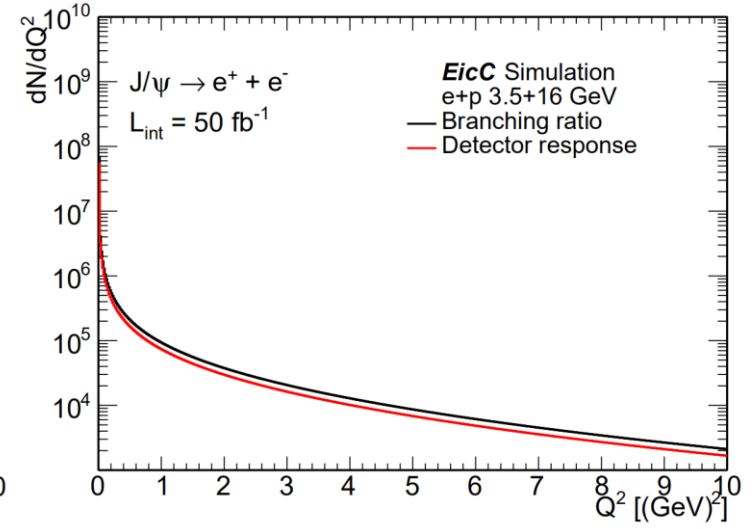
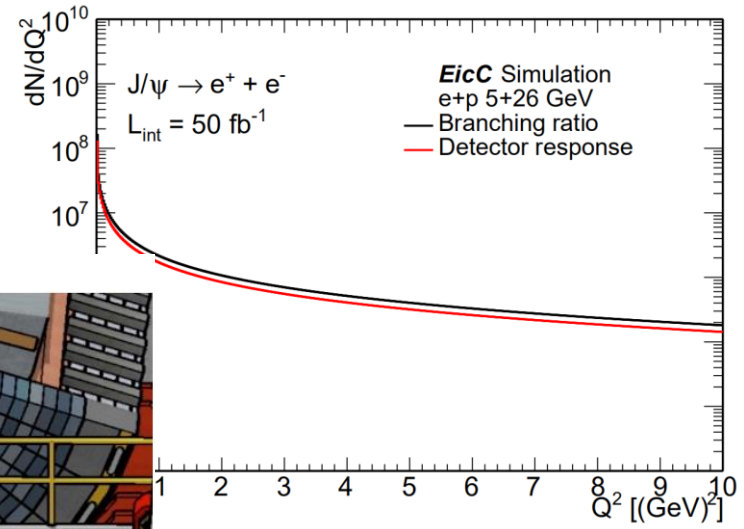
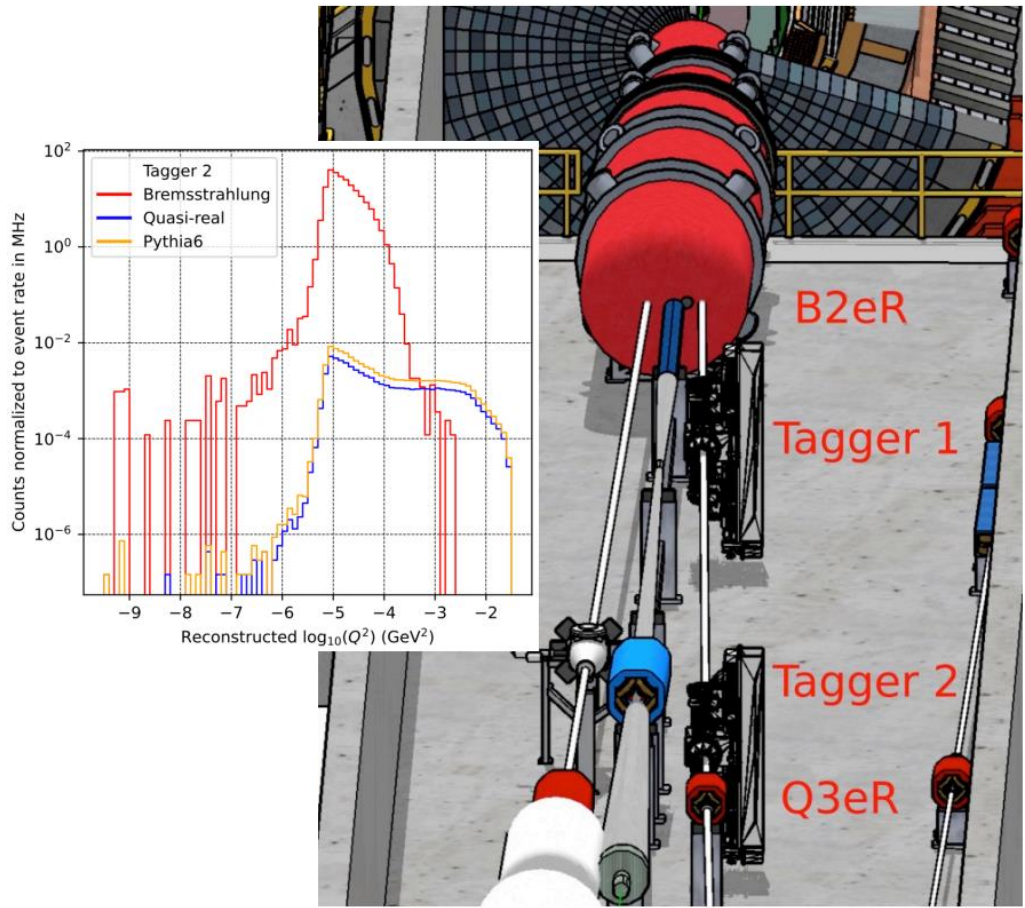
$$w = \frac{10201 - 2625 Q}{65000} \text{ and } 0 < Q \leq \frac{10201}{2625} \text{ and } t = \cos^{-1}\left(\frac{3875 Q - 314799}{2625 Q + 314799}\right)$$

$\cos^{-1}(x)$ is the inverse cosine function

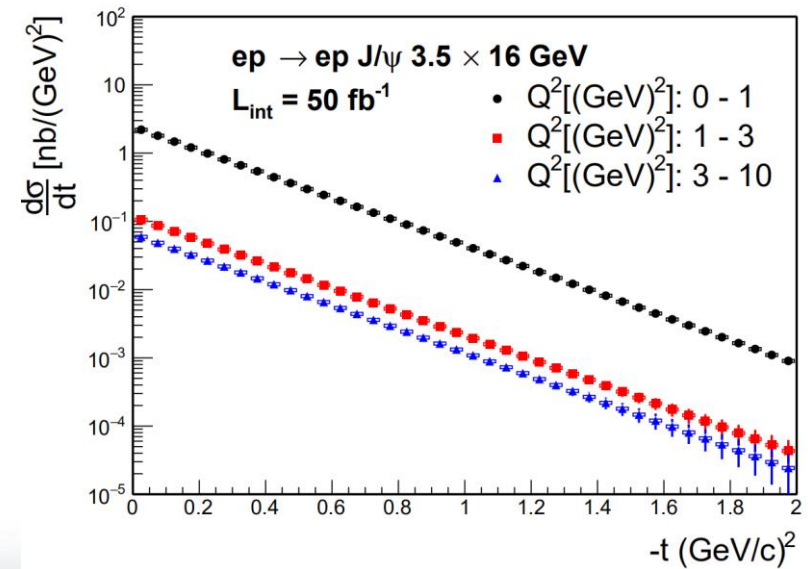
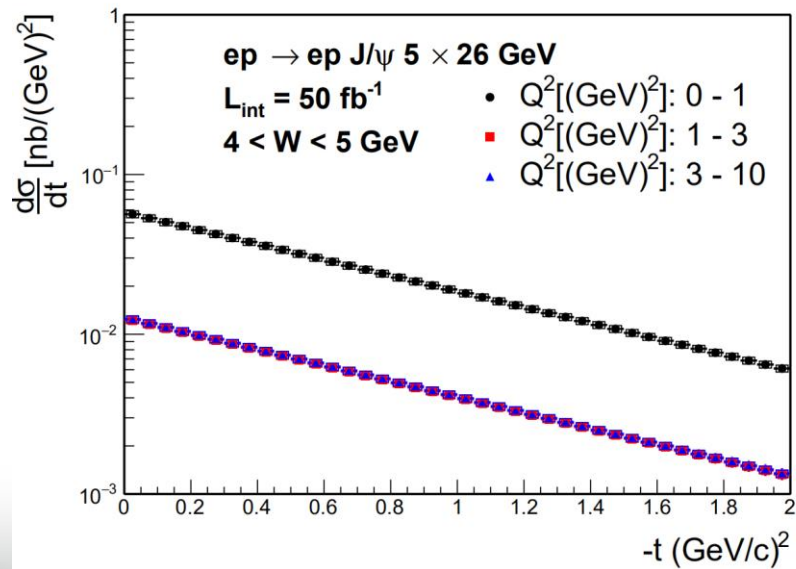
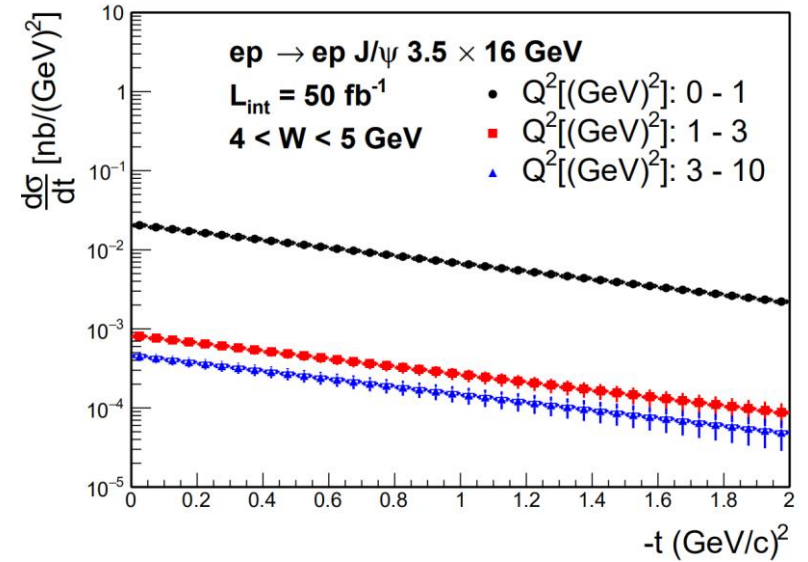
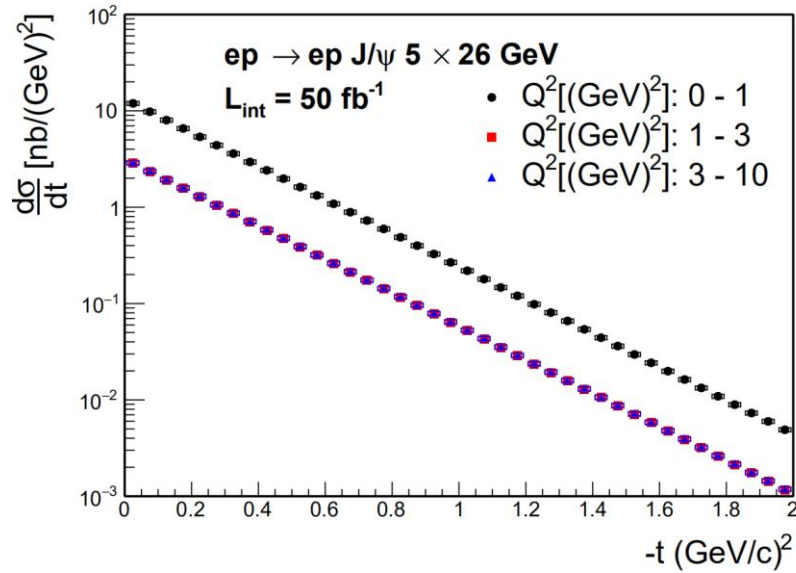
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Materials



Materials



Materials – EPIC (EIC)

News: voted logo!; New simulation framework (in process - EICrecon)



At EIC:

Asymmetric system: no two photon sources interference [more statistics at low t , baseline]
Coulomb dissociation should be suppressed due to the limited EM field by electron side.
Low momentum fraction x “Gluon sea” will enhance the cross section.