Photon detectors 1/2

Samo Korpar

University of Maribor and J. Stefan Institute, Ljubljana

8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics -Detector and Electronics August 18 – 22, 2011, Beijing, China



Photon detectors (slide 1)





EDIT2011 photo-detectors team:

Nicoleta Dinu (LAL Orsay) Thierry Gys (CERN) Christian Joram (CERN) Samo Korpar (Univ. of Maribor and JSI Ljubljana) Yuri Musienko (Fermilab/INR) Veronique Puill (LAL, Orsay) Dieter Renker (TU Munich)





# Outline:

- Basics
- Typical applications
- Requirements on photon detectors
- Detector types



# Applications

- Cherenkov light based:
  - Cherenkov threshold detectors, RICH detectors, TOF, Calorimeters ...
- Scintillator based:
  - Calorimeters, TOF, fiber trackers, medical imaging ...



## **Cherenkov** radiation

 threshold - radiation is emitted when charged particles moves through the medium faster than the speed of light

$$\beta = \frac{v}{c} > \frac{1}{n}$$

• Cherenkov angle - angle between the particle and photon directions  $\cos \vartheta_{c} = \frac{1}{\beta n}$ 

• number of photons - depends on refractive index  $\rightarrow$  Cherenkov angle

$$\frac{d^2 N}{dEdl} \approx \frac{370}{eV \, cm} \sin^2 \vartheta_C \qquad \left(\frac{dN}{d\lambda} = \frac{ch}{\lambda^2} \frac{dN}{dE}\right)$$

 $\rightarrow$  high sensitivity in blue to UV region

- prompt emission no decay constant as with scintillators
- $\rightarrow$  enables precise time measurements
- light is polarized E lies in the plane defined by particle and photon momenta

# **Cherencov detectors**

threshold Cherenkov counter

$$p_{thr} = \frac{mc}{\sqrt{n^2-1}}$$

• Ring Imaging CHerenkov counter (RICH)  $\rightarrow$  measurement of Cherenkov angle  $\rightarrow$  particle velocity. Base designs:





# **Applications using scintilators**

- Calorimeters:
- Belle calorimeter with CsI(Tl)
   (λ~550 nm) and PIN photodiodes
   ~ 50000 photons/MeV



- CMS calorimeter with PbWO<sub>4</sub>
- ( $\lambda$ ~420–430 nm) and APDs ~ 100 photons/MeV
- Time-Of-Flight detectors
- Fiber trackers
- Medical imaging (PET, ...)

# $\rightarrow$ high sensitivity in blue-grean region

Photon detectors (slide 7)











# Basics:

- The human eye as a photo-detector
- Photoelectric effect
- Photosensitive materials and windows



## The human eye



- The first proto-eyes evolved among animals 540 million years ago.
- Light passes through the cornea, pupil and lens before hitting the retina. The iris controls the size of the pupil and therefore, the amount of light that enters the eye. Also, the color of your eyes is determined by the iris.
- The vitreous is a clear gel that provides constant pressure to maintain the shape of the eye.
- The retina is the area of the eye that contains the receptors (rods for low light contrast and cones for colors) that respond to light. The receptors respond to light by generating electrical impulses that travel out of the eye through the optic nerve to the brain.

The optic nerve contains 1.2 million nerve fibers. This number is low compared to the roughly 100 million photoreceptors in the retina.



Rods and cones



Spectral sensitivity rods & cones



The human eye can detect light pulse of 10-40 photons. Taking into account that absorption of light in retina is ~10-20% and transparency of vitreous is ~50%

 $\rightarrow$  ~2-8 photons give detectable signal.



## Eye performance

After having been built many billion times, the eye can be considered as a very successful and reliable photo-detector.

It provides...

- Good spatial resolution. <1 mm, with certain accessories even <0.01 mm</li>
- Very large dynamic range (1:106) + automatic threshold adaptation
- Energy (wavelength) discrimination \ colours
- Long lifetime. Performance degradation in second half of life-cycle can be easily mitigated.

Weak points:

- Modest sensitivity: 500 to 900 photons must arrive at the eye every second for our brain to register a conscious signal
- Modest speed. Data taking rate ~ 10Hz (incl. processing)
- Trigger capability is very poor. "Look now"  $\rightarrow$  Time jitter ~1 s.

# $\rightarrow$ There is room for improvement







### Visual photo-transduction

Visual photo-transduction is a VERY COMPLEX process by which light is converted into electrical signals in the rod and cone cells of the retina of the eye.



See e.g. http://en.wikipedia.org/wiki/Phototransduction

Photon detectors (slide 12)



# Photo-effect

First we need to convert light into detectable electronic signal

Principle:

Use photoelectric effect to 'convert' photons

( $\gamma$ ) to photoelectrons (pe)

- Details depend on the type of the photosensitive material (see below).
- Photon detection involves often materials like
   K, Na, Rb, Cs (alkali metals). They have the
   smallest electronegativity → highest tendency
   to release electrons.
- Most photo-detectors make use of solid or gaseous photosensitive materials.
- Photo-effect can in principle also be observed from liquids.





A. Einstein. Annalen der Physik 17 (1905) 132–148

Photon detectors (slide 13)



### Solid photocathode

Good materials for solid photocathode are semiconductors

• absorbed  $\gamma$ 's impart energy to electrons (e) in the material; If  $E_{\gamma} > E_{g}$ , electrons are lifted to conductance band.

 $\rightarrow$  In a Si-photodiode, these electrons can create a photo-current.  $\rightarrow$  Photon detected by Internal Photoeffect.

However, if the detection method requires extraction of the electron into vacuum, 2 more steps must be accomplished:



• energized e's diffuse through the material, losing part of their energy (~random walk) due to electron-phonon scattering.  $\Delta E \sim 0.05 \text{ eV}$  per collision. Free path between 2 collisions is ~ 2.5 - 5 nm  $\rightarrow$  escape depth  $\lambda_e$  ~ some tens of nm.

only e's reaching the surface with sufficient excess energy escape from it
 → External Photoeffect

$$E_{\gamma} = h \nu > W_{ph} = E_G + E_A$$



### Opaque vs semitransparent photocathode

opaque





0.4

3

**Red light** ( $\lambda \approx 600 \text{ nm}$ )  $\alpha \approx 1.5 \cdot 10^{5} \text{ cm}^{-1}$ λ **≈** 60 nm

Blue light (I  $\approx$  400 nm)  $\alpha \approx 7 \cdot 10^5 \text{ cm}^{-1}$ λ **≈** 15 nm

Blue light is more strongly absorbed than red light !

### → Make semitransparent photocathode just as thick as necessary!

August	18 – 22, 2	2011, Beijin	ig, China		
8 <sup>th</sup> Sumi	mer Topio	cal Seminar	• on Frontier	of Particle	Physics

**Photon detectors** (slide 15)

### Photosensitive materials – photo-cathodes



Photon detectors (slide 16)



### Semitransparent photo-cathodes



Bialkali: SbKCs, SbRbCs Multialkali: SbNa<sub>2</sub>KCs (alkali metals have low work function)



# **Recent improvements of photo-cathode QE**

QE Comparison of semitransparent bialkali QE



Photon detectors (slide 18)



### Light absorption in Silicon





# QE in gaseous detectors

Gaseous detectors (MWPCs, TPCs) use admixtures os photosensitive substances to gain photosensitivity in UV/VUV region.





<b>→</b>	

molecule	formula	E <sub>1</sub> [eV] (λ <sub>1</sub> [nm])	<b>max.</b> ε <sub>Q</sub> (Ε)	$\lambda_{ph}$ (at 293K)
TEA	$(C_2H_5)_3N$	7.5 (164)	0.33 (8.2)	0.43 mm
TMAE	$C_2[(CH_3)_2N]_4$	5.36 (230)	0.51 (8.3)	26 mm
DMA	(CH <sub>3</sub> ) <sub>2</sub> NH	8.3 (148)	0.2 (9.2)	
TMA	(CH <sub>3</sub> ) <sub>3</sub> N	7.9 (156)	0.27 (8.6)	

Photosensitive agent is admixed to the counting gas of a MWPC by bubbling the gas through the liquid agent at a given temperature  $\rightarrow$  concentration control.



### Window transmission

2 types of losses:

 Fresnel reflection at interface air/window and window/photocathode RFresnel = (n-1)<sup>2</sup> / (n+1)<sup>2</sup> n = refractive index (wavelength dependent!) N<sub>glass</sub> ~ 1.5, R<sub>Fresnel</sub> = 0.04 (per interface)

 Bulk absorption due to impurities or intrinsic cut-off limit. Absorption is proportional to window thickness (for low absorption)



Photon detectors (slide 21)











#### Newport

August 18 – 22, 2011, Beijing, China 8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics Photon detectors (slide 22)

Samo Korpar University of Maribor and Jožef Stefan Institute

### **Requirements on photo-detectors**

Basic properties of photo-detectors and Requirements:

- Sensitivity
- Linearity
- Signal fluctuations
- Time response
- Rate capability / aging
- Dark count rate
- Operation in magnetic fields
- Radiation tolerance





• UV-blue sensitivity is required for detectors based on Cherenkov light (RICH, water Cherenkov telescope, Imaging Atmospheric Cherenkov Telescopes (HES II, CTA ...)).

• Blue-green sensitivity is required for calorimeters (CMS, ILC HCAL ...), TOF detectors, fiber trackers detecting scintillation light.



Requirement: Photo-current response of the photo-detector is linear with incident radiation over a wide range. Any variation in response with incident radiation represents a variation in the linearity of the detector.





	PMT	HPD	MCP- PMT	APD	SiPM
Dynamic range (p.e.)	10 <sup>6</sup>	10 <sup>7</sup>	10 <sup>7</sup>	10 <sup>7</sup>	10 <sup>3</sup>



Example of dynamic range required : HCAL of ILC Min: 20 photons/mm<sup>2</sup> (µ for calibration) Max: 5x10<sup>3</sup> photons/mm<sup>2</sup> (high-energy jet) (C. Cheshkov et al., NIM A440(2000)38)

August 18 – 22, 2011, Beijing, China 8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics

Linearity

Photon detectors (slide 25)

Samo Korpar University of Maribor and Jožef Stefan Institute



# Signal fluctuations



PMT

 $\sigma_{out}^2/N_{out}^2$ 

Statistical fluctuation of the avalanche multiplication widen the response of a photo-detector to a given photon signal beyond what would be expected from simple photoelectron statistics (Poissonian distribution)



APD

→ multiplication fluctuations are characterized by Excess Noise Factor - ENF

definition

$$ENF = \frac{\sigma_{pe}^{2} / N_{pe}^{2}}{\sigma_{pe}^{2} / N_{pe}^{2}}$$
$$ENF = 1 + \frac{\sigma_{M}^{2}}{M^{2}}$$
$$\frac{\sigma_{E}}{E} = \sqrt{\frac{ENF}{N_{pe}}}$$

M - multiplication  $(N_{out} = M \cdot N_{pe})$ 

Energy resolution

- Impacts photon counting capability at low light levels
- Deteriorates energy resolution of the calorimeters

Typical ENF values for different sensors

sensor	ENF
PMT	1-1.5
APD	2 @ gain=50
HPD, HAPD	~1
SiPM	1-1.5
MCP-PMT	1-1,5

### Time response



### Some typical signals:



PMT





Applications requiring good timing:

- Cherenkov light based TOF systems
- Time-Of-Propagation counter (Belle II)
- Focusing DIRC with chromatic correction (SuperB)

- Light travels 3 mm in 10ps (vakuum)
- Rise time, fall time (or decay time)
- Duration
- Transit time ( $\Delta t$ ): time between the arrival
- of the photon and the electrical signal
- $\rightarrow$  trigger decision time
- Transit time spread (TTS): transit time variation between different events
- $\rightarrow$  timing resolution



Photon detectors (slide 27)



## High rate operation, aging

Rate capability: inversely proportional to the time needed, after the arrival of one photon, to get ready to receive the next SiPM **MCP-PMT** 



Aging (long-term operation at high counting rates): how is the photo-detector behavior changed when operated at high counting rate during several years ?



Parameter affected (generally in a negative way):

- quantum efficiency
- dark current

August 18 – 22, 2011, Beijing, China 8th Summer Topical Seminar on Frontier of Particle Physics Photon detectors (slide 28)

Samo Korpar University of Maribor and Jožef Stefan Institute



# Dark count rate (DCR)

Sensors produce signals even in total darkness!

### DCR of PMTs:

- depends on the cathode type, the cathode area, and the temperature.
- few kHz (threshold = 1 p.e.)
- is highest for cathodes with high sensitivity at long wavelengths.
- Temporarily increases considerably after exposure to daylight







DCR of SiPMs:

- depends on the pixel size, the bias voltage, the temperature
- quite high (0.3–2MHz/mm<sup>2</sup> at room temp, threshold = 1 p.e.)

DCR depends strongly on the threshold level  $\rightarrow$  not a problem for detection of many photon signals (threshold > 10).

Can be efficiently reduced by lowering the temperature.



#### DCR of different photocathodes

### Magnetic field tolerance

• Earth's magnetic field = 30-60 μT





PMT very sensitive to magnetic Field  $\rightarrow$  shielding required (µ metal)



MCP-PMT tolerant to magnetic field up to  $\sim$  2T (6 µm pores).



PD, APD, SiPM insensitive to magnetic field

Typical requirements 1.5T @ Belle II, 2T @ PANDA, SuperB, 4T CMS, ILC ...



## **Radiation tolerance**



Damages caused by:

- ionizing radiation: energy deposited in the detector material by particles and by
- photons from electromagnetic showers
- (the unit of absorbed dose is Gray [Gy]  $\rightarrow$  1 Gy = 1 J/kg = 100 rad ).
- neutrons created in hadronic shower, also in the forward shielding of the detectors and in beam collimators
- $\rightarrow$  Result is degradation of DRC, gain QE ...



- Belle II ARICH photon detector 10<sup>12</sup> n/cm<sup>2</sup> + 100 krad
- At LHC, the ionizing dose is ~  $2x10^6$  Gy /  $r_T^2$  / year ( $r_T$  = transverse distance to the beam)
- $\rightarrow$  CMS ECAL (10 years) 2x10<sup>13</sup> n/cm<sup>2</sup> + 250 krad

# Detector types

- PMT
- MAPMT, Flat-panel PMT
- MCP-PMT
- Photosensitive gas detectors (MWPC / MPGD)
- PIN diode
- APD
- HPD, HAPD
- G-APD / SiPM



### 'Family tree' of photo-detectors



Photon detectors (slide 33)



# Photo-multiplier tubes (PMT's)

Principle of operation:

- Photo-emission from photo-cathode
- Secondary emission (SE) from N dynodes:
  - dynode gain g ~ 3-50 (function off incoming electron energy E);
  - total gain M:

 $M = \prod g_i$ 





- Example:
  - 10 dynodes with g = 4
  - M = 4<sup>10</sup> ~ 10<sup>6</sup>

Photon detectors (slide 34)



(Hamamatsu)

# PMT: gain fluctuations (ENF)

Mainly determined by the fluctuations of the number of secondary electrons emitted from the dynodes;

- Poisson distribution:  $P_i(m; \delta_i) = \frac{\delta_i^m e^{-\delta_i}}{m!}$
- Standard deviation:  $\frac{\sigma_m}{\delta} = \frac{\sqrt{\delta}}{\delta} = \frac{1}{\sqrt{\delta}}$

• 
$$ENF = \frac{1}{\delta_1} + \frac{1}{\delta_1 \delta_2} + \frac{1}{\delta_1 \delta_2 \delta_3} \dots \left( = \frac{1 - \frac{1}{\delta^{N+1}}}{1 - \frac{1}{\delta}} \approx \frac{1}{\delta} \right)$$

 $\rightarrow$  fluctuations dominated by 1st dynode gain





August 18 – 22, 2011, Beijing, China 8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics



# PMT: different dynode structures

### Position sensitive types



# Mesh Mesh TYPE Mesh TYPE Metal-channel (fine-machining techniques)

Modern micro-machining techniques allow fabricating fine dynode structures. Avalanche is confined in a narrow channel.

→ Multi-anode designs
 → some tolerance to
 modest magnetic field

The design of a dynode structure is a compromise between:

- collection efficiency (input optics: from cathode to first dynode)
- gain (minimize losses of electrons during passage through structure)
- transit time and transit time spread (minimize length of path and deviations)
- immunity to magnetic field



### PMT: timing and magnetic field

Rough estimation of transit time: 
$$t \approx N \cdot \sqrt{\frac{21}{a}} = \frac{N \cdot l}{\sqrt{\frac{eU}{2m_e}}} = \frac{0.1\text{m}}{\sqrt{\frac{e \cdot 100\text{V}}{2 \cdot 0.5 \text{ MeV}/c^2}}} = \frac{0.1\text{m}}{0.01 \cdot c} \approx 33 \text{ ns}$$

To optimize TTS:

 Compact construction (short distances between dynodes) keeps the overall transit time small (~10 ns).

• "Fast" PMT's require well-designed input electron optics to equalize travel times of photoelectrons  $\rightarrow$  transit time spread < 100 ps;



Figure 13-8: Magnetic characteristics of typical photomultiplier tubes

- PMT's are in general very sensitive to magnetic fields,
  even to earth field (30-60 mT = 0.3-0.6 Gauss).
- Magnetic shielding required.



## PMT: multi-anode and flat-panel





Multi-anode (Hamamatsu H7546):

- Up to 8 x 8 channels (2 x 2 mm<sup>2</sup> each);
- Size: 28 x 28 mm<sup>2</sup>;
- Active area 18.1 x 18.1 mm<sup>2</sup> (41%);
- Bialkali PC: QE ≈ 25 45% @ λ<sub>max</sub> = 400 nm;
- Gain ≈ 3x10<sup>5</sup>;
- Gain uniformity typ. 1 : 2.5;
- Cross-talk typ. < 2%</li>



Flat-panel (Hamamatsu H8500):

- 8 x 8 channels (5.8 x 5.8 mm<sup>2</sup> each)
- Excellent active area coverage (89%)

Photon detectors (slide 38)



# HERA-B RICH MAPMT module





 Lens system used to eliminate dead space



Photon detectors (slide 39)





August 18 – 22, 2011, Beijing, China 8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics Photon detectors (slide 40)

Samo Korpar University of Maribor and Jožef Stefan Institute

## PMT: scintillating fiber tracker with MAPMTs

#### Working principle of scintillating plastic fibres :



Photon detectors (slide 41)



Technology: Scintillating plastic fibres, <u>square</u> cross-section,
 500 μ m overall width, single cladded (10 μ m). Type: Kuraray SCSF-78.



Photon detectors (slide 42)





~2x1400 fibres

Photon detectors (slide 43)





Photon detectors (slide 44)





Photon detectors (slide 45)

# Belle II ARICH prototype

Photon detector

- 4x4 array Hamamatsu H8500
- 1024 channels
- 52.5 mm pitch (84% eff. Area)
- does not work in magnetic field
- 2cm thick aerogel sample, n=~1.04





August 18 – 22, 2011, Beijing, China 8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics Photon detectors (slide 46)

Samo Korpar University of Maribor and Jožef Stefan Institute

# Micro Channel plate PMT (MCP-PMT)

Similar to ordinary PMT – dynode structure is replaced by MCP. Basic characteristics:

- Gain ~  $10^6 \rightarrow$  single photon
- Collection efficiency ~ 60%
- Small thickness, high field
   → small TTS
- Works in magnetic field
- Segmented anode
   → position sensitive





MCP gain depends on L/D ratio – typically 1000 For L/D=40





August 18 – 22, 2011, Beijing, China 8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics

**PHOTONIS** 

Photon detectors (slide 47)



### MCP-PMT: single photon pulse height and timing



Gain in a single channel saturates at high gains due to space charge effect  $\rightarrow$  peaking distribution for single photoelectron

Typical single photon timing distribution with narrow main peak ( $\sigma \sim 40$  ps) and contribution from photoelectron back-scattering.

Photoelectron back-scattering produces rather long tail in timing distribution and position resolution.





August 18 – 22, 2011, Beijing, China 8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics

Photon detectors (slide 48)

Samo Korpar University of Maribor and Jožef Stefan Institute

## **MCP-PMT:** photoelectron timing and position

Photoelectron travel time and range:

$$t_0 \approx l \sqrt{\frac{2 m_e}{U e_0}}$$
$$d_0 \approx 2 l \sqrt{\frac{E_0}{U e_0}} \sin(\alpha)$$

Backscatering delay and range:

 $t_1 = 2 t_0 \sin(\beta)$   $d_1 = 2 l \sin(2\beta)$ 

Parameters used:

- U = 200 V
- I = 6 mm
- $E_0 = 1 \text{ eV}$
- m<sub>e</sub> = 511 keV/c<sup>2</sup>
- $e_0 = 1.6 \ 10^{-19} \ As$



August 18 – 22, 2011, Beijing, China 8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics

Photon detectors (slide 49)

Samo Korpar University of Maribor and Jožef Stefan Institute



### MCP-PMT: charge sharing

Secondary electrons spread when traveling from MCP out electrode to anode and can hit more than one anode  $\rightarrow$  Charge sharing Can be used to improve spatial resolution.

Fraction of the charge detected by left pad as a function of light spot position (red laser)





Slices at equal charge sharing for red and blue laser) – pad boundary. Resolution limited by photoelectron energy.

August 18 – 22, 2011, Beijing, China 8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics Photon detectors (slide 50) e



# **MCP-PMT: operation in magnetic field**

- Narrow amplification channel and proximity focusing electron optics allow operation in magnetic field (~ axial direction).
- Amplification depends on magnetic field strength and direction.
- Effects of charge sharing and photoelectron backscattering on position resolution are strongly reduced while effects on timing remain





K. Inami @ PD07

Gain vs. Magnetic field for MCP-PMT samples with different pore diameter.

TTS vs. Magnetic field for MCP-PMT samples with different pore diameter.

# **MCP-PMT: Ion feedback and aging**

- During the amplification process atoms of residual gas get ionized → travel back toward the photocathode and produce secondary pulse
- Ion bombardment damages the photocathode reducing QE
- Thin Al foil (few mm) blocks ion feedback but also about half of the electrons → placed between the MCPs





Change of relative QE during the typical aging test. MCP-PMTs without AI protection show rapid reduction of QE.



## **MCP-PMT: TOF applications**

 Excellent timing properties require fast light source → Cherenkov radiator directly attached to the MCP-PMT

 Can be used as dedicated TOF (SuperB end-cap PID option) or as part of the proximity focusing RICH (Belle-II end-cap PID option)







K. Inami @ PD07



**Proximity focusing** aerogel RICH with **TOF** capability

> Separation of 2 GeV pions and protons with 0.6 m flight length (start counter s  $\sim$  15 ps).



**Photon detectors** (slide 53)



# **MCP-PMT: RICH with timing information**

### DIRC concept (BaBar) – 2D imaging



Focusing DIRC with chromatic correction (SuperB) uses measured time of propagation to correct chromatic error.

$$t_p = \frac{L_{path}}{v_g}$$
  $v_g = \frac{c}{n(\lambda) - \lambda} \frac{dn}{d\lambda}$  (group velocity)





TOP (Time-Of-Propagation) counter based on DIRC concept (Belle-II). Using linear array of MCP-PMTs to measure one coordinate and time of propagation (length of photon path) to obtain 2D image  $\rightarrow$ compact detector. (pion, kaon)



# MCP-PMT TOF PET

- PET based on Cherenkov light
- Data taken with black painted PbF<sub>2</sub> crystals:
- 15 mm: r.m.s. ~ 37 ps FWHM ~ 95 ps

• 5 mm: r.m.s. ~ 30 ps FWHM ~ 70 ps



August 18 – 22, 2011, Beijing, China 8<sup>th</sup> Summer Topical Seminar on Frontier of Particle Physics Photon detectors (slide 55)

Samo Korpar University of Maribor and Jožef Stefan Institute

# MCP-PMT TOF PET

- Data taken at three different point source positions spaced by 20 mm:
- average time shift 125 ps
- timing resolution ~ 40 ps
- position resolution ~ 6 mm RMS,
  - ~ 14 mm FWHM

Black painted 15 mm PbF<sub>2</sub> crystals.



Photon detectors (slide 56)

