



BESIII



全国第二十二届重味物理和CP破坏研讨会

Research on inclusive decay at BESIII

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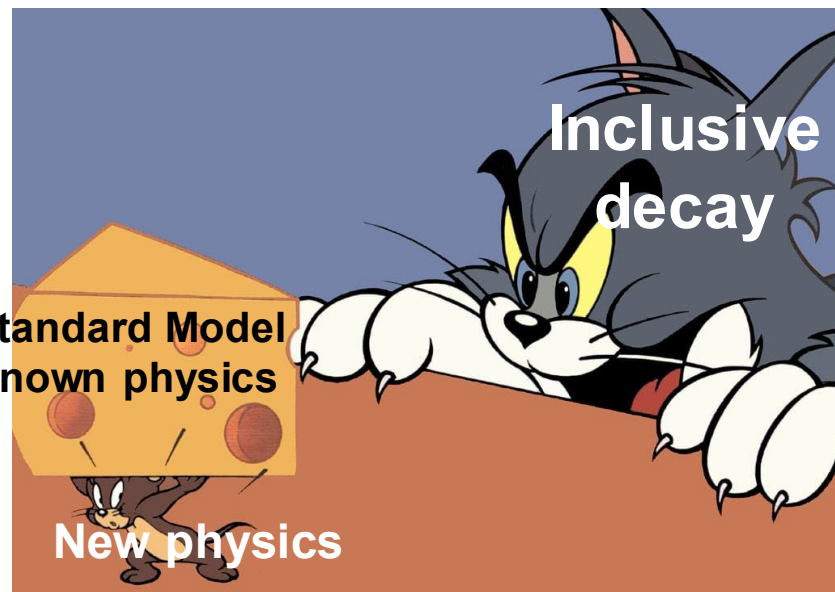
Lanzhou University (兰州大学)

(On behalf of the BESIII Collaboration)

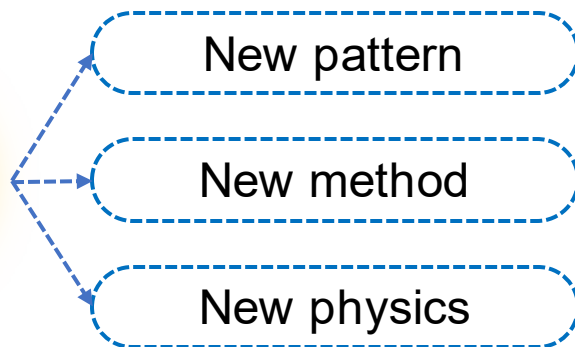
2023.12.17

- Introduction to inclusive decay
- Methods for inclusive decay
- Inclusive decays at BESIII
- Summary & prospect

• Why study inclusive decay?



Inclusive decay



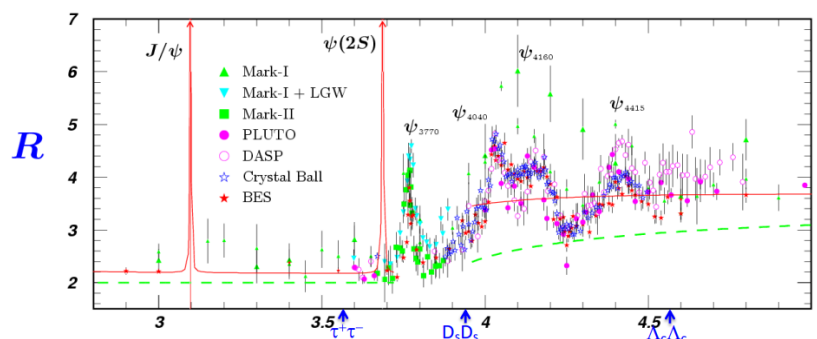
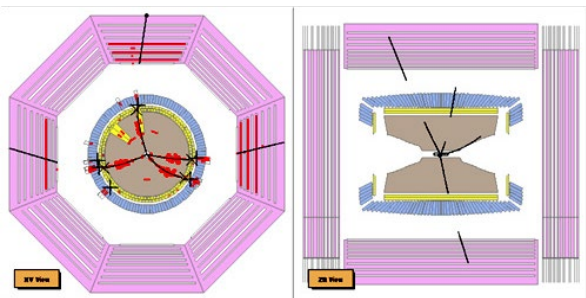
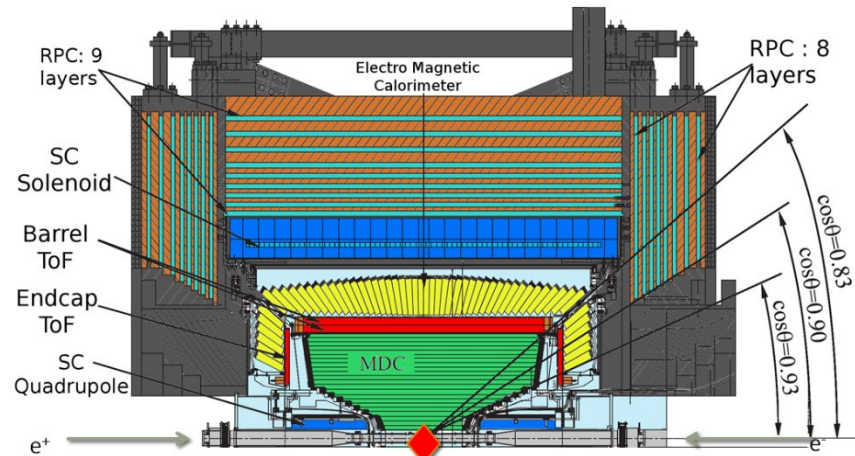
Increasing attention on inclusive decay!

Growing numbers of experimental research, but less theoretical.

- BEPCII



BESIII



First HEP collider in China (1988)
 c.m.s energy: 2 ~ 5 GeV
 Max luminosity: $1 \times 10^{33} \text{cm}^{-2}\text{s}^{-1}$

Non-perturbative
 $\tau - \text{charm}$ region
 τ^\pm , D/D_S , Λ_c^+ ...

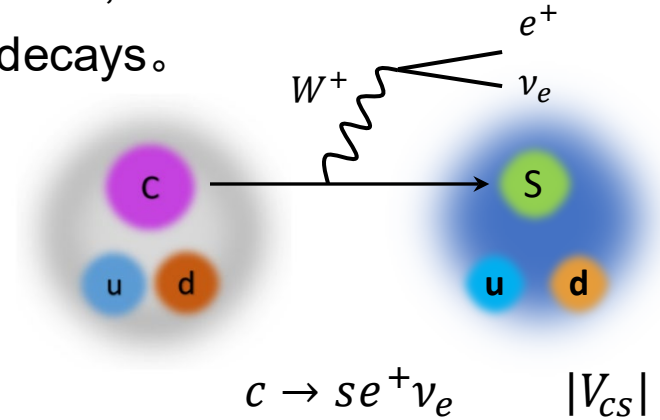
J/ψ : $2.97 \text{fb}^{-1}(10\text{B})$
 $\psi(3686)$: $4.07 \text{fb}^{-1}(2.7\text{B})$
 $\psi(3770)$: 20fb^{-1}
 $4.6 \sim 4.95 \text{GeV}$: 6.4fb^{-1}

- Inclusive decay:**

- Decay as $A \rightarrow B + X$, B is a certain particle, X contains any possible particles, then this decay is called an inclusive decay of particle A ;
- Inclusive decay is the sum of a series of exclusive decays.

- Motivation:**

- Provide verifications for SM parameters;
- Guide for undiscovered exclusive decays;
- Study the characteristics of a series of decays.



- Research objects:**

- BF;
- Decay parameter;
- CPV
- ...

$$\Lambda_c^+ \rightarrow \Lambda X_{(exclusive)} \approx (30.1 \pm 1.2)\%$$

$$\Lambda_c^+ \rightarrow \Lambda X_{(inclusive)} = (38.2 \pm 2.6)\%$$

$$\frac{\mathfrak{B}(\Lambda_c^+ \rightarrow \Lambda X)_{exclusive}}{\mathfrak{B}(\Lambda_c^+ \rightarrow \Lambda X)_{inclusive}} = (78.8 \pm 6.3)\%$$

=> Any other decay modes?

• D^+ :

▼ Inclusive modes			
Γ_1	e^+ semileptonic	CLEO,2010	$(16.07 \pm 0.30)\%$
Γ_2	μ^+ anything	BES2,2008	$(17.6 \pm 3.2)\%$
Γ_3	K^- anything	BES2,2007	$(25.7 \pm 1.4)\%$
Γ_4	\bar{K}^0 anything + K^0 anything	BES3,2023	$(61 \pm 5)\%$
Γ_5	K^+ anything	BES2,2007	$(5.9 \pm 0.8)\%$
Γ_6	$K^*(892)^-$ anything	BES2,2006	$(6 \pm 5)\%$
Γ_7	$\bar{K}^*(892)^0$ anything	BES,2005	$(23 \pm 5)\%$
Γ_8	$K^*(892)^0$ anything	BES,2005	$< 6.6\%$
Γ_9	η anything	CLEO,2006	$(6.3 \pm 0.7)\%$
Γ_{10}	η' anything	CLEO,2006	$(1.04 \pm 0.18)\%$
Γ_{11}	ϕ anything	BES3,2019	$(1.12 \pm 0.04)\%$

D^0 :

▼ Inclusive modes			
Γ_5	e^+ anything	CLEO,2010	[4] $(6.49 \pm 0.11)\%$
Γ_6	μ^+ anything	BES2,2008	$(6.8 \pm 0.6)\%$
Γ_7	K^- anything	BES2,2007	$(54.7 \pm 2.8)\%$
Γ_8	\bar{K}^0 anything + K^0 anything	BES3,2023	$(47 \pm 4)\%$
Γ_9	K^+ anything	BES2,2007	$(3.4 \pm 0.4)\%$
Γ_{10}	$K^*(892)^-$ anything	BES2,2006	$(15 \pm 9)\%$
Γ_{11}	$\bar{K}^*(892)^0$ anything	BES,2005	$(9 \pm 4)\%$
Γ_{12}	$K^*(892)^+$ anything	BES2,2006	$< 3.6\%$
Γ_{13}	$K^*(892)^0$ anything	BES,2005	$(2.8 \pm 1.3)\%$
Γ_{14}	η anything	CLEO,2006	$(9.5 \pm 0.9)\%$
Γ_{15}	η' anything	CLEO,2006	$(2.48 \pm 0.27)\%$
Γ_{16}	ϕ anything	BES3,2019	$(1.08 \pm 0.04)\%$

• Λ_c^+ :

▼ Inclusive modes			
Γ_{76}	e^+ anything	$(3.95 \pm 0.35)\%$	→ BESIII, PRL
Γ_{77}	p anything	$(50 \pm 16)\%$	→ BESIII, on-going
Γ_{78}	n anything	$(50 \pm 16)\%$	→ BESIII, PRD
Γ_{79}	Λ anything	$(38.2^{+2.9}_{-2.4})\%$	→ BESIII, PRL
Γ_{80}	K_S^0 anything	$(9.9 \pm 0.7)\%$	→ BESIII, EPJC
Γ_{81}	3prongs	$(24 \pm 8)\%$	

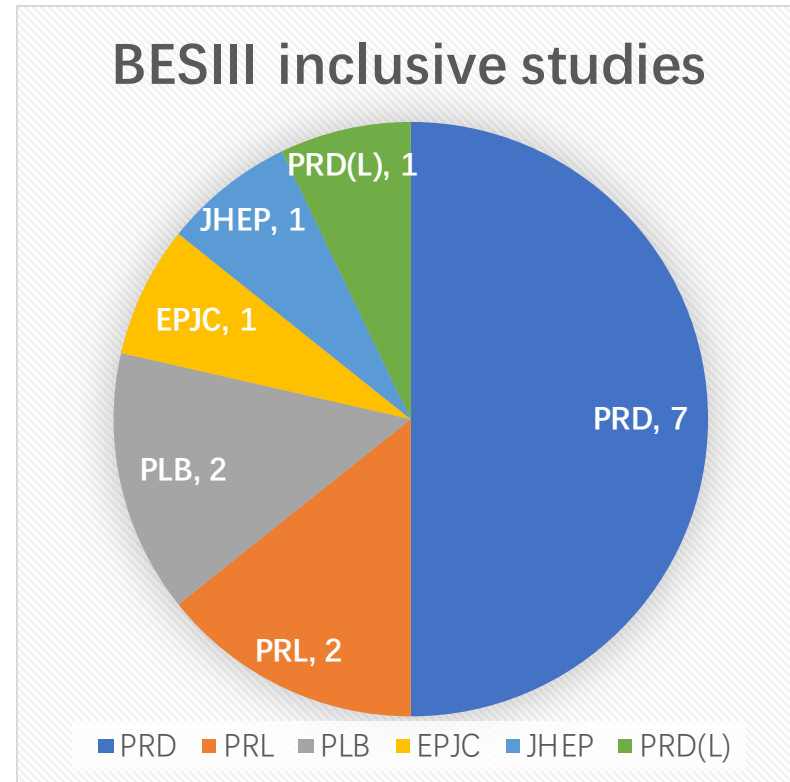
• D_s^+ :

Inclusive modes			
Γ_1	e^+ semileptonic	BES3,2021	[1] $(6.33 \pm 0.15)\%$
Γ_2	π^+ anything	CLEO,2009	$(119.3 \pm 1.4)\%$
Γ_3	π^- anything	CLEO,2009	$(43.2 \pm 0.9)\%$
Γ_4	π^0 anything	CLEO,2009	$(123 \pm 7)\%$
Γ_5	K^- anything	CLEO,2009	$(18.7 \pm 0.5)\%$
Γ_6	K^+ anything	CLEO,2009	$(28.9 \pm 0.7)\%$
Γ_7	K_S^0 anything	CLEO,2009	$(19.0 \pm 1.1)\%$
Γ_8	η anything	CLEO,2009	[2] $(29.9 \pm 2.8)\%$
Γ_9	ω anything	CLEO,2009	$(6.1 \pm 1.4)\%$
Γ_{10}	η' anything	BES3,2015	[3] $(10.3 \pm 1.4)\%$
Γ_{11}	$f_0(980)$ anything, $f_0 \rightarrow \pi^+\pi^-$	CLEO,2009	$< 1.3\%$
Γ_{12}	ϕ anything	CLEO,2009	$(15.7 \pm 1.0)\%$
Γ_{13}	K^+K^- anything	CLEO,2009	$(15.8 \pm 0.7)\%$
Γ_{14}	$K_S^0 K^+$ anything	CLEO,2009	$(5.8 \pm 0.5)\%$
Γ_{15}	$K_S^0 K^-$ anything	CLEO,2009	$(1.9 \pm 0.4)\%$
Γ_{16}	$2 K_S^0$ anything	CLEO,2009	$(1.70 \pm 0.32)\%$
Γ_{17}	$2 K^+$ anything	CLEO,2009	$< 2.6 \times 10^{-3}$
Γ_{18}	$2 K^-$ anything	CLEO,2009	$< 6 \times 10^{-4}$

J/ψ : none

ψ' : $K_S^0 X$ (BES3, 2021)

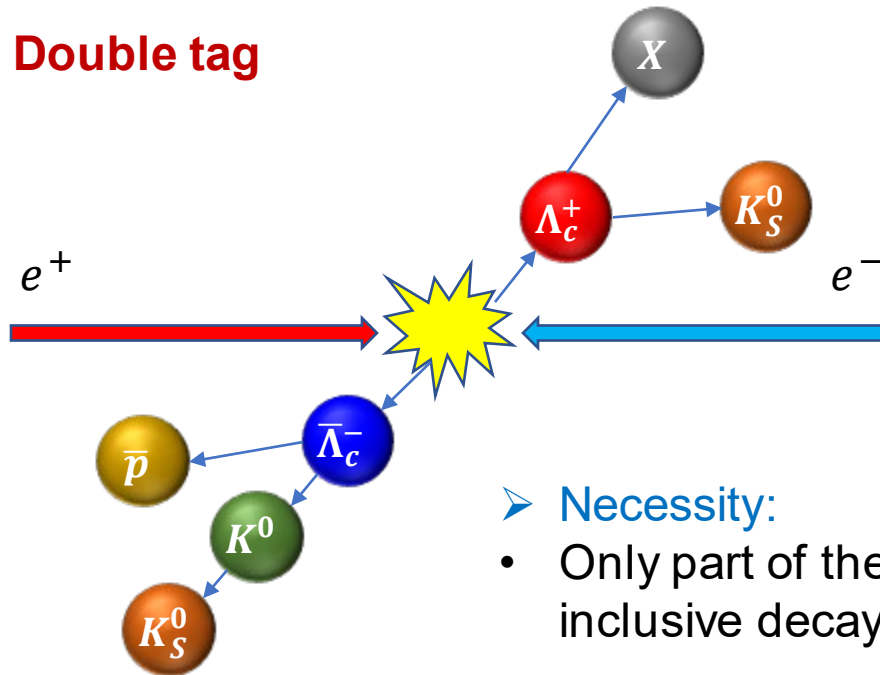
PDG not record yet



	D^0/D^+	D_s^+	Λ_c^+	Others (J/ψ , ψ' , hyperon)
Single charged track		$Xe^+\nu_e$	$Xe^+\nu_e(2)$	
Multi charged tracks	$\pi^+\pi^+\pi^-X$	$\pi^+\pi^+\pi^-X$		
Long lived inter-particle	K_S^0X		ΛX , K_S^0X	$\psi(3686) \rightarrow K_S^0X$
Short lived inter-particle	ϕX	$\eta'X$		$\Sigma^- \rightarrow \Sigma^+X$
Neutron			$\bar{\Lambda}_c^- \rightarrow \bar{n}X$	

Will be introduced in this report.

• Double tag



➤ Necessity:

- Only part of the final states are reconstructed in inclusive decay, single-tag(ST) is not executable.

➤ Reasonability:

- The Λ_c are produced in pairs at threshold on BESIII, no other accompanied particles, 4-momentum conservation.

➤ Advantage:

- Absolute BF, decay parameter, CPV;
- Less background than ST;
- Cancel out some systematic uncertainties.

- **Data driven** Using control sample from data to determine the efficiency of inclusive decay.

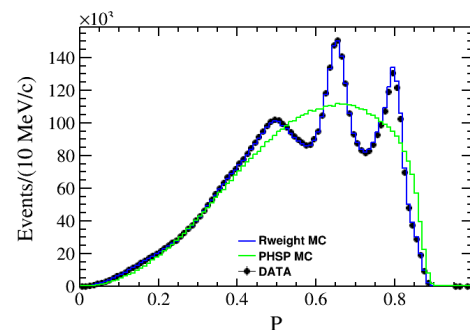
➤ **Necessity:**

- The inclusive decay contains multiple exclusive decays, of which the phase space is complicated.
- There are still undiscovered exclusive decays.
- The efficiency in different phase space may vary greatly.

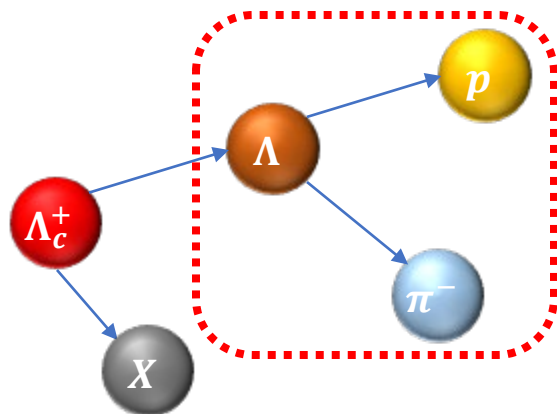
➤ **Reasonability:**

- The detector doesn't matter the history of particles.

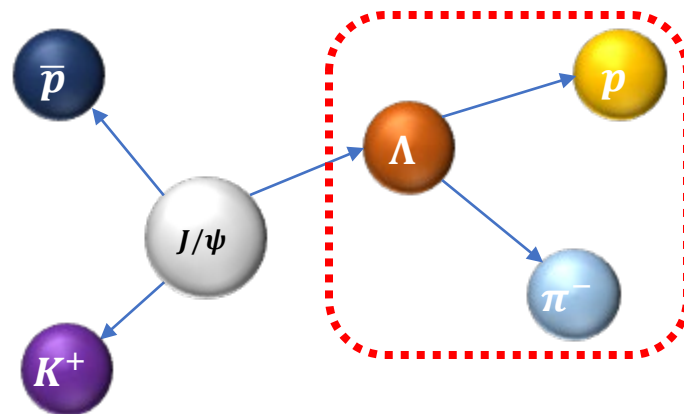
MC can not simulate the real data well.



Signal sample

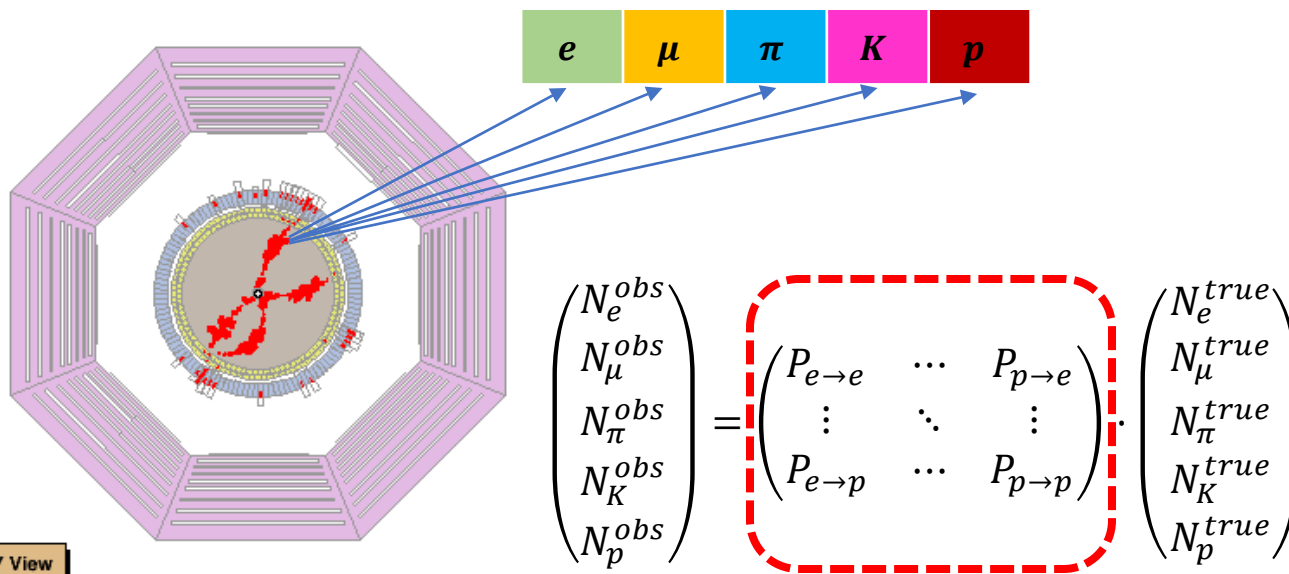


Control sample



• **Unfolding**

Apply for single charged particles (e, μ, π, K, p)



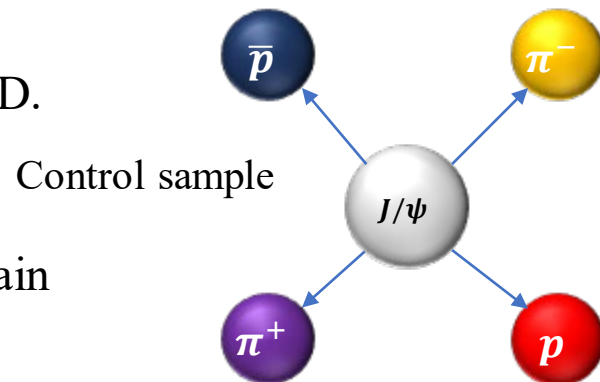
XY View

➤ **Necessity:**

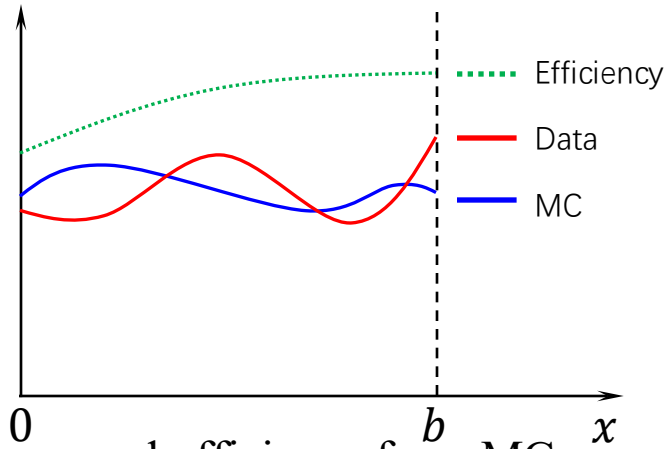
- The stable charged particle can only be confirmed by PID.
- Loss and mistakes in PID.

➤ **Difficulties:**

- Study control samples of 5 particles (e, μ, π, K, p) to obtain 5x5 elements of PID matrix;
- Unfolding in each phase space point.



- **Reweight**



Suppose that a variable x distribute differently in MC and data: $\rho_{MC}(x)$ $\rho_{data}(x)$

Problem:

How much of the difference of yields between using the efficiency from MC N'_{data} and real data N_{data} ?

- Averaged efficiency from MC:

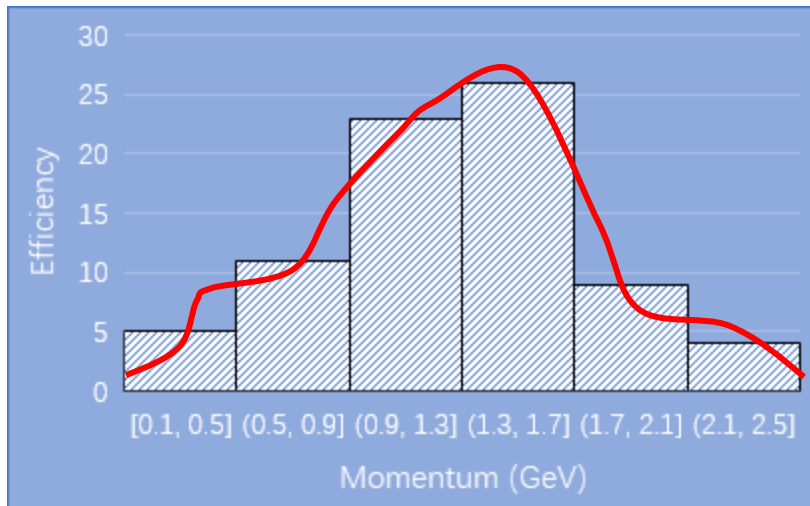
- $$\overline{\varepsilon_{MC}} = \frac{n_{MC}}{N_{MC}} = \frac{\int_b N_{MC}(x)\varepsilon_{MC}(x)dx}{\int_b N_{MC}(x)dx} = \int_b \rho_{MC}(x)\varepsilon_{MC}(x)dx, \quad \rho_{MC}(x) = \frac{N_{MC}(x)}{\int_b N_{MC}(x)dx}$$

- Using averaged efficiency from MC to obtained the yields:

- $$N'_{data} = \frac{n_{data}}{\overline{\varepsilon_{MC}}} = \frac{\int_b N_{data}(x)\varepsilon_{data}(x)dx}{\int_b \rho_{MC}(x)\varepsilon_{MC}(x)dx} = N_{data} \left[\frac{\int_b \rho_{data}(x)\varepsilon_{data}(x)dx}{\int_b \rho_{MC}(x)\varepsilon_{MC}(x)dx} \right] \rho_{data}(x) = \frac{N_{data}(x)}{\int_b N_{data}(x)dx}$$

- Dynamic binning

The efficiency varies greatly in phase space.



$$\bar{\varepsilon} = \frac{\sum_{b_i} n_{b_i}}{\sum_{b_i} N_{b_i}}, \quad \varepsilon_{b_i} = \frac{n_{b_i}}{N_{b_i}}$$

The averaged efficiency is influenced by the phase space distribution. If the efficiency varies largely, the binning scheme will bring sizable bias.

Loose binning => systematic uncertainty

Tight binning => statistical uncertainty.

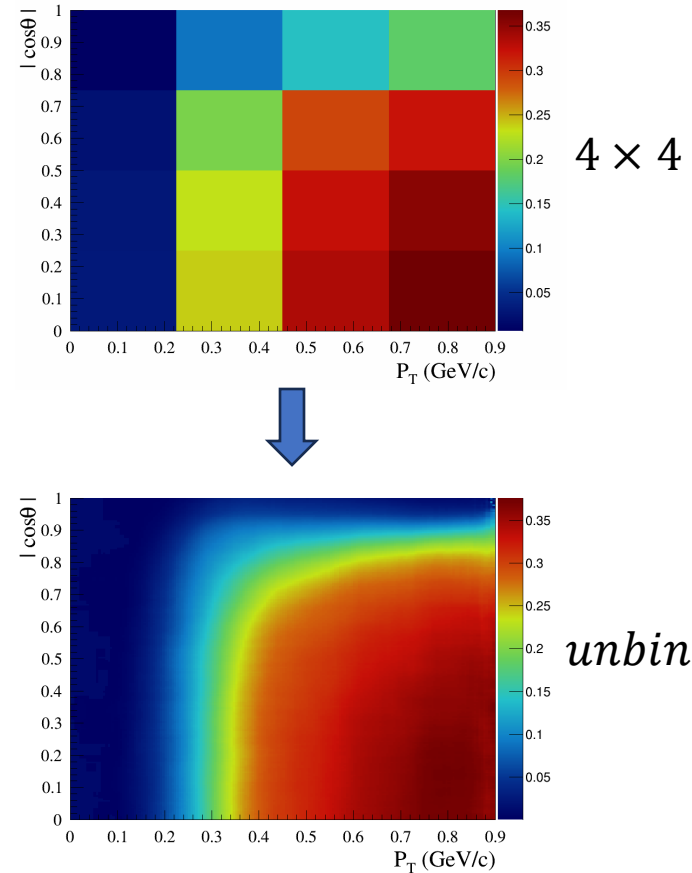
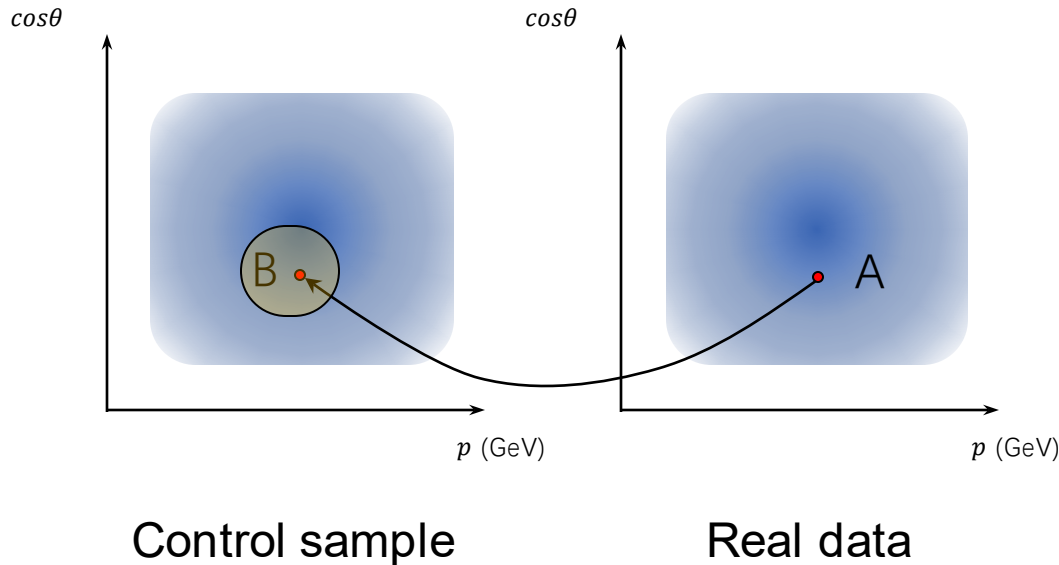
➤ Necessity:

- Efficiency varies with the phase space distribution, MC differs with data;
- The binning scheme will influence the uncertainty.

➤ Difficulties:

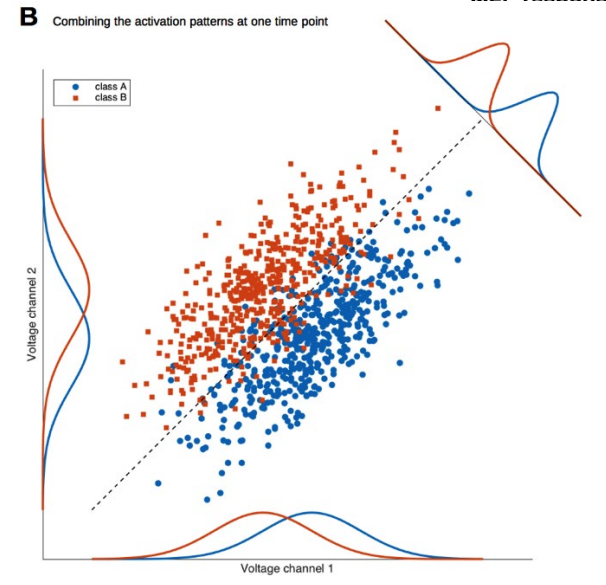
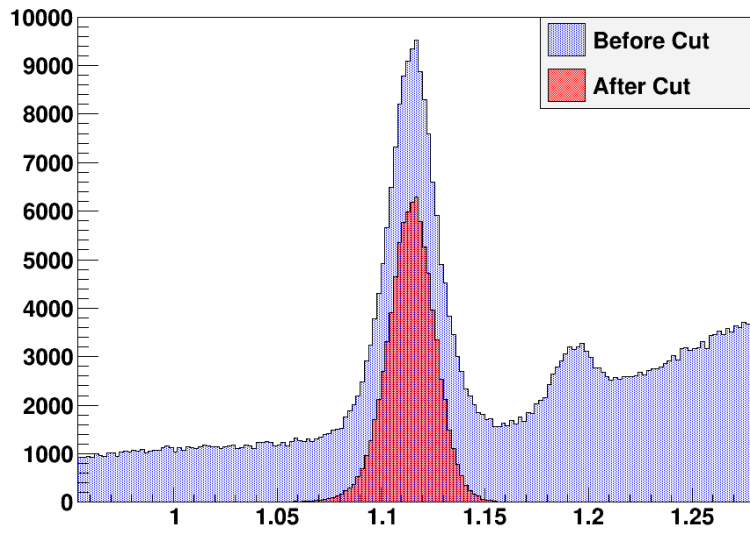
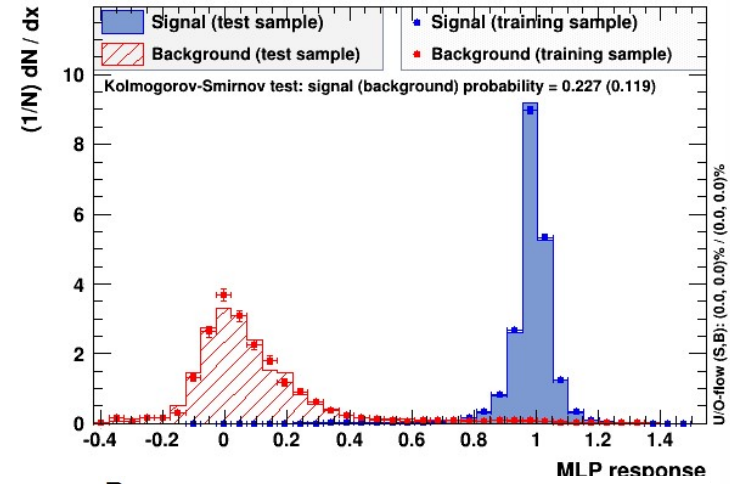
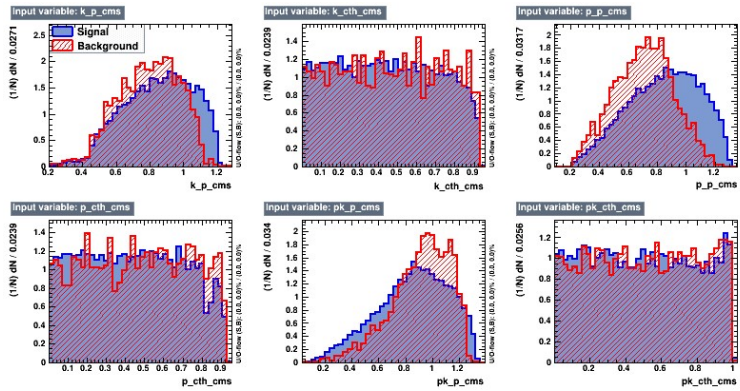
- Reduce the sys. & sta. uncertainties simultaneously.

- Dynamic binning



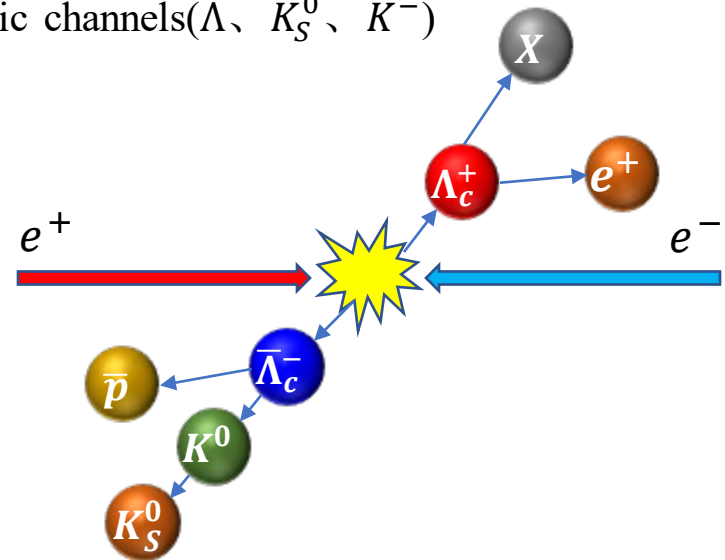
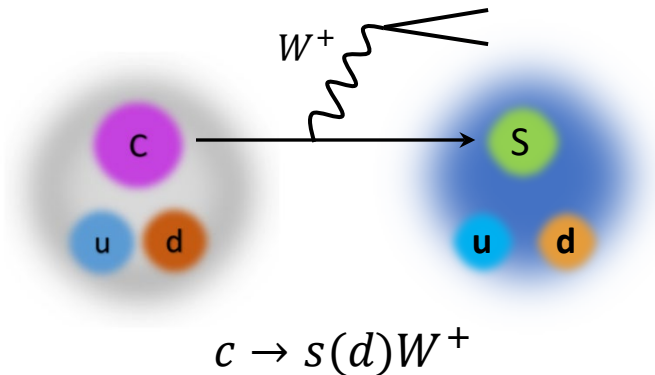
- For a certain point **A** in the phase space of real data, we can look for its corresponding point **B** in the control sample, then calculate the efficiency using the neighborhood region of **B**. The systematic and statistic uncertainty can be balanced by varying the size of neighborhood of **B**.

• Multivariate Analysis



- $\Lambda_c^+ \rightarrow X e^+ \nu_e$: [Phys. Rev. Lett. 121 251801](#) X.Z. H, et al. BESIII 2018
[Phys. Rev. D 107 052005](#) Lei Li, et al. BESIII 2023

In HQET, the u 、 d plays as passive quarks, the decay of Λ_c^+ is dominated by $c \rightarrow s$ transition, including are semi-leptonic channels ($e^+ \nu_e$ or $\mu^+ \nu_e$) and non-leptonic channels (Λ 、 K_S^0 、 K^-)



Example: $\Gamma(\Lambda_c^+ \rightarrow X e^+ \nu_e) / \Gamma(D^+ \rightarrow X e^+ \nu_e)$, theories provide different predictions, effective-quark predicts it to be 1.67, heavy-quark expansion predicts it to be 1.2. Precise measurement can distinguish different theories.

• PID Unfolding:

$$\begin{pmatrix} n_e^{obs} \\ n_\mu^{obs} \\ n_\pi^{obs} \\ n_K^{obs} \\ n_p^{obs} \end{pmatrix} = \begin{pmatrix} \epsilon_{e \rightarrow e} & \epsilon_{\mu \rightarrow e} & \epsilon_{\pi \rightarrow e} & \epsilon_{K \rightarrow e} & \epsilon_{p \rightarrow e} \\ \epsilon_{e \rightarrow \mu} & \epsilon_{\mu \rightarrow \mu} & \epsilon_{\pi \rightarrow \mu} & \epsilon_{K \rightarrow \mu} & \epsilon_{p \rightarrow \mu} \\ \epsilon_{e \rightarrow \pi} & \epsilon_{\mu \rightarrow \pi} & \epsilon_{\pi \rightarrow \pi} & \epsilon_{K \rightarrow \pi} & \epsilon_{p \rightarrow \pi} \\ \epsilon_{e \rightarrow K} & \epsilon_{\mu \rightarrow K} & \epsilon_{\pi \rightarrow K} & \epsilon_{K \rightarrow K} & \epsilon_{p \rightarrow K} \\ \epsilon_{e \rightarrow p} & \epsilon_{\mu \rightarrow p} & \epsilon_{\pi \rightarrow p} & \epsilon_{K \rightarrow p} & \epsilon_{p \rightarrow p} \end{pmatrix} \cdot \begin{pmatrix} N_e^{truth} \\ N_\mu^{truth} \\ N_\pi^{truth} \\ N_K^{truth} \\ N_p^{truth} \end{pmatrix}$$



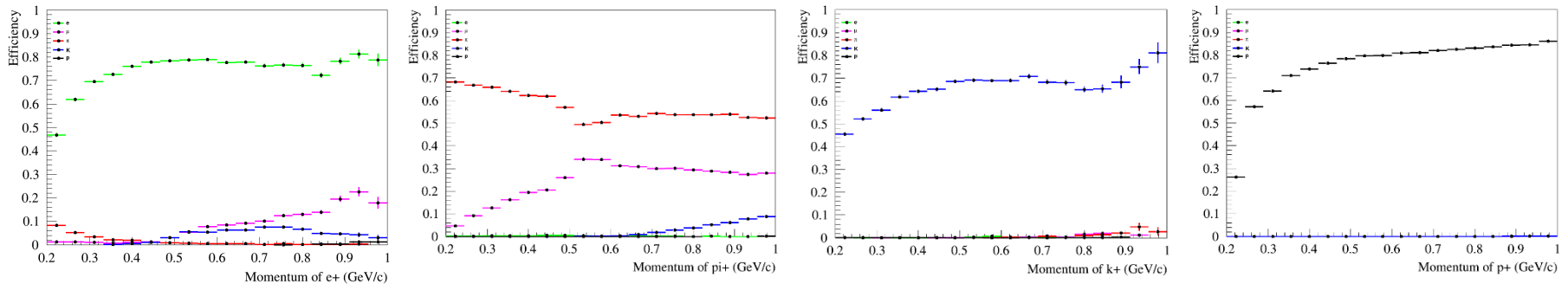
Basic idea: matrix inversion to estimate the number of each kind of particle.

• **Control sample:**

Pure control sample is essential for PID unfolding:

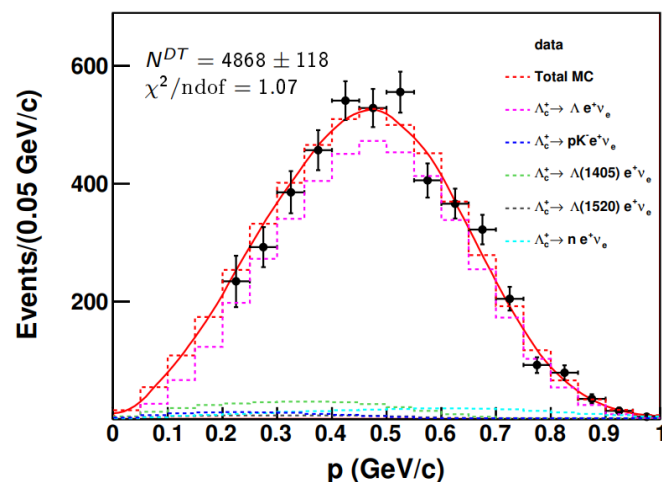
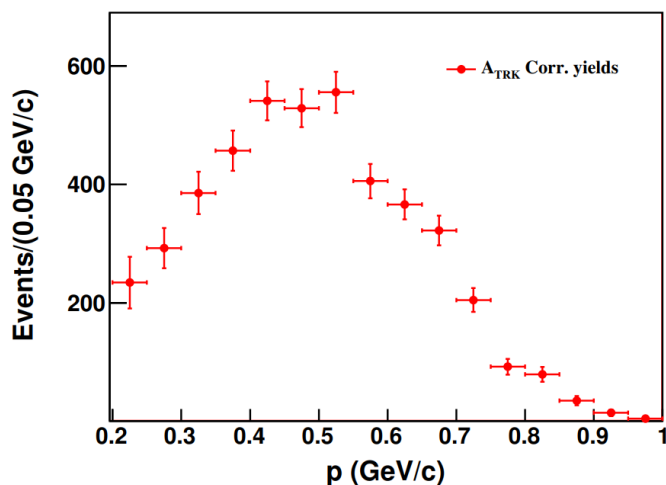
- ▶ e^\pm : $e^+e^- \rightarrow \gamma e^+e^-$;
- ▶ π^\pm : $J/\psi \rightarrow K^+K^-\pi^+\pi^-(\pi^0)$ and $J/\psi \rightarrow p\bar{p}\pi^+\pi^-(\pi^0)$;
- ▶ K^\pm : $J/\psi \rightarrow K^+K^-\pi^+\pi^-(\pi^0)$ and $J/\psi \rightarrow K^+K^-K^+K^-(\pi^0)$.
- ▶ $p(\bar{p})$: $J/\psi \rightarrow p\bar{p}\pi^+\pi^-(\pi^0)$.

Then calculate the efficiency for each track identified as a certain particle.



• **Inverse & extension:**

By solving the matrix equation, the yield of $\Lambda_c^+ \rightarrow X e^+ \nu_e$ can be obtained.



The electron with momentum below 0.2 GeV can not be detected by the spectrometer, the efficiency is extremely low. Extension to the whole region is essential to obtain the total yield.

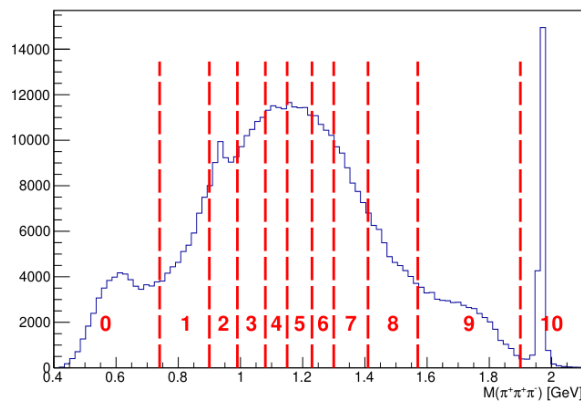
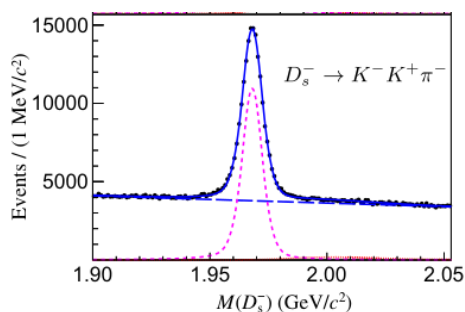
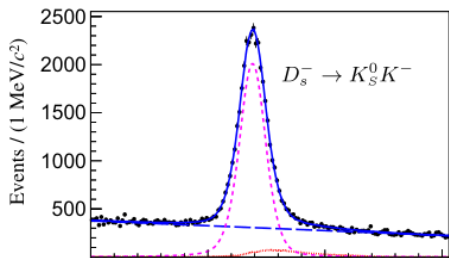
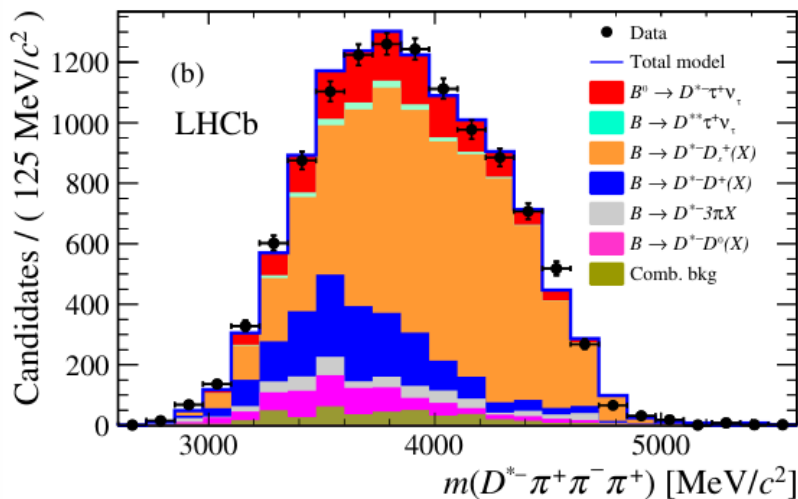
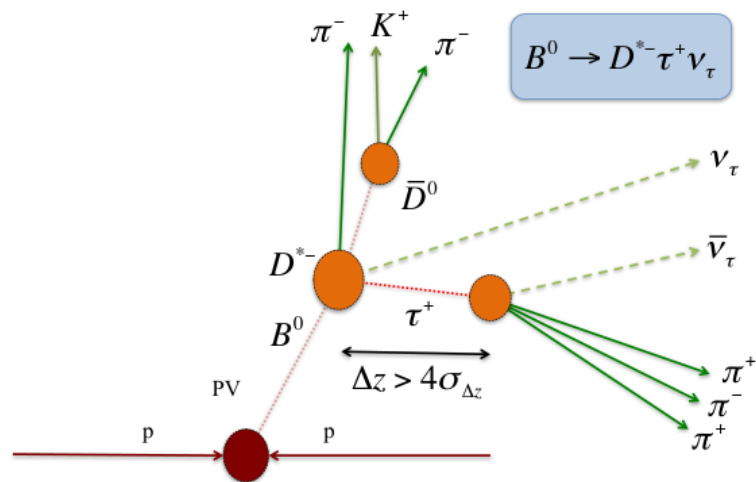
Latest result from BESIII is $\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e) = (4.06 \pm 0.10 \pm 0.09)\%$, the ratio with $D^+ \rightarrow X e^+ \nu_e$ is 1.28 ± 0.05 .

Effective-quark theory: 1.67
Heavy-quark expansion theory: 1.2

[[Phys. Rev. D 107, 052005](https://arxiv.org/abs/1708.02505)]

- $D_s^+ \rightarrow \pi^+ \pi^+ \pi^- X$: [Phys. Rev. D 108 032001](#) H.Cai, L.Y. Dong, L. Sun, et al. BESIII 2023

Estimate the leading background in $B^0 \rightarrow D^{*-} \tau^+ \nu_\tau, \tau^+ \rightarrow \pi^+ \pi^+ \pi^- \nu_\tau$ (test LFU).

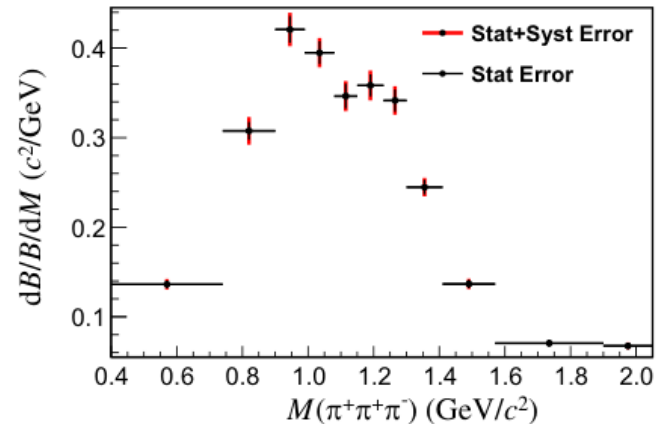


• $D_S^+ \rightarrow \pi^+ \pi^+ \pi^- X$:

$M(\pi^+ \pi^+ \pi^-)$ interval	1	2	3	4	5	6
Raw yield	2300.8 ± 71.1	2883.4 ± 85.8	2405.7 ± 77.6	2630.0 ± 81.3	1944.3 ± 70.6	2276.2 ± 74.3
K_S^0 contribution	59.1 ± 1.3	148.2 ± 2.1	115.0 ± 1.8	93.6 ± 1.7	47.7 ± 1.2	48.4 ± 1.2
MisID contribution	190.1 ± 2.4	297.3 ± 3.0	214.6 ± 2.5	226.6 ± 2.6	164.3 ± 2.2	171.8 ± 2.2
Total background	249.2 ± 2.7	445.5 ± 3.6	329.6 ± 3.1	320.2 ± 3.1	212.0 ± 2.5	220.2 ± 2.5
Background subtracted yield	2051.6 ± 71.1	2437.9 ± 85.9	2076.1 ± 77.7	2309.8 ± 81.4	1732.2 ± 70.7	2056.0 ± 74.4
$M(\pi^+ \pi^+ \pi^-)$ interval	7	8	9	10	11	
Raw yield	1924.3 ± 65.2	2182.5 ± 68.8	1926.0 ± 65.5	1993.0 ± 63.7	767.7 ± 34.0	
K_S^0 contribution	31.1 ± 1.0	36.9 ± 1.0	31.1 ± 1.0	10.7 ± 0.6	1.4 ± 0.2	
MisID contribution	127.5 ± 1.9	169.0 ± 2.2	168.3 ± 2.2	126.3 ± 1.9	3.9 ± 0.3	
Total background	158.7 ± 2.2	205.9 ± 2.5	199.4 ± 2.4	137.0 ± 2.0	5.3 ± 0.4	
Background subtracted yield	1765.6 ± 65.2	1976.6 ± 68.8	1726.6 ± 65.5	1856.0 ± 63.7	762.4 ± 34.0	

Results:

$$B(D_S^+ \rightarrow \pi^+ \pi^+ \pi^- X) = (32.81 \pm 0.35_{\text{stat}} \pm 0.63_{\text{syst}})\%$$



• $\Lambda_c^+ \rightarrow \Lambda X$:

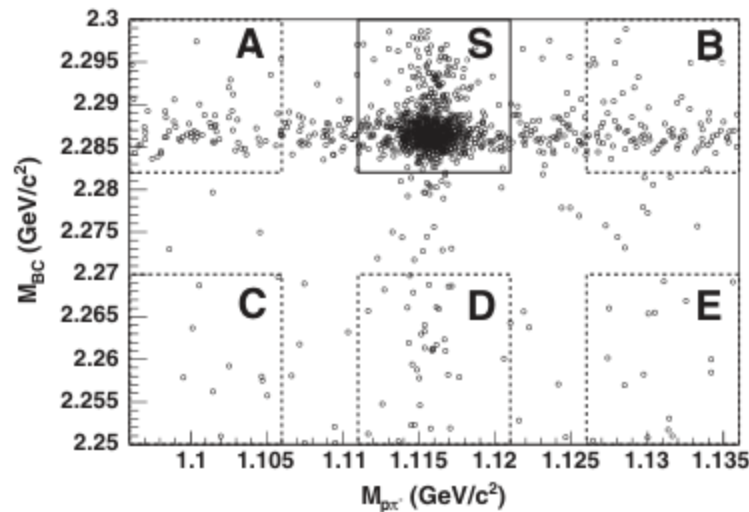
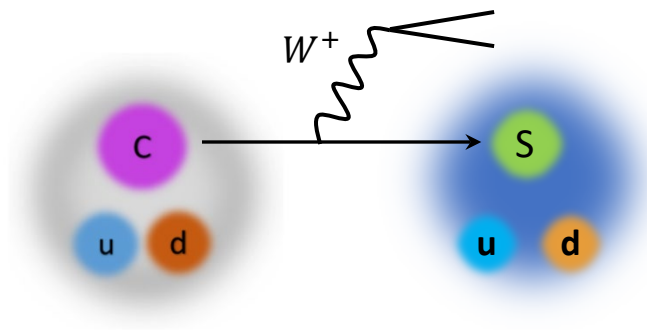
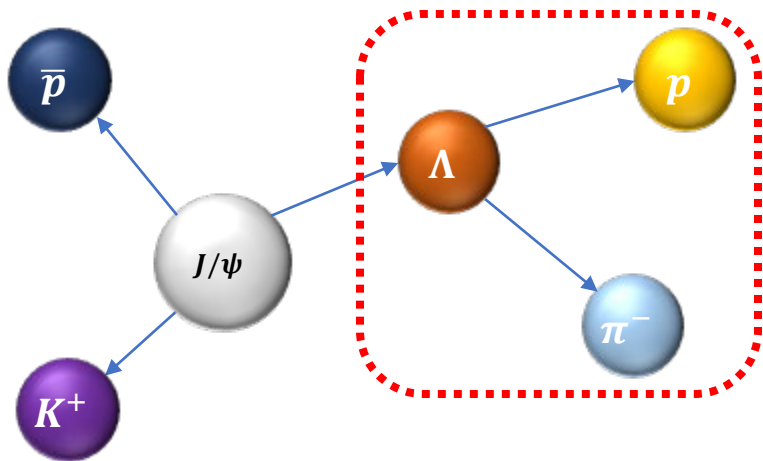
[Phys. Rev. Lett. 121 062003](#)

D. Xiao, et al. BESIII 2018

Sum of all exclusive: $(30.1 \pm 1.2)\%$.

Challenge: efficiency of Λ reconstruction.

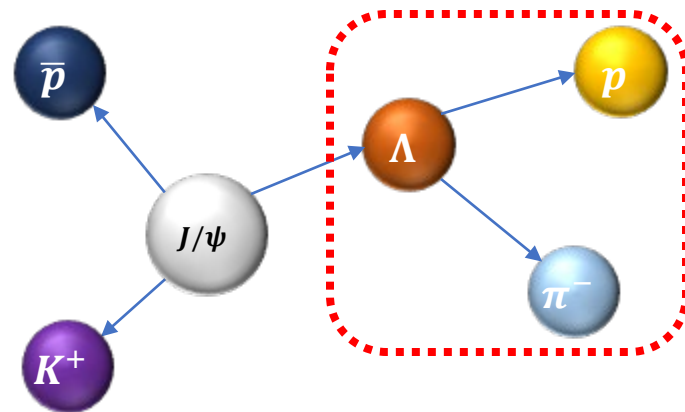
Data Driven:



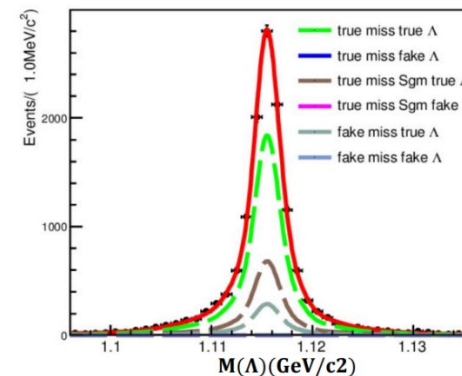
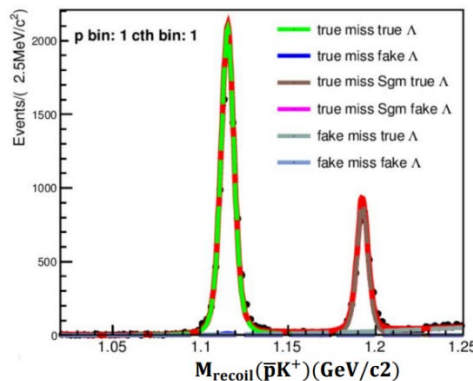
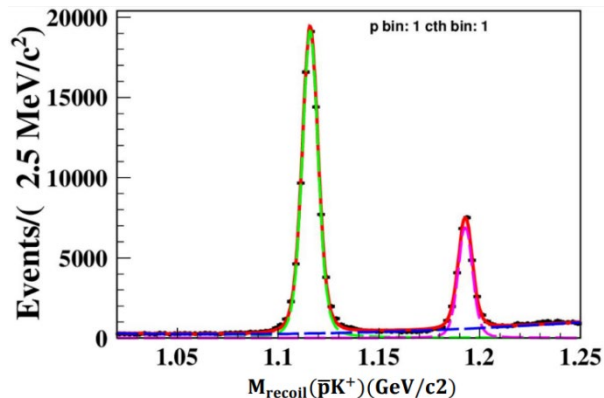
• Control sample & binning:

Taking advantage of high statistics of J/ψ (10^{10})

Control channel: $J/\psi \rightarrow \bar{p}K^+\Lambda$



Fit the spectrum of recoil mass of \bar{p} and K^+ before find a Λ :



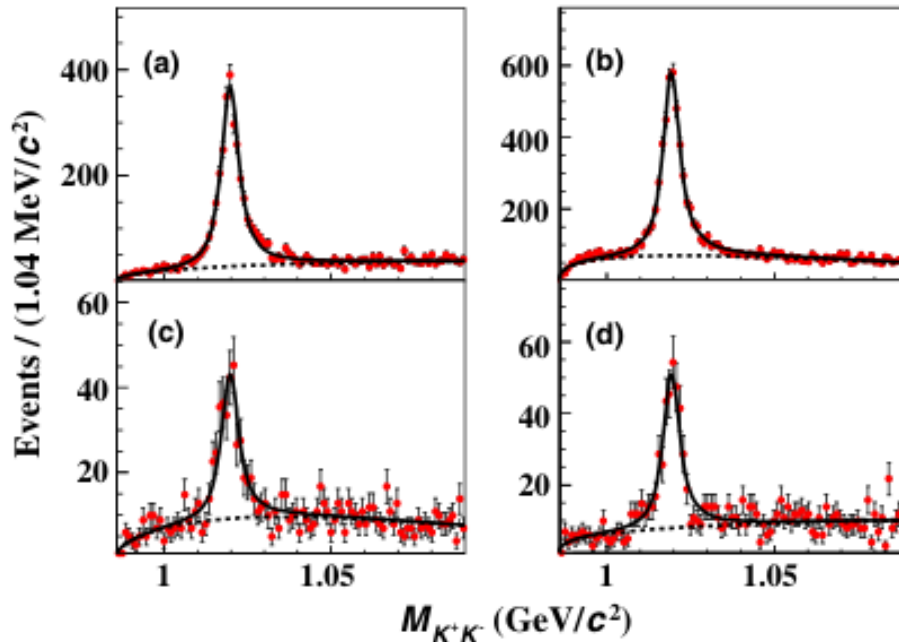
Results:

Then fit the $M_{recoil}(\bar{p}K^+) v.s. M_{p\pi^-}(\Lambda)$ after finding a Λ . $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda + X) = (38.2^{+2.8}_{-2.3})\%$

- $D^{0/+} \rightarrow \phi X$: [Phys. Rev. D 100 072006](#)

The efficiency is also obtained from MC. The remaining difference between data and MC is studied with data-driven hadronic events.

- **Fit & sideband subtraction**



S.Q. Qu, J.H. Wei, et al. BESIII 2019

Decay mode	\mathcal{B}
$D^+ \rightarrow \phi \pi^+ \pi^0$	$(2.3 \pm 1.0)\%$
$D^+ \rightarrow \phi \rho^+$	$< 1.5\%$
$D^+ \rightarrow \phi \pi^+$	$(5.70 \pm 0.14) \times 10^{-3}$
$D^+ \rightarrow \phi K^+$	$(8.86 \pm 1.14) \times 10^{-6}$
Sum	$(2.87 \pm 1.00)\%$
$D^0 \rightarrow \phi \gamma$	$(2.81 \pm 0.19) \times 10^{-5}$
$D^0 \rightarrow \phi K_S^0$	$(4.13 \pm 0.31) \times 10^{-3}$
$D^0 \rightarrow \phi K_L^0$	$(4.13 \pm 0.31) \times 10^{-3}$
$D^0 \rightarrow \phi \omega$	$< 2.1 \times 10^{-3}$
$D^0 \rightarrow \phi(\pi^+ \pi^-)_{S\text{-wave}}$	$(20 \pm 10) \times 10^{-5}$
$D^0 \rightarrow (\phi \rho^0)_{S\text{-wave}}$	$(14.0 \pm 1.2) \times 10^{-4}$
$D^0 \rightarrow (\phi \rho^0)_{D\text{-wave}}$	$(8.5 \pm 2.8) \times 10^{-5}$
$D^0 \rightarrow (\phi \rho^0)_{P\text{-wave}}$	$(8.1 \pm 3.8) \times 10^{-5}$
$D^0 \rightarrow \phi \pi^0$	$(1.17 \pm 0.04) \times 10^{-3}$
$D^0 \rightarrow \phi \eta$	$(1.81 \pm 0.46) \times 10^{-4}$
Sum	$(1.14 \pm 0.09)\%$

Results:

	This work	CLEO [2]
$D^+ \rightarrow \phi X$	$1.135 \pm 0.034 \pm 0.031$	$1.03 \pm 0.10 \pm 0.07$
$D^0 \rightarrow \phi X$	$1.091 \pm 0.027 \pm 0.035$	$1.05 \pm 0.08 \pm 0.07$

- $\bar{\Lambda}_c^- \rightarrow \bar{n}X$: [Phys. Rev. D 108 L031101](#) L.Q. Zhang, et al. BESIII 2023

$\Gamma_{\pi\pi}$	p anything	$(50 \pm 16)\%$
$\Gamma_{\pi\pi}$	n anything	$(50 \pm 16)\%$

from PDG

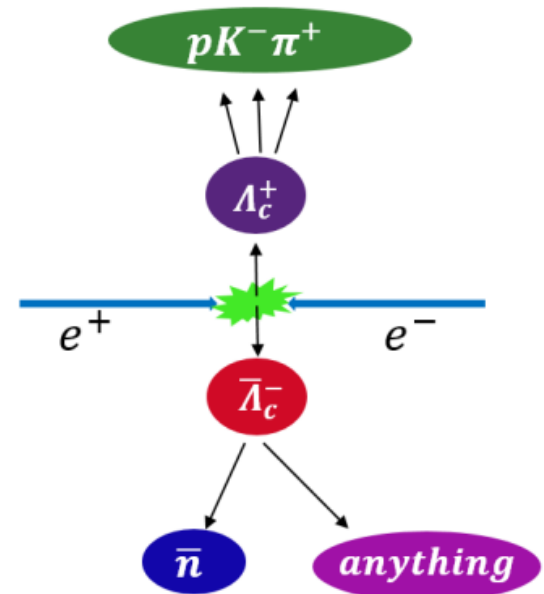
The sum of exclusive decays of $\Lambda_c^+ \rightarrow pX$ and $\Lambda_c^+ \rightarrow nX$ are 44.5%、25.4%. Precise determination of inclusive decay may help search for undiscovered exclusive decays.

• **Tag mode:**

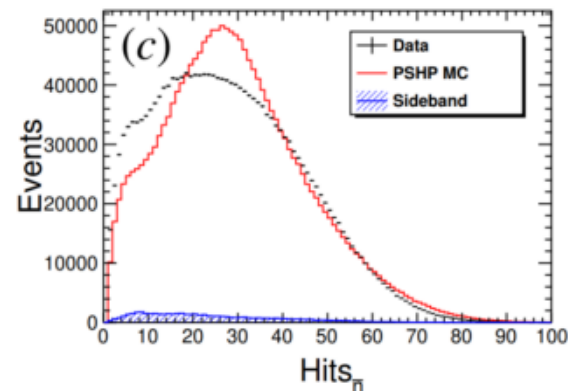
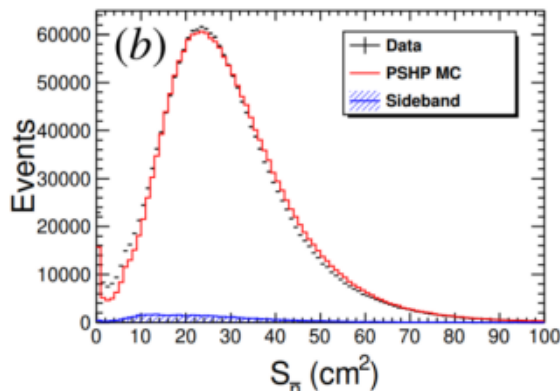
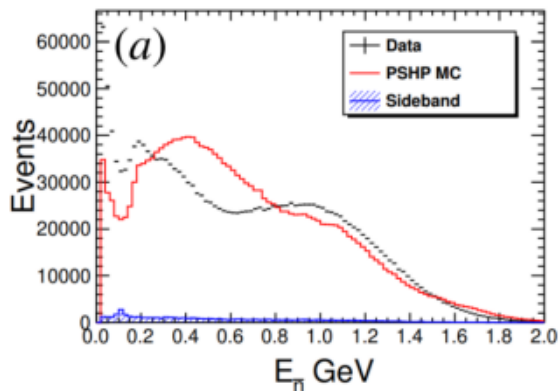
Only choose the $\Lambda_c^+ \rightarrow pK^-\pi^+$ as tag mode.
(Highest statistics, lowest background)

• **Control sample:** choose $J/\psi \rightarrow p\bar{n}\pi^-$.

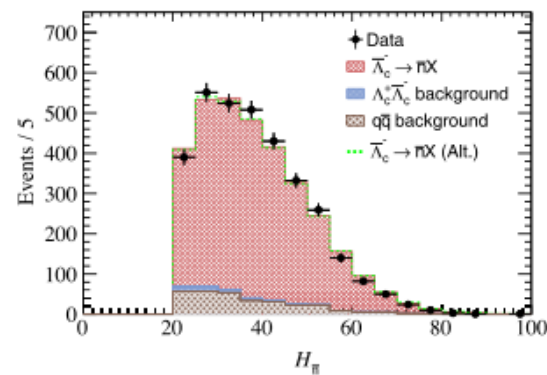
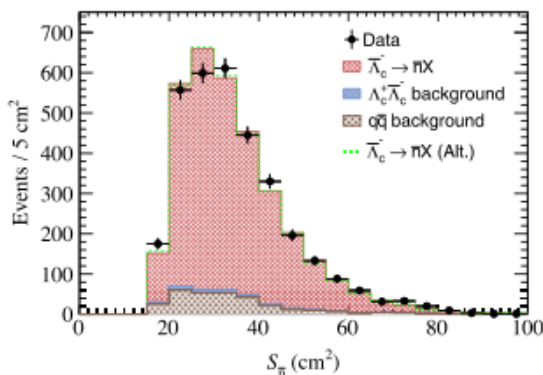
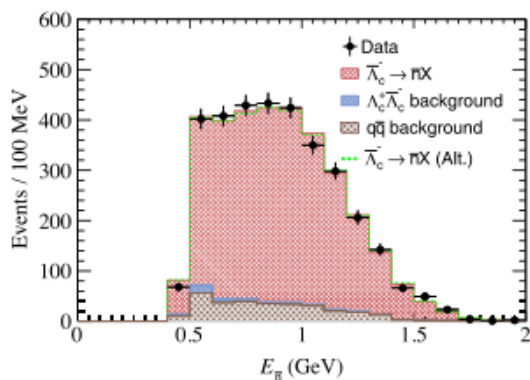
- $E_{\bar{n}} > 0.48 \text{ GeV}$
- Number of hits $Hits_{\bar{n}} > 20$
- second moment $S_{\bar{n}} > 18 \text{ cm}^2$
- $N_{\bar{p}} = 0$



• **Reweight:**



Discrepancy between MC and data \Rightarrow Reweight the MC using data-driven.



Results: $B(\bar{\Lambda}_c^- \rightarrow \bar{n} + X) = (32.4 \pm 0.7 \pm 1.5)\%$ **Sum of exclusive:** $(25.4 \pm 0.8)\%$

- BESIII has obtained a series of achievement on inclusive decays, mature analytical techniques are developed.
- Inclusive decays of Λ_c^+ are widely studied, on-going analyses:
 - $\Lambda_c^+ \rightarrow \Lambda X$, $\Lambda_c^+ \rightarrow K_S^0 X$, $\Lambda_c^+ \rightarrow p X$, $\Lambda_c^+ \rightarrow \Sigma^+ X$, $\Lambda_c^+ \rightarrow \Sigma^0 X$, $\Lambda_c^+ \rightarrow X \mu^+ \nu_\mu$
- Inclusive decays of charmed meson are performed mainly on BES2 and CLEO, waiting for update:
 - $D^{0/+} \rightarrow X e^+ \nu_e$, $D^{0/+} \rightarrow X \mu^+ \nu_\mu$, $D^{0/+} \rightarrow K^\pm X \dots$
- Inclusive decays of charmonium remain blank, possible analyses:
 - $J/\psi \rightarrow p X$, $J/\psi \rightarrow n X$, $J/\psi \rightarrow K_S^0 X \dots$
- Some BNV channels can be searched via inclusive decay:
 - $J/\psi \rightarrow \Lambda_c^+ X$, $J/\psi \rightarrow pp X$, $D^{0/+} \rightarrow p X \dots$

- Dataset at BESIII: (from [BESIII physics page](#))

FOR J/ψ

Sample type	Ecms (GeV)	Run ID	Event number (Int. luminosity)
On- J/ψ (2009)	3.097	9947-10878	$224.0 \pm 1.3M$ (80 pb-1)
On- J/ψ (2012)	3.097	27255-28236	$1088.5 \pm 4.4M$ (315 pb-1)
On- J/ψ (2017-2019)	3.097	52940-54976 55861-56546 56788-59015	$8774.0 \pm 39.4M$ (2571 pb-1)

FOR Ψ (3686)

Sample type	Ecms (GeV)	Run ID	Event number (Int. luminosity)
On- Ψ (3686) (2009)	3.686	8093-9025	$107.0 \pm 0.8M$ (161.63 \pm 0.13 pb-1)
On- Ψ (3686) (2012)	3.686	25338-27090	$341.1 \pm 2.1M$ (506.92 \pm 0.23 pb-1)

FOR Ψ (3770)

Sample type	Ecms (GeV)	Run ID	Int. luminosity
On- Ψ (3770) (2010)	3.773	11414-13988 14395-14604	$2931.8 \pm 0.2 \pm 13.8$ pb-1
On- Ψ (3770) (2011)	3.773	20448-23454	

For above 4.6 GeV:

Energy points	4.600 GeV	4.612 GeV	4.628 GeV	4.641 GeV	4.661 GeV	4.682 GeV	4.698 GeV
Lumi(pb^{-1})	566.90	103.45	519.93	548.15	527.55	1664.34	534.40

- BESIII is an ideal platform to study inclusive decay!
- Eager for theoretical research!



Thanks for your attention!