

# **Charmed baryon spectrum and their decay patterns**

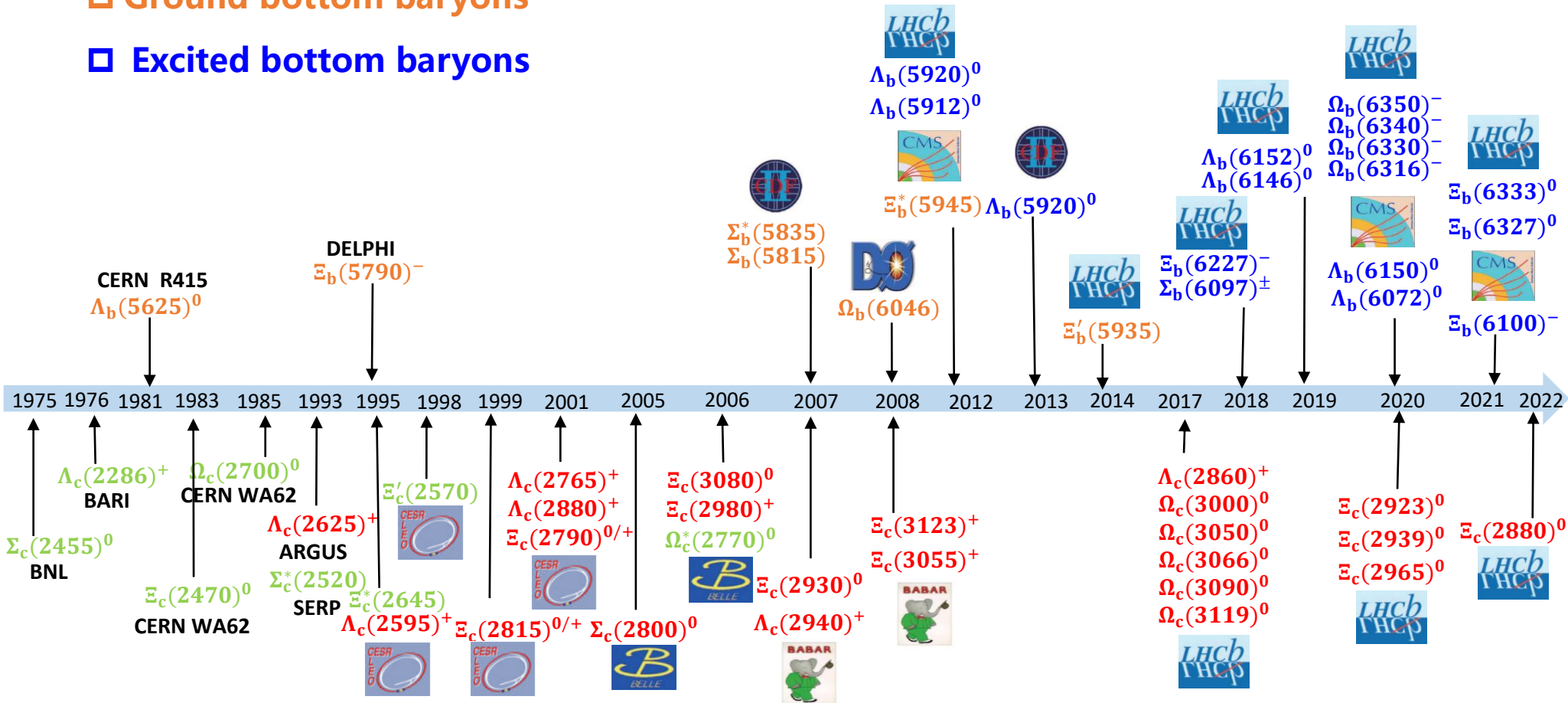
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**Southeast University**

**Collaborators: Er-Liang Cui, Hui-Min Yang, Wei Chen, Atsushi Hosaka, Xiang Liu, Shi-Lin Zhu.**

Ground bottom baryons

Excited bottom baryons



Ground charmed baryons

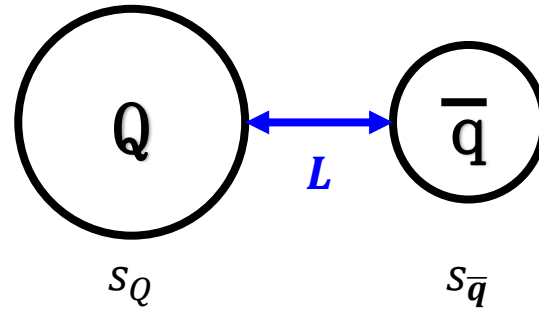
Excited charmed baryons

# Contents

- **Internal structure of heavy mesons**
- Internal structure of heavy baryons
- QCD sum rule analyses

# Internal structure of heavy mesons

heavy meson ( $Q - \bar{q}$ )



$$J = s_Q + s_{\bar{q}} + L$$

# Internal structure of heavy mesons

Based on the **heavy quark effective theory**, the leading order Lagrangian does not depend on  $m_Q$ . Hence, the two heavy hadrons with the same light degree of freedom form a degenerate doublet:

$$\text{heavy meson } (Q - \bar{q}) : \quad J = s_Q + (L + s_{\bar{q}})_{j_l}$$

spin of the light degree of freedom

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$$L = 1 : \begin{cases} j_l = 1/2, J^P = (0^+, 1^+) \\ j_l = 3/2, J^P = (1^+, 2^+) \end{cases}$$



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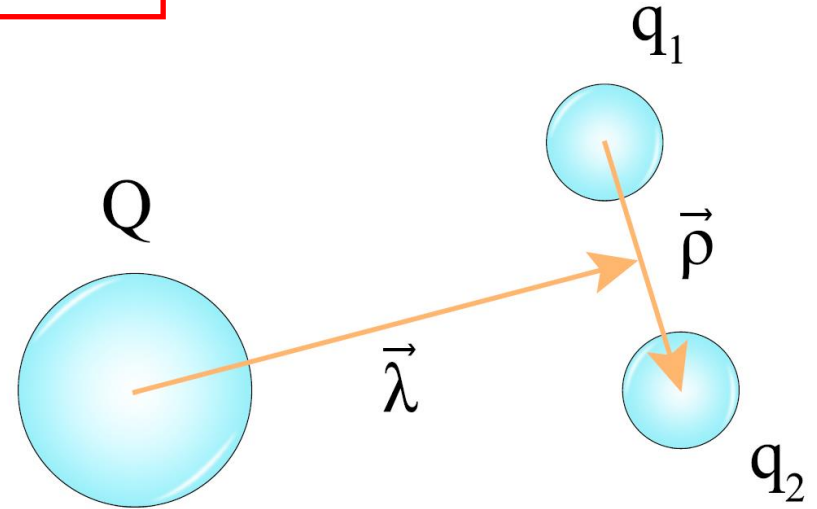
$$L = 2 : \begin{cases} j_l = 3/2, J^P = (1^-, 2^-) \\ j_l = 5/2, J^P = (2^-, 3^-) \end{cases}$$

# Contents

- Internal structure of heavy mesons
- **Internal structure of heavy baryons**
- QCD sum rule analyses

# Internal structure of heavy baryons

heavy baryon ( $Q - q_1 - q_2$ ):



**$\lambda$ -excitation and  $\rho$ -excitation**

$$J = s_Q + s_{q_1} + s_{q_2} + l_\rho + l_\lambda$$

$$= s_Q + (s_{q_1} + s_{q_2} + l_\rho + l_\lambda) \mathbf{j}_l$$

spin of the light degree of freedom

# Internal structure of heavy baryons

**The Pauli principle** can be directly applied to **the two light quarks**:

➤ color  $\longrightarrow \bar{\mathbf{3}}_C$  antisymmetric

➤ orbital  $\longrightarrow l_\rho \begin{cases} \text{symmetric} \\ \text{antisymmetric} \end{cases}$

➤ spin  $\longrightarrow s_{qq} = \begin{cases} \mathbf{1} \text{ symmetric} \\ \mathbf{0} \text{ antisymmetric} \end{cases}$

➤ SU(3) flavor  $\longrightarrow \begin{cases} \mathbf{6}_F \text{ symmetric} \\ \bar{\mathbf{3}}_F \text{ antisymmetric} \end{cases}$

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**Totally Antisymmetric**

# Internal structure of heavy baryons

## S-wave heavy baryons:

- color  $\longrightarrow \bar{\mathbf{3}}_C$  antisymmetric
- orbital  $\longrightarrow l_\rho = 0$  symmetric
- spin  $\longrightarrow s_{qq} = \begin{cases} \mathbf{1} & \text{symmetric} \\ \mathbf{0} & \text{antisymmetric} \end{cases}$
- SU(3) flavor  $\longrightarrow \begin{cases} \mathbf{6}_F & \text{symmetric} \\ \bar{\mathbf{3}}_F & \text{antisymmetric} \end{cases}$

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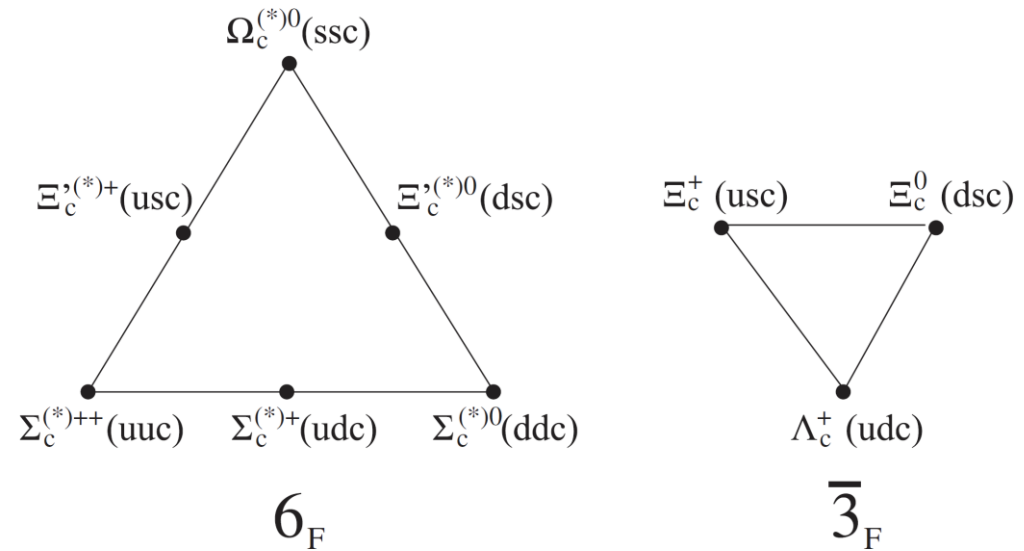
$$L = 0 \begin{cases} \mathbf{j}_l = \mathbf{s}_{qq} = \mathbf{0}, J^P = 1/2^+ & \longleftrightarrow \bar{\mathbf{3}}_F \\ \mathbf{j}_l = \mathbf{s}_{qq} = \mathbf{1}, J^P = (1/2^+, 3/2^+) & \longleftrightarrow \mathbf{6}_F \end{cases}$$



# Internal structure of heavy baryons

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- color  $\rightarrow \bar{\mathbf{3}}_C$  antisymmetric
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# Internal structure of heavy baryons

## S-wave charmed baryons

$$L = 0 \begin{cases} \mathbf{j}_l = \mathbf{0}, J^P = 1/2^+ \\ \mathbf{j}_l = \mathbf{1}, J^P = (1/2^+, 3/2^+) \end{cases} \quad \begin{array}{l} \bar{3}_F: \Lambda_c, \Xi_c \\ 6_F: (\Sigma_c, \Sigma_c^*), (\Xi_c', \Xi_c^*), (\Omega_c, \Omega_c^*) \\ \quad \quad \quad \uparrow \quad \uparrow \\ \quad \quad \quad 1/2^+ \quad 3/2^+ \end{array}$$

## S-wave bottom baryons

$$L = 0 \begin{cases} \mathbf{j}_l = \mathbf{0}, J^P = 1/2^+ \\ \mathbf{j}_l = \mathbf{1}, J^P = (1/2^+, 3/2^+) \end{cases} \quad \begin{array}{l} \bar{3}_F: \Lambda_b, \Xi_b \\ 6_F: (\Sigma_b, \Sigma_b^*), (\Xi_b', \Xi_b^*), (\Omega_b, \Omega_b^*) \\ \quad \quad \quad \uparrow \quad \uparrow \\ \quad \quad \quad 1/2^+ \quad 3/2^+ \end{array}$$

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$\bar{3}_F: \Lambda_c, \Xi_c$

$6_F: (\Sigma_c, \Sigma_c^*), (\Xi'_c, \Xi_c^*), (\Omega_c, \Omega_c^*)$

$\uparrow \quad \uparrow$

$1/2^+ \quad 3/2^+$

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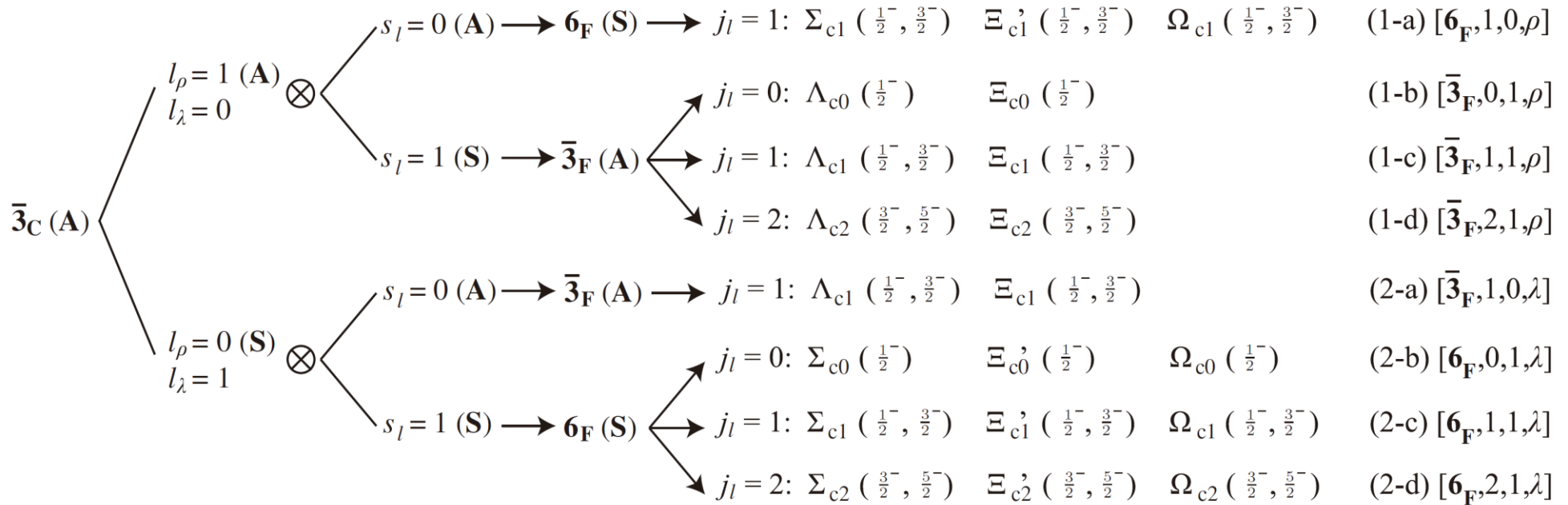
$\uparrow \quad \uparrow \quad \uparrow$

$1/2^+ \quad 3/2^+ \quad \boxed{\text{missing}}$

# Internal structure of heavy baryons

**P-wave charmed baryons**

8 multiplets, 35 baryons, e.g., 7  $\Omega_c$  baryons



**$\lambda$ -excitation and  $\rho$ -excitation ( $l_\rho + l_\lambda = 1$ )**

# Currents for P-wave charmed baryons of the flavor $6_F$

$$[6_F, 1, 0, \rho] \left\{ \begin{array}{l} J_{1/2, -, 6_F, 1, 0, \rho} = i\epsilon_{abc} ([D_t^\mu q^{aT}] C \gamma_5 q^b - q^{aT} C \gamma_5 [D_t^\mu q^b]) \gamma_t^\mu \gamma_5 h_v^c, \\ J_{3/2, -, 6_F, 1, 0, \rho}^\alpha = i\epsilon_{abc} ([D_t^\mu q^{aT}] C \gamma_5 q^b - q^{aT} C \gamma_5 [D_t^\mu q^b]) \left( g_t^{\alpha\mu} - \frac{1}{3} \gamma_t^\alpha \gamma_t^\mu \right) h_v^c, \end{array} \right.$$

$$[6_F, 0, 1, \lambda] \quad J_{1/2, -, 6_F, 0, 1, \lambda} = i\epsilon_{abc} ([D_t^\mu q^{aT}] C \gamma_t^\mu q^b + q^{aT} C \gamma_t^\mu [D_t^\mu q^b]) h_v^c.$$

$$[6_F, 1, 1, \lambda] \left\{ \begin{array}{l} J_{1/2, -, 6_F, 1, 1, \lambda} = i\epsilon_{abc} ([D_t^\mu q^{aT}] C \gamma_t^\nu q^b + q^{aT} C \gamma_t^\nu [D_t^\mu q^b]) \sigma_t^{\mu\nu} h_v^c, \\ J_{3/2, -, 6_F, 1, 1, \lambda}^\alpha = i\epsilon_{abc} ([D_t^\mu q^{aT}] C \gamma_t^\nu q^b + q^{aT} C \gamma_t^\nu [D_t^\mu q^b]) \left( g_t^{\alpha\mu} \gamma_t^\nu \gamma_5 - g_t^{\alpha\nu} \gamma_t^\mu \gamma_5 - \frac{1}{3} \gamma_t^\alpha \gamma_t^\mu \gamma_t^\nu \gamma_5 + \frac{1}{3} \gamma_t^\alpha \gamma_t^\nu \gamma_t^\mu \gamma_5 \right) h_v^c. \end{array} \right.$$

$$[6_F, 2, 1, \lambda] \left\{ \begin{array}{l} J_{3/2, -, 6_F, 2, 1, \lambda}^\alpha = i\epsilon_{abc} ([D_t^\mu q^{aT}] C \gamma_t^\nu q^b + q^{aT} C \gamma_t^\nu [D_t^\mu q^b]) \times \left( g_t^{\alpha\mu} \gamma_t^\nu \gamma_5 + g_t^{\alpha\nu} \gamma_t^\mu \gamma_5 - \frac{2}{3} g_t^{\mu\nu} \gamma_t^\alpha \gamma_5 \right) h_v^c, \\ J_{5/2, -, 6_F, 2, 1, \lambda}^{\alpha_1 \alpha_2} = i\epsilon_{abc} \left( [D_t^{\alpha_1} q^{aT}] C \gamma_t^{\alpha_2} q^b + q^{aT} C \gamma_t^{\alpha_2} [D_t^{\alpha_1} q^b] + [D_t^{\alpha_2} q^{aT}] C \gamma_t^{\alpha_1} q^b + q^{aT} C \gamma_t^{\alpha_1} [D_t^{\alpha_2} q^b] \right. \\ \left. - \frac{2}{3} g_t^{\alpha_1 \alpha_2} g_t^{\mu\nu} \times ([D_t^\mu q^{aT}] C \gamma_t^\nu q^b + q^{aT} C \gamma_t^\nu [D_t^\mu q^b]) \right) h_v^c. \end{array} \right.$$

# General discussions on hadronic currents

- Hadronic currents well describe **the internal color, flavor, spin, and orbital quantum numbers.**
- Hadronic currents well describe **the internal symmetries of hadrons**, e.g,  
**the Pauli principle is automatically satisfied.**

# Contents

- Internal structure of heavy mesons
- Internal structure of heavy baryons
- **QCD sum rule analyses**

# QCD Sum Rules

- In sum rule analyses, we consider **two-point correlation functions**:

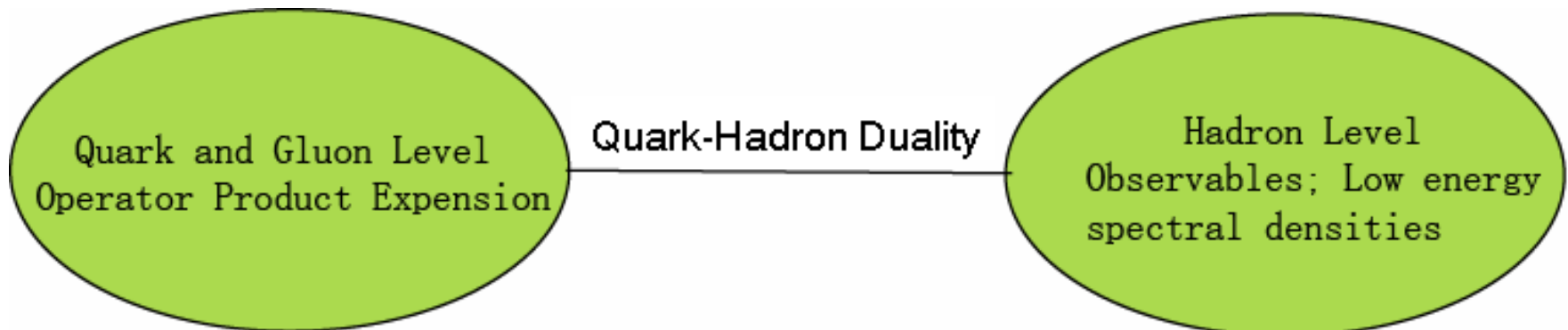
$$\begin{aligned}\Pi(q^2) &\stackrel{\text{def}}{=} i \int d^4x e^{iqx} \langle 0 | T \eta(x) \eta^\dagger(0) | 0 \rangle \\ &\approx \sum_n \langle 0 | \eta | n \rangle \langle n | \eta^\dagger | 0 \rangle\end{aligned}$$

where  $\eta$  is the current which can couple to **hadronic states**.

- By using the **dispersion relation**, we can obtain the **spectral density**

$$\Pi(q^2) = \int_{s_<}^{\infty} \frac{\rho(s)}{s - q^2 - i\varepsilon} ds$$

- In QCD sum rule, we can calculate these matrix elements from QCD (**OPE**) and relate them to observables by using **dispersion relation**.





## Quark and Gluon Level

(Convergence of OPE)

$$\Pi_{OPE}(q^2) \xrightarrow[\substack{\text{dispersion relation} \\ s = -q^2}]{\hspace{10em}} \rho_{OPE}(s) = a_n s^n + a_{n-1} s^{n-1}$$

Quark-Hadron Duality

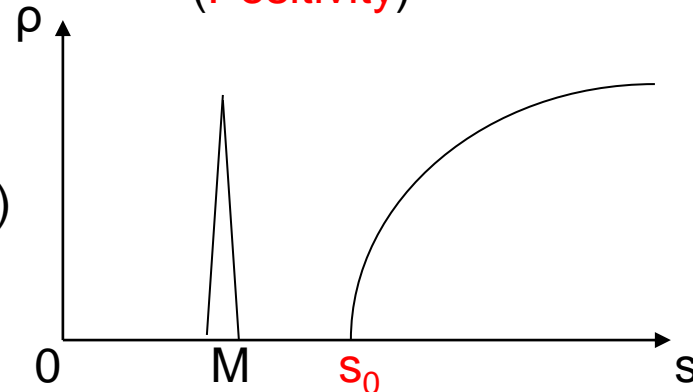
## Hadron Level

$$\Pi_{phys}(q^2) = f_x^2 \frac{1}{q^2 - M^2} \longleftrightarrow \rho_{phys}(s) = \lambda_x^2 \delta(s - M_x^2) + \dots$$

(for boson case)

(Positivity)

(Sufficient amount of Pole contribution)



# Mass spectrum

# P-wave charmed baryons of the flavor $6_F$

Multiplet	B	$\omega_c$ (GeV)	Working region (GeV)	$\bar{\Lambda}$ (GeV)	Baryon ( $j^P$ )	Mass (GeV)	Difference (MeV)	Decay constant (GeV <sup>4</sup> )
$[6_F, 1, 0, \rho]$	$\Sigma_c$	1.74	$0.27 < T < 0.32$	$1.25 \pm 0.11$	$\Sigma_c(1/2^-)$	$2.77 \pm 0.14$	$15 \pm 6$	$0.067 \pm 0.017$ ( $\Sigma_c^-(1/2^-)$ )
					$\Sigma_c(3/2^-)$	$2.79 \pm 0.14$		$0.031 \pm 0.008$ ( $\Sigma_c^-(3/2^-)$ )
	$\Xi'_c$	1.87	$0.26 < T < 0.34$	$1.36 \pm 0.10$	$\Xi'_c(1/2^-)$	$2.88 \pm 0.14$	$13 \pm 5$	$0.059 \pm 0.014$ ( $\Xi'_c^-(1/2^-)$ )
					$\Xi'_c(3/2^-)$	$2.89 \pm 0.14$		$0.028 \pm 0.007$ ( $\Xi'_c^-(3/2^-)$ )
	$\Omega_c$	2.00	$0.26 < T < 0.35$	$1.48 \pm 0.09$	$\Omega_c(1/2^-)$	$2.99 \pm 0.15$	$12 \pm 5$	$0.105 \pm 0.023$ ( $\Omega_c^-(1/2^-)$ )
					$\Omega_c(3/2^-)$	$3.00 \pm 0.15$		$0.049 \pm 0.011$ ( $\Omega_c^-(3/2^-)$ )
$[6_F, 0, 1, \lambda]$	$\Sigma_c$	1.35	$T = 0.27$	$1.10 \pm 0.04$	$\Sigma_c(1/2^-)$	$2.83 \pm 0.05$	–	$0.045 \pm 0.008$ ( $\Sigma_c^-(1/2^-)$ )
	$\Xi'_c$	1.57	$0.27 < T < 0.29$	$1.22 \pm 0.08$	$\Xi'_c(1/2^-)$	$2.90 \pm 0.13$	–	$0.041 \pm 0.009$ ( $\Xi'_c^-(1/2^-)$ )
	$\Omega_c$	1.78	$0.27 < T < 0.31$	$1.37 \pm 0.09$	$\Omega_c(1/2^-)$	$3.03 \pm 0.18$	–	$0.081 \pm 0.020$ ( $\Omega_c^-(1/2^-)$ )
$[6_F, 1, 1, \lambda]$	$\Sigma_c$	1.72	$T = 0.33$	$1.03 \pm 0.12$	$\Sigma_c(1/2^-)$	$2.73 \pm 0.17$	$41 \pm 16$	$0.045 \pm 0.011$ ( $\Sigma_c^-(1/2^-)$ )
					$\Sigma_c(3/2^-)$	$2.77 \pm 0.17$		$0.021 \pm 0.005$ ( $\Sigma_c^-(3/2^-)$ )
	$\Xi'_c$	1.72	$T = 0.34$	$1.14 \pm 0.09$	$\Xi'_c(1/2^-)$	$2.91 \pm 0.12$	$38 \pm 14$	$0.041 \pm 0.008$ ( $\Xi'_c^-(1/2^-)$ )
					$\Xi'_c(3/2^-)$	$2.95 \pm 0.12$		$0.019 \pm 0.004$ ( $\Xi'_c^-(3/2^-)$ )
	$\Omega_c$	1.72	$T = 0.35$	$1.22 \pm 0.07$	$\Omega_c(1/2^-)$	$3.04 \pm 0.10$	$36 \pm 13$	$0.069 \pm 0.011$ ( $\Omega_c^-(1/2^-)$ )
					$\Omega_c(3/2^-)$	$3.07 \pm 0.09$		$0.032 \pm 0.005$ ( $\Omega_c^-(3/2^-)$ )
$[6_F, 2, 1, \lambda]$	$\Sigma_c$	1.50	$0.28 < T < 0.29$	$1.09 \pm 0.09$	$\Sigma_c(3/2^-)$	$2.78 \pm 0.13$	$86 \pm 36$	$0.055 \pm 0.013$ ( $\Sigma_c^-(3/2^-)$ )
					$\Sigma_c(5/2^-)$	$2.87 \pm 0.11$		$0.033 \pm 0.008$ ( $\Sigma_c^-(5/2^-)$ )
	$\Xi'_c$	1.72	$0.27 < T < 0.32$	$1.24 \pm 0.12$	$\Xi'_c(3/2^-)$	$2.96 \pm 0.20$	$66 \pm 27$	$0.057 \pm 0.016$ ( $\Xi'_c^-(3/2^-)$ )
					$\Xi'_c(5/2^-)$	$3.02 \pm 0.18$		$0.034 \pm 0.009$ ( $\Xi'_c^-(5/2^-)$ )
	$\Omega_c$	1.85	$0.26 < T < 0.33$	$1.35 \pm 0.11$	$\Omega_c(3/2^-)$	$3.08 \pm 0.19$	$59 \pm 24$	$0.103 \pm 0.026$ ( $\Omega_c^-(3/2^-)$ )
					$\Omega_c(5/2^-)$	$3.14 \pm 0.18$		$0.062 \pm 0.016$ ( $\Omega_c^-(5/2^-)$ )

# Decay properties

$$\Omega_c^0(1/2^-) \rightarrow \Xi_c + \bar{K} \text{ (S-wave)}$$

$$\Omega_c^0(1/2^-) \rightarrow \Xi_c + \bar{K}^* \rightarrow \Xi_c + \bar{K} + \pi$$

$$\Omega_c^0(1/2^-) \rightarrow \Xi_c^* + \bar{K} \text{ (D-wave)}$$

... ..

**Total: 128 decay channels**

# P-wave charmed baryons of the flavor $6_F$

HQET state	Mixing	Mixed state	Mass (GeV)				
$[\Sigma_c(\frac{1}{2}^-), 0, 1, \lambda]$	$\theta_1 \approx 0^\circ$	$[\Sigma_c(\frac{1}{2}^-), 0, 1, \lambda]$	$2.83_{-0.04}^{+0.06}$	$23_{-43}^{+19}$	$\Gamma(\Sigma_c(1/2^-) \rightarrow \Lambda_c \pi) \neq 0$ $\Gamma_S(\Sigma_c(1/2^-) \rightarrow \Sigma_c \pi) = 37_{-28}^{+60}$ $\Gamma_S(\Sigma_c(1/2^-) \rightarrow \Lambda_c \rho \rightarrow \Lambda_c \pi \pi) = 9.2_{-9.2}^{+37.0}$ $\Gamma_S(\Sigma_c(1/2^-) \rightarrow \Sigma_c \rho \rightarrow \Sigma_c \pi \pi) = 1.2_{-1.0}^{+2.1}$	$48_{-29}^{+70}$	$\Sigma_c(2800)^0$
$[\Sigma_c(\frac{1}{2}^-), 1, 1, \lambda]$		$[\Sigma_c(\frac{1}{2}^-), 1, 1, \lambda]$	$2.73_{-0.18}^{+0.17}$				
$[\Sigma_c(\frac{3}{2}^-), 1, 1, \lambda]$	$\theta_2 = 37 \pm 5^\circ$	$ \Sigma_c(\frac{3}{2}^-)\rangle_1$	$2.75_{-0.17}^{+0.17}$	$68_{-51}^{+51}$	$\Gamma_D(\Sigma_c(3/2^-) \rightarrow \Lambda_c \pi) = 13_{-9}^{+20}$ $\Gamma_D(\Sigma_c(3/2^-) \rightarrow \Sigma_c \pi) = 3.3_{-2.2}^{+4.2}$ $\Gamma_S(\Sigma_c(3/2^-) \rightarrow \Sigma_c^* \pi) = 6.4_{-4.7}^{+10.3}$	$24_{-10}^{+23}$	$\Sigma_c(2800)^0$
$[\Sigma_c(\frac{3}{2}^-), 2, 1, \lambda]$		$ \Sigma_c(\frac{3}{2}^-)\rangle_2$	$2.80_{-0.12}^{+0.14}$				
$[\Sigma_c(\frac{5}{2}^-), 2, 1, \lambda]$	-	$[\Sigma_c(\frac{5}{2}^-), 2, 1, \lambda]$	$2.87_{-0.11}^{+0.12}$	-	$\Gamma_D(\Sigma_c(3/2^-) \rightarrow \Lambda_c \pi) = 23_{-16}^{+35}$ $\Gamma_S(\Sigma_c(3/2^-) \rightarrow \Sigma_c^* \pi) = 3.5_{-2.7}^{+6.1}$	$28_{-16}^{+36}$	
$[\Xi_c'(1/2^-), 0, 1, \lambda]$	$\theta_1 \approx 0^\circ$	$[\Xi_c'(1/2^-), 0, 1, \lambda]$	$2.90_{-0.12}^{+0.13}$	$27_{-27}^{+16}$	$\Gamma_S(\Xi_c'(1/2^-) \rightarrow \Lambda_c \bar{K}) = 400_{-270}^{+610}$ $\Gamma_S(\Xi_c'(1/2^-) \rightarrow \Xi_c \pi) = 360_{-250}^{+550}$	$760_{-370}^{+820}$	-
$[\Xi_c'(1/2^-), 1, 1, \lambda]$		$[\Xi_c'(1/2^-), 1, 1, \lambda]$	$2.91_{-0.12}^{+0.13}$				
$[\Xi_c'(\frac{3}{2}^-), 1, 1, \lambda]$	$\theta_2 = 37 \pm 5^\circ$	$ \Xi_c'(\frac{3}{2}^-)\rangle_1$	$2.94_{-0.11}^{+0.12}$	$56_{-35}^{+30}$	$\Gamma(\Xi_c'(1/2^-) \rightarrow \Lambda_c \bar{K}) \neq 0$ $\Gamma(\Xi_c'(1/2^-) \rightarrow \Xi_c \pi) \neq 0$ $\Gamma_S(\Xi_c'(1/2^-) \rightarrow \Xi_c' \pi) = 12_{-8}^{+15}$ $\Gamma_S(\Xi_c'(1/2^-) \rightarrow \Xi_c \rho \rightarrow \Xi_c \pi \pi) = 1.7_{-1.7}^{+7.6}$	$14_{-8}^{+17}$	$\Xi_c(2923)^0$
$[\Xi_c'(\frac{3}{2}^-), 2, 1, \lambda]$		$ \Xi_c'(\frac{3}{2}^-)\rangle_2$	$2.97_{-0.15}^{+0.24}$				
$[\Xi_c'(\frac{5}{2}^-), 2, 1, \lambda]$	-	$[\Xi_c'(\frac{5}{2}^-), 2, 1, \lambda]$	$3.02_{-0.14}^{+0.23}$	-	$\Gamma_D(\Xi_c'(3/2^-) \rightarrow \Lambda_c \bar{K}) = 2.3_{-1.7}^{+4.3}$ $\Gamma_D(\Xi_c'(3/2^-) \rightarrow \Xi_c \pi) = 4.6_{-3.3}^{+8.1}$ $\Gamma_D(\Xi_c'(3/2^-) \rightarrow \Xi_c' \pi) = 2.0_{-1.2}^{+2.2}$ $\Gamma_S(\Xi_c'(3/2^-) \rightarrow \Xi_c^* \pi) = 2.1_{-1.5}^{+2.6}$	$12_{-4}^{+10}$	$\Xi_c(2939)^0$
$[\Omega_c(\frac{1}{2}^-), 1, 0, \rho]$	$\theta'_1 \approx 0^\circ$	$[\Omega_c(\frac{1}{2}^-), 1, 0, \rho]$	$2.99_{-0.15}^{+0.15}$	$12_{-5}^{+5}$	$\Gamma_D(\Xi_c'(3/2^-) \rightarrow \Lambda_c \bar{K}) = 6.3_{-4.7}^{+11.6}$ $\Gamma_D(\Xi_c'(3/2^-) \rightarrow \Xi_c \pi) = 11_{-8}^{+19}$ $\Gamma_S(\Xi_c'(3/2^-) \rightarrow \Xi_c^* \pi) = 1.3_{-0.94}^{+1.80}$	$19_{-9}^{+22}$	$\Xi_c(2965)^0$
$[\Omega_c(\frac{3}{2}^-), 1, 0, \rho]$	$\theta'_2 \approx 0^\circ$	$[\Omega_c(\frac{3}{2}^-), 1, 0, \rho]$	$3.00_{-0.15}^{+0.15}$				
$[\Omega_c(\frac{1}{2}^-), 0, 1, \lambda]$	$\theta_1 \approx 0^\circ$	$[\Omega_c(\frac{1}{2}^-), 0, 1, \lambda]$	$3.03_{-0.09}^{+0.18}$	$51_{-29}^{+26}$	$\Gamma_D(\Xi_c'(5/2^-) \rightarrow \Lambda_c \bar{K}) = 6.3_{-4.6}^{+11.4}$ $\Gamma_D(\Xi_c'(5/2^-) \rightarrow \Xi_c \pi) = 9.6_{-6.8}^{+15.8}$ $\Gamma_D(\Xi_c'(5/2^-) \rightarrow \Xi_c^* \pi) = 1.5_{-1.1}^{+2.6}$	$18_{-8}^{+20}$	-
$[\Omega_c(\frac{1}{2}^-), 1, 1, \lambda]$		$[\Omega_c(\frac{1}{2}^-), 1, 1, \lambda]$	$3.04_{-0.09}^{+0.11}$				
$[\Omega_c(\frac{3}{2}^-), 1, 1, \lambda]$	$\theta_2 \approx 37 \pm 5^\circ$	$ \Omega_c(\frac{3}{2}^-)\rangle_1$	$3.06_{-0.09}^{+0.10}$	$12_{-5}^{+5}$	$\Gamma(\Omega_c(1/2^-) \rightarrow \Xi_c \bar{K}) \neq 0$ $\Gamma(\Omega_c(3/2^-) \rightarrow \Xi_c \bar{K}) \neq 0$	$\sim 0$	$\Omega_c(3000)^0$
$[\Omega_c(\frac{3}{2}^-), 2, 1, \lambda]$		$ \Omega_c(\frac{3}{2}^-)\rangle_2$	$3.09_{-0.17}^{+0.22}$				
$[\Omega_c(\frac{5}{2}^-), 2, 1, \lambda]$	-	$[\Omega_c(\frac{5}{2}^-), 2, 1, \lambda]$	$3.14_{-0.15}^{+0.21}$	-	$\Gamma_S(\Omega_c(1/2^-) \rightarrow \Xi_c \bar{K}) = 980_{-670}^{+1530}$	$980_{-670}^{+1530}$	-
$[\Omega_c(\frac{1}{2}^-), 1, 1, \lambda]$	$\theta_1 \approx 0^\circ$	$[\Omega_c(\frac{1}{2}^-), 1, 1, \lambda]$	$3.04_{-0.09}^{+0.11}$	$27_{-23}^{+15}$	$\Gamma(\Omega_c(1/2^-) \rightarrow \Xi_c \bar{K}) \neq 0$	$\sim 0$	$\Omega_c(3050)^0$
$[\Omega_c(\frac{3}{2}^-), 1, 1, \lambda]$		$ \Omega_c(\frac{3}{2}^-)\rangle_1$	$3.06_{-0.09}^{+0.10}$				
$[\Omega_c(\frac{3}{2}^-), 2, 1, \lambda]$	$\theta_2 \approx 37 \pm 5^\circ$	$ \Omega_c(\frac{3}{2}^-)\rangle_2$	$3.09_{-0.17}^{+0.22}$	$51_{-29}^{+26}$	$\Gamma_D(\Omega_c(3/2^-) \rightarrow \Xi_c \bar{K}) = 2.0_{-1.5}^{+3.5}$ $\Gamma_D(\Omega_c(3/2^-) \rightarrow \Xi_c \bar{K}) = 6.3_{-4.8}^{+11.2}$	$2.0_{-4.8}^{+3.5}$	$\Omega_c(3066)^0$
$[\Omega_c(\frac{5}{2}^-), 2, 1, \lambda]$		$ \Omega_c(\frac{5}{2}^-)\rangle_2$	$3.14_{-0.15}^{+0.21}$				
$[\Omega_c(\frac{5}{2}^-), 2, 1, \lambda]$	-	$[\Omega_c(\frac{5}{2}^-), 2, 1, \lambda]$	$3.14_{-0.15}^{+0.21}$	-	$\Gamma_D(\Omega_c(3/2^-) \rightarrow \Xi_c \bar{K}) = 5.5_{-4.1}^{+9.6}$	$5.5_{-4.1}^{+9.6}$	$\Omega_c(3119)^0$

# Our QCD sum rule studies

- 1502.01103 **Masses** of P-wave charmed baryons ( $\bar{3}_F$  and  $6_F$ )
- 1510.05267 **Masses** of P-wave bottom baryons ( $\bar{3}_F$  and  $6_F$ )
- 1611.02677 **Masses** of D-wave charmed/bottom baryons ( $\bar{3}_F$ )
- 1707.03712 **Masses** of D-wave charmed/bottom baryons ( $6_F$ )
- 1703.07703 **Decays** of P-wave charmed baryons ( $\bar{3}_F$  and  $6_F$ , partly)
- 1903.10369 **Decays** of P-wave bottom baryons ( $6_F$ , partly)
- 1909.13575 **Decays** of P-wave bottom baryons ( $\bar{3}_F$  and  $6_F$ , partly)
- 2003.07488 **Masses/Decays** of P-wave bottom baryons ( $6_F$ , fully)
- 2106.15488 **Masses/Decays** of P-wave charmed baryons ( $6_F$ , fully)

# Heavy baryons possibly known

## P-wave charmed baryons of the flavor $\bar{3}_F$

$$L = 1, \mathbf{j}_l = \mathbf{1}, J^P = (1/2^-, 3/2^-) \quad \bar{3}_F \begin{cases} (\Lambda_c(2595), \Lambda_c(2625)) \\ (\Xi_c(2790), \Xi_c(2815)) \end{cases}$$

$1/2^-$                        $3/2^-$

## P-wave bottom baryons of the flavor $\bar{3}_F$

$$L = 1, \mathbf{j}_l = \mathbf{1}, J^P = (1/2^-, 3/2^-) \quad \bar{3}_F \begin{cases} (\Lambda_b(5912), \Lambda_b(5920)) \\ (\Xi_b(?), \Xi_b(6100)) \end{cases}$$

$1/2^-$                        $3/2^-$

  
missing

# Heavy baryons possibly known

## D-wave charmed baryons of the flavor $\bar{3}_F$

$$L = 2, \mathbf{j}_l = \mathbf{2}, J^P = (3/2^+, 5/2^+) \quad \bar{3}_F \begin{cases} (\Lambda_c(2860), \Lambda_c(2880)) \\ (\Xi_c(3055), \Xi_c(3080)) \end{cases}$$

$3/2^+$                        $5/2^+$

## D-wave bottom baryons of the flavor $\bar{3}_F$

$$L = 2, \mathbf{j}_l = \mathbf{2}, J^P = (3/2^+, 5/2^+) \quad \bar{3}_F \begin{cases} (\Lambda_b(6146), \Lambda_b(6152)) \\ (\Xi_b(6327), \Xi_b(6333)) \end{cases}$$

$3/2^+$                        $5/2^+$

# Heavy baryons not well known

## P-wave charmed baryons of the flavor $6_F$

$$L = 1, j_l = ?, J^P = ?^-$$

$$6_F \left\{ \begin{array}{l} \Sigma_c(2800) \\ \Xi_c(2923), \Xi_c(2939), \Xi_c(2965) \\ \Omega_c(3000), \Omega_c(3050), \Omega_c(3066), \Omega_c(3090), \Omega_c(3119) \end{array} \right.$$

Many of them are missing

## P-wave bottom baryons of the flavor $6_F$

$$L = 1, j_l = ?, J^P = ?^-$$

$$6_F \left\{ \begin{array}{l} \Sigma_b(6097) \\ \Xi_b(6227) \\ \Omega_b(6316), \Omega_b(6330), \Omega_b(6340), \Omega_b(6350) \end{array} \right.$$

Many of them are missing

# Summary

- Thanks to the efforts of experimentalists, various signals of heavy baryons and exotic hadrons were observed in recent years, making hadron physics popular once more.
- Different from exotic hadrons, we know the internal structure of heavy mesons and heavy baryons much better. Especially, the heavy quark effective theory plays an important role.
- All the above assignments are just possible assignments. We propose to search for more excited heavy hadrons in future experiments.

**Thank you very much!**