

The 2023 International Workshop on the High  
Energy Circular Electron Positron Collider  
Nanjing, 2023 Oct.



# FLAVOR PHYSICS AT CEPC

## - A GENERAL PERSPECTIVE

Tao Liu

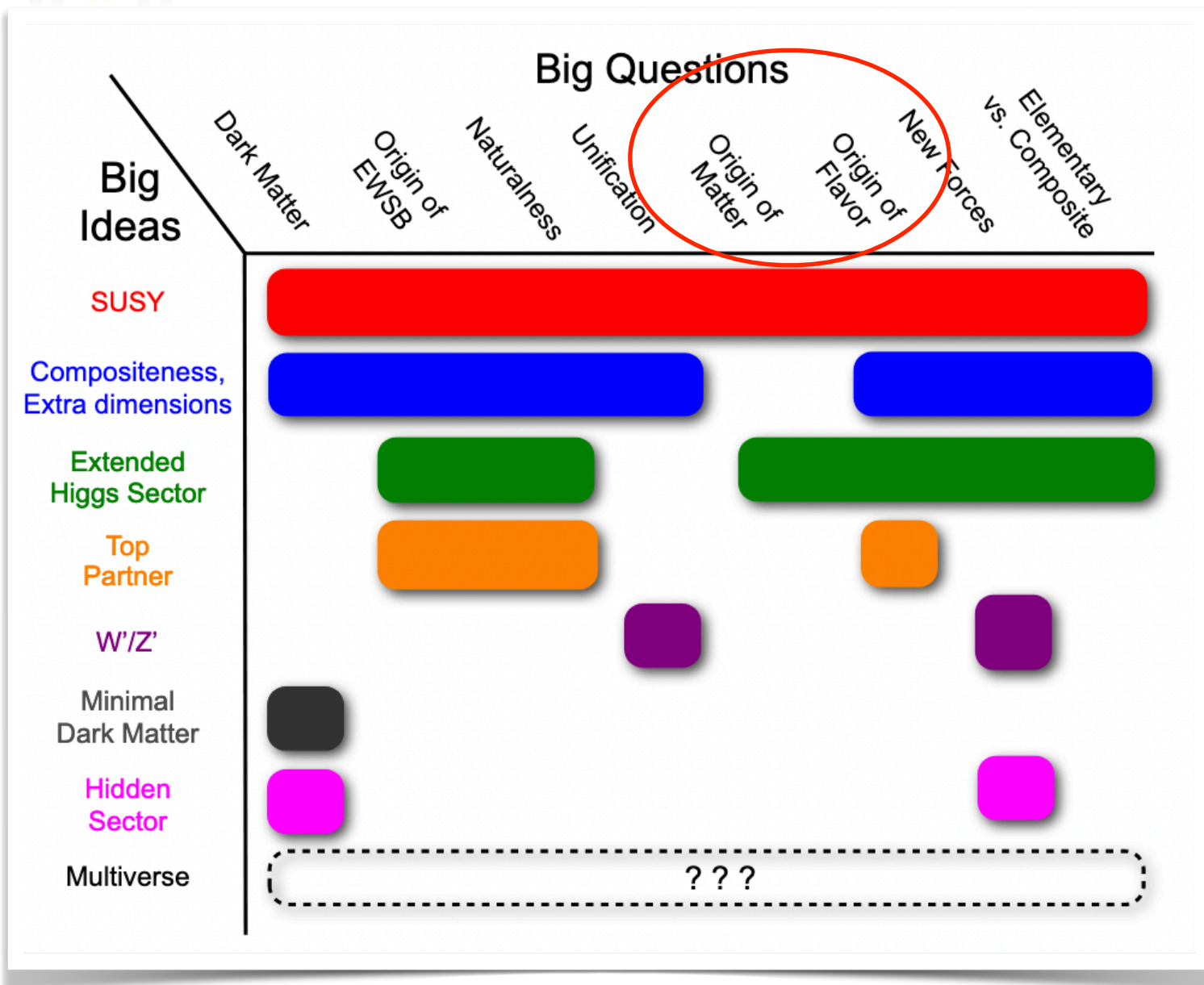
The Hong Kong University of Science and Technology

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# Flavor Physics



$$\mathcal{L}_{\text{SM}} \supset i\bar{\psi}\not{D}\psi + \bar{\psi}_i y_{ij} \psi_j \phi$$

- Coupling pattern
- Mass texture
- Underlying symmetry
- CP phase
- ... ..

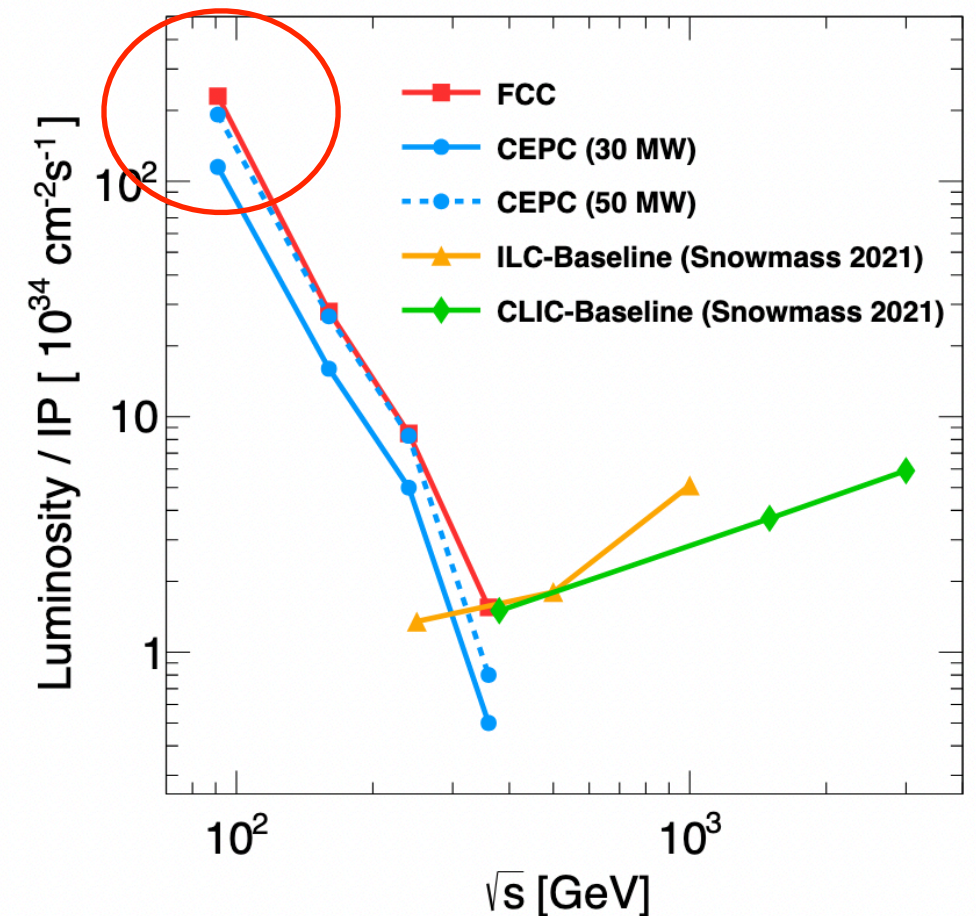
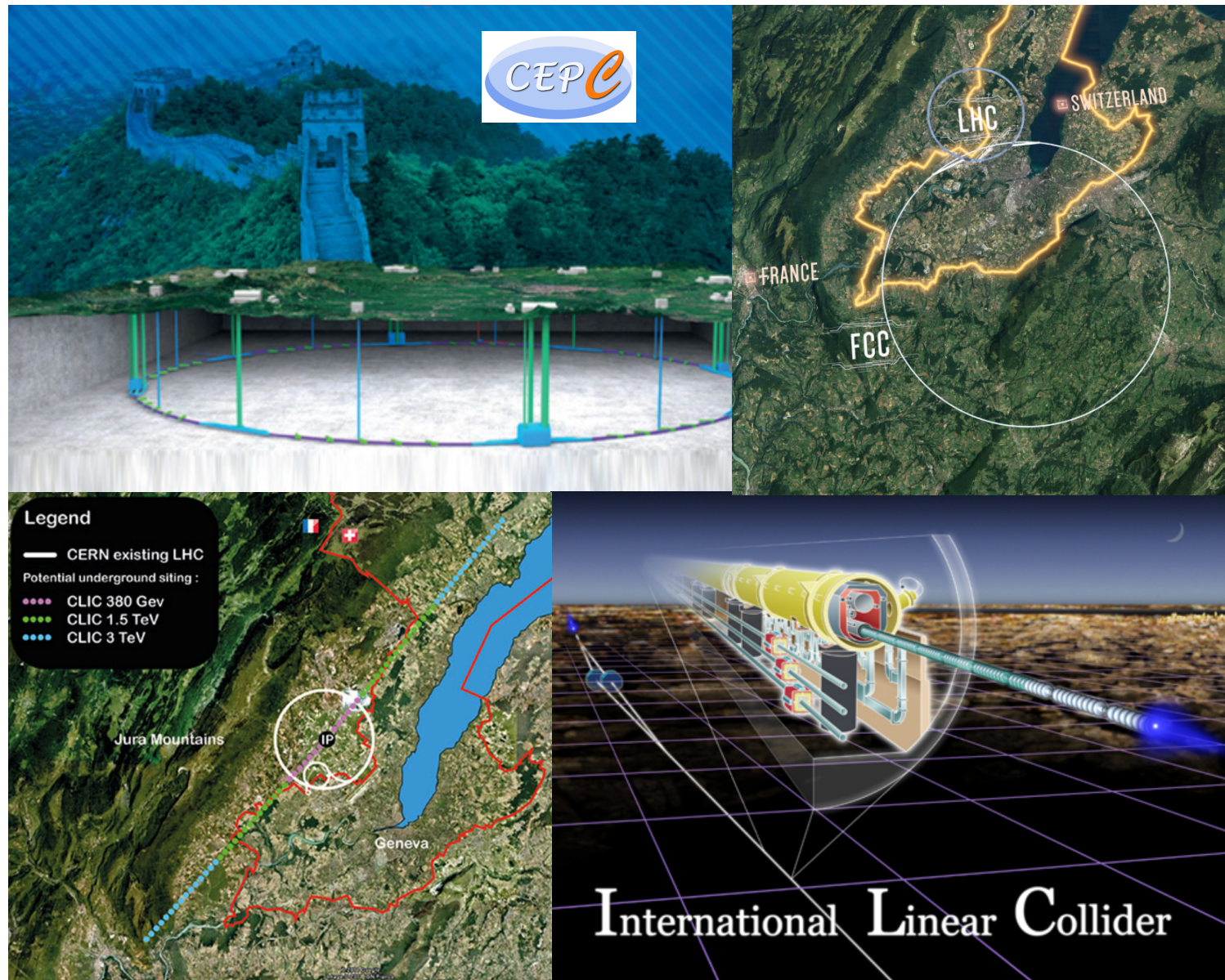
[Working group report for Snowmass 2013]





# Precision Frontier of Next Decades

The precision frontier of next decades in Higgs and electroweak physics is expected to be defined by a new  $e^-e^+$  collider.



Circular version is especially suited for the study on flavor physics, for its high luminosity at Z pole





# Key Collider Features for Flavor Physics

## Clean collider environment

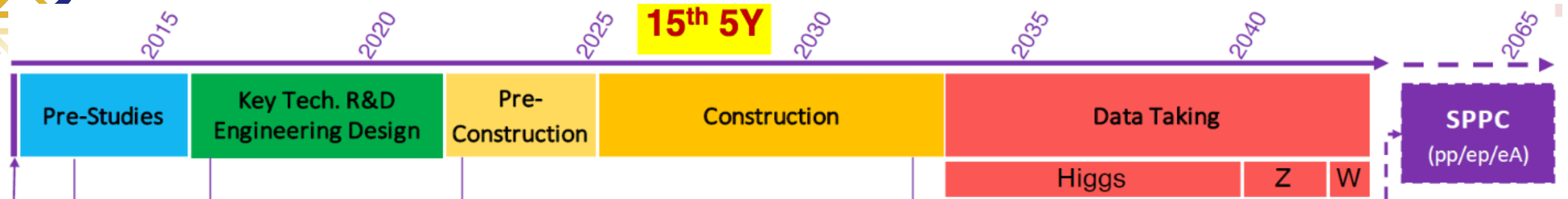
- Low QCD backgrounds
- Negligible pile-ups
- Approximately fixed  $E_{\text{cm}}$
- Beam energy much larger than the quark and lepton masses
  - Boosted dynamics
  - Higher precision of measuring momentum and efficiency for reconstructing vertex
  - Belle II: asymmetric beam energy has been taken to improve event reconstruction
- High production rate of relevant mesons, baryons, leptons, etc. at Z pole
  - Belle II has no statistics for heavy hadrons due to the limitation of energy threshold.

Channel	Belle II	LHCb	Giga-Z	Tera-Z	10×Tera-Z
$B^0, \bar{B}^0$	$5.3 \times 10^{10}$	$\sim 6 \times 10^{13}$	$1.2 \times 10^8$	$1.2 \times 10^{11}$	$1.2 \times 10^{12}$
$B^\pm$	$5.6 \times 10^{10}$	$\sim 6 \times 10^{13}$	$1.2 \times 10^8$	$1.2 \times 10^{11}$	$1.2 \times 10^{12}$
$B_s, \bar{B}_s$	$5.7 \times 10^8$	$\sim 2 \times 10^{13}$	$3.2 \times 10^7$	$3.2 \times 10^{10}$	$3.2 \times 10^{11}$
$B_c^\pm$	-	$\sim 4 \times 10^{11}$	$2.2 \times 10^5$	$2.2 \times 10^8$	$2.2 \times 10^9$
$\Lambda_b, \bar{\Lambda}_b$	-	$\sim 2 \times 10^{13}$	$1.0 \times 10^7$	$1.0 \times 10^{10}$	$1.0 \times 10^{11}$





# Roadmap of CEPC-SppC (Upon Approval)



[Xinchou Lou, 2022 HEP program at JCIAS, HKUST]

Particle	$E_{c.m.}$ (GeV)	Years	SR Power (MW)	Lumi. /IP ( $10^{34}\text{cm}^{-2}\text{s}^{-1}$ )	Integrated Lumi. /yr ( $\text{ab}^{-1}$ , 2 IPs)	Total Integrated L ( $\text{ab}^{-1}$ , 2 IPs)	Total no. of events
$H^*$	240	10	50	8.3	2.2	21.6	$4.3 \times 10^6$
			30	5	1.3	13	$2.6 \times 10^6$
Z	91	2	50	192**	50	100	$4.1 \times 10^{12}$
			30	115**	30	60	$2.5 \times 10^{12}$
W	160	1	50	26.7	6.9	6.9	$2.1 \times 10^8$
			30	16	4.2	4.2	$1.3 \times 10^8$
$t\bar{t}$	360	5	50	0.8	0.2	1.0	$0.6 \times 10^6$
			30	0.5	0.13	0.65	$0.4 \times 10^6$

[see Yuhui Li's talk]

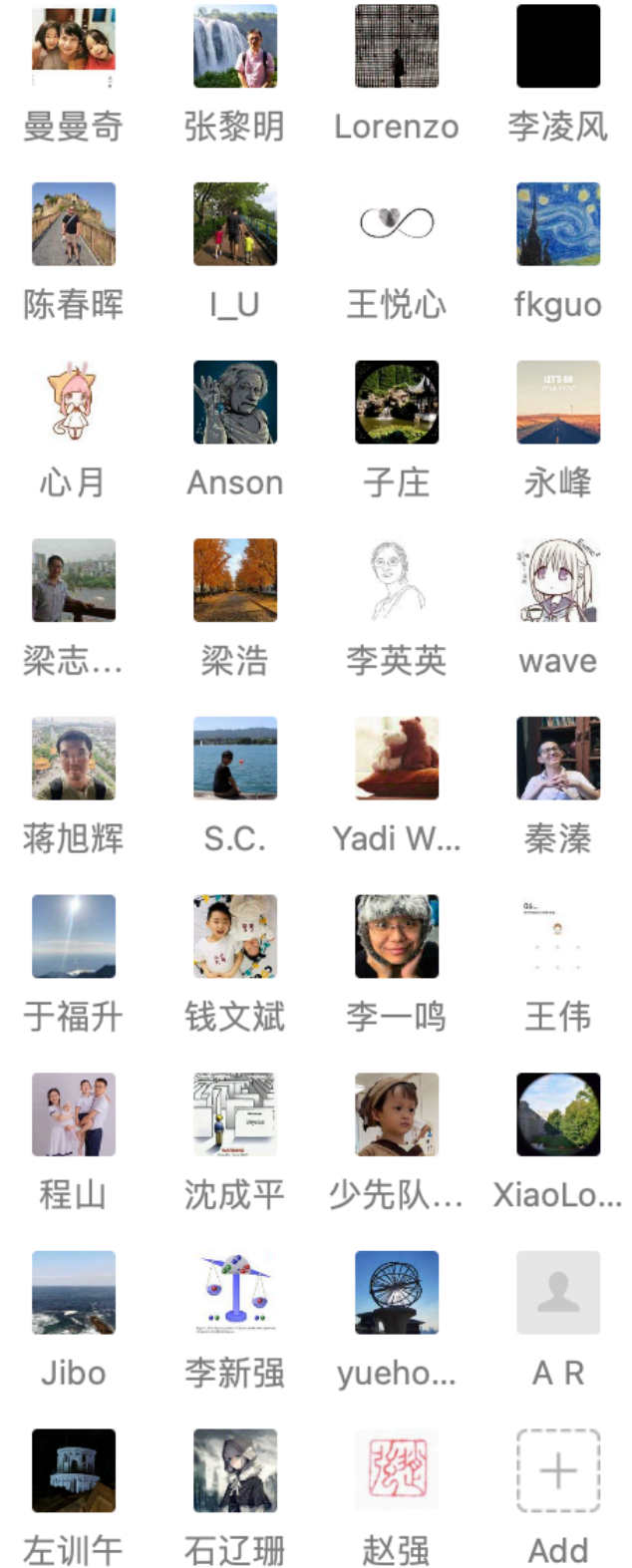




# White Paper on Flavor Physics at CEPC

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# The Goals

- Present a phase-I picture on the CEPC potential, mainly at Z pole, in exploring flavor physics
- Identify “golden” channels for critical physics
  - High scientific value
  - Challenging or even inaccessible for existing experiments
    - complex event topology
    - suppressed productions at other machines
- Develop new observables or methodologies, e.g., ML-based ones, for flavor physics
- As the technology roadmap is close for CEPC and FCC-ee, many of the CEPC studies can be applied to FCC-ee and vice versa

Most highlights below involve tau lepton decays:

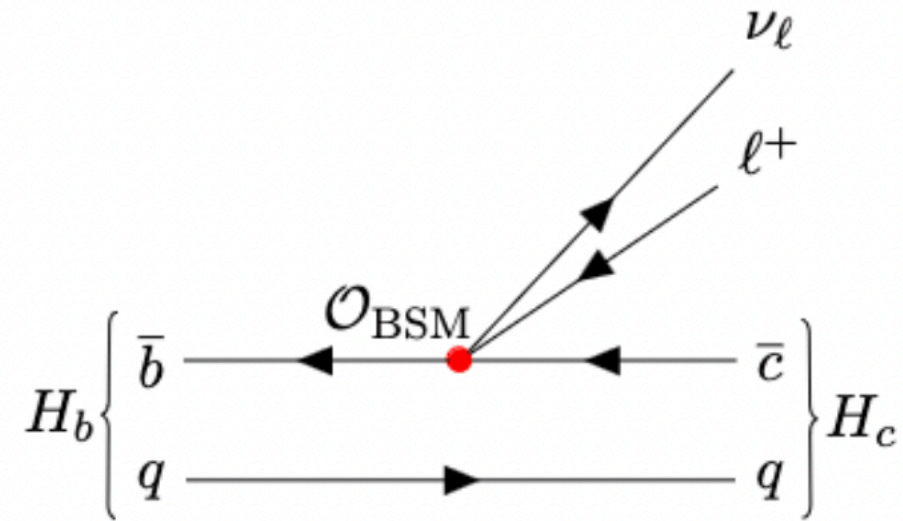
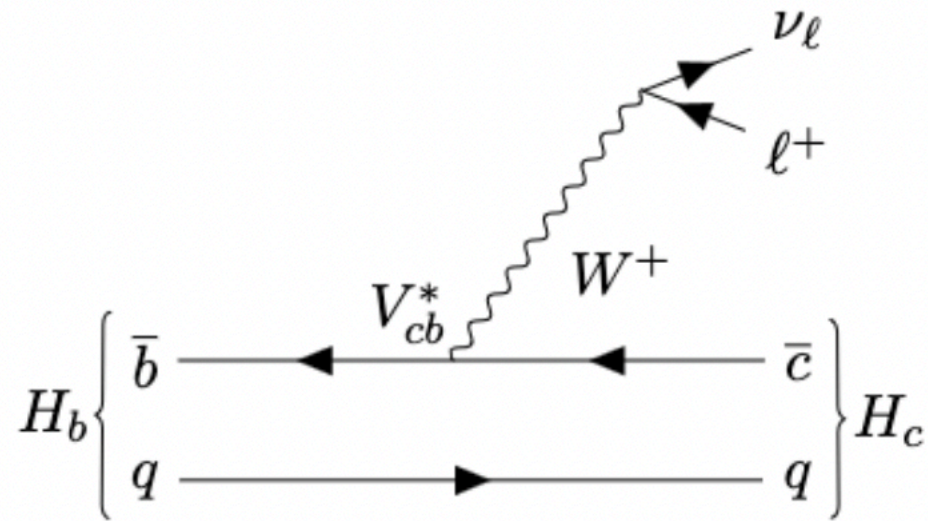
- Scientifically, crucial for achieving a picture of all flavors.
- Technically, multi-body decays for tau leptons complicate the event topology and kinematics.
  - The decay products tend to be soft in B-factories, while the signature of neutrinos as missing momentum is inaccessible at hadron colliders.
  - The reconstruction of tau leptons and other intermediate particles can benefit from the excellent collider environment of the CEPC and the high-performance of its detector.
- => define a series of the most representative cases for flavor physics at the CEPC.





# Highlight I - $b \rightarrow c\tau\nu$

Historically, FCCC-mediated beta decays have resulted in the discovery of weak interactions. They can be used to test lepton flavor universality.



	$H_b$	$H_c$	SM Prediction <sup>2</sup>	Experimental Average
<del><math>R_D</math></del>	<del><math>B^0, B^\pm</math></del>	<del><math>D^0, D^\pm</math></del>	<del>0.307 [1, 2]</del>	<del><math>0.340 \pm 0.030</math> [3]</del>
<del><math>R_{D^*}</math></del>	<del><math>B^0, B^\pm</math></del>	<del><math>D^{*0}, D^{*\pm}</math></del>	<del>0.253 [1, 2]</del>	<del><math>0.295 \pm 0.014</math> [3]</del>
$R_{J/\psi}$	$B_c$	$J/\psi$	0.289 [4–6]	$0.71 \pm 0.17 \pm 0.18$ [7]
$R_{D_s}$	$B_s$	$D_s$	0.393 [2, 8–13]	N/A
$R_{D_s^*}$	$B_s$	$D_s^*$	0.303 [2, 8, 10, 13]	N/A
$R_{\Lambda_c}$	$\Lambda_b$	$\Lambda_c$	0.334 [14–18]	$0.242 \pm 0.076$ [19]

$$R_{H_c} \equiv \frac{\text{Br}(H_b \rightarrow H_c \tau \nu)}{\text{Br}(H_b \rightarrow H_c \ell \nu)}$$

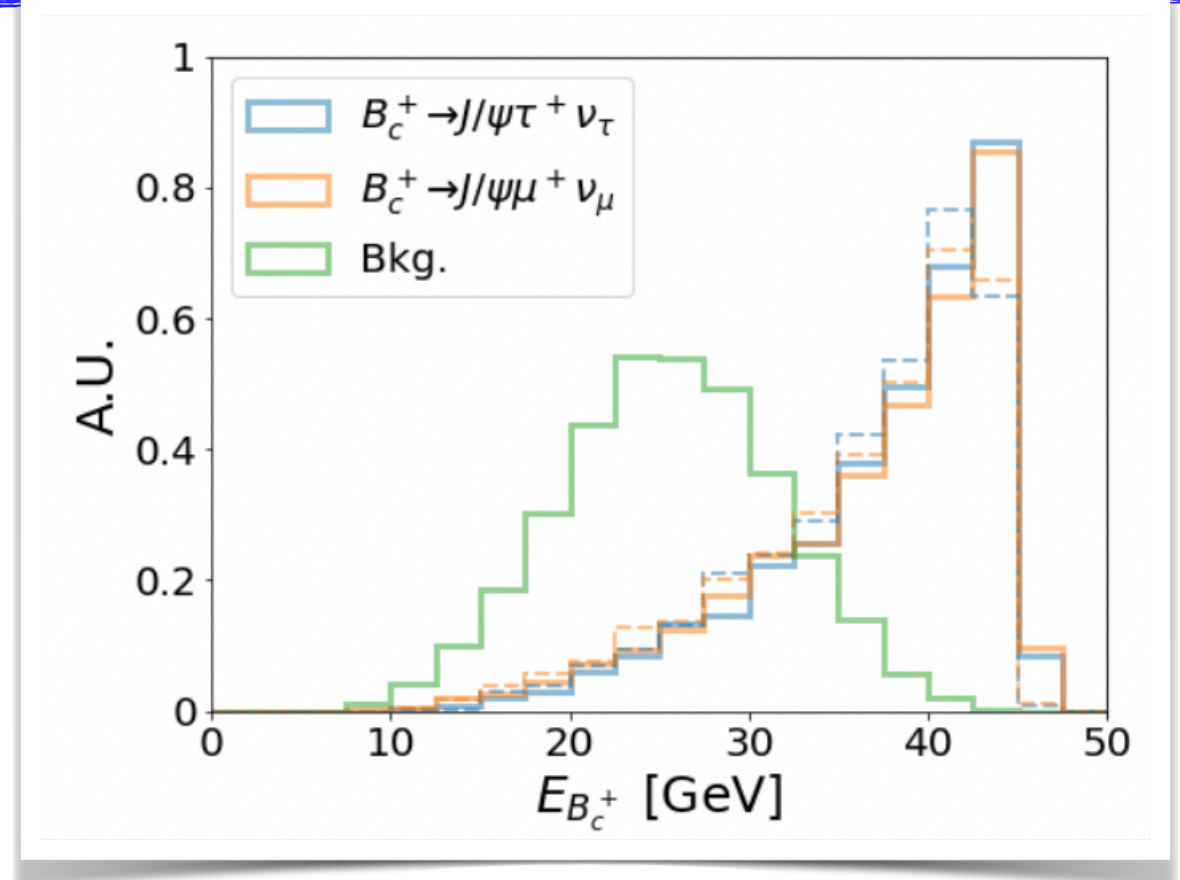
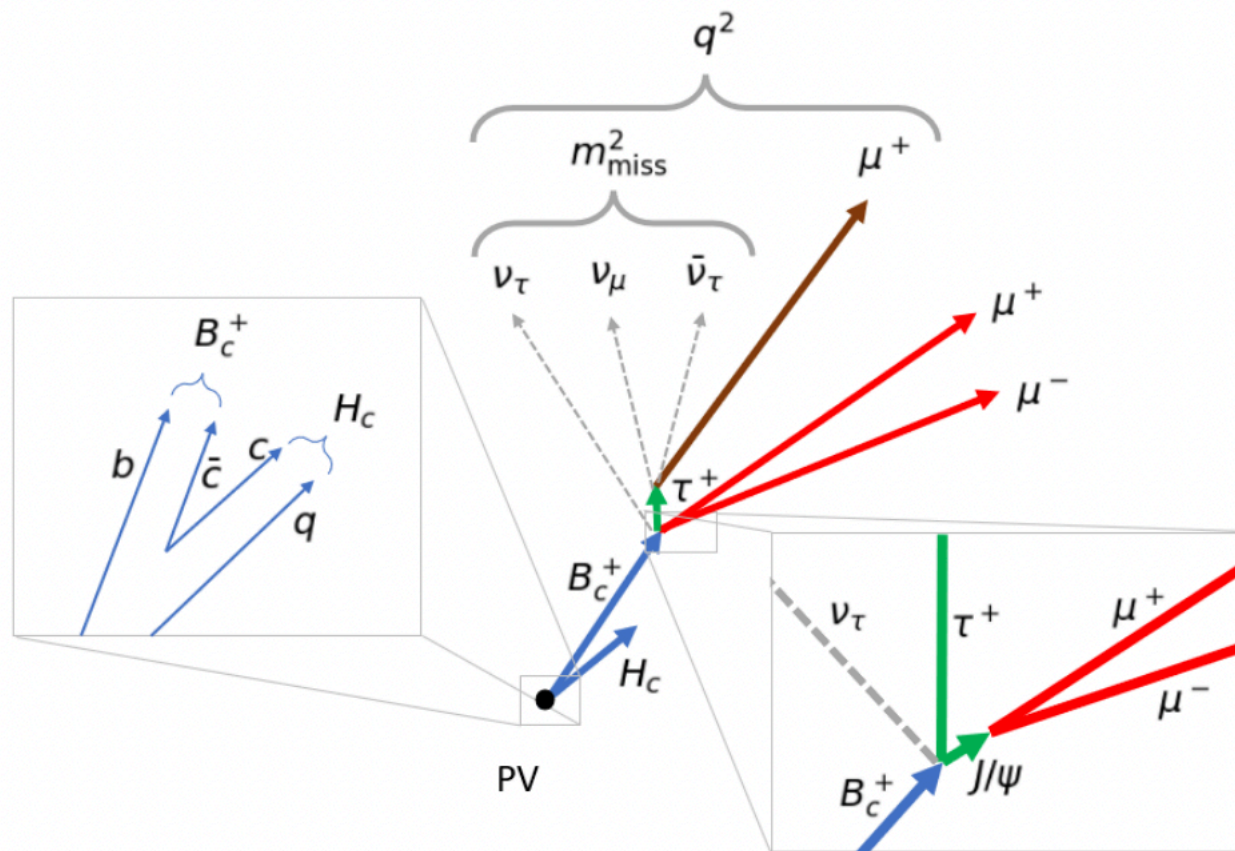
Current measurements:  
either no sensitivity or  
have a precision ~30%.





# Highlight I - $b \rightarrow c\tau\nu$

Track-based strategy  
(approximate reconstructed J/psi  
vertex as the  $B_c^+$  vertex)



$R_{J/\psi}$	$4.25 \times 10^{-2}$
Rel. precision	$(1.35 \times 10^{-2})$
$R_{D_s}$	$4.09 \times 10^{-3}$
Rel. precision	$(1.30 \times 10^{-3})$
$R_{D_s^*}$	$3.26 \times 10^{-3}$
Rel. precision	$(1.03 \times 10^{-3})$
$R_{\Lambda_c}$	$9.77 \times 10^{-4}$
Rel. precision	$(3.09 \times 10^{-4})$

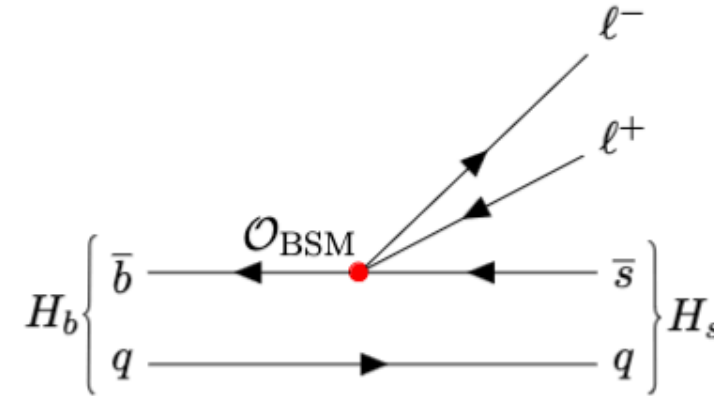
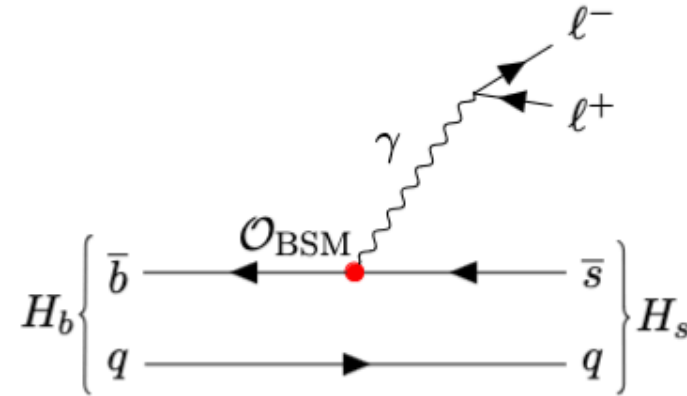
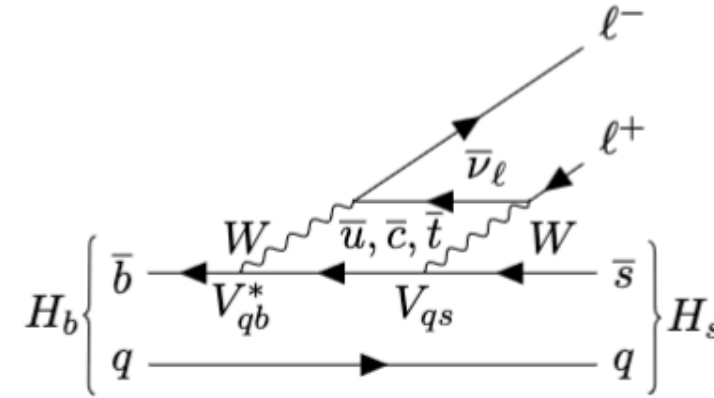
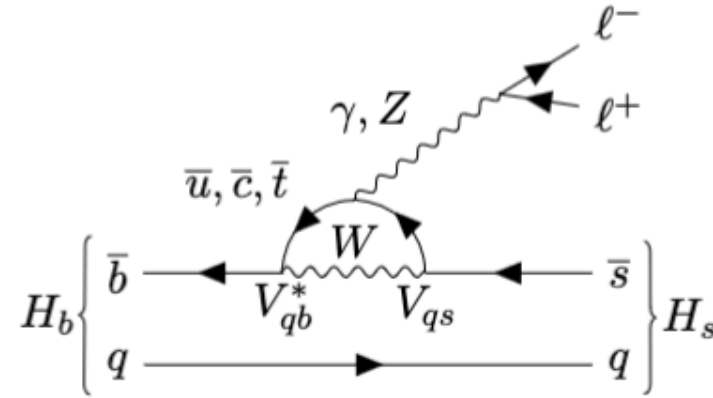
[T. Ho, X. Jiang, T. Kwok, L. Li and TL, arXiv: 2212.02433]

See also [Amhis et al. (2021), Zheng et al. (2020)]





# Highlight II - $b \rightarrow s\tau\tau$



Channel	SM prediction for BR	$q^2 \equiv m_{\tau\tau}^2$ (GeV <sup>2</sup> )
$B^0 \rightarrow K^{*0}\tau^+\tau^-$	$(0.98 \pm 0.10) \times 10^{-7}$ [11]	[15,19]
$B_s \rightarrow \phi\tau^+\tau^-$	$(0.86 \pm 0.06) \times 10^{-7}$ [11]	[15,18.8]
$B^+ \rightarrow K^+\tau^+\tau^-$	$(1.20 \pm 0.12) \times 10^{-7}$ [11]	[15,22]
$B_s \rightarrow \tau^+\tau^-$	$(7.73 \pm 0.49) \times 10^{-7}$ [12]	-

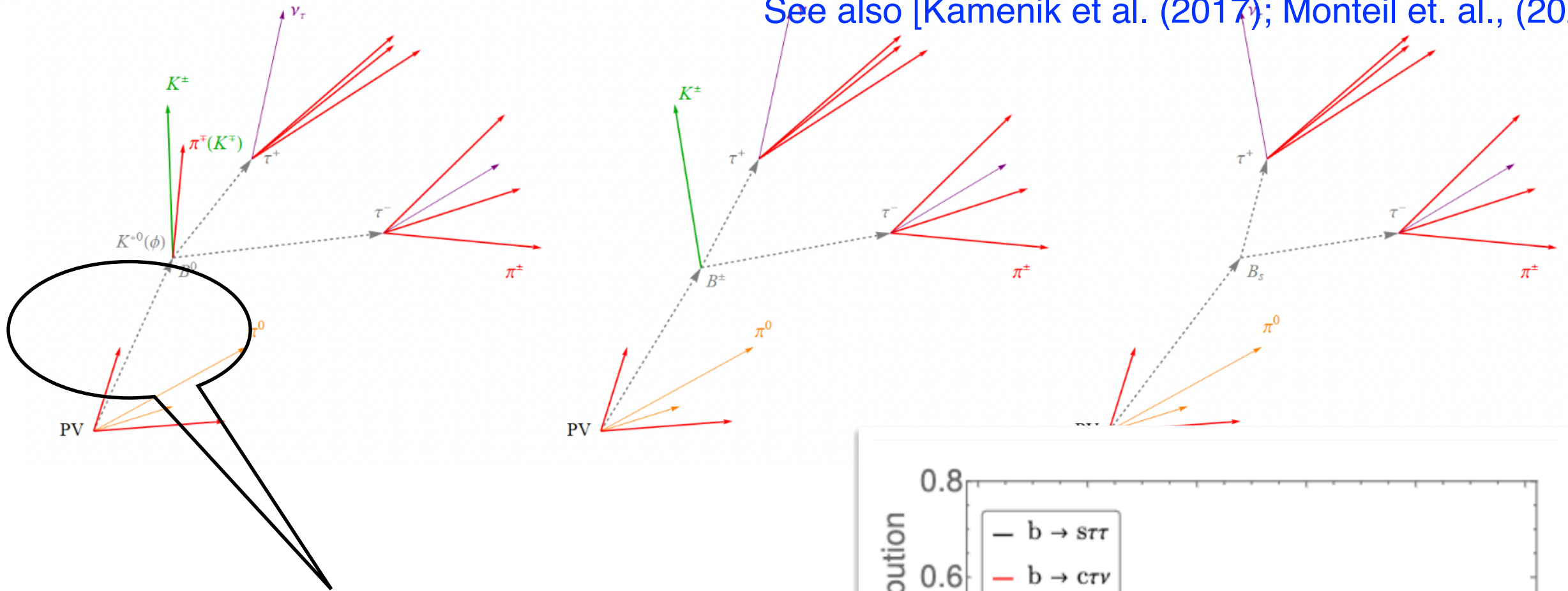
Current sensitivity is still far from the SM prediction.



# Highlight II - $b \rightarrow s\tau\tau$

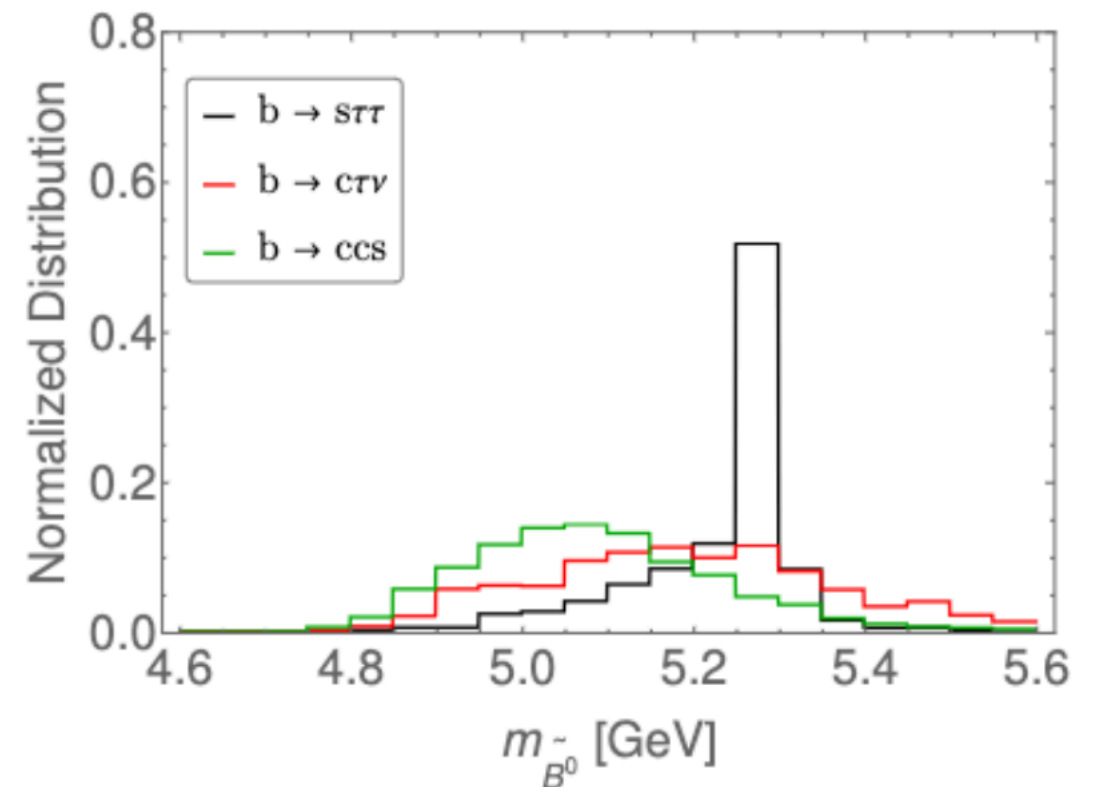
[TL and L. F. Li, JHEP (2021)]

See also [Kamenik et al. (2017); Monteil et. al., (2021)]



Track-based  
reconstruction strategy

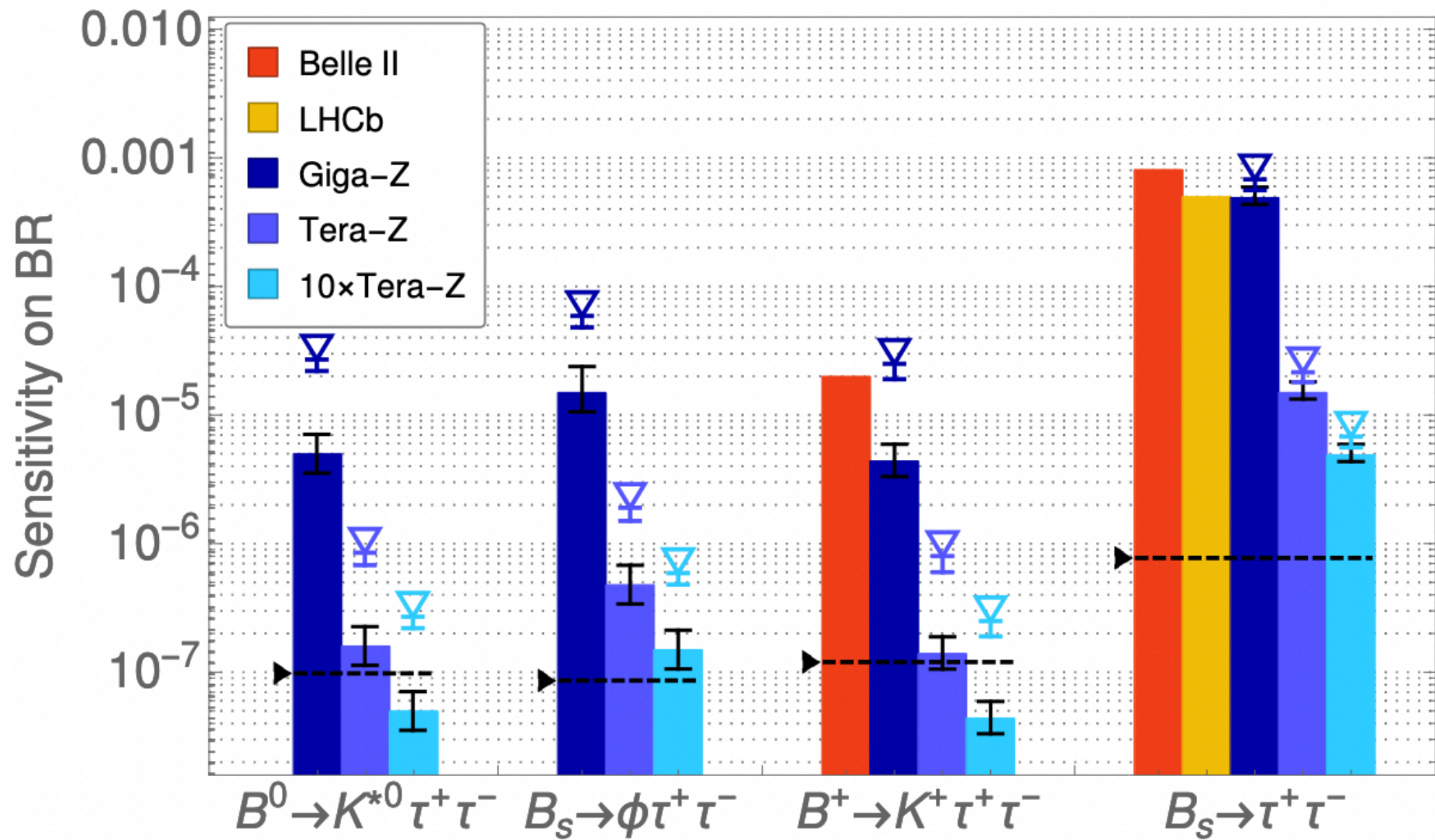
$$\vec{p}_{\nu,i} = \frac{-\vec{p}_{K^{*0}} \times \vec{V}_{B^0} \cdot \vec{V}_{\tau,j}}{\vec{V}_{\tau,i} \times \vec{V}_{B^0} \cdot \vec{V}_{\tau,j}} \vec{V}_{\tau,i} - \vec{p}_{3\pi,i}$$





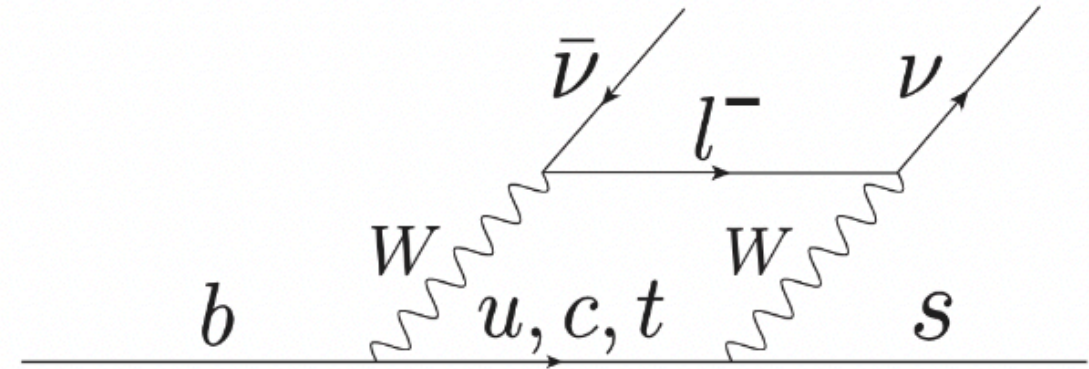
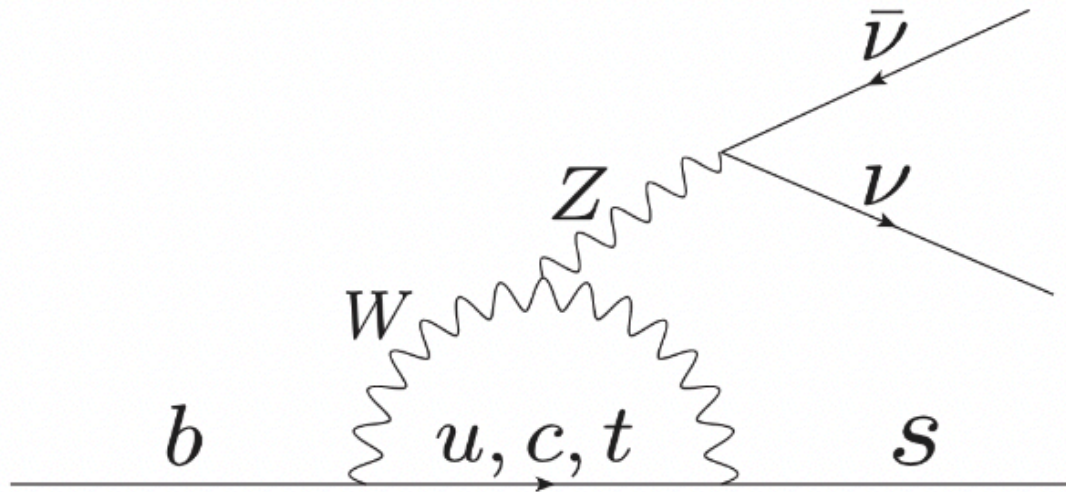


## Highlight II - $b \rightarrow s\tau\tau$





# Highlight III - $b \rightarrow s\nu\nu$

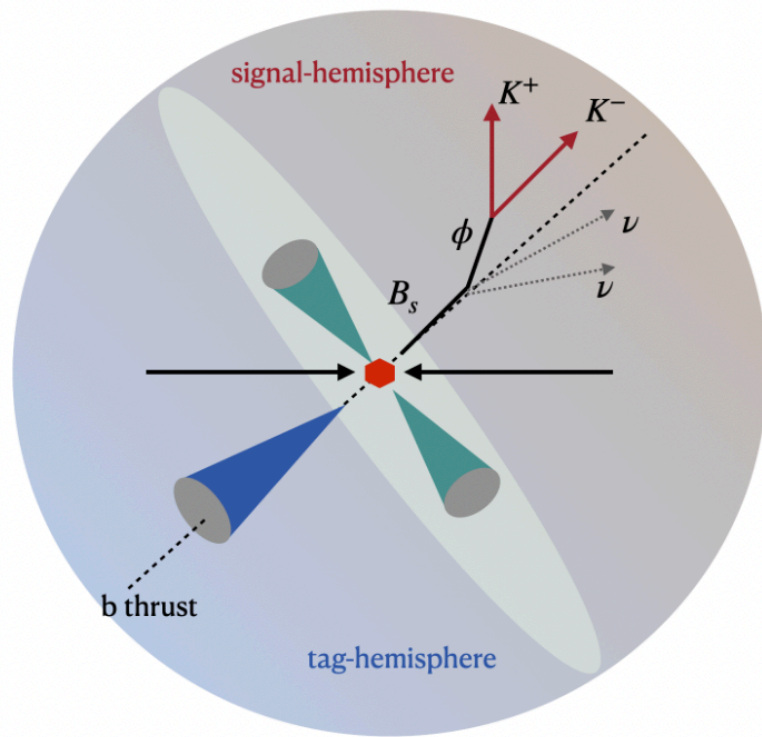


	Current Limit	Detector	SM Prediction
$\text{BR}(B^0 \rightarrow K^0 \nu \bar{\nu})$	$< 2.6 \times 10^{-5}$ [3]	BELLE	$(3.69 \pm 0.44) \times 10^{-6}$ [1]
$\text{BR}(B^0 \rightarrow K^{*0} \nu \bar{\nu})$	$< 1.8 \times 10^{-5}$ [3]	BELLE	$(9.19 \pm 0.99) \times 10^{-6}$ [1]
$\text{BR}(B^\pm \rightarrow K^\pm \nu \bar{\nu})$	$< 1.6 \times 10^{-5}$ [4]	BABAR	$(3.98 \pm 0.47) \times 10^{-6}$ [1]
$\text{BR}(B^\pm \rightarrow K^{*\pm} \nu \bar{\nu})$	$< 4.0 \times 10^{-5}$ [5]	BELLE	$(9.83 \pm 1.06) \times 10^{-6}$ [1]
$\text{BR}(B_s \rightarrow \phi \nu \bar{\nu})$	$< 5.4 \times 10^{-3}$ [6]	DELPHI	$(9.93 \pm 0.72) \times 10^{-6}$

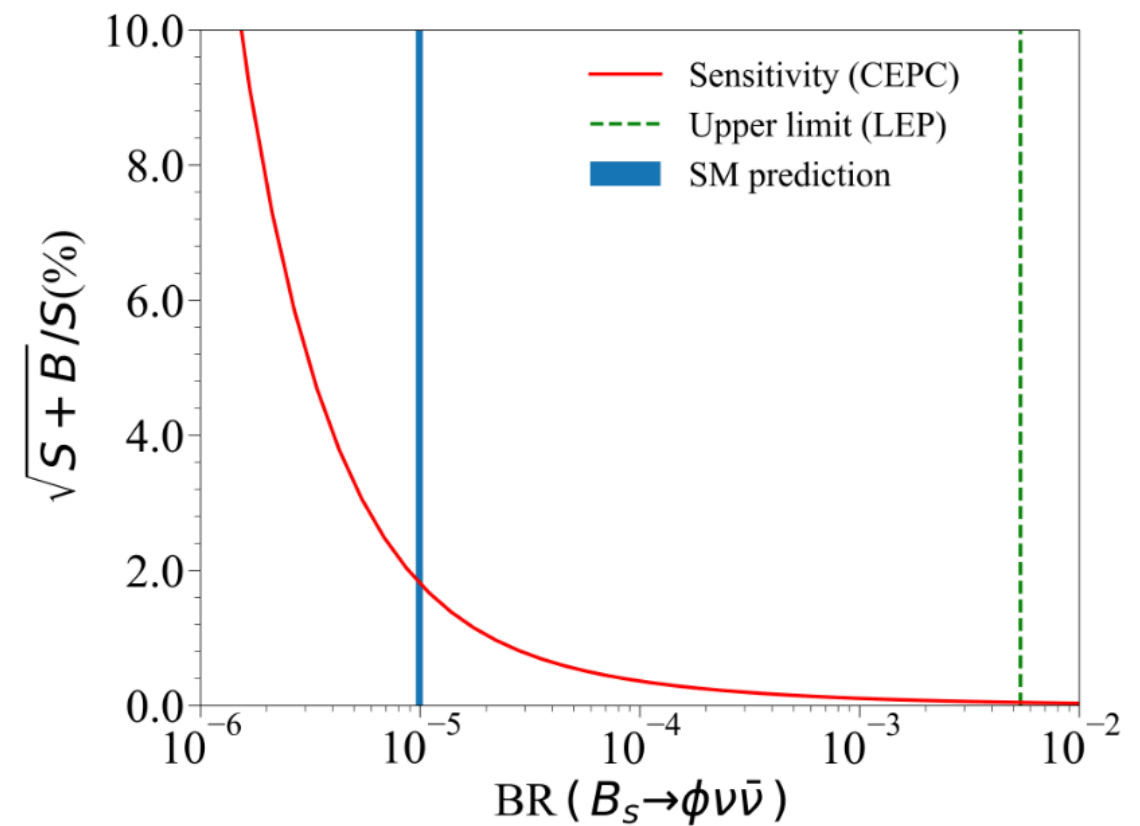
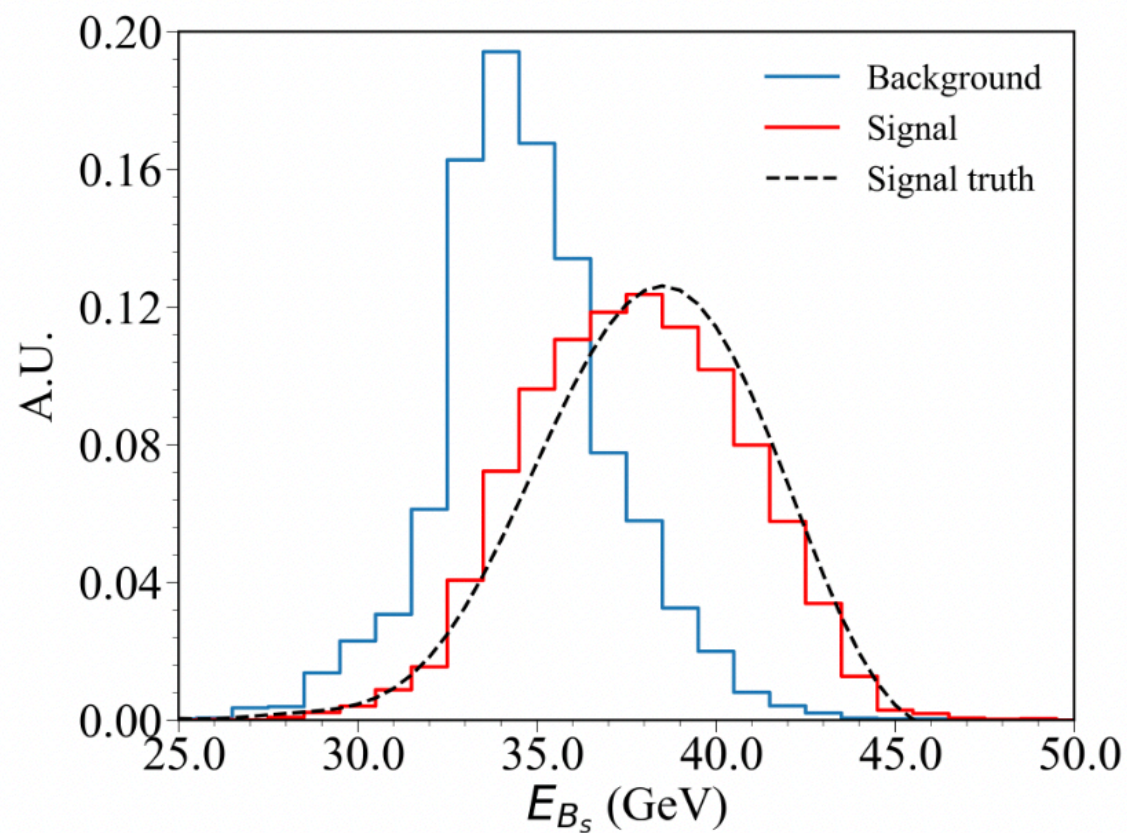


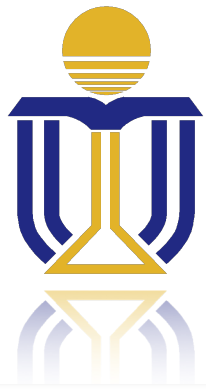


# Highlight III - $b \rightarrow s\nu\nu$

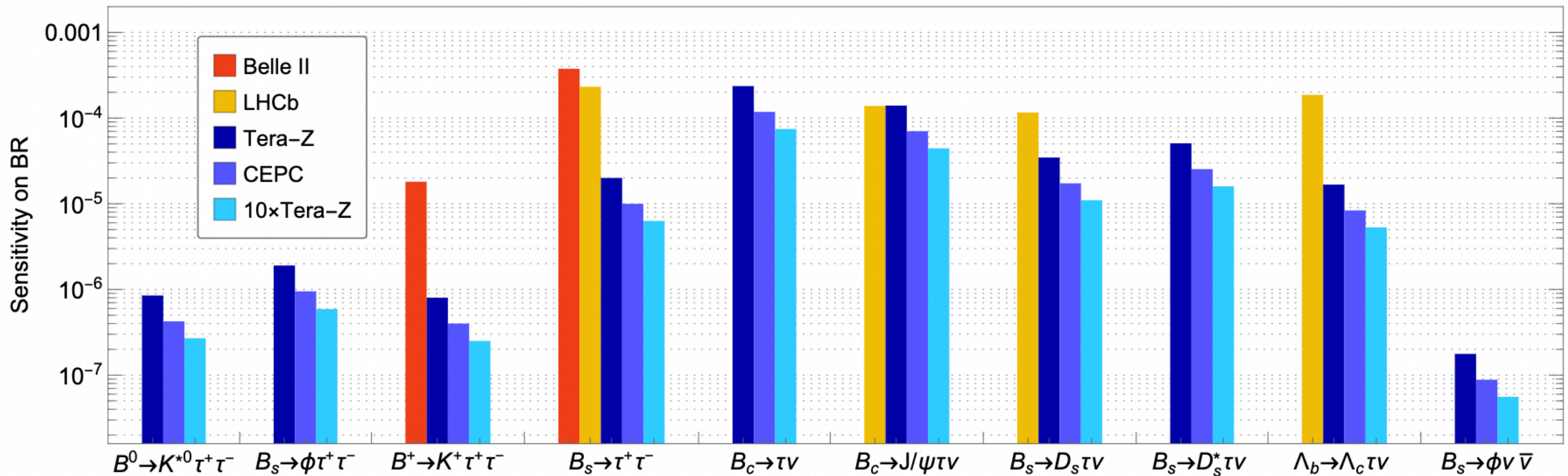


[L. Li, M. Ruan, et. al., Phys.Rev.D 105 (2022)]  
See also [Batell et al. (2011), Dror et al. (2017)]





# An Overall Picture



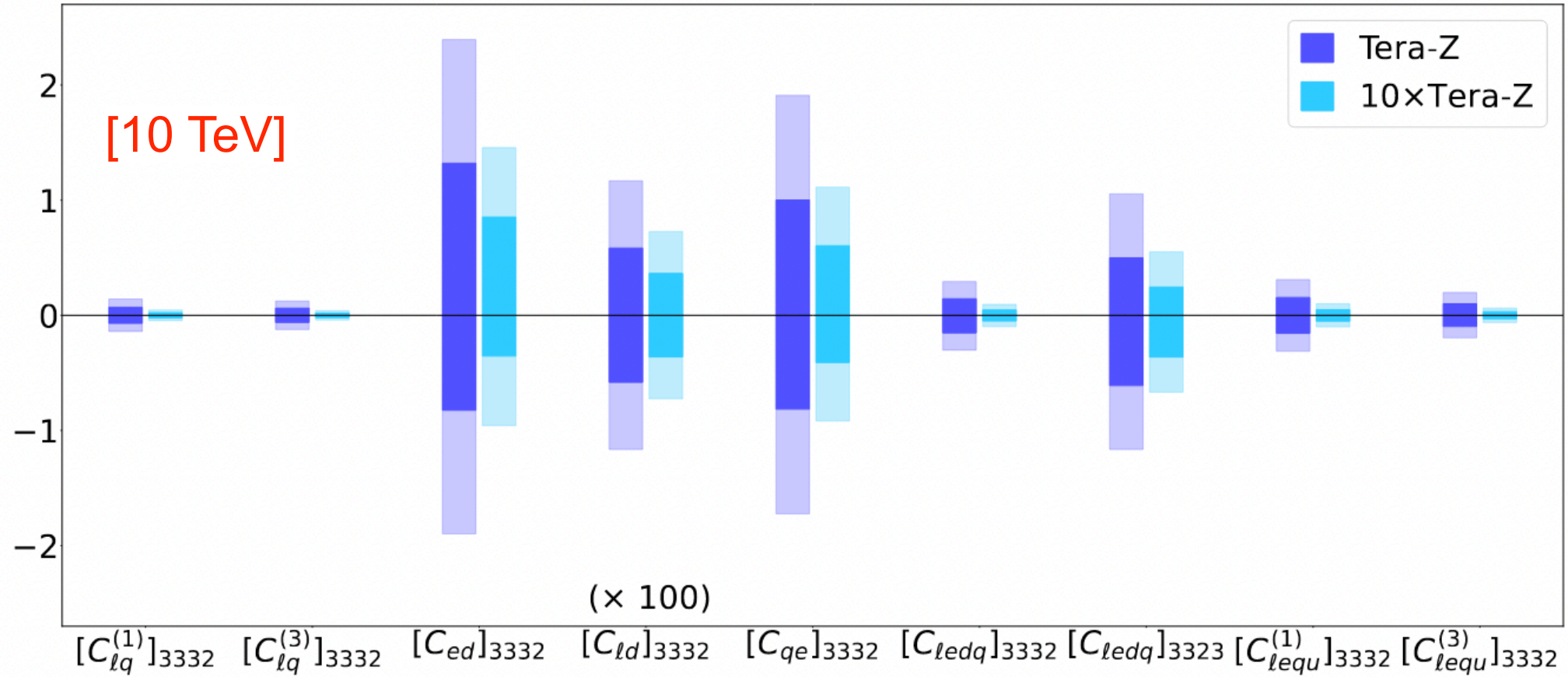
Important for achieving a full test of lepton flavor universality, one of the main hypothetical principles in the SM.





# Interpretation in SMEFT

SMEFT operators	SMEFT operators (down basis)
$[O_{lq}^{(1)}]_{3332}$	$[\bar{\nu}\gamma^\mu P_L \nu + \bar{\tau}\gamma^\mu P_L \tau][\bar{b}\gamma_\mu P_L s]$
$[O_{lq}^{(3)}]_{3332}$	$2V_{cs}^*[\bar{\nu}\gamma^\mu P_L \tau][\bar{b}\gamma_\mu P_L c] - [\bar{\nu}\gamma^\mu P_L \nu - \bar{\tau}\gamma^\mu P_L \tau][\bar{b}\gamma_\mu P_L s]$
$[O_{ed}]_{3332}$	$[\bar{\tau}\gamma^\mu P_R \tau][\bar{b}\gamma_\mu P_R s]$
$[O_{ld}]_{3332}$	$[\bar{\nu}\gamma^\mu P_L \nu + \bar{\tau}\gamma^\mu P_L \tau][\bar{b}\gamma_\mu P_R s]$
$[O_{qe}]_{3332}$	$[\bar{\tau}\gamma^\mu P_R \tau][\bar{b}\gamma_\mu P_L s]$
$[O_{ledq}]_{3332}$	$V_{cs}^*[\bar{\nu}P_R \tau][\bar{b}P_L c] + [\bar{\tau}P_R \tau][\bar{b}P_L s]$
$[O_{ledq}]_{3323}$	$[\bar{\tau}P_R \tau][\bar{s}P_L b]$
$[O_{lequ}^{(1)}]_{3332}$	$V_{cs}^*[\bar{\nu}P_R \tau][\bar{b}P_R c]$
$[O_{lequ}^{(3)}]_{3332}$	$V_{cs}^*[\bar{\nu}\sigma^{\mu\nu} P_R \tau][\bar{b}\sigma_{\mu\nu} P_R c]$





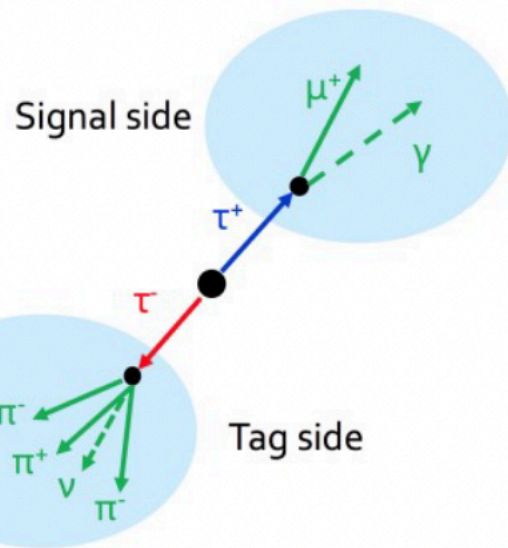
## Highlight IV - Tau Physics

[Pich (2014); Celis et al. (2014); Calibbi and Signorelli (2018);  
Calibbi et. al. (2021, 2022) Dam (2019, 2021)]

Z pole is also good for the test of lepton flavor violation

Measurement	Current [104–106]	FCC [107]	CEPC prelim.	Comments
BR( $Z \rightarrow \tau\mu$ )	$< 6.5 \times 10^{-6}$	$\mathcal{O}(10^{-9})$	same [108]	$\tau\tau$ bkg, $\sigma(p_{\text{track}})$ & $\sigma(E_{\text{beam}})$ limited
BR( $Z \rightarrow \tau e$ )	$< 5.0 \times 10^{-6}$	$\mathcal{O}(10^{-9})$		
BR( $Z \rightarrow \mu e$ )	$< 7.5 \times 10^{-7}$	$10^{-8} - 10^{-10}$	$1 \times 10^{-9}$ [109]	PID limited

$\sim \mathcal{O}(10^{10} - 10^{11}) \tau^+ \tau^-$  pair events are expected to produce at Z pole



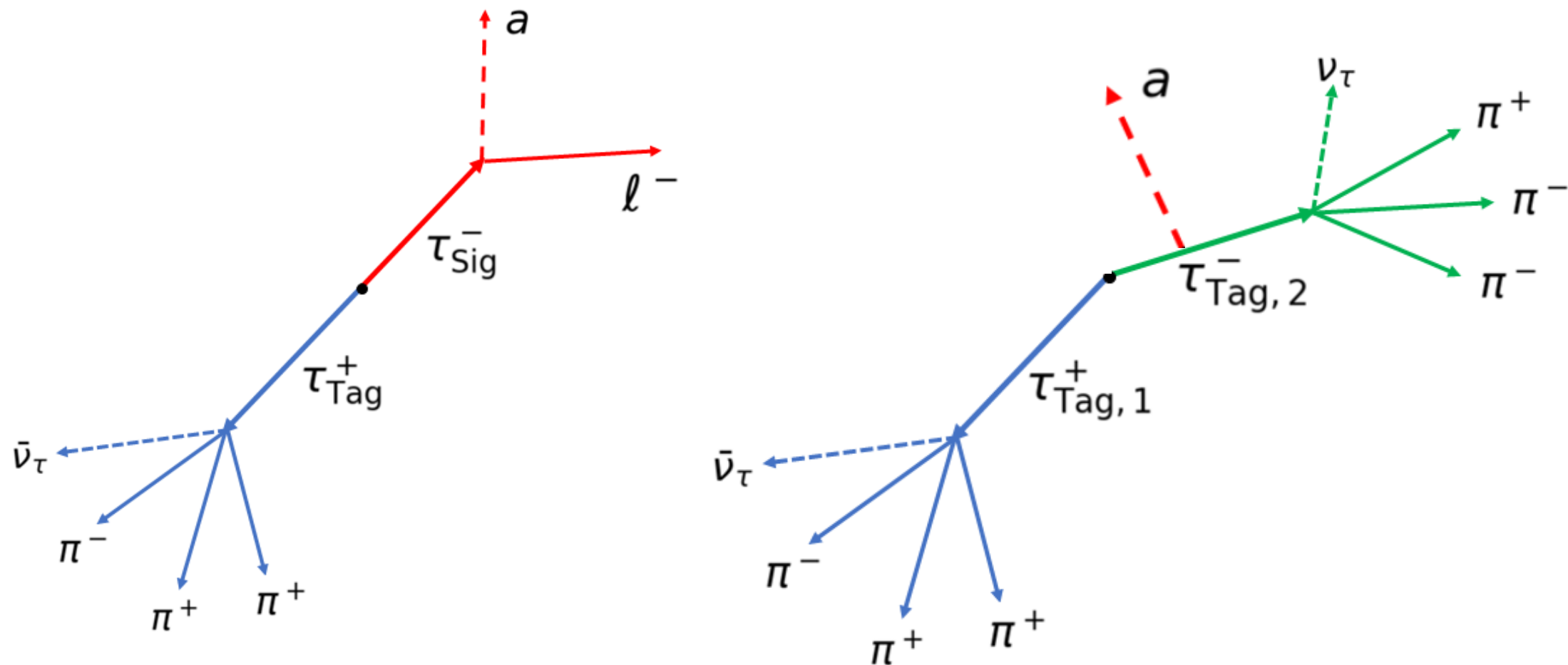
Measurement	Current [149]	FCC [107]	CEPC prelim. [108]	Comments
Lifetime [sec]	$\pm 5 \times 10^{-16}$	$\pm 1 \times 10^{-18}$		from 3-prong decays, stat. limited 0.1× the ALEPH systematics $\sigma(p_{\text{track}})$ limited
BR( $\tau \rightarrow \ell \nu \bar{\nu}$ )	$\pm 4 \times 10^{-4}$	$\pm 3 \times 10^{-5}$		
m( $\tau$ ) [MeV]	$\pm 0.12$	$\pm 0.004 \pm 0.1$		
BR( $\tau \rightarrow \mu\mu\mu$ )	$< 2.1 \times 10^{-8}$	$\mathcal{O}(10^{-10})$	same	bkg free
BR( $\tau \rightarrow eee$ )	$< 2.7 \times 10^{-8}$	$\mathcal{O}(10^{-10})$		
BR( $\tau \rightarrow e\mu\mu$ )	$< 2.7 \times 10^{-8}$	$\mathcal{O}(10^{-10})$		
BR( $\tau \rightarrow \mu ee$ )	$< 1.8 \times 10^{-8}$	$\mathcal{O}(10^{-10})$		
BR( $\tau \rightarrow \mu\gamma$ )	$< 4.4 \times 10^{-8}$	$\sim 2 \times 10^{-9}$	$\mathcal{O}(10^{-10})$	$Z \rightarrow \tau\tau\gamma$ bkg, $\sigma(p_\gamma)$ limited
BR( $\tau \rightarrow e\gamma$ )	$< 3.3 \times 10^{-8}$	$\sim 2 \times 10^{-9}$		





# Highlight V - Light Hidden Bosons

[A. Kwok, TL and L. F. Li, in preparation]

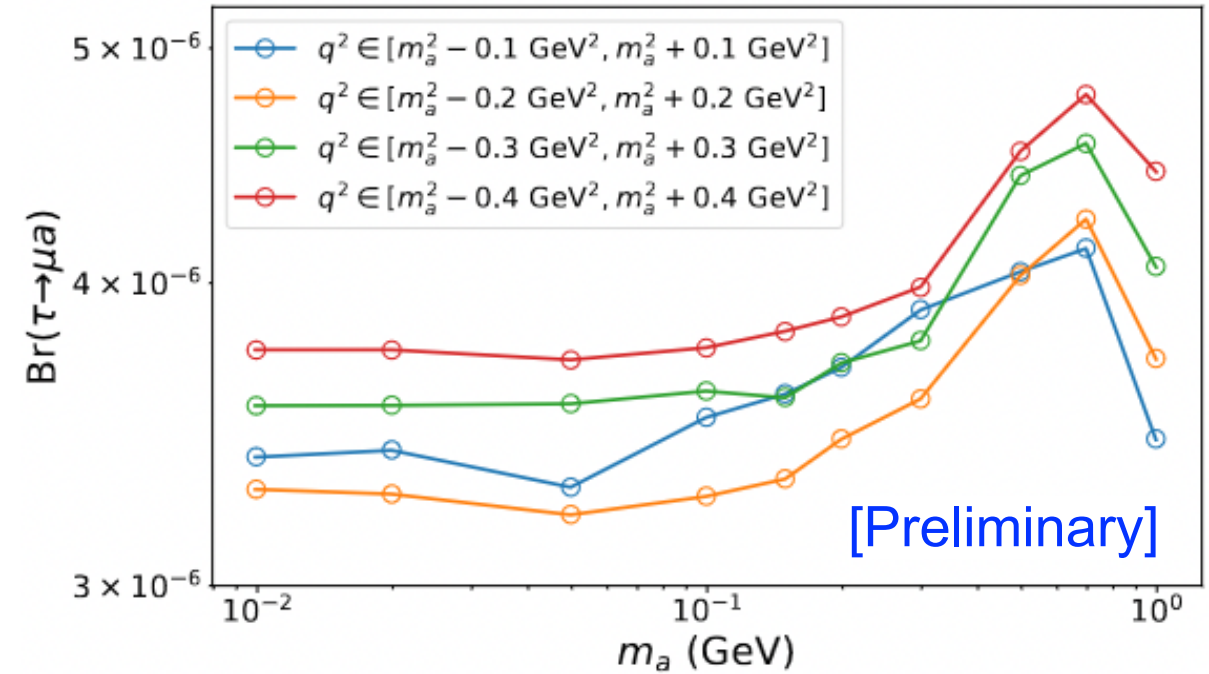
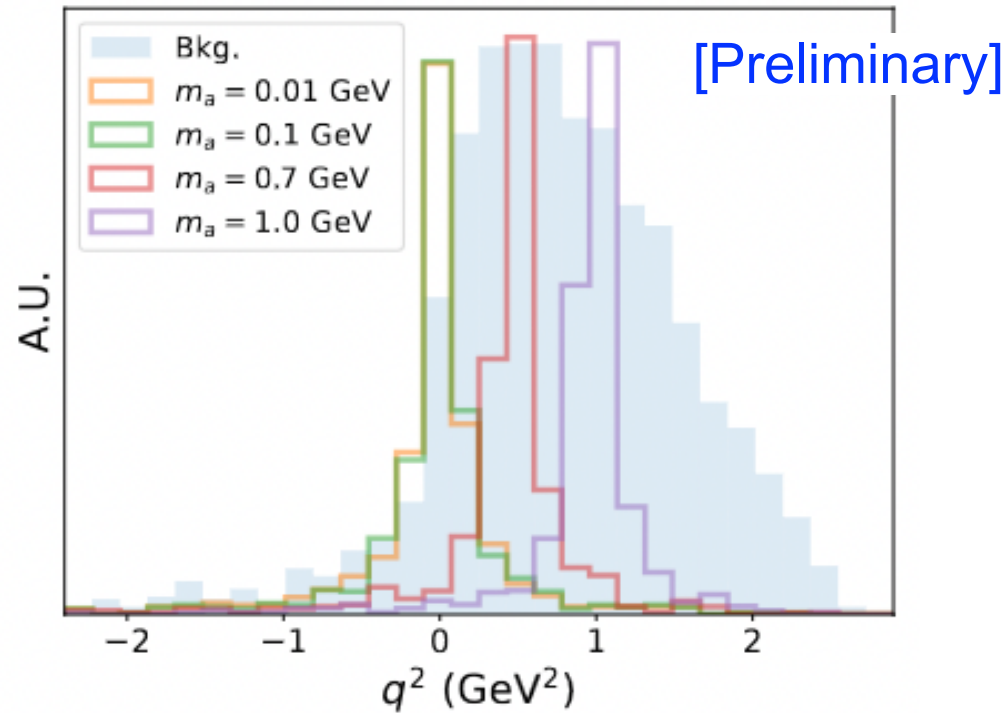


- The light boson can be invisible (missing energy) or visible
- The coupling can be flavor-conserving or violating
- The discussions are applied for both lepton and quark sector



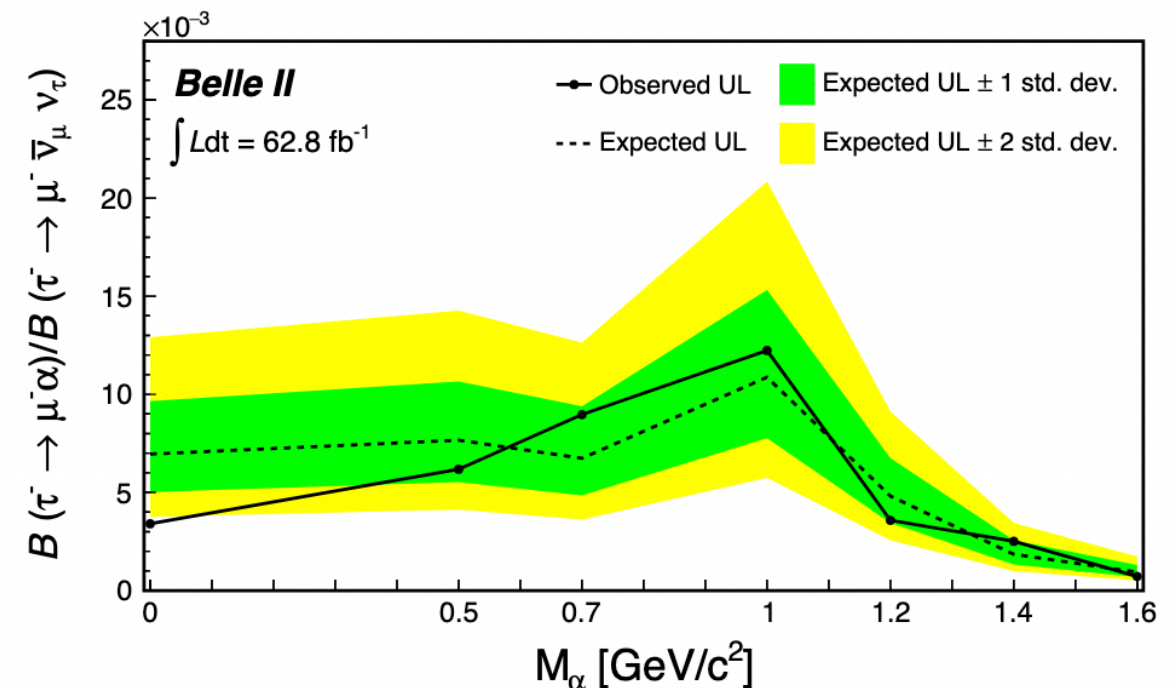
# Highlight V - Light Hidden Bosons

$$Z \rightarrow \tau(\rightarrow \ell + \text{Missing})\tau(\rightarrow 3\pi\nu)$$

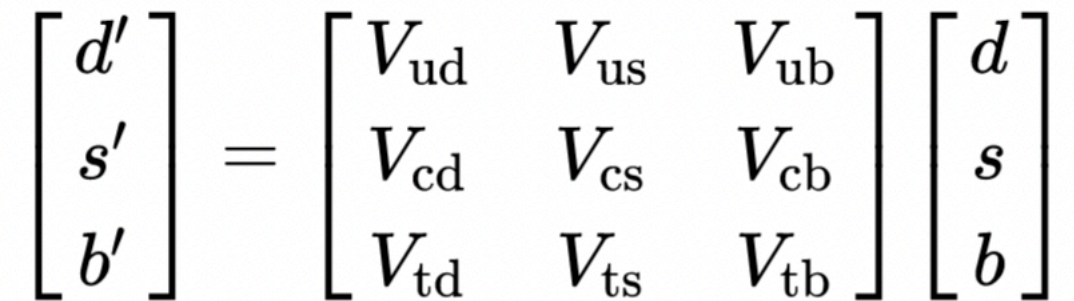


Translate to  $\text{Br}(\tau \rightarrow \mu a) \sim O(10^{-5})$   
for Belle II (50/ab)

[Belle II collaboration,  
Phys.Rev.Lett (2023)]





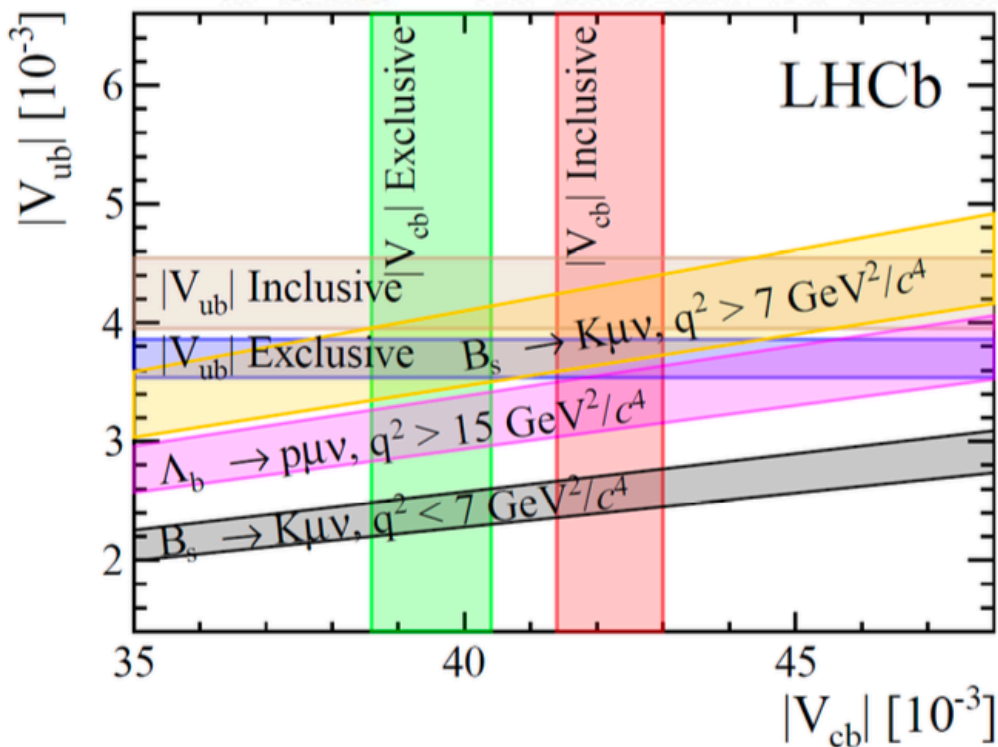


$$\begin{bmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{bmatrix}$$

- A CEPC version will be very informative
- Relevant inputs are still missing
- A task for next stage work



# Highlight VI - CKM Measurement

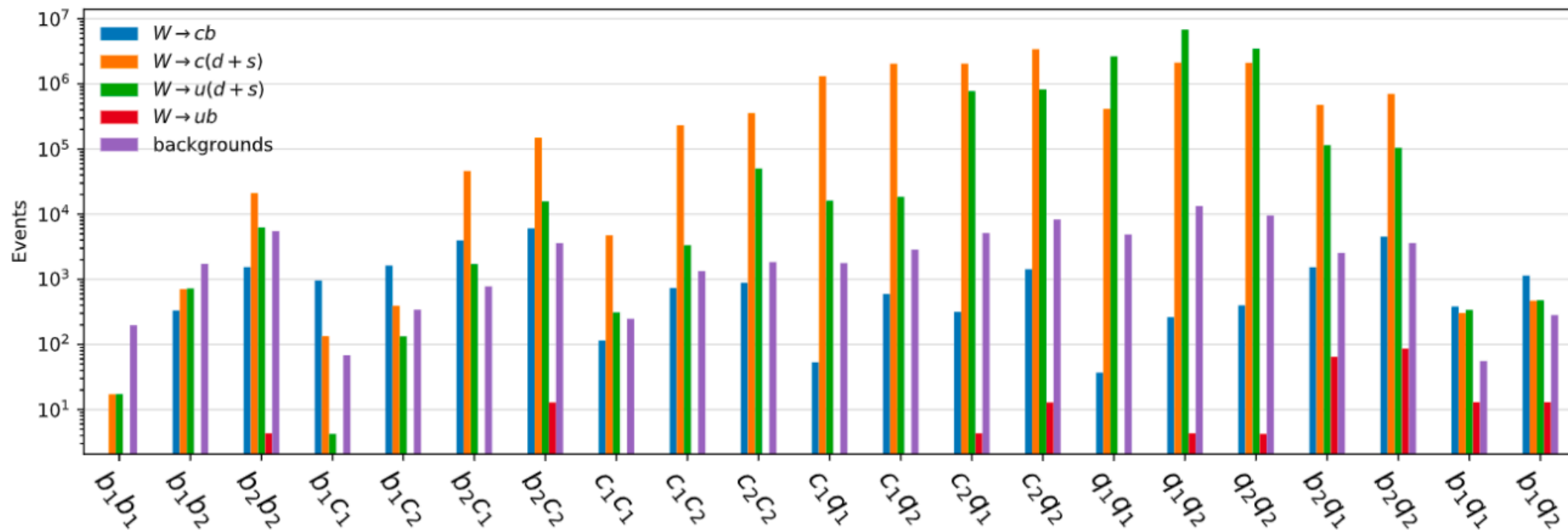


One relevant case is to determine  $V_{cb}$

- Measure  $b \rightarrow c$  transition at Z pole
- Measure  $W \rightarrow bc$  at WW threshold

Current precision is of percent level. Could be improved by one more order of magnitude

[Liang et. al., in preparation]







# Other Opportunities

[For more details,  
see Lingfeng Li's talk]

[See Qin Qin's talk]

[See Fusheng Yu's talk]

[For more details,  
see Tsz Hong Kwok's talk]

[See Guo Fengkun's talk]

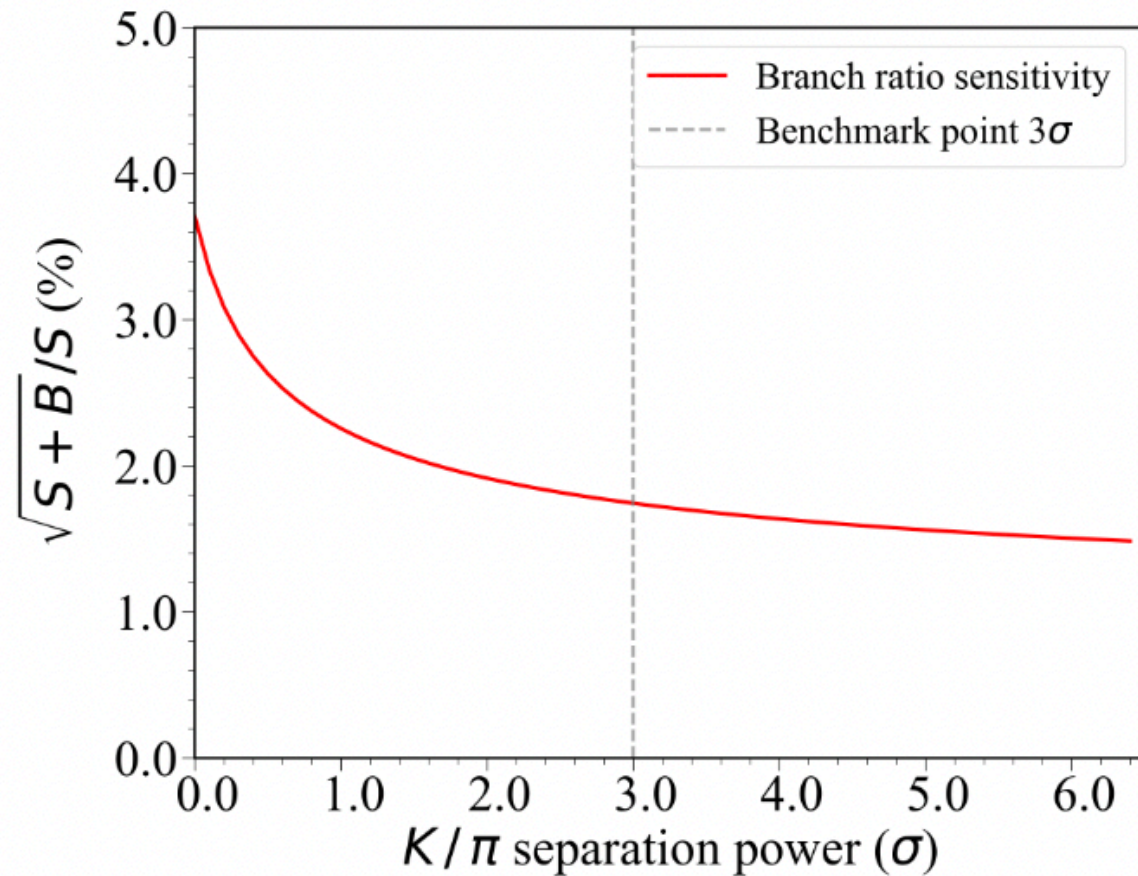
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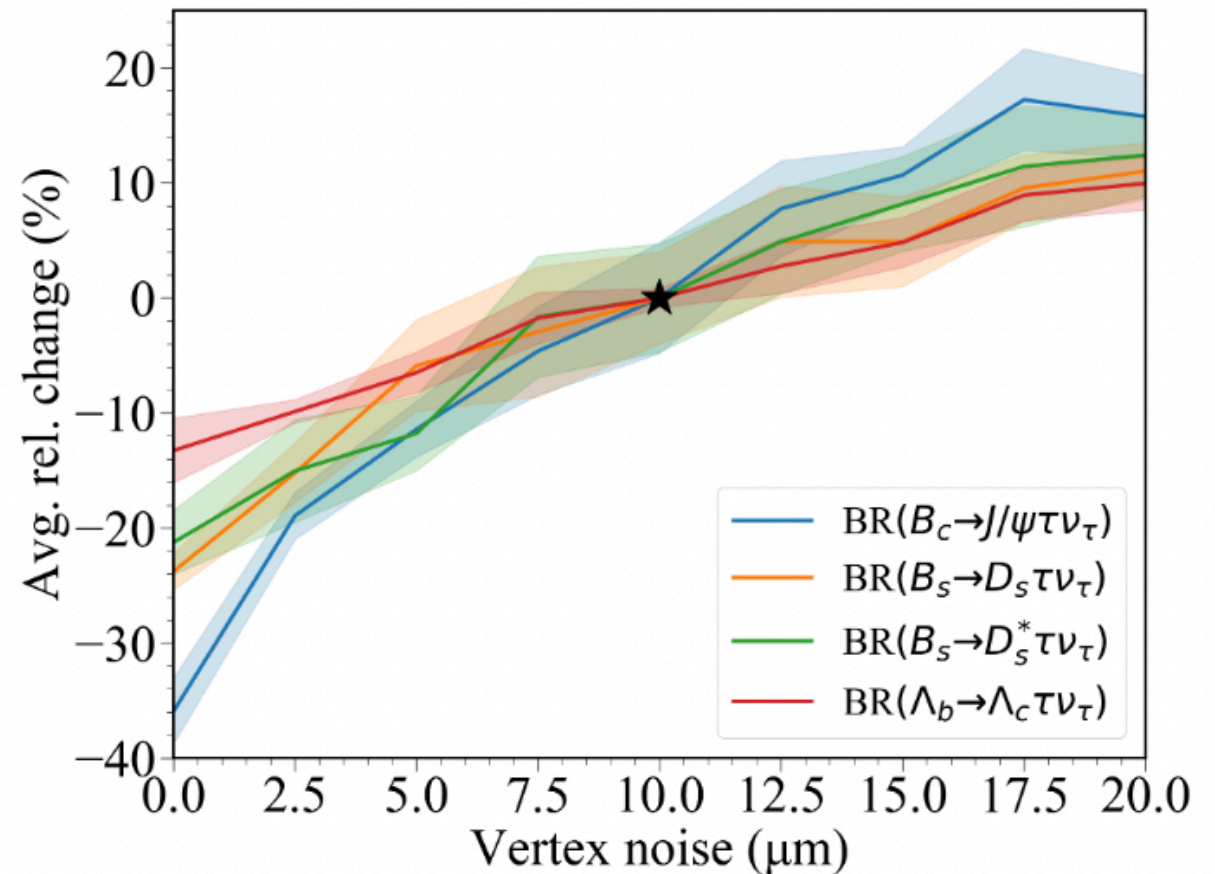


## More Comments

- Detector performance
  - Baseline detector profile has been applied for most of these studies
  - Study on the relation between the sensitivities and detector performance can help to optimize both detector design and physics target precision



BR( $B_s \rightarrow \phi \nu \bar{\nu}$ ) vs. PID performance



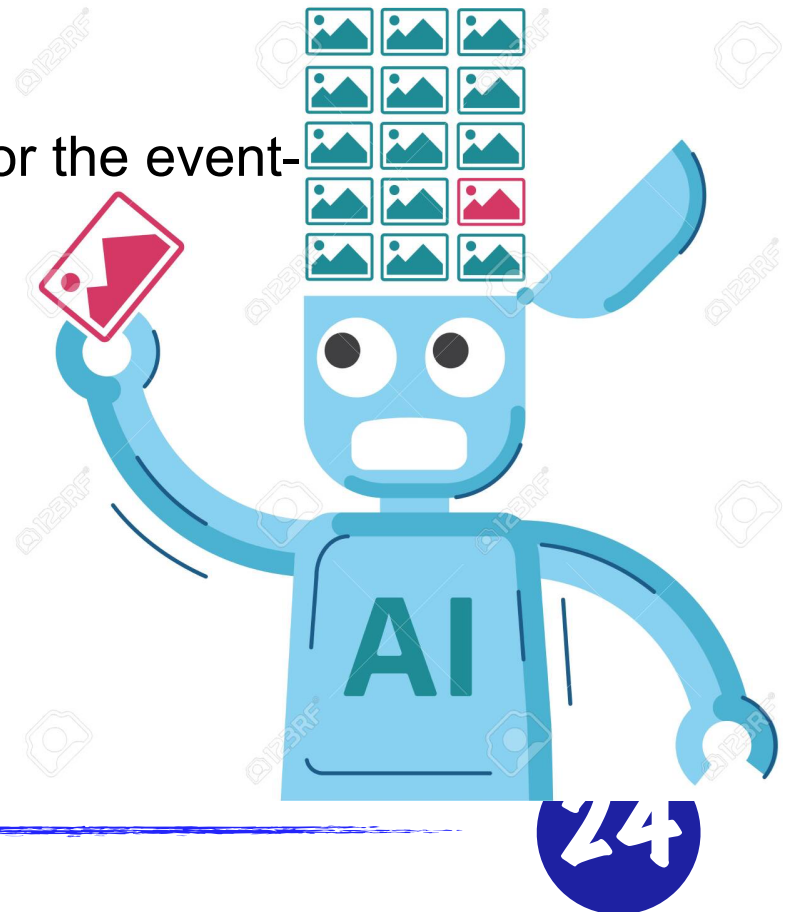
BR( $H_b \rightarrow H_c \tau \nu_\tau$ ) vs. detector vertex noise





## More Comments

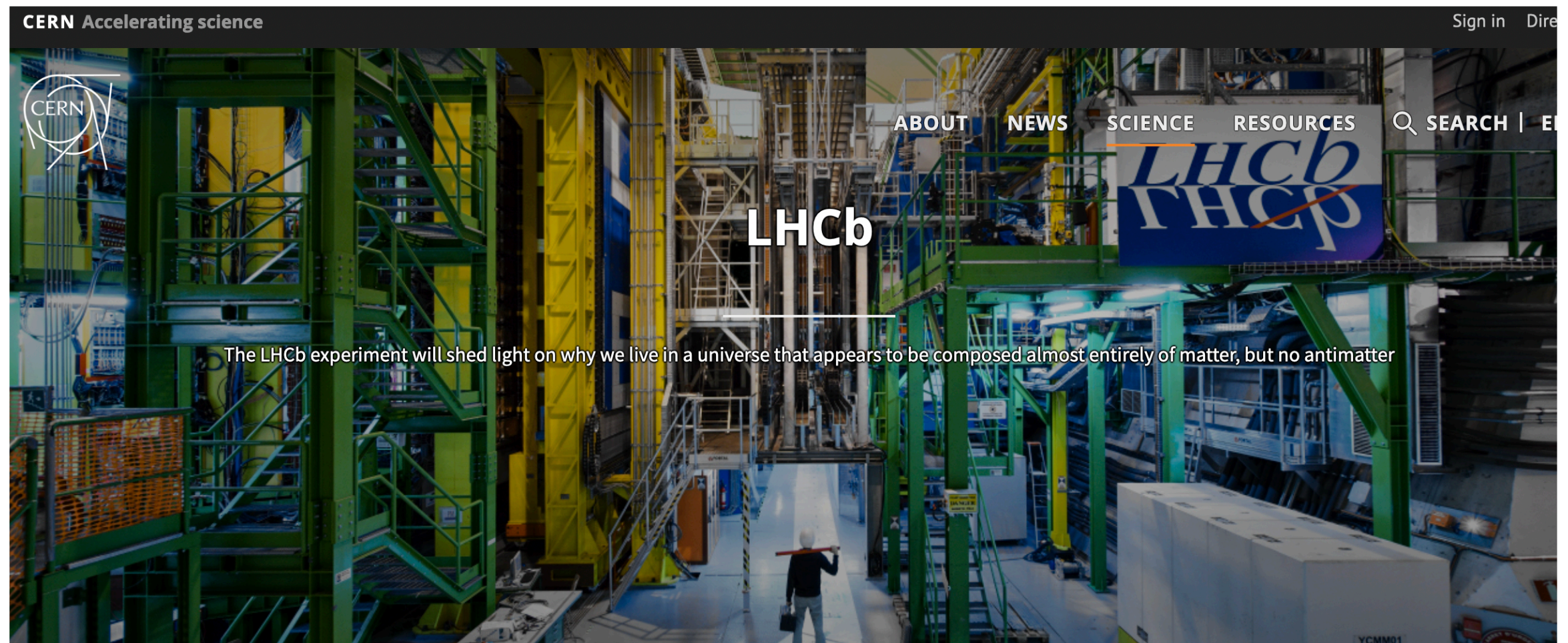
- Systematics understanding
  - Current discussions of sensitivities are essentially statistical
  - Can the experimental systematics be controlled to be below or comparable to the statistical ones?
  - Can theoretical accuracy for the background calculations and the signal predictions catch up with experiment progress by the time of CEPC data taking?
- Advanced analysis tools such as deep neural network
  - Many of these studies so far are cut-based
  - To what extent the ML tool can help if the event topology is complex or the event-level message is relevant





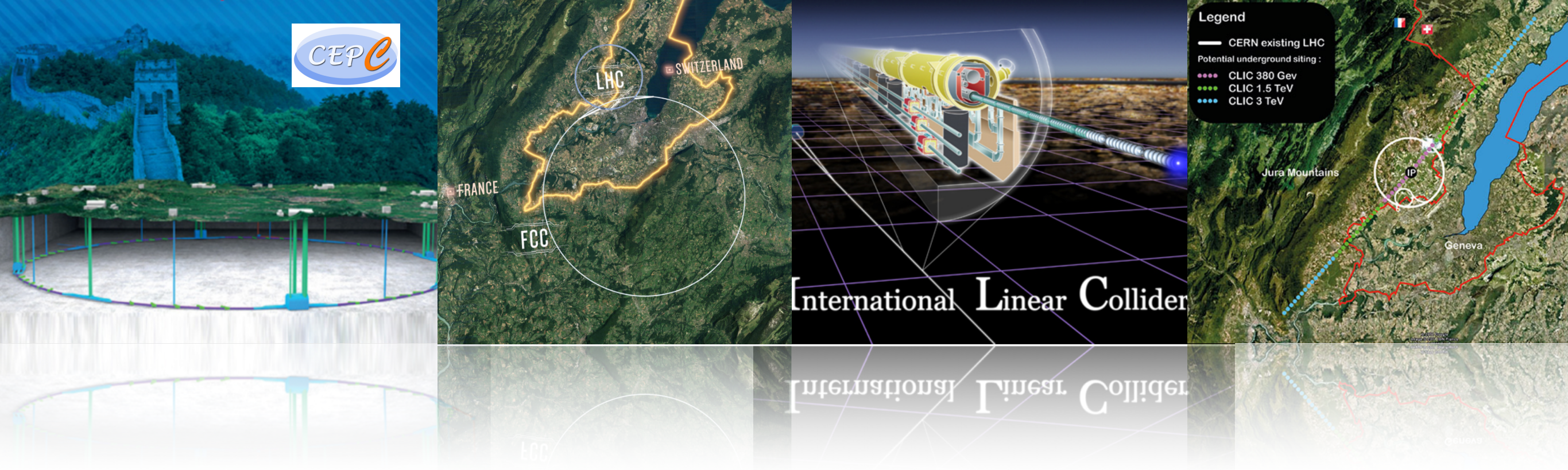
## More Comments

- Theoretical understanding
  - Full understanding on the relationship between various flavor phenomena and fundamental physics is demanded
  - Explore the potential impacts of flavor physics for the matter evolution of the universe, such as the origin of baryon asymmetry (for an early effort, see, [\[TL, M. Ramsey-Musolf, J. Shu, Phys.Rev.Lett. 108 \(2012\)\]](#))



The [Large Hadron Collider beauty](#) (LHCb) experiment specializes in investigating the slight differences between matter and antimatter by studying a type of particle called the "beauty quark", or "b quark".





## Take-home Message

We live at a unique juncture in history!

As a multi-functional machine, we would like to know the capability of the next-generation  $e^-e^+$  colliders like CEPC, to push forward the relevant physics frontiers.

As part of its physics potential, Higgs physics, electroweak precision measurements and top physics at such an  $e^-e^+$  collider have been extensively studied

Flavor physics is of high scientific value. The opportunities brought up by such a machine should be fully explored also. Efforts have been initiated in recent years. But, more comprehensive study is still needed. Stay tuned!





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*Thank you!*