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BESIII上粲介子半轻衰变到轻标量介子的研究进展

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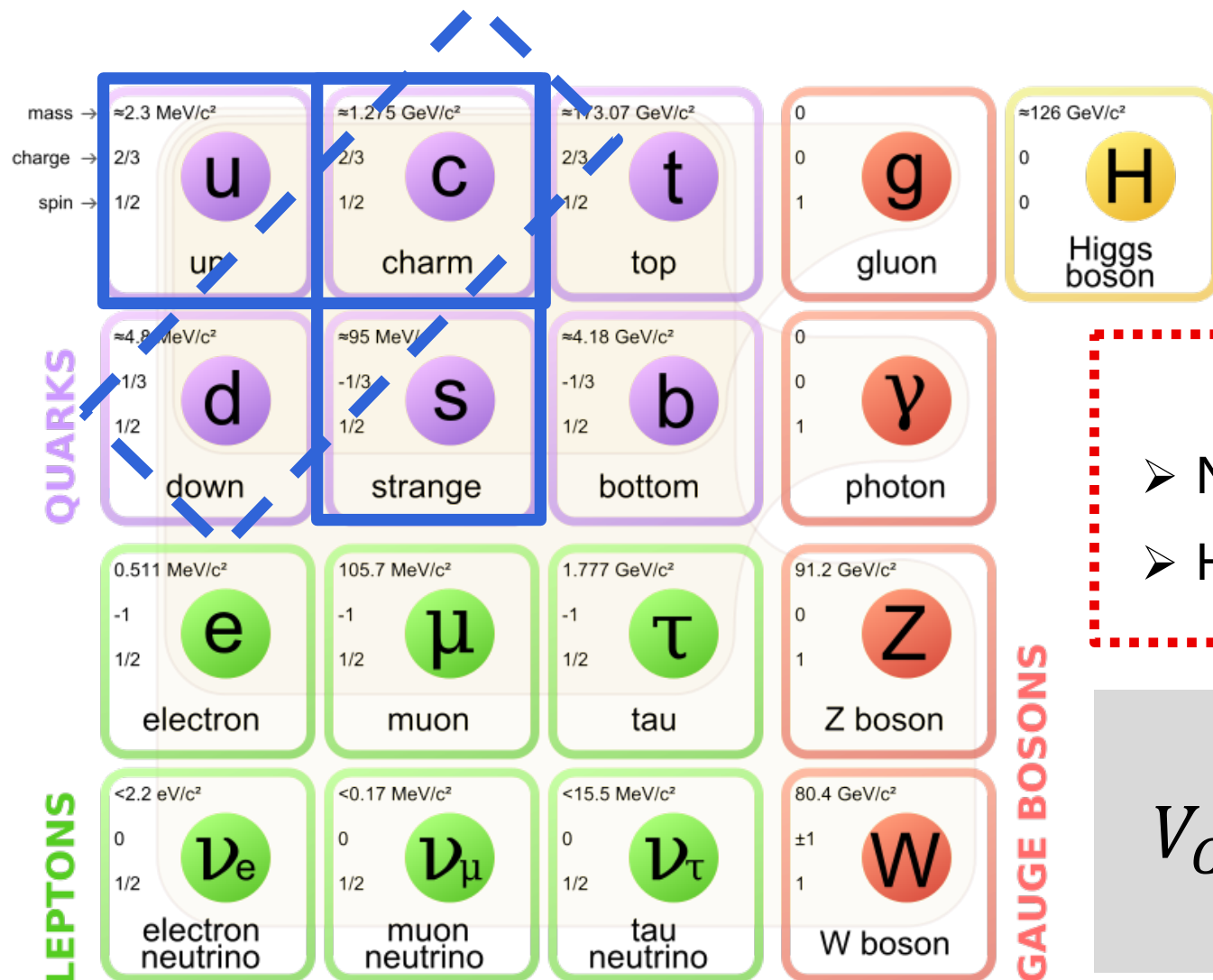
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Summary and prospect

Physics motivation



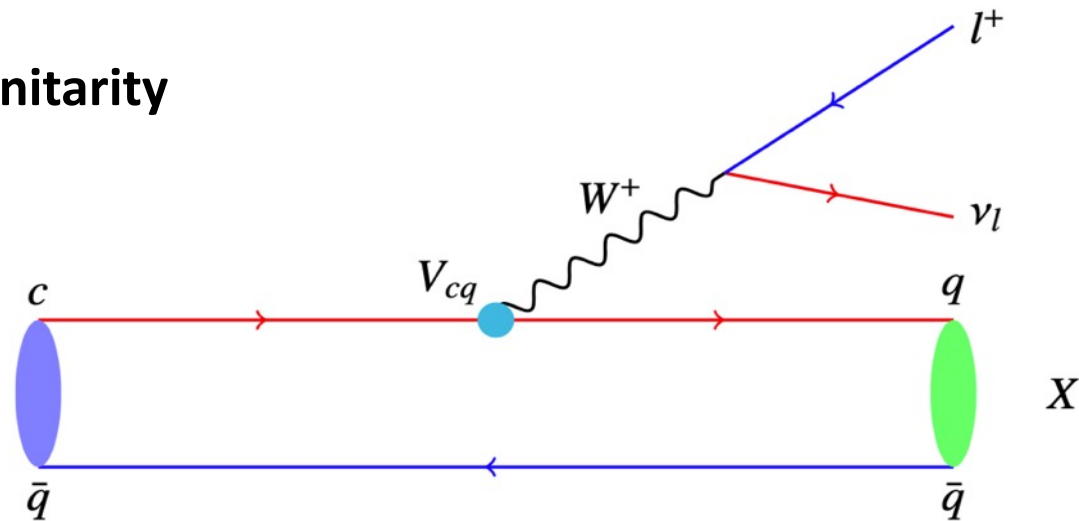
Charm physics

- Nonperturbative region -> **QCD**
- High precision frontier -> **SM test**

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



- Hadronic **Form factor (FF)** -> **Test different QCD models**
- CKM matrix elements $V_{cd(s)}$ -> **Test CKM matrix unitarity**
- $\mathcal{B}(D_{(s)} \rightarrow X \mu^+ \nu_\mu) / \mathcal{B}(D_{(s)} \rightarrow X e^+ \nu_e)$
-> **Lepton flavor universality (LFU) test.**
- Branching fraction and FF measurement
-> **Good laboratory for light scalar mesons study**



$$A(D \rightarrow X \ell \nu) = \frac{G_F}{\sqrt{2}} V_{cq}^* \bar{\nu} \gamma_\mu (1 - \gamma_5) \ell \langle X | \bar{q} \gamma^\mu (1 - \gamma_5) c | D_{(s)} \rangle$$

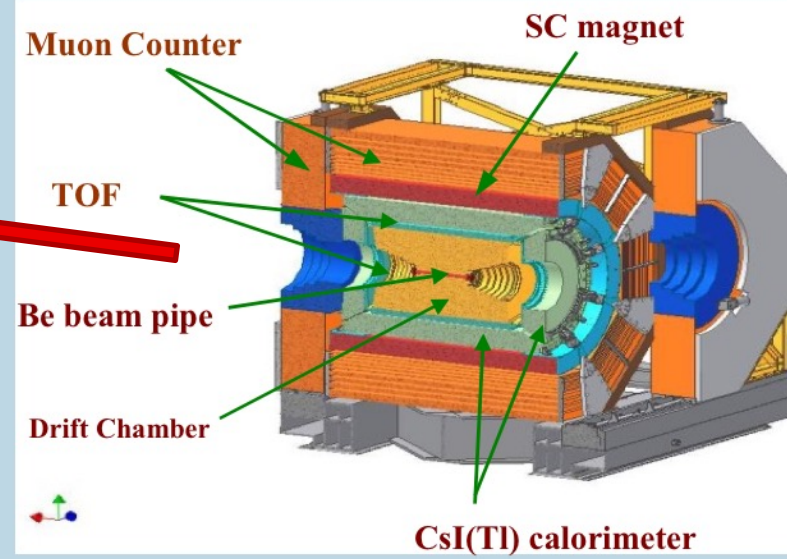
$$\Gamma(D_{(s)} \rightarrow P(S) \ell^+ \nu_\ell) \propto |V_{cd(s)}|^2 |f_+(q^2)|^2 dq^2$$

$$\Gamma(D_{(s)} \rightarrow V \ell^+ \nu_\ell) \propto |V_{cd(s)}|^2 \mathfrak{I}(A_1(q^2), A_2(q^2), V(q^2)) dq^2$$

BESIII experiment

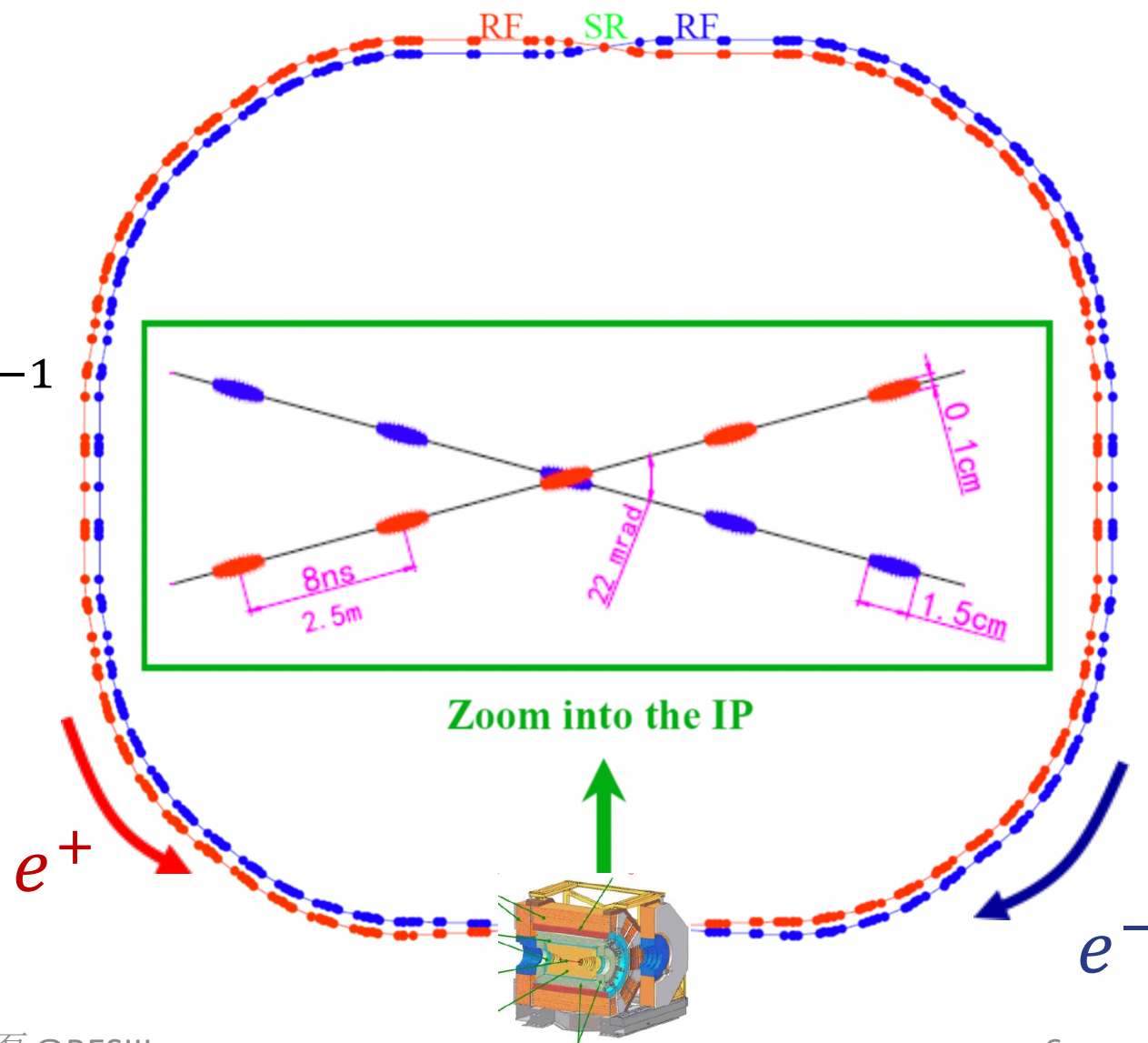


BESIII Detector

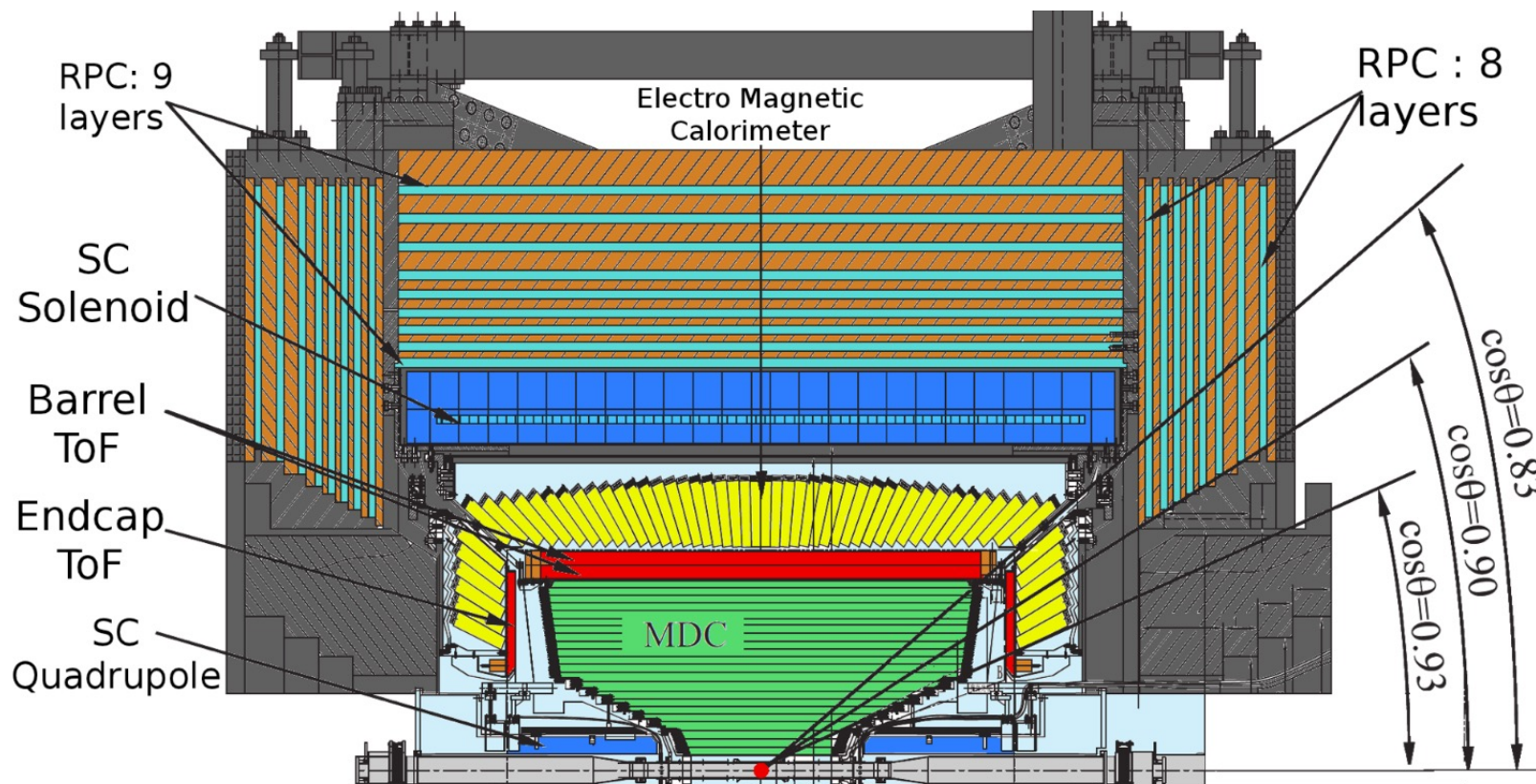


BEPCII collider

- Two ring symmetric e^+e^- collider
- Circumference: 240 m
- Design luminosity: $1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
- Achieved time: 5 April, 2016
- E_{cm} : 2 – 5 GeV
- Beam crossing angle: 22 mrad



BESIII detector



MDC

$$\frac{\delta p}{p} < 0.5\% \text{ @1 GeV}$$

$$\frac{\delta(dE/dx)}{dE/dx} < 6\%$$

TOF

$$\delta t \text{ 80 ps Barrel}$$

$$\delta t \text{ 110 ps Endcap}$$

EMC

$$\frac{\delta E}{E} < 2.5\% \text{ @1 GeV}$$

$$\delta z = 0.6/\sqrt{E}$$

MUC

$$\delta(xy) < 2 \text{ cm}$$

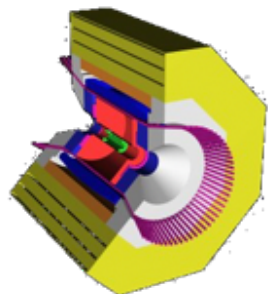
BESIII Collaboration

Political Map of the World, November 2011

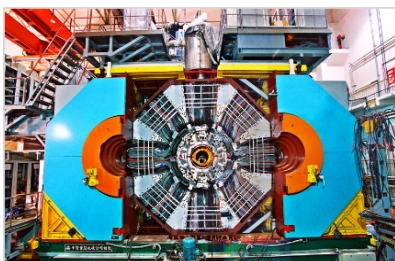


Data sample

CLEO-c



BESIII



- Symmetric e^+e^- collider
- E_{cm} : 2 – 5 GeV
- Charm collected through pair-production near threshold



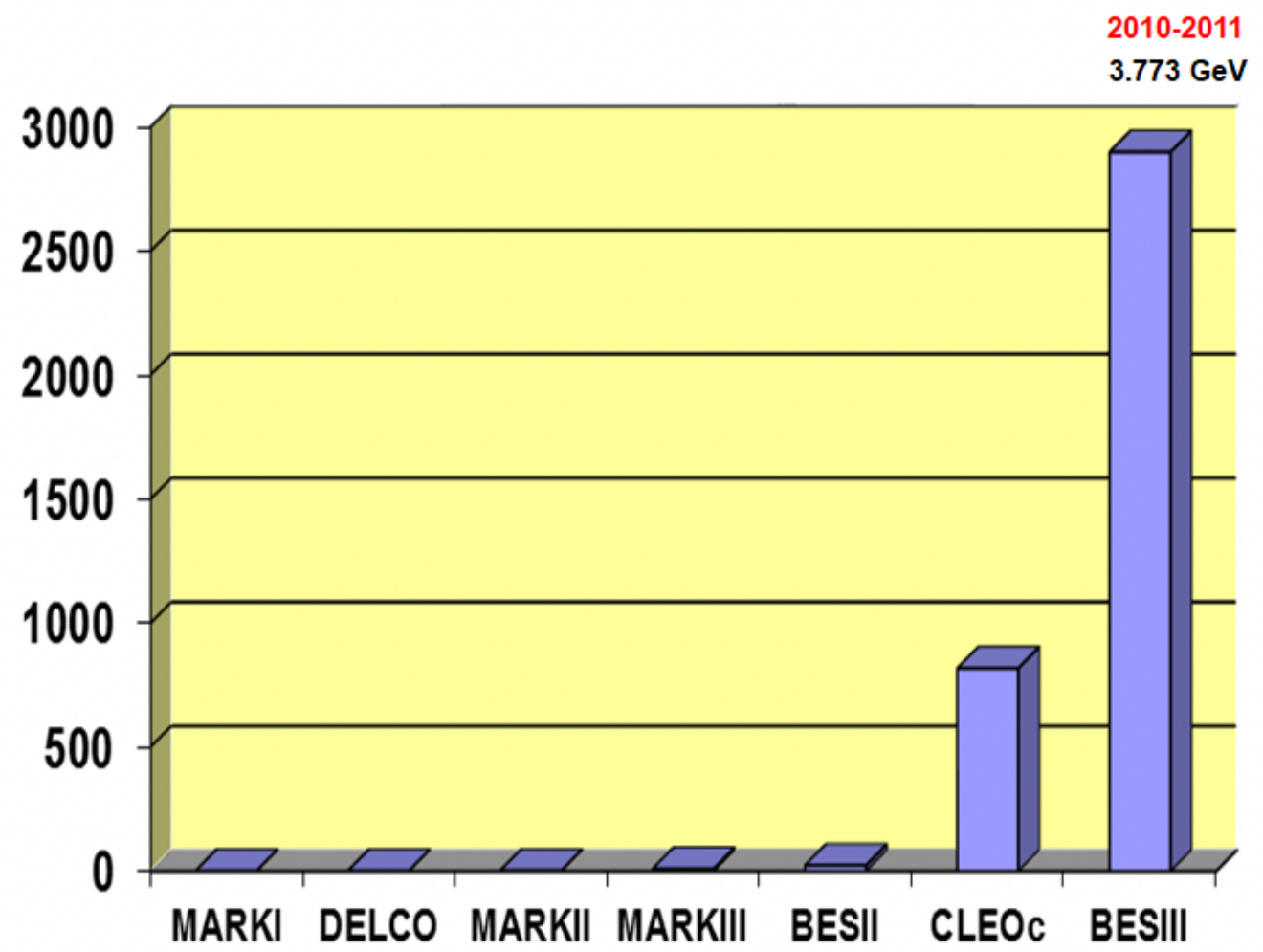
Belle, Belle-II

- Asymmetric e^+e^- collider
- E_{cm} : 10.8 GeV
- Charm collected through $b\bar{b}$ decays and $c\bar{c}$

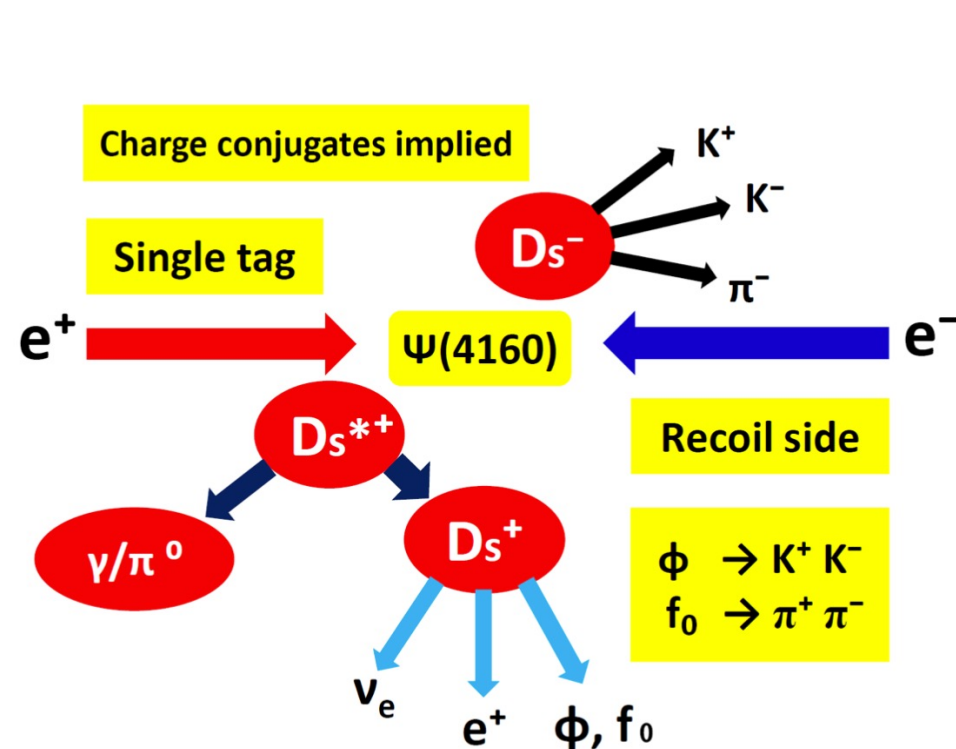


Experiment	Data size	Energy region	Time
BESIII	$D^{+(0)}: 2.93 \text{ fb}^{-1}$ $D_s^+: 7.33 \text{ fb}^{-1}$	3.773 GeV 4.123-4.223 GeV	2010-2011 2013-2017
CLEO-c	$D^{+(0)}: 0.82 \text{ fb}^{-1}$ $D_s^+: 0.6 \text{ fb}^{-1}$	3.770 GeV 4.170 GeV	Till 2008
BABAR	468 fb^{-1}	Near $\Upsilon(4S)$	Till 2008
Belle	976 fb^{-1}	Near $\Upsilon(4S)$	Till 2010

$D^{0(+)}$ samples at $\psi(3770)$



Take Ds decay as an example (complicated case)



$$\mathcal{B}_\gamma(D_S^{*+} \rightarrow \gamma D_S)$$

$$N_{tag} = 2N_{D_S^+ D_S^-} \mathcal{B}_{tag} \epsilon_{tag}$$

$$N_{sig} = 2N_{D_S^+ D_S^-} \mathcal{B}_{tag} \mathcal{B}_{sig} \mathcal{B}_\gamma \epsilon_{sig}$$

$$\mathcal{B}_{sig} = \frac{N_{sig}}{\mathcal{B}_\gamma N_{tag} \epsilon_{sig} / \epsilon_{tag}}$$

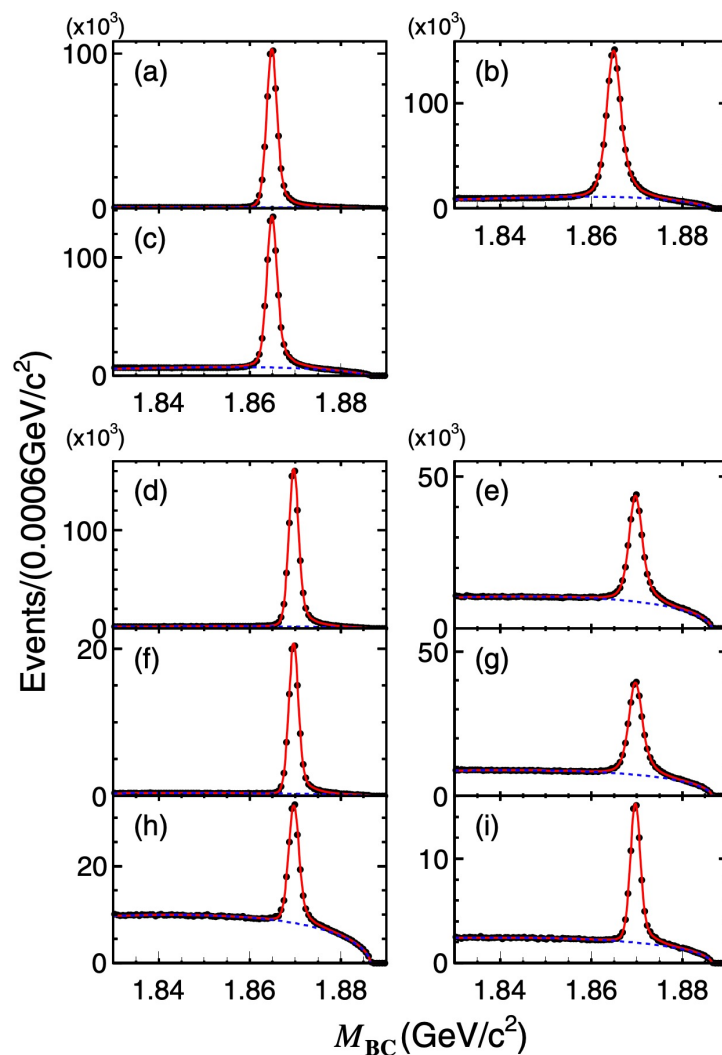
$$\mathcal{B}_{sig} = \frac{N_{sig}}{\mathcal{B}_\gamma \sum_\alpha N_{tag}^\alpha \epsilon_{sig}^\alpha / \epsilon_{tag}^\alpha}$$

$$U_{miss} = E_{miss} - |\vec{p}_{miss}|$$

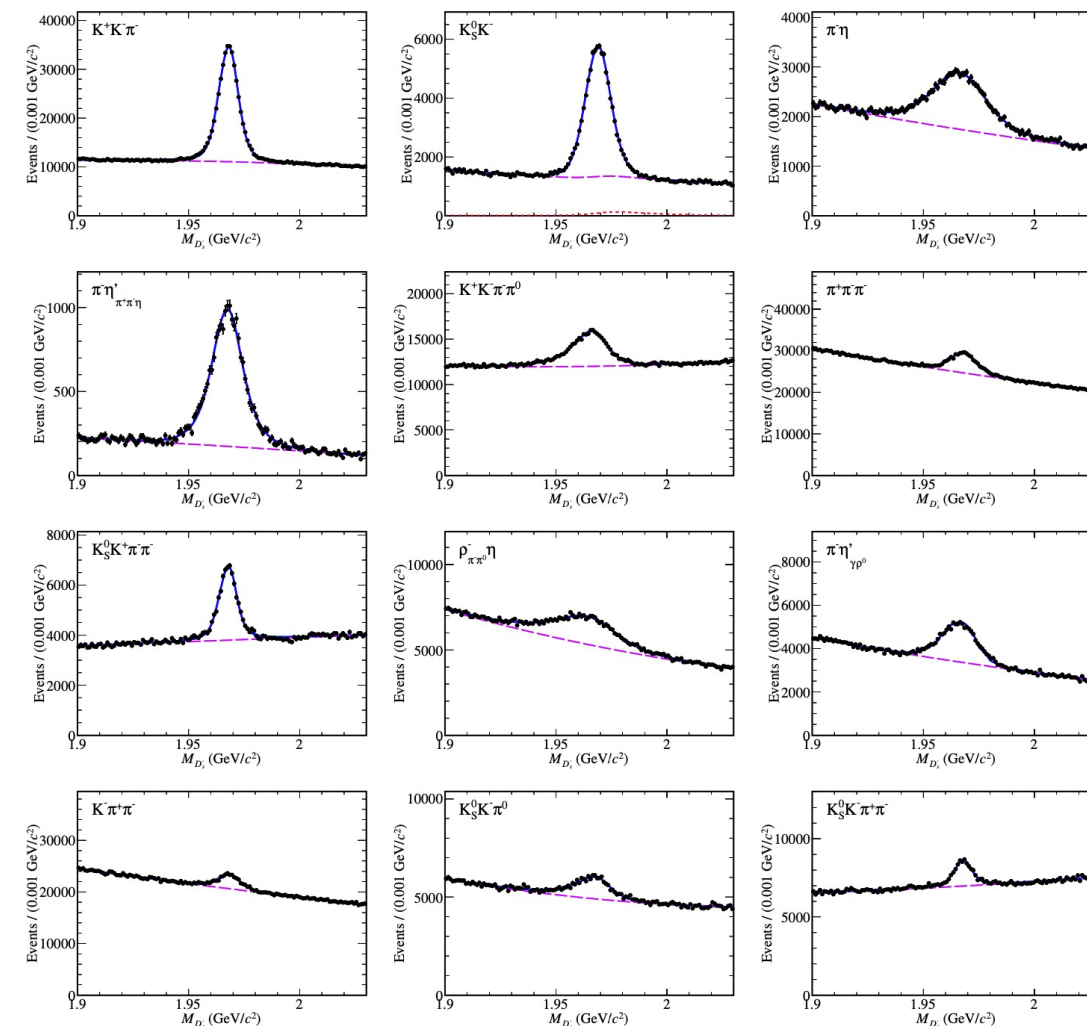
$$M_{miss}^2 = E_{miss}^2 - |\vec{p}_{miss}|^2$$

Analysis method: Single Tag sample

$D^0: \sim 2.76 \text{ M}$



$D^+: \sim 1.57 \text{ M}$



$D_s: 0.77 \text{ M}$

The differential decay rate of $D_{(s)} \rightarrow S \ell \nu_\ell$

$$\Gamma(D_{(s)} \rightarrow S \ell^+ \nu_\ell)/dq^2 \propto |V_{cd(s)}|^2 |f_+(q^2)|^2$$

$$S: a_0(980), f_0(500), f_0(980)$$

- Use least χ^2 method to fit the measured partial decay width in different q^2 bin
- Taking the correlations among q^2 bins into account
- FF in different form (The width needs to be considered ?)

– **Single pole form**

$$f_+(q^2) = \frac{f_+(0)}{1 - q^2/M_{pole}^2}$$

– **Modified pole model**

$$f_+(q^2) = \frac{f_+(0)}{\left(1 - \frac{q^2}{M_{pole}^2}\right) \left(1 - \alpha \frac{q^2}{M_{pole}^2}\right)}$$

– **ISGW2 model**

$$f_+(q^2) = f_+(q_{max}^2) \left(1 + \frac{r^2}{12}(q_{max}^2 - q^2)\right)^{-2}$$

– **Series expansion model**

$$f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{k=1}^{\infty} r_k(t_0) [z(t, t_0)]^k\right)$$

- Point-like differential decay rate:

$$\frac{d\Gamma(D_{(s)} \rightarrow S \ell^+ \nu_\ell)}{dq^2} = \frac{G_F^2 |V_{cs}|^2}{24\pi^3} p_{f_0}^3 |f_+(q^2)|^2$$

- Double differential decay rate:

(N.N.Achasov *et al.*, PRD102,016022(2020); W. Wang, PLB759,501(2016))

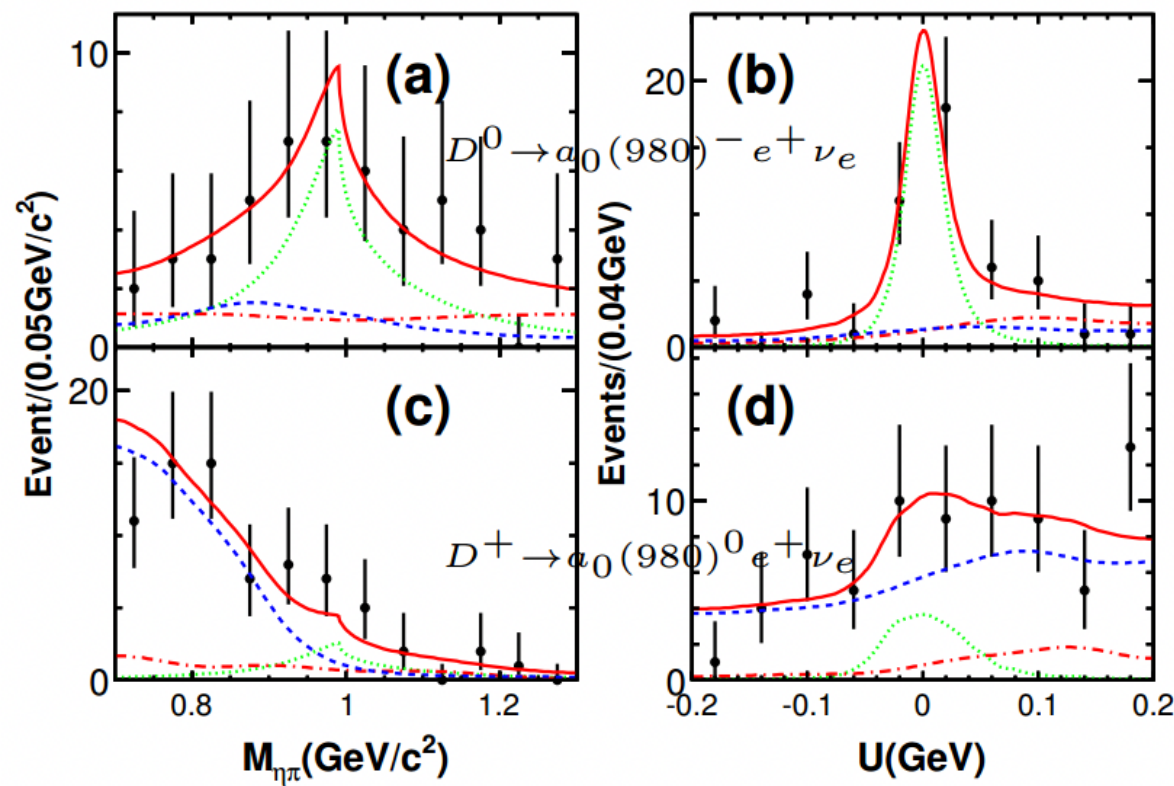
$$\frac{d^2\Gamma(D_{(s)} \rightarrow S \ell^+ \nu_\ell)}{ds dq^2} = \frac{G_F^2 |V_{cs}|^2}{192\pi^4 m_{D_{(s)}}^3} \lambda^{\frac{3}{2}}(m_{D_{(s)}}^2, s, q^2) |f_+(q^2)|^2 P(s)$$

$$P(s) = \begin{cases} \frac{g_1 \rho_{\pi\pi}}{|m_0^2 - s - i(g_1 \rho_{\pi\pi} + g_1 \rho_{KK})|^2}, & \text{Flatte: } a_0(980)/f_0(980) \\ \frac{m_{f_0} \Gamma(s)}{(s - m_{f_0}^2)^2 + m_{f_0}^2 \Gamma^2(s)}, & \text{RBW: } f_0(500) \end{cases}$$

First observation of $D^0 \rightarrow a_0(980)^- e^+ \nu_e$

Phys. Rev. Lett. 121, 081802 (2018)

- 2.93 fb⁻¹ data @ 3.773 GeV
- $N_{sig}^{D^0} = 25.7^{+6.4}_{-5.7}$
- $N_{sig}^{D^+} = 10.2^{+5.0}_{-4.1}$
- BFs help to understand the nature of the $a_0(980)$



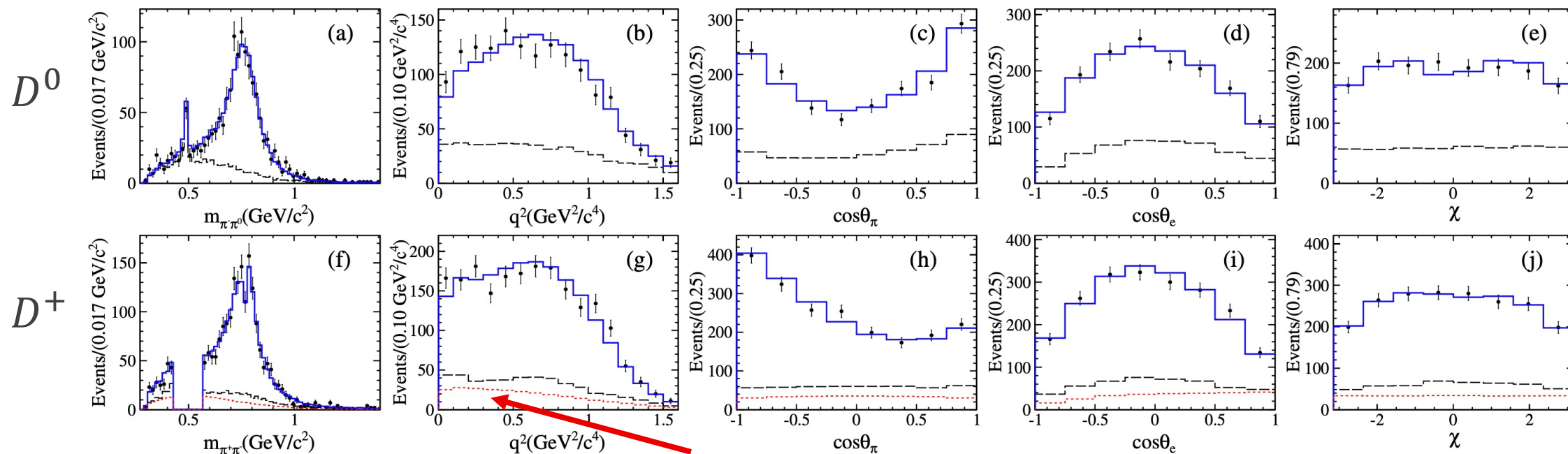
Decay	BF ($\times 10^{-4}$)	Significance
$D^0 \rightarrow a_0(980)^- e^+ \nu_e, a_0(980)^- \rightarrow \eta \pi^-$	$1.33^{+0.33}_{-0.29} \pm 0.09$	6.4σ
$D^+ \rightarrow a_0(980)^0 e^+ \nu_e, a_0(980)^0 \rightarrow \eta \pi^0$	$1.66^{+0.81}_{-0.66} \pm 0.11$ < 3.0 (90% C.L.)	2.9σ

First observation of $D^+ \rightarrow f_0(500)e^+ \nu_e$

Phys. Rev. Lett. 122, 062001 (2019)

$$N_{sig}^{D^0} = 1498 \text{ (Bkg: } \sim 33.3\%)$$

$$N_{sig}^{D^+} = 2017 \text{ (Bkg: } \sim 23.8\%)$$



➤ 2.93 fb⁻¹ data @ 3.773 GeV

$$f_{f_0(500)} = (25.7 \pm 1.6 \pm 1.1)\%$$

➤ $R = \frac{\mathcal{B}(D^+ \rightarrow f_0(500)e^+ \nu_e) + \mathcal{B}(D^+ \rightarrow f_0(980)e^+ \nu_e)}{\mathcal{B}(D^+ \rightarrow a_0(980)e^+ \nu_e)} > 2.7 @ 90\% CL$

➤ Favor tetraquark (R=3, PRD82, 034016(2010)) for f_0 and a_0

Signal mode	This analysis ($\times 10^{-3}$)
$D^0 \rightarrow \pi^- \pi^0 e^+ \nu_e$	$1.445 \pm 0.058 \pm 0.039$
$D^0 \rightarrow \rho^- e^+ \nu_e$	$1.445 \pm 0.058 \pm 0.039$
$D^+ \rightarrow \pi^- \pi^+ e^+ \nu_e$	$2.449 \pm 0.074 \pm 0.073$
$D^+ \rightarrow \rho^0 e^+ \nu_e$	$1.860 \pm 0.070 \pm 0.061$
$D^+ \rightarrow \omega e^+ \nu_e$	$2.05 \pm 0.66 \pm 0.30$
$D^+ \rightarrow f_0(500)e^+ \nu_e, f_0(500) \rightarrow \pi^+ \pi^-$	$0.630 \pm 0.043 \pm 0.032$
$D^+ \rightarrow f_0(980)e^+ \nu_e, f_0(980) \rightarrow \pi^+ \pi^-$	< 0.028



Phys. Rev. D. 105, L031101 (2022)

- 6.32 fb⁻¹ data @ 4.178-4.226 GeV
- $N_{sig}^{f_0(980)} = 54.8 + 10.1$ (7.8 σ significance)

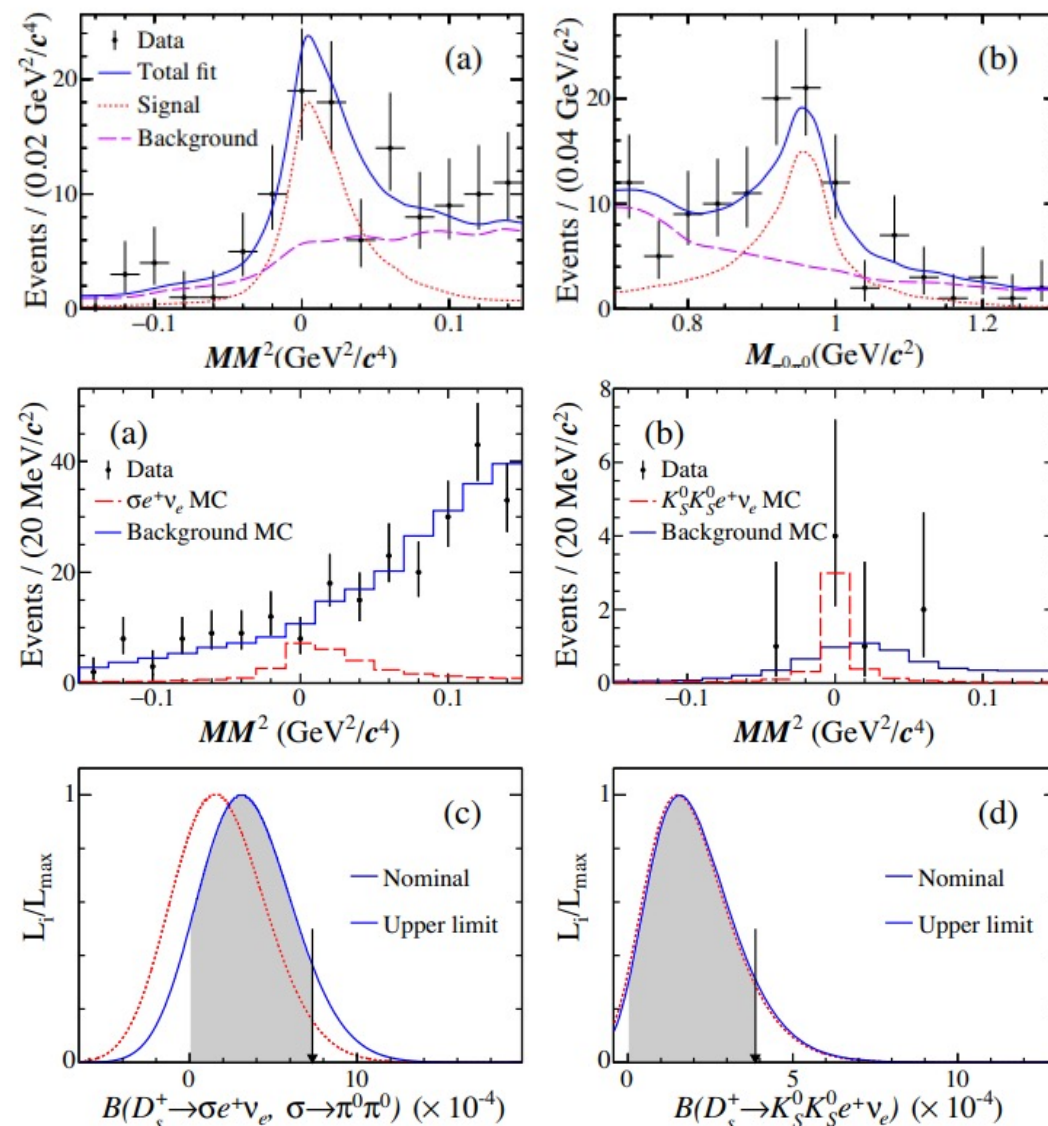
- First BF's Measurement:

$$\mathcal{B}(D_s^+ \rightarrow f_0(980)e^+ \nu_e, f_0(980) \rightarrow \pi^0 \pi^0) \\ = (7.9 \pm 1.4 \pm 0.4) \times 10^{-4}$$

- No significant signal:

$$\mathcal{B}(D_s^+ \rightarrow f_0(500)e^+ \nu_e, f_0(500) \rightarrow \pi^0 \pi^0) < 7.3 \times 10^{-4} \\ \mathcal{B}(D_s^+ \rightarrow K_S^0 K_S^0 e^+ \nu_e) < 3.8 \times 10^{-4}$$

- BF's help to understand the nature of the $f_0(500)$ and $f_0(980)$, and test different theoretical calculations.



Arxiv: 2303.12927 (submitted to PRL)

➤ 7.33 fb⁻¹ data @ 4.128-4.226 GeV

➤ $N_{sig} = 439 \pm 33$

$$\mathcal{B}(D_s^+ \rightarrow f_0(980) e^+ \nu_e, f_0(980) \rightarrow \pi^+ \pi^-)$$

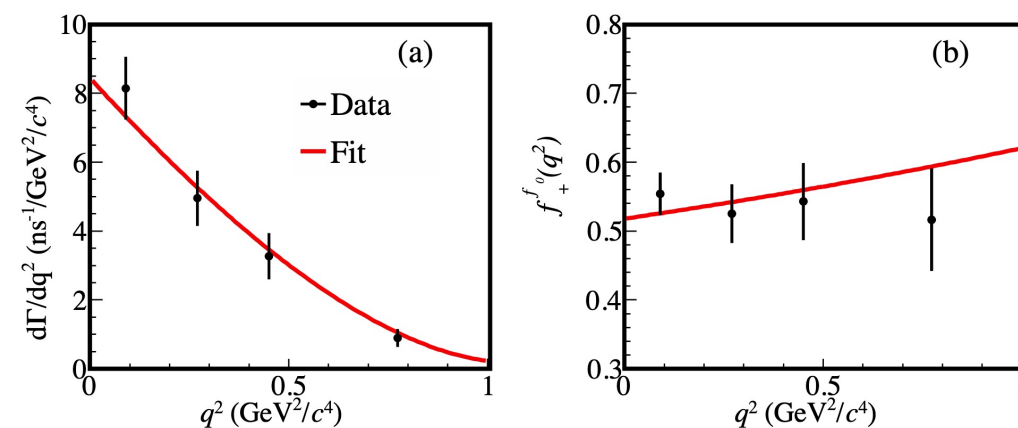
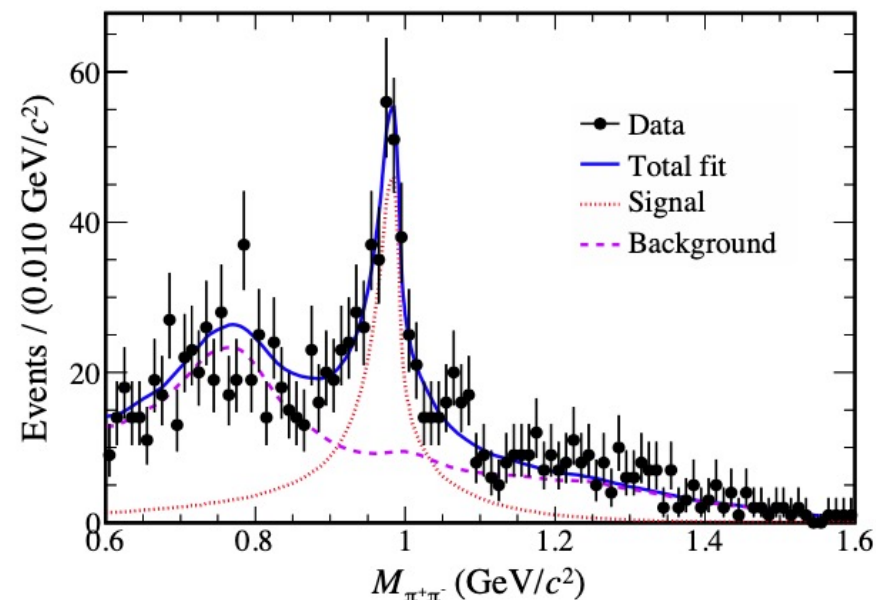
$$= (1.72 \pm 0.13 \pm 0.10) \times 10^{-3}$$

→ $s\bar{s}$ is dominant based on $q\bar{q}$ mixture picture

➤ **First form factor measurement** based on single pole:

$$f_+^{f_0}(0) |V_{cs}| = 0.504 + 0.017 + 0.35$$

ps: Have considered the width effect of the $f_0(980)$



Summary:

- BESIII has the largest data samples at $D\bar{D}/D_s D_s^*$ threshold.
- Light scalar mesons are studied systematically via semi-leptonic D decay.
- BF and FF measurements help to understand the nature of light scalar mesons.

Prospect:

- BESIII has **8 fb⁻¹** @3.773 GeV now.
- In the coming 2024, BESIII will have **20 fb⁻¹** @3.773 GeV in total.
- More results are on the way!

Thank you!