



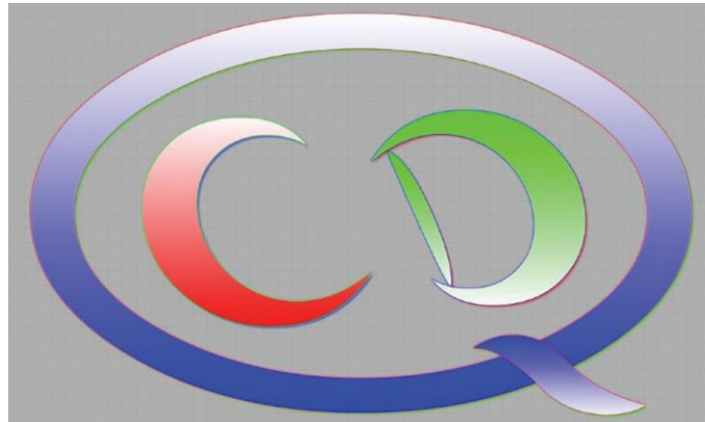
Strangeness in nuclear systems (B6)

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Publications (NSFC No. 12070131001)

- ❑ X.-X. Sun, S.-G. Zhou, Angular momentum projection in the deformed relativistic Hartree-Bogoliubov theory in continuum, *Phys. Rev. C*. 104 (2021) 064319.
- ❑ X.-X. Sun, S.-G. Zhou, Rotating deformed halo nuclei and shape decoupling effects, *Science Bulletin*. 66 (2021) 2072–2078.
- ❑ Y.-T. Rong, Z.-H. Tu, S.-G. Zhou, New effective interactions for hypernuclei in a density-dependent relativistic mean field model, *Phys. Rev. C*. 104 (2021) 054321.
- ❑ G.G. Adamian, N.V. Antonenko, H. Lenske, L.A. Malov, S.-G. Zhou, Self-consistent methods for structure and production of heavy and superheavy nuclei, *Eur. Phys. J. A*. 57 (2021) 89.
- ❑ K. Zhang, M.-K. Cheoun, Y.-B. Choi, P.S. Chong, J. Dong, Z. Dong, X. Du, L. Geng, E. Ha, X.-T. He, C. Heo, M.C. Ho, E.J. In, S. Kim, Y. Kim, C.-H. Lee, J. Lee, H. Li, Z. Li, T. Luo, J. Meng, M.-H. Mun, Z. Niu, C. Pan, P. Papakonstantinou, X. Shang, C. Shen, G. Shen, W. Sun, X.-X. Sun, C.K. Tam, Thavayongnong, C. Wang, X. Wang, S.H. Wong, J. Wu, X. Wu, X. Xia, Y. Yan, R.W.-Y. Yeung, T.C. Yiu, S. Zhang, W. Zhang, X. Zhang, Q. Zhao, S.-G. Zhou, Nuclear mass table in deformed relativistic Hartree–Bogoliubov theory in continuum, I: Even–even nuclei, *At. Data Nucl. Data Tables*. 144 (2022) 101488.
- ❑ X.-Q. Wang, X.-X. Sun, S.-G. Zhou, Microscopic study of higher-order deformation effects on the ground states of superheavy nuclei around ^{270}Hs , *Chin. Phys. C*. 46 (2022) 024107.

- ❑ C.G. Wang, R. Han, C. Xu, H. Hua, R.A. Bark, S.Q. Zhang, S.Y. Wang, T.M. Shneidman, S.G. Zhou, J. Meng, S.M. Wyngaardt, A.C. Dai, F.R. Xu, X.Q. Li, Z.H. Li, Y.L. Ye, D.X. Jiang, C.G. Li, C.Y. Niu, Z.Q. Chen, H.Y. Wu, D.W. Luo, S. Wang, D.P. Sun, C. Liu, Z.Q. Li, N.B. Zhang, R.J. Guo, P. Jones, E.A. Lawrie, J.J. Lawrie, J.F. Sharpey-Schafer, M. Wiedeking, S.N.T. Majola, T.D. Bucher, T. Dinoko, B. Maqabuka, L. Makhathini, L. Mdletshe, O. Shirinda, K. Sowazi, First evidence of an octupole rotational band in Ge isotopes, *Phys. Rev. C.* 106 (2022) L011303.
- ❑ Z.-H. Tu, S.-G. Zhou, Effects of the ϕ Meson on the Properties of Hyperon Stars in the Density-dependent Relativistic Mean Field Model, *Astrophys. J.* 925 (2022) 16.
- ❑ Z.-H. Tu, 1S_0 hyperon superfluidity in neutron stars from a separable pairing force of finite range, *Phys. Rev. C.* 106 (2022) 025806.
- ❑ C. Pan, M.-K. Cheoun, Y.-B. Choi, J. Dong, X. Du, X.-H. Fan, W. Gao, L. Geng, E. Ha, X.-T. He, J. Huang, K. Huang, S. Kim, Y. Kim, C.-H. Lee, J. Lee, Z. Li, Z.-R. Liu, Y. Ma, J. Meng, M.-H. Mun, Z. Niu, P. Papakonstantinou, X. Shang, C. Shen, G. Shen, W. Sun, X.-X. Sun, J. Wu, X. Wu, X. Xia, Y. Yan, T.C. Yiu, K. Zhang, S. Zhang, W. Zhang, X. Zhang, Q. Zhao, R. Zheng, S.-G. Zhou, DRHBc Mass Table Collaboration, Deformed relativistic Hartree-Bogoliubov theory in continuum with a point-coupling functional. II. Examples of odd Nd isotopes, *Phys. Rev. C.* 106 (2022) 014316.
- ❑ X.-Q. Deng, S.-G. Zhou, Examination of promising reactions with ^{241}Am and ^{244}Cm targets for the synthesis of new superheavy elements within the dinuclear system model with a dynamical potential energy surface, *Phys. Rev. C.* 107 (2023) 014616.
- ❑ X.-X. Sun, S.-G. Zhou, Models for Pairing Phenomena, in: I. Tanihata, H. Toki, T. Kajino (Eds.), *Handbook of Nuclear Physics*, Springer Nature Singapore, Singapore, 2022: pp. 1–34.

Outline

- Introduction
- New effective interactions for hypernuclei in density-dependent relativistic mean field model
- Effects of ϕ meson on properties of hyperon stars in density-dependent relativistic mean field model
- Summary & perspectives

Covariant Density Functional Theory (CDFT)

$$\begin{aligned} \mathcal{L} = & \sum_B \bar{\psi}_B \left(i\gamma_\mu \partial^\mu - M_B - g_{\sigma B} \sigma - g_{\sigma^* B} \sigma^* - g_{\omega B} \gamma_\mu \omega^\mu - g_{\phi B} \gamma_\mu \phi^\mu - g_{\rho B} \gamma_\mu \vec{\tau} \cdot \vec{\rho}^\mu - e\gamma_\mu \frac{1 - \tau_3}{2} A^\mu \right) \psi_B \\ & + \psi_\Lambda \frac{f_{\omega\Lambda\Lambda}}{4M_\Lambda} \sigma_{\mu\nu} \Omega^{\mu\nu} \psi_\Lambda + \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma - \frac{1}{2} m_\sigma^2 \sigma^2 + \frac{1}{2} \partial_\mu \sigma^* \partial^\mu \sigma^* - \frac{1}{2} m_{\sigma^*}^2 \sigma^{*2} - \frac{1}{4} \Omega^{\mu\nu} \Omega_{\mu\nu} + \frac{1}{2} m_\omega^2 \omega^\mu \omega_\mu \\ & - \frac{1}{4} S^{\mu\nu} S_{\mu\nu} + \frac{1}{2} m_\phi^2 \phi^\mu \phi_\mu - \frac{1}{4} \vec{R}^{\mu\nu} \vec{R}_{\mu\nu} + \frac{1}{2} m_\rho^2 \vec{\rho}^\mu \vec{\rho}_\mu - \frac{1}{4} F^{\mu\nu} F_{\mu\nu}, \end{aligned}$$

Serot_Walecka1986_ANP16-1

Reinhard1989_RPP52-439

Ring1996_PPNP37-193

$$[\boldsymbol{\alpha} \cdot \mathbf{p} + V_B + T_B + \Sigma_R + \beta(M_B + S_B)]\psi_{iB} = \varepsilon_i \psi_{iB},$$

Vretenar_Afanasjev_Lalazissis_Ring2005_PR409-101

$$(-\Delta + m_\sigma^2)\sigma = -g_{\sigma N} \rho_N^s - g_{\sigma\Lambda} \rho_\Lambda^s,$$

Meng_Toki_SGZ_Zhang_Long_Geng2006_PPNP57-470

$$(-\Delta + m_{\sigma^*}^2)\sigma^* = -g_{\sigma^* \Lambda} \rho_\Lambda^s,$$

Liang_Meng_SGZ2015_PR570-1

$$(-\Delta + m_\omega^2)\omega_0 = g_{\omega N} \rho_N^v + g_{\omega\Lambda} \rho_\Lambda^v - \frac{f_{\omega\Lambda\Lambda}}{2M_\Lambda} \rho_\Lambda^T,$$

Meng_SGZ2015_JPG42-093101

$$(-\Delta\phi + m_\phi^2)\phi = g_{\phi\Lambda} \rho_\Lambda^v,$$

Meng (ed.), Relativistic Density Functional for Nuclear structure (World Scientific, 2016)

$$(-\Delta + m_\rho^2)\rho_0 = g_{\rho N} (\rho_n^v - \rho_p^v),$$

$$-\Delta A_0 = e\rho_p^v.$$

MDC-CDFT ($\beta_{20}, \beta_{22}, \beta_{30}, \beta_{32}, \beta_{40}, \dots$)

- Axially deformed harmonic oscillator (ADHO) basis Ring_Gambhir_Lalazissis1997_CPC105-77

$$\left[-\frac{\hbar^2}{2M} \nabla^2 + V_B(z, \rho) \right] \Phi_\alpha(\mathbf{r}\sigma) = E_\alpha \Phi_\alpha(\mathbf{r}\sigma) \quad V_B(z, \rho) = \frac{1}{2} M (\omega_\rho^2 \rho^2 + \omega_z^2 z^2)$$

$$\Phi_\alpha(\mathbf{r}\sigma) = C_\alpha \phi_{n_z}(z) R_{n_\rho}^{m_l}(\rho) \frac{1}{\sqrt{2\pi}} e^{im_l \varphi} \chi_{s_z}(\sigma)$$

- Fourier expansion for densities & potentials

$$f(\rho, \varphi, z) = f_0(\rho, z) \frac{1}{\sqrt{2\pi}} + \sum_{n=1}^{\infty} f_n(\rho, z) \frac{1}{\sqrt{\pi}} \cos(2n\varphi) \quad f = V \text{ or } \rho$$

- A modified linear constraint method

$$E' = E_{\text{RMF}} + \sum_{\lambda\mu} \frac{1}{2} C_{\lambda\mu} Q_{\lambda\mu} \quad C_{\lambda\mu}^{(n+1)} = C_{\lambda\mu}^{(n)} + k_{\lambda\mu} \left(\beta_{\lambda\mu}^{(n)} - \beta_{\lambda\mu} \right)$$

MDC-CDFT ($\beta_{20}, \beta_{22}, \beta_{30}, \beta_{32}, \beta_{40}, \dots$)

ph channel	Non-linear	Density-dependent
Meson exchange	NL3, NL3*, PK1, ...	DD-ME1, DD-ME2, ...
Point Coupling	PC-F1, PC-PK1, ...	DD-PC1, ...

MDC-RMF

MDC-RHB

pp channel	BCS	Bogoliubov
Constant gap	√	-
Constant strength	√	-
Delta force	√	√
Separable force	√	√

Lu_Zhao_Zhao_SGZ
2014_PRC89-014323

Zhao_Lu_Zhao_SGZ
2017_PRC95-014320

Applications of MDC-CDFTs

- Potential energy surface, ground state & fission properties
 - $(\beta_{20}, \beta_{22}, \beta_{30})$: 1-, 2- & 3-dim PES of ^{240}Pu & B_f 's of actinides
 - (β_{20}, β_{22}) : Shape polarization effect of Λ
 - (β_{20}) : Superdeformed shapes in Λ hypernuclei
 - (β_{20}) : Third barriers in light actinides
 - (β_{20}, β_{30}) : Octupole correlations & shape transitions
 - $(\beta_{20}, \beta_{22}, \beta_{30})$: Octupole correlations in $M\chi D$
 - (β_{20}, β_{32}) : Nuclear Tetrahedral shapes
 - $(\beta_{20}, \beta_{22}, \beta_{30})$: 1-, 2-, & 3-dim PES of ^{270}Hs
 - $(\beta_{\lambda\mu}, R)$: Clustering, bubble & toroidal structure; GMR
- Fission dynamics based on PES from MDC-CDFTs
 - Spontaneous fission
 - Induced fission
- Angular momentum & parity projected MDC-CDFTs
 - Clustering & exotic shapes

MultiDimensionally-
Constrained
Covariant Density
Functional Theories

MDC-CDFT ($\beta_{20}, \beta_{22}, \beta_{30}, \beta_{32}, \beta_{40}, \dots$)

ph channel	Non-linear	Density-dependent
Meson exchange	NL3, NL3*, PK1, ...	DD-ME1, DD-ME2, ...
Point Coupling	PC-F1, PC-PK1, ...	DD-PC1, ...

□ Motivation of the present work

- Not many effective DD interactions for hypernuclei
- Spherical shapes assumed when these effective interactions were obtained though most observed hypernuclei are deformed

□ Aim of the present work

- New effective DD interactions for hypernuclei with deformation effects considered in fitting

Density dependent (DD) coupling constants

$$\mathcal{L} = \sum_B \bar{\psi}_B \left(i\gamma_\mu \partial^\mu - M_B - g_{\sigma B} \sigma - g_{\sigma^* B} \sigma^* - g_{\omega B} \gamma_\mu \omega^\mu - g_{\phi B} \gamma_\mu \phi^\mu - g_{\rho B} \gamma_\mu \vec{\tau} \cdot \vec{\rho}^\mu - e\gamma_\mu \frac{1 - \tau_3}{2} A^\mu \right) \psi_B$$

$$+ \psi_\Lambda \frac{f_{\omega\Lambda\Lambda}}{4M_\Lambda} \sigma_{\mu\nu} \Omega^{\mu\nu} \psi_\Lambda + \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma - \frac{1}{2} m_\sigma^2 \sigma^2 + \frac{1}{2} \partial_\mu \sigma^* \partial^\mu \sigma^* - \frac{1}{2} m_{\sigma^*}^2 \sigma^{*2} - \frac{1}{4} \Omega^{\mu\nu} \Omega_{\mu\nu} + \frac{1}{2} m_\omega^2 \omega^\mu \omega_\mu$$

$$- \frac{1}{4} S^{\mu\nu} S_{\mu\nu} + \frac{1}{2} m_\phi^2 \phi^\mu \phi_\mu - \frac{1}{4} \vec{R}^{\mu\nu} \vec{R}_{\mu\nu} + \frac{1}{2} m_\rho^2 \vec{\rho}^\mu \vec{\rho}_\mu - \frac{1}{4} F^{\mu\nu} F_{\mu\nu},$$

$$g_{mB}(\rho^\nu) = g_{mB}(\rho_{\text{sat}}) f_{mB}(x), \quad x = \rho^\nu / \rho_{\text{sat}},$$

$$R_m = g_{m\Lambda}(\rho_{\text{sat}}) / g_{mN}(\rho_{\text{sat}})$$

R_σ and R_ω

$$f_{mN}(x) = \begin{cases} a_m \frac{1 + b_m(x + d_m)^2}{1 + c_m(x + d_m)^2}, & m = \sigma \text{ or } \omega \\ e^{-a_\rho(x - 1)}, & m = \rho, \end{cases}$$

$$f_\sigma(1) = 1, f_\omega(1) = 1, f_\sigma''(0) = 0, f_\omega''(0) = 0, \text{ and } f_\sigma''(1) = f_\omega''(1)$$

New effective DD interactions

Rong(荣宇婷)_Tu(涂中豪)_
SGZ 2021_PRC104-054321

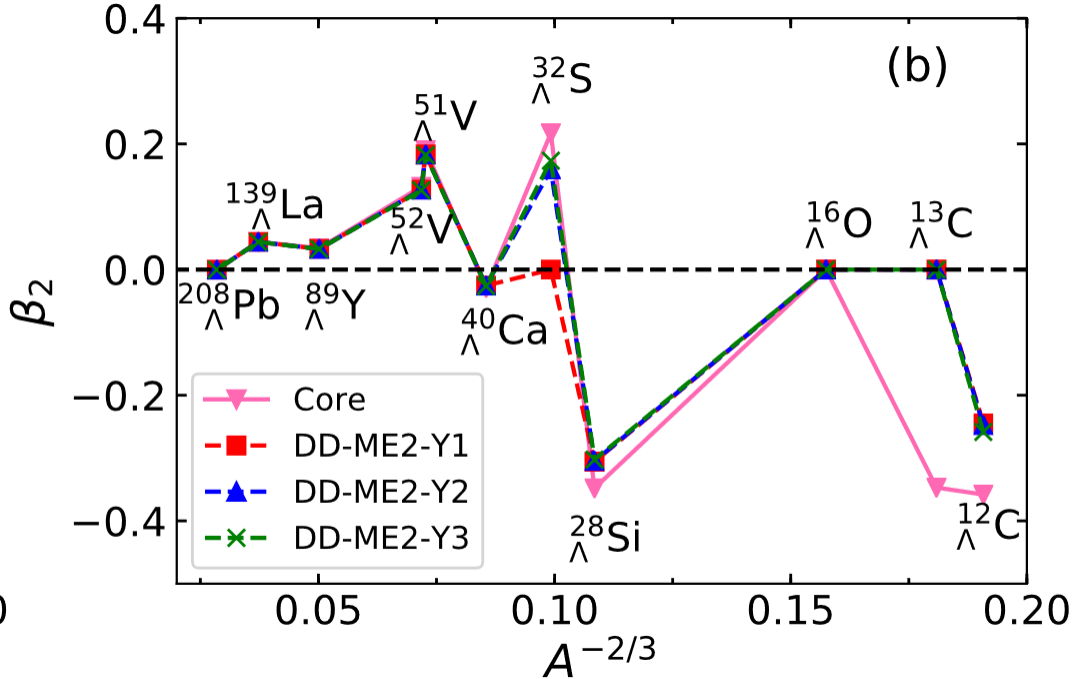
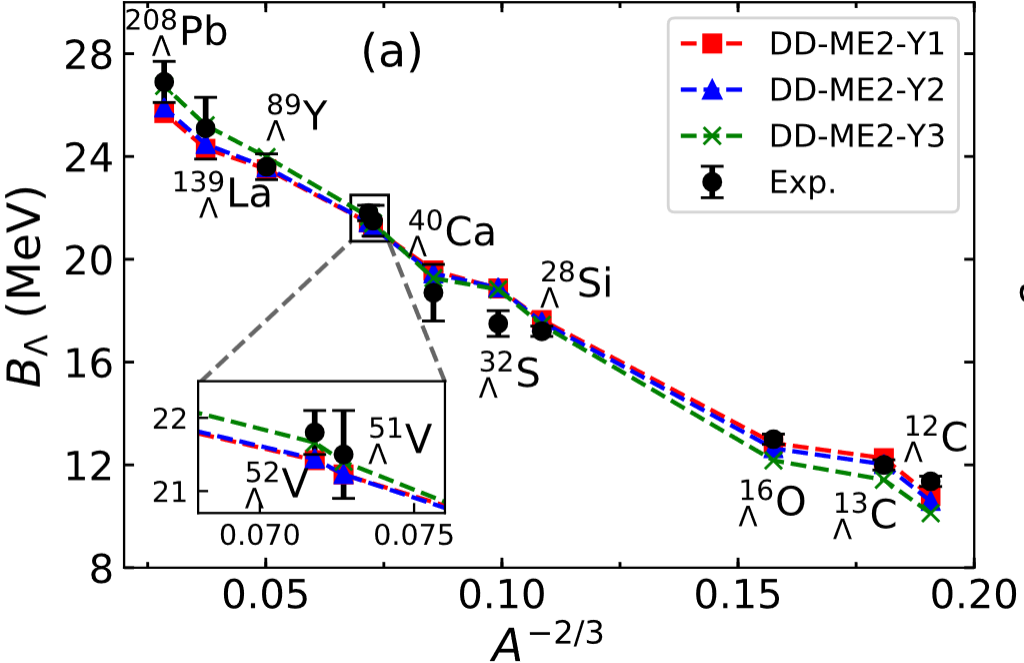
Hypernucleus	Expt.	DD-ME-Yi				PKDD-Yi			
		$i = 0$	$i = 1$	$i = 2$	$i = 3$	$i = 0$	$i = 1$	$i = 2$	$i = 3$
${}_{\Lambda}^{12}\text{C}$	11.36 ± 0.20	25.514	10.789	10.588	10.120	25.566	10.854	10.514	10.013
${}_{\Lambda}^{13}\text{C}$	12.0 ± 0.2	28.080	12.262	12.023	11.422	27.814	11.932	11.534	10.944
${}_{\Lambda}^{16}\text{O}$	13.0 ± 0.2	27.516	12.849	12.643	12.174	27.771	13.089	12.684	12.105
${}_{\Lambda}^{28}\text{Si}$	17.2 ± 0.2	34.724	17.643	17.560	17.450	34.857	17.731	17.578	17.469
${}_{\Lambda}^{32}\text{S}$	17.5 ± 0.5	36.814	18.865	18.895	18.827	36.341	18.824	18.695	18.640
${}_{\Lambda}^{40}\text{Ca}$	18.7 ± 1.1	36.600	19.566	19.448	19.265	36.730	19.756	19.493	19.235
${}_{\Lambda}^{51}\text{V}$	21.5 ± 0.6	39.126	21.227	21.228	21.401	39.095	21.251	21.221	21.407
${}_{\Lambda}^{52}\text{V}$	21.8 ± 0.3	39.429	21.422	21.440	21.662	39.348	21.400	21.402	21.649
${}_{\Lambda}^{89}\text{Y}$	23.6 ± 0.5	41.882	23.511	23.576	23.974	41.788	23.501	23.578	24.018
${}_{\Lambda}^{139}\text{La}$	25.1 ± 1.2	42.691	24.306	24.479	25.215	42.226	23.987	24.295	25.210
${}_{\Lambda}^{208}\text{Pb}$	26.9 ± 0.8	44.489	25.687	25.893	26.746	44.029	25.337	25.694	26.729
$\bar{\chi}^2$			2.543	1.867	0.185		2.580	1.889	0.211
$\bar{\chi}_{\text{all}}^2$		2956.907	2.543	3.009	6.690	2954.595	2.580	3.666	9.233
Δ		17.175	0.711	0.672	0.668	17.048	0.816	0.712	0.716
δ		98.221	3.759	3.840	4.817	97.776	4.018	4.060	5.419
R_{σ}		0.667	0.366	0.417	0.577	0.667	0.367	0.464	0.659
R_{ω}		0.667	0.352	0.415	0.611	0.667	0.353	0.472	0.712
$\sigma_{R_{\sigma}}^{+}$			0.053	0.036	0.080		0.080	0.092	0.084
$\sigma_{R_{\sigma}}^{-}$			0.079	0.071	0.082		0.088	0.093	0.085

New effective DD interactions

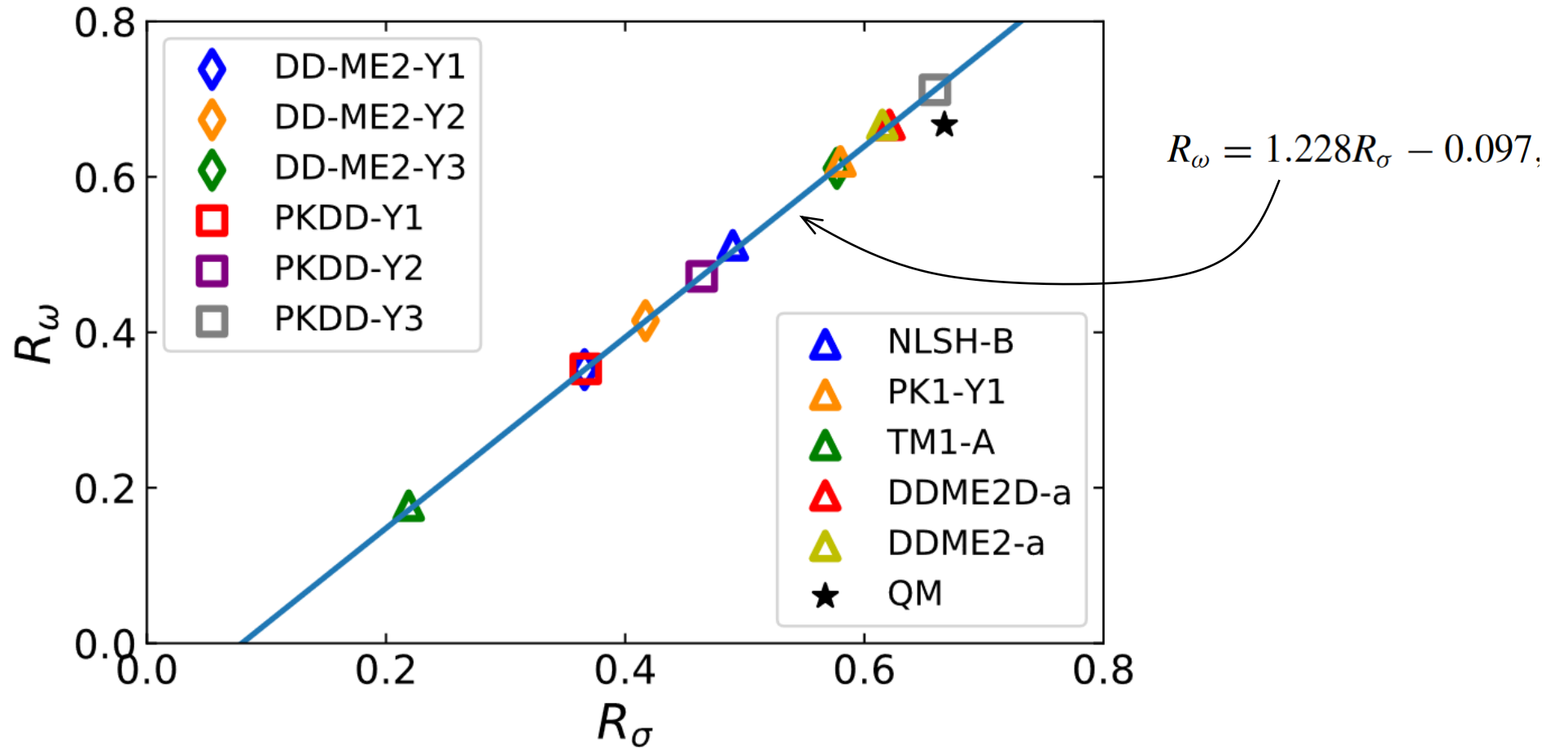
Rong(荣宇婷)_Tu(涂中豪)_
SGZ 2021_PRC104-054321

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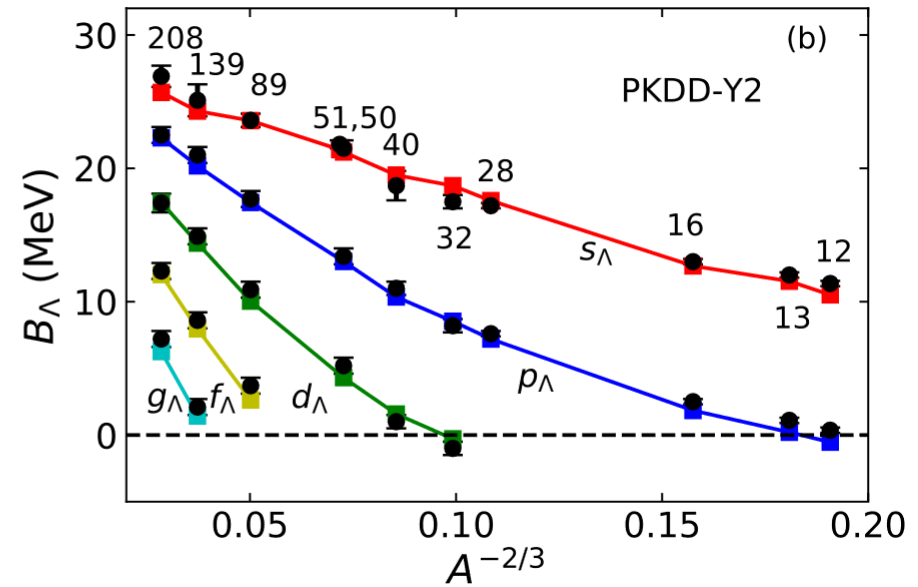
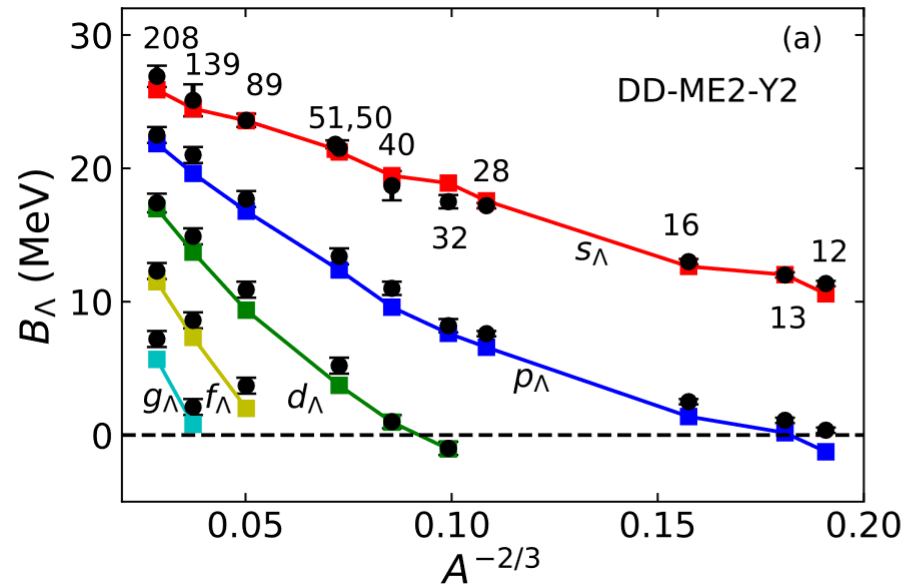
Ground state properties



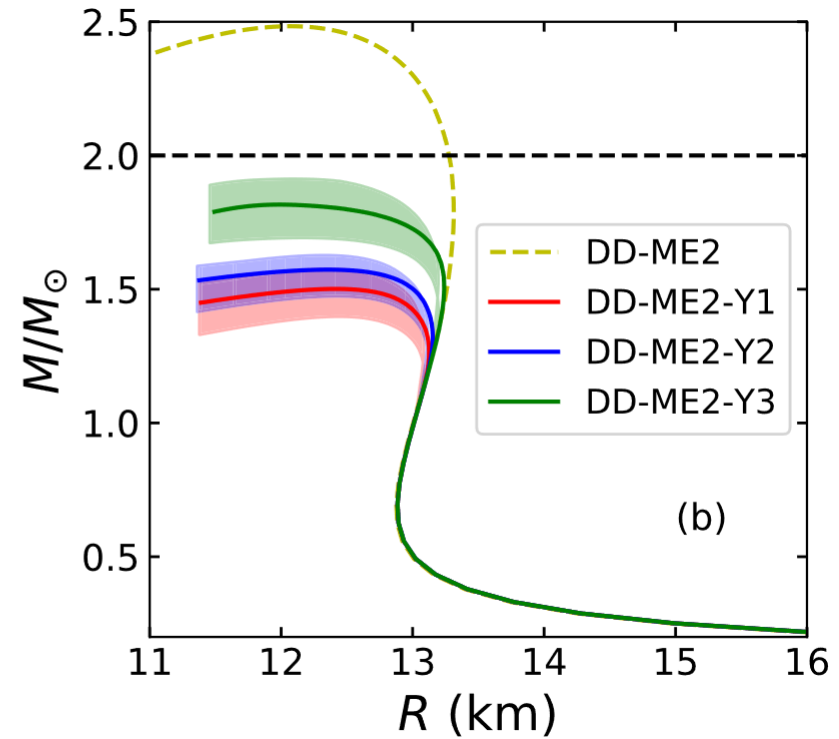
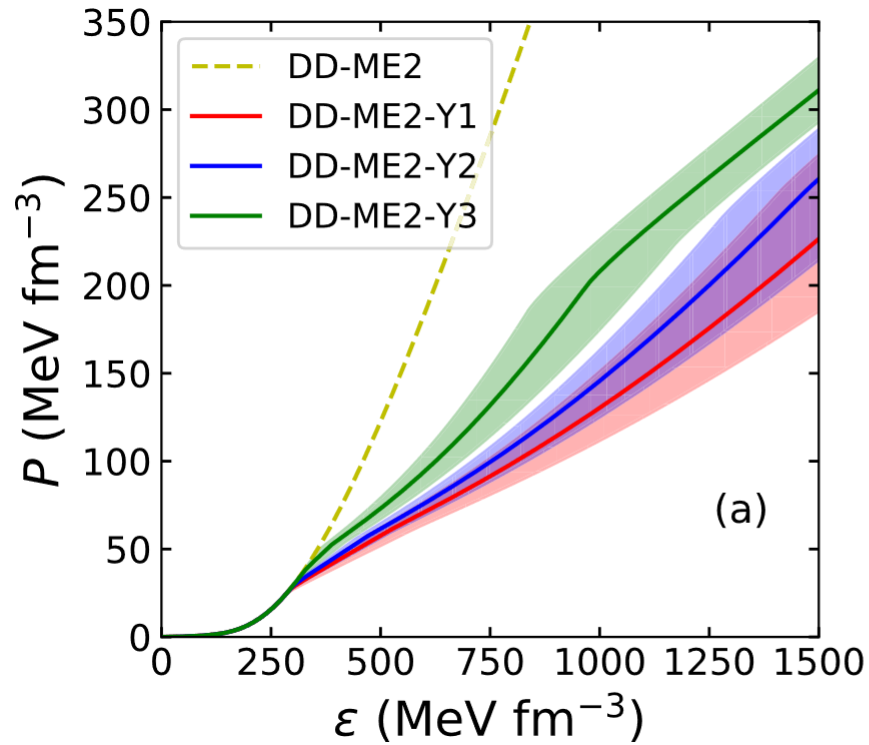
Linear relation between R_σ & R_ω



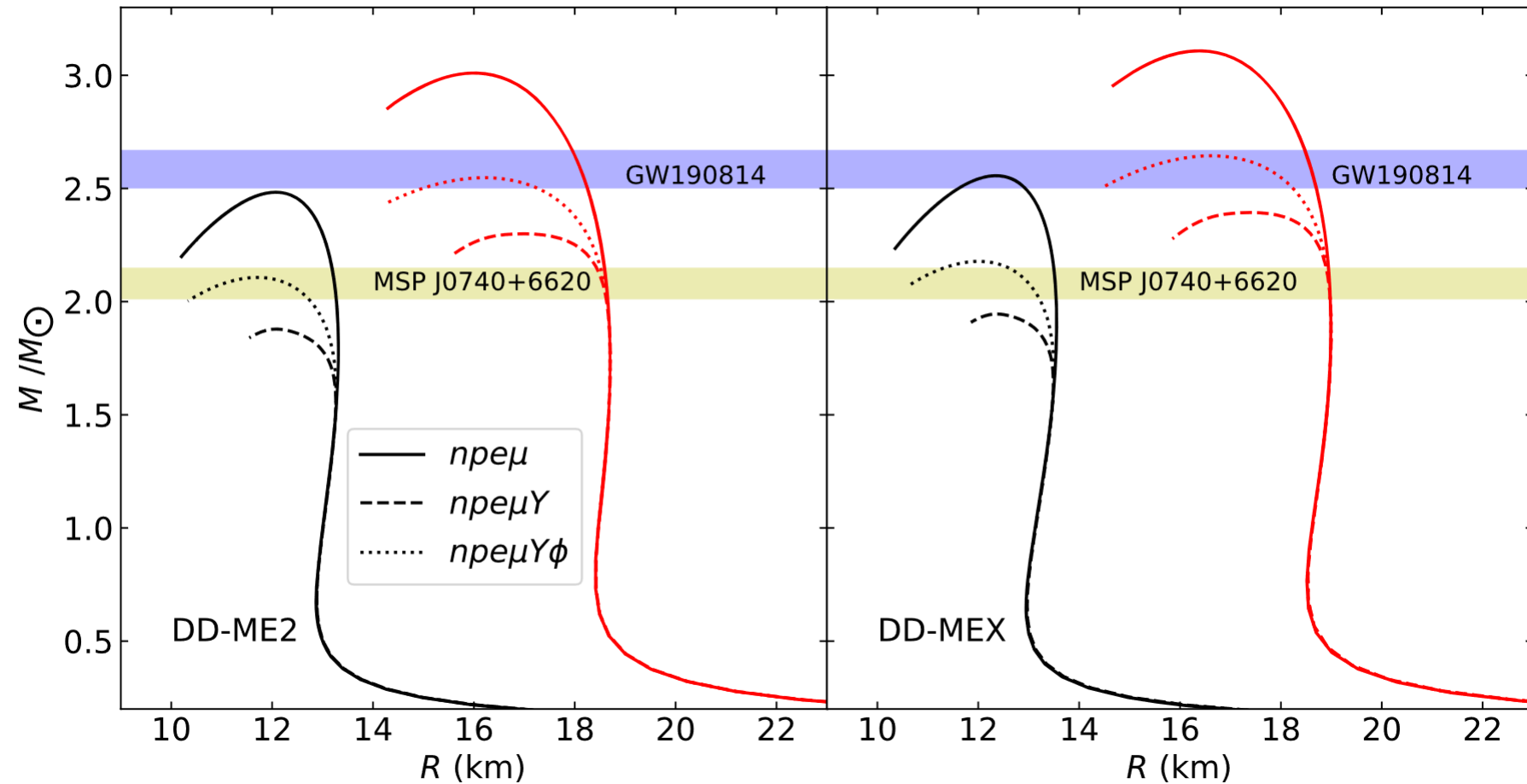
Single Λ states



Neutron (hyperon) stars: Hyperon puzzle



An attempt toward solving hyperon puzzle



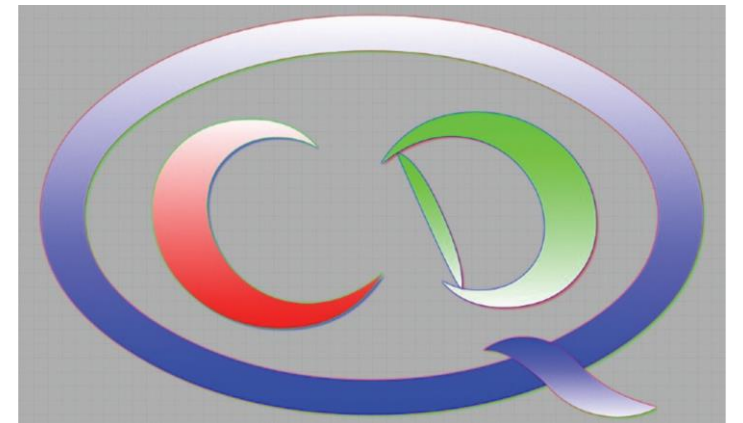
Summary & perspectives

□ Summary

- New effective interactions for hypernuclei in density-dependent relativistic mean field model
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□ Perspectives

- More on shape effects in hypernuclei
- Connection with no-core shell model calculations
- ...



Summary & perspectives

□ Summary

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□ Perspectives

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Thanks

谢谢

