

Formation & evolution of galaxies & SMBHs

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Outline of lectures

1. Structure formation & assembly of dark halos
2. Gas cooling & angular momentum
3. Star formation & feedback
4. Galaxy mergers & morphologies
5. Cosmic evolution of galaxies
6. Formation of black holes
7. BH binaries & spin
8. Co-evolution of galaxies & AGN

Lecture 7:

SMBH binaries & spin

Further reading for lecture 7

- Single & binary black holes & their influence on nuclear structure by David Merritt (extended version at [arXiv:astro-ph/0301257](https://arxiv.org/abs/astro-ph/0301257), 2003)
- Evolution of massive black hole spins by Marta Volonteri ([arXiv:1002.3827](https://arxiv.org/abs/1002.3827), 2010)

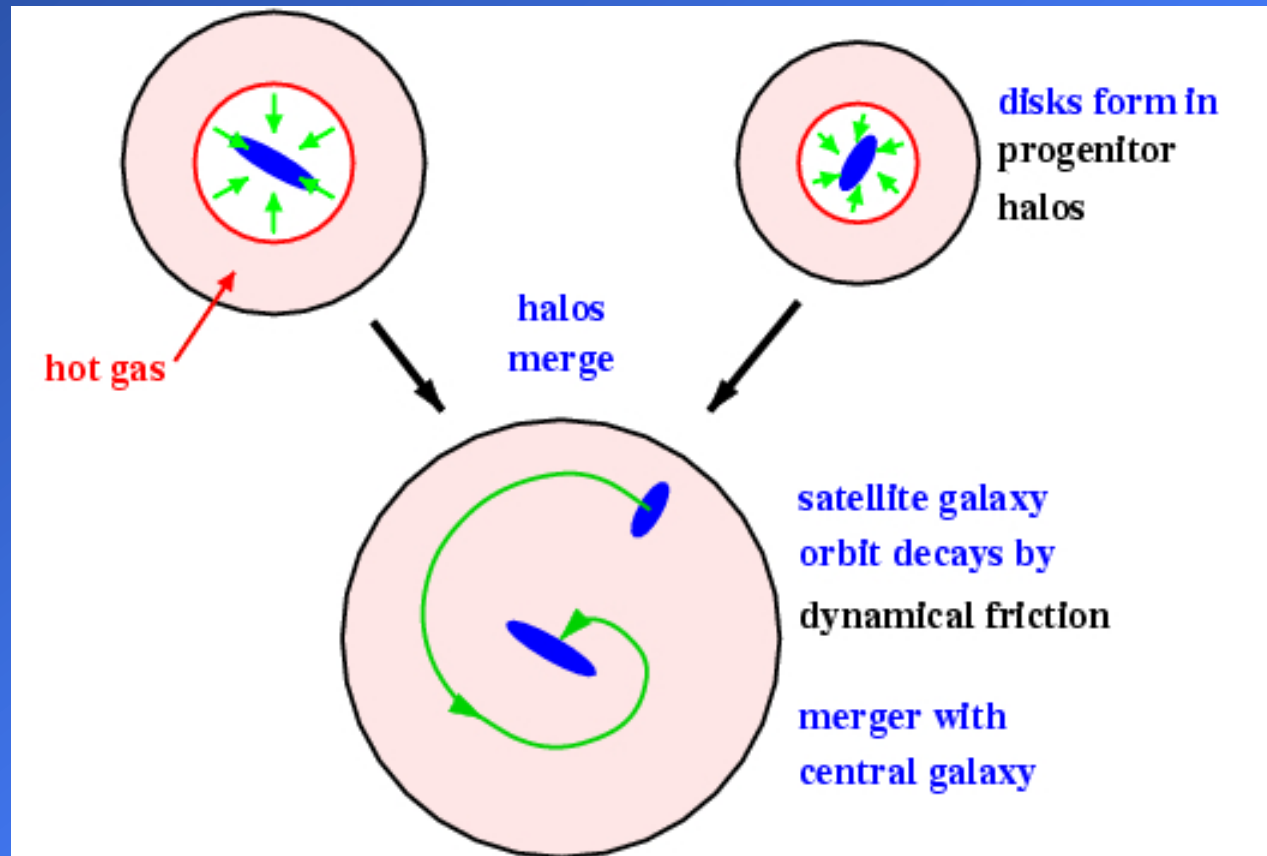
Lecture 7 outline

- SMBH binaries & SMBH spin
 - SMBH binaries & mergers
 - gravitational radiation & recoil
 - origin of SMBH spin through gas accretion & mergers

SMBH mergers

Merging of central BHs in galaxies

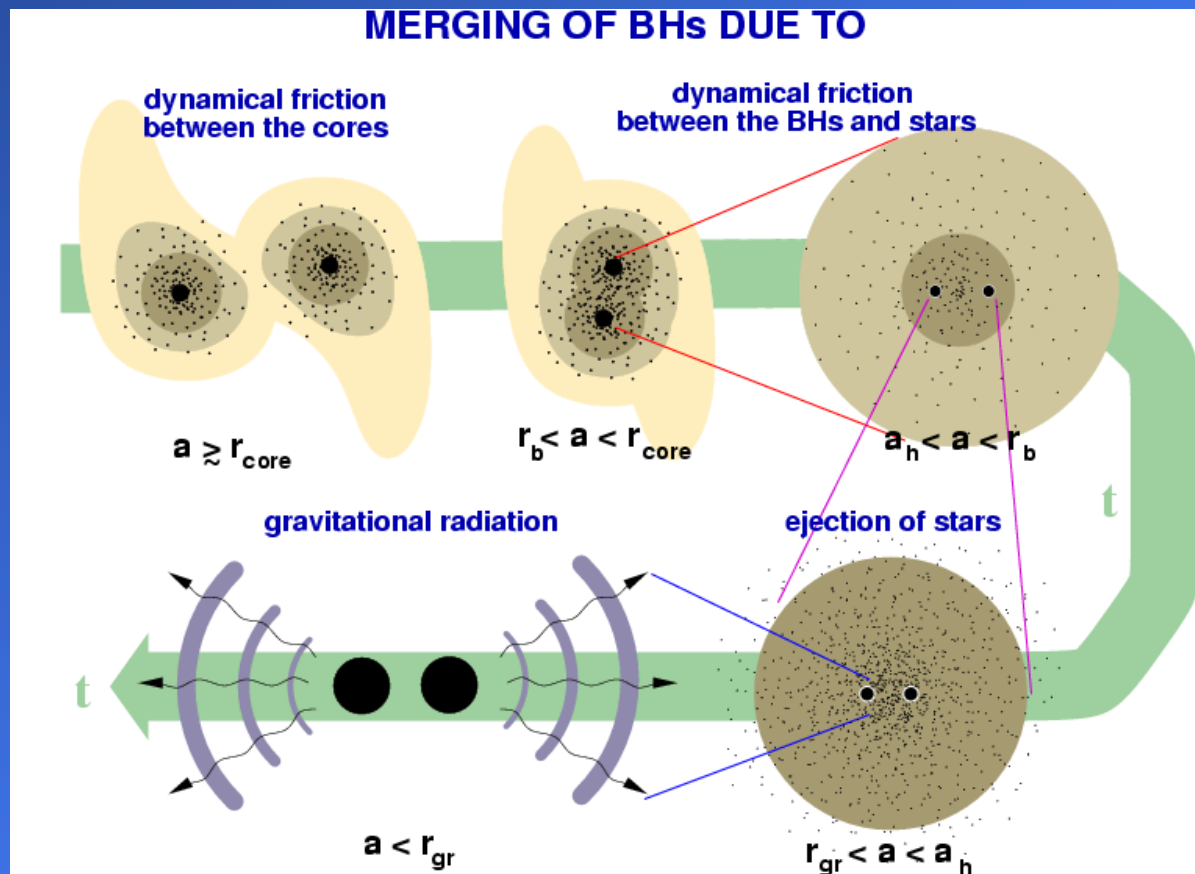
- galaxy merger



- BH merger in multiple stages:
 - DM halos merge (structure formation)
 - galaxies merge in common halo (dynamical friction against halo)

Merging of central BHs in galaxies

- BH-BH merger within galaxy nucleus



different processes dominate on different scales:

- dynamical friction of BH against stars
- dynamical friction of BH in gas disk
- gravitational radiation

Dynamical friction against stars & loss cone

- dynamical friction against stars, orbits shrink on timescale

$$t_{fric} = \frac{1.17}{\ln \Lambda} \frac{r^2 V_c}{G M_{BH}} = \frac{1.17}{\ln \Lambda} \frac{M(< r)}{M_{BH}} t_{orb}$$

- effective until BH binary becomes self-gravitating at separation:

$$a_b = \frac{G(M_1 + M_2)}{2\sigma^2}$$

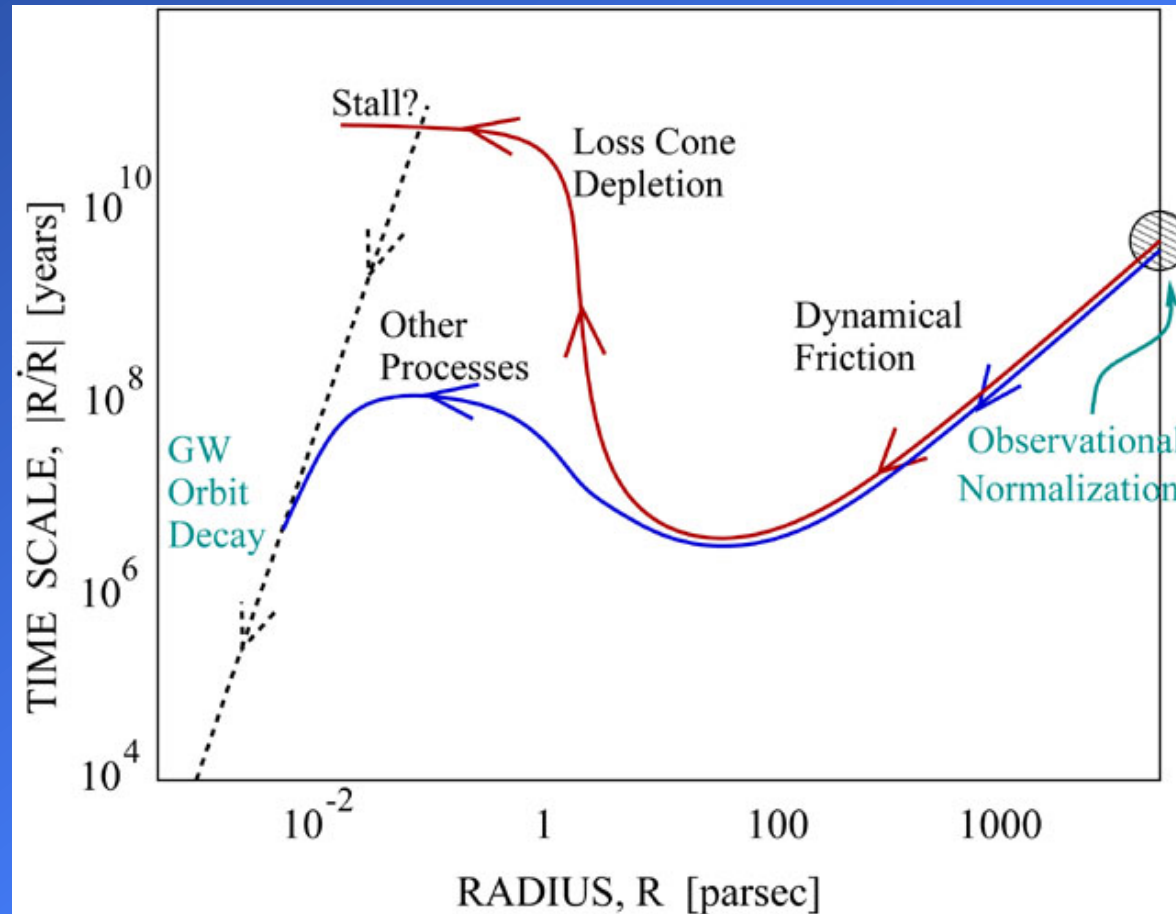
where σ = velocity dispersion of stars

- following this, BH binary hardens ($V > \sigma$), further shrinkage is due to 3-body interactions (BH+BH+star), on timescale (where $H \sim 15$):

$$t_h = \frac{\sigma}{G \rho_* a H}$$

- however, this results in ejection of stars on orbits taking them close to binary – “loss cone” – so orbit shrinkage timescale becomes v. long

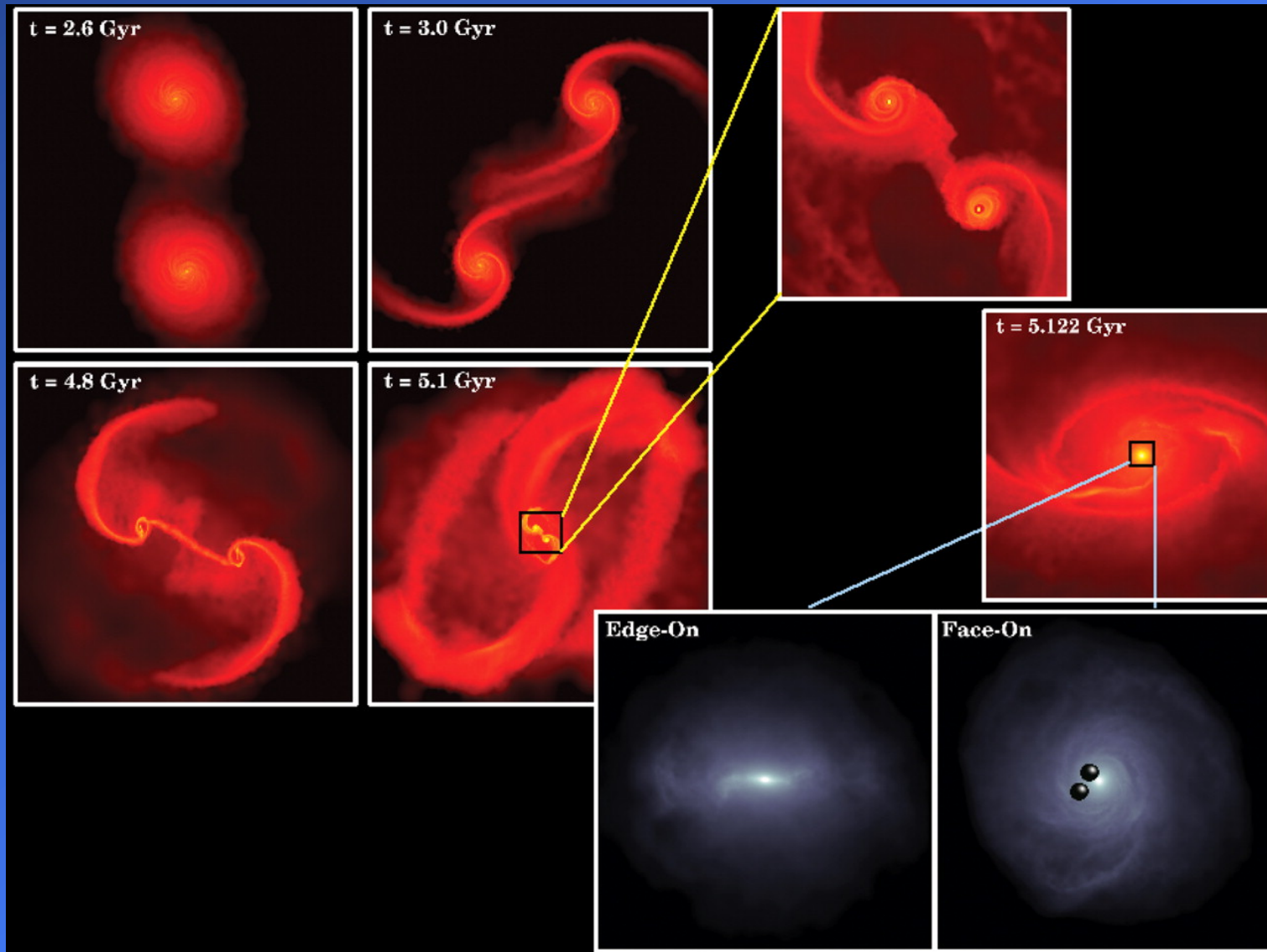
Evolution of BH binary separation



Role of gas in BH mergers

- loss cone effects may cause orbital shrinkage of BH binary to stall before reaches separation at which GW loss effective
- BH drag against gas may play crucial role
- obs => massive self-gravitating gas disks at centres of many merging galaxies
- BH moving through gaseous disk gravitationally excites wake in gas which exerts orbital drag on BH, similar to dynamical friction from stars
- unlike stars, gas dissipates energy so not ejected by BH interaction
- can cause BH orbits to shrink rapidly

simulation of merger of 2 galaxies containing black holes & gas



two
 $3 \times 10^6 M_{\odot}$
BHs
followed to
separation
 ~ 1 pc
- merge in
nuclear gas
disk $M \sim$
 $3 \times 10^9 M_{\odot}$,
 $r \sim 80$ pc

Gravitational radiation

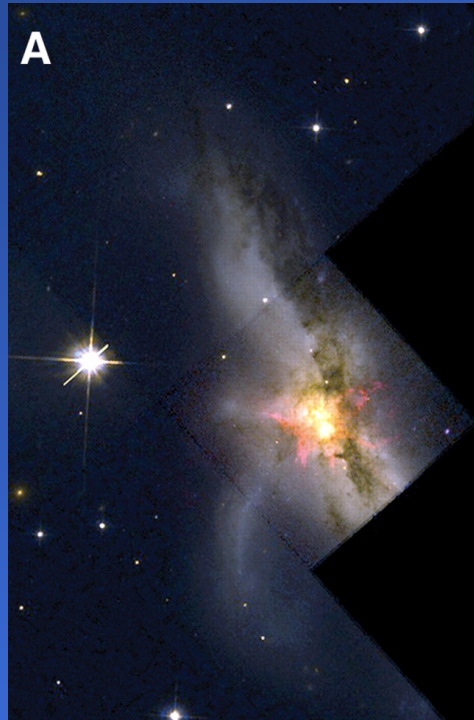
- emission of gravitational waves from BH binary carries away energy & angular momentum, causing orbit to shrink on timescale:

$$t_{\text{GR}} = \frac{5c^4 a^4}{256G^3 M_1 M_2 (M_1 + M_2)}$$

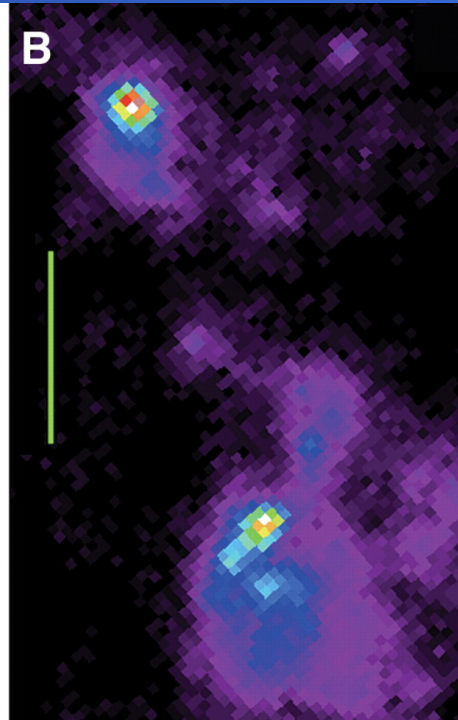
- NB strong dependence on binary separation
- v.slow at first, but final stages v. rapid

Observational evidence for binary BHs

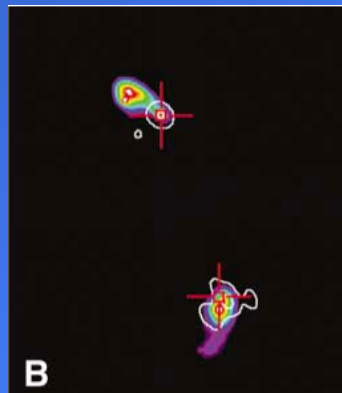
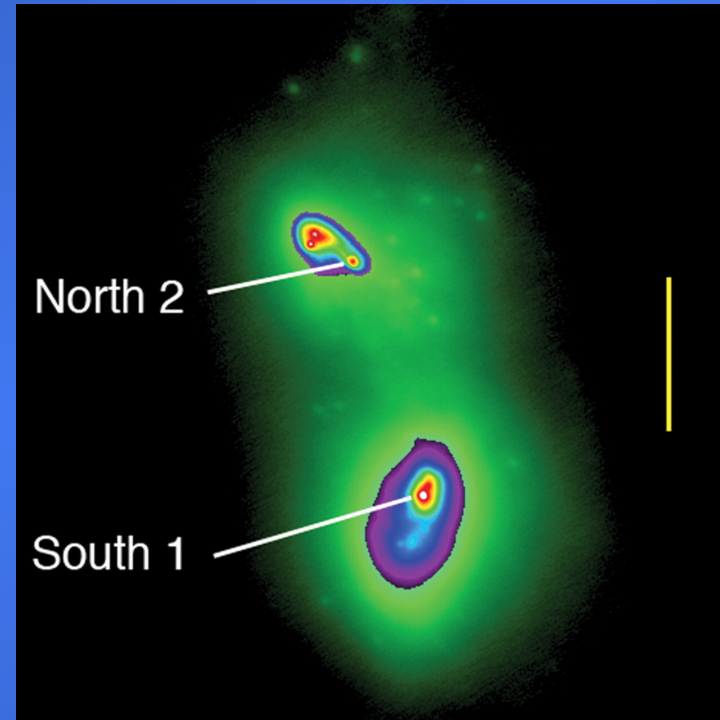
optical



optical (zoom)



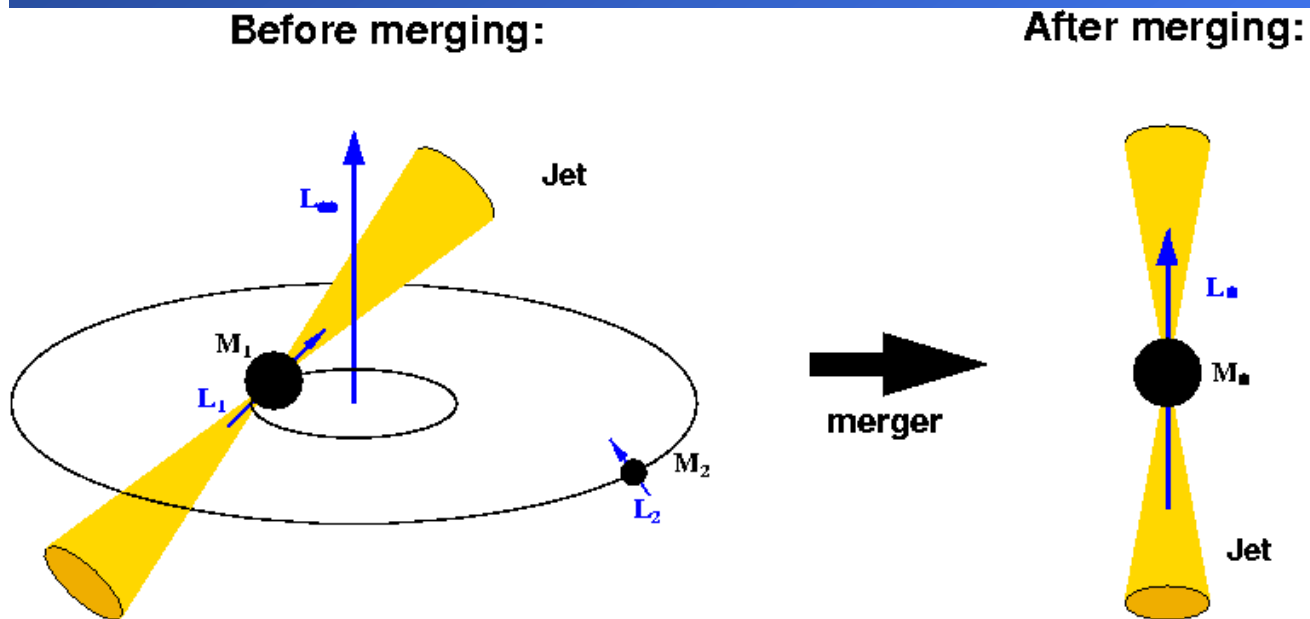
K-band (zoom)



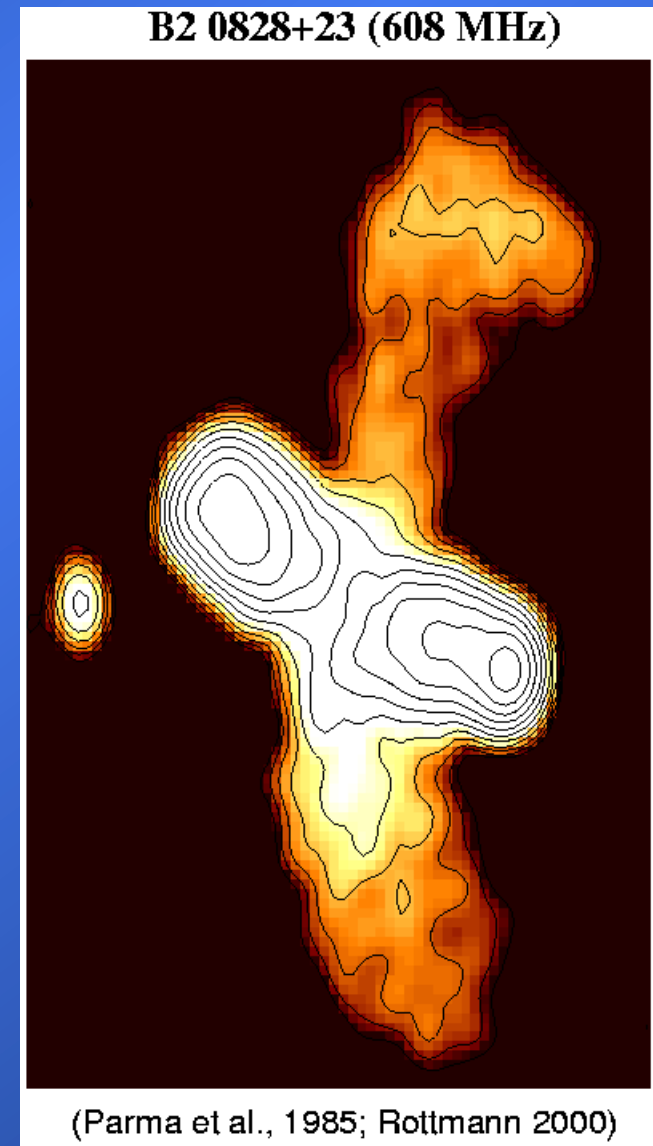
Max et al 2007

- NGC 6240: merger of 2 spiral galaxies
- double stellar nucleus seen in optical & K-band, sepn ~ 800 pc
- each nucleus hosts AGN seen radio & X-rays
- each AGN surrounded by dust disk, seen in mid-IR

Observational signature of BH mergers



sudden change of spin axis of BH due to BH-BH merger => change in direction of radio jet

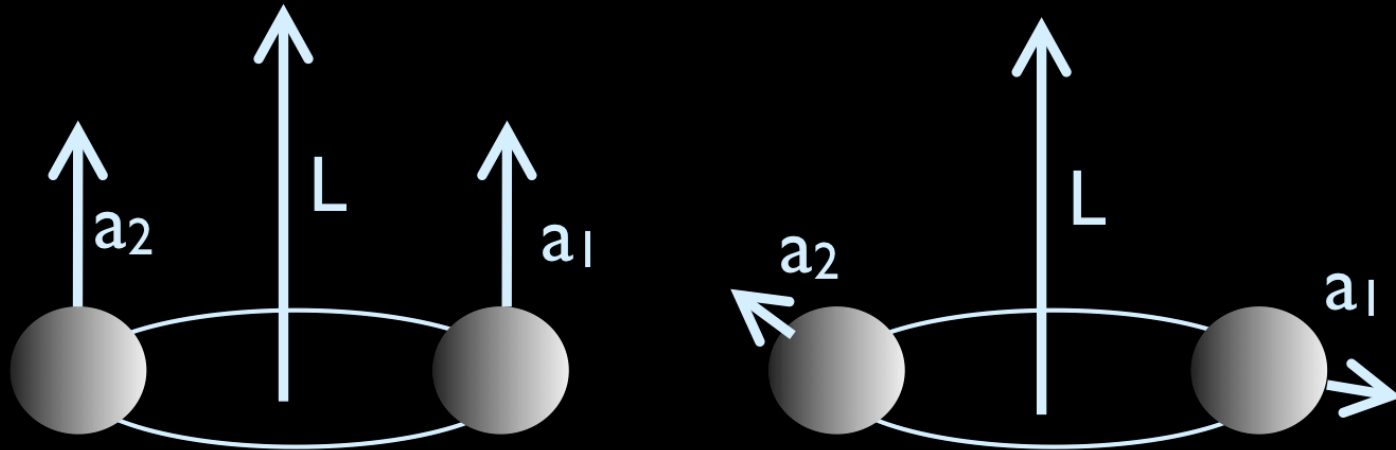


Gravitational radiation & BH recoil

BH recoil from gravitational radiation

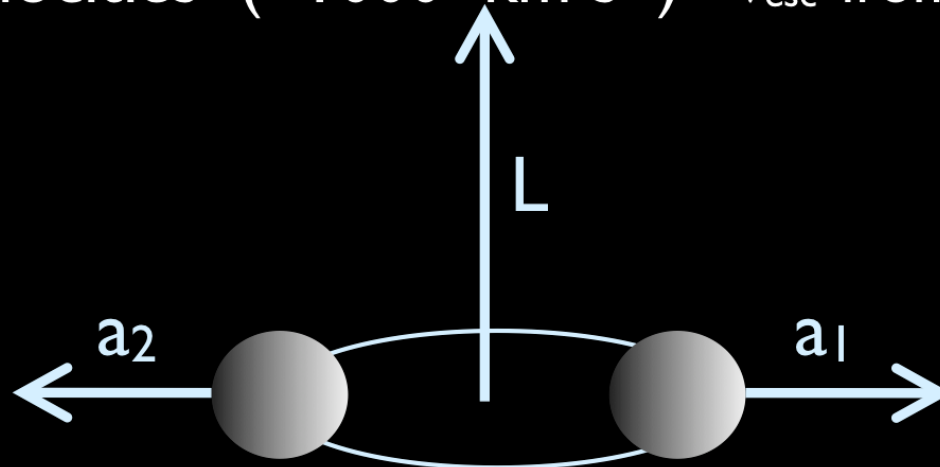
- final in-spiral of BH binary due GW emission very rapid => anisotropic distribution of GW emission
- but GWs carry momentum => BH formed by BH-BH merger has recoil velocity
- V_{rec} depends strongly on mass ratio $q=M_2/M_1$ & on BH spins & orientations
- max V_{rec} for $q\sim 0.4$, V_{rec} small for $q\ll 1$
- non-spinning BHs: V_{rec} up to ~ 200 km/s
- spinning BHs: V_{rec} up to ~ 3000 km/s
 - depends on alignment of spins rel to orbital plane:
 - aligned or anti-aligned with orbital axis => low V_{rec}
 - spins in opposite dirns in orbital plane => high V_{rec}

Recoiling MBHs

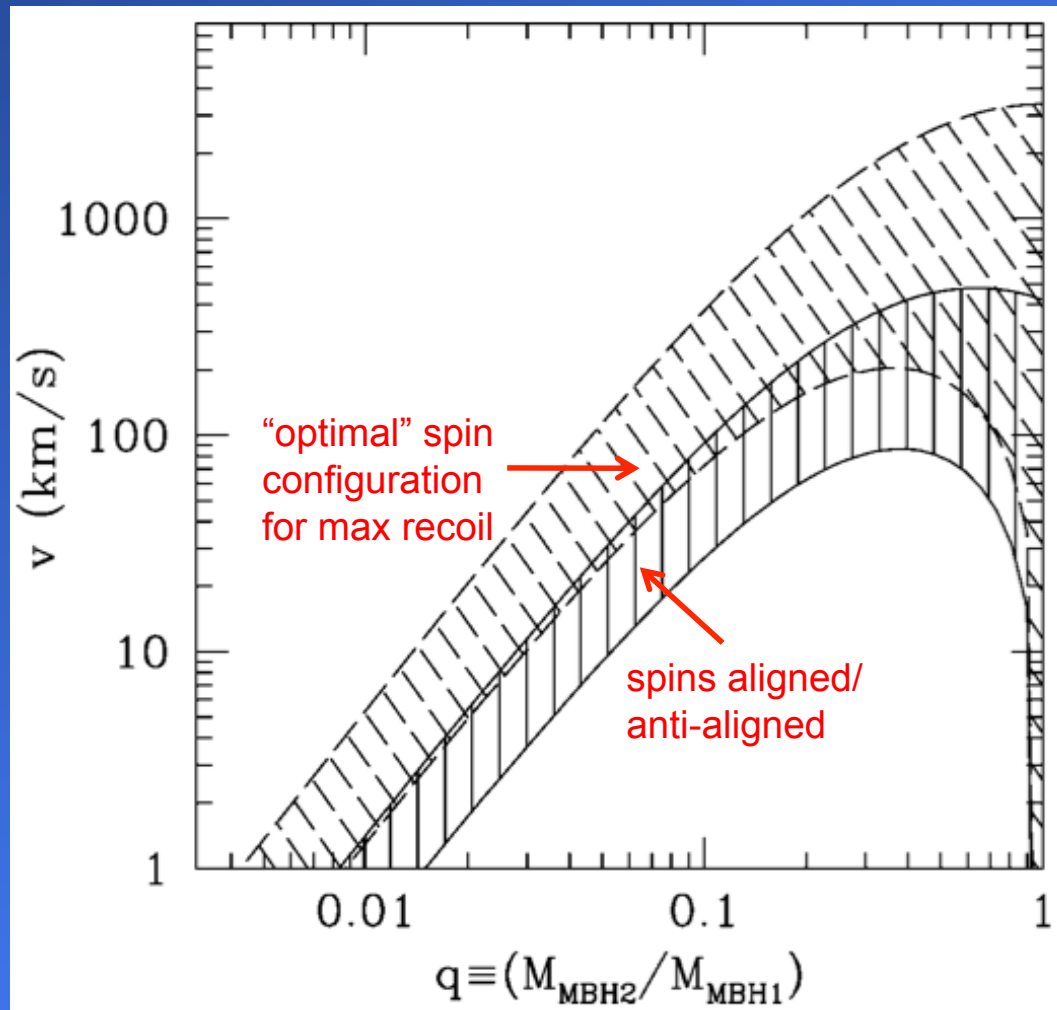


Low kick velocities ($\sim 100 \text{ km s}^{-1}$) $\sim v_{\text{esc}}$ from high- z galaxies

High kick velocities ($\sim 1000 \text{ km s}^{-1}$) $\sim v_{\text{esc}}$ from today's galaxies

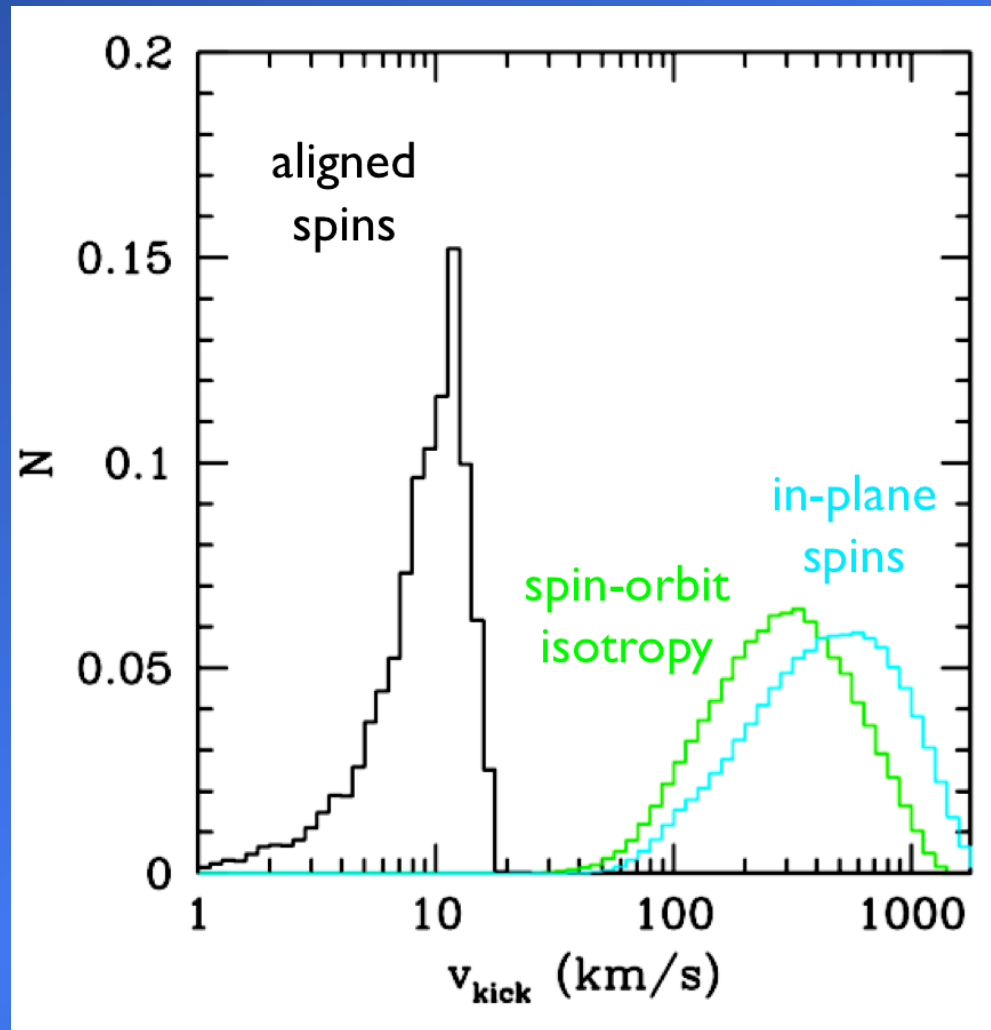


Recoil velocities in BH mergers



results based on
results of GR
simulations of
merging BHs

Distribution of kick velocities



results from
theoretical model
for BH formation
& merging, for
different
assumptions
about alignment
of spins

Volonteri 2009

Consequences of GW recoil for SMBH growth

- GW recoil can eject merging BHs from halo if $V_{\text{rec}} > V_{\text{esc}}$, preventing buildup of SMBHs by multiple mergers
- recoil largest when merging BHs have similar masses
- potentially serious problem for SMBH growth from Pop III remnants, since these form in halos with very low V_c ($\Rightarrow$ low V_{esc}) which then merge
- also problem for BH seeds formed in dense star clusters, since cluster has low V_{esc}
- lesser problem for massive BH seeds formed in larger halos, since V_{esc} larger & equal mass BH mergers less likely

Spin directions of merging BHs

- orientation of BH spins in merger relative to orbital plane depends on whether BHs brought together by dynamical friction against stars or against gas disk
- stars => isotropic distribution of BH spins
- gas disk => BH spins may become aligned with angular momentum of gas disk, if BHs have accretion disks (effect of gravitational torques)

Origin of SMBH spin

Dimensionless spin parameter : $a = cJ_{BH} / GM_{BH}^2$

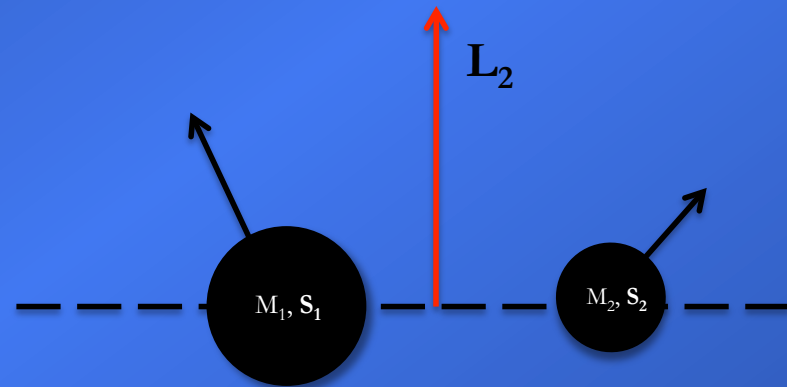
$0 \leq a \leq 0.998 : \begin{cases} a = 0 \rightarrow \text{Schwarzschild BH} \\ a = 0.998 \rightarrow \text{Maximally rotating BH} \end{cases}$

Growth of mass & angular momentum of black holes

- main processes for growing mass of BHs are:
 - BH-BH mergers
 - accretion of gas from an accretion disk
- both of these also effective at changing angular momentum

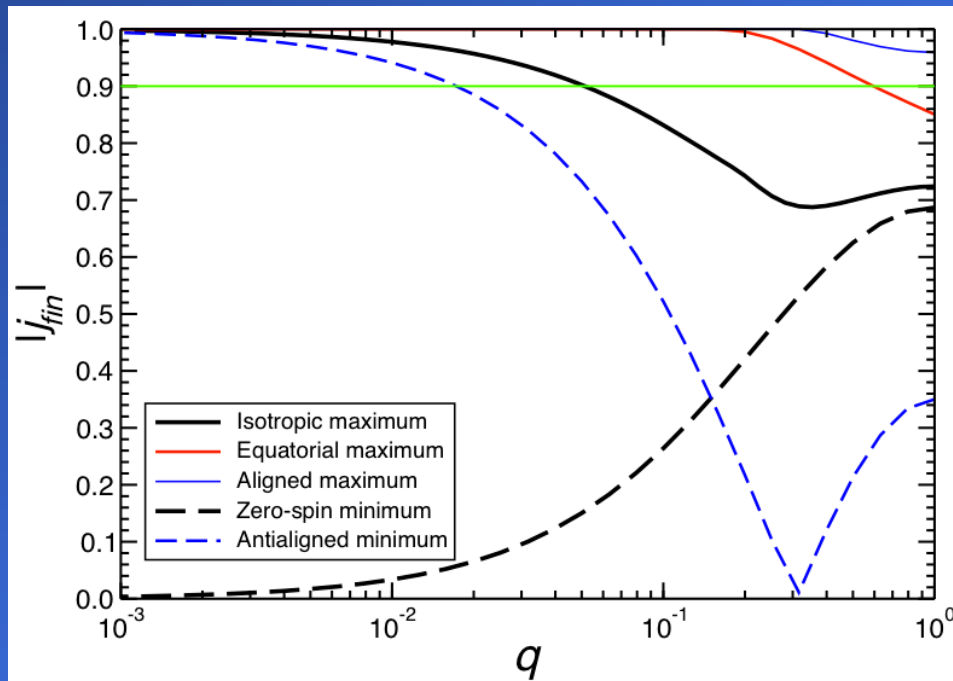
Change of spin in BH-BH mergers

- Binary BHs form during galaxy mergers
- The binary hardens due to emission of gravitational waves
- During the merger the satellite BH transfers its orbital angular momentum and spin to the central BH
- The final remnant is always a rotating BH



Spin in BH-BH mergers

final BH spins averaged over initial spins
& angles



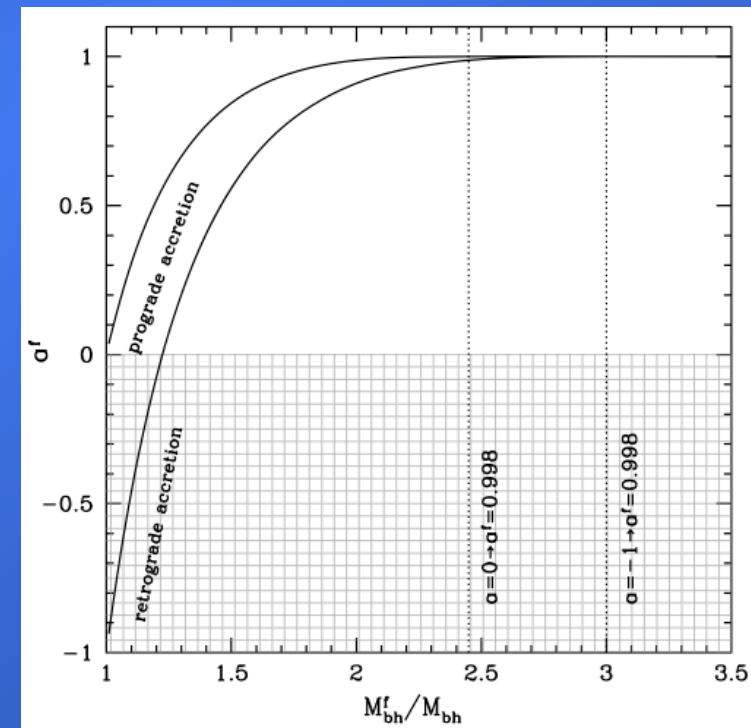
Berti & Volonteri 2008

- final spin depends on $q=M_2/M_1$, on spins of both BHs, and on orientation of spins relative to orbital ang mtn
- merge equal mass non-spinning BHs $\rightarrow a=0.69$
- equal-mass maximally spinning BHs with spins aligned with orb ang mtn $\rightarrow a=0.96$
- isotropic distribns of spins $\rightarrow$ lower average final spins

- aligned spins $\Rightarrow$ v.rapidly rotating BHs ($a>0.9$)
- isotropic spins:
 - major merger ($q\sim 1$) $\Rightarrow$ moderate rotation – typical $a\sim 0.7$
 - many minor BH mergers ($q\ll 1$) $\Rightarrow$ low spin

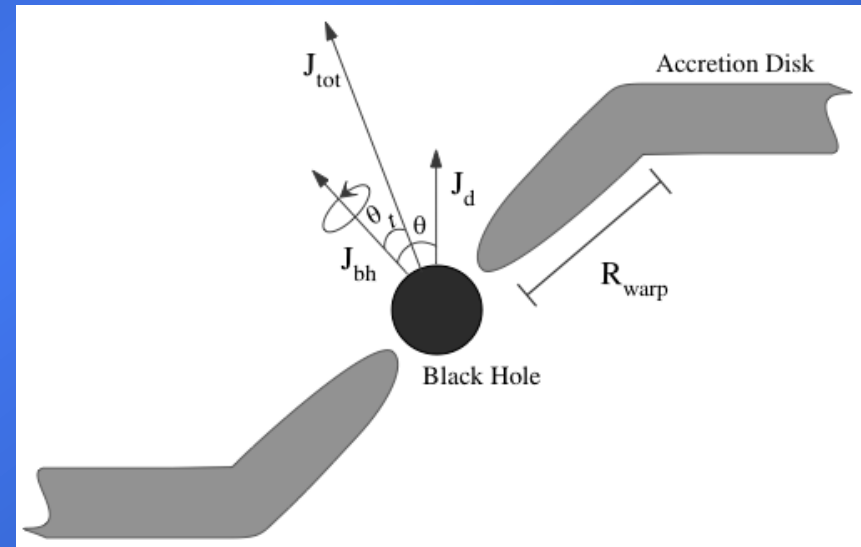
Change of BH spin by gas accretion

- Gas accretes via an accretion disk transfers its angular momentum at the last stable orbit to the BH
- Co-rotating gas – spin up
- Counter-rotating gas – spin down
- gas accretion very effective at changing spin:
 - non-rotating BH gets spun up to max rotation ($a=0.998$) after increasing mass by factor 2.44
 - maximally rotating BH in counter-rotating disk gets spun down to $a=0$ after increasing mass by factor 1.22



Alignment of BH spin with accretion disk

- Lens-Thirring torque (GR effect) + accretion disk viscosity $\rightarrow$ align or anti-align inner accretion disk with BH
- grav torque of outer disk on inner $\rightarrow$ BH spin eventually aligns with angular momentum of outer accretion disk (if $J_{\text{disk}} > 2J_{\text{BH}}$)
 - happens rapidly for thin accretion disk
 - more slowly for thick disk



Evolution of BH spin for accreting BH

(A) Prolonged/coherent accretion

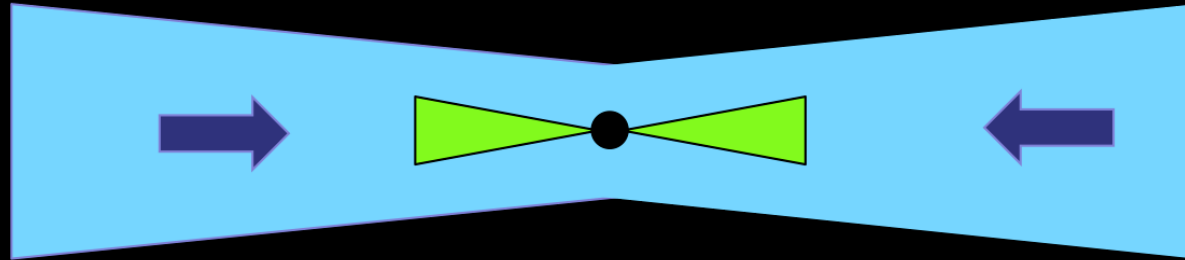
- PROLONGED accretion of gas (leading to M_{BH} increasing by factor $>2-3$) from gas disk which maintains CONSTANT orientation should therefore lead to maximally spinning ($a=0.998$) BH aligned with accretion disk
=> BHs which grow mainly by coherent gas accretion should be very rapidly spinning

Evolution of BH spin for accreting BH

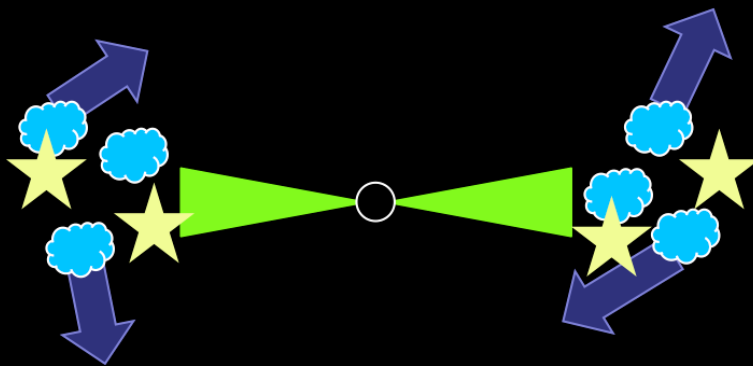
(B) Chaotic accretion

- Alternative idea is that accretion from disk with mass M_{acc} split into many small episodes $\Delta M_{\text{episode}} \ll M_{\text{acc}}$ each having RANDOM orientation of ang mtn – CHAOTIC accretion (King & Pringle 2006)
 - physical mechanism producing random orientations of different episodes not clear, but might be due to energy injection by star formation triggered by grav instability of accretion disk
 - chaotic accretion should lead to slowly rotating BHs ($a \sim 0.1-0.3$) with randomly oriented spins

Coherent vs Chaotic accretion



Coherent: accreted material has $\sim$ constant direction of angular momentum vector



Chaotic: accretion of droplets of material with random direction of the angular momentum vector

(King & Pringle 2006)

