

第十六届粒子物理、核物理和宇宙学交叉学科前沿问题研讨会
南开大学，天津，2023年7月1-3日

CP violation in beauty decays

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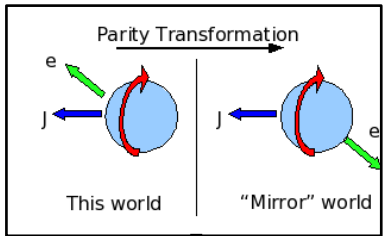
Courtesy Symmetry Magazine

Outline

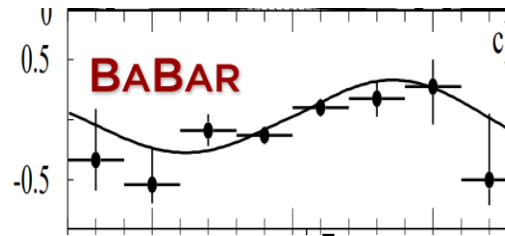
- CP violation and CKM mechanism
- Time-dependent CP violation & detection
- B^0 CP violating phase 2β
- B_s^0 CP violating phase ϕ_s
- CKM angle γ
- Summary

Discoveries of P & CP violation

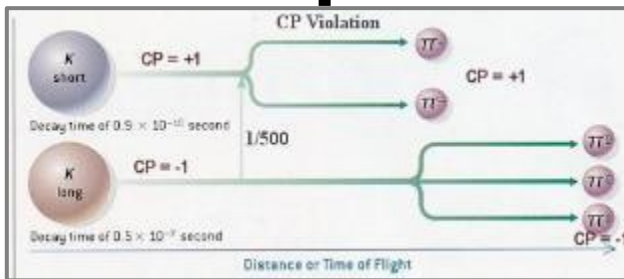
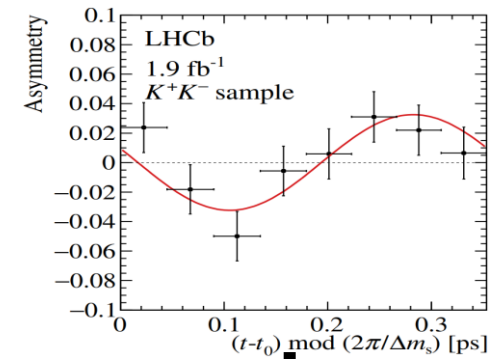
P violation
1956, Wu e al.



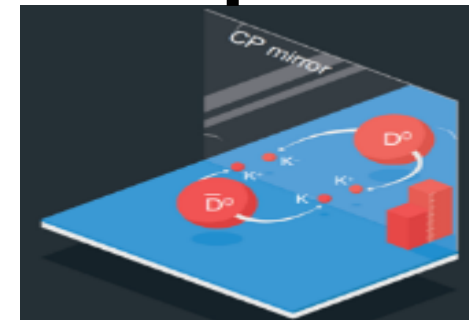
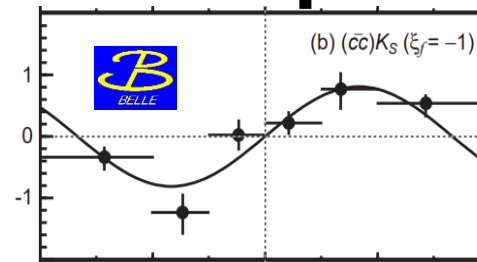
Time-dependent CP violation in B^0 decays
2001, BaBar & Belle



Time-dependent CP violation in B_s^0 decays
2020, LHCb



CP violation in K^0 mixing
1964, Cronin, Fitch et al.



CP violation in D^0 decay
2019, LHCb

CKM mechanism

$$\mathcal{L}_{\text{SM}} = \underbrace{\mathcal{L}_G(\psi, W, \phi)}_{\text{kinetic energy gauge IA}} + \underbrace{\mathcal{L}_H(\phi)}_{\text{Higgs potential} \rightarrow \text{spontaneous symmetry breaking}} + \underbrace{\mathcal{L}_Y(\psi, \phi)}_{\text{Yukawa IA} \rightarrow \text{fermion masses}}$$

EWSB & diagonalisation of Yukawa mass matrix \Rightarrow CKM quark mixing matrix

$$\mathcal{L}_{W\pm} = \frac{g}{\sqrt{2}} (\bar{U}_L \gamma^\mu W_\mu^+ V_{CKM} D_L + \bar{D}_L \gamma^\mu W_\mu^- V_{CKM}^+ U_L)$$

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

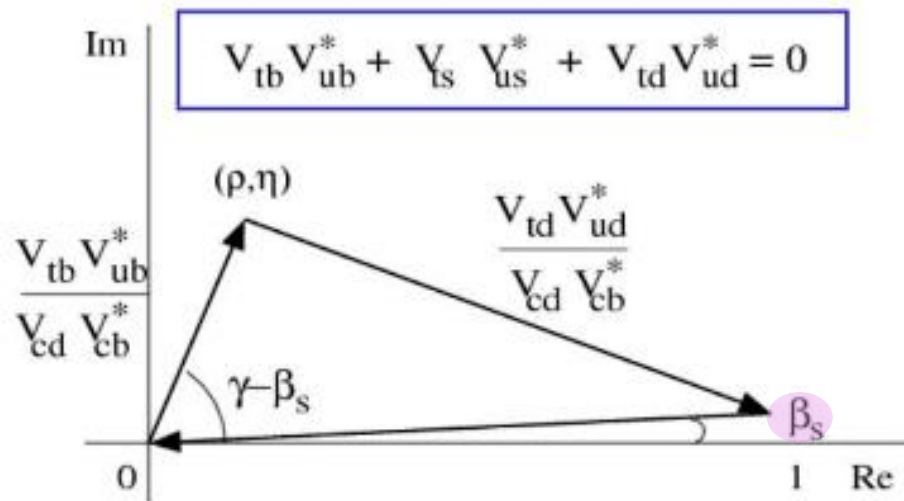
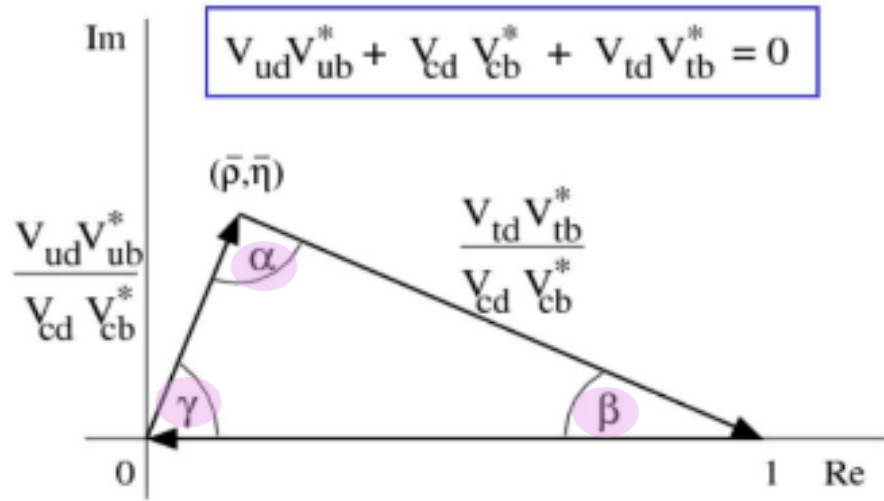
$$V_{CKM} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(r - ih) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - r - ih) & -A\lambda^2 & 1 \end{pmatrix}$$

L.Wolfenstein PRL 51 (1983) 1945

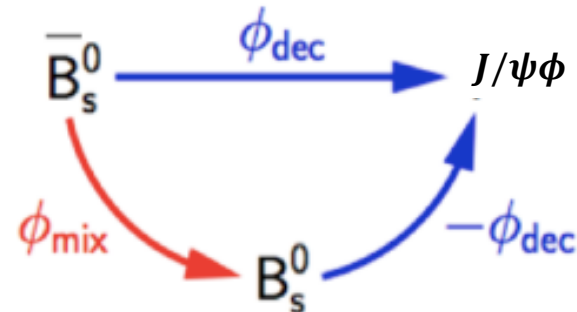
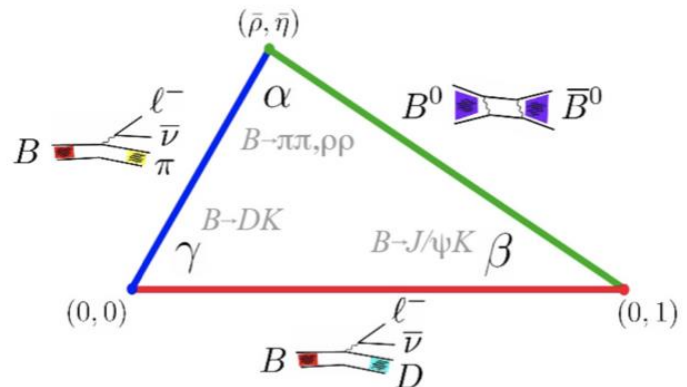
Four parameters (A, λ, ρ, η) to be measured in data.

$\eta \neq 0 \Rightarrow$ source of CP violation (CPV) in quark sector.

Unitarity of CKM matrix



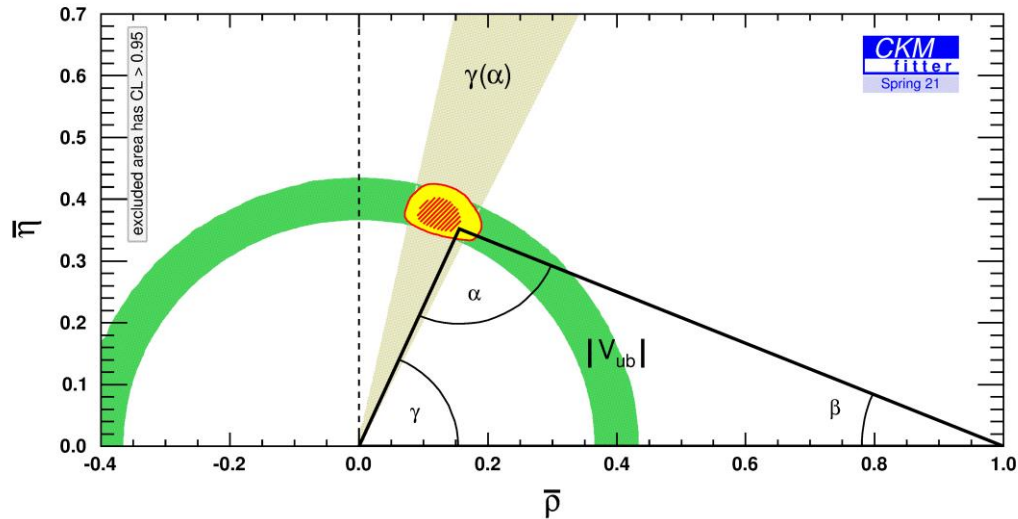
B decays plays huge roles in measurements of sides (**rates**, B_q^0 **mixing**) and angles (**CP asymmetries**)



Over-constraining CKM matrix

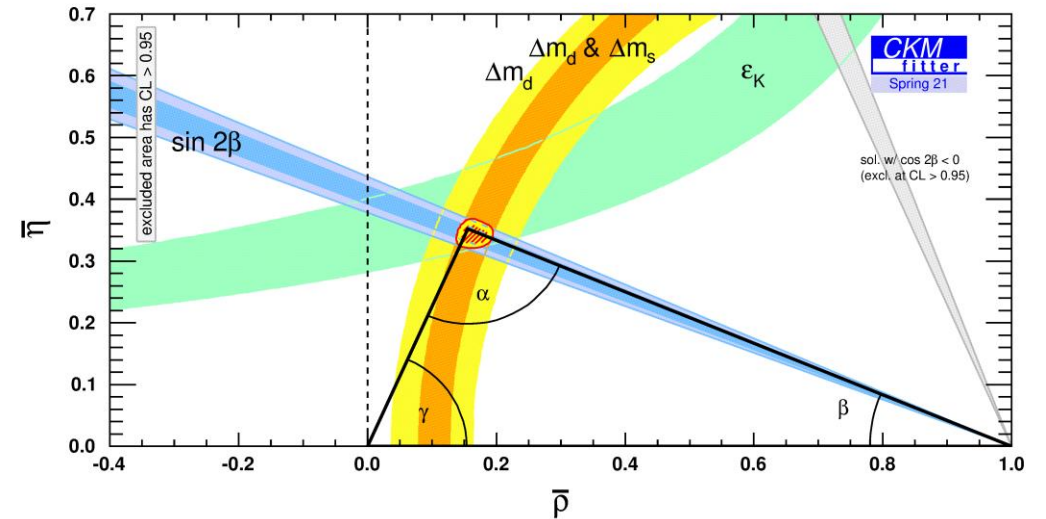
☐ Measurements from tree-level processes provide the SM benchmark

- γ in $B \rightarrow Dh$
- V_{ub} in $B \rightarrow \pi l^- \bar{\nu}$



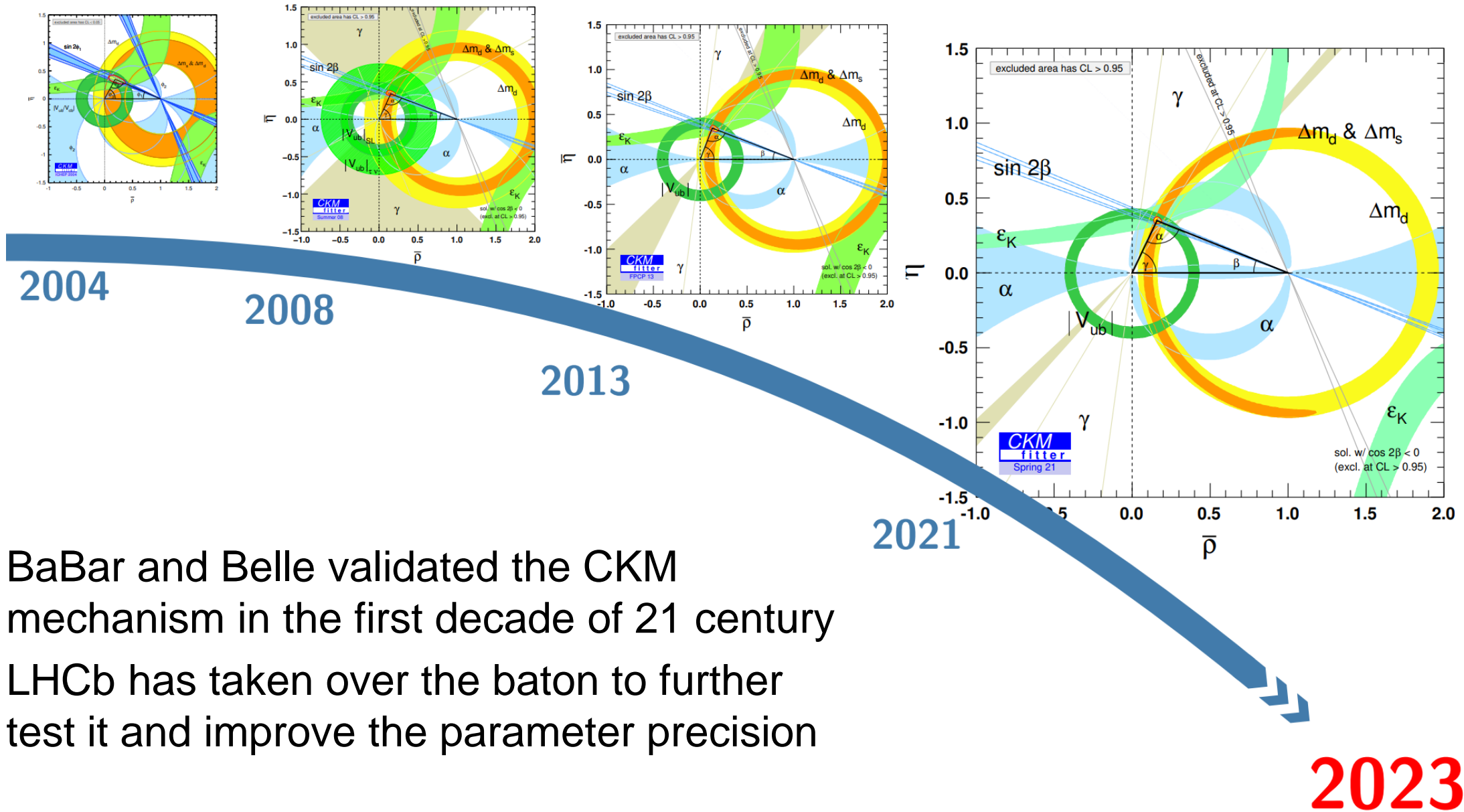
☐ Measurements from loop processes provide sensitivity to NP

- β in $B^0 \rightarrow J/\psi K_S^0$
- Mixing parameters Δm_d and Δm_s
- CPV in kaon mixing
- ...

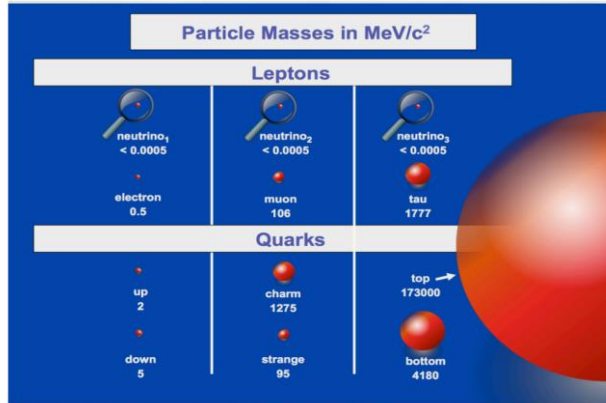


通过全局拟合确定CKM参数，考察不同测量之间一致性检验CKM机制

Great successes



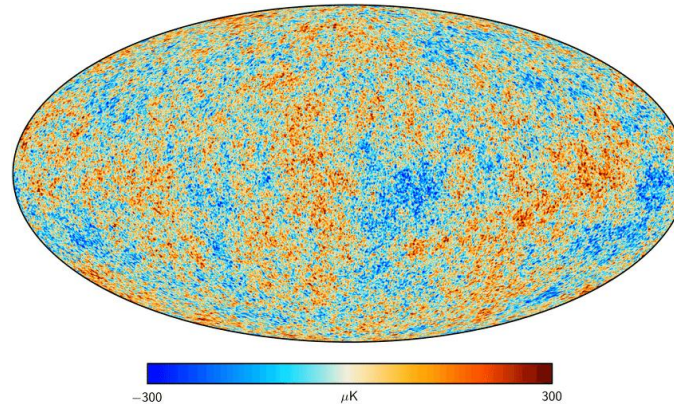
Open questions in flavour



$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

CKM prediction

$$\frac{n_B - n_{\bar{B}}}{n_\gamma} \sim 10^{-20}$$



Cosmological observation

$$\frac{n_B - n_{\bar{B}}}{n_\gamma} \sim 10^{-10}$$

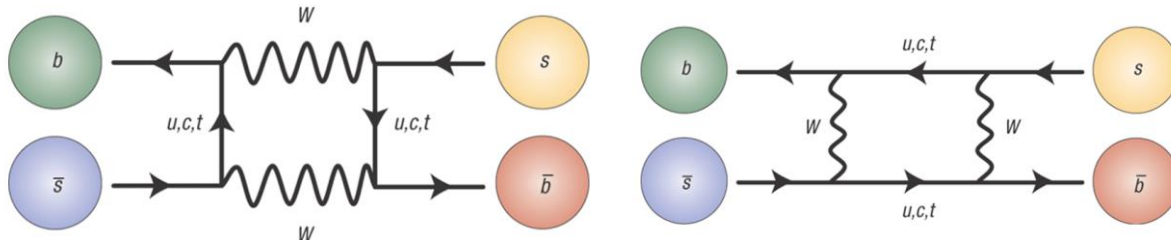
- What is the dynamic origin of the patterns of quark mass and flavour mixing?
 - Is there any source of CP violation beyond the Yukawa couplings?
- ⇒ **New physics beyond the SM is expected at very high energy scale**

Time-dependent CP violation & detection

Neutral B mixing and CPV

□ Neutral B mesons: $B^0 = (\bar{b}d)$ $\bar{B}^0 = (b\bar{d})$ $B_s^0 = (\bar{b}s)$ $\bar{B}_s^0 = (b\bar{s})$

□ $B_q^0 - \bar{B}_q^0$ ($q = d, s$) oscillation

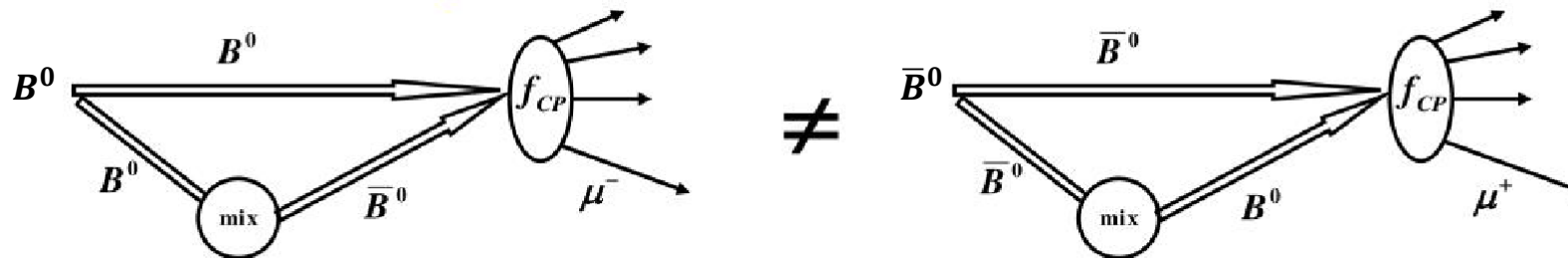


$$B_L = p|B_q\rangle + q|\bar{B}_q\rangle$$

$$B_H = p|B_q\rangle - q|\bar{B}_q\rangle$$

$$\Delta m_q = m_H - m_L, \Delta\Gamma_q = \Gamma_L - \Gamma_H$$

□ CPV in interference of B_q^0 decay to CP eigenstate with and w/o mixing



$$\Gamma(B^0 \rightarrow f_{CP}) \neq \Gamma(\bar{B}^0 \rightarrow f_{CP})$$

Measuring TD-CPV

$$A_{CP}(t) = \frac{\Gamma(\bar{B}_q^0(t) \rightarrow f_{CP}) - \Gamma(B_q^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}_q^0(t) \rightarrow f_{CP}) + \Gamma(B_q^0(t) \rightarrow f_{CP})} = \eta_f \frac{C \cos(\Delta m_q t) + S \sin(\Delta m_q t)}{\cosh \frac{\Delta \Gamma_q t}{2} + A_\Delta \sinh \frac{\Delta \Gamma t}{2}}$$

$S \neq 0$: mixing induced CPV

$C \neq 0$: direct CPV in decay

η_f : CP eigen-value

□ Requirements

- Identify the initial flavour B or \bar{B}
- Reconstruct the proper decay time t
- If the final state is a mixture of CP-even and CP-odd states, such as $B_s^0 \rightarrow J/\psi\phi$ and $B_s^0 \rightarrow \phi\phi$, perform angular analysis

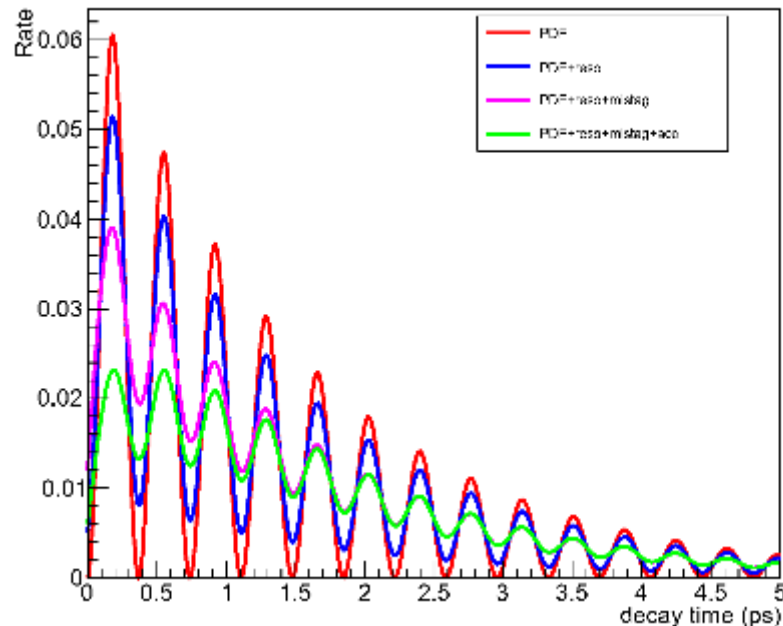
Experimental effects

$$\Delta m_s = 17.7 \text{ ps}^{-1}$$

$$\sigma_t = 50 \text{ fs}$$

$$\omega = 0.2$$

$$\epsilon(t) = 1/(1 + \exp(-2t))$$



- Times resolution σ_t

$$S \rightarrow e^{-\frac{(\Delta m \sigma_t)^2}{2}} S = D_{\text{time}} S$$

$$D_{\text{time}} \sim 0.7 \text{ for } \Delta m_s = 17.7 \text{ ps}^{-1} \text{ with } \sigma_t = 50 \text{ fs}$$
$$\sim 0.7 \text{ for } \Delta m_d = 0.5 \text{ ps}^{-1} \text{ with } \sigma_t = 1.5 \text{ ps}$$

- Wrong tag probability ω

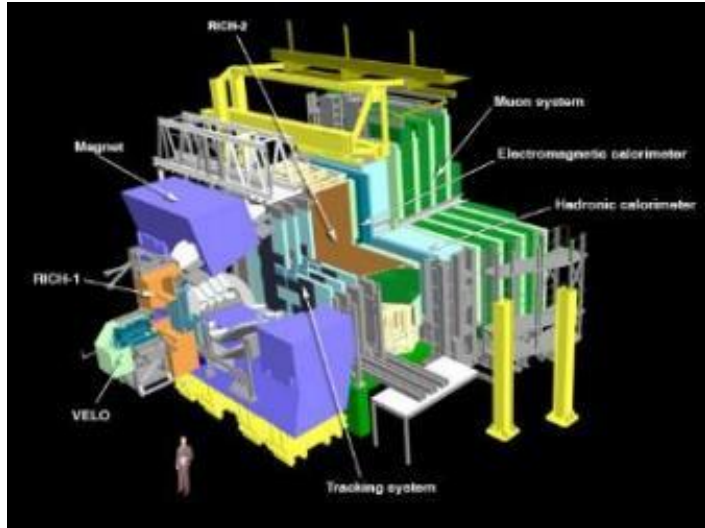
$$S \rightarrow (1 - 2\omega) S$$

- Decay-time dependent efficiency $\epsilon(t)$

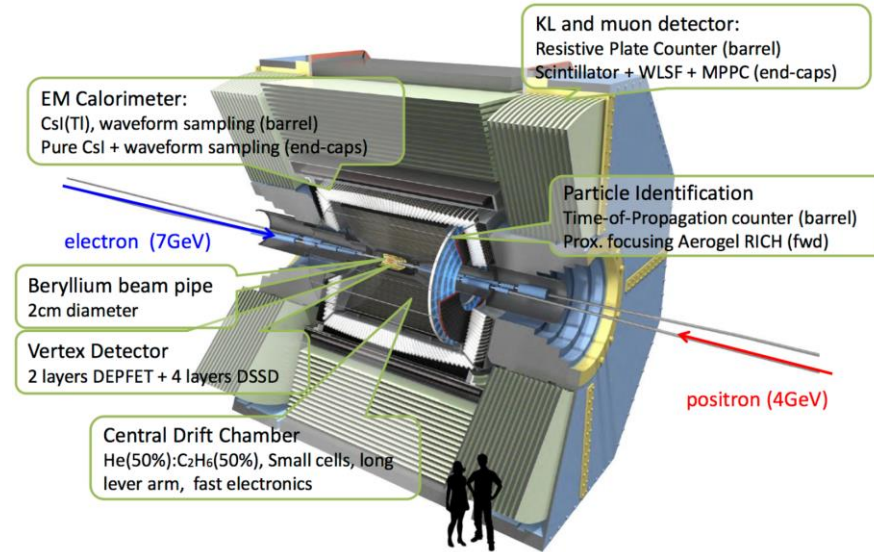
$$P(t) \rightarrow \epsilon(t) P(t)$$

Obtain info on σ_t , ω and $\epsilon(t)$ from data using control channels

Ongoing beauty experiments

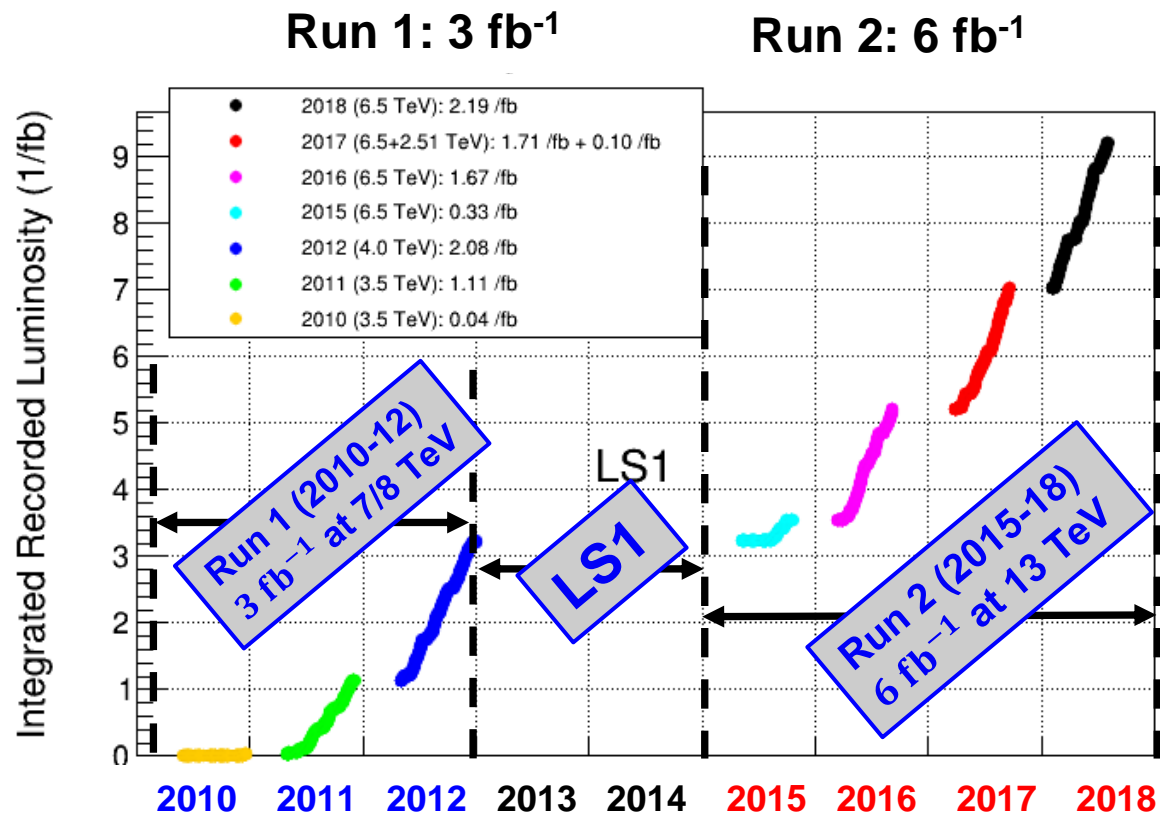


- Flavour experiment at LHC
- All b and c hadron species
- Excellent vertexing, tracking, PID
- 9 fb^{-1} @ 7, 8, 13 TeV



- SuperB factory at SuperKeKB
- Low background e^+e^- collision
- B^0, B^\pm
- 362 fb^{-1} @ $\Upsilon(4S)$

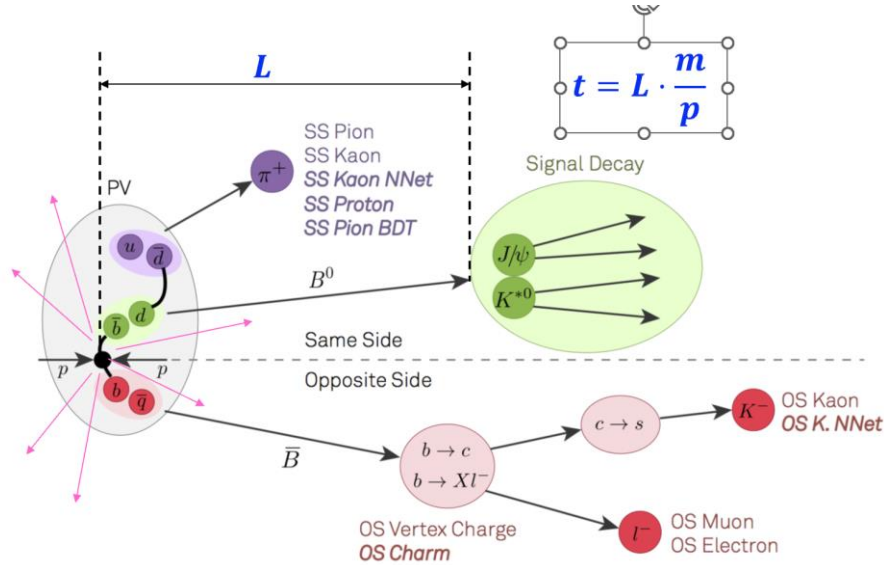
LHCb data taking in Run 1&2



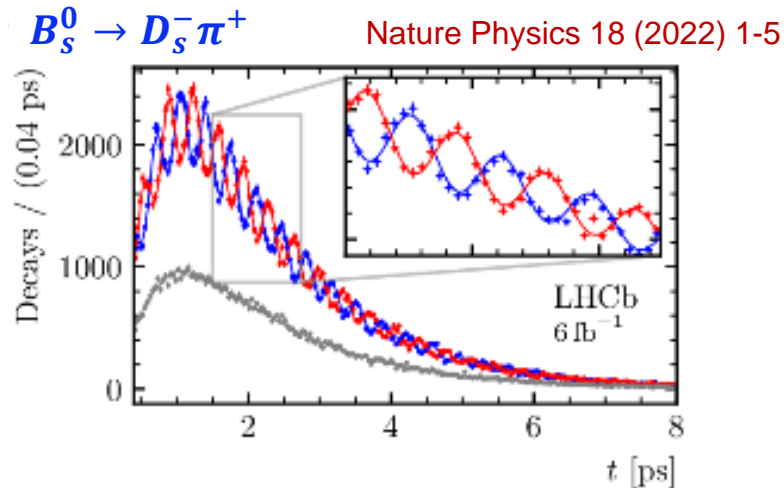
之前的LHCb物理结果大多数基于2017年前采集的数据。

此次报告的结果均利用当前全部可用数据进行了更新。

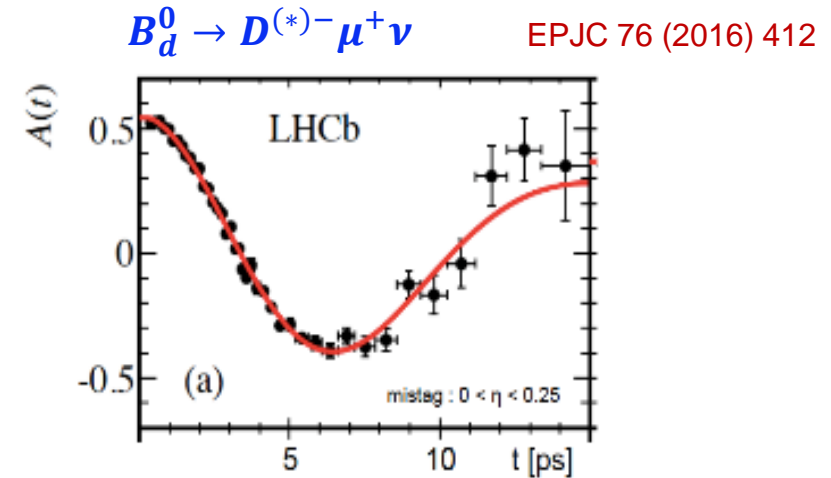
The LHCb approach



- Large boost from pp collision
 $\beta\gamma \sim 10, L \sim 1 \text{ cm}$
- Silicon vertex system
 $\sigma_t \sim 45 \text{ fs}$
- Flavour tagging: info from other B & fragmentation particles
 $\epsilon_{\text{tag}}(1 - 2\omega)^2 \sim 5\%$

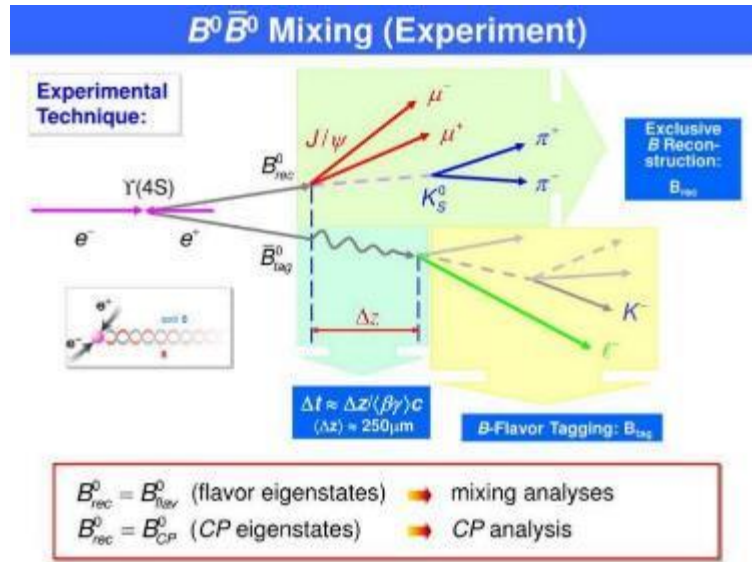


$$\Delta m_s = 17.7656 \pm 0.0057 \text{ ps}^{-1}$$



$$\Delta m_d = 0.5050 \pm 0.0021 \pm 0.0010 \text{ ps}^{-1}$$

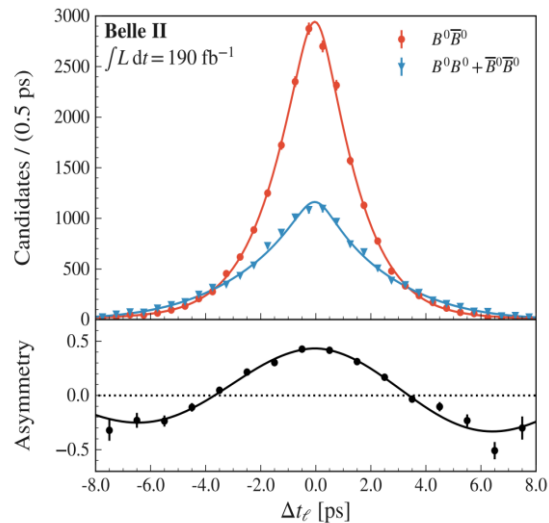
The Belle II approach



- Asymmetric e^+e^- collision
 $\beta\gamma = 0.28$, $\Delta z \sim 200 \mu\text{m}$
- Silicon vertex detector
 $\sigma_t \sim 1.5 \text{ ps}$
- Flavour tagging: info from other B
 $\epsilon_{tag}(1 - 2\omega)^2 \sim 40\%$



PRD 107 (2023) L091102 **new!**

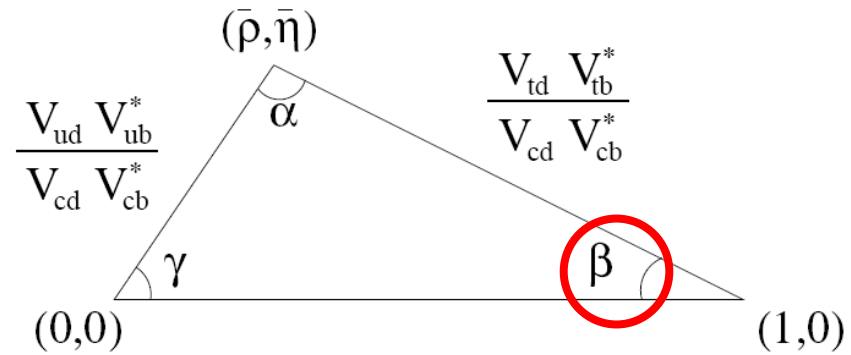


$$\Delta m_d = 0.516 \pm 0.008 \pm 0.005 \text{ ps}^{-1}$$

$$\tau_{B^0} = 1.499 \pm 0.013 \pm 0.005 \text{ ps}$$

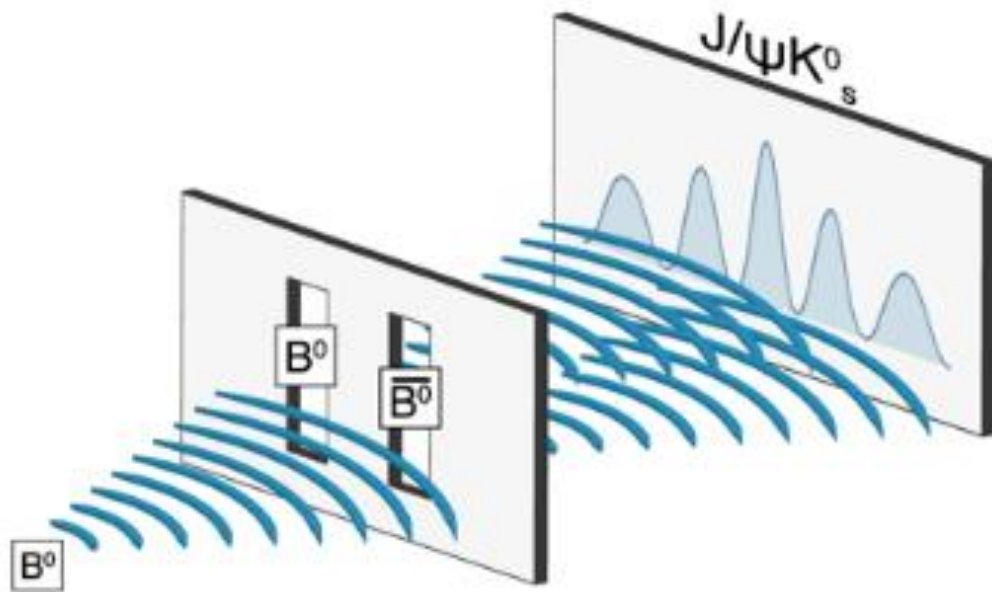
Belle: $\Delta m_d = 0.509 \pm 0.004 \pm 0.005 \text{ ps}^{-1}$

B^0 CP violating phase 2β

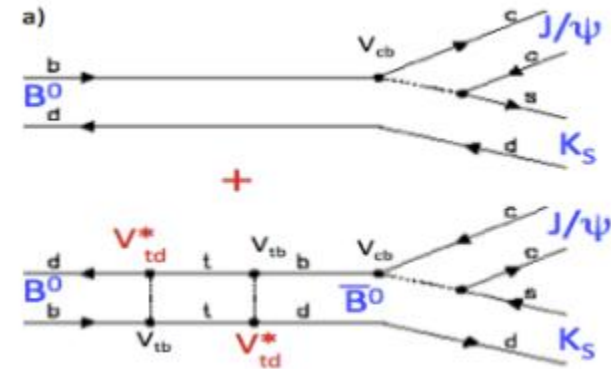


B^0 mixing phase $\phi_d = 2\beta^{\text{eff}}$

B factory flagship!



Golden mode $B^0 \rightarrow J/\psi K_S^0$

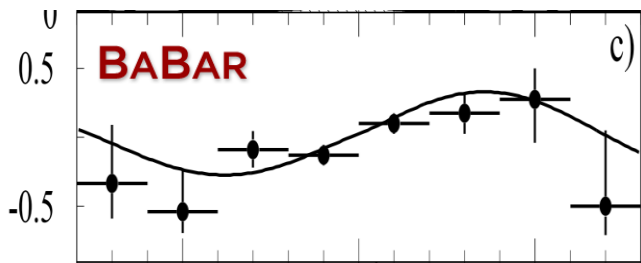


$$A_{CP}(t) \approx -\sin 2\beta \sin(\Delta m_d t)$$

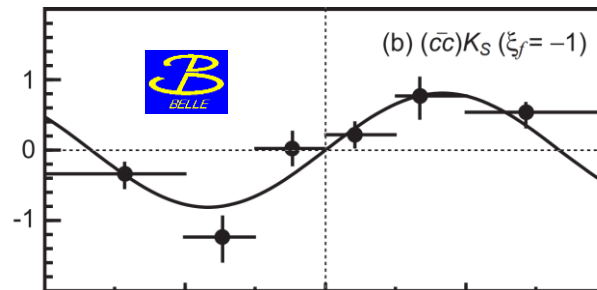
- 1981: I. I. Bigi & A. Santa pointed out the expectation of large CP violation in $B^0 \rightarrow J/\psi K_S^0$ decay
- 1987: P. Oddone proposed construction of asymmetric B factories
- 1999: BABAR and BELLE started running

History

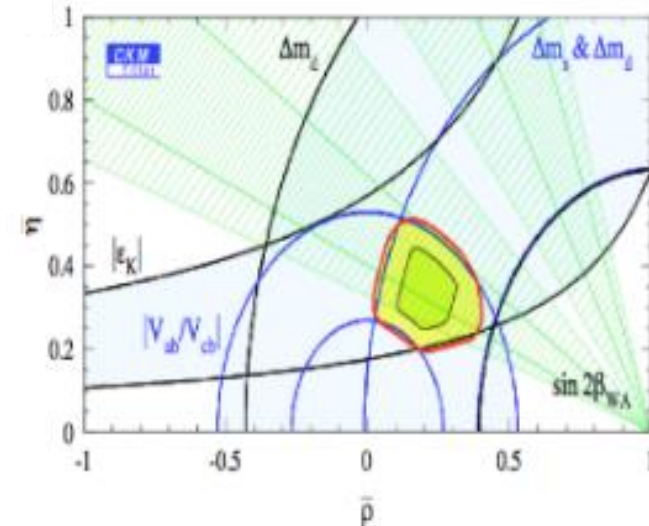
First measurements confirmed CKM prediction



Babar, PRL 87 (2001) 091801



Belle, PRL 87 (2001) 091802



Status before 2023

Belle: $\sin 2\beta = 0.67 \pm 0.02 \pm 0.01$

PRL 108 (2012) 171802

BaBar: $\sin 2\beta = 0.69 \pm 0.03 \pm 0.01$

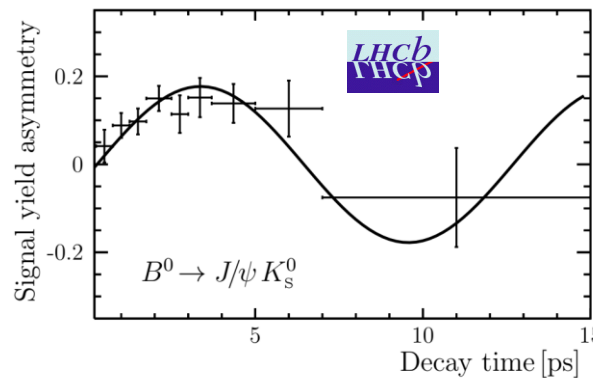
PRD 79 (2009) 072009

LHCb Run 1: $\sin 2\beta = 0.760 \pm 0.034$

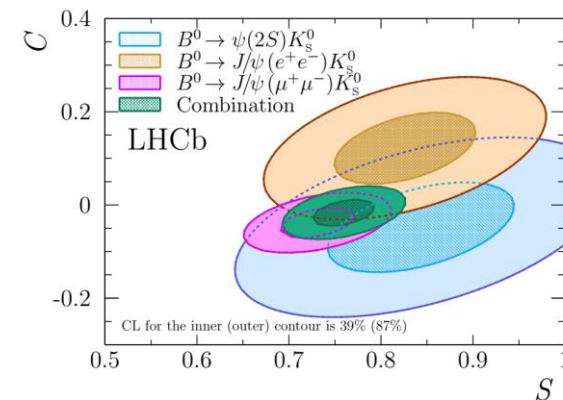
JHEP 11 (2017) 170

→ Recent update using Run2 data follows

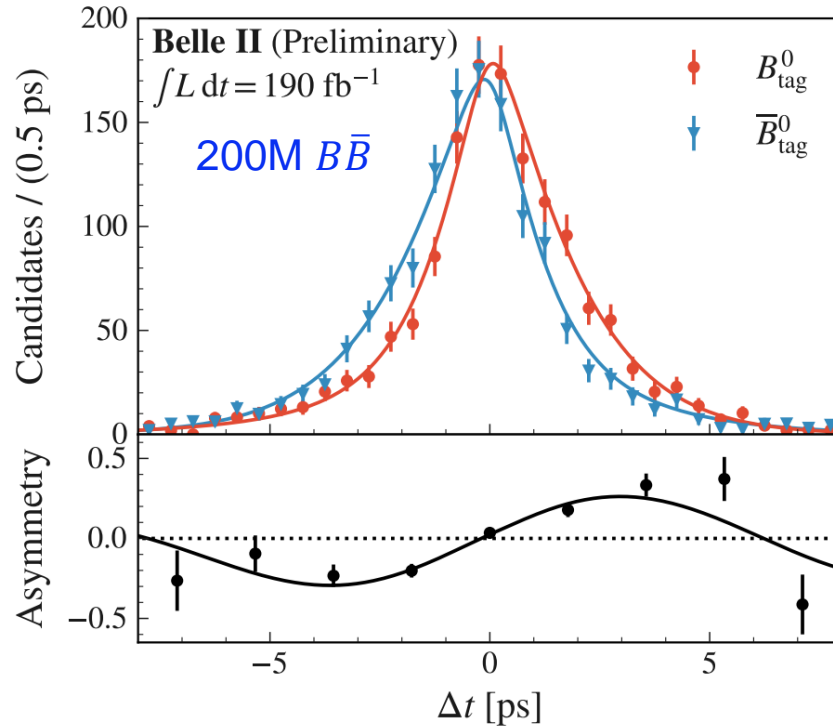
黄金道 $B^0 \rightarrow J/\psi K_S^0$



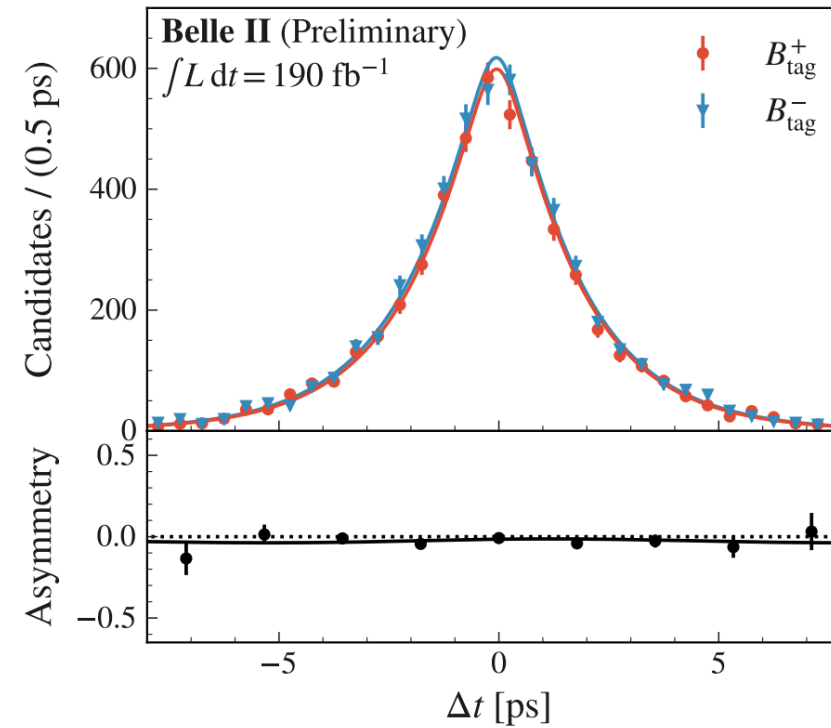
$b \rightarrow c\bar{c}s$ 过程联合



$B_d^0 \rightarrow J/\psi K_S^0$

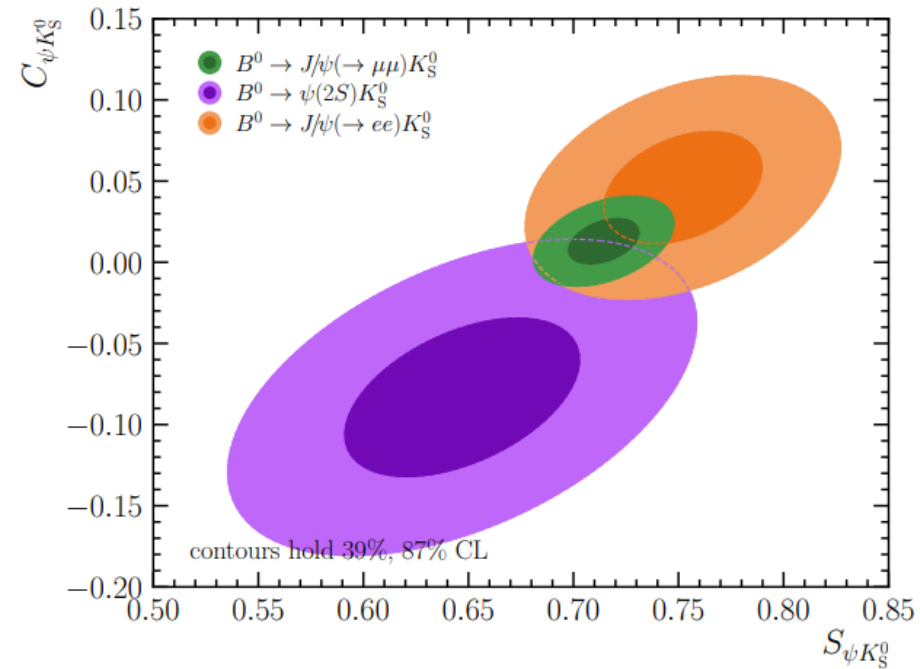
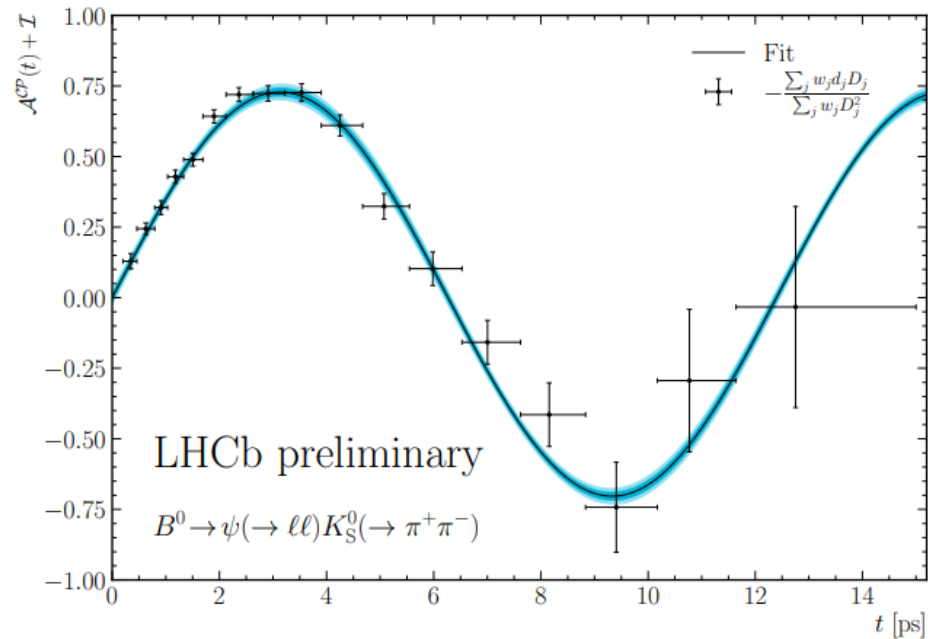


$B^+ \rightarrow J/\psi K^+$ for test of method



$\sin 2\beta = 0.720 \pm 0.062 \pm 0.016, \quad C = 0.094 \pm 0.044 \begin{matrix} +0.042 \\ -0.017 \end{matrix}$

Belle: $\sin 2\beta = 0.67 \pm 0.02 \pm 0.01$ (772M $B\bar{B}$)



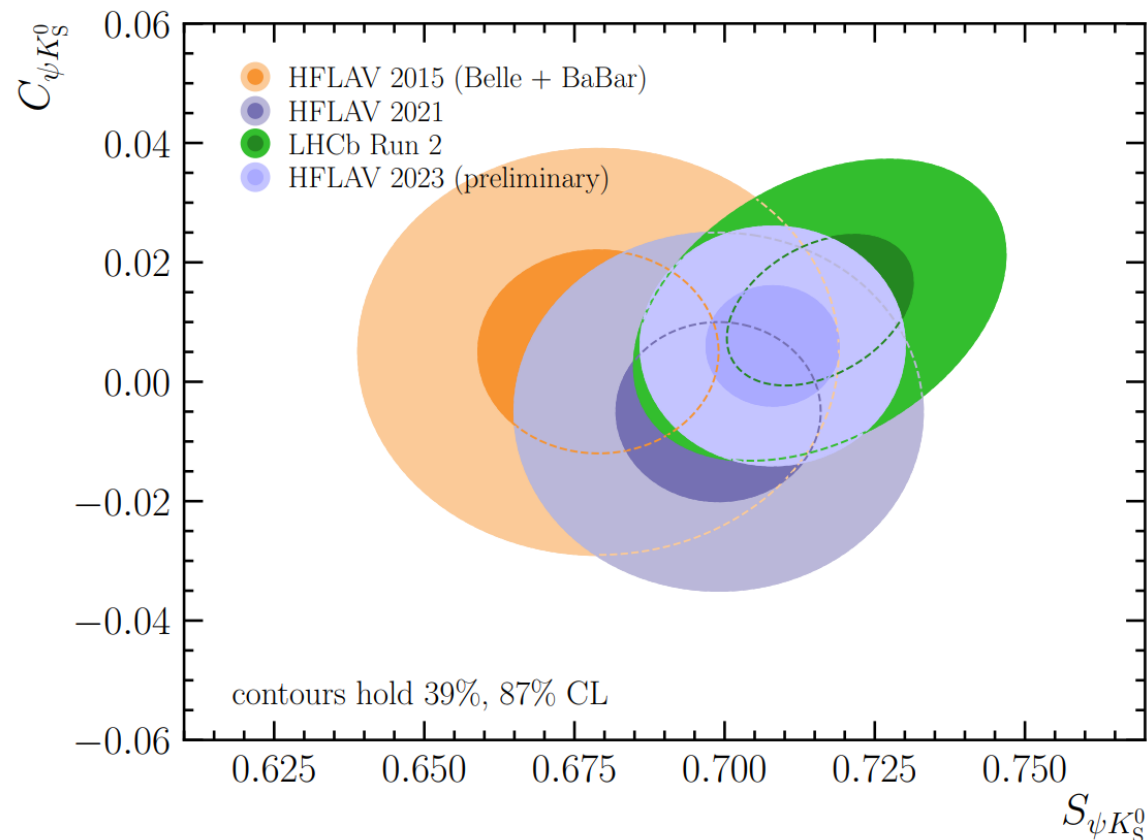
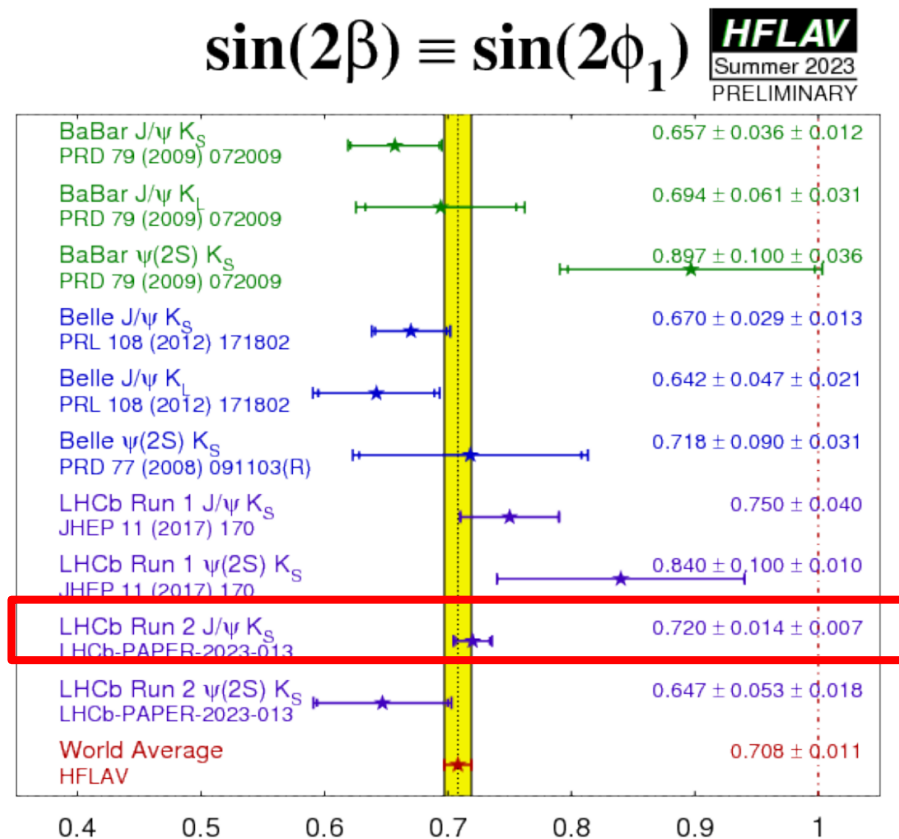
Study of $B^0 \rightarrow J/\psi(\rightarrow \mu\mu)K_S^0$, $B^0 \rightarrow J/\psi(\rightarrow ee)K_S^0$, $B^0 \rightarrow \psi(2S)K_S^0$ using Run2 data

Run2: $\sin 2\beta = 0.716 \pm 0.013 \pm 0.008$, $C = 0.012 \pm 0.012 \pm 0.003$

Run1: $\sin 2\beta = 0.760 \pm 0.034$

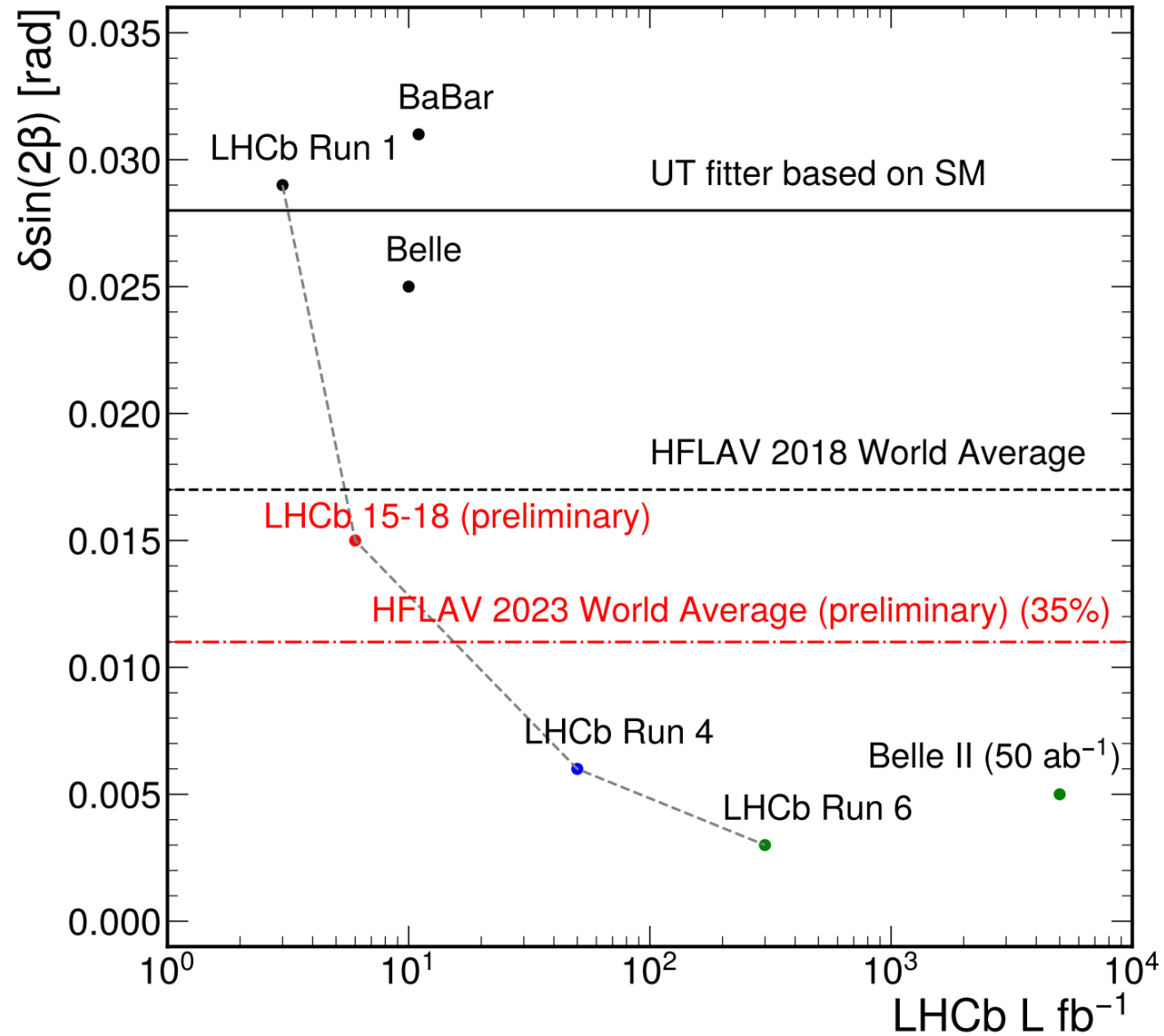
Run1+Run2: $\sin 2\beta = 0.724 \pm 0.014$

New world average of $\sin 2\beta$

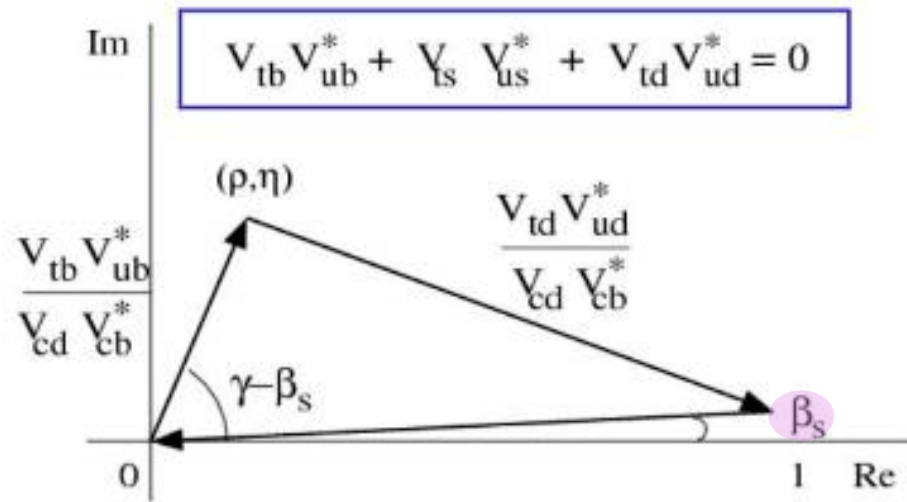


- LHCb has achieved the most precise single measurement, **improving WA by 35%**
- Consistent with SM prediction: $\sin 2\beta = 0.731_{-0.016}^{+0.029}$ (CKMFitter)

Projection for $\sin 2\beta$



B_s^0 CP violating phase ϕ_s

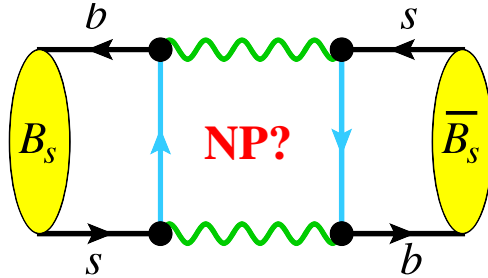


$$\phi_s = -2\beta_s^{eff}$$

B_s^0 mixing phase ϕ_s

LHCb flagship!

□ ϕ_s : sensitive probe of NP in mixing



$$\phi_s = \phi_s^{\text{SM}} + \Delta\phi^{\text{NP}}$$

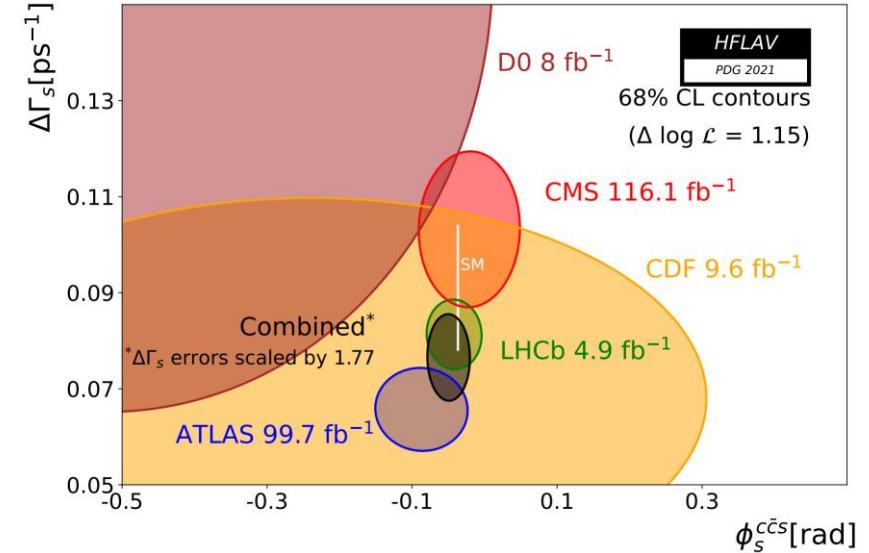
$$\phi_s^{\text{SM}} \approx -2\beta_s = -0.037 \pm 0.001 \text{ rad (UTFit)}$$

□ **Golden mode:** $B_s^0 \rightarrow J/\psi K^+ K^-$

$$A_{CP}(t) \propto \eta_f \sin\phi_s \sin(\Delta m_s t)$$

- CP eigenvalue of final state $\eta_f = (-1)^L$
- **Angular analysis** to separate CP even and odd states

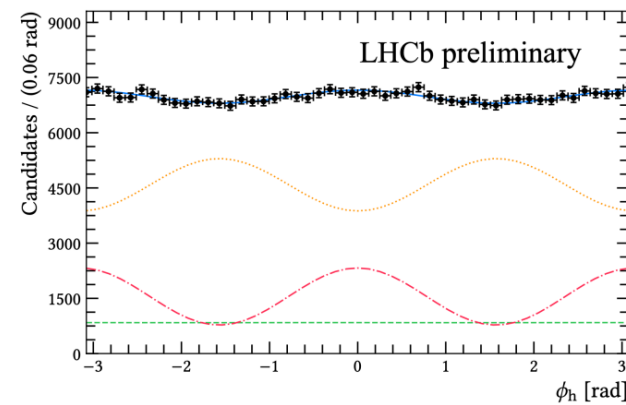
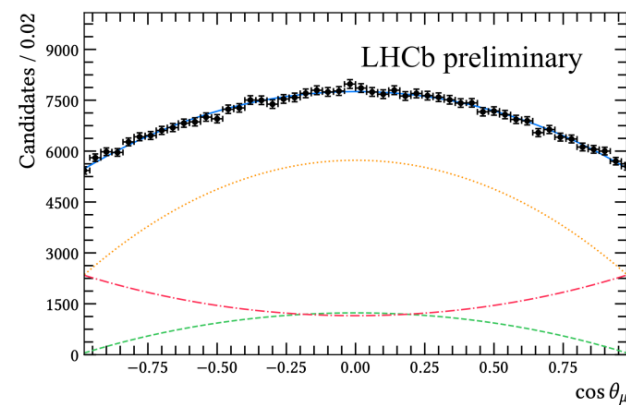
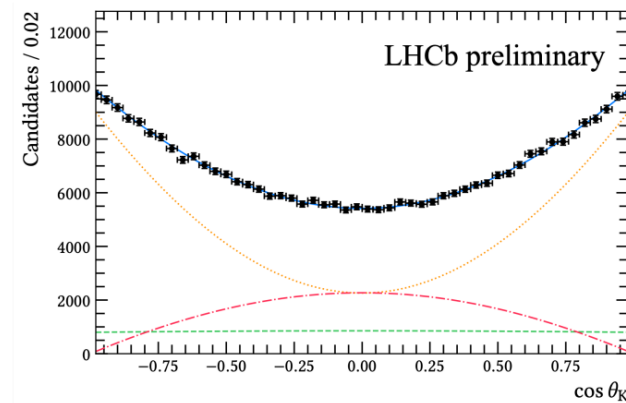
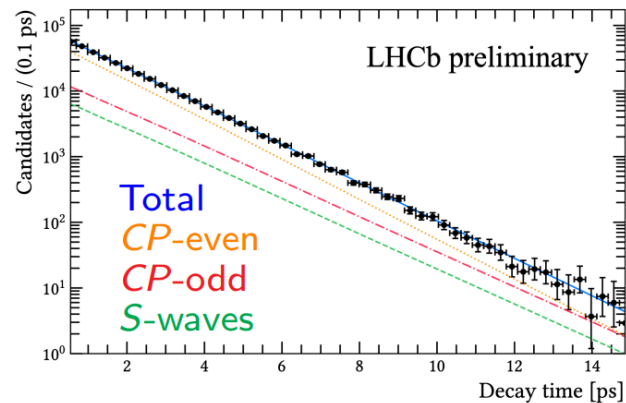
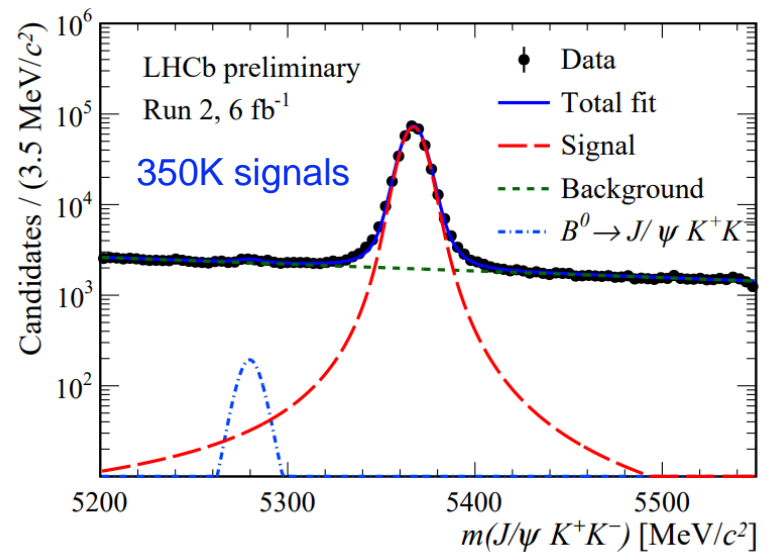
□ Major players: LHCb, ATLAS, CMS

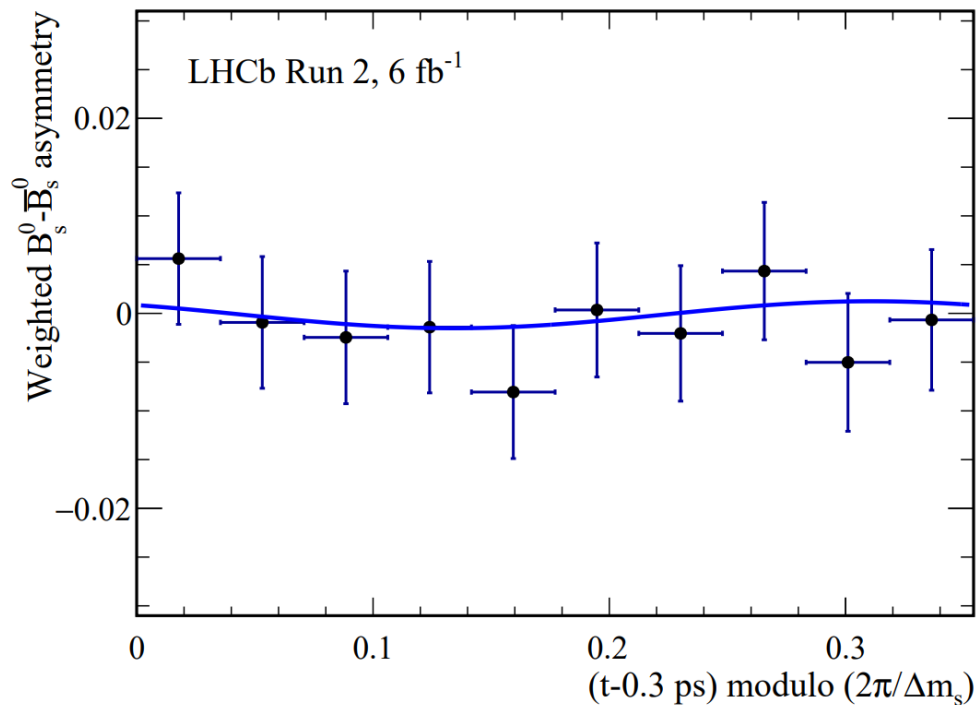


Previous LHC analysis of $B_s^0 \rightarrow J/\psi K^+ K^-$ used Run1+2015+2016 data

$$\phi_s^{J/\psi KK} = -0.081 \pm 0.032 \text{ rad} \quad \text{EPJC 79 (2019) 706}$$

→ **New result using also 2017+2018 data**





No sign of polarization dependence

No sign of CP violation

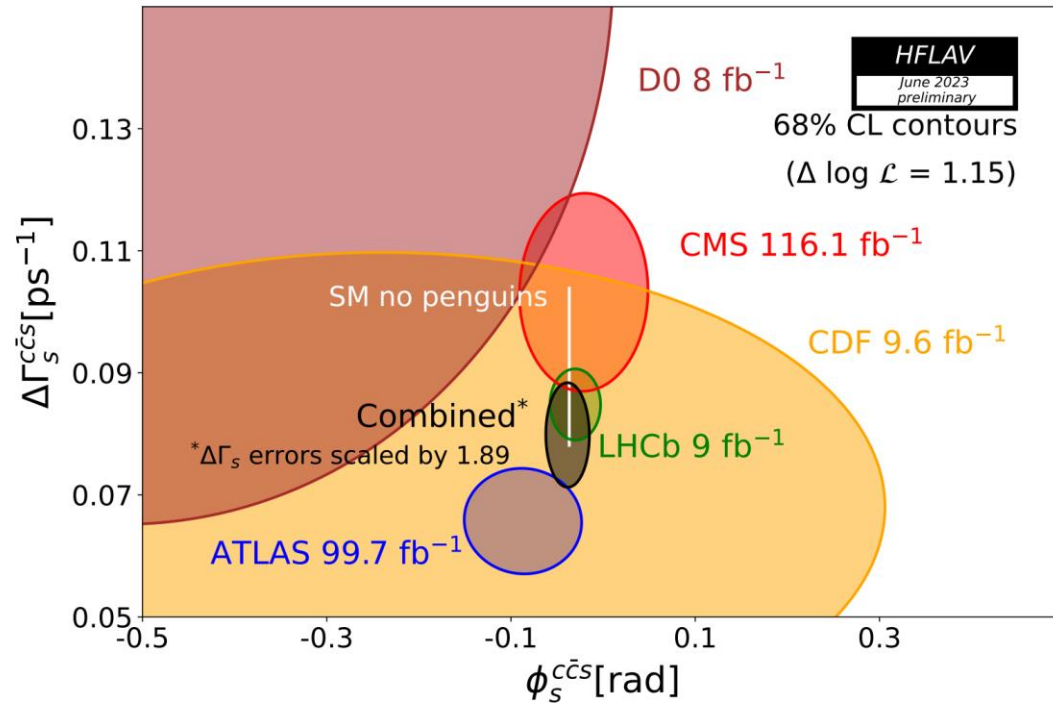
Run2: $\phi_s^{J/\psi KK} = -0.039 \pm 0.022 \pm 0.006$ rad

Run1: $\phi_s^{J/\psi KK} = -0.058 \pm 0.049 \pm 0.006$ rad

Run1 + Run2: $\phi_s^{J/\psi KK} = -0.044 \pm 0.020$ rad

Parameters	Values (stat. unc. only)
ϕ_s^0 [rad]	-0.034 ± 0.023
$\phi_s^{\parallel} - \phi_s^0$ [rad]	-0.002 ± 0.021
$\phi_s^{\perp} - \phi_s^0$ [rad]	$-0.001 \begin{smallmatrix} +0.020 \\ -0.021 \end{smallmatrix}$
$\phi_s^S - \phi_s^0$ [rad]	$0.022 \begin{smallmatrix} +0.027 \\ -0.026 \end{smallmatrix}$
$ \lambda^0 $	$0.969 \begin{smallmatrix} +0.025 \\ -0.024 \end{smallmatrix}$
$ \lambda^{\parallel}/\lambda^0 $	$0.982 \begin{smallmatrix} +0.055 \\ -0.052 \end{smallmatrix}$
$ \lambda^{\perp}/\lambda^0 $	$1.107 \begin{smallmatrix} +0.082 \\ -0.076 \end{smallmatrix}$
$ \lambda^S/\lambda^0 $	$1.121 \begin{smallmatrix} +0.084 \\ -0.078 \end{smallmatrix}$

New world average of ϕ_s



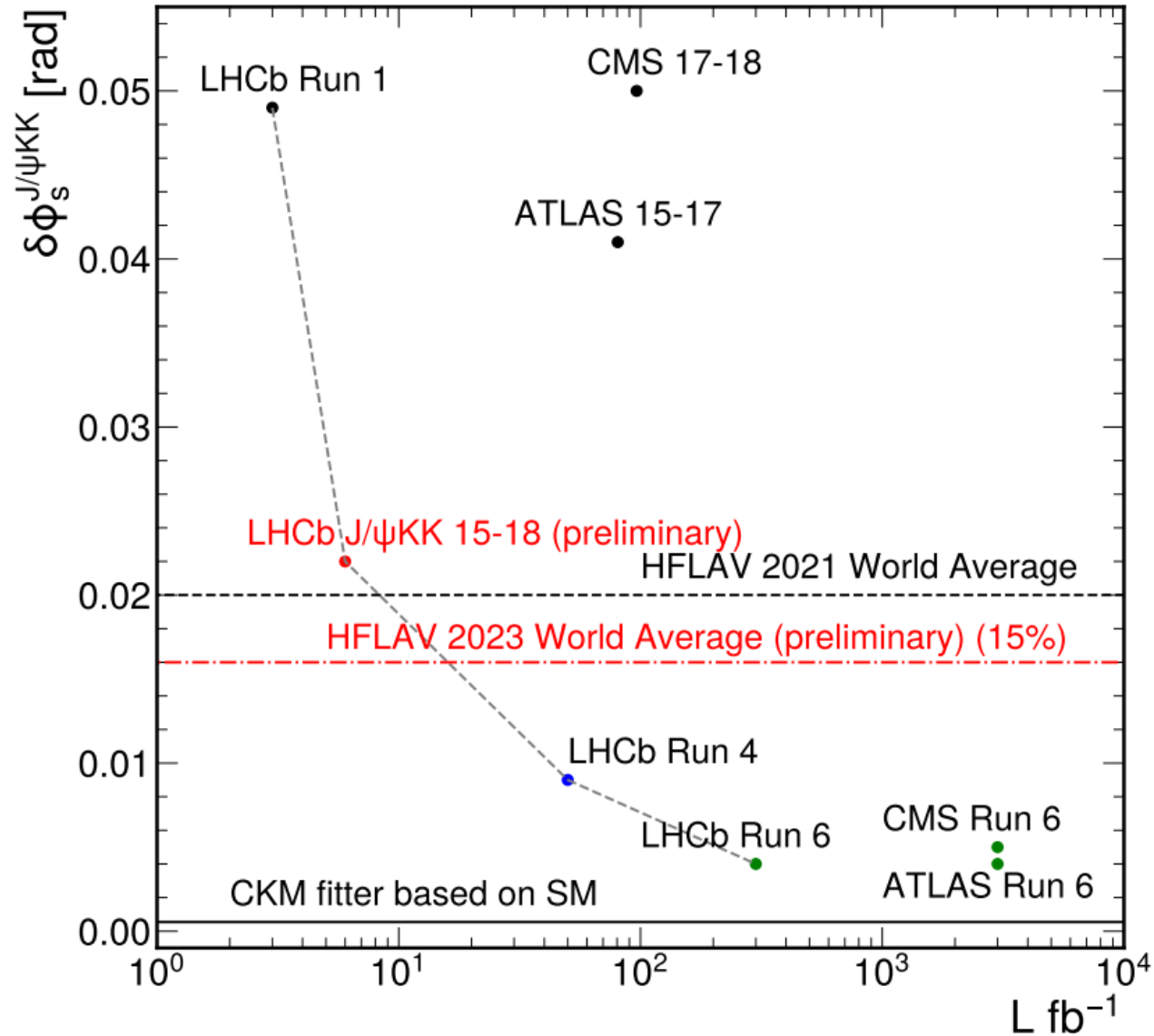
- $\phi_s^{J/\psi KK} = -0.050 \pm 0.017$ rad \rightarrow improved by 23%

- $\phi_s^{ccs} = -0.039 \pm 0.016$ rad \rightarrow improved by 15%

- Consistent with the prediction of Global fits assuming SM:³

$$\phi_s^{\text{CKMfitter}} \approx (-0.0368^{+0.0006}_{-0.0009}) \text{ rad}, \quad \phi_s^{\text{UTfitter}} = -0.0370 \pm 0.0010 \text{ rad}$$

Projection for ϕ_s

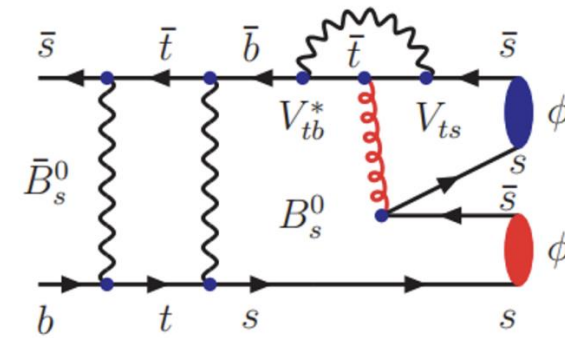


New CPV result in $B_s^0 \rightarrow \phi\phi$

arXiv:2304.06198

new!

- Penguin-mediated $b \rightarrow s\bar{s}s$ decay
- Sensitive to NP in mixing and penguin diagrams
- Tiny CPV expected in SM: $\phi_s^{s\bar{s}s} = 0.00 \pm 0.02$ rad
- Time-dependent angular analysis as for $B_s^0 \rightarrow J/\psi\phi$

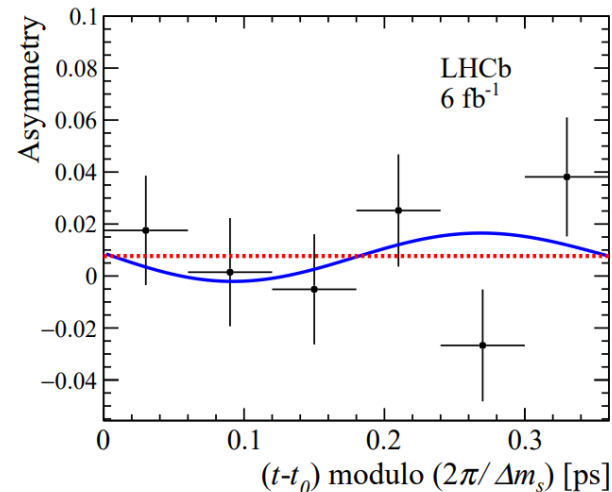
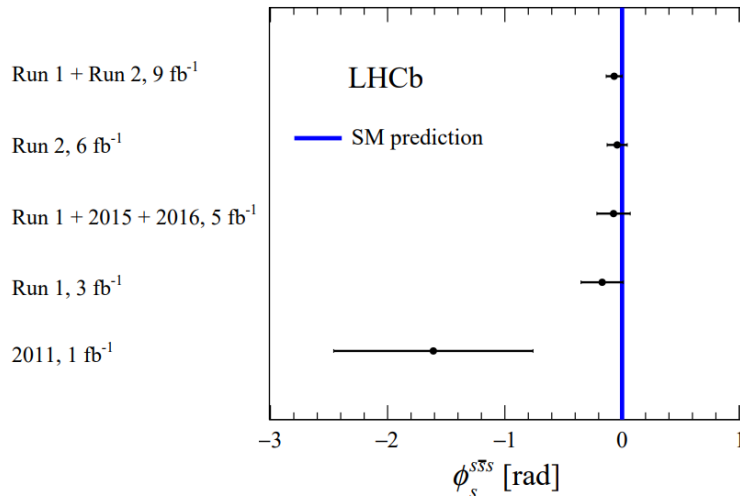


Previous Run1+2015+2016: $\phi_s^{s\bar{s}s} = -0.073 \pm 0.115 \pm 0.027$ rad

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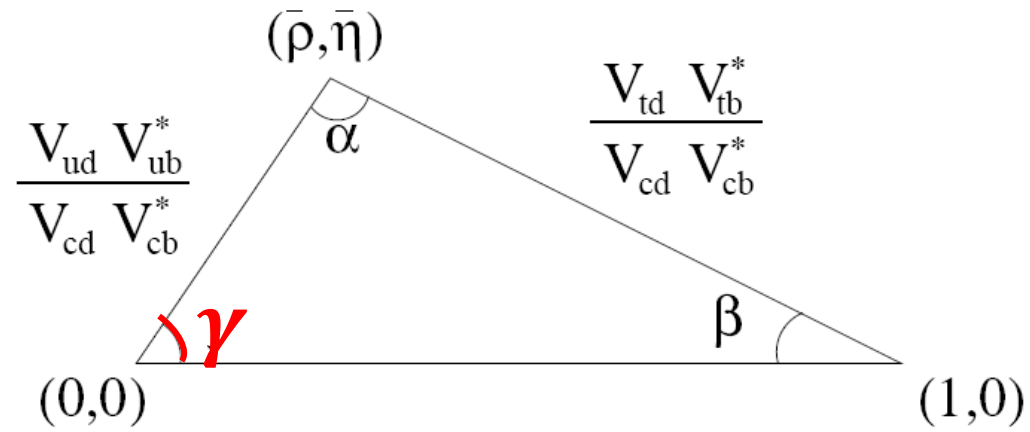
Adding 2016+2018

Run1+Run2: $\phi_s^{s\bar{s}s} = -0.074 \pm 0.069$ rad



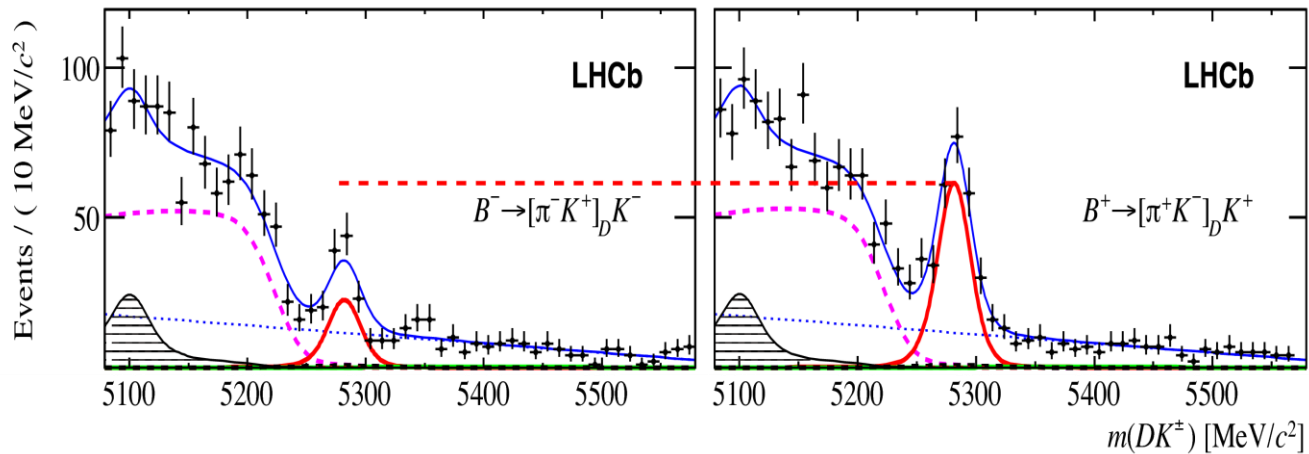
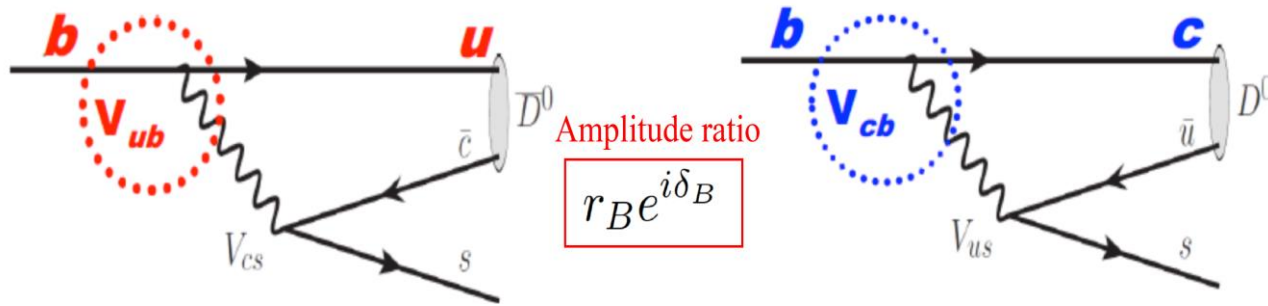
No sign of CP violation

CKM angle γ



γ measurement methods

□ Measure γ through $b \rightarrow u$ and $b \rightarrow c$ interference in $B \rightarrow Dh$ decays, which leads to direct CP violation.



□ Can use many B decay modes

- $B^+ \rightarrow Dh^+, B^+ \rightarrow D^*h^+, B^+ \rightarrow DK^{*+}, B^+ \rightarrow Dh^+\pi^+\pi^-$
- $B^0 \rightarrow DK^{*0}, B^0 \rightarrow D^\mp\pi^\pm$
- $B_s^+ \rightarrow D_s^\mp K^\pm, B_s^+ \rightarrow D_s^\mp K^\pm\pi^+\pi^-$

□ And many D^0 decay modes

- 2-body: $D^0 \rightarrow K^+\pi^-, D^0 \rightarrow h^+h^-$
- 3-body: $D^0 \rightarrow K_S^0 h^+h^-$
- 4-body: $D^0 \rightarrow K^-\pi^+\pi^-\pi^+, D^0 \rightarrow K^-K^+\pi^-\pi^+$

$$\frac{N(B^-) - N(B^+)}{N(B^-) + N(B^+)} = A_{CP^+} = \frac{1}{R_{CP^+}} 2r_B (2F_+ - 1) \sin(\delta_B) \sin(\gamma)$$

Previous status

□ B factories each: $\sigma_\gamma \approx 15^\circ$

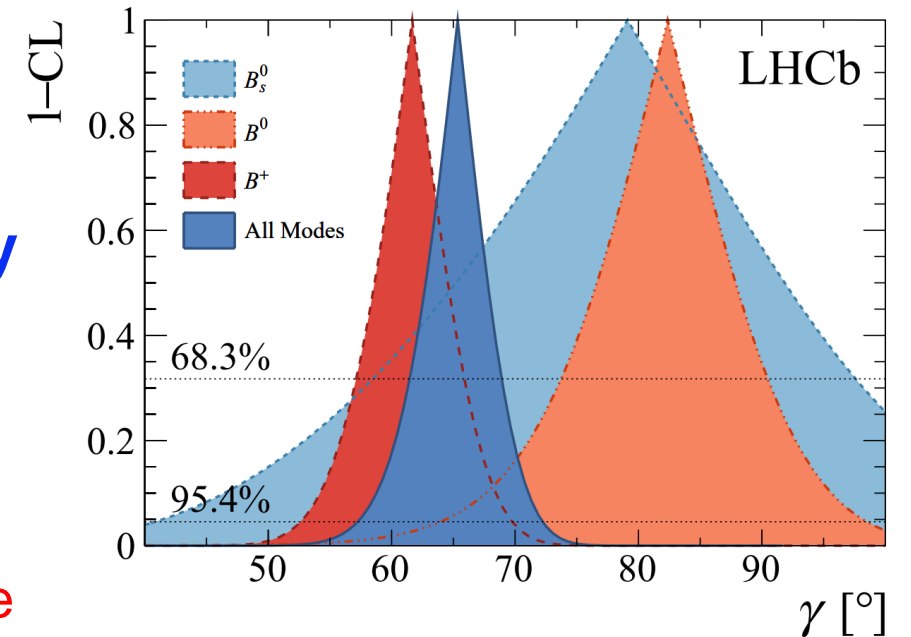
BaBar: $\gamma = (70 \pm 18)^\circ$ PRD 87 (2015) 052 015

BELLE: $\gamma = (73^{+13}_{-15})^\circ$ arXiv: 1301.2033

□ LHCb previous combination of many decay modes: $\sigma_\gamma \approx 4^\circ$

LHCb: $\gamma = (65.4^{+3.8}_{-4.2})^\circ$ JHEP 12 (2021) 141

An updated combination recently performed to include several new measurements



New γ results with $B \rightarrow Dh$ decays

□ γ in $B^\pm \rightarrow D[K^\mp \pi^\pm \pi^\pm \pi^\mp]h^\pm$ [arXiv:2209.03692](https://arxiv.org/abs/2209.03692)

$$\Gamma_{B^\pm \rightarrow D[K^\mp \pi^\pm \pi^\pm \pi^\mp]K^\pm} \propto r_{K3\pi}^2 + (r_B^K)^2 + 2r_{K3\pi}r_B^K R_{K3\pi} \cos(\delta_B^K + \delta_{K3\pi} \pm \gamma)$$

$$\Gamma_{B^\pm \rightarrow D[K^\pm \pi^\mp \pi^\mp \pi^\pm]K^\pm} \propto 1 + (r_{K3\pi}r_B^K)^2 + 2r_{K3\pi}r_B^K R_{K3\pi} \cos(\delta_B^K - \delta_{K3\pi} \pm \gamma),$$

- Decay rates measured in bins of $K3\pi$ phase space
- Bin-by-bin strong-phase difference $\delta_{K3\pi}$ and coherence factor $R_{K3\pi}$ are measured by CLEO-c and BESIII in quantum-correlated $D\bar{D}$ decays

$$\gamma = (54.8_{-5.8}^{+3.8} \text{ }_{-0.6}^{+0.6} \text{ }_{-4.3}^{+6.7})^\circ$$

Uncertainty of external inputs dominates!

□ γ in $B^\pm \rightarrow D[h^\pm h'^\mp \pi^0]h^\pm$ [JHEP 07 \(2022\) 099](https://arxiv.org/abs/2207.099)

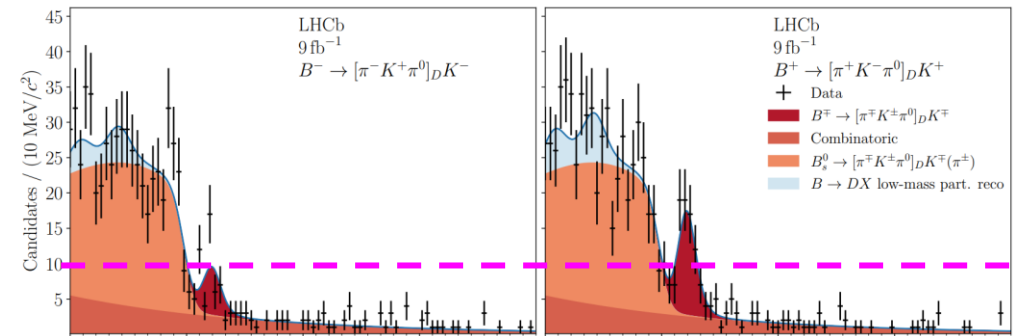
- Evidence for CPV in $B^\pm \rightarrow [\pi^\pm K^\mp \pi^0]_D K^\pm$

$$\gamma = (56_{-19}^{+24})^\circ$$

□ γ in $B^\pm \rightarrow D[K^+ K^- \pi^+ \pi^-]h^\pm$

$$\gamma = (116_{-14}^{+12})^\circ$$

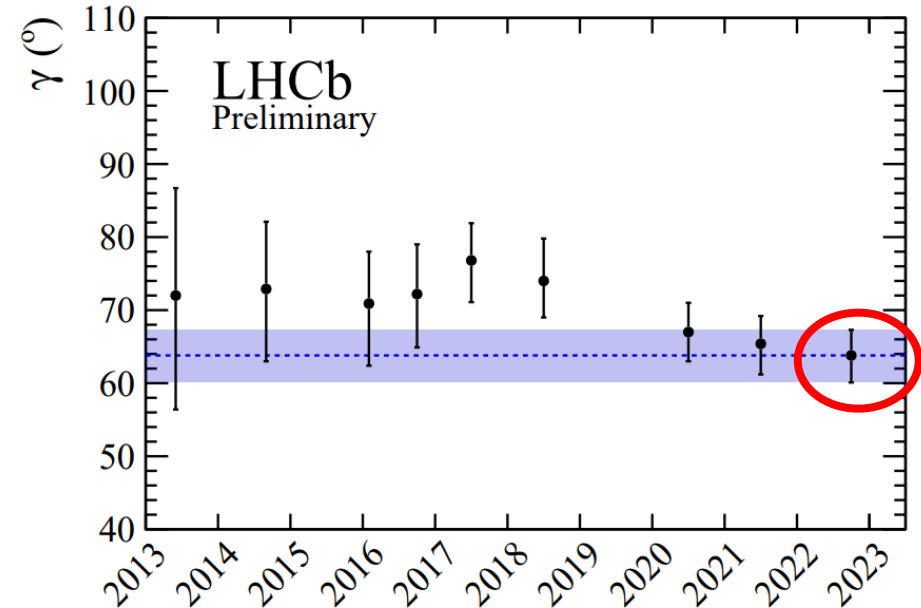
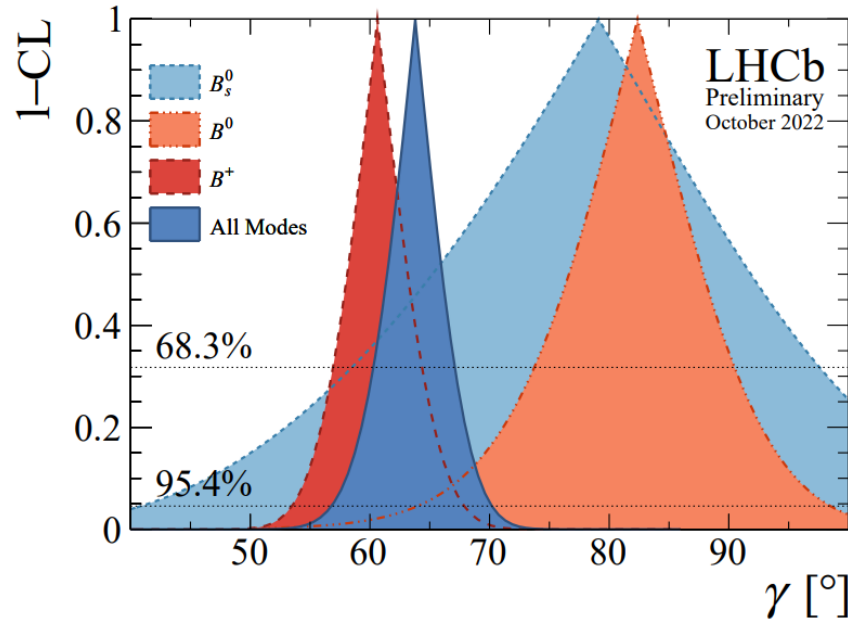
[arXiv:2301.10328](https://arxiv.org/abs/2301.10328) **new!**



Determine γ from CP violation measurements in $B \rightarrow Dh$

- Many B and D decay modes
- D decay amplitudes and strong phases from CLEO-c and BESIII

$B^\pm \rightarrow DK^{(*)\pm}$
 $B^0 \rightarrow DK^{*0}$
 $B^0 \rightarrow D^\mp \pi^\pm$
 $B_s^0 \rightarrow D_s^\mp K^\pm (\pi\pi)$
 $D \rightarrow K^+ \pi^-$
 $D \rightarrow K^+ \pi^-$
 $D \rightarrow h^+ h^- \pi^0$
 $D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$
 $D \rightarrow K^+ \pi^- \pi^0$
 $D \rightarrow K^\pm \pi^\mp \pi^+ \pi^-$
 $D \rightarrow K_S^0 K^\pm \pi^\mp$
 $D \rightarrow K_S^0 K^\pm \pi^\mp$



LHCb: $\gamma = (63.8^{+3.5}_{-3.7})^\circ$

10% improvement

CKMFitter prediction: $\gamma = (65.5^{+1.1}_{-2.7})^\circ$

γ measurement at Belle II

Model-independent analysis of $B^\pm \rightarrow D[K_S^0 h^+ h^-] h^\pm$

- Data from Belle (711 fb⁻¹) and Belle II (128 fb⁻¹)
- Bin-by-bin D^0 strong-phase parameter c_i and s_i from CLEO-c and BESIII

$$N_i(B^0) = h^{B^0} \left[F_{-i} + (x_+^2 + y_+^2) F_i + 2\kappa \sqrt{F_i F_{-i}} (x_+ c_i - y_+ s_i) \right],$$

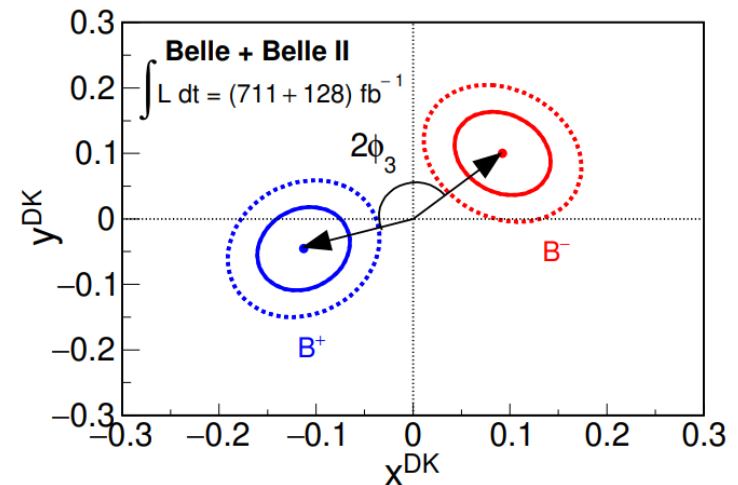
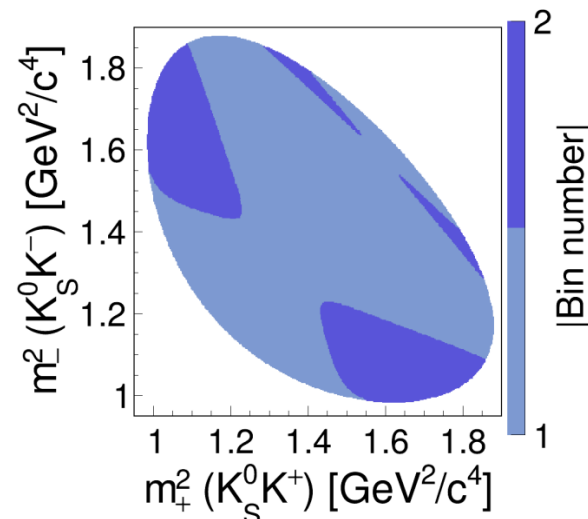
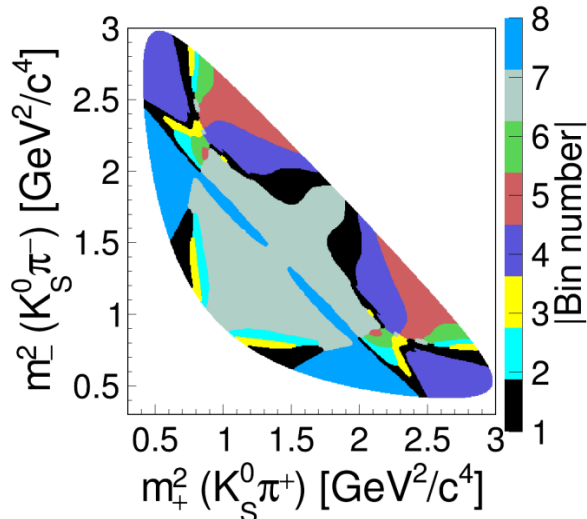
$$N_i(\bar{B}^0) = h^{\bar{B}^0} \left[F_i + (x_-^2 + y_-^2) F_{-i} + 2\kappa \sqrt{F_i F_{-i}} (x_- c_i + y_- s_i) \right],$$

$$x_\pm \equiv r_{B^0} \cos(\delta_{B^0} \pm \gamma),$$

$$y_\pm \equiv r_{B^0} \sin(\delta_{B^0} \pm \gamma).$$

$$\gamma = \phi_3 = (78.4 \pm 11.4(\text{stat}) \pm 0.5(\text{syst}) \pm 1.0(\text{ext}))^\circ$$

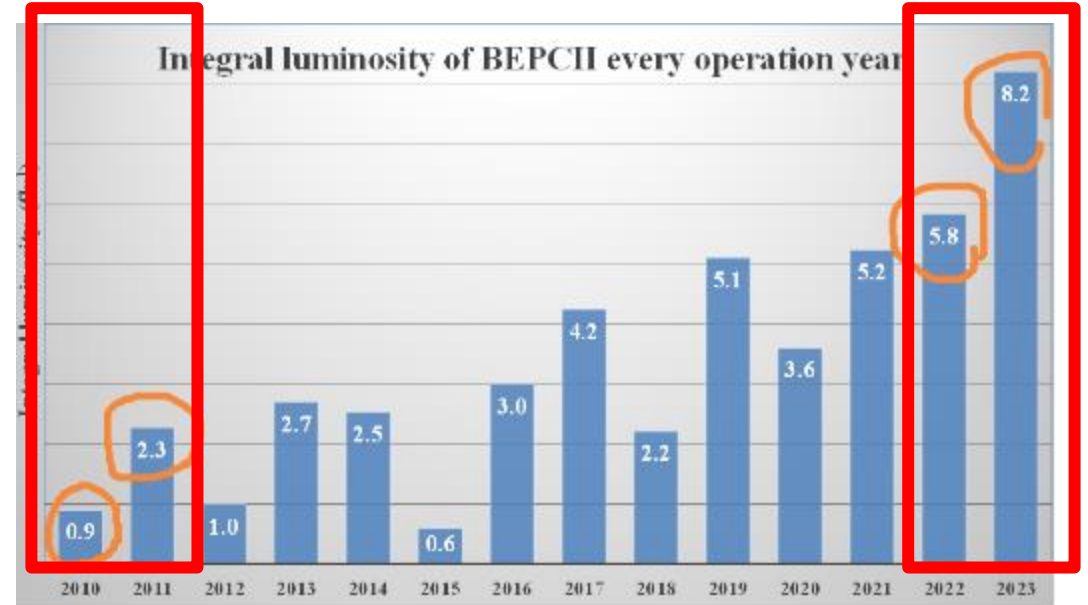
JHEP 02 (2022) 063



mode	Para.	Ref.
$D^0 \rightarrow K_S^0 \pi^+ \pi^-$	Strong phase	PRD 101 (2020) 112002
$D^0 \rightarrow K_S^0 K^+ K^-$	Strong phase	PRD 102 (2020) 052008
$D^0 \rightarrow K^+ \pi^-$	Strong phase	EPJC 82 (2022) 1009
$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$	Strong phase	arXiv:2103.05988
$D^0 \rightarrow K^+ K^- \pi^+ \pi^-$	Strong phase	arXiv:2212.06489
$D^0 \rightarrow K^+ K^- \pi^+ \pi^-$	CP-even fraction	arXiv:2305.03975
$D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	CP-even fraction	arXiv:2208.10098

Used for D parameters

To be used



- Current BESIII measurements of D^0 strong-phase parameters used 3 fb^{-1} of $\psi(3770) \rightarrow D\bar{D}$ data
- BESIII will accumulate 20 fb^{-1} of $\psi(3770) \rightarrow D\bar{D}$ data this year
- Significant improvements in D^0 decay parameters are expected

Summary

- LHCb has achieved unprecedented precision in study of beauty CP violation, pushing flavour physics into a new era
- Belle II is ramping up and producing interesting physics results

