



# The lattice design of SppC collider ring

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# Content



- SppC lattice design and nonlinearity optimization
- Error correction scheme
- Geometric compatibility between CEPC and SppC



# SppC parameters



Parameter	Value	Unit
<b>General design parameters</b>		
Circumference	100	km
Beam energy	62.5	TeV
Lorentz gamma	66631	
Dipole field	20	T
Dipole curvature radius	10415.4	m
Arc filling factor	0.78	
Total dipole magnet length	65.442	km
Arc length	83.9	km
Number of long straight sections	8	
Total straight section length	16.1	km
Energy gain factor in collider rings	19.53	
Injection energy	3.2	TeV
Number of IPs	2	
Revolution frequency	3.00	kHz
<b>Physics performance and beam parameters</b>		
Initial luminosity per IP	$4.3 \cdot 10^{34}$	$\text{cm}^{-2}\text{s}^{-1}$
Beta function at collision	0.50	m
Circulating beam current	0.19	A
Nominal beam-beam tune shift limit per IP	0.015	
Bunch separation	25	ns
Number of bunches	10080	
Bunch population	$4.0 \cdot 10^{11}$	
Accumulated particles per beam	$4.0 \cdot 10^{15}$	
Normalized rms transverse emittance	1.2	mm
Beam life time due to burn-off	8.1	hours
Total inelastic cross section	161	mb
Reduction factor in luminosity	0.81	
Full crossing angle	73	mrاد
rms bunch length	60	mm
rms IP spot size	3.0	mm
Beta at the first parasitic encounter	28.6	m
rms spot size at the first parasitic encounter	22.7	mm
Stored energy per beam	4.0	GJ
SR power per beam	2.2	MW
SR heat load at arc per aperture	26.3	W/m
Energy loss per turn	11.4	MeV

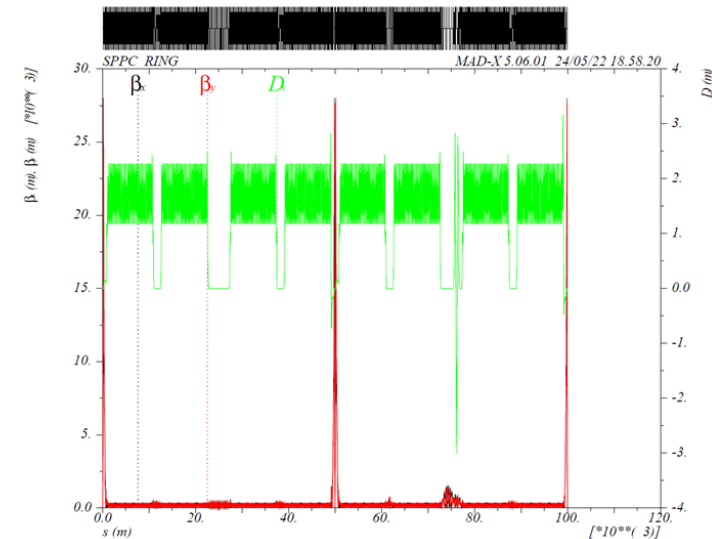
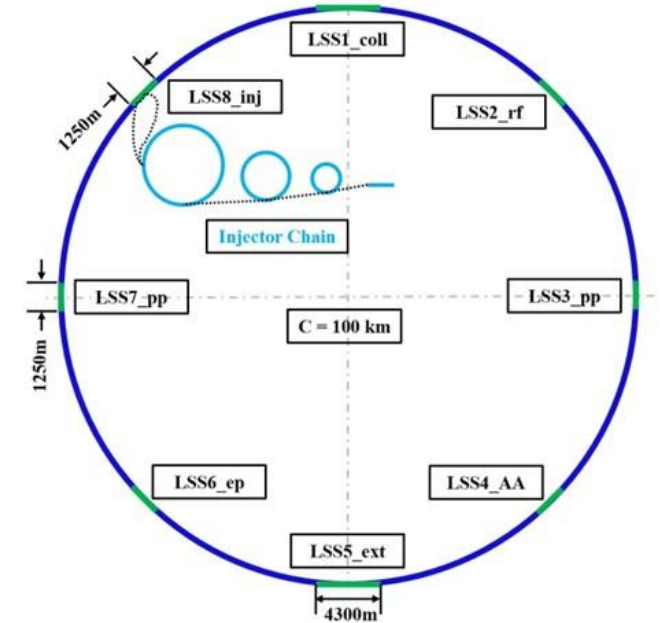
\*CEPC TDR



# SppC lattice design



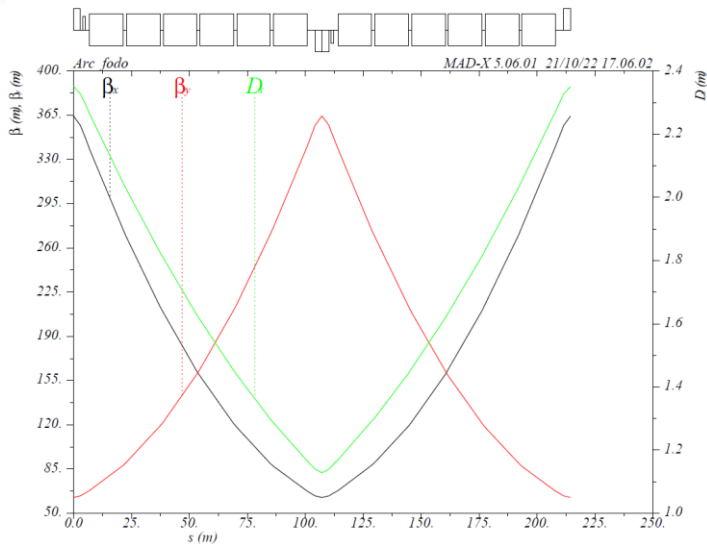
- Compatible with CEPC, 100km, 2 IPs
- 8 arc sections
  - 2-in-1 yoke-sharing magnets
  - both interleaved and non-interleaved sextupoles studied
- 4 short straight sections
  - RF region, dual-harmonic RF system (800 and 400 MHz)
  - injection section after injection chain
  - Space reserved for e-p collision
- 2 long straight sections
  - collimation section for both betatron and momentum
  - extraction section
- 2 interaction regions
  - anti-symmetric interaction region
  - chromaticity corrected with arc sextupoles



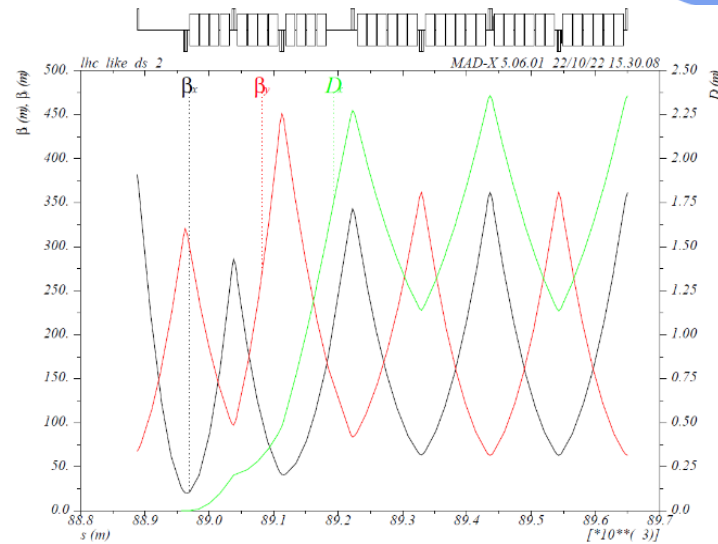




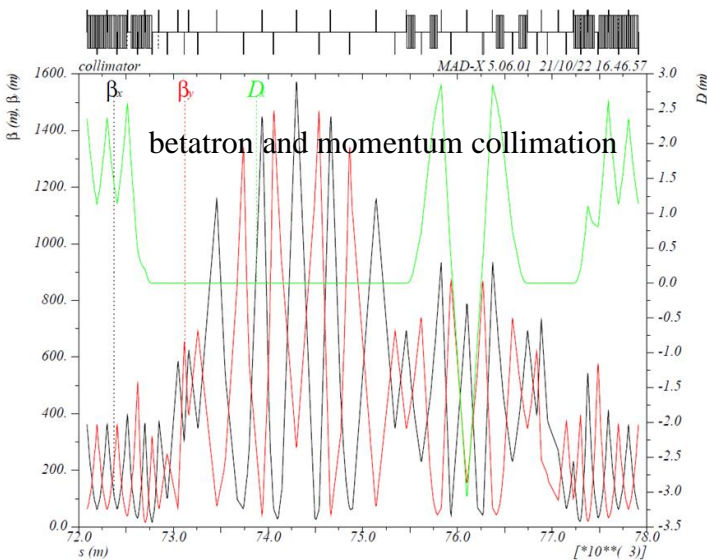
# Lattice optics



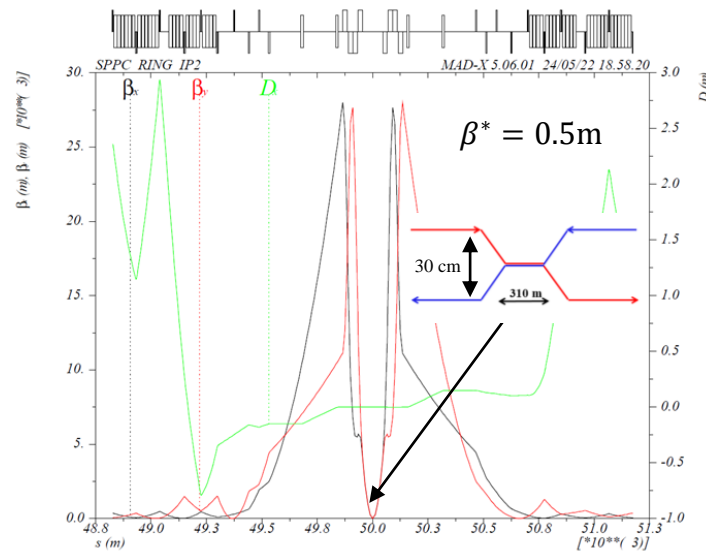
Arc FODO cell



Dispersion suppressor



Collimation section



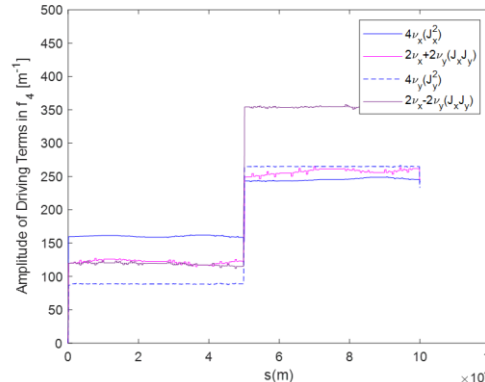
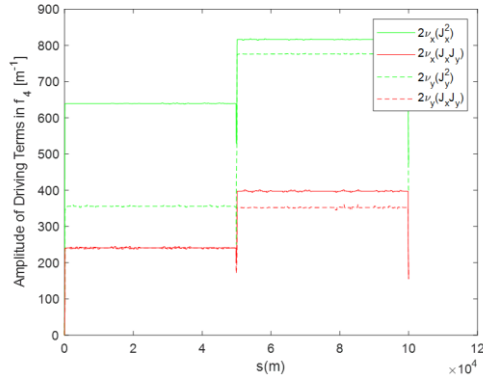
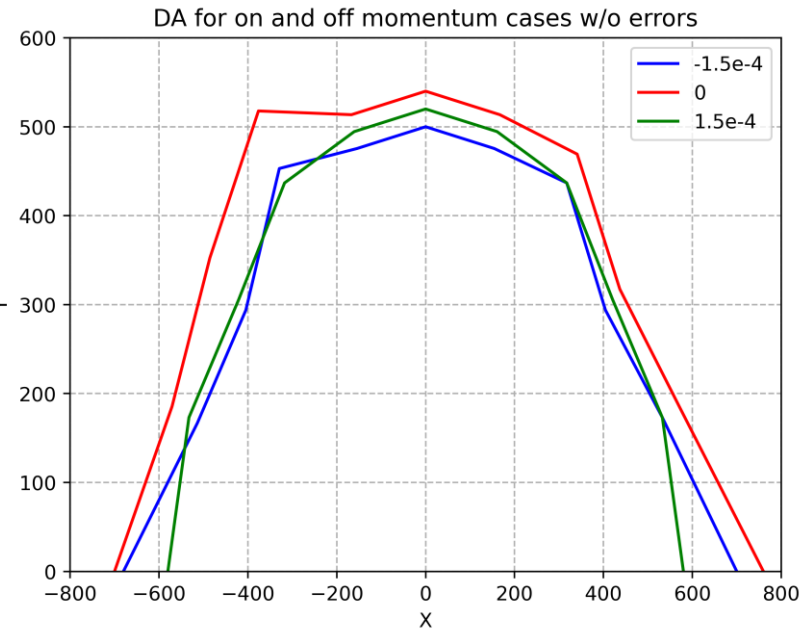
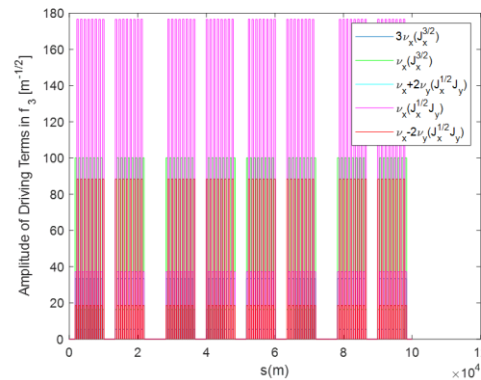
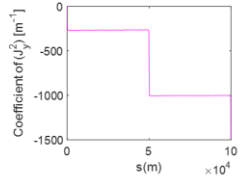
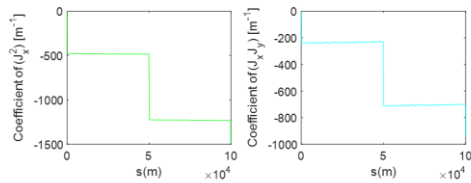
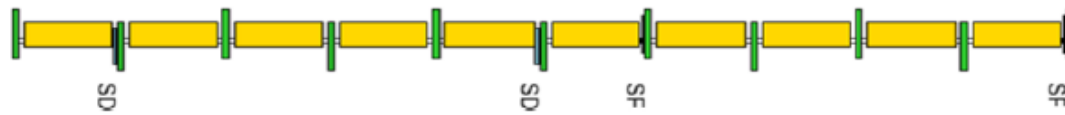
Interaction region



# Nonlinearity optimization with non-interleaved sextupoles



- 5 FODO cells per period. Most nonlinearities are cancelled in 4 periods and the tune shifts are significantly reduced compared with the interleaved scheme.
- Since the number of sextupoles is less than interleaved scheme, the sextupoles in arc will be stronger, thus the length of sextupoles is doubled to 1m to weaken the sextupoles.



Tune shift coefficients and RDTs



# Content



- SppC lattice design and nonlinearity optimization
- **Error correction scheme**
- Geometric compatibility between CEPC and SppC



# SppC lattice error table



- Gaussian distribution, and truncated at  $3\sigma$ ;
- The table at top energy is similar with that at collider energy, except some field errors due to residual circuit caused by ramping down.

Element	Error	Error desc.	Units	Main dipole	Separation dipole
Dipole	$\sigma(x), \sigma(y)$		mm	0.5	0.5
	$\sigma(\psi)$	roll angle	mrad	0.5	0.5
	$\sigma(\delta B/B)$	random b1	%	0.1	0.05
	$\sigma(\delta B/B)$	random b2	$10^{-4}$ units	0.9	0.1/1.1
	$\sigma(\delta B/B)$	random a2	$10^{-4}$ units	1.0	0.1/0.2
	$\sigma(\delta B/B)$	uncert. a2	$10^{-4}$ units	1.0	TBD
				Main quadrupole	IR triplet / other
Quad.	$\sigma(x), \sigma(y)$		mm	0.5	0.15/0.5
	$\sigma(\psi)$	roll angle	mrad	0.5	0.05/0.5
	$\sigma(\delta B/B)$	random b2	%	0.1	0.005/0.1
BPM	$\sigma(x), \sigma(y)$		mm	0.2	0.2
	$\sigma(\text{read})$		mm	0.05	0.05

\*Reference radius of field error is 17 mm.

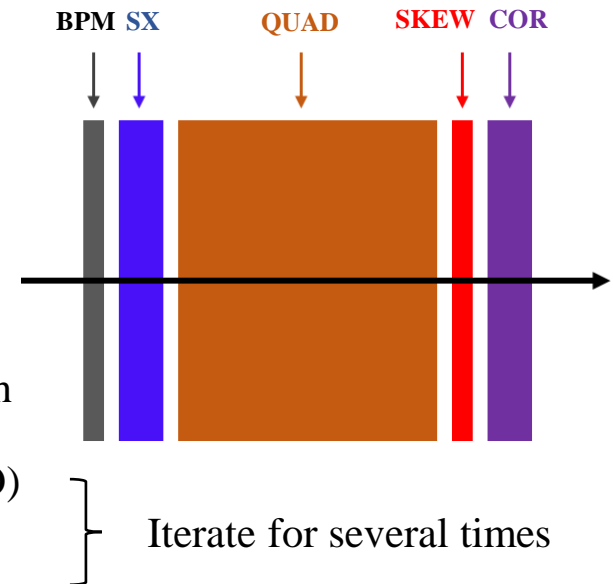


# SppC lattice correction scheme



## Based on response matrix method

- Software: Accelerator Toolbox (AT) on MATLAB
1. Apply the errors
  2. First turn trajectory correction
  3. Closed orbit correction with increasing sextupole strength
  4. Beta-beating and horizontal dispersion correction (LOCO)
  5. Coupling and vertical dispersion correction
  6. Tune and chromaticity correction



Response matrix represents the relationship between the strength variation of the dipole correction magnet in the storage ring and the resulting closed orbit distortion of the beam:

$$\begin{pmatrix} \Delta x \\ \Delta y \end{pmatrix} = R \begin{pmatrix} \Delta \theta_x \\ \Delta \theta_y \end{pmatrix}$$



# SppC lattice correction scheme



938 BPMs and 477 dipole correctors installed near the quadrupoles in the ring.

## First turn trajectory correction:

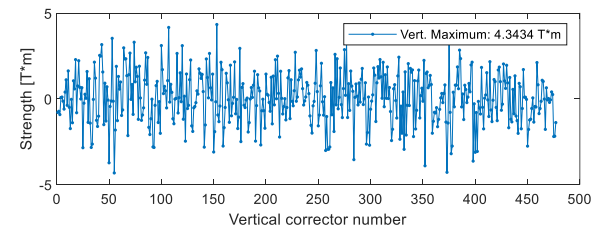
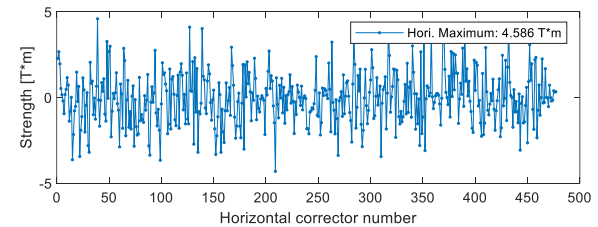
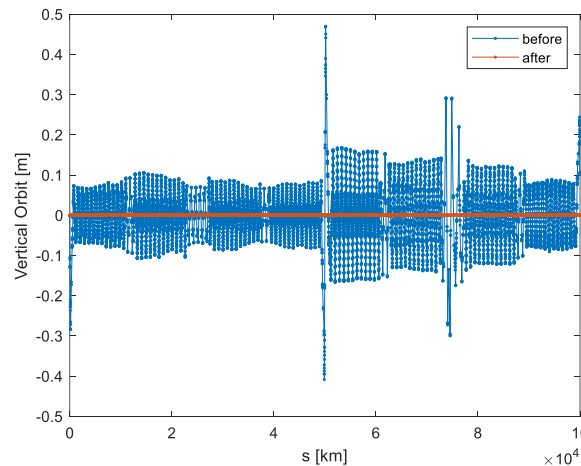
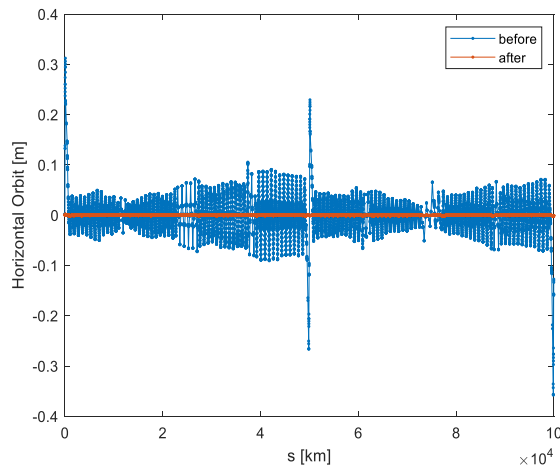
- Use BPMs and dipole correctors to find the closed orbit, 85% of the machines with errors can be corrected successfully in this step.

## Closed orbit correction:

- Solve the equation with the response matrix of lattice:  $\vec{u} + A\vec{\theta} = \mathbf{0}$

$\vec{u}$ : vector of orbit at BPM, A: response matrix,  $\vec{\theta}$ : vector of corrector strength

- Sextupole off, then after each 10% increase, the closed orbit is corrected once until the set value is reached.



$COD_{x,y,rms} < 0.4 \text{ mm}$

Comparison of closed orbit before and after correction

Corrector strength less than 5 T\*m



# SppC lattice correction scheme

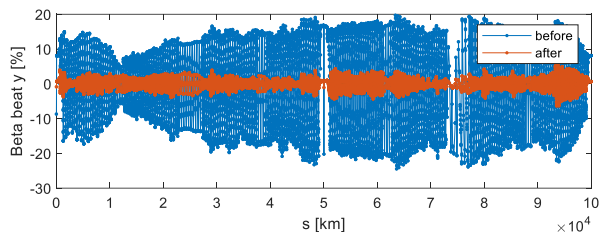
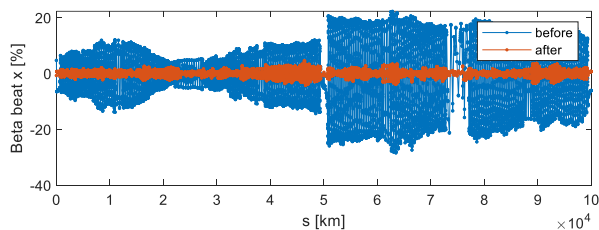


## Beta-beating and horizontal dispersion correction:

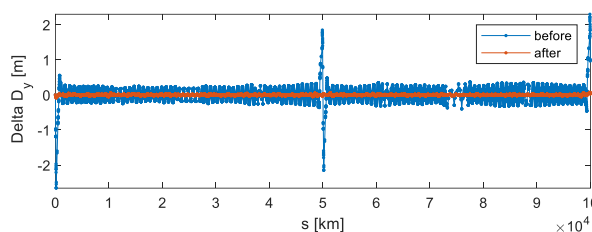
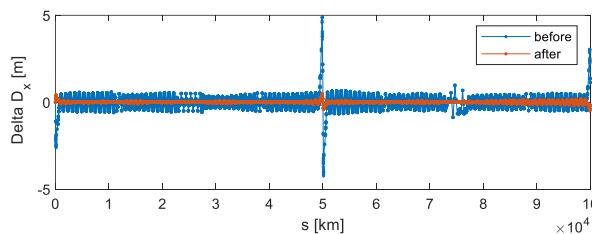
- Use the LOCO program to fit the response matrix itself.
- Minimize the difference between measured and theoretical response matrix by varying the quadrupole strength to correct the beam envelope function:

$$\chi^2 = \sum_{ij} \frac{(M_{meas,ij} - M_{model,ij})^2}{\sigma^2}$$

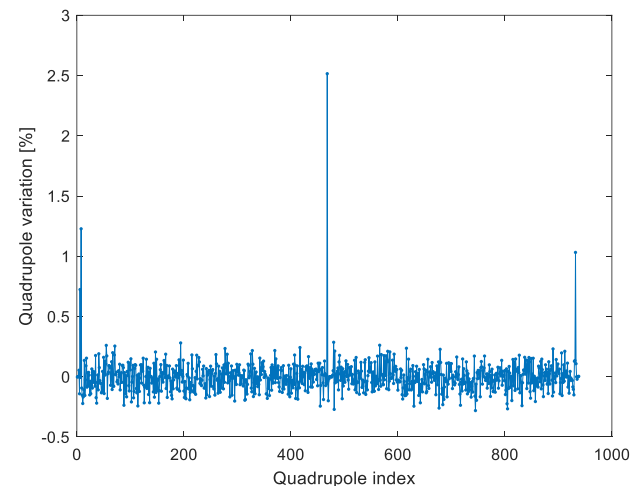
$\sigma$ : BPM noise given by multiple measurements of BPMs.



Beta-beating  
before and after correction



Dispersion deviation  
before and after correction



Quadrupole variation **less than 3%**



# SppC lattice correction scheme

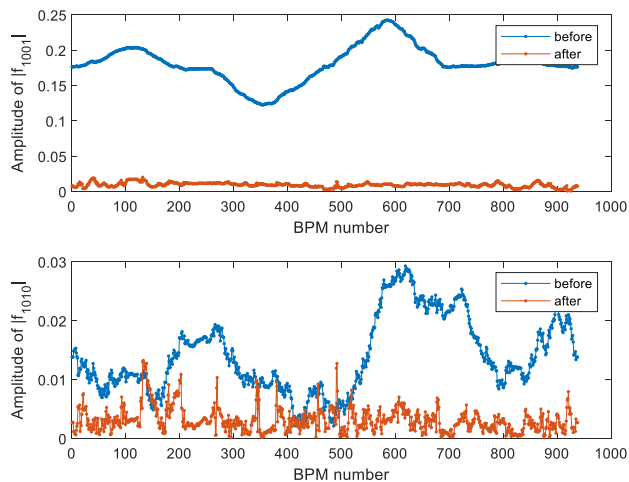


## Coupling and vertical dispersion correction:

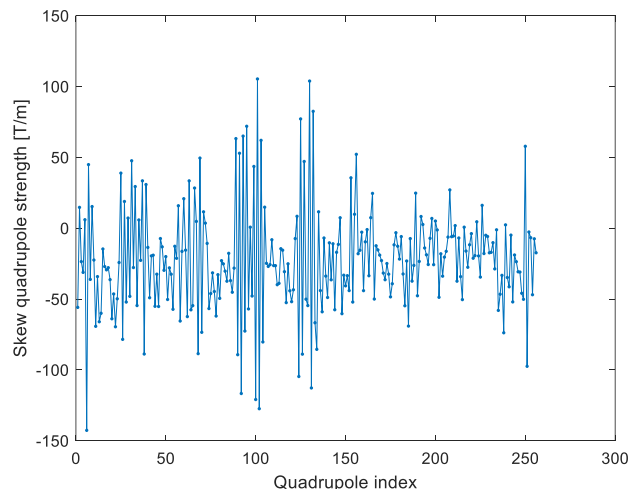
- Correct the linear coupling RDTs by the skew quadrupoles in lattice:

$$\begin{pmatrix} \overrightarrow{f_{1001}} \\ \overrightarrow{f_{1010}} \\ \overrightarrow{D_y} \end{pmatrix}_{meas} + M \overrightarrow{K_s} = \mathbf{0}$$

- $f_{1001}$  and  $f_{1010}$ : RDTs of difference and sum resonance, respectively;  $K_s$ : Skew quadrupole strength.
- Focus more on the correction of  $f_{1001}$  since the tune is close to difference resonance.



Linear coupling RDTs  
before and after correction



Skew quadrupole strength  
less than 150T/m





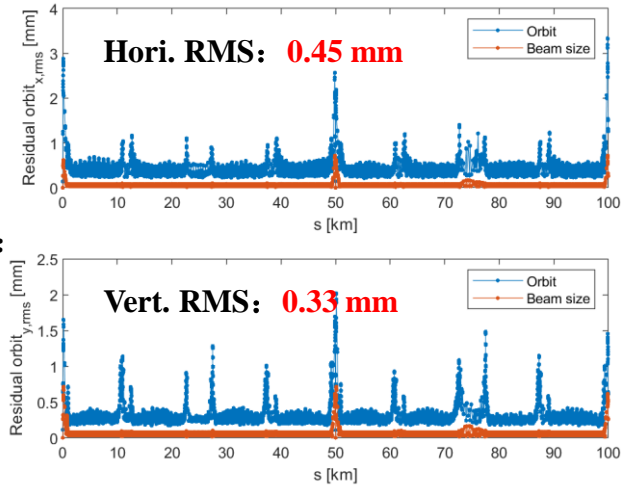
# SppC lattice correction results



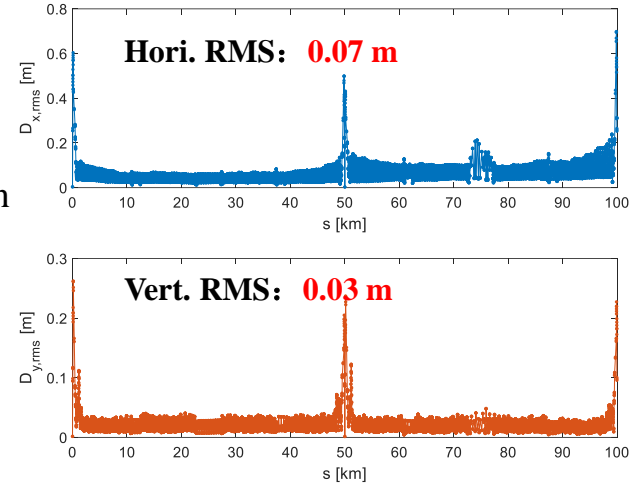
## For collision

- 84 of 100 machines successfully corrected. Figures show the RMS results of those machines.

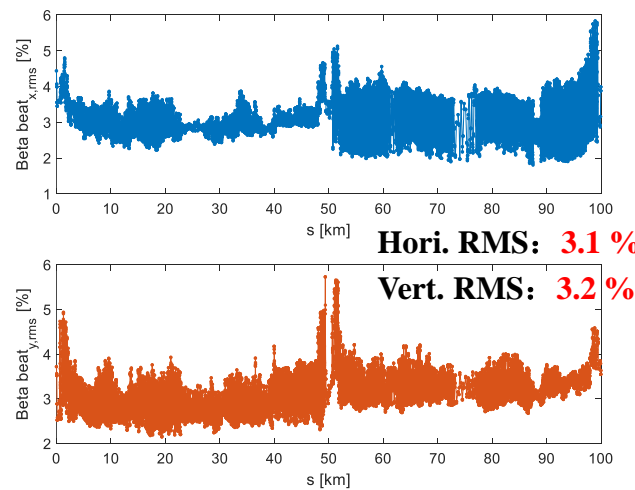
Residual orbit and beam size:



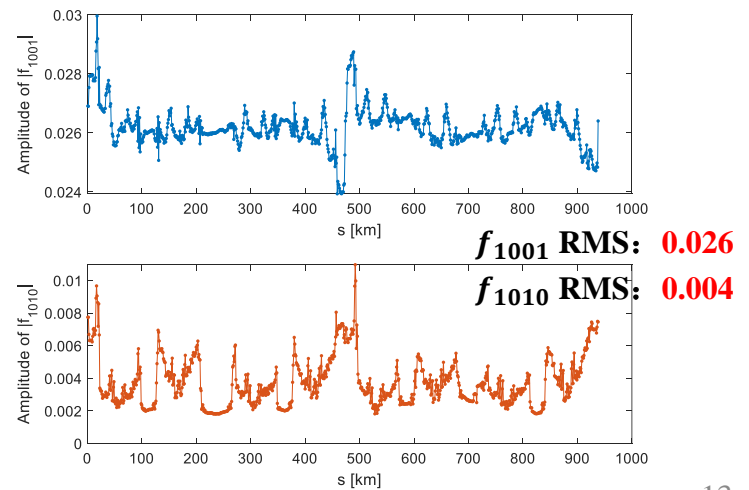
Dispersion deviation:



Beta-beating:



Linear coupling:



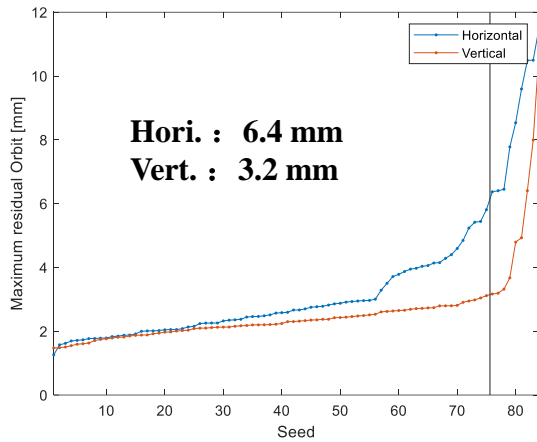


# SppC lattice correction results

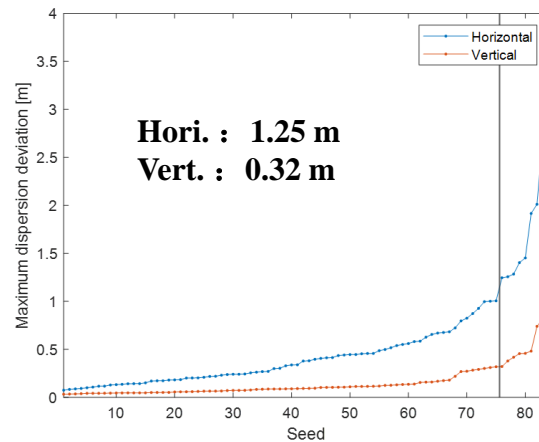


## For collision

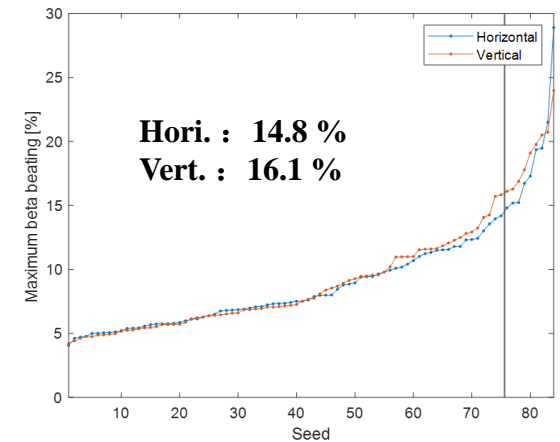
- From the maximum values distribution the 90-percentile is calculated over all 84 machines.



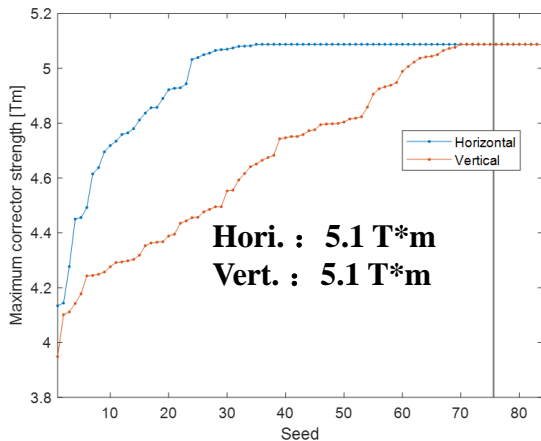
Residual orbit



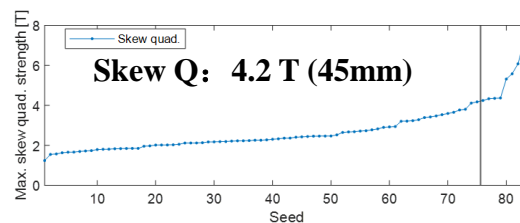
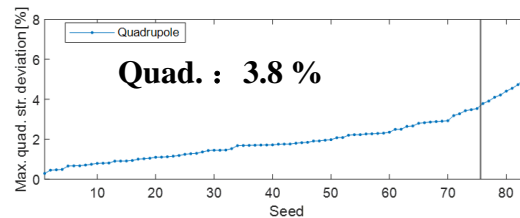
Dispersion deviation



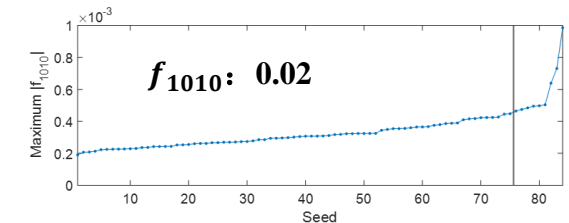
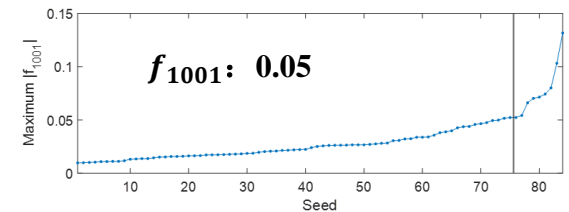
Beta-beating



Corrector strength



Quadrupole deviation and skew quadrupole strength



Linear coupling RDTs



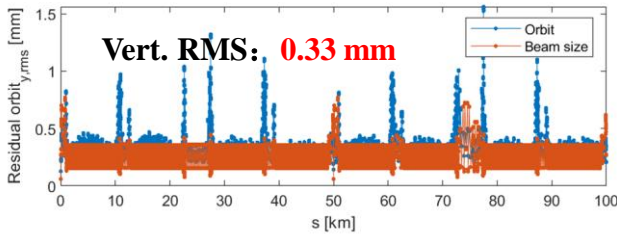
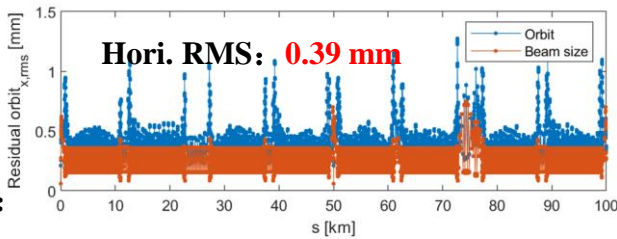
# SppC lattice correction results



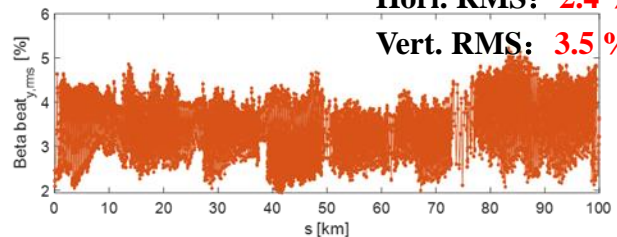
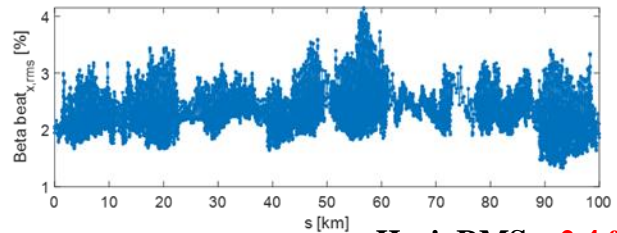
## For injection

- 82 of 100 machines successfully corrected. Figures show the RMS results of those machines.

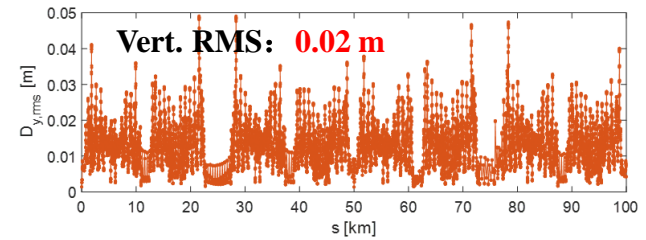
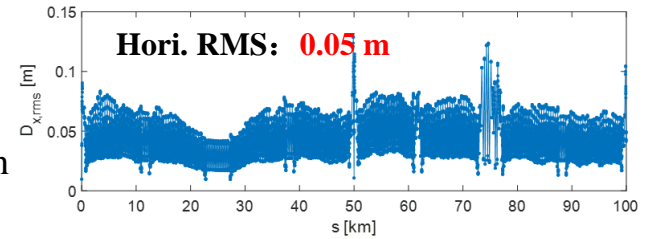
Residual orbit and beam size:



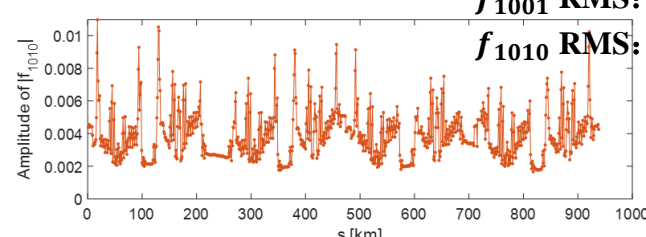
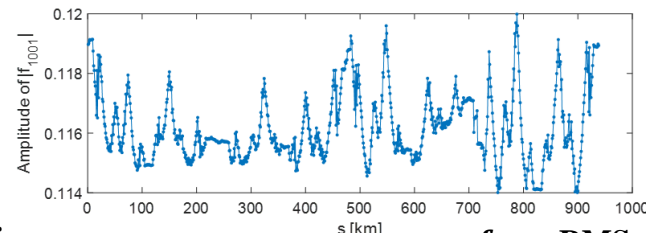
Beta-beating:



Dispersion deviation:



Linear coupling:



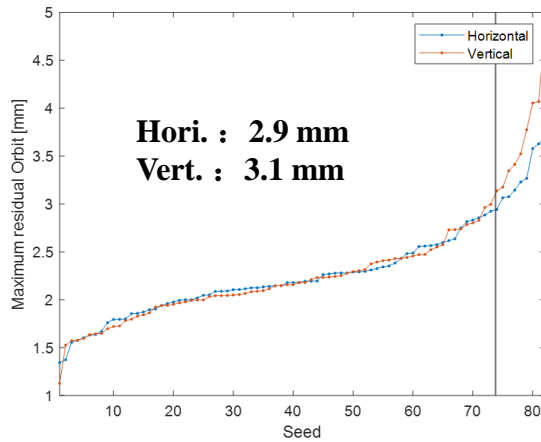


# SppC lattice correction results

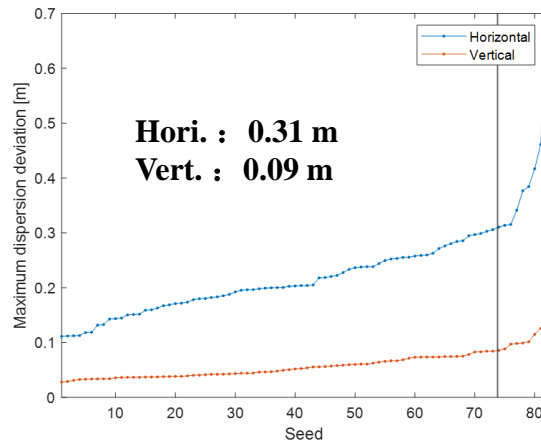


## For injection

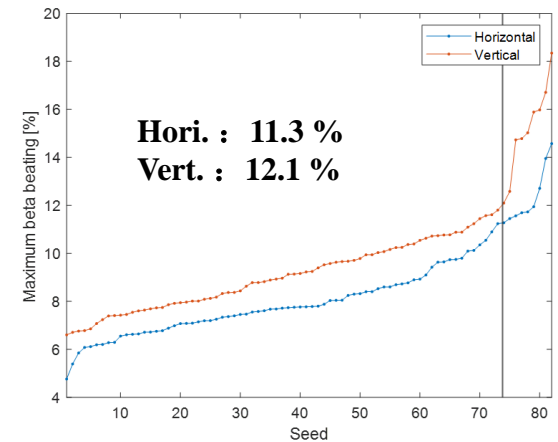
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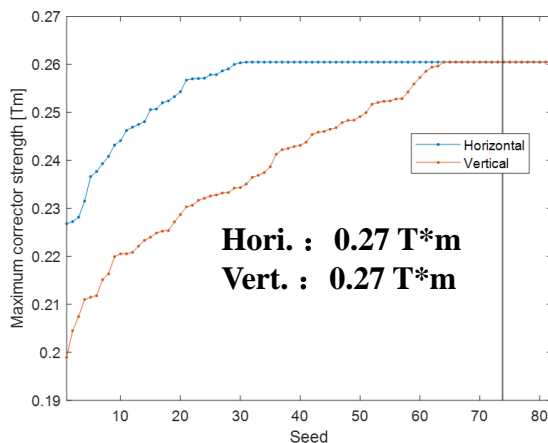
Residual orbit



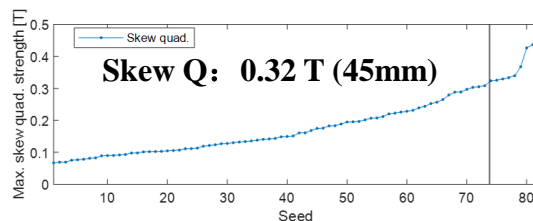
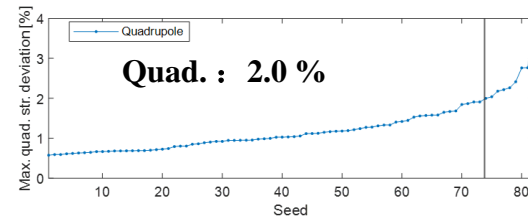
Dispersion deviation



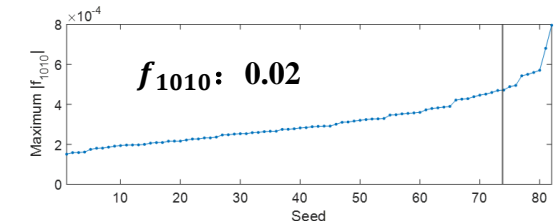
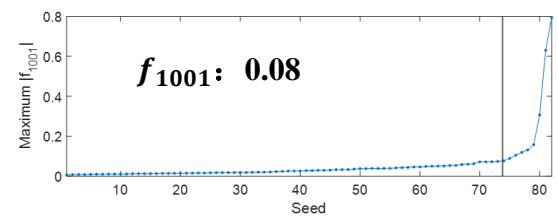
Beta-beating



Corrector strength



Quadrupole deviation and skew quadrupole strength



Linear coupling RDTs

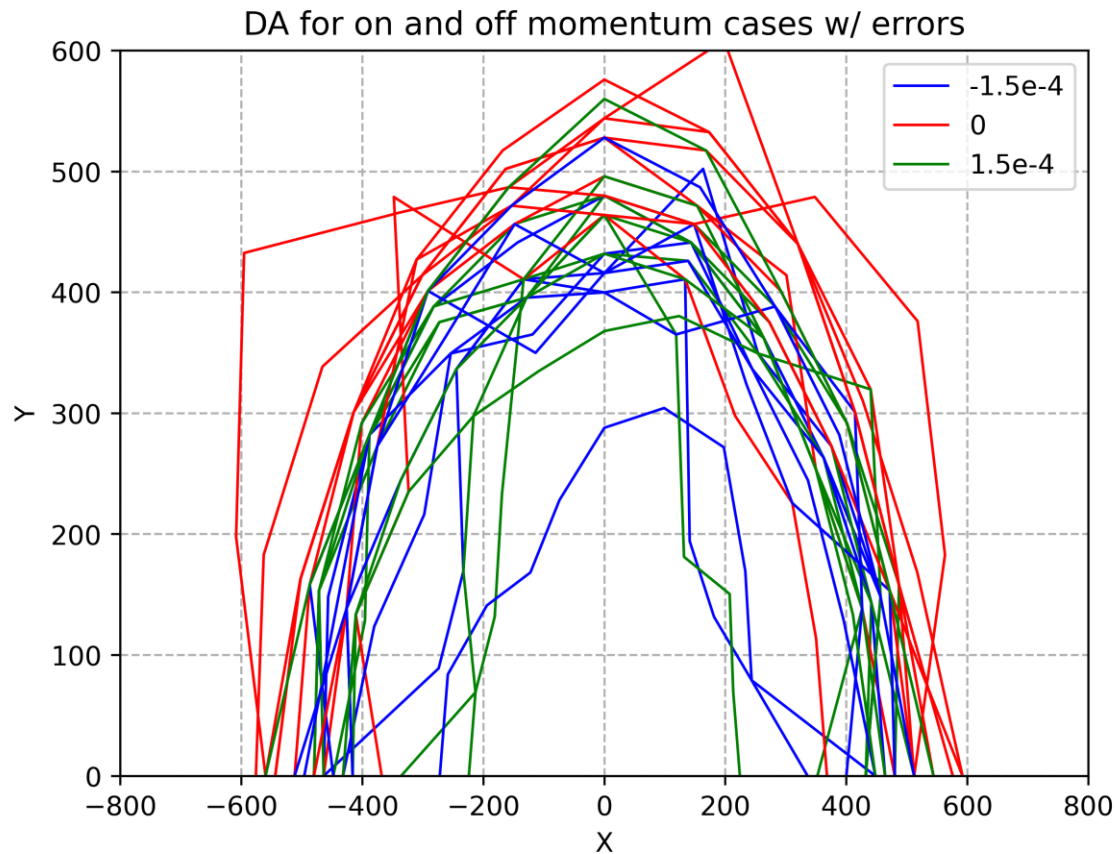


# Dynamic aperture



- Performed by SAD code, with error correction scheme and RF on;
- Tracking for 100,000 turns;
- Synchrotron radiation and beam-beam effect have not been included yet.

Can be further optimized





# Content



- SppC lattice design and nonlinearity optimization
- Error correction scheme
- Geometric compatibility between CEPC and SppC



# CEPC-SppC compatibility



- Geometry compatibility of the CEPC and SPPC
  - The SPPC will share the tunnel of CEPC as much as possible.
  - The SPPC locates outside of CEPC
  - In the 8 arc regions and 4 short straight sections, two machines share the tunnel (distance of machine centers=3.5m)
  - In the 4 long straight sections, the SPPC will bypass the CEPC (distance of machine centers at IPs=23m as the big size of CEPC and SPPC detectors)
    - IP1 and IP3 for CEPC interaction and SPPC collimation, IP2 and IP4 for CEPC RF and SPPC interaction

## Tunnel in the ARC

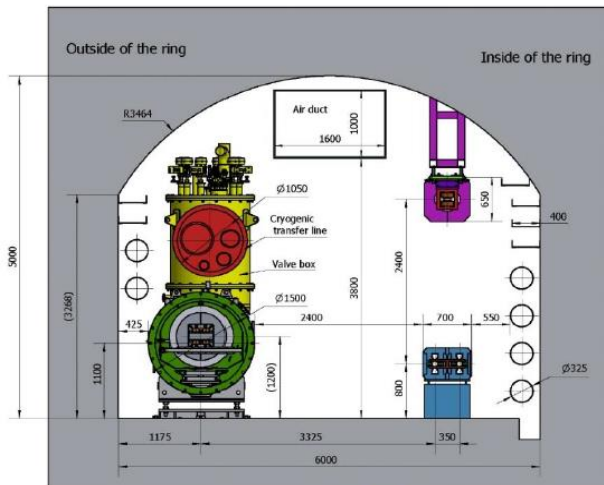
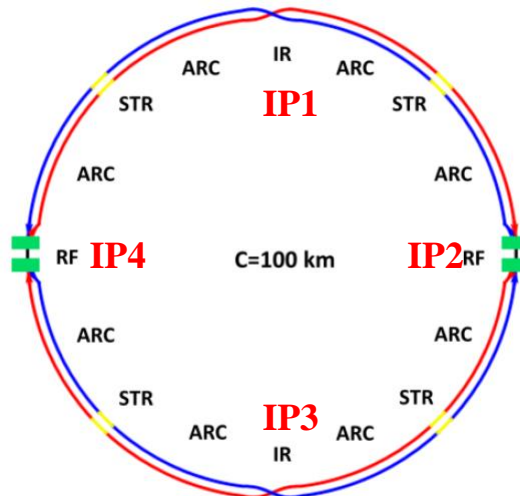
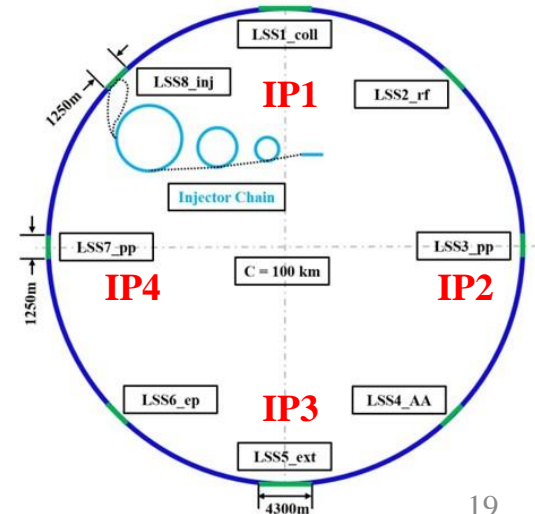


Figure 2.1: Tunnel cross section in the arc region

## CEPC Layout



## SPPC Layout





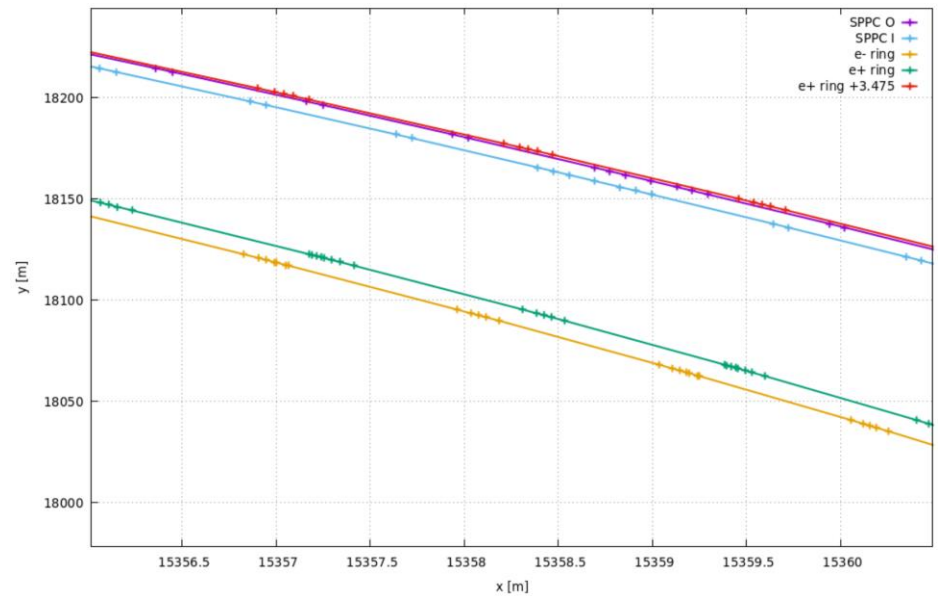
## With bypass

### SPPC updated to double ring:

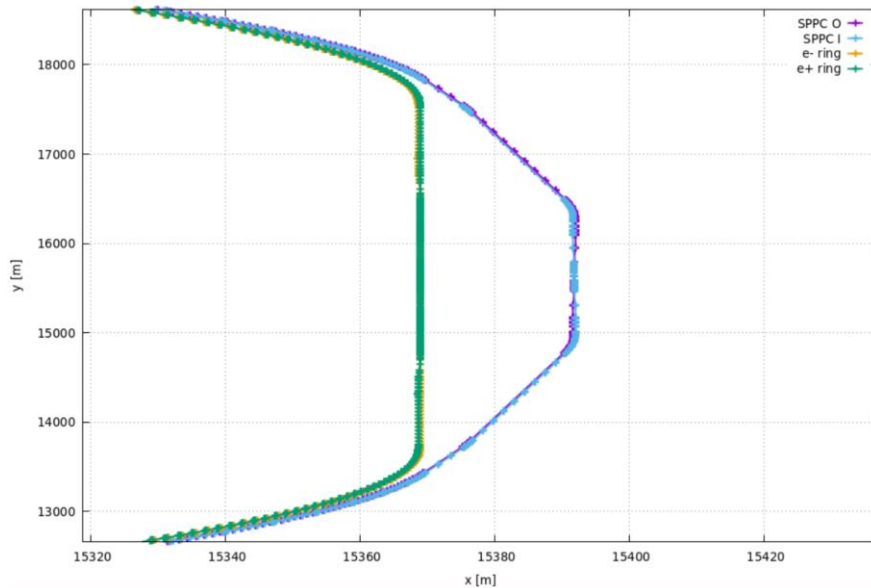
- Strength of dipole (arc and bypass): **20.31 T**
- Swap at IP2 and IP4
- Double ring separation: **30 cm**

### Distance of two machine's centers:

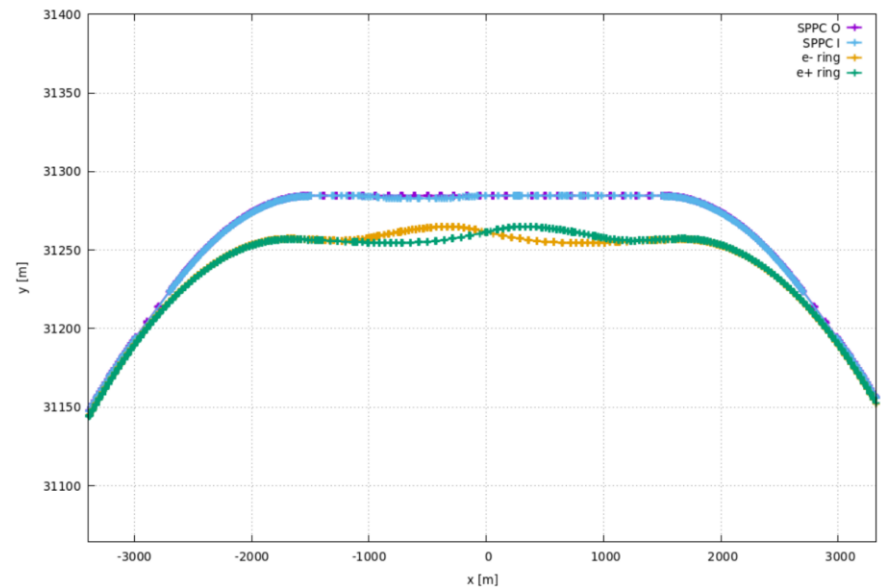
- Separation with CEPC at ARC: **3.5 m**
- Separation with CEPC at IPs: **23 m**



Geometry of arc section

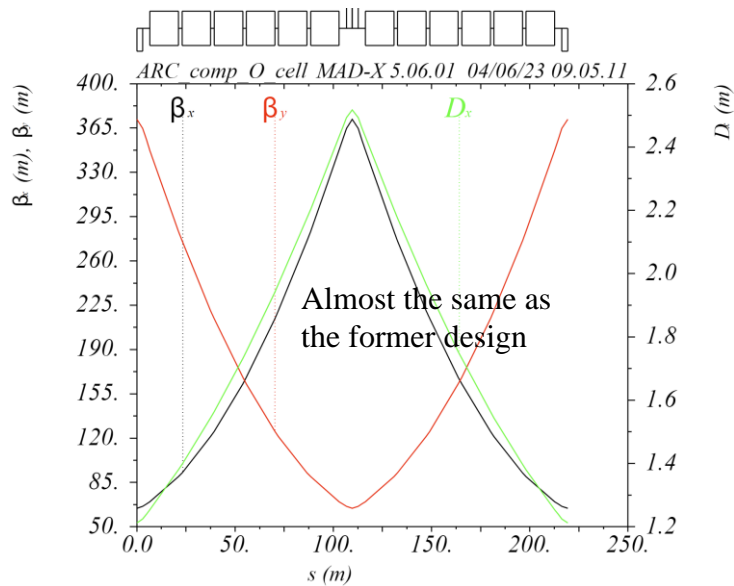


Geometry of bypass at IP2  
with a total length of 4399 m

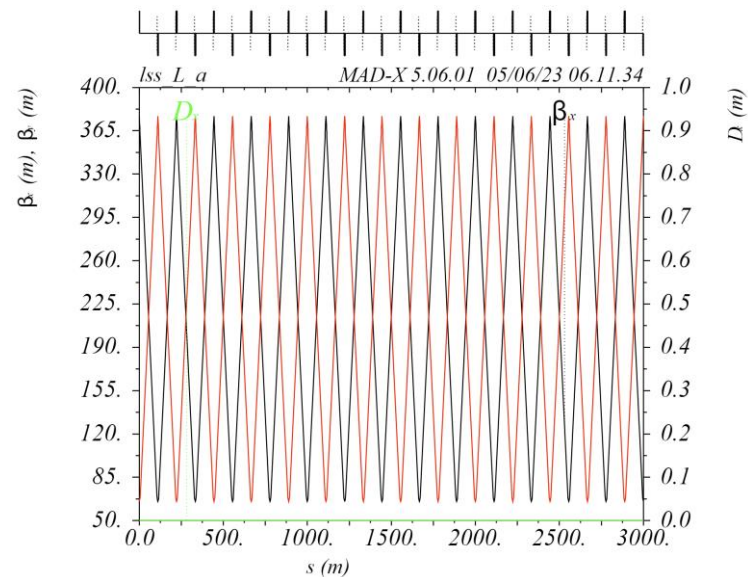


Geometry of bypass at IP3  
with a total length of 5985.34 m

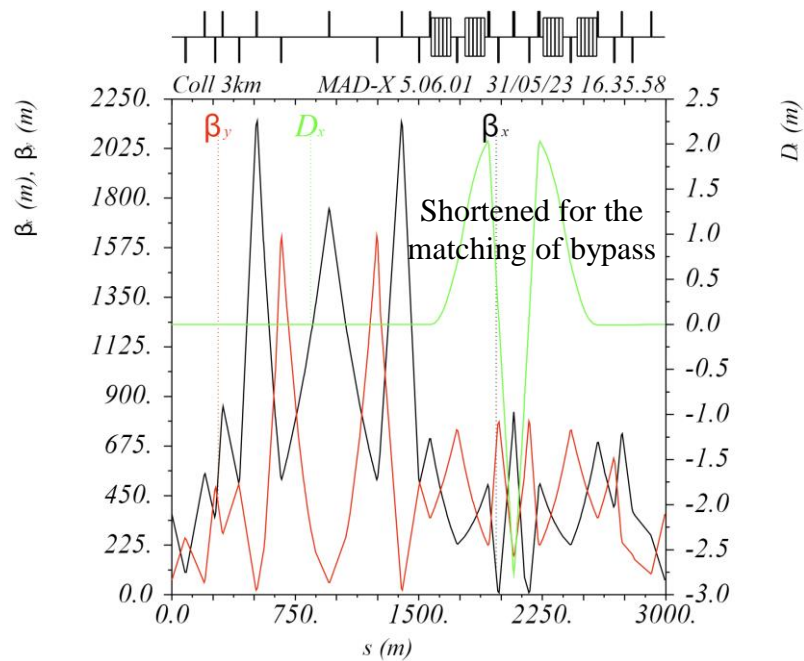




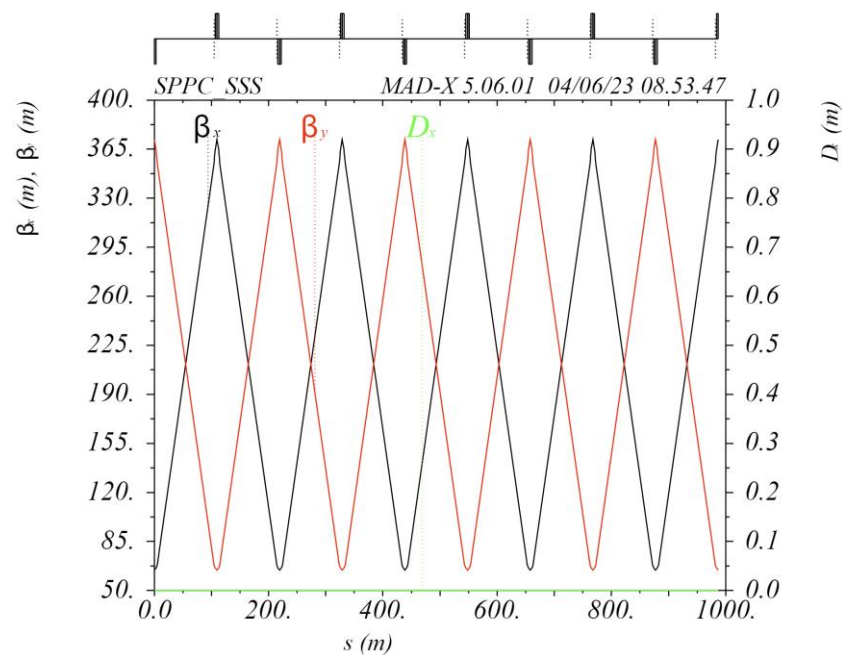
New Arc cell



3 km long straight section



3 km collimation section



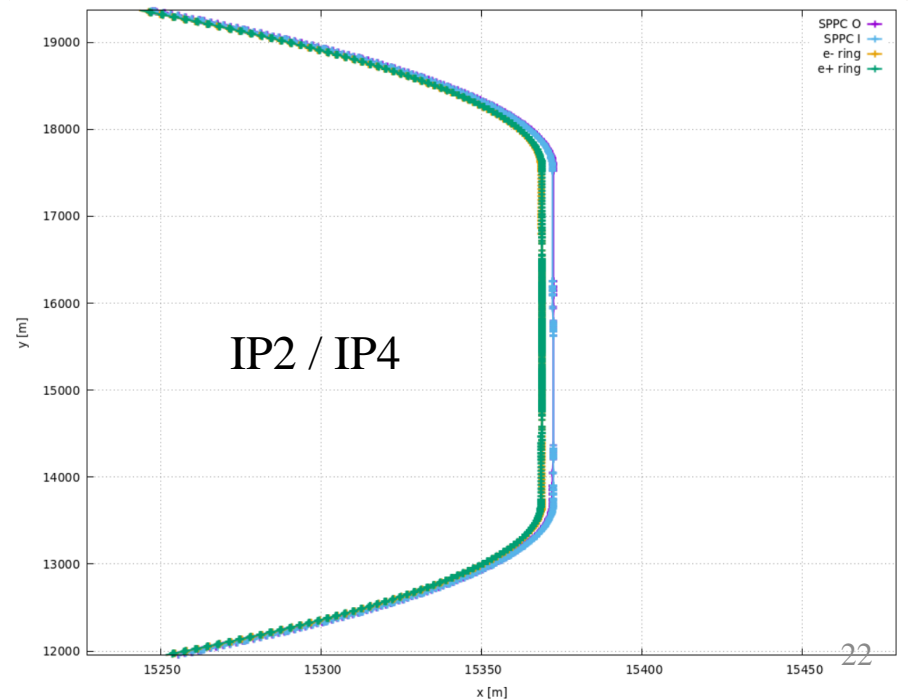
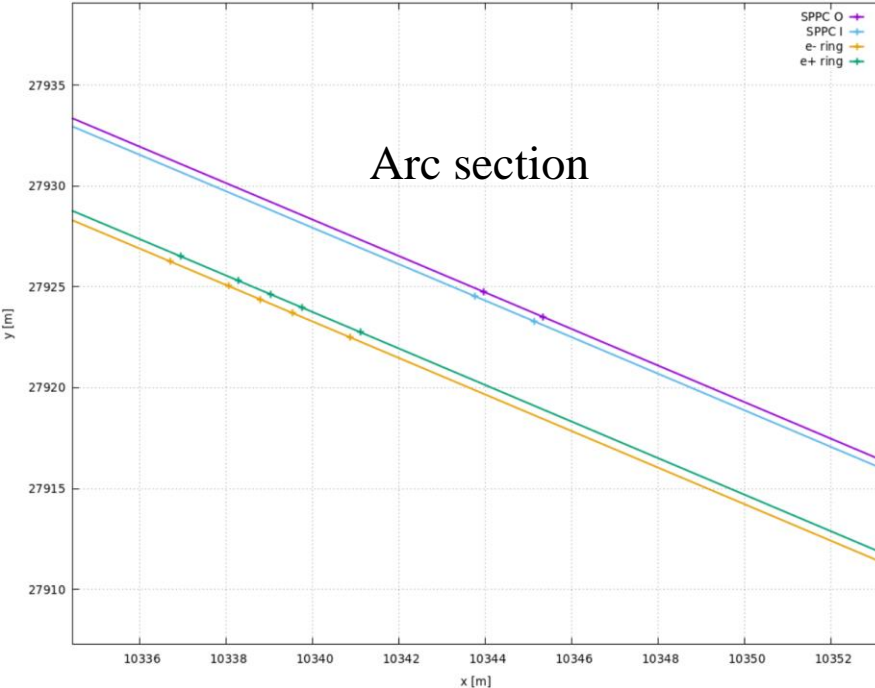
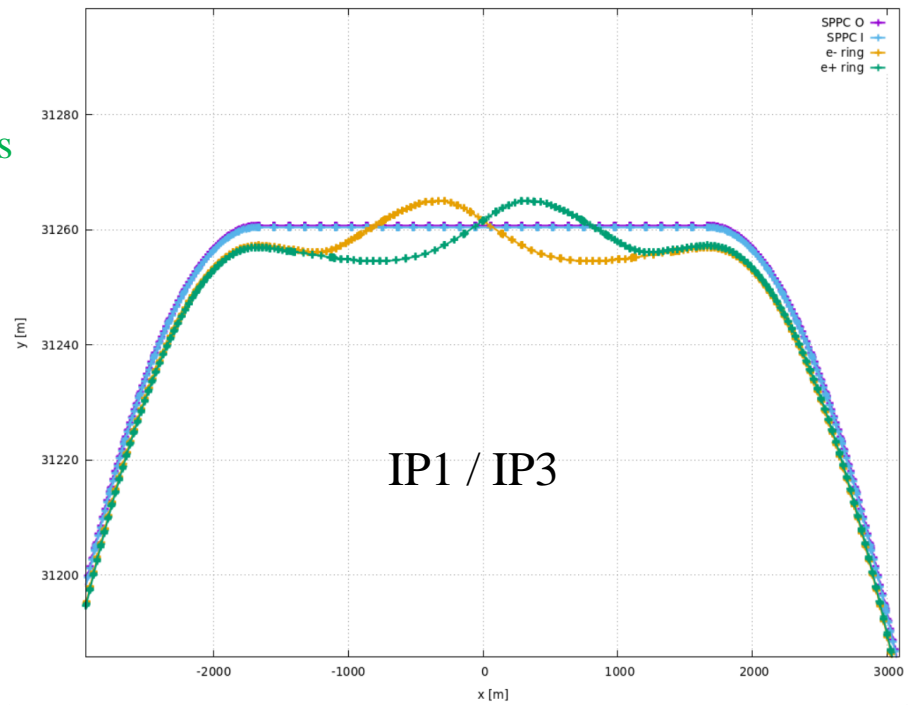
986.84 m short straight section

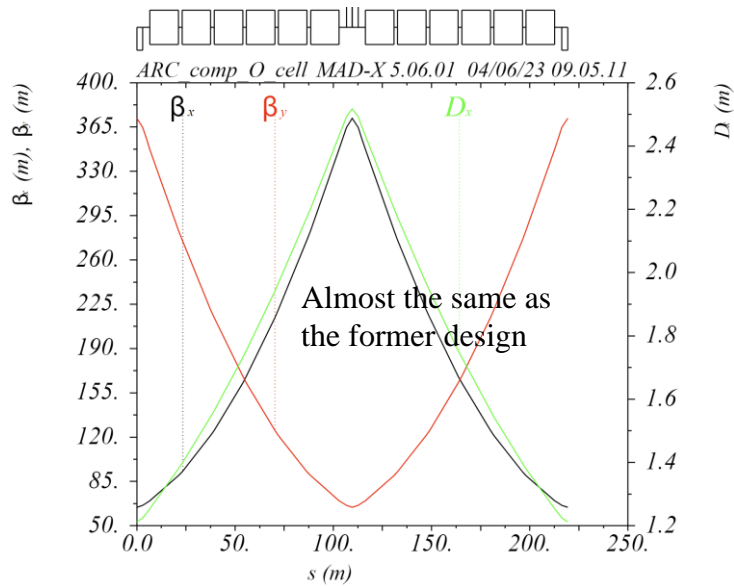
## Without bypass for the absence of CEPC detectors

### SPPC updated to double ring:

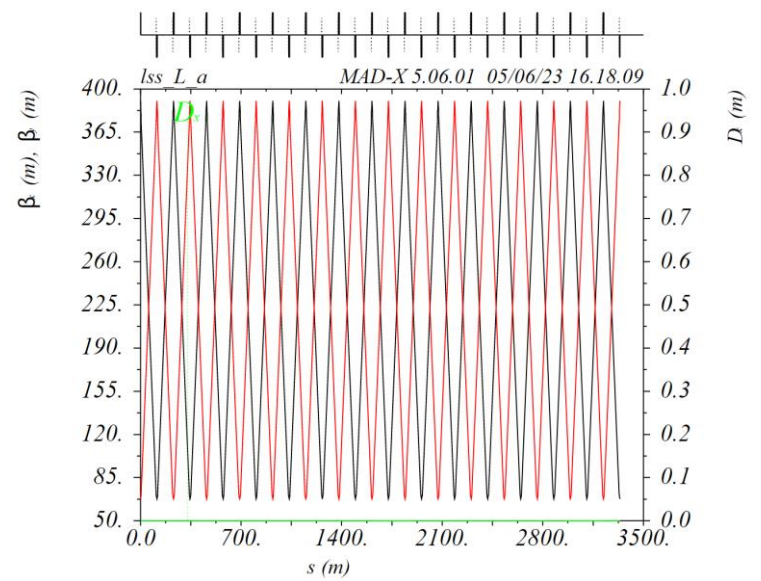
- Strength of dipole (arc and bypass): **20.31 T**
- Swap at IP2 and IP4
- Double ring separation: **30 cm**

Distance of two machine's centers: **3.5 m**

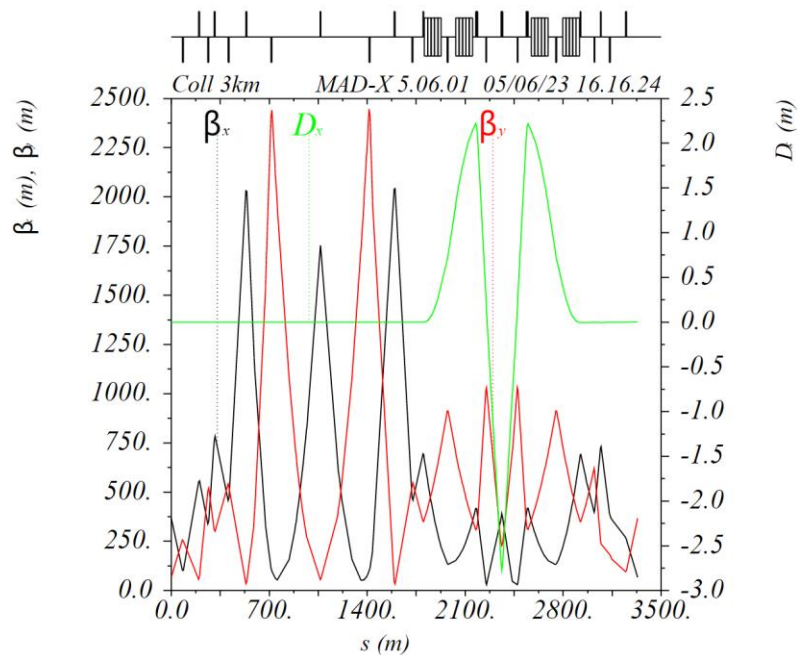




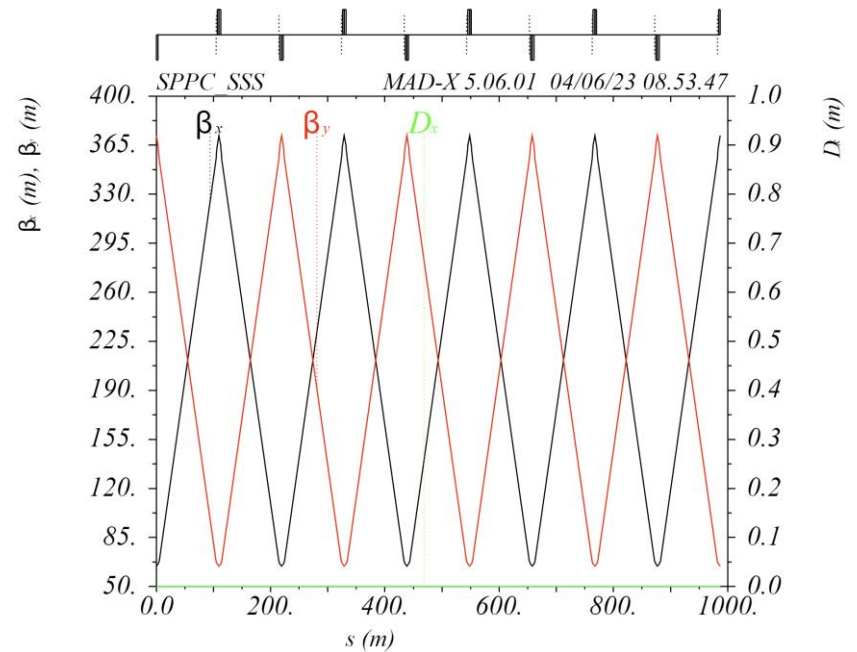
New Arc cell



3337.13 m long straight section



3337.13 m collimation section



986.84 m short straight section

# Geometric parameters of SPPC and CEPC



With bypass:

	SPPC before	SPPC after	CEPC
<b>Arc between SSS and final focus</b>	10487.52 m	9962.31 m	10270.44 m
<b>Arc between SSS and collimation/extraction</b>	10487.52 m	8865.69 m	10185.70 m
<b>Arc cell</b>	213.42 m	219.32 m	54.63 m
<b>Linear section at IP1/IP3</b>	4300 m	3000 m	3337.13 m
<b>Linear section at IP2/IP4</b>	1250 m	1250 m	3776.90 m
<b>Short straight section</b>	1250 m	986.84 m	986.84 m
<b>Bypass at IP1/IP3</b>	/	5985.34 m	/
<b>Bypass at IP2/IP4</b>	/	4399 m	/
<b>Circumference</b>	100000 m	100027.44 m	100000.0 m

\*Arc including DIS sections

Without bypass:

	SPPC before	SPPC after	CEPC
<b>Arc between SSS and final focus</b>	10487.52 m	10273.29 m	10270.44 m
<b>Arc between SSS and collimation/extraction</b>	10487.52 m	10188.55 m	10185.70 m
<b>Arc cell</b>	213.42 m	219.32 m	54.63 m
<b>Linear section at IP1/IP3</b>	4300 m	3337.13 m	3337.13 m
<b>Linear section at IP2/IP4</b>	1250 m	3776.90 m	3776.90 m
<b>Short straight section</b>	1250 m	986.84 m	986.84 m
<b>Circumference</b>	100000 m	100021.84 m	100000.0 m

\*Arc including DIS sections



# Summary

- A global correction scheme based on response matrix method is presented. Lattices at both collision and injection energy with errors have been corrected.
- For the compatibility of CEPC and SppC, two kinds of SppC lattice design are presented for the presence or absence of bypass respectively.
- Further improve the global correction results to get a more relaxed tolerance.

***Thanks for your attention!***