



Simulation studies of the WXPT-TPC

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On behalf of WXPT-TPC group

21th 核电子学与核探测技术学术年会

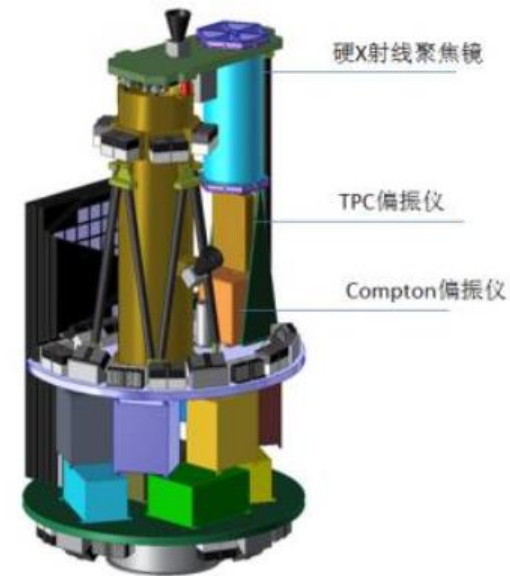
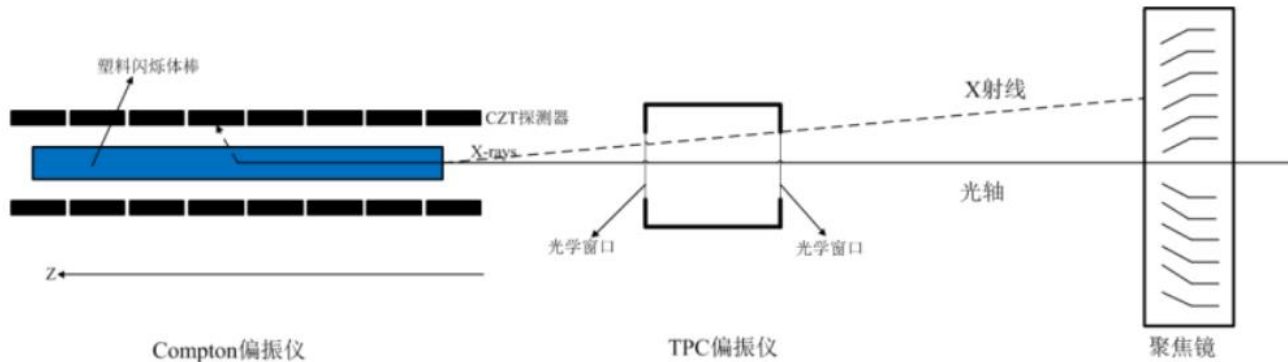


- Background introduction
- Dimensions design of WXPT-TPC
- Working gas choices of WXPT-TPC
- Summary and plan



Background

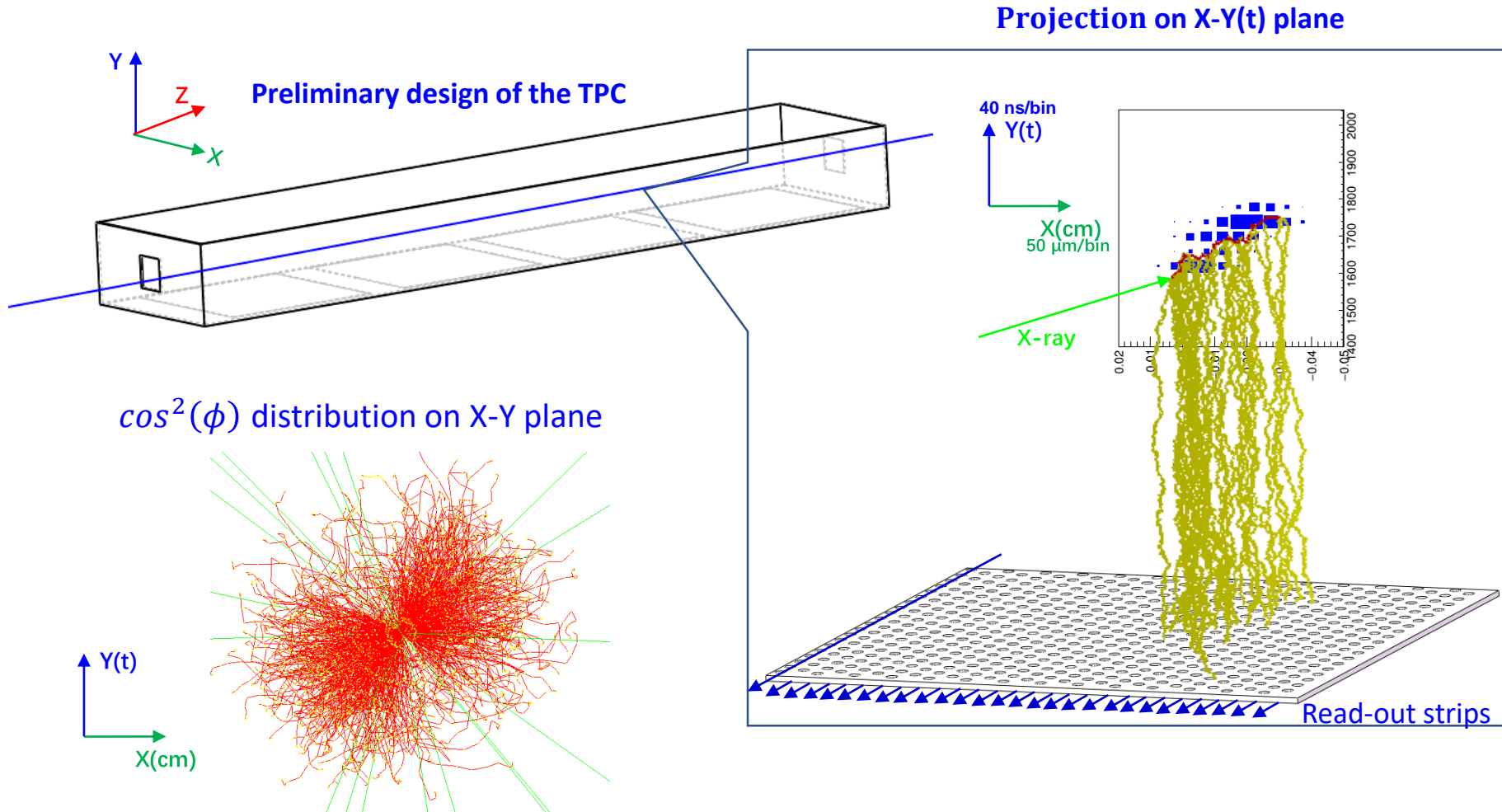
- The **Wide band X-ray Polarization Telescope (WXPT)**
- Spectral-polarimetry studies of the extreme Universe in the 3-500 keV band
 - silicon multilayer mirrors with $f \sim 10$ m (3-60 keV)[TBC]
 - A time projection chamber (TPC) polarimeter (3-10 keV)
 - A Compton polarimeter (10-60 keV)
 - Extend to 500 keV (soft γ -ray)





Background

X-ray polarization detection

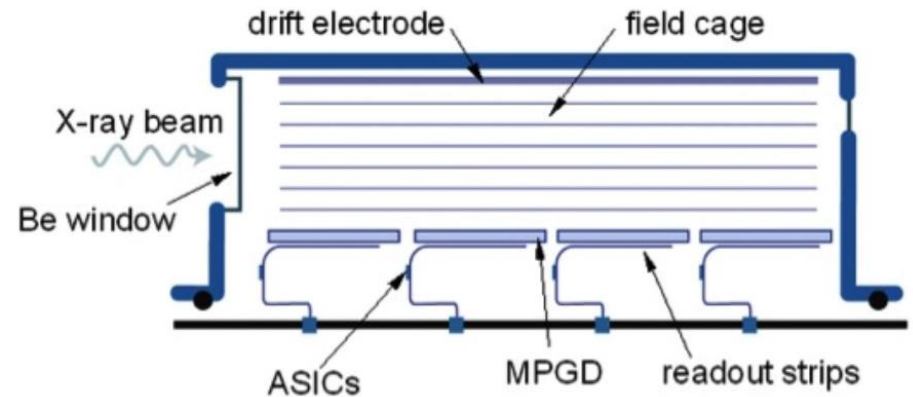


Background



Requirements_[TBC]

- Energy range 3 ~ 10 keV
 - Emit focal spot < 1 cm
 - Angle resolution < 1'
 - Transparency > 90% (@ 10 keV)
 - Be window 20 mm × 20 mm
 - MF > 0.4 @ 6 keV
 - Position resolution < 140 μm
 - Spatial resolution < 200 μm
-
- Depth, height, relative position of the GEM and drift electrode within a TPC (limitation)
 - **distribution of Electric field and X-ray transparency**
 - Gas choice and working condition (optimization)
 - **Quality factor ($MF \times \sqrt{PDE}$)**

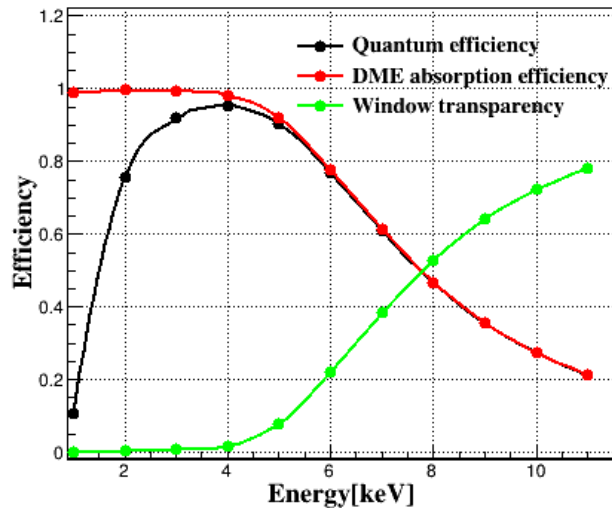




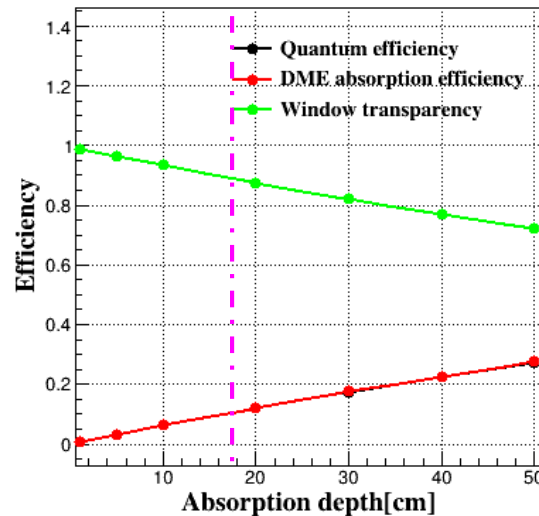
Detection efficiency

Different depth and pressure

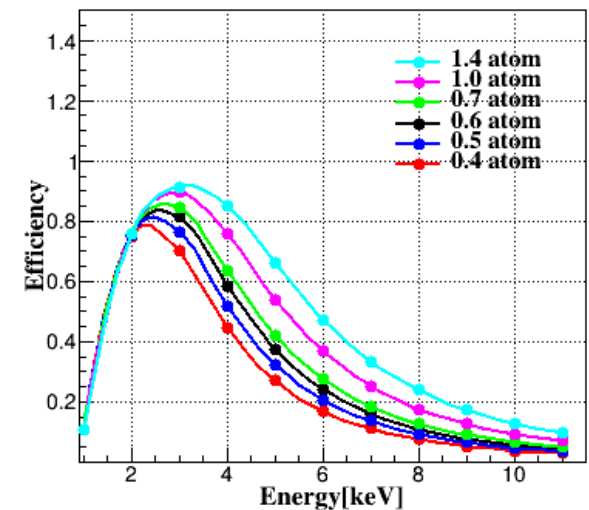
Absorption depth 50 cm



X-ray 10 keV



0.5DME+0.5Ne
depth of 10 cm



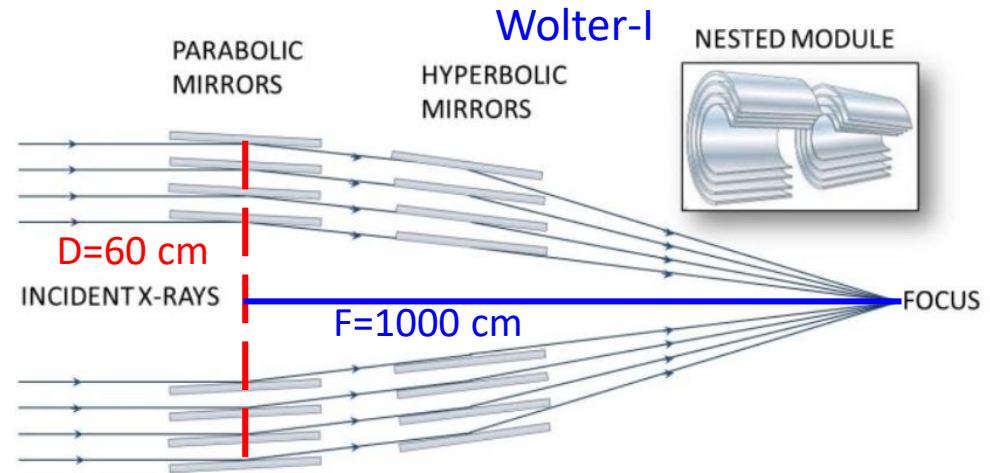
- Detection efficiency versus energy (>10 keV) follows an exponential function
- For 0.5DME+0.5Ne, 0.6 atom, transparency > 90% @ 10 keV as depth < 18 cm
- For 0.5DME+0.5Ne, depth of 10 cm, transparency > 90% @ 10 keV as pressure < 1 atom



Dimension

TPC requirement

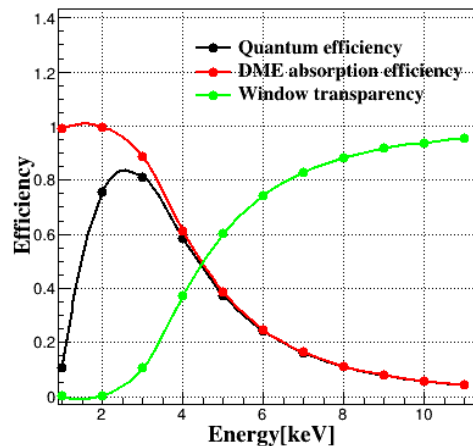
- ① Defocus spot limit is width of the scatter bar with 1 cm
- ② Angle resolution $< 1'$
- ③ X-ray transparency $> 90\%$ (@ 10 keV)



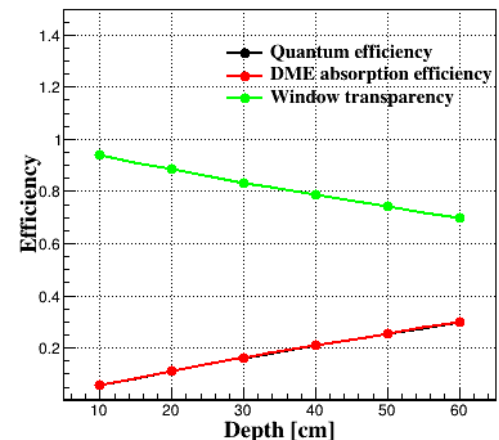
TPC depth

- ① Depth of the TPC < 66 cm
 - ② Depth of the TPC < 10 cm ($f=10$ m)
 - ③ Depth of the TPC < 18 cm
- Transparency $\sim 93\%$ (@ 10 keV)

Absorption depth 10 cm



X-ray 10 keV



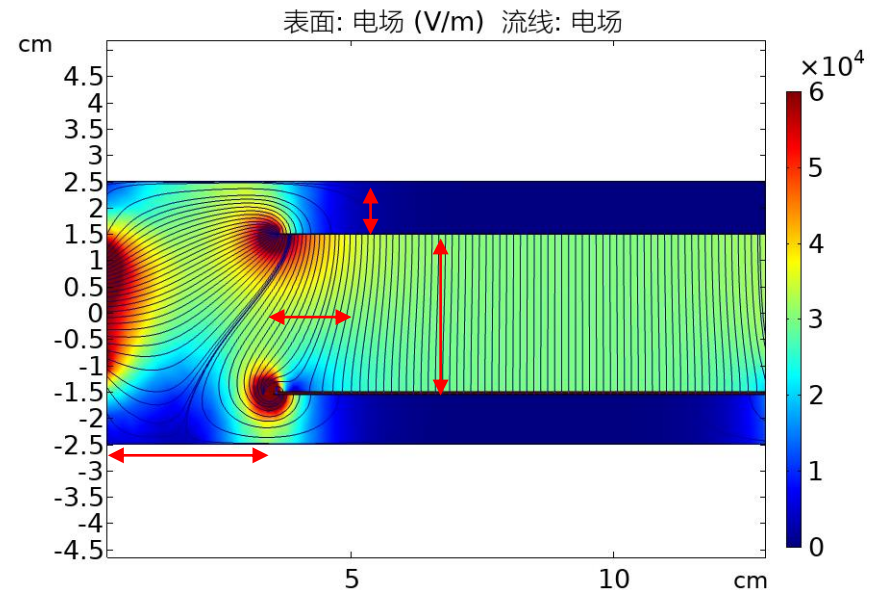
0.5DME+0.5Ne 0.6 atom

Dimension



GEM and drift electrode

- Distance between beryllium window and end point of the drift plane
- Absorption depth and position
- Electric field of drift region
- Limited of the distortion of the electric field (EF)
- Electrons amplification (safe distance)
- deviation of position (EF distortion)

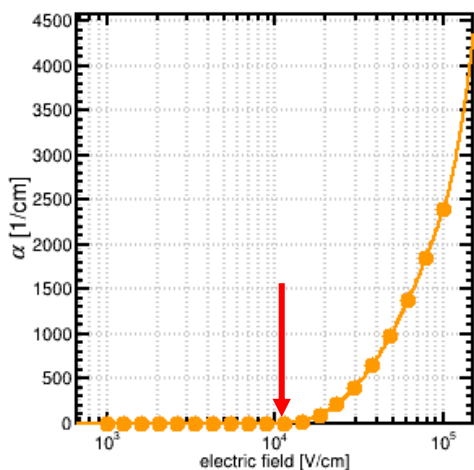


Dimension

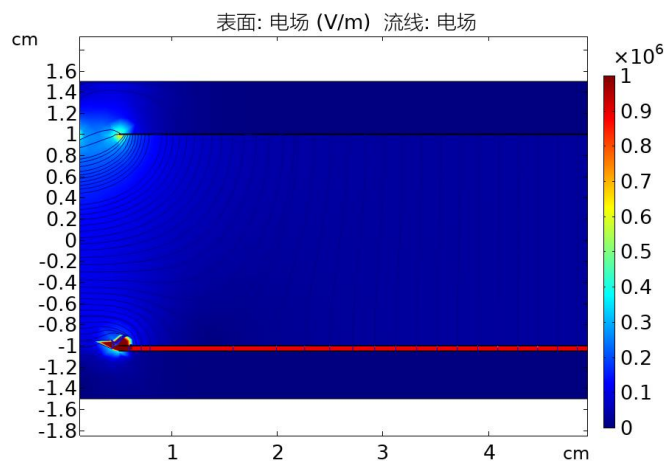


Optimization of the drift region

Townsend coefficient

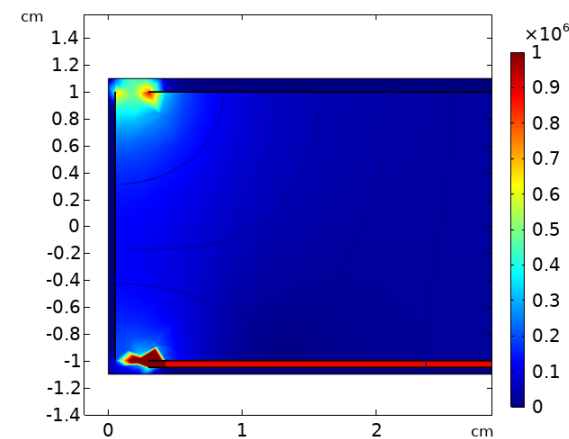


Electric field $< 10^4$ V/cm



0.5 cm 0.5 cm

Electric field distribution



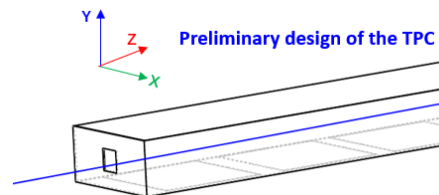
0.3 cm 0.1 cm

- Distance between beryllium window and end point of the drift plane **0.3 cm**
- Drift depth is **2 cm** (limited on size of Be)
- Height of the TPC **> 2.2 cm**

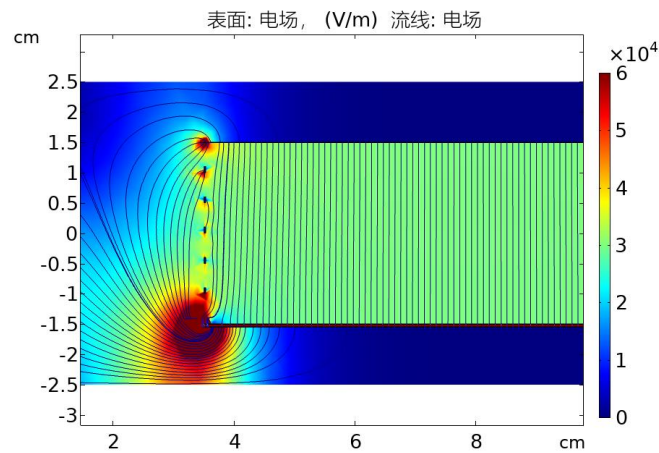
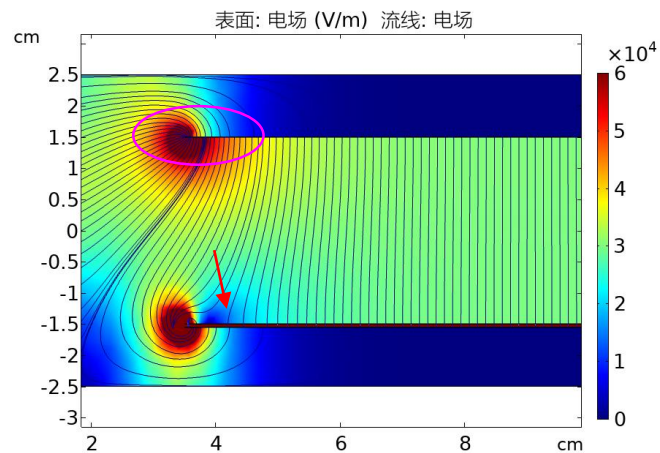
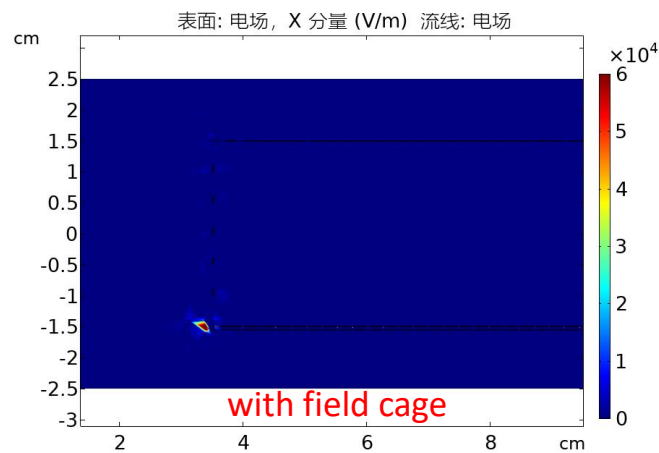
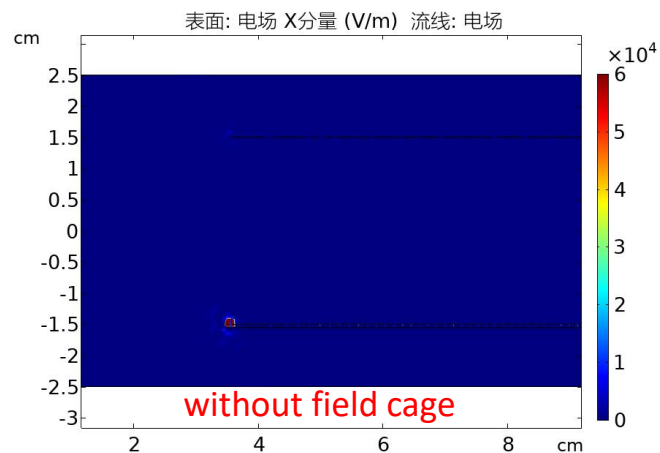
Dimension



Optimization of electric field



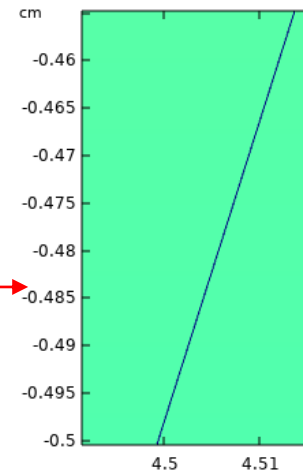
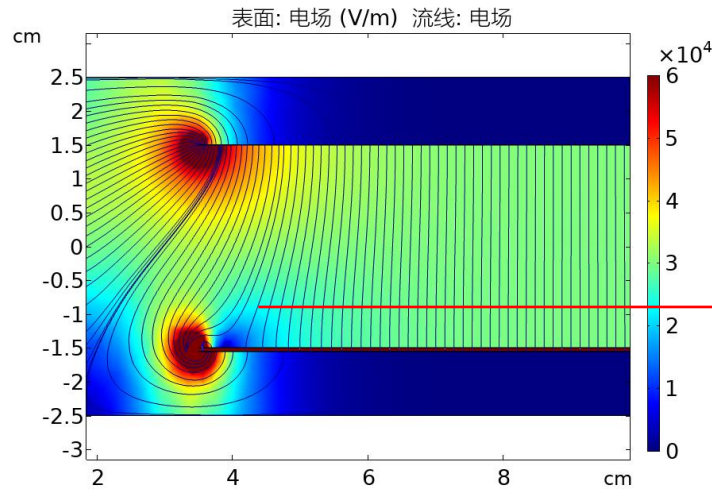
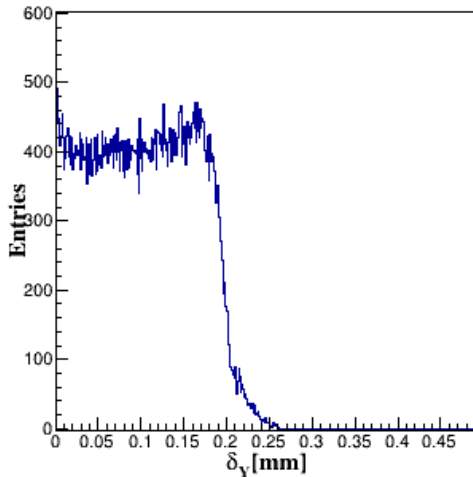
Position and timing ← X and Y direction



Dimension



Timing distortion

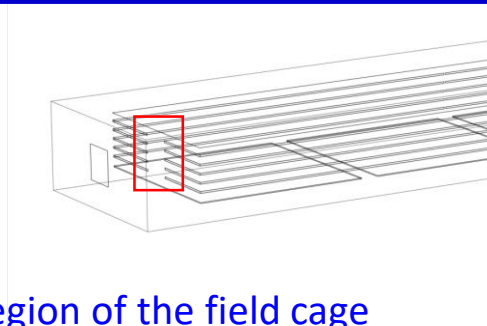


- Distance between two adjacent ionization electrons < 0.25 mm (Mean free path)
- Timing distortion characterized as distance < 0.1 mm (smaller than diffusion [0.15 mm])
- The drift region is accepted if ionization electrons can drift through the GEM plane

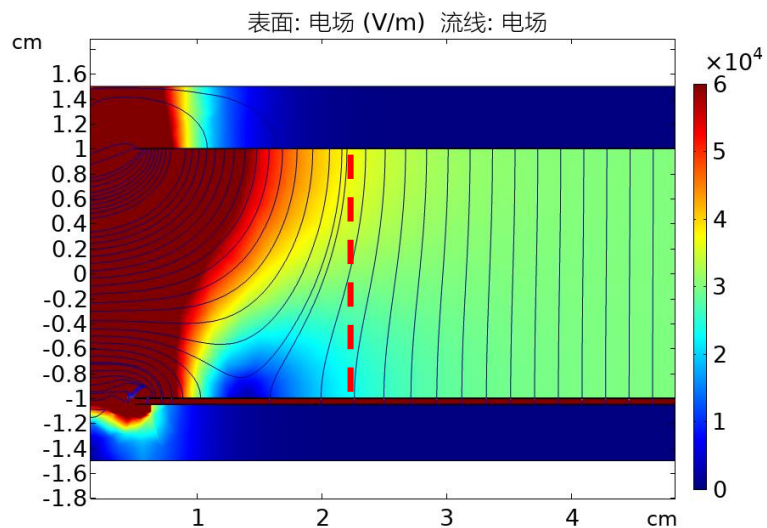
Dimension



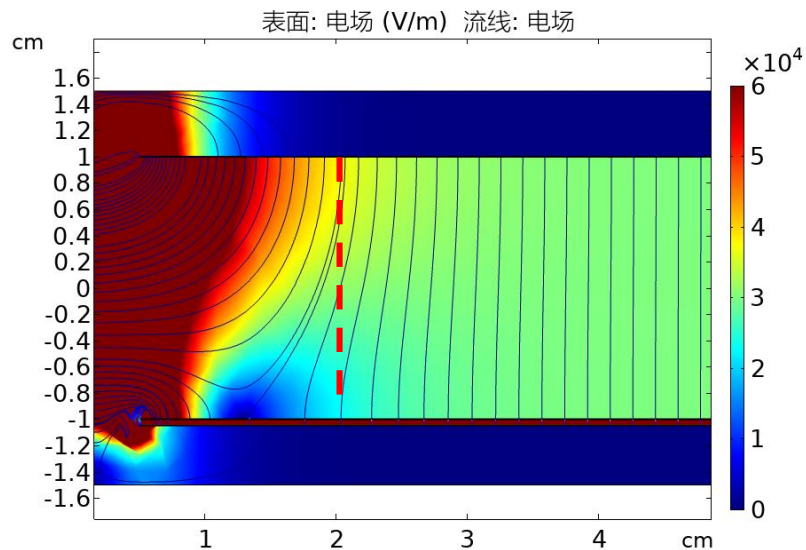
Timing influence



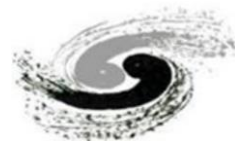
Get the time distribution in this region



Cut the shield region of the field cage



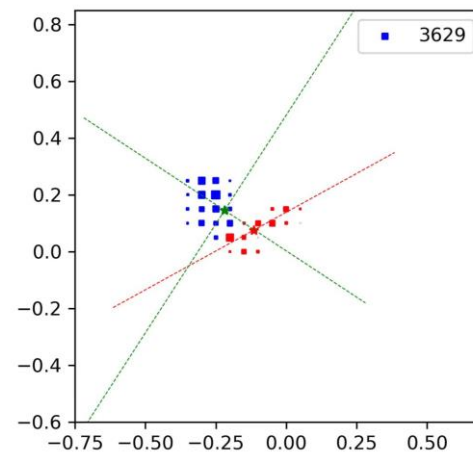
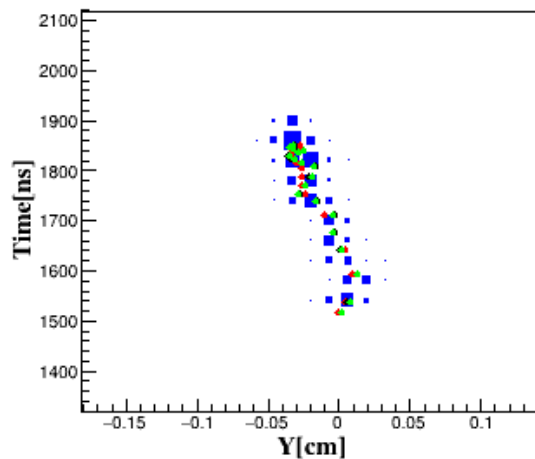
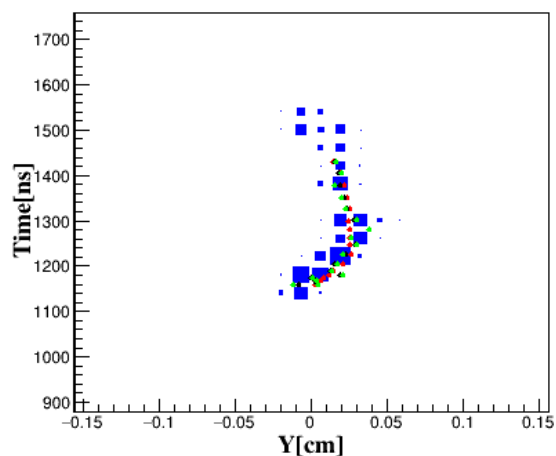
- Increase 1% effective events with field cage
- The affection is not obvious with field cage



Sample generation

Image generation

- Fast simulation framework
- trip distance (130 μm) and drift time (40 ns)
- Effective gain 3000 with Polya function (PDF sampling)

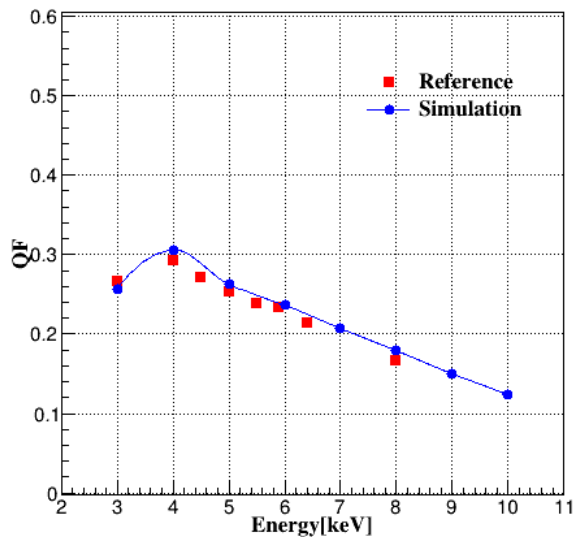


Validation

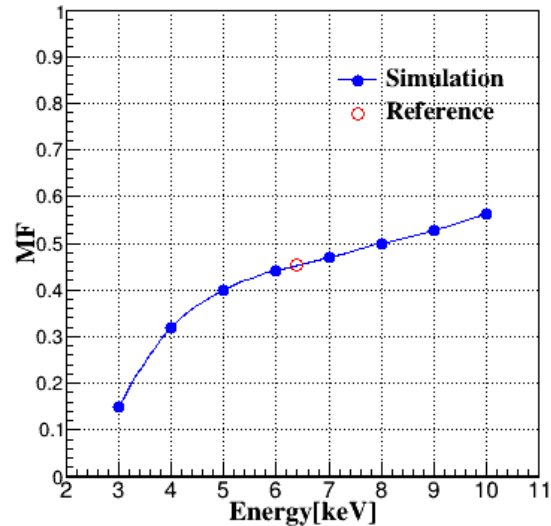


Comparison

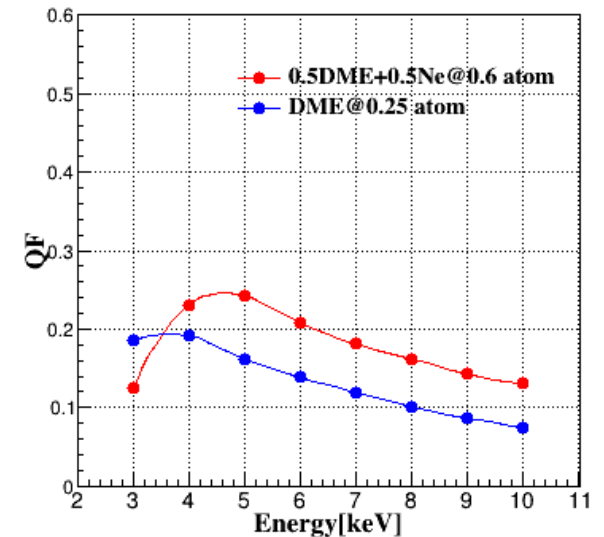
DME, 0.25 atom, 32 cm



0.5DME+0.5Ne, 0.6 atom, 94% Efficiency



Depth of 10 cm





Candidate

6.4 keV, 0.6 atom, 0.33 cm/us

Gas	L [%]	RDE[%]	D[$\mu\text{m}\sqrt{\text{cm}}$]	EF[V/cm]	L/D	L/D $\times\sqrt{E}$
DME	0.69	0.63	0.72	600	0.958333	0.760654
NE	1.91	0.96	16.33	41	0.116963	0.114599
CO2	0.85	0.89	1.04	270	0.817308	0.771047
He	10.5	0.001	5.75	60	1.826087	0.057746
Ar	0.39	4.03	14.39	250	0.027102	0.054407
CH4	1.87	0.12	4.31	15	0.433875	0.150299
DME+CO2	0.76	0.76	1.02	280	0.745098	0.649561
DME+Ne	1	1	1	307	1	1
DME+Ar	0.30	3.23	0.99	300	0.30303	0.544612
DME+CH4	0.96	0.34	0.98	315	0.979592	0.571195

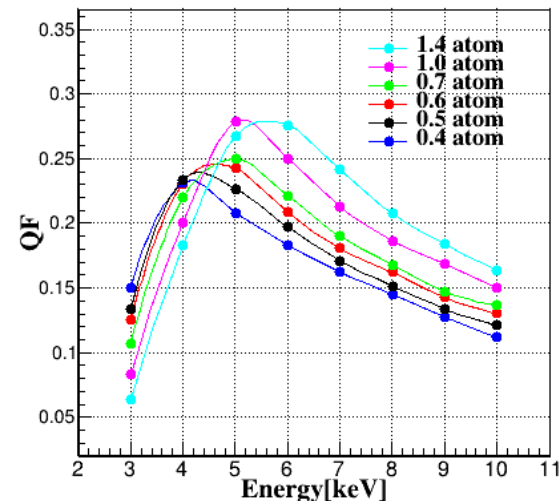
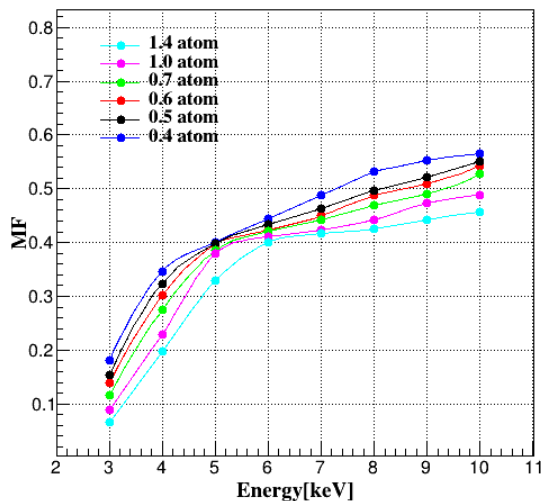
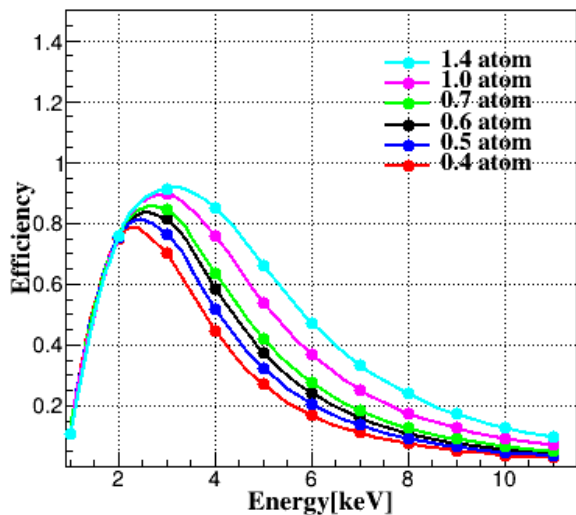
L=Length RDE=Relative Detection Efficiency D=Diffusion EF= Electric Field

Optimization



Pressure scan

0.5DME+0.5Ne, 10 cm



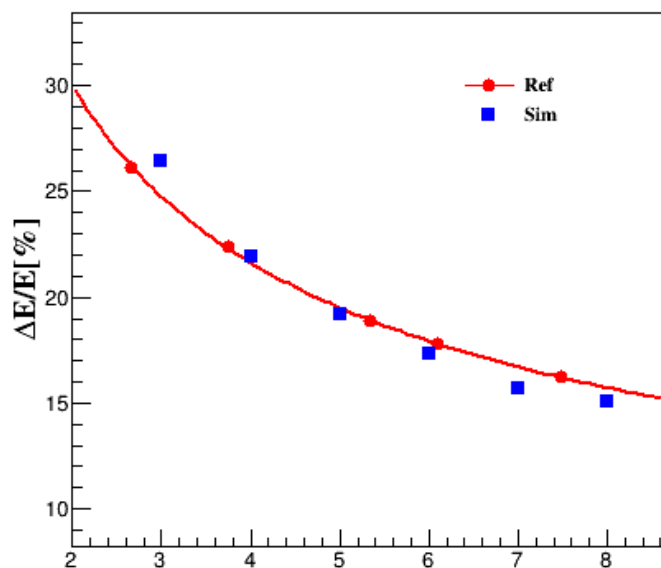
- MF > 0.4 @ 6keV as pressure < 1 atom



Energy resolution

spectrum

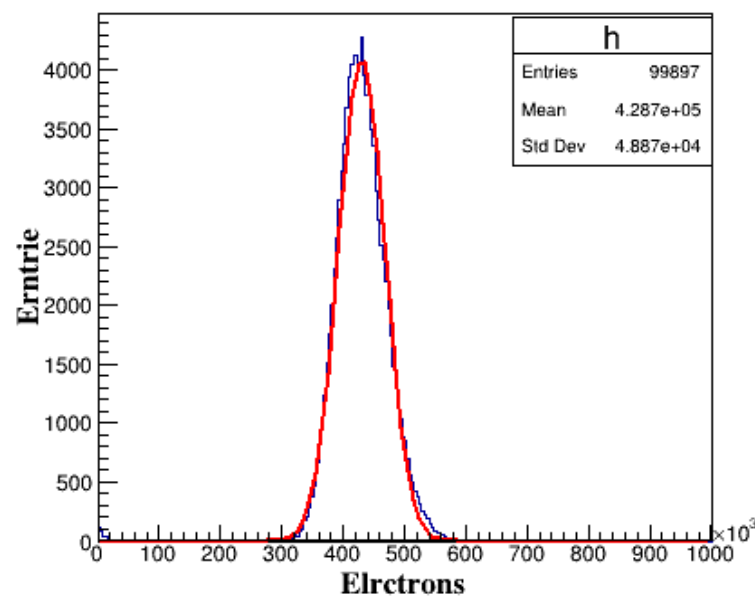
DME 0.8 atom



6 keV, 0.5DME+0.5Ne

Sim 20.7%

Ref 20%



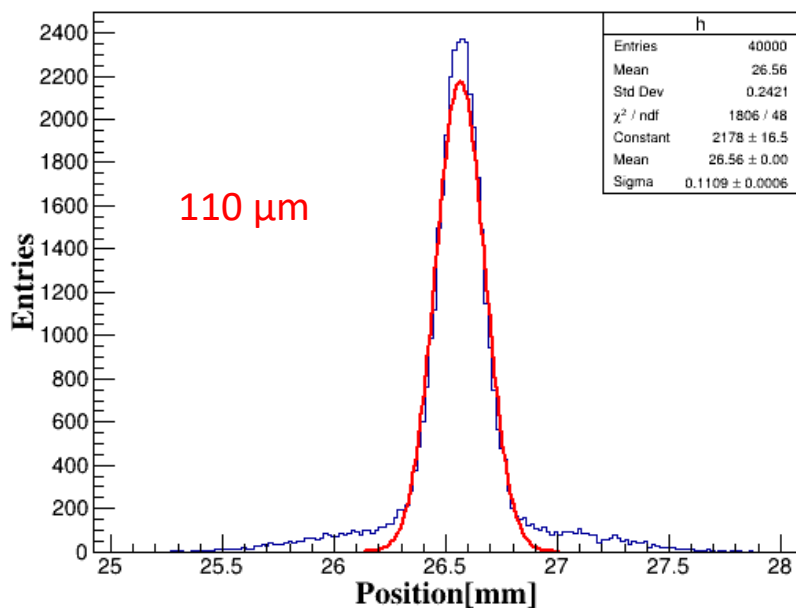
- Energy resolution < 30% @6keV for both of them

Position resolution

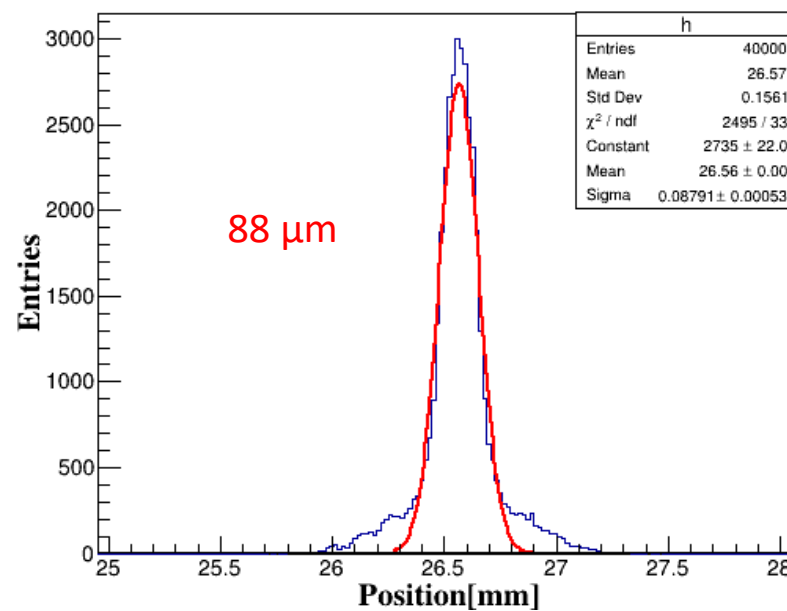


5 keV

DME 0.25 atom



0.5DME+0.5Ne 0.6atom



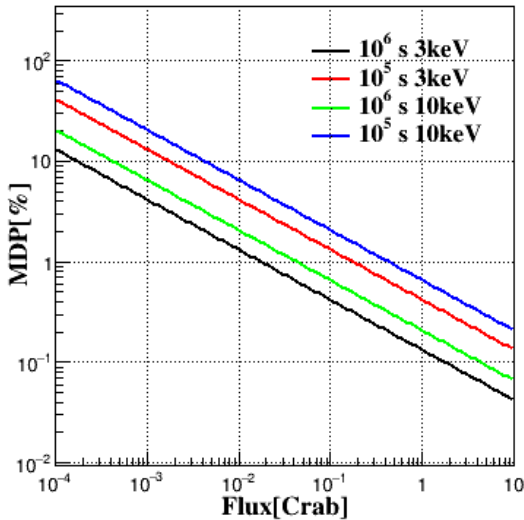
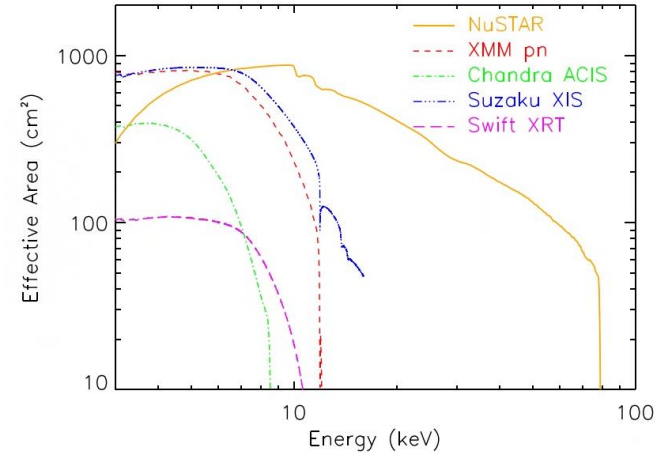
- Position resolution $< 140 \mu\text{m}$ for both of them without rotation



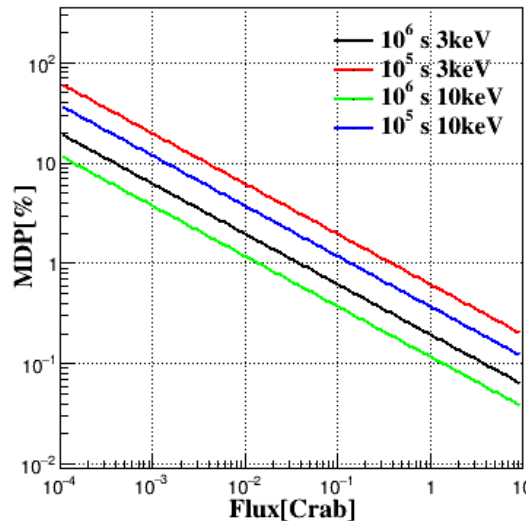
Refer NuSTAR focus mirror

- $305 \text{ cm}^2 @ 3 \text{ keV}$, $780 \text{ cm}^2 @ 10 \text{ keV}$
- QF 0.185 @ 3 keV, DME, 0.25atom
- QF 0.074 @ 10 keV, DME, 0.25atom
- QF 0.125 @ 3 keV, DME+Ne, 0.6atom
- QF 0.130 @ 10 keV, DME+Ne, 0.6atom

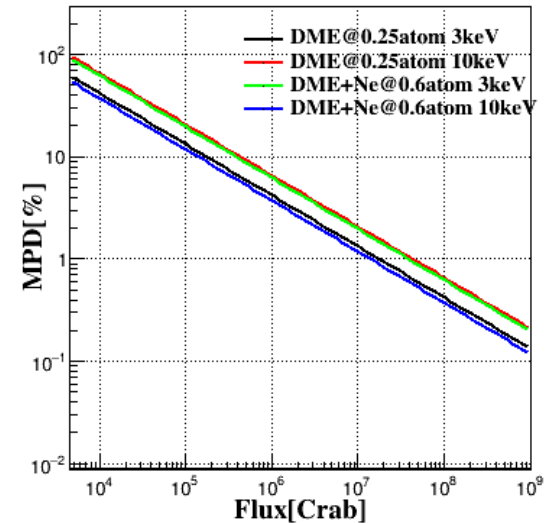
$$\text{MDP} = \frac{4.29}{\mu \sqrt{F_s A_{\text{eff}} \epsilon T}}$$



DME, 0.25atom



DME+Ne, 0.6atom



1 mCrab

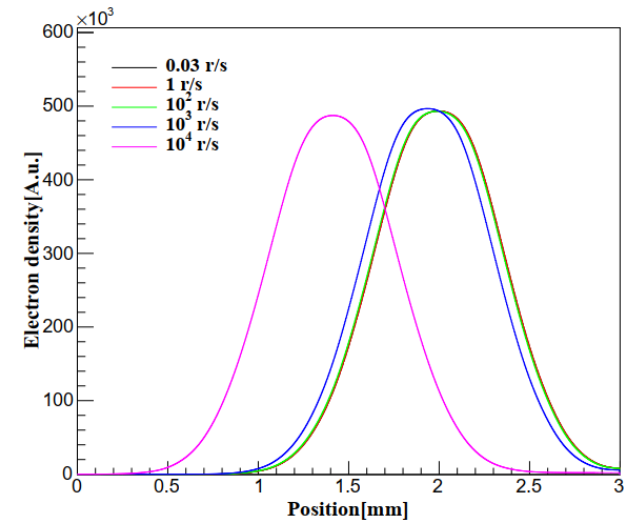
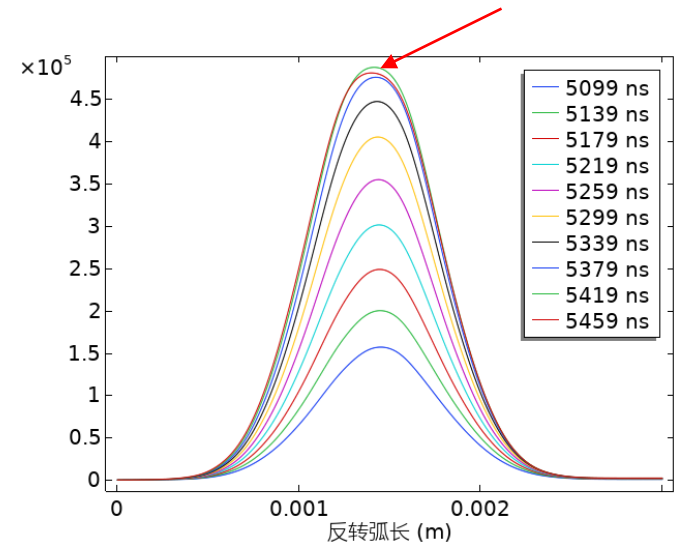
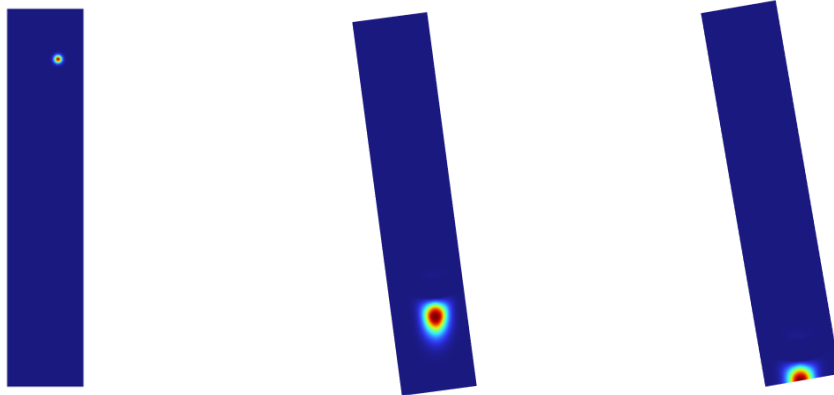


Rotate mode

Dependence of angular velocity and optimization

- Hard to evaluate distortion for each electron
- average behavior
- Initial position at point (2 mm, 13 mm)
- DME@0.25atom, 196V/cm

r.p.s	10000	1000	100	1	0
Position [μm]	586.10	59.74	7.06	1.25	1.19
Timing [ns]	12	6	1	<1	<1

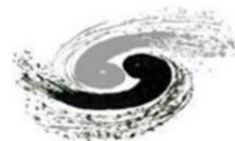


Summary



- Distance between beryllium window and GEM >0.3 cm
- Drift depth is 2 cm (limited on size of Be)
- Height of the TPC > 2.2 cm
- Depth of the TPC is 10 cm (f=10 m)

- DME or 0.5MDE+0.5Ne is good choice, both of them can satisfy $MF > 0.4 @ 6 \text{ keV}$
- Position resolution <140 μm without rotating mode
- Pure DME is better for X-ray observation at low energy (< 4 keV)
- 0.5MDE+0.5Ne is better for X-ray observation at high energy (4 ~10 keV)
- Little impact on photoelectric imaging with rotating mode



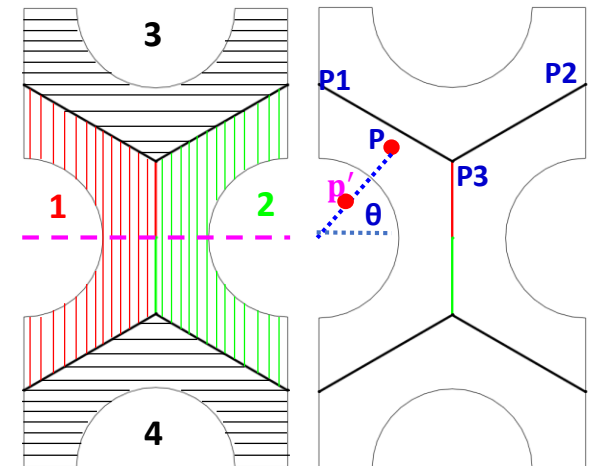
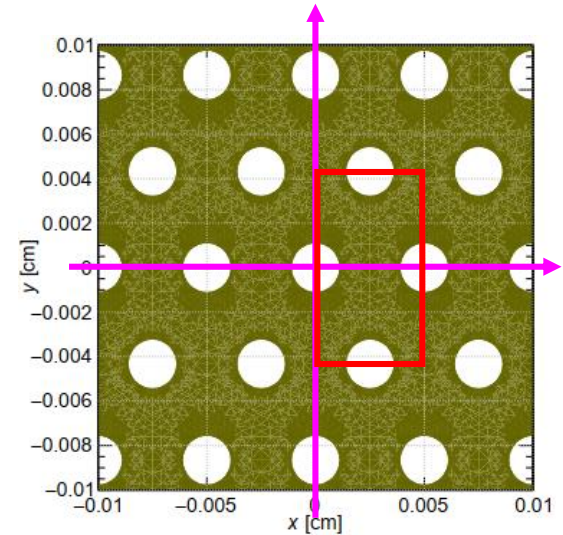
Back up

Sample generation



Fast simulation

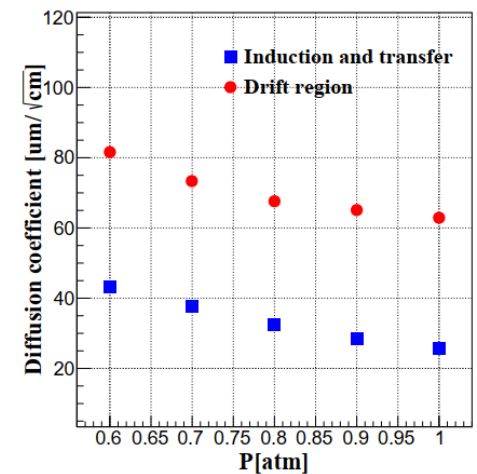
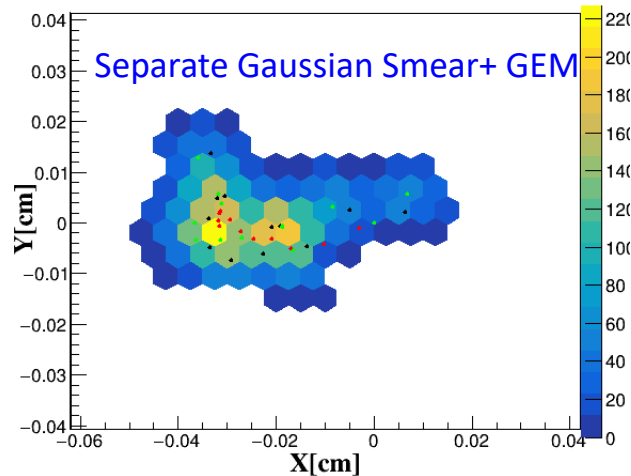
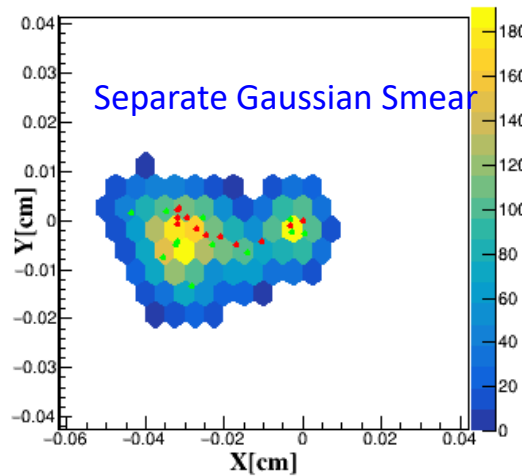
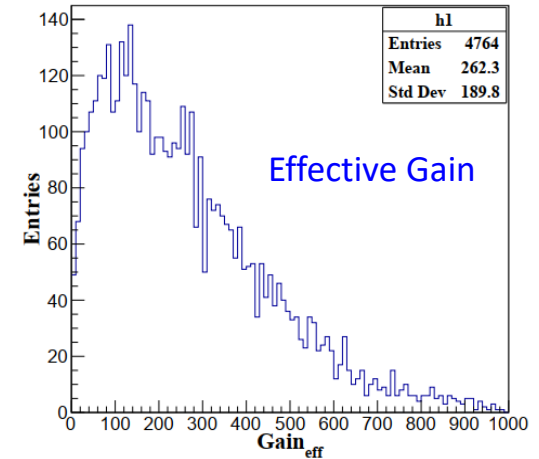
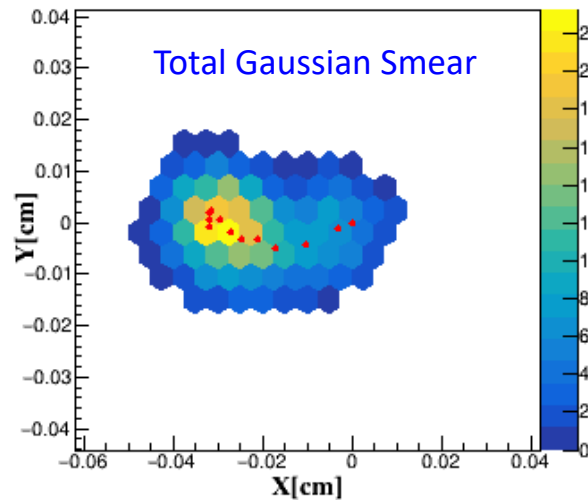
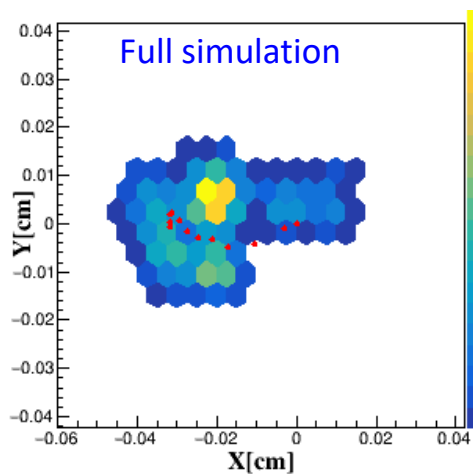
- Sampling point $P(x,y)$
- Find the related minimal period region (MPR)
- Judge the upper/lower part of the MPR
- Find the boundary point $P1,P2,P3$
- Give the boundary linear
- Compare the value of the point (x,y) with the boundary linear
- Obtain the nearest GEM hole coordinate $P0$
- Calculate the ratio R of distance $[P,P0]$ over distance $[P1,P2]$
- Calculate the angle θ and the radius r ,
 $r=R \times R_a$ (the radius of GEM hole)
- Obtain the initial multiplier point p'



Sample generation



Image Generation

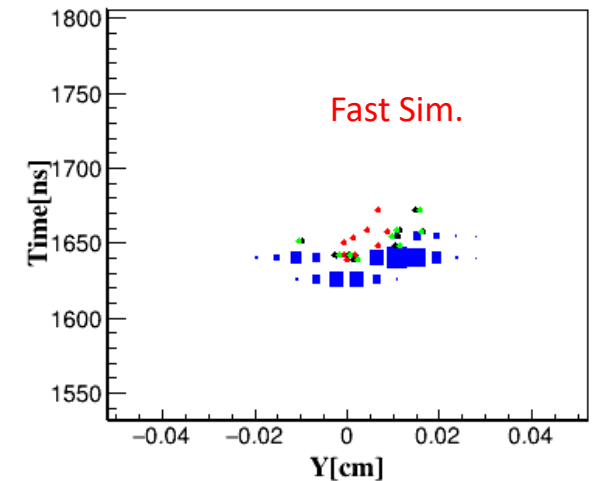
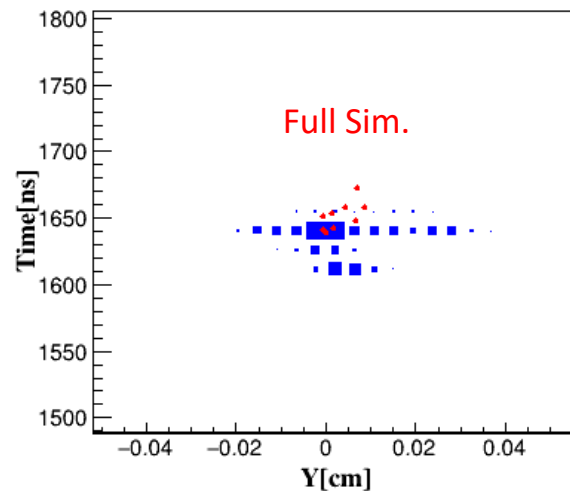
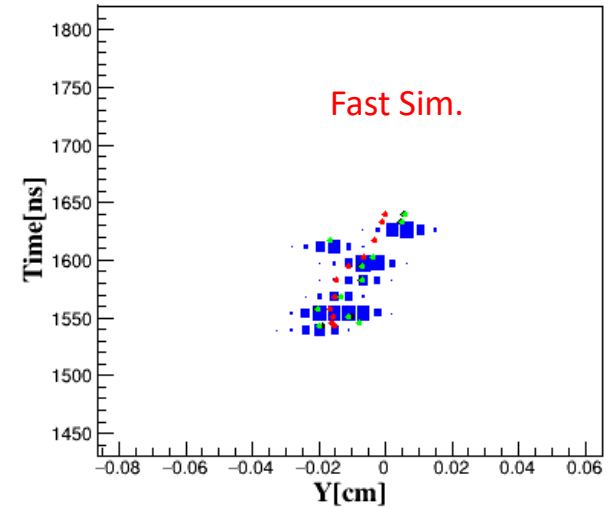
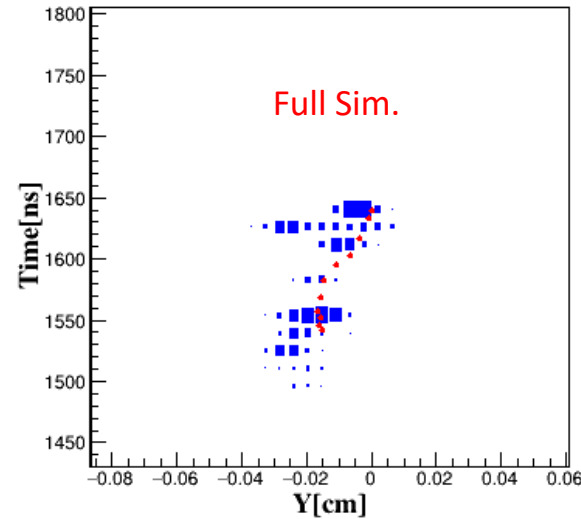


Sample generation



Fast simulation

- **Input parameters**
 - GEM pitch D
 - GEM hole R
 - GEM plane H
 - Read-out plane h
 - Effective gain G
 - Standard deviation σ_G
 - Diffusion coefficient σ_D
 - Drift velocity v_D
 - Induction region σ_I
 - Induction region v_I



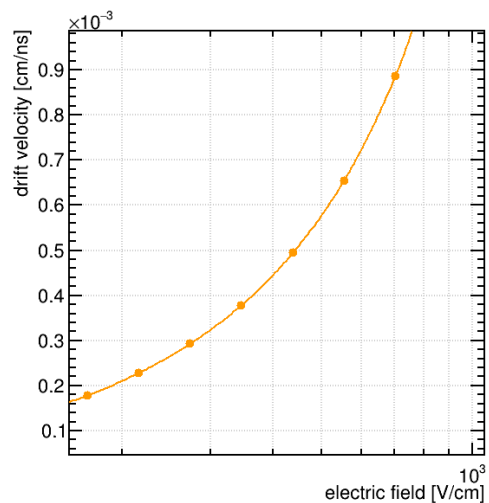


Sample generation

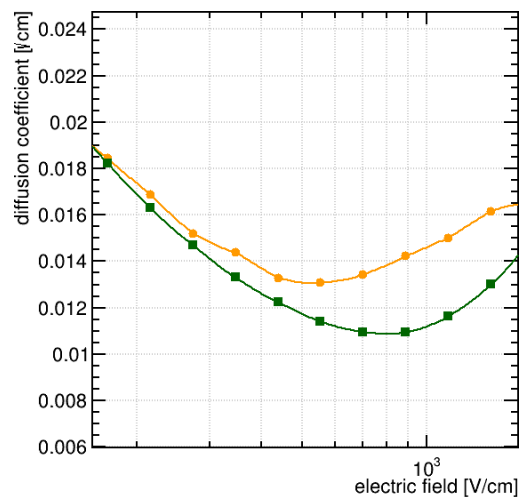
Input parameters

0.5DME+0.5Ne, 0.6 atom,

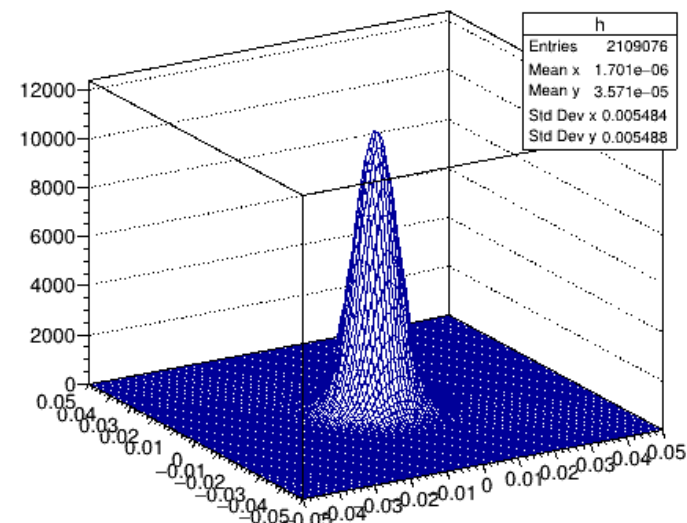
Drift velocity 3.3mm/us



Diffusion $0.0140\sqrt{cm}$



Diffusion 0.005 cm



Pressure



Parameters scan

4 keV, 0.5DME+0.5Ne, 0.33 cm/us, 10 cm

Gas	L [%]	RDE[%]	D[$\mu\text{m}\sqrt{\text{cm}}$]	EF[V/cm]	L/D	L/D $\times\sqrt{E}$
0.3	0.411	0.36	200	150	1.431343	0.858806
0.4	0.308	0.44	173	200	1.240043	0.822551
0.5	0.241	0.52	153	250	1.097129	0.791151
0.6	0.201	0.58	140	300	1	0.761577
0.7	0.171	0.64	127	356	0.937831	0.750264
0.8	0.148	0.68	121	408	0.851939	0.702527
0.9	0.131	0.72	114	464	0.800384	0.679148
1	0.115	0.75	107	510	0.748593	0.648301
1.1	0.106	0.78	101	563	0.730998	0.6456
1.2	0.096	0.81	98	612	0.682303	0.614072
1.3	0.088	0.83	95	658	0.645195	0.587801
1.4	0.081	0.85	90	710	0.626866	0.577942

Charge behavior model



- Combination of charges and electric field

$$\frac{\partial \rho}{\partial t} = -\vec{\nabla} \cdot (\rho \vec{v} - D \vec{\nabla} \rho) + R$$

ρ is the unknown

$$\rho_v = \frac{Q_e}{\epsilon_0} (n_i - n_e)$$

For what concerns the boundary conditions, some examples

$$\vec{n} \cdot \vec{J}^{tot} = 0$$

No flux

$$-\vec{n} \cdot \vec{J}^{tot} = \Phi(\vec{x}, t)$$

Input flux

$$\vec{n} \cdot \vec{J}^{diff} = 0$$

Output

$$\rho = \Psi(\vec{x}, t)$$

Concentration

$$\vec{\nabla} \cdot \vec{D} = \rho$$

$$\vec{D} = \epsilon \vec{E}$$

$$\vec{E} = -\vec{\nabla} V$$

$$\vec{\nabla} \cdot \epsilon \vec{\nabla} V = -\rho$$

$$R = n_e u (\alpha - C_a - X)$$