

CP violation in charmed baryon decays with $SU(3)$ flavor symmetry

arXiv : 2310.05491, 2312.xxxxx

全国第二十二届重味物理和CP破坏研讨会

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Dec 17, 2023



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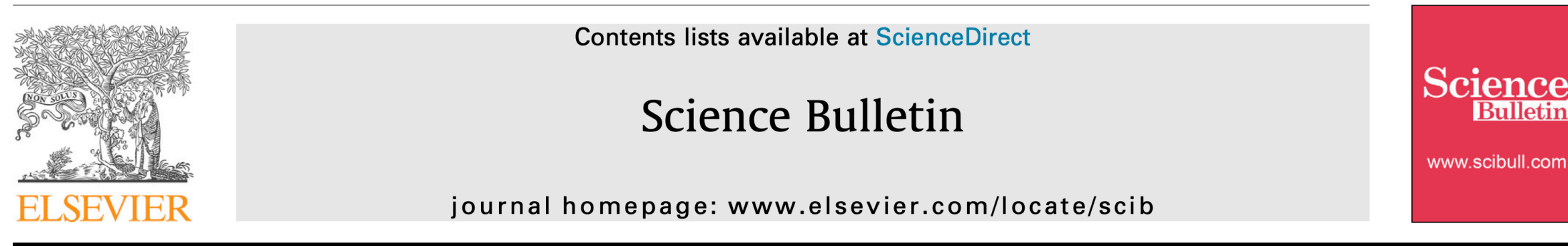
Charmed baryons decays

BESIII : $e^+e^- \rightarrow \Lambda_c^+ \Lambda_c^-$ at 4.6 GeV, providing clean background

Observation of the Singly Cabibbo Suppressed Decay $\Lambda_c^+ \rightarrow n\pi^+$

M. Ablikim *et al.* (BESIII Collaboration)
Phys. Rev. Lett. **128**, 142001 – Published 4 April 2022

Belle : e^+e^- collisions at $\Upsilon(4S)$ or $\Upsilon(5S)$



Article
 Search for CP violation and measurement of branching fractions and decay asymmetry parameters for $\Lambda_c^+ \rightarrow \Lambda h^+$ and $\Lambda_c^+ \rightarrow \Sigma^0 h^+$ ($h = K, \pi$)
 The Belle Collaboration ¹

LHCb : pp collisions, largest charmed hadron samples

Observation of the Doubly Charmed Baryon Ξ_{cc}^+

R. Aaij *et al.* (LHCb Collaboration)
Phys. Rev. Lett. **119**, 112001 – Published 11 September 2017

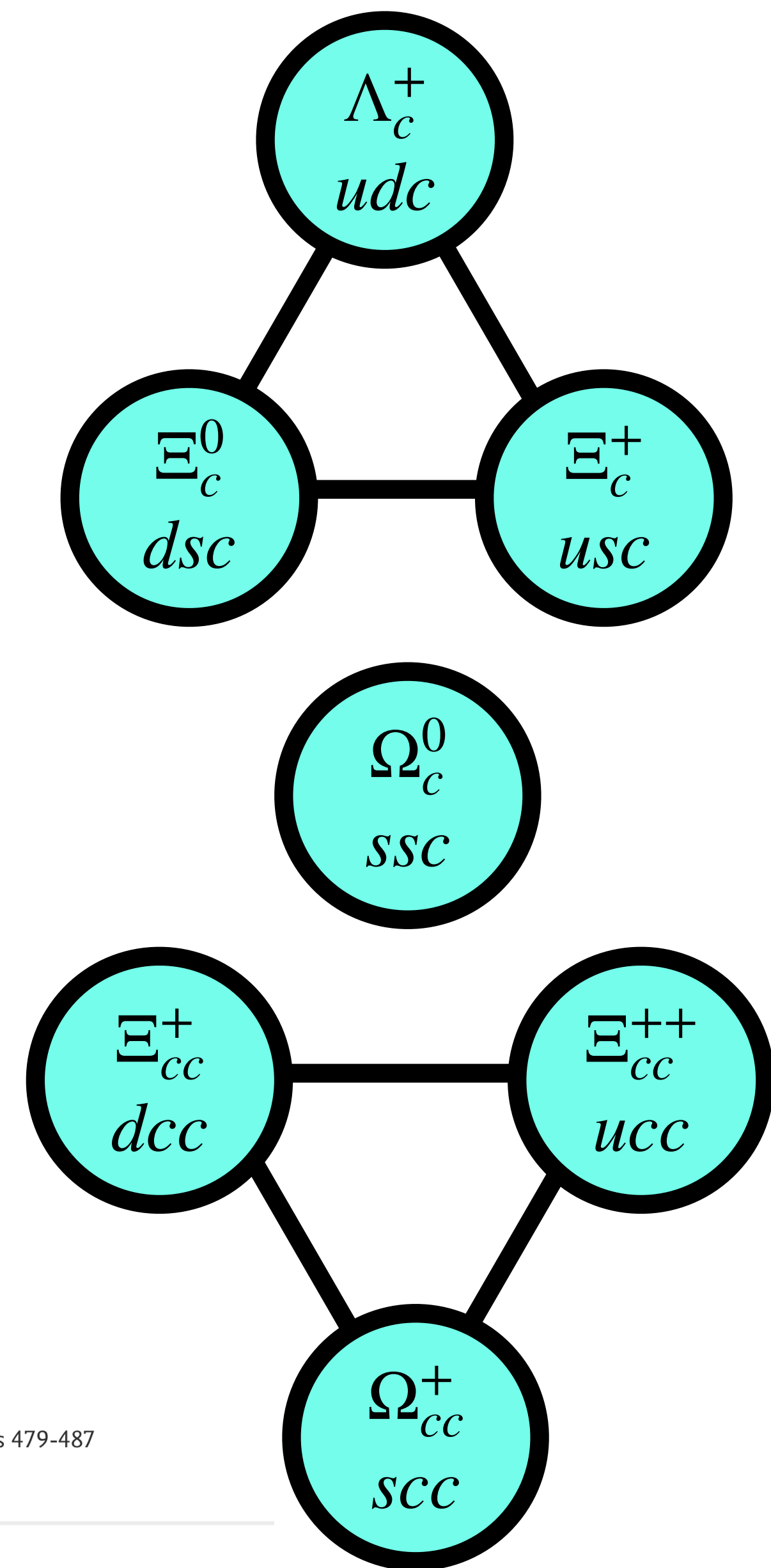
PhysiCS See Viewpoint: [A Doubly Charming Particle](#)



Science Bulletin
 Volume 67, Issue 5, 15 March 2022, Pages 479-487

Article
 Measurement of the lifetimes of promptly produced Ω_c^0 and Ξ_c^0 baryons

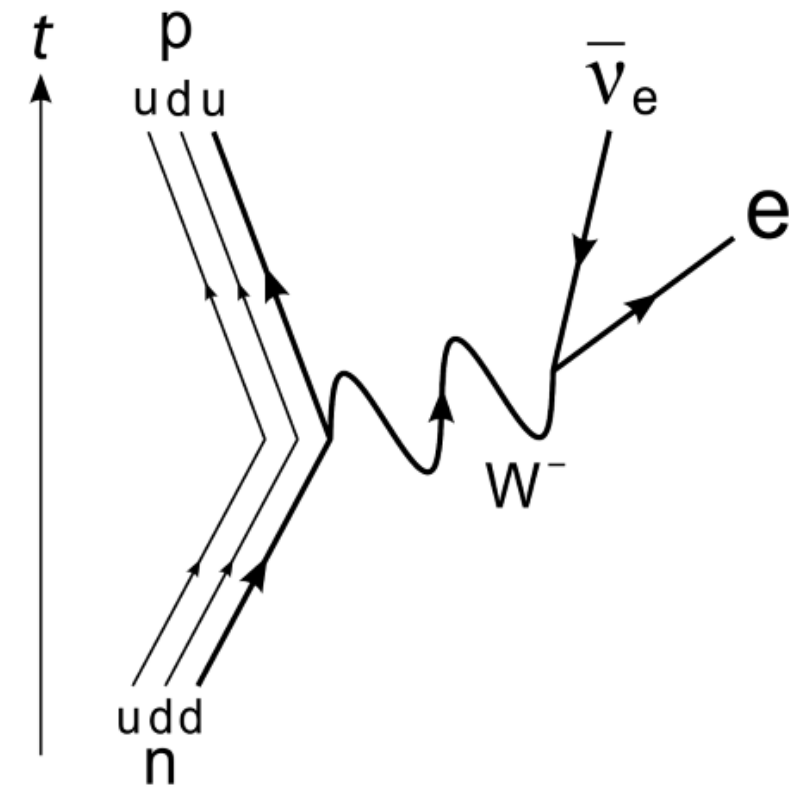
LHCb Collaboration ¹



- CP violation in charm - overview

$$V_{CKM} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

$$V_{CKM} V_{CKM}^\dagger = 1$$

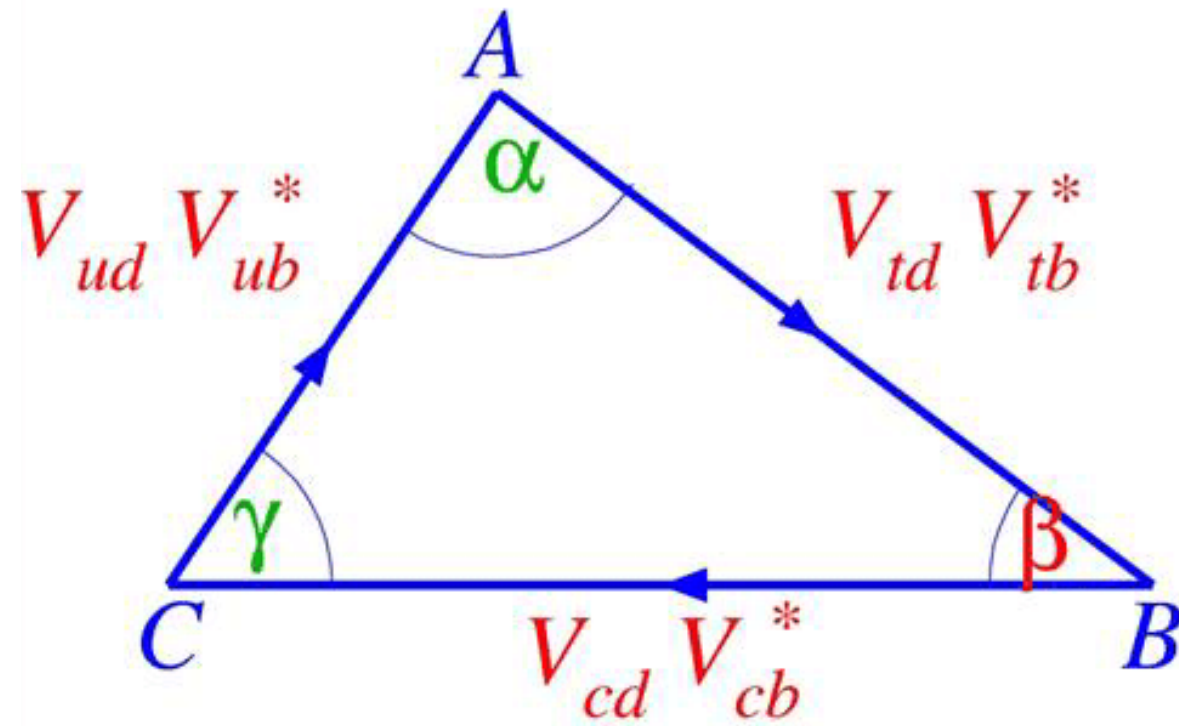


$V_{CKM} \neq V_{CKM}^*$ under the phase rotations of $(U_q(1))^6 \rightarrow$ CP violation.

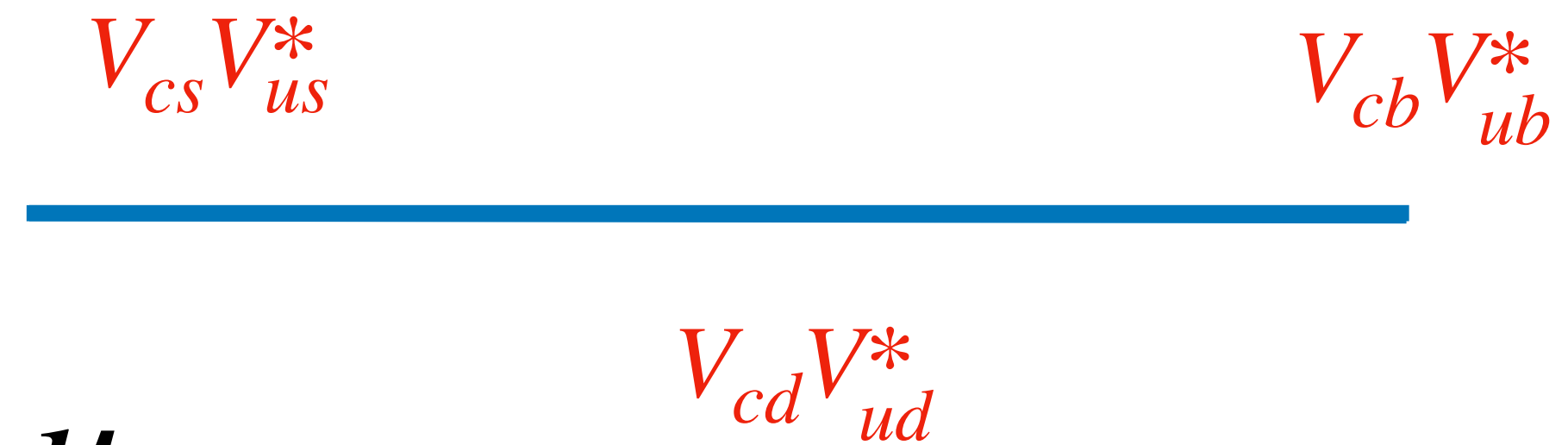
$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

$$V_{ud} V_{cd}^* + V_{us} V_{cs}^* + V_{ub} V_{cb}^* = 0$$

$b \rightarrow d$



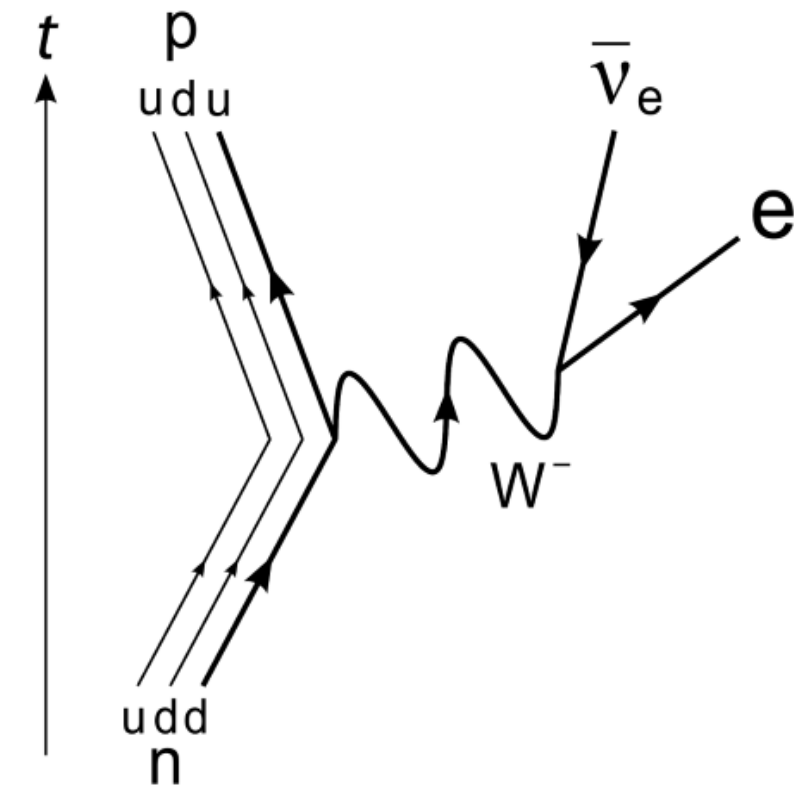
$c \rightarrow u$



- CP violation in charm - overview

$$V_{CKM} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

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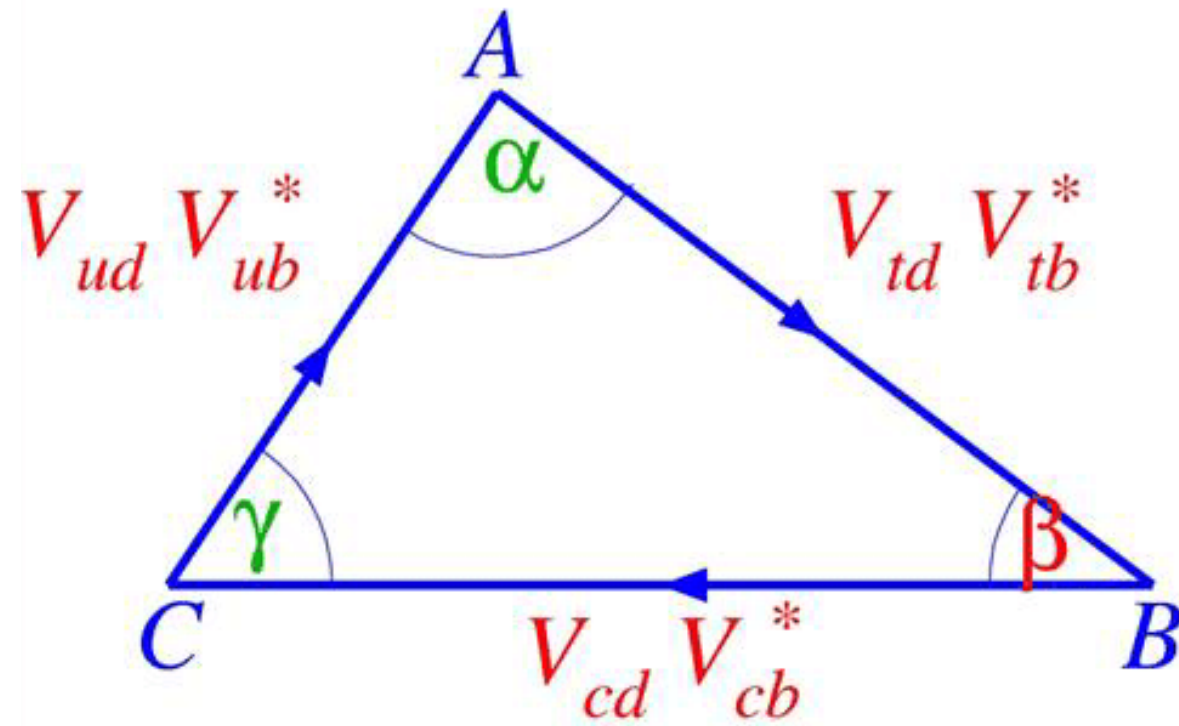


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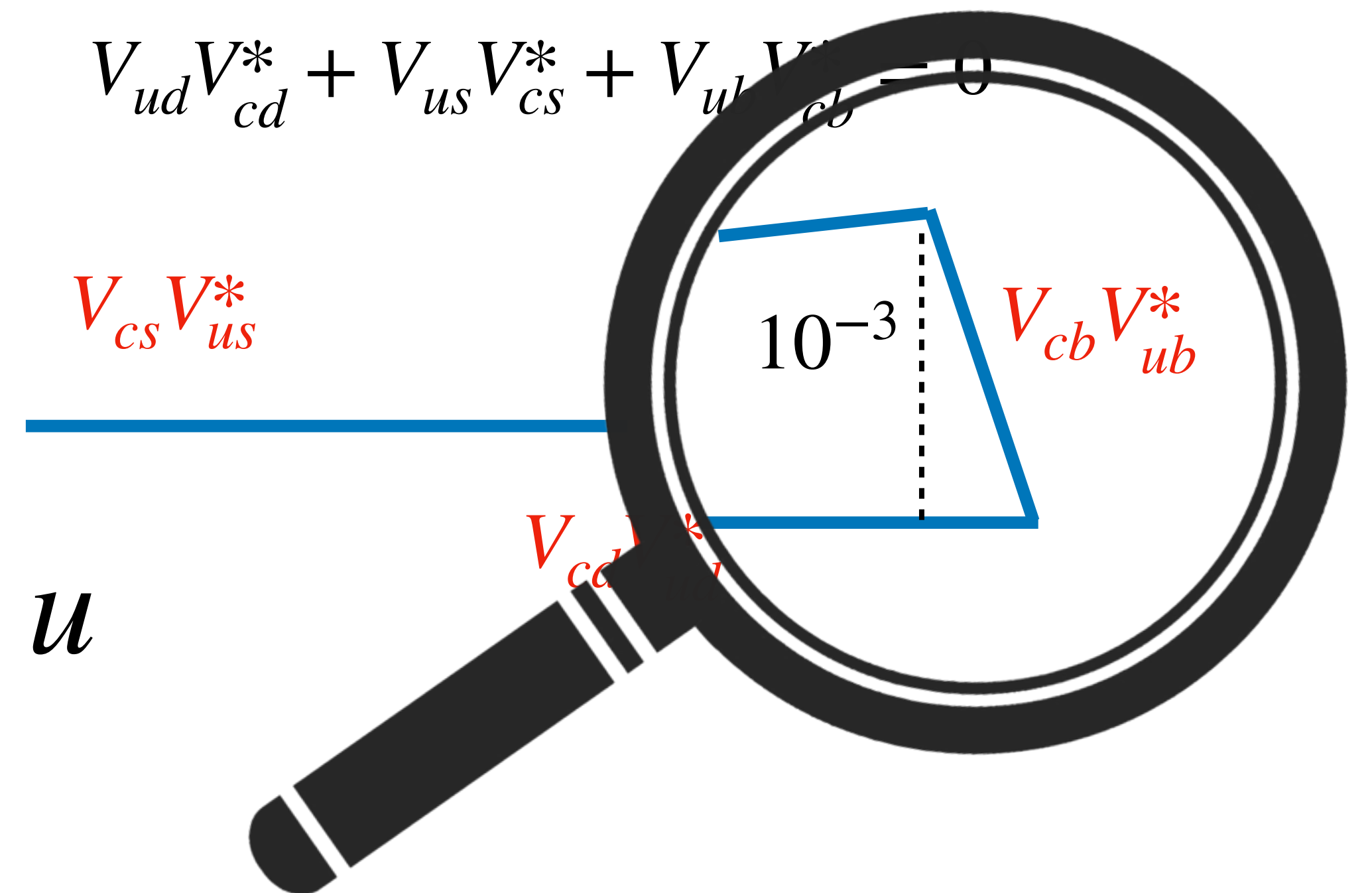
$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

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$b \rightarrow d$



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SU(3) flavor analysis

$$\lambda_{d,s} \text{ Tree} + \underbrace{\lambda_b \text{ Penguin}}_{V_{cd}V_{ud}^*}$$

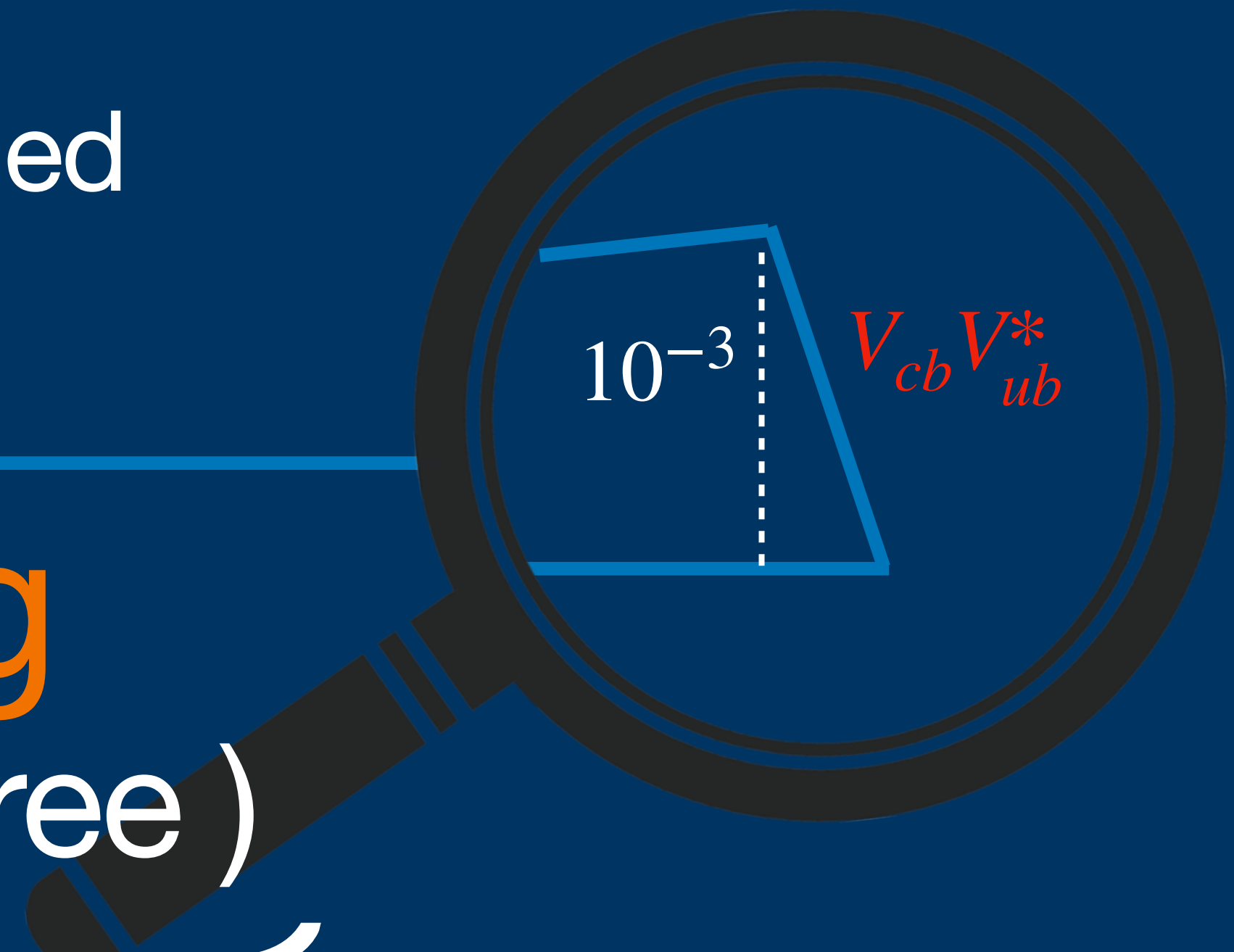
Insensitive to CP-even quantities & undetermined

$$\lambda_q = V_{cq}^* V_{uq}$$

Pole model + Rescattering

$$\lambda_{d,s} \text{ Tree} + \underbrace{\lambda_b \text{ Tree} \times (\text{Penguin} / \text{Tree})}_{V_{cb}V_{ub}^*}$$

Determined by the PM + rescattering



- SU(3) flavor analysis — Tree**

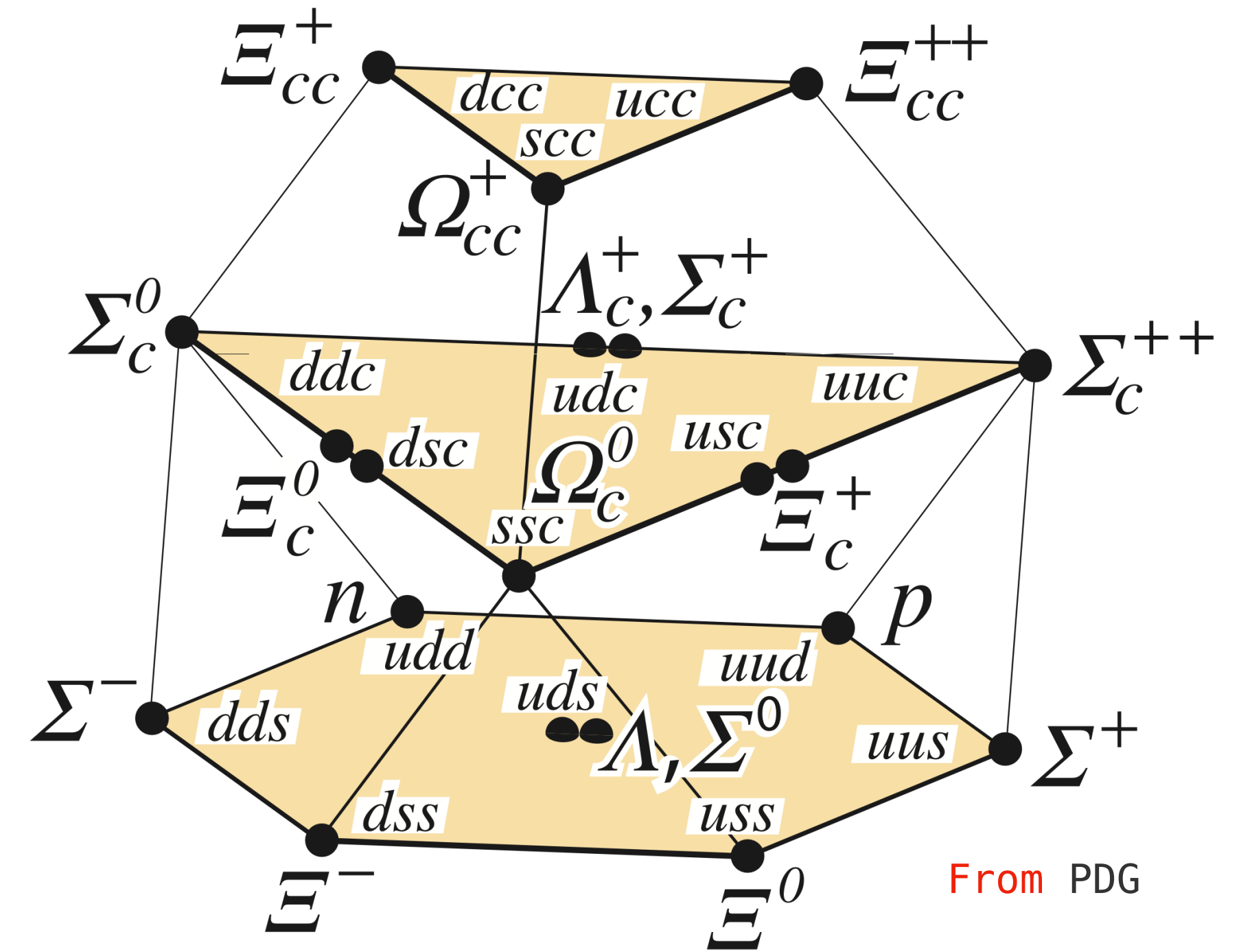
$$\mathcal{M} = \langle \mathbf{BM}; t \rightarrow \infty | \mathcal{H}_{\text{eff}} | \mathbf{B}_c \rangle = i\bar{u} (F - G\gamma_5) u_c$$

SU(3) flavor representations :

$$\mathbf{B}_c = (\Xi_c^0, -\Xi_c^+, \Lambda_c^+),$$

$$\mathbf{B}_n = \begin{pmatrix} \frac{1}{\sqrt{6}}\Lambda + \frac{1}{\sqrt{2}}\Sigma^0 & \Sigma^+ & p \\ \Sigma^- & \frac{1}{\sqrt{6}}\Lambda - \frac{1}{\sqrt{2}}\Sigma^0 & n \\ \Xi^- & \Xi^0 & -\sqrt{\frac{2}{3}}\Lambda \end{pmatrix},$$

$$M = \begin{pmatrix} \frac{1}{\sqrt{2}}(\pi^0 + c_\phi\eta + s_\phi\eta') & \pi^+ & K^+ \\ \pi^- & \frac{1}{\sqrt{2}}(-\pi^0 + c_\phi\eta + s_\phi\eta') & K^0 \\ K^- & \bar{K}^0 & -s_\phi\eta + c_\phi\eta' \end{pmatrix},$$



- **SU(3) flavor analysis — Tree**

$$\mathcal{H}_{eff} = \frac{G_F}{\sqrt{2}} \left[\sum_{qq'} V_{qc}^* V_{q'u} \left(C_+ O_+^{qq'} + C_- O_-^{qq'} \right) - \lambda_b \sum_{i=3\sim 6} C_i O_i \right] \quad \lambda_q = V_{cq}^* V_{uq}$$

$$O_{\pm}^{qq'} = (\bar{u}q')_{V-A} (\bar{q}c)_{V-A} \pm (\bar{q}q')_{V-A} (\bar{u}c)_{V-A} \quad \underbrace{\mathbf{3} \otimes \mathbf{3} \otimes \bar{\mathbf{3}}}_{\mathcal{H}_{eff}} = \underbrace{(\mathbf{15} \oplus \mathbf{3}_+)}_{O_+} \oplus \underbrace{(\bar{\mathbf{6}} \oplus \mathbf{3}_-)}_{O_-}$$

$$\mathcal{H}(\bar{\mathbf{6}}) = \begin{pmatrix} 0 & 0 & 0 \\ 0 & V_{cs}^* V_{ud} & -\lambda_s - \frac{\lambda_b}{2} \\ 0 & -\lambda_s - \frac{\lambda_b}{2} & V_{cd}^* V_{us} \end{pmatrix}$$

$$\mathcal{H}(\mathbf{3}_-) = \lambda_b \left(-\frac{1}{2}, 0, 0 \right), \quad \mathcal{H}(\mathbf{3}_+) = \lambda_b \left(-\frac{1}{4}, 0, 0 \right),$$

$$\mathcal{H}(\mathbf{15})_{ij}^{ij} = \left(\begin{pmatrix} \frac{\lambda_b}{2} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}_{ij}, \begin{pmatrix} 0 & -\lambda_s - \frac{3\lambda_b}{4} & V_{cs}^* V_{ud} \\ -\lambda_s - \frac{3\lambda_b}{4} & 0 & 0 \\ V_{cs}^* V_{ud} & 0 & 0 \end{pmatrix}_{ij}, \begin{pmatrix} 0 & V_{cd}^* V_{us} & \lambda_s + \frac{\lambda_b}{4} \\ V_{cd}^* V_{us} & 0 & 0 \\ \lambda_s + \frac{\lambda_b}{4} & 0 & 0 \end{pmatrix}_{ij} \right)_k$$

$$\lambda_d + \lambda_s + \lambda_b = 0$$

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$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} \left[\sum_{qq'} V_{qc}^* V_{q'u} \left(C_+ O_+^{qq'} + C_- O_-^{qq'} \right) - \lambda_b \sum_{i=3\sim 6} C_i O_i \right] \quad \langle \mathbf{BP} | \mathcal{H}_{\text{eff}} | \mathbf{B}_c \rangle = i\bar{u} (F - G\gamma_5) u_c$$

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For CP-even quantities it is safe to take $\lambda_b \rightarrow 0$

$$\begin{aligned} \mathcal{M} = & a_{15} \times (T_{c\bar{3}})_i (H_{\bar{15}})_j^{\{ik\}} (\bar{T}_8)_k^j P_l^i + b_{15} \times (T_{c\bar{3}})_i (H_{\bar{15}})_j^{\{ik\}} (\bar{T}_8)_k^l P_l^j + c_{15} \times (T_{c\bar{3}})_i (H_{\bar{15}})_j^{\{ik\}} (\bar{T}_8)_l^j P_k^l \\ & + d_{15} \times (T_{c\bar{3}})_i (H_{\bar{15}})_l^{\{jk\}} (\bar{T}_8)_j^l P_k^i + e_{15} \times (T_{c\bar{3}})_i (H_{\bar{15}})_l^{\{jk\}} (\bar{T}_8)_j^i P_k^l + a_6 \times (T_{c\bar{3}})^{[ik]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_k^j P_l^i \\ & + b_6 \times (T_{c\bar{3}})^{[ik]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_k^l P_l^j + c_6 \times (T_{c\bar{3}})^{[kl]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_l^j P_k^i + d_6 \times (T_{c\bar{3}})^{[ik]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_k^i P_l^j. \end{aligned}$$

To date, there are in total **30** data points but $9 \times 2(\text{S- \& P-waves}) \times 2(\text{complex}) - 1 = \mathbf{35}$

- **SU(3) flavor analysis — Tree**

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In the absence of final state interactions \rightarrow **18**

- **SU(3) flavor analysis — Tree**

(2019) 16 input, 10 parameters* (2023) 28 input, 18 parameters (2023) 28 input, 18 parameters

$$\alpha(\Lambda_c^+ \rightarrow \Xi^0 K^+) = \quad 0.94^{+0.06}_{-0.11} \quad 0.91^{+0.03}_{-0.04} \quad 0.955 \pm 0.018$$

First Measurement of the Decay Asymmetry of pure W-exchange Decay $\Lambda_c^+ \rightarrow \Xi^0 K^+$

(Dated: **September 8, 2023**)

Based on 4.4 fb^{-1} of e^+e^- annihilation data collected at the center-of-mass energies between 4.60 and 4.70 GeV with the BESIII detector at the BEPCII collider, the pure W -exchange decay $\Lambda_c^+ \rightarrow \Xi^0 K^+$ is studied with a full angular analysis. The corresponding decay asymmetry is measured for the first time to be $\alpha_{\Xi^0 K^+} = 0.01 \pm 0.16(\text{stat.}) \pm 0.03(\text{syst.})$. This result reflects the interference between the S - and P -wave amplitudes. The phase shift between S - and P -wave amplitudes is $\delta_p - \delta_s = -1.55 \pm 0.25(\text{stat.}) \pm 0.05(\text{syst.}) \text{ rad.}$

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(2019) 16 input,
10 parameters*

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- Free parameters: 18 \rightarrow 10

$$A_{(\mathbf{B}_c \rightarrow \mathbf{B}_n M)} = a_0 H(6)_{ij}(\mathbf{B}'_c)^{ik}(\mathbf{B}_n)_k^j(M)_l^l + a_1 H(6)_{ij}(\mathbf{B}'_c)^{ik}(\mathbf{B}_n)_k^l(M)_l^j + a_2 H(6)_{ij}(\mathbf{B}'_c)^{ik}(M)_k^l(\mathbf{B}_n)_l^j + a_3 H(6)_{ij}(\mathbf{B}_n)_k^i(M)_l^j(\mathbf{B}'_c)^{kl} + a'_0(\mathbf{B}_n)_j^i(M)_l^l H(\overline{15})_i^{jk}(\mathbf{B}_c)_k + a_4 H(\overline{15})_k^{li}(\mathbf{B}_c)_j(M)_i^j(\mathbf{B}_n)_l^k + a_5(\mathbf{B}_n)_j^i(M)_l^l H(\overline{15})_i^{jk}(\mathbf{B}_c)_k + a_6(\mathbf{B}_n)_j^i(M)_l^m H(\overline{15})_m^{li}(\mathbf{B}_c)_j + a_7(\mathbf{B}_n)_i^l(M)_j^i H(\overline{15})_l^{jk}(\mathbf{B}_c)_k,$$

PLB 794, 19(2019)

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+) = \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ K_S^0)$$

EXP(2022): $(4.7 \pm 1.0) \times 10^{-4}$ $(4.8 \pm 1.4) \times 10^{-4}$

BESIII PRD 106, no.5, 052003 (2022)

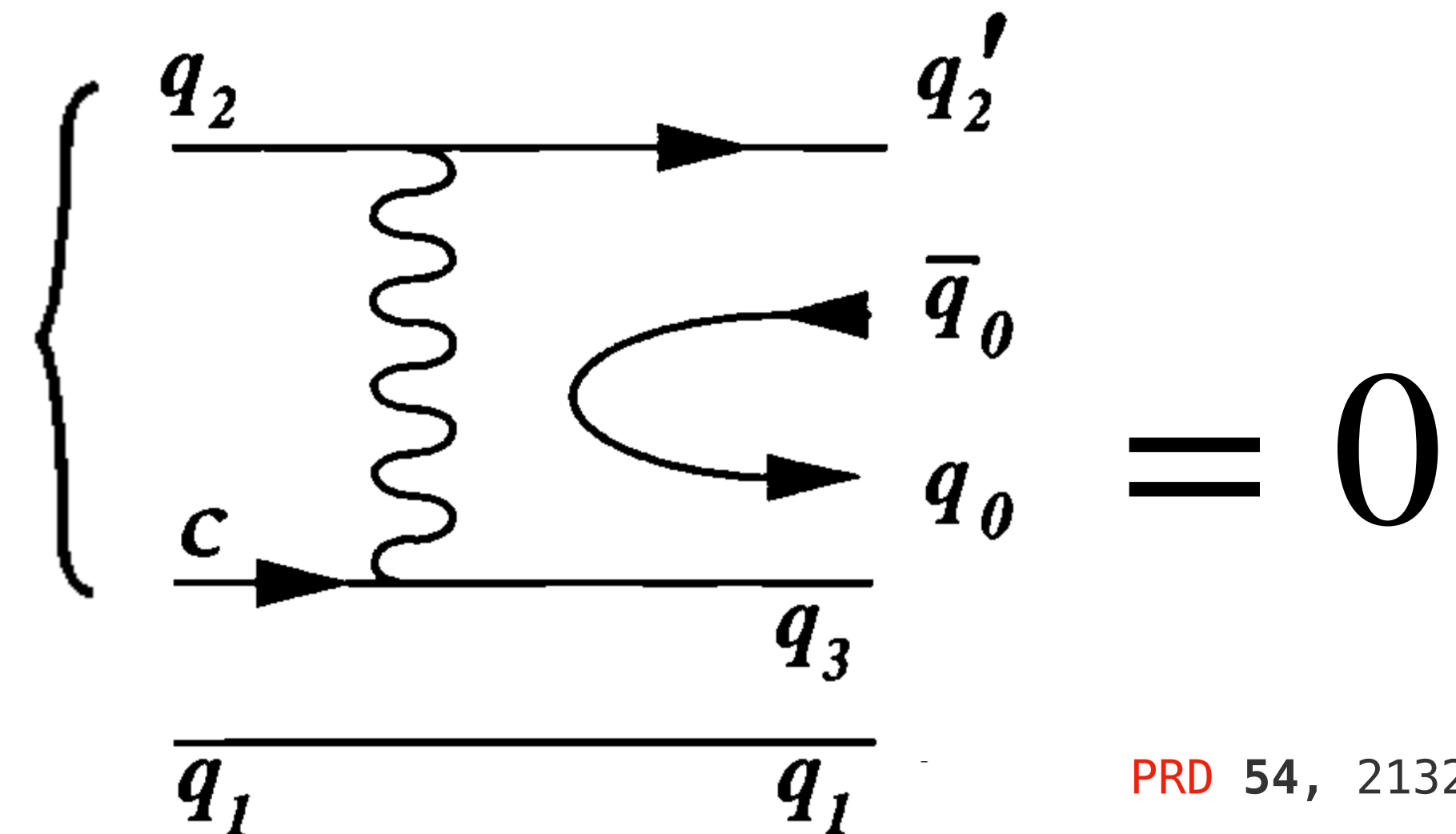
- The Körner-Pati-Woo theorem:

$$\langle q_a q_b q_c | O_+^{qq'} | \mathbf{B}_i \rangle = 0$$

Color symmetric

Color singlet

$$O_+^{qq'} = \frac{1}{2} \left[(\bar{u}q')_{V-A} (\bar{q}c)_{V-A} + (\bar{q}q')_{V-A} (\bar{u}c)_{V-A} \right],$$



PRD 54, 2132 (1996)

Chau, Cheng, Tseng

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Considering the Körner-Pati-Woo theorem: \rightarrow **10**

- **SU(3) flavor analysis — Tree**

(2023) 29 input, 19 parameters* (2023) 28 input, 18 parameters (2023) 28 input, 18 parameters

$$\alpha(\Lambda_c^+ \rightarrow \Xi^0 K^+) = \quad -0.15 \pm 0.14 \quad 0.91^{+0.03}_{-0.04} \quad 0.955 \pm 0.018$$

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Considering the Körner-Pati-Woo theorem: \rightarrow **19**

- **SU(3) flavor analysis — Tree**

$$\beta = \frac{2 \operatorname{Im}(S^*P)}{|S|^2 + |P|^2}$$

- **Sizable strong phases**

- **KPW + SU(3)**

$$\frac{\tau_{\Lambda_c^+}}{\tau_{\Xi_c^0}} \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+) = \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+) + 3\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda \pi^+) - \frac{1}{s_c^2} \mathcal{B}(\Lambda_c^+ \rightarrow n \pi^+)$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e) = (2.38 \pm 0.44) \%$$

×

LQCD, **CPC 46**, 011002 (2022)

$$\frac{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)}{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e)} = 1.37 \pm 0.08$$

Belle, **PRL 127** 121803 (2021)

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$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+) = (3.26 \pm 0.63) \%$$



Channels	$\mathcal{B}_{\text{exp}}(\%)$	α_{exp}	$\mathcal{B}(\%)$	α	β
$\Lambda_c^+ \rightarrow p K_S$	1.59(8)	*0.18(45)	1.55(7)	-0.40(49)	0.32(29)
$\Lambda_c^+ \rightarrow \Lambda^0 \pi^+$	1.30(6)	-0.755(6)	1.29(5)	-0.75(1)	-0.13(19)
$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	1.27(6)	-0.466(18)	1.27(5)	-0.47(2)	0.88(2)
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	1.25(10)	-0.48(3)	1.27(5)	-0.47(2)	0.88(2)
$\Lambda_c^+ \rightarrow \Xi^0 K^+$	**0.55(7)	0.01(16)	0.40(3)	-0.15(14)	-0.29(22)
$\Lambda_c^+ \rightarrow \Lambda^0 K^+$	0.064(3)	-0.585(52)	0.063(3)	-0.56(5)	0.82(5)
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	0.0382(25)	-0.54(20)	0.0365(21)	-0.52(10)	0.48(24)
$\Lambda_c^+ \rightarrow n \pi^+$	0.066(13)		0.067(8)	-0.78(12)	-0.63(15)
$\Lambda_c^+ \rightarrow \Sigma^+ K_S$	0.048(14)		0.036(2)	-0.52(10)	0.48(24)
$\Lambda_c^+ \rightarrow p \pi^0$	< 0.008		0.02(1)		-0.82(32)
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	0.32(4)	-0.99(6)	0.32(4)	-0.93(4)	-0.32(16)
$\Lambda_c^+ \rightarrow p \eta$	0.142(12)		0.145(26)	-0.42(61)	0.64(40)
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	0.437(84)	-0.46(7)	0.420(70)	-0.44(25)	0.86(6)
$\Lambda_c^+ \rightarrow p \eta'$	0.0484(91)		0.0520(114)	-0.59(9)	0.76(14)
$\Xi_c^+ \rightarrow \Xi^0 \pi^+$	1.6(8)		0.90(16)	-0.94(6)	0.32(21)
$\Xi_c^0 \rightarrow \Xi^- \pi^+$	****1.43(32)	* -0.64(5)	2.72(9)	-0.71(3)	0.36(20)
Channels	$\mathcal{R}_X^{\text{exp}}$	α_{exp}	\mathcal{R}_X	α	β
$\Xi_c^0 \rightarrow \Lambda^0 K_S$	0.225(13)		0.233(9)	-0.47(29)	0.66(20)
$\Xi_c^0 \rightarrow \Xi^- K^+$	**0.0275(57)		0.0410(4)	-0.75(4)	0.38(20)
$\Xi_c^0 \rightarrow \Sigma^0 K_S$	0.038(7)		0.038(7)	-0.07(117)	-0.83(28)
$\Xi_c^0 \rightarrow \Sigma^+ K^-$	0.123(12)		0.132(11)	-0.21(18)	-0.39(29)

• SU(3) flavor analysis — Tree

PDG $> 4\sigma$
 $(1.43 \pm 0.32) \%$

SU(3)
 $(2.72 \pm 0.09) \%$

Belle $< 2\sigma$
 $(1.80 \pm 0.52) \%$

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e) = (2.38 \pm 0.44) \%$$

×

LQCD, CPC 46, 011002 (2022)

$$\frac{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)}{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e)} = 1.37 \pm 0.08$$

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Belle, PRL 127 121803 (2021)

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$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	1.27(6)	-0.466(18)	1.27(5)	-0.47(2)	0.88(2)
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	1.25(10)	-0.48(3)	1.27(5)	-0.47(2)	0.88(2)
$\Lambda_c^+ \rightarrow \Xi^0 K^+$	**0.55(7)	0.01(16)	0.40(3)	-0.15(14)	-0.29(22)
$\Lambda_c^+ \rightarrow \Lambda^0 K^+$	0.064(3)	-0.585(52)	0.063(3)	-0.56(5)	0.82(5)
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	0.0382(25)	-0.54(20)	0.0365(21)	-0.52(10)	0.48(24)
$\Lambda_c^+ \rightarrow n\pi^+$	0.066(13)		0.067(8)	-0.78(12)	-0.63(15)
$\Lambda_c^+ \rightarrow \Sigma^+ K_S$	0.048(14)		0.036(2)	-0.52(10)	0.48(24)
$\Lambda_c^+ \rightarrow p\pi^0$	< 0.008		0.02(1)		-0.82(32)
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	0.32(4)	-0.99(6)	0.32(4)	-0.93(4)	-0.32(16)
$\Lambda_c^+ \rightarrow p\eta$	0.142(12)		0.145(26)	-0.42(61)	0.64(40)
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	0.437(84)	-0.46(7)	0.420(70)	-0.44(25)	0.86(6)
$\Lambda_c^+ \rightarrow p\eta'$	0.0484(91)		0.0520(114)	-0.59(9)	0.76(14)
$\Xi_c^+ \rightarrow \Xi^0 \pi^+$	1.6(8)		0.90(16)	-0.94(6)	0.32(21)
$\Xi_c^0 \rightarrow \Xi^- \pi^+$	****1.43(32)	* -0.64(5)	2.72(9)	-0.71(3)	0.36(20)
Channels	$\mathcal{R}_X^{\text{exp}}$	α_{exp}	\mathcal{R}_X	α	β
$\Xi_c^0 \rightarrow \Lambda^0 K_S$	0.225(13)		0.233(9)	-0.47(29)	0.66(20)
$\Xi_c^0 \rightarrow \Xi^- K^+$	**0.0275(57)		0.0410(4)	-0.75(4)	0.38(20)
$\Xi_c^0 \rightarrow \Sigma^0 K_S$	0.038(7)		0.038(7)	-0.07(117)	-0.83(28)
$\Xi_c^0 \rightarrow \Sigma^+ K^-$	0.123(12)		0.132(11)	-0.21(18)	-0.39(29)

● SU(3) flavor analysis — Tree

$$F = \tilde{f}^a (P^\dagger)_l^l \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (\mathbf{B}^\dagger)_k^j + \tilde{f}^b \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (\mathbf{B}^\dagger)_k^l (P^\dagger)_l^j + \tilde{f}^c \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (P^\dagger)_k^l (\mathbf{B}^\dagger)_l^j + \tilde{f}^d \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}^\dagger)_k^i (P^\dagger)_l^j (\mathbf{B}_c)^{kl} + \tilde{f}^e (\mathbf{B}^\dagger)_i^j \mathcal{H}(\mathbf{15})_l^{\{ik\}} (P^\dagger)_k^l (\mathbf{B}_c)_j + \cancel{\lambda_b \mathcal{H}(\mathbf{3})},$$

$CP \propto \tilde{f}^e, \tilde{g}^e$

$$A_{CP}^{dir} = \frac{\Gamma - \bar{\Gamma}}{\Gamma + \bar{\Gamma}}, \quad \alpha_{CP} = \frac{\alpha + \bar{\alpha}}{2},$$

$$\beta_{CP} = \frac{\beta + \bar{\beta}}{2}, \quad \gamma_{CP} = \frac{\gamma - \bar{\gamma}}{2}.$$

CP-odd quantities $\sim 10^{-4}$

$$a_{D \rightarrow K^+ K^-}^{dir} - a_{D \rightarrow \pi^+ \pi^-}^{dir} = (-1.57 \pm 0.29) \times 10^{-3}$$

Channels	$\mathcal{B}(10^{-3})$	$\alpha_{CP}(10^{-3})$	$\beta_{CP}(10^{-3})$	$\gamma_{CP}(10^{-3})$	$A_{CP}^{dir}(10^{-3})$
$\Lambda_c^+ \rightarrow p\pi^0$	0.16(2)	-0.61(39)	-0.43(48)	0.53(145)	0.01(1)
$\Lambda_c^+ \rightarrow p\eta$	1.45(25)	0.05(17)	0.04(14)	-0.07(22)	-0.03(4)
$\Lambda_c^+ \rightarrow p\eta'$	0.52(11)	-0.02(7)	0.01(4)	0.00(4)	0.00(1)
$\Lambda_c^+ \rightarrow n\pi^+$	0.67(8)	0.12(20)	0.13(26)	-0.28(40)	-0.01(2)
$\Lambda_c^+ \rightarrow \Lambda^0 K^+$	0.63(2)	-0.03(10)	0.03(5)	0.04(24)	0.01(1)
$\Xi_c^+ \rightarrow \Sigma^+ \pi^0$	2.11(14)	0.06(13)	-0.01(13)	-0.09(42)	-0.07(7)
$\Xi_c^+ \rightarrow \Sigma^+ \eta$	0.70(32)	-0.10(22)	0.09(73)	0.29(57)	0.01(4)
$\Xi_c^+ \rightarrow \Sigma^+ \eta'$	1.13(23)	0.03(7)	-0.01(2)	-0.01(4)	-0.01(0)
$\Xi_c^+ \rightarrow \Sigma^0 \pi^+$	3.04(11)	-0.01(6)	-0.01(11)	0.05(21)	0.05(5)
$\Xi_c^+ \rightarrow \Xi^0 K^+$	1.04(13)	0.02(14)	0.13(18)	-0.18(25)	-0.02(2)
$\Xi_c^+ \rightarrow \Lambda^0 \pi^+$	0.32(9)	0.0(19)	0.36(30)	0.20(19)	0.00(1)
$\Xi_c^0 \rightarrow \Sigma^0 \pi^0$	0.34(2)	-0.04(12)	0.25(39)	0.12(12)	0.00(1)
$\Xi_c^0 \rightarrow \Sigma^0 \eta$	0.12(5)	-0.11(22)	0.09(73)	0.29(57)	0.00(1)
$\Xi_c^0 \rightarrow \Sigma^0 \eta'$	0.19(4)	0.03(7)	-0.01(2)	-0.01(4)	0.00(1)
$\Xi_c^0 \rightarrow \Sigma^- \pi^+$	1.83(6)	0.02(7)	-0.09(21)	0.03(12)	0.02(3)
$\Xi_c^0 \rightarrow \Xi^- K^+$	1.12(3)	0.02(5)	-0.08(16)	0.02(11)	0.01(1)
$\Xi_c^0 \rightarrow \Lambda^0 \pi^0$	0.09(1)	0.07(20)	-0.27(25)	-0.15(17)	0.00(1)
$\Xi_c^0 \rightarrow \Lambda^0 \eta$	0.43(11)	0.06(12)	0.11(14)	-0.01(2)	-0.01(1)
$\Xi_c^0 \rightarrow \Lambda^0 \eta'$	0.68(13)	0.00(1)	0.00(1)	0.00(1)	0.00(1)

SU(3) flavor analysis

$$\lambda_{d,s} \text{ Tree} + \underbrace{\lambda_b \text{ Penguin}}_{V_{cd}V_{ud}^*}$$

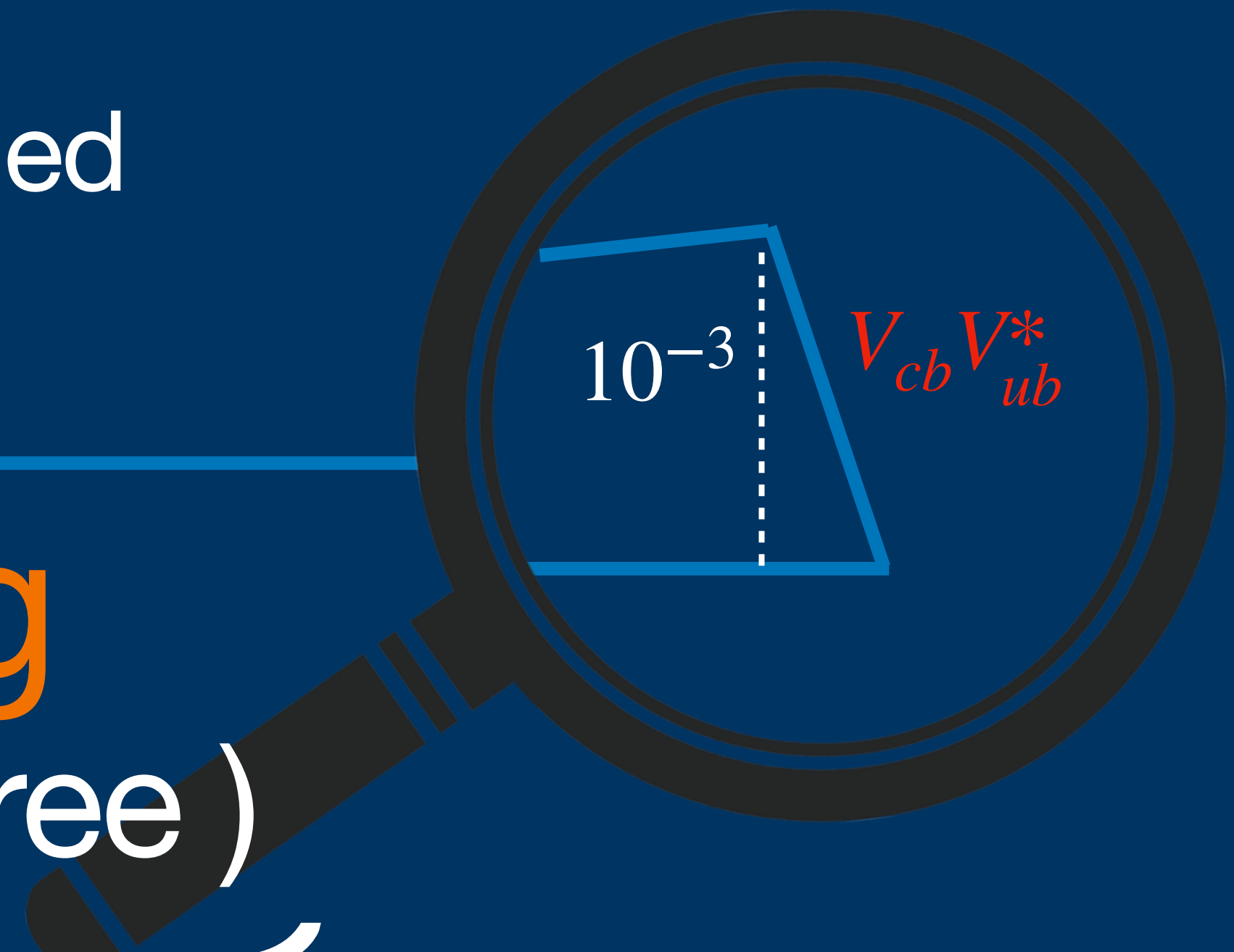
Insensitive to CP-even quantities & undetermined

$$\lambda_q = V_{cq}^* V_{uq}$$

Pole model + Rescattering

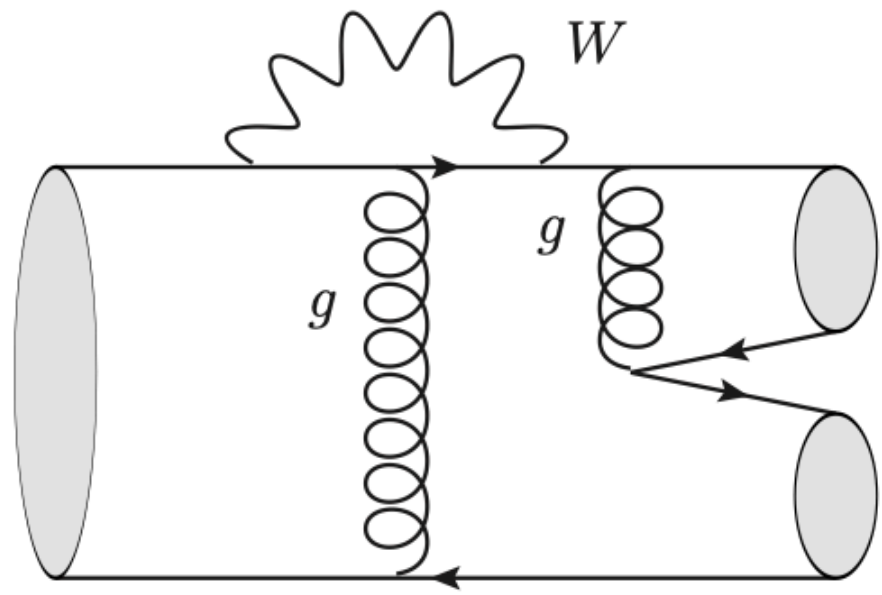
$$\lambda_{d,s} \text{ Tree} + \underbrace{\lambda_b \text{ Tree} \times (\text{Penguin} / \text{Tree})}_{V_{cb}V_{ub}^*}$$

Determined by the PM + rescattering

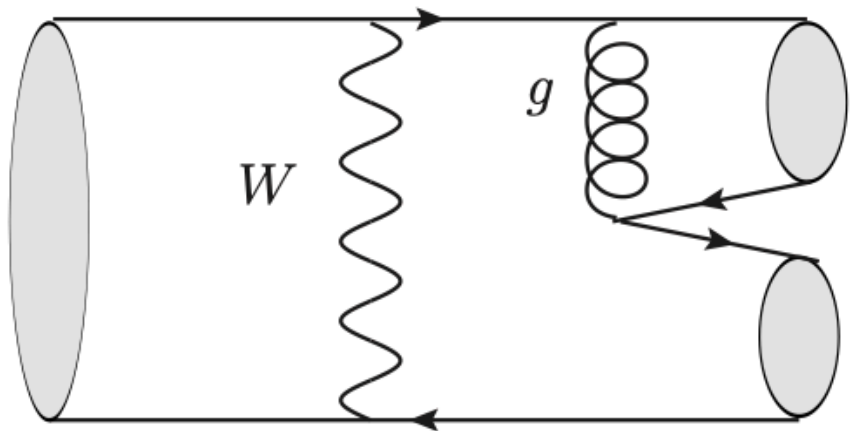
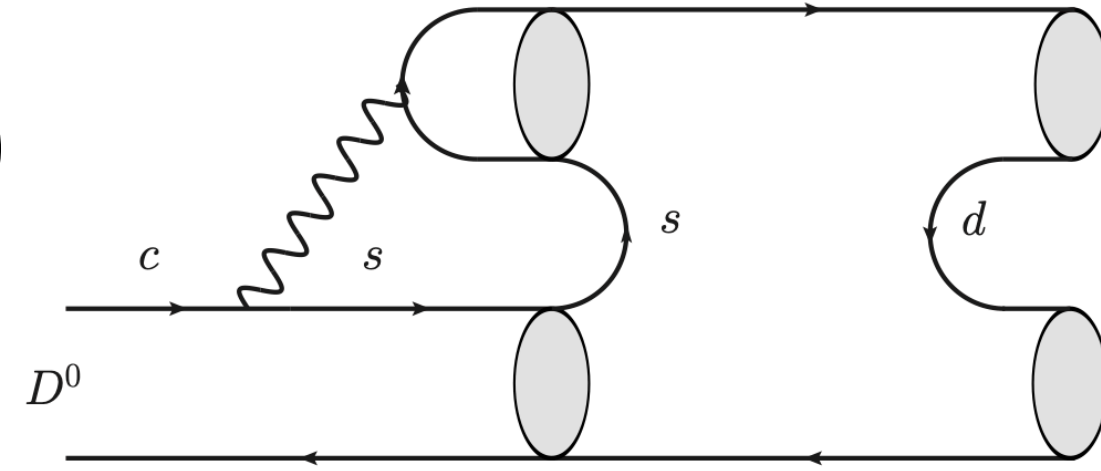


● Pole model + Rescattering — Penguin / Tree

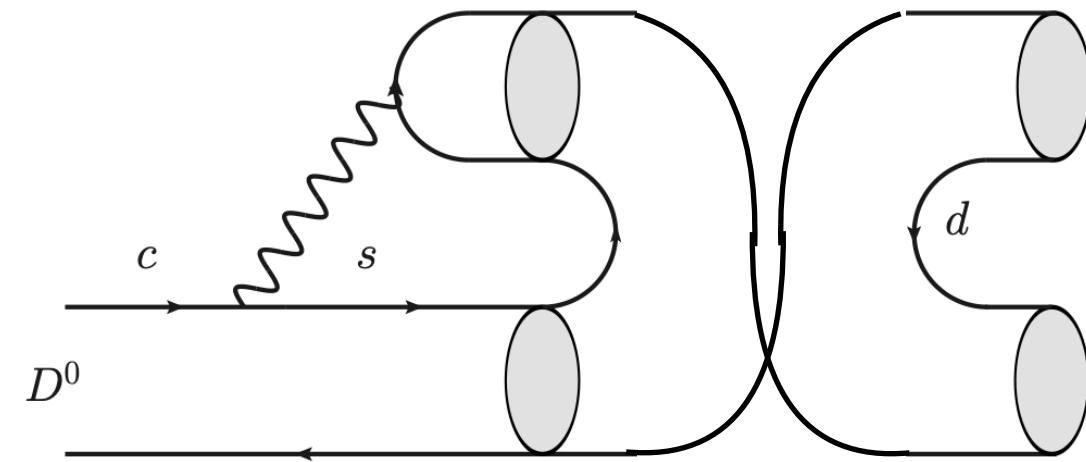
b – loop is absent!



LD
=

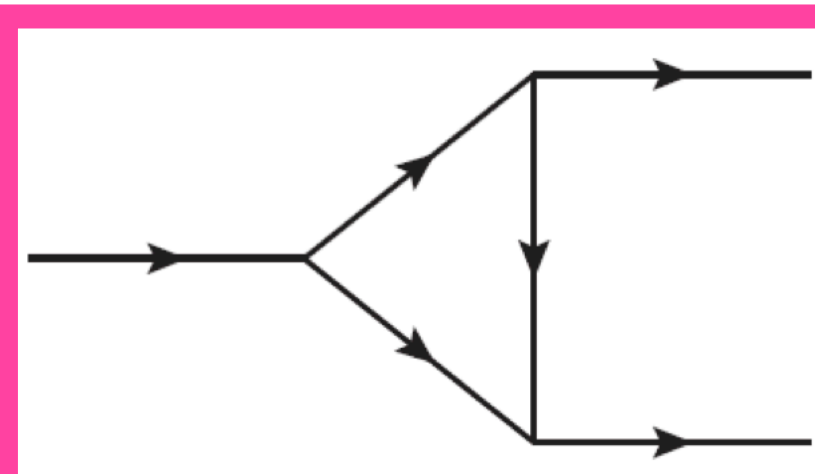


LD
=



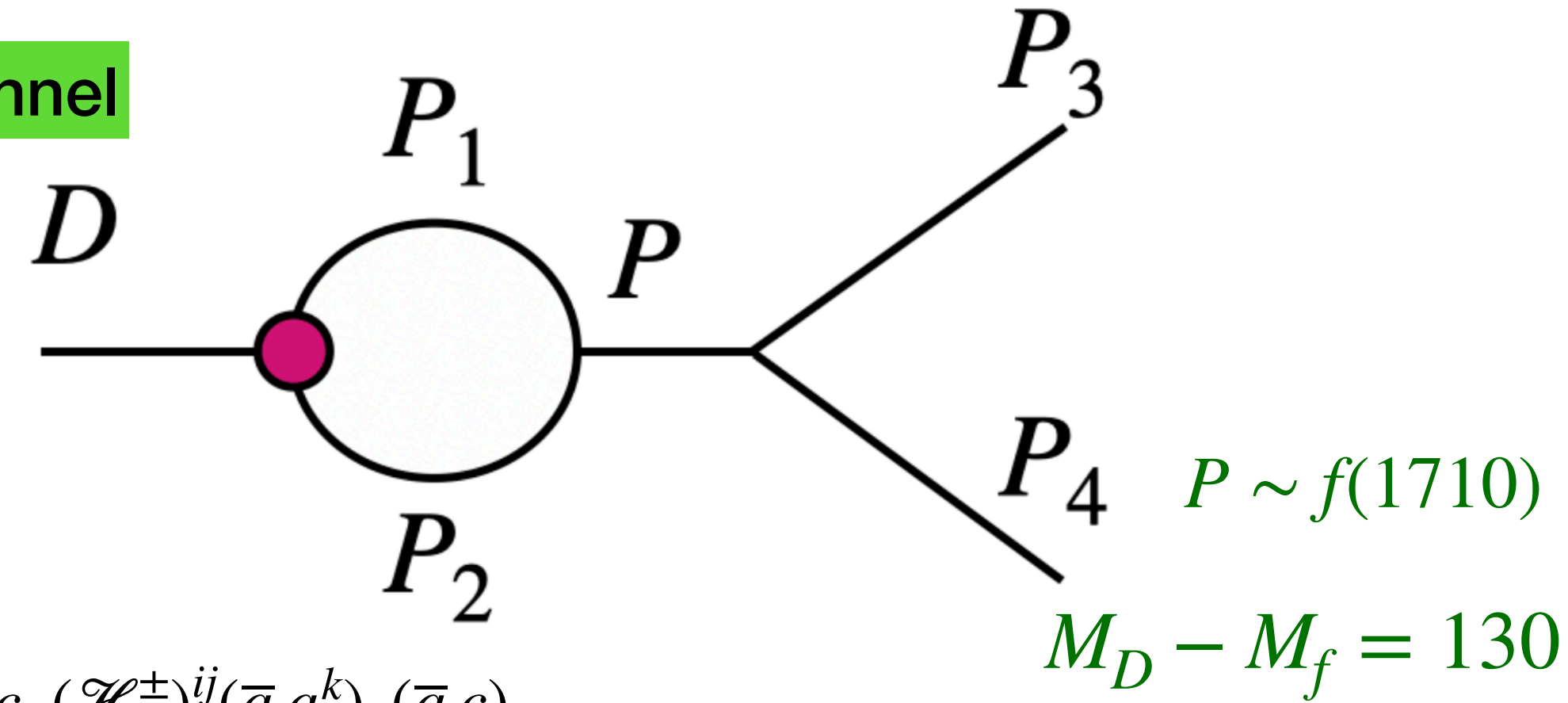
“Hence, it is plausible to assume that PE is of the same order of magnitude as E. We took PE = E.”

PRD 100, 093002 (2019)



Proved by Di Wang
JHEP 03, 155 (2022)

For s-channel



Phys. Rev. D 81, 074021 (2010)

$$\mathcal{H}_{eff}^{\pm} = \frac{G_F}{\sqrt{2}} c_{\pm} (\mathcal{H}^{\pm})_{ij}^{jk} (\bar{q}_i q^k)_L (\bar{q}_j c)_L,$$

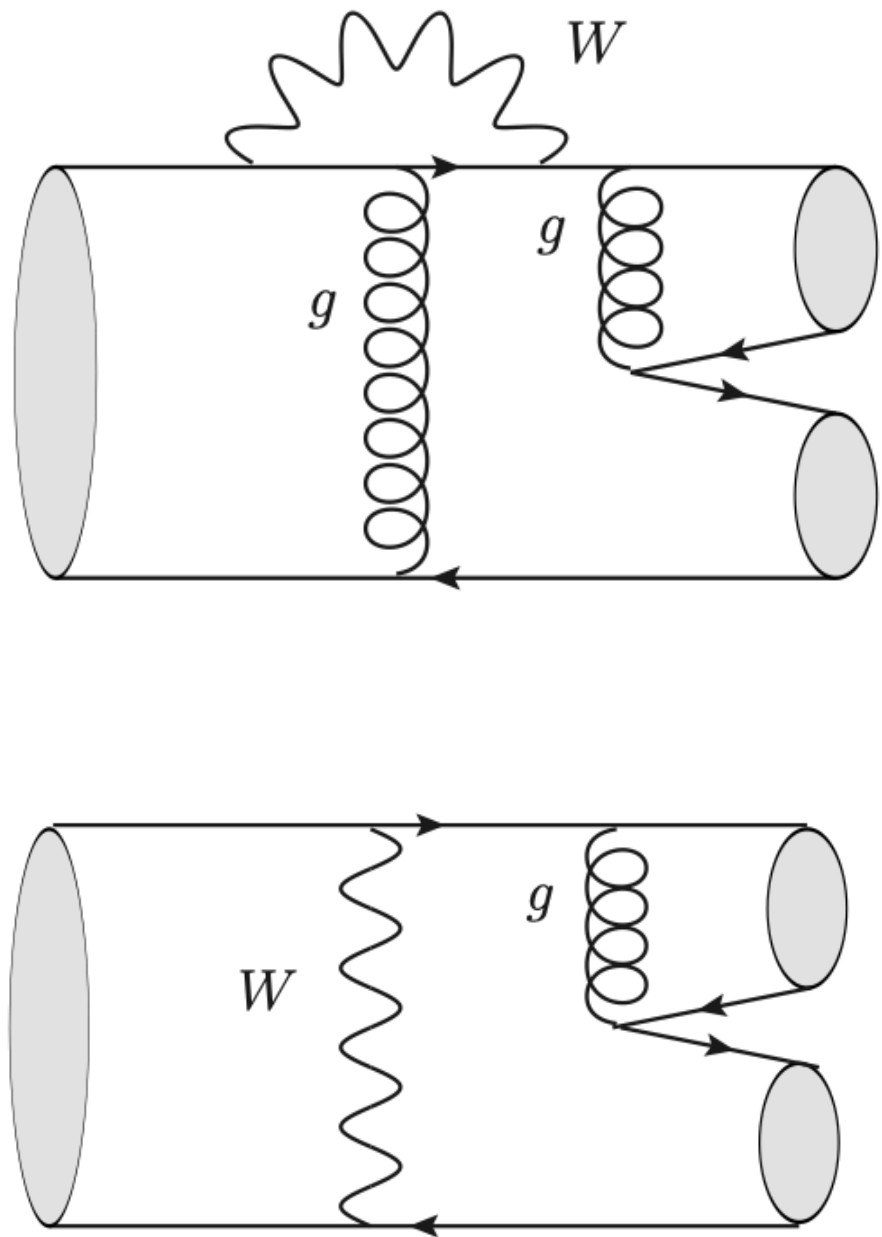
$$\langle P | \mathcal{H}_{eff}^{\pm} | D \rangle = T \sum_{P_1, P_2} \underbrace{D_i(\mathcal{H}^{\pm})_{ij}^{jk} (P_1^{\dagger})_j^i (P_2^{\dagger})_k^i}_{\text{Weak; } D \rightarrow P_1 P_2} \cdot \underbrace{((P_1)_n^m (P_2)_o^n (P^{\dagger})_m^o + (P_1)_n^m (P_2)_m^o (P^{\dagger})_o^n)}_{\text{Strong; } P_1 P_2 \rightarrow P},$$

Penguin / Tree = 1

$$= T \left(1 \mp \frac{2}{3} \right) \left(\underbrace{D_i(\mathcal{H}^{\pm})_{jk}^{ij} (P^{\dagger})_j^i}_{P\text{-exchange}} + \underbrace{D_i(\mathcal{H}^{\pm})_{ij}^{jk} (P^{\dagger})_k^j}_{W\text{-exchange}} \right)$$

Completeness relation: $\sum_{\lambda_8} (\lambda_8)_j^i (\lambda_8^{\dagger})_l^k = \delta_l^i \delta_j^k - \frac{1}{3} \delta_j^i \delta_l^k$

● Pole model + Rescattering — Penguin / Tree



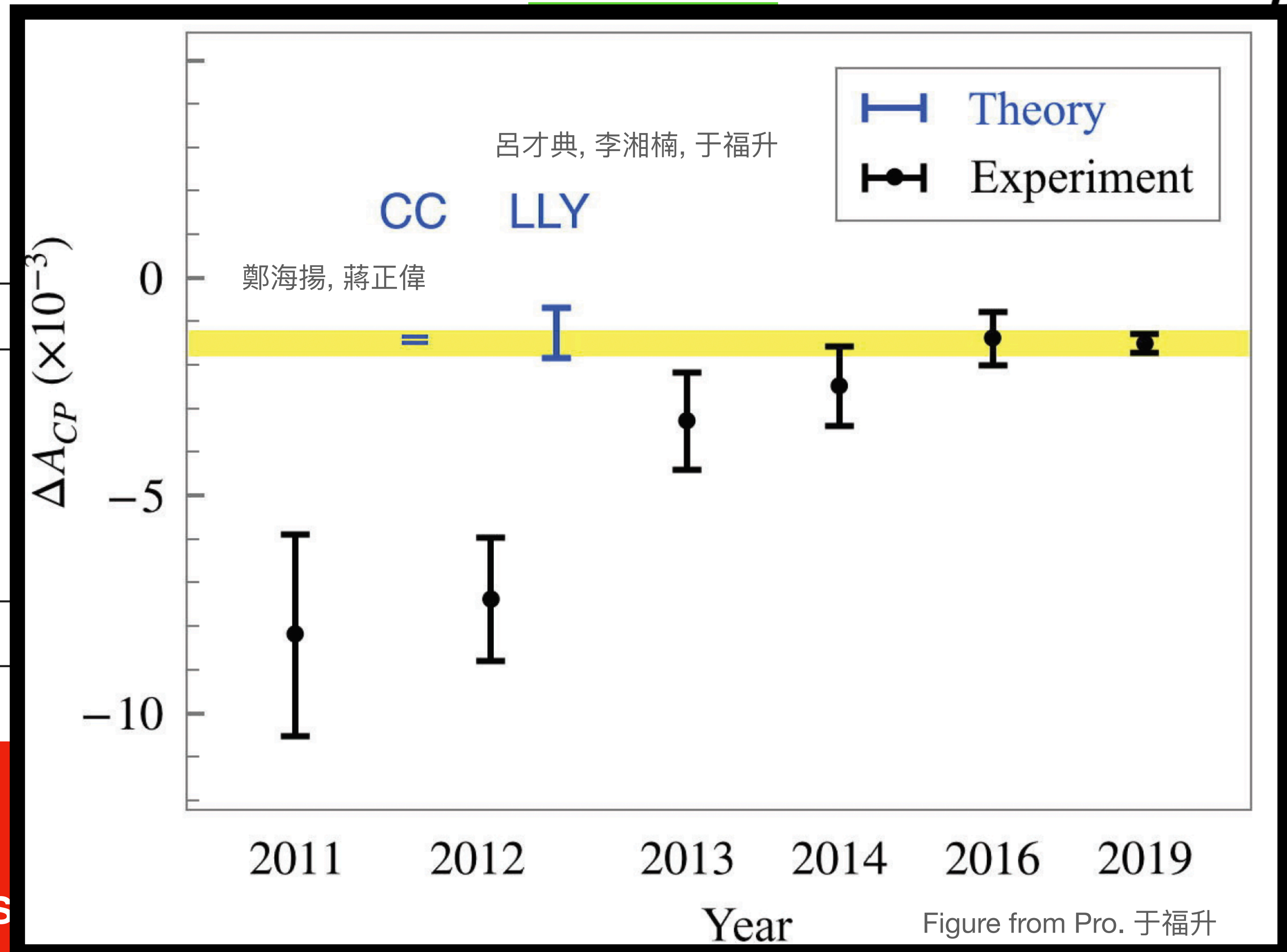
LD
 \equiv

LD
 \equiv

D^0

D^0

“Hence, it is plausible to assume that PE is of the same order of magnitude as E. We took PE = E.”
PRD 100, 093002 (2019)



Proved by Di Wang
JHEP 03, 155 (2022)

Completeness relation: $\sum_{\lambda_8} (\lambda_8)_j^i (\lambda_8)_l^k = \delta_l^i \delta_j^k - \frac{1}{3} \delta_j^i \delta_l^k$

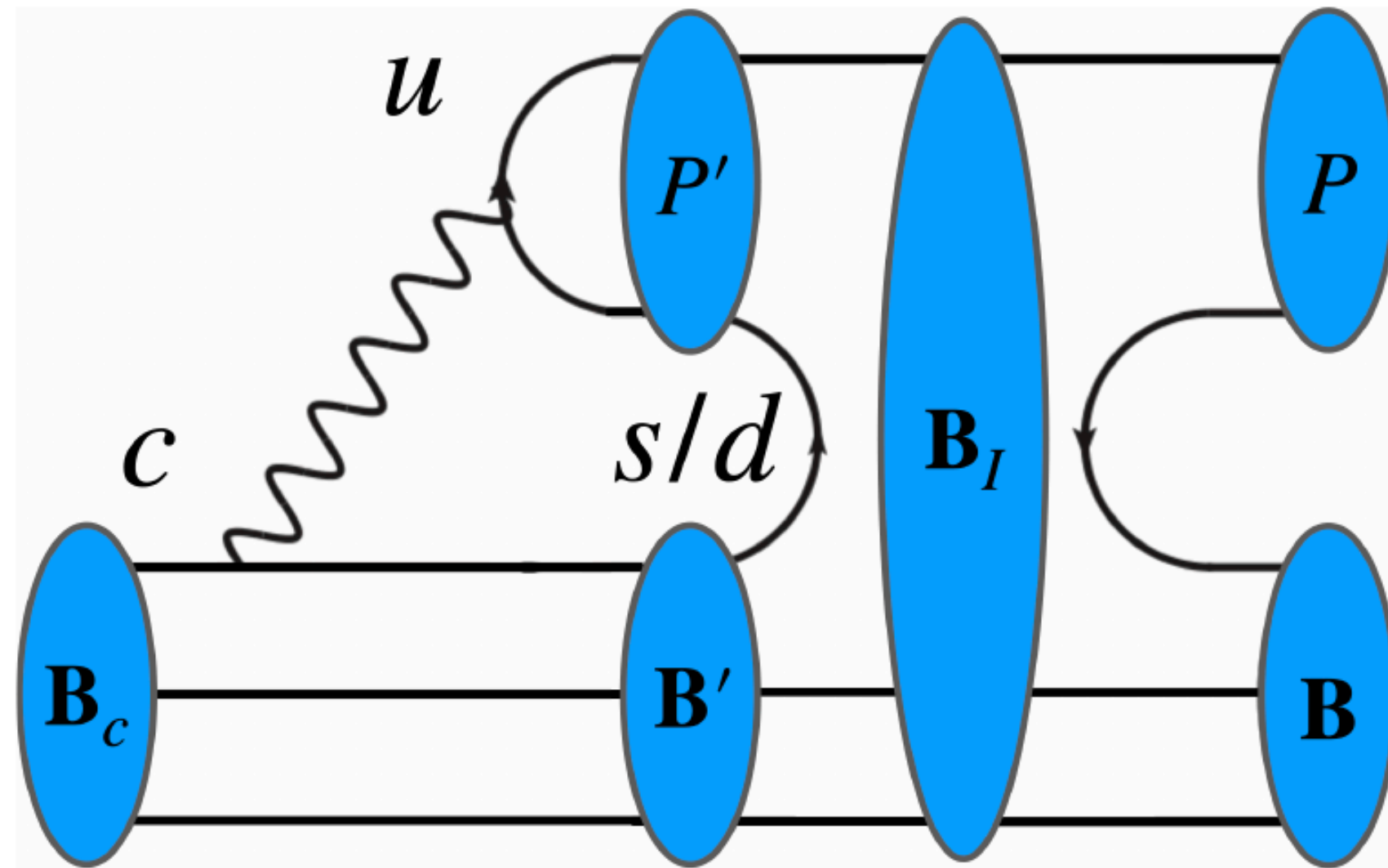
$P \sim f(1710)$
 $M_D - M_f = 130$
D 81, 074021 (2010)

$(P_1)_n^m (P_2)_m^o (P^\dagger)_o^n$
 $P_1 P_2 \rightarrow P$
1
 $(P^\dagger)_k^j$
range

Figure from Pro. 于福升

● Pole model + Rescattering — Penguin / Tree

b – loop is absent!

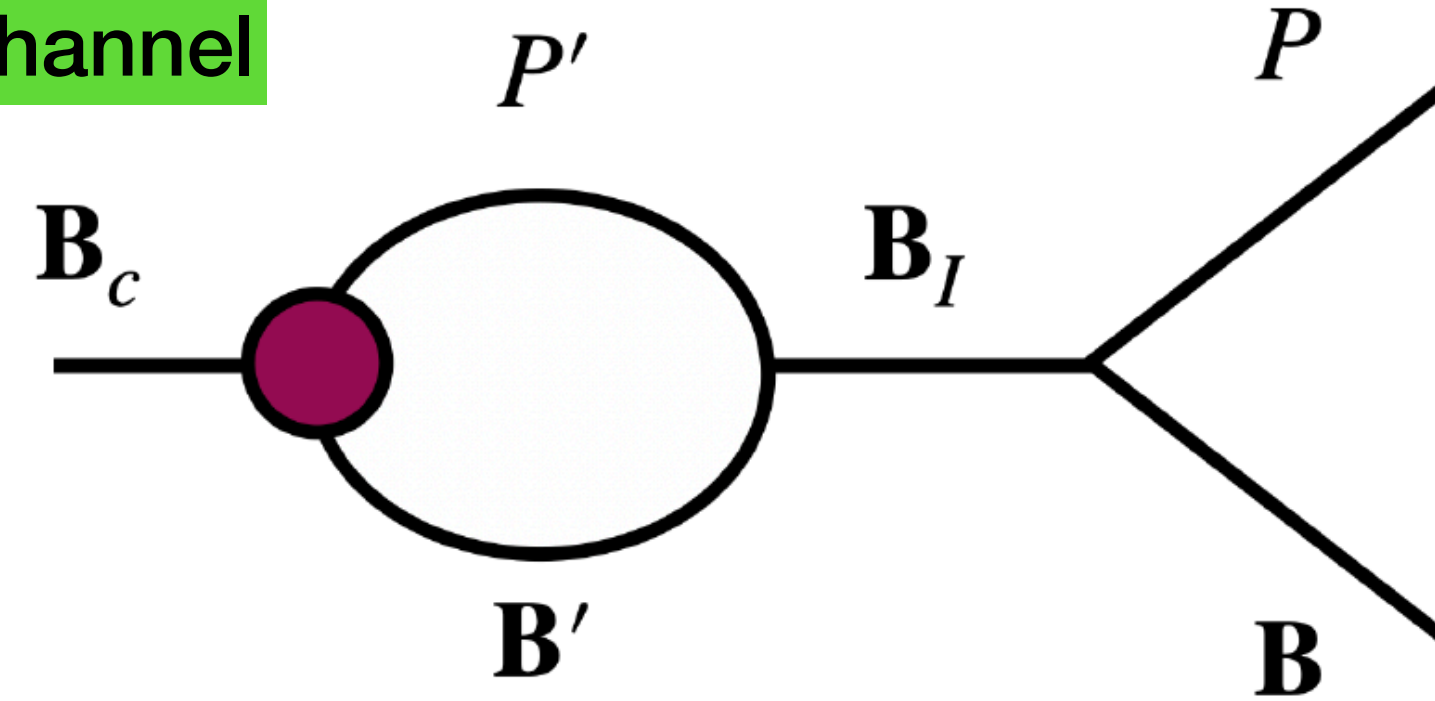


$$F_s^{\text{pole}} = \frac{\tilde{E}_s^-}{f_P} \left\{ \frac{1}{\sqrt{2}} \mathcal{H}(\bar{\mathbf{6}})_{kl} (\mathbf{B}_c)^{[ki]} \left[(P^\dagger)_n^l (\mathbf{B}^\dagger)_i^n + g_s^- (P^\dagger)_i^n (\mathbf{B}^\dagger)_n^l \right] - \lambda_b \frac{7 - 2g_s^-}{2 + 8g_s^-} \left[(\mathbf{B}_c)_i \mathcal{H}(\bar{\mathbf{3}})^k \left[(P^\dagger)_j^i (\mathbf{B}^\dagger)_k^j + g_s^- (P^\dagger)_k^j (\mathbf{B}^\dagger)_j^i \right] - \frac{1 + g_s^-}{3} (\mathbf{B}_c)_i \mathcal{H}(\mathbf{3}_-)^i (P^\dagger)_k^j (\mathbf{B}^\dagger)_k^j \right] \right\}$$

Ratio between 3 & $\bar{6}$ is determined

$$CP \propto \bar{\mathbf{6}} \times \mathbf{3}$$

For s-channel



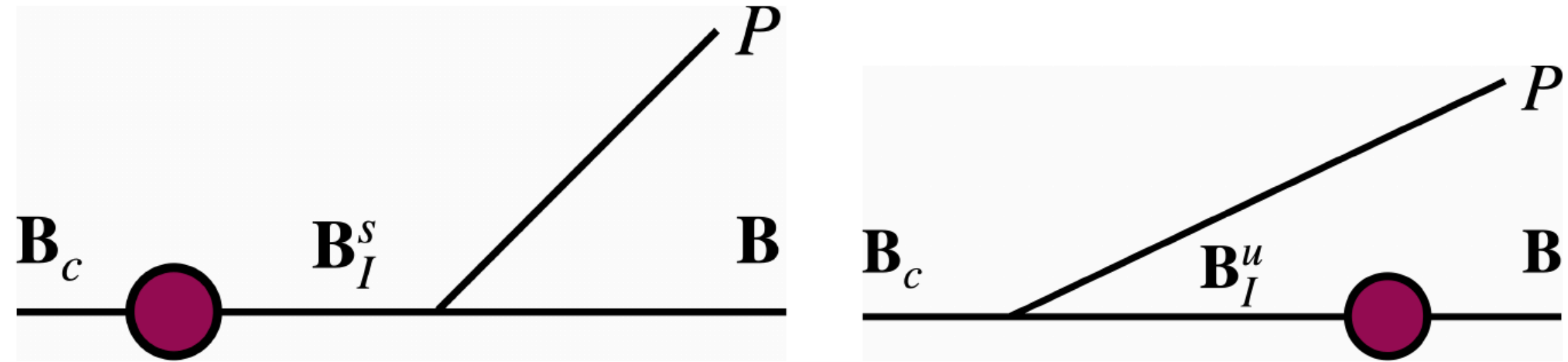
$$a_{\mathbf{B}_I \mathbf{B}_c}^{RE} \propto \sum_{\mathbf{B}', P'} \underbrace{\left((\mathbf{B}_c)_i \mathcal{H}_l^{jk} (\mathbf{B}'^\dagger)_j^i (P'^\dagger)_k^l \right)}_{\text{Weak; } \mathbf{B}_c \rightarrow \mathbf{B}' P'} \cdot \underbrace{(P')_m^o \left(g_{12}^{s\pm} (\mathbf{B}')_n^m (\mathbf{B}'^\dagger)_o^n + g_{21}^{s\pm} (\mathbf{B}'^\dagger)_n^m (\mathbf{B}')_o^n \right)}_{\text{Strong; } \mathbf{B}' P' \rightarrow \mathbf{B}_I}$$

$$= \left(\frac{8}{3} g_{21}^{s\pm} + \frac{2}{3} g_{12}^{s\pm} \right) \left(\frac{1}{\sqrt{2}} (\mathbf{B}_c)^{[lj]} \mathcal{H}(\bar{\mathbf{6}})_{kl} (\mathbf{B}'^\dagger)_j^k - \lambda_b \frac{7 - 2g_s^\pm}{2 + 8g_s^\pm} (\mathbf{B}_c)_i \mathcal{H}(\mathbf{3}_-)^k (\mathbf{B}'^\dagger)_k^i \right),$$

$a_{\mathbf{B}_c \mathbf{B}_I}^{RE}$ becomes complex if $M_{\mathbf{B}_c} > M_{\mathbf{B}'} + M_{P'}$

Completeness relation: $\sum_{\lambda_8} (\lambda_8)_j^i (\lambda_8^\dagger)_l^k = \delta_l^i \delta_j^k - \frac{1}{3} \delta_j^i \delta_l^k$

● Pole model + Rescattering — Penguin / Tree



$$\tilde{E}_s^- = (18.0 \pm 0.8)e^{i(-0.271 \pm 0.017)}, \quad \tilde{E}_s^+ = (9.9 \pm 1.2)e^{i(-0.424 \pm 0.144)},$$

$$\tilde{E}_{u\bar{3}}^- = 22.0 \pm 1.4, \quad \tilde{E}_{u\bar{6}}^- = -24.4 \pm 0.7, \quad \tilde{E}_{u\bar{6}}^+ = -15.0 \pm 1.1,$$

$$a^+ = (0.401 \pm 0.025)e^{i(-0.104 \pm 0.122)}, \quad a^0 = 0.4e^{-i(164 \pm 7)^\circ}$$

Case in charmed baryons; arXiv: 2312.xxxx

$a^+, T \propto$ Color-allowed tree, $a^0, C \propto$ Color-suppressed tree

Case in D meson; Phys. Rev. D 100, 093002 (2019)

$$T = 3.113 \pm 0.011,$$

$$C = (2.767 \pm 0.029)e^{-i(151.3 \pm 0.3)^\circ},$$

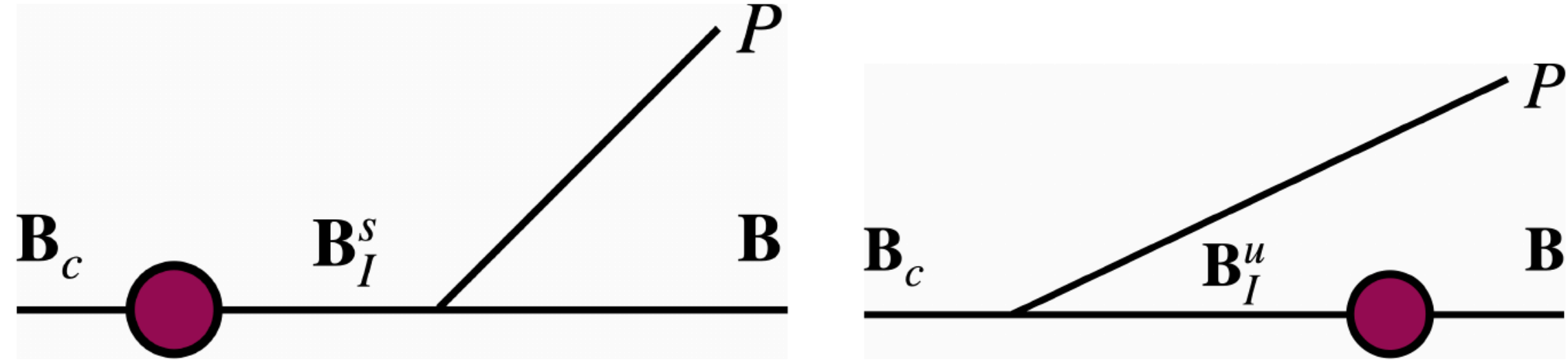
30 input,
10 parameters

Preliminary results

Channels	$\mathcal{B}_{\text{exp}}(\%)$	α_{exp}	$\mathcal{B}(\%)$	α	β	γ
$\Lambda_c^+ \rightarrow pK_S$	1.59(8)	0.18(50)*	1.55(6)	-0.76(2)	-0.11(3)	0.65(3)
$\Lambda_c^+ \rightarrow \Lambda\pi^+$	1.30(6)*	-0.755(6)	1.23(5)	-0.75(1)	-0.13(9)	0.64(2)
$\Lambda_c^+ \rightarrow \Sigma^0\pi^+$	1.27(6)	-0.466(18)	1.31(5)	-0.47(2)	0.01(5)	0.88(1)
$\Lambda_c^+ \rightarrow \Sigma^+\pi^0$	1.25(10)	-0.48(3)	1.31(5)	-0.47(2)	0.01(5)	0.88(1)
$\Lambda_c^+ \rightarrow \Xi^0K^+$	0.55(7)*	0.01(16)**	0.45(3)	-0.31(11)	-0.29(7)	0.91(4)
$\Lambda_c^+ \rightarrow \Lambda K^+$	0.064(3)	-0.585(52)	0.062(3)	-0.55(5)	0.10(10)	0.83(3)
$\Lambda_c^+ \rightarrow \Sigma^0K^+$	0.0382(25)*	-0.54(20)	0.0347(22)	-0.61(4)	-0.04(4)	0.79(3)
$\Lambda_c^+ \rightarrow n\pi^+$	0.066(13)		0.058(7)	-0.70(11)	-0.29(12)	0.66(7)
$\Lambda_c^+ \rightarrow \Sigma^+K_S$	0.048(14)		0.035(2)	-0.61(4)	-0.04(4)	0.79(3)
$\Lambda_c^+ \rightarrow p\pi^0$	0.016(7)		0.017(3)	-0.52(17)	-0.45(13)	0.73(7)
$\Xi_c^+ \rightarrow \Xi^0\pi^+$	1.60(80)*		0.54(9)	-0.78(10)	0.09(10)	0.61(13)
$\Xi_c^0 \rightarrow \Xi^-\pi^+$	1.43(32)****	-0.64(5)	3.04(9)	-0.68(3)	-0.02(4)	0.73(3)
Channels	$\mathcal{R}_X^{\text{exp}}$	α_{exp}	\mathcal{R}_X	α	β	γ
$\Xi_c^0 \rightarrow \Lambda K_S$	0.225(13)**		0.191(6)	-0.68(2)	-0.04(3)	0.74(2)
$\Xi_c^0 \rightarrow \Xi^-K^+$	0.0275(57)**		0.0431(8)	-0.71(2)	-0.02(4)	0.71(3)
$\Xi_c^0 \rightarrow \Sigma^0K_S$	0.038(7)		0.041(6)	-0.62(9)	-0.60(11)	0.50(5)
$\Xi_c^0 \rightarrow \Sigma^+K^-$	0.123(12)*		0.135(10)	-0.41(14)	-0.38(9)	0.83(7)

	β	$\delta_p - \delta_s$
Data	-0.64 ± 0.70	-1.55 ± 0.25
Theory	-0.29 ± 0.07	-0.75 ± 0.23

● Pole model + Rescattering — Penguin / Tree



$$\tilde{E}_s^- = (18.0 \pm 0.8)e^{i(-0.271 \pm 0.017)}, \quad \tilde{E}_s^+ = (9.9 \pm 1.2)e^{i(-0.424 \pm 0.144)},$$

$$\tilde{E}_{u\bar{3}}^- = 22.0 \pm 1.4, \quad \tilde{E}_{u\bar{6}}^- = -24.4 \pm 0.7, \quad \tilde{E}_{u\bar{6}}^+ = -15.0 \pm 1.1,$$

$$a^+ = (0.401 \pm 0.025)e^{i(-0.104 \pm 0.122)}, \quad a^0 = 0.4e^{-i(164 \pm 7)^\circ}$$

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$a^+, T \propto$ Color-allowed tree, $a^0, C \propto$ Color-suppressed tree

Case in D meson; Phys. Rev. D 100, 093002 (2019)

$$T = 3.113 \pm 0.011, \quad C = (2.767 \pm 0.029)e^{-i(151.3 \pm 0.3)^\circ},$$

30 input,
10 parameters

Channels	$\mathcal{B}(10^{-3})$	$\alpha_{CP}(10^{-3})$	$\beta_{CP}(10^{-3})$	$\gamma_{CP}(10^{-3})$	$A_{CP}^{dir}(10^{-3})$
$\Lambda_c^+ \rightarrow \Sigma^+ K_{S/L}$	0.35(2)	0.06(2)	-0.20(2)	0.04(1)	0.27(2)
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	0.35(2)	0.00(1)	-0.01(1)	0.00(1)	0.00(1)
$\Lambda_c^+ \rightarrow p\pi^0$	0.17(3)	0.14(39)	0.83(39)	0.62(22)	4.19(33)
$\Lambda_c^+ \rightarrow n\pi^+$	0.58(7)	0.30(16)	0.35(28)	0.47(13)	3.30(16)
$\Lambda_c^+ \rightarrow \Lambda K^+$	0.62(3)	0.03(5)	-0.06(5)	0.03(4)	0.57(7)
$\Xi_c^+ \rightarrow \Sigma^+ \pi^0$	2.70(17)	0.02(2)	0.04(3)	0.02(1)	-0.30(2)
$\Xi_c^+ \rightarrow \Sigma^0 \pi^+$	2.57(9)	0.02(1)	0.08(1)	0.01(1)	-0.11(1)
$\Xi_c^+ \rightarrow \Xi^0 K^+$	1.19(14)	-0.52(8)	-0.18(14)	-0.80(11)	-2.44(12)
$\Xi_c^+ \rightarrow pK_{S/L}$	0.97(7)	-0.07(2)	0.27(3)	-0.07(2)	-0.24(2)
$\Xi_c^+ \rightarrow \Lambda\pi^+$	0.51(11)	-0.38(6)	-0.10(18)	-0.55(19)	-1.81(20)
$\Xi_c^0 \rightarrow \Sigma^+ \pi^-$	0.35(1)	0.08(13)	-0.28(5)	-0.10(7)	-1.45(6)
$\Xi_c^0 \rightarrow \Sigma^0 \pi^0$	0.46(1)	-0.03(1)	0.06(1)	-0.01(1)	0.13(2)
$\Xi_c^0 \rightarrow \Sigma^- \pi^+$	1.57(1)	-0.01(1)	0.08(1)	0.00(1)	0.02(2)
$\Xi_c^0 \rightarrow \Xi^0 K_{S/L}$	0.34(1)	-0.03(3)	-0.08(4)	-0.02(1)	-0.62(3)
$\Xi_c^0 \rightarrow \Xi^- K^+$	1.31(1)	0.00(1)	-0.08(1)	0.00(1)	-0.03(2)
$\Xi_c^0 \rightarrow pK^-$	0.23(1)	-0.10(14)	0.32(5)	0.14(10)	1.43(6)
$\Xi_c^0 \rightarrow nK_{S/L}$	0.36(1)	0.04(4)	0.12(5)	0.03(2)	0.61(4)
$\Xi_c^0 \rightarrow \Lambda\pi^0$	0.11(1)	-0.25(3)	-0.03(13)	-0.37(11)	-1.60(17)

Preliminary results

What have been done

$$\underbrace{\text{Tree}[\lambda_{d,s} + \lambda_b]}_{\text{SU(3) flavor symmetry}} \underbrace{(\text{Penguin / Tree})}_{\text{PM \& Rescattering}}$$

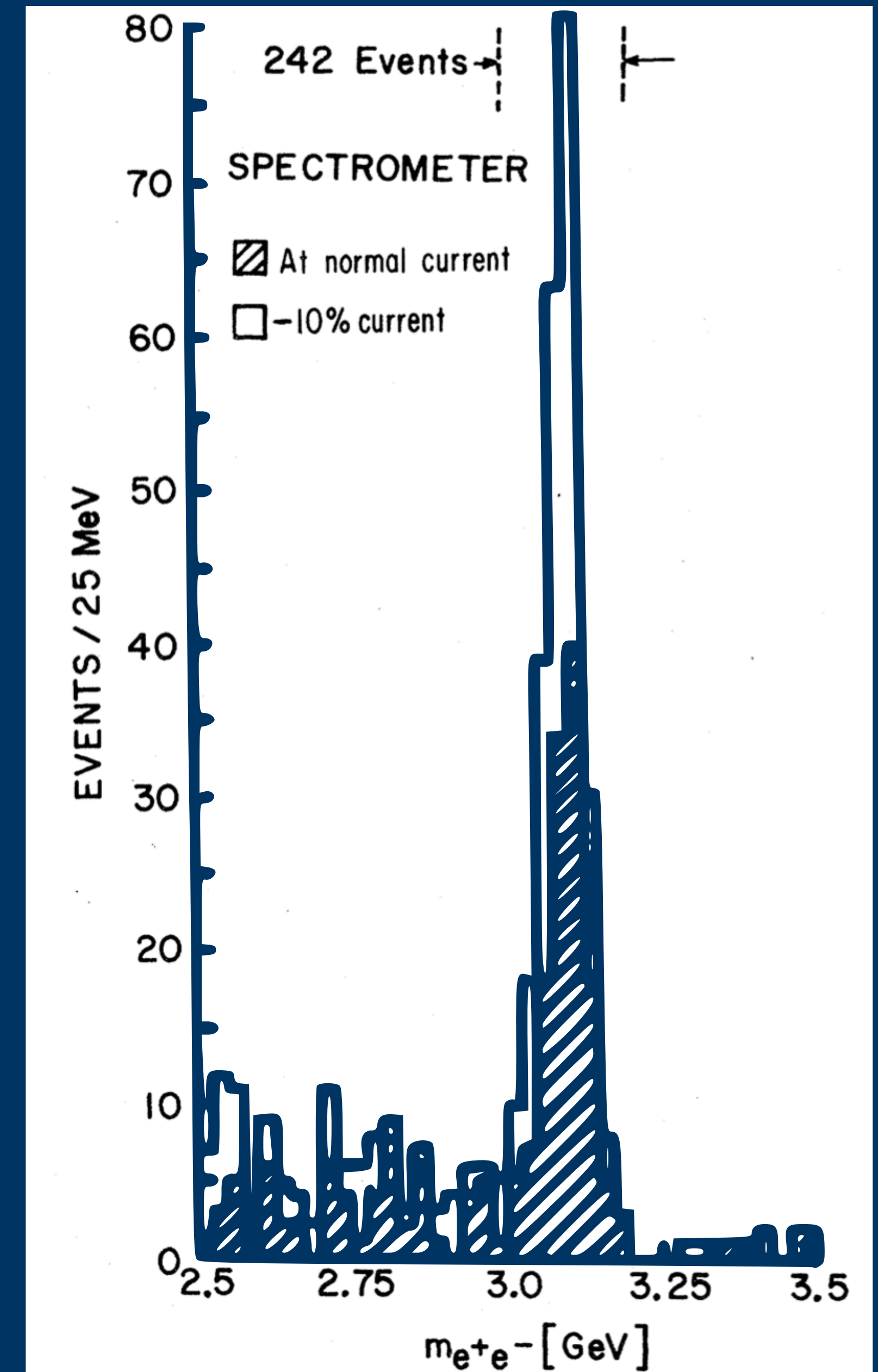
SU(3) flavor symmetry

PM & Rescattering

What we need

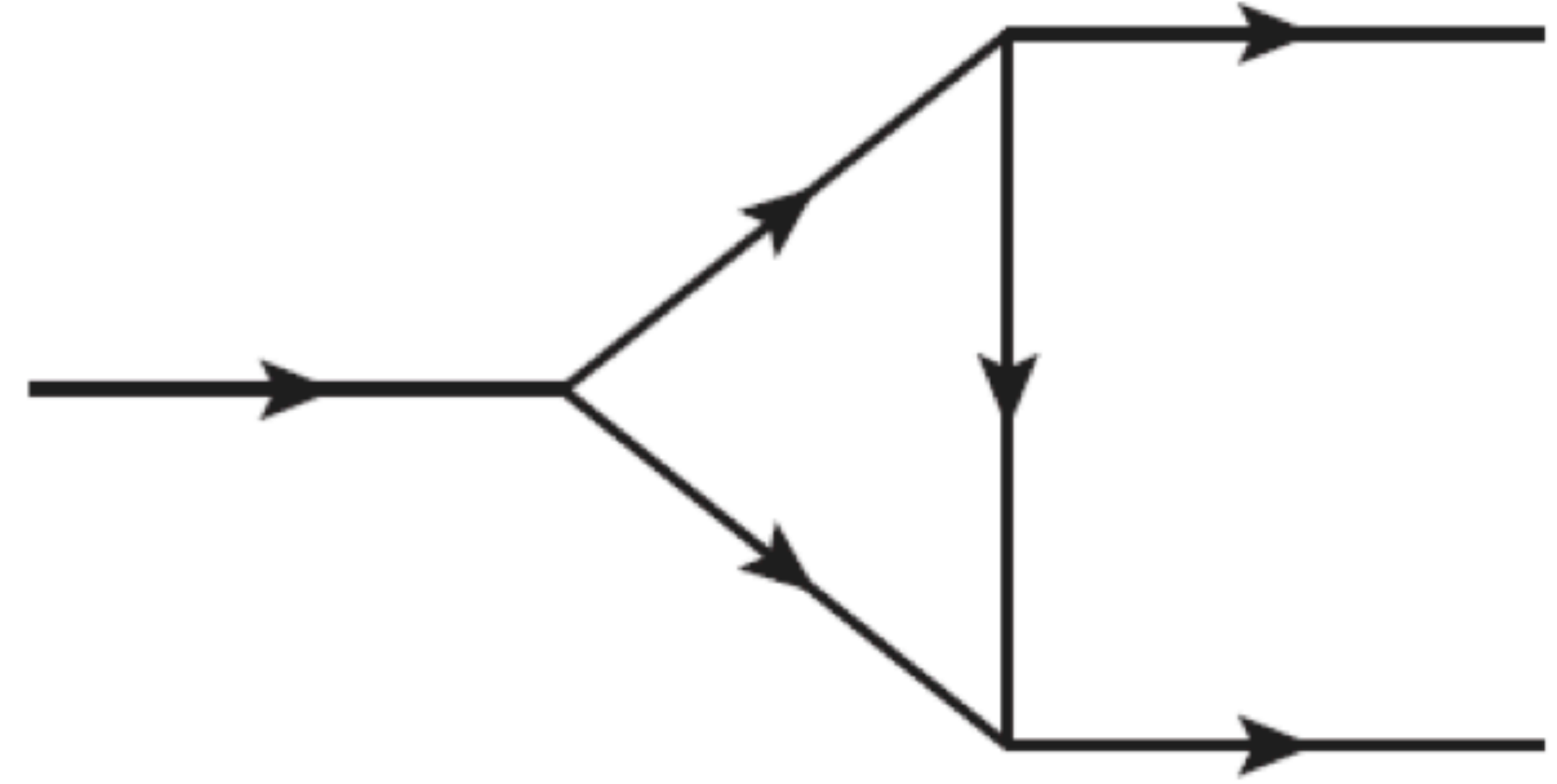
Measurements of β and γ in near future

Measurements of A_{CP} in STCF



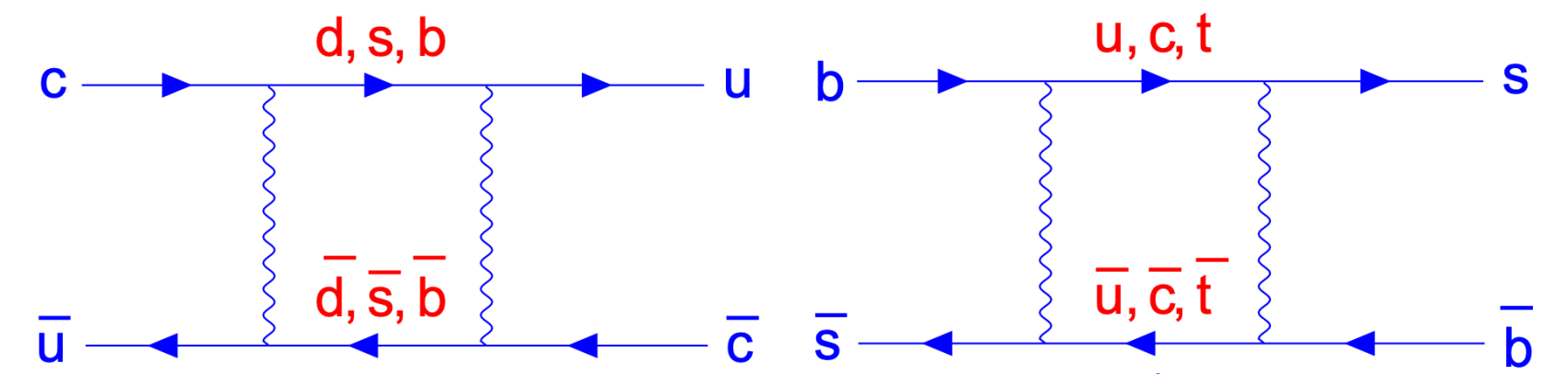
● Pole model + Rescattering

PLB 794, 19(2019) $\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+) = \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ K_S^0)$
 $(4.7 \pm 1.0) \times 10^{-4} \quad (4.8 \pm 1.4) \times 10^{-4}$
 BESIII PRD 106, no.5, 052003 (2022)



$$\begin{aligned} \mathcal{M} = & a_{15} \times (T_{c\bar{3}})_i (H_{\bar{15}})_j^{\{ik\}} (\bar{T}_8)_k^j P_l^l + b_{15} \times (T_{c\bar{3}})_i (H_{\bar{15}})_j^{\{ik\}} (\bar{T}_8)_k^l P_l^j + c_{15} \times (T_{c\bar{3}})_i (H_{\bar{15}})_j^{\{ik\}} (\bar{T}_8)_l^j P_k^l \\ & + d_{15} \times (T_{c\bar{3}})_i (H_{\bar{15}})_l^{\{jk\}} (\bar{T}_8)_j^l P_k^i + e_{15} \times (T_{c\bar{3}})_i (H_{\bar{15}})_l^{\{jk\}} (\bar{T}_8)_j^i P_k^l + a_6 \times (T_{c\bar{3}})^{[ik]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_k^j P_l^l \\ & + b_6 \times (T_{c\bar{3}})^{[ik]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_k^l P_l^j + c_6 \times (T_{c\bar{3}})^{[kl]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_l^j P_k^l + d_6 \times (T_{c\bar{3}})^{[ik]} (H_{\bar{6}})_{\{ij\}} (\bar{T}_8)_k^i P_l^j. \end{aligned}$$

● CP violation in charm - overview

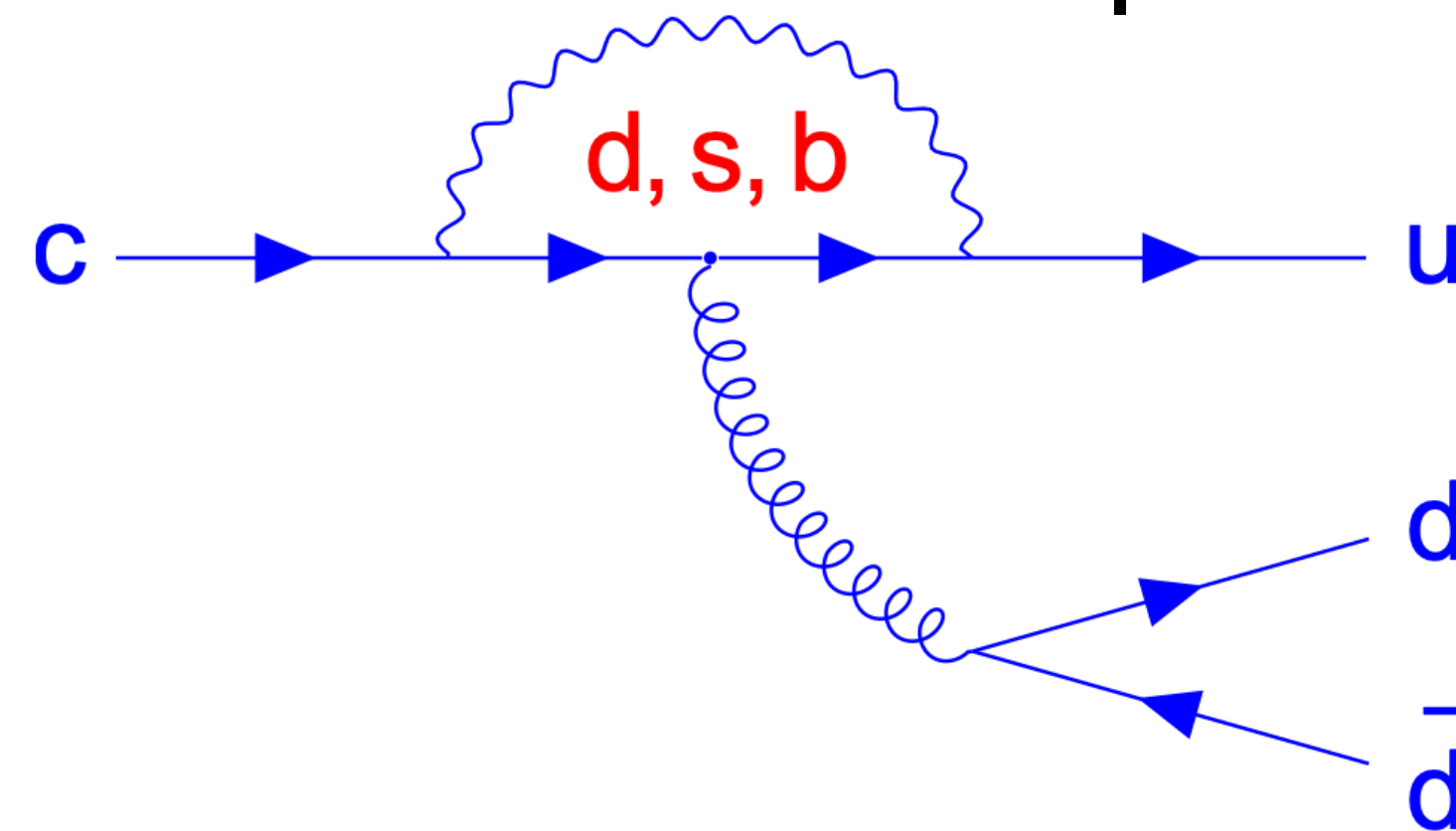
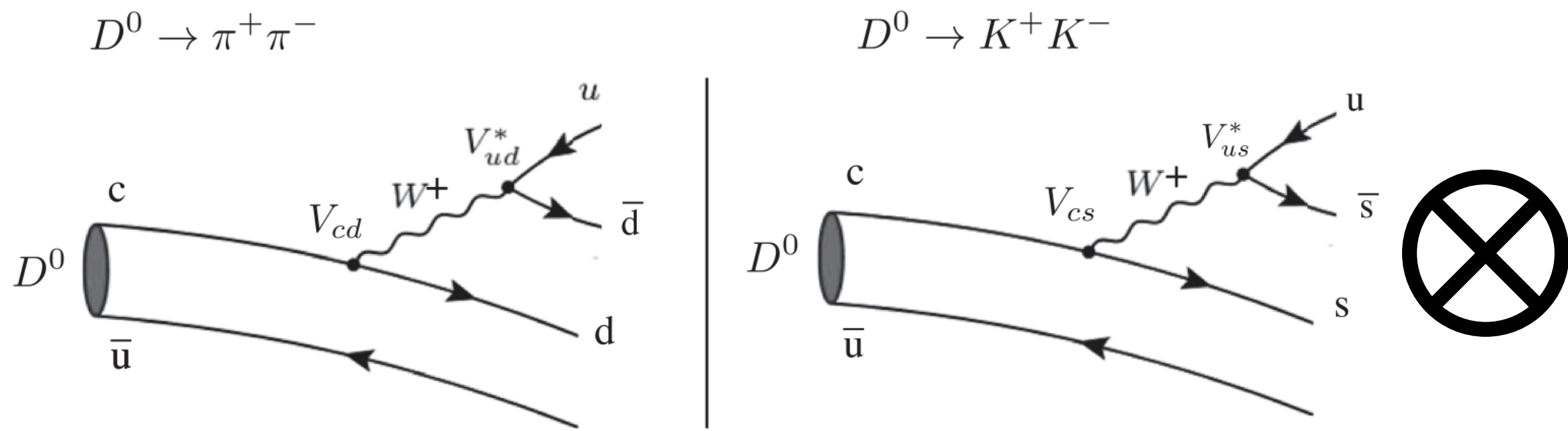


Ann. Rev. Nucl. Part. Sci. 71, 59-85 (2021)

$$a_{CP}(f; t) \equiv \frac{\Gamma(D^0(t) \rightarrow f) - \Gamma(\bar{D}^0(t) \rightarrow f)}{\Gamma(D^0(t) \rightarrow f) + \Gamma(\bar{D}^0(t) \rightarrow f)} \approx a_f^{\text{dir}} + \frac{t}{\tau_{D^0}} \Delta Y_f$$

$$|\Delta a_{CP}^{SD}| \leq 2.6 \times 10^{-4}$$

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$$\Delta a_{CP}^{\text{dir}} = a_{K^+K^-}^{\text{dir}} - a_{\pi^+\pi^-}^{\text{dir}} = (-1.57 \pm 0.29) \times 10^{-3}$$

Phys. Rev. Lett. 122, 211803 (2019)

$$a_{K^+K^-}^{\text{dir}} = (7.7 \pm 5.7) \times 10^{-4}, \quad a_{\pi^+\pi^-}^{\text{dir}} = (23.2 \pm 6.1) \times 10^{-4}.$$

Phys. Rev. Lett. 131, 091802 (2023)

- Backup slide

$$\begin{aligned}
 & g_{n\Sigma^- K^-}^- : g_{pN\pi^-}^- : g_{p\Lambda K^-}^- : g_{\Sigma^- \Lambda \pi^+}^- : g_{\Sigma^- \Sigma^0 \pi^+}^- : g_{\Lambda \Sigma^0 \pi^0}^- \\
 & = 1 : g_s^- : \frac{1}{\sqrt{6}} (1 - 2g_s^-) : \frac{1}{\sqrt{6}} (1 + g_s^-) : \frac{1}{\sqrt{2}} (g_s^- - 1) : \frac{1}{\sqrt{6}} (1 + g_s^-).
 \end{aligned}$$

$$\begin{aligned}
 & \Gamma_{N(1535)}^{N\pi} : \Gamma_{\Sigma(1620)}^{\Lambda\pi} : \Gamma_{\Sigma(1620)}^{\Sigma\pi} : \Gamma_{\Sigma(1620)}^{N\bar{K}} : \Gamma_{\Lambda(1670)}^{N\bar{K}} : \Gamma_{\Lambda(1670)}^{\Sigma\pi} \\
 & = 44.1 \pm 14.8 : 3.51 \pm 1.53 : 6.63 \pm 2.70 : 13.7 \pm 10.5 : 8.0 \pm 1.9 : 12.8 \pm 5.1,
 \end{aligned}$$

- Pole model + Rescattering — Penguin / Tree

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} \left[\sum_{qq'} V_{qc}^* V_{q'u} \left(C_+ O_+^{qq'} + C_- O_-^{qq'} \right) - \lambda_b \sum_{i=3\sim 6} C_i O_i \right] \quad \langle \mathbf{BP} | \mathcal{H}_{\text{eff}} | \mathbf{B}_c \rangle = i\bar{u} (F - G\gamma_5) u_c$$

$$O_{\pm}^{qq'} = (\bar{u}q')_{V-A} (\bar{q}c)_{V-A} \pm (\bar{q}q')_{V-A} (\bar{u}c)_{V-A} \quad \underbrace{\mathbf{3} \otimes \mathbf{3} \otimes \bar{\mathbf{3}}}_{\mathcal{H}_{\text{eff}}} = \underbrace{(\mathbf{15} \oplus \mathbf{3}_+)}_{O_+} \oplus \underbrace{(\bar{\mathbf{6}} \oplus \mathbf{3}_-)}_{O_-}$$

$$F = \tilde{f}^a (P^\dagger)_l^i \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (\mathbf{B}^\dagger)_k^j + \tilde{f}^b \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (\mathbf{B}^\dagger)_k^l (P^\dagger)_l^j + \tilde{f}^c \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (P^\dagger)_k^l (\mathbf{B}^\dagger)_l^j$$

$$+ \tilde{f}^d \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}^\dagger)_k^i (P^\dagger)_l^j (\mathbf{B}_c)^{kl} + \tilde{f}^e (\mathbf{B}^\dagger)_i^j \mathcal{H}(\mathbf{15})_l^{\{ik\}} (P^\dagger)_k^l (\mathbf{B}_c)_j + \lambda_b F_3, \quad \begin{array}{l} \text{Sensitive to CP-odd} \\ \text{Insensitive to CP-even} \end{array}$$

$$F_3 = \tilde{f}_3^a (\mathbf{B}_c)_j \mathcal{H}(\mathbf{3})^i (\mathbf{B}^\dagger)_i^j (P^\dagger)_k^k + \tilde{f}_3^b (\mathbf{B}_c)_k \mathcal{H}(\mathbf{3})^i (\mathbf{B}^\dagger)_i^j (P^\dagger)_j^k + \tilde{f}_3^c (\mathbf{B}_c)_i \mathcal{H}(\mathbf{3})^i (\mathbf{B}^\dagger)_k^j (P^\dagger)_j^k$$

$$+ \tilde{f}_3^d (\mathbf{B}_c)_j \mathcal{H}(\mathbf{3})^i (\mathbf{B}^\dagger)_k^j (P^\dagger)_i^k,$$

$SU(3)_F$ breaking effects are expected to be much larger than F_3 !

To date, there are in total **30** data points

$$(4 + 1 + 4) \times 2(\text{S- \& P-waves}) \times 2(\text{complex}) - 1 = \mathbf{35}$$

● Pole model + Rescattering — Penguin / Tree

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} \left[\sum_{qq'} V_{qc}^* V_{q'u} \left(C_+ O_+^{qq'} + C_- O_-^{qq'} \right) - \lambda_b \sum_{i=3\sim 6} C_i O_i \right] \quad \langle \mathbf{BP} | \mathcal{H}_{\text{eff}} | \mathbf{B}_c \rangle = i\bar{u} (F - G\gamma_5) u_c$$

$$O_{\pm}^{qq'} = (\bar{u}q')_{V-A} (\bar{q}c)_{V-A} \pm (\bar{q}q')_{V-A} (\bar{u}c)_{V-A} \quad \underbrace{3 \otimes 3 \otimes \bar{3}}_{\mathcal{H}_{\text{eff}}} = \underbrace{(\mathbf{15} \oplus \cancel{\mathbf{3}_+})}_{O_+} \oplus \underbrace{(\bar{\mathbf{6}} \oplus \cancel{\mathbf{3}_-})}_{O_-}$$

$$F = \tilde{f}^a (P^\dagger)_l^i \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (\mathbf{B}^\dagger)_k^j + \tilde{f}^b \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (\mathbf{B}^\dagger)_k^l (P^\dagger)_l^j + \tilde{f}^c \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (P^\dagger)_k^l (\mathbf{B}^\dagger)_l^j \\ + \tilde{f}^d \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}^\dagger)_k^i (P^\dagger)_l^j (\mathbf{B}_c)^{kl} + \tilde{f}^e (\mathbf{B}^\dagger)_i^j \mathcal{H}(\mathbf{15})_l^{\{ik\}} (P^\dagger)_k^l (\mathbf{B}_c)_j + \lambda_b \cancel{\Gamma_3},$$

$$\mathcal{H}(\bar{\mathbf{6}}) = \begin{pmatrix} 0 & 0 & 0 \\ 0 & V_{cs}^* V_{ud} & -\lambda_s - \frac{\lambda_b}{2} \\ 0 & -\lambda_s - \frac{\lambda_b}{2} & V_{cd}^* V_{us} \end{pmatrix} \quad \mathcal{H}(\mathbf{15})_k^{ij} = \left(\begin{pmatrix} \frac{\lambda_b}{2} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}_{ij}, \begin{pmatrix} 0 & -\lambda_s - \frac{3\lambda_b}{4} & V_{cs}^* V_{ud} \\ -\lambda_s - \frac{3\lambda_b}{4} & 0 & 0 \\ V_{cs}^* V_{ud} & 0 & 0 \end{pmatrix}_{ij}, \begin{pmatrix} 0 & V_{cd}^* V_{us} & \lambda_s + \frac{\lambda_b}{4} \\ V_{cd}^* V_{us} & 0 & 0 \\ \lambda_s + \frac{\lambda_b}{4} & 0 & 0 \end{pmatrix}_{ij} \right)_k$$

To date, there are in total **30** data points

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$$(4 + 1 + \cancel{4}) \times 2(\text{S- \& P-waves}) \times 2(\text{complex}) - 1 = \cancel{35}$$

● Pole model + Rescattering — Penguin / Tree

$$F = \tilde{f}^a (P^\dagger)_l^l \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (\mathbf{B}^\dagger)_k^j + \tilde{f}^b \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (\mathbf{B}^\dagger)_k^l (P^\dagger)_l^j + \tilde{f}^c \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}_c)^{ik} (P^\dagger)_k^l (\mathbf{B}^\dagger)_l^j + \tilde{f}^d \mathcal{H}(\bar{\mathbf{6}})_{ij} (\mathbf{B}^\dagger)_k^i (P^\dagger)_l^j (\mathbf{B}_c)^{kl} + \tilde{f}^e (\mathbf{B}^\dagger)_i^j \mathcal{H}(\mathbf{15})_l^{\{ik\}} (P^\dagger)_k^l (\mathbf{B}_c)_j + \lambda_b F_3,$$

$CP \propto \tilde{f}^e, \tilde{g}^e$

$$A_{CP}^{dir} = \frac{\Gamma - \bar{\Gamma}}{\Gamma + \bar{\Gamma}}, \quad \alpha_{CP} = \frac{\alpha + \bar{\alpha}}{2},$$

$$\beta_{CP} = \frac{\beta + \bar{\beta}}{2}, \quad \gamma_{CP} = \frac{\gamma - \bar{\gamma}}{2}.$$

$$f^x = 1.80(35), 0.91(30), 0.96(5), 0.31(31), 0.55(63),$$

$$\delta_f^x = 1.66(31), 0, -2.20(39), -0.57(31), -0.58(50),$$

$$g^x = 6.11(1.67), 7.01(29), 0.69(43), 1.31(39), 1.62(1.34),$$

$$\delta_g^x = -1.77(34), 2.60(0.37), 2.03(0.43), 2.39(0.74), 1.98(1.03)$$

CP-odd quantities $\sim 10^{-4}$

$$a_{D \rightarrow K^+ K^-}^{dir} - a_{D \rightarrow \pi^+ \pi^-}^{dir} = (-1.57 \pm 0.29) \times 10^{-3}$$

Channels	$\mathcal{B}(10^{-3})$	$\alpha_{CP}(10^{-3})$	$\beta_{CP}(10^{-3})$	$\gamma_{CP}(10^{-3})$	$A_{CP}^{dir}(10^{-3})$
$\Lambda_c^+ \rightarrow p\pi^0$	0.16(2)	-0.61(39)	-0.43(48)	0.53(145)	0.01(1)
$\Lambda_c^+ \rightarrow p\eta$	1.45(25)	0.05(17)	0.04(14)	-0.07(22)	-0.03(4)
$\Lambda_c^+ \rightarrow p\eta'$	0.52(11)	-0.02(7)	0.01(4)	0.00(4)	0.00(1)
$\Lambda_c^+ \rightarrow n\pi^+$	0.67(8)	0.12(20)	0.13(26)	-0.28(40)	-0.01(2)
$\Lambda_c^+ \rightarrow \Lambda^0 K^+$	0.63(2)	-0.03(10)	0.03(5)	0.04(24)	0.01(1)
$\Xi_c^+ \rightarrow \Sigma^+ \pi^0$	2.11(14)	0.06(13)	-0.01(13)	-0.09(42)	-0.07(7)
$\Xi_c^+ \rightarrow \Sigma^+ \eta$	0.70(32)	-0.10(22)	0.09(73)	0.29(57)	0.01(4)
$\Xi_c^+ \rightarrow \Sigma^+ \eta'$	1.13(23)	0.03(7)	-0.01(2)	-0.01(4)	-0.01(0)
$\Xi_c^+ \rightarrow \Sigma^0 \pi^+$	3.04(11)	-0.01(6)	-0.01(11)	0.05(21)	0.05(5)
$\Xi_c^+ \rightarrow \Xi^0 K^+$	1.04(13)	0.02(14)	0.13(18)	-0.18(25)	-0.02(2)
$\Xi_c^+ \rightarrow \Lambda^0 \pi^+$	0.32(9)	0.0(19)	0.36(30)	0.20(19)	0.00(1)
$\Xi_c^0 \rightarrow \Sigma^0 \pi^0$	0.34(2)	-0.04(12)	0.25(39)	0.12(12)	0.00(1)
$\Xi_c^0 \rightarrow \Sigma^0 \eta$	0.12(5)	-0.11(22)	0.09(73)	0.29(57)	0.00(1)
$\Xi_c^0 \rightarrow \Sigma^0 \eta'$	0.19(4)	0.03(7)	-0.01(2)	-0.01(4)	0.00(1)
$\Xi_c^0 \rightarrow \Sigma^- \pi^+$	1.83(6)	0.02(7)	-0.09(21)	0.03(12)	0.02(3)
$\Xi_c^0 \rightarrow \Xi^- K^+$	1.12(3)	0.02(5)	-0.08(16)	0.02(11)	0.01(1)
$\Xi_c^0 \rightarrow \Lambda^0 \pi^0$	0.09(1)	0.07(20)	-0.27(25)	-0.15(17)	0.00(1)
$\Xi_c^0 \rightarrow \Lambda^0 \eta$	0.43(11)	0.06(12)	0.11(14)	-0.01(2)	-0.01(1)
$\Xi_c^0 \rightarrow \Lambda^0 \eta'$	0.68(13)	0.00(1)	0.00(1)	0.00(1)	0.00(1)

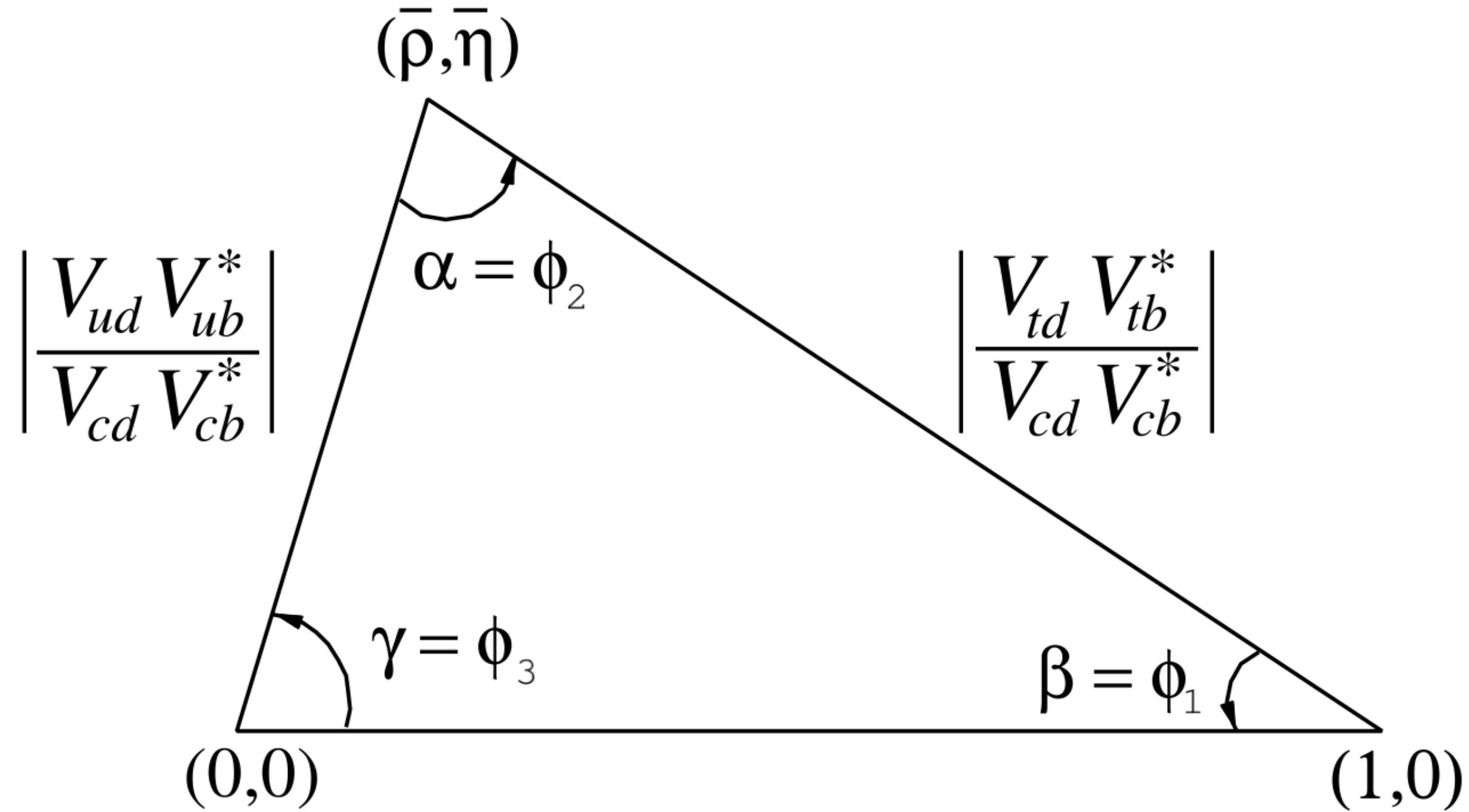


Figure 11.1: Sketch of the unitarity triangle.

The CKM matrix elements are fundamental parameters of the SM, so their precise determination is important. The unitarity of the CKM matrix imposes $\sum_i V_{ij} V_{ik}^* = \delta_{jk}$ and $\sum_j V_{ij} V_{kj}^* = \delta_{ik}$. The six vanishing combinations can be represented as triangles in a complex plane, of which the ones obtained by taking scalar products of neighboring rows or columns are nearly degenerate. The areas of all triangles are the same, half of the Jarlskog invariant, J [7], which is a phase-convention independent measure of CP violation, $\text{Im}[V_{ij} V_{kl} V_{il}^* V_{kj}^*] = J \sum_{m,n} \epsilon_{ikm} \epsilon_{jln}$.