

Deciphering the Long-distance Penguin contribution to $B \rightarrow \gamma\gamma$ decays

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QQ, Y.-L. Shen, C. Wang, Y.-M. Wang, *Phys.Rev.Lett.* 131(2023)091902



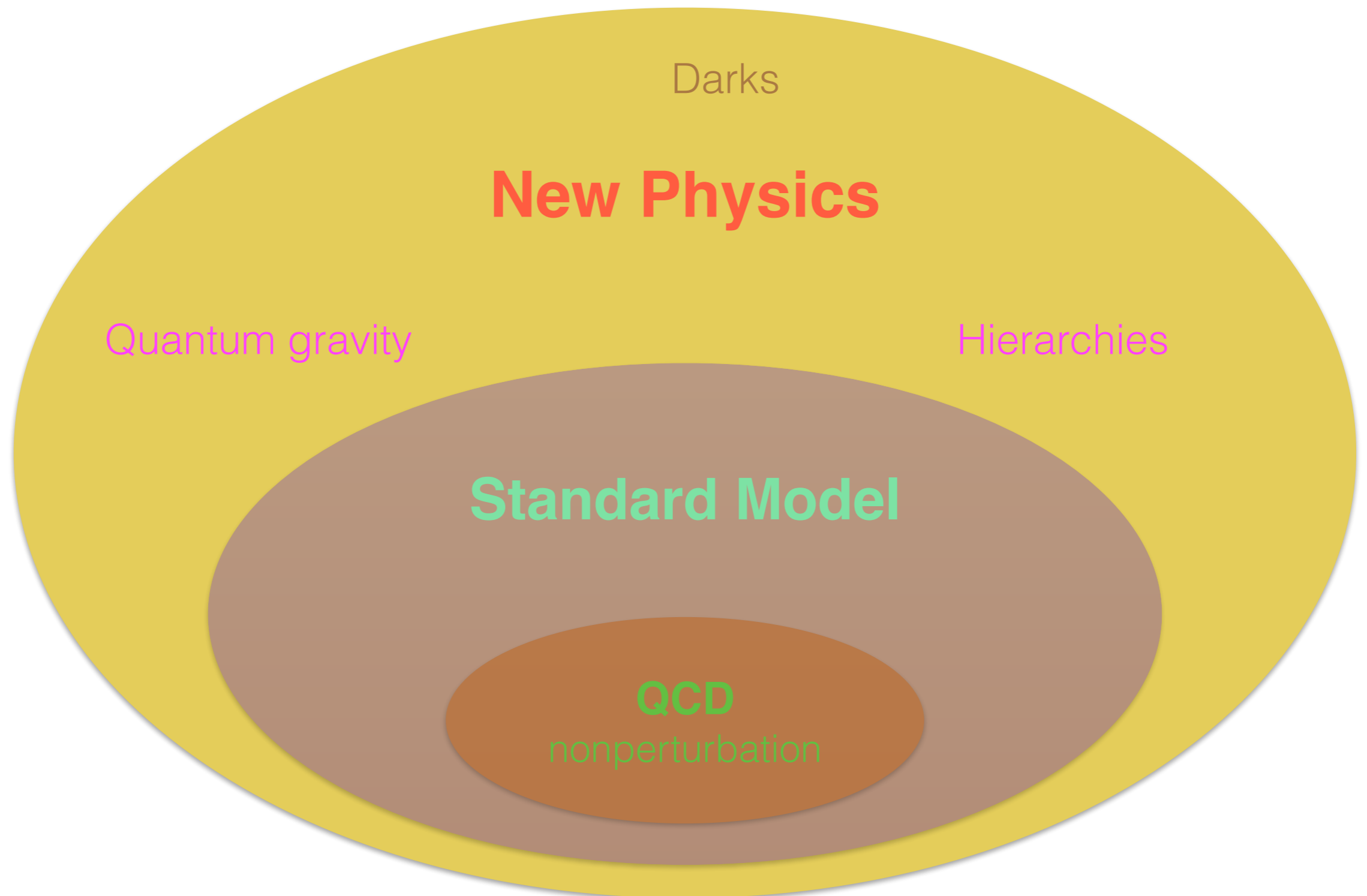
The 20th Workshop of Heavy Flavor Physics and CP Violation
Shanghai, 15-18 July 2023



Contents

- Why $\bar{B} \rightarrow \gamma\gamma$?
- History of (1) $\bar{B} \rightarrow \gamma\gamma$ and (2) the long-distance penguin contribution
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B decays are important!



Why $\bar{B} \rightarrow \gamma\gamma$?

- **FCNC:** Sensitive to [dynamics beyond the SM](#), e.g. [CP violation](#)
- **Simplest** decay (as $B \rightarrow \mu^+ \mu^-$): to address the intricate [strong interaction mechanism](#) of the heavy-meson systems

— — [structure of the B meson](#)

Belle II

Physics Book

Process	Observable	Theory	Sys. limit (Discovery) [ab ⁻¹]	vs LHCb	vs Belle	Anomaly	NP
● $B \rightarrow X_s l^+ l^-$	R_{X_s}	***	>50	***	***	**	***
● $B \rightarrow K^{(*)} e^+ e^-$	$R(K^{(*)})$	***	>50	**	***	***	***
● $B \rightarrow X_s \gamma$	$Br.$	**	1-5	***	*	*	**
● $B_{d,(s)} \rightarrow \gamma\gamma$	$Br., A_{CP}$	**	> 50(5)	**	**	-	**
● $B \rightarrow K^* e^+ e^-$	P'_5	**	>50	***	**	***	***
● $B \rightarrow K \tau l$	$Br.$	***	>50	**	***	**	***

Why $\bar{B} \rightarrow \gamma\gamma$?

- Sensitive to dynamics beyond the SM (FCNC), e.g. CP violation
- **Simplest** decay (as $B \rightarrow \mu^+ \mu^-$) to address the intricate strong interaction mechanism of the heavy-meson systems

— — structure of the B meson

Belle II Physics Book

Observables	Belle 0.71 ab ⁻¹ (0.12 ab ⁻¹)	Belle II 5 ab ⁻¹	Belle II 50 ab ⁻¹
Br($B_d \rightarrow \gamma\gamma$)	< 740%	30%	9.6%
$A_{CP}(B_d \rightarrow \gamma\gamma)$	—	78%	25%
Br($B_s \rightarrow \gamma\gamma$)	< 250%	23%	—

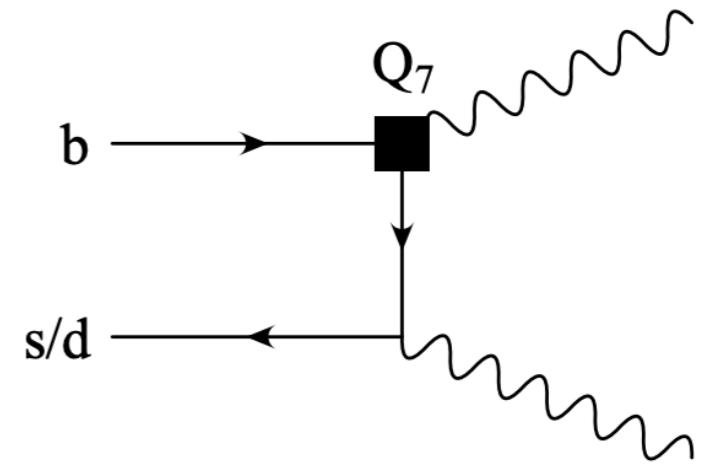
$$\mathcal{BR}(B_d \rightarrow \gamma\gamma) = (1.352_{-0.745}^{+1.242}) \times 10^{-8}, \quad \mathcal{BR}(B_s \rightarrow \gamma\gamma) = (2.964_{-1.614}^{+1.800}) \times 10^{-7}$$

[Y.-L. Shen, Y.-M. Wang, Y.-B. Wei, 2009.02723]

CEPC will have a better performance.

History of $\bar{B} \rightarrow \gamma\gamma$

- LO + NLO



$$\bar{A}(\bar{B}_q \rightarrow \gamma\gamma) = -\frac{4 G_F}{\sqrt{2}} \frac{\alpha_{\text{em}}}{4\pi} \epsilon^{*\alpha}(p) \epsilon^{*\beta}(q) \times \sum_{p=u,c} V_{pb} V_{pq}^* \sum_{i=1}^8 C_i T_{i,\alpha\beta}^{(p)},$$

Leading power

$$T_{i,\alpha\beta}^{(p)} = i m_{B_q}^3 \left[\left(g_{\alpha\beta}^\perp - i \epsilon_{\alpha\beta}^\perp \right) F_{i,L}^{(p)} - \left(g_{\alpha\beta}^\perp + i \epsilon_{\alpha\beta}^\perp \right) F_{i,R}^{(p)} \right],$$

Two polarizations

$F_L^{\text{LP}} \propto m_b \int_0^\infty \frac{d\omega}{\omega} \phi_B^+(\omega, \mu) \propto \frac{m_b}{\lambda_b}$

[Bosch, Buchalla, hep-ph/0208202; Descotes-Genon, Sacharajda, hep-ph/0212162]

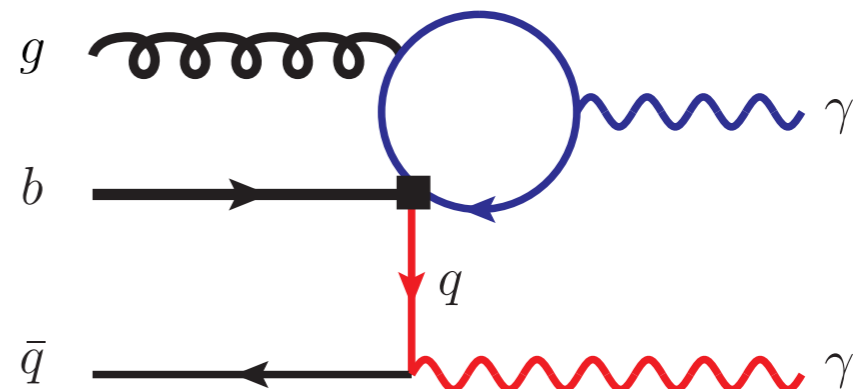
- NLL corrections + Systematic power corrections

both $\sim \mathcal{O}(10\%)$

[Y.-L. Shen, Y.-M. Wang, Y.-B. Wei, 2009.02723]

- One important but tough piece missing — — **long-distance**

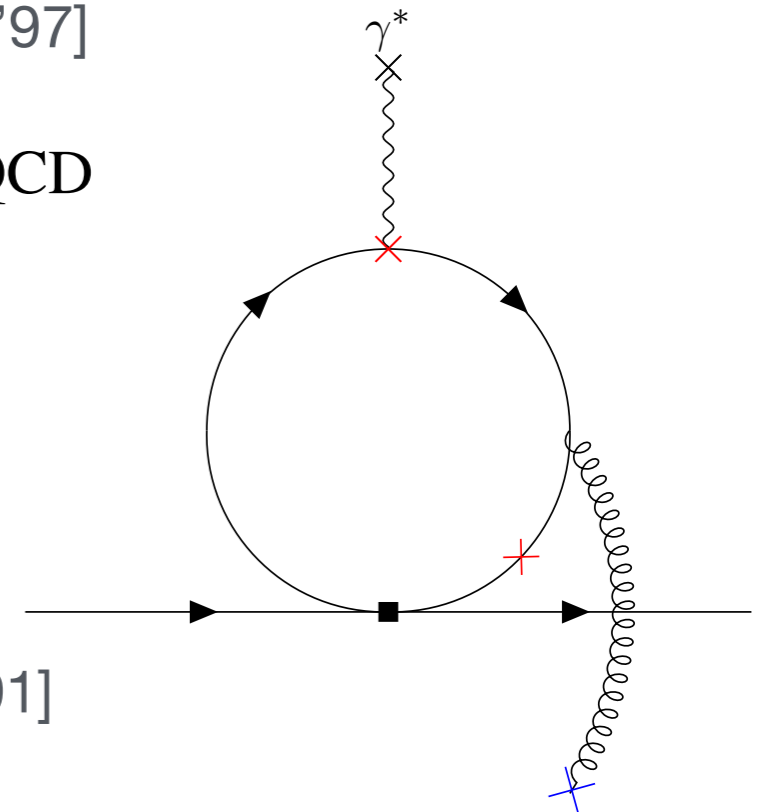
penguin contribution



History of Long-distance penguin contribution

In inclusive $b \rightarrow s$ decays

- Realized in $\bar{B} \rightarrow X_s \gamma$, expansion of $(\Lambda_{\text{QCD}}^2/m_c^2)(m_b \Lambda_{\text{QCD}}/m_c^2)^n$
[Voloshin, '96; Ligeti, Randall, Wise, '97; Buchalla, Isidori, Rey, '97]
- Factorization in $\bar{B} \rightarrow X_s \gamma$ using SCET, $m_c^2 \sim m_b \Lambda_{\text{QCD}}$
[Benzke, Lee, Neubert, Paz, 1003.5012]
- Factorization in $\bar{B} \rightarrow X_s \ell \ell$
[Benzke, Hurth, Turczyk, 1705.10366]
- Phenomenological Application in $\bar{B} \rightarrow X_{d,s} \ell \ell$
[Huber, Hurth, Enrico, Jenkins, **QQ**, Vos, 1908.07507, 2007.04191]

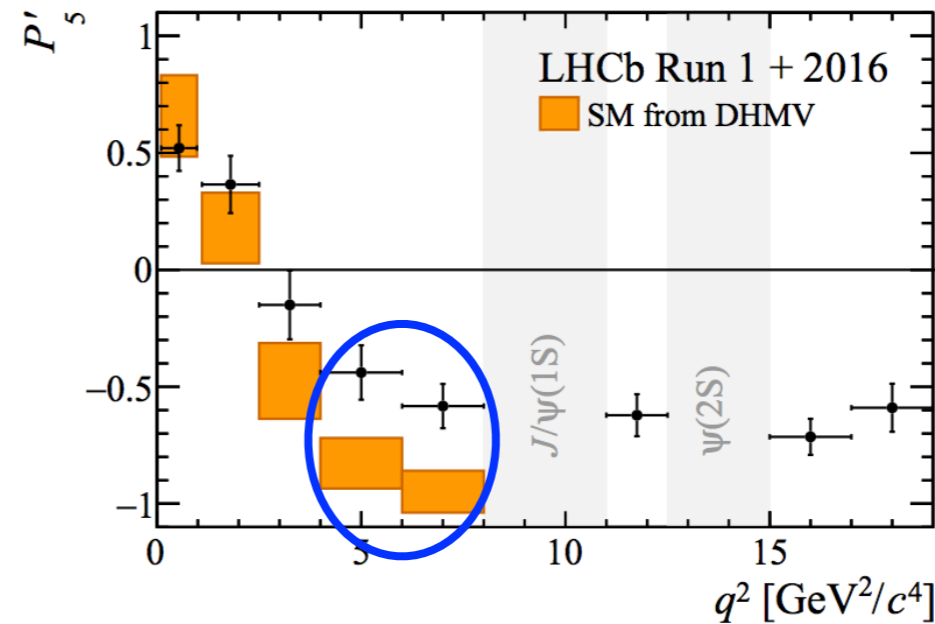
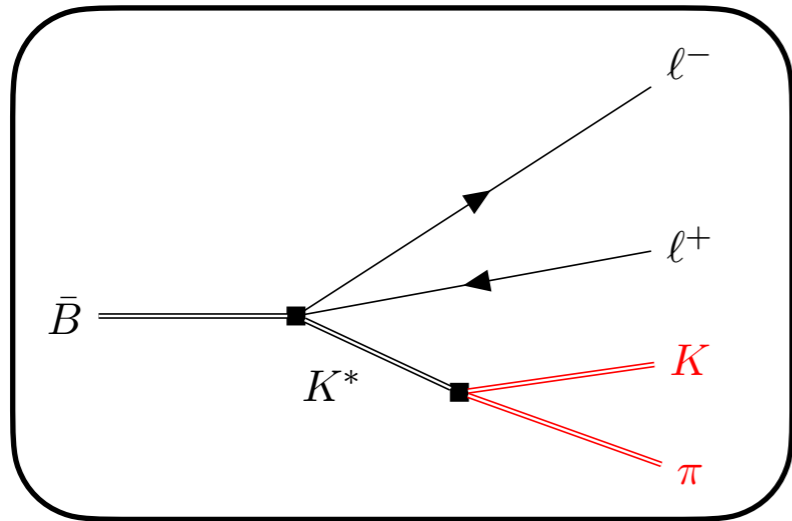


Soft gluon from charm-loop

In exclusive $b \rightarrow s$ decays

- Initiated in $B \rightarrow K^* \gamma$
[Khodjamirian, Ruckl, Stoll, Wyler, '97]
- Developed in $B \rightarrow K^* \ell \ell$
[Khodjamirian, Mannel, Pivovarov, Wang, 1006.4945]

History of Long-distance penguin contribution



P'_5 : an angular-distribution observable

[LHCb, 2003.04831]

Charm-loop effect in $B \rightarrow K^{(*)} \ell^+ \ell^-$ and $B \rightarrow K^* \gamma$

A. Khodjamirian (Siegen U.), Th. Mannel (Siegen U.), A.A. Pivovarov (Siegen U.), Y.-M. Wang (Siegen U.)

Jun, 2010

35 pages

Published in: *JHEP* 09 (2010) 089

e-Print: [1006.4945](https://arxiv.org/abs/1006.4945) [hep-ph]

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Factorization

Factorization

$$\mathcal{H}_{\text{eff}} = \frac{4 G_F}{\sqrt{2}} \sum_{p=u,c} V_{pb} V_{pq}^* \left[C_1(\nu) P_1^p(\nu) + C_2(\nu) P_2^p(\nu) + \sum_{i=3}^8 C_i(\nu) P_i(\nu) + \sum_{i=3}^6 C_i(\nu) P_i^Q(\nu) \right] + \text{h.c.},$$

$$P_1^p = (\bar{q}_L \gamma_\mu T^a p_L) (\bar{p}_L \gamma^\mu T^a b_L),$$

$$P_2^p = (\bar{q}_L \gamma_\mu p_L) (\bar{p}_L \gamma^\mu b_L),$$

$$P_3 = (\bar{q}_L \gamma_\mu b_L) \sum_{q'} (\bar{q}' \gamma^\mu q'),$$

$$P_4 = (\bar{q}_L \gamma_\mu T^a b_L) \sum_{q'} (\bar{q}' \gamma^\mu T^a q'),$$

$$P_5 = (\bar{q}_L \gamma_{\mu_1} \gamma_{\mu_2} \gamma_{\mu_3} b_L) \sum_{q'} (\bar{q}' \gamma^{\mu_1} \gamma^{\mu_2} \gamma^{\mu_3} q'),$$

$$P_6 = (\bar{q}_L \gamma_{\mu_1} \gamma_{\mu_2} \gamma_{\mu_3} T^a b_L) \sum_{q'} (\bar{q}' \gamma^{\mu_1} \gamma^{\mu_2} \gamma^{\mu_3} T^a q'),$$

Factorization

Integrate out the hard and hard-collinear d.o.f.

$$M = H * J * S \quad (m_b \gg m_c \sim \mathcal{O}(\sqrt{\Lambda m_b}) \gg \Lambda_{\text{QCD}})$$

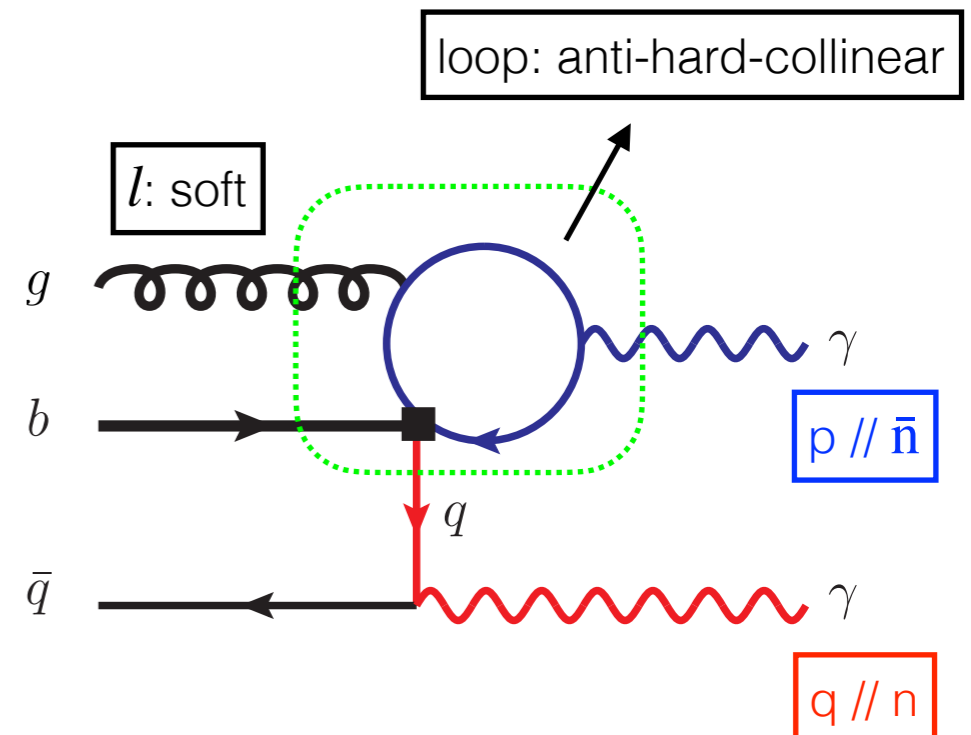
First-step match:

$$M \ni \left(C_2 - \frac{C_1}{2N_c} \right) Q_p \left[F\left(\frac{m_p^2 - i0^+}{(p-l)^2}\right) - 1 \right] \frac{p^\alpha}{(p-l)^2} \left[\bar{q}(\tilde{q}) \gamma_\beta P_L G_{\mu\alpha} \tilde{F}^{\mu\beta} b(v) \right]$$

$$F(x) = 4x \arctan^2\left(\frac{1}{\sqrt{4x-1}}\right)$$

$$(p-l)^2 = -2p \cdot l = -m_b \bar{n} \cdot l$$

 Non-local operator!



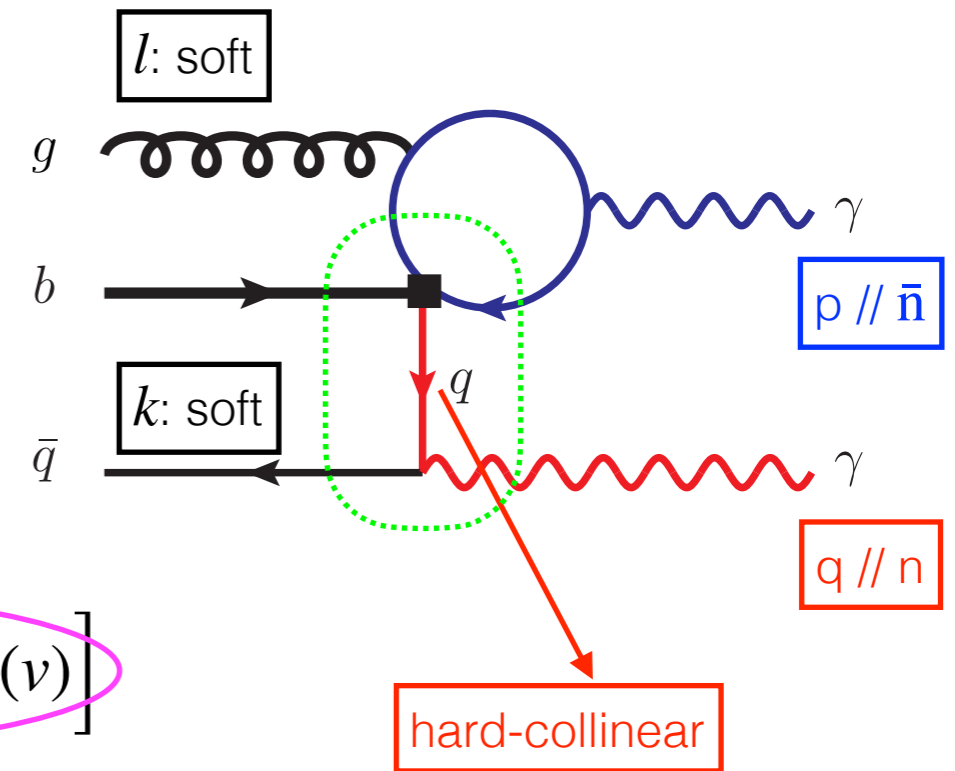
Factorization

Second-step match:

$$\langle \gamma(p) \gamma(q) | \bar{q} \gamma_\beta P_L G_{\mu\alpha} \tilde{F}^{\mu\beta} b | g(l) b(v) \bar{q}(k) \rangle$$

$$\Rightarrow \frac{i g_{em} e_q}{(q-k)^2} \epsilon^{\mu\beta\lambda\tau} p_\lambda \epsilon_\tau^*(p) \epsilon_\rho^*(q) \times \left[\bar{q}(k) \gamma_\perp^\rho \not{q} \gamma_\beta P_L G_{\mu\alpha}(\ell) b(v) \right]$$

$$(q-k)^2 = -2q \cdot k = -m_b n \cdot k$$



- The hard-kernel (jet functions) depends on 2 different light-cone components of the gluon and light quark momenta.
- It becomes evident to introduce the 3-particle B-meson distribution amplitude with 2 light-cone directions.

$$H \star J \star \bar{J} \star \Phi_G$$

Factorization

The explicit factorization formula:

$$\sum_{i=1}^8 C_i F_{i,L}^{(p), \text{soft } 4q} = -\frac{Q_q f_{B_q}}{m_{B_q}} \int_{-\infty}^{+\infty} \frac{d\omega_1}{\omega_1} \int_{-\infty}^{+\infty} \frac{d\omega_2}{\omega_2} \left(C_2 - \frac{C_1}{2N_c} \right) Q_p \left[F\left(-\frac{m_p^2}{m_b \omega_2}\right) - 1 \right] \times \Phi_G(\omega_1, \omega_2, \mu)$$

The light quark momentum component $\omega_1 = n \cdot k$;

The soft gluon momentum component $\omega_2 = \bar{n} \cdot l$.

The novel B-meson DA:

$$\begin{aligned} & \langle 0 | \bar{q}_s(\tau_1 n) (g_s G_{\mu\nu})(\tau_2 \bar{n}) \bar{n}^\nu \not{n} \gamma_\perp^\mu \gamma_5 h_\nu(0) | \bar{B}_\nu \rangle \\ & = 2 \tilde{f}_B(\mu) m_B \int_{-\infty}^{+\infty} d\omega_1 \int_{-\infty}^{+\infty} d\omega_2 \exp[-i(\omega_1 \tau_1 + \omega_2 \tau_2)] \Phi_G(\omega_1, \omega_2, \mu) \end{aligned}$$

- The quark and gluon fields are localized on 2 distinct light-cone directions.

Non-trivial RG evolution of this soft function, mixing positive into negative support of $\omega_{1,2}$. See an upcoming paper [Huang, Ji, Shen, Wang, Wang, Zhao, 2023].

Factorization

The (tree-level) normalization conditions of Φ_G :

Matching the conventional 3-particle B meson DAs as τ_1 or $\tau_2 \rightarrow 0$.

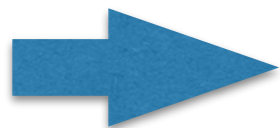
$$\langle 0 | \bar{q}(z_1)(g_s G_{\mu\nu})(z_2) \bar{n}^\nu \not{n} \gamma_\perp^\mu \gamma_5 h_\nu(0) | \bar{B}_\nu \rangle = 2\tilde{f}_B(\mu)\Phi_4(z_1, z_2, \mu)$$

Twist 4

$$\langle 0 | \bar{q}(z_1)(g_s G_{\mu\nu})(z_2) n^\nu \not{n} \gamma_\perp^\mu \gamma_5 h_\nu(0) | \bar{B}_\nu \rangle = 2\tilde{f}_B(\mu)\Phi_5(z_1, z_2, \mu)$$

Twist 5

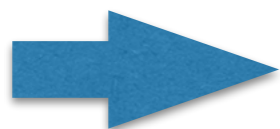
[Braun, Ji, Manashov, 1703.02446]



$$\int_0^\infty d\omega_1 \Phi_G(\omega_1, \omega_2, \mu) = \int_0^\infty d\omega_1 \Phi_4(\omega_1, \omega_2, \mu),$$

$$\int_0^\infty d\omega_2 \Phi_G(\omega_1, \omega_2, \mu) = \int_0^\infty d\omega_2 \Phi_5(\omega_1, \omega_2, \mu),$$

$$\int_0^\infty d\omega_1 \int_0^\infty d\omega_2 \Phi_G(\omega_1, \omega_2, \mu) = \frac{\lambda_E^2 + \lambda_H^2}{3},$$



The power counting: $F_L^{\text{soft}, 4q} / F_L^{\text{LP}} \sim \lambda_B / m_b$

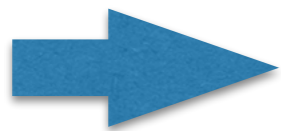
Factorization

The asymptotic behaviors of Φ_G :

$$\Phi_G(\omega_1, \omega_2, \mu) \sim \omega_1 \omega_2^2 \text{ at } \omega_1, \omega_2 \rightarrow 0$$

The explicit factorization formula:

$$\sum_{i=1}^8 C_i F_{i,L}^{(p), \text{soft } 4q} = -\frac{Q_q f_{B_q}}{m_{B_q}} \int_0^{+\infty} \frac{d\omega_1}{\omega_1} \int_0^{+\infty} \frac{d\omega_2}{\omega_2} \left(C_2 - \frac{C_1}{2N_c} \right) Q_p \left[F\left(-\frac{m_p^2}{m_b \omega_2}\right) - 1 \right] \times \Phi_G(\omega_1, \omega_2, \mu)$$

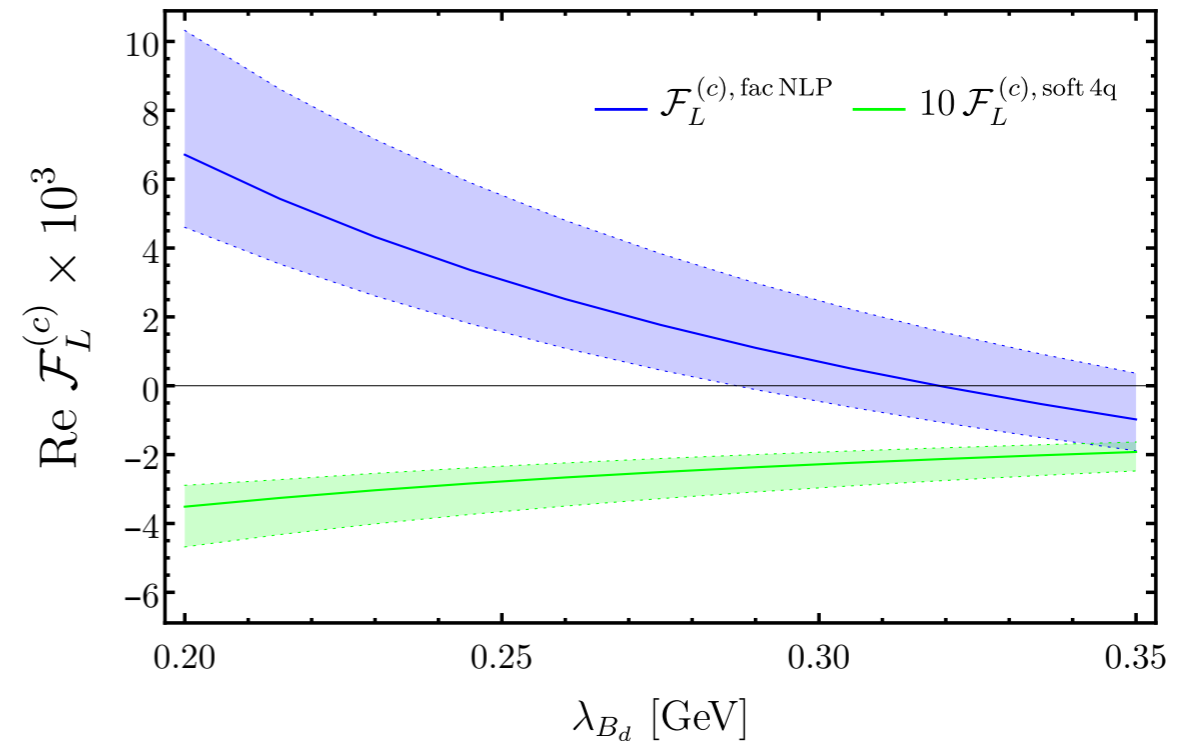
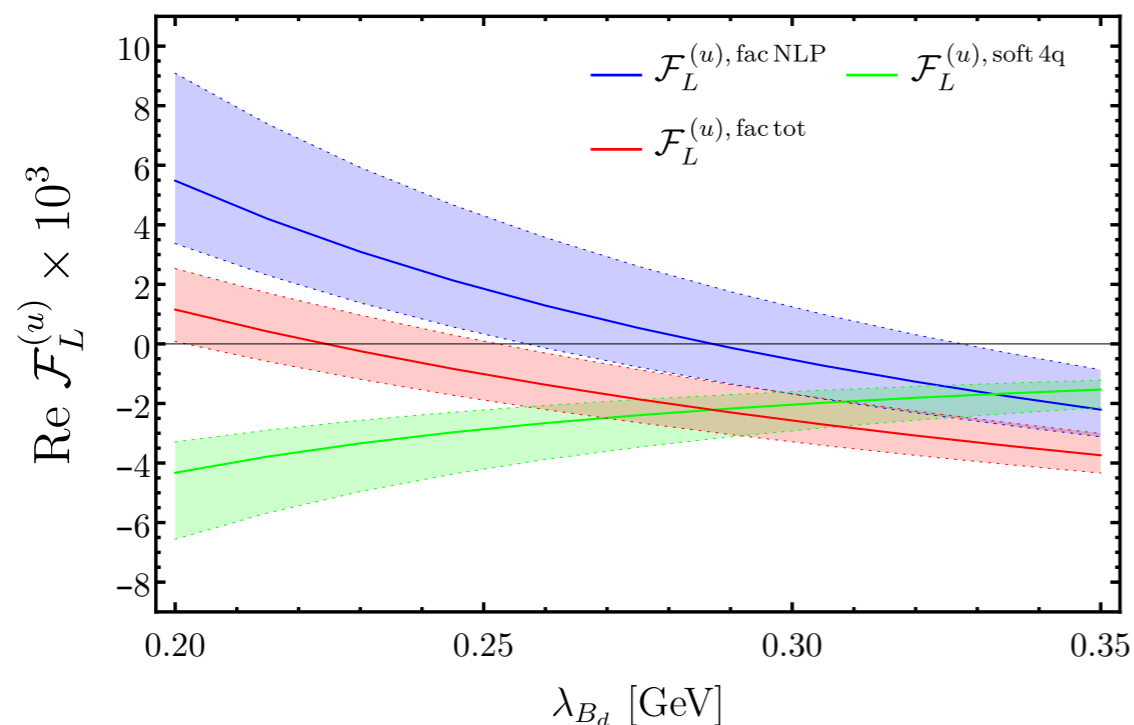


The convolution integral converges.

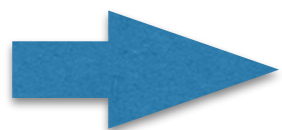
Numerics

The Φ_G parametrization:

$$\Phi_G(\omega_1, \omega_2, \mu_0) = \frac{\lambda_E^2 + \lambda_H^2}{6} \frac{\omega_1 \omega_2^2}{\omega_0^5} \exp\left(-\frac{\omega_1 + \omega_2}{\omega_0}\right) \frac{\Gamma(\beta + 2)}{\Gamma(\alpha + 2)} U\left(\beta - \alpha, 4 - \alpha, \frac{\omega_1 + \omega_2}{\omega_0}\right)$$



- The up-loop contribution dominates; the charm-loop is 1-order smaller.
- The new power correction accidentally cancels the previous ones.



Clean channel to determine λ_B and to probe new physics.

Numerics

The B_d results:

	Central Value	Total Error	λ_{B_d}	$\{\hat{\sigma}_{B_d}^{(1)}, \hat{\sigma}_{B_d}^{(2)}\}$	μ	ν	μ_h	$\bar{\Lambda}$	m_c^{PS}
$10^8 \times \mathcal{BR}$	1.929 [1.900]	+1.096 -1.012	+0.680 -0.439	+0.736 -0.779	+0.083 -0.299	+0.278 -0.287	+0.246 -0.066	+0.212 -0.200	+0.043 -0.043
f_{\parallel}	0.408 [0.407]	+0.044 -0.046	+0.015 -0.015	+0.016 -0.033	+0.002 -0.009	+0.037 -0.026	+0.007 -0.002	+0.005 -0.006	+0.002 -0.002
f_{\perp}	0.592 [0.593]	+0.046 -0.044	+0.015 -0.015	+0.033 -0.016	+0.009 -0.002	+0.026 -0.037	+0.002 -0.007	+0.006 -0.005	+0.002 -0.002
$\mathcal{A}_{\text{CP}}^{\text{dir}, \parallel}$	0.126 [0.129]	+0.043 -0.027	+0.007 -0.004	+0.017 -0.010	+0.013 -0.008	+0.027 -0.018	+0.024 -0.012	+0.007 -0.007	+0.004 -0.004
$\mathcal{A}_{\text{CP}}^{\text{mix}, \parallel}$	-0.197 [-0.154]	+0.053 -0.084	+0.019 -0.036	+0.001 -0.002	+0.021 -0.047	+0.026 -0.040	+0.015 -0.029	+0.011 -0.013	+0.008 -0.009
$\mathcal{A}_{\Delta\Gamma}^{\parallel}$	-0.972 [-0.980]	+0.024 -0.013	+0.009 -0.004	+0.003 -0.002	+0.013 -0.005	+0.013 -0.007	+0.010 -0.004	+0.004 -0.003	+0.002 -0.002
$\mathcal{A}_{\text{CP}}^{\text{dir}, \perp}$	0.330 [0.326]	+0.078 -0.053	+0.015 -0.012	+0.060 -0.035	+0.035 -0.014	+0.012 -0.024	+0.014 -0.010	+0.018 -0.016	+0.018 -0.017
$\mathcal{A}_{\text{CP}}^{\text{mix}, \perp}$	0.136 [0.101]	+0.087 -0.066	+0.043 -0.028	+0.015 -0.035	+0.025 -0.014	+0.060 -0.038	+0.026 -0.012	+0.003 -0.003	+0.009 -0.008
$\mathcal{A}_{\Delta\Gamma}^{\perp}$	0.934 [0.940]	+0.017 -0.030	+0.000 -0.003	+0.009 -0.019	+0.007 -0.017	+0.001 -0.002	+0.005 -0.009	+0.006 -0.007	+0.007 -0.008

Summary and prospects

- We have factorized the long-distance penguin contribution to $\bar{B} \rightarrow \gamma\gamma$ decay, for the first time in an exclusive decay.
- A novel B-meson DA is introduced, with quark and gluon fields localized on two different light-cone directions. It will open a new subfield about the inner structure of the B meson.
- The new contribution cancels the known factorizable power corrections, making $\bar{B} \rightarrow \gamma\gamma$ a clean channel to determine λ_B and to probe the non-standard dynamics.
- The developed formalism has a broad field of applications to the entire spectrum of the exclusive FCNC B-meson decays, including flagship modes, e.g. $B \rightarrow K^*\gamma$, $B \rightarrow K^*\mu\mu$.

Thank you!

Backup

	B_d	B_s
$\mathcal{A}^{\text{LP,NLL}} [10^{-4}]$	$3.4 + 1.9i$	$-20 - 0.37i$
$\mathcal{A}^{\text{fac,NLP}} [10^{-4}]$	$-0.15 - 0.53i$	$0.92 + 2.6i$
$\mathcal{A}_R^{\text{fac,NLP}} [10^{-4}]$	$0.25 - 0.36i$	$-1.6 + 2.6i$
$\mathcal{A}^{\text{had},\gamma} [10^{-4}]$	$-0.30 - 0.17i$	$1.4 - 0.0021i$
$\mathcal{A}^{\text{soft},4q} [10^{-4}]$	$(-0.0079 + 0.078i)$	$-0.11 + 0.016i$
$(F_u^{\text{LP,NLL}}, F_c^{\text{LP,NLL}})$	$(-0.056 - 0.0092i, -0.048 - 0.0019i)$	$(-0.057 - 0.0094i, -0.049 - 0.0020i)$
$(F_u^{\text{had},\gamma}, F_c^{\text{had},\gamma})$	$(0.0051 + 0.00092i, 0.0043 + 0.00019i)$	$(0.0094 + 0.0016i, 0.0034 + 0.00016i)$
$(F_u^{\text{soft},4q}, F_c^{\text{soft},4q})$	$(-0.0024, -0.00025)$	$(-0.0021, -0.00025)$
$(F_u^{\text{HC}}, F_c^{\text{HC}})$	$(0.0055, 0.0055)$	$(0.0067, 0.0067)$
$(F_u^{\text{mq}}, F_c^{\text{mq}})$	$(0.000049, 0.000049)$	$(0.00078, 0.00078) [0.00079]$
$(F_u^{\text{A}_2}, F_c^{\text{A}_2})$	$(-0.0010, -0.0010)$	$(-0.0011, -0.0011)$
$(F_u^{\text{HT}}, F_c^{\text{HT}})$	$(0.0046, 0.0046) [0.0047]$	$(0.0048, 0.0048) [0.0050]$
$(F_u^{\text{Q}_b}, F_c^{\text{Q}_b})$	$(-0.0036, -0.0036)$	$(-0.0043, -0.0043)$
$(F_u^{\text{WA}}, F_c^{\text{WA}})$	$(-0.0049 + 0.000092i, -0.0037 + 0.0056i)$	$(-0.0059 + 0.00011i, -0.0045 + 0.0065i)$
$(F_u^{\text{fac,NLP}}, F_c^{\text{fac,NLP}})$	$(0.00054 + 0.000092i, 0.0018 + 0.0056i)$	$(0.00098 + 0.00011i, 0.0023 + 0.0065i)$
	$[(0.00063 + 0.000092i, 0.0019 + 0.0056i)]$	$(0.0011 + 0.00011i, 0.0024 + 0.0065i)$
$(F_{R,u}^{\text{fac,NLP}}, F_{R,c}^{\text{fac,NLP}})$	$(-0.0046 + 0.000092i, -0.0033 + 0.0056i)$	$(-0.0054 + 0.00011i, -0.0041 + 0.0065i)$

$$A = V_{uq}^* V_{ub} F_u + V_{cq}^* V_{cb} F_c \quad (q = d, s)$$