

From Hadronic Interactions to the Relativistic Description of Nuclear Structure

Yilong Yang (cover Jie Meng)

Peking University

Email: yl_yang@pku.edu.cn

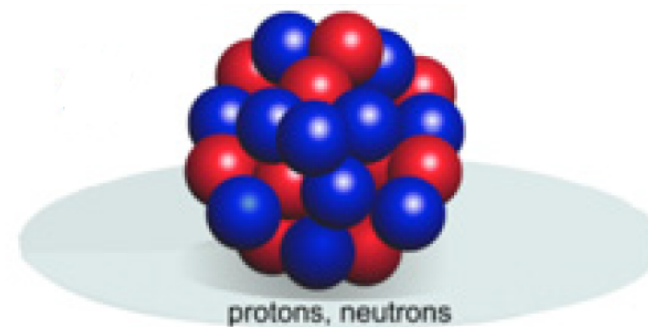
Challenge of nuclear structure theory

- Nuclear structure encompasses phenomena over a **wide range of energy scale**.
- The choice of degrees of freedom depends on the resolution of the theoretical microscope (the specific physics question).

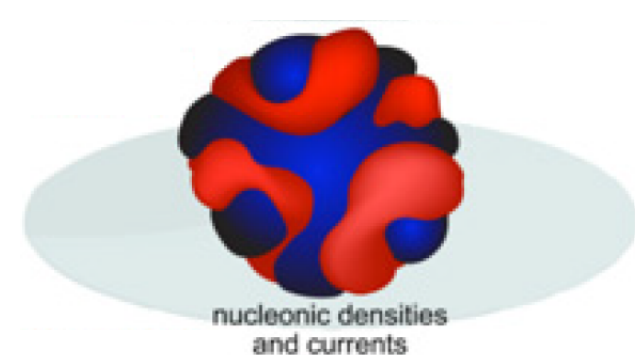
Lattice QCD



Ab initio



DFT

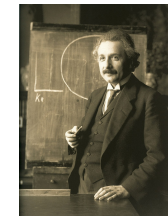


High resolution

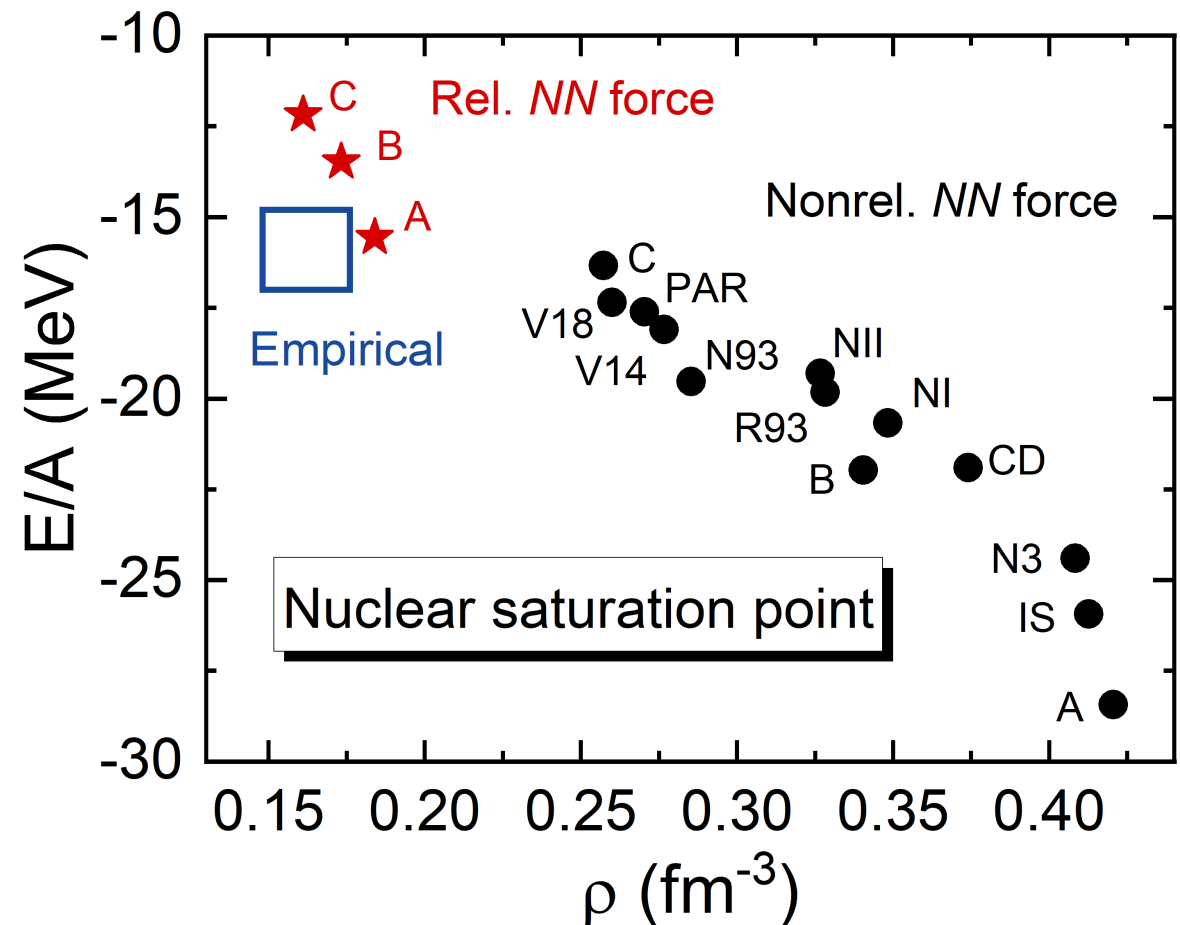
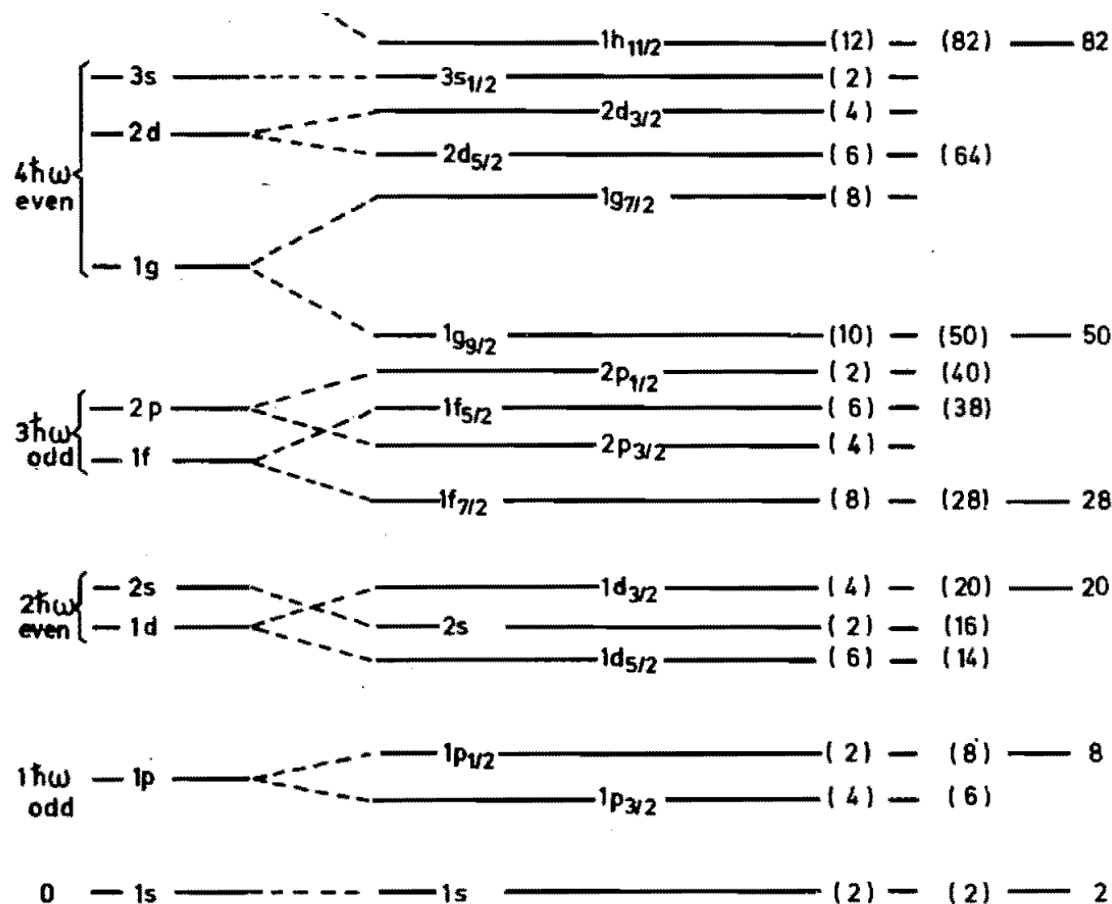
Low resolution

Why relativistic framework?

- ✓ Lorentz invariance is one of **the most fundamental symmetry in nature**
- ✓ Large spin-orbit splitting in nuclei
- ✓ Relativistic nuclear saturation
- ✓



Einstein Dirac Mayer Jensen

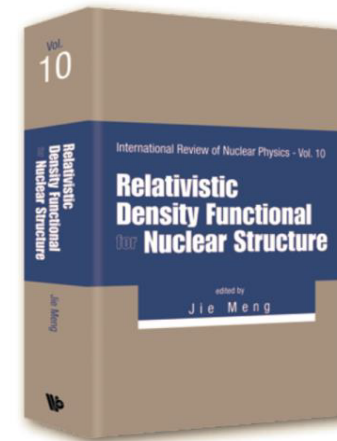
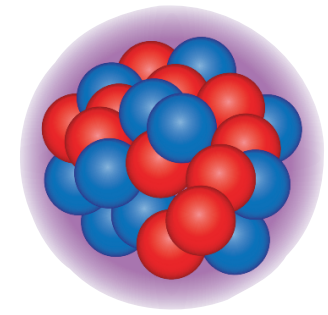


P. Ring and P. Schuck, *The Nuclear Many-Body Problem* (1980)

Data from Z. H. Li et. al., *PRC* 74, 047304 (2006)

Major research interests

- ✓ *Hadronic interactions from Lattice QCD*
- ✓ *Relativistic ab initio calculations of nuclei*
- ✓ Deep-learning Quantum Monte Carlo methods
- ✓ Nuclear relativistic density functional theory
- ✓ *DRHBc nuclear mass table*
- ✓ Exotic rotations and deformations of nuclei
- ✓ Nuclear fission and fusion dynamics
- ✓ Nucleosynthesis processes in astrophysics
- ✓ Test of fundamental symmetries in nuclear systems
- ✓



Editor: Jie Meng
Authors from China,
Croatia, France, Germany,
Italy, Japan, and USA.



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Review

Towards an *ab initio* covariant density functional theory for nuclear structure

Shihang Shen^{a,b,c}, Haozhao Liang^{d,e}, Wen Hui Long^{f,g}, Jie Meng^{a,h,i,*}, Peter Ring^{d,j}



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Review

Beyond-mean-field approaches for nuclear neutrinoless double beta decay in the standard mechanism

J.M. Yao^{a,b,*}, J. Meng^{c,d}, Y.F. Niu^e, P. Ring^f



Group members

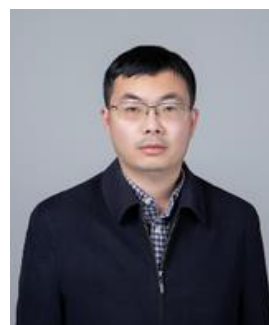
Professors:



Jie Meng



Shuangquan
Zhang



Pengwei Zhao



Peter Ring

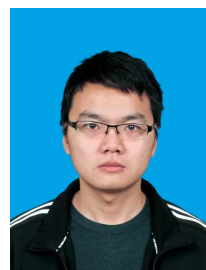
Overseas Distinguished
Professor



Dario Vretenar

High-end Foreign
Expert

Research Fellow:



Yakun Wang

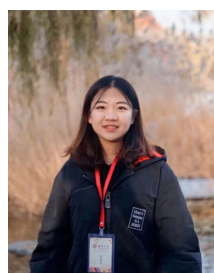
Students:



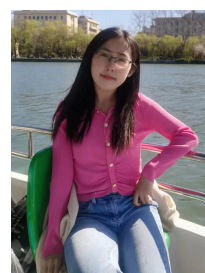
Yan Lyu



Cong Pan



Yanyu Chen



Yiping Wang



Dandan Zhang



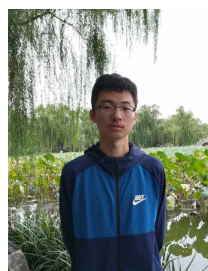
Xiaokai Du



Fangfang Xu



Weijiang Zou



Xiaofei Jiang



Bo Li



Yilong Yang



Lingyi Dai



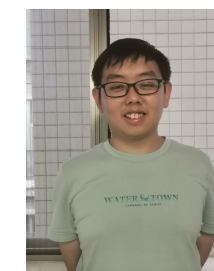
Teng Qu



Chang Zhou



Tianxing Huang



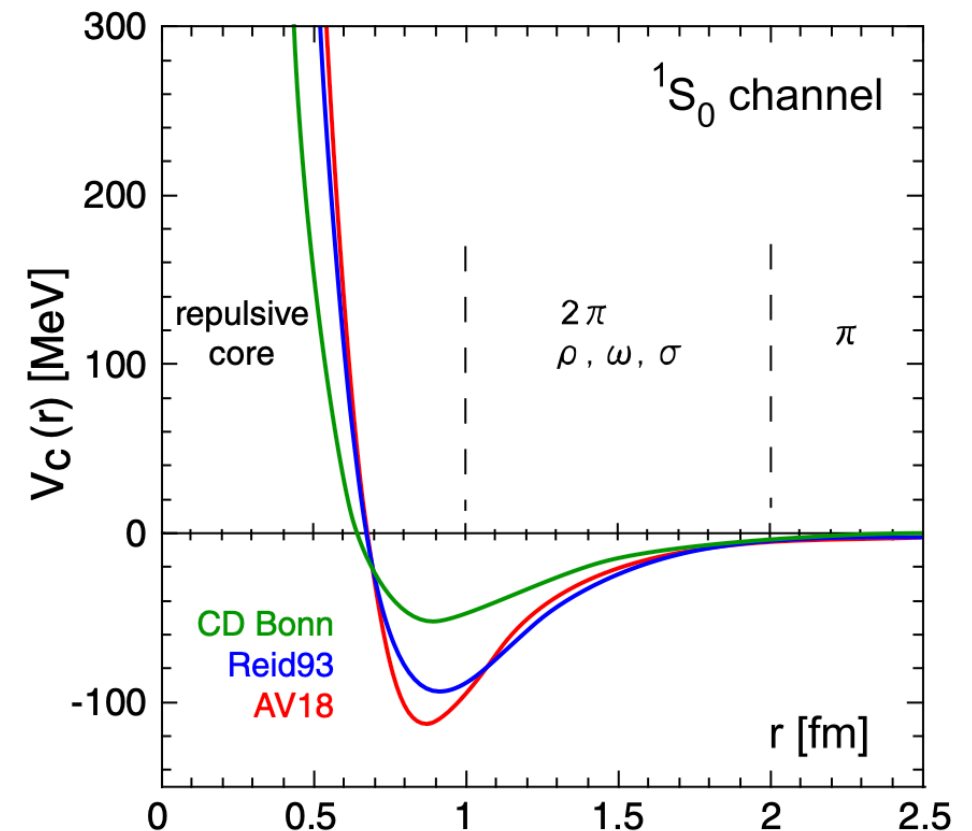
Peng Guo

Hadronic interactions from Lattice QCD



Nucleon-nucleon interactions

- The nucleon-nucleon (NN) interaction is one of **the most fundamental inputs** for the theoretical description of nuclear systems.
- Phenomenological NN interactions
 - AV18, Bonn, ...
- EFT-based NN interactions
 - Chiral EFT, Pionless EFT, ...
- Theoretical descriptions of nuclear systems suffer from uncertainties from various models of NN interactions.



N. Ishii, S. Aoki, and T. Hatsuda, PRL 99, 022001 (2007)

Goal: Deriving (relativistic) NN interactions from Lattice QCD simulations

Hadronic interactions from Lattice QCD

- A systematic study of hadron-hadron interactions by (2+1)-flavor lattice QCD with nearly physical light-quark masses

- ▶ Meson-meson: D^*-D

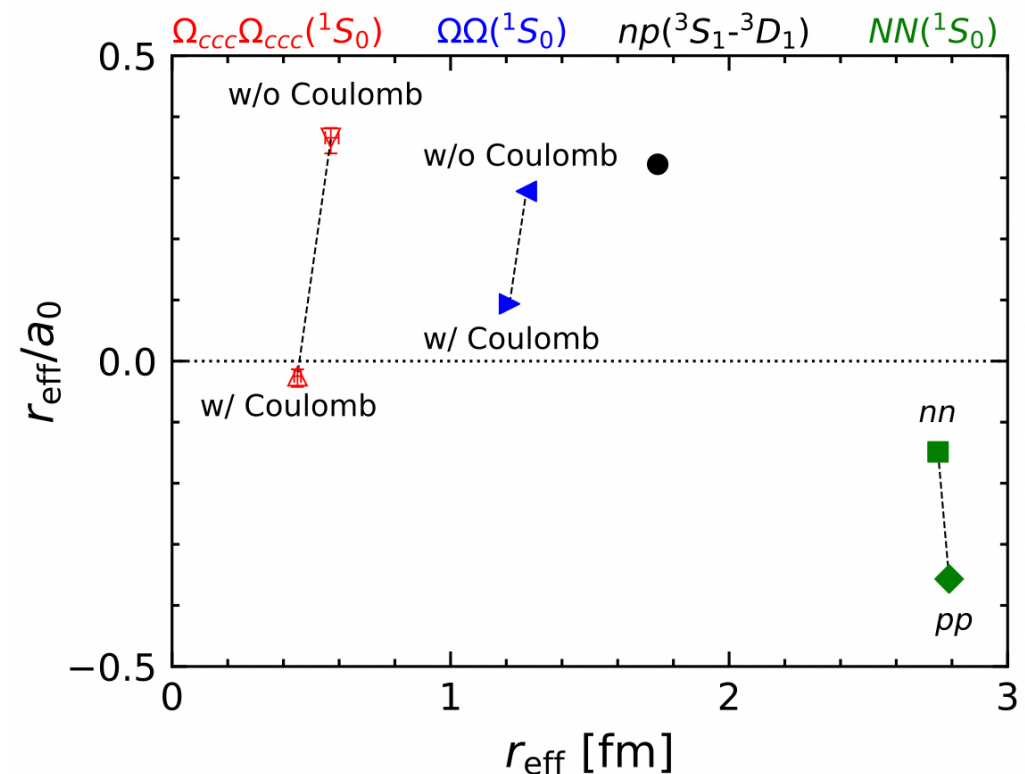
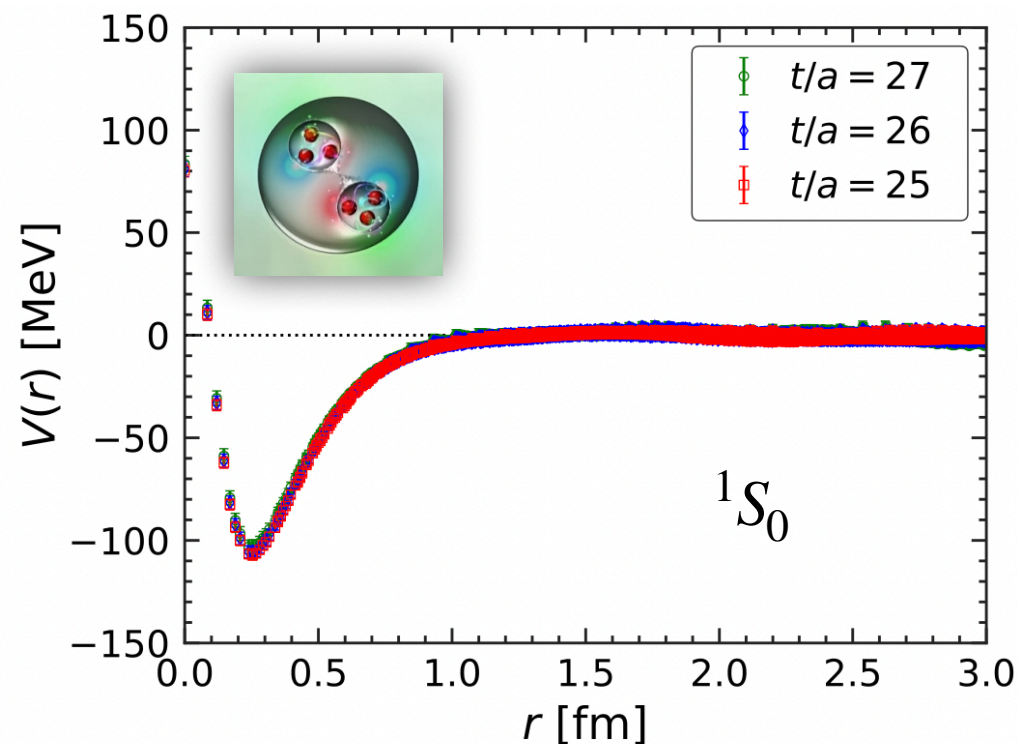
Y. Lyu, S. Aoki, T. Doi, T. Hatsuda, Y. Ikeda, and J. Meng, arXiv: 2302.04505 (2023)

- ▶ Baryon-meson: $N-\phi$

Y. Lyu, T. Doi, T. Hatsuda, Y. Ikeda, J. Meng, K. Sasaki, and T. Sugiura, PRD 106, 074507 (2022)

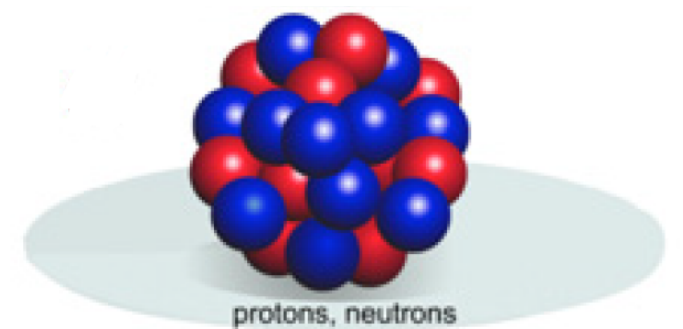
- ▶ Baryon-baryon: $\Omega_{ccc}-\Omega_{ccc}$, $\Omega_{sss}-\Omega_{sss}$

Y. Lyu, H. Tong, T. Sugiura, S. Aoki, T. Doi, T. Hatsuda, J. Meng, and T. Miyamoto, PRL 127, 072003 (2021); PRD 106, 074507 (2022)



Y. Lyu and H. Tong et. al., PRL 127, 072003 (2021)

Relativistic ab initio calculations of nuclei



Relativistic nucleon-nucleon interactions

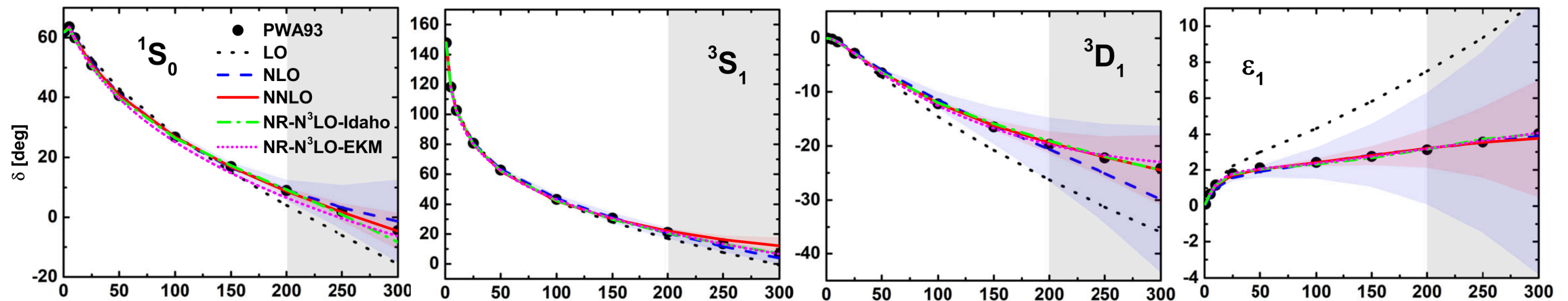
- Starting point: the relativistic NN interaction that reproduces NN scattering data
(Bonn, pionless EFT, chiral EFT, ...)

R. Machleidt, Adv. Nucl. Phys. 19, 189 (1989)

E. Epelbaum and J. Gegelia, PLB 716, 338 (2012)

J. X. Lu, C. X. Wang, Y. Xiao, L. S. Geng, J. Meng, and P. Ring, PRL 128, 142002 (2022)

.....



NN Scattering phase shift from relativistic chiral NN interactions

Taken from Lu2022PRL

Goal: providing accurate descriptions of light nuclei and nuclear matter

Relativistic Brueckner theory in full Dirac space

- The **first fully self-consistent** relativistic Brueckner Hartree-Fock calculations in the **full Dirac space**.

- ▶ Nuclear equation of state and symmetry energy

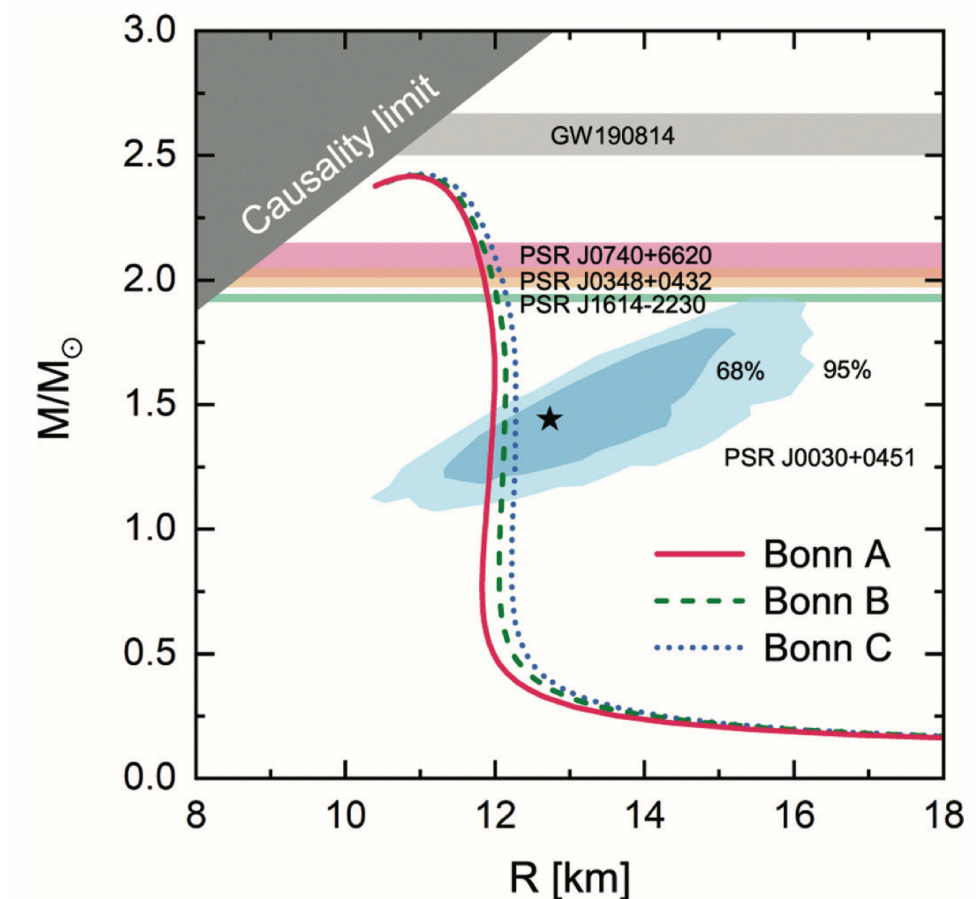
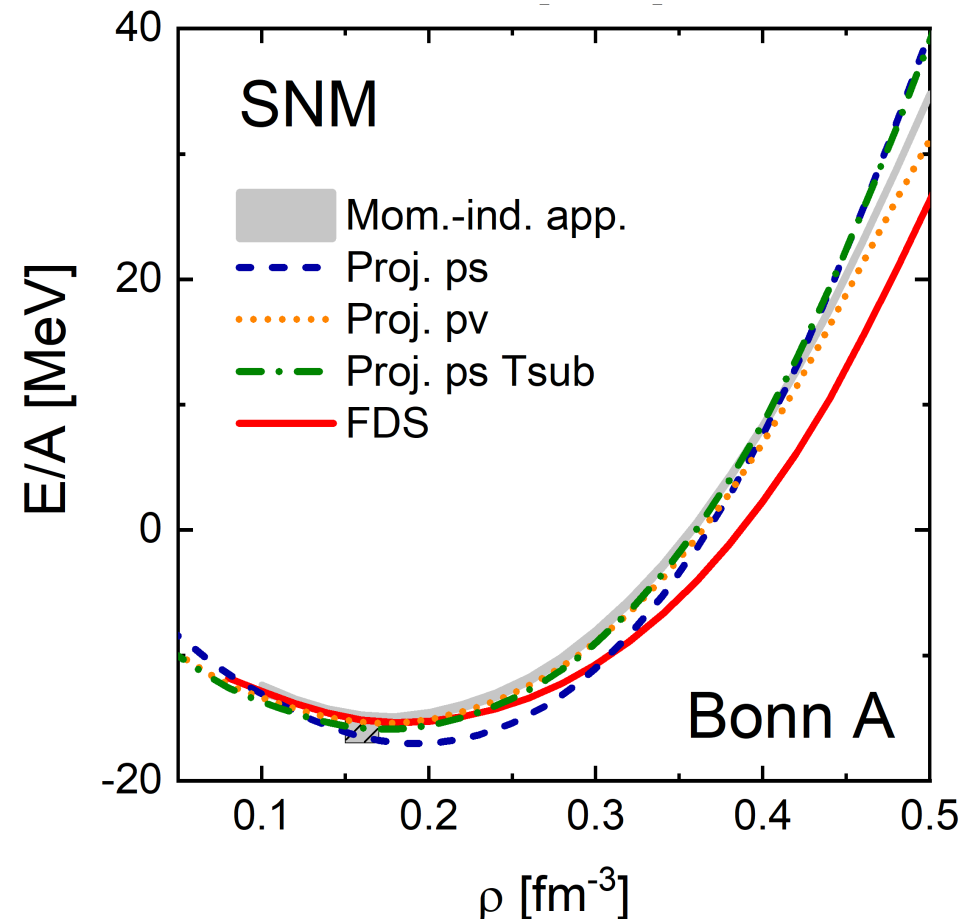
- ▶ Neutron star physics

- ▶

S. B. Wang, Q. Zhao, P. Ring, and J. Meng, PRC 103, 054319 (2021)

S. B. Wang, H. Tong, Q. Zhao, C. C. Wang, P. Ring, and J. Meng, PRC 106, L021305 (2022)

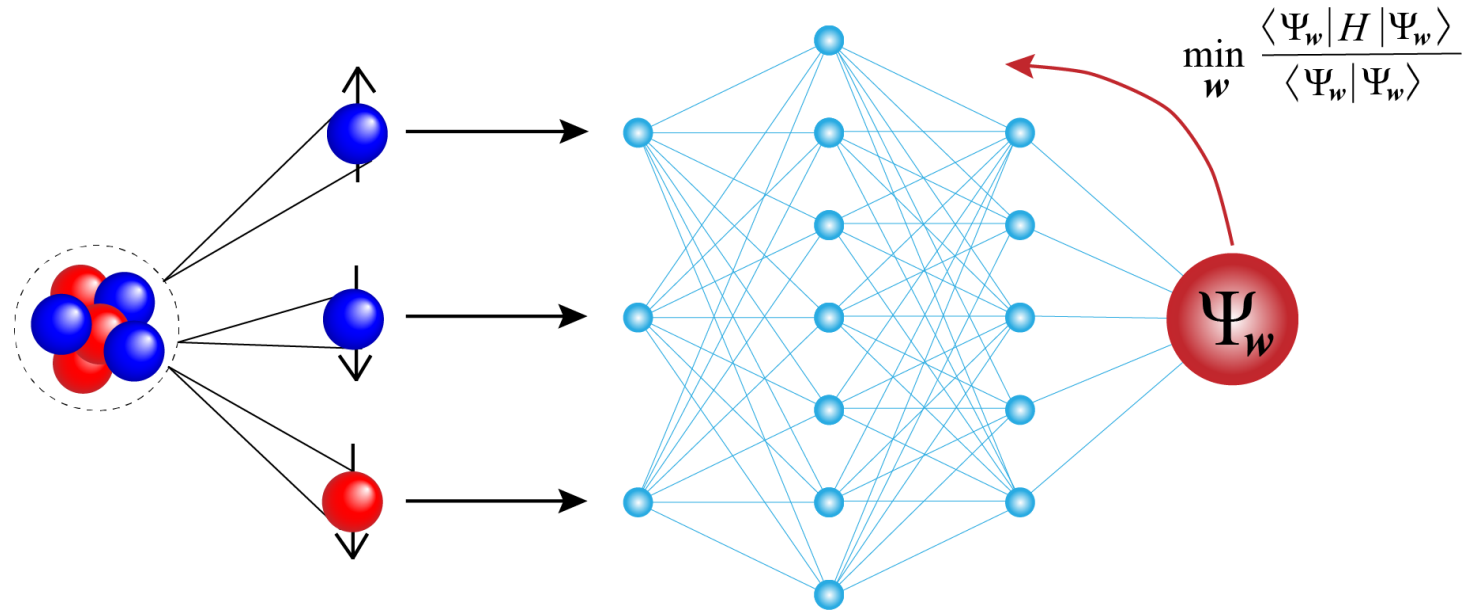
S. B. Wang, H. Tong, Q. Zhao, C. C. Wang, P. Ring, and J. Meng, arXiv:2304.13333 (2023)



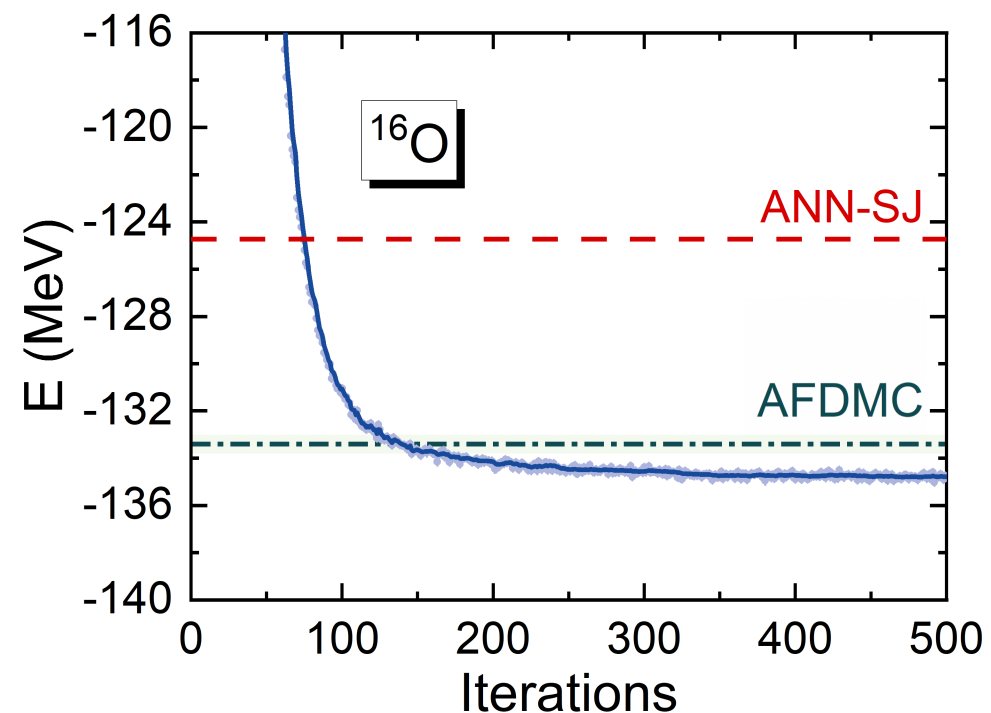
Relativistic Quantum Monte Carlo

- A new relativistic ab initio many-body method is developed by combining Quantum Monte Carlo and artificial neural-networks.

- Neural-network wave function



- Benchmark in light nuclei

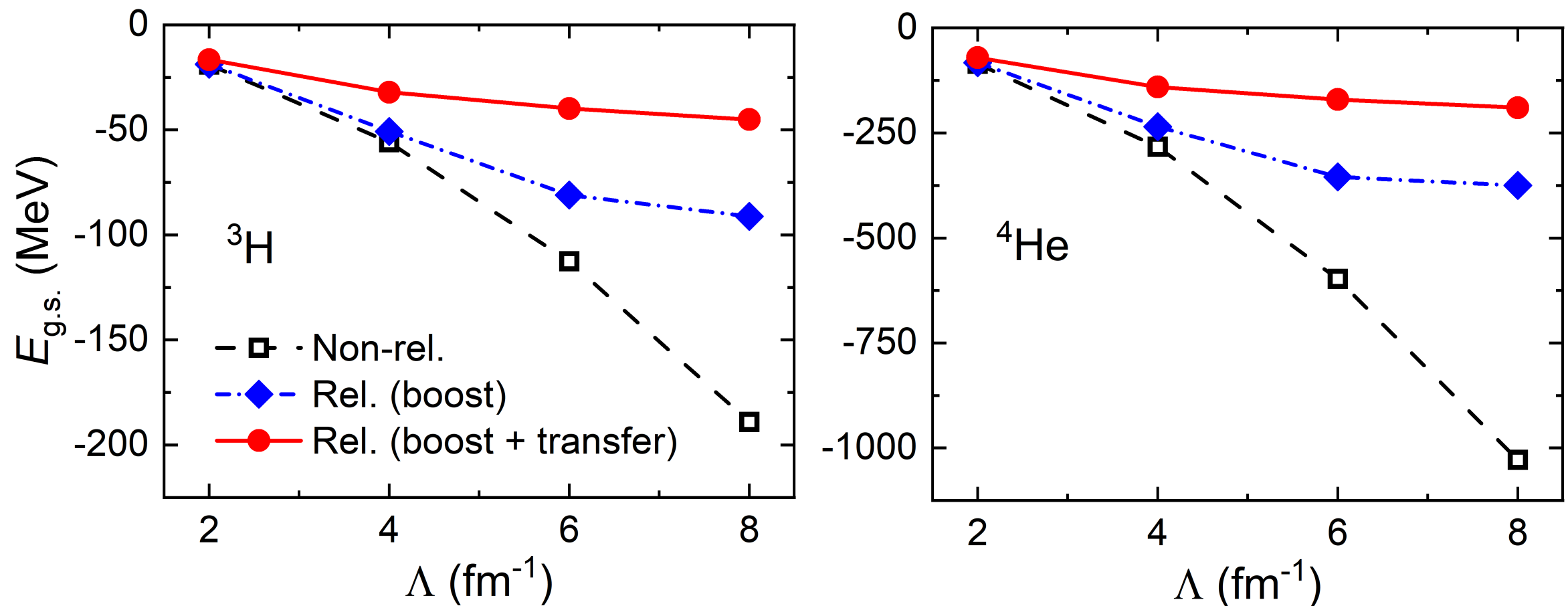


LO χ EFT Hamiltonian: Schiavilla et. al., PRC 103, 054003 (2021)

YLY and P. W. Zhao, Phys. Rev. C 107, 034320 (2023)

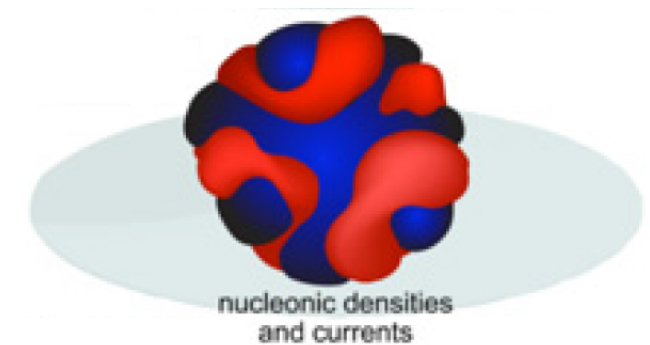
Relativistic effects in light nuclei

- As a first step, the light nuclei are studied starting from nuclear interactions derived from pionless EFT.
- Relativistic effects have a crucial impact on the **renormalizability** of few-nucleon systems in pionless EFT.



YLY and P. W. Zhao, Phys. Lett. B 835, 137587 (2022)

DRHBc nuclear mass table



Nuclear density functional theory

- The many-body problem is mapped onto a one-body problem.

Hohenberg-Kohn Theorem

The **exact ground-state energy** of a quantum many-body system is a **universal functional of the density**.

$$E[\rho] = E_{\text{kin}}[\rho] + E_{\text{int}}[\rho]$$

Kohn-Sham DFT

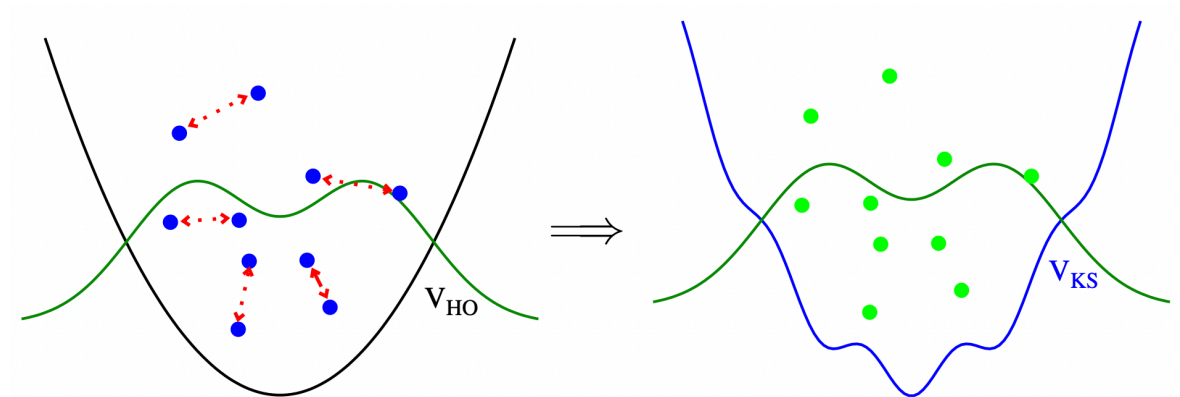


Fig from Drut2010PPNP

$$E[\rho] \Rightarrow \hat{h} = \frac{\delta E}{\delta \rho} \Rightarrow \hat{h}\varphi_i = \varepsilon_i\varphi_i \Rightarrow \rho = \sum_{i=1}^A |\varphi_i|^2$$

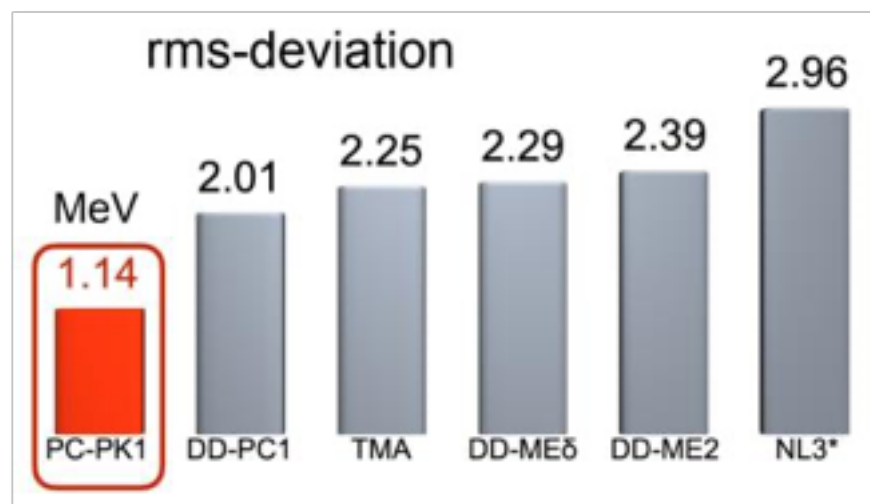
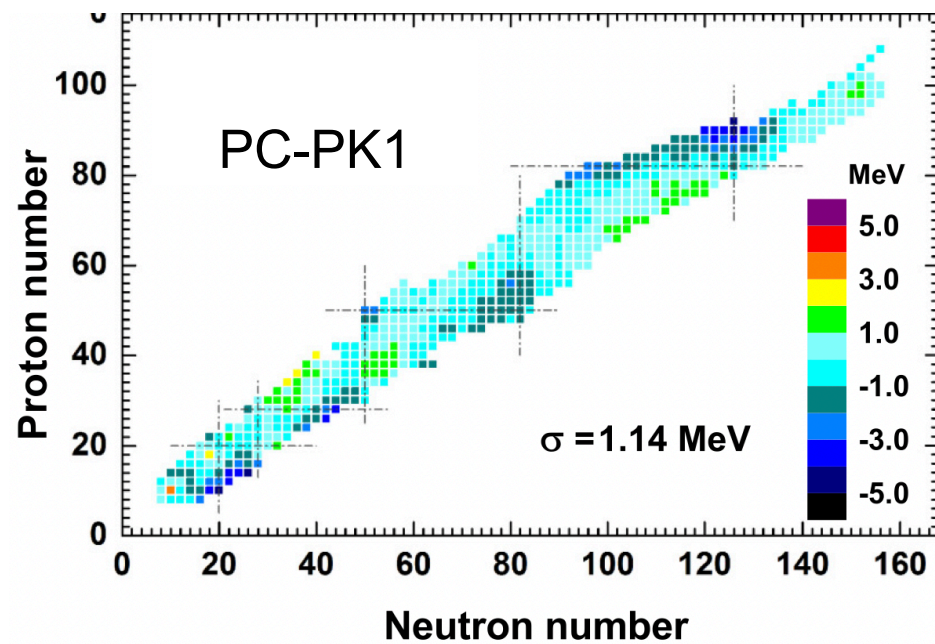
Goal: Predicting nuclear properties on the nuclear landscape based on an accurate and unified energy density functional

Relativistic density functional: PC-PK1

- One of **the most accurate** relativistic density functional PC-PK1

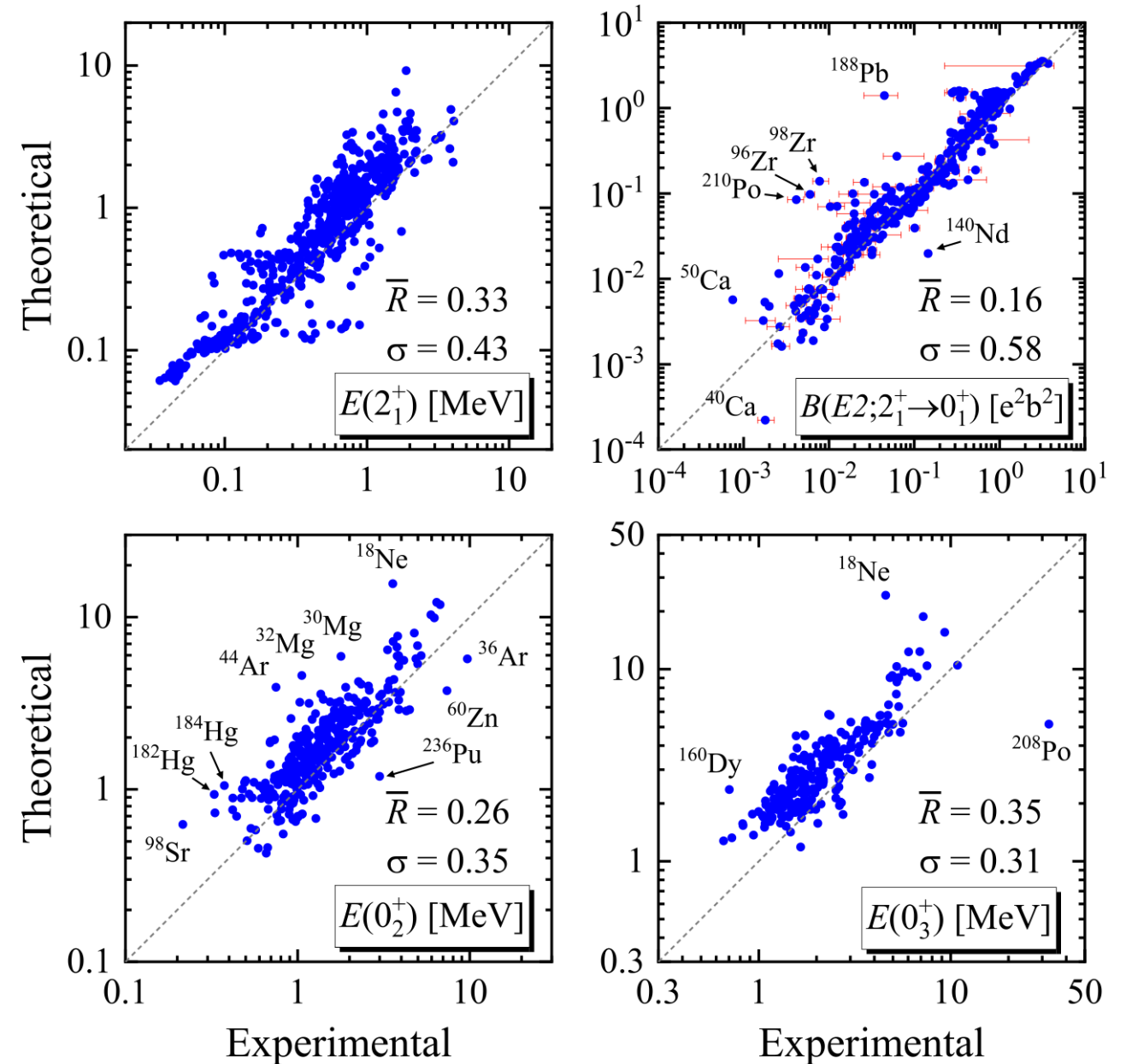
P. W. Zhao, Z. P. Li, J. M. Yao, and J. Meng, PRC 82, 054319 (2010)

✓ Nuclear mass



K. Q. Lu, Z. X. Li, Z. P. Li, J. M. Yao, J. Meng, PRC 91, 027304 (2015)

✓ Low-lying excited states



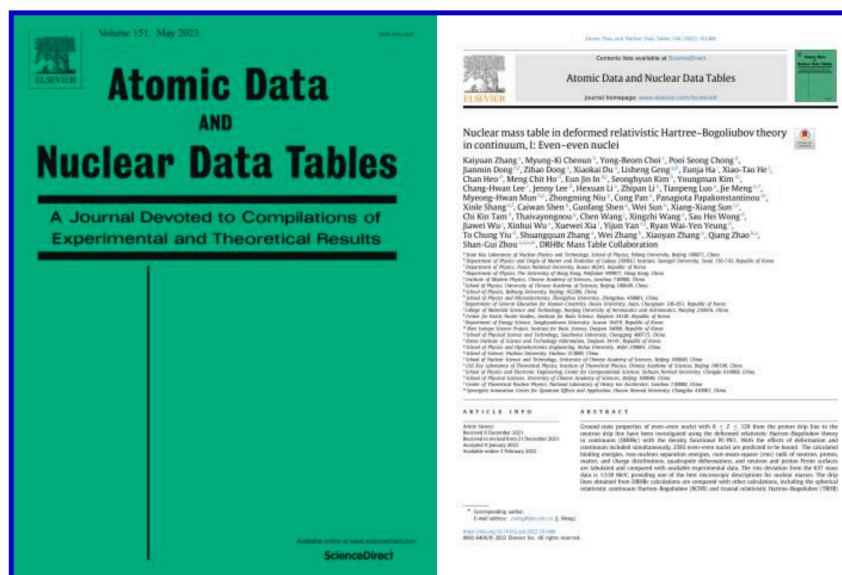
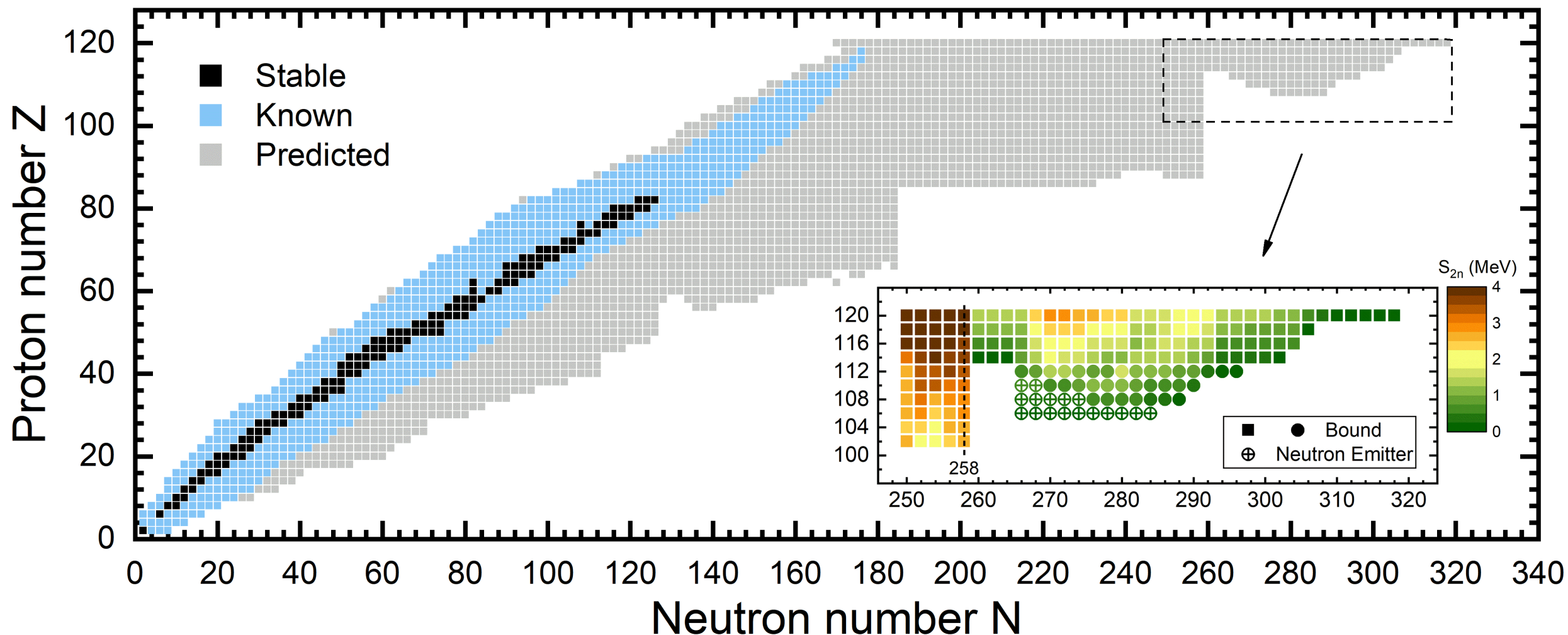
YLY, P. W. Zhao, and Z. P. Li, PRC 107, 024308 (2023)

DRHBc collaboration

- The **deformed relativistic Hartree-Bogoliubov theory in continuum (DRHBc)** was developed to simultaneously include deformation, pairing correlations, and continuum effects, providing a **proper description for exotic nuclei**.
- The DRHBc Mass Table Collaboration:



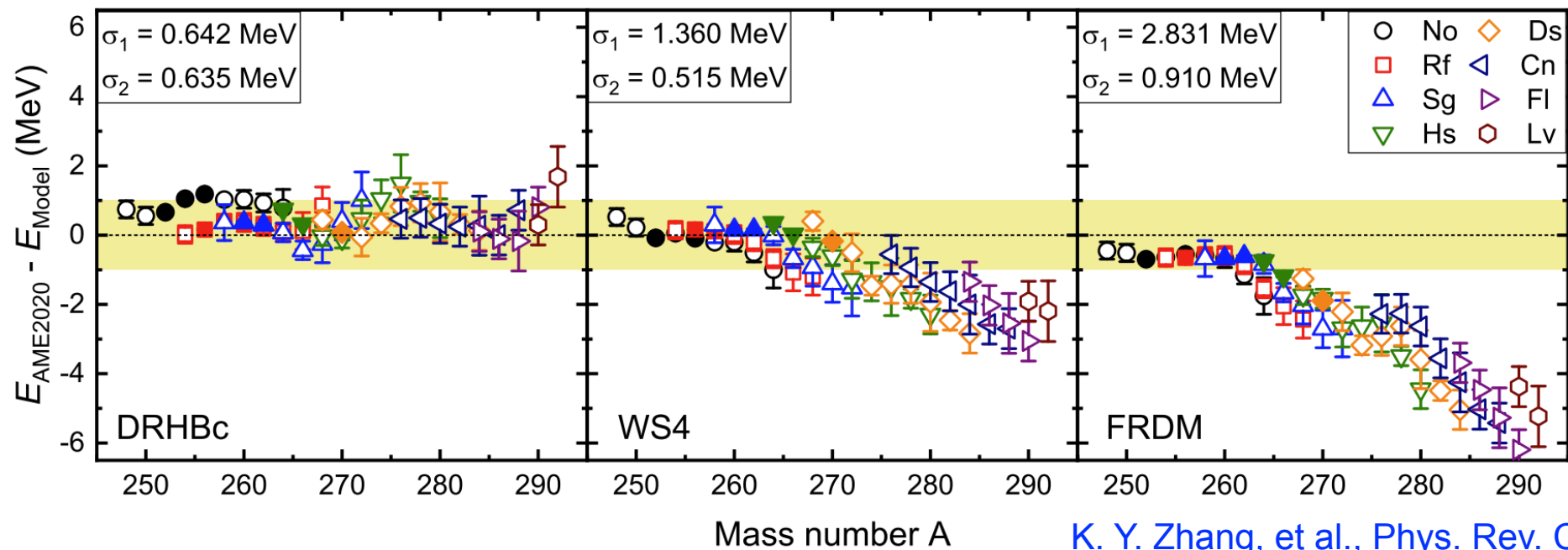
DRHBc mass table for even-even nuclei



- ✓ Including **deformation, pairing, and continuum effects** simultaneously
 - ✓ Among the **most accurate** mass table
- K. Y. Zhang et. al., (DRHBc Mass Table Collaboration), ADNDT 144, 101488 (2022)

Further applications

- Accurate predictions for superheavy nuclei ($Z \geq 102$).



K. Y. Zhang, et al., Phys. Rev. C 104, L021301 (2021)

- DRHBc theory for odd nuclei.
The DRHBc mass table for odd nuclei is under construction.

PHYSICAL REVIEW C 106, 014316 (2022)

Deformed relativistic Hartree-Bogoliubov theory in continuum with a point-coupling functional. II. Examples of odd Nd isotopes

Cong Pan (潘琮),¹ Myung-Ki Cheoun,² Yong-Beom Choi,³ Jianmin Dong (董建敏),^{4,5} Xiaokai Du (杜晓凯),¹ Xiao-Hua Fan (范小华),⁶ Wei Gao (高威),⁷ Lisheng Geng (耿立升),^{8,7} Eunja Ha,⁹ Xiao-Tao He (贺晓涛),¹⁰ Jinke Huang (黄靳苛),⁷ Kun Huang (黄坤),¹⁰ Seonghyun Kim,² Youngman Kim,¹¹ Chang-Hwan Lee,³ Jenny Lee,¹² Zhipan Li (李志攀),⁶ Zhi-Rui Liu (刘治瑞),¹⁰ Yiming Ma (马艺铭),¹³ Jie Meng (孟杰),^{1,*} Myeong-Hwan Mun,^{2,14} Zhongming Niu (牛中明),¹⁵ Panagiota Papakonstantinou,¹¹ Xinle Shang (尚新乐),^{4,5} Caiwan Shen (沈彩万),¹⁶ Guofang Shen (申国防),⁸ Wei Sun (孙玮),⁶ Xiang-Xiang Sun (孙向向),^{17,18} Jiawei Wu (吴佳威),¹⁰ Xinhui Wu (吴鑫辉),¹ Xuewei Xia (夏学伟),¹⁹ Yijun Yan (晏一珺),^{4,5} To Chung Yiu,¹² Kaiyuan Zhang (张开元),^{1,20} Shuangquan Zhang (张双全),¹ Wei Zhang (张炜),⁷ Xiaoyan Zhang (张晓燕),¹⁵ Qiang Zhao (赵强),^{21,1} Ruyou Zheng (郑茹尤),⁸ and Shan-Gui Zhou (周善贵)^{18,22,23,24}
(DRHBc Mass Table Collaboration)

- Providing accurate nuclear mass inputs for nuclear physics and astrophysics applications.

Summary

- **The goal is to describe nuclear structure in the relativistic framework starting from different degrees of freedom.**
 - Deriving (relativistic) NN interactions from Lattice QCD simulations
 - Providing accurate ab initio descriptions of light nuclei and nuclear matter
 - Predicting nuclear properties on the nuclear landscape based on an accurate and unified energy density functional
- **Some representative progress:**
 - ✓ Deriving D^*-D , $N-\phi$, $\Omega_{ccc}-\Omega_{ccc}$, and $\Omega_{sss}-\Omega_{sss}$ interactions from lattice QCD
 - ✓ Developing the relativistic Brueckner Hartree-Fock method in full Dirac space and the relativistic Quantum Monte Carlo method
 - ✓ Constructing the DRHBc mass table for even-even nuclei

Acknowledgments

Professors: Jie Meng, Shuangquan Zhang, and Pengwei Zhao

Group members: Yakun Wang, Yiping Wang , Dandan Zhang, Yanyu Chen, Xiaokai Du, Fangfang Xu, Weijiang Zou, Xiaofei Jiang, Bo Li, Lingyi Dai, Teng Qu, Chang Zhou, Tianxing Huang, Peng Guo

Thank you!

Appendix
