

# 相对论重离子碰撞中QCD相图的实验研究



罗晓峰

华中师范大学

QCD and Medium to High Energy Nuclear Physics Summer School



## 古希腊唯物主义哲学家：德谟克利特(~公元前370年) 率先提出原子论（万物由原子构成）

马克思和恩格斯赞美他是古希腊人中“第一个百科全书式的学者”

**“一尺之棰，日取其半，万世不竭”《庄子-天下篇》**

~ 公元前300年



**物质是否无限可分？  
组成我们物质世界的基本单元是什么？**







# More is different – 多即不同

<http://science.sciencemag.org/content/177/4047/393>

4 August 1972, Volume 177, Number 4047

## SCIENCE

### 凝聚态物理的<<独立宣言>>

#### More Is Different

Broken symmetry and the nature of the hierarchical structure of science.

P. W. Anderson

The reductionist hypothesis may still be a topic for controversy among philosophers, but among the great majority of active scientists I think it is accepted without question. The workings of our minds and bodies, and of all the animate or inanimate matter of which we have any detailed knowledge, are assumed to be controlled by the same set of fundamental laws, which except under certain extreme conditions we feel we know pretty well.

It seems inevitable to go on uncritically to what appears at first sight to be an obvious corollary of reductionism: that if everything obeys the same fundamental laws, then the only scientists who are studying anything really fundamental are those who are working on those laws. In practice, that amounts to some astrophysicists, some elementary particle physicists, some logicians and other mathematicians, and few others. This point of view, which it is the main purpose of this article to oppose, is expressed in a rather well-known passage by Weiskopf (1):

Looking at the development of science in the Twentieth Century one can distinguish two trends, which I will call "intensive" and "extensive" research, lacking a better terminology. In short: intensive research goes for the fundamental laws, extensive research goes for the ex-

planation of phenomena in terms of known fundamental laws. As always, distinctions of this kind are not unambiguous, but they are clear in most cases. Solid state physics, plasma physics, and perhaps also biology are extensive. High energy physics and a good part of nuclear physics are intensive. There is always much less intensive research going on than extensive. Once new fundamental laws are discovered, a large and ever increasing activity begins in order to apply the discoveries to hitherto unexplained phenomena. Thus, there are two dimensions to basic research. The frontier of science extends all along a long line from the newest and most modern intensive research, over the extensive research recently spawned by the intensive research of yesterday, to the broad and well developed web of extensive research activities based on intensive research of past decades.

The effectiveness of this message may be indicated by the fact that I heard it quoted recently by a leader in the field of materials science, who urged the participants at a meeting dedicated to "fundamental problems in condensed-matter physics" to accept that there were few or no such problems and that nothing was left but extensive science, which he seemed to equate with device engineering.

The main fallacy in this kind of thinking is that the reductionist hypothesis does not by any means imply a "constructionist" one: The ability to reduce everything to simple fundamental laws does not imply the ability to start from those laws and reconstruct the universe. In fact, the more the elementary particle physicists tell us about the nature of the fundamental laws, the

less relevance they seem to have to the very real problems of the rest of science, much less to those of society.

The constructionist hypothesis breaks down when confronted with the twin difficulties of scale and complexity. The behavior of large and complex aggregates of elementary particles, it turns out, is not to be understood in terms of a simple extrapolation of the properties of a few particles. Instead, at each level of complexity entirely new properties appear, and the understanding of the new behaviors requires research which I think is as fundamental in its nature as any other. That is, it seems to me that one may array the sciences roughly linearly in a hierarchy, according to the idea: The elementary entities of science X obey the laws of science Y.

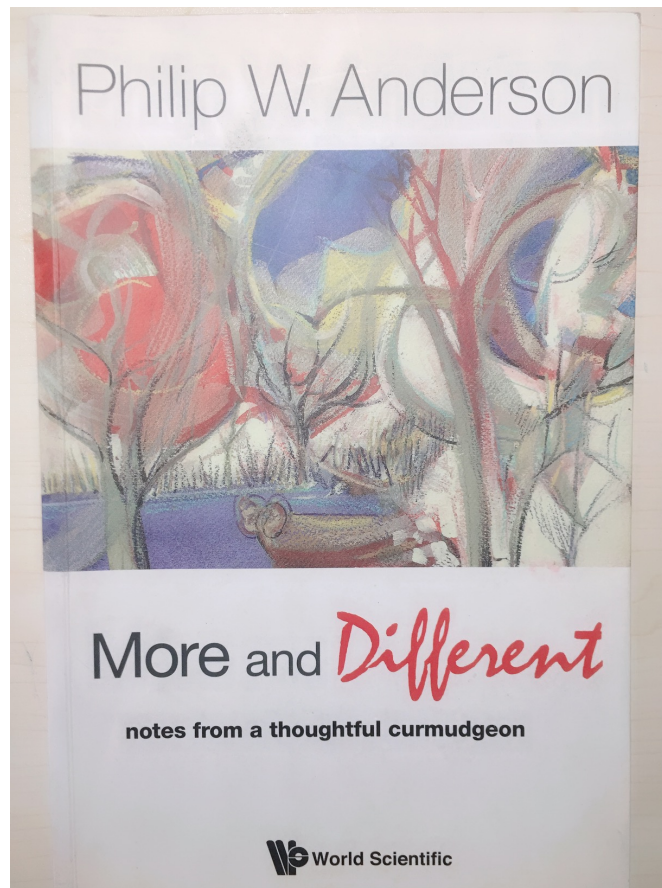
X	Y
solid state or many-body physics	elementary particle physics
chemistry	many-body physics
molecular biology	chemistry
cell biology	molecular biology
·	·
·	·
psychology	physiology
social sciences	psychology

But this hierarchy does not imply that science X is "just applied Y." At each stage entirely new laws, concepts, and generalizations are necessary, requiring inspiration and creativity to just as great a degree as in the previous one. Psychology is not applied biology, nor is biology applied chemistry.

In my own field of many-body physics, we are, perhaps, closer to our fundamental, intensive underpinnings than in any other science in which non-trivial complexities occur, and as a result we have begun to formulate a general theory of just how this shift from quantitative to qualitative differentiation takes place. This formulation, called the theory of "broken symmetry," may be of help in making more generally clear the breakdown of the constructionist converse of reductionism. I will give an elementary and incomplete explanation of these ideas, and then go on to some more general speculative comments about analogies at

The author is a member of the technical staff of the Bell Telephone Laboratories, Murray Hill, New Jersey 07971, and visiting professor of theoretical physics at Cavendish Laboratory, Cambridge, England. This article is an expanded version of a Regener Lecture given in 1967 at the University of California, La Jolla.

## 安德森 (1923-): 美国理论物理学家 “对磁性和无序体系电子结构的基础 理论研究”获1977年诺贝尔物理学奖







# Quantum Chromodynamics (QCD)



The Nobel Prize in Physics 2004

"for the discovery of asymptotic freedom in the theory of the strong interaction"



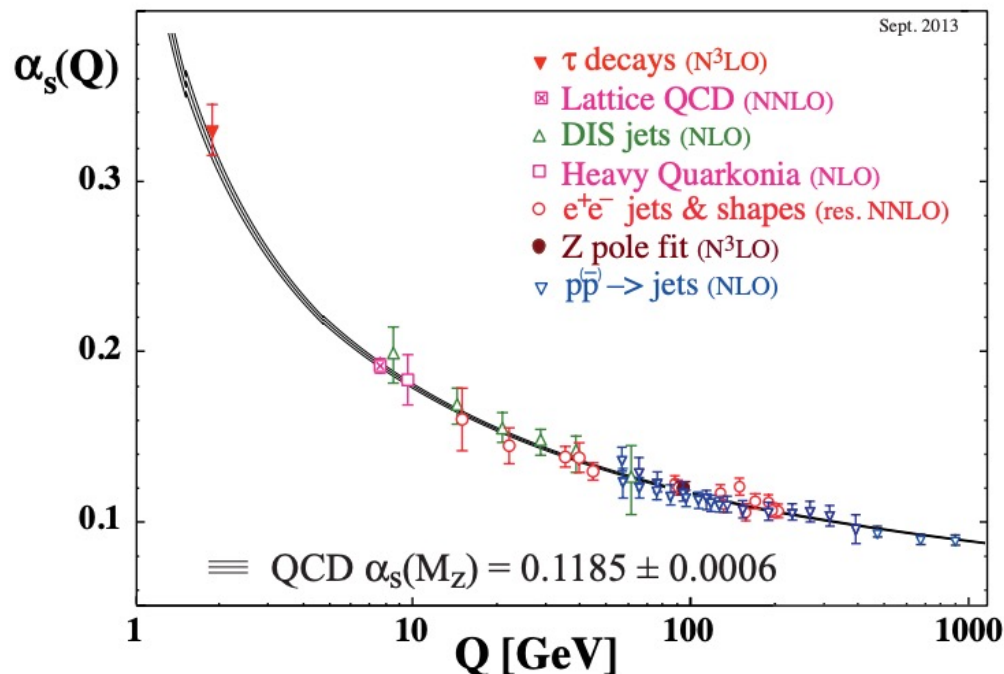
David J. Gross



H. David Politzer



Frank Wilczek



➤ **Asymptotic freedom:** Quarks and Gluons weakly interacting

1): when getting close

2): large momentum transfer.

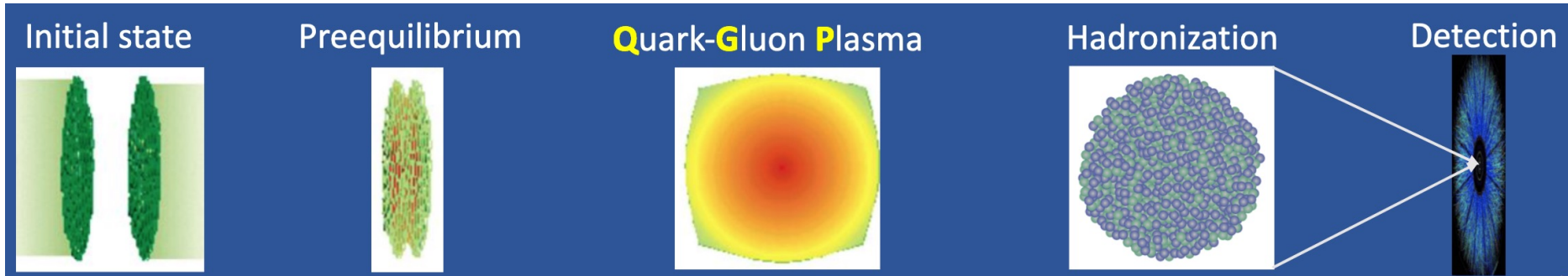
➤ **Color Confinement**

如何研究夸克层次的凝聚态物理？

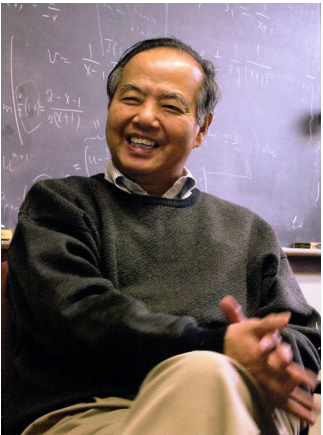
Free the quarks and gluons from hadrons !



# 相对论重离子碰撞：加热到万亿度( $10^{12}$ °C)！！



人类目前为止制造的最高温度：约为太阳中心温度的10万倍。



**T. D. Lee (1926-)**

获得1957年诺贝尔物理学奖

T. D. Lee and G. C. Wick, Phys. Rev. D 9, 2291 (1974).  
Vacuum stability and vacuum excitation in a spin-0 field theory.



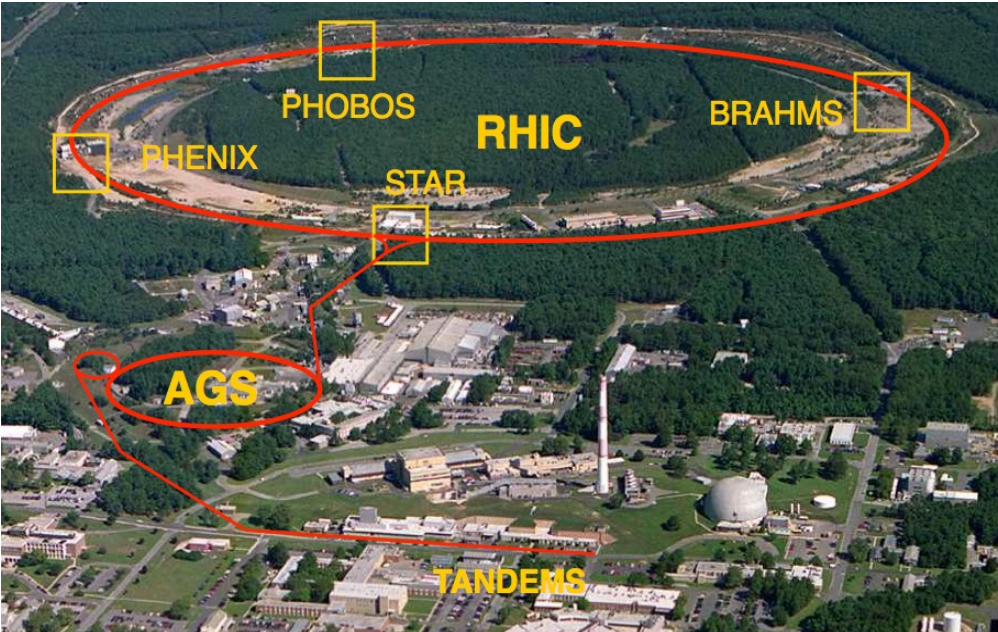
太阳核心温度：20000000 K (夸克仍被禁闭在强子中)

重离子被加速到接近光速发生对撞，创造出高温高密环境使夸克解禁闭形成夸克胶子等离子体。





# High Energy Nuclear Collision Experiments



## RHIC@BNL, USA

- RHIC: The high energy heavy-ion collider  $\sqrt{s} = 200 - 7.7$  GeV
- RHIC: The highest energy polarized proton collider (500 GeV)



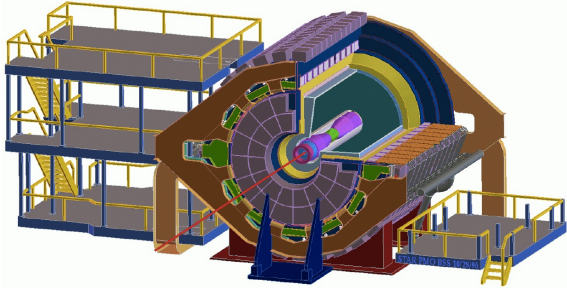
## Large Hadron Collider

## LHC@CERN, Geneva

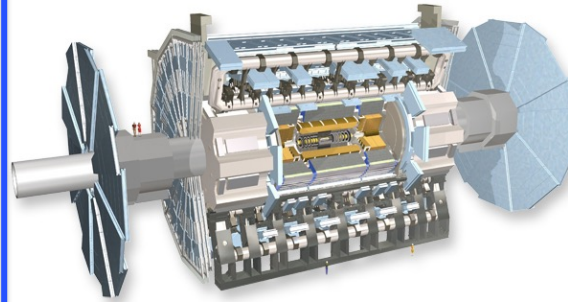
- LHC: The highest energy heavy-ion collider  $\sqrt{s} = 5.4$  TeV
- LHC: The highest energy proton collider  $\sqrt{s} = 14$  TeV



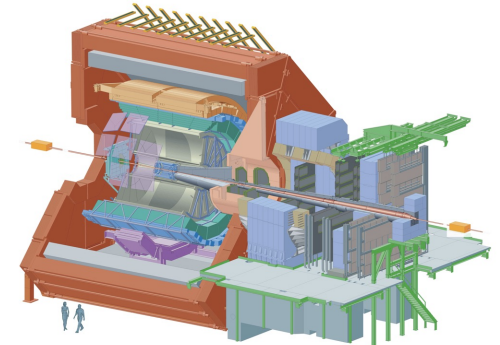
# RHIC和LHC上的高能物理实验



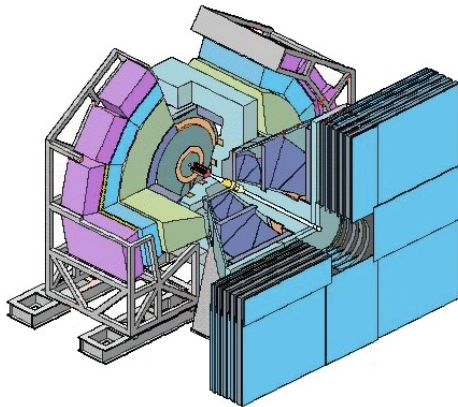
**STAR**



**ATLAS**

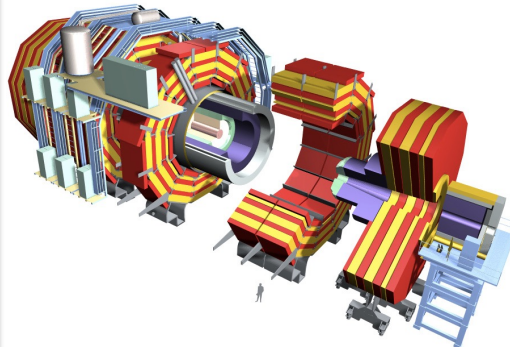


**ALICE**



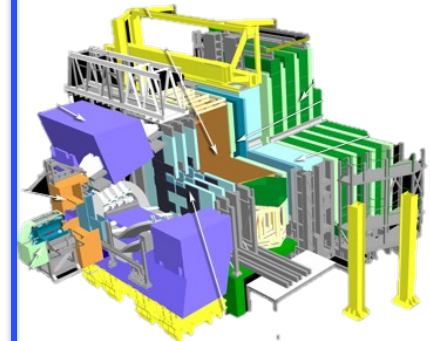
**PHENIX**

*Higgs Discovery*



**CMS**

*Pentaquark*



**LHCb**



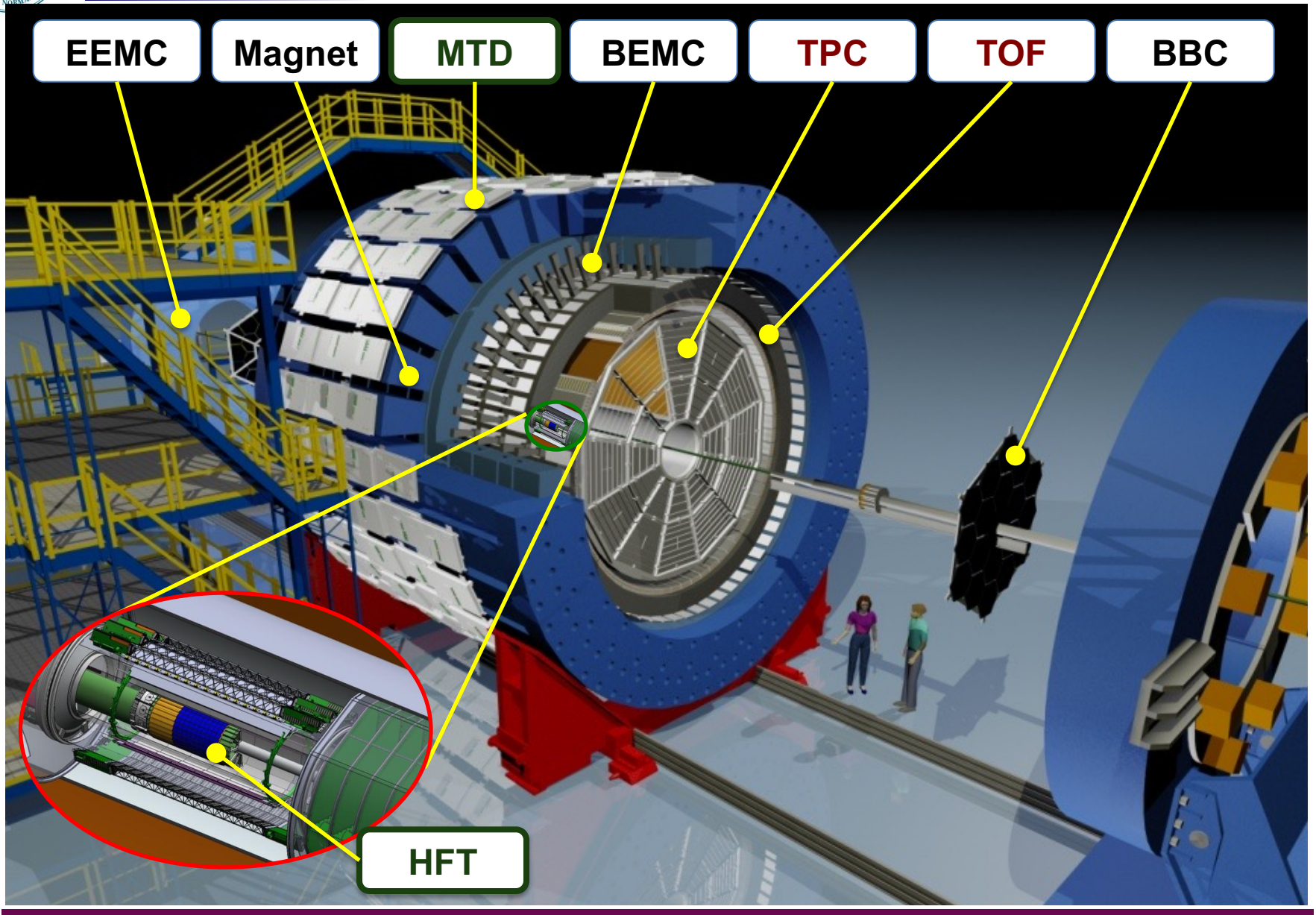
# STAR Collaboration







# STAR Detector System







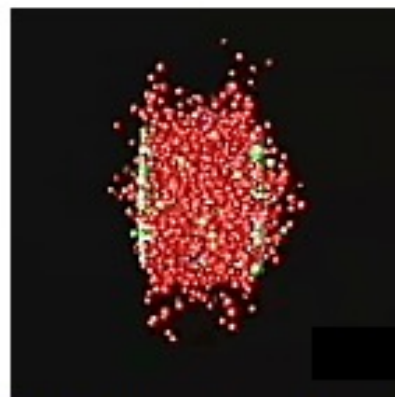
# 研究课题



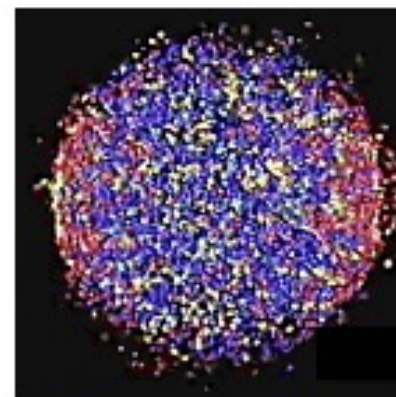
1. Ions about to collide\*



2. Ion collision

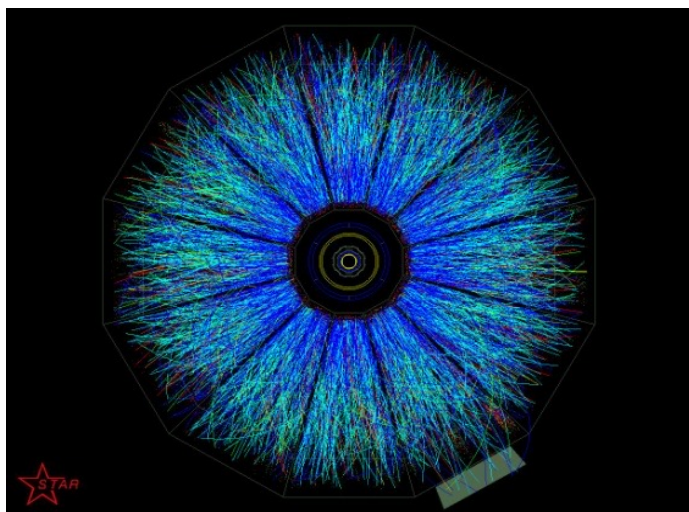


3. Quarks, gluons freed



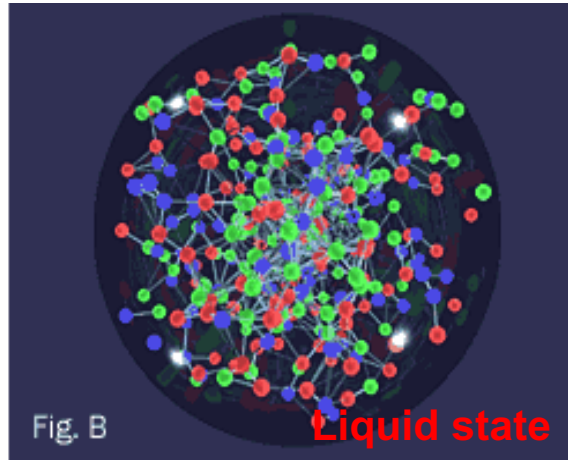
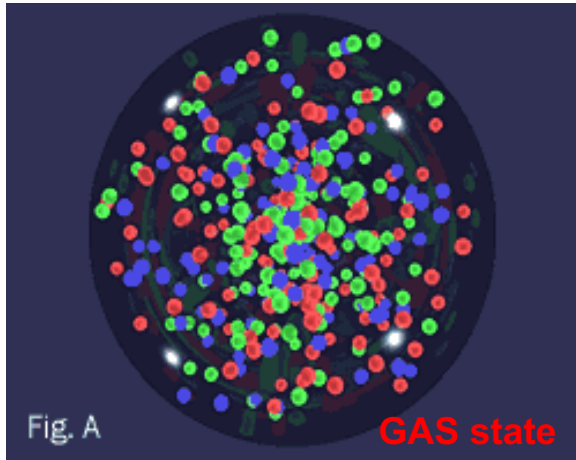
4. Plasma created

STAR时间投影室探测到的带电粒子径迹



- 1、夸克胶子等离子体性质：集体流、奇异粒子产生、重味以及喷注、两粒子关联、双轻子产生等
- 2、QCD相图结构、寻找QCD相变临界点：守恒荷涨落与关联、轻核产生、间歇等
- 3、新粒子以及奇异粒子态：超核、反物质等
- 4、QCD真空性质与强电磁场：手征磁效应、手征磁波超子极化、UPC光光相互作用

# Scientists Serve Up “Perfect” Liquid



Quark matter studied in nuclear collisions, since 1987 at BNL/AGS (2.7-4.8 GeV), 1996 at CERN/SPS (6.2-17.3 GeV), since 2000 at BNL/RHIC (7.7-200 GeV), since 2010 at the CERN/LHC at  $\sqrt{s_{NN}} = 2.76-5.02$  TeV.

Experimental observations support the formation of **strongly couple and liquid like** Quark-Gluon Plasma (sQGP) in Heavy-ion Collisions.

- Low viscosity
- Rapid thermalization
- Heavy quark suppression and Jet quenching
- Partonic collectivity
- Strong electromagnetic field and large vorticity

**RHIC White Paper  
2005 :**

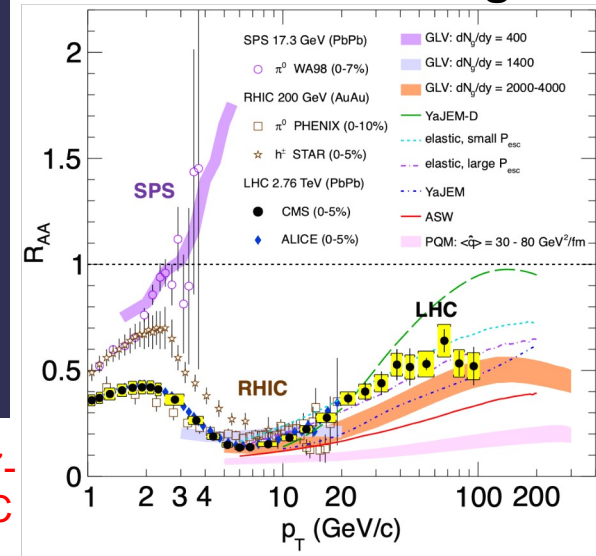
## Hunting the Quark Gluon Plasma

RESULTS FROM THE FIRST 3 YEARS AT RHIC

ASSESSMENTS BY THE EXPERIMENTAL COLLABORATIONS

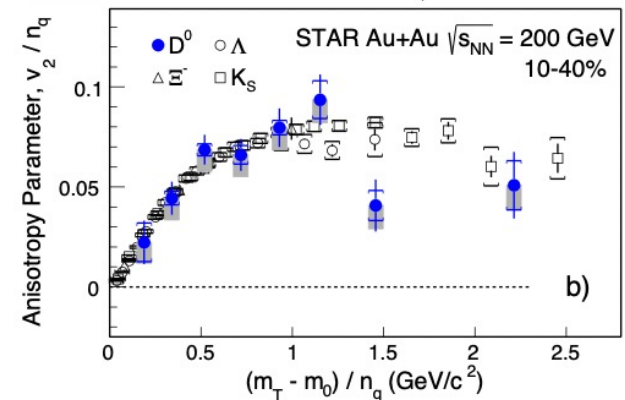
April 18, 2005

## Jet Quenching



Eur.Phys.J. C72,1945 (2012).

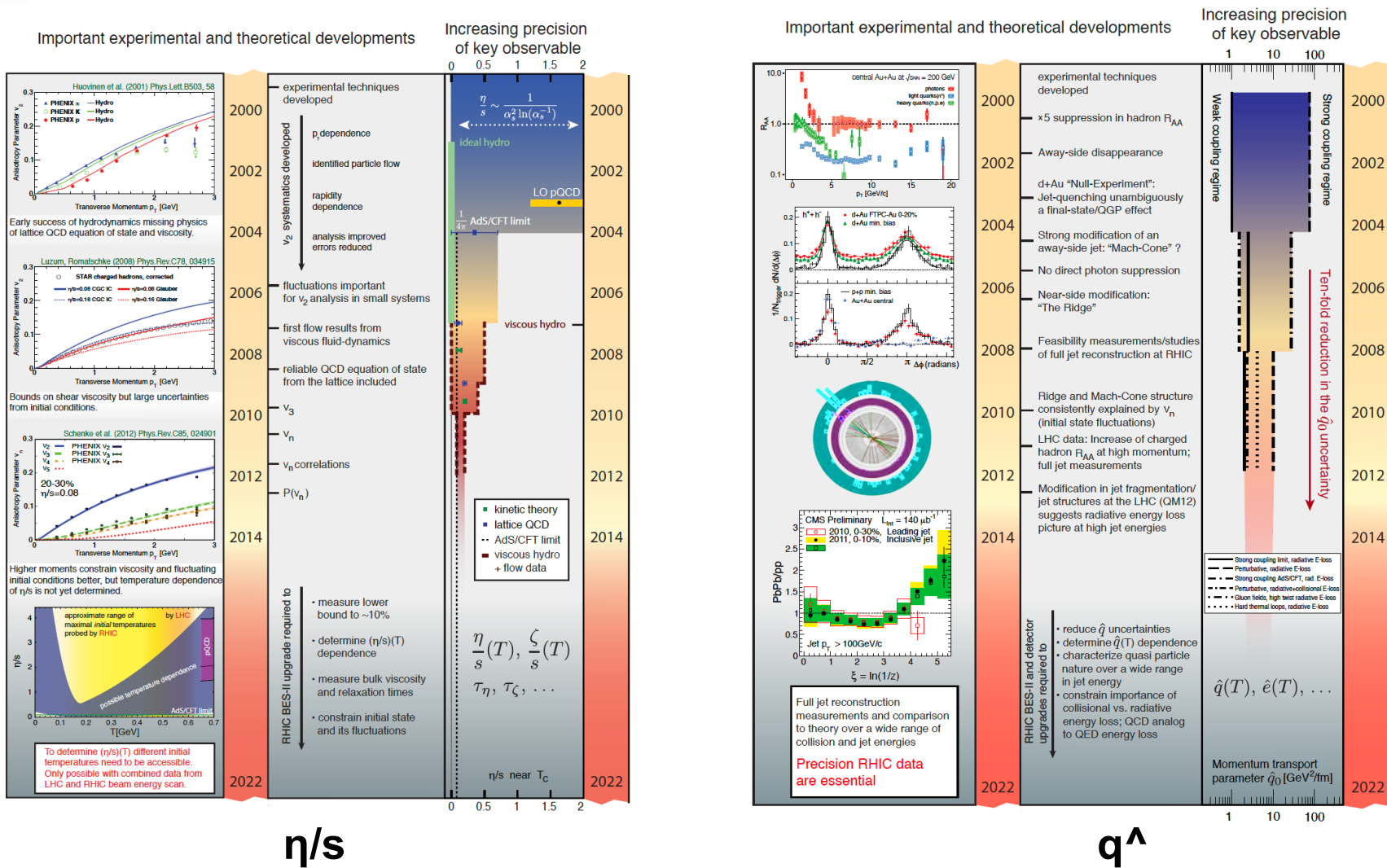
## Partonic Collectivity $v_2$



Phys. Rev. Lett. **117**, 212301 (2017).



# Quantifying the Properties of Hot and Dense QCD Matter



Hot QCD White Paper, arXiv : 2303.17254

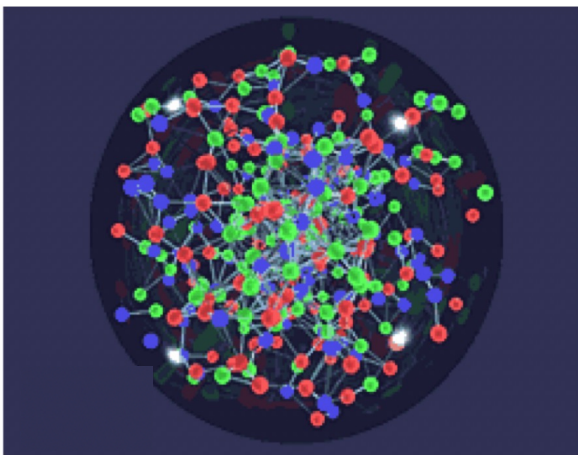
Hot and Dense QCD Matter : [https://www.bnl.gov/npp/docs/bass\\_rhi\\_wp\\_final.pdf](https://www.bnl.gov/npp/docs/bass_rhi_wp_final.pdf)





# QGP物质形态与相变

## QGP新物态

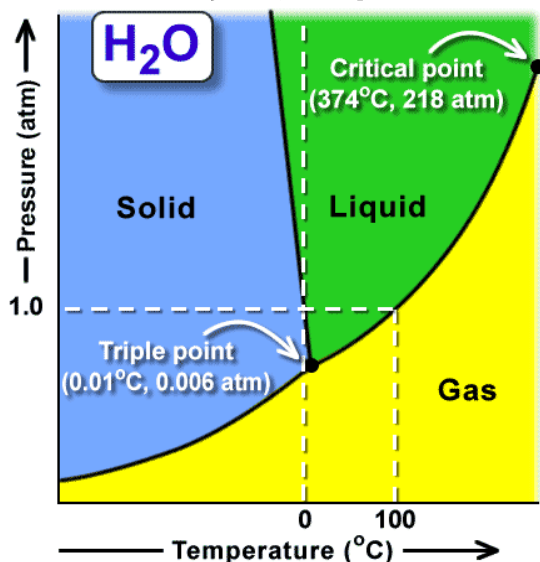


一定温度和密度下的热力学性质，如：

- 状态方程
- 粘滞系数
- 输运系数

改变外部条件：研究发生相变形成QGP的条件和信号，探索相结构，一级相变边界、临界点？

## 水的相图

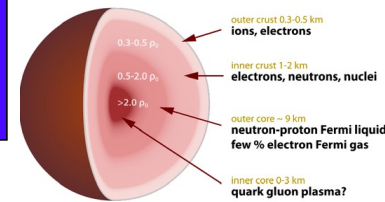
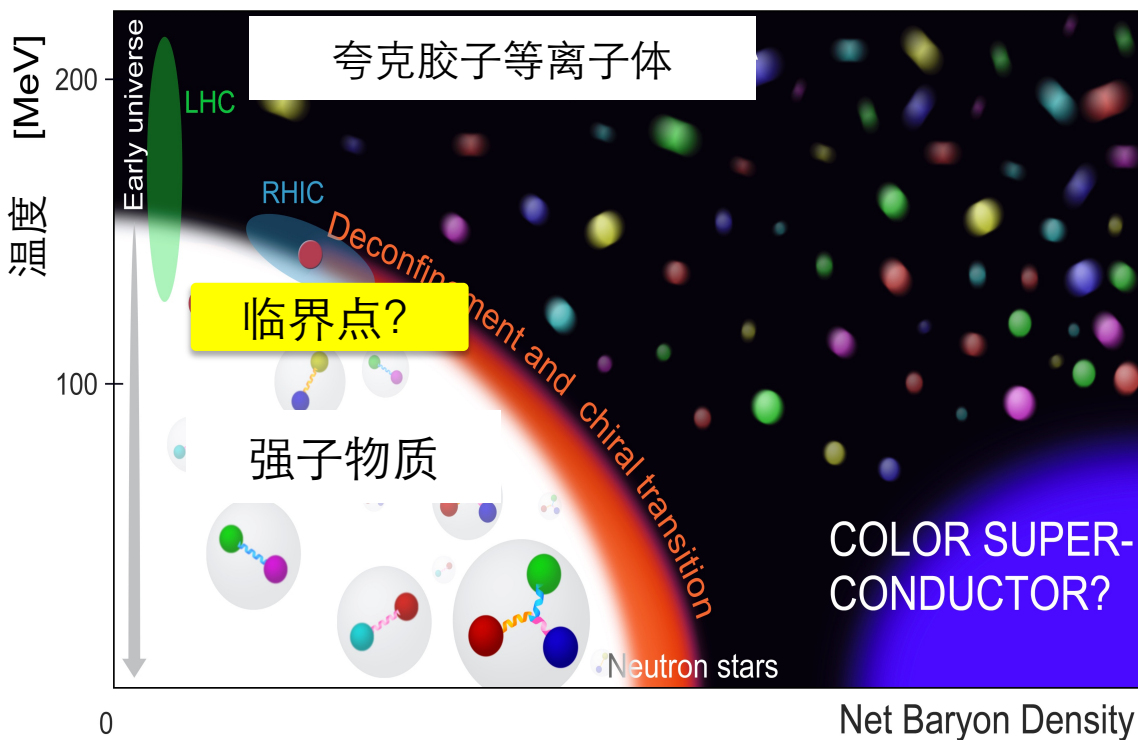
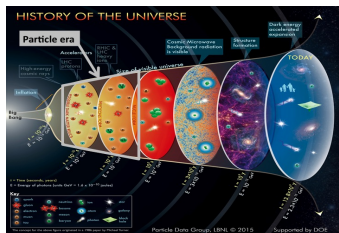


内因：相互作用、系统对称性  
外因：外部条件的改变

水的固液气相变：  
电磁相互作用主导

# 强相互作用 (QCD) 物质相图

QCD相图结构被发现杂志评为：本世纪物理学11大未解决难题之一



Smooth Crossover at  $\mu_B=0$ .

Transition Temperature :  $T_c \sim 156$  MeV

Y. Aoki, et al. Nature 443, 675 (2006).

A. Bazavov et al.(HotQCD), Phys. Lett. B 795, 15 (2019)

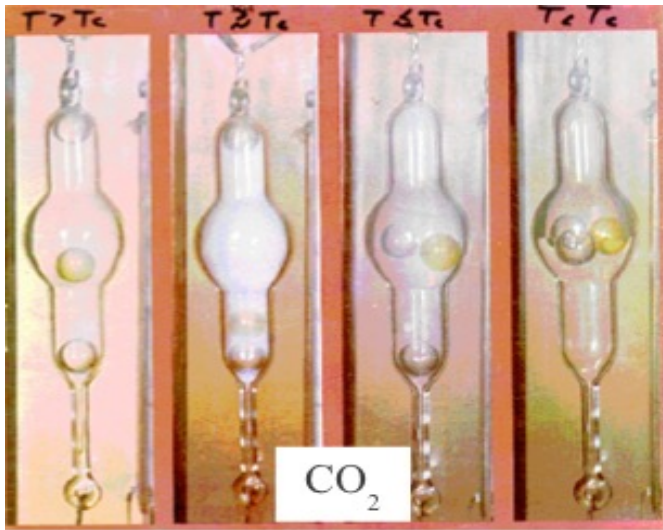
**关键科学问题：高重子密度区是否存在一级相变边界和对应的相变临界点。**

马余刚、许怒、刘峰，基于HIAF集群的QCD相结构研究，中国科学:物理学 力学 天文学,2020,50(11):124



# 临界点和临界现象

T. Andrews. Phil. Trans. Royal Soc., 159:575, 1869.



First CP is discovered in 1869 for CO<sub>2</sub> by Andrews.

$$T_c = 31^\circ\text{C}$$

Can we discover the critical point of quark matter ?

$$T_c \sim \text{Trillion } (10^{12})^\circ\text{C}$$

- **临界点：一级相变线终结点，发生二级相变**
- **密度涨落增强与关联长度增大：临界乳光现象**
- **系统的对称性决定临界指数：即热力学的临界发散行为**
- **有限尺度效应.**



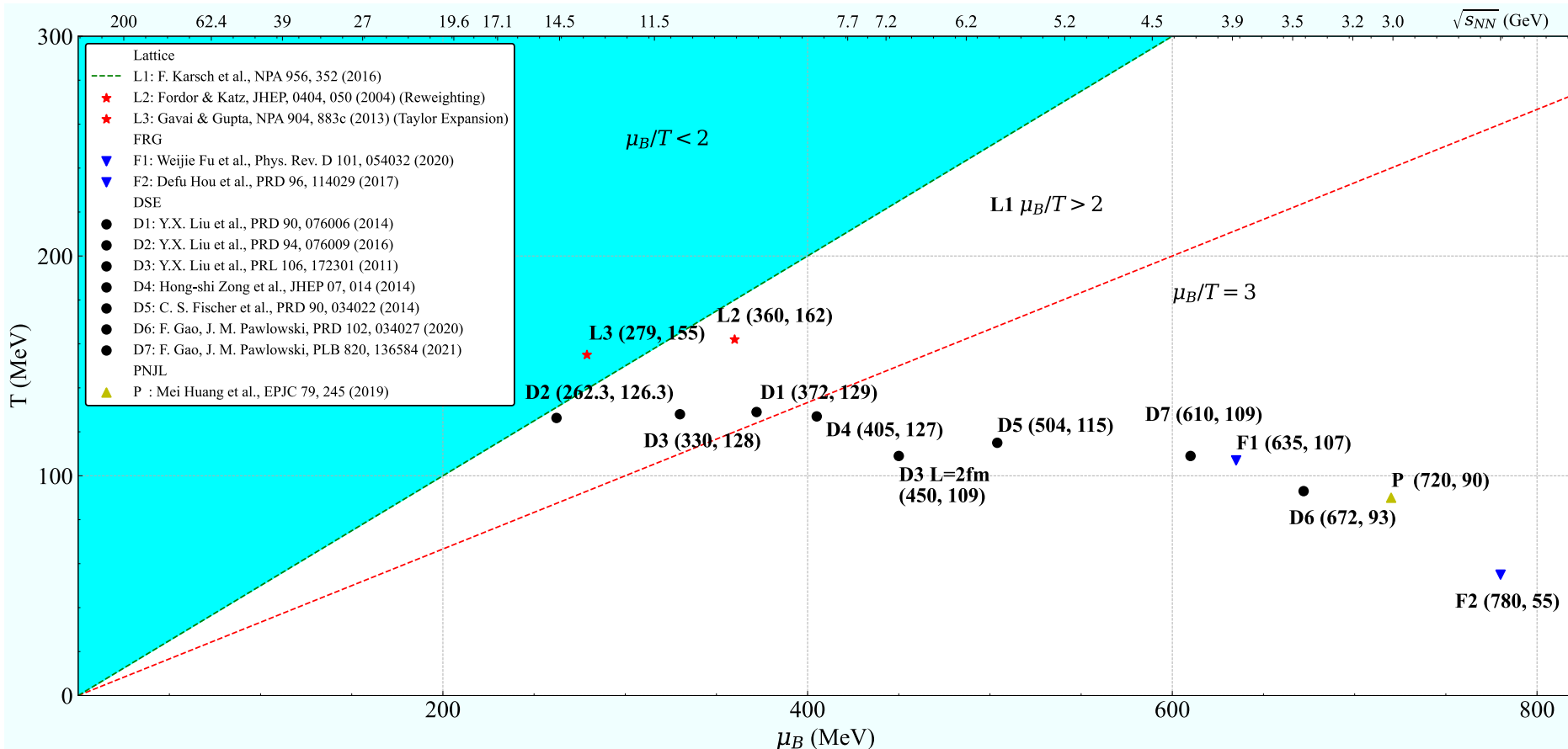
科普书(国家科技进步奖获奖丛书)  
**边缘奇迹：相变和临界现象**  
于淦, 郝柏林, 陈晓松 著





# QCD临界点位置：理论模型计算

Preliminary collection from Lattice, DSE, FRG and PNJL (2004-2021)

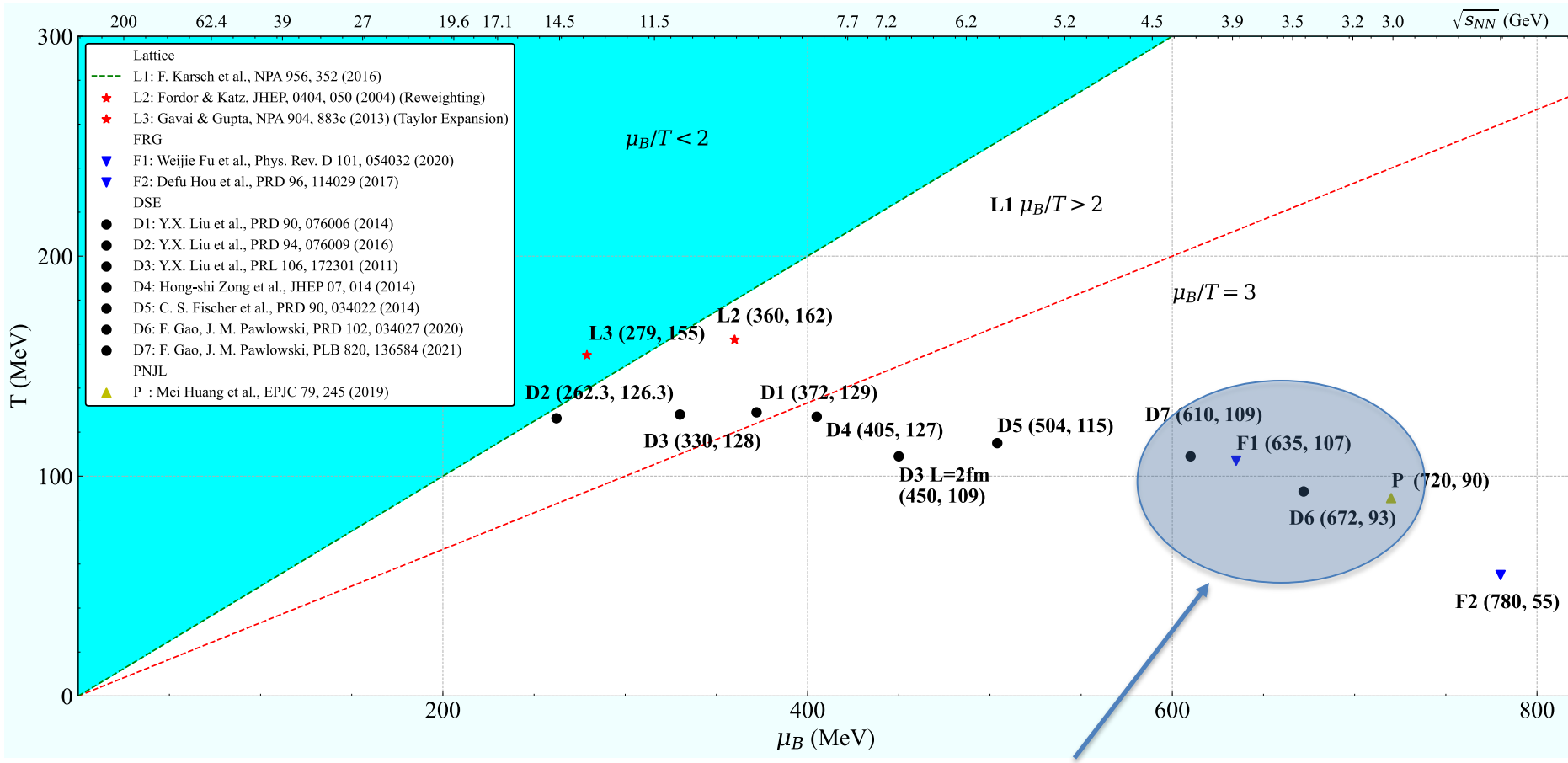


理论上确定QCD相变临界点的位置有较大的不确定性。



# QCD临界点位置：理论模型计算

Preliminary collection from Lattice, DSE, FRG and PNJL (2004-2021)



- 格点QCD:  $\mu_B/T_c > 2$
- DSE、FRG (临界点重子化学势范围  $\mu_B \sim 600 - 670$  MeV).



# Relativistic “Minds” Collisions (2006.03)



Organizers: T. Ludlam, H. Ritter, G. Stephans, M. Gazdzicki, B. Friman, F. Videbaek, T. Satogata, K. Rajagopal, L. McLerran  
<https://www.bnl.gov/riken/QCDRhic/default.asp>

## Motivation & Plans

The workshop is motivated by a growing body of theoretical and experimental evidence that the critical point on the QCD phase diagram, if it exists, should appear on the QGP transition boundary at baryo-chemical potential  $\sim 100 - 500$  MeV, corresponding to heavy ion collisions with c.m. energy in the range 5 - 50 GeV/u. **Identifying and pinning down this point with experimental measurements would be a major step forward in the world-wide effort to determine the properties of QCD at high temperature and density.**

### Thursday, March 9

8:30 – 9:00	Registration	
Chair: T. Ludlam		
9:00 – 9:10	Welcome	T. Ludlam (10)
9:10 – 9:50	Introduction and overview	K. Rajagopal (35+5)
9:50 – 10:25	Lattice results on the QCD critical point	F. Karsch (30+5)
10:25	Break (15)	
10:40 – 11:05	Fluctuations at the critical point	M. Stephanov (20+5)
11:05 – 11:40	Experimental overview & prospects for RHIC	G. Roland (30+5)
11:40 – 12:15	RHIC machine considerations	T. Satogata (30+5)
12:15	Lunch	
Chair: George Stephans		
1:30 – 2:00	Excitation function – NA 49 results	P. Seyboth (25+5)
2:00 – 2:30	Excitation function—onset of deconfinement	E. Shuryak (25+5)
2:30 – 2:50	Soft mode of the QCD critical point	H. Fujii (15+5)
2:50 – 3:10	Baryon number fluctuation near the critical point	Y. Hatta (15+5)
3:10	Break (15)	
3:25 – 3:55	Hydro evolution near the QCD critical point	C. Nonaka (15+5)
3:55 – 4:25	Future prospects for the CERN SPS	M. Gazdzicki (25+5)
4:25 – 5:00	Experiments with PHENIX near the critical point	P. Steinberg (25+10)
5:00 – 5:35	Experiments with STAR near the critical point	T. Nayak (25+10)
6:15	Reception and dinner	

### Friday, March 10

Chair: F. Videbaek		
8:30 – 9:30	Low energy operation of RHIC: AGS low energy extraction performance Luminosity monitoring issues Low energy electron cooling	N. Tsoupas (15+5) A. Drees (15+5) A. Fedotov (15+5)
9:30 – 10:00	Energy dependence of temperature and baryochemical potential	K. Redlich (25+5)
10:00 – 10:25	Observable power laws at the QCD critical point	N. Antoniou (20+5)
10:25	Break (15)	
10:40 – 11:10	The CBM experiment at FAIR	P. Senger (25+5)
11:10 – 11:35	Excitation function – experimental perspective	N. Xu (20+5)
11:35 – 12:00	Experience with CERES	H. Appelshauser (20+5)
12:00 – 12:25	Critical point at SPS energy?	R. Stock (20+5)
12:25	Lunch	
Chair: L. McLerran		
2:00 – 2:30	Lattice calculations at finite baryon potential	Z. Fodor (25+5)
2:30 – 3:00	Fluctuations and correlations	V. Koch (25+5)
3:00 – 3:25	Hadron production and phase changes	J. Rafelski (20+5)
3:25 – 3:45	Can we discover the first-order phase transition at RHIC?	J. Randrup (15+5)
3:45	Break (15)	
4:00 – 4:20	Signals of the first order phase transition	H. Stoecker (15+5)
4:20 – 5:30	Summary/discussion – prospects for experiments at RHIC	Discussion Leaders : H.-G. Ritter & T. Roser
5:30	Adjourn	

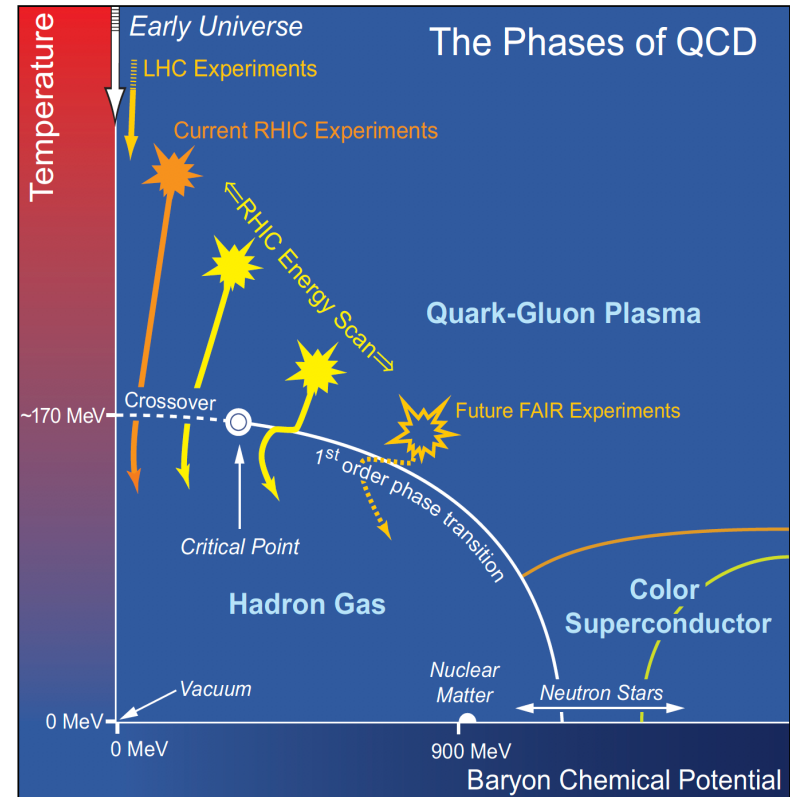
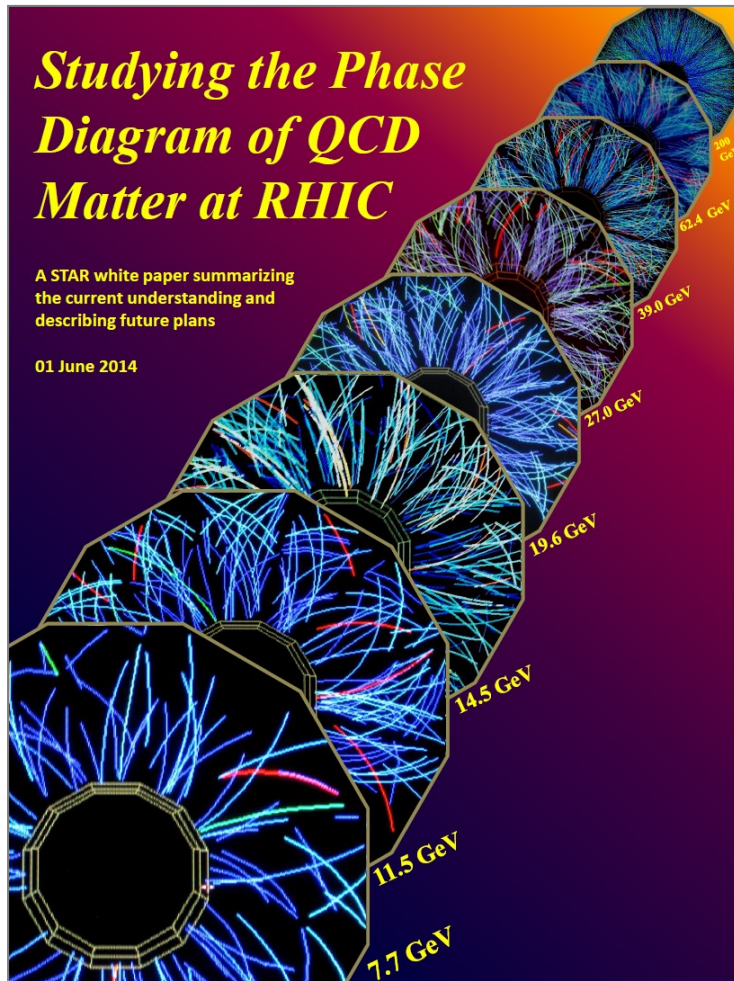




# STAR Beam Energy Scan Adventure

## BES-II White Paper (2014)

- BES first proposed to PAC 2006.
- STAR BES campaign formally started in 2010
- BES-II officially requested in 2014, starts 2019(18)



## Main Motivation:

- Looking for turning off QGP signals observed at RHIC top energy.
- Mapping out the crossover and/or 1<sup>st</sup> order QCD phase boundary
- Search for the signatures of possible QCD critical point.

STAR, arXiv:1007.2613

<https://drupal.star.bnl.gov/STAR/starnotes/public/sn0493>

<https://drupal.star.bnl.gov/STAR/starnotes/public/sn0598>



# Fluctuations Probes the QCD Phase Transition

## 1. Fluctuations signals the QCD Critical Point.

热力学强度量与延展量的涨落相关

M. Stephanov, K. Rajagopal, E. Shuryak, Phys. Rev. Lett. 81, 4816 (1998).  
M. Stephanov, K. Rajagopal, E. Shuryak, Phys. Rev. D 60, 114028 (1999).

比热 -> 能量涨落  
不可压缩系数->粒子数涨落

## 2. Fluctuations signals the Quark Deconfinement.

S. Jeon and V. Koch, Phys. Rev. Lett. 85, 2076(2000).  
M. Asakawa, U. Heinz and B. Muller, Phys. Rev. Lett. 85, 2072 (2000).



系统关联长度

Two-point correlation functions of magnetic moment:

$$G(\vec{r}) = \langle S(\vec{r})S(0) \rangle - \langle S(\vec{r}) \rangle \langle S(0) \rangle$$

In 3D case:  $G(\vec{r}) \propto \frac{1}{r} e^{-r/\xi(t)}$        $\xi(t) = \xi_0 |t|^{-1/2}$   
t : reduced temperature

**Susceptibility**  
**(2<sup>nd</sup> fluctuations)**

$$\chi \propto \int G(\vec{r}) d\vec{r} \propto \xi^2(t)$$

**Correlation length**



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比热 -> 能量涨落

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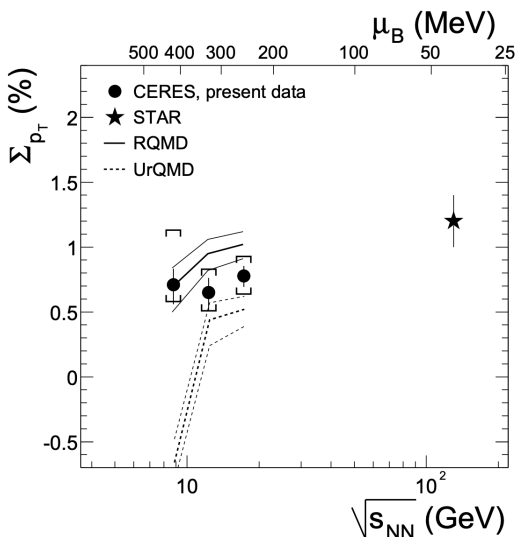
S. Jeon and V. Koch, Phys. Rev. Lett. 85, 2076(2000).

M. Asakawa, U. Heinz and B. Muller, Phys. Rev. Lett. 85, 2072 (2000).



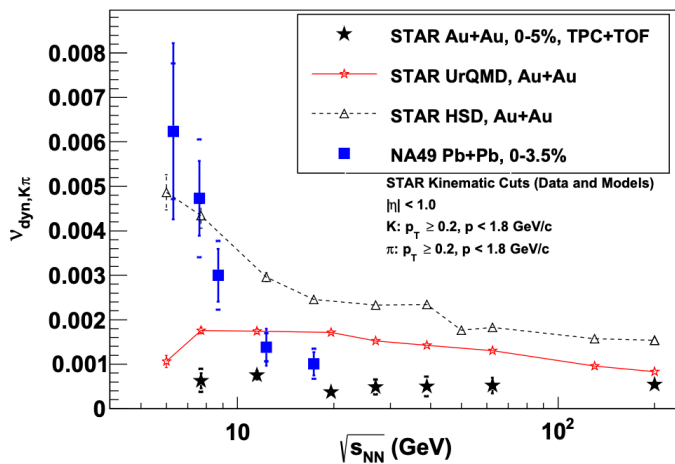
系统关联长度

### Mean $p_T$ fluctuations



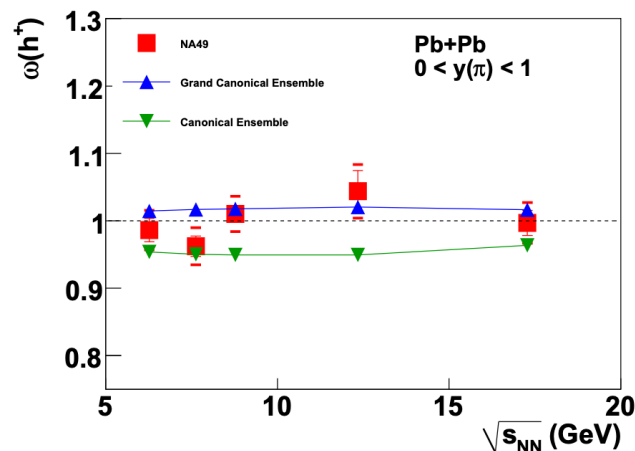
CERES, Nucl. Phys. A 727:97,2003  
STAR, Phys. Rev. C 99 (2019) 44918

### Particle ratio fluctuations



STAR, Phys. Rev. C 92 (2015) 21901  
NA49, Phys. Rev. Lett. 86 (2001) 1965

### Multiplicity fluctuations



NA49, Phys. Rev. C 78 (2008) 034914





# INT 2008-2b : The QCD Critical Point

**Organizer:** <https://www.int.washington.edu/PROGRAMS/08-2b.html>

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Lawrence Berkeley National Laboratory  
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July 28, 2008	S. Gupta	<a href="#">"New results in QCD at finite <math>\mu</math>"</a>
July 29, 2008	M.P. Lombardo	<a href="#">"The QCD critical point at imaginary <math>\mu</math>"</a>
July 29, 2008	S. Ejiri	<a href="#">"Numerical study of the critical point in lattice QCD at high temperature and density"</a>
July 30, 2008	K. Fukushima	<a href="#">"What can we learn from model studies on the chiral critical end-point?"</a>
July 30, 2008	B. Klein	<a href="#">"Scaling and Finite-Size Scaling Analysis of Critical Behavior in Lattice QCD"</a>
July 31, 2008	J. Braun	<a href="#">"Chiral Phase Boundary from Quark-Gluon Dynamics"</a>
July 31, 2008	C. Ratti	<a href="#">"A quasiparticle model for QCD thermodynamics"</a>
August 4, 2008	J. Verbaarschot	<a href="#">"Phase of the Fermion Determinant and the Phase Diagram of QCD"</a>
August 5, 2008	R. Lacey	<a href="#">"The Role of Energy Scans at RHIC"</a>
August 5, 2008	L. Ferroni	<a href="#">"Space and Phase Space saturation: a simple Bag-Model-inspired picture for a smooth transition to QGP"</a>
August 6, 2008	M. Asakawa	<a href="#">"QCD Critical Point and its Effect on Physical Observables"</a>
August 6, 2008	T. Hell	<a href="#">"Thermodynamics of a Nonlocal PNJL Model for Two and Three Flavors"</a>
August 7, 2008	C. Miao	<a href="#">"QCD Equation of State and Fluctuations on the Lattice"</a>
August 11, 2008	K. Rajagopal	<a href="#">"The Search for the QCD Critical Point Using Lattice QCD Calculations-Part 1"</a> <a href="#">Part 2</a>
August 11, 2008	F. Karsch	<a href="#">"Lattice results on the QCD critical point"</a>
August 11, 2008	J. Randrup	<a href="#">"Spinodal decomposition: A tool for seeing the phase transition?"</a>
August 11, 2008	H. Caines	<a href="#">"STAR and the RHIC Energy Scan"</a>
August 11, 2008	K. Homma	<a href="#">"Fluctuations and Search for the QCD Critical Point"</a>
August 12, 2008	G. Stephans	<a href="#">"Experimental Exploration of the QCD Phase Diagram"</a>
August 12, 2008	K.F. Liu	<a href="#">"Finite Density Phase Transition with Canonical Ensemble Approach"</a>
August 12, 2008	C. Nonaka	<a href="#">"Hydrodynamic Expansion with the QCD Critical Point in Heavy Ion Collisions"</a>
August 12, 2008	M. Mitrovski	<a href="#">"Energy and System Size Dependence of Hadron Production from NA49"</a>
August 12, 2008	T. Schuster	<a href="#">"Energy and System Size Dependence of Fluctuations: NA49 results and NA61 plans"</a>
August 12, 2008	G. Westfall	<a href="#">"K/pi Fluctuations and the Balance Function-Part 1"</a> <a href="#">Part 2</a> <a href="#">Part 3</a>

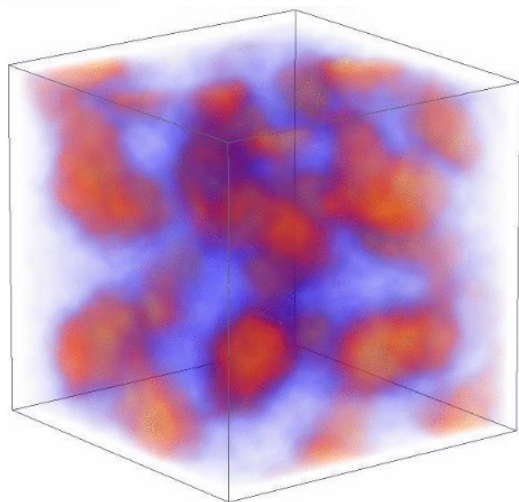
August 13, 2008	K. Redlich	<a href="#">"Charge Fluctuations and transport coefficients near CEP"</a>
August 13, 2008	H. Fujii	<a href="#">"Spectral functions near the QCD critical point in chiral models"</a>
August 13, 2008	R. Karabowicz	<a href="#">"The CBM Experiment"</a>
August 13, 2008	P. Stankus	<a href="#">"Critical Point Scans at RHIC Full Energy"</a>
August 14, 2008	L. McLerran	<a href="#">"The QCD Phase Diagram: The Large N Limit"</a>
August 14, 2008	P. de Forcrand	<a href="#">"Towards a controlled lattice study of the QCD chiral critical point"</a>
August 14, 2008	S. Roessner	<a href="#">"The interplay of flavour- and Polyakov-loop- degrees of freedom --- A PNJL model analysis"</a>
August 14, 2008	J. Liao	<a href="#">"Magnetic Component of Strongly Coupled Quark Gluon Plasma &amp; QCD Phase Diagram from E-M Duality Perspective"</a>
August 14, 2008	H. Stoecker	<a href="#">"Cosmic matter in the Lab: FAIR=The International Facility for Antiproton and Ion Research"</a>
August 15, 2008	R. Scharenberg	<a href="#">"STAR's measurement of long-Range forward backward multiplicity correlations in Heavy Ion central Au-Au collisions at <math>\sqrt{s}=200</math> GeV"</a>
August 15, 2008	D. Blaschke	<a href="#">"Nonlocal Chiral Quark Models &amp; Critical (End-)Point"</a>
August 18, 2008	C. Greiner	<a href="#">"Fast chemical equilibration of hadrons-the importance of multiparticle collisions in heavy ion reactions"</a>
August 19, 2008	K. Mitsuani	<a href="#">"The possible quasi-particle picture of the quark near Tc and its effect on the dilepton production rate"</a>
August 20, 2008	J-W. Chen	<a href="#">"Phase Transitions and the perfectness of Fluids"</a>
August 21, 2008	M. Tachibana	<a href="#">"Spectral Continuity of Hadrons in Dense QCD"</a>

[https://www.int.washington.edu/talks/WorkShops/int\\_08\\_2b/](https://www.int.washington.edu/talks/WorkShops/int_08_2b/)

## Need sensitive experimental observable !!



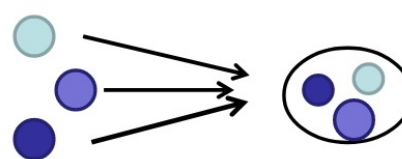
# QCD临界点灵敏观测量：守恒荷高阶矩和轻核产生



In the vicinity of critical point and/or 1<sup>st</sup> order phase transition

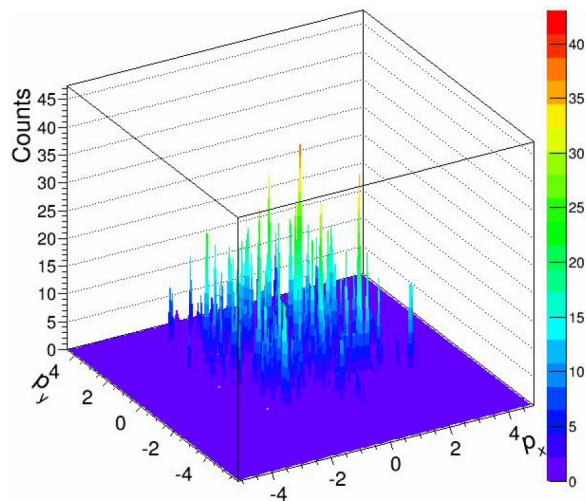


Large density fluctuations and Baryon clustering



Higher moments of conserved charge (B, Q, S) distributions

light nuclei production



**Experimental Signatures:**  
**Non-monotonic variation as a function of collision energy.**



# The history of higher-order fluctuations observables

**Universality, the QCD critical / tricritical point and the quark number susceptibility** #1  
Yoshitaka Hatta (Kyoto U. and Wako, RIKEN), Takashi Ikeda (RIKEN BNL) (Oct, 2002)  
Published in: *Phys.Rev.D* 67 (2003) 014028 • e-Print: [hep-ph/0210284](#) [hep-ph]  
pdf DOI cite 337 citations

**Proton number fluctuation as a signal of the QCD critical endpoint** #2  
Y. Hatta (Kyoto U. and Wako, RIKEN), M.A. Stephanov (Illinois U., Chicago and RIKEN BNL) (Jan, 2003)  
Published in: *Phys.Rev.Lett.* 91 (2003) 102003, *Phys.Rev.Lett.* 91 (2003) 129901 (erratum) • e-Print: [hep-ph/0302002](#) [hep-ph]  
pdf DOI cite 239 citations

**Hadronic fluctuations at the QCD phase transition** #1  
S. Ejiri (Bielefeld U. and Tokyo U.), F. Karsch (Bielefeld U. and Brookhaven), K. Redlich (Wroclaw U. and CERN) (Sep, 2005)  
Published in: *Phys.Lett.B* 633 (2006) 275-282 • e-Print: [hep-ph/0509051](#) [hep-ph]  
pdf links DOI cite 273 citations

**Non-Gaussian fluctuations near the QCD critical point** #7  
M.A. Stephanov (Illinois U., Chicago) (Sep, 2008)  
Published in: *Phys.Rev.Lett.* 102 (2009) 032301 • e-Print: [0809.3450](#) [hep-ph]  
pdf DOI cite 527 citations

**Third moments of conserved charges as probes of QCD phase structure** #5  
Masayuki Asakawa (Osaka U.), Shinji Ejiri (Brookhaven), Masakiyo Kitazawa (Osaka U.) (Apr, 2009)  
Published in: *Phys.Rev.Lett.* 103 (2009) 262301 • e-Print: [0904.2089](#) [nucl-th]  
pdf DOI cite 200 citations

**Using Higher Moments of Fluctuations and their Ratios in the Search for the QCD Critical Point** #24  
Christiana Athanasiou (MIT), Krishna Rajagopal (MIT), Misha Stephanov (Illinois U., Chicago) (Jun, 2010)  
Published in: *Phys.Rev.D* 82 (2010) 074008 • e-Print: [1006.4636](#) [hep-ph]  
pdf DOI cite 148 citations

2002

2003

2005

2008

2009

2010





# Higher Moments of Conserved Quantities (B, Q, S)

- Higher order cumulants/moments: describe the shape of distributions and quantify fluctuations. (sensitive to the correlation length ( $\xi$ ))

$$\langle \delta N \rangle = N - \langle N \rangle$$

$$C_1 = M = \langle N \rangle$$

$$C_2 = \sigma^2 = \langle (\delta N)^2 \rangle$$

$$C_3 = S\sigma^3 = \langle (\delta N)^3 \rangle$$

$$C_4 = \kappa\sigma^4 = \langle (\delta N)^4 \rangle - 3 \langle (\delta N)^2 \rangle^2$$

$$\langle (\delta N)^3 \rangle_c \approx \xi^{4.5}, \quad \langle (\delta N)^4 \rangle_c \approx \xi^7$$

M. A. Stephanov, Phys. Rev. Lett. 102, 032301 (2009).

M. Asakawa, S. Ejiri and M. Kitazawa, Phys. Rev. Lett. 103, 262301 (2009).

M. A. Stephanov, Phys. Rev. Lett. 107, 052301 (2011).

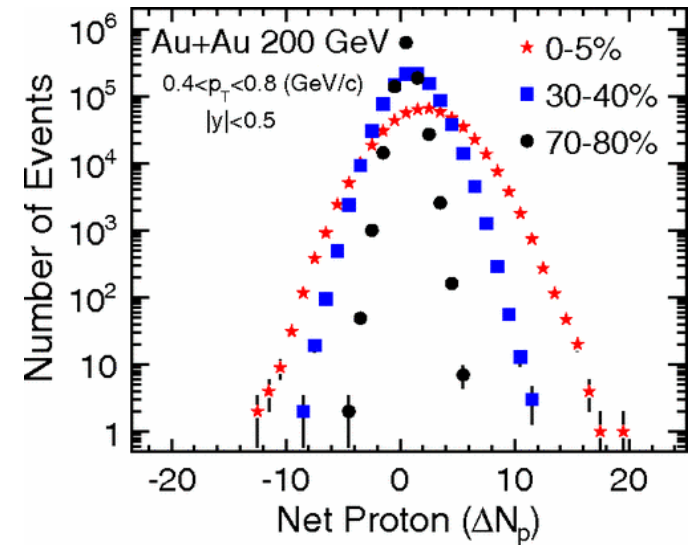
- Direct connect to the susceptibility of the system.

$$\frac{\chi_q^4}{\chi_q^2} = \kappa\sigma^2 = \frac{C_{4,q}}{C_{2,q}} \quad \frac{\chi_q^3}{\chi_q^2} = S\sigma = \frac{C_{3,q}}{C_{2,q}},$$

$$\chi_q^{(n)} = \frac{1}{VT^3} \times C_{n,q} = \frac{\partial^n (p/T^4)}{\partial (\mu_q)^n}, q = B, Q, S$$

S. Ejiri et al, Phys. Lett. B 633 (2006) 275. Cheng et al, PRD (2009) 074505. B. Friman et al., EPJC 71 (2011) 1694. F. Karsch and K. Redlich, PLB 695, 136 (2011). S. Gupta, et al., Science, 332, 1525(2012). A. Bazavov et al., PRL109, 192302(12) // S. Borsanyi et al., PRL111, 062005(13)

## Event-by-Event Distribution



First Measurement : 2009-2010

STAR, PRL105, 022302 (2010).

➤ **Net-Proton:**  $N_p - N_{\bar{p}}$   
(proxy: Net-Baryon)

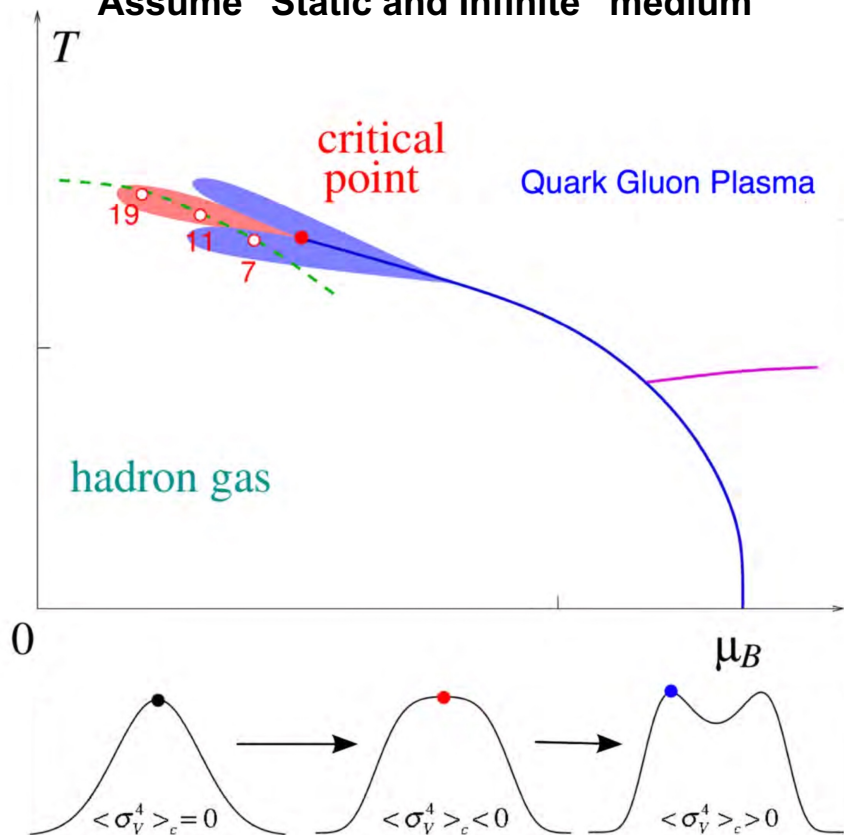
➤ **Net-Charge:**  $N_{Q^+} - N_{Q^-}$

➤ **Net-Kaon:**  $N_{K^+} - N_{K^-}$   
(proxy: Net-Strangeness)



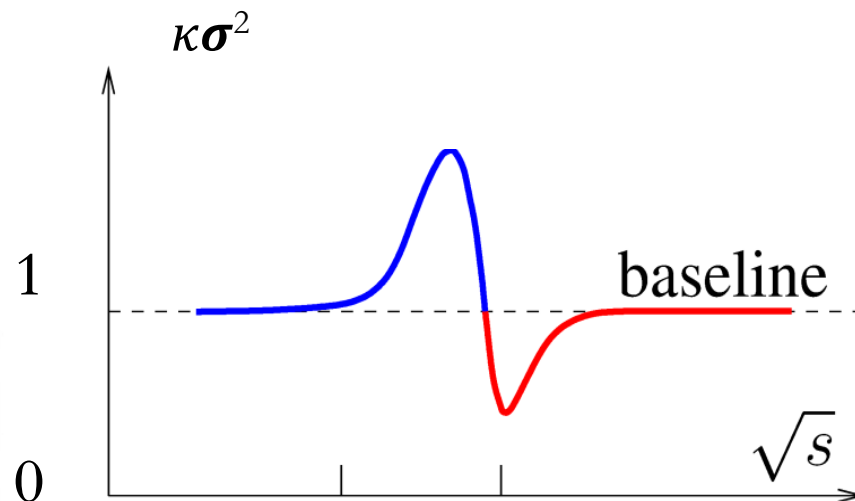
# Signals of QCD Critical Point : Theory/Model

Assume "Static and Infinite" medium



Caveats : Non-equilibrium, finite size/time effects

- M. Asakawa, M. Kitazawa, B. Müller, PRC 101, 034913 (2020).
- S Mukherjee, R. Venugopalan, Y Yin, PRL 117, 222301 (2016).
- S. Wu, Z. Wu, H. Song, PRC 99, 064902 (2019).



$$\kappa \sigma^2 = 1 \quad (\text{Poisson Fluctuations})$$

Characteristic signature of CP:  
Non-monotonic energy dependence

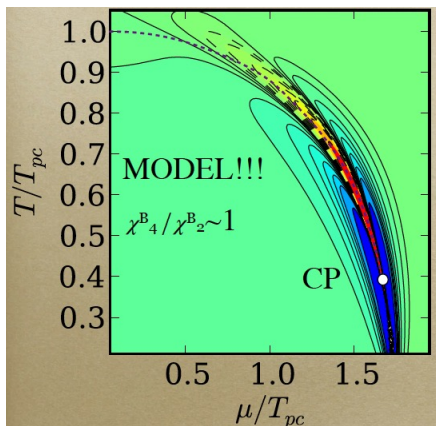
**“Oscillation Pattern”**  
**Especially the Peak at low energies**

- M. Stephanov, PRL107, 052301 (2011); J. Phys. G 38, 124147 (2011).
- Schaefer et al., PRD 85, 034027 (2012); W. Fu et al., PRD 94, 116020 (2016).
- J.W. Chen, J. Deng, et al., PRD 93, 034037 (2016). PRD 95,014038 (2017).
- W. K. Fan, X. Luo, H.S. Zong, IJMPA 32, 1750061 (2017);
- G. Shao et al., EPJC 78, 138 (2018) ; Z. Li et al., EPJC 79, 245 (2019).
- A. Bzdak et al., Phys. Rep. 853, 1(2020). D. Mroczek et al, arXiv: 2008.04022.



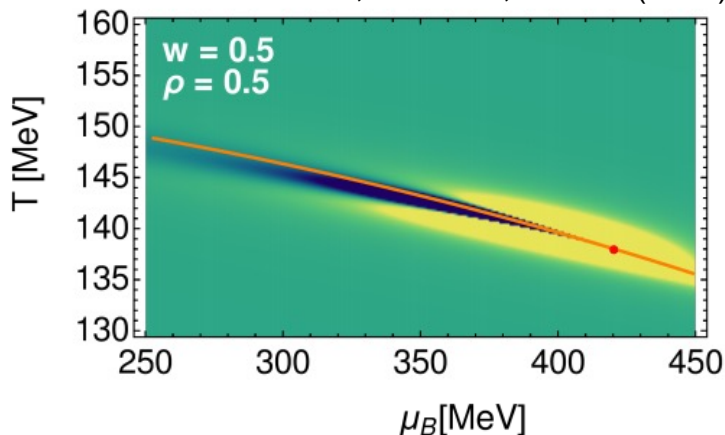
# Critical Contributions to Fourth-order Fluctuations ( $\kappa\sigma^2$ )

**PQM** V. Skokov, QM2012



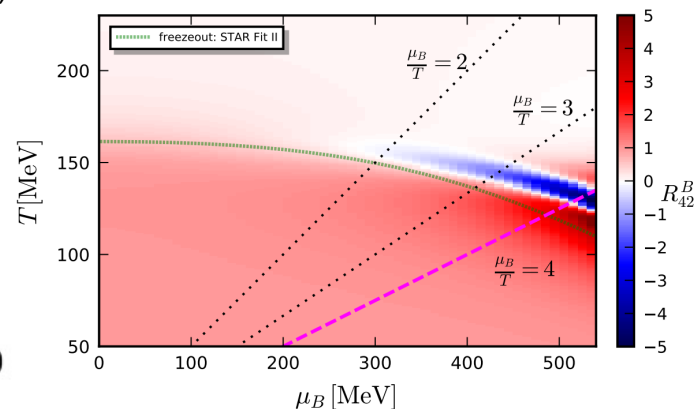
**3D Ising Mapping**

D. Mroczek et al, PRC 103, 034901 (2021)

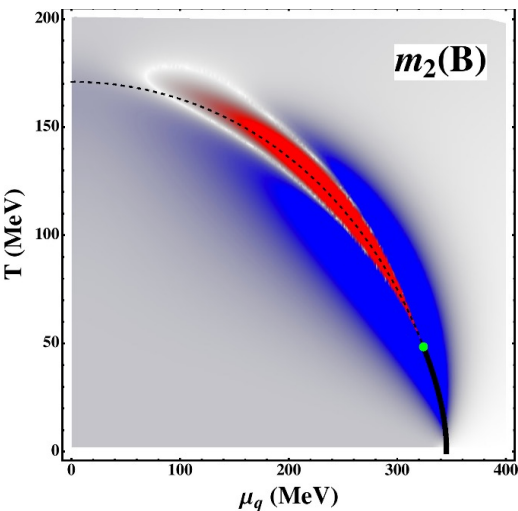


**FRG**

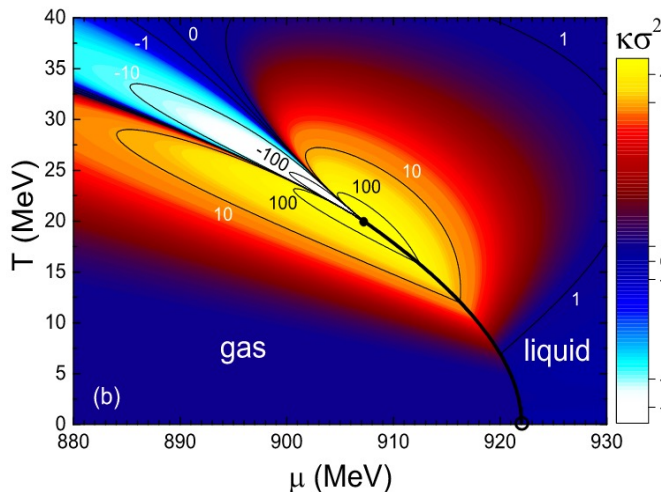
付伟杰等 PRD 104 (2021) 9, 094047



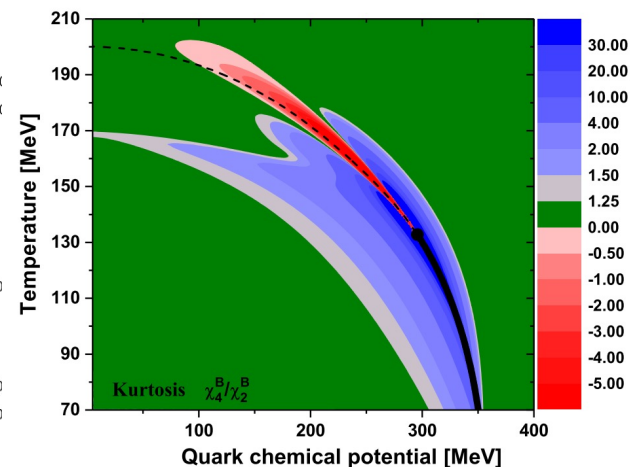
**NJL**



**Symmetry and Universality  
van der Waals (VDW)**



**PNJL**



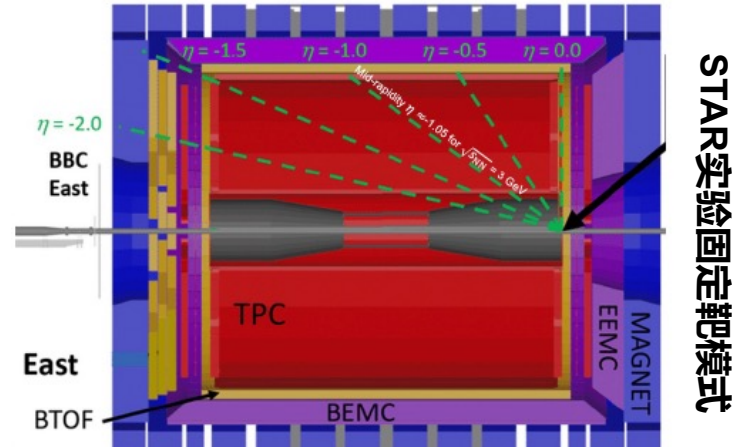
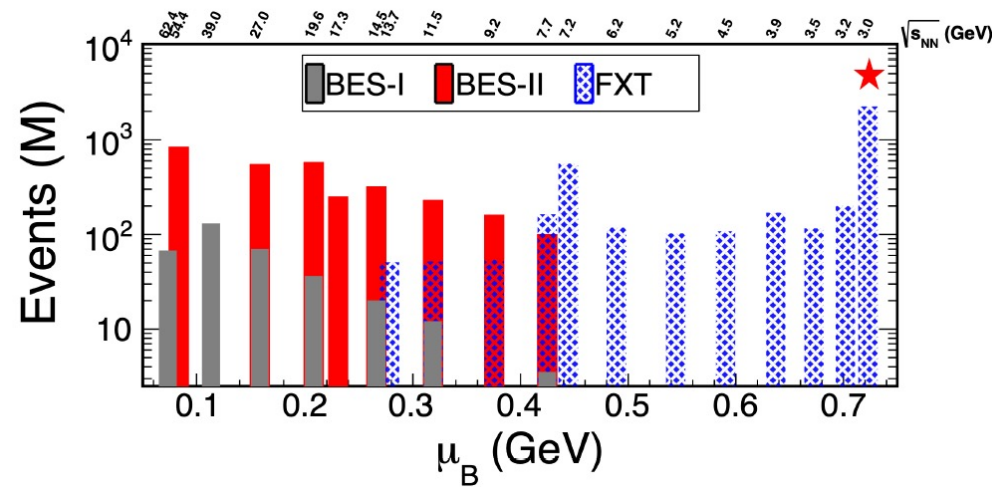
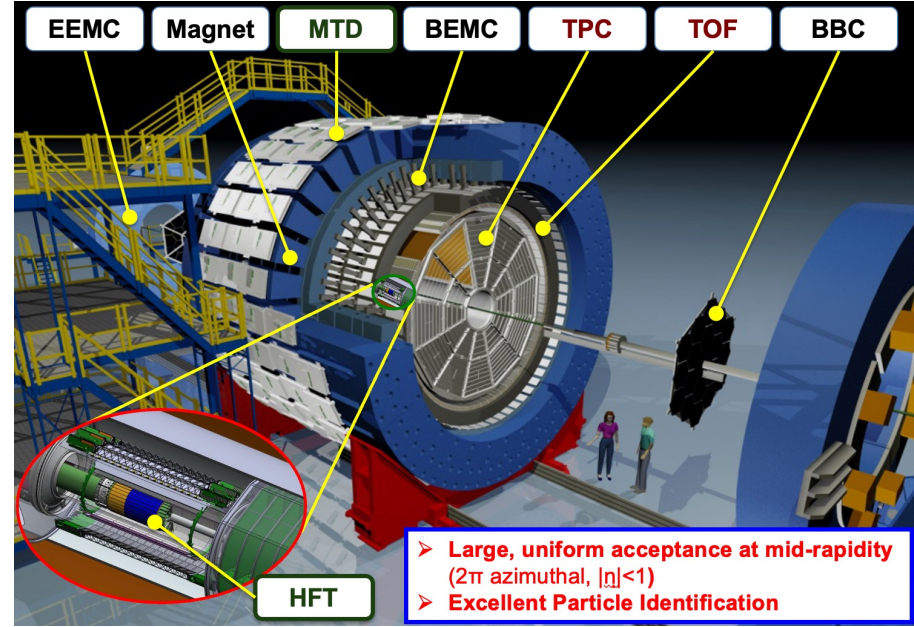
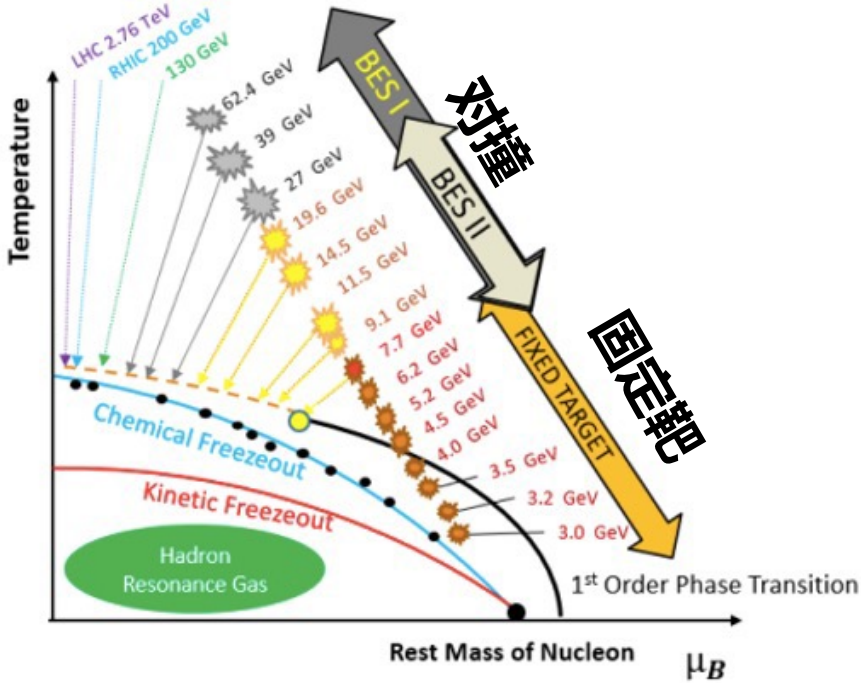
邓建等, PRD93, 034037 (2016)

Vovchenko et al., PRC92, 054901 (2015)

邵国运等, EPJC 78, 138 (2018)  
黄梅等, EPJC 79, 245 (2019).



# RHIC Beam Energy Scan (BES) Program (2010-2021)





# RHIC能量扫描数据统计表

Au+Au Collisions at RHIC (RHIC 金核-金核碰撞)									
Collider Runs (对撞模式)					Fixed-Target Runs (固定靶模式)				
	$\sqrt{s_{NN}}$ (GeV)	#Events	$\mu_B$ (MeV)	Run		$\sqrt{s_{NN}}$ (GeV)	#Events	$\mu_B$ (MeV)	Run
	碰撞能量	事例率	重子化学势	采集时间		碰撞能量	事例率	重子化学势	采集时间
1	200	380 M	25	Run-10,19	1	13.7 (100)	50 M	280	Run-21
2	62.4	46 M	75	Run-10	2	11.5 (70)	50 M	320	Run-21
3	54.4	1200 M	85	Run-17	3	9.2 (44.5)	50 M	370	Run-21
4	39	86 M	112	Run-10	4	7.7 (31.2)	260 M	420	Run-18,19,20
5	27	585 M	156	Run-11,18	5	7.2 (26.5)	470 M	440	Run-18,20
6	19.6	595 M	206	Run-11,19	6	6.2 (19.5)	120 M	490	Run-20
7	17.3	256 M	230	Run-21	7	5.2 (13.5)	100 M	540	Run-20
8	14.6	340 M	262	Run-14,19	8	4.5 (9.8)	110 M	590	Run-20
9	11.5	57 M	316	Run-10,20	9	3.9 (7.3)	120 M	633	Run-20
10	9.2	160 M	372	Run-10,20	10	3.5 (5.75)	120 M	670	Run-20
11	7.7	104 M	420	Run-21	11	3.2 (4.59)	200 M	699	Run-19
					12	3.0 (3.85)	2300 M	750	Run-18,21

STAR, arXiv:1007.2613

<https://drupal.star.bnl.gov/STAR/starnotes/public/sn0493>

<https://drupal.star.bnl.gov/STAR/starnotes/public/sn0598>

- x10-20 more statistics in BES-II compared to BES-I at collider energies
- BES-II: 8 collider energies (7.7 – 54.4GeV) / 12 FXT energies (3.0 - 13.7 GeV)
- $\mu_B$  coverage :  $25 < \mu_B < 750$  MeV.



# Major Upgrades for BES-II

All 3 detectors fully installed prior to start of Run-19  
Very successful and important for BES-II



## iTPC:

- Improves  $dE/dx$
- Extends  $\eta$  coverage from 1.0 to 1.5
- Lowers  $p_T$  cut-in from 125 to 60 MeV/c
- Ready in 2019



## eTOF:

- Forward rapidity coverage
- PID at  $\eta = 0.9$  to 1.5
- **Borrowed from CBM-FAIR**
- Ready in 2019



## EPD:

- Improves trigger
- Better centrality & event plane measurements
- Ready in 2018

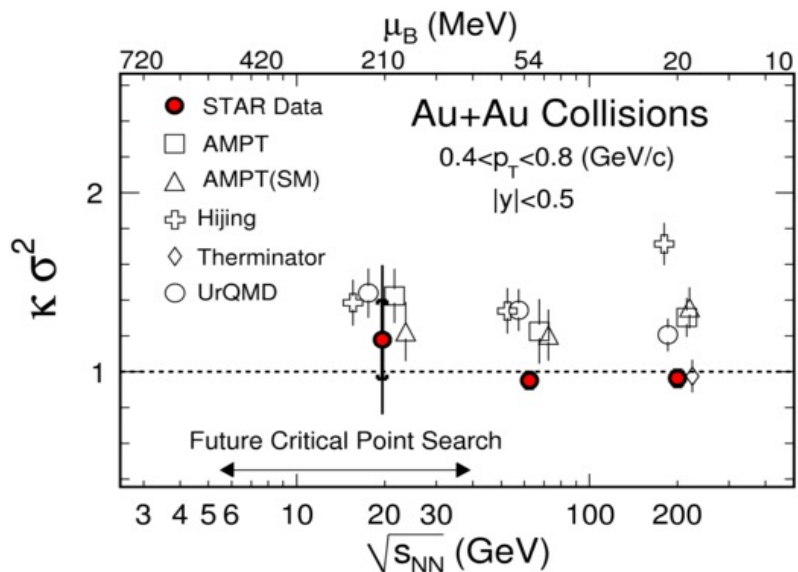
- 1) **Enlarge rapidity acceptance**
- 2) **Improve particle identification**
- 3) **Enhance centrality/event plane resolution**

iTPC: <https://drupal.star.bnl.gov/STAR/starnotes/public/sn0619>  
eTOF: STAR and CBM eTOF group, arXiv: 1609.05102  
EPD: J. Adams, et al. Nucl. Instr. Meth. A 968, 163970 (2020)





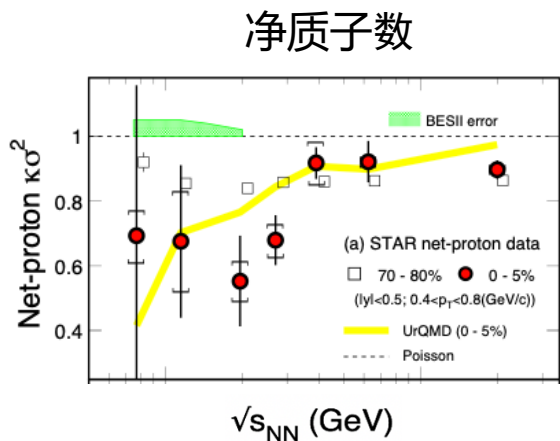
# 第一阶段能量扫描高阶矩测量结果



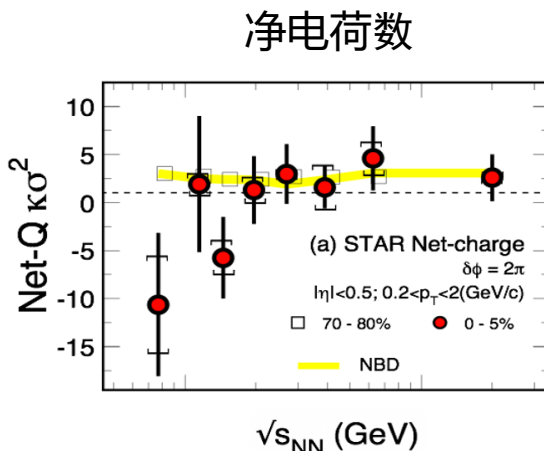
2010年首次测量：验证了该观测量在STAR重离子碰撞实验中的可行性

STAR, Phys. Rev. Lett. 105, 022302(2010).

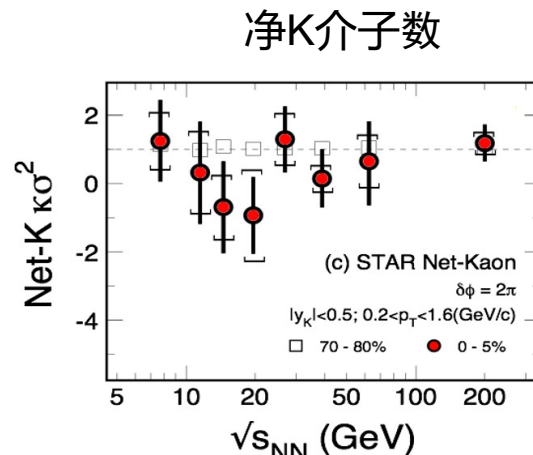
寻找QCD临界点信号：非单调能量依赖



STAR, PRL 112, 032302 (2014).



STAR, PRL113, 092301 (2014).



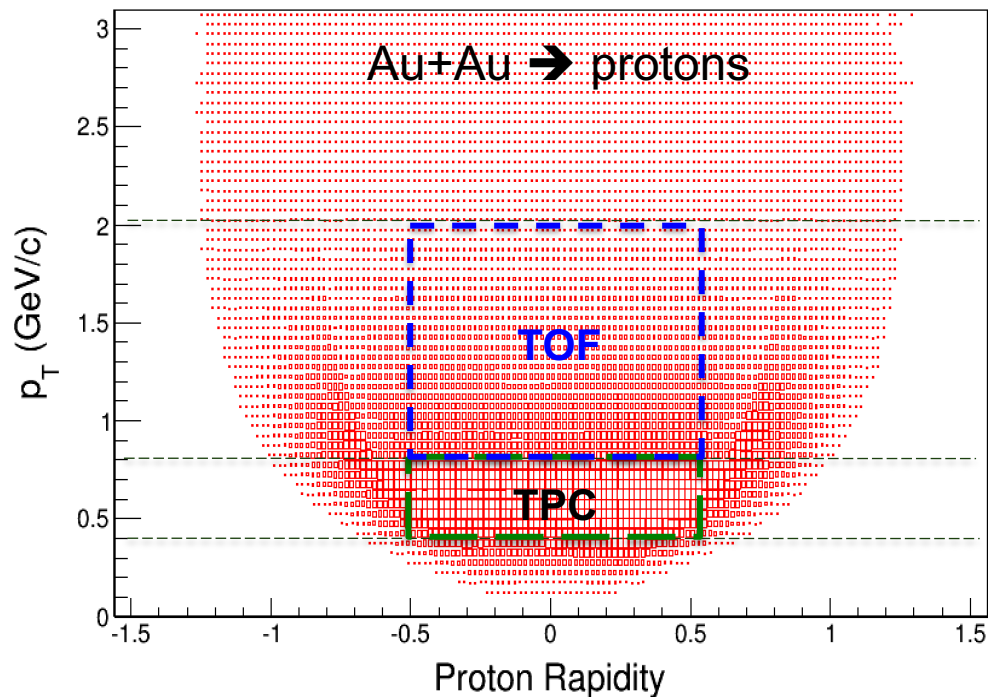
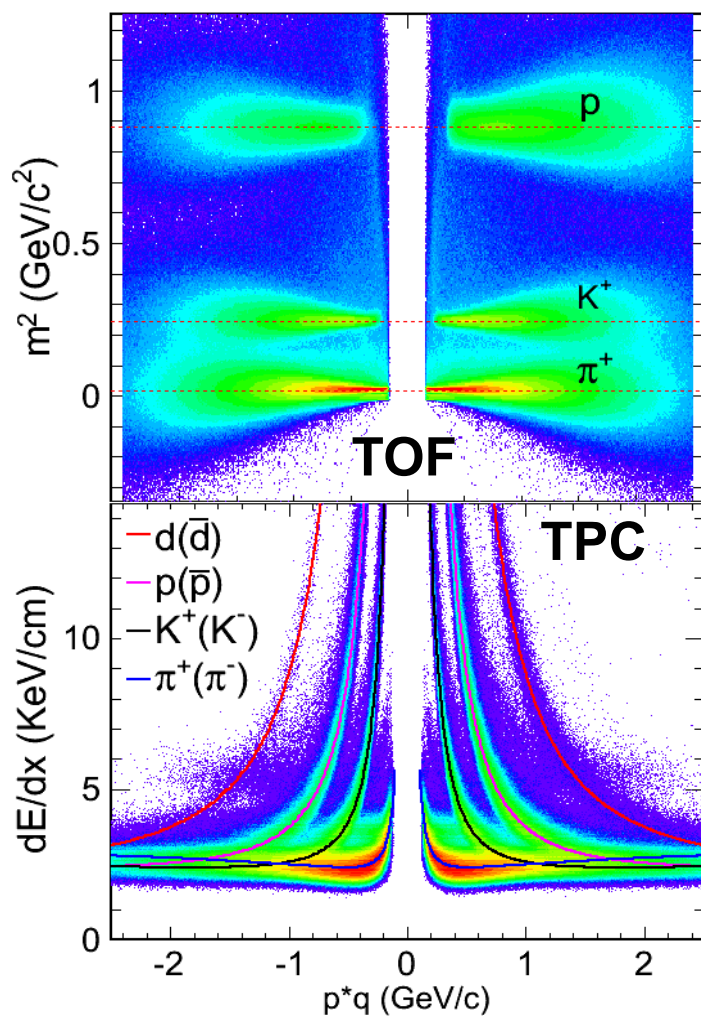
STAR, PLB 785, 551 (2018).

# Extend $p_T$ Acceptance

**Multi-Particle Correlations : Larger acceptance  $\rightarrow$  Larger signal**

B. Ling, M. Stephanov, Phys. Rev. C 93, 034915 (2016)

姜丽佳, 李鹏飞, 宋慧超, Phys. Rev. C 94, 024918 (2016)



**Acceptance:  $|y| \leq 0.5$ ,  $0.4 \leq p_T \leq 2 \text{ GeV}/c$**

**Efficiency corrections:**

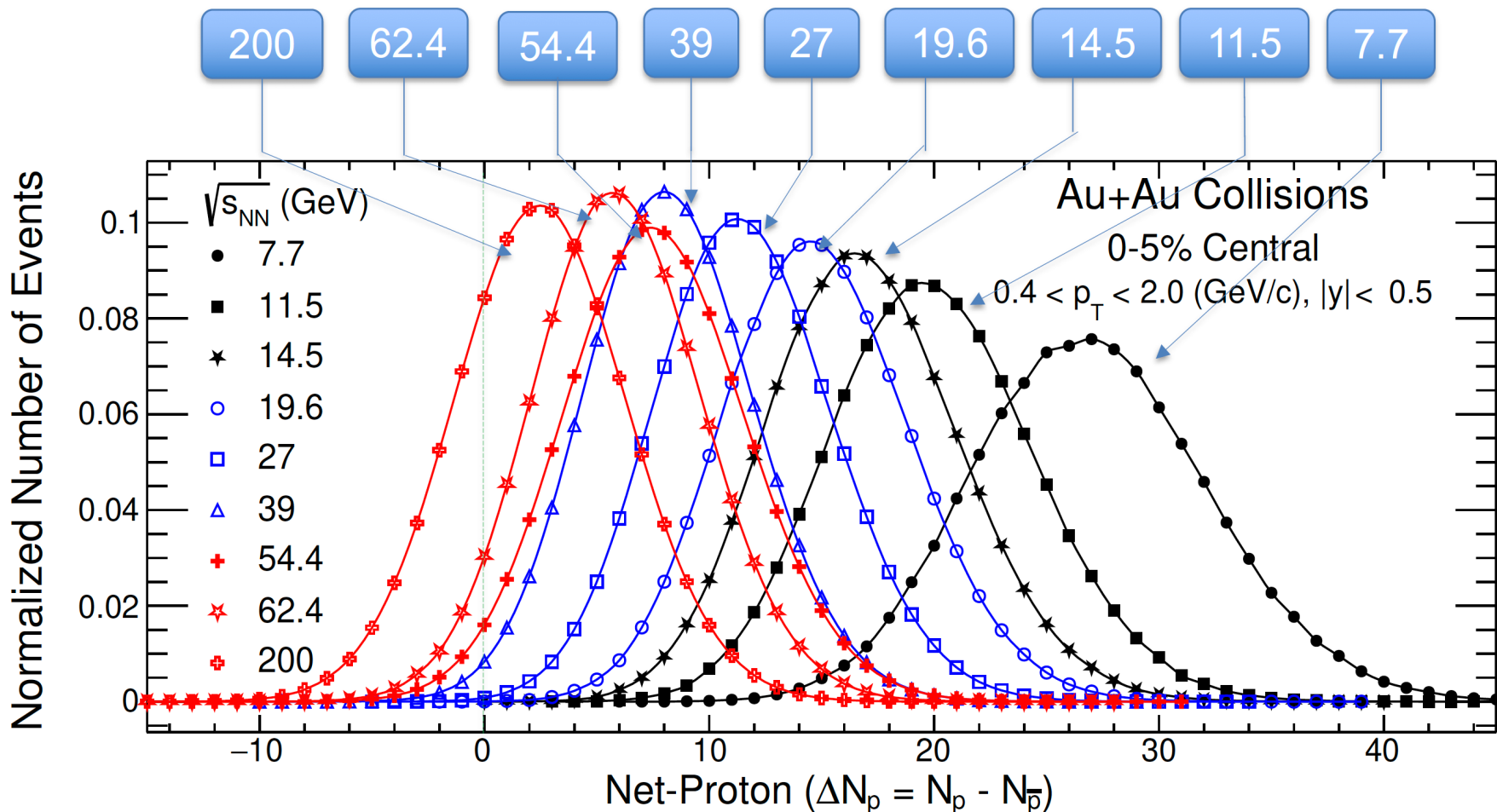
TPC ( $0.4 \leq p_T \leq 0.8 \text{ GeV}/c$ ):  $\epsilon_{\text{TPC}} \sim 0.8$

TPC+TOF ( $0.8 \leq p_T \leq 2 \text{ GeV}/c$ ):  $\epsilon_{\text{TPC}} * \epsilon_{\text{TOF}} \sim 0.5$

XFL, Phys. Rev. C 91, 034907 (2015).



# Raw Event-by-Event Net-Proton Distributions

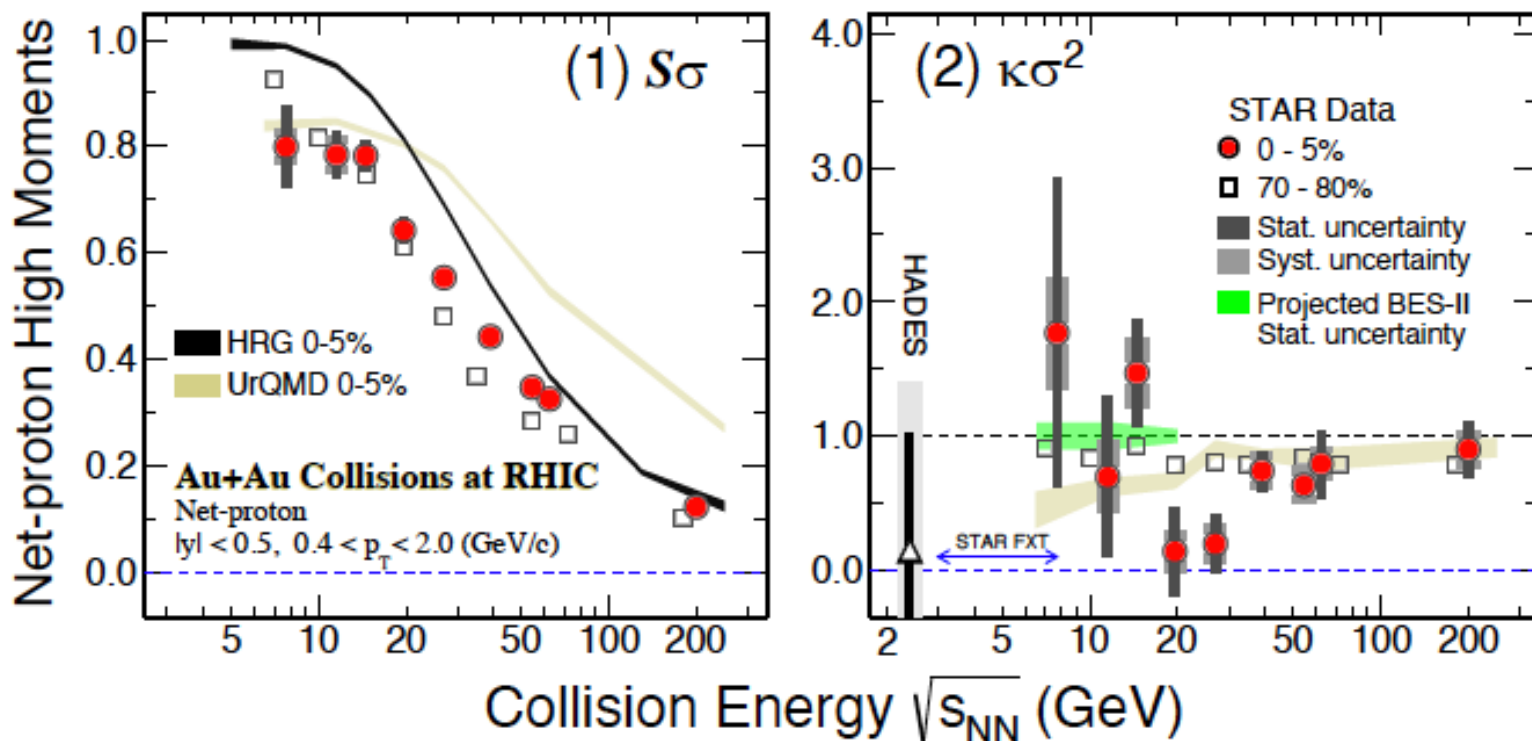


Mean values increase when decreasing energy:  
Interplay between baryon stopping and pair production.

STAR, PRL 126, 092301 (2021)  
STAR, PRC104, 024902 (2021)



# Energy Dependence of Cumulant Ratios : $S\sigma$ and $\kappa\sigma^2$



- HRG (GCE) and transport model predicted monotonical energy dependence. Suppression at low energy due to conservation.
- Observe a non-monotonic energy dependence (7.7-62.4 GeV) in 0-5% net-proton  $\kappa\sigma^2$  with a significant of  $3.1\sigma$

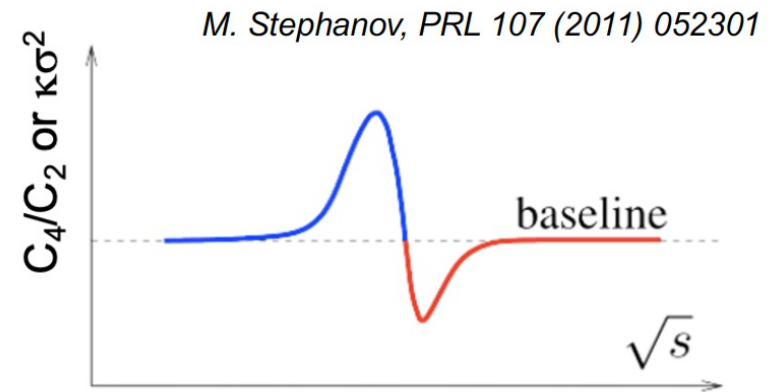
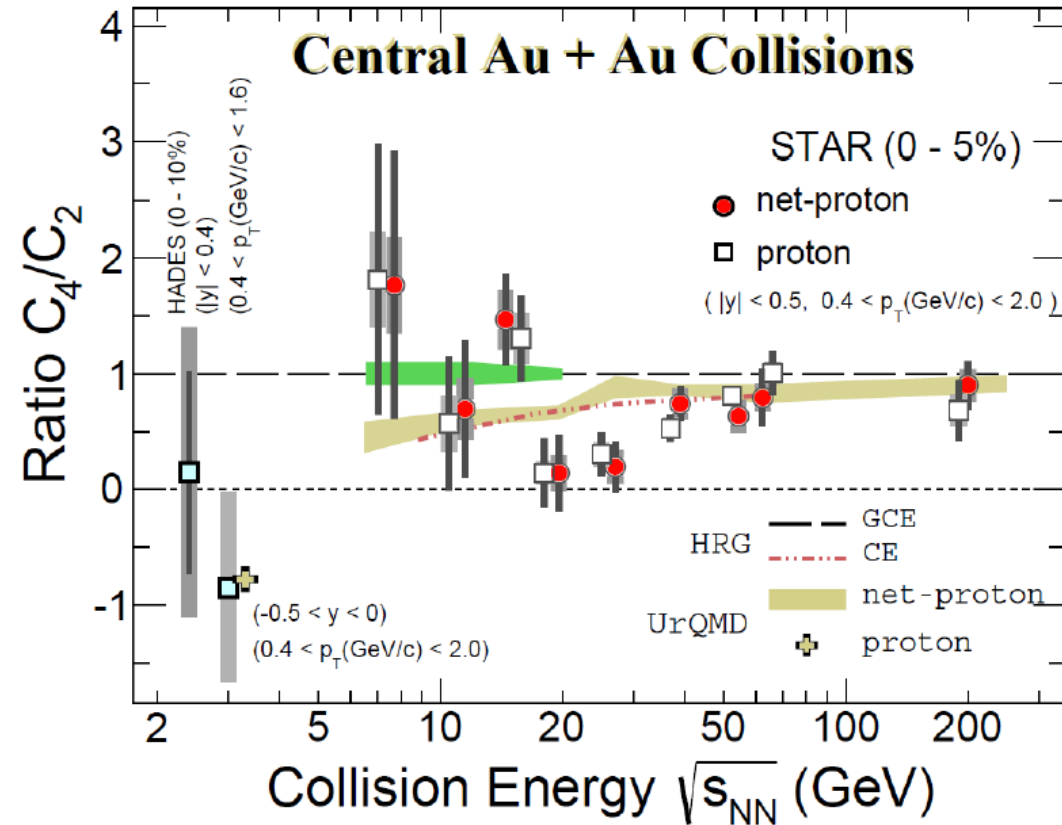
STAR, Phys. Rev. Lett. 126, 092301 (2021)

STAR, Phys. Rev. C 104, 024902 (2021)

HADES, Phys. Rev. C 102, 024914 (2020)



# Energy Dependence of (Net-) Proton Fourth-order Fluctuations

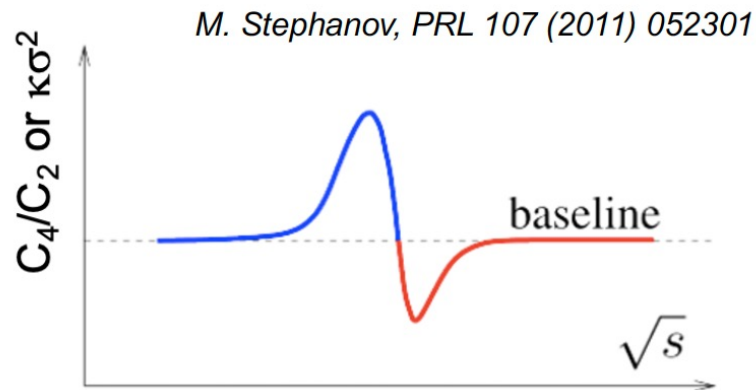
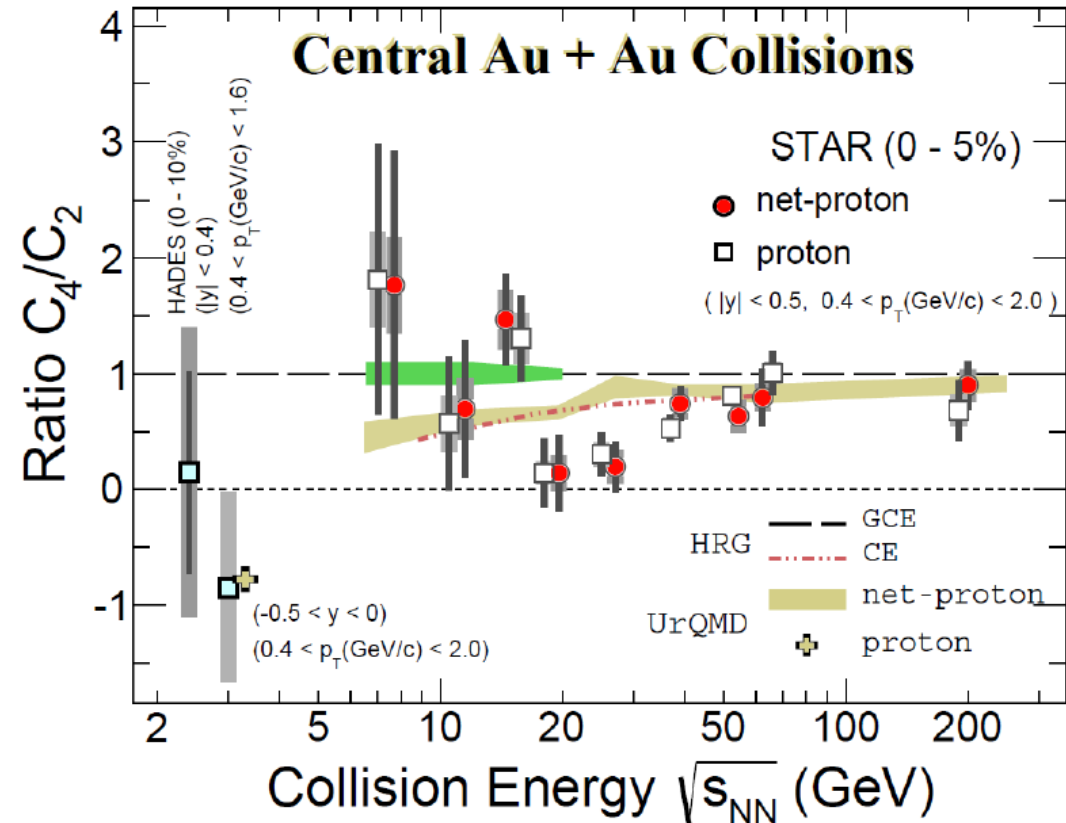


- BES-I**: Phys. Rev. Lett. 126, 092301 (2021)  
Phys. Rev. C 104, 024902 (2021)
- 3 GeV**: Phys. Rev. Lett. 128, 202303 (2022)  
Phys. Rev. C 107, 024908 (2023)

- Non-monotonic energy dependence in central Au+Au collisions ( $3.1\sigma$ )
- The suppression of  $C_4/C_2$  at 3 GeV is consistent with UrQMD. Hadronic dominated.
- The QCD critical point, if exists in heavy ion collisions, could likely be at energy higher than 3 GeV.

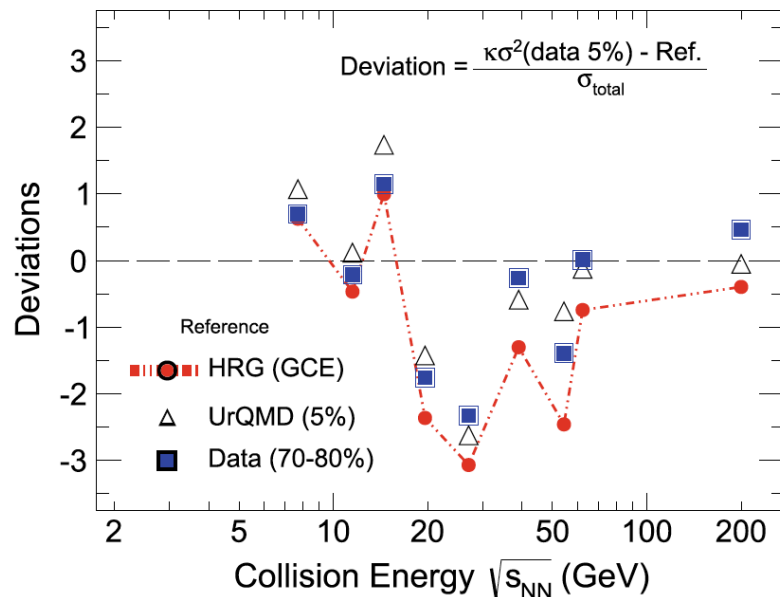


# Energy Dependence of (Net-) Proton Fourth-order Fluctuations



**BES-I**: Phys. Rev. Lett. 126, 092301 (2021)  
 Phys. Rev. C 104, 024902 (2021)

**3 GeV**: Phys. Rev. Lett. 128, 202303 (2022)  
 Phys. Rev. C 107, 024908 (2023)

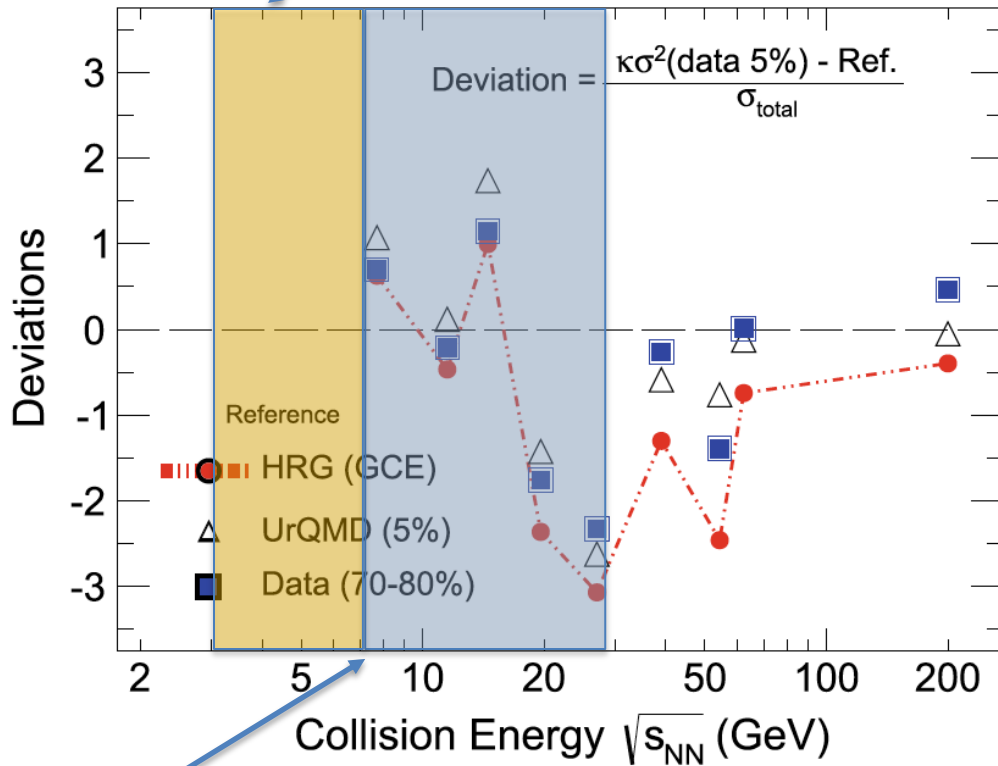






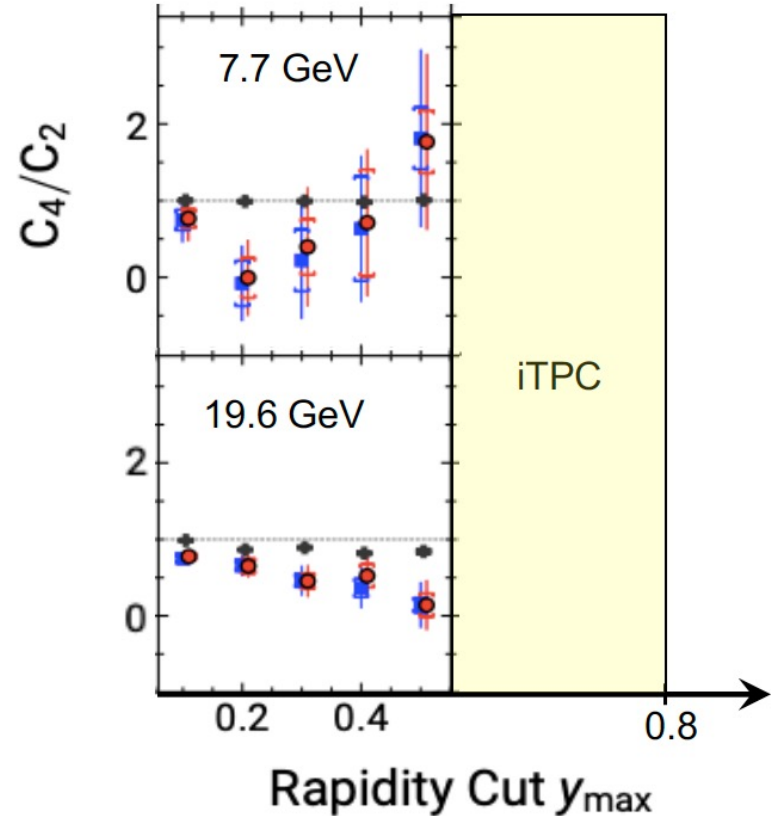
# Prospects from BES-II

Fixed-target energies  
(3 - 7.7 GeV)



BES-II Collider Energies :  
 10-20 times more statistics  
 Extended acceptance and PID

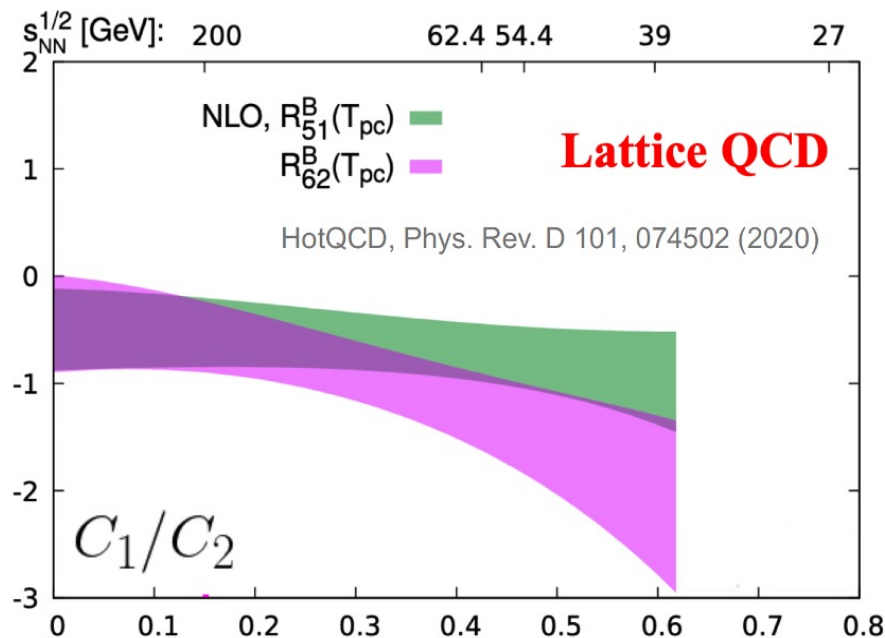
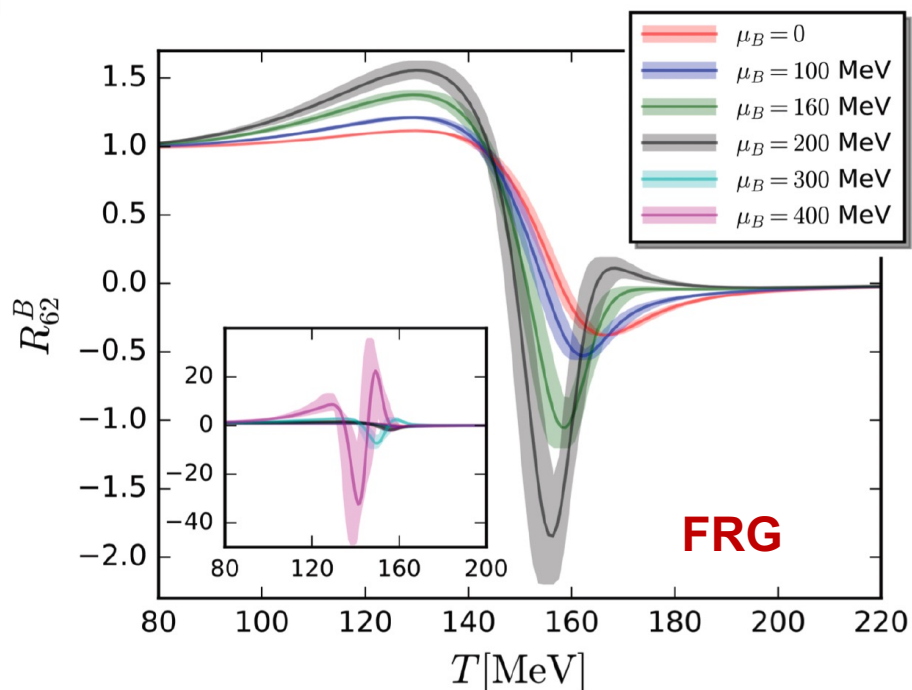
STAR, PRC 104 (2021) 024902



Rapidity coverages at BES-II  
 Collider:  $|y| < y_{\text{max}} = 0.8$   
 FXT:  $-1.0 < y < 0.5$  @ 3 GeV



# Higher-order baryon number fluctuations



付伟杰, XFL等, Phys. Rev. D 104, (2021) 094047 (Editor Suggestion)

A. Bazavov, et al. (hotQCD), Phys. Rev. D 101, 074502 (2020);

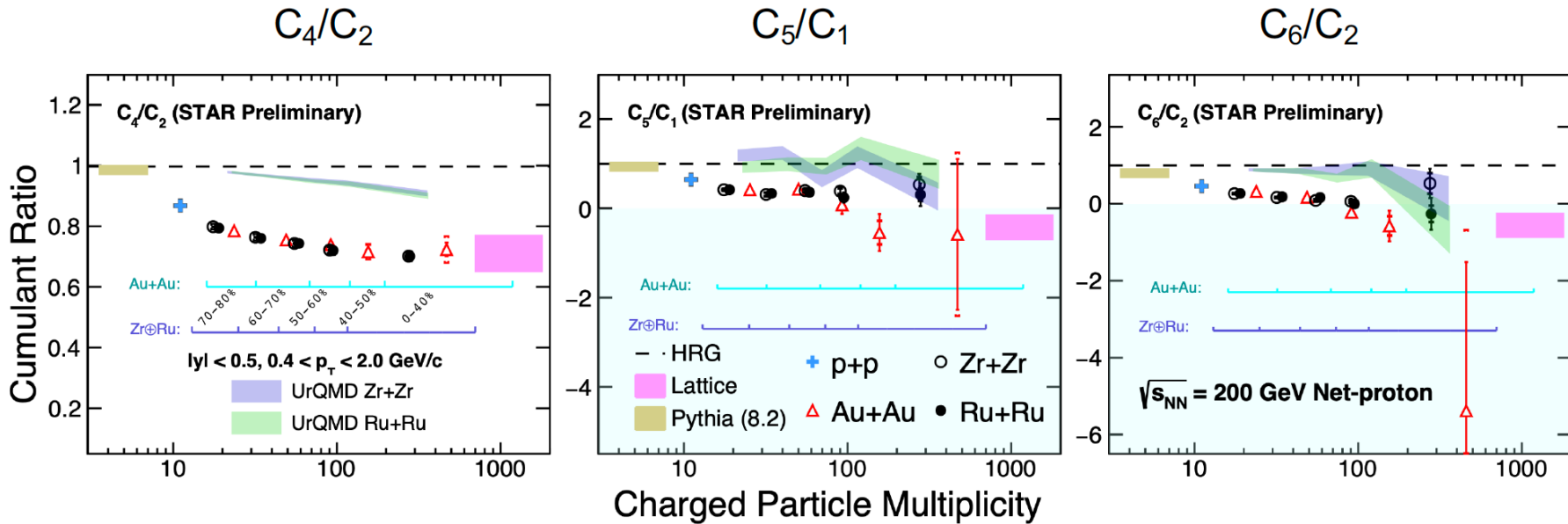
- Higher-order fluctuations are more sensitive to QCD phase transition.
- Negative  $C_n$  ( $n > 4$ ) near  $T_c$  due to chiral crossover.

-> Serve as experimental evidence for the formation of thermalized QGP and smooth crossover transition !



# $C_5/C_1$ and $C_6/C_2$ : System Size Dependence

200 GeV : p+p, Ru+Ru, Zr+Zr and Au+Au



Isobar and p+p : under collaboration review

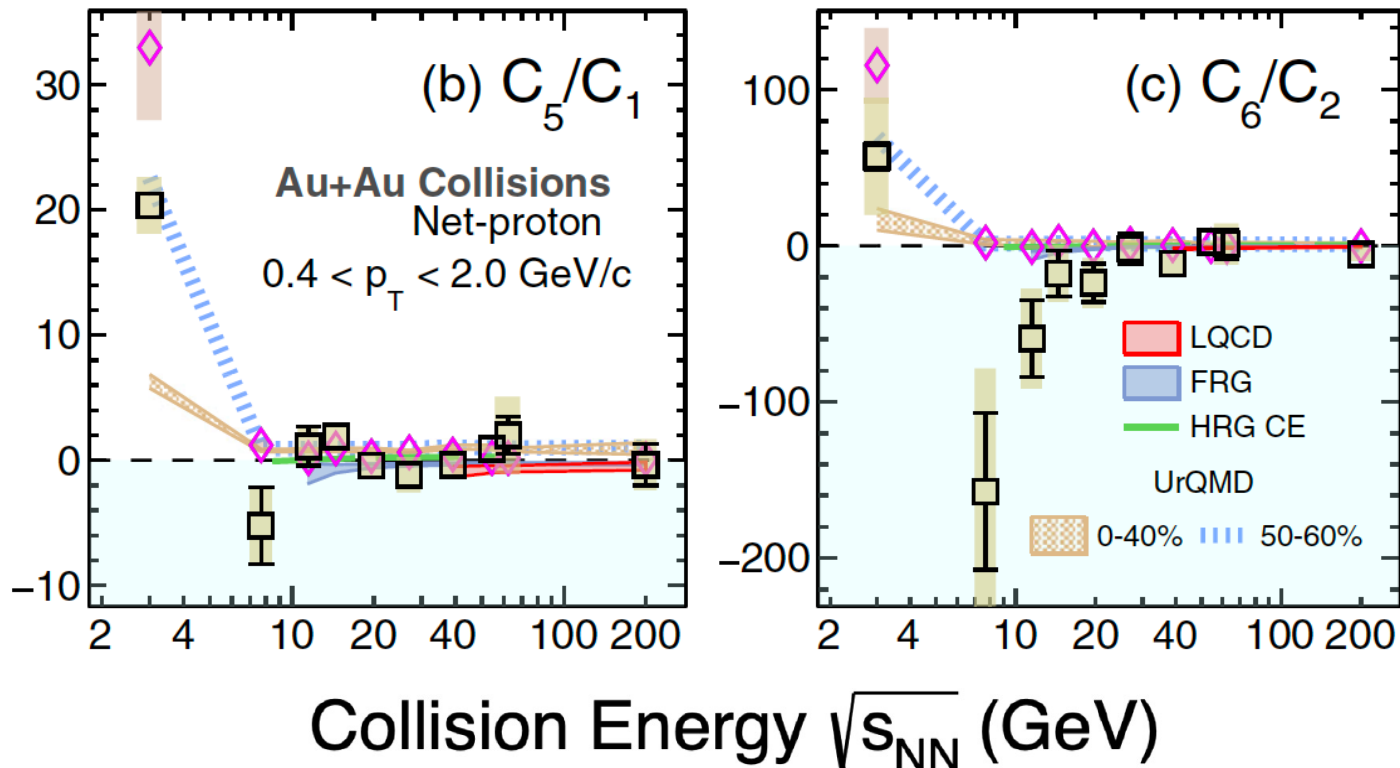
200 GeV Au+Au: PRC 104 (2021) 024902; PRL 126.092301 (2021), PRL 127, 262301 (2021).

- Cumulant ratios (up to  $C_6$ ) of net-proton from p+p, Au+Au and isobar data, systematic decreasing trend with multiplicity, approaching LQCD calculations
- Most central Au+Au collision results become consistent with Lattice QCD prediction for the formation of thermalized QCD matter and smooth crossover transition.





# $C_5/C_1$ and $C_6/C_2$ : Energy Dependence



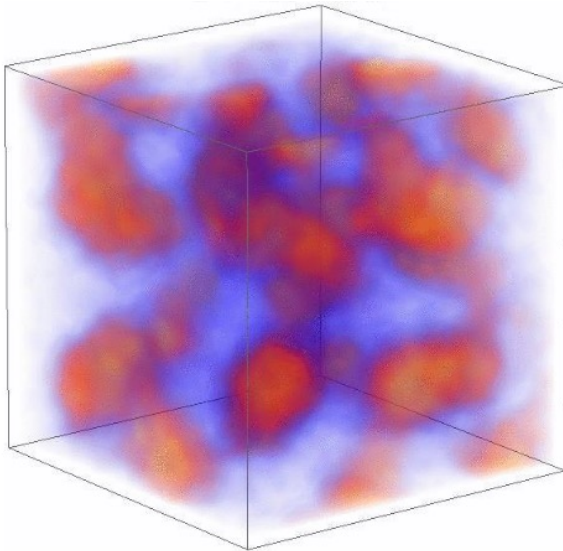
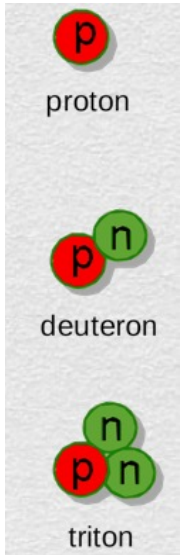
1.  $C_5/C_1$  and  $C_6/C_2$  (0-40%): Consistent with Lattice QCD with  $\mu_B < 110$  MeV. ( $> 39$  GeV)
2.  $C_6/C_2$  progressively negative with decreasing collision energy down to 7.7 GeV.  
 $\sim 1.7$  sigma to be negative sign.
3. 3 GeV 0-40% results : large initial volume fluctuations and consistent with UrQMD.

STAR, Phys. Rev. Lett. 130, 082301 (2023)



# Light nuclei production as probes of QCD phase structure

Near first order P.T. or critical point :  
large density fluctuations and baryon clustering



Based on coalescence model:

$$N_d = \frac{3}{2^{1/2}} \left( \frac{2\pi}{m_0 T_{eff}} \right)^{3/2} N_p \langle n \rangle (1 + C_{np})$$

$$N_t = \frac{3^{3/2}}{4} \left( \frac{2\pi}{m_0 T_{eff}} \right)^3 N_p \langle n \rangle^2 (1 + \Delta n + 2C_{np})$$

**New observable : Yield ratio of light nuclei**

$$N_t \cdot N_p / N_d^2 \approx g(1 + \Delta n)$$

Neutron density fluctuations  $\Delta n = \langle (\delta n)^2 \rangle / \langle n \rangle^2$   
 $g=0.29$

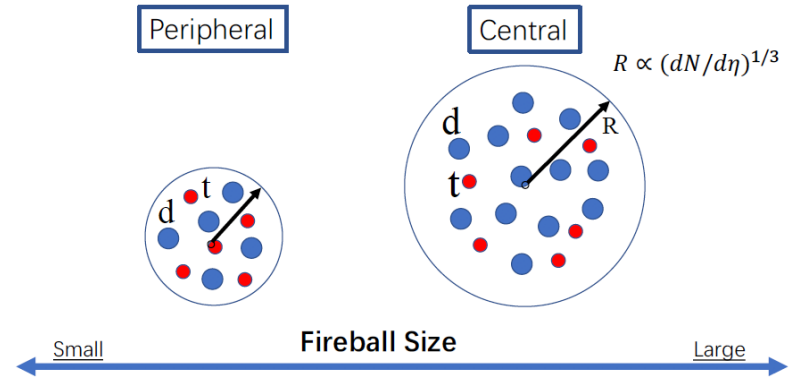
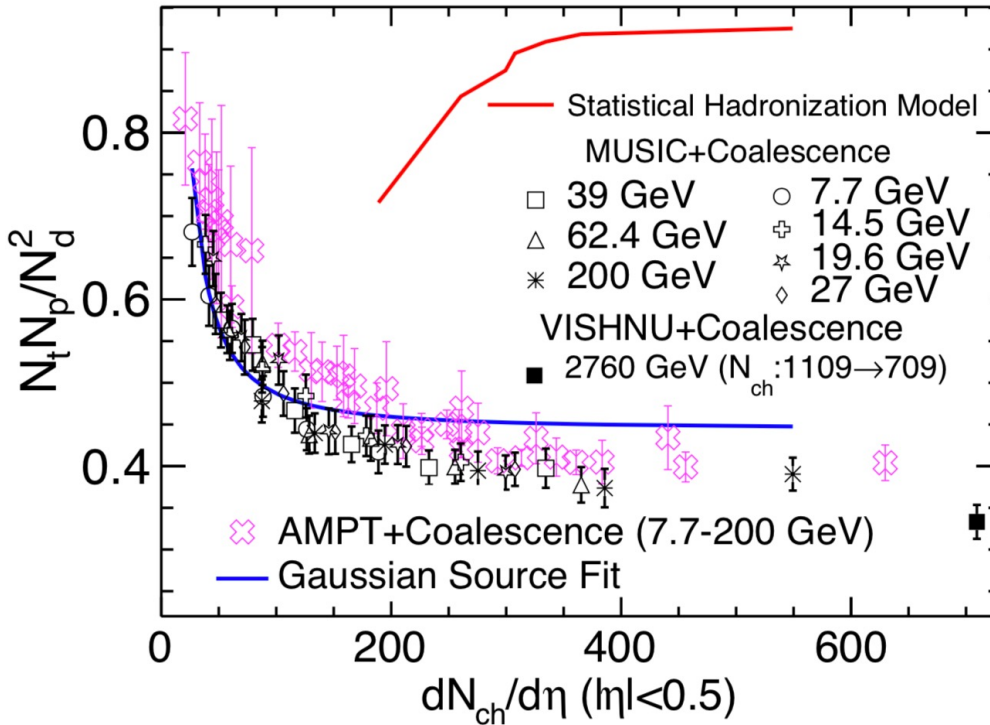
Yield ratio of light nuclei is sensitive to the baryon density fluctuations and can be used to probe the signature of 1st order phase transition and/or critical point in heavy-ion collisions.

K.J. Sun, L.W. Chen, C.M. Ko, and Z.B. Xu, PLB 774, 103 (2017);

K.J. Sun, L.W. Chen, C.M. Ko, J. Pu, and Z.B. Xu, PLB781, 499 (2018)

Edward Shuryak, Juan M. Torres-Rincon, PRC 100, 024903 (2019); PRC 101, 034914 (2020); EPJA 56, 241 (2020).

# Size effect in coalescence production of light nuclei



$$\frac{N_t N_p}{N_d^2} = \frac{4}{9} \left( \frac{1 + \frac{2r_d^2}{3R^2}}{1 + \frac{r_t^2}{2R^2}} \right)^3 = \frac{4}{9} \left( 1 + \frac{\frac{4}{3}r_d^2 - r_t^2}{2R^2 + r_t^2} \right)^3$$

$r_t$  and  $r_d$ : matter radius of Triton and deuteron.

$$R \propto (dN_{ch}/d\eta)^{1/3}$$

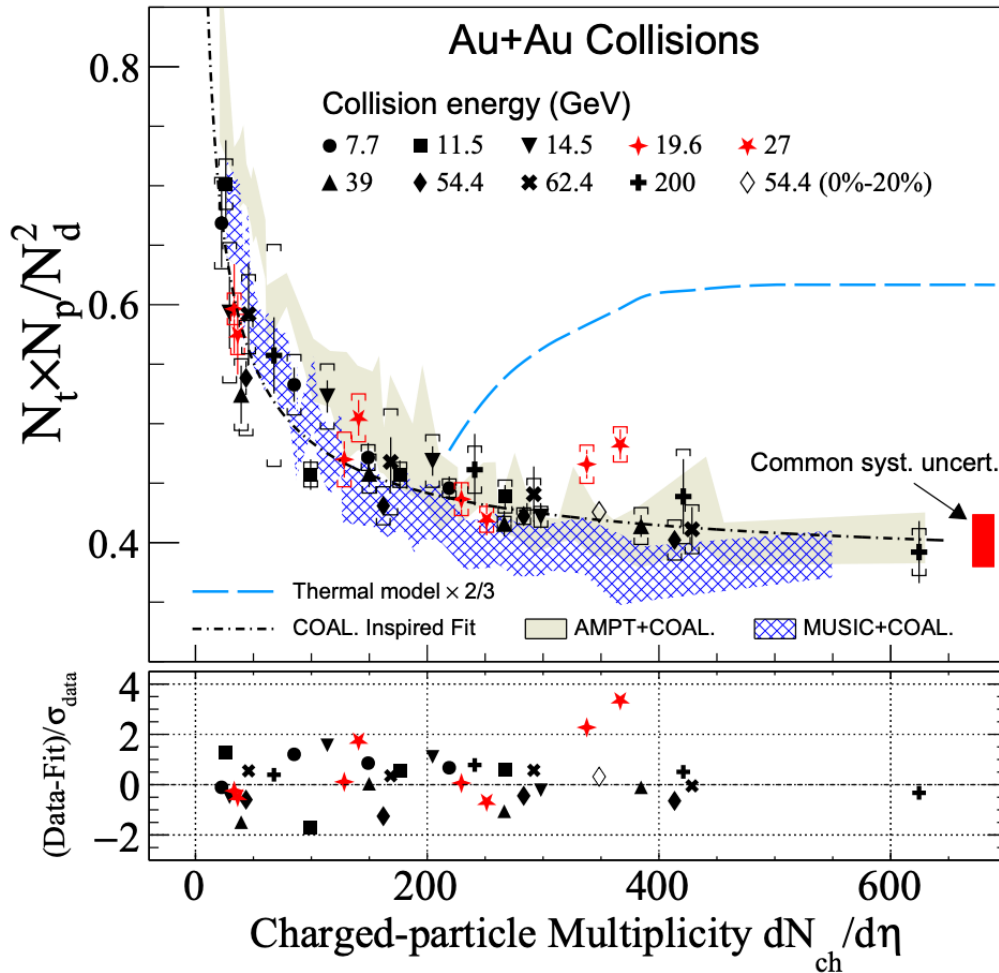
R: Radius of spherical Gaussian emission source

W. Zhao, K.-j. Sun, C. M. Ko, and X. Luo, Phys. Lett. B 820, 136571 (2021);  
 K.-J. Sun, C. M. Ko, and B. Dönigus, Phys. Lett. B 792, 132 (2019)

- Due to size effect in coalescence, yield ratio shows scaling behavior and decreasing with increasing the charged particle multiplicity.
- This multiplicity scaling can be used to validate the production mechanism of light nuclei and serve as a baseline to search for the critical point in heavy-ion collisions



# Charged-particle Multiplicity Dependence of Light Nuclei Yield Ratio

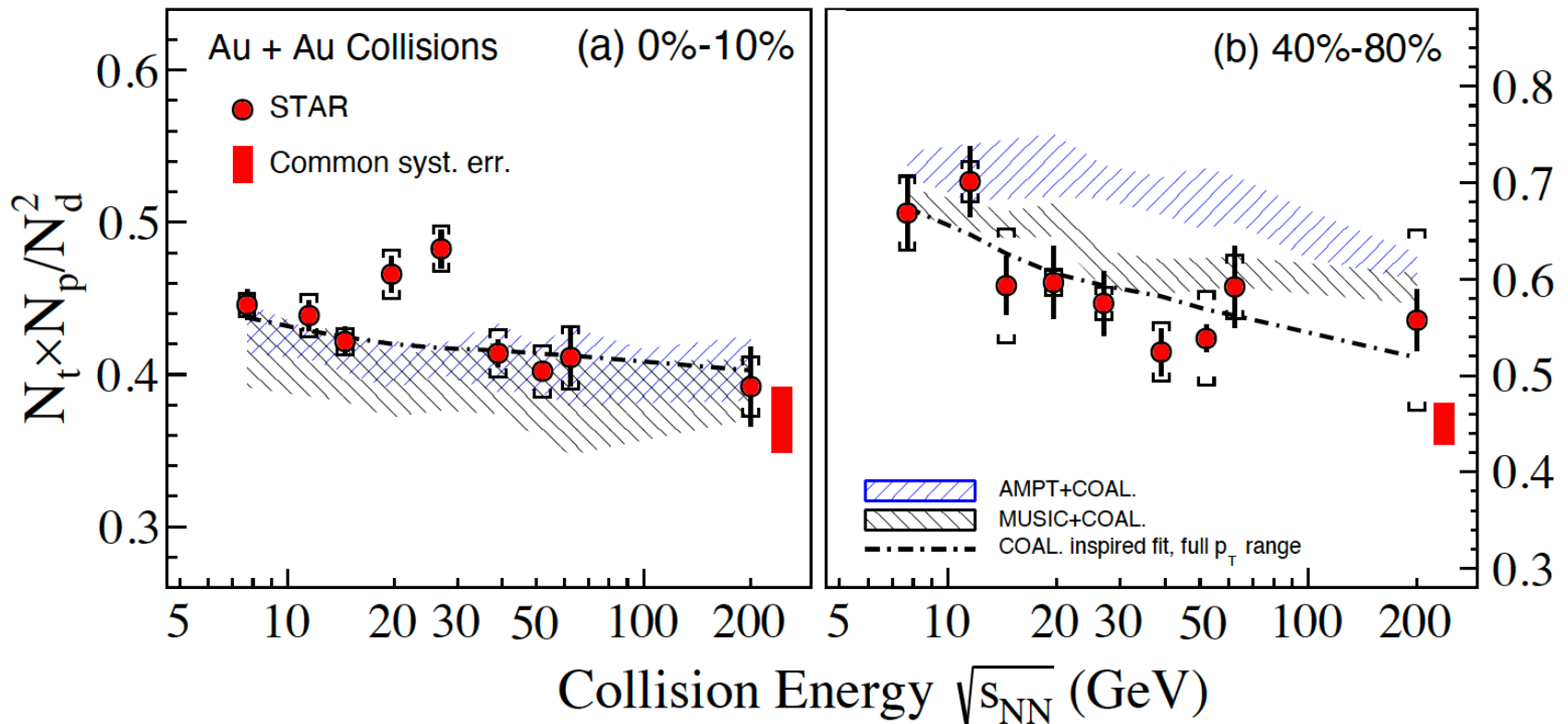


- The yield ratio exhibits a scaling behavior: Trend driven by interplay between the size of light nuclei and the size of fireball created in HIC
- The ratio of 19.6 and 27 GeV from 0% - 10% centrality show enhancements to the coalescence baseline with a combined significance of  $4.1 \sigma$
- The thermal model overestimates the experimental data, shows clear difference compared to coalescence model

STAR, Phys. Rev. Lett. 130, 202301 (2023)



# Energy Dependence of Light Nuclei Yield Ratio



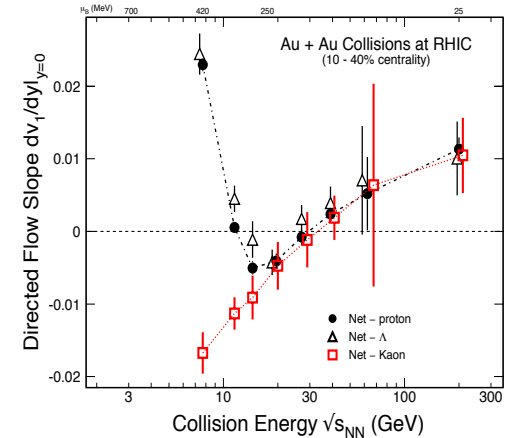
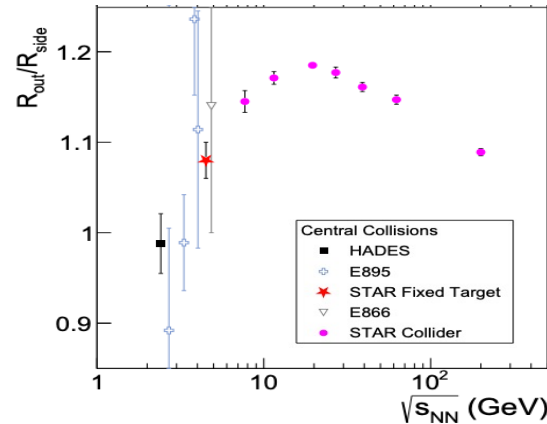
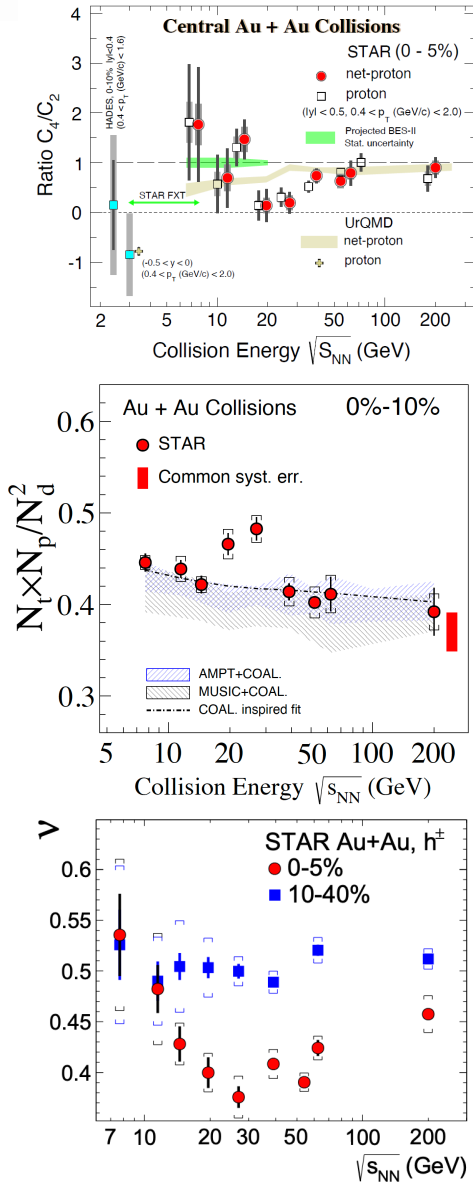
STAR, Phys. Rev. Lett. 130, 202301 (2023)

- Yield ratio shows a non-monotonic dependence on collision energy in 0-10% Au + Au collisions, with a peak around 20-30 GeV.
- Flat energy dependence of yield ratio observed in JAM, AMPT, UrQMD, hybrid model.

JAM : H. Liu et al, Phys. Lett. B 805, 135452 (2020).  
AMPT : K. Sun, C. M. Ko, PRC 103,064909 (2021).

Hydro + transport + coal. : W. Zhao et al., PRC 102,044912 (2020)  
UrQMD: X. G. Deng, Y. G. Ma, Phys. Lett. B 808, 135668 (2020)

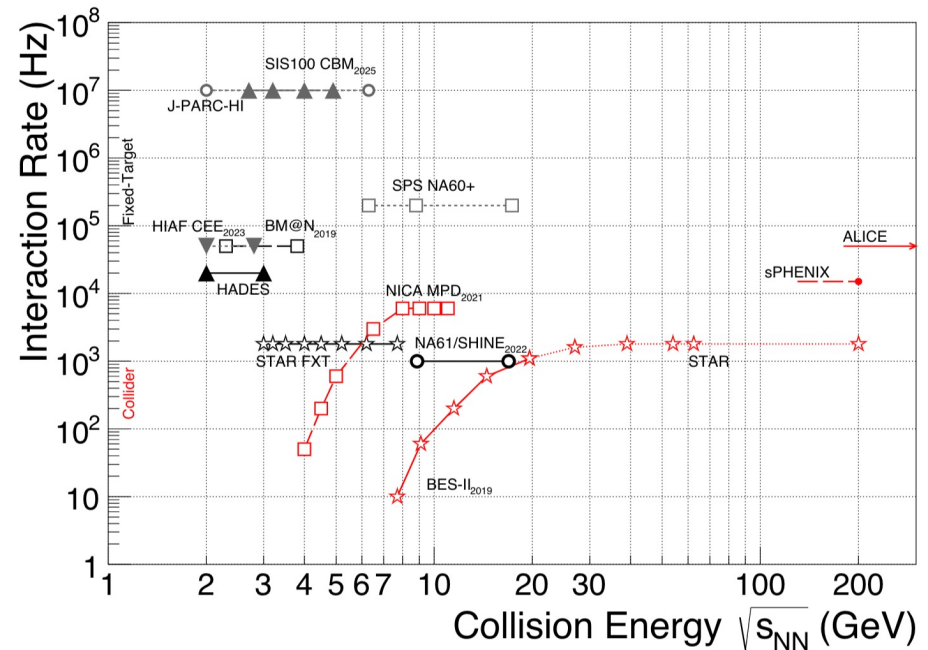
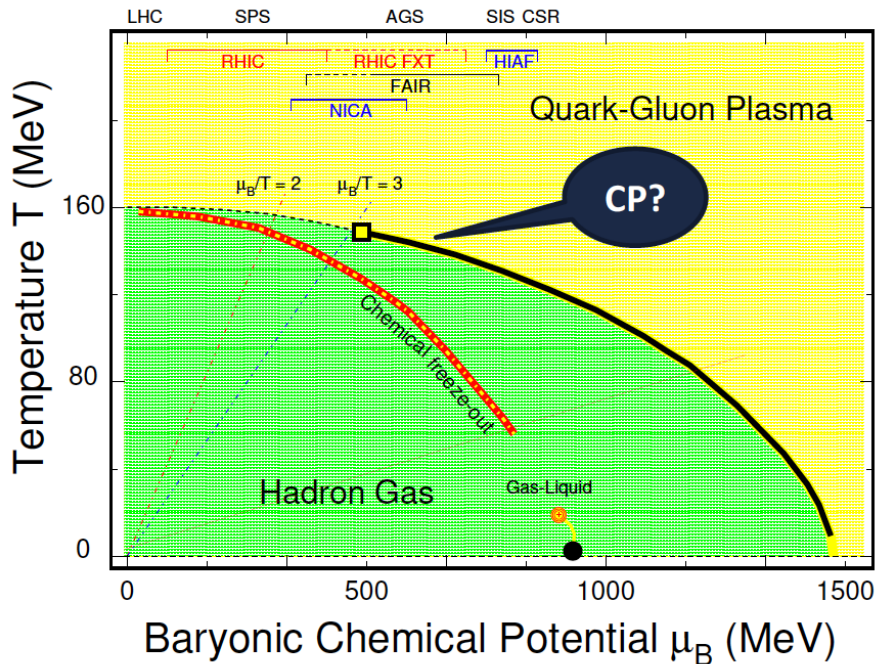
# Summary



- 1) Au+Au collisions at 39-200 GeV,  $\mu_B < 110$  MeV  
**QGP EOS dominant, smooth crossover transition.**
- 2) At 3 GeV collisions,  $\mu_B \sim 750$  MeV, different EOS comparing to high energy.  
**hadronic dominated !**
- 3) BES-I : **QCD critical point between 3 – 39 GeV??**  
 What is the physics behind the structure around 20 ~ 27 GeV ?
- 4) BES-II (data taken completed !), **analysis ongoing:**  
 7.7 ~ 19.6 GeV (collider)  
 3 ~ 7.7 GeV (FXT)



# Outlook

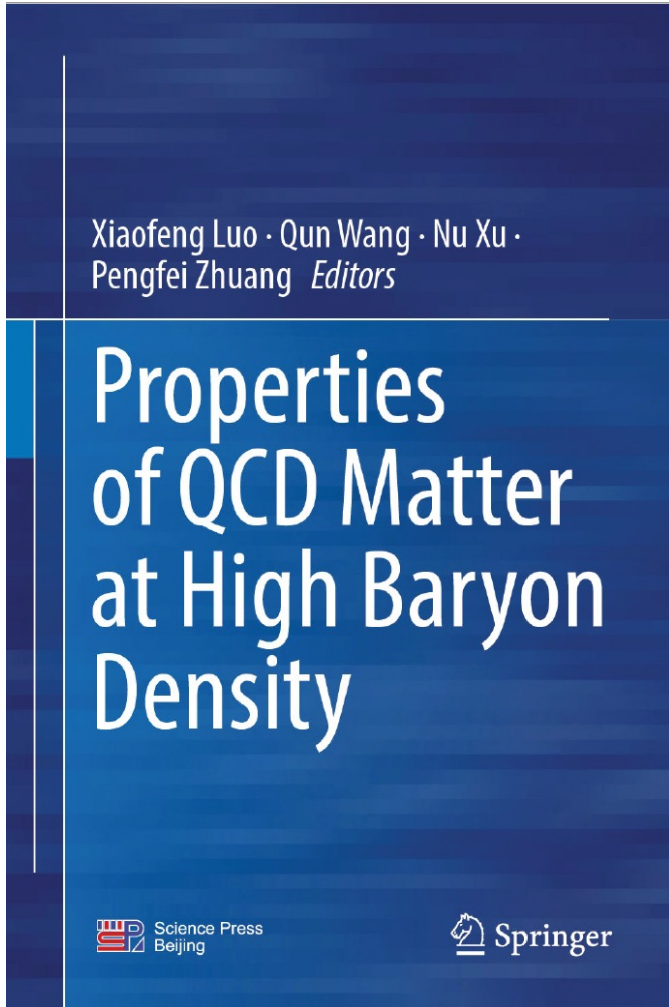


万亿摄氏度下烹煮夸克汤：核物质相结构和量子色动力学相变临界点的实验研究

科普(前沿进展):  
XFL、刘峰、许怒, 《物理》 50(2), (2021)

- Mapping out the QCD phase structure at **high baryon density** with **high precision**:
- (1) RHIC BES-II : Collider ( $\sqrt{s_{NN}} = 7.7 - 19.6$  GeV) and FXT ( $\sqrt{s_{NN}} = 3 - 7.7$  GeV) mode.
  - (2) Future Facilities ( $\sqrt{s_{NN}} = 2 - 11$  GeV) : FAIR/CBM, NICA/MPD, HIAF/CEE, JPARC-HI.

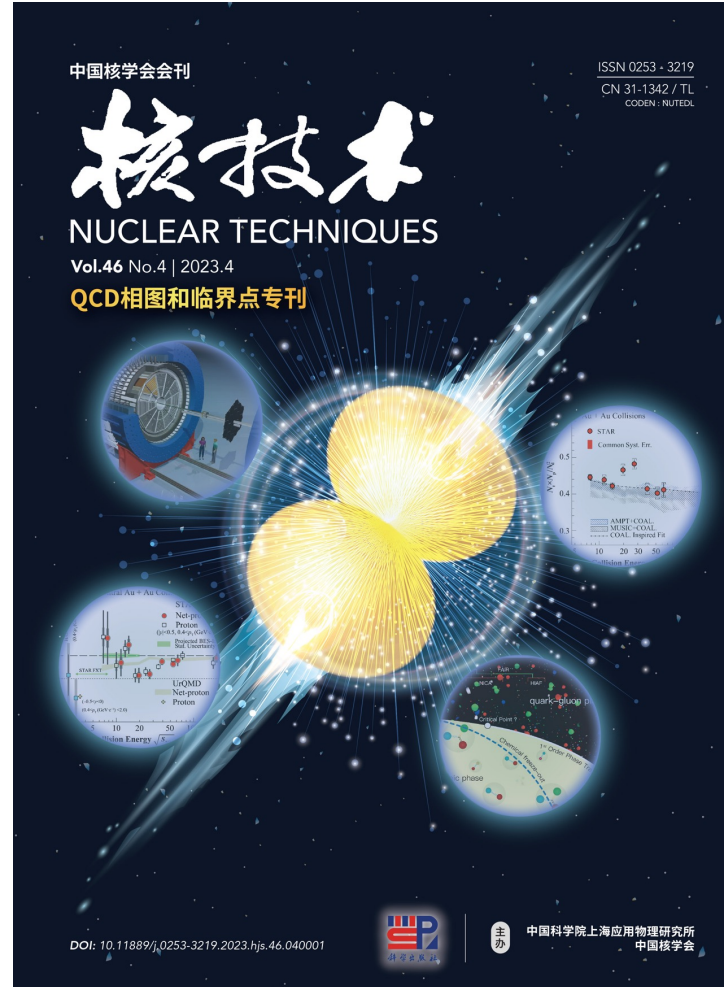
**Stay tuned for the exciting physics from High Baryon Density !**



“高重子密度区QCD物质的性质” (2022)

<https://inspirehep.net/literature/2611423>

<https://link.springer.com/book/10.1007/978-981-19-4441-3>



核技术 “QCD相图和临界点专刊” (2023)

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主编：马余刚



谢谢大家！