

新强子态研究新进展

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兰州大学

第十六届粒子物理、核物理和宇宙学交叉学科前沿问题研讨会
2023年6月30日-7月4日

Outline

- Background
- Pentaquark is always a focused point
- Abundant phenomena around tetraquark candidates
- Pay more attention to the study of light hadron spectroscopy
- Summary-Never underestimate the ability of experiment



兰州理论物理中心
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Key Laboratory of Theoretical Physics of Gansu Province

Many light hadrons

(1950's & 1960's)

Volume 8, number 3

PHYSICS LETTERS

1 February 1964



Quark model

A SCHEMATIC MODEL OF BARYONS AND MESONS

M. GELL-MANN

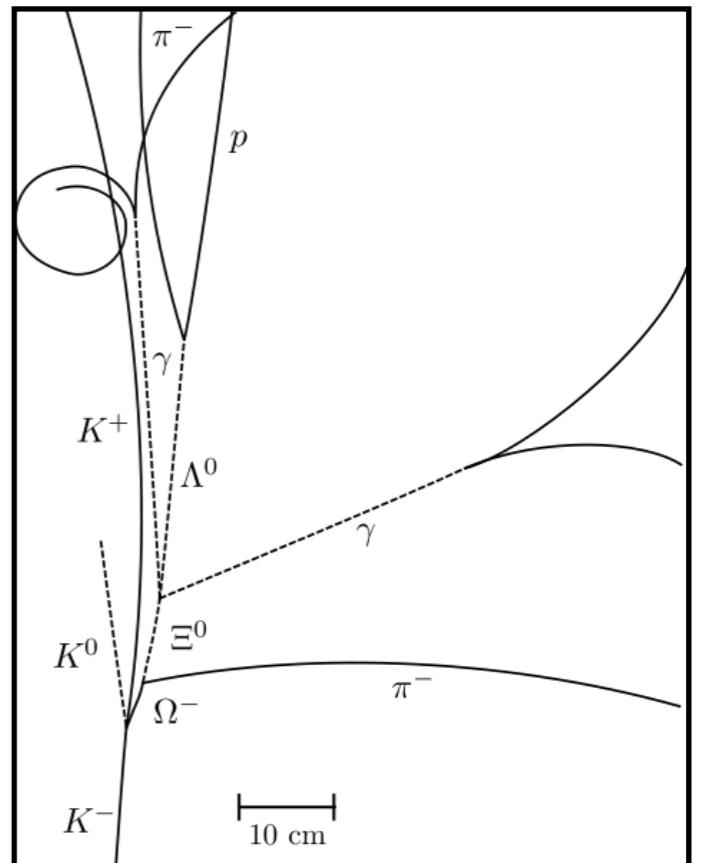
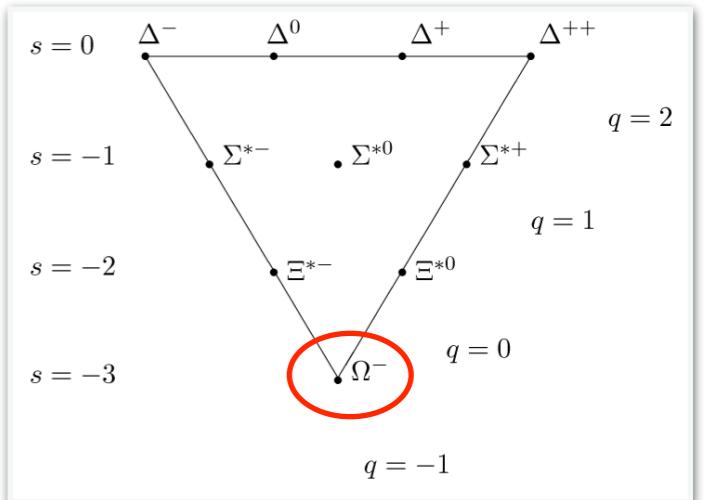
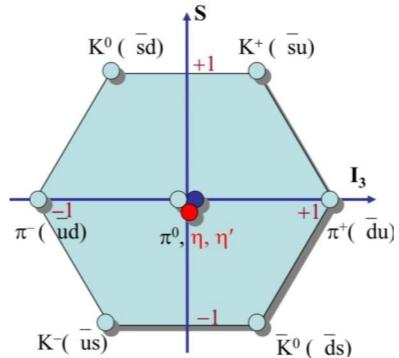
California Institute of Technology, Pasadena, California

Received 4 January 1964

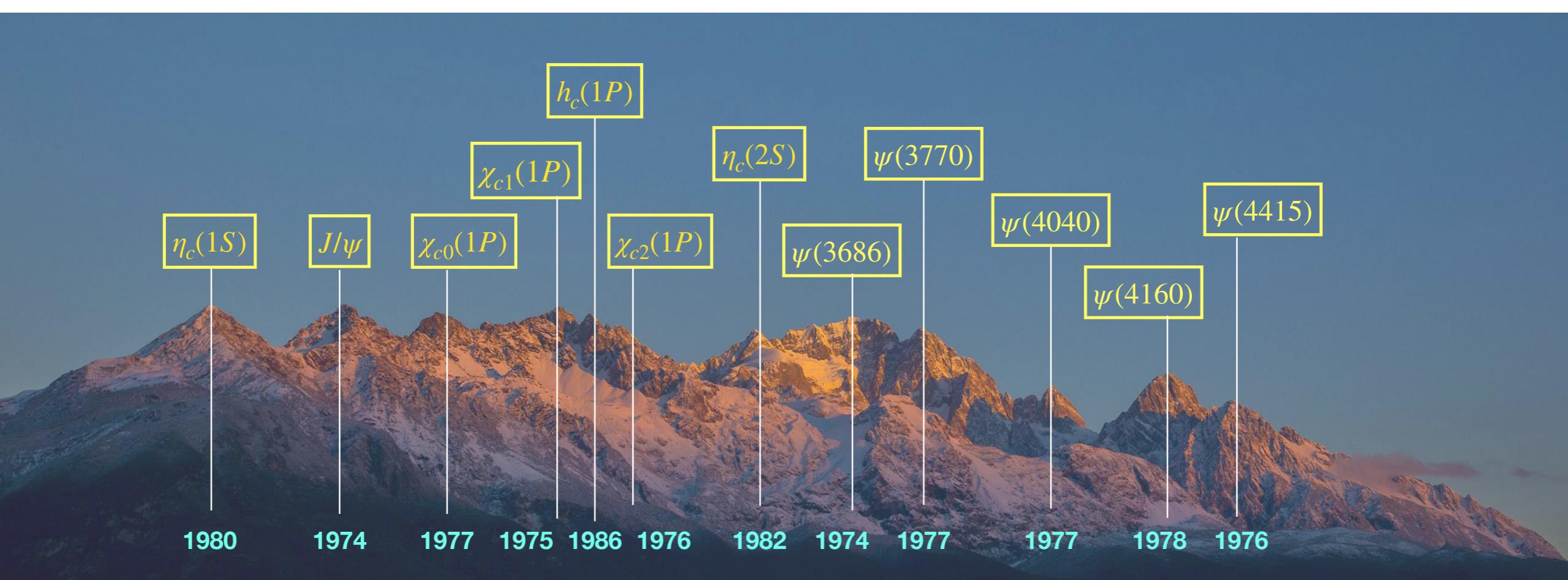
If we assume that the strong interactions of baryons and mesons are correctly described in terms of the broken "eightfold way" 1-3), we are tempted to look for some fundamental explanation of the situation. A highly promised approach is the purely dynamical "bootstrap" model for all the strongly interacting particles within which one may try to derive isotopic spin and strangeness conservation and broken eightfold symmetry from self-consistency alone 4). Of course, with only strong interactions, the orientation of the asymmetry in the unitary space cannot be specified; one hopes that in some way the selection of specific components of the F-spin by electromagnetism and the weak interactions determines the choice of isotopic spin and hypercharge directions.

ber $n_t - n_{\bar{t}}$ would be zero for all known baryons and mesons. The most interesting example of such a model is one in which the triplet has spin $\frac{1}{2}$ and $z = -1$, so that the four particles d^- , s^- , u^0 and b^0 exhibit a parallel with the leptons.

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon b if we assign to the triplet t the following properties: spin $\frac{1}{2}$, $z = -\frac{1}{3}$, and baryon number $\frac{1}{3}$. We then refer to the members $u^{\frac{2}{3}}$, $d^{-\frac{1}{3}}$, and $s^{-\frac{1}{3}}$ of the triplet as "quarks" 6) q and the members of the anti-triplet as anti-quarks \bar{q} . Baryons can now be constructed from quarks by using the combinations $(q q q)$, $(q q q \bar{q})$, etc., while mesons are made out of $(q \bar{q})$, $(q q \bar{q} \bar{q})$, etc. It is assuming that the lowest



Status of charmonium family (1974-1982)



Most of charmonia listed in PDG were observed

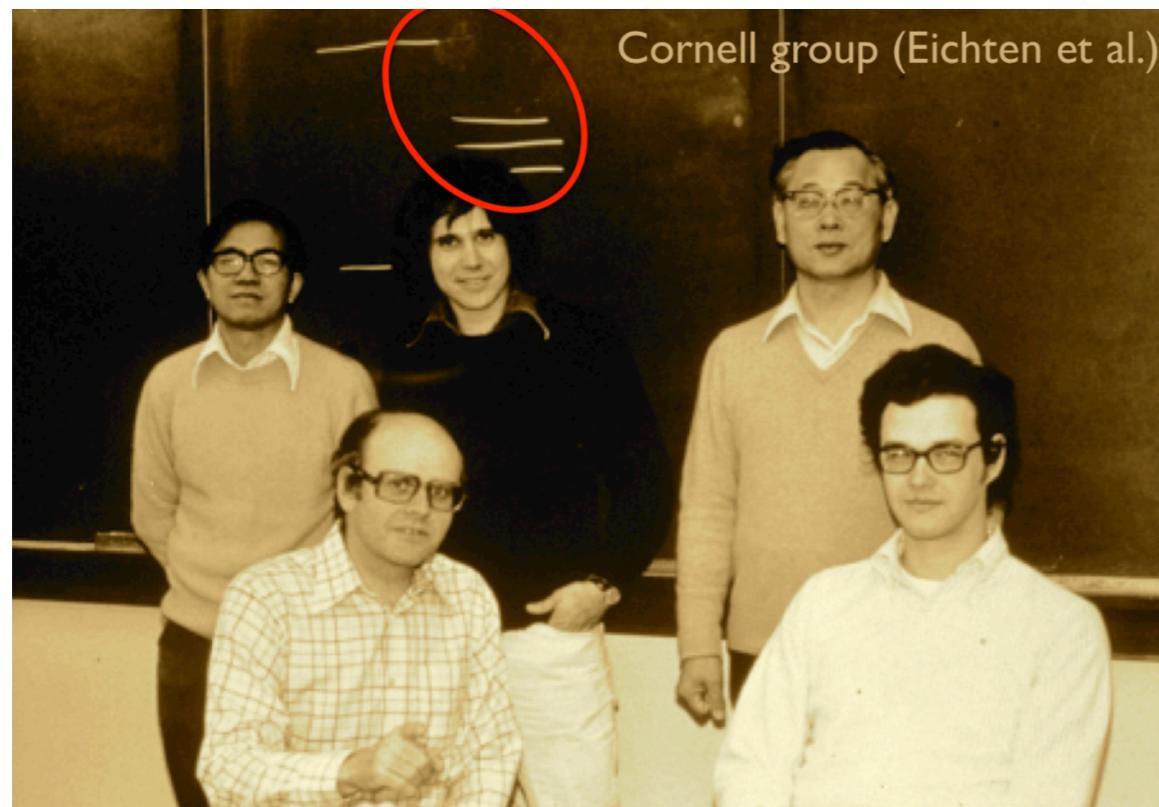
Charmonium: The model

E. Eichten,* K. Gottfried, T. Kinoshita, K. D. Lane,* and T.-M. Yan†

Laboratory of Nuclear Studies, Cornell University, Ithaca, New York 14853

(Received 9 February 1978)

A comprehensive treatment of the charmonium model of the ψ family is presented. The model's basic assumption is a flavor-symmetric instantaneous effective interaction between quark color densities. This interaction describes both quark-antiquark binding and pair creation, and thereby provides a unified approach for energies below and above the threshold for charmed-meson production. If coupling to decay channels is ignored, one obtains the "naive" model wherein the dynamics is completely described by a single charmed-quark pair. A detailed description of this "naive" model is presented for the case where the instantaneous potential is a superposition of a linear and Coulombic term. A far more realistic picture is attained by incorporating those terms in the interaction that couple charmed quarks to light quarks. The coupled-channel formalism needed for this purpose is fully described. Formulas are given for the inclusive e^+e^- cross section and for e^+e^- annihilation into specific charmed-meson pairs. The influence of closed decay channels on ψ states below charm threshold is investigated, with particular attention to leptonic and radiative widths.



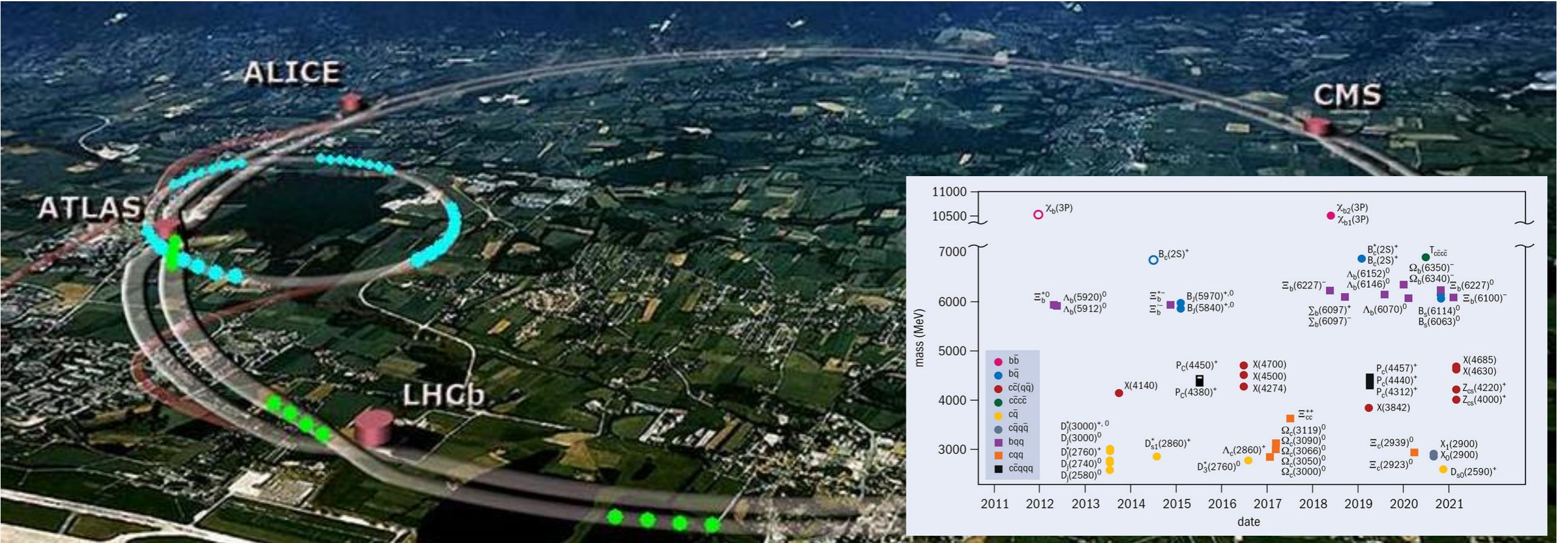
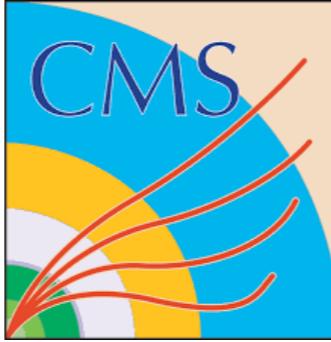
color gauge interaction leads to forces that are so strong at large distances that quarks are permanently confined in color-neutral bound states—the mesons and baryons. We also adopt this assumption.

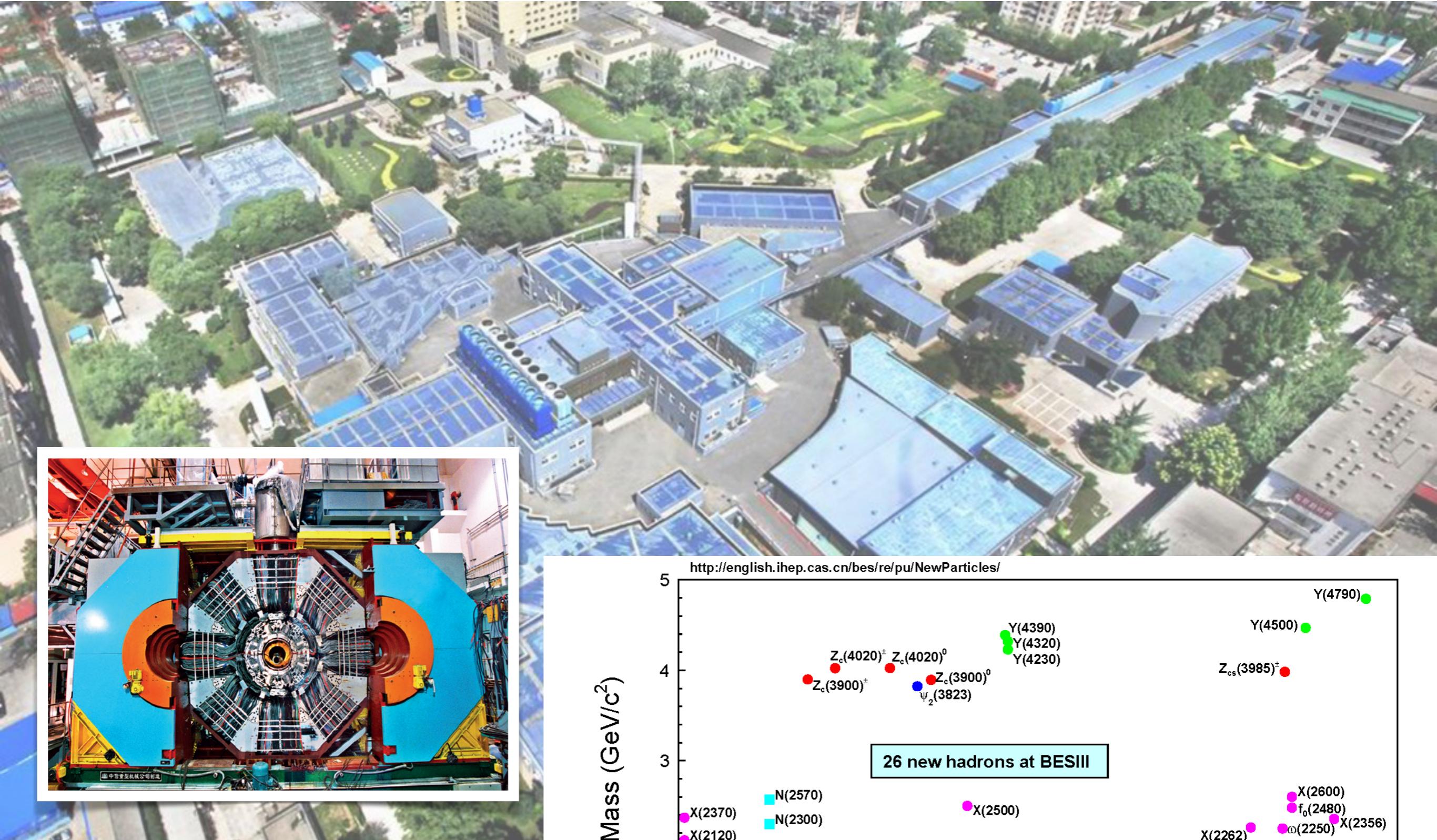
Secondly, the large masses of the ψ resonances and charmed mesons lead to the assumption that the charmed quarks are so heavy that they may be treated nonrelativistically.⁴ No one has yet succeeded in calculating the effective form of the interquark forces from quantum chromodynamics,¹⁶ even in the nonrelativistic limit. To fill this gap we postulate that in this limit many of the gross features of the potential between the charmed quarks can be simulated by the potential

$$V(r) = -\frac{\kappa}{r} + \frac{r}{a^2}. \quad (1.1)$$

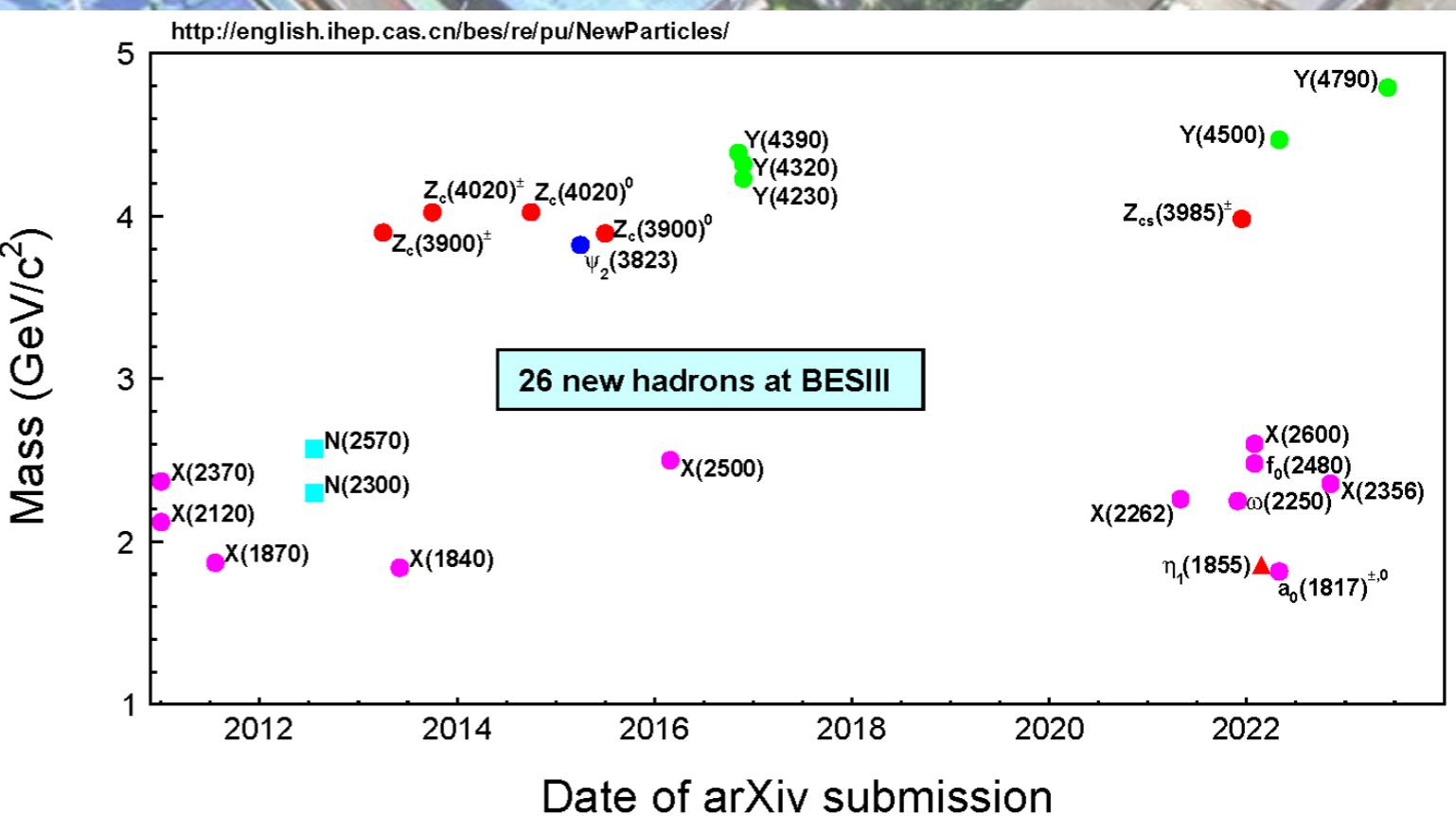
Cornell potential

Experimental status of new hadronic states (2003-now)

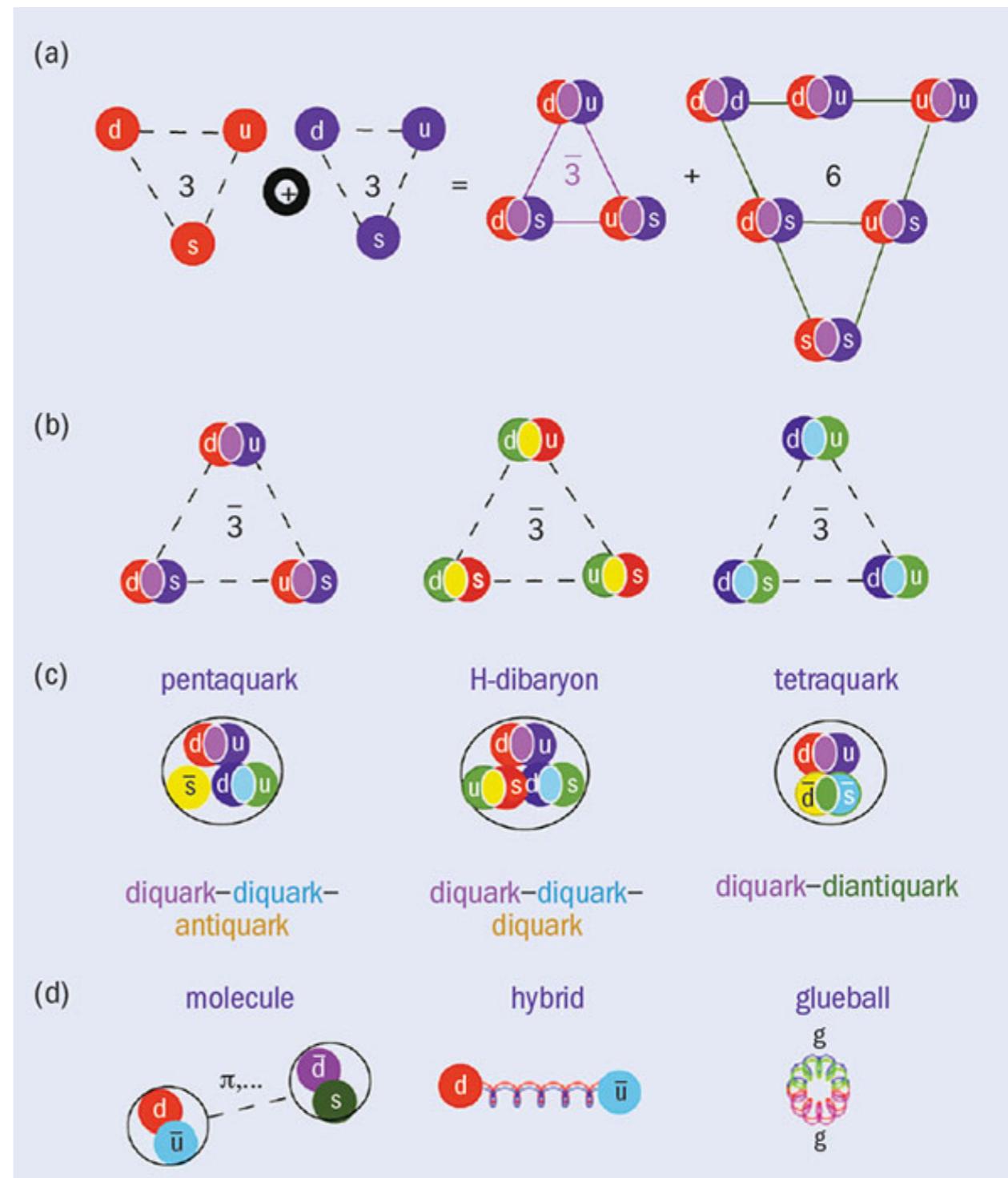




BESIII



"Particle Zoo 2.0"—Exotic states



1. The hidden-charm pentaquark and tetraquark states **960 citations**
H.X. Chen, W. Chen, X. Liu, S.L. Zhu
Phys.Rept. 639 (2016) 1-121
2. Hadronic molecules **933 citations**
F.K. Guo, C. Hanhart, U.G. Meissner, Q. Wang, Q. Zhao, B.S. Zou
Rev.Mod.Phys. 90 (2018) 015004
3. Multiquark resonances **568 citations**
A. Esposito, A. Pilloni, A.D. Polosa
Phys.Rept. 668 (2017) 1-97
4. A review of the open charm and open bottom systems **317 citations**
H.X. Chen, W. Chen, X. Liu, Y.R. Liu, S.L. Zhu
Rept.Prog.Phys.80 (2017) 076201
5. Pentaquark and tetraquark states **472 citations**
Y.R. Liu, H.X. Chen, W. Chen, X. Liu, S.L. Zhu
Prog.Part.Nucl.Phys. 107 (2019) 237-320
6. The XYZ states: experimental and theoretical status and perspectives **527 citations**
N. Brambilla, S. Eidelman, C. Hanhart, A. Nefediev, C.P. Shen, C.E. Thomas, A. Vairo, C.Z. Yuan
Phys.Rept. 873 (2020) 1-154
7. An updated review of the new hadron states **164 citations**
H.X. Chen, W. Chen, X. Liu, Y.R. Liu, S.L. Zhu
Rept.Prog.Phys.86 (2023) 026201
-

Long
reviews

1.

Pentaquark is always a focused point

Summary of pentaquark observations

• $X_b \rightarrow (J/\psi p) \dots$

$$\Lambda_b^0 \rightarrow (J/\psi p) K^-$$

$$\Lambda_b^0 \rightarrow (J/\psi p) \pi^-$$

$$B_s^0 \rightarrow (J/\psi p) \bar{p}$$

• $X_b \rightarrow (J/\psi \Lambda) \dots$

$$\Xi_b^- \rightarrow (J/\psi \Lambda) K^-$$

$$B^- \rightarrow (J/\psi \Lambda) \bar{p}$$

Threshold: $\Sigma_c^{(*)+} \bar{D}^{(*)0} / \Sigma_c^{(*)++} D^{(*)-}$

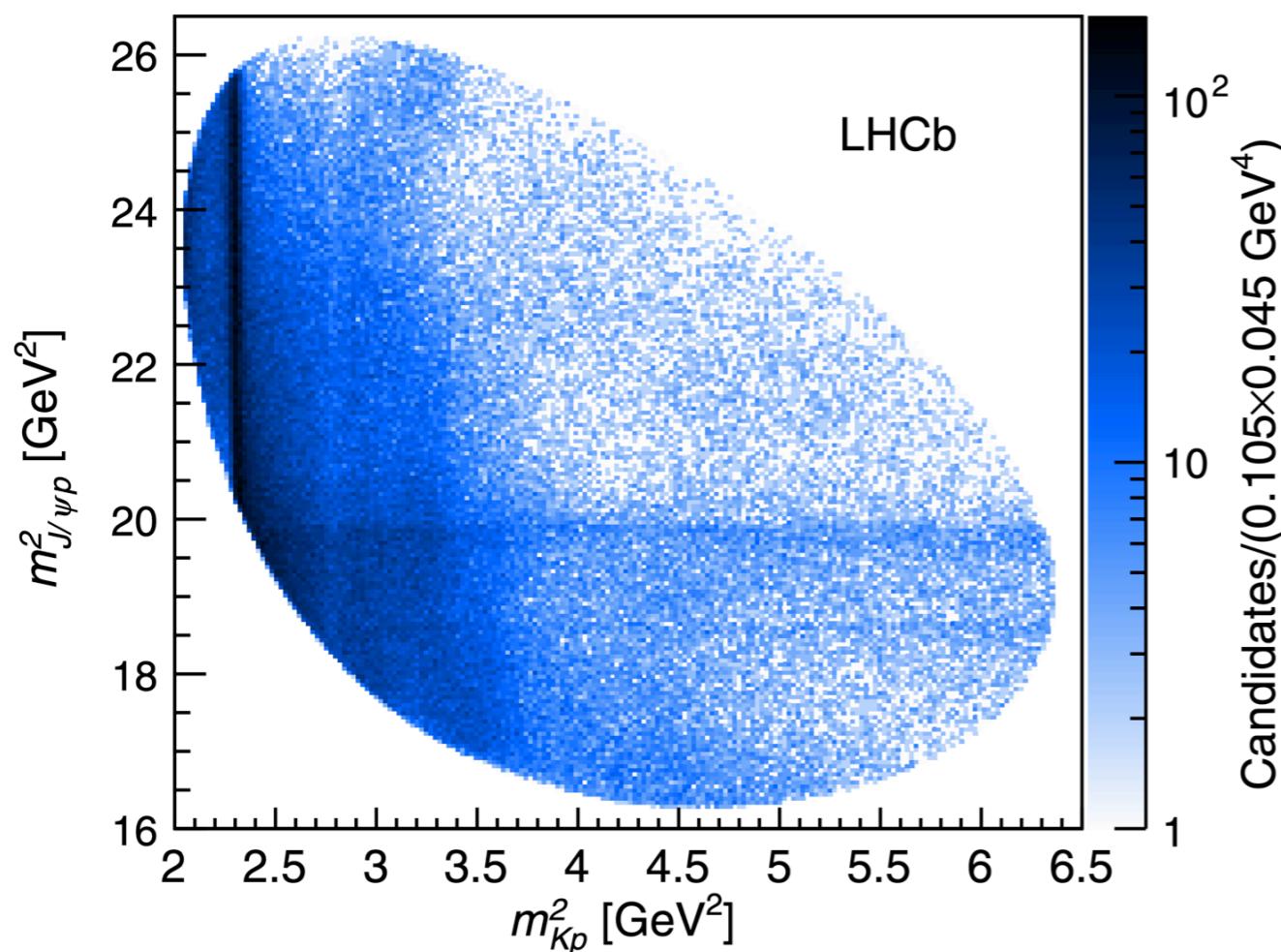
$$P_{\psi}^N$$

Threshold: $\Xi_c^{(*)0} \bar{D}^{(*)0} / \Xi_c^{(*)+} D^{(*)-}$

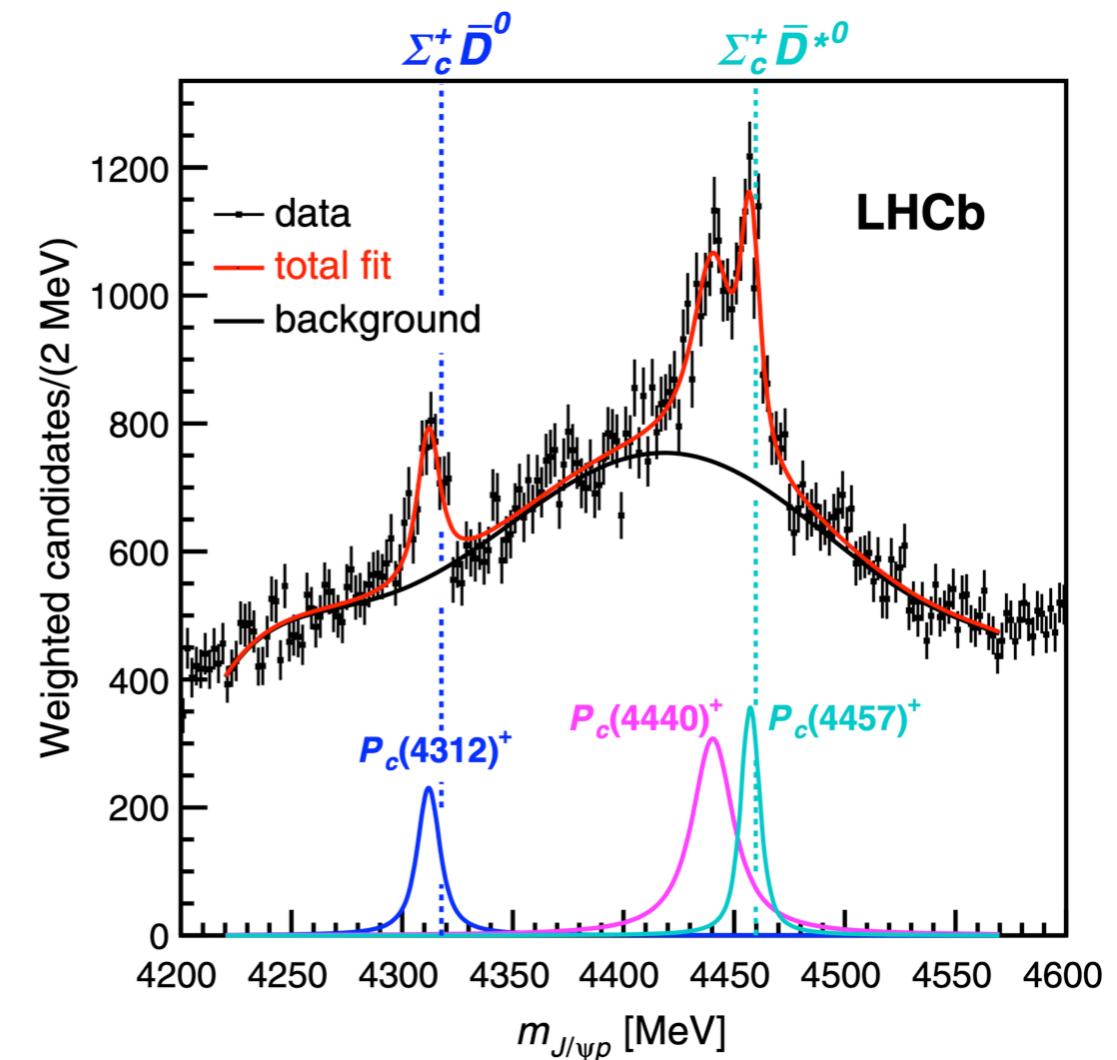
$$P_{\psi s}^{\Lambda}$$

$P_\psi^N(4312)$ $P_\psi^N(4440)$ $P_\psi^N(4457)$ 

$$\Lambda_b^0 \rightarrow (J/\psi p) K^-$$



The first pentaquark

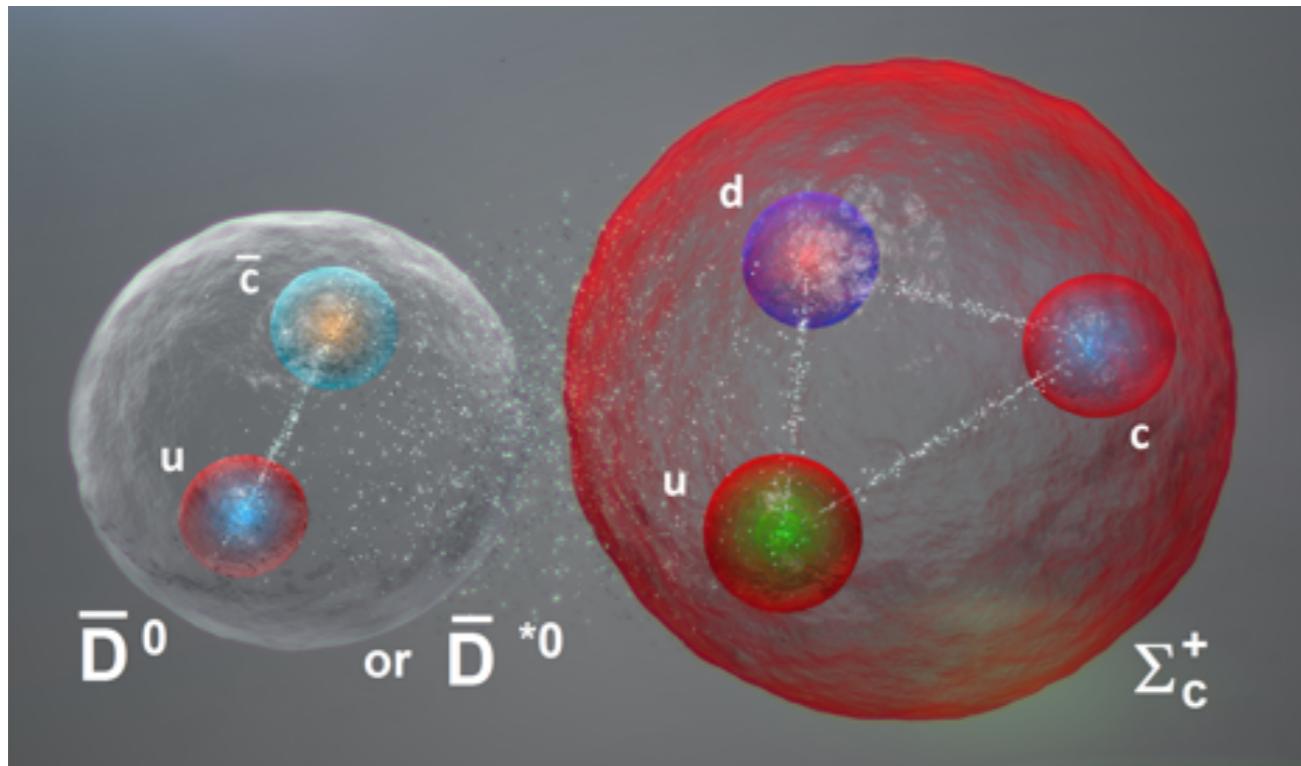


LHCb Collaboration: PRL 115 (2015) 072001; PRL 122 (2019) 222001

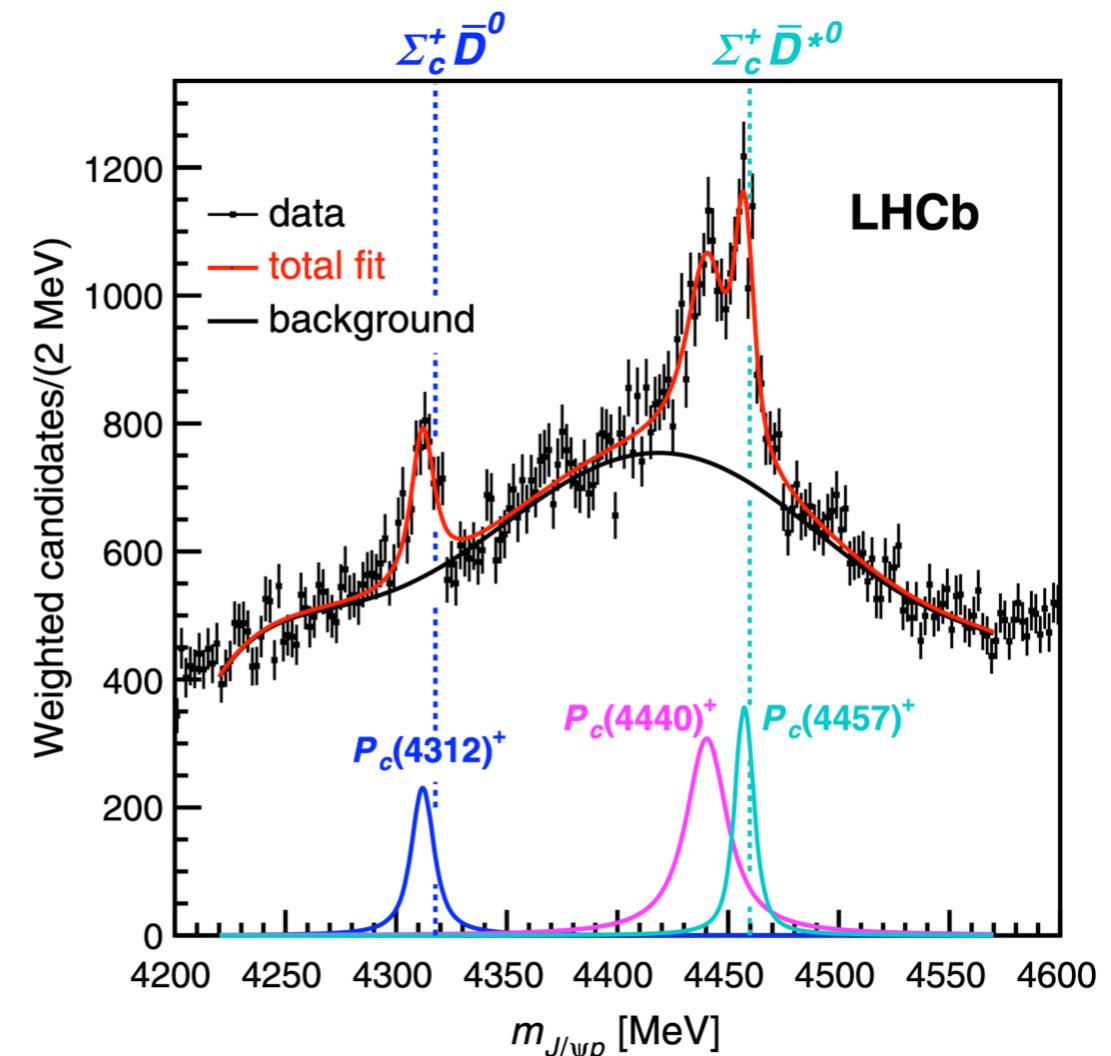
$$P_\psi^N(4312) \quad P_\psi^N(4440) \quad P_\psi^N(4457)$$



$$\Lambda_b^0 \rightarrow (J/\psi p) K^-$$



The first pentaquark



高精度的实验数据支持分子态构型

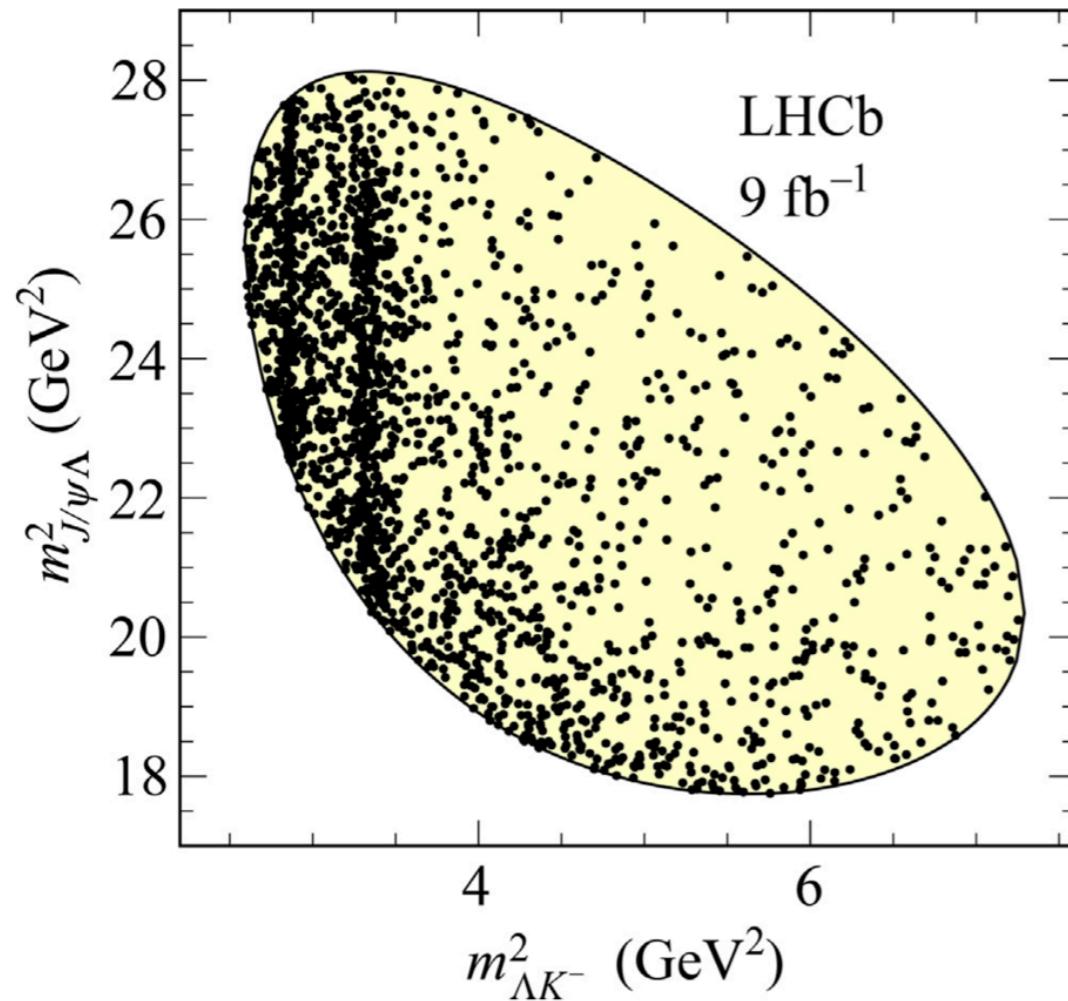
LHCb Collaboration: PRL 115 (2015) 072001; PRL 122 (2019) 222001

$P_{\psi S}^{\Lambda}(4459)$

Hint for the strange partners



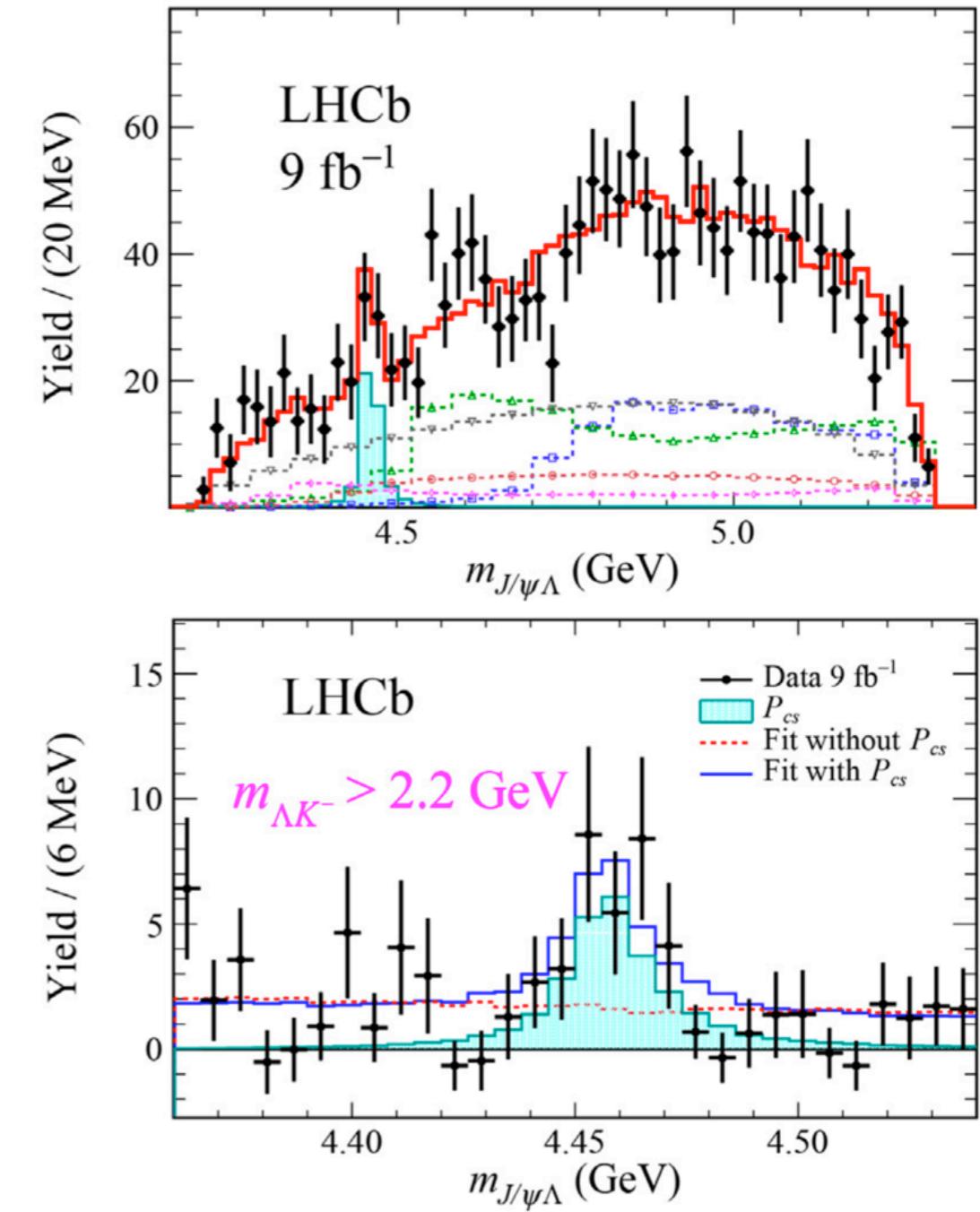
$$\Xi_b^- \rightarrow (J/\psi \Lambda) K^-$$



$$M = 4458 \pm 2.9^{+4.7}_{-1.1} \text{ MeV}$$

$$\Gamma = 17.3 \pm 6.5^{+8.0}_{-5.7} \text{ MeV}$$

4.3σ significance



LHCb: Sci.Bull. 66 (2021) 1278-1287

$P_{\psi S}^{\Lambda}(4338)$

Another strange partner



$$B^- \rightarrow (J/\psi \Lambda) \bar{p}$$

Amplitude contributions:

- $NR(\bar{p}\Lambda)$
- $NR(\bar{p}J/\psi)$
- $P_{\psi S}^{\Lambda}(J/\psi \Lambda)$

Fit results:

$$m = 4338.2 \pm 0.7 \text{ MeV}$$

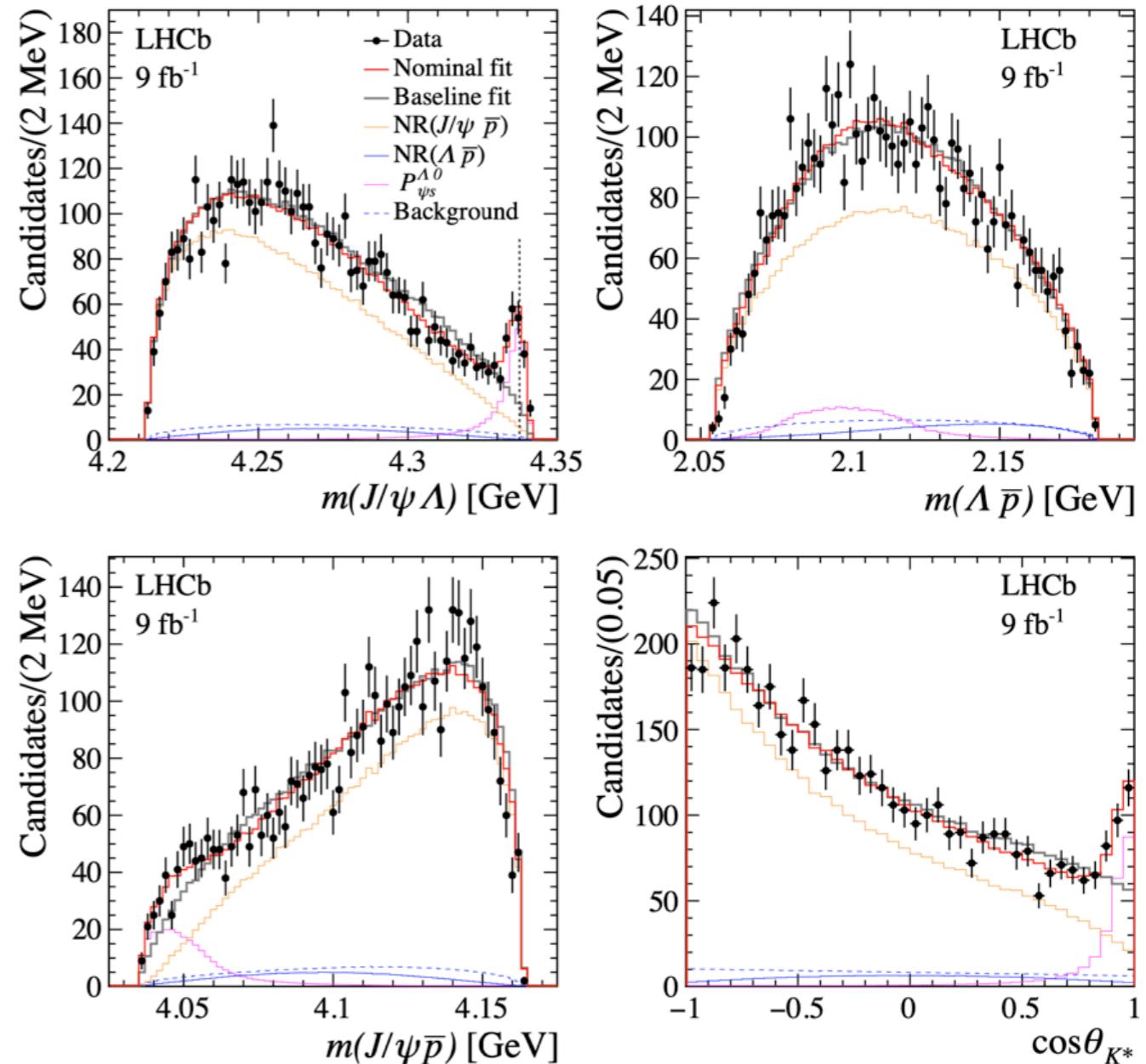
$$\Gamma = 7.0 \pm 1.2 \text{ MeV}$$

Spin-parity:

$J^P = 1/2^-$ is preferred

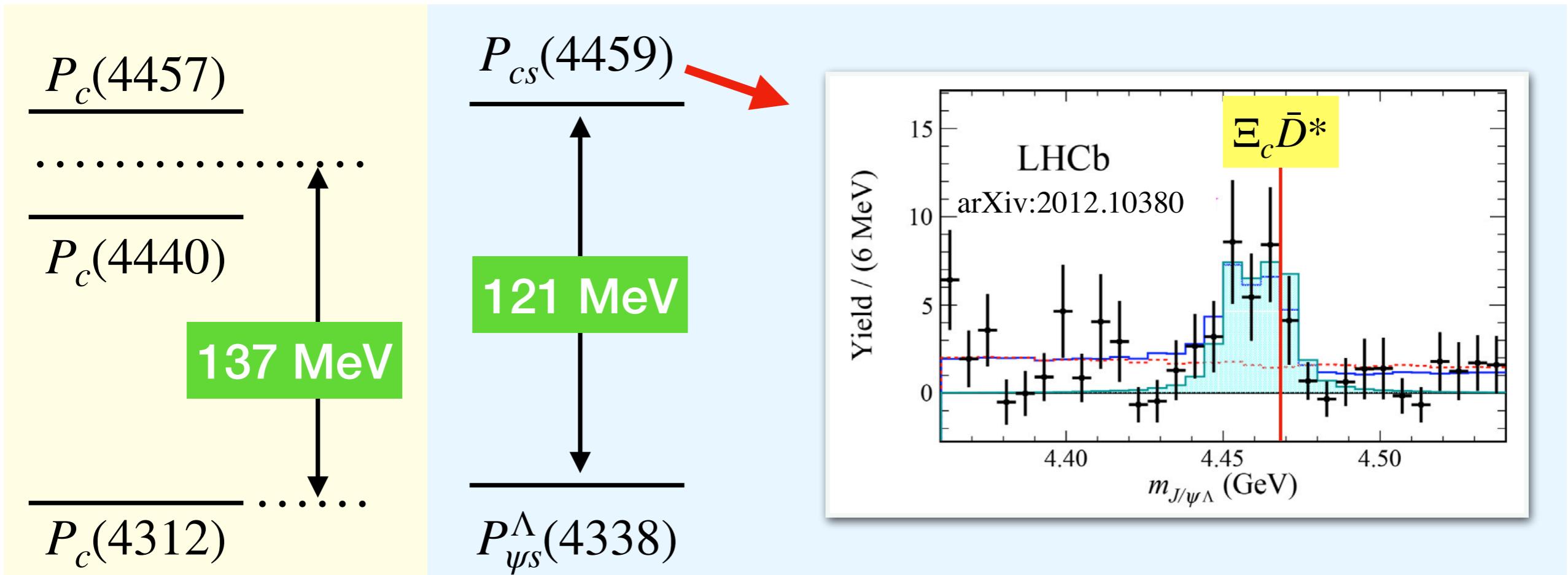
Significance:

$> 10\sigma$



LHCb: arXiv:2210.10346

Similarity between P_ψ^N and $P_{\psi S}^\Lambda$



$$\Xi_b^- \rightarrow J/\psi \Lambda K$$

F.L. Wang, Xiang Liu, Phys.Lett.B 835(2022)137583

Bound state properties for the S-wave isoscalar $\Xi_c \bar{D}^{(*)}$ systems by considering the $S-D$ wave mixing effect. Here, the cutoff Λ , binding energy E , and root-mean-square radius r_{RMS} are in units of GeV, MeV, and fm, respectively.

$\Xi_c \bar{D}(J^P = 1/2^-)$				
Λ	E	r_{RMS}		
1.41	-0.35	4.73		
1.61	-4.82	1.64		
1.79	-12.49	1.10		

$\Xi_c \bar{D}^*(J^P = 1/2^-)$				
Λ	E	r_{RMS}	P($^2S_{\frac{1}{2}}/{}^4D_{\frac{1}{2}}$)	
1.39	-0.34	4.70	100.00/o(0)	
1.57	-4.71	1.63	100.00/o(0)	
1.74	-12.21	1.10	100.00/o(0)	

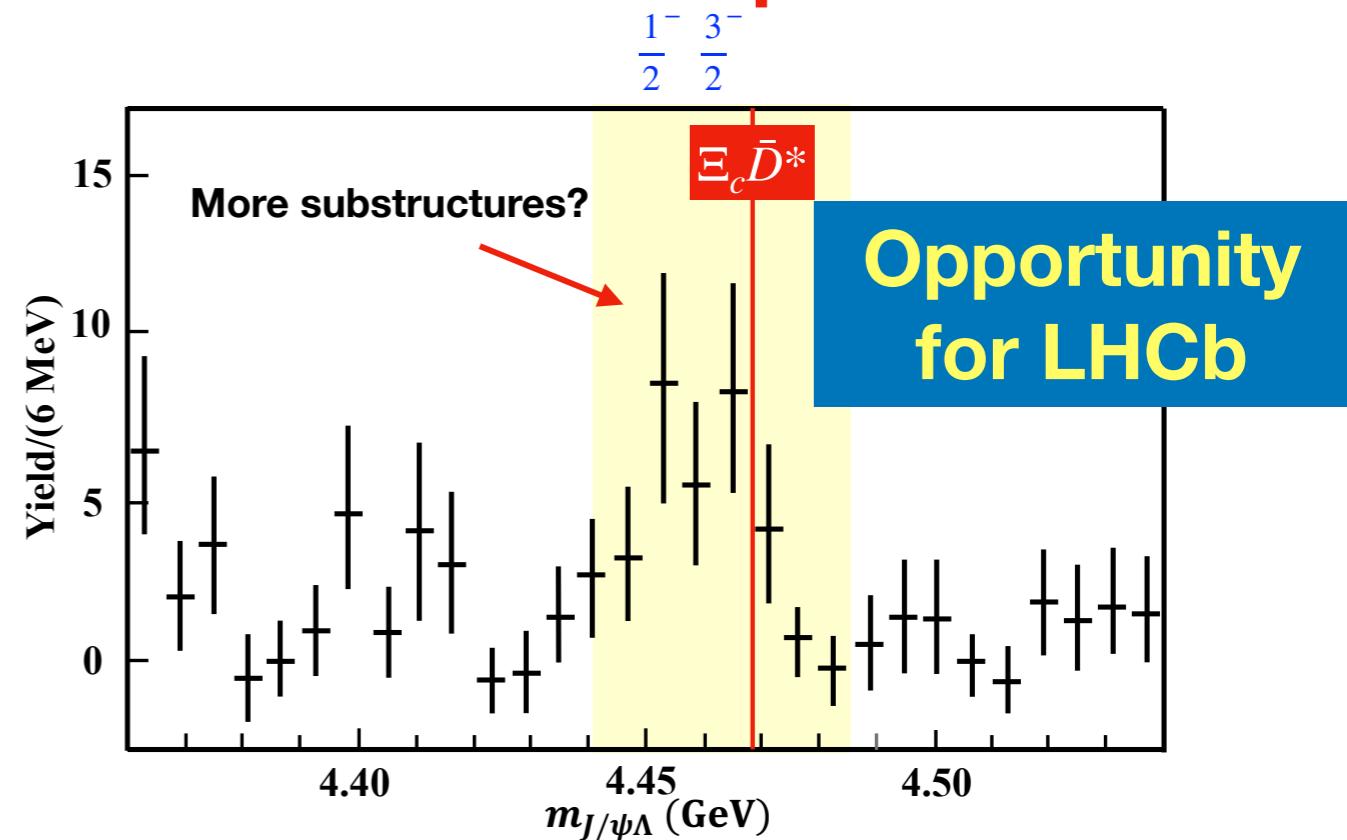
$\Xi_c \bar{D}^*(J^P = 3/2^-)$				
Λ	E	r_{RMS}	P(${}^4S_{\frac{3}{2}}/{}^2D_{\frac{3}{2}}/{}^4D_{\frac{3}{2}}$)	
1.39	-0.34	4.70	100.00/o(0)/o(0)	
1.57	-4.71	1.63	100.00/o(0)/o(0)	
1.74	-12.21	1.10	100.00/o(0)/o(0)	

Bound state properties for the S-wave isoscalar $\Xi_c \bar{D}^*$ system by performing the coupled channel analysis. Here, the cutoff Λ , binding energy E , and root-mean-square radius r_{RMS} are in units of GeV, MeV, and fm, respectively. Additionally, Λ and Λ' denote the cutoff parameters of the $\Xi_c \bar{D}^*$ and $\Xi_c' \bar{D}^*$ channels, respectively.

Λ	Λ'	E	r_{RMS}	P($\Xi_c \bar{D}^*/\Xi_c' \bar{D}^*$)
$\Xi_c \bar{D}^*(J^P = 1/2^-)$				
1.12	0.92	-0.30	4.74	97.75/2.25
1.16	0.96	-4.33	1.58	89.46/10.54
1.20	1.00	-14.67	0.89	77.76/22.24
$\Xi_c \bar{D}^*(J^P = 3/2^-)$				
1.31	1.11	-0.29	4.87	99.73/0.27
1.43	1.23	-4.52	1.64	98.54/1.46
1.56	1.36	-15.01	0.98	96.48/3.52

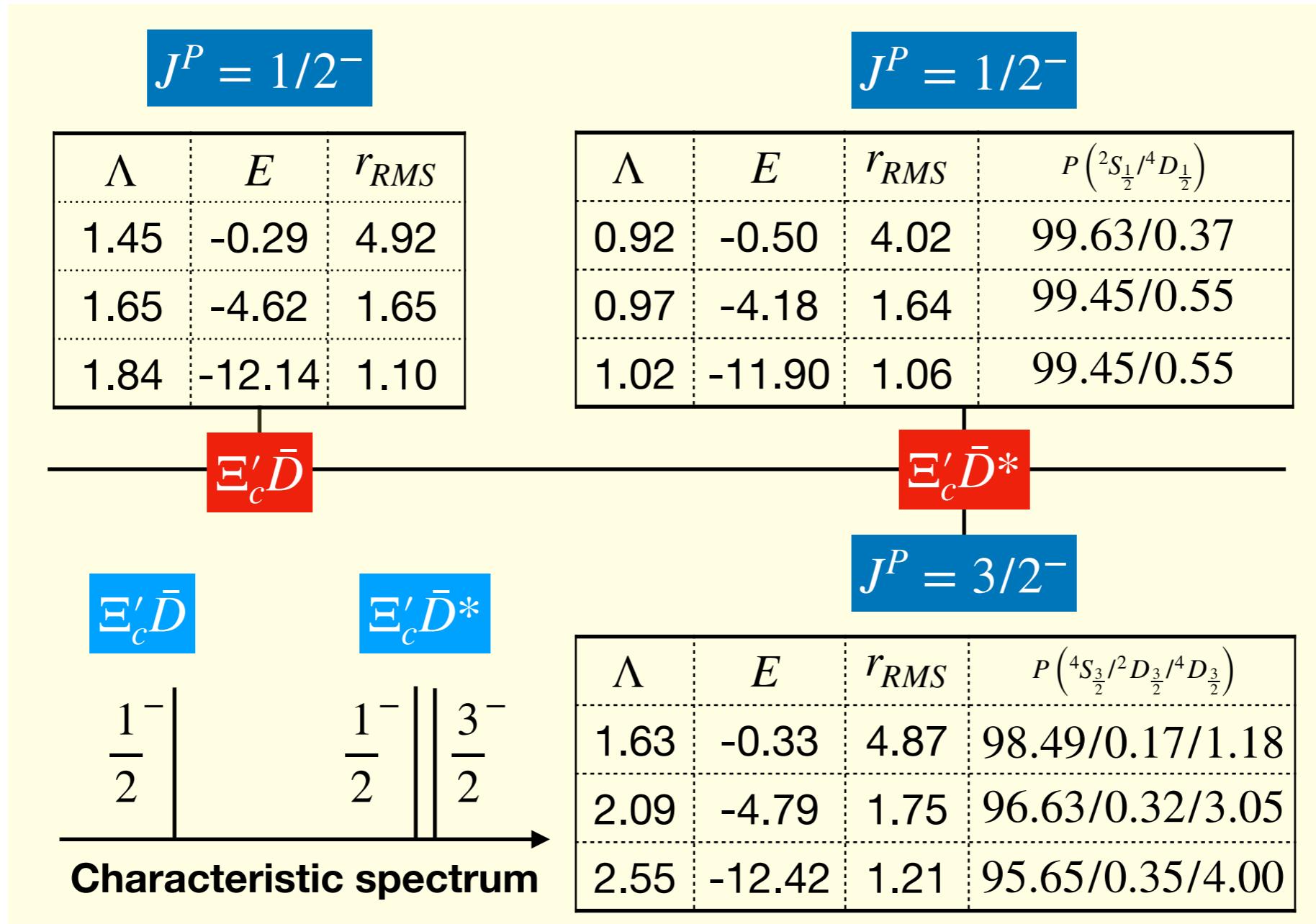
There exists mass degeneration for the S-wave isoscalar $\Xi_c \bar{D}^*$ states with $J^P = 1/2^-$ and $J^P = 3/2^-$ when adopting same cutoff value. Coupled-channel may result in the violation of mass degeneration.

Double-peak structure can be tested with more precise data



F.L. Wang, Xiang Liu, Phys.Lett.B 835(2022)137583

Similar behavior happen for the $\Xi_c' \bar{D}$ systems



F.L. Wang, Xiang Liu, Phys.Lett.B 835(2022)137583

2.

Abundant phenomena around tetraquark candidates

Tetraquark candidates

$J/\psi\pi^+$

$J/\psi K^+$

$J/\psi\phi$

$J/\psi J/\psi$

T_ψ^b (Z_c)

$T_{\psi\bar{s}}^\theta$ (Z_{cs})

$T_{\psi\phi}$ (X)

$T_{\psi\psi}$ ($T_{cc\bar{c}\bar{c}}$)

3900, 4430,...

4000, 4220,...

4140, 4274, 4500...

6900,...

$D^0 D^0 \pi^+$

$D^+ K^-$

$D_s^\pm \pi^+$

T_{cc}

T_{cs}

$T_{c\bar{s}}$

3874

2900

2900

LHCb proposal for the new name
convention of exotic hadrons
[arXiv:2206.15233]

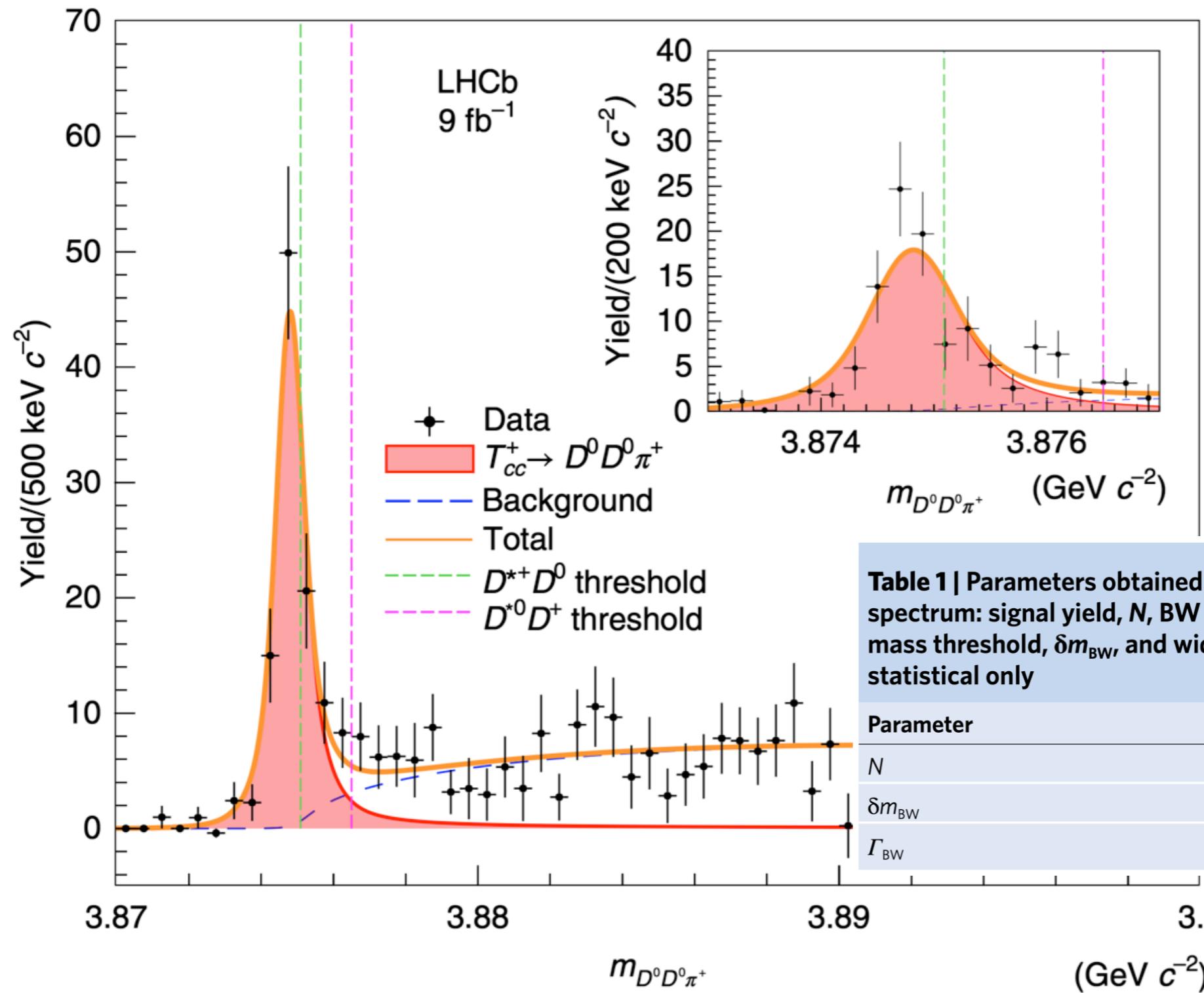


Table 1 | Parameters obtained from the fit to the $D^0 D^0 \pi^+$ mass spectrum: signal yield, N , BW mass relative to the $D^{*+} D^0$ mass threshold, δm_{BW} , and width, Γ_{BW} . The uncertainties are statistical only

Parameter	Value
N	117 ± 16
δm_{BW}	$-273 \pm 61 \text{ keV } c^{-2}$
Γ_{BW}	$410 \pm 165 \text{ keV}$

Coupled-channel analysis of the possible $D^{(*)}D^{(*)}$, $\bar{B}^{(*)}\bar{B}^{(*)}$ and $D^{(*)}\bar{B}^{(*)}$ molecular states

Ning Li,^{1,2,*} Zhi-Feng Sun,^{3,4,†} Xiang Liu,^{3,4,‡} and Shi-Lin Zhu^{1,5,6,§}

¹Department of Physics and State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing 100871, China

²Institut für Kernphysik and Jülich Center for Hadron Physics, Forschungszentrum Jülich, D-52425 Jülich, Germany

³School of Physical Science and Technology, Lanzhou University, Lanzhou 730000, China

⁴Research Center for Hadron and CSR Physics, Lanzhou University and Institute of Modern Physics of CAS, Lanzhou 730000, China

⁵Center of High Energy Physics, Peking University, Beijing 100871, China

⁶Collaborative Innovation Center of Quantum Matter, Beijing 100871, China

(Received 22 November 2012; revised manuscript received 17 September 2013; published 3 December 2013)

We perform a coupled-channel study of the possible deuteron-like molecules with two heavy flavor quarks, including the systems of $D^{(*)}D^{(*)}$ with double charm, $\bar{B}^{(*)}\bar{B}^{(*)}$ with double bottom, and $D^{(*)}\bar{B}^{(*)}$ with both charm and bottom, within the one-boson-exchange potential model. In our study, we take into account the S - D mixing which plays an important role in the formation of the loosely bound deuteron, and particularly, the coupled-channel effect in the flavor space. According to our results, the state $D^{(*)}D^{(*)}[I(J^P) = 0(1^+)]$ with double charm, the states $\bar{B}^{(*)}\bar{B}^{(*)}[I(J^P) = 0(1^+), 1(1^+)]$, $(\bar{B}^{(*)}\bar{B}^{(*)})_s[J^P = 1^+, 2^+]$ and $(\bar{B}^{(*)}\bar{B}^{(*)})_{ss}[J^P = 1^+, 2^+]$ with double bottom, and the states $D^{(*)}\bar{B}^{(*)}[I(J^P) = 0(1^+), 0(2^+)]$ with both charm and bottom might be good molecule candidates. However, the states $D^{(*)}D^{(*)}[I(J^P) = 0(2^+), 1(0^+), 1(1^+), 1(2^+)]$, $(D^{(*)}D^{(*)})_s[J^P = 0^+, 2^+]$ and $(D^{(*)}D^{(*)})_{ss}[J^P = 0^+, 1^+, 2^+]$ with double charm and the state $D^{(*)}\bar{B}^{(*)}[I(J^P) = 1(1^+)]$ with both charm and bottom are not supported to be

Binding energy

LHCb result of T_{cc}

-273 keV

Our prediction

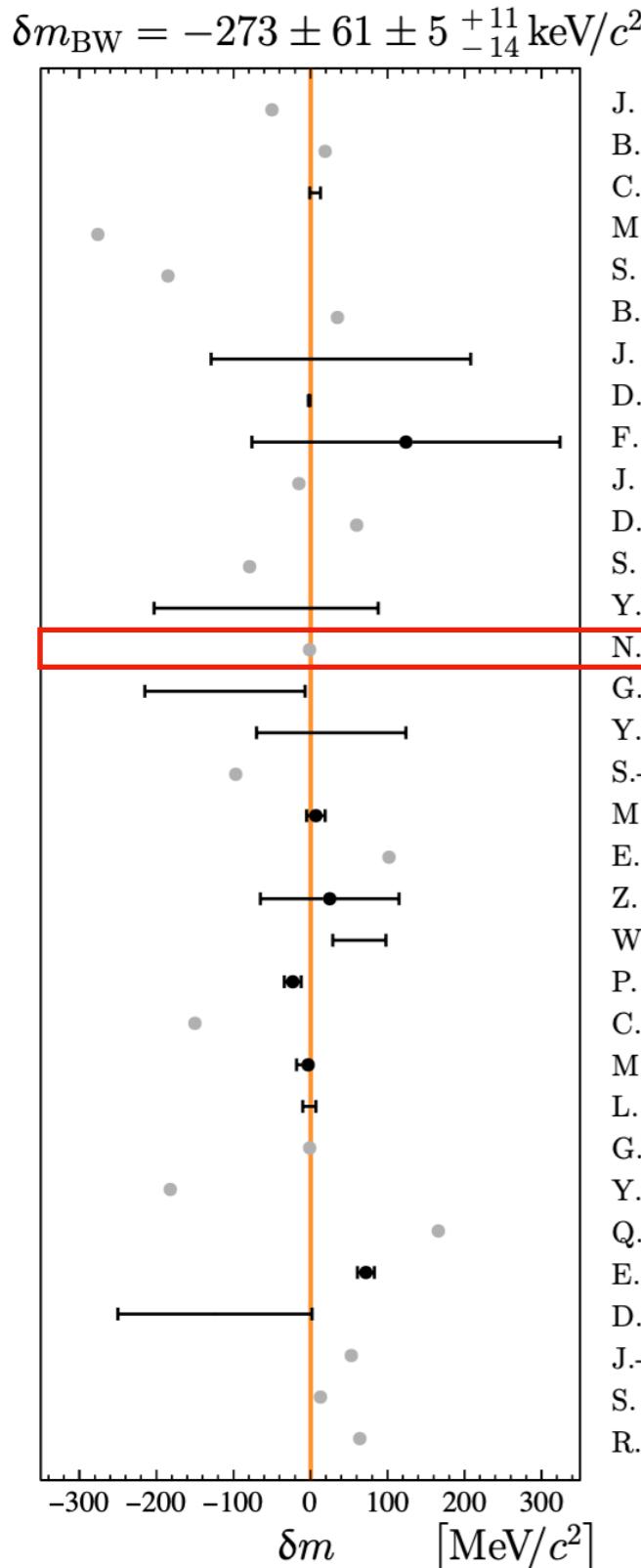
-470 keV

I	J^P	$D^{(*)}D^{(*)}$						OBE
		OPE						
0	0 ⁺	* * *						* * *
		Λ (GeV)	1.05	1.10	1.15	1.20	0.95	
		B.E. (MeV)	1.24	4.63	11.02	20.98	0.47	
		M (MeV)	3874.61	3871.22	3864.83	3854.87	3875.38	
		r_{rms} (fm)	3.11	1.68	1.12	0.84	4.46	
		P_1 (%)	96.39	92.71	88.22	83.34	97.97	
0	1 ⁺	* * *						0.15
		Λ (GeV)	1.05	1.10	1.15	1.20	0.95	
		B.E. (MeV)	1.24	4.63	11.02	20.98	0.47	
		M (MeV)	3874.61	3871.22	3864.83	3854.87	3875.38	
		r_{rms} (fm)	3.11	1.68	1.12	0.84	4.46	
		P_1 (%)	96.39	92.71	88.22	83.34	97.97	

Perfect $D\bar{D}^*$ molecular prediction matching the T_{cc} observation at LHCb

P_4 (%)	0.08	0.13	0.14	0.13	0.04	0.09	0.08	0.05
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9年前给出精准预测



Chinese Physics Letters

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EDITORS' SUGGESTION

Perfect DD^* Molecular Prediction Matching the T_{cc} Observation at LHCb

Ning Li, Zhi-Feng Sun, Xiang Liu, and Shi-Lin Zhu

Chin. Phys. Lett. 2021, 38 (9): 092001

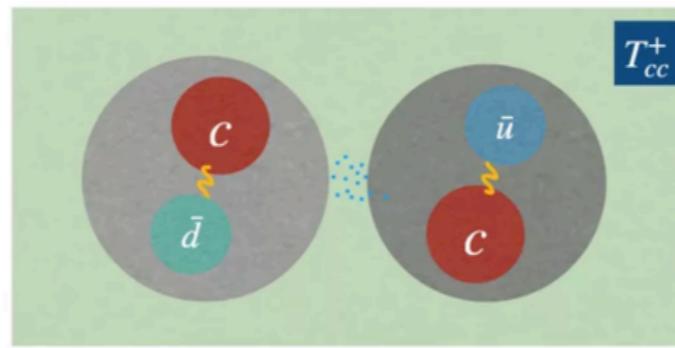
亮点介绍

最近，欧洲核子中心的LHCb实验通过研究质子与质子对撞产生的 $D^0D^0\pi^+$ 的不变质量谱，发现了名为 T_{cc}^+ 的窄共振态结构，其共振态参数和衰变行为与2012年李宁、孙志峰、刘翔和朱世琳发表在Phys. Rev. D 88 (2013) 114008的关于双粲分子态类型的四夸克态的理论预言非常吻合。作者回顾并评述了给出这一理论预言的历程，指出了 T_{cc}^+ 发现的重要物理意义，并对未来围绕 T_{cc}^+ 展开的研究工作进行了展望。

原文链接

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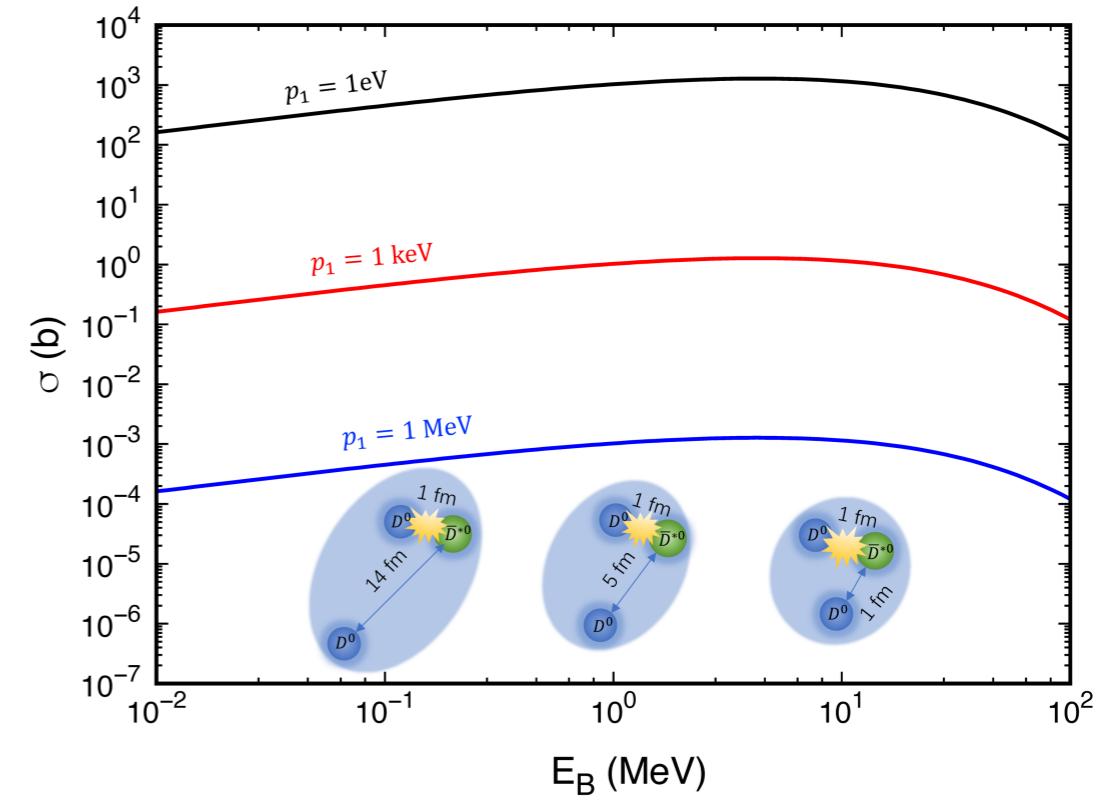
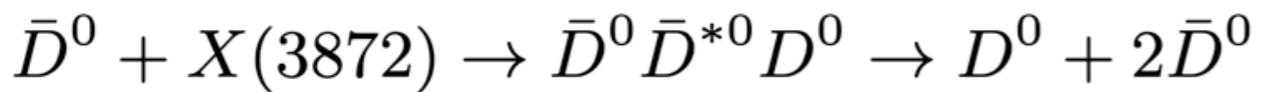
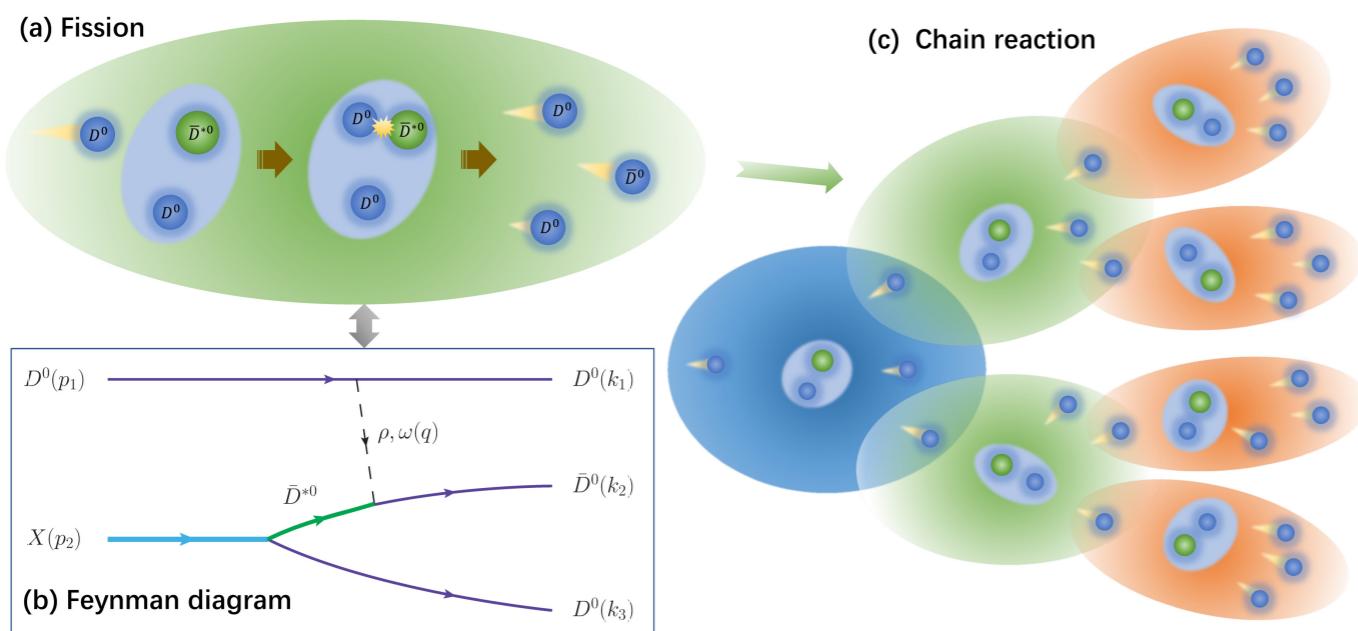
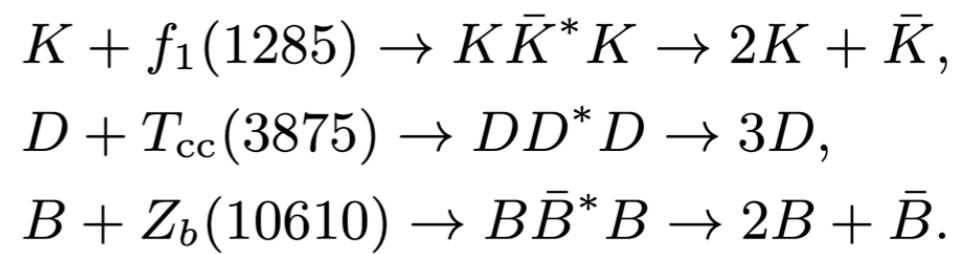


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Induced Fission-Like Process of Hadronic Molecular States

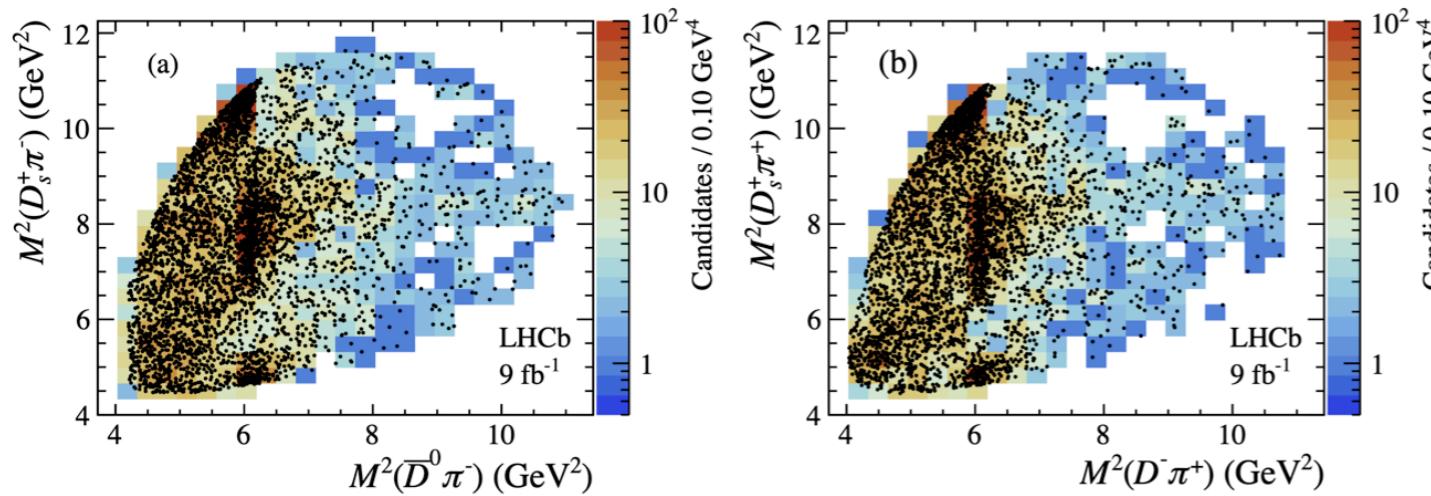
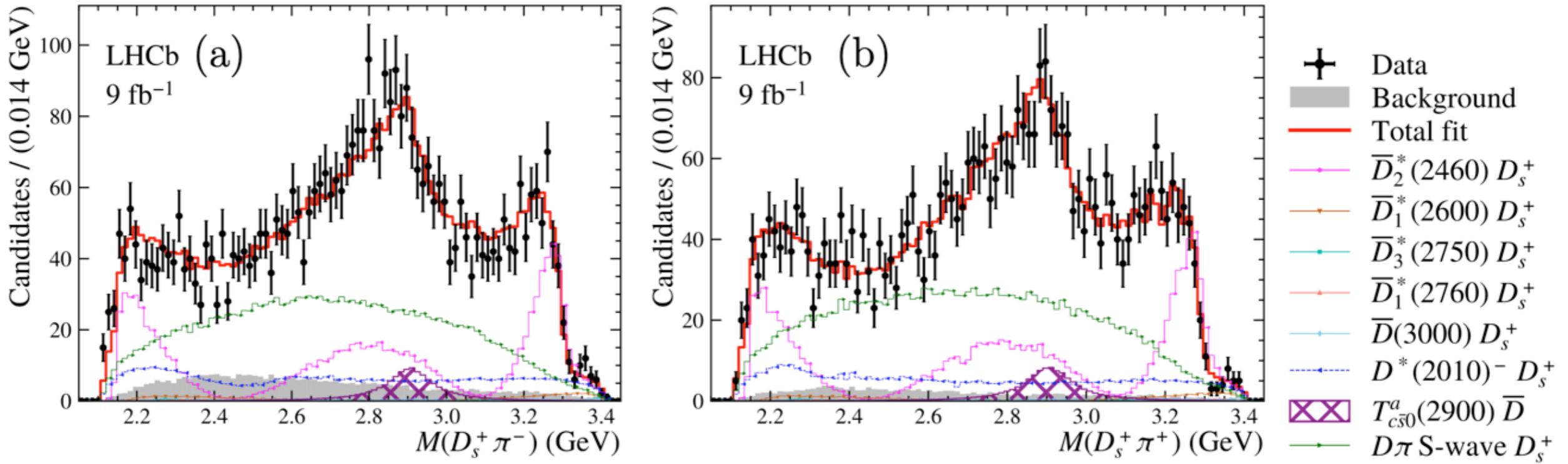
Jun He(何军)^{1,2}, Dian-Yong Chen(陈殿勇)^{2,3}, Zhan-Wei Liu(刘占伟)^{2,4}, and Xiang Liu(刘翔)^{2,4*}

We predict a new physical phenomenon, induced fission-like process and chain reaction of hadronic molecular states. As a molecular state, if induced by a D meson, the $X(3872)$ can split into $D\bar{D}$ final state which is forbidden due to the spin-parity conservation. The breeding of the D meson of the reaction, such as $D^0X(3872) \rightarrow D^0\bar{D}^0D^0$, makes the chain reaction of $X(3872)$ matter possible. We estimate the cross section of the D meson induced fission-like process of $X(3872)$ into two D mesons. With very small D^0 beam momentum of 1 eV, the total cross section reaches an order of 1000 b, and decreases rapidly with the increasing beam momentum. With the transition of D^* meson in molecular states to a D meson, the $X(3872)$ can release large energy, which is acquired by the final mesons. The momentum distributions of the final D mesons are analyzed. In the laboratory frame, the spectator D meson in molecular state concentrates in the low momentum area. The energy from the transition from D^* to D meson is mainly acquired by two scattered D mesons. The results suggest that the D meson environment will lead to the induced fission-like process and chain reaction of the $X(3872)$. Such a phenomenon can be extended to other hadronic molecular states.



$T_{c\bar{s}0}^a(2900)$

$B^0 \rightarrow \bar{D}^0 D_s^+ \pi^-$ $B^+ \rightarrow D^- D_s^+ \pi^+$



$T_{c\bar{s}0}^a(2900)^0 : M = 2.892 \pm 0.014 \pm 0.015$ GeV,
 $\Gamma = 0.119 \pm 0.026 \pm 0.013$ GeV,

$T_{c\bar{s}0}^a(2900)^{++} : M = 2.921 \pm 0.017 \pm 0.020$ GeV,
 $\Gamma = 0.137 \pm 0.032 \pm 0.017$ GeV,

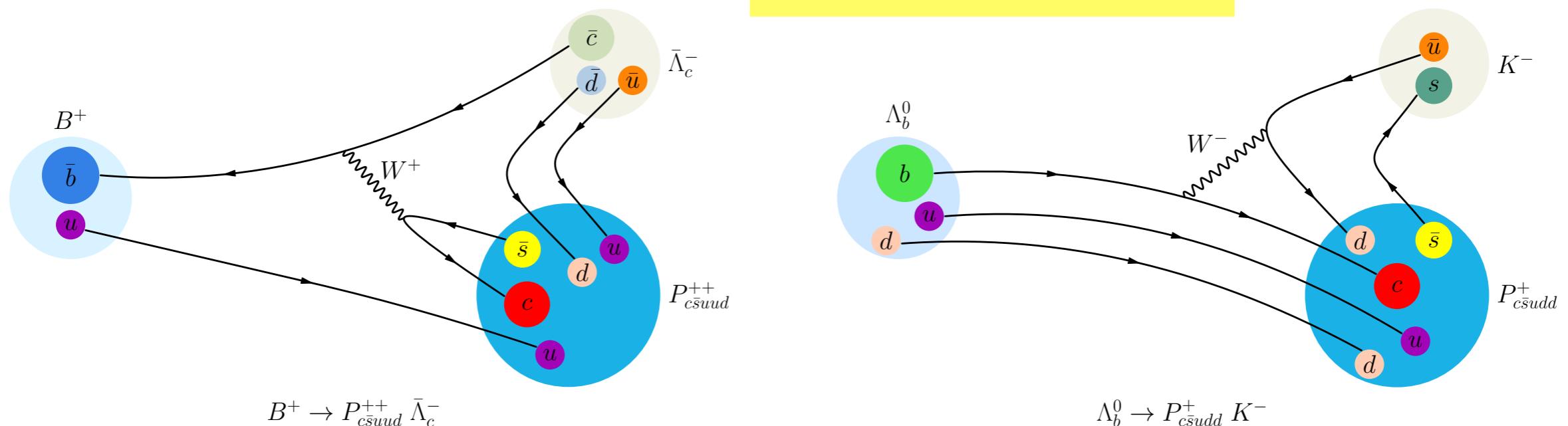
LHCb: arXiv:2212.02716; arXiv:2212.02717

Discovery of $T_{c\bar{s}0}^a(2900)^{0,++}$ implies new charmed-strange pentaquark system

Hong-Tao An,^{1,2,*} Zhan-Wei Liu^{1,2,3,†} Fu-Sheng Yu^{1,3,4,5,‡} and Xiang Liu^{1,2,3,§}

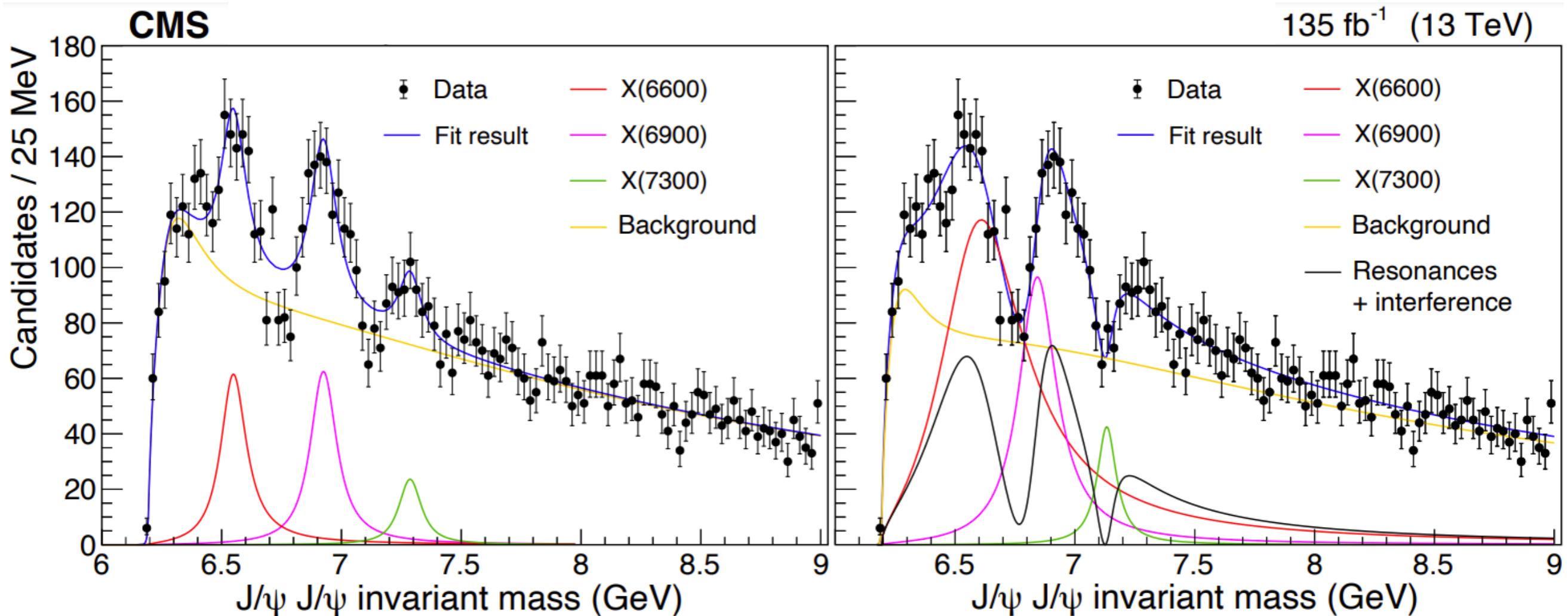
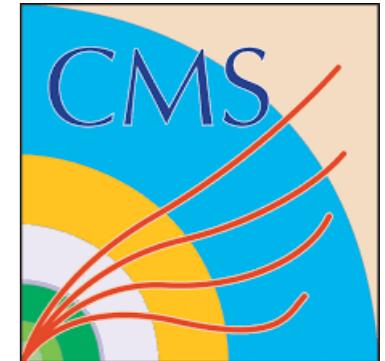
Inspired by the very recently discovered tetraquark states $T_{c\bar{s}0}^a(2900)^{0,++}$ from the LHCb Collaboration, we predict the existence of a new charmed-strange pentaquark system, $c\bar{s}nnn$, which is closely connected to $c\bar{s}n\bar{n}$ by exchanging \bar{n} into nn with $n = u, d$. Especially, it is suggested to experimentally search for the predicted new pentaquark system via the weak decays of B mesons or b baryons, with the support from the study of the mass spectrum and the decay properties. The predicted new pentaquark system must attract extensive attention from experimentalists and theorists when it constructs the “particle zoo 2.0” in the near future.

让我们拭目以待!



$T_{\psi\psi}$

More peaks in di- J/ψ invariant mass spectrum



CMS Collaboration: arXiv:2306.07164

$T_{\psi\psi}$

ATLAS is joining this party



arXiv: 2304.08962

di- J/ψ	model A	model B
m_0	$6.41 \pm 0.08^{+0.08}_{-0.03}$	$6.65 \pm 0.02^{+0.03}_{-0.02}$
Γ_0	$0.59 \pm 0.35^{+0.12}_{-0.20}$	$0.44 \pm 0.05^{+0.06}_{-0.05}$
m_1	$6.63 \pm 0.05^{+0.08}_{-0.01}$	—
Γ_1	$0.35 \pm 0.11^{+0.11}_{-0.04}$	—
m_2	$6.86 \pm 0.03^{+0.01}_{-0.02}$	$6.91 \pm 0.01 \pm 0.01$
Γ_2	$0.11 \pm 0.05^{+0.02}_{-0.01}$	$0.15 \pm 0.03 \pm 0.01$
$\Delta s/s$	$\pm 5.1\%^{+8.1\%}_{-8.9\%}$	—
$J/\psi + \psi(2S)$	model α	model β
m_3 or m	$7.22 \pm 0.03^{+0.01}_{-0.03}$	$6.96 \pm 0.05 \pm 0.03$
Γ_3 or Γ	$0.09 \pm 0.06^{+0.06}_{-0.03}$	$0.51 \pm 0.17^{+0.11}_{-0.10}$
$\Delta s/s$	$\pm 21\% \pm 14\%$	$\pm 20\% \pm 12\%$

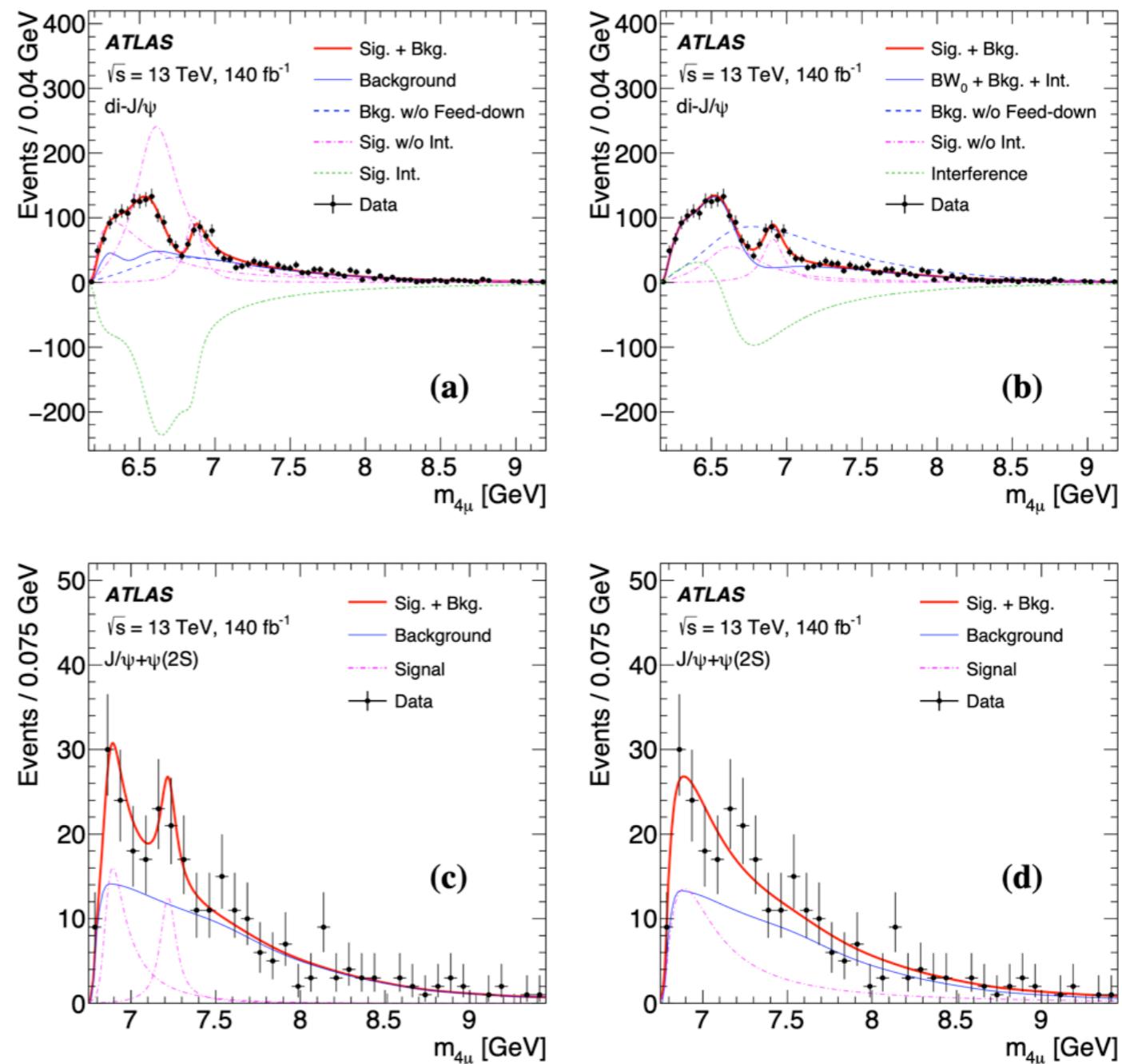
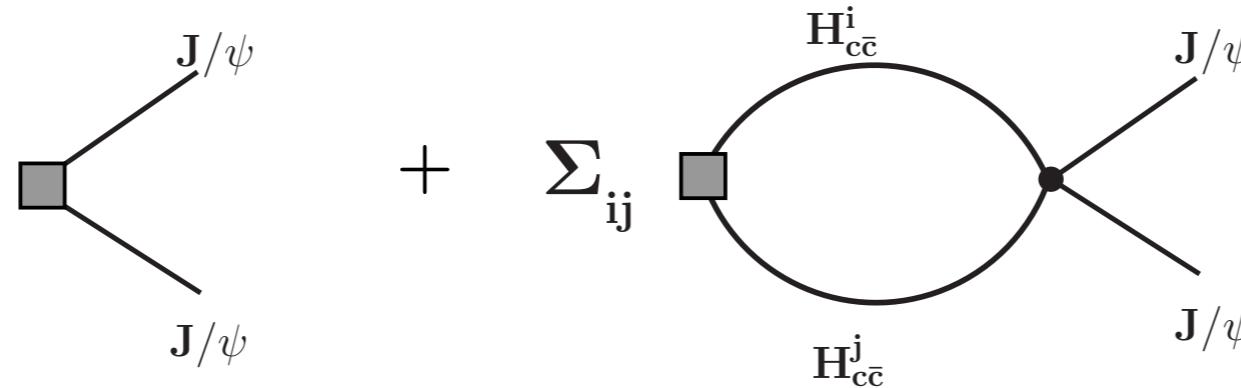


Figure 1: The fit to the mass spectra in the signal regions in the di- J/ψ (a,b) and $J/\psi + \psi(2S)$ (c,d) channels. Fit results for models A (a), B (b), α (c) and β (d) are shown. The purple dash-dotted lines represent the components of individual resonances, and the green short dashed ones represent the interferences among them.

Dynamical rescattering mechanism to produce the fully charm peak structures



$$\begin{aligned} \mathcal{A}^2 = & | \mathcal{A}_{direct}(m_{J/\psi J/\psi}) + \sum_{mn} e^{i\phi^{mn}} \mathcal{A}_{mn}(m_{J/\psi J/\psi}) |^2 \\ & + | \mathcal{A}'_{direct}(m_{J/\psi J/\psi}) + \sum_{mn} e^{i\phi^{mn}} \mathcal{A}'_{mn}(m_{J/\psi J/\psi}) |^2 \end{aligned}$$

$$\mathcal{A}_{direct}^2 = g_{direct}^2 e^{c_0 m_{ij}} \frac{1}{8\pi} \frac{\sqrt{\lambda(m_{ij}^2, m_i^2, m_j^2)}}{m_{ij}^2},$$

$$\mathcal{A}_{ij}^2(m_{J/\psi J/\psi}) = g_{ij}^2 L_{ij}^2(m_{J/\psi J/\psi}) \frac{e^{c_0 m_{J/\psi J/\psi}} p_{J/\psi}}{m_{J/\psi J/\psi}},$$

$$L_{ij}(m_{J/\psi J/\psi}) = \int \frac{dq^4}{(2\pi)^4} \frac{e^{-(2\vec{q})^2/\alpha^2}}{(q^2 - m_i^2 + i\epsilon)((P - q)^2 - m_j^2 + i\epsilon)} \\ = \frac{i}{4m_i m_j} \left\{ \frac{-\mu\alpha}{\sqrt{2}(2\pi)^{3/2}} + \frac{\mu\sqrt{2\mu m_0} \left(\text{erfi} \left[\frac{\sqrt{8\mu m_0}}{\alpha} \right] - i \right)}{2\pi/e^{-\frac{8\mu m_0}{\alpha^2}}} \right\}$$

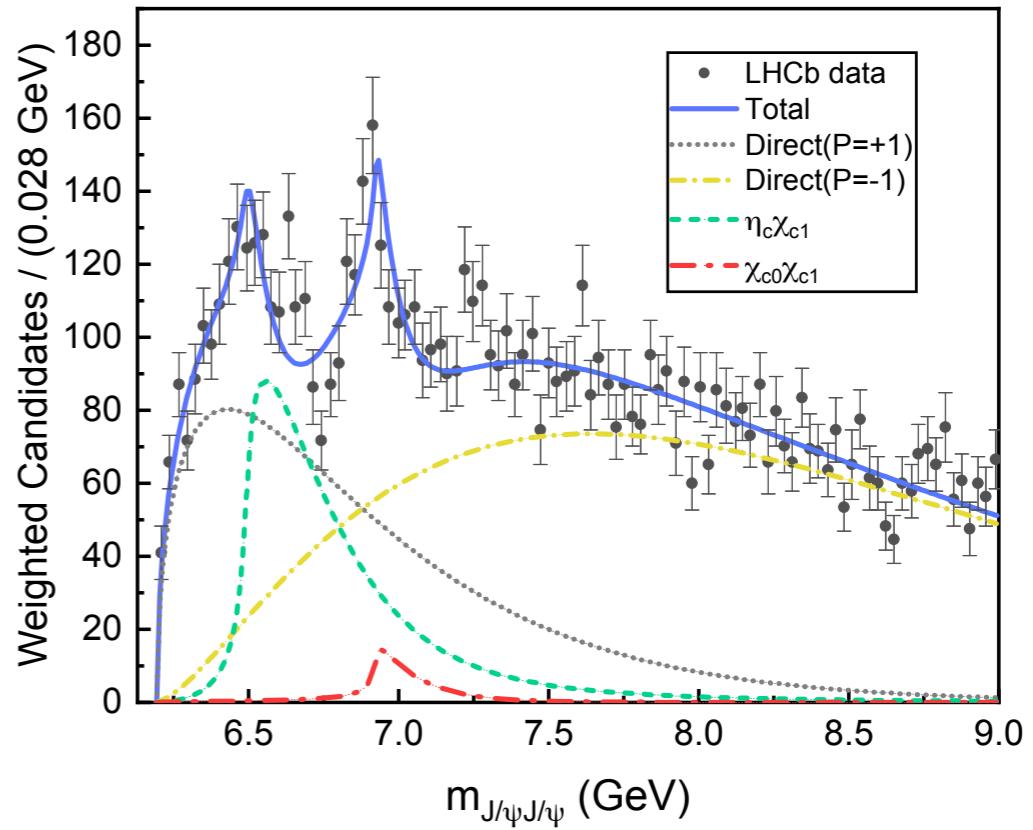
J.Z. Wang, D.Y. Chen, Xiang Liu and T. Matsuki, PRD 103 (2021) L071503
 J.Z. Wang, Xiang Liu, PRD 106 (2022) 054015

TABLE I. The parameters for reproducing the line shape of LHCb data with $\chi_{c1}\eta_c$ and $\chi_{c0}\chi_{c1}$ rescattering contributions. In this scenario, we set the parameter $\alpha_{\chi_{c1}\eta_c} = \alpha_{\chi_{c0}\chi_{c1}} = \alpha$.

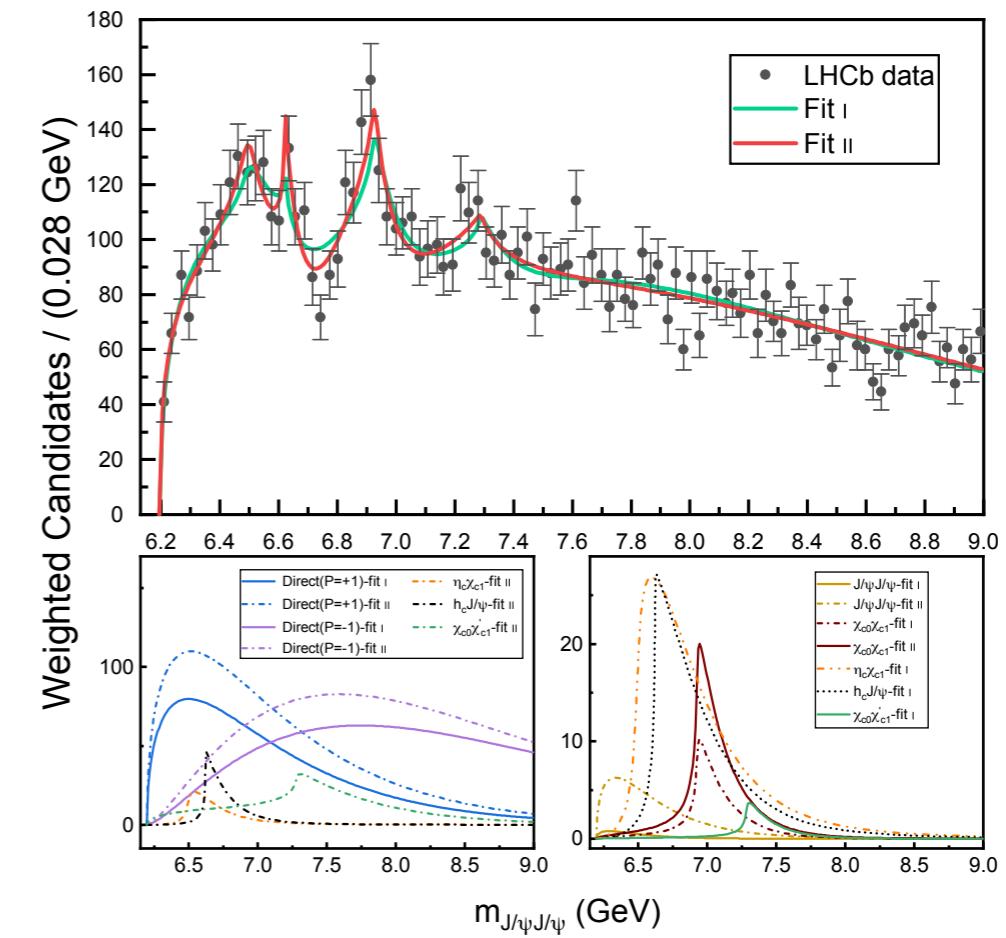
Parameter	Value	Parameter	Value
c_0	-1.99 ± 0.01	c'_0	-1.02 ± 0.04
$ g'_{\text{direct}}/g_{\text{direct}} $	0.0232 ± 0.0037	$ g_{\eta_c\chi_{c1}}/g'_{\text{direct}} $	198 ± 46
$ g_{\chi_{c0}\chi_{c1}}/g_{\text{direct}} $	55.9 ± 8.2	$\phi_{\eta_c\chi_{c1}}$	3.22 ± 0.07
$\phi_{\chi_{c0}\chi_{c1}}$	1.87 ± 0.16	α	1.40 ± 0.10

TABLE II. The parameters for reproducing the line shape of LHCb data in two fitting schemes of Fit I and Fit II.

Parameters	Fit I	Fit II
c_0 (GeV $^{-1}$)	-1.52 ± 0.02	-1.45 ± 0.01
c'_0 (GeV $^{-1}$)	-0.946 ± 0.058	-1.05 ± 0.01
$ g'_{\text{direct}}/g_{\text{direct}} $	0.0767 ± 0.0204	0.137 ± 0.042
$ g_{J/\psi J/\psi}/g_{\text{direct}} $	8.53 ± 3.64	14.0 ± 1.4
$ g_{\eta_c\chi_{c1}}/g'_{\text{direct}} $	91.6 ± 75.4	112 ± 28
$ g_{J/\psi h_c}/g'_{\text{direct}} $	69.7 ± 16.1	109 ± 8
$ g_{\chi_{c0}\chi_{c1}}/g_{\text{direct}} $	33.3 ± 8.2	38.5 ± 7.6
$ g_{\chi_{c0}\chi'_{c1}}/g_{\text{direct}} $	25.8 ± 10.6	19.0 ± 4.3
$\phi_{J/\psi J/\psi}$ (rad)	1.53 ± 0.51	3.16 ± 0.19
$\phi_{\eta_c\chi_{c1}}$ (rad)	2.69 ± 0.20	2.80 ± 0.15
$\phi_{J/\psi h_c}$ (rad)	4.40 ± 0.33	2.95 ± 0.24
$\phi_{\chi_{c0}\chi_{c1}}$ (rad)	2.14 ± 0.18	2.89 ± 0.20
$\phi_{\chi_{c0}\chi'_{c1}}$ (rad)	2.00 ± 0.33	3.23 ± 0.20
$\alpha_{J/\psi J/\psi}$ (GeV)	1.71 ± 0.01	2.30 ± 0.21
$\alpha_{\eta_c\chi_{c1}}$ (GeV)	1.71 ± 0.01	1.20 ± 0.21
$\alpha_{J/\psi h_c}$ (GeV)	1.71 ± 0.01	1.20 ± 0.03
$\alpha_{\chi_{c0}\chi_{c1}}$ (GeV)	1.71 ± 0.01	1.73 ± 0.26
$\alpha_{\chi_{c0}\chi'_{c1}}$ (GeV)	1.71 ± 0.01	5.20 ± 0.05
$\chi^2/\text{d.o.f.}$	1.41	1.25



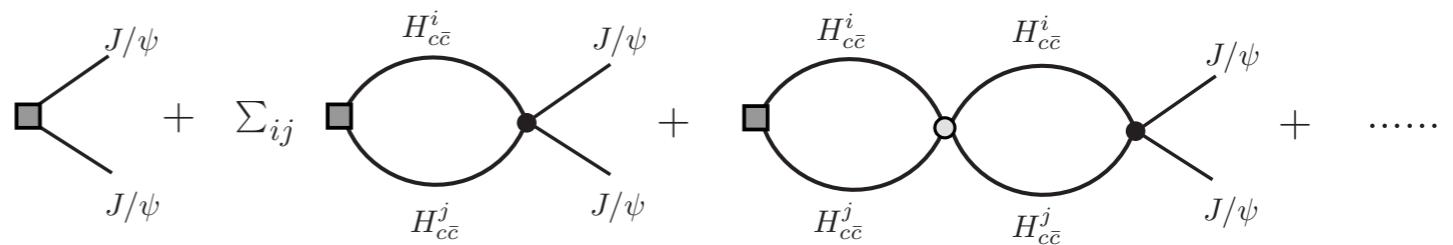
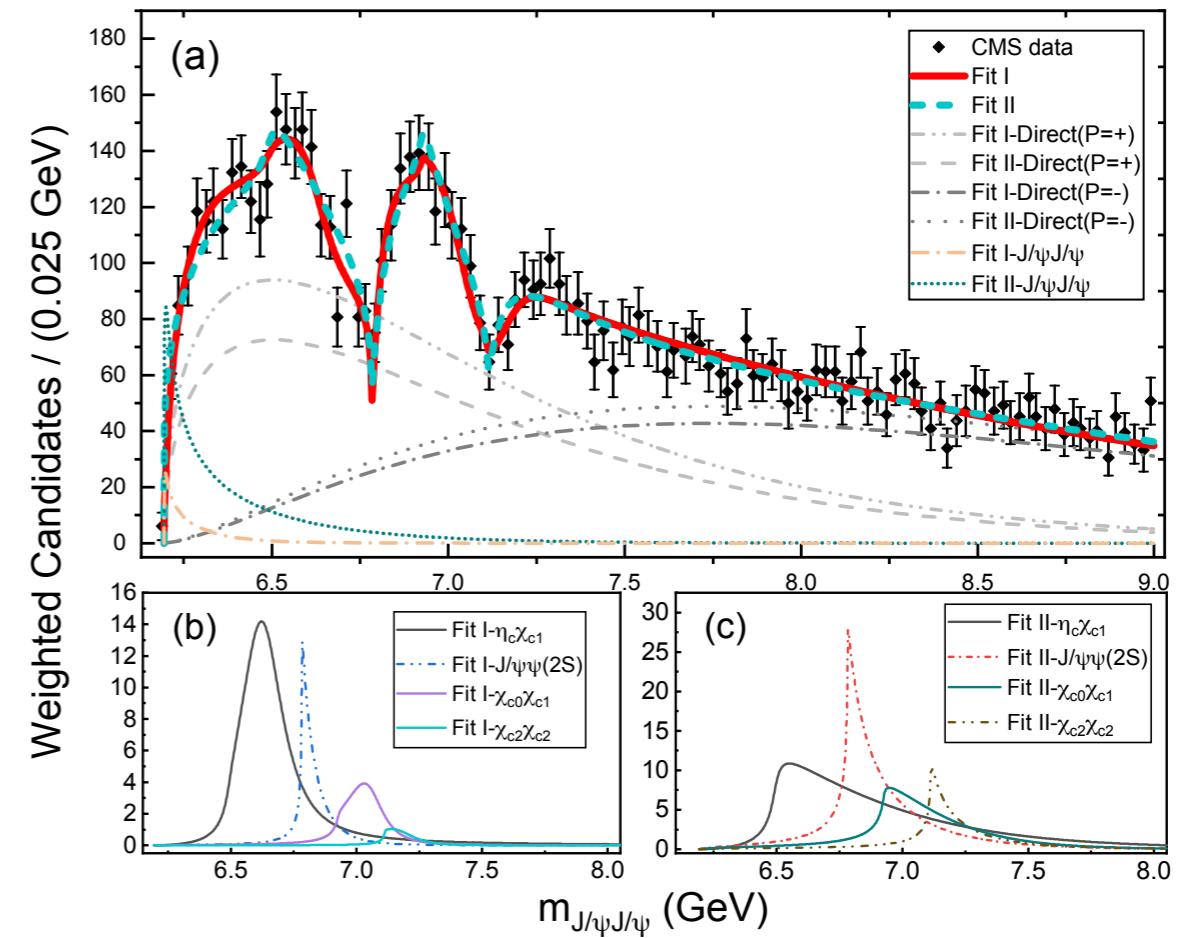
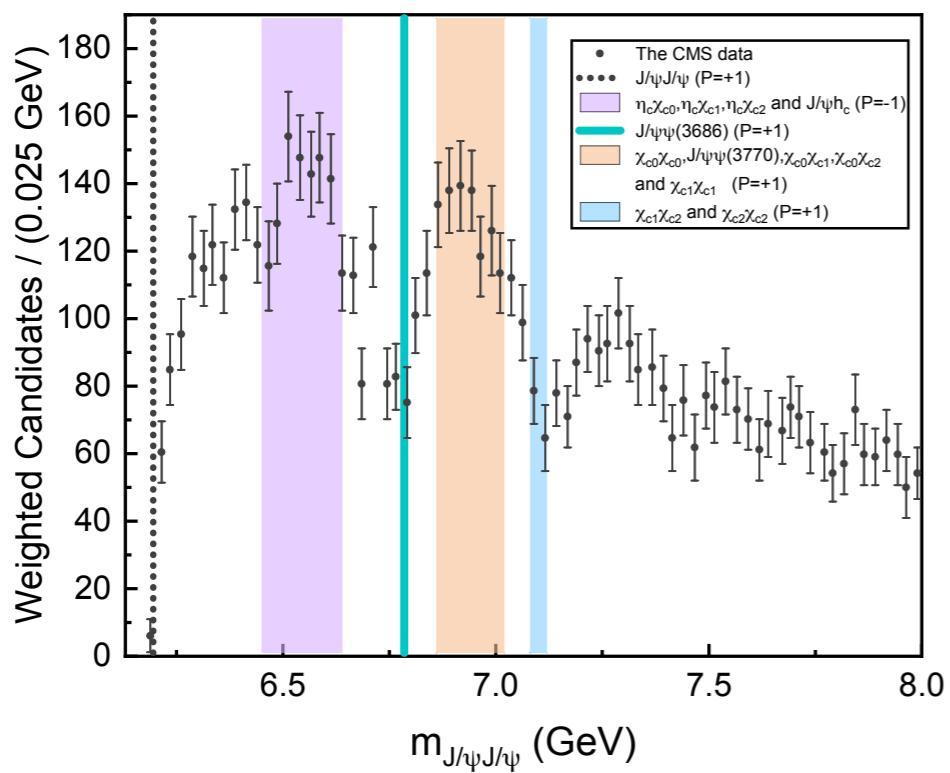
Reproduce the LHCb data well



Reproduce the CMS data well!

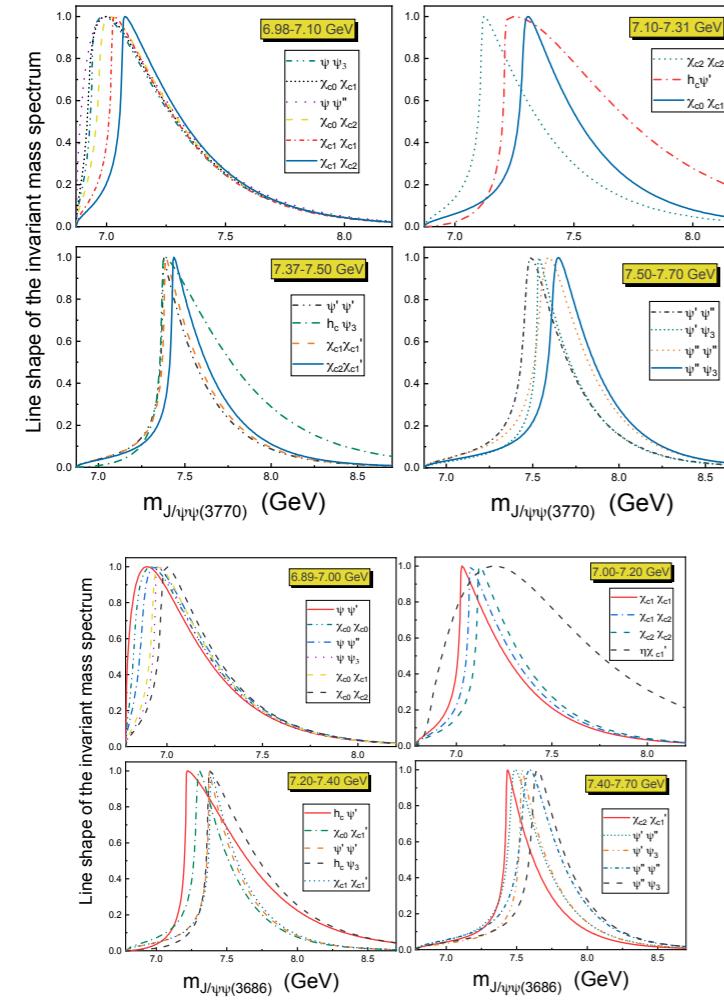
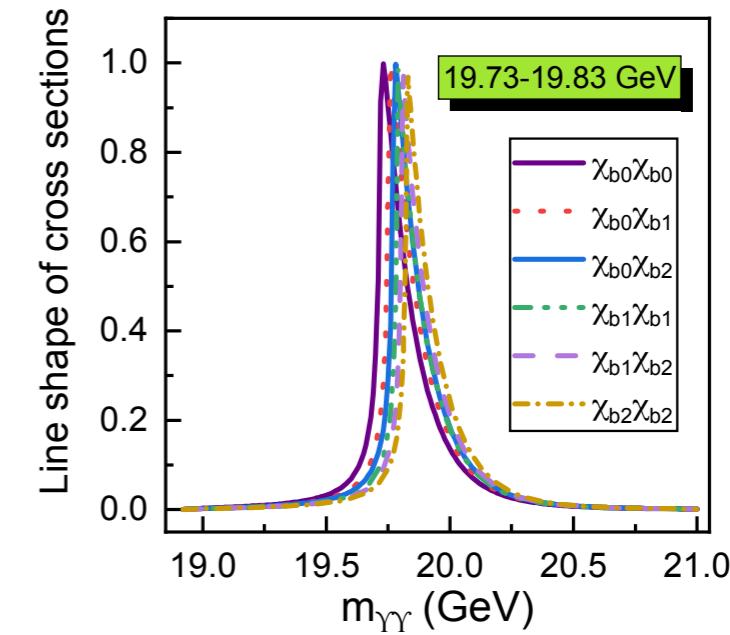
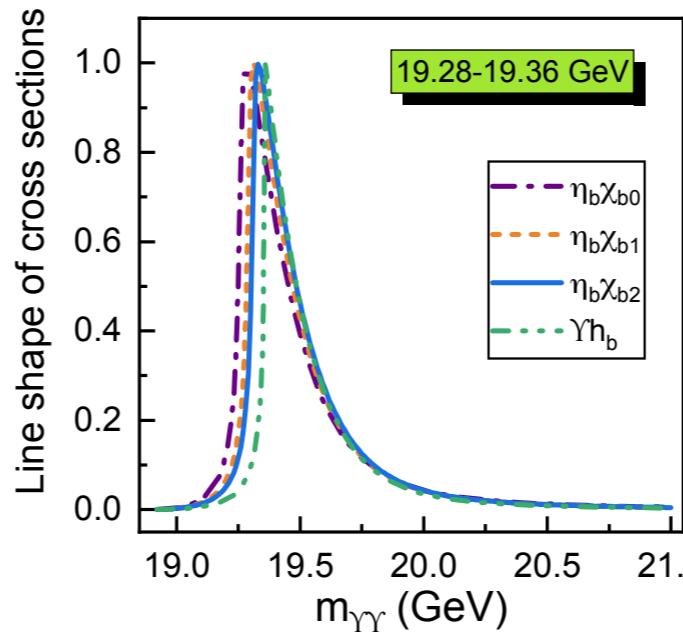
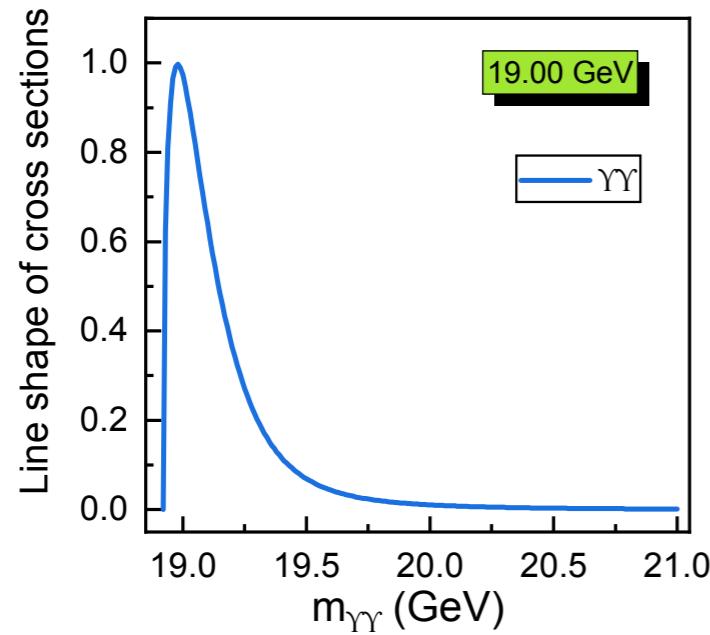
TABLE I. The fitted parameters for reproducing the line shape of the CMS data within the fit-I and fit-II schemes.

Parameters	Fit I	Fit II
$ g'_{\text{direct}}/g_{\text{direct}} $	0.0575 ± 0.0009	0.0699 ± 0.0010
$g_{\eta_c \chi_{c1}}/g_{\text{direct}}$	125 ± 26	28.2 ± 2.7
$g_{J/\psi\psi(3686)}/g_{\text{direct}}$	-26.1 ± 4.7	-16.4 ± 1.7
$g_{\chi_{c0}\chi_{c1}}/g_{\text{direct}}$	32.9 ± 5.8	16.2 ± 1.4
$g_{\chi_{c2}\chi_{c2}}/g_{\text{direct}}$	-15.3 ± 6.1	-12.3 ± 1.4
$\mathcal{C}_{J/\psi J/\psi}$	-144 ± 14	-82.3 ± 1.8
$\mathcal{C}_{\eta_c \chi_{c1}}$	342 ± 107	-21.3 ± 18.7
$\mathcal{C}_{J/\psi\psi(3686)}$	-20 ± 40	-32.0 ± 5.5
$\mathcal{C}_{\chi_{c0}\chi_{c1}}$	380 ± 54	20.0 ± 50.6
$\mathcal{C}_{\chi_{c2}\chi_{c2}}$	145 ± 175	-41.4 ± 13.3
α (GeV)	0.871 ± 0.046	1.813 ± 0.030
$\chi^2/\text{d.o.f.}$	0.657	0.699



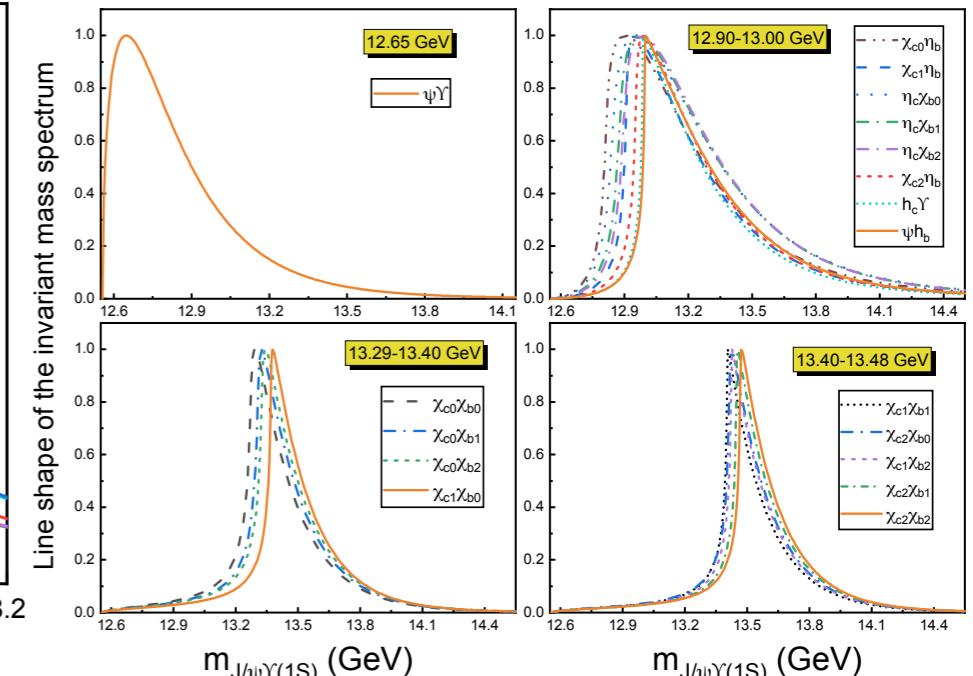
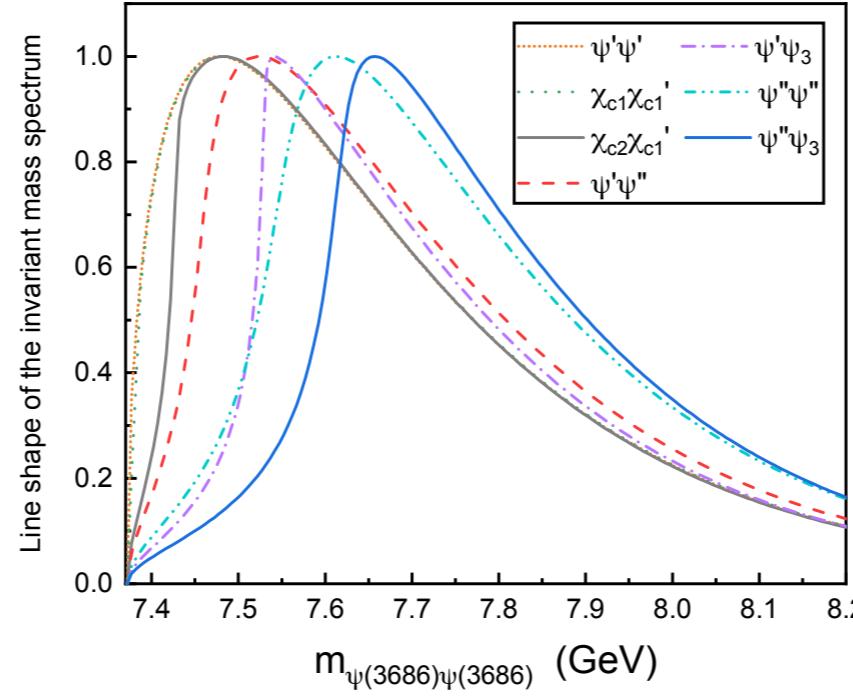
J.Z. Wang, Xiang Liu, PRD 106 (2022) 054015

Predictions for the peak line shape in di- Υ invariant mass spectrum



J.Z. Wang, D.Y. Chen, Xiang Liu and T. Matsuki, PRD 103 (2021) L071503

More predictions



J.Z. Wang, Xiang Liu and T. Matsuki, PLB 816 (2021) 136209

3.

**Pay more attentions to the study
of light hadron spectroscopy**

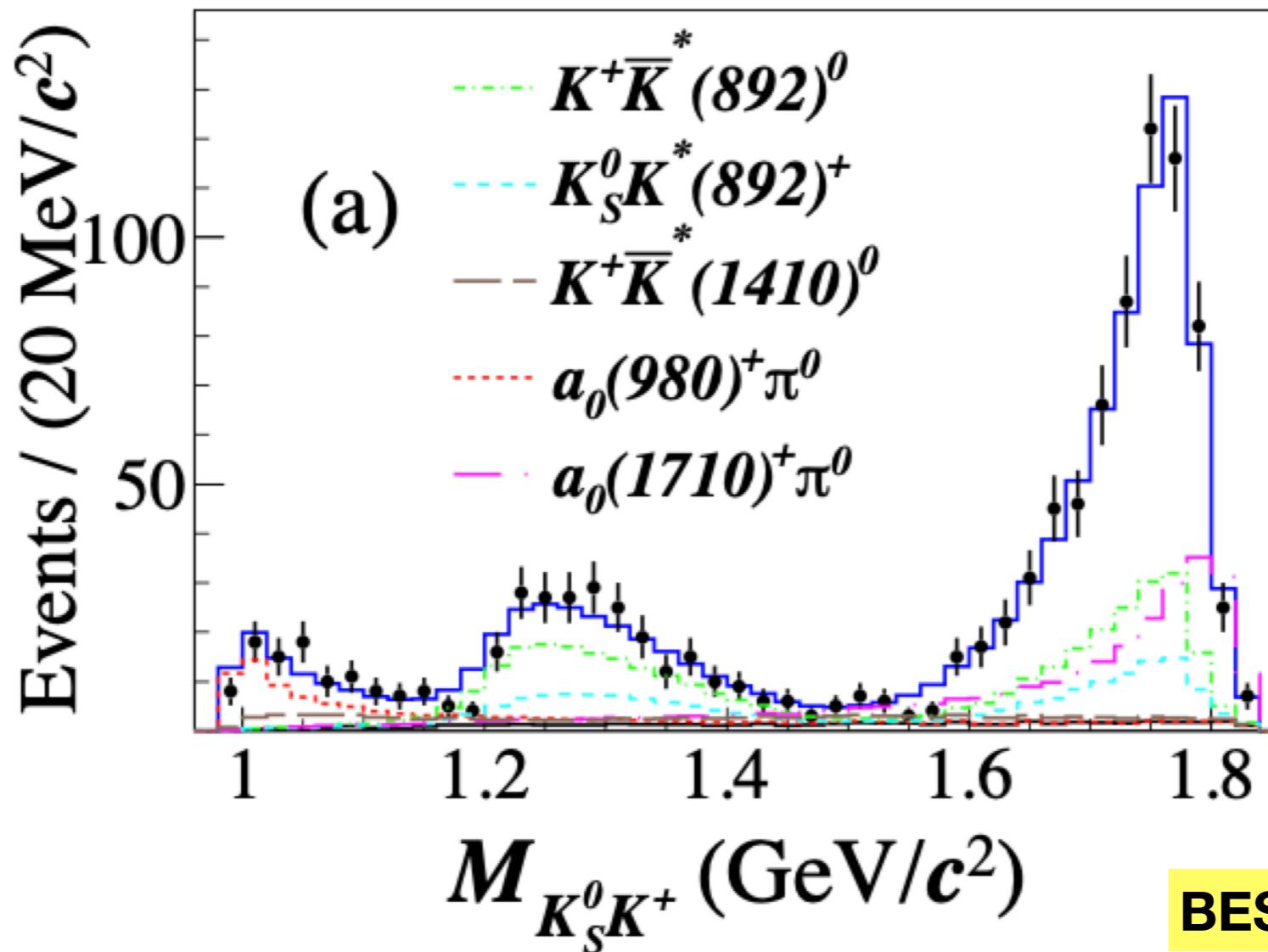


Observation of $\underline{a_0(1710)^+} \rightarrow K_S^0 K^+$ in study of the $D_s^+ \rightarrow K_S^0 K^+ \pi^0$ decay

Challenge for $f_0(1710)$ as glueball

$$M = 1.817 \pm 0.008(\text{stat}) \pm 0.020(\text{syst}) \text{ GeV}$$

$$\Gamma = 0.097 \pm 0.022(\text{stat}) \pm 0.015(\text{syst}) \text{ GeV}$$



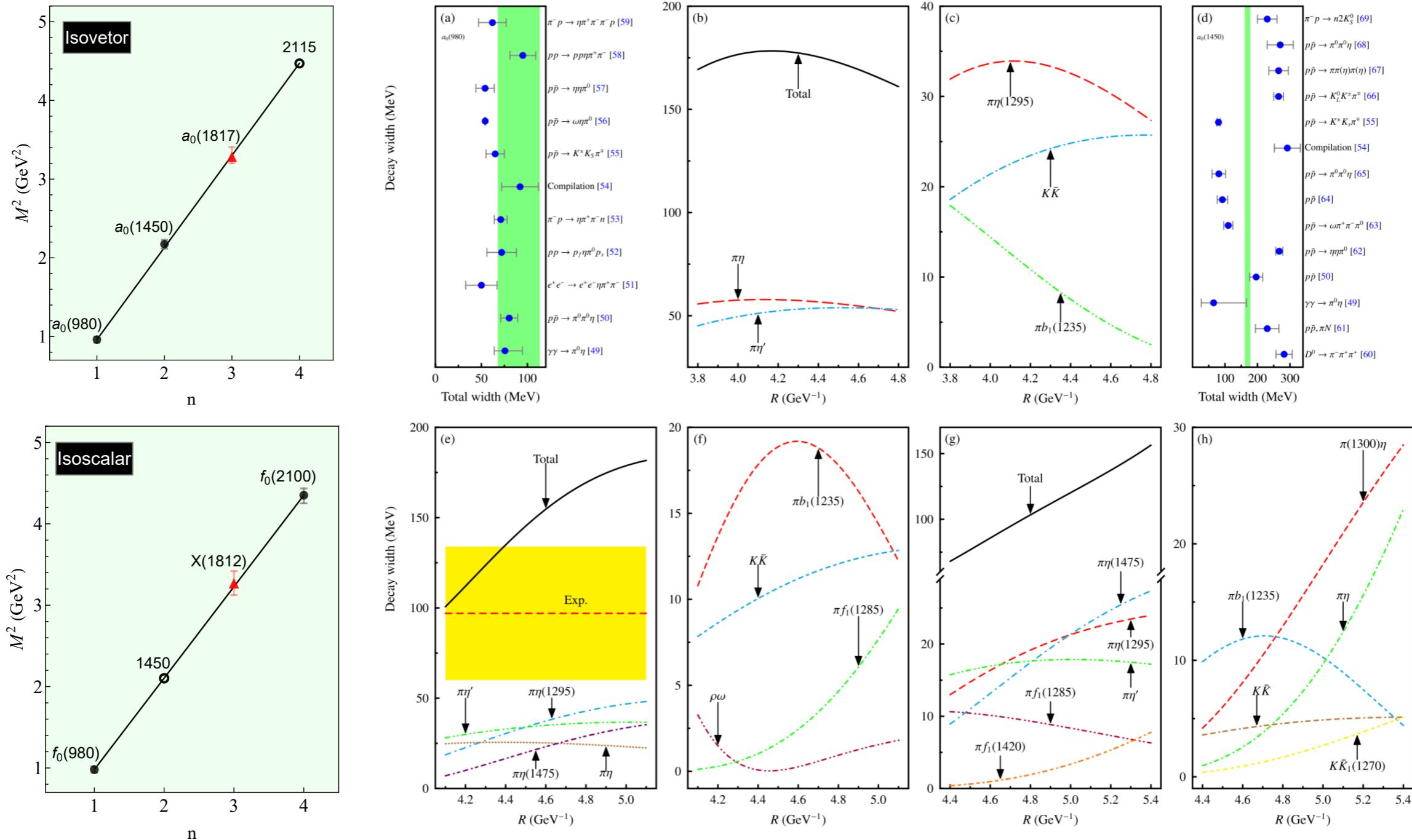
BESIII

BESIII, arXiv:2204.09614

It is safe to assign $f_0(1710)$ as glueball

Newly observed $a_0(1817)$ as the scaling point of constructing the scalar meson spectroscopy

Dan Guo^{1,2,*}, Wei Chen^{3,†}, Hua-Xing Chen^{5,‡}, Xiang Liu^{1,2,3,7,§}, and Shi-Lin Zhu^{6,||}



Construct light hadron spectroscopy always on the road

PHYSICAL REVIEW D **107**, 072001 (2023)

**Study of the reactions $e^+e^- \rightarrow K^+K^-\pi^0\pi^0\pi^0$, $e^+e^- \rightarrow K_S^0K^\pm\pi^\mp\pi^0\pi^0$,
and $e^+e^- \rightarrow K_S^0K^\pm\pi^\mp\pi^+\pi^-$ at center-of-mass energies
from threshold to 4.5 GeV using initial-state radiation**

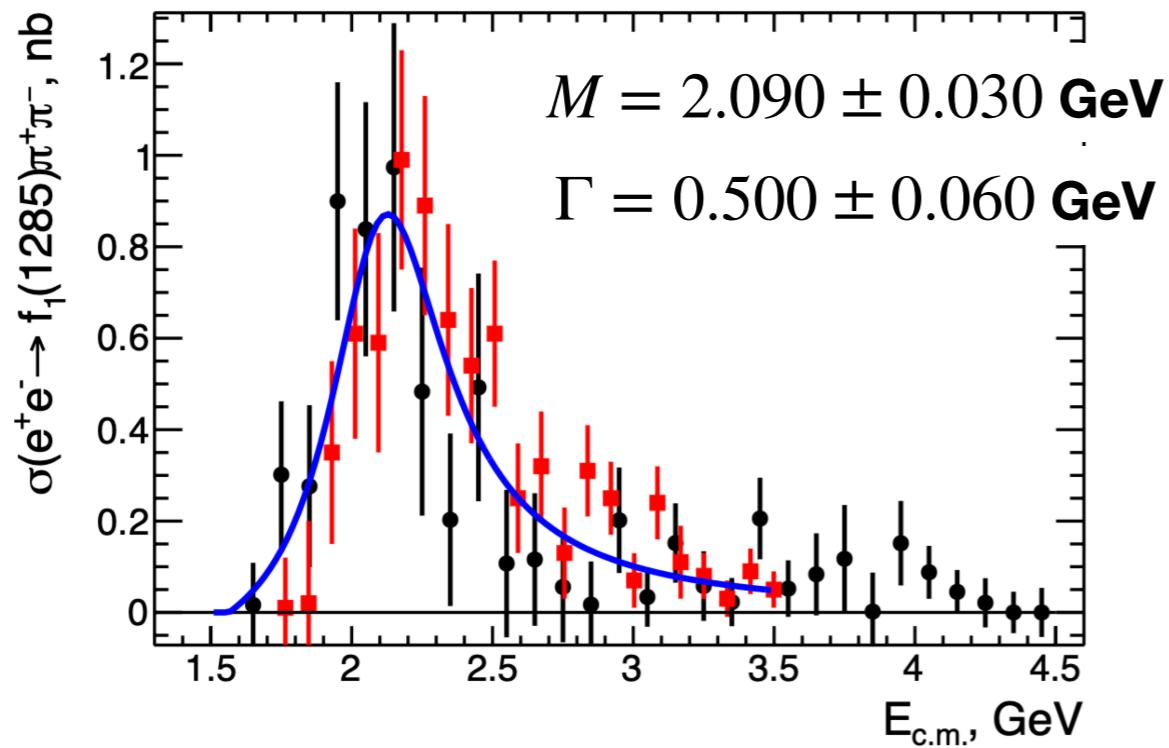
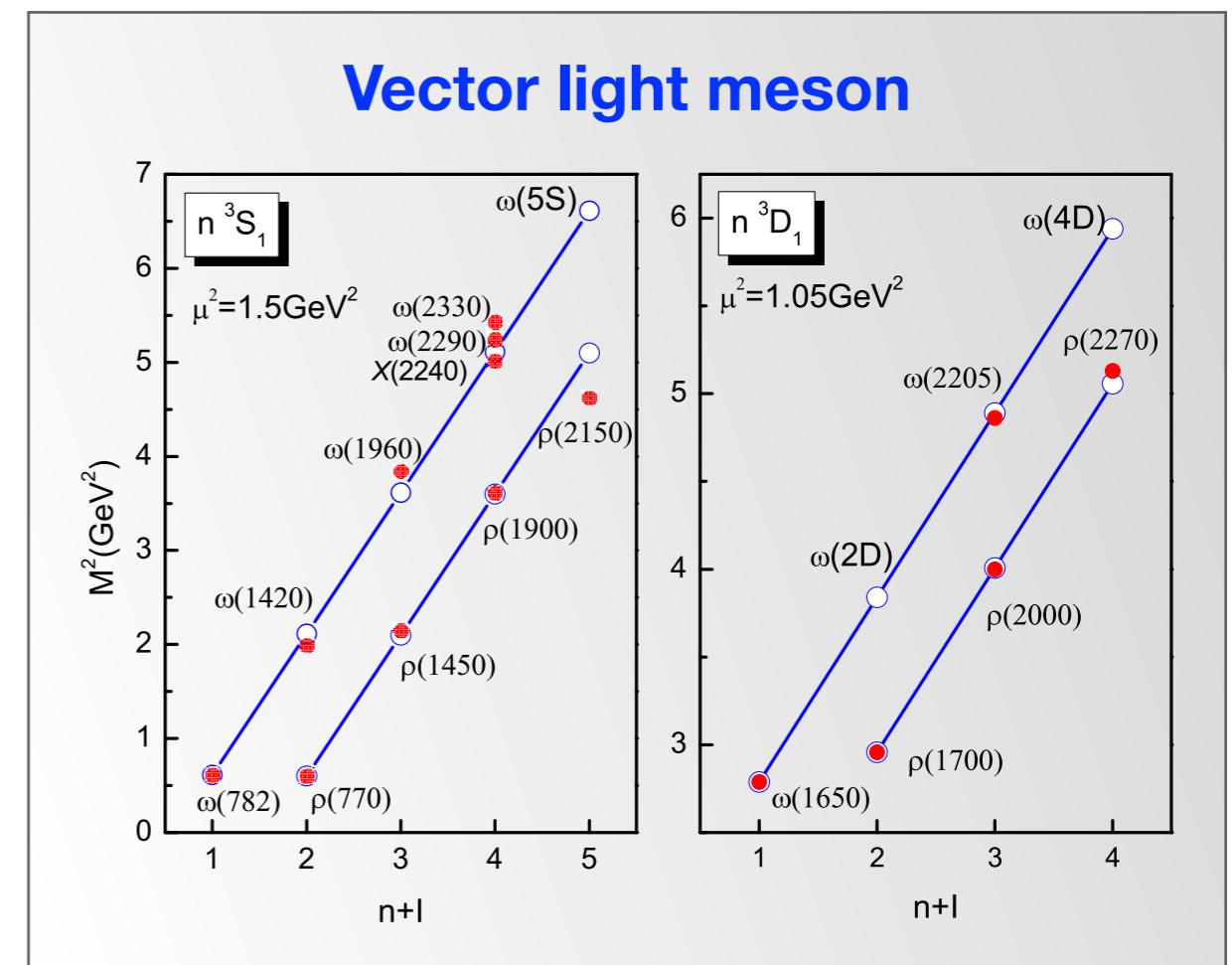


FIG. 13: The measured $e^+e^- \rightarrow f_1(1285)\pi^+\pi^-$ cross section from the present analysis (dots) in comparison with previous measurement (squares) [12]. The solid curve is fit explained in the text.



Our knowledge of light hadron spectroscopy is helpful to establish exotic states

Model with only K^*

$P_{\psi S}^\Lambda(4338)$



Amplitude contributions:

- NR($\bar{p}\Lambda$)
- $K_{2,3,4}^*$ → peaks out of phsp, no obvious contribution in $\bar{p}\Lambda$ distribution

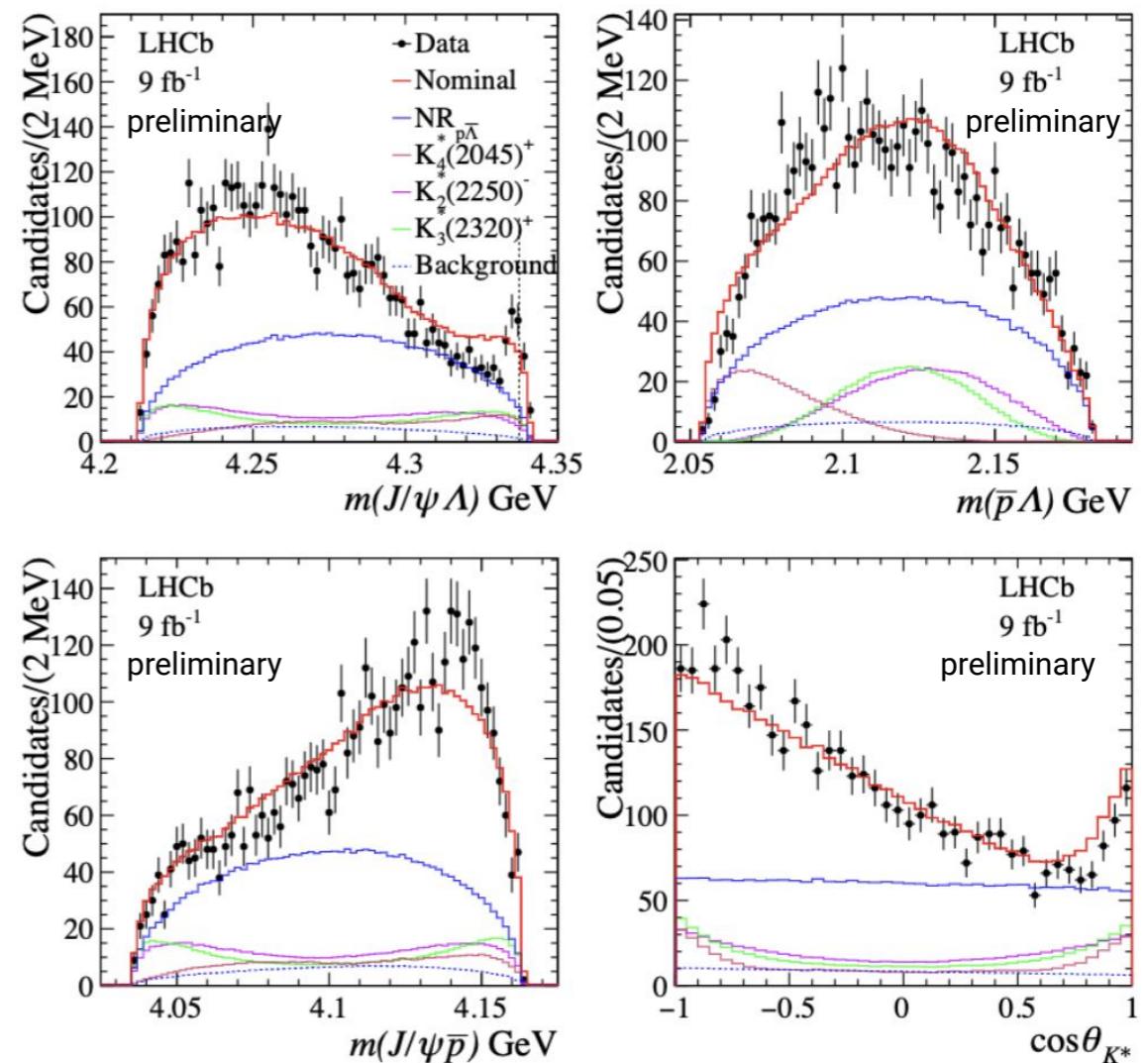
Resonance	Mass (MeV)	Natural width (MeV)	J^P
$K_4^*(2045)^+$	2045 ± 9	198 ± 30	4^+
$K_2^*(2250)^+$	2247 ± 17	180 ± 30	2^-
$K_3^*(2320)^+$	2324 ± 24	150 ± 30	3^+

PDG 2020

Model with K^* cannot describe data

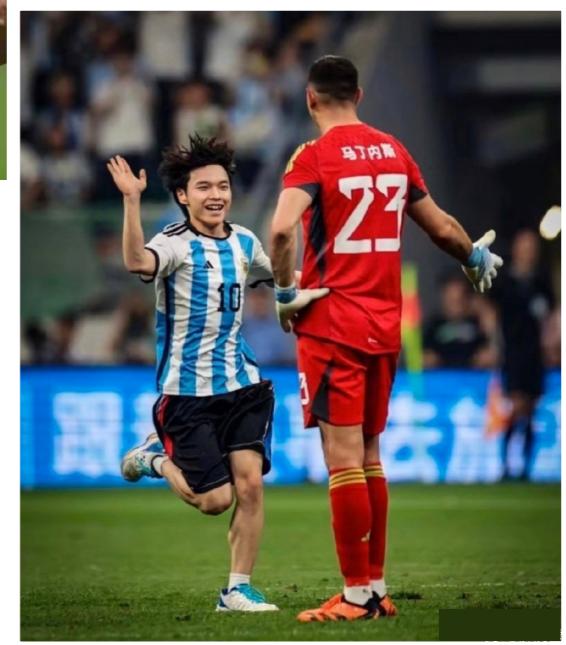
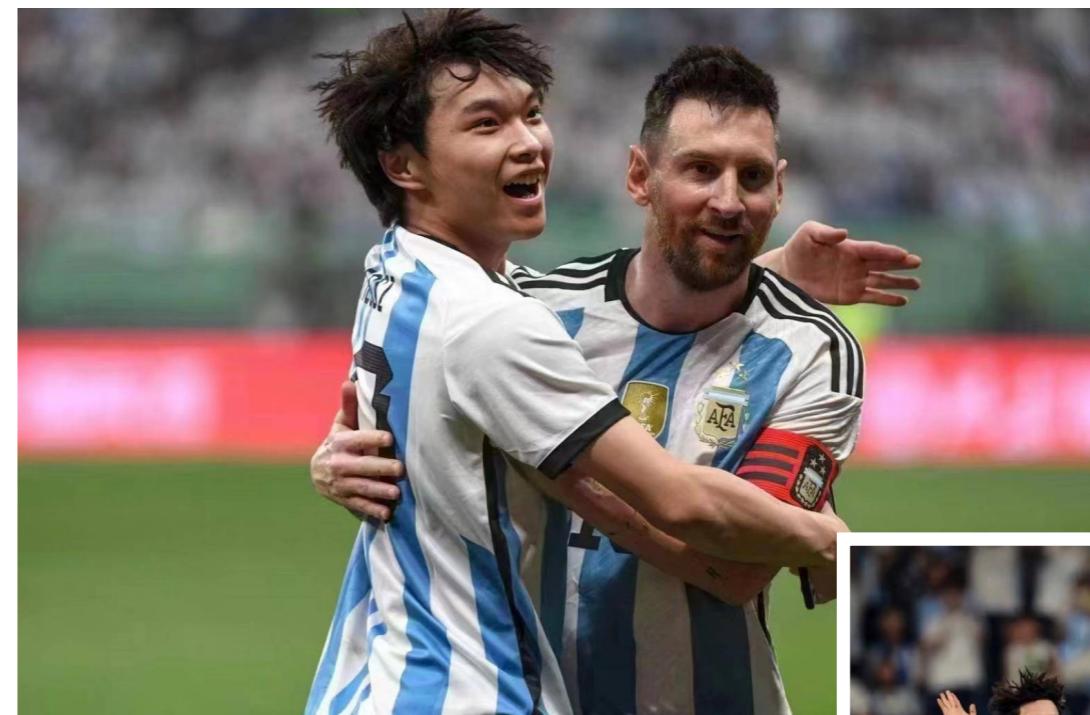
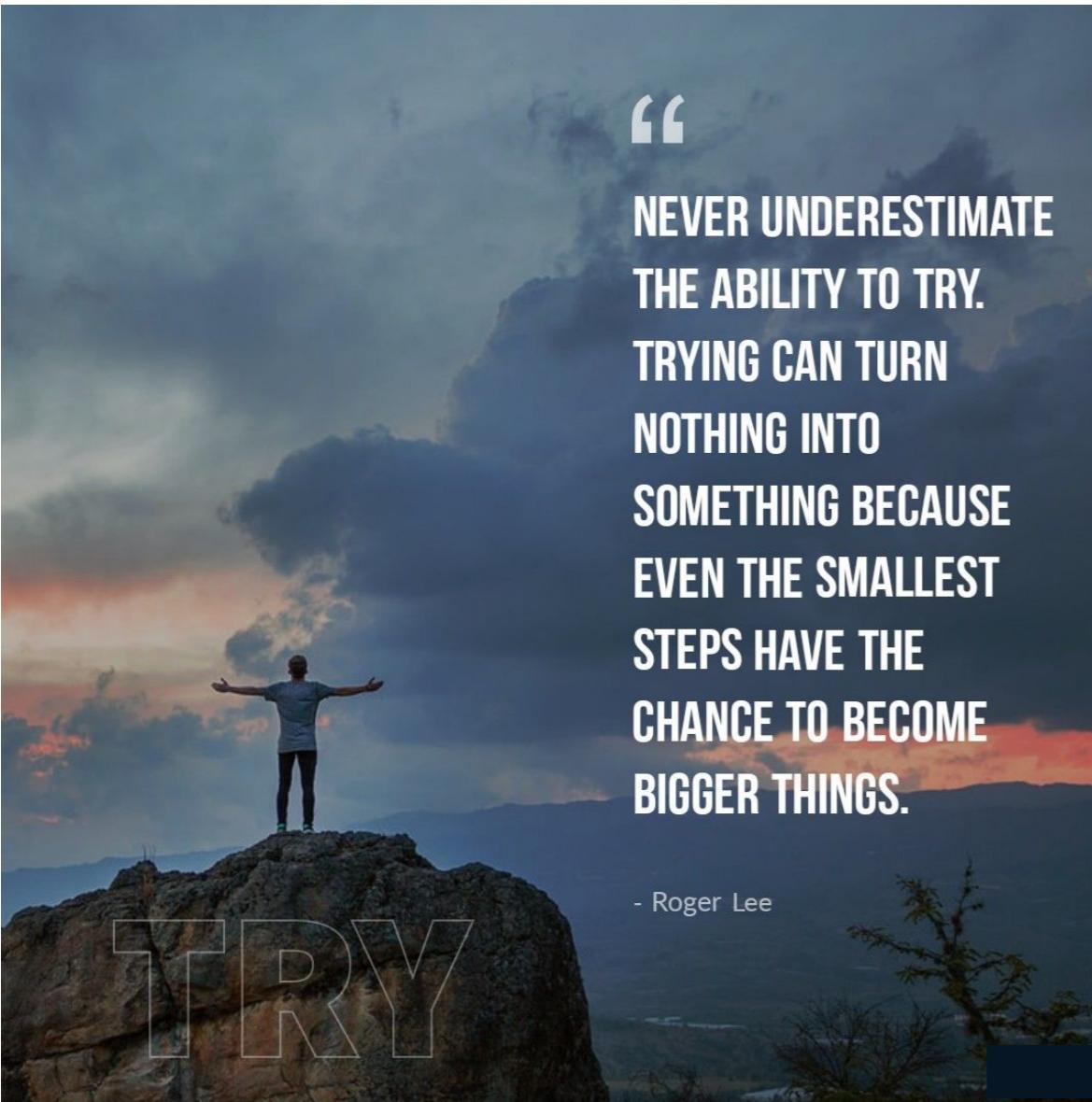
Goodness-of-fit test

$$\chi^2/ndf = 123/33$$



4.

Summary – Never underestimate the ability of experiment



Hidden-bottom hadronic decays of $\Upsilon(10753)$ with a $\eta^{(\prime)}$ or ω emission

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²*Research Center for Hadron and CSR Physics, Lanzhou University
and Institute of Modern Physics of CAS, Lanzhou 730000, China*

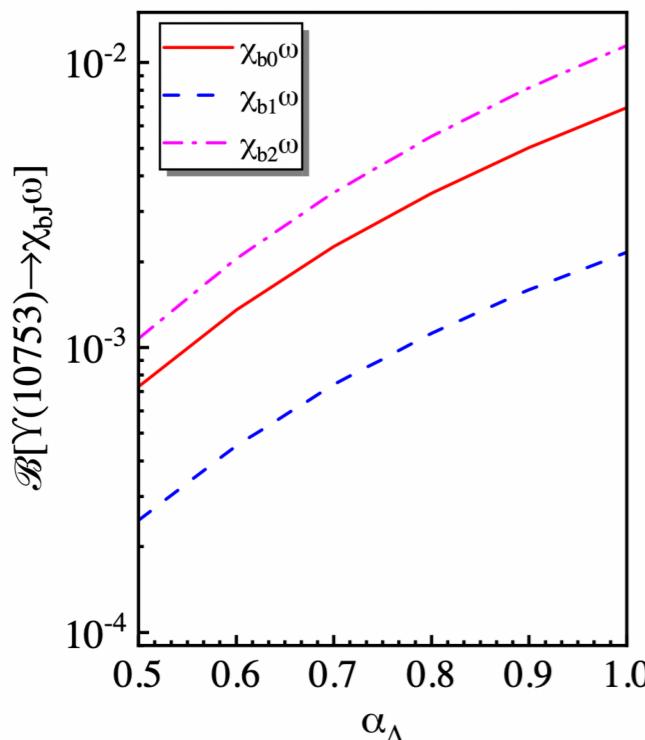
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In this work, we propose the 4S-3D mixing scheme to assign the $\Upsilon(10753)$ into the conventional bottomonium family. Under this interpretation, we further study its hidden-bottom hadronic decays with a



include $\Upsilon(10753) \rightarrow \Upsilon(1S)\eta^{(\prime)}$, $\Upsilon(10753) \rightarrow h_b(1P)\eta$, and $\Upsilon(10753) \rightarrow \chi_{bJ}\omega$. Since the $\Upsilon(10753)$ is above the $B\bar{B}$ threshold, the coupled-channel effect cannot be ignored. To calculate partial decay widths of these $\Upsilon(10753)$ hidden-bottom decays, we apply the quark-exchange mechanism. Our result shows that these discussed decay processes own considerable branching ratios, in an order of magnitude of 10^{-4} – 10^{-3} , which can be accessible at Belle II and other future experiments.

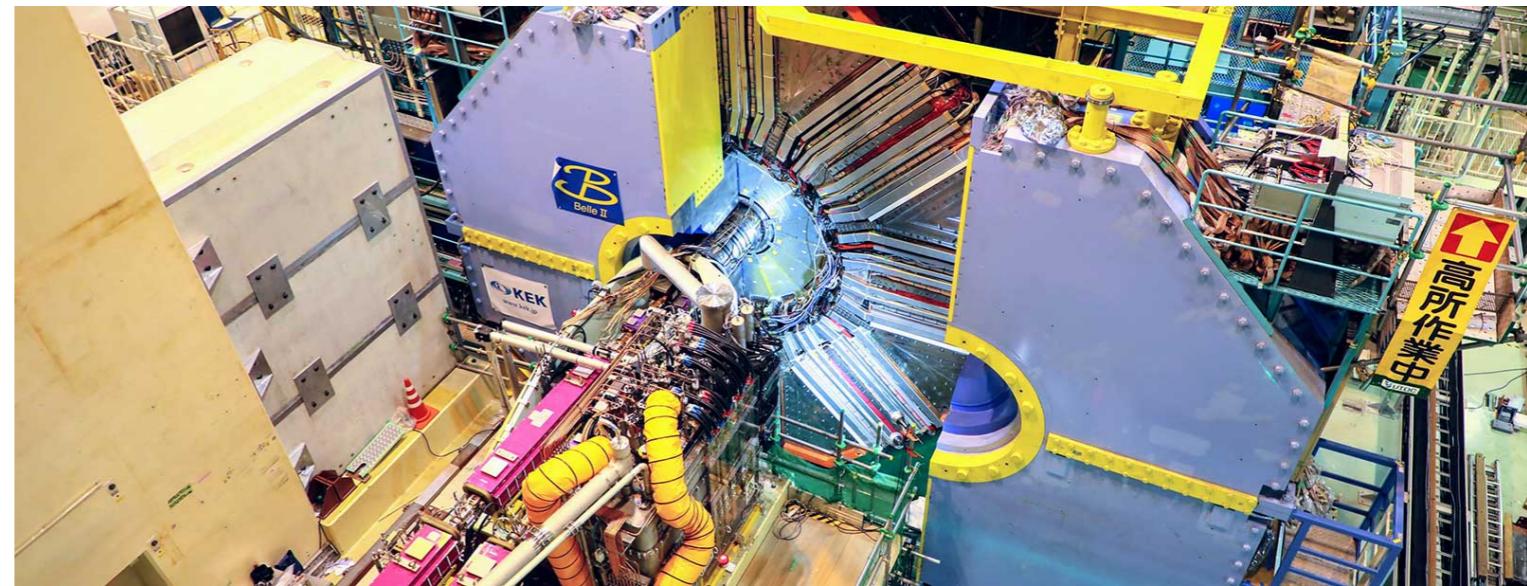
In 2021, we predicted $\Upsilon(10753) \rightarrow \chi_{bJ}\omega$ with sizable branching ratios

First analysis of Belle II energy scan data



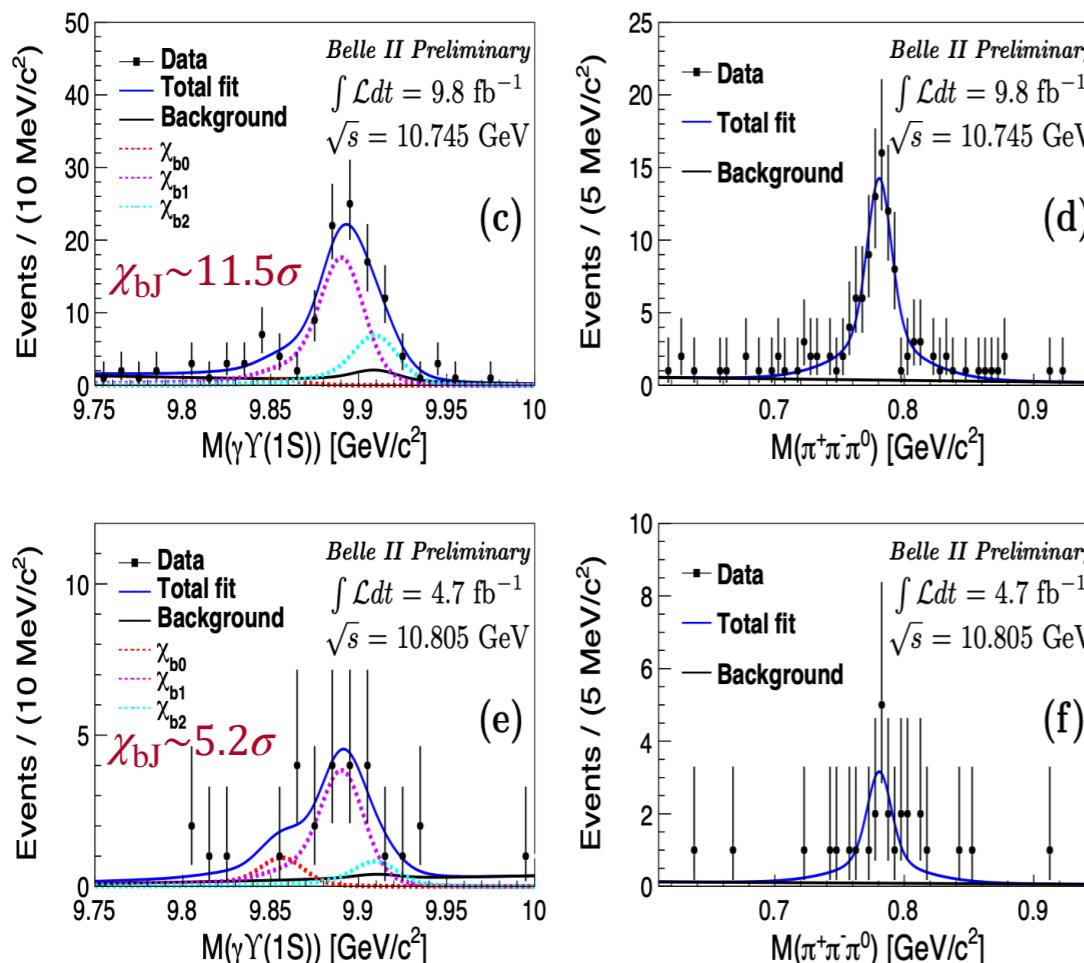
Qingping Ji (Henan Normal University)

(On behalf of the Belle II Collaboration)



Observation of $e^+e^- \rightarrow \omega\chi_{bJ}$

New for ICHEP !



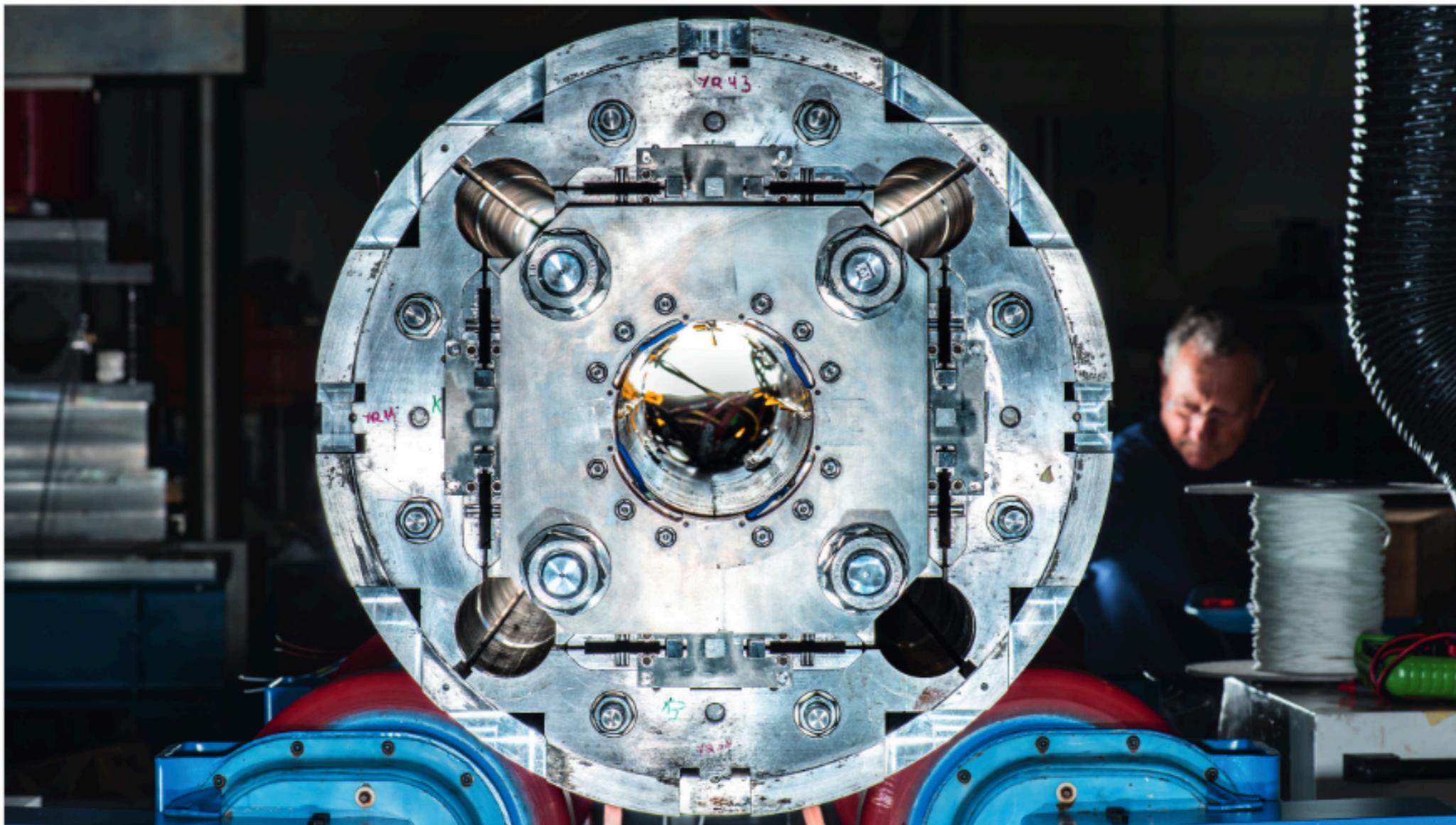
Two dimensional unbinned maximum likelihood fit to $M(\gamma Y(1S))$ and $M(\pi^+\pi^-\pi^0)$.

Channel	\sqrt{s} (GeV)	$N^{\text{sig.}}$	$\sigma_B^{(\text{up})}$ (pb)
$e^+e^- \rightarrow \omega\chi_{b1}$	10.745	$68.9^{+13.7}_{-13.5}$	$3.6^{+0.7}_{-0.7}$ (stat.) ± 0.4 (syst.)
$e^+e^- \rightarrow \omega\chi_{b2}$		$27.6^{+11.6}_{-10.0}$	$2.8^{+1.2}_{-1.0}$ (stat.) ± 0.5 (syst.)
$e^+e^- \rightarrow \omega\chi_{b1}$	10.805	$15.0^{+6.8}_{-6.2}$	1.6 @ 90% C.L.
$e^+e^- \rightarrow \omega\chi_{b2}$		$3.3^{+5.3}_{-3.8}$	1.5 @ 90% C.L.

No evident signal are found at $\sqrt{s} = 10.710$ GeV.

The High-Luminosity LHC: a new horizon for science and technology

The High-Luminosity LHC (HL-LHC) is a major upgrade of the Large Hadron Collider (LHC). The LHC collides tiny particles of matter (protons) at an energy of 13 TeV in order to study the fundamental components of matter and the forces that bind them together. The High-Luminosity LHC will make it possible to study these in more detail by increasing the number of collisions by a factor of between five and ten.



Prototype of a quadrupole magnet for the High-Luminosity LHC. (Image: Robert Hradil, Monika Majer/ProStudio22.ch)

Thank you for your attention!

