



Highlights of Recent Charm Results @ LHCb

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Outline

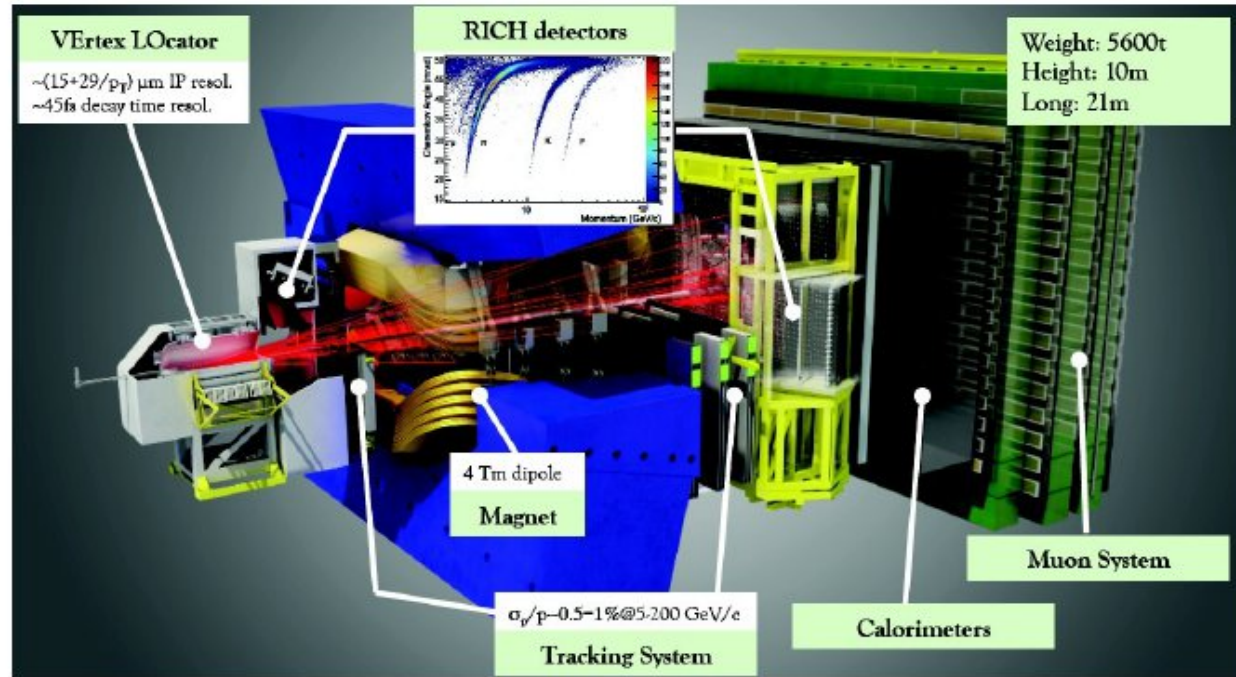
- Experimental details
- Charm mixing & CPV
- Direct CPV in multi-body charm decays
- Rare charm decays
- Prospects & outlook

Up-to-date LHCb charm results can be found at

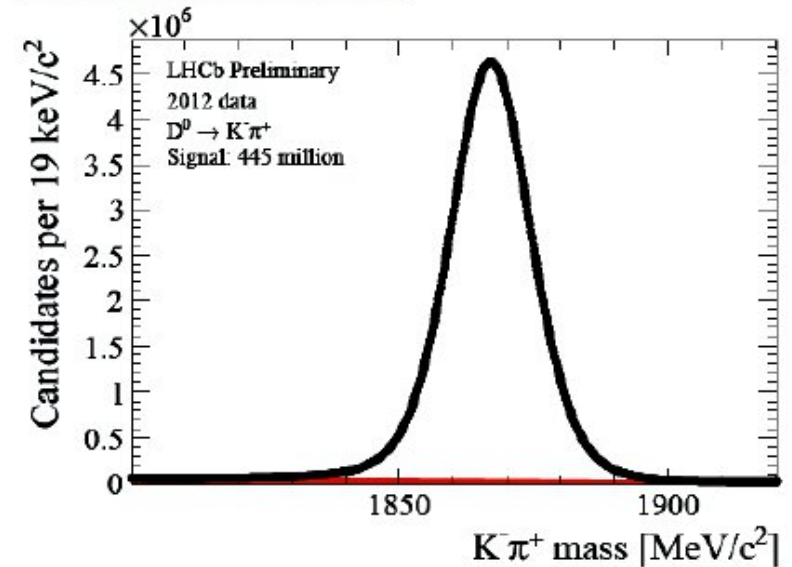
https://lhcbproject.web.cern.ch/Publications/LHCbProjectPublic/Summary_Charm.html

More than 90 papers and counting!

LHCb as a charm factory



LHCb-CONF-2016-005



- LHCb acceptance: $2 < \eta < 5$ (forward region)
- Large production cross-section

[JHEP 03 (2016) 159]

$$\sigma(pp \rightarrow c\bar{c}) = (2369 \pm 3 \pm 152 \pm 118) \mu\text{b} @ 13 \text{ TeV} \quad \sim 20 \times \sigma(pp \rightarrow b\bar{b}X)$$

- More than 1 billion $D^0 \rightarrow K\pi^+$ collected by LHCb between 2011 and 2018
- Run2: Turbo stream from online reconstruction

[Comput. Phys. Commun. 208 (2016) 35]

Charm mixing & CPV

- Charm mixing – a well-established fact:
 - Mass eigenstates are related to their flavor eigenstates via $|D_{1,2}\rangle \equiv p|D^0\rangle \pm q|\bar{D}^0\rangle$, with $|q|^2 + |p|^2 \equiv 1$
 - **Mixing parameters** based on the mass and width differences: $x \equiv (m_2 - m_1)/\Gamma$, $y \equiv (\Gamma_2 - \Gamma_1)/2\Gamma$, with $\Gamma \equiv (\Gamma_2 + \Gamma_1)/2$

- *CP* violation contributions:

- In decays: amplitudes for a process and its conjugate differ

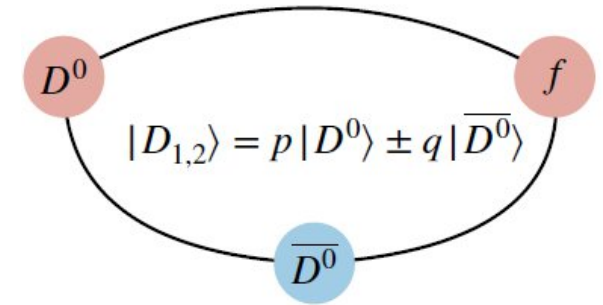
Direct *CP* violation $\left| \frac{\bar{A}_f}{A_f} \right|^{\pm 2} \approx 1 \pm A_d \rightarrow a_{CP}^{dir} \approx -\frac{1}{2} A_d$

- In mixing: rates of $D^0 \rightarrow \bar{D}^0$ and $\bar{D}^0 \rightarrow D^0$ differ

Indirect *CP* violation $\left| \frac{q}{p} \right|^{\pm 2} \approx 1 \pm A_m \rightarrow a_{CP}^{ind} = -\frac{A_m}{2} y \cos \phi + x \sin \phi$

ϕ : weak phase, A_m : CPV from mixing

- In interference between mixing and decay diagrams

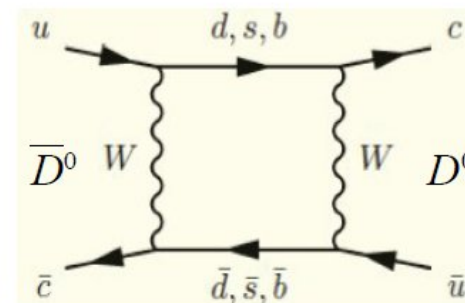


Unitarity triangle for charm

$$V_{ud}V_{cd}^* + V_{us}V_{cs}^* + V_{ub}V_{cb}^* = 0$$

$$\sim \lambda \quad \sim \lambda \quad \sim \lambda^5$$

$$\lambda = \sin(\theta_c) \sim 0.23$$



Expected CPV very small in charm

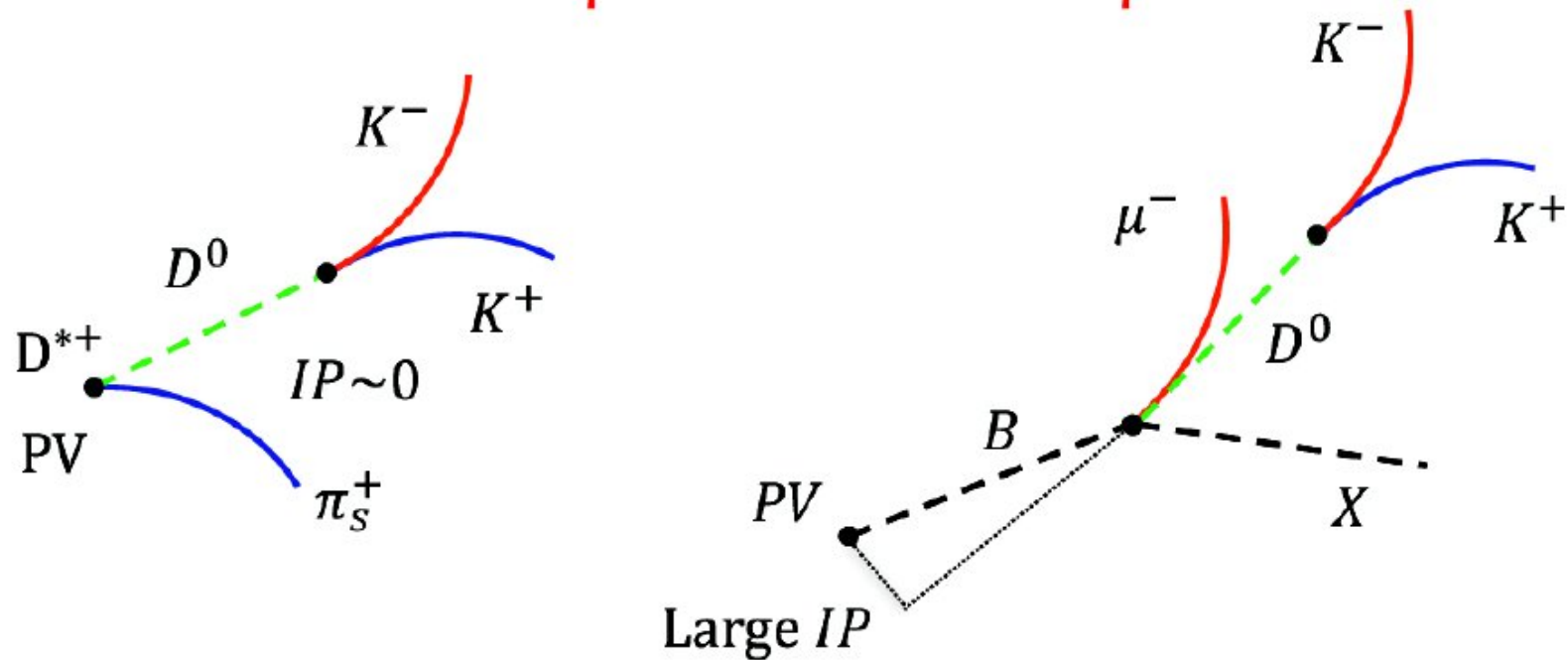
- Effectively 2-generation system
- 3rd generation and CPV enter through loops

NP if CPV found?

D^0 production at LHCb

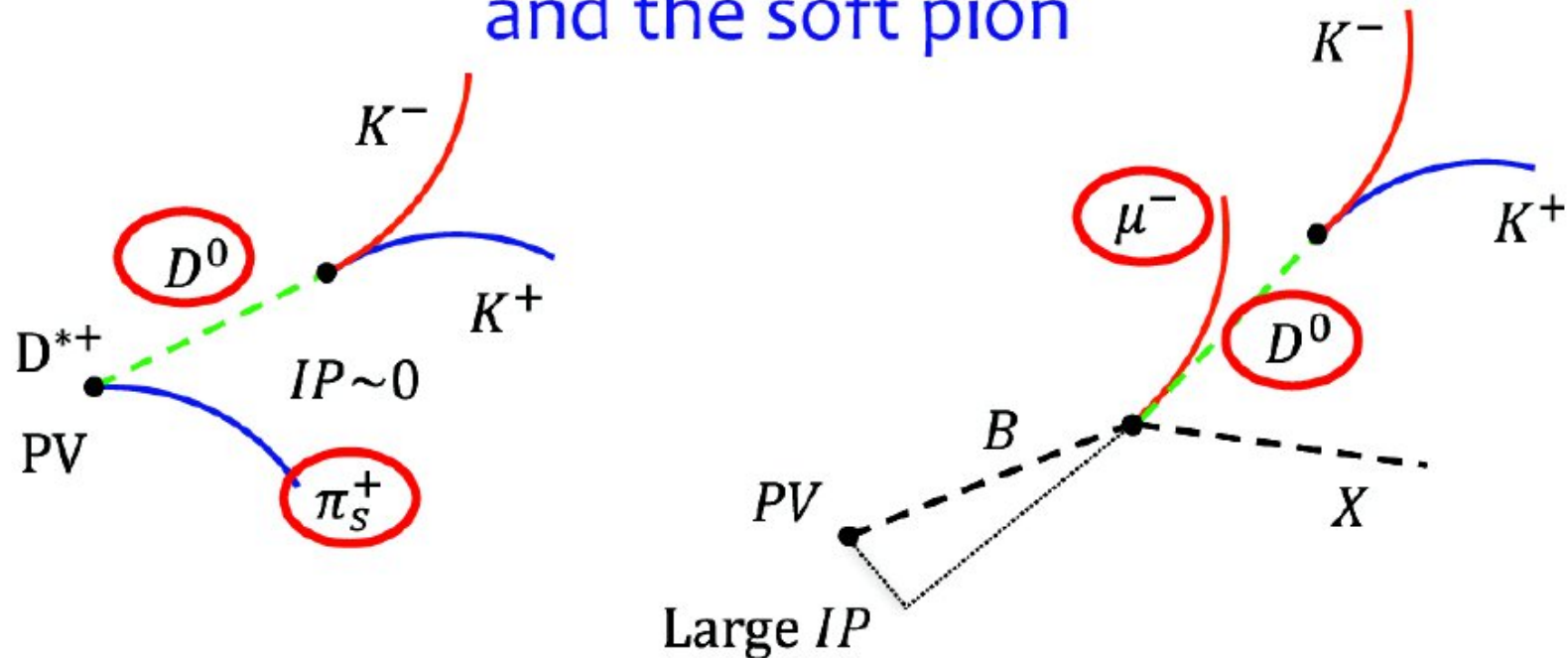
Two mechanisms of D^0 production

Independent data sample



D^0 flavor tagging at LHCb

Experimentally we can tag D^0 flavour at production by means of the charge of the muon and the soft pion



CPV in $D^0 \rightarrow K^+ K^- / \pi^+ \pi^-$

- Using Run 2 (5.6 fb⁻¹) data with ~70M $D^0 \rightarrow K^+ K^-$ candidates
- Combination of two methods using Cabibbo-favored (no CPV) $D^0/D^+/D_s^+$ decays to cancel detector/production asymmetries in $D^0 \rightarrow K^+ K^-$:

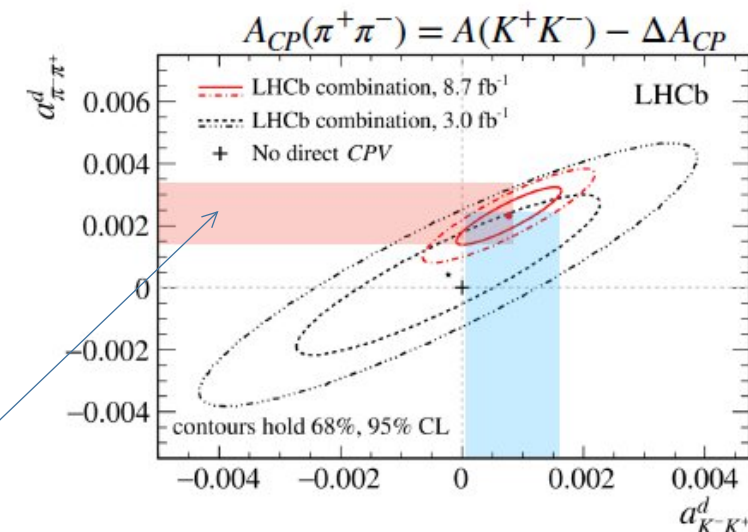
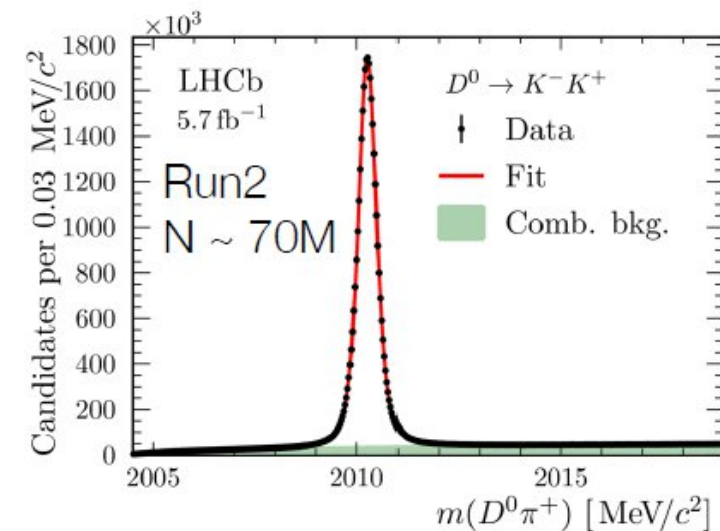
$$A_{CP}(K^+ K^-) = [6.8 \pm 5.4(\text{stat}) \pm 1.6(\text{sys})] \times 10^{-4}$$

- Combination with Run1 & ΔA_{CP} results yields:

$$a_{CP}^d(K^+ K^-) = [7.7 \pm 5.7] \times 10^{-4}$$

$$a_{CP}^d(\pi^+ \pi^-) = [23.2 \pm 6.1] \times 10^{-4}$$

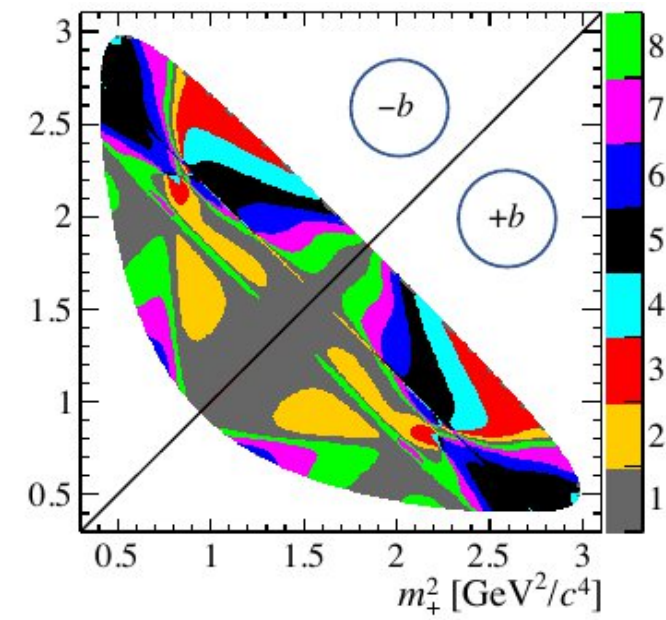
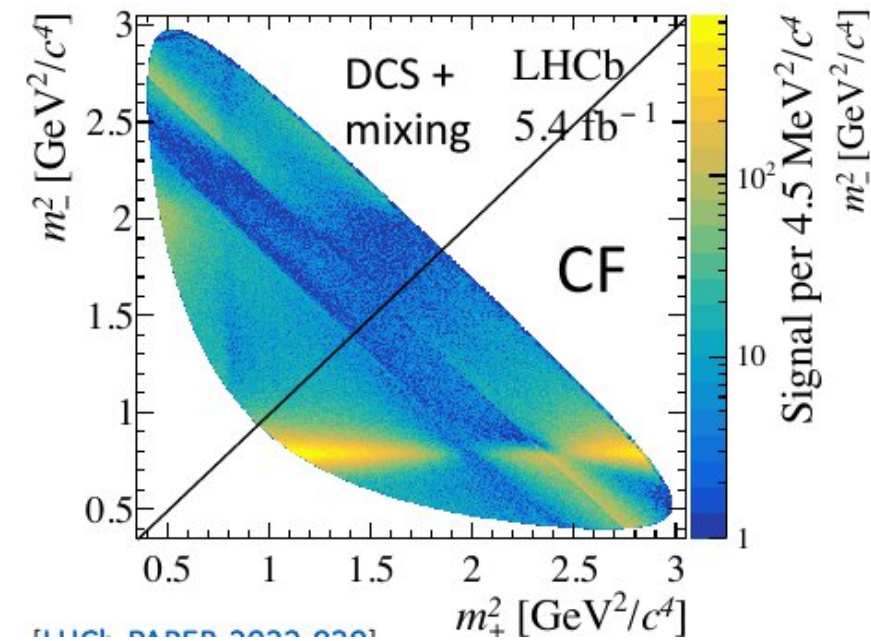
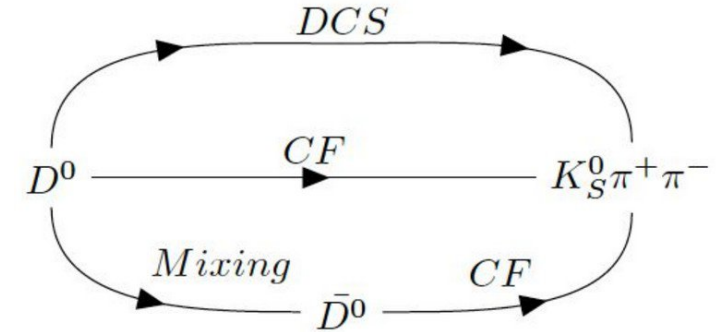
$$\rho(a_{KK}^d, a_{\pi\pi}^d) = 88\%$$



First evidence (3.8σ) of CPV in $D^0 \rightarrow \pi^+ \pi^-$!

$D^0 - \bar{D}^0$ oscillation in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

- Run2 prompt (SL) datasets with $\sim 31\text{M}$ (3.7M) candidates
- Bin-flip method: model-independent approach, no need for modeling of Dalitz-plot efficiency & decay amplitudes



Simultaneous fit of the yield ratio R_b^\pm (\pm for initial D^0/\bar{D}^0) between $+b$ and $-b$ in bins of D^0 decay time t :

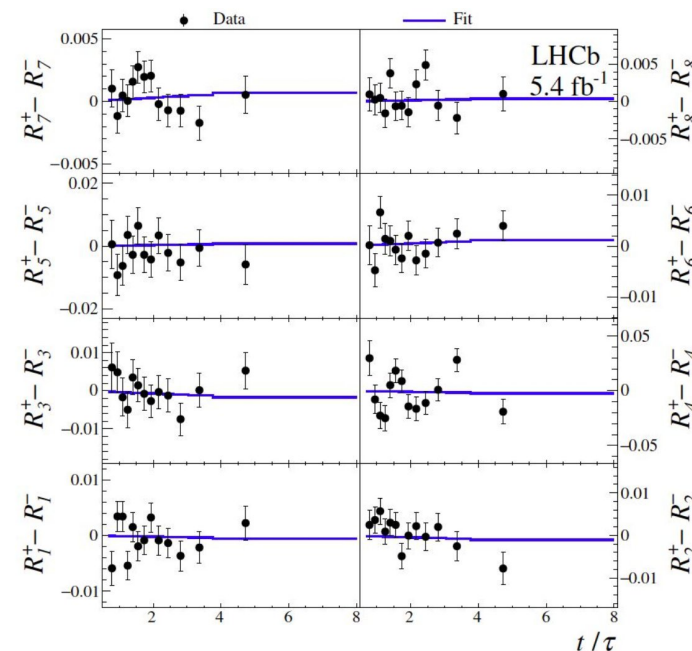
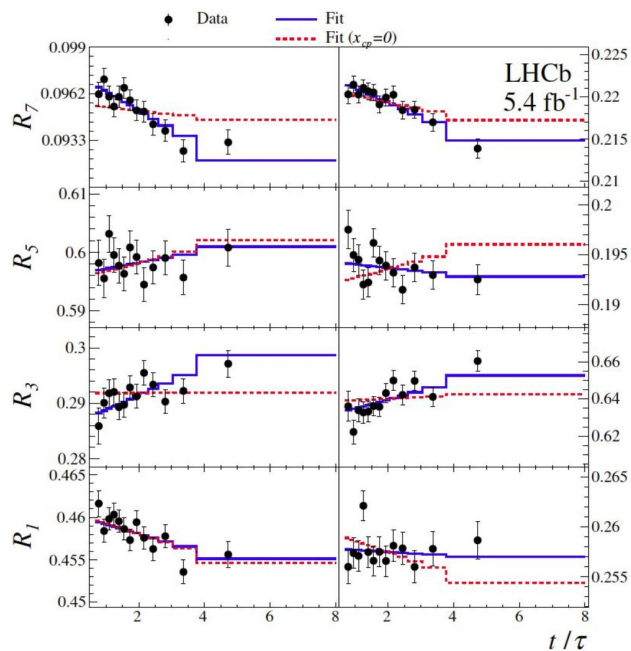
$$R_b^\pm(t) \approx r_b - \sqrt{r_b}[(1 - r_b)c_b y - (1 + r_b)s_b x]\Gamma t$$

- $r_b \equiv R_b(t = 0)$
- c_b and s_b : parameters related to the strong phase differences between $\pm b$ regions (based on external inputs from [CLEO](#) and [BESIII](#)).

$D^0 - \bar{D}^0$ oscillation in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

Mixing measurement: $D^0 + \bar{D}^0$

CPV measurement: $D^0 - \bar{D}^0$



$$x_{CP} = (3.97 \pm 0.46 \pm 0.29) \times 10^{-3}$$

$$y_{CP} = (4.59 \pm 1.20 \pm 0.85) \times 10^{-3}$$

$$\Delta x = (-0.27 \pm 0.18 \pm 0.01) \times 10^{-3}$$

$$\Delta y = (0.20 \pm 0.36 \pm 0.13) \times 10^{-3}$$

$$x = (3.98_{-0.54}^{+0.56}) \times 10^{-3}$$

$$y = (4.6_{-1.4}^{+1.5}) \times 10^{-3}$$

$$|q/p| = 0.996 \pm 0.052$$

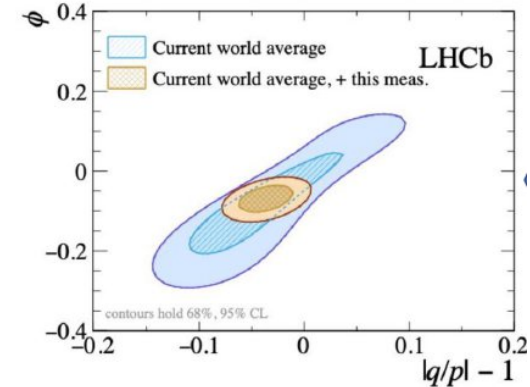
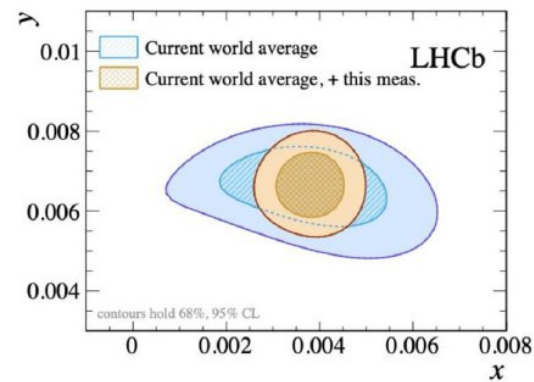
$$\phi = 0.056_{-0.051}^{+0.047}$$

First observation of non-zero x ($>7\sigma$)

$$R_{bj}^{\pm} = \frac{r_b [1 + \frac{1}{4} t_j^2 \text{Re}(z_{CP}^2 - \Delta z^2)] + \frac{1}{4} t_j^2 |z_{CP} \pm \Delta z|^2 + \sqrt{r_b} t_j \text{Re}[\mathbf{X}_b^*(z_{CP} \pm \Delta z)]}{[1 + \frac{1}{4} t_j^2 \text{Re}(z_{CP}^2 - \Delta z^2)] + r_b \frac{1}{4} t_j^2 |z_{CP} \pm \Delta z|^2 + \sqrt{r_b} t_j \text{Re}[\mathbf{X}_b(z_{CP} \pm \Delta z)]}$$

where $z_{CP} \pm \Delta z = -(\frac{q}{p})^{\pm}(y + ix)$ and r_b is ratio without mixing $\mathbf{X}_b = \mathbf{c}_b - i\mathbf{s}_b$

LHCb measures tiny mass difference between particles

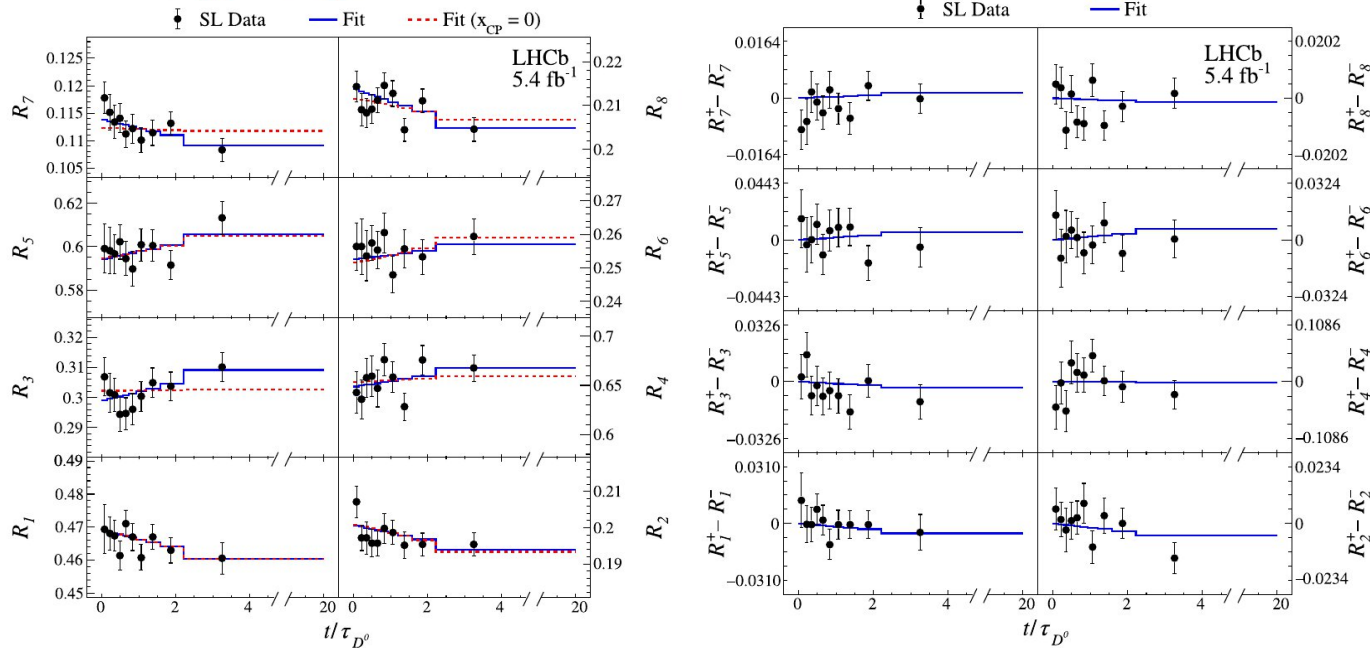


World Averages significantly improved!

$D^0 - \bar{D}^0$ oscillation in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

Mixing measurement: $D^0 + \bar{D}^0$

CPV measurement: $D^0 - \bar{D}^0$



$$x_{CP} = [4.01 \pm 0.45(\text{stat}) \pm 0.20(\text{syst})] \times 10^{-3},$$

$$y_{CP} = [5.51 \pm 1.16(\text{stat}) \pm 0.59(\text{syst})] \times 10^{-3},$$

$$\Delta x = [-0.29 \pm 0.18(\text{stat}) \pm 0.01(\text{syst})] \times 10^{-3},$$

$$\Delta y = [0.31 \pm 0.35(\text{stat}) \pm 0.13(\text{syst})] \times 10^{-3}.$$

$$x = (4.01 \pm 0.49) \times 10^{-3},$$

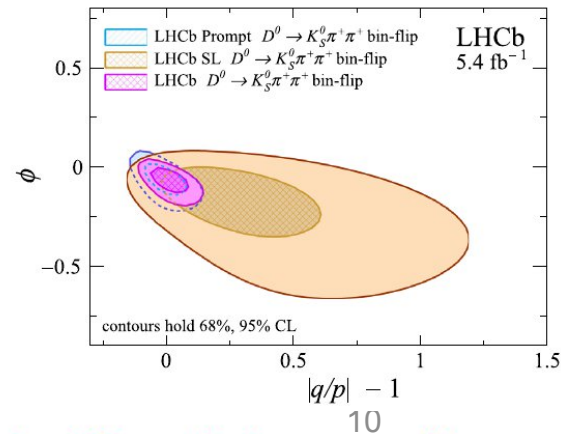
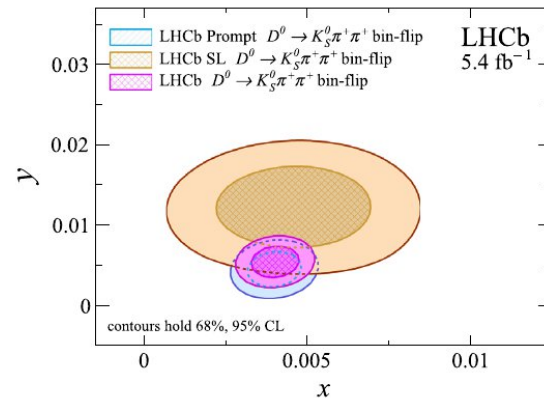
$$y = (5.5 \pm 1.3) \times 10^{-3},$$

$$|q/p| = 1.012_{-0.048}^{+0.050},$$

$$\phi = -0.061_{-0.044}^{+0.037} \text{ rad.}$$

$$R_{bj}^{\pm} = \frac{r_b [1 + \frac{1}{4} t_j^2 \text{Re}(z_{CP}^2 - \Delta z^2)] + \frac{1}{4} t_j^2 |z_{CP} \pm \Delta z|^2 + \sqrt{r_b} t_j \text{Re}[\mathbf{X}_b^*(z_{CP} \pm \Delta z)]}{[1 + \frac{1}{4} t_j^2 \text{Re}(z_{CP}^2 - \Delta z^2)] + r_b \frac{1}{4} t_j^2 |z_{CP} \pm \Delta z|^2 + \sqrt{r_b} t_j \text{Re}[\mathbf{X}_b^*(z_{CP} \pm \Delta z)]},$$

where $z_{CP} \pm \Delta z = -(\frac{q}{p})^{\pm}(y + ix)$ and r_b is ratio without mixing $\mathbf{X}_b = \mathbf{c}_b - i\mathbf{s}_b$



World Averages significantly improved!

Direct CPV in 3-body D decays

- In multi-body decays, strong phase δ vary across the phase space
- Locally enhanced CPV effects possible due to interference
 - Already observed in charmless 3-body B^+ decays by LHCb [see e.g. [PRD 108 \(2023\) 012008](#)]
- Recent model-independent searches for direct CPV on Dalitz-plot planes of:
 - $D_{(s)}^+ \rightarrow K^- K^+ K^+$ [JHEP 07 (2023) 067]
 - $D^0 \rightarrow \pi^+ \pi^- \pi^0$ [JHEP 09 (2023) 129]
 - $D^0 \rightarrow K_S^0 K^\pm \pi^\mp$ [arXiv:2310.19397]

All dominated by
CS/DCS amplitudes

Direct CPV in $D_{(S)}^+ \rightarrow K^- K^+ K^+$

- Run 2 (5.6 fb^{-1}) data
- Binned method:

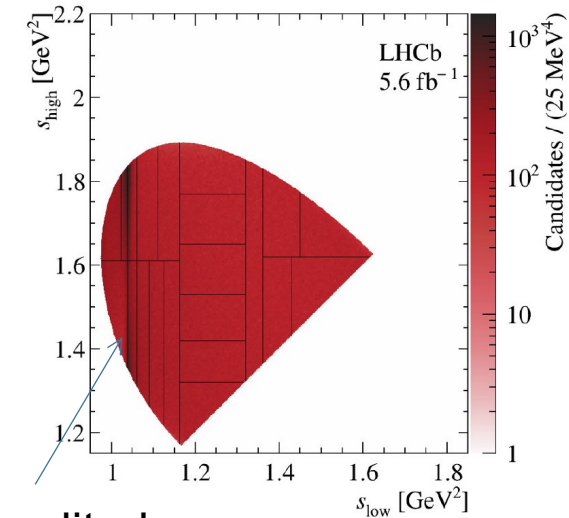
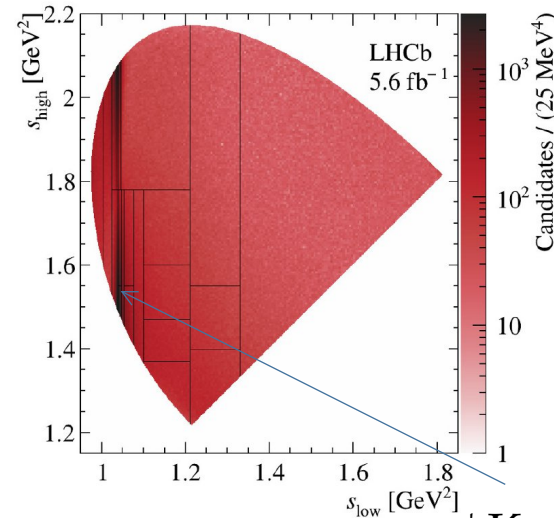
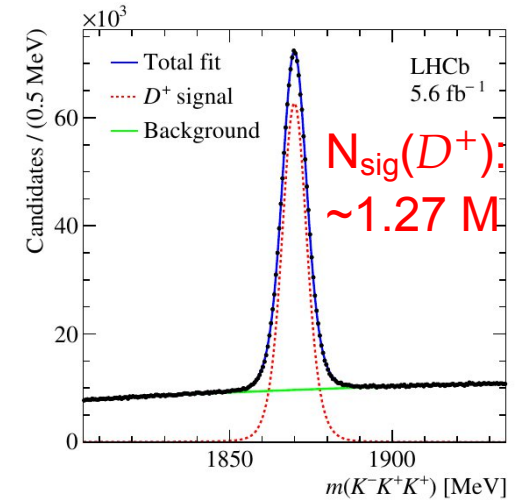
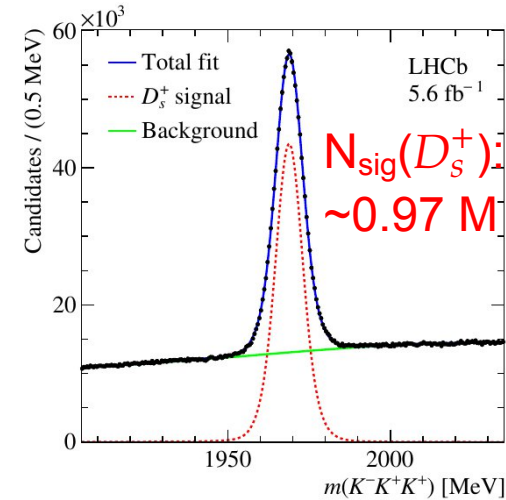
$$S_{CP}^i = \frac{N_+^i - \alpha N_-^i}{\sqrt{\alpha(\delta_{N_+^i}^2 + \delta_{N_-^i}^2)}} \quad \alpha = \frac{\sum N_+^i}{\sum N_-^i}$$

Global asymmetry

- S_{CP}^i follows standard normal distribution if no CPV

$$\chi^2 = \sum (S_{CP}^i)^2 \quad \text{exclude CP conservation if } p < 3 \times 10^{-7} \text{ (} n_{\text{dof}} = n_{\text{bins}}(21) - 1 \text{)}$$

- Validation with CF decays $D_S^+ \rightarrow K^- K^+ \pi^+$ and $D^+ \rightarrow K^- \pi^+ \pi^+$
- Measured p-values 13.3% (31.6%) for D_S^+ (D^+) decays



ϕ_K amplitudes

Adaptive binning with improved sensitivity to S-wave/P-wave interference effects

Direct CPV in $D_{(S)}^+ \rightarrow K^- K^+ K^+$

- Run 2 (5.6 fb^{-1}) data
- Binned method:

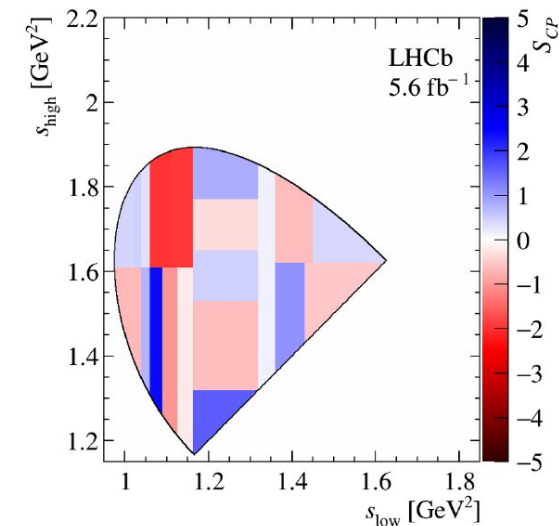
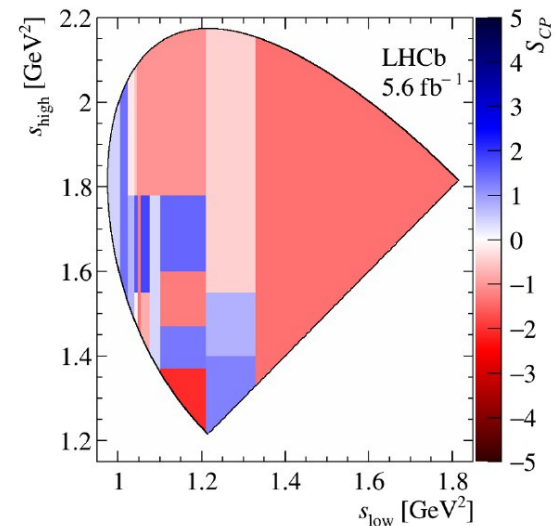
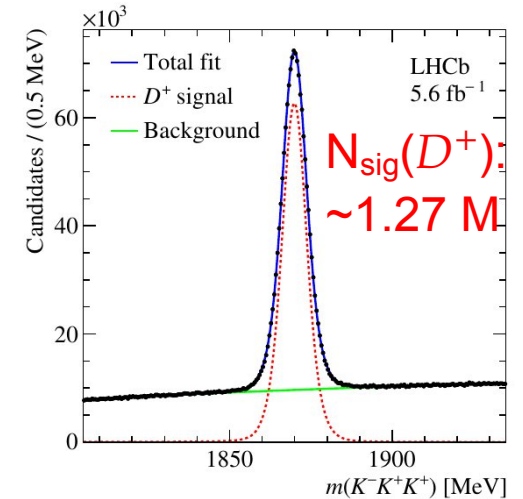
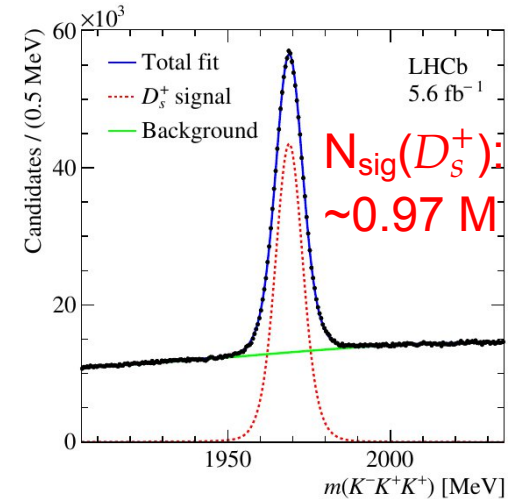
$$S_{CP}^i = \frac{N_+^i - \alpha N_-^i}{\sqrt{\alpha(\delta_{N_+^i}^2 + \delta_{N_-^i}^2)}} \quad \alpha = \frac{\sum N_+^i}{\sum N_-^i}$$

Global asymmetry

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$$\chi^2 = \sum (S_{CP}^i)^2 \quad \text{exclude CP conservation if } p < 3 \times 10^{-7} \text{ (} n_{\text{dof}} = n_{\text{bins}}(21) - 1 \text{)}$$

- Validation with CF decays $D_S^+ \rightarrow K^- K^+ \pi^+$ and $D^+ \rightarrow K^- \pi^+ \pi^+$
- Measured p-values 13.3% (31.6%) for D_S^+ (D^+) decays



Direct CPV in $D^0 \rightarrow \pi^+ \pi^- \pi^0$

- Dominated by $D^0 \rightarrow \rho^\pm \pi^\mp$ amplitudes
 - Could be related to recent evidence of CPV in $D^0 \rightarrow \pi^+ \pi^-$
- Run 2 (6 fb^{-1}) data with D^0 from D^{*+} and tagged by π_s^+
- Unbinned energy test method by comparing weighted distance between pairs in phase space:

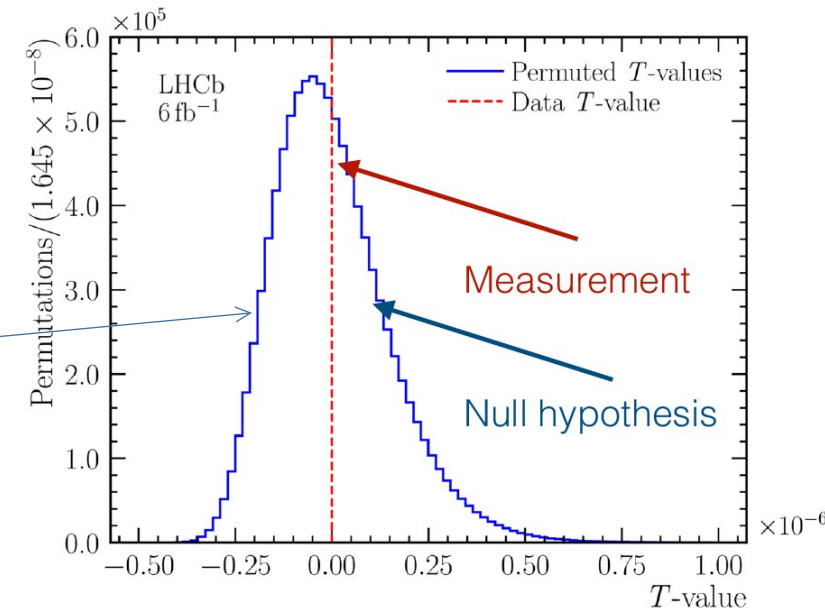
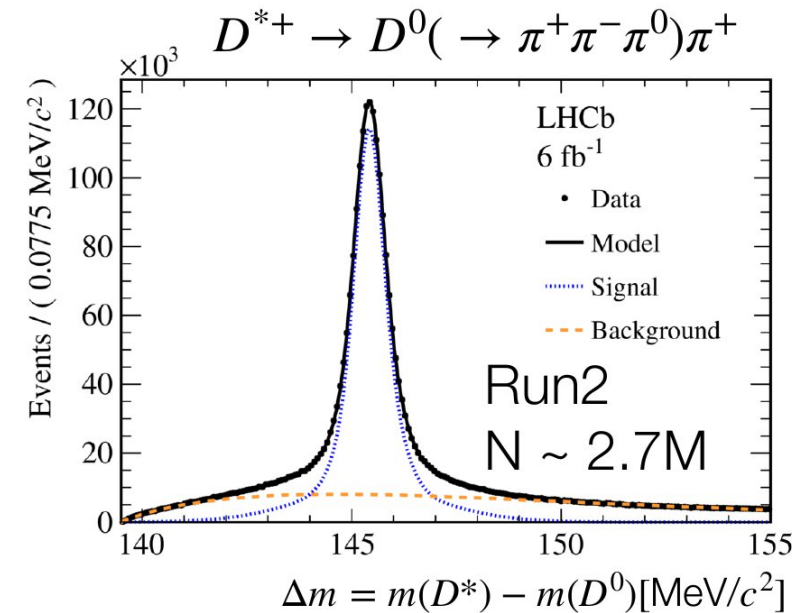
$$T = \sum_{i,j>i}^n \frac{\Psi_{ij}}{2n(n-1)} + \sum_{i,j>i}^{\bar{n}} \frac{\Psi_{ij}}{2\bar{n}(\bar{n}-1)} - \sum_{i,j}^{\bar{n}} \frac{\Psi_{ij}}{n\bar{n}}$$

Average distance candidates same flavour Average distance candidates opposite flavour

$$\Psi_{ij} = e^{-d_{ij}^2/2\delta^2}$$

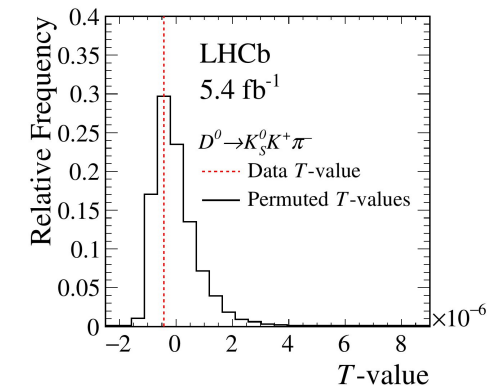
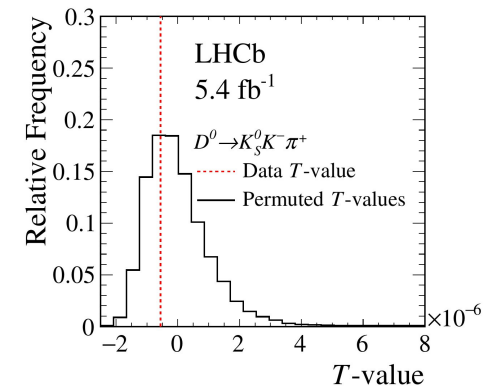
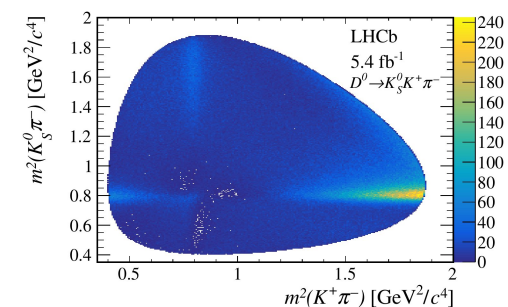
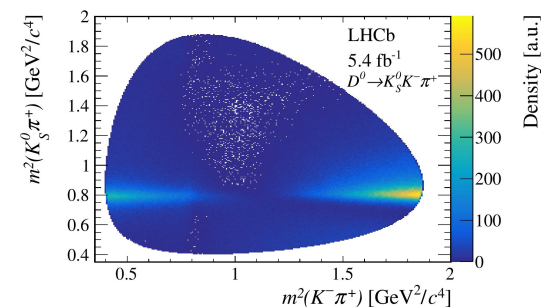
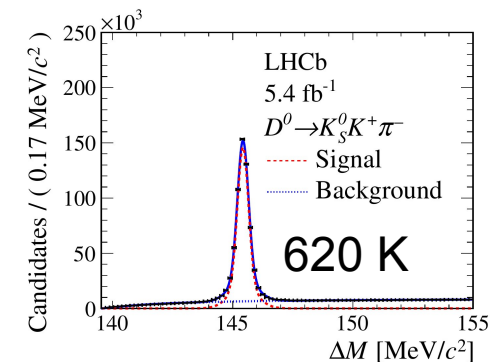
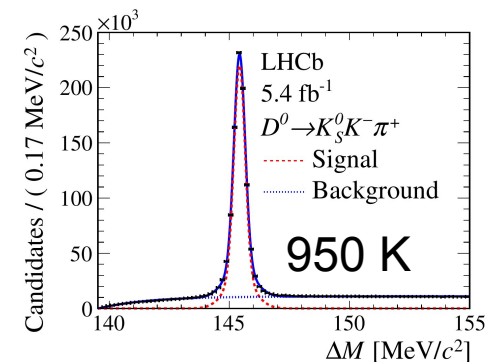
$$d_{ij} = [(\Delta s_{12})_{ij}^2 + (\Delta s_{13})_{ij}^2 + (\Delta s_{23})_{ij}^2]$$

- Null hypothesis from permutations of T-values with randomized tags
- Validation with CF decay $D^0 \rightarrow K^- \pi^+ \pi^0$
- Measured p-value 62%: **no hint for CPV!**



Direct CPV in $D^0 \rightarrow K_S^0 K^\pm \pi^\mp$

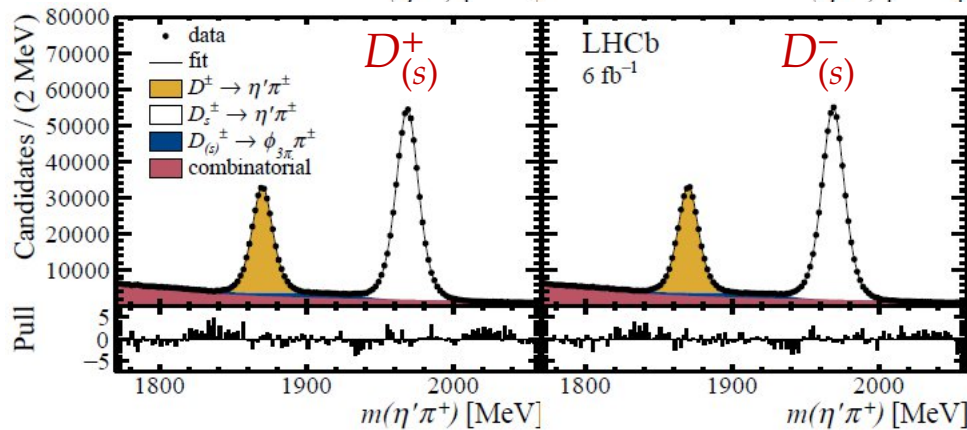
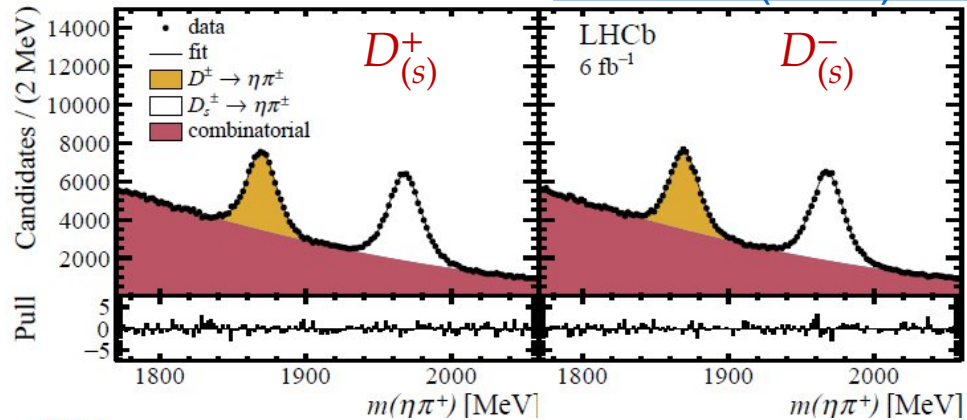
- Dominated by SCS amplitudes including $D^0 \rightarrow K^{*\mp} K^\pm / K^{*0} K_S^0$
- Run 2 (5.4 fb⁻¹) data with D⁰ from D^{*+} and tagged by π_S^+
- Unbinned energy test method as in $D^0 \rightarrow \pi^+ \pi^- \pi^0$
- Control modes: $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^- / K_S^0 \pi^+ \pi^-$
- Measured p-values 70% (66%) for $D^0 \rightarrow K_S^0 K^- \pi^+$ ($D^0 \rightarrow K_S^0 K^+ \pi^+$): **no hint for CPV!**



Hadronic decays with π^0/η

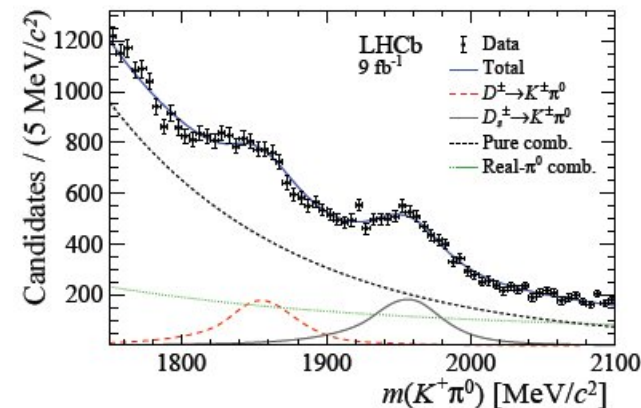
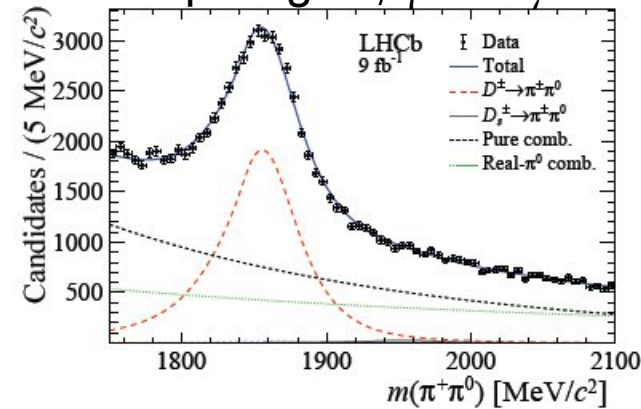
No CPV found
Almost all are world's best!

Requiring $\eta^{(\prime)} \rightarrow \pi\pi\gamma$ [JHEP 04 \(2023\) 081](#)

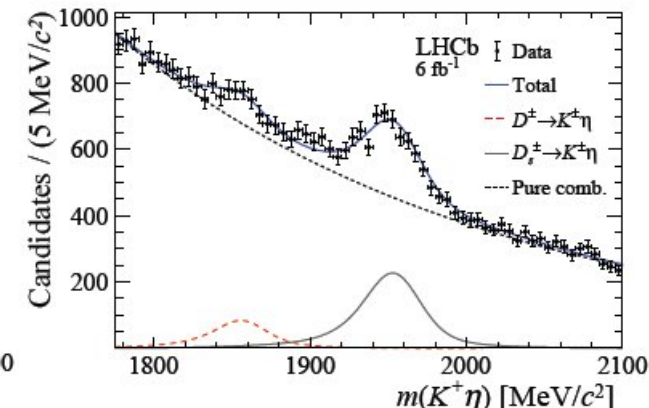
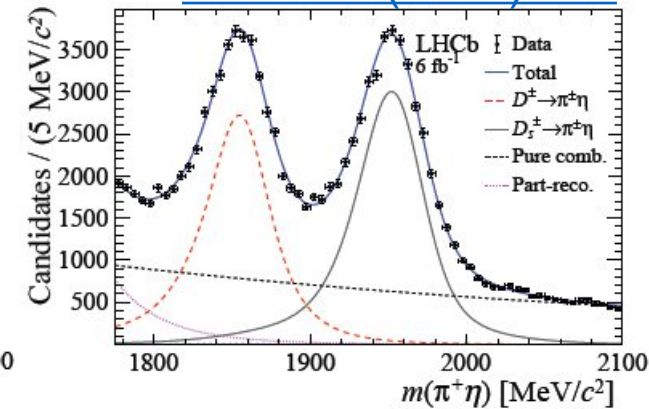


Measurement of CP asymmetries
in $D_{(s)}^+ \rightarrow \eta\pi^+$ and $D_{(s)}^+ \rightarrow \eta'\pi^+$

Requiring $\pi^0/\eta \rightarrow ee\gamma$



[JHEP 06 \(2021\) 019](#)



Search for CP violation in
 $D_{(s)}^+ \rightarrow h^+\pi^0$ and $D_{(s)}^+ \rightarrow h^+\eta$ decays

Overview of rare charm decays @ LHCb

branching ratios, especially regions away from the resonances

- search for $D^0 \rightarrow \mu^+ \mu^-$ [PLB 725 15-24 (2013)] [PRL 131 (2023) 041804]
- search for $D^{+(s)} \rightarrow h^+ l^+ l^-$ [PLB 724 203-212 (2013)] [JHEP 06 44 (2021)]
- search for $\Lambda_c^+ \rightarrow p \mu^+ \mu^-$ [PRD 97 091101 (2018)]
- search for $D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$ [PLB 728 234-243 (2014)]
- observation of $D^0 \rightarrow h^+ h^{(\prime)-} V(\mu^+ \mu^-)$ [PLB 757 558-567 (2016)], [PRL 119, 181805 (2017)]

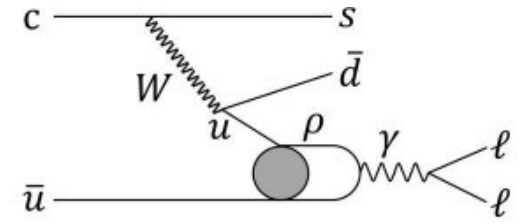
null tests based on (approximate) symmetries

- lepton-flavor/number-violation
 - search for $D^0 \rightarrow \mu^+ e^-$ [PLB 754 167 (2016)]
 - search for $D^{+(s)} \rightarrow h^+ l^+ l^{(\prime)+}$, $D^{+(s)} \rightarrow h^+ \mu^\pm e^\mp$ [JHEP 06 44 (2021)]
- angular observables and CP asymmetries
 - angular analysis and search for CPV in $D^0 \rightarrow h^+ h^- \mu^+ \mu^-$ [PRL 121 091801 (2018)], [LHCb-PAPER-2021-035] [PRL 128 (2022) 221801]

$D^0 \rightarrow K \pi^+ V(\mu^+ \mu^-)$
 $D^0 \rightarrow \pi^+ \pi^- V(\mu^+ \mu^-)$
 $D^0 \rightarrow K^+ K^- V(\mu^+ \mu^-)$

VMD

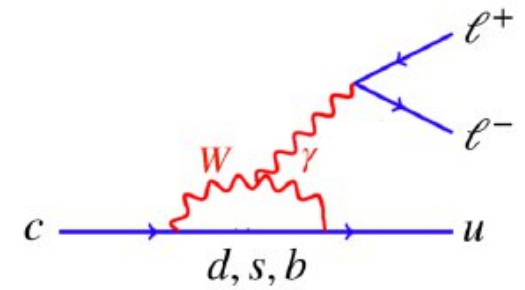
10^{-6}
 10^{-8}



$D^{+(s)} \rightarrow h^+ \mu^+ \mu^-$
 $\Lambda_c^+ \rightarrow p \mu^+ \mu^-$
 $D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$

FCNC

10^{-9}
 10^{-12}



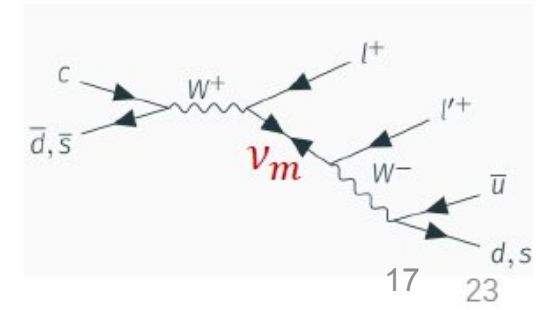
$D^0 \rightarrow \mu^\pm \mu^\pm$

10^{-12}

$D^{+(s)} \rightarrow h^+ \mu^+ \mu^+$
 $D^0 \rightarrow e^\pm \mu^\mp$

LFV, LNV, BNV

10^{-15}
 0



Search for $D^0 \rightarrow \mu^+ \mu^-$

- FCNC & helicity suppression

- Predictions: $\mathcal{B}^{s.d.}(D^0 \rightarrow \mu^+ \mu^-) \sim 10^{-18}$
 $\mathcal{B}^{(\gamma)}(D^0 \rightarrow \mu^+ \mu^-) < 2.3 \times 10^{-11}$

- Full Run1+2 analysis (9 fb⁻¹), D^0 from prompt $D^{*+} \rightarrow D^0 \pi_{tag}^+$

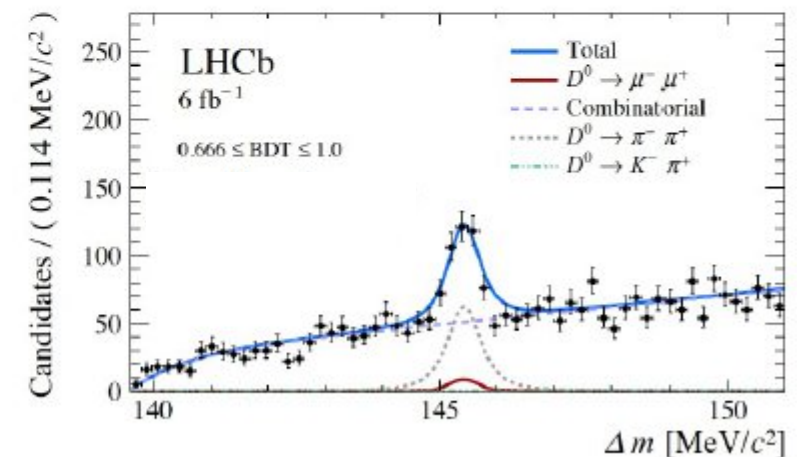
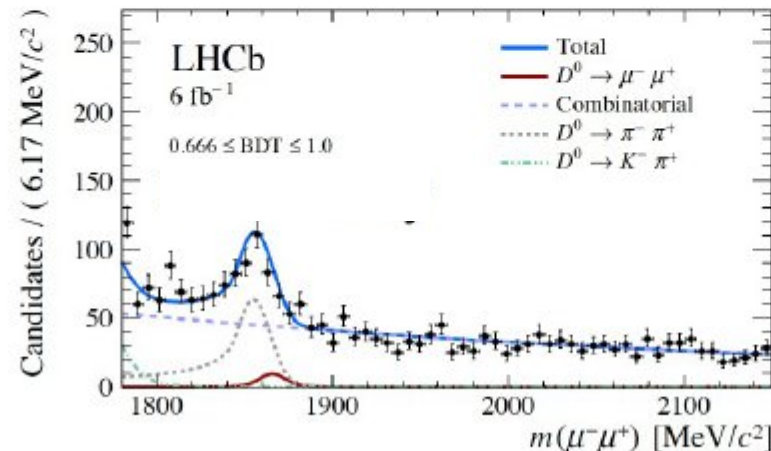
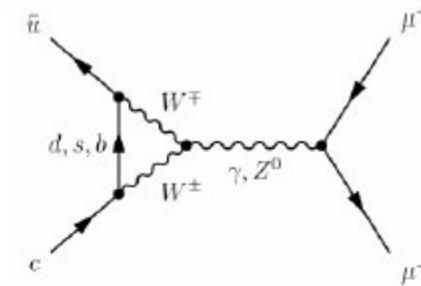
- Normalization channel: $\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) = \alpha N_{D^0 \rightarrow \mu^+ \mu^-}$, $\alpha \sim \frac{\mathcal{B}(D^0 \rightarrow h^- \pi^+) \epsilon_{D^0 \rightarrow h^- \pi^+}}{N_{D^0 \rightarrow h^- \pi^+} \epsilon_{D^0 \rightarrow \mu^+ \mu^-}} \sim 2 \times 10^{-11}$

- 2D simultaneous fits in
3 BDT bins per run:

Peaking mostly from
 π/μ misID

- Final result:

$$\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) < 2.9(3.3) \times 10^{-9} \text{ at } 90(95)\% \text{ C.L.}$$



Improvement of more a factor of two!

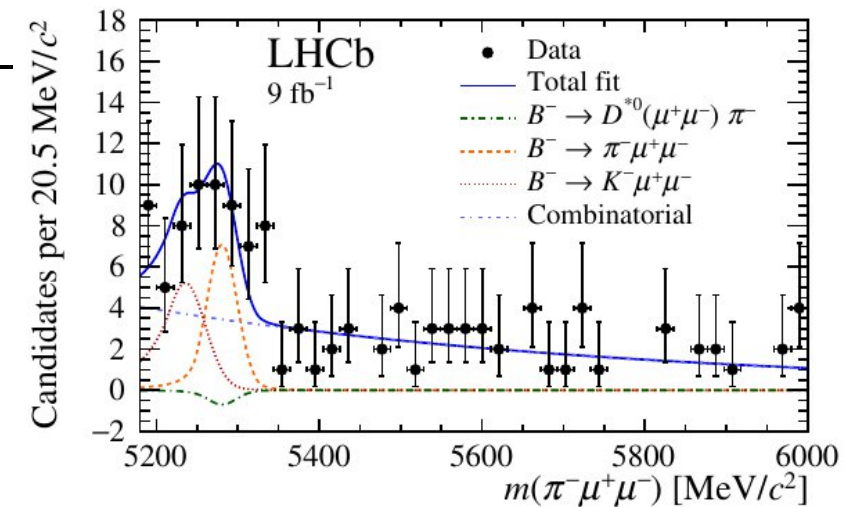
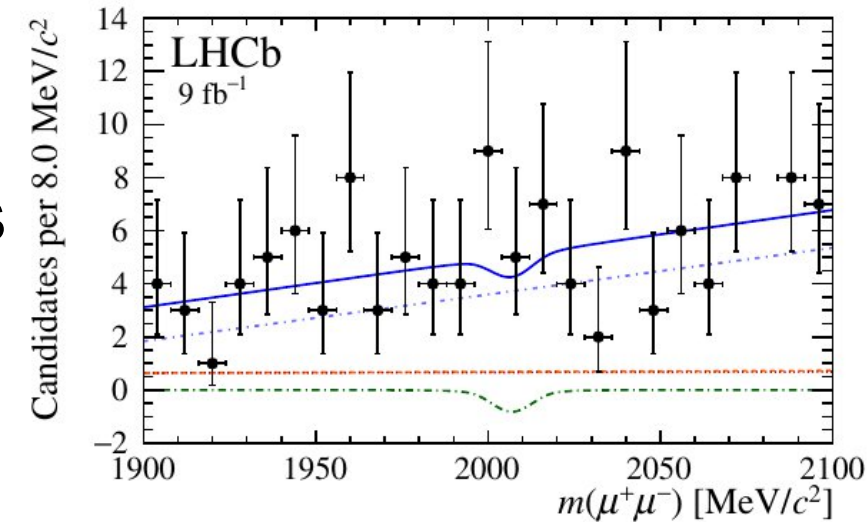
Search for $D^{*0} \rightarrow \mu^+ \mu^-$ in B decay

- Leptonic D^* decays offer a complementary approach to constraining Wilson coefficients
- Highly suppressed in SM: $BF \sim 10^{-18}$
- Search in the decay chain of $B^- \rightarrow D^{*0}(\rightarrow \mu^+ \mu^-)\pi^-$
- Normalization channel: $B^- \rightarrow J/\psi(\rightarrow \mu^+ \mu^-)K^-$
- First search:

$$\frac{\epsilon_{J/\psi K^-}}{N_{J/\psi K^-}} = 1.21 \pm 0.03$$

$$N_{J/\psi K^-} = (2316 \pm 8) \times 10^3$$

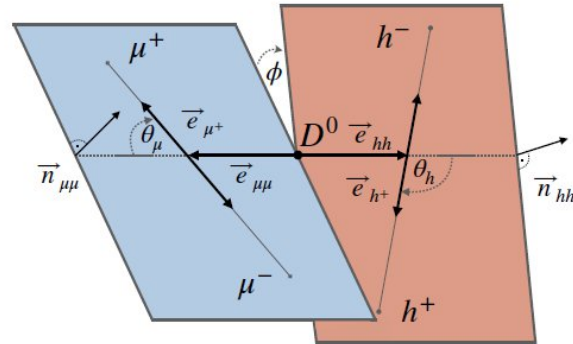
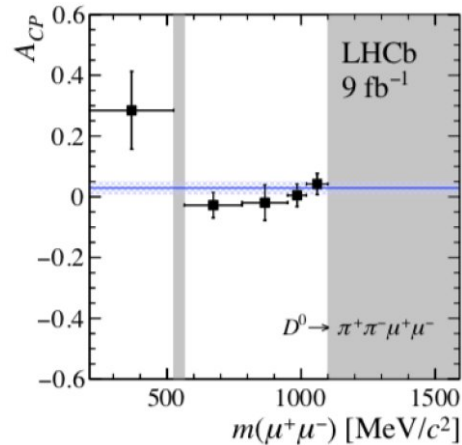
$$\mathcal{B}(D^{*0} \rightarrow \mu^+ \mu^-) < 2.6 \times 10^{-8} \text{ at } 90\% \text{ CL}$$



CPV & angular analysis of $D^0 \rightarrow hh\mu^+\mu^-$

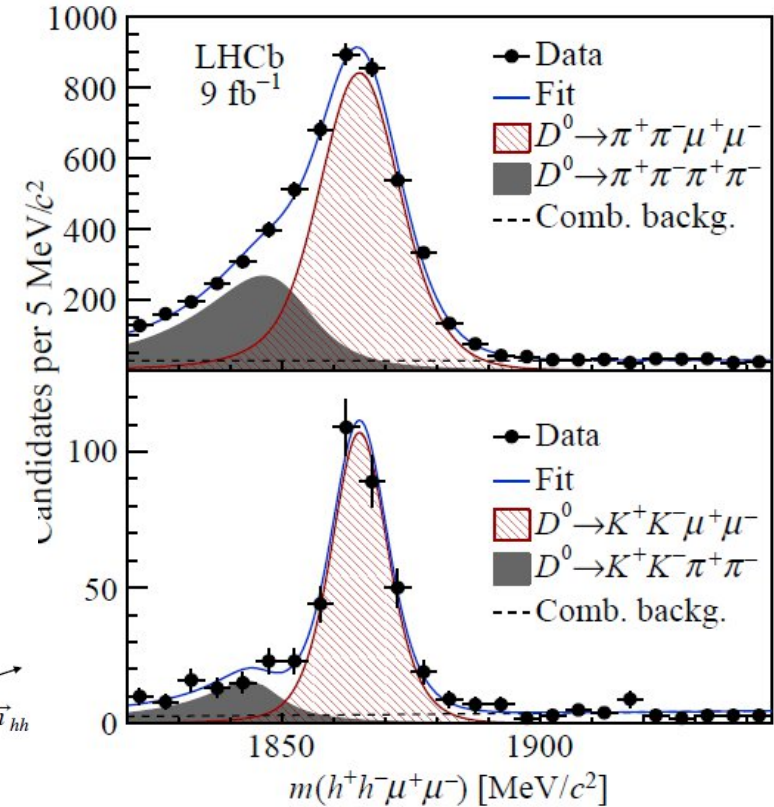
- Rarest charm meson decays observed, dominated by resonant contributions
- First full angular analysis with 9 fb^{-1} data
- D^0 selected from flavor specific $D^{*+} \rightarrow D^0\pi^+$

All results consistent with SM
No CPV found



$$p^2 = m^2(h^+h^-)$$

$$q^2 = m^2(\mu^+\mu^-)$$



$$N(D^0 \rightarrow \pi^+\pi^-\mu^+\mu^-) \sim 3500$$

$$N(D^0 \rightarrow K^+K^-\mu^+\mu^-) \sim 300$$

$$A_{CP} = \frac{\Gamma(D^0 \rightarrow h^+h^-\mu^+\mu^-) - \Gamma(\bar{D}^0 \rightarrow h^+h^-\mu^+\mu^-)}{\Gamma(D^0 \rightarrow h^+h^-\mu^+\mu^-) + \Gamma(\bar{D}^0 \rightarrow h^+h^-\mu^+\mu^-)}$$

Run3 and beyond...



Rare decays

Mixing & CPV

Observable	Current LHCb (up to 9 fb ⁻¹)	Upgrade I (23 fb ⁻¹)	Upgrade II (50 fb ⁻¹)	Upgrade II (300 fb ⁻¹)
Charm				
$\Delta A_{CP} (D^0 \rightarrow K^+ K^-, \pi^+ \pi^-)$	29×10^{-5} [5]	17×10^{-5}	—	3.0×10^{-5}
$A_{\Gamma} (D^0 \rightarrow K^+ K^-, \pi^+ \pi^-)$	13×10^{-5} [38]	4.3×10^{-5}	—	1.0×10^{-5}
$\Delta x (D^0 \rightarrow K_s^0 \pi^+ \pi^-)$	18×10^{-5} [37]	6.3×10^{-5}	4.1×10^{-5}	1.6×10^{-5}

Reaching for **sub-10⁻⁴** precision

	Mode	Upgrade (50 fb ⁻¹)	Upgrade II (300 fb ⁻¹)
Limits on BFs	$D^0 \rightarrow \mu^+ \mu^-$	4.2×10^{-10}	1.3×10^{-10}
	$D^+ \rightarrow \pi^+ \mu^+ \mu^-$	10^{-8}	3×10^{-9}
	$D_s^+ \rightarrow K^+ \mu^+ \mu^-$	10^{-8}	3×10^{-9}
	$\Lambda_c^+ \rightarrow p \mu^+ \mu^-$	1.1×10^{-8}	4.4×10^{-9}
	$D^0 \rightarrow e \mu$	10^{-9}	4.1×10^{-9}
Stat. precision on asymmetries	$D^+ \rightarrow \pi^+ \mu^+ \mu^-$	0.2%	0.08%
	$D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$	1%	0.4%
	$D^0 \rightarrow \pi^+ K^- \mu^+ \mu^-$	0.3%	0.13%
	$D^0 \rightarrow K^+ \pi^- \mu^+ \mu^-$	12%	5%
	$D^0 \rightarrow K^+ K^- \mu^+ \mu^-$	4%	1.7%

A new detector & no hw trigger: expecting benefits to A_{CP} measurements in hadronic channels, esp. for those with at least one K_S

Summary

- LHCb is in fact a charm factory and has the world's largest sample of charm decays
- High statistics and superb detector performance allow for high precision measurements on charm CP, rare decays, etc.
 - Observations of charm CPV, difference in D^0 mass eigenstates, etc.
- Still more charm results in the pipeline with full Run1+2 data, stay tuned!
 - For example, semileptonic D^0 decays, dielectron channels, radiative charm decays, charm baryons, ...
- Run3 for LHCb has started, expecting fruitful years to come...
- Synergy across different experiments on charm physics: BESIII, BELLE(II), future STCF, ...

Backup Slides