



西南大學

Fully heavy tetraquark production at LHC

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Based on arXiv: 2009.08450 , 2304.11142

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Outline:

1. Introduction

2. NRQCD factorization for T_{4c} production

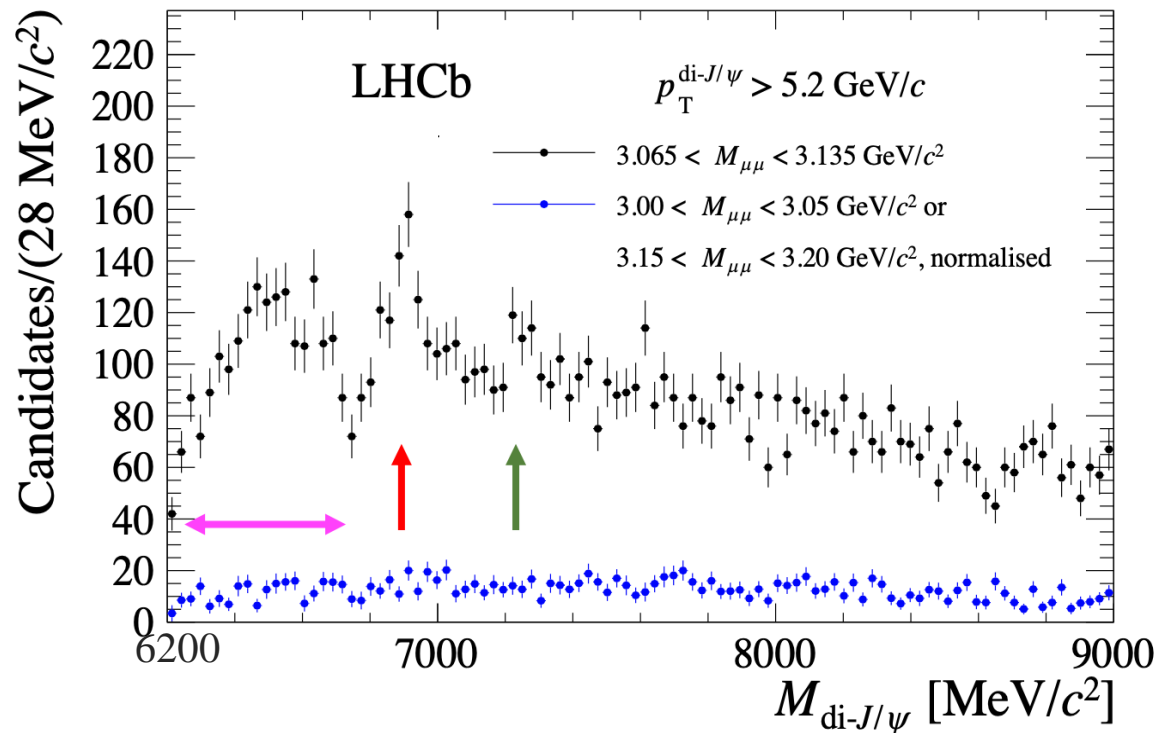
3. T_{4c} production at LHC

4. Summary

1. Introduction

Sci.Bull. 65 (2020) 23, 1983-1993

In 2020, LHCb collaboration observed some structures in the di- J/ψ mass spectrum (CM energies of 7, 8, and 13 TeV, with an integrated luminosity of 9 fb^{-1}).

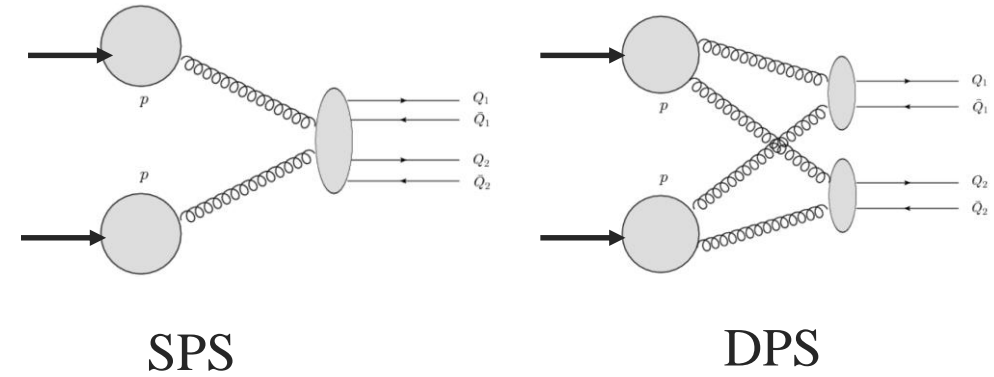


- **Broad structure** at 6.2 – 6.8 GeV slightly above di- J/ψ mass threshold
- **Narrow peak** at 6.9 GeV
- **Hint of another structure** at 7.2 GeV
- **Structure not present** in J/ψ background sample

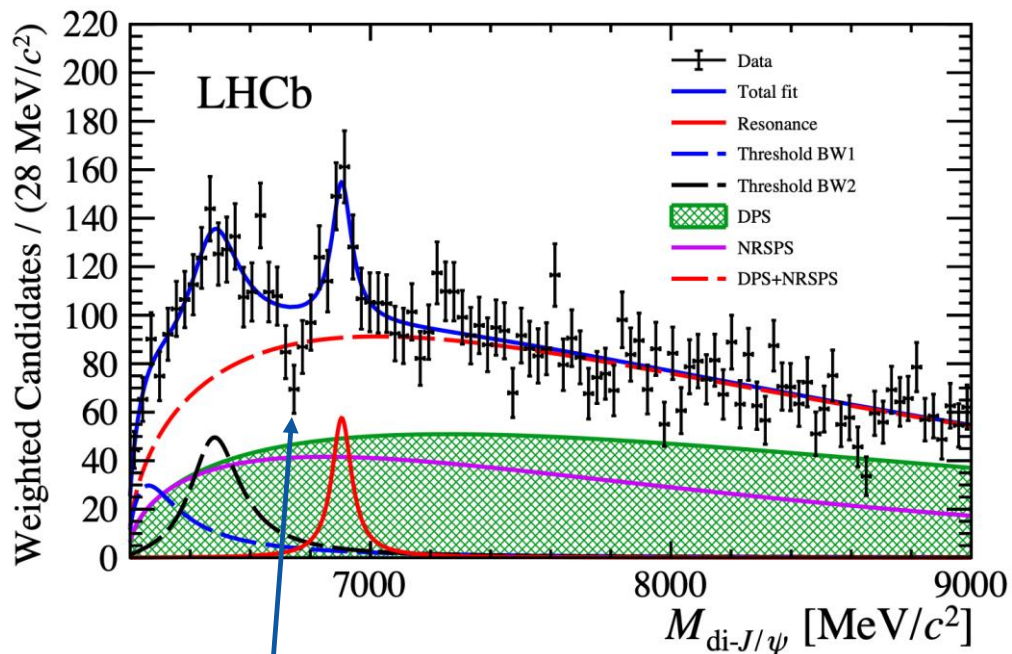
1. Introduction

Sci.Bull. 65 (2020) 23, 1983-1993

LHCb adopt several methods to fit the experimental data.



Model I



Can not explain the dip around 6.75 GeV !

- X(6900) structure as a resonance
- Threshold enhancement by a superposition of two resonances
- Other Background: NRSPS (nonresonant single-parton scattering) + DPS (double-parton scattering)
- Without any interferences

The determined mass and width for the narrow structure:

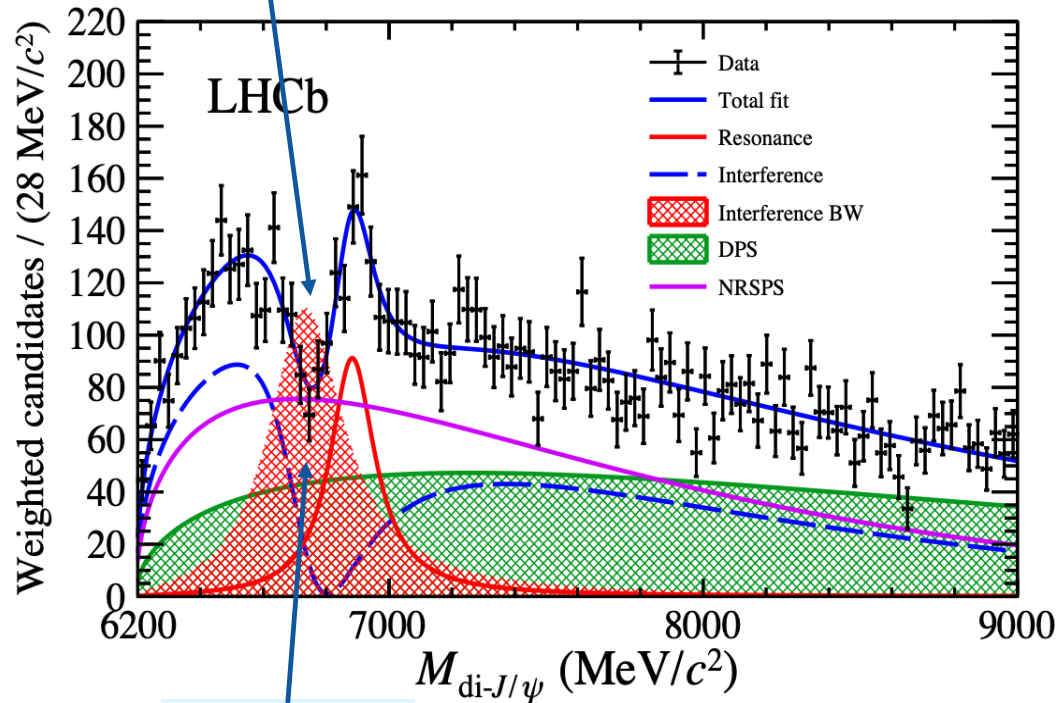
$$M = 6950 \pm 11 \pm 7 \text{ MeV}$$

$$\Gamma = 80 \pm 19 \pm 33 \text{ MeV}$$

1. Introduction

Well fitted the dip

Model II



Wide BW

$$m = 6741 \text{ MeV}/c^2$$
$$\Gamma = 288 \text{ MeV}/c^2$$

- X(6900) structure as a resonance
- Threshold enhancement by interference between NRSPS and a wide resonance
- Other background: DPS

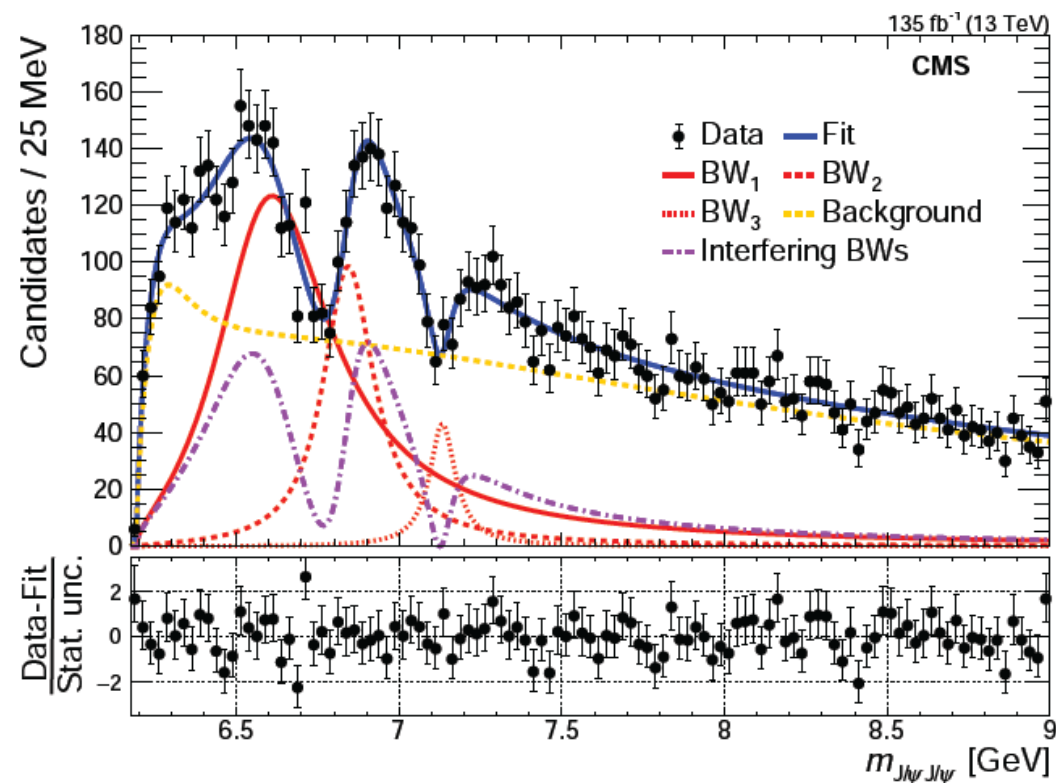
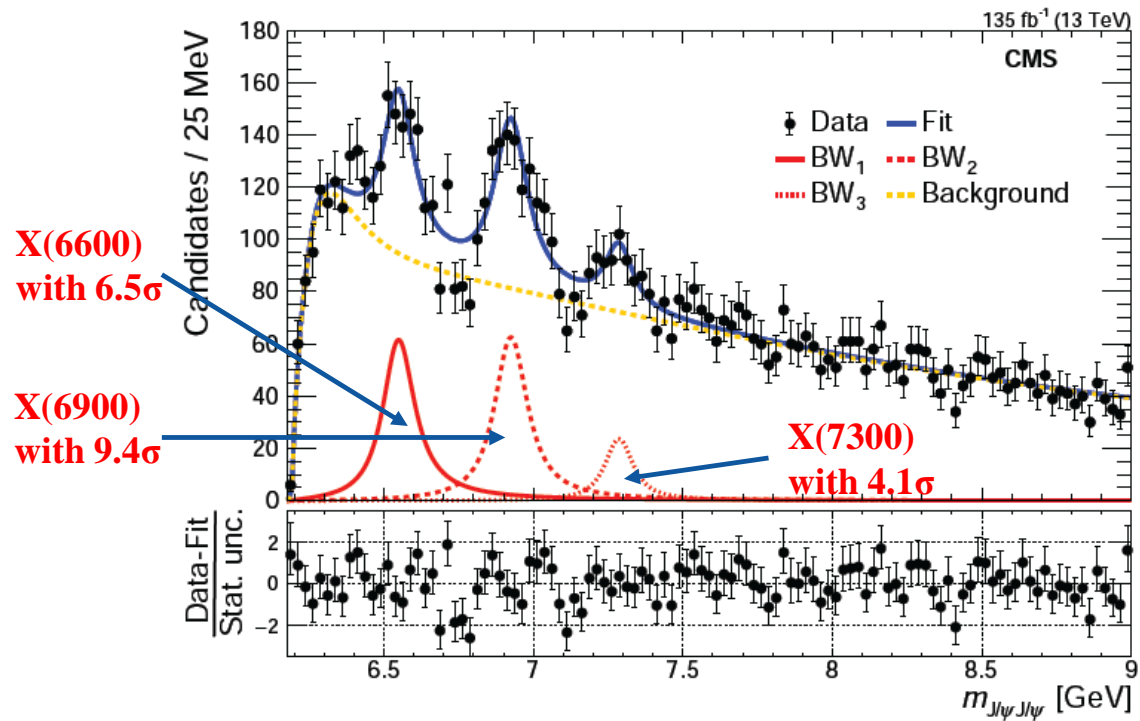
The determined mass and width for the narrow structure:

$$M = 6886 \pm 11 \pm 11 \text{ MeV}$$

$$\Gamma = 168 \pm 33 \pm 69 \text{ MeV}$$

1. Introduction

CMS collaboration 2306.07164



➤ Signals: 3 resonances

➤ Background: NRSPS+DPS+BW₀(model a threshold enhancement)

➤ Without interference

$$M = 6927 \pm 9 \pm 5 \text{ MeV}$$

$$\Gamma = 122 \pm 22 \pm 19 \text{ MeV}$$

$$M = 6552 \pm 10 \pm 12 \text{ MeV}$$

$$M = 7287 \pm 19 \pm 5 \text{ MeV}$$

$$\Gamma = 124 \pm 29 \pm 34 \text{ MeV}$$

$$\Gamma = 95 \pm 46 \pm 20 \text{ MeV}$$

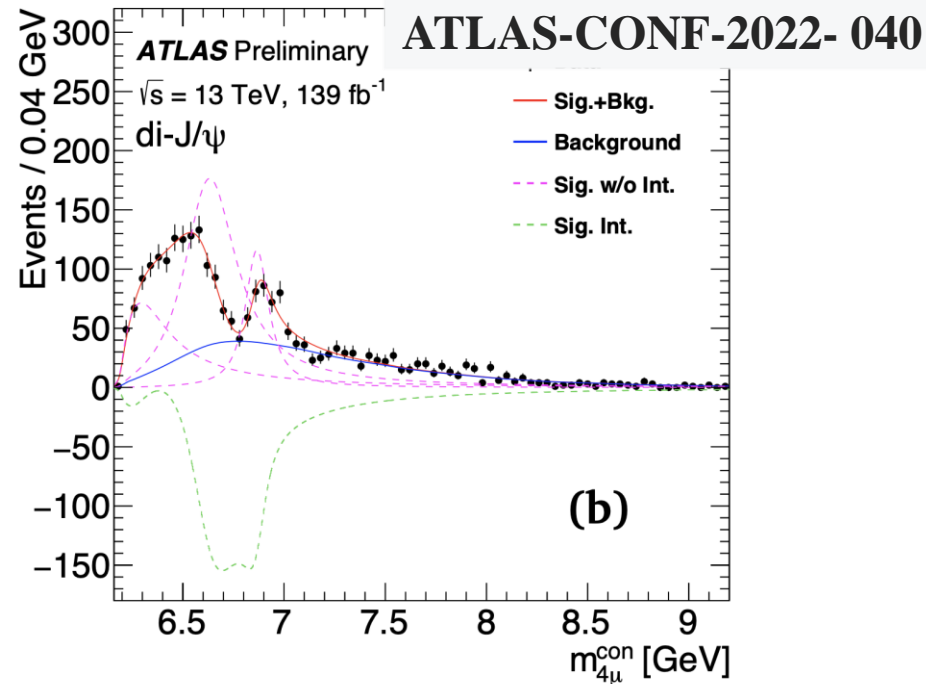
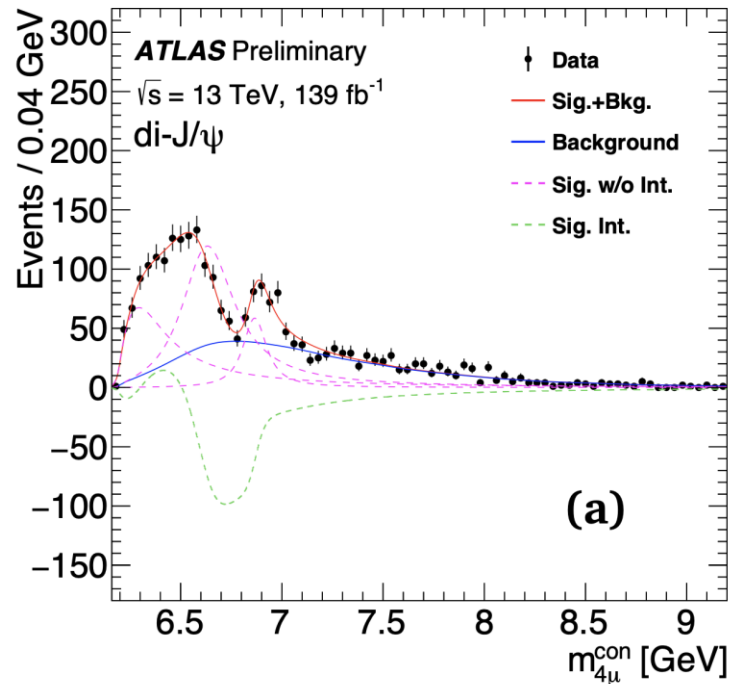
➤ Signals: 3 resonances

➤ Background: NRSPS+DPS+BW₀

➤ Interference between the 3 BWs (By assuming all the signals have the same J^{PC})

1. Introduction

ATLAS collaboration



Statistically significant excesses are seen in the di-J/ ψ channel consistent with a narrow resonance at **6.9 GeV** and **a broader structure at lower mass**

In the bottom sector, the searches by LHCb (2018) and CMS (2020) are inconclusive.

1. Introduction

On the theoretical side

- The explorations on fully heavy tetraquark date back to 1970s
Iwasaki, PRL(1976); Chao, ZPC(1981); Ader et al. PRD(1982)
- Extensive studies are performed after the discovery of X(6900) (e.g., **>280 works** by inspire-hep)
e.g., the excellent works by Y.B. Dong, S.L. Zhu, X. Liu, F.K. Guo, Q. Zhao, Z.G. Wang, J.L. Ping.....'s groups.
- Theoretical studies are based on various approaches: constituent quark models, QCD sum rules, Lattice, color evaporation model ...

1. Introduction

On the theoretical side

- Interpretations on the nature of the fully-heavy charm quark state are still **controversial**
- ✓ **P-wave tetraquark** (M.-S. Liu et al., 2020; H.-X. Chen et al., 2020, R. Zhu 2020).
- ✓ **Radial excitation of 0^{++}** (Z.-G. Wang, 2020; Lü et al., 2020; Giron, Lebed, 2020; Karliner& Rosner, 2020; J. Zhao et al., 2020; R. Zhu, 2020; B.-C. Yang et al., 2020; Z. Zhao, 2020; H.-W. Keet et al., 2020),
- ✓ **Ground state S-wave tetraquark** (Gordillo et al., 2020).
- ✓ **$\chi_{c0}\chi_{c0}$ molecular state** (Albuquerque et al., 2020)
- ✓ **0^{++} hybrid** (B.-D. Wan, C.-F. Qiao, 2020),
- ✓ **Resonance formed in charmonium-charmonium scattering** (G. Yang et al., 2020; X. Jin et al., 2020), or the **kinematic cusp arising from final-state interaction** (J.-Z. Wang et al., 2020; X.-K. Dong et al., 2020; Z.-H. Guo 2021; C. Gong et al. 2020).

1. Introduction

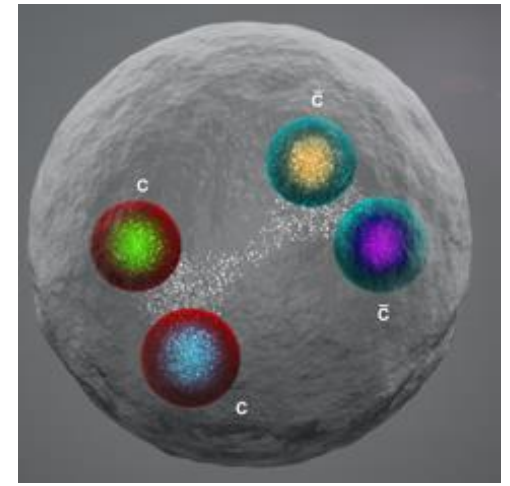
On the theoretical side

While the spectra and decay properties have been widely studied, the production mechanism of fully-heavy tetraquarks was relatively rare.

It is worthwhile to study the fully-heavy tetraquarks production in various colliders, particularly based on factorization.

Similar ideas can be found in the papers of Y.-Q. Ma, H. F. Zhang, 2020;
R.-L. Zhu, 2020

2. NRQCD factorization on T_{4c} production



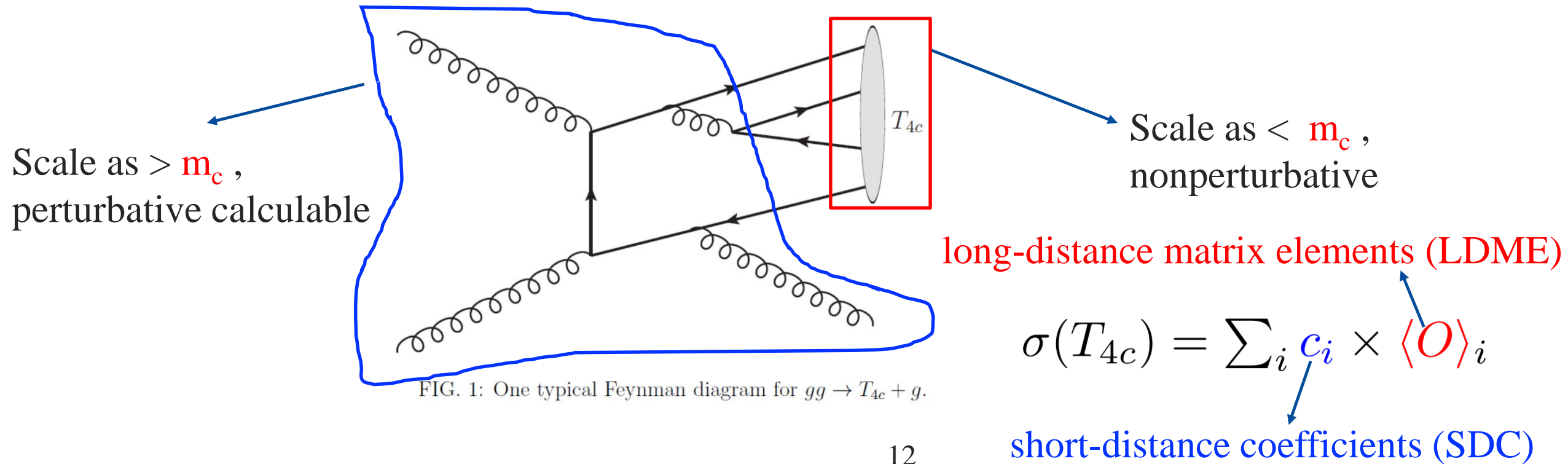
For simplification, X(6900) is dubbed T_{4c}

- Since the charm quark is too heavy, T_{4c} is free from the light constituents contamination. **Thus T_{4c} is widely believed to be a fully-heavy compact tetraquark state** (Other possibilities exist)
- Analogous to the fact that heavy quarkonia are the simplest hadrons, the fully-charmed tetraquark may be the simplest exotic hadrons from theoretical perspective
- Whether is it possible to understand the T_{4c} production **in the framework of NRQCD?**
Like the case of quarkonium production

$T_{4c}: cc\bar{c}\bar{c}$

2. NRQCD factorization on T_{4c} production

A key observation is that, prior to hadronization, two charms and two anticharms have to be created at a rather large energy $> m_c$, thus one can invoke asymptotic freedom to factorize the production rate as the product of the perturbatively calculable short-distance part and the nonperturbative long-distance part



2. NRQCD factorization on T_{4c} production

We construct the operators in **diquark-antidiquark basis**

The diquark (cc) in **spin-singlet**

$$[\psi_a^T (i\sigma^2) \psi_b]$$

The diquark in **spin-triplet**

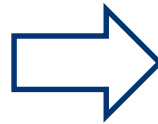
$$[\psi_a^T (i\sigma^2) \sigma^i \psi_b]$$

Color indices

Due to the identities,

$$[\psi_a^T (i\sigma^2) \psi_b] = [\psi_b^T (i\sigma^2) \psi_a]$$

$$[\psi_a^T (i\sigma^2) \sigma^i \psi_b] = -[\psi_b^T (i\sigma^2) \sigma^i \psi_a]$$



The color indices in **spin-singlet** are symmetric

The color indices in **spin-triplet** are antisymmetric

So the spin configuration and color configuration of the diquark are correlated

2. NRQCD factorization on T_{4c} production

Assuming T_{4c} to be a **S-wave tetraquark** (the J^{PC} quantum number can be 0^{++} , 1^{+-} and 2^{++}).

The complement annihilation operators for T_{4c} are

$$\mathcal{O}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{(0)} = -\frac{1}{\sqrt{3}}[\psi_a^T(i\sigma^2)\sigma^i\psi_b][\chi_c^\dagger\sigma^i(i\sigma^2)\chi_d^*] \mathcal{C}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{ab;cd},$$

$$\mathcal{O}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{i;(1)} = -\frac{i}{\sqrt{2}}[\psi_a^T(i\sigma^2)\sigma^j\psi_b][\chi_c^\dagger\sigma^k(i\sigma^2)\chi_d^*] \epsilon^{ijk} \mathcal{C}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{ab;cd},$$

$$\mathcal{O}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{ij;(2)} = [\psi_a^T(i\sigma^2)\sigma^k\psi_b][\chi_c^\dagger\sigma^l(i\sigma^2)\chi_d^*] \Gamma^{ij;kl} \mathcal{C}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{ab;cd},$$

$$\mathcal{O}_{\mathbf{6}\otimes\bar{\mathbf{6}}}^{(0)} = [\psi_a^T(i\sigma^2)\psi_b][\chi_c^\dagger(i\sigma^2)\chi_d^*] \mathcal{C}_{\mathbf{6}\otimes\bar{\mathbf{6}}}^{ab;cd}$$

where

$$\mathcal{C}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{ab;cd} \equiv \frac{1}{(\sqrt{2})^2} \epsilon^{abm} \epsilon^{cdn} \frac{\delta^{mn}}{\sqrt{3}} = \frac{1}{2\sqrt{N_c}} (\delta^{ac}\delta^{bd} - \delta^{ad}\delta^{bc}) \quad \text{Anti-symmetric color tensor}$$

$$\mathcal{C}_{\mathbf{6}\otimes\bar{\mathbf{6}}}^{ab;cd} \equiv \frac{1}{2\sqrt{6}} (\delta^{ac}\delta^{bd} + \delta^{ad}\delta^{bc}) \quad \text{Symmetric color tensor}$$

2. NRQCD factorization on T_{4c} production

The corresponding $\mathbf{J}^{\mathbf{PC}}$ quantum number for each operator

$$\mathcal{O}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{(0)} = -\frac{1}{\sqrt{3}}[\psi_a^T(i\sigma^2)\sigma^i\psi_b][\chi_c^\dagger\sigma^i(i\sigma^2)\chi_d^*] \mathcal{C}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{ab;cd}, \quad \Rightarrow \quad \mathbf{J}^{\mathbf{PC}} = \mathbf{0}^{++}$$

$$\mathcal{O}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{i;(1)} = -\frac{i}{\sqrt{2}}[\psi_a^T(i\sigma^2)\sigma^j\psi_b][\chi_c^\dagger\sigma^k(i\sigma^2)\chi_d^*] \epsilon^{ijk} \mathcal{C}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{ab;cd}, \quad \Rightarrow \quad \mathbf{J}^{\mathbf{PC}} = \mathbf{1}^{+-}$$

$$\mathcal{O}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{ij;(2)} = [\psi_a^T(i\sigma^2)\sigma^k\psi_b][\chi_c^\dagger\sigma^l(i\sigma^2)\chi_d^*] \Gamma^{ij;kl} \mathcal{C}_{\bar{\mathbf{3}}\otimes\mathbf{3}}^{ab;cd}, \quad \Rightarrow \quad \mathbf{J}^{\mathbf{PC}} = \mathbf{2}^{++}$$

$$\mathcal{O}_{\mathbf{6}\otimes\bar{\mathbf{6}}}^{(0)} = [\psi_a^T(i\sigma^2)\psi_b][\chi_c^\dagger(i\sigma^2)\chi_d^*] \mathcal{C}_{\mathbf{6}\otimes\bar{\mathbf{6}}}^{ab;cd} \quad \Rightarrow \quad \mathbf{J}^{\mathbf{PC}} = \mathbf{0}^{++}$$

$$\psi_a(t, x) \stackrel{P}{\leftrightarrow} \psi_a(t, -x)$$

$$\psi_a(t, x) \stackrel{C}{\leftrightarrow} -i\sigma^2 \chi_a^*(t, x)$$

$$\chi_a(t, x) \stackrel{P}{\leftrightarrow} -\chi_a(t, -x)$$

$$\chi_a(t, x) \stackrel{C}{\leftrightarrow} i\sigma^2 \psi_a^*(t, x)$$



3. T_{4c} production at LHC

Applying the NRQCD factorization, we compute the T_{4c} (**S-wave**) production at LHC

We compute the T_{4c} production through **two different ways**.

Fixed-order production

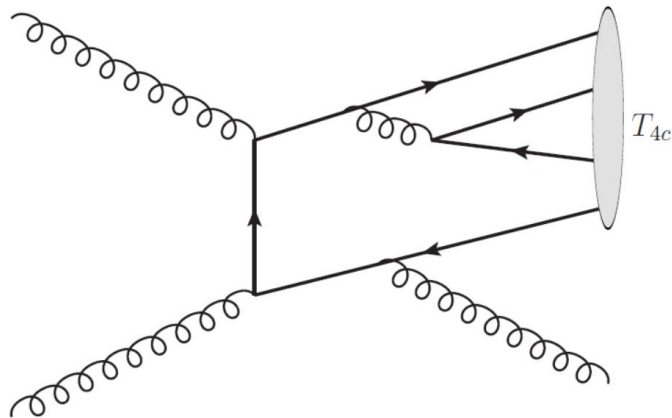
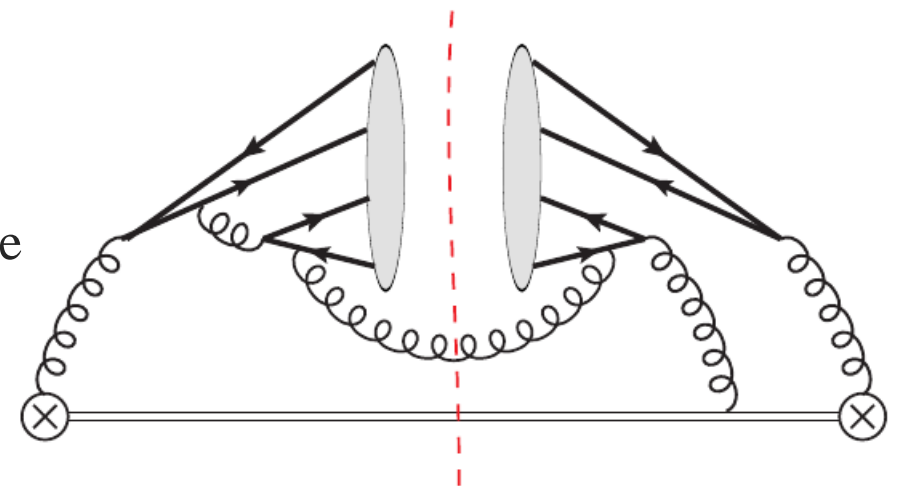


FIG. 1: One typical Feynman diagram for $gg \rightarrow T_{4c} + g$.

$$\alpha_s \sim 0.1$$
$$m_{T_{4c}} \sim 7 \text{ GeV}$$

By naive estimation,
at $p_T > 20 \text{ GeV}$,
fragmentation dominate
at $p_T < 20 \text{ GeV}$,
fixed-order dominate

Fragmentation production



Relative to the fixed-order production, the differential cross section of the fragmentation production suffers $\mathcal{O}(\alpha_s)$ suppression, however is enhanced by $p_T^2/m_{T_{4c}}^2$ at large p_T .

3. T_{4c} production at LHC

The NRQCD factorization for the **fixed-order T_{4c} production** at LHC

$$\frac{d\hat{\sigma}(T_{4c}^{(J)} + X)}{d\hat{t}} = \frac{2m_{T_{4c}}}{m_c^{14}} \left[F_{3,3}^{(J)} \langle O_{3,3}^{(J)} \rangle + 2F_{3,6}^{(J)} \langle O_{3,6}^{(J)} \rangle + F_{6,6}^{(J)} \langle O_{6,6}^{(J)} \rangle \right]$$

where

The SDCs can be perturbatively matched

$$O_{3,3}^{(J)} = \mathcal{O}_{\bar{3} \otimes 3}^{(J)} \sum_X |T_{4c}^J + X\rangle \langle T_{4c}^J + X| \mathcal{O}_{\bar{3} \otimes 3}^{(J)\dagger}$$

$$O_{6,6}^{(0)} = \mathcal{O}_{6 \otimes \bar{6}}^{(0)} \sum_X |T_{4c}^0 + X\rangle \langle T_{4c}^0 + X| \mathcal{O}_{6 \otimes \bar{6}}^{(0)\dagger}$$

$$O_{3,6}^{(0)} = \mathcal{O}_{\bar{3} \otimes 3}^{(0)} \sum_X |T_{4c}^0 + X\rangle \langle T_{4c}^0 + X| \mathcal{O}_{6 \otimes \bar{6}}^{(0)\dagger}$$

Have been constructed previously

642 Feynman diagrams

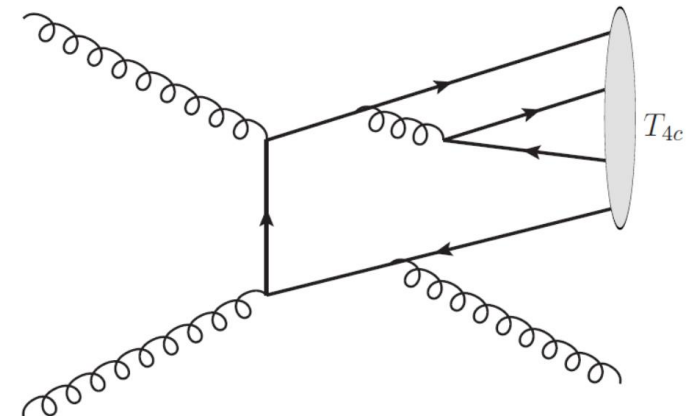


FIG. 1: One typical Feynman diagram for $gg \rightarrow T_{4c} + g$.

3. T_{4c} production at LHC

The LDMEs are **universal**, however **nonperturbative**. We resort to the quark models. One can relate the LDMEs to the phenomenological wave functions at the origin

$$\langle O_{3,3}^{(J)} \rangle = \langle 0 | \mathcal{O}_{\bar{\mathbf{3}} \otimes \mathbf{3}}^{(J)} | T_{4c} \rangle \langle T_{4c} | \mathcal{O}_{\bar{\mathbf{3}} \otimes \mathbf{3}}^{(J)+} | 0 \rangle \approx 16(2J + 1) \psi_3(0) \psi_3^*(0)$$

$$\langle O_{6,6}^{(0)} \rangle = \langle 0 | \mathcal{O}_{\mathbf{6} \otimes \bar{\mathbf{6}}}^{(0)} | T_{4c} \rangle \langle T_{4c} | \mathcal{O}_{\mathbf{6} \otimes \bar{\mathbf{6}}}^{(0)+} | 0 \rangle \approx 16 \psi_6(0) \psi_6^*(0),$$

$$\langle O_{3,6}^{(0)} \rangle = \text{Re}[\langle 0 | \mathcal{O}_{\bar{\mathbf{3}} \otimes \mathbf{3}}^{(0)} | T_{4c} \rangle \langle T_{4c} | \mathcal{O}_{\mathbf{6} \otimes \bar{\mathbf{6}}}^{(0)+} | 0 \rangle] \approx 16 \psi_3(0) \psi_6^*(0),$$

where $\psi(0)$ denotes the four-body Schrödinger wave function at the origin.

	LDME	Model I	Model II
	$\langle O_{3,3}^{(0)} \rangle [\text{GeV}^9]$	0.0347	0.0187
0^{++}	$\langle O_{3,6}^{(0)} \rangle [\text{GeV}^9]$	0.0211	-0.0161
	$\langle O_{6,6}^{(0)} \rangle [\text{GeV}^9]$	0.0128	0.0139
1^{+-}	$\langle O_{3,3}^{(1)} \rangle [\text{GeV}^9]$	0.0780	0.0480
2^{++}	$\langle O_{3,3}^{(2)} \rangle [\text{GeV}^9]$	0.072	0.0628

Model I: EPJC80,871 (2020);

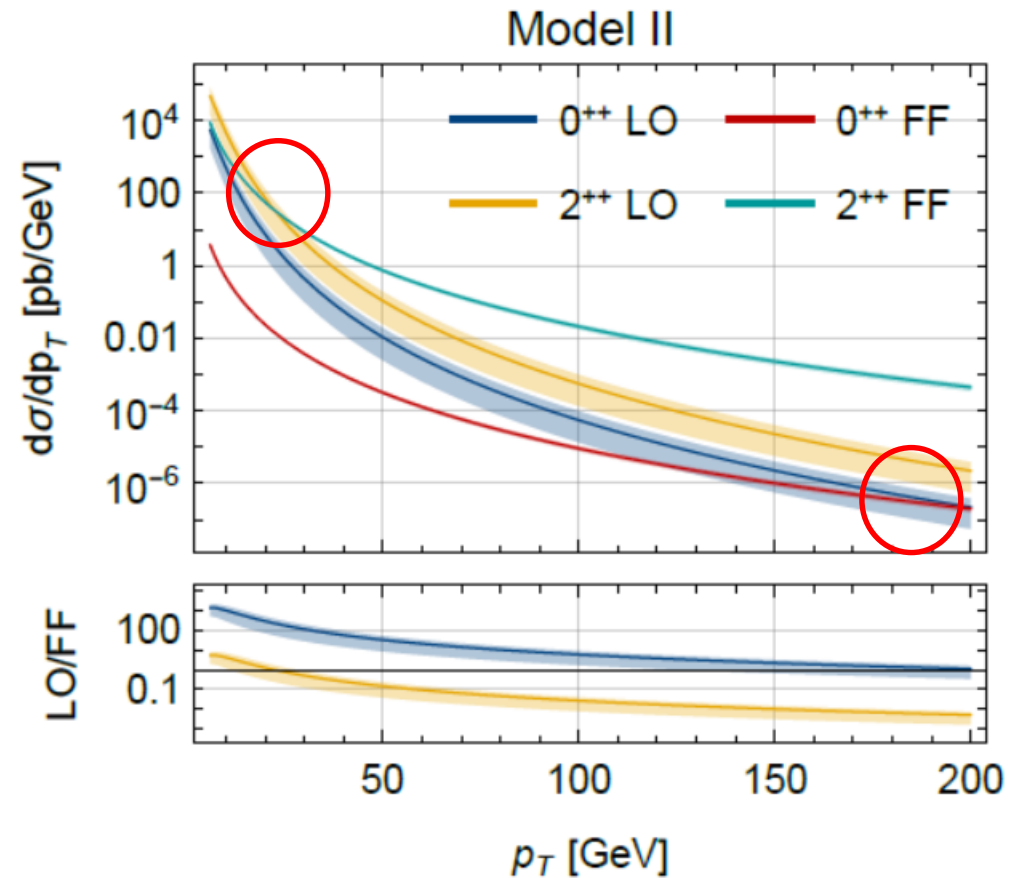
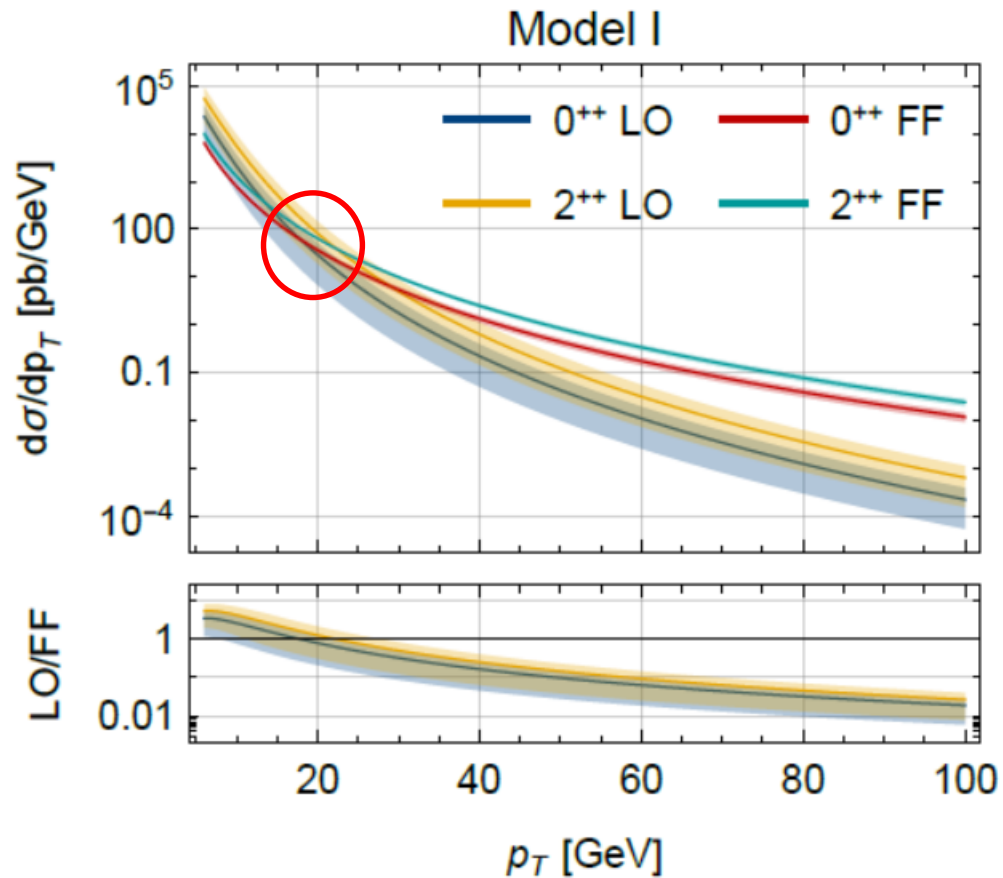
by Q. F. Lü, D. Y. Chen and Y. B. Dong

Model II: arXiv: 2006.11952;

by M. S. liu, F. X. Liu, X. H. Zhong and Q. Zhao

3. T_{4c} production at LHC

Comparison of the p_T distributions of the T_{4c} between **fixed-order** and **fragmentation** predictions



3. T_{4c} production at LHC

By assuming the integrated luminosity of **3000 fb⁻¹**.

	Model I		Model II	
	σ [nb]	$N_{\text{events}}/10^9$	σ [nb]	$N_{\text{events}}/10^9$
0^{++}	37 ± 26	110 ± 80	9 ± 6	27 ± 19
1^{+-}	0.28 ± 0.16	0.8 ± 0.5	0.17 ± 0.10	0.52 ± 0.29
2^{++}	93 ± 65	280 ± 200	81 ± 57	240 ± 170

Table 1: The integrated production rates for various S -wave T_{4c} states ($6 \text{ GeV} \leq p_T \leq 100 \text{ GeV}$) and the estimated event yields.

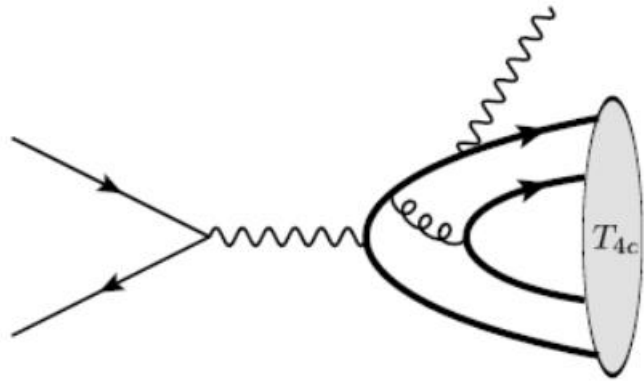
Remarks:

1. The cross section for 1^{+-} is two order-of-magnitude smaller than the other two channels.
2. The cross sections and event numbers for 1^{+-} and 2^{++} are insensitive to the Model. The condition for 0^{++} is different.

3. T_{4c} production at LHC

2011.03039 Feng, Huang, Jia, **SWL**, Zhang

2104.03887 Huang, Feng, Jia, **SWL**, Yang, Zhang



Only for 0^{++}
 2^{++}

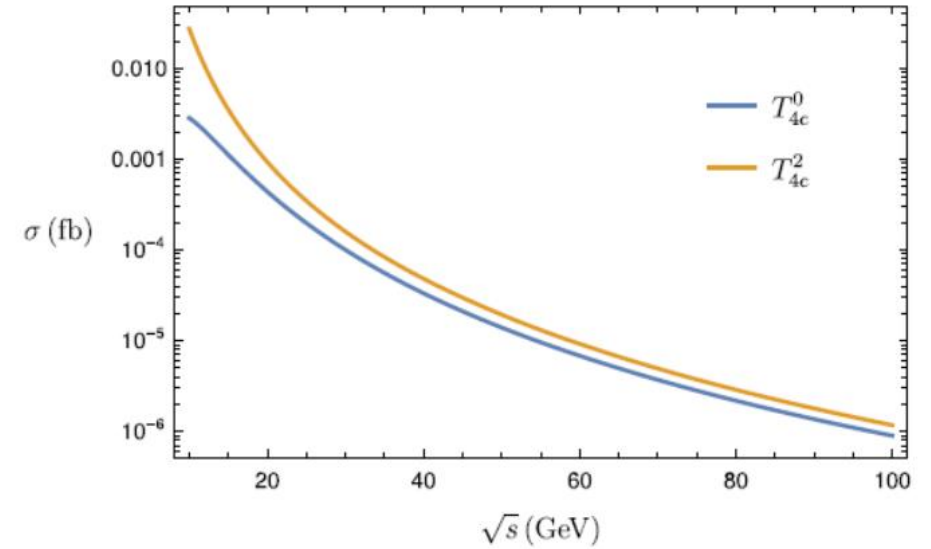
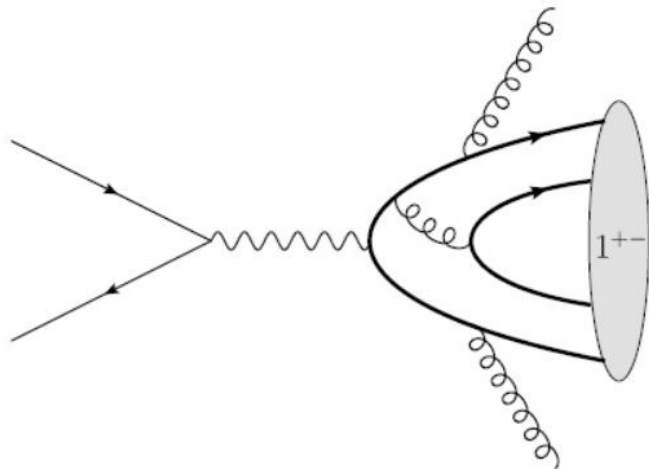
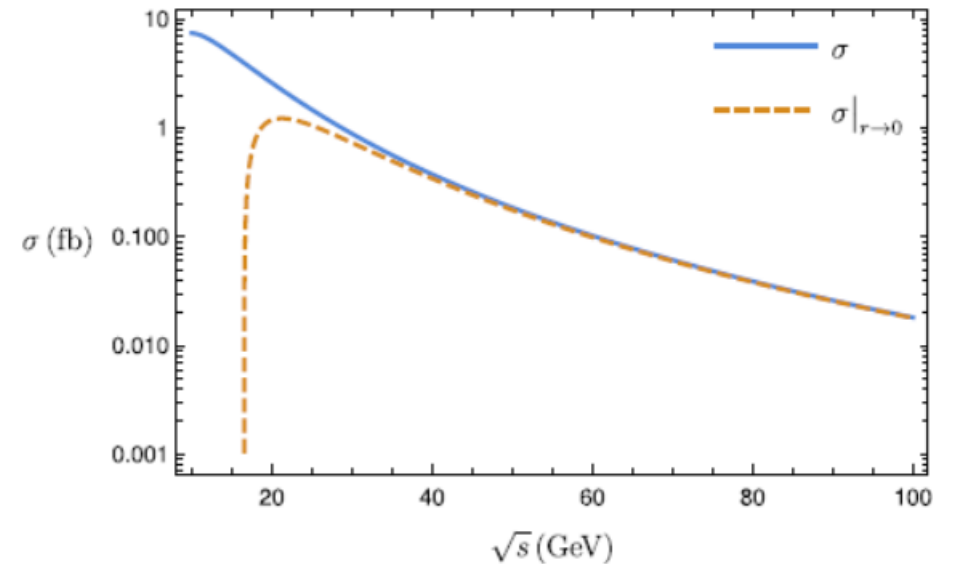


Fig. 2. The total cross sections of $e^+e^- \rightarrow \gamma + T_{4c}^J$ ($J = 0, 2$) as a function of the center-of-mass energy.



Only for 1^{+-}



4. Summary

1. We **propose a NRQCD factorization formula** for T_{4c} production.
2. We compute the T_{4c} production at LHC in two different ways: **fixed-order** computation and **fragmentation** function computation. We find the fragmentation production may be dominant at high $p_T > 20$ GeV.
3. The cross sections can reach **dozens nano-bar** for $J^{PC} = 0^{++}$ and 2^{++} , while less than 1 nb for 1^{+-} .
4. The cross sections at B factories are very small.

Thanks for your attention!