



*Università degli Studi di Firenze*



# **Coevolution of AGN, BHs and their host galaxies: the observational foundations**

*Beijing international summer school*

*“The physics and evolution of AGN”*

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# Outline of lectures

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- ★ Part 1: *Supermassive black holes in galactic nuclei: detections and mass measurements* (2 lectures)
- ★ Part 2: *Scaling relations between black holes and their host galaxies* (2 lectures)
- ★ Part 3: *The cosmological evolution of AGN and BHs* (2 lectures)
- ★ Part 4: *The observational signatures of coevolution* (2 lectures)



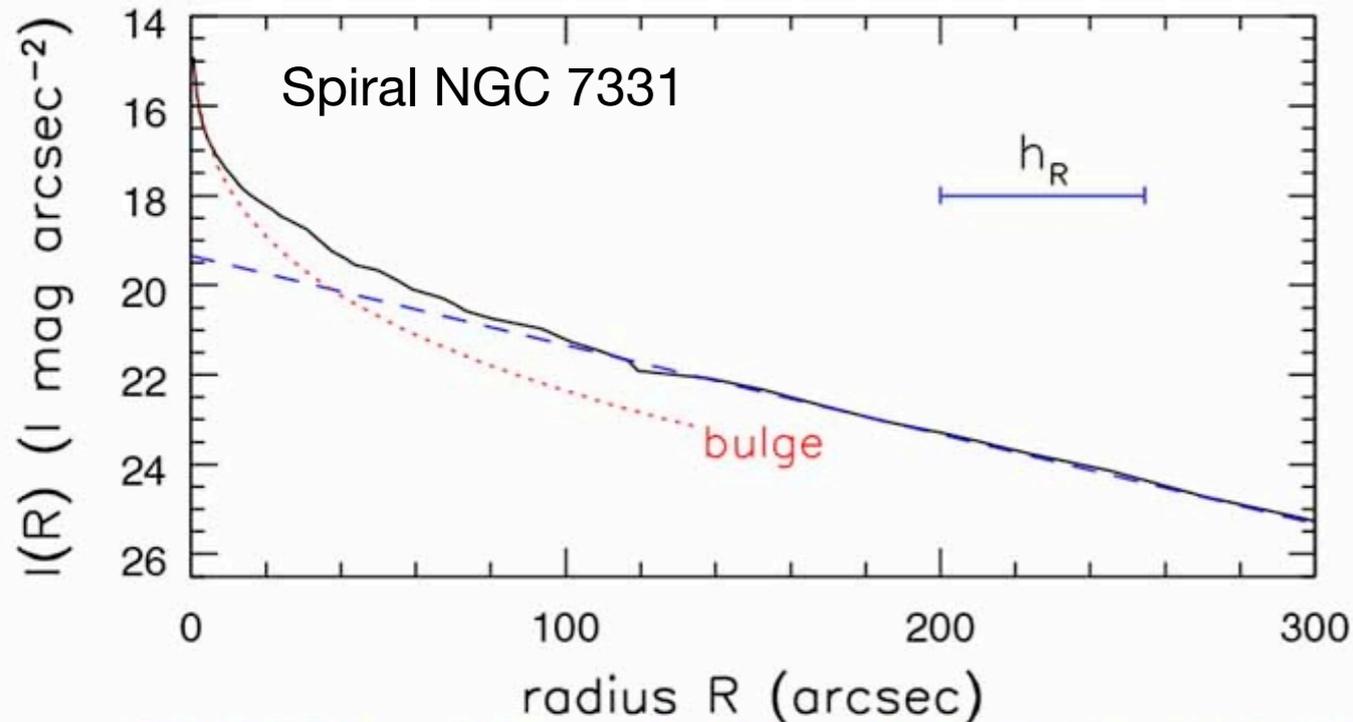
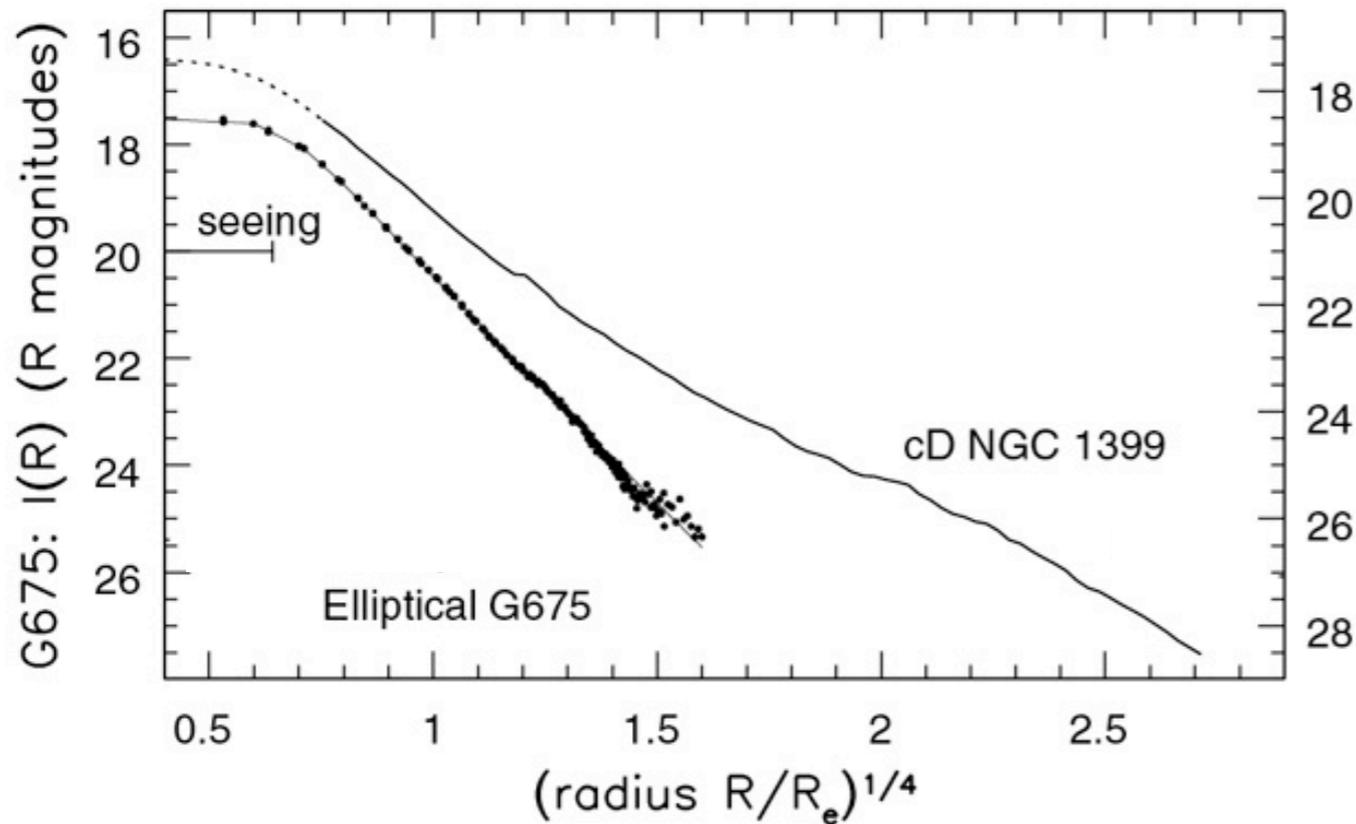
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# **Part 2: scaling *relations between BHs and host galaxies***

# Galaxy structural parameters

Surface brightness profiles of galaxies:



Ellipticals

★ Sersic profile

$$\Sigma(R) = \Sigma_e \exp\{-b_n[(R/R_e)^{1/n} - 1]\}$$

Spirals

★ Bulge: Sersic profile

★ Disk: exponential profile

$$\Sigma_b(R) = \Sigma_e \exp\{-b_n[(R/R_e)^{1/n} - 1]\}$$

$$\Sigma_d(R) = \Sigma_0 \exp\{-(R/h_R)\}$$

Spheroids (Ellipticals or bulges)

★  $\Sigma_e$ ,  $R_e$ ,  $n$  are “structural parameters”

★  $\sigma_e$  (L weighted velocity dispersion with  $R_e$ ),  $L_e$  (L within  $R_e$ ) are another structural parameter

# The Fundamental Plane

There exist several relations among scaling parameters like

★  $R_e - \Sigma_e$  Kormendy relation

★  $\sigma_e - L_e$  Faber-Jackson relation

These relations are just the projection of a 3-variate relation which is called the Fundamental plane of elliptical galaxies (spheroids)

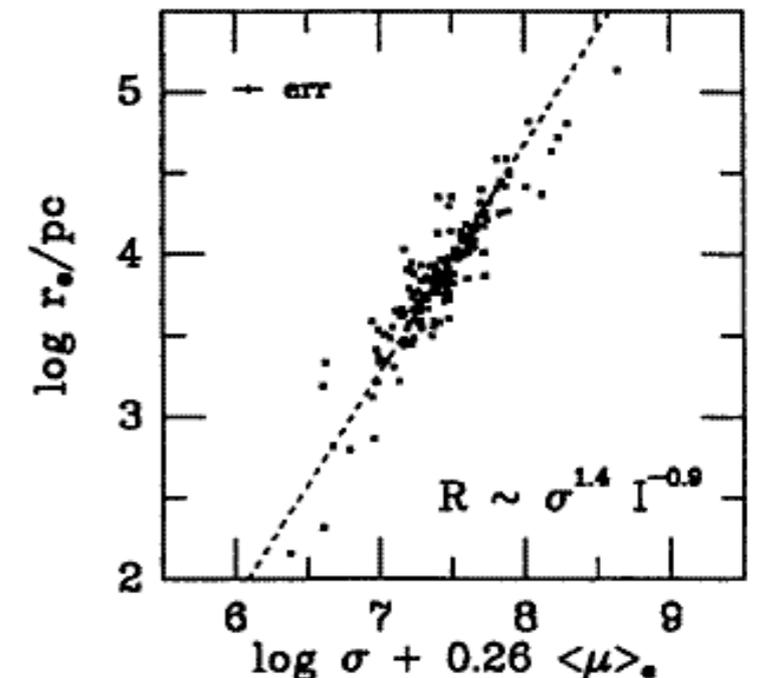
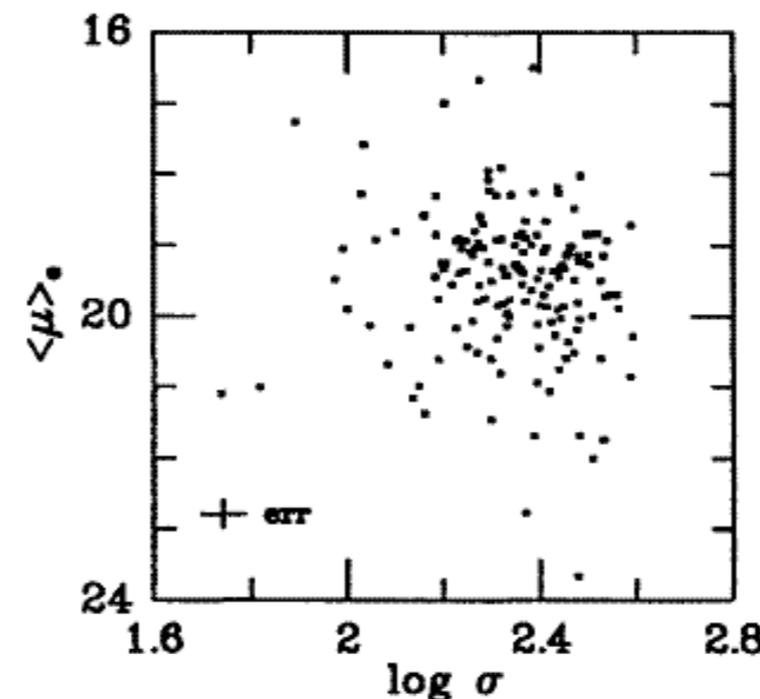
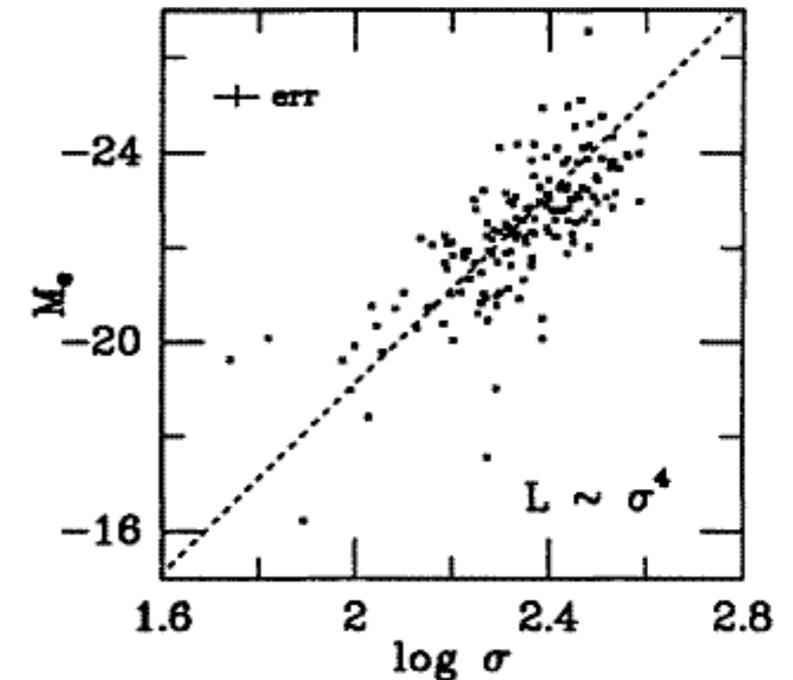
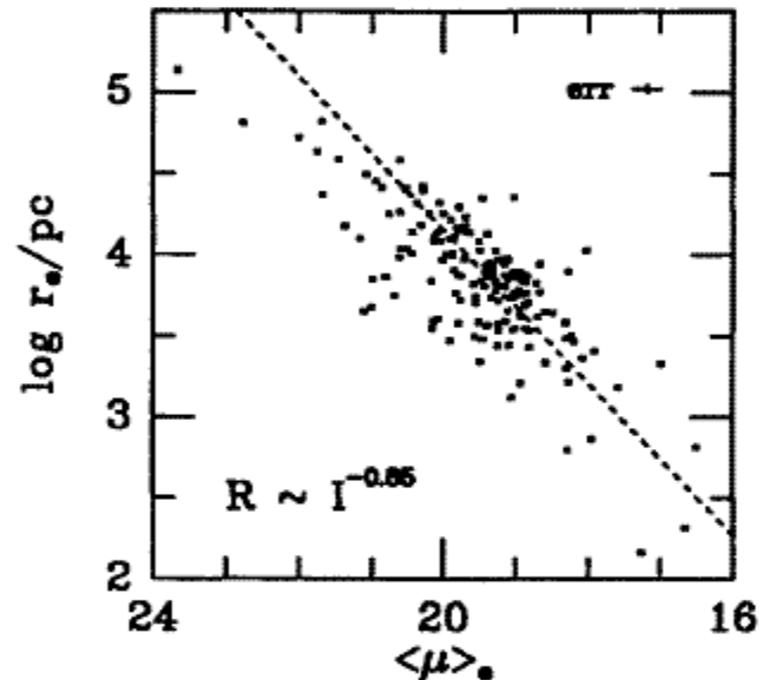
★  $\log R_e = \alpha \log \sigma_e + \beta \log \Sigma_e$

this is a “plane” in the log space of  $R_e \sigma_e \Sigma_e$

Equivalent to

★  $R_e \sim \sigma_e^{1.4} \Sigma_e^{-0.9}$

Other relations are projection of fundamental plane and have thus larger dispersion



# The Fundamental Plane

★  $R_e \propto \sigma_e^{1.4} \Sigma_e^{-0.85}$  What is its physical meaning?

Assume spheroids are an homologous family (i.e. same structure):

Virial theorem:  $V^2 = G M/R_g$

Mass/Light Ratio:  $M/L = Y$

Observed quantities are:

$$R_e = k_r R_g$$

$$\sigma^2 = k_v V^2$$

$$\Sigma_e = L/2 (\pi R_e^2)^{-1}$$

substituting in virial theorem

$$R_e = (2\pi G k_r k_v Y)^{-1} \sigma^2 \mu_e^{-1}$$

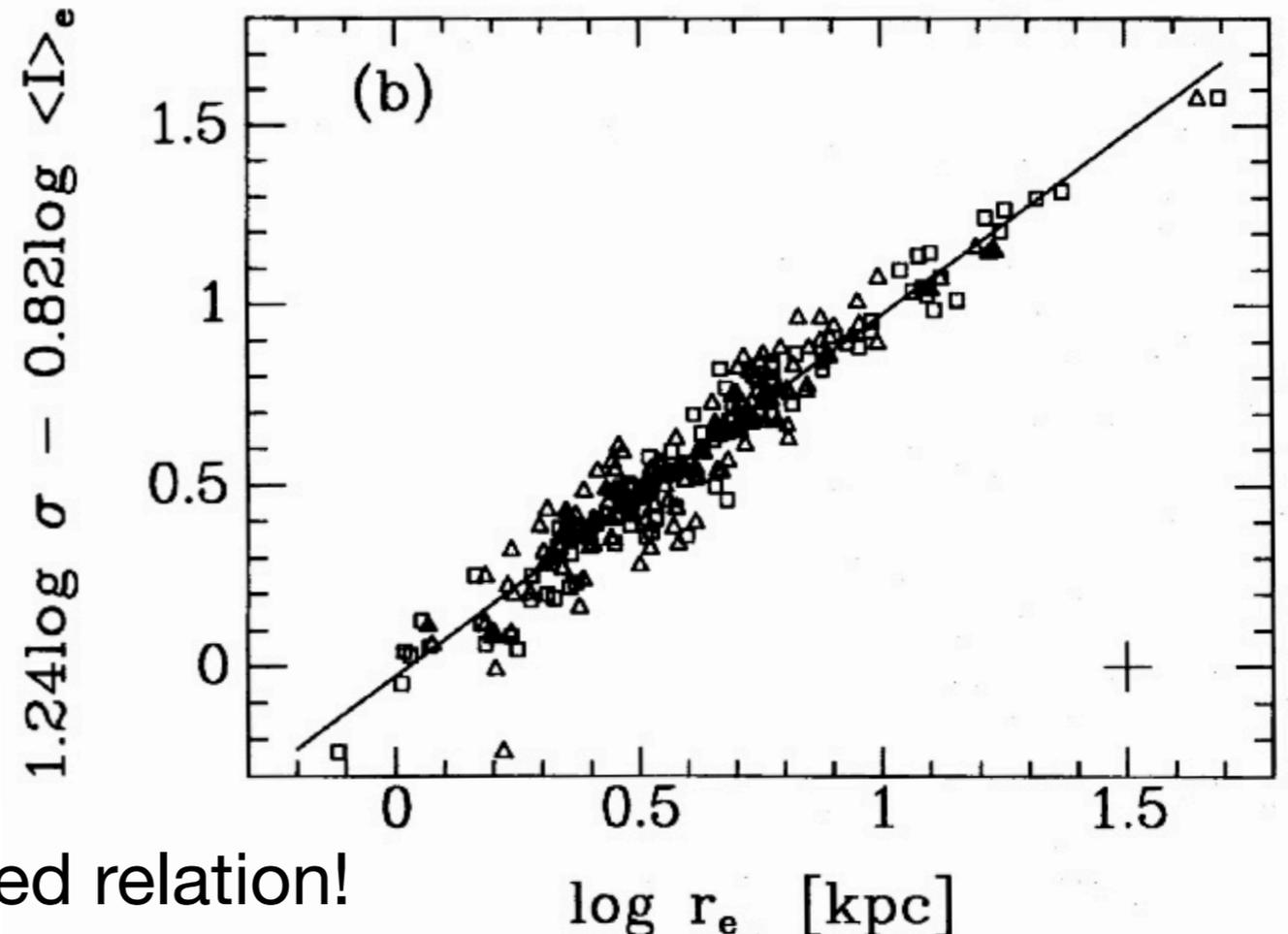
★  $R_e \propto \sigma_e^2 \Sigma_e^{-1}$  different from observed relation!

It is then trivial to show that fundamental plane corresponds to

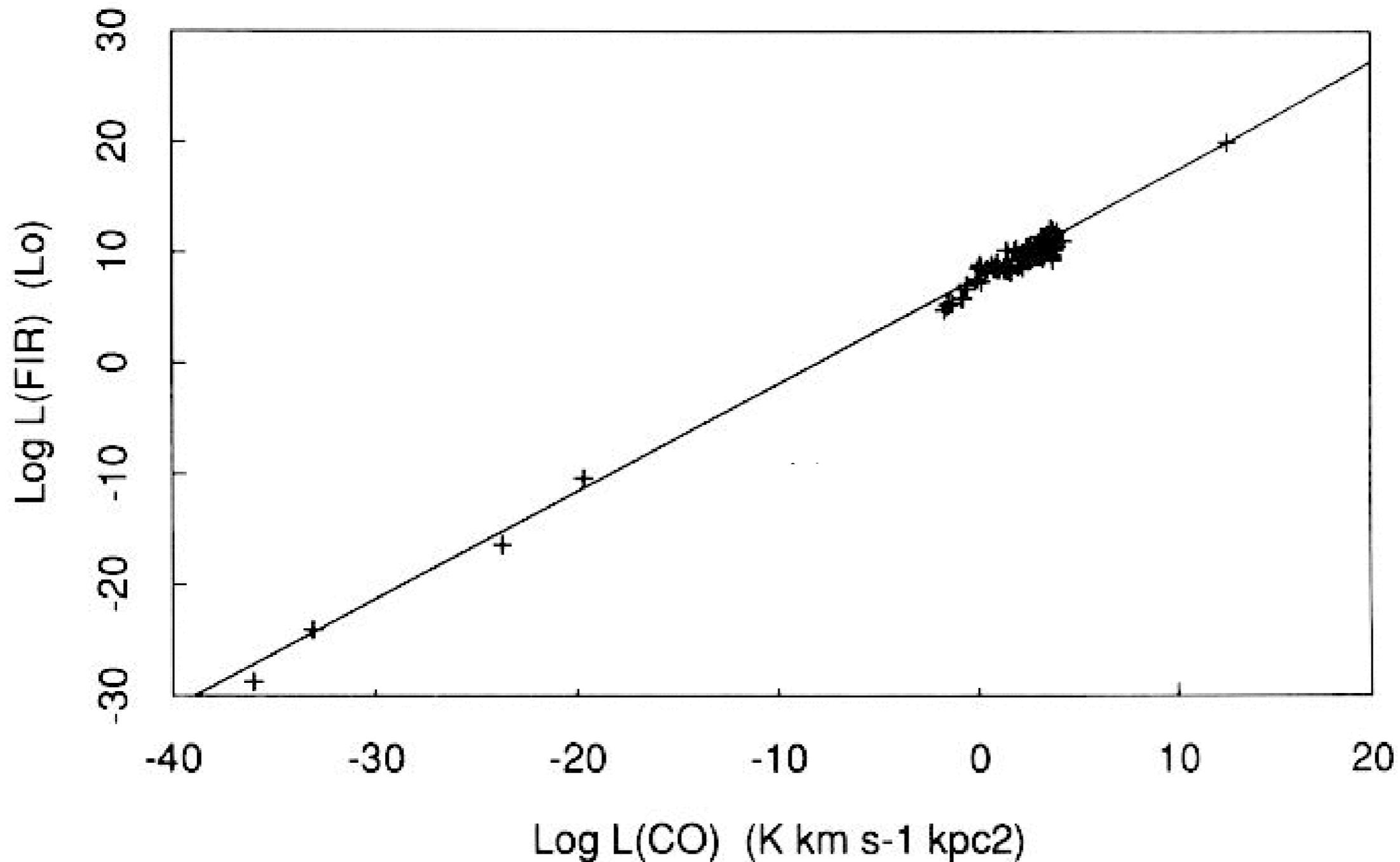
$$★ R_e \propto \sigma_e^{1.4} \Sigma_e^{-0.85} \rightarrow \rightarrow M/L \propto L^{0.2}$$

That is M/L depends weakly on luminosity (older and more metal rich stellar populations in more luminous ellipticals).

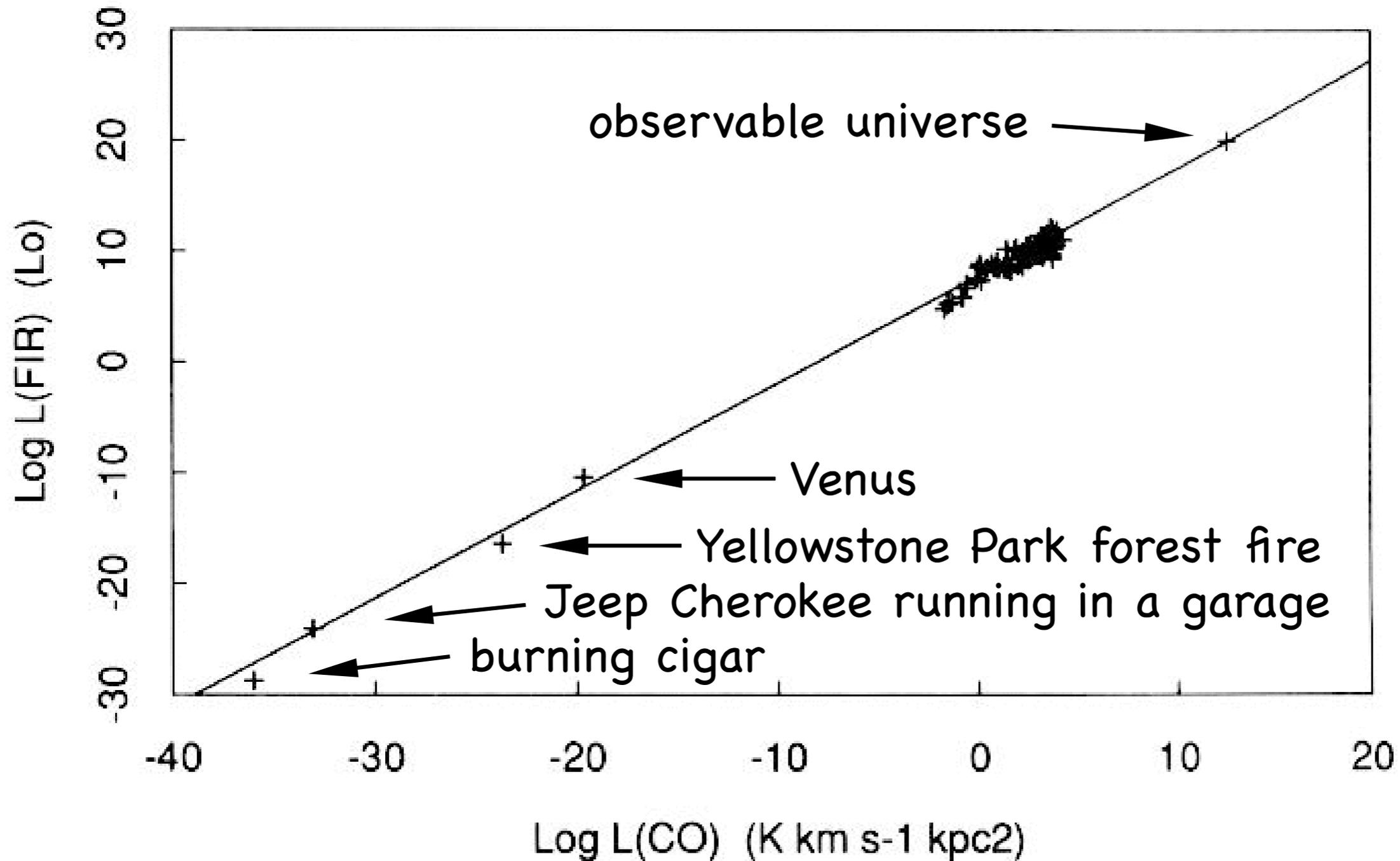
Dependence on  $L^{0.2}$  is the “tilt” of the FP with respect to a homologous family (which would have  $M/L = \text{constant}$ ).



# Do not abuse of correlations!



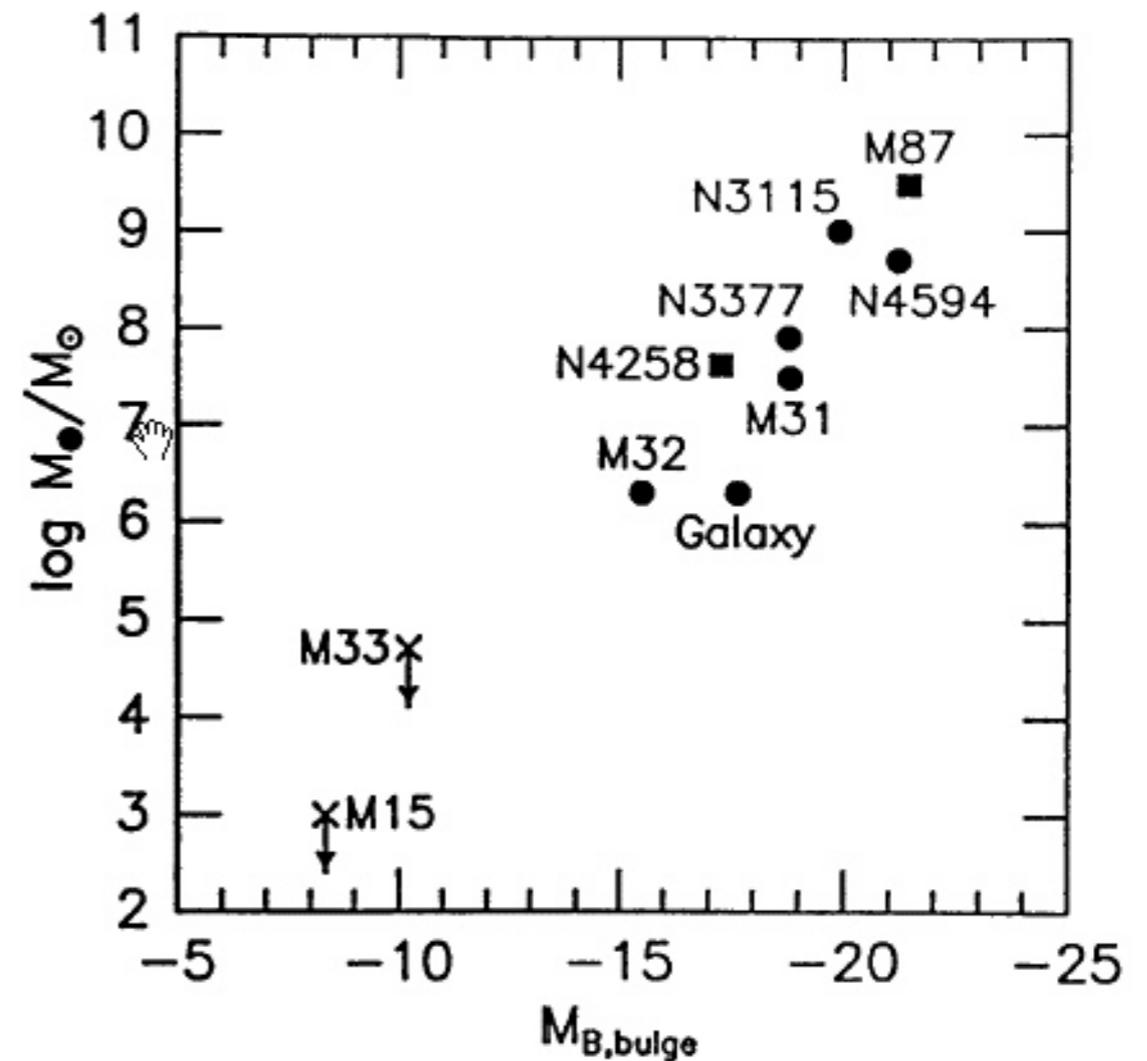
# Do not abuse of correlations!



# First hints of BH-galaxy relations

Kormendy & Richstone (1995) suggest the existence of a correlation between the total blue magnitude of the *host spheroid* ( $M_{B,\text{bulge}}$ ) and  $M_{\text{BH}}$ .

★ bulge (spheroid) = entire galaxy in case of an elliptical

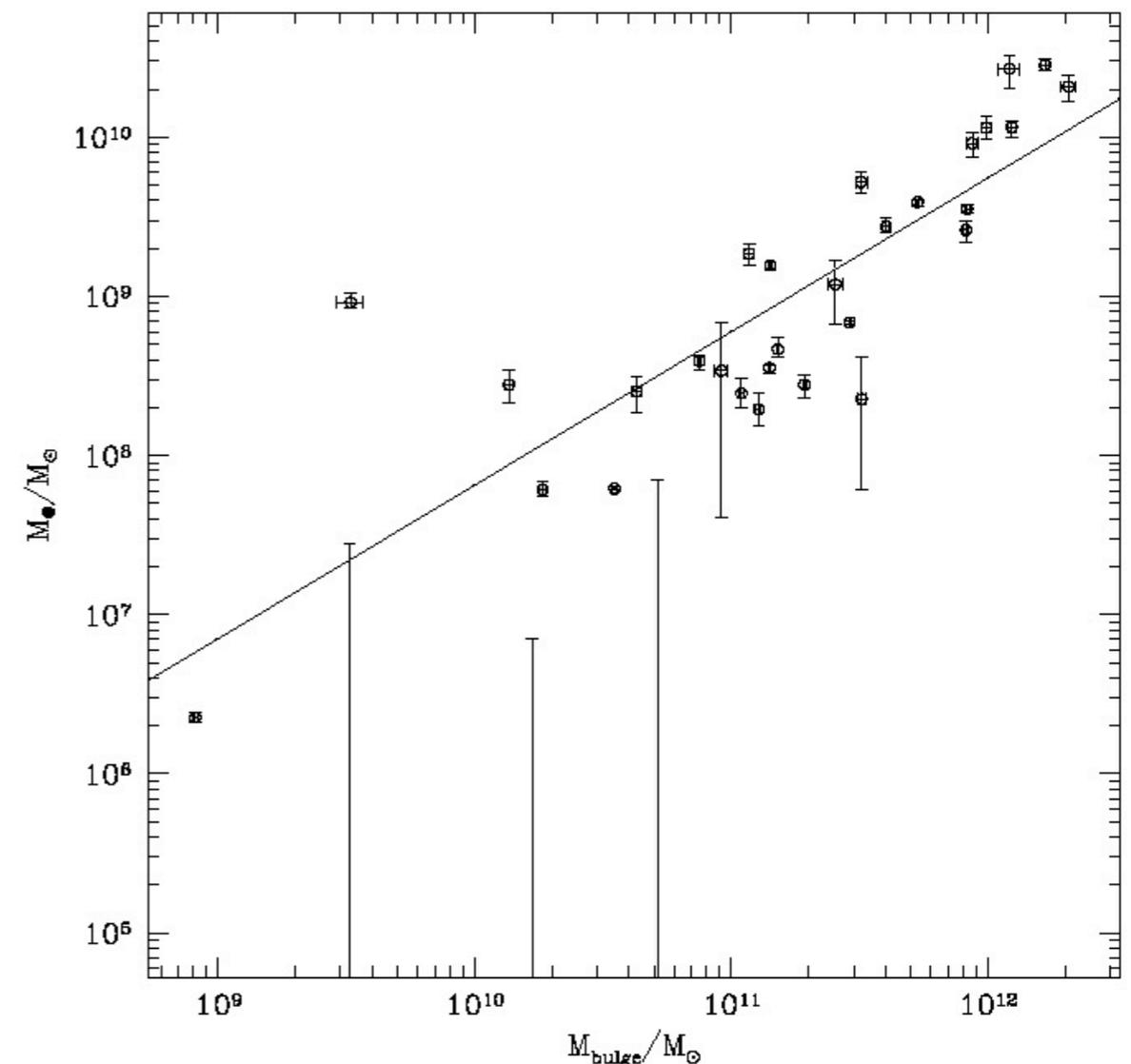


Kormendy & Richstone 1995

# More evidence ...

Magorrian et al. (1998) find a correlation between  $M_{\text{BH}}$  and *bulge* masses (“Magorrian” relation)

- ★ They use mostly low resolution ground based data.
- ★ Use stellar kinematics with axisymmetric 2-l dynamical models.
- ★ They find  $M_{\text{BH}}/M_{\text{bulge}} \sim 0.006$ .
- ★ Most mass estimates have been shown to be much overestimated (use of 2-l models).

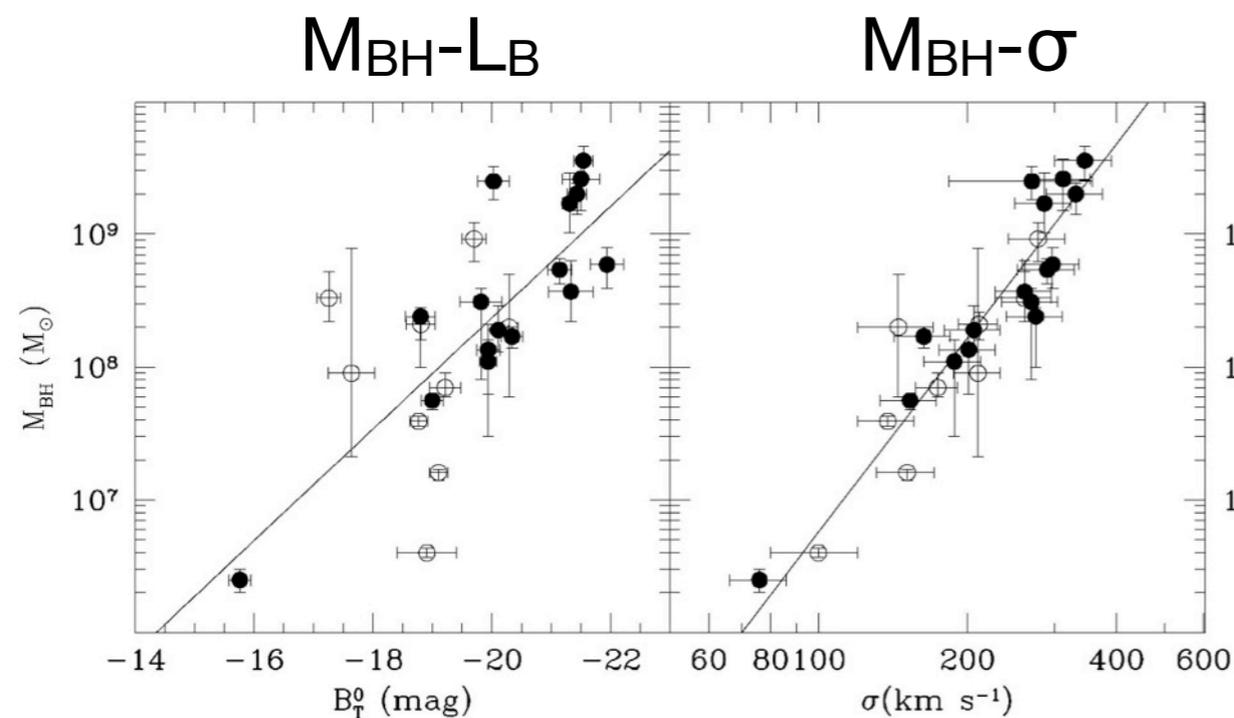


Magorrian et al. 1998

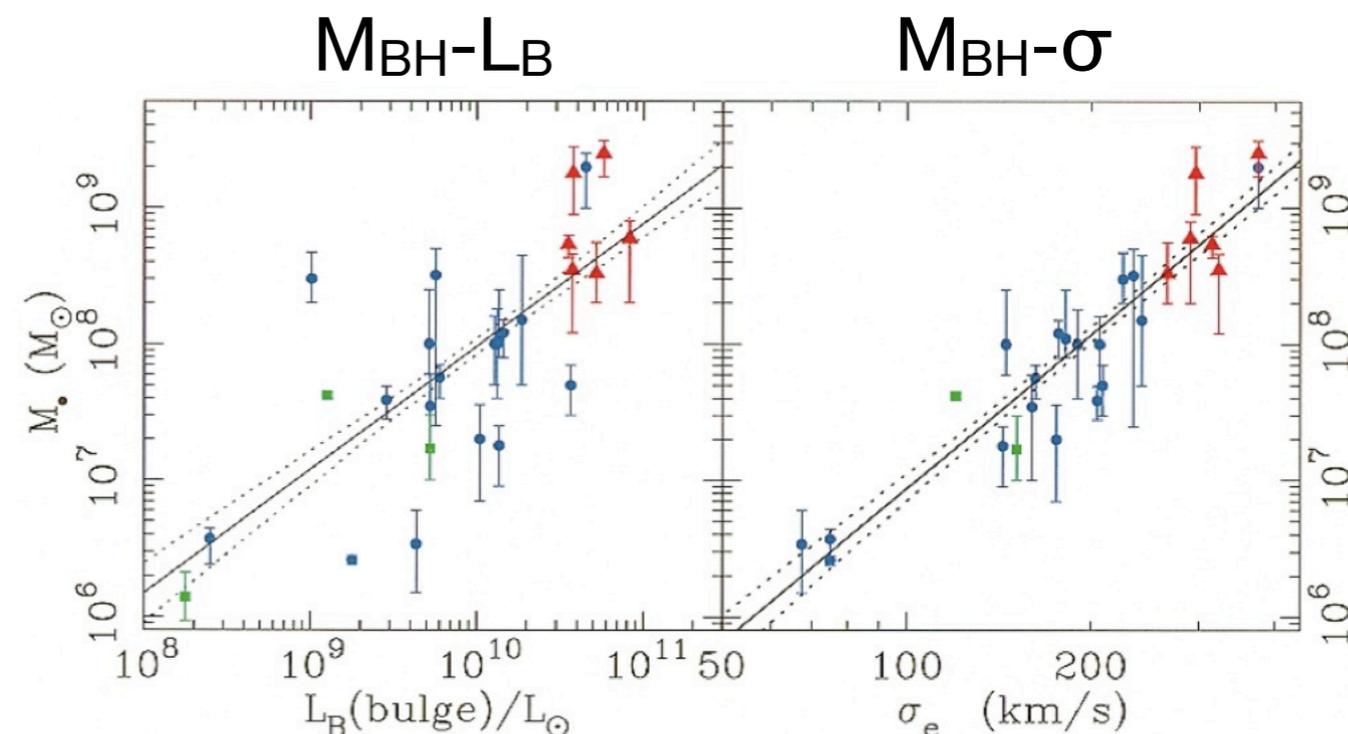
# The $M_{\text{BH}}-\sigma$ correlation

Two groups (Ferrarese & Merritt 2000, Gebhardt et al. 2000) independently find a tight relation between  $M_{\text{BH}}$  and the velocity dispersion of the stars in the galaxy bulge  $\sigma$  (within  $R_e$  or  $R_c=R_e/8$ )

- ★  $R_e$  and  $R_c$  much larger than BH sphere of influence,  $\sigma$  should not be affected by BH, only by galaxy grav. potential!
- ★ Big and hot debate about the slope  $M_{\text{BH}} \sim \sigma^5$  (FM00) and  $M_{\text{BH}} \sim \sigma^4$  (G00)
- ★ Relation with  $\sigma$  is tighter than relation with B luminosity.



Ferrarese & Merritt 2000



Gebhardt et al. 2000

# What is the meaning of “tight”?

The  $M_{\text{BH}}-\sigma$  relation is considered the best one because it is tighter than the  $M_{\text{BH}}-M_{\text{B,bulge}}$  and  $M_{\text{BH}}-M_{\text{bulge}}$  correlations.

Tightness is related to the intrinsic scatter of  $M_{\text{BH}}-X$  correlations, i.e. the dispersion in BH masses for given  $X$  (eg  $\log \sigma$ ) beyond measurement errors

★ “perfect” relation

$$P(M|V) = \delta(M - a - bV)$$

$$M = \log M_{\text{BH}}$$

$$V = \log \sigma$$

★ with errors on  $M_{\text{BH}}$  measurement observed scatter is

$$P(M_{\text{obs}}|V) = \int P(M_{\text{obs}}|M)P(M|V)dM$$

$$P(M_{\text{obs}}|V) \frac{1}{\sqrt{2\pi}\sigma_M} \exp \left[ -\frac{1}{2} \left( \frac{M_{\text{obs}} - a - bV}{\sigma_M} \right)^2 \right]$$

# Intrinsic scatter

★ a possible real (non perfect) relation

$$P(M|V) = \frac{1}{\sqrt{2\pi}\sigma_0} \exp \left[ -\frac{1}{2} \left( \frac{M - a - bV}{\sigma_0} \right)^2 \right]$$

★ observed distribution for given V ( $\sigma_M$  error on  $M_{obs}$ )

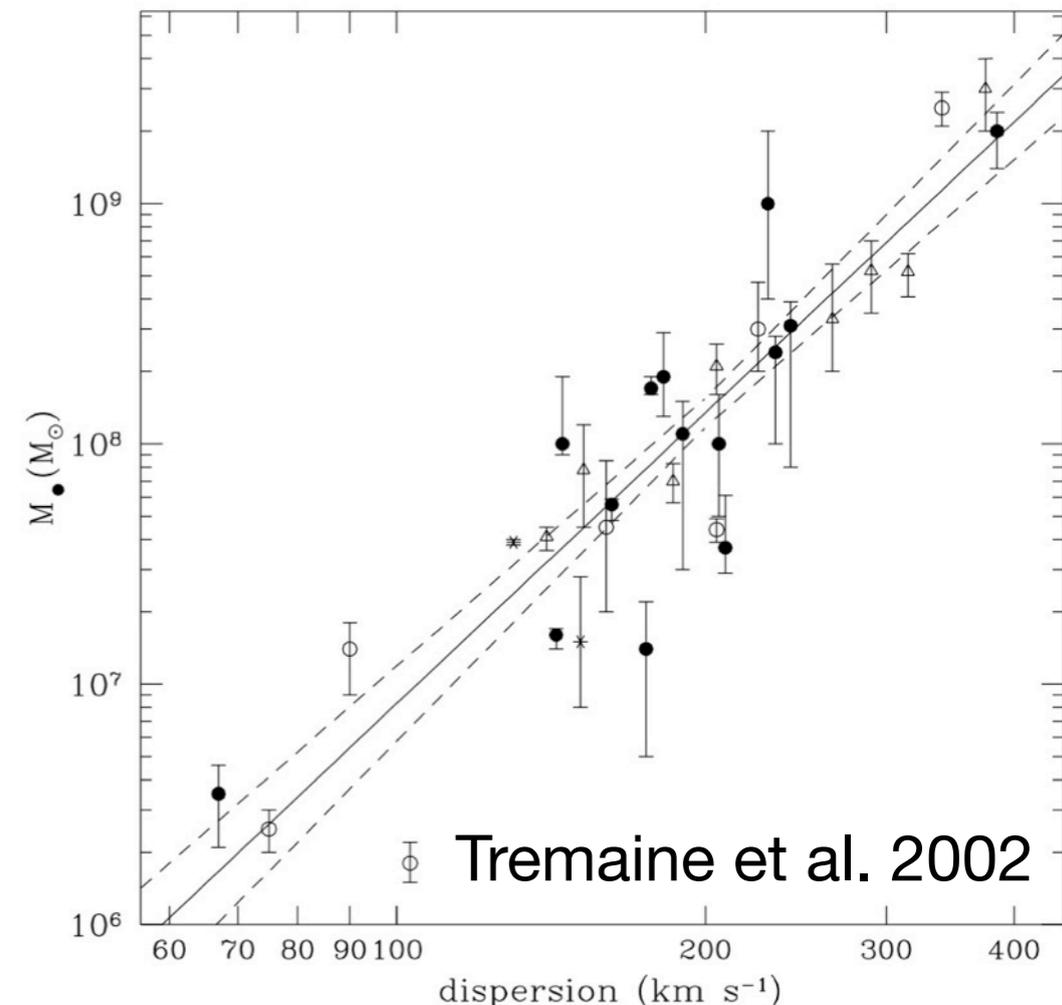
$$P(M_{obs}|V) = \frac{1}{\sqrt{2\pi(\sigma_0^2 + \sigma_M^2)}} \exp \left[ -\frac{1}{2} \frac{(M_{obs} - a - bV)^2}{(\sigma_0^2 + \sigma_M^2)} \right]$$

observed dispersion (scatter, rms of fit residuals) of relation is therefore

$$\sigma_{obs} = \sqrt{\sigma_0^2 + \sigma_M^2}$$

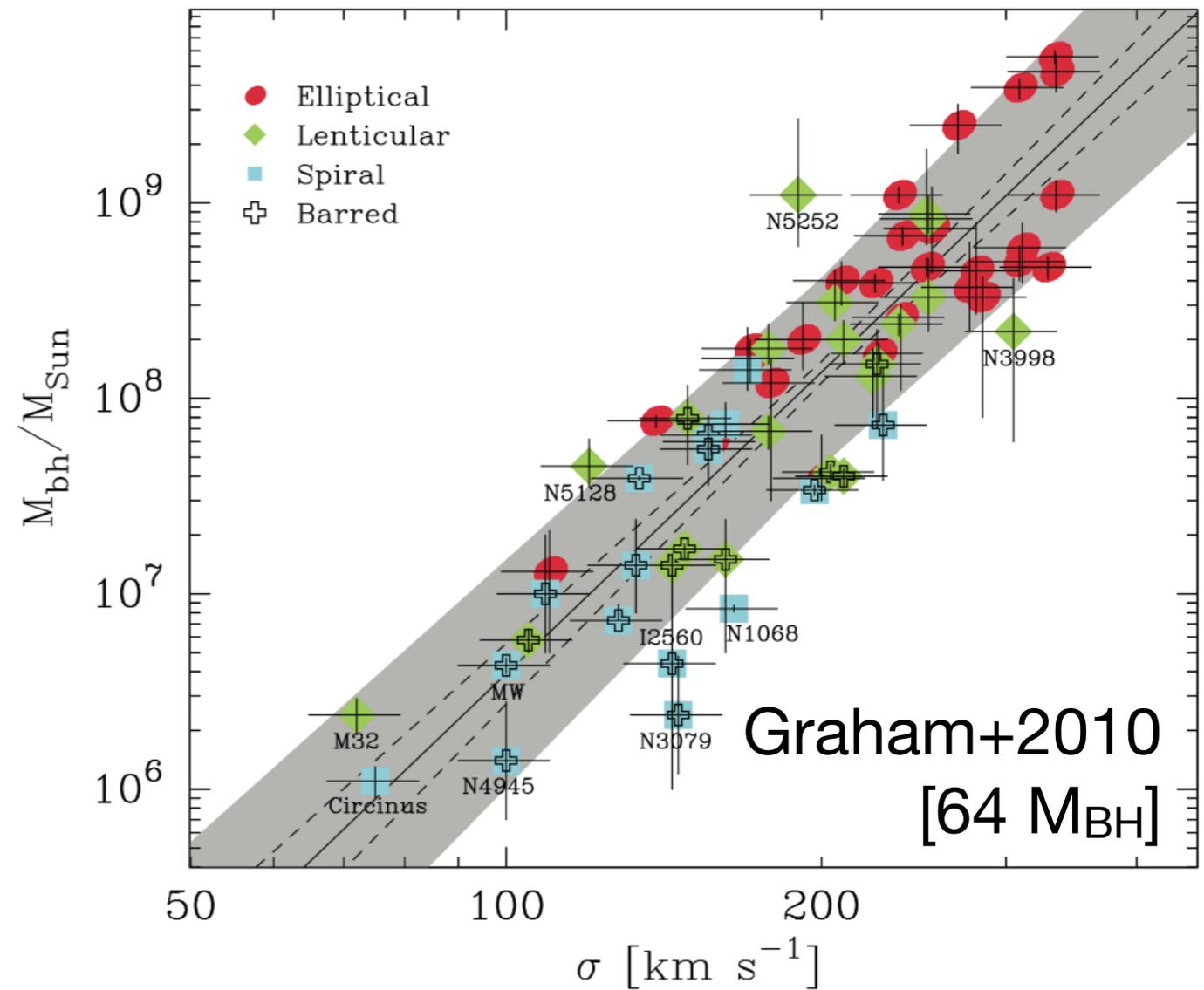
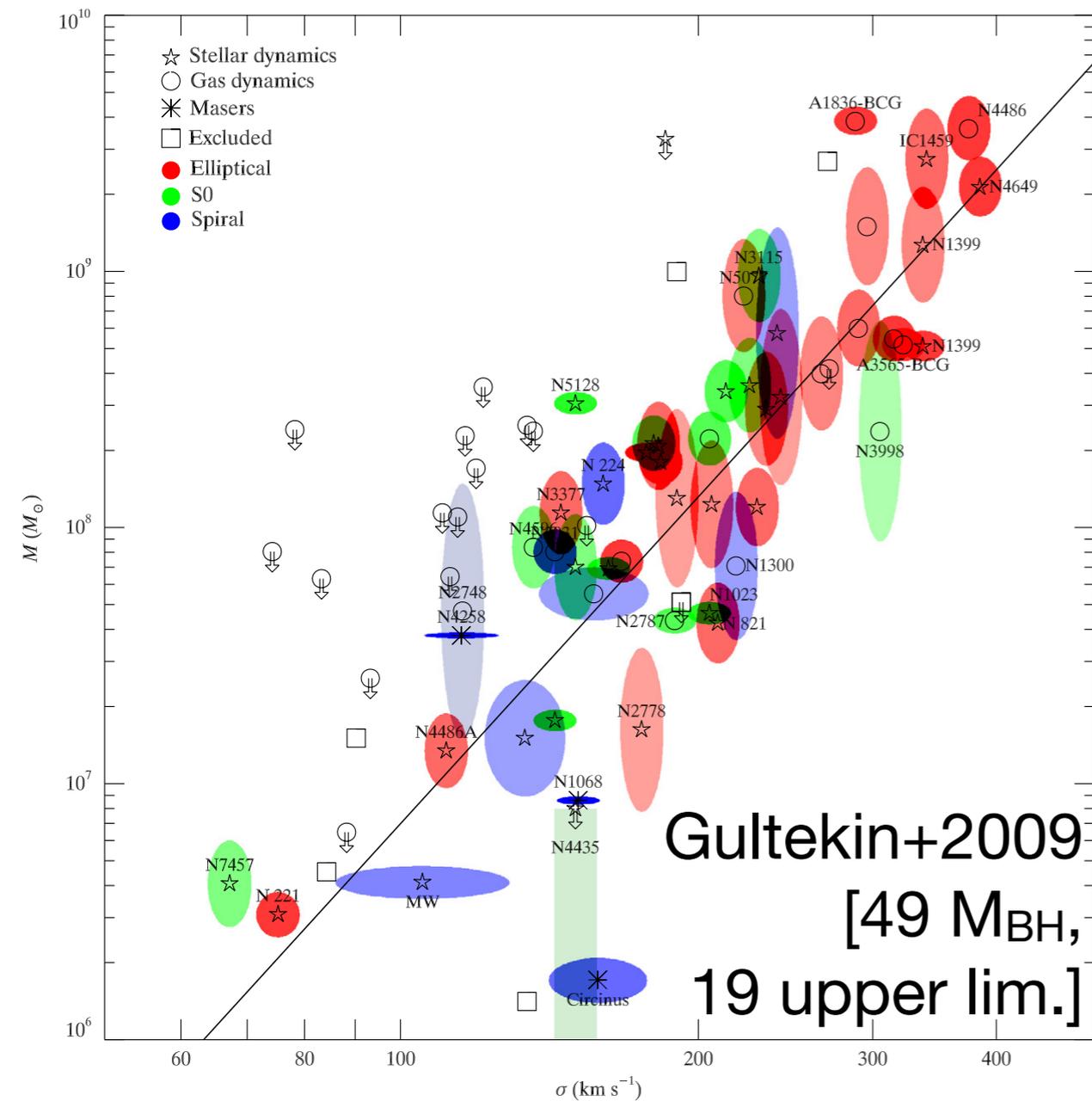
intrinsic scatter of  $M_{BH}$ - $\sigma$  relation is estimated to be  $\sim 0.3$ - $0.4$  dex (factor 2-2.5 dispersion of  $M_{BH}$  for given sigma).

*Beware that intrinsic scatter depends critically on the “accuracy” on  $M_{BH}$  errors!*



# $M_{\text{BH}}-\sigma$

Countless papers in literature, considered two of the most recent ones!



$$\log(M_{\text{BH}}/M_{\odot}) = (8.12 \pm 0.08) + (4.24 \pm 0.41) \log(\sigma/200 \text{ km s}^{-1})$$

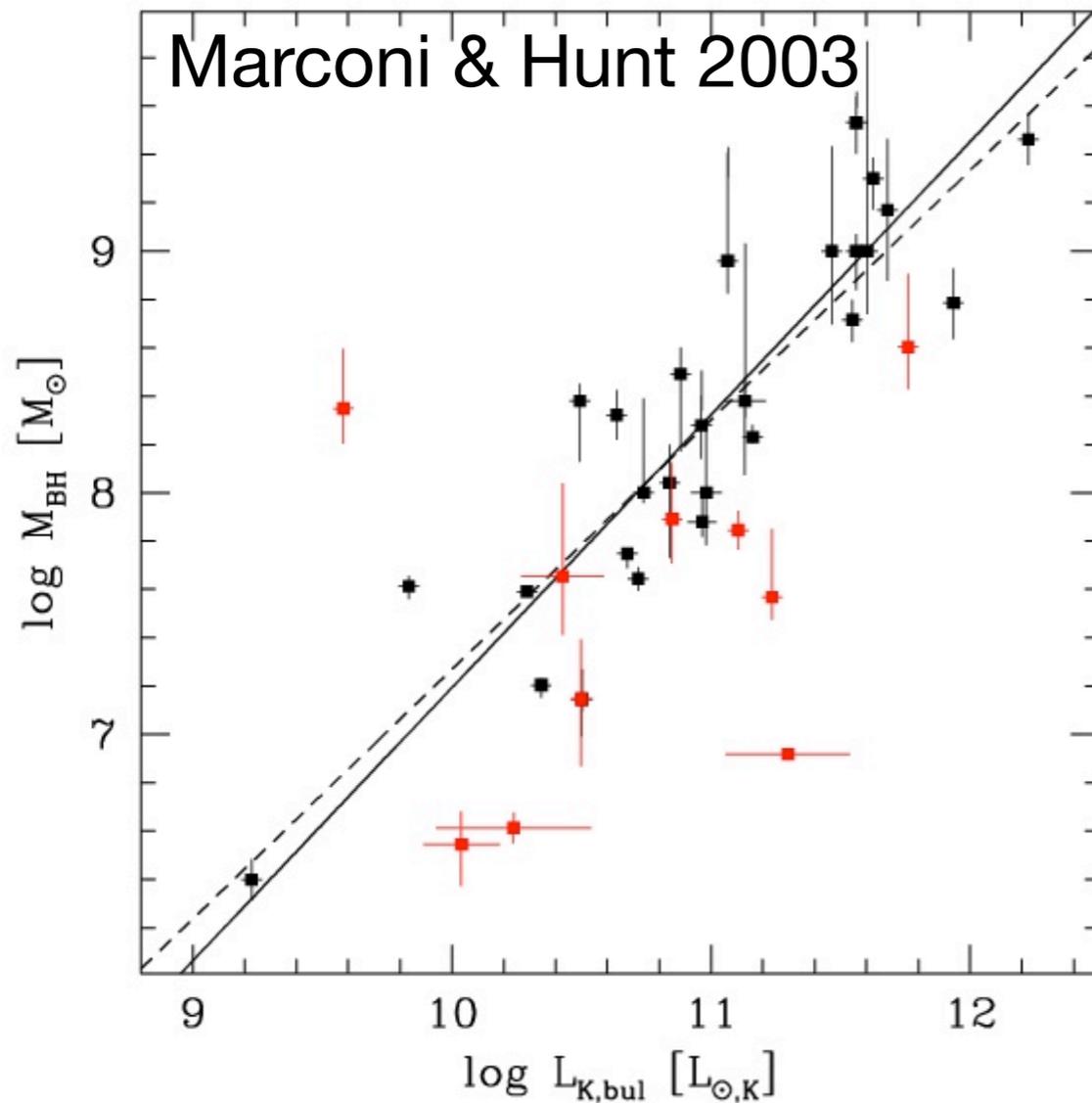
$$\sigma_0 = 0.44 \pm 0.06 \text{ dex} \quad \text{Gultekin+2009}$$

$$\log(M_{\text{BH}}/M_{\odot}) = (8.13 \pm 0.05) + (5.13 \pm 0.34) \log(\sigma/200 \text{ km s}^{-1})$$

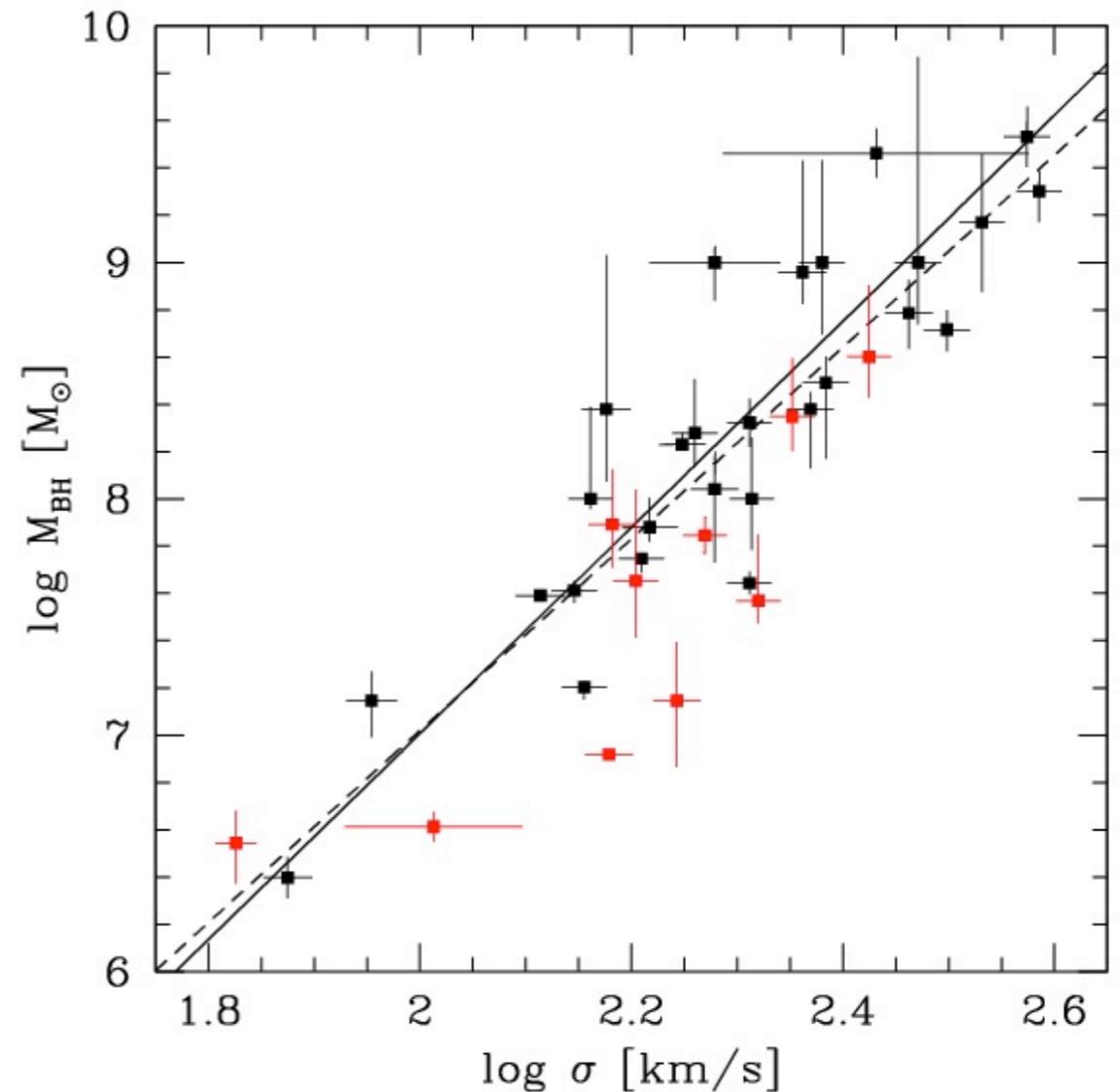
$$\sigma_0 = 0.32 \pm 0.05 \text{ dex} \quad \text{Graham+2010}$$

- ★ Still problems related to sample selection (e.g. which BH masses to consider reliable ...)
- ★ adopted fitting methods (e.g. how to take into account the intrinsic scatter ...)
- ★ adopted errors in  $M_{\text{BH}}$  and  $\sigma$ 
  - Gültekin takes 5% to  $\sigma$ , Graham takes 10% and this allows steeper slope
  - also smaller error in Gültekin gives larger intrinsic dispersion (0.44 vs 0.32)
- ★ intrinsic scatter increases with increasing samples ... maybe  $M_{\text{BH}}-\sigma$  relation is not so tight after all!
- ★  $M_{\text{BH}}-\sigma$  relation with ellipticals only appears to be tighter (i.e. bulges of spiral galaxies define a less tight relation than ellipticals):  
0.31 $\pm$ 0.06 vs 0.44 $\pm$ 0.06 (Gültekin+09)  
0.27 $\pm$ 0.06 vs 0.32 $\pm$ 0.06 (Graham+10)

# $M_{\text{BH}}$ vs Luminosity in the NIR



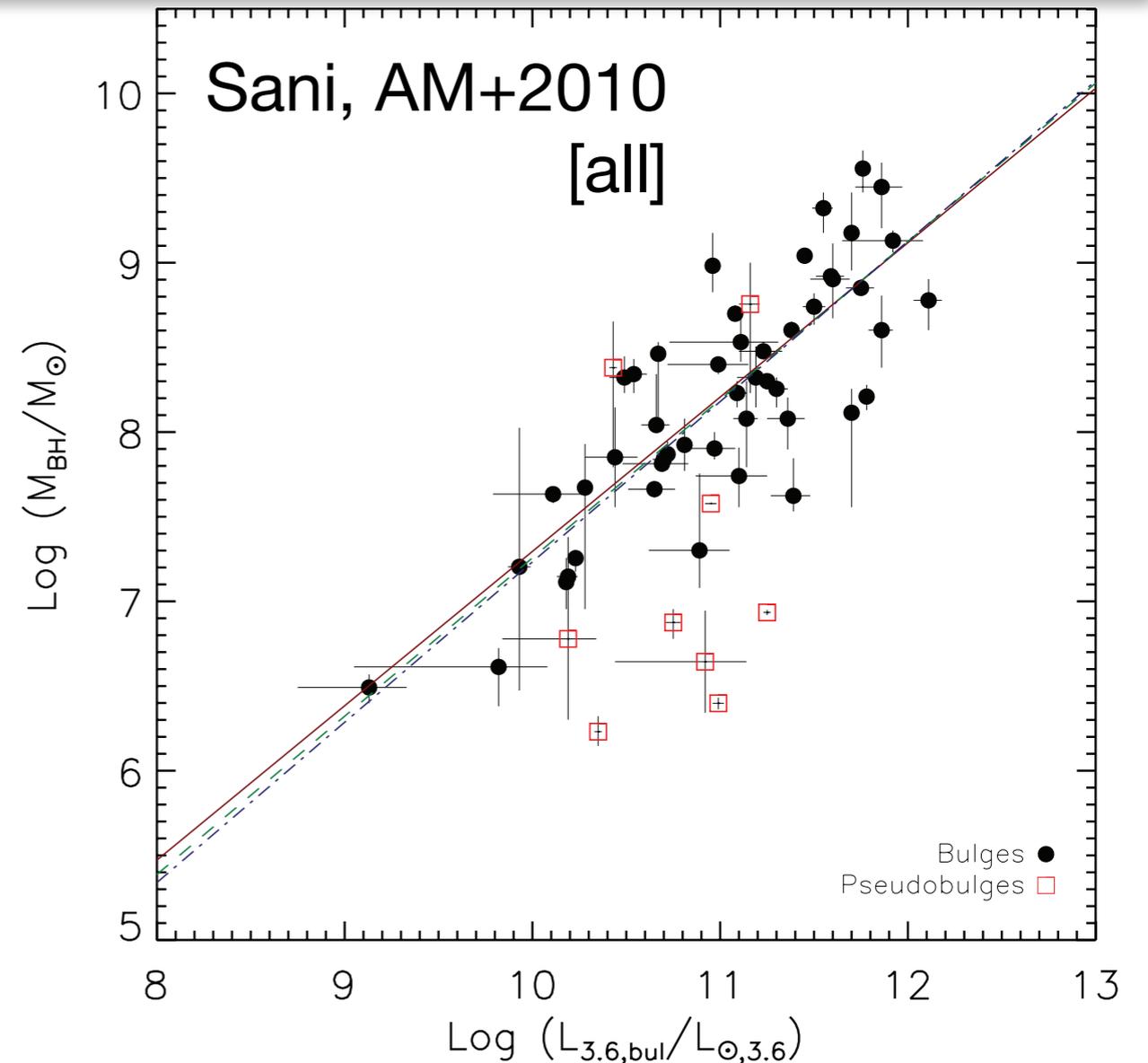
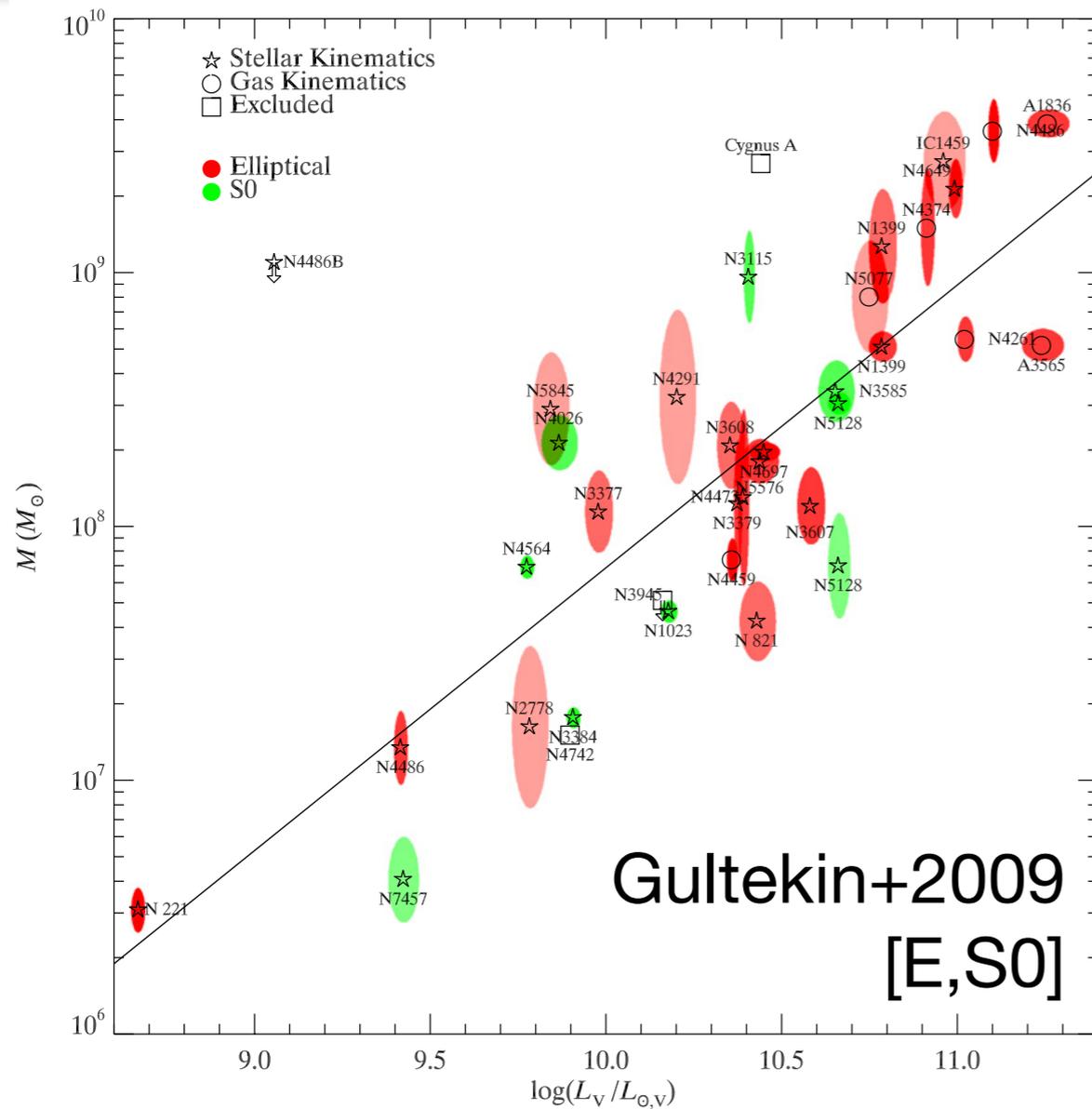
$M_{\text{BH}}-L_{\text{K,bul}}$  (rms 0.3 in  $\log M_{\text{BH}}$ )



$M_{\text{BH}}-\sigma$  (rms 0.25 in  $\log M_{\text{BH}}$ )

Investigate the  $M_{\text{BH}}-L_{\text{bul}}$  relation in the near-IR and consider *only secure BH masses* and galaxy structural parameters.

$M_{\text{BH}}-L$  relation is not worse than  $M_{\text{BH}}-\sigma$  relation!



$$\log(M_{\text{BH}}/M_{\odot}) = (8.95 \pm 0.11) + (1.11 \pm 0.18) \log\left(\frac{L_V}{10^{11} L_{\odot,V}}\right)$$

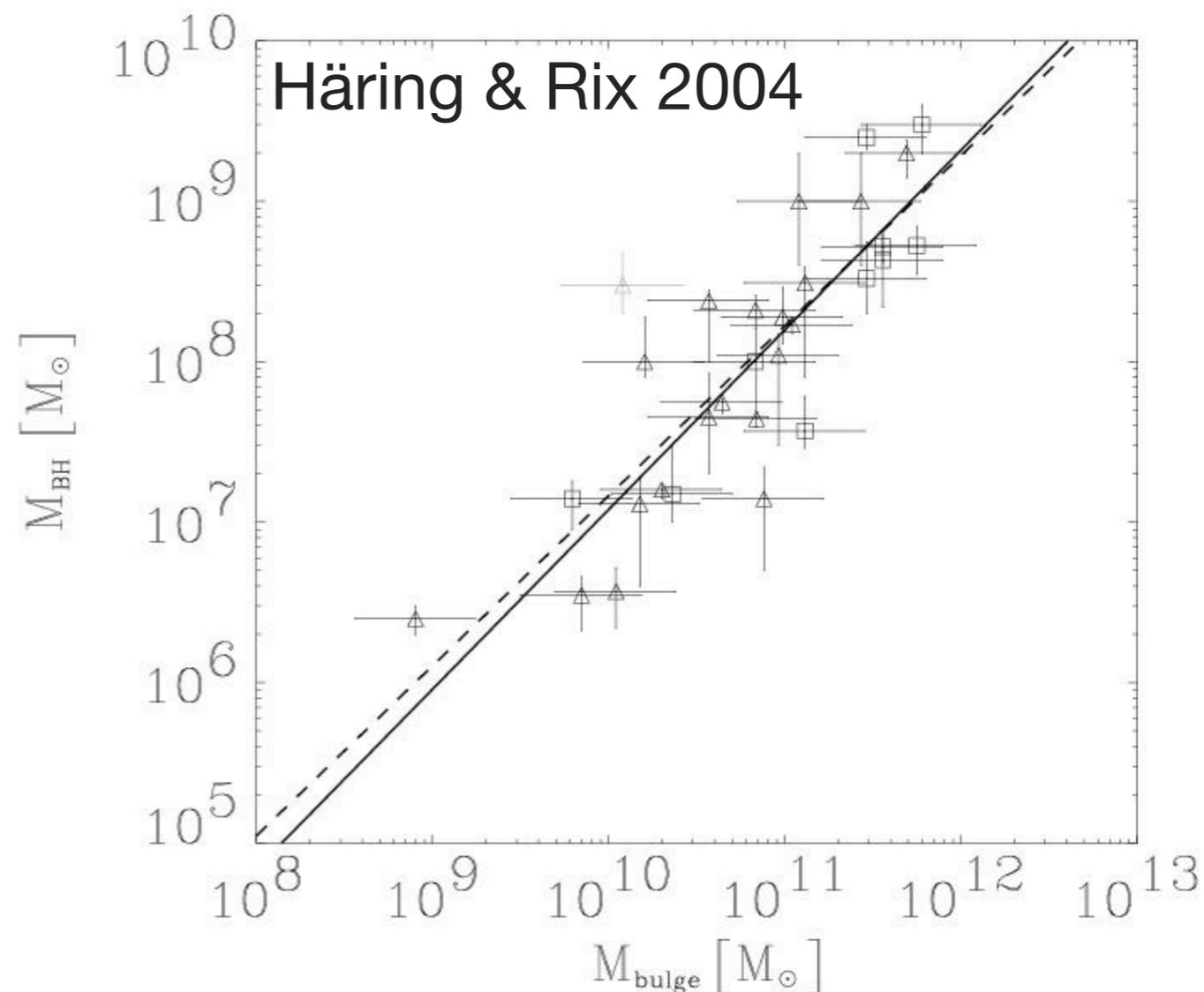
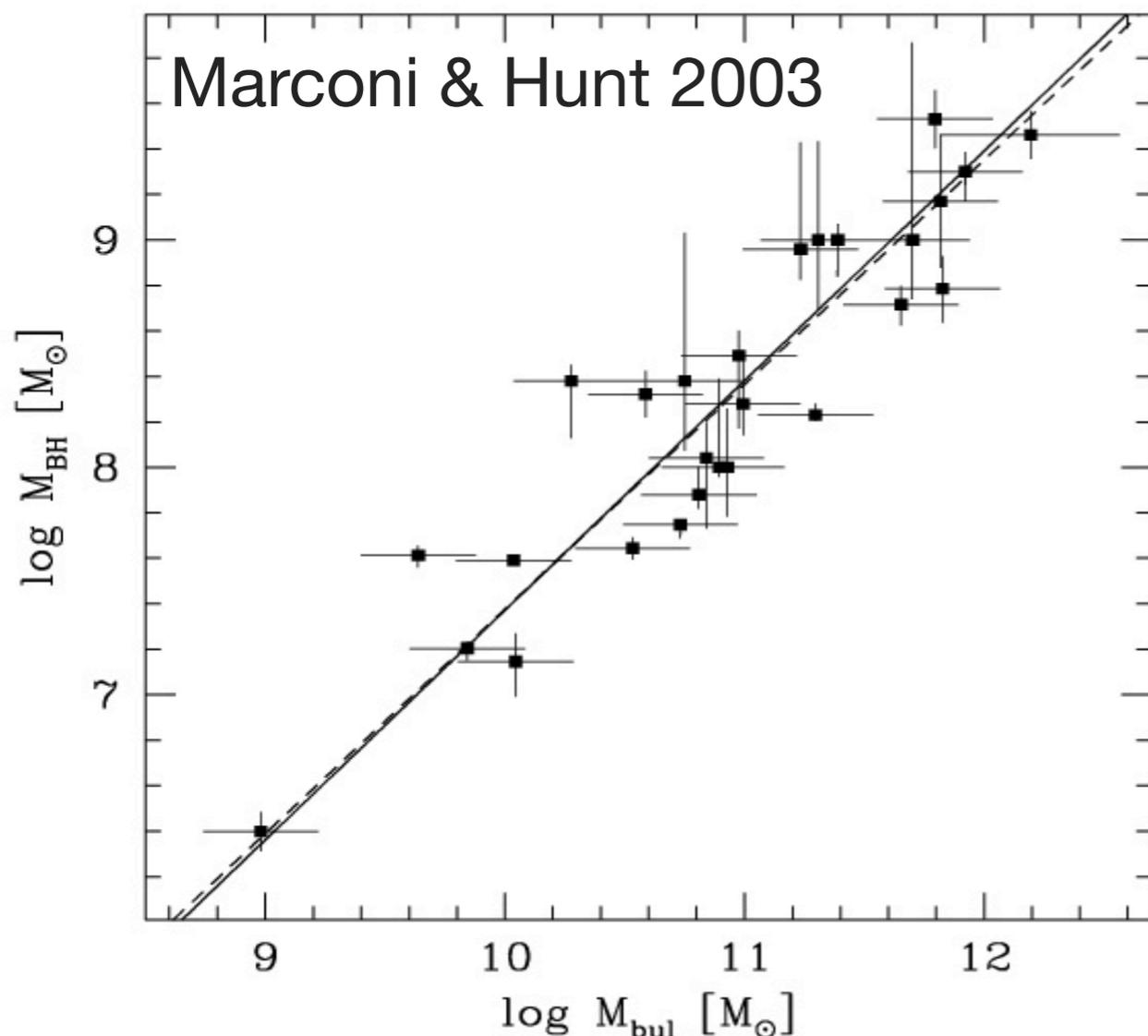
$\sigma_0 = 0.38 \pm 0.09 \text{ dex}$  Gultekin+2009

$$\log(M_{\text{BH}}/M_{\odot}) = (8.19 \pm 0.06) + (0.93 \pm 0.10) \log\left(\frac{L_{3.6 \mu\text{m}}}{10^{11} L_{\odot,3.6 \mu\text{m}}}\right)$$

$\sigma_0 = 0.38 \pm 0.05 \text{ dex}$  Sani, AM+2010

- ★ Difficulties in accurate decomposition of bulge and disk, especially in later type spirals.
- ★ Similar dispersion as  $M_{BH-\sigma}$ 
  - $0.38 \pm 0.09$  vs  $0.31 \pm 0.06$  (E+S0, Gültekin+09)
  - $0.38 \pm 0.05$  vs  $0.33 \pm 0.04$  (E+S0, Gültekin+09)

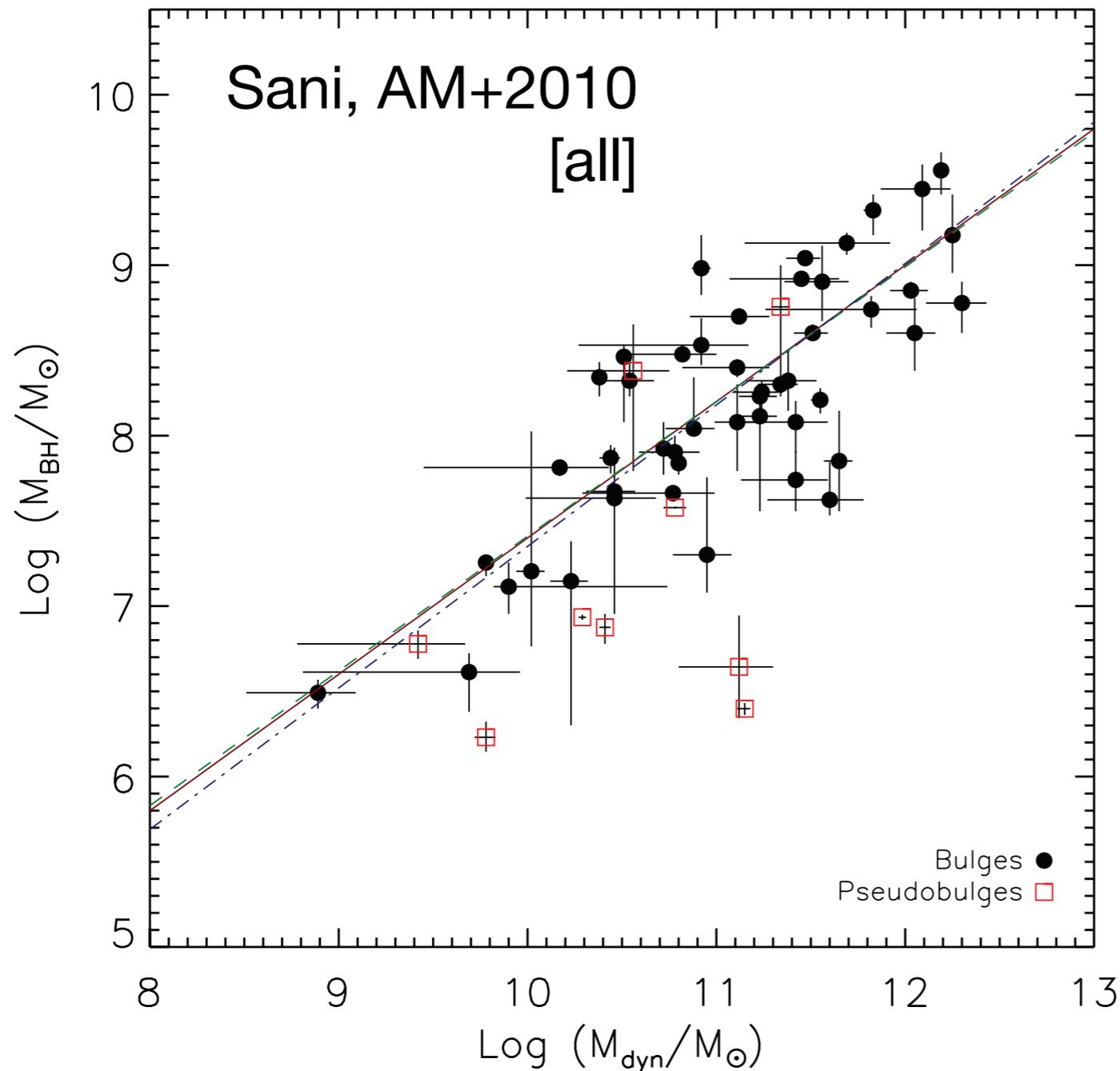
# $M_{\text{BH}}-M_{\text{bul}}$



- ★ Tight correlation  $M_{\text{BH}}$  vs virial bulge mass ( $\approx R_e \sigma_e^2$ ) with *intrinsic dispersion*  $\sigma_0 \sim 0.25$ .
- ★ Linear slope ( $0.96 \pm 0.07$ ), average ratio  $M_{\text{BH}}/M_{\text{bul}} \approx 0.002$ .
- ★ Häring & Rix 2004 find  $\sigma_0 \sim 0.3$  in  $\log M_{\text{BH}}$  with  $M_{\text{bul}}$  from dynamical models.

# $M_{BH}-M_{bul}$

Countless papers in literature,  
considered the most recent one!



★  $M_{vir}$  from virial theorem

$$M_{vir} = 5 \frac{R_e \sigma^2}{G}$$

★ Similar dispersion as other relations.

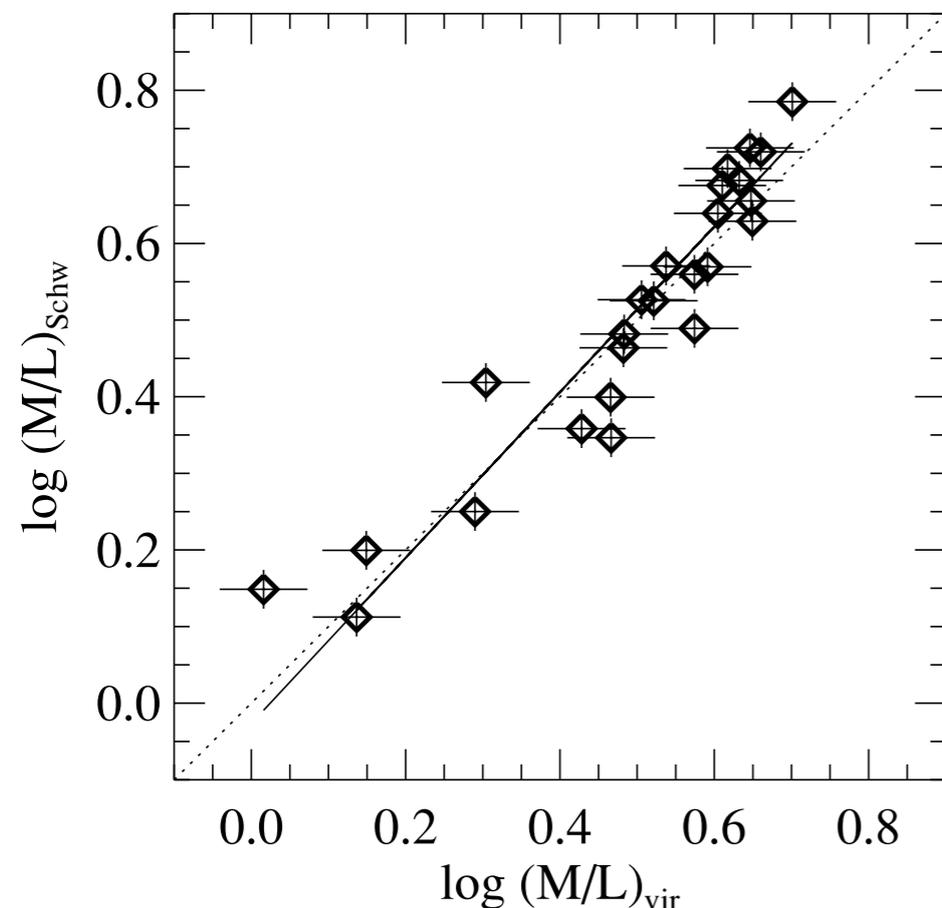
★ This is really a relation of  $M_{BH}$  with a combination of bulge parameters.

★ Does  $M_{vir}$  really represents bulge mass?

$$\log(M_{BH}/M_{\odot}) = (8.20 \pm 0.06) + (0.79 \pm 0.09) \log\left(\frac{M_{vir}}{10^{11} M_{\odot}}\right)$$
$$\sigma_0 = 0.37 \pm 0.05 \text{ dex}$$

# Accuracy of virial bulge mass

- ★ Cappellari et al. 2006 studied a sample of E+S0 galaxies with
  - integral field kinematics (SAURON)
  - HST imaging
  - 3-I Schwarzschild dynamical modeling
- ★ They measured dynamical masses with high accuracy
- ★ They demonstrated that tilt of FP is due to M/L variations, and not to variation in the dynamical structure of galaxies.
- ★ As a by-product they verified the accuracy of virial mass estimates in the central regions of E+S0 galaxies ...



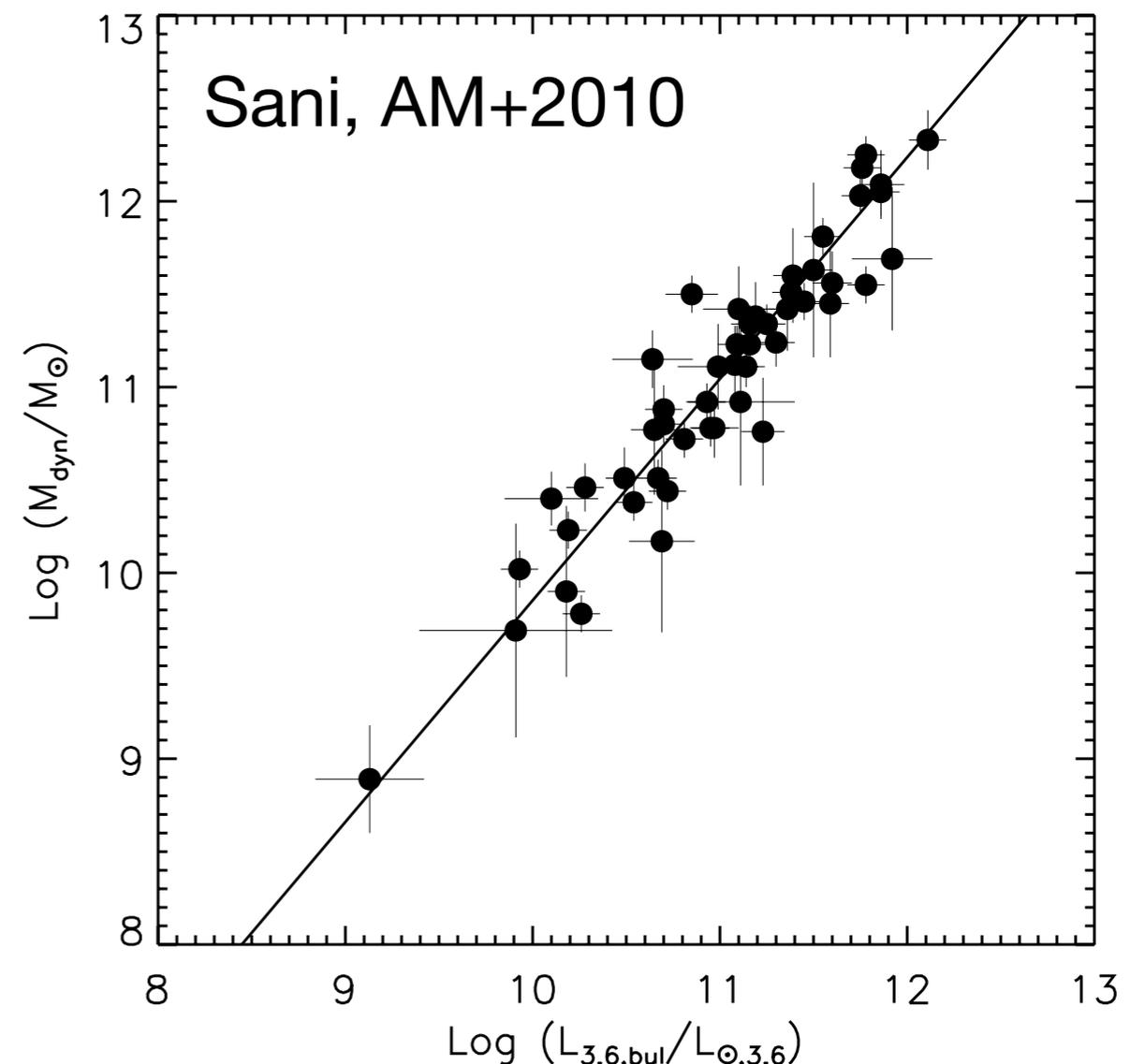
$$\left(\frac{M}{L}\right)_{vir,I} = (5 \pm 1) \frac{R_e \sigma^2}{G L_I}$$

$$\sigma_0 \simeq 0.06 \text{ dex}$$

*$M_{vir}$  is an excellent surrogate of more complex (and expensive) dynamical models!*

# L vs M<sub>star</sub>

- ★ Virial masses provide accurate dynamical masses
- ★ Comparing bulge luminosities with dynamical masses, we find that the M<sub>BH</sub>-L correlation is obviously a correlation with stellar mass (neglecting contributions from dark matter ...)
- ★ Luminosity at 3.6 μm is an excellent tracer of (stellar) mass

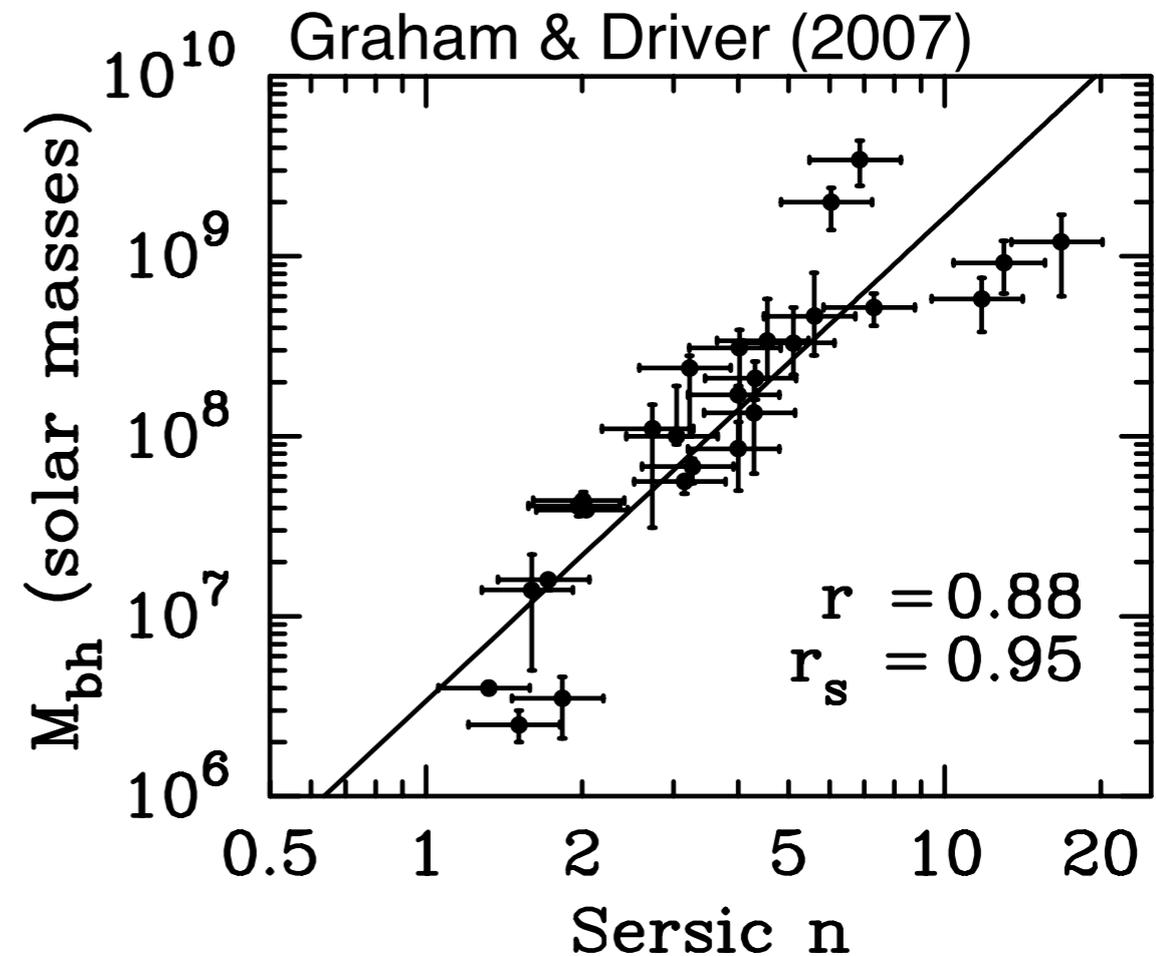
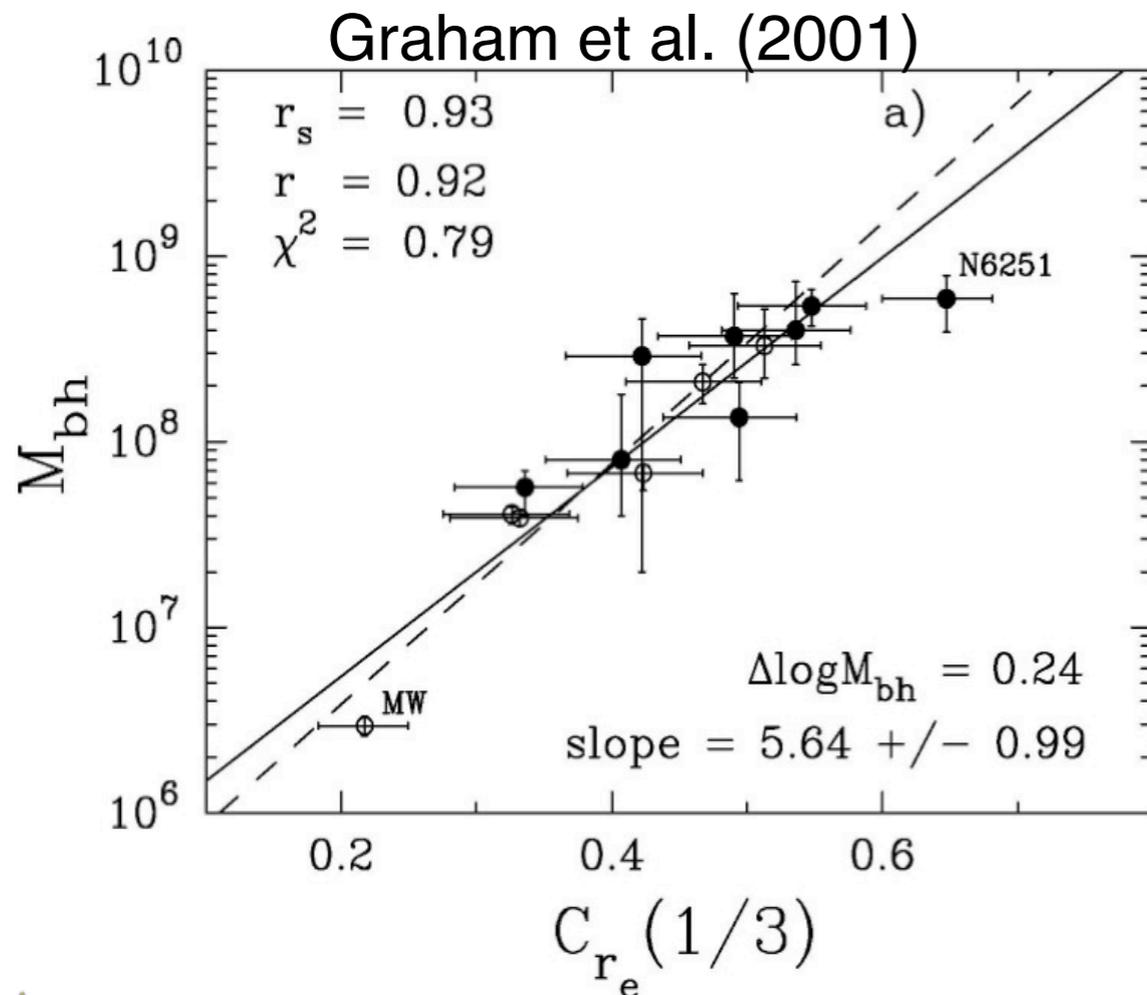


$$\log(M_{\text{vir}} / M_{\odot}) = (11.04 \pm 0.03) + (1.18 \pm 0.07) \log \left( \frac{L_{3.6 \mu\text{m}}}{10^{11} L_{\odot, 3.6 \mu\text{m}}} \right)$$

$$\sigma_0 = (0.13 \pm 0.04) \text{ dex}$$

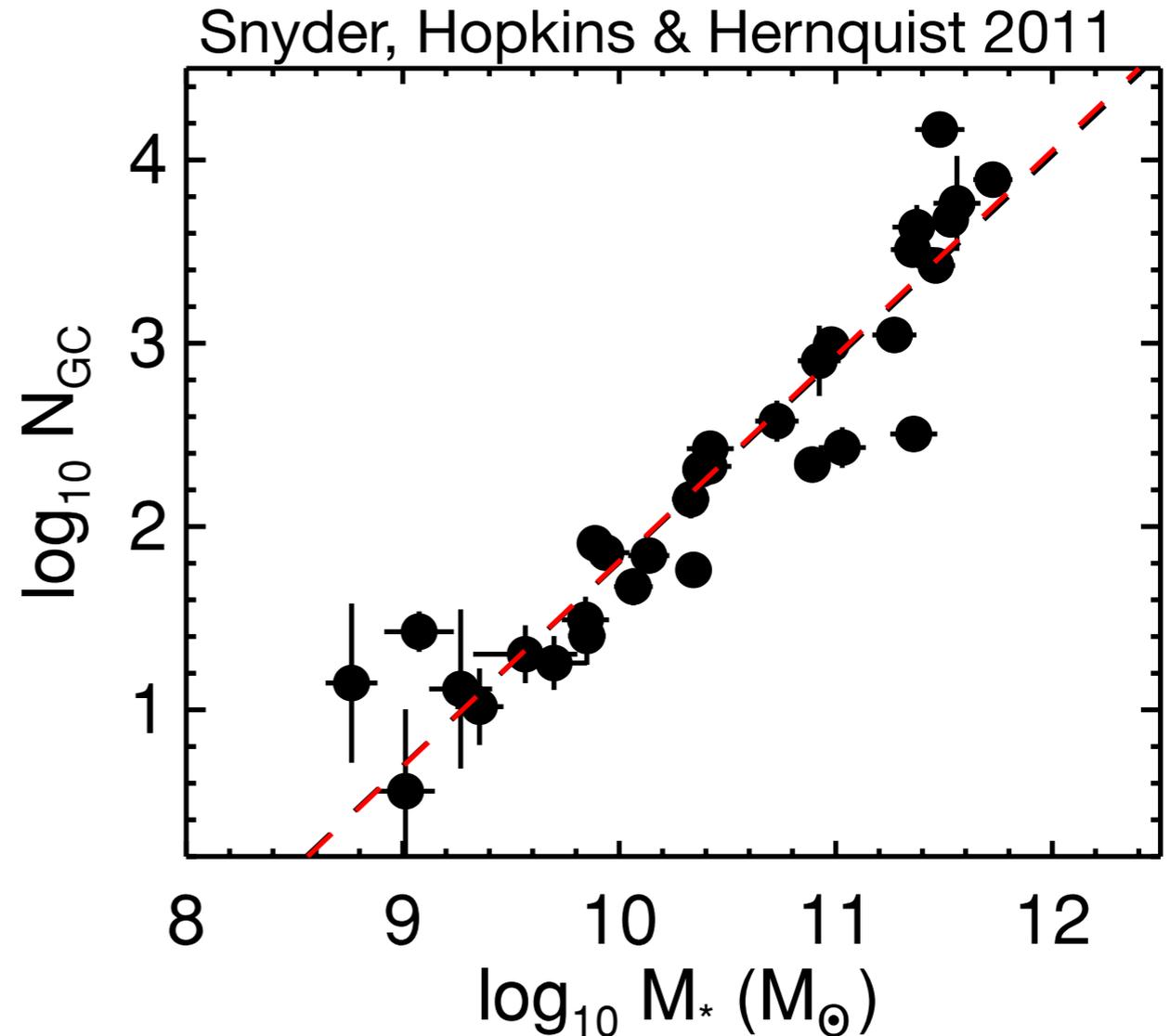
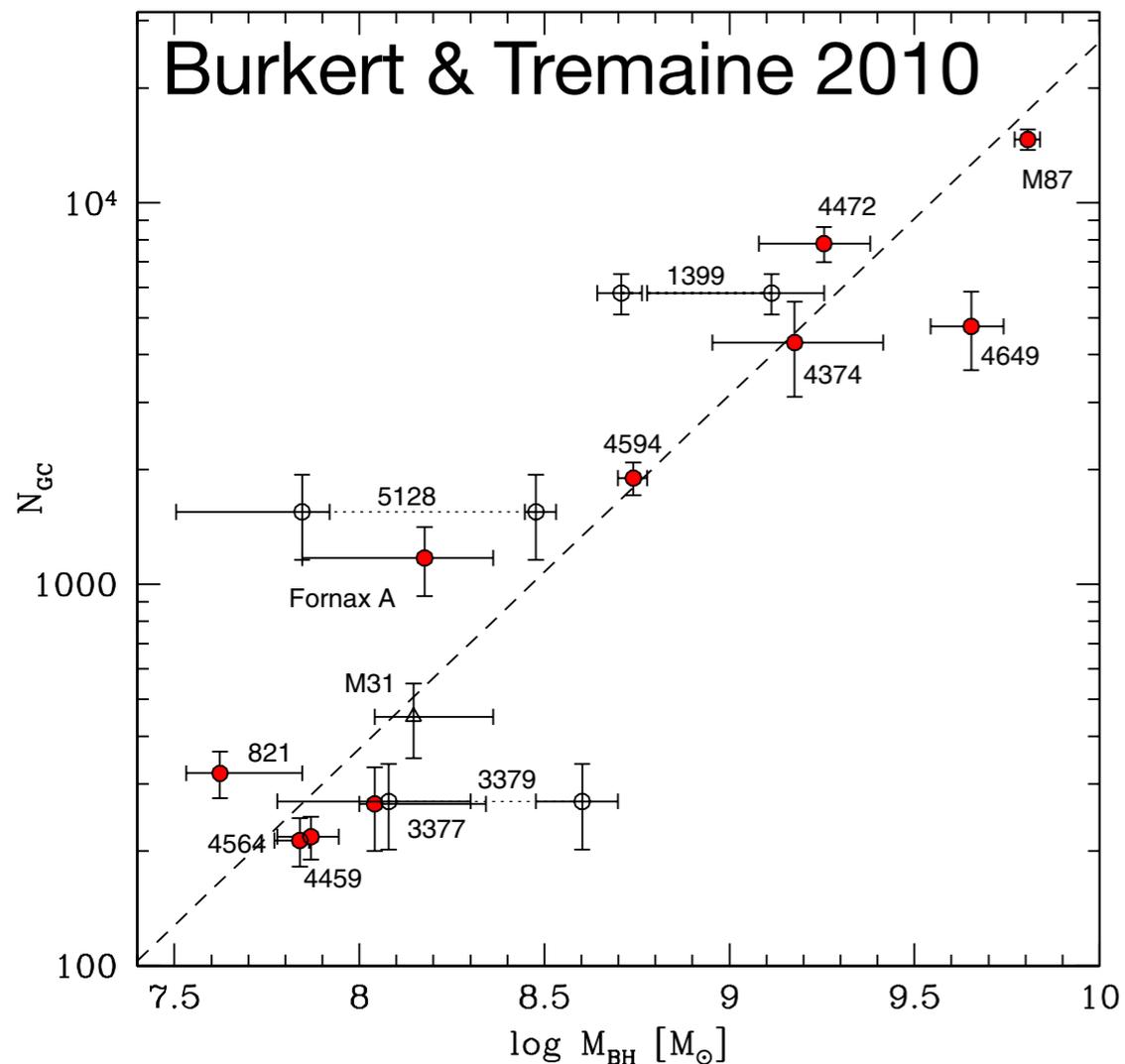
# $M_{BH}$ vs bulge light concentration

- ★ Graham et al. (2001) found that  $M_{BH}$  is tightly correlated with the concentration index of bulge light [  $C_{Re} (1/3) = F(R_e/3)/F(R_e)$  ]
- ★ BH mass also correlates with Sersic index,  $\Sigma(r) \sim \exp(r^{1/n})$ ,  $n$  Sersic index (Graham & Driver 2007)



- ★ Kormendy relation ( $\Sigma_e - R_e$ ) combined with  $n - R_e$  relation (Caon et al. 1993) can be used to explain  $M_{BH}$  vs  $C, n$  correlation.
- ★ *Sersic index is obviously directly related to other structural parameters of the spheroid and, through them, to  $M_{BH}$ .*

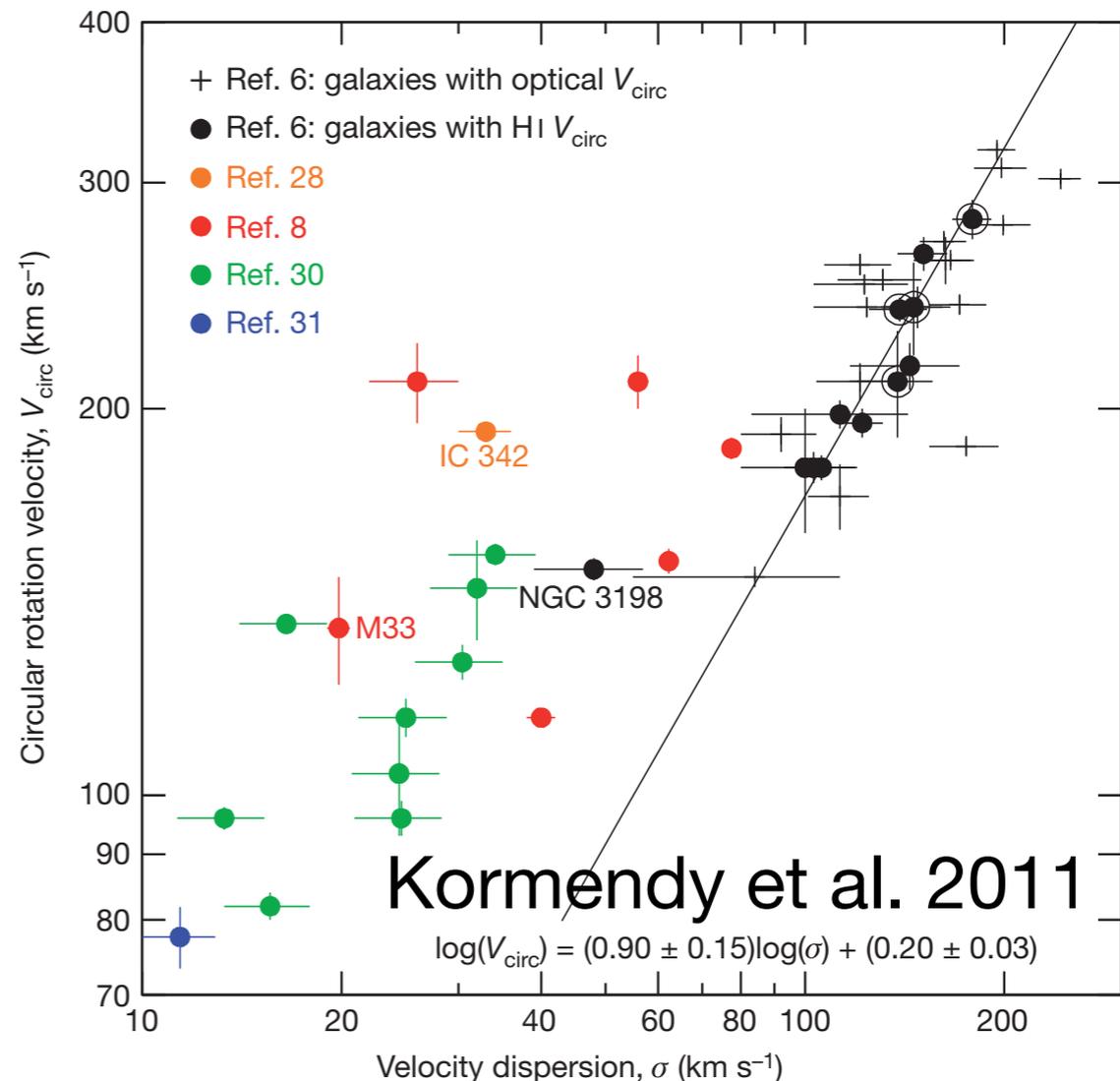
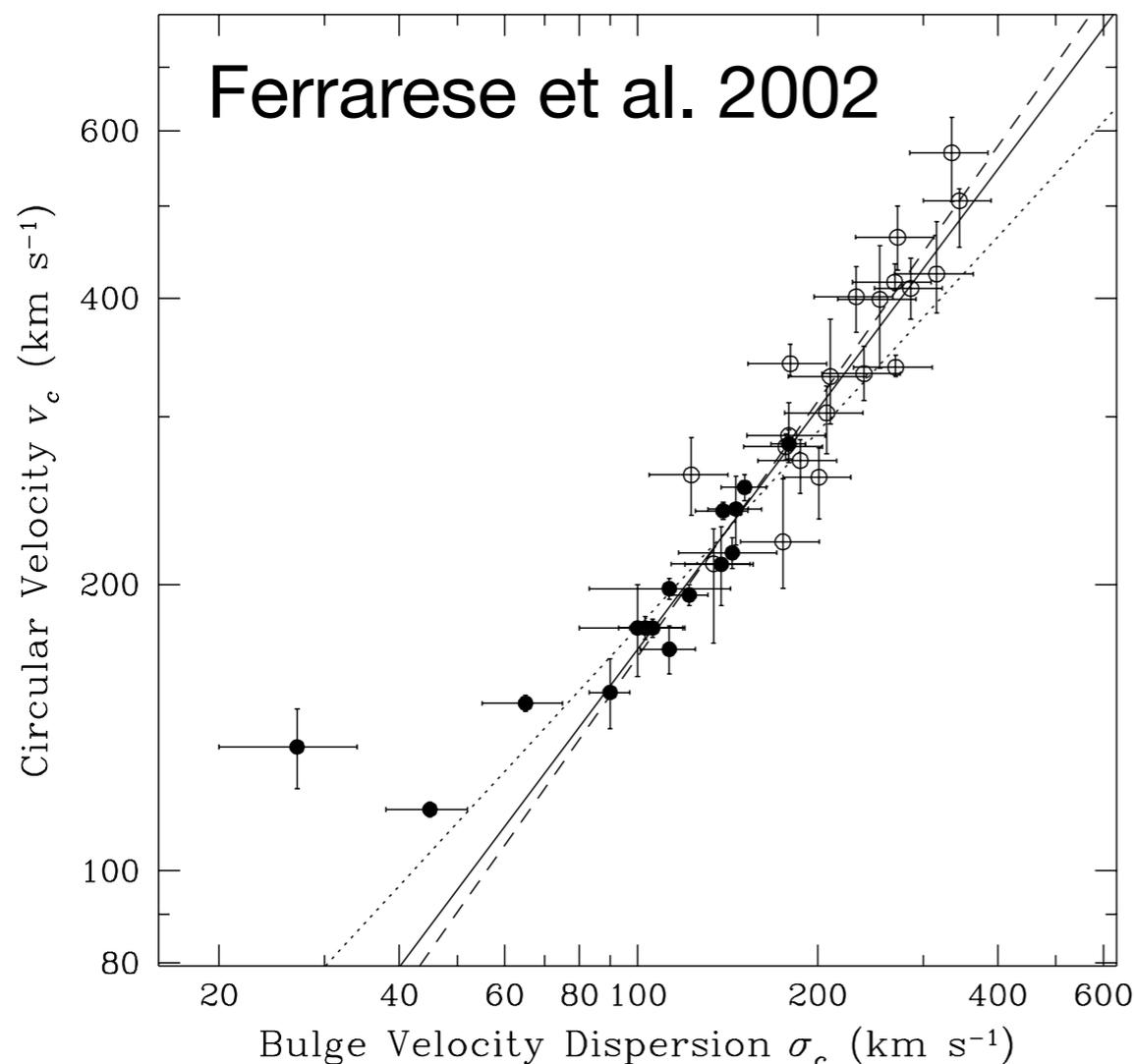
# $M_{BH}$ vs number of GCs



- ★ Burkert & Tremaine (2010) presented a correlation between  $M_{BH}$  and number of Globular Clusters implying  $M_{BH} \sim$  total mass in GCs
- ★ Snyder et al. (2011) show that there is not a direct “physical” correlation between  $M_{BH}$  and  $N_{GC}$ , but that  *$N_{GC}$  is directly linked to  $M_{star}$  and  $\sigma$ , and through them, to  $M_{BH}$*

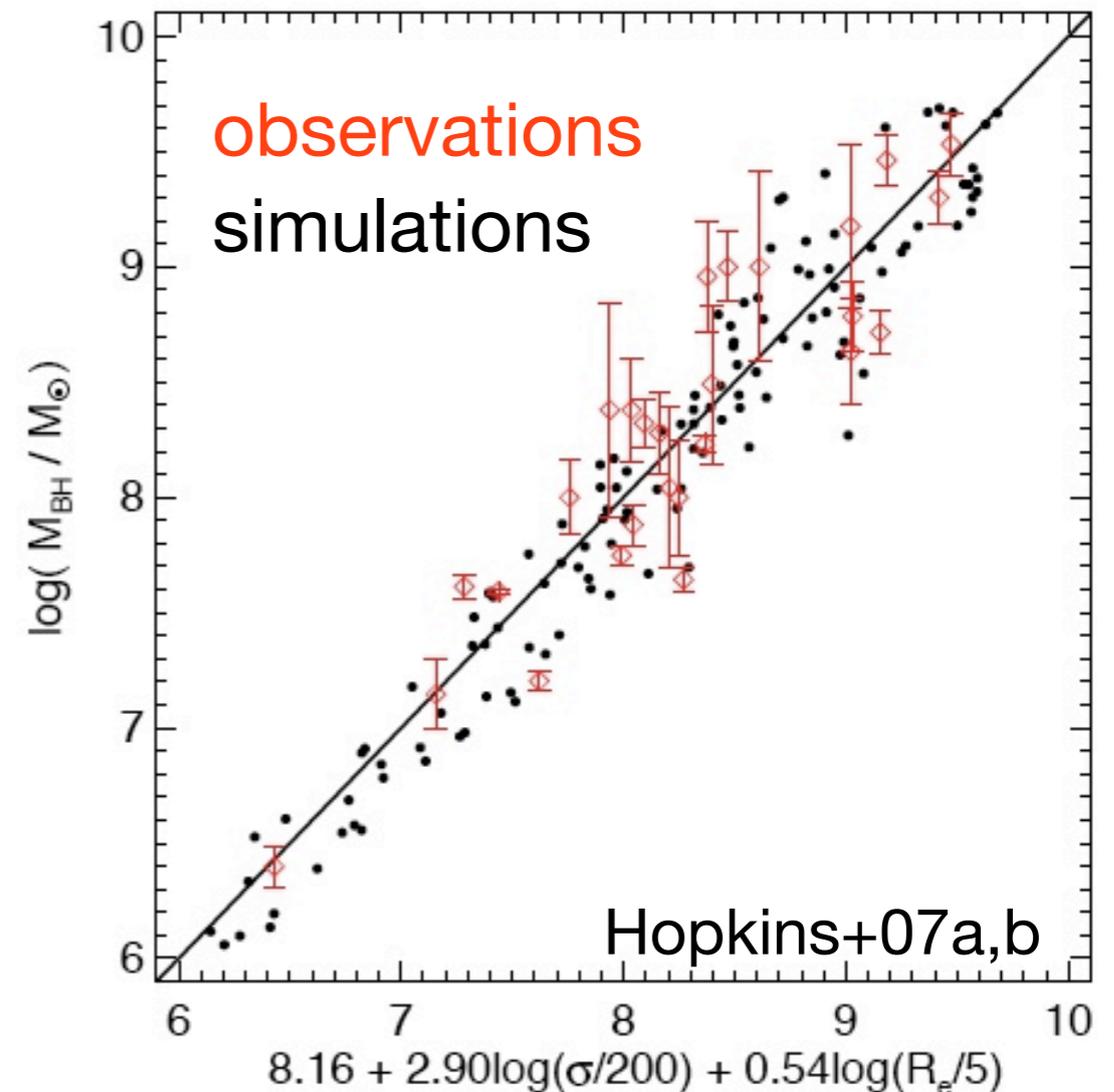
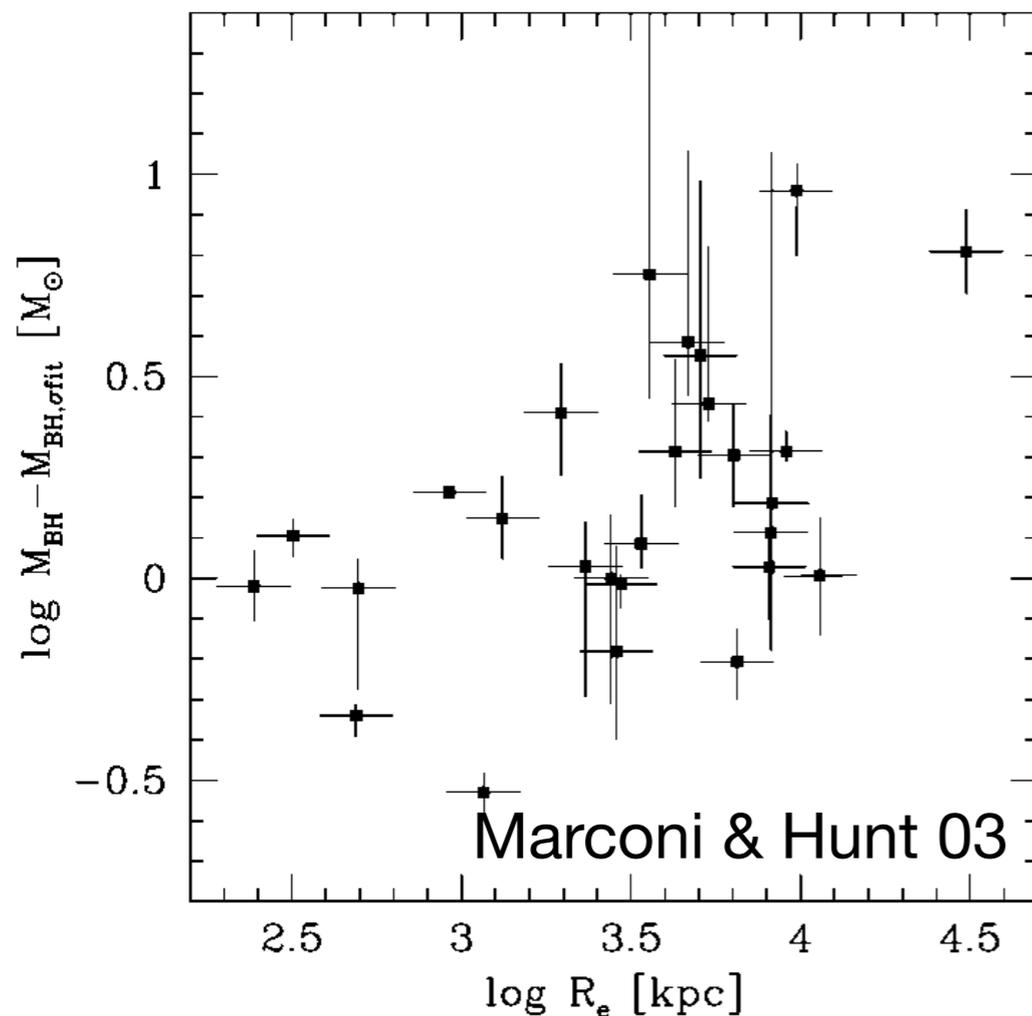
# $M_{\text{BH}}$ -dark matter halo

- ★ Ferrarese et al. 2002 find a tight correlation between  $\sigma$  and the galaxy circular velocity  $V_c$  measured where rotation curve is flat
- ★ Since  $\sigma$  is related to  $M_{\text{BH}}$ , and  $V_c$  is related to  $M_{\text{DM}}$  (mass of dark matter halo), this implies a non-linear relation  $M_{\text{BH}}-M_{\text{DM}}$  ( $M_{\text{BH}}/M_{\text{DM}} \sim 10^{-4} - 10^{-5}$ )
- ★ Recently questioned by Kormendy et al. 2011.
- ★ No correlation at all or does it break down at small  $\sigma$ ?
- ★ In any case, is it a real relation, or a “secondary” one like for  $n$  and  $N_{\text{GC}}$ ?



# BH fundamental plane

- ★ Correlation of  $M_{\text{BH}}$  with virial bulge mass ( $\sim R_e \sigma^2$ ) suggests that  $M_{\text{BH}}$  might correlate with combination of  $R_e$ ,  $\sigma$
- ★ Indeed residuals of  $M_{\text{BH}}-\sigma$  (weakly) correlate with  $R_e$  (Marconi & Hunt 2003)
- ★ Hopkins et al. (2007a,b) propose a “fundamental plane” for  $M_{\text{BH}}$  found *both in data and from models* (see also Barway & Kembhavi 07, Aller & Richstone 07, Feoli & Mancini 2009).



# BH fundamental plane

- ★ The BH fundamental plane is in practice a correlation of BH mass with gravitational binding energy (Hopkins et al. 2007, Aller & Richstone 2007, Feoli & Mancini 2009)

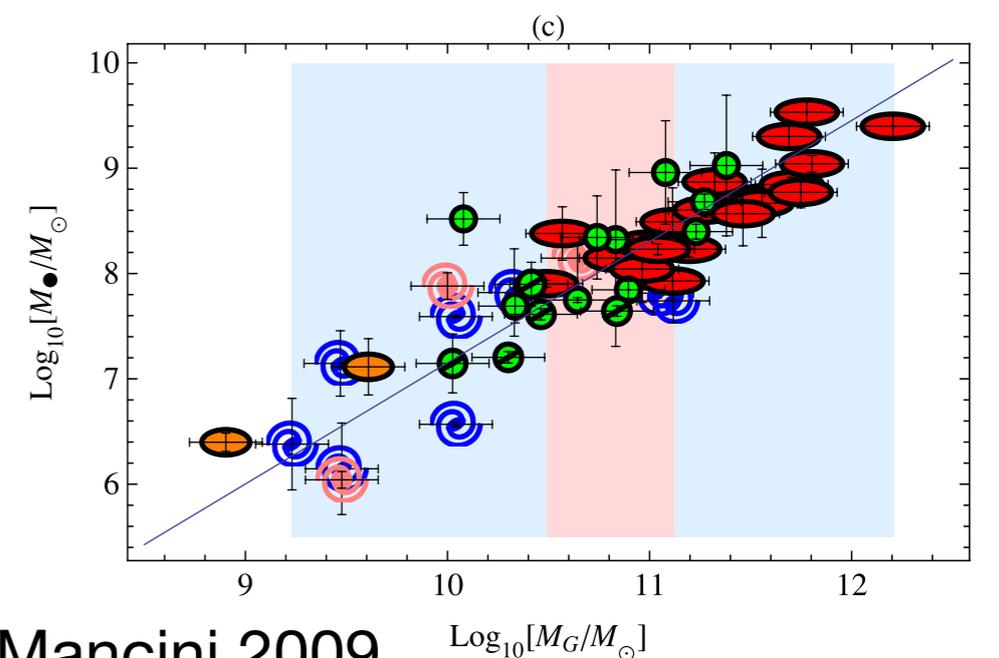
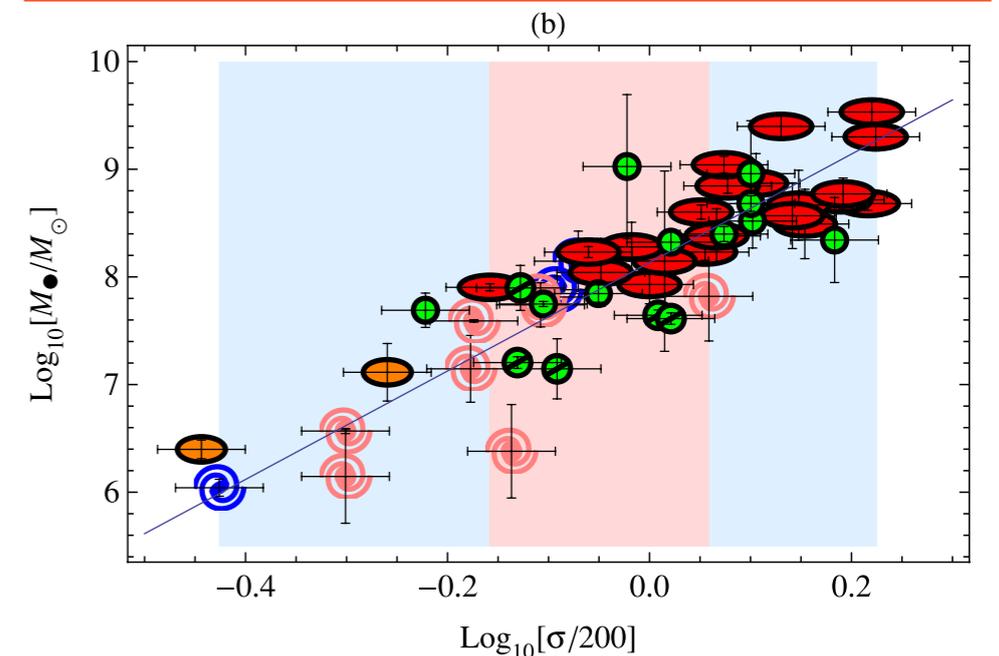
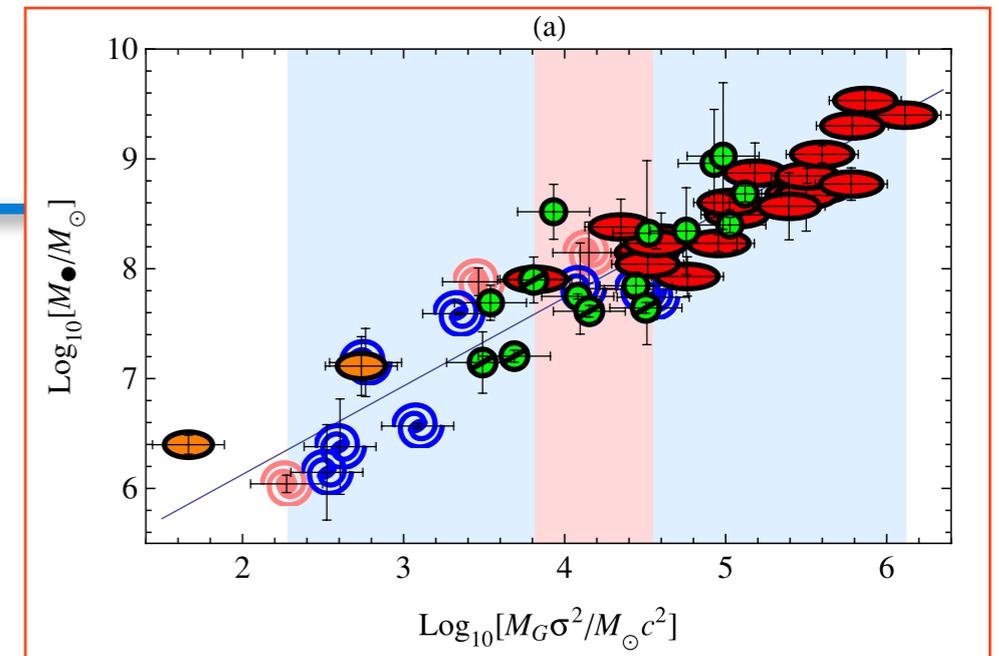
$$M_{\text{BH}} \sim (M_{\text{vir}} \sigma^2)^{0.7-0.8}$$

- ★ Virial theorem (K kinetic energy, W gravitational binding energy) states

$$W + 2K = 0$$

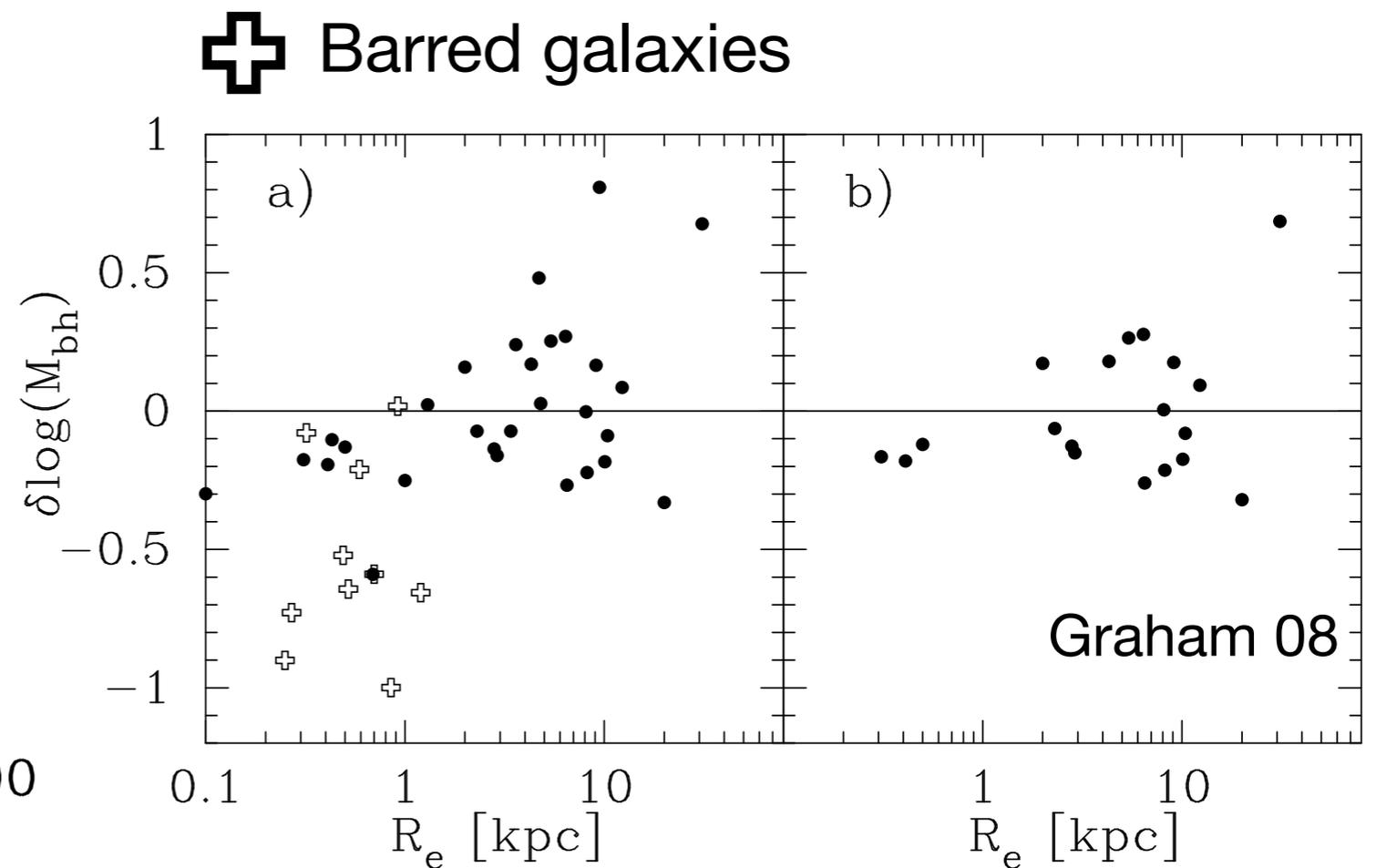
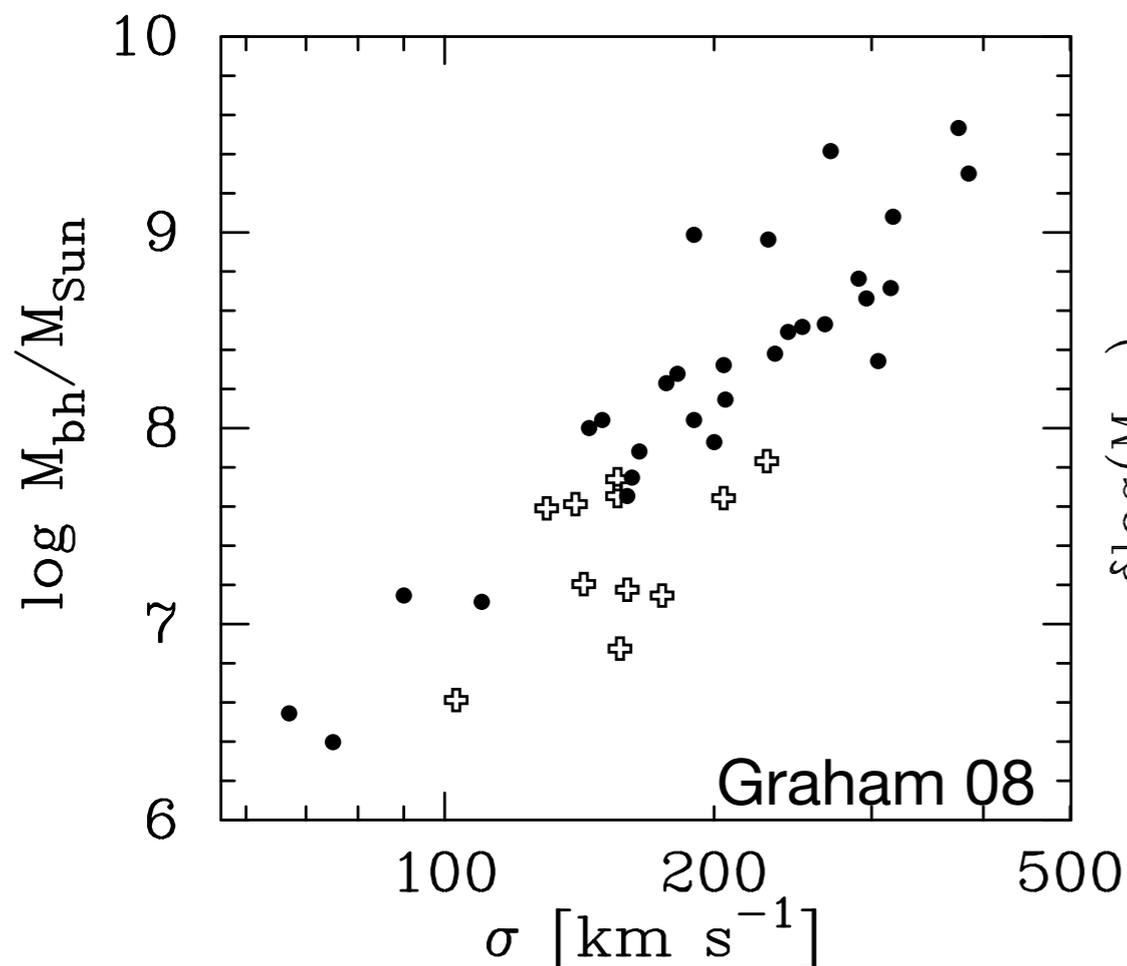
hence

$$|W| = 2K = M\sigma^2 \sim M_{\text{vir}}\sigma^2 \propto R_e\sigma^4$$



# BH fundamental plane?

- ★ Graham 08 shows
  - Barred galaxies are systematically offset from  $M_{\text{BH}}-\sigma$  relation (but not from  $M_{\text{BH}}-L$ )
  - the need of FP is driven by “barred” galaxies. The bar affects  $\sigma$  and a combination of  $\sigma$ ,  $R_e$  gives a tighter relation.
- ★ Hu 08 notices the offset nature of “pseudobulges” (from mostly barred galaxies) in  $M_{\text{BH}}-\sigma$  relation



# Pseudobulges

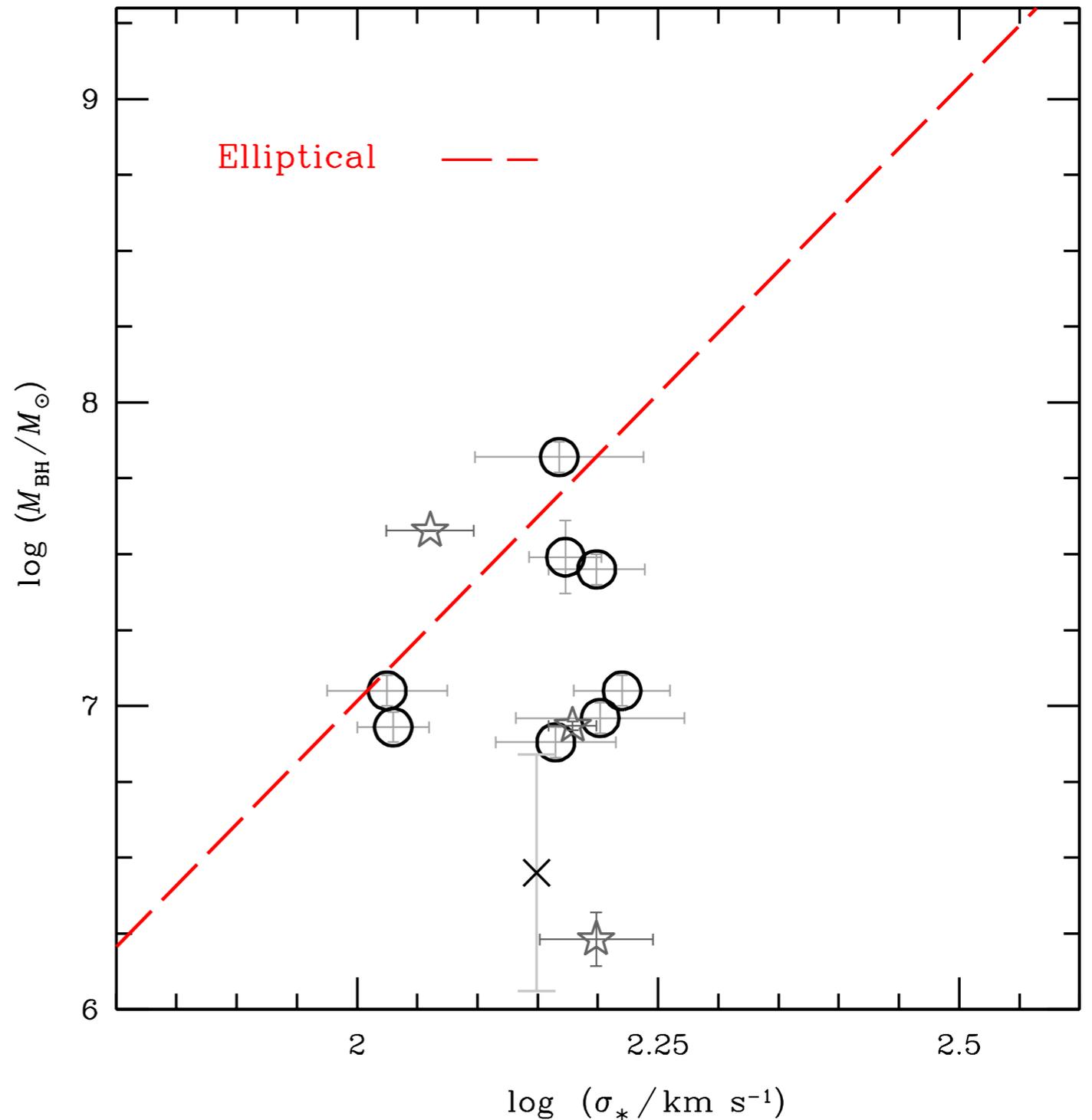
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A pseudobulge is a bulge with disk-like properties and therefore is different from a “classical” bulge (see review by Kormendy & Kennicutt 2004)

- has a flatter, more disk-like shape than a classical bulge
  - is mostly rotation supported (i.e.  $V_{\text{rot}}/\sigma$  larger than in bulges)
  - is deviant in L- $\sigma$  (Faber-Jackson) relation for having small  $\sigma$
  - can show spiral structure or nuclear bars (within the bulge part of profile)
  - nearly exponential surface brightness profiles (e.g.  $n < 2$ )
  - has star formation and younger stellar populations than classical bulges
- ★ *Pseudobulges resides mostly in barred and oval galaxies  
(pseudobulges  $\leftarrow \rightarrow$  barred galaxies)*
- ★ Classical bulges are believed to be the result of the merger driven galaxy formation process, same structural properties as elliptical galaxies
- ★ *Pseudobulges are believed to be the result of secular processes in the disk driven by non-axisymmetries in the potential: a bar can build a concentration of gas and stars in the center of a galaxy which then becomes a pseudobulge*

# Pseudobulges

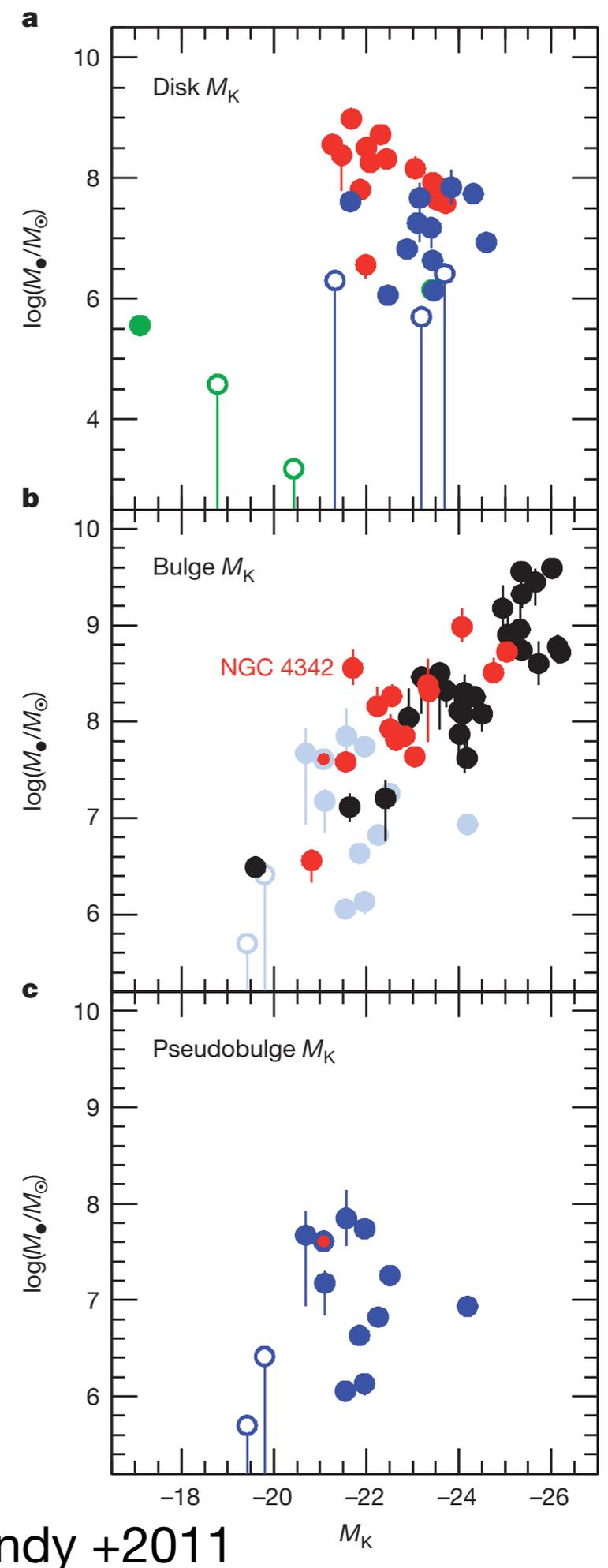
- ★ Accurate  $M_{\text{BH}}$  measurements from  $\text{H}_2\text{O}$  masers are offset w.r.t. relation for Elliptical galaxies (Greene et al. 2010)
- ★ *At least 7 out of 9 masers galaxies have pseudobulges.*
- ★ Does this really indicate a different relation for pseudobulges, or a different  $M_{\text{BH}}-\sigma$  relation in general?



Greene et al. 2010

# Pseudobulges

- ★ “Secure” correlations are between  $M_{\text{BH}}$  and structural parameters of *ellipticals and classical bulges*
- ★ There is no correlation with disks (e.g. Kormendy et al. 2011)
- ★ Barred galaxies and pseudobulges appear deviant from  $M_{\text{BH}}$ -galaxy relations
  - ▣ it is very likely that a barred galaxy hosts a pseudobulge, likely same phenomenon
- ★ Do pseudobulges or barred galaxies define a different correlation or no correlation at all?
  - ▣ offset correlation with larger scatter (Hu 2008)
  - ▣ no correlation at all (Kormendy +2011)
- ★ What is the origin of the offset nature?
  - ▣ different BH growth?
  - ▣ dynamical effects of bar seen as *larger*  $\sigma$ ?



# A much needed summary ...

---

We have many correlations with spheroid (bulge) structural parameters

- $M_{\text{BH}}-\sigma$
- $M_{\text{BH}}-L$  ( $M_{\text{star}}$ )
- $M_{\text{BH}}-M_{\text{dyn}}$
- $M_{\text{BH}}-n$
- $M_{\text{BH}}-N_{\text{GC}}$
- $M_{\text{BH}}-M_{\text{DM}}$
- $M_{\text{BH}}$  “fundamental plane”:  $M_{\text{BH}} \sim \sigma^\alpha R^\beta$
- There might be different correlations for bulges and pseudobulges
- $M_{\text{BH}}$  does not correlate with disk properties

★ Is there a fundamental relation?

★ Are they reliable?

★ What is the physical origin of these correlations?

# Is there a fundamental relation?

---

- $M_{\text{BH}}-\sigma$
- $M_{\text{BH}}-L$  ( $M_{\text{star}}$ )
- $M_{\text{BH}}-M_{\text{dyn}}$
- $M_{\text{BH}}-n$      *likely indirect relation*
- $M_{\text{BH}}-N_{\text{GC}}$    *likely indirect relation*
- $M_{\text{BH}}-M_{\text{DM}}$    *likely indirect relation*
- $M_{\text{BH}}$  “fundamental plane”:  $M_{\text{BH}} \sim \sigma^\alpha R^\beta$
- There might be different correlations for bulges and pseudobulges  
*focus on elliptical galaxies and classical bulges only ...*
- $M_{\text{BH}}$  does not correlate with disk properties  
*forget about disks ...*

# Are these relations independent?

---

Assume the basic correlation is  $M_{BH} \sim M_{bulge}$

Combine with galaxy scaling relations:

★  $M_{BH} \sim L_{bulge}^{1.1}$  consistent with  $M_{BH} \sim M_{bulge}$  if  $(M/L)_{bulge} \sim L_{bulge}^{0.1}$  (consistent with fundamental plane)

★ Faber-Jackson  $L \sim \sigma^4$  implies  $M_{BH} \sim (\sigma^4)^{1.1} \sim \sigma^{4.4}$

All  $M_{BH}$ -galaxy correlations can be explained as the result of a fundamental relation (e.g.  $M_{BH} \sim M_{bulge}$ ) combined with galaxy scaling relations.

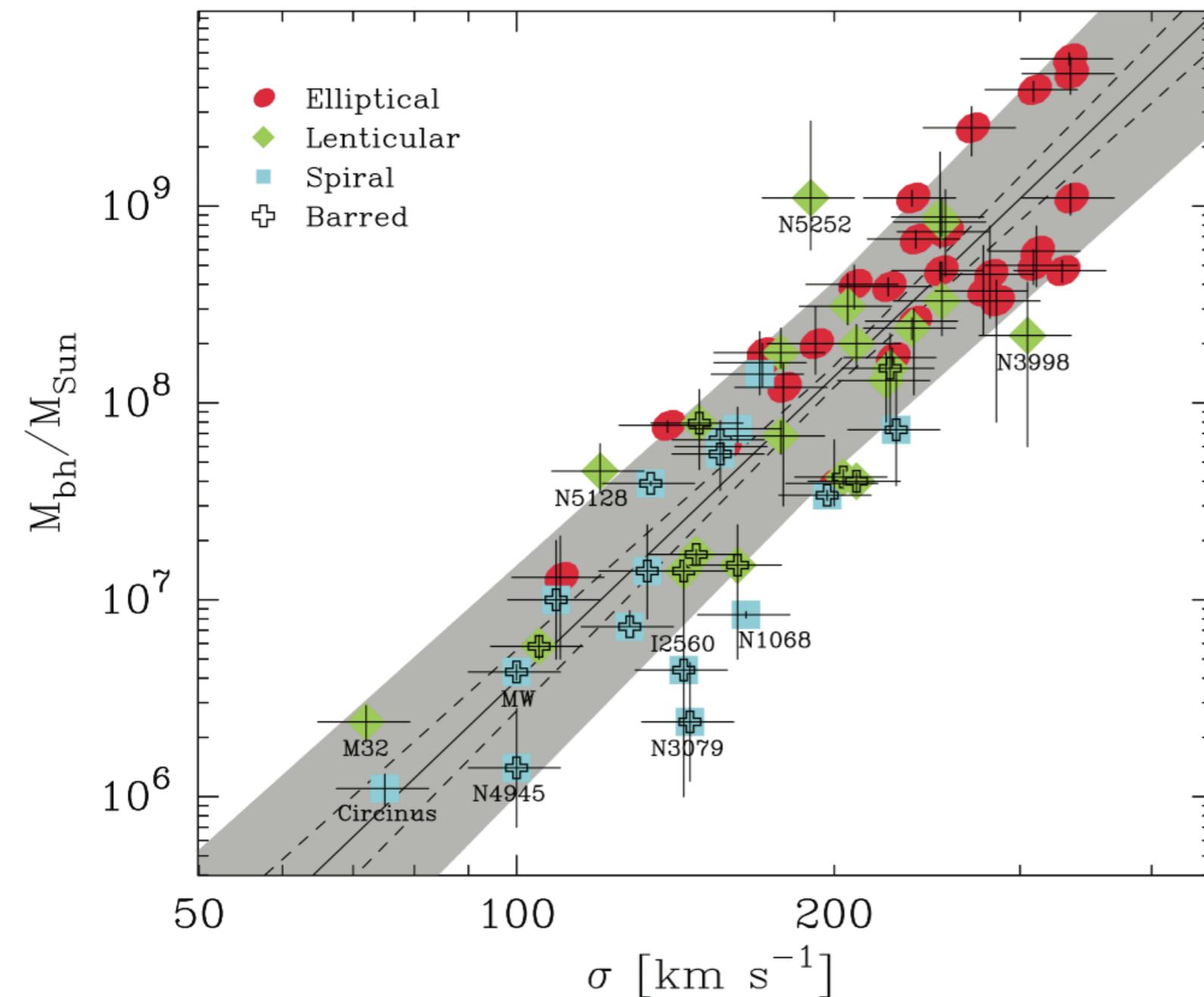
***Big Black Holes are in big galaxies!***

This argument is too simple, does not take into account intrinsic scatters but indicate that one must take into account the intrinsic relations among the various parameters (eg. Fundamental Plane of elliptical galaxies).

# Observational biases

Recall the  $R_{\text{BH}} = \Delta\theta$  for BH detection, then maximum distance at which a BH can be detected is

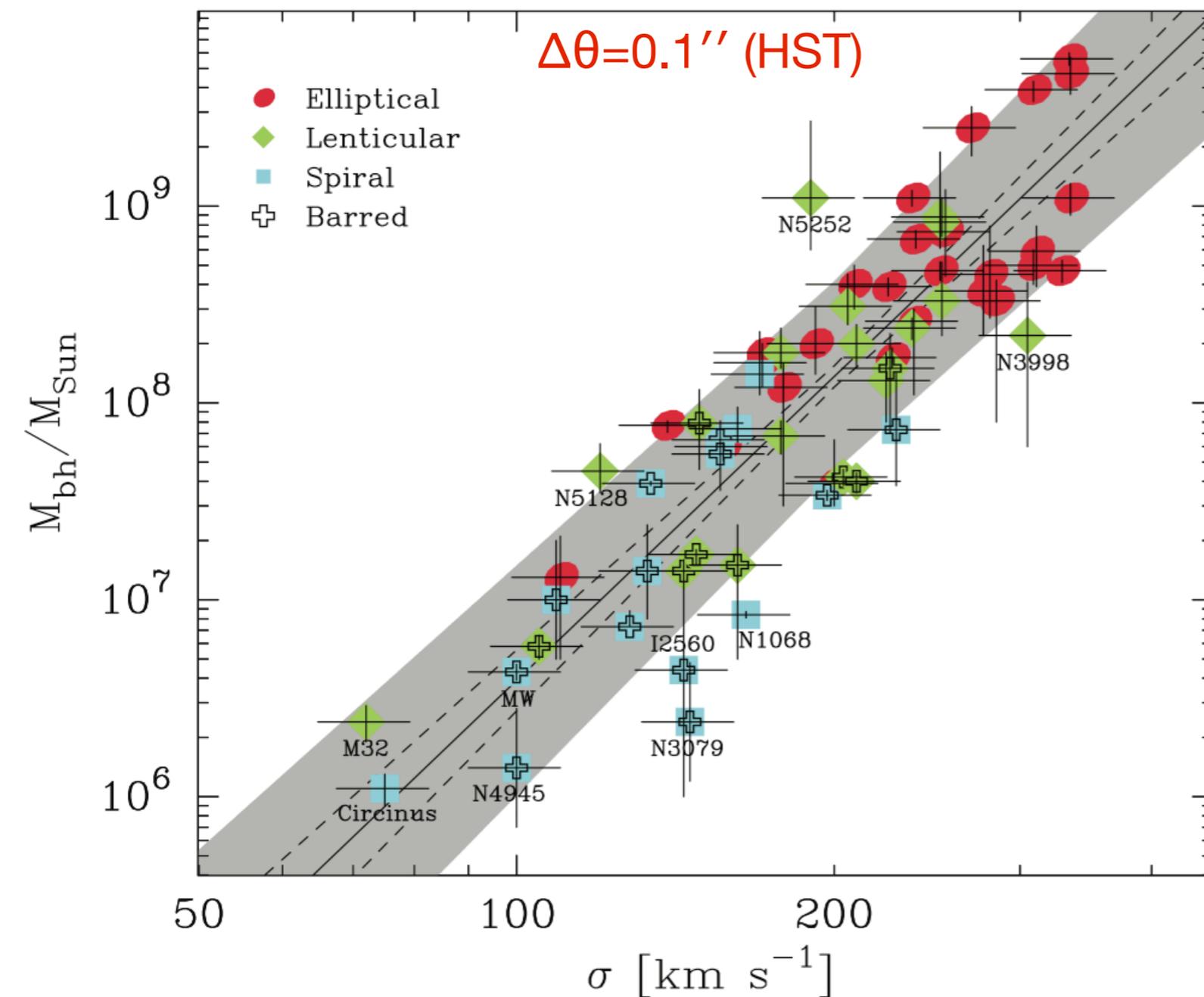
$$D = 22 \text{ Mpc} \left( \frac{M_{\text{BH}}}{10^8 M_{\odot}} \right) \left( \frac{\sigma_{\star}}{200 \text{ km/s}} \right)^{-2} \left( \frac{\Delta\theta}{0.1''} \right)^{-1}$$



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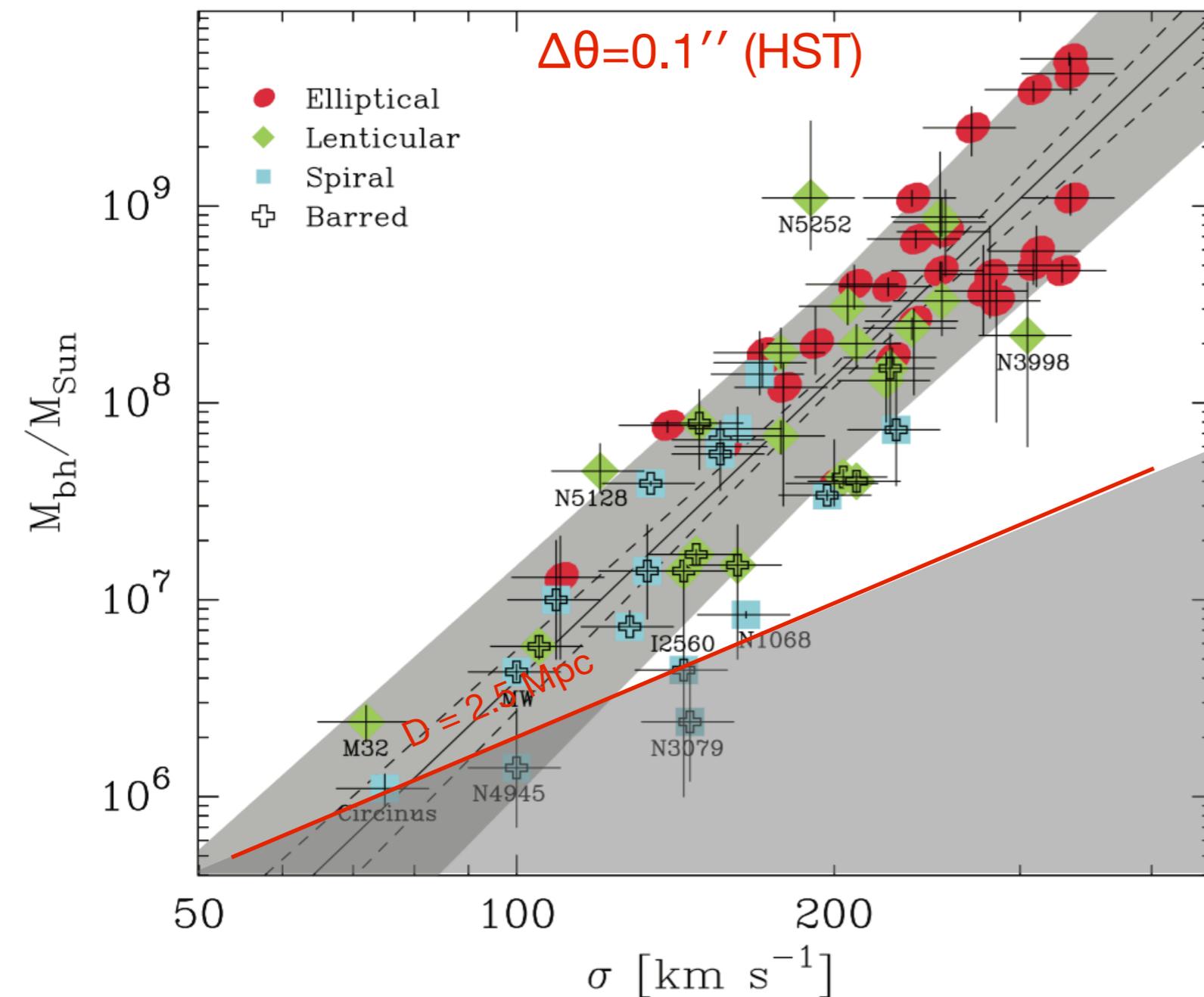
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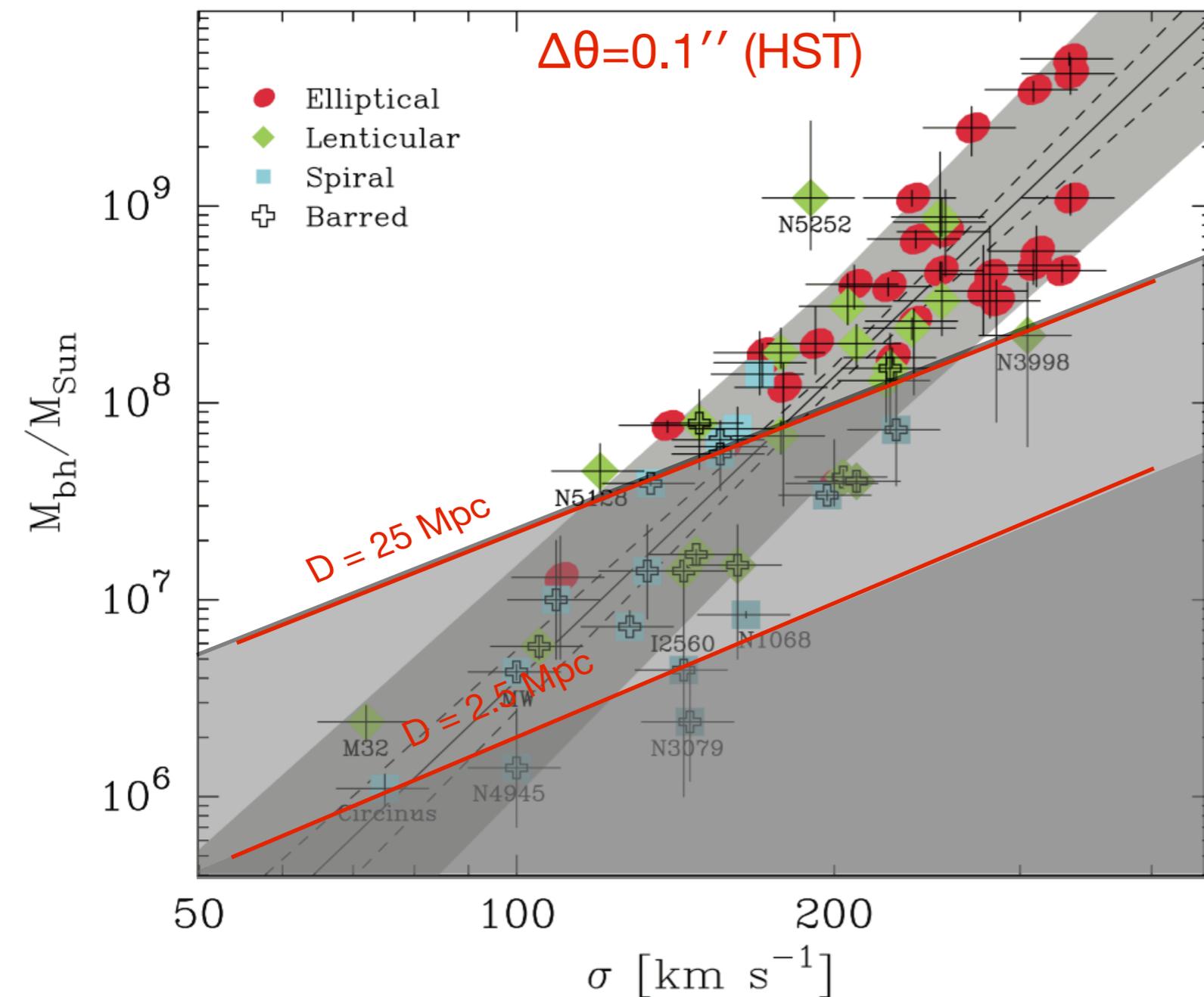
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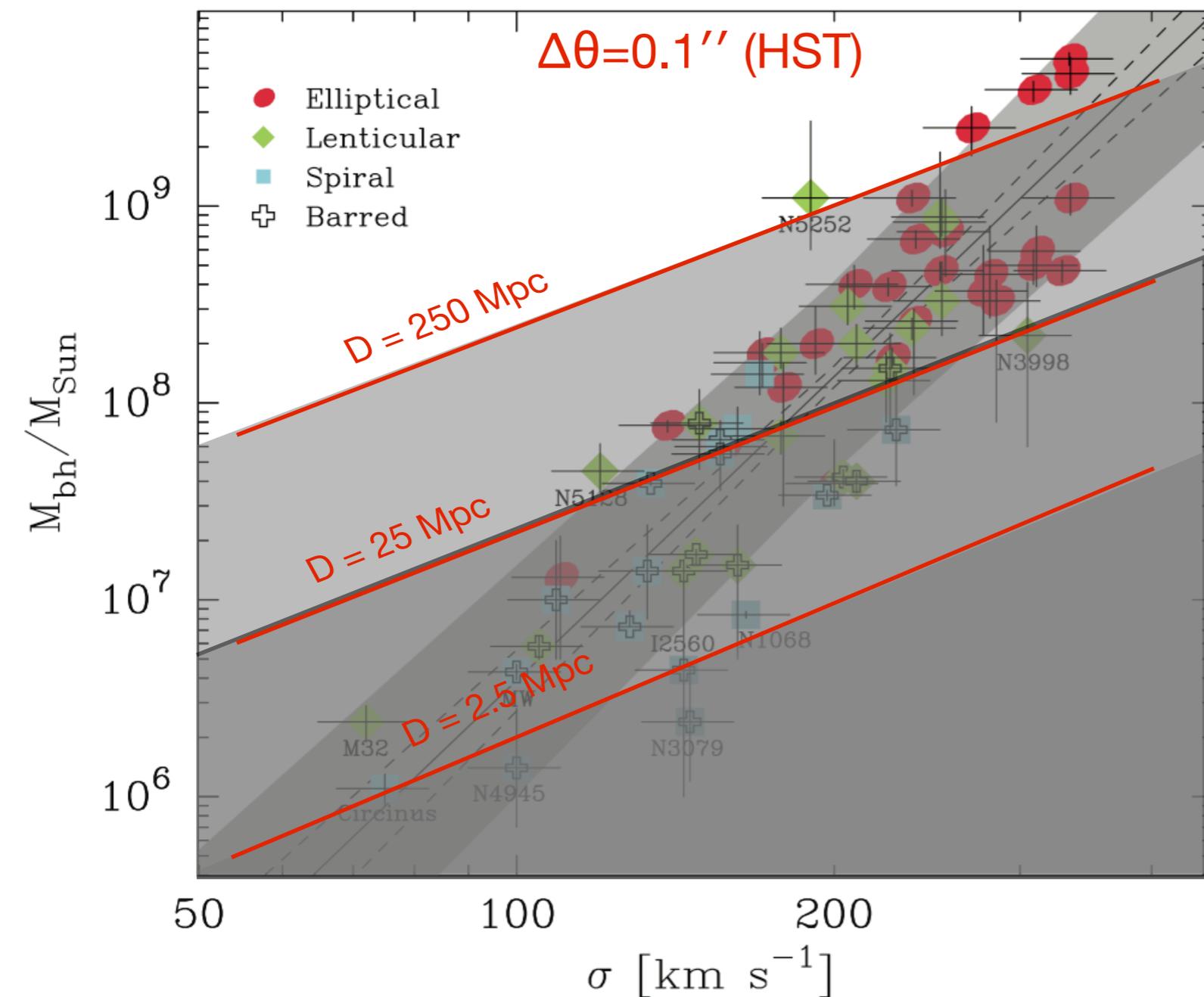
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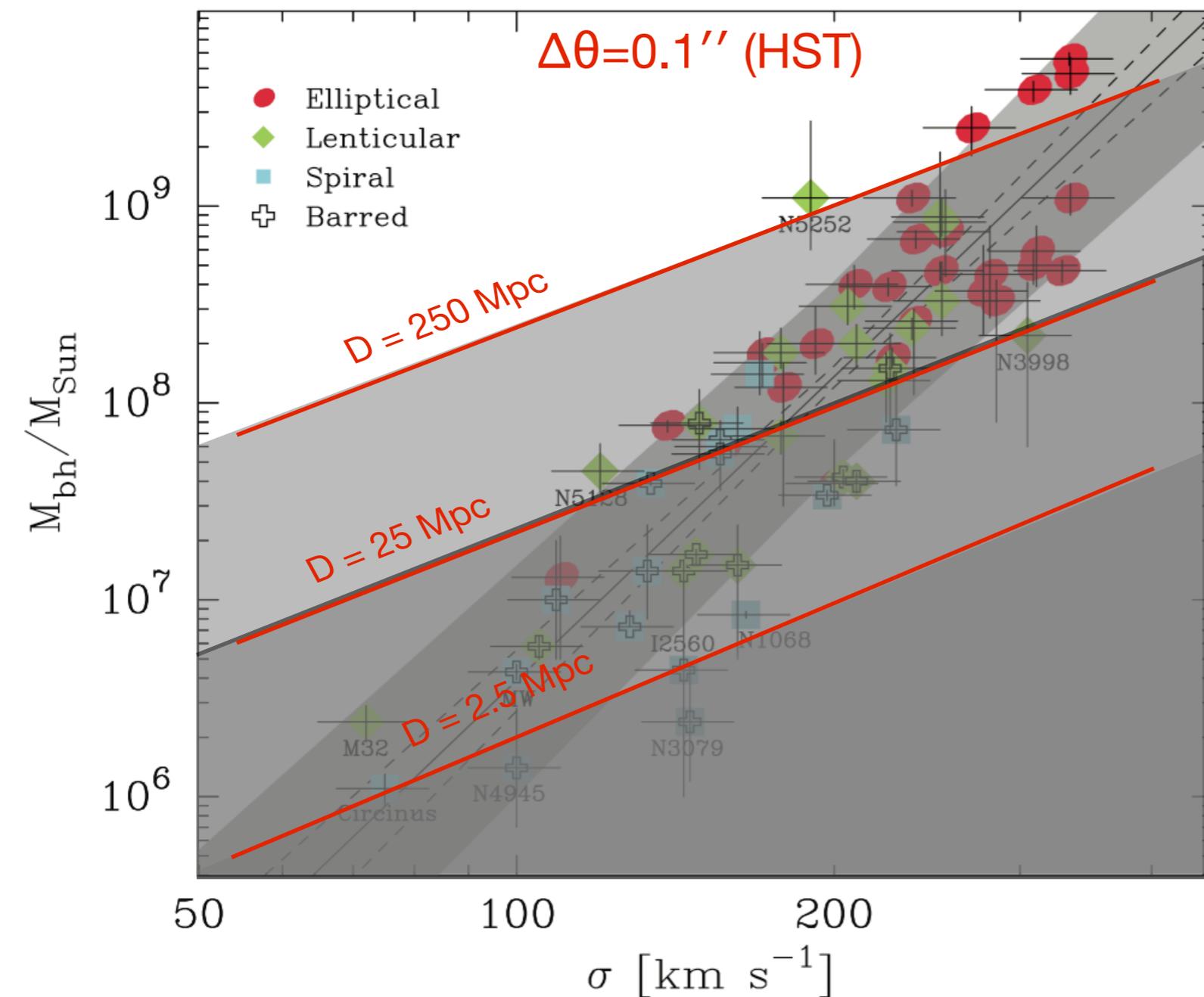
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NO detection areas on  $M_{BH}-\sigma$  diagram for given  $\Delta\theta$ ,  $D$ :

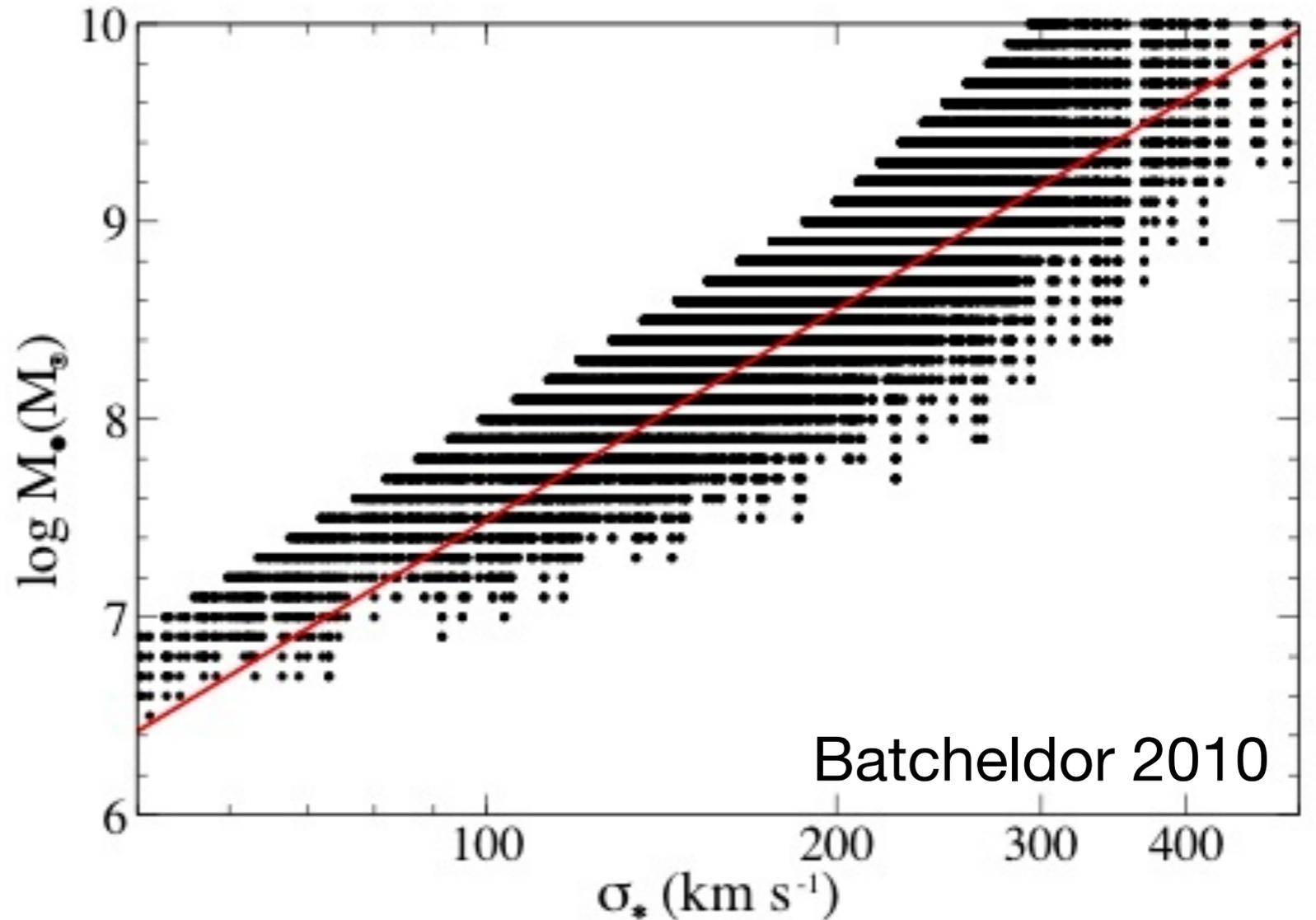
- ★ Direct  $M_{BH}$  measures are limited to the local universe ( $D \sim 250$  Mpc)
- ★ There are definitely no BHs above the correlation (big BHs in small galaxies)
- ★ The area below the correlation is 'biased' and cannot be explored (small BHs in big galaxies?)

# An upper envelope?

$M_{\text{BH}}-\sigma$  an “upper envelope”?

Batcheldor (2010):

- ★ Take all galaxies with  $\sigma$  from Leda database and assign them random  $M_{\text{BH}}$  within  $0-M_{\text{BH}}(\sigma)$
- ★ cut away those objects for which  $R_{\text{BH}} < 0.1''$  (max spatial resolution with HST)
- ★ Observed  $M_{\text{BH}}-\sigma$  with correct slope and scatter is reproduced!
- ★ We are missing small BHs in large galaxies (if they exist).
- ★  *$M_{\text{BH}}-\sigma$  might be an upper envelope!*
- ★ *However analysis by Gültekin et al. 2011 suggests this is not possible (at least in Early types) because we have too many detections already ...*



# Problems and open issues

Problems and open issues  
(beyond those on  $M_{\text{BH}}$ ):

★ 64 galaxies with  $M_{\text{BH}}$   
(Graham+2010)

★ difficult to assess the  
reliability and accuracy of  
all points;

★ few points at low/high  
mass ends

■ #9  $10^6 < M_{\text{BH}} < 10^7 M_{\odot}$

■ #7  $10^9 < M_{\text{BH}} < 5 \cdot 10^9 M_{\odot}$

★ mostly E/S0, few spirals

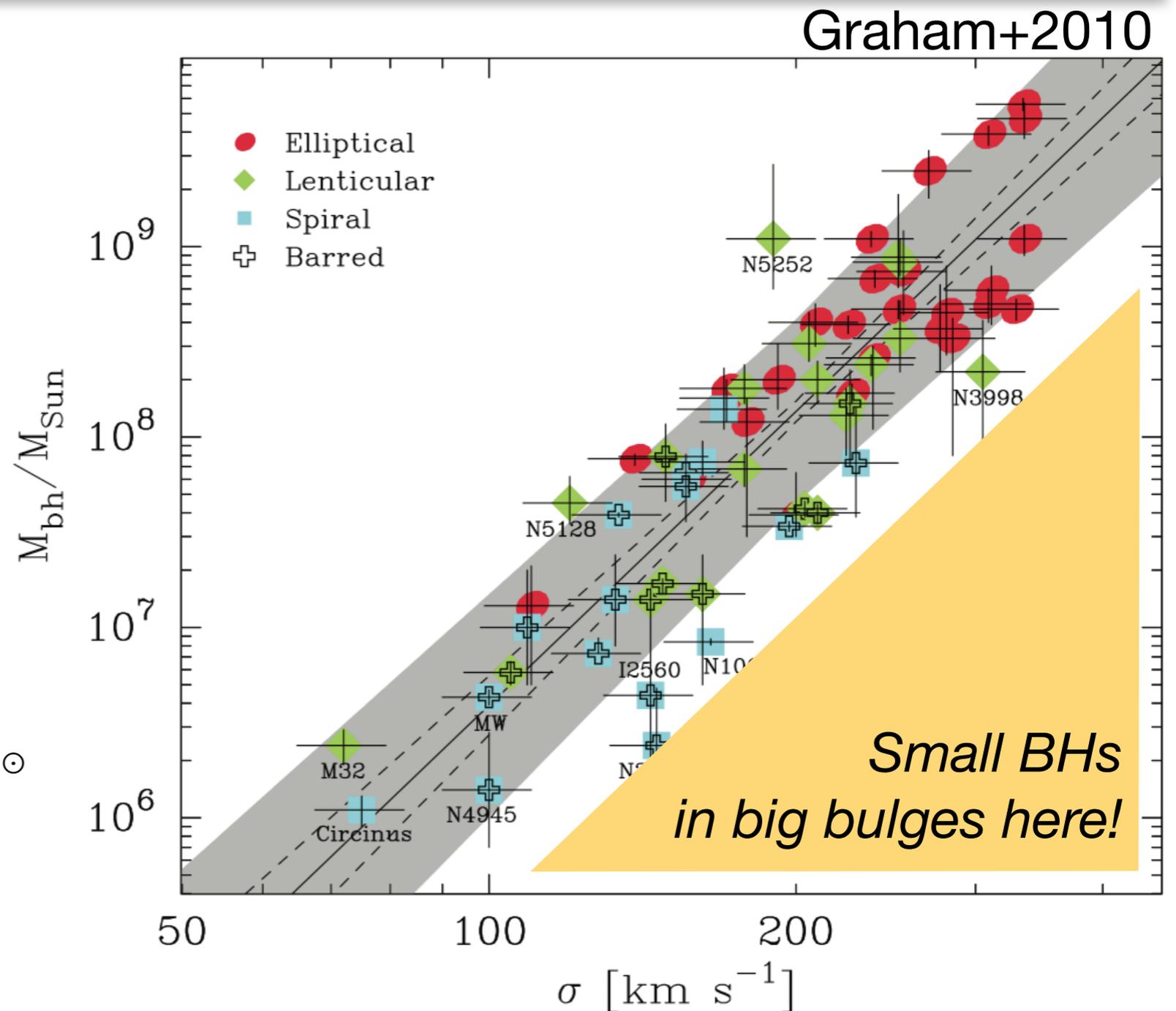
■ #48 E+S0

■ #16 Spirals

★ is there really a BH fundamental plane?

★ do all galaxies follow the same correlation?

★ are there small BHs in massive galaxies (e.g.  $M_{\text{BH}}$ -galaxy relations an upper envelope)?



# What is the physical origin?

---

How does the BH know about its host galaxy and galaxy about its BH?

Radius of BH sphere of gravitational influence:  $R_{BH} = \frac{GM_{BH}}{\sigma_{\star}^2}$

Observed correlation:

$$M_{BH} \simeq 10^{-3} M_{sph}$$

Spheroid virial mass:

$$M_{sph} \simeq 5 \frac{\sigma_{\star}^2 R_{sph}}{G}$$

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Spheroid virial mass:

$$M_{sph} \simeq 5 \frac{\sigma_{\star}^2 R_{sph}}{G}$$

$$R_{BH} = \frac{GM_{BH}}{\sigma_{\star}^2} \simeq 5 \times 10^{-3} R_{sph}$$

$$V_{BH} \simeq 1.3 \times 10^{-7} V_{sph}$$

The volume under the BH influence is only  $\sim 10^{-7}$  of the total volume.

No gravitational “exchange” of information!

# BH-galaxy coevolution

---

If BH grown by accretion, the energy released during growth is

$$L = \varepsilon \dot{M}_{acc} c^2$$

$$\dot{M}_{BH} = (1 - \varepsilon) \dot{M}_{acc}$$

$$E_{grow} = \frac{\varepsilon}{1 - \varepsilon} M_{BH} c^2$$

The gravitational binding energy of the virialized spheroid is

$$E_{grav} \simeq M_{sph} \sigma_{\star}^2$$

$$\frac{E_{grow}}{E_{grav}} \simeq \frac{\varepsilon}{1 - \varepsilon} \left( \frac{M_{BH}}{M_{sph}} \right) \left( \frac{\sigma_{\star}}{c} \right)^{-2} = 250 \left( \frac{\sigma_{\star}}{200 \text{ km s}^{-1}} \right)^{-2}$$

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Energy released by accreting BH (i.e. AGN) can affect galaxy structure and can unbind, eg, gas in the galaxy.

AGN feedback can let the galaxy know about the BH!

By regulating the feeding to the BH the galaxy can let the BH know about it!

# The need for AGN feedback (eg King 2010)

- ★ Assume AGN emit (close) to the Eddington ratio and that there is a radiation driven outflow from the AGN: can explain  $M_{\text{BH}}-\sigma$
- ★ Two relevant cases for  $\dot{m} = \dot{M} / \dot{M}_{\text{Edd}}$ 
  - $\dot{m} \sim 1$  momentum driven outflow which sweeps ISM in a shell. This shell recollapses unless  $M_{\text{BH}}$  has reached critical value

$$M_{\text{BH}} = \frac{f_g \sigma_T}{\pi m_p G^2} \sigma^4 = 3.7 \times 10^8 M_{\odot} \left( \frac{\sigma}{200 \text{ km}} \right)^4$$

*~OK*

- $\dot{m} \gg 1$  energy driven outflow which sweeps ISM gas in a shell; imposing expansion work equal to E injection rate (Silk & Rees 1998)

$$M_{\text{BH}} = \frac{f_g \sigma_T}{\pi m_p G^2 c} \sigma^5 = 2.4 \times 10^5 M_{\odot} \left( \frac{\sigma}{200 \text{ km}} \right)^5$$

*too small!*

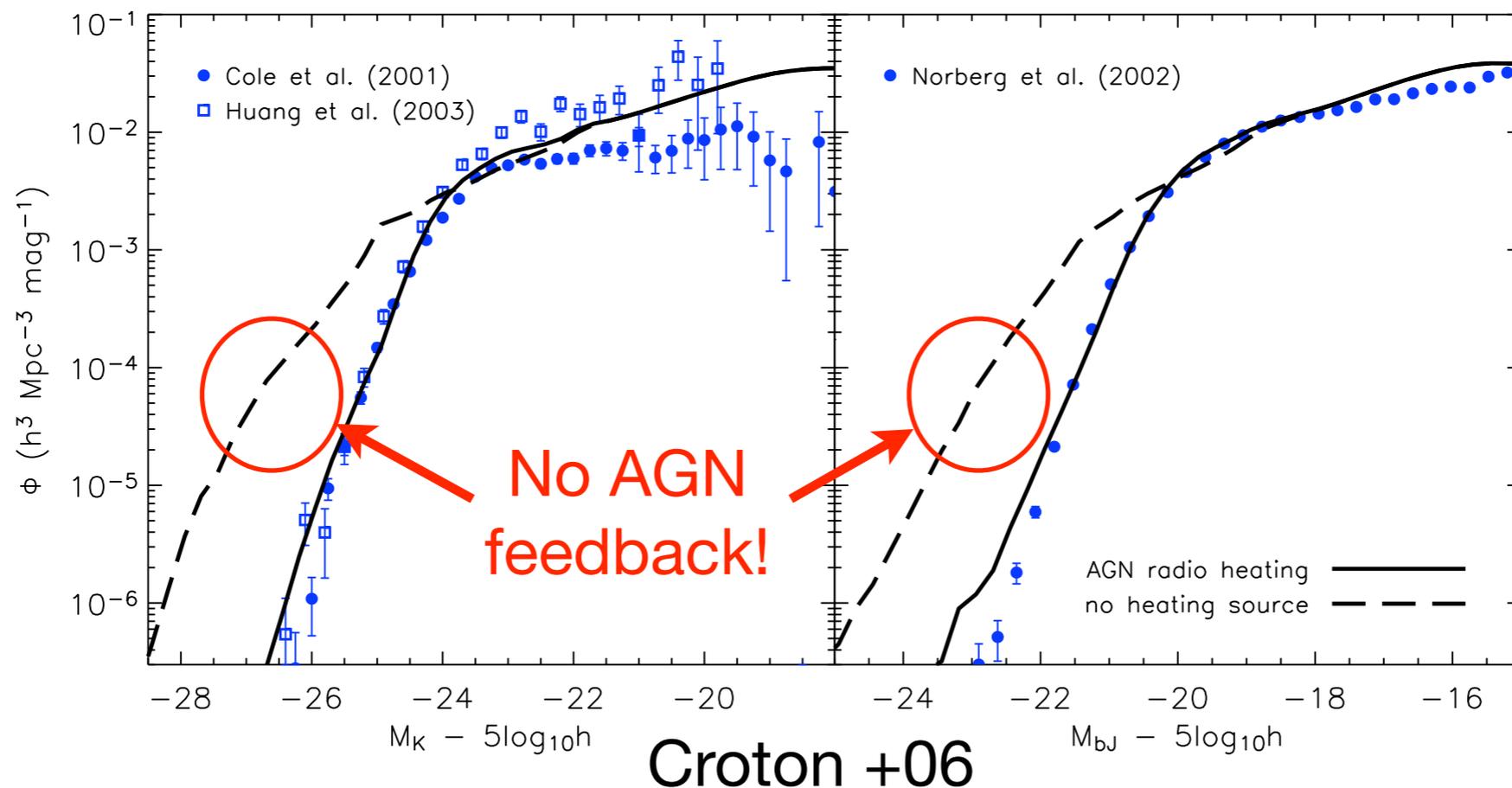
- ★ Slope and normalization different in the two cases
- ★ No free parameters, the energy driven case does not seem to appear in nature (bubble blown in energy driven case should break up for Rayleigh-Taylor instability due to large density contrast in shock)

# The need for AGN feedback

AGN feedback (i.e. BH growth) can affect galaxy growth and explain  $M_{\text{BH}}$ -galaxy relation → **Cedric's lectures**

But AGN feedback is also needed to explain observed galaxy properties (e.g. apparent anti-hierarchical behaviour of galaxy evolution, red colors of ellipticals, steepness of optical luminosity function).

*AGN phases are fundamental in the evolution of galaxies.*



# The ultimate goal...

---

Several models can explain  $M_{\text{BH}}$ -galaxy relations with various “flavours” of AGN feedback on the host galaxy.

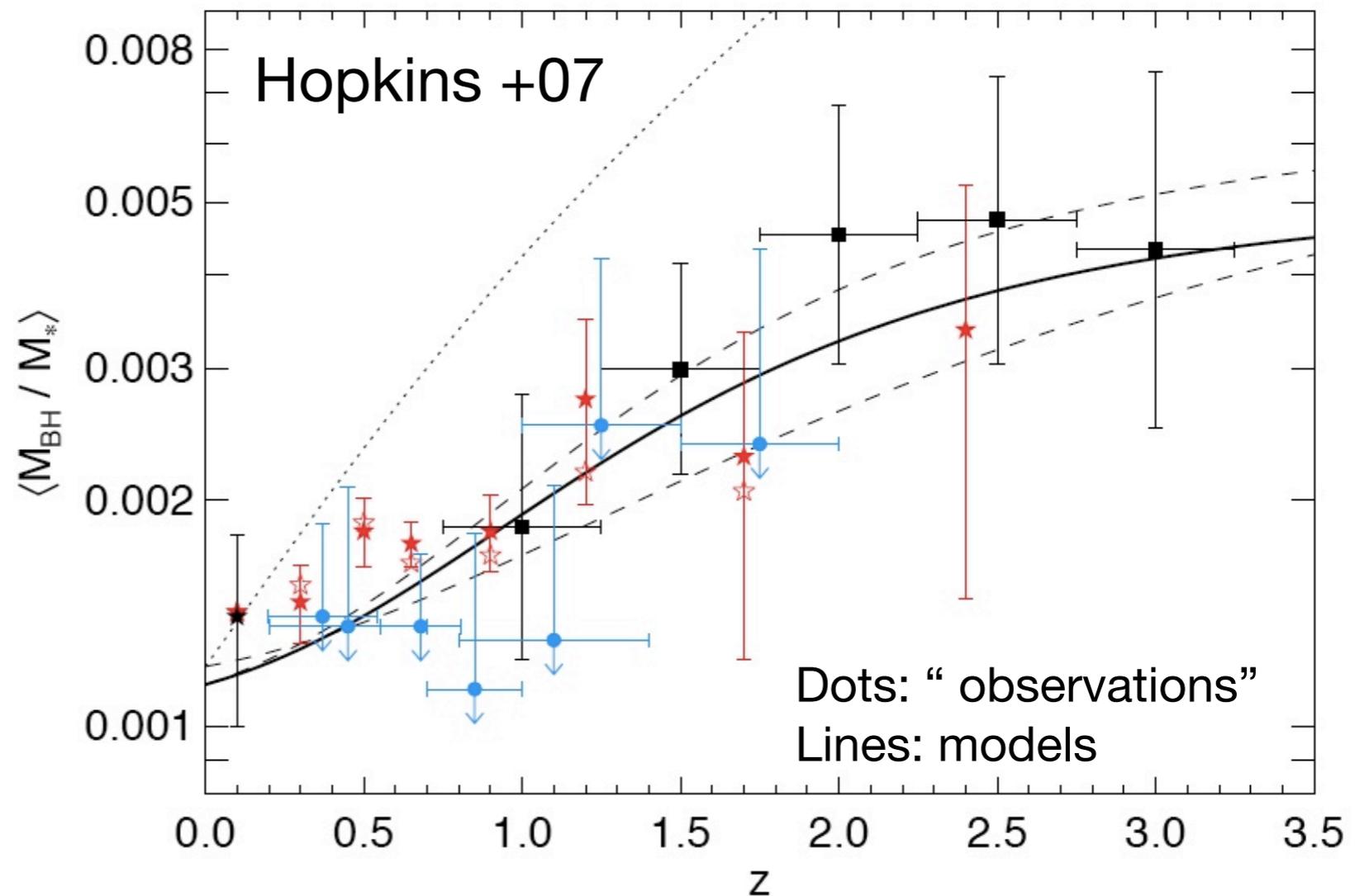
Silk & Rees 98, Kauffman & Haehnelt 00, Cavaliere & Vittorini 00, Granato+ 04, 06, Murray +04, Di Matteo+05, Cattaneo+ 05, Miralda-Escudè & Kollmeier 05, Monaco & Fontanot 05, Croton +06, Hopkins +06, Malbon +06, Marulli +08

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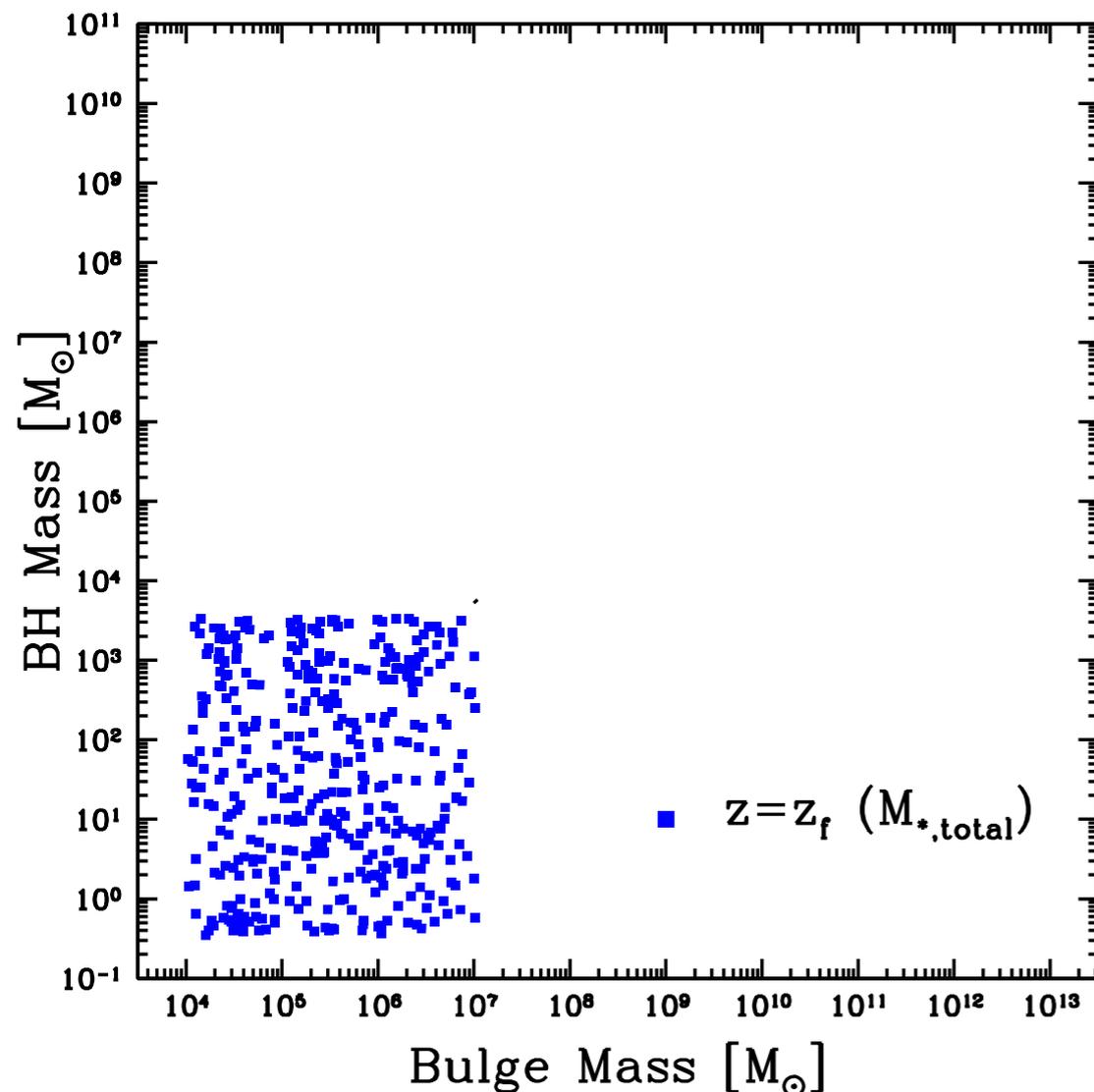
Redshift evolution of  $M_{\text{BH}}$ -galaxy relations can constraint BH growth and galaxy evolutionary models.



Fundamental to measure  $M_{\text{BH}}$  at ALL redshifts!

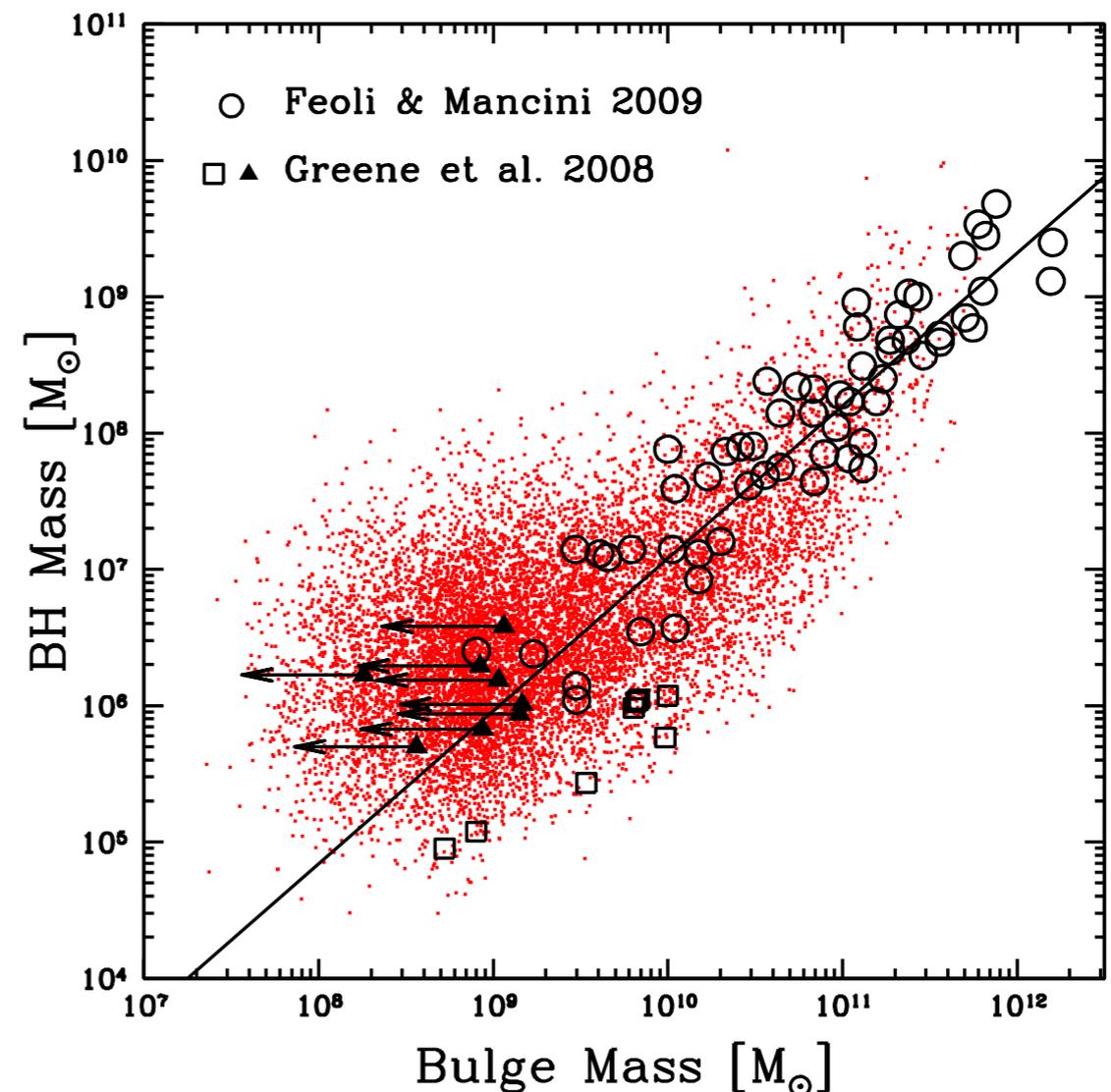
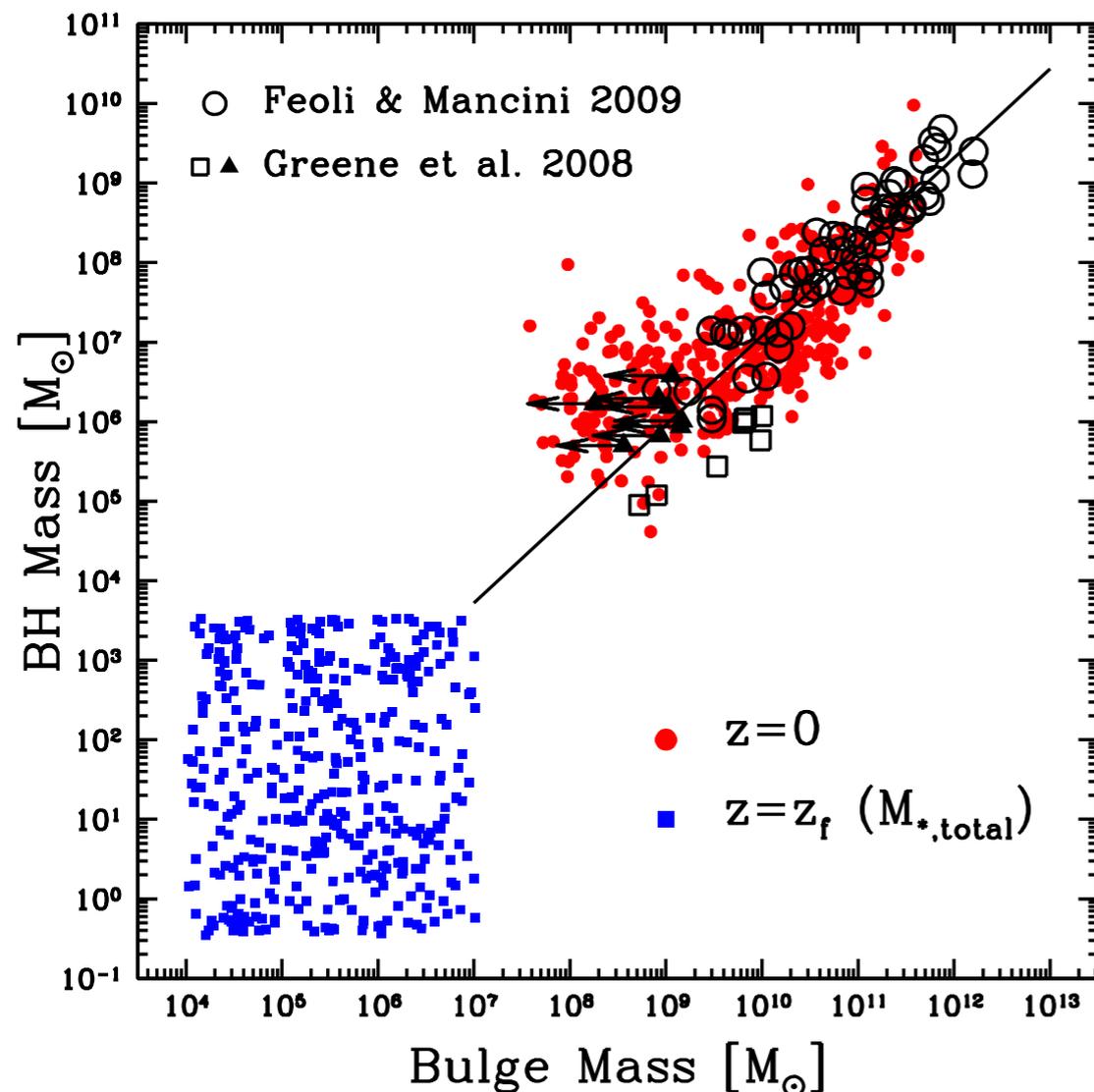
# Do we really need feedback?

- ★ Populate dark halo merger trees with uncorrelated BH and  $M_{\text{star}}$
- ★ Follow evolution with recipes for star formation and BH accretion that reproduce what is globally observed (see later) but without any coupling of the two for individual galaxies (*no feedback*).
- ★ It is possible to recreate the  $M_{\text{BH}}-M$  relation at  $z=0$  with correct slope!
- ★  $M_{\text{BH}}-M$  can also be the result of random merging events (Peng 2007)



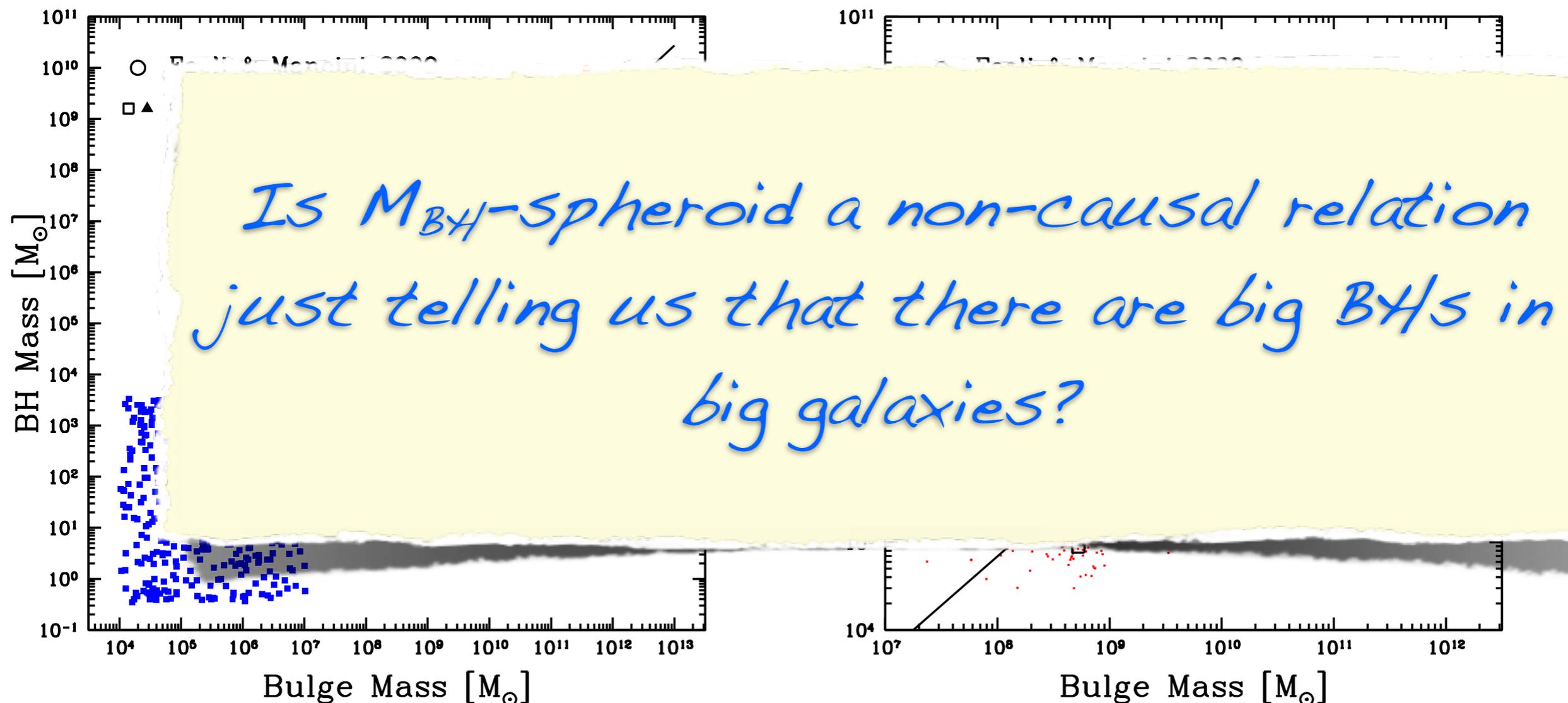
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# Demography of local black holes

---

The following ingredients allow a demography of BHs in the nearby universe:

- ★ assume BHs resides in the nuclei of *all* nearby galaxies
- ★ assume *all* BHs follow the scaling relations with host spheroid (bulge):  
 $M_{\text{BH}}-\sigma, L$
- ★ combine with the luminosity- or  $\sigma$ - function of spheroids
- ★ obtain the mass function on BHs in the local universe

# Demography of local black holes

$$dN = \phi(M_{\text{BH}})dM_{\text{BH}}$$

number of BHs per unit volume with mass in  $M_{\text{BH}}, M_{\text{BH}}+dM_{\text{BH}}$  range

$$\phi(M_{\text{BH}}) = \int_0^{+\infty} P(M_{\text{BH}}|L_{\text{sph}})\phi(L_{\text{sph}})dL_{\text{sph}}$$

$\phi(L_{\text{sph}}), \phi(\sigma_e)$  are  $L_{\text{sph}}, \sigma_e$  functions of spheroids  
 $P(M_{\text{BH}}|L_{\text{sph}}), P(M_{\text{BH}}|\sigma_e)$  are the scaling relations written as conditional probabilities

$$\phi(M_{\text{BH}}) = \int_0^{+\infty} P(M_{\text{BH}}|\sigma_e)\phi(\sigma_e)d\sigma_e$$

$$\rho_{\text{BH}} = \int_0^{+\infty} M_{\text{BH}}\phi(M_{\text{BH}})dM_{\text{BH}}$$

BH mass density

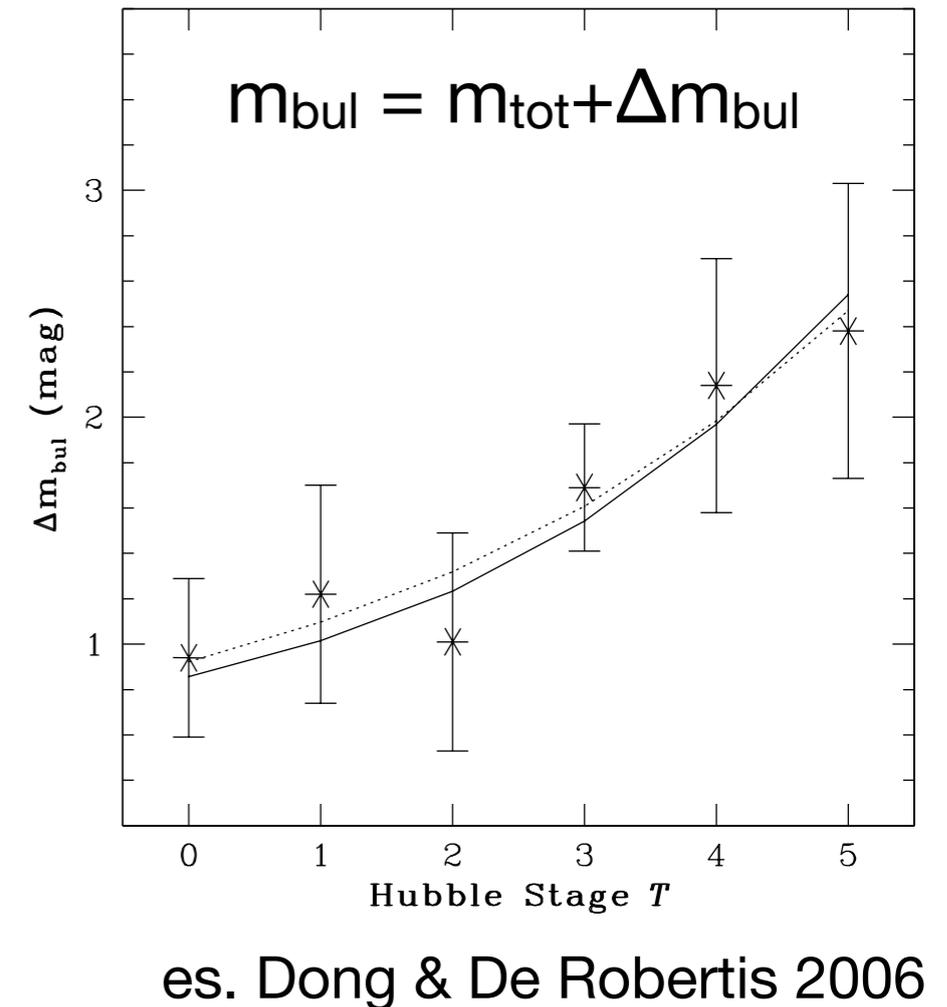
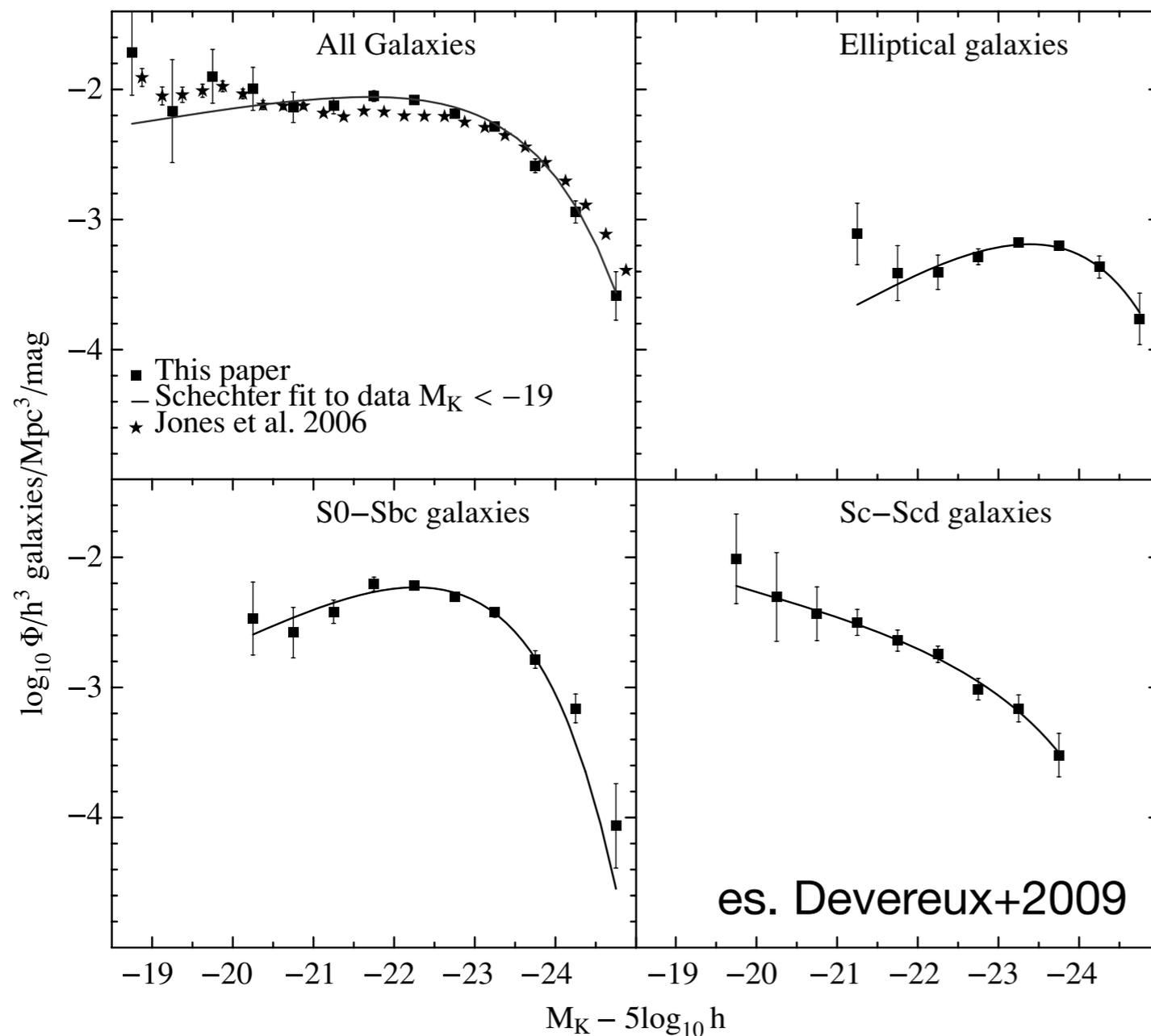
For example:

$$P(M_{\text{BH}}|\sigma_e) = \exp \left[ -\frac{1}{2} \left( \frac{\log(M_{\text{BH}}/M_{\odot}) - a - b \log(\sigma_e/200 \text{ km s}^{-1})}{\sigma_0} \right)^2 \right]$$

is the  $M_{\text{BH}}-L_{\text{sph}}$  relation with intrinsic scatter  $\sigma_0$  (assumed normally distributed).

# Luminosity function of spheroids

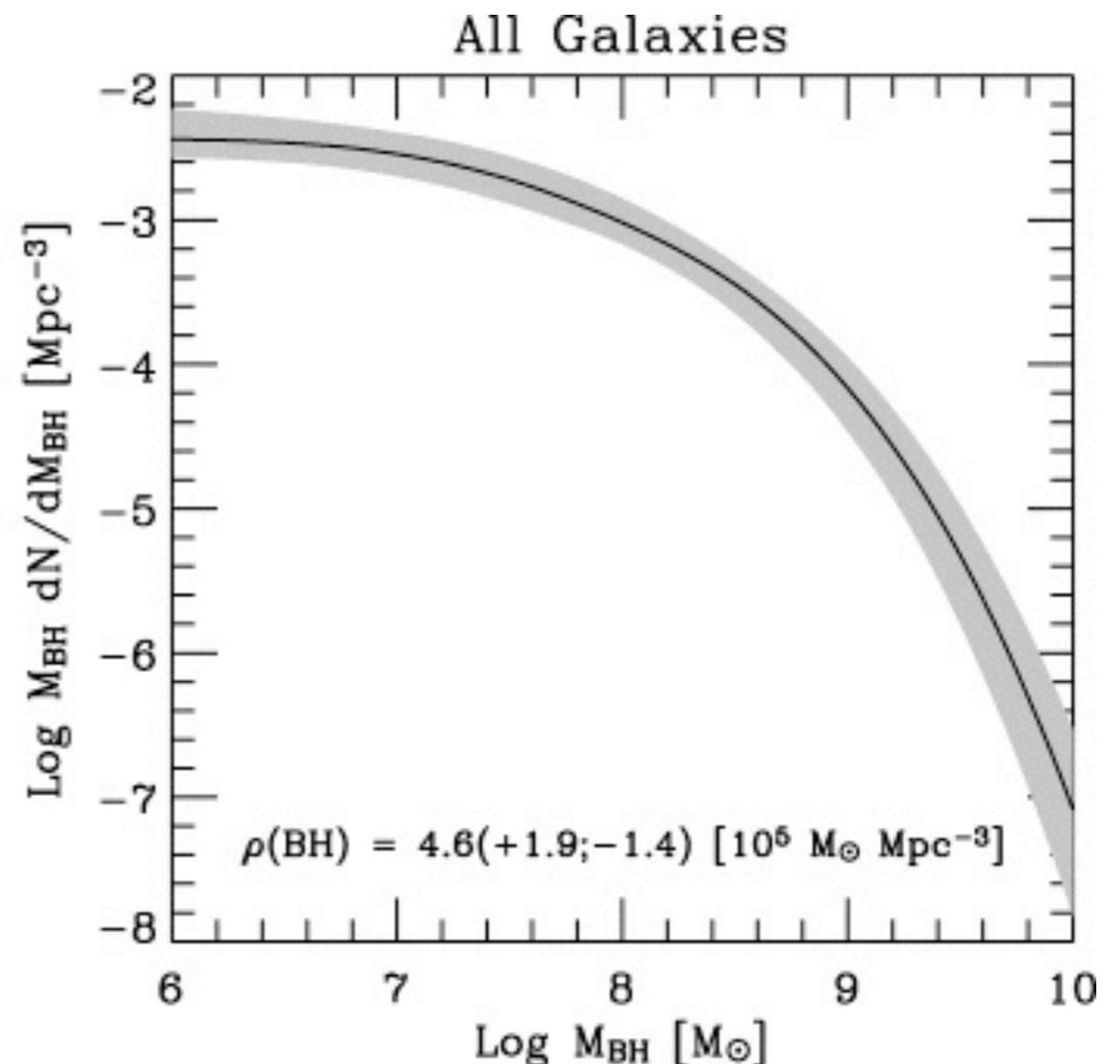
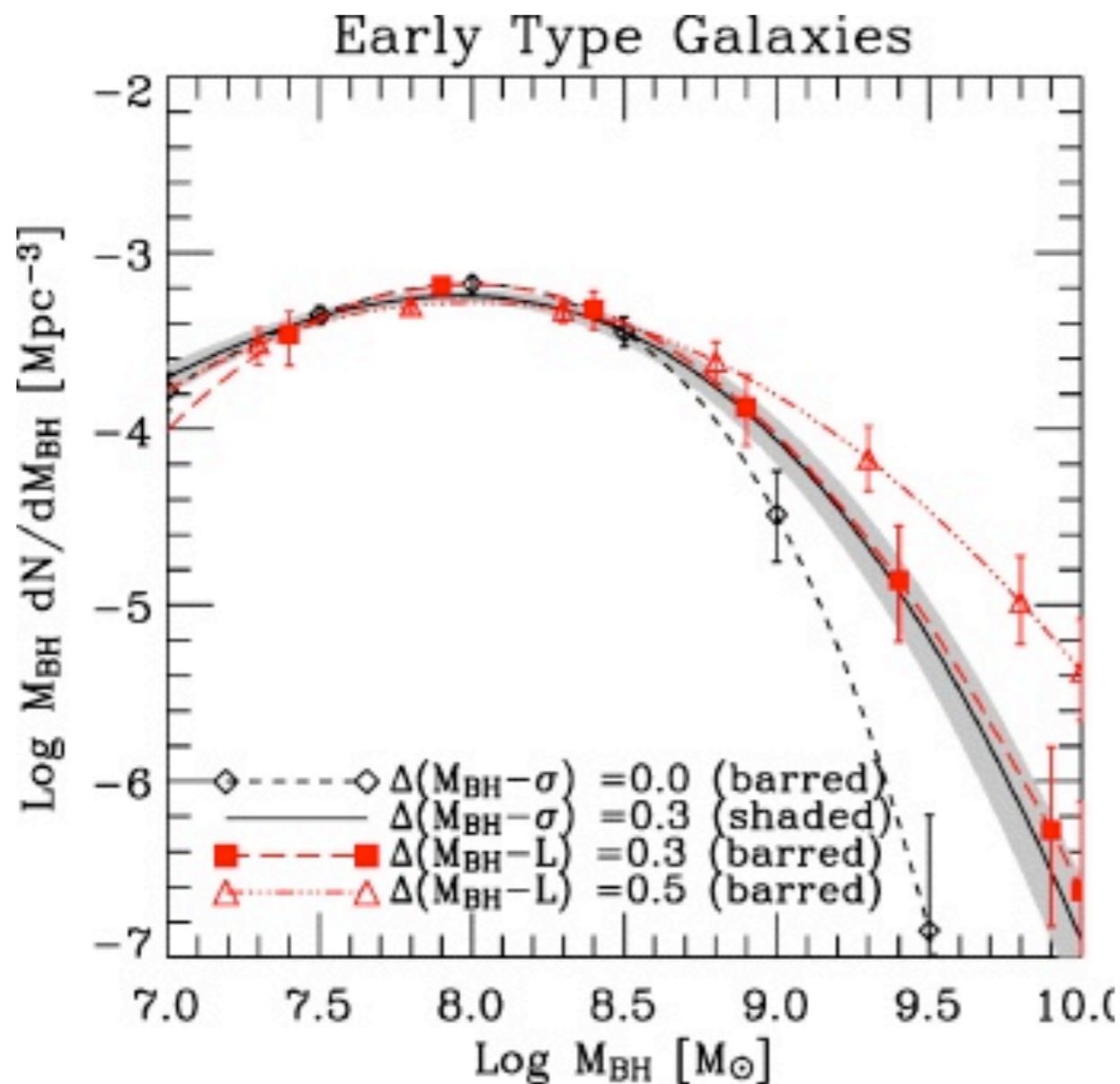
- ★ To obtain the luminosity function of spheroids, one has to apply a bulge/total correction (B/T=1 for ellipticals).
- ★ B/T depends on the morphological type  
→ *need LF per morphological type*



# Local BH mass function

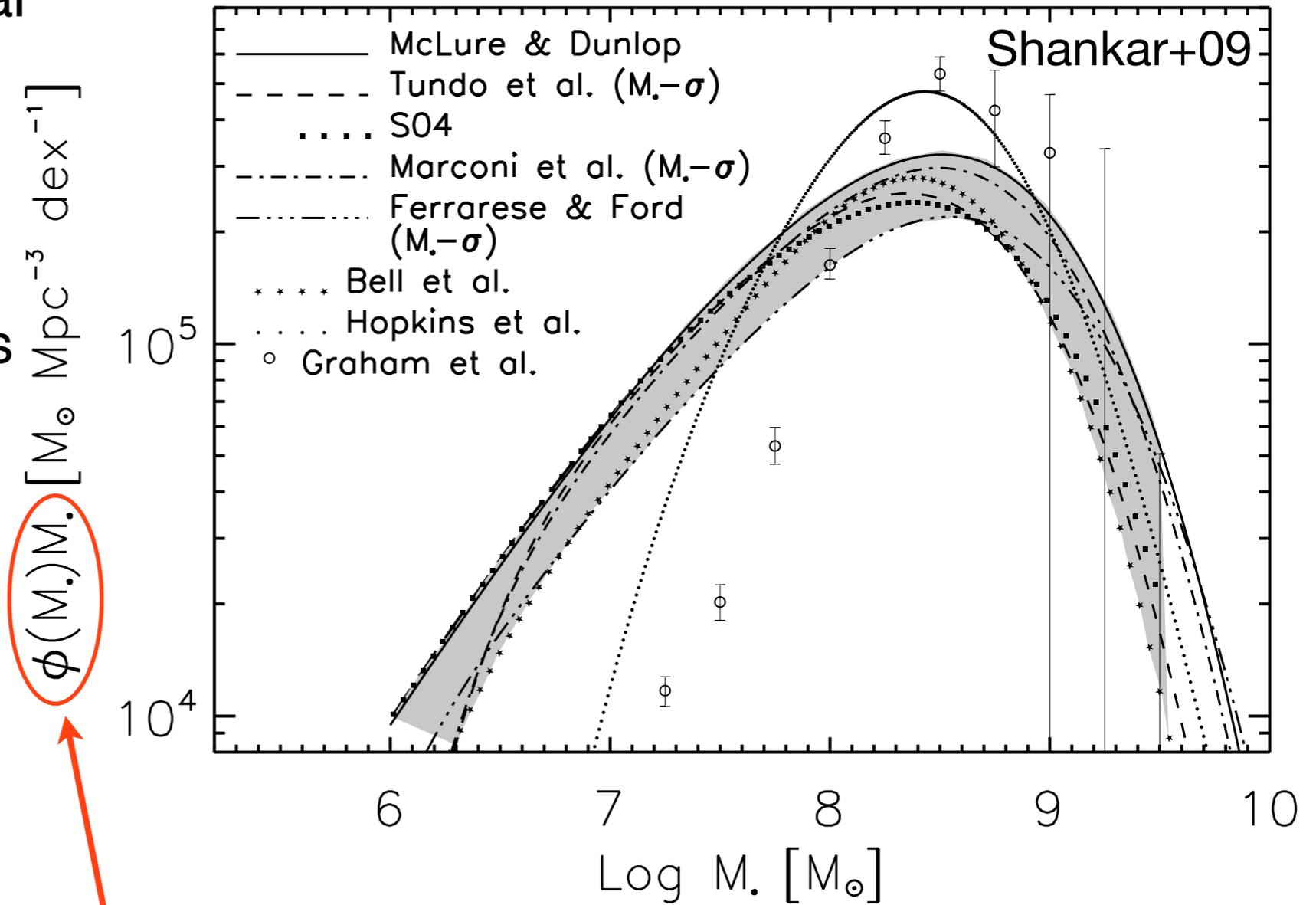
For 0 intrinsic dispersion, the BH mass function is just the  $L/\sigma$  function rescaled:  $P(M_{BH}|L_{sph})$  is a Dirac's  $\delta$  function.

The intrinsic dispersion significantly affects the high mass tail of the BH mass function.



# Local BH mass function

- ★ Overall there is a general agreement (or not so large disagreement) among estimates from different authors.
- ★ The integrated BH mass density is  
 $\rho_{\text{BH}} \approx 3.5\text{-}5.5 \times 10^5 M_{\odot} \text{Mpc}^{-3}$
- ★ Uncertainty are mostly due to  $M_{\text{BH}}$ -galaxy relations!
- ★  $\rho_{\text{BH}}$  depends mostly on the zero points of the correlations



$\phi(M) M$  is directly the contribution to  $\rho_{\text{BH}}$

Salucci +99, Yu & Tremaine 02, Marconi +04, Shankar +04, Tamura+06, Tundo +07, Hopkins +07, Graham +07, Shankar +08, Vika+09 et many al.

# Local BH mass function

Li+11 has estimated the BHMF up to  $z \sim 2$ , using the MBH-Mstar relation (and its redshift evolution, see last lecture) and  $\phi(M_{\text{star}})$ .

Their nice work matches previous results at  $z=0$ , indicating that the estimates of the BHMF and BH mass density appear to be robust.

