

# Light Scalars at Future Collider

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*Based on work with F. Kling, S. Li, S. Su, W. Su*

The 2023 international workshop on the high energy Circular Electron Positron Collider @ Nanjing



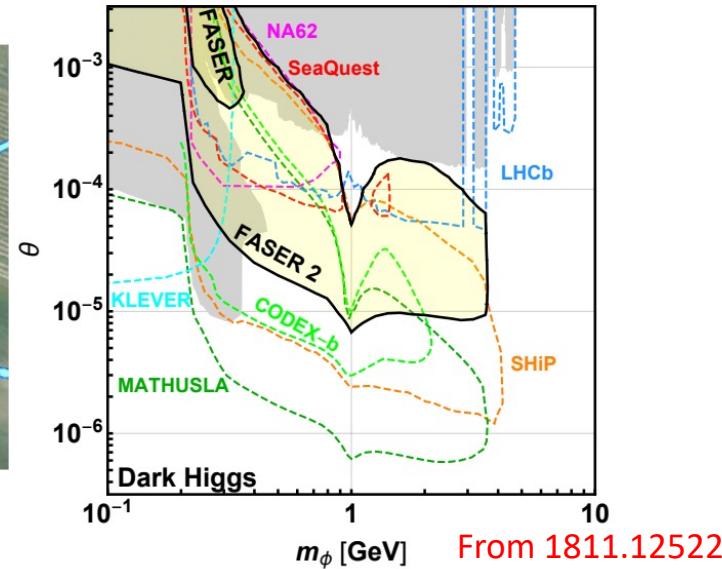
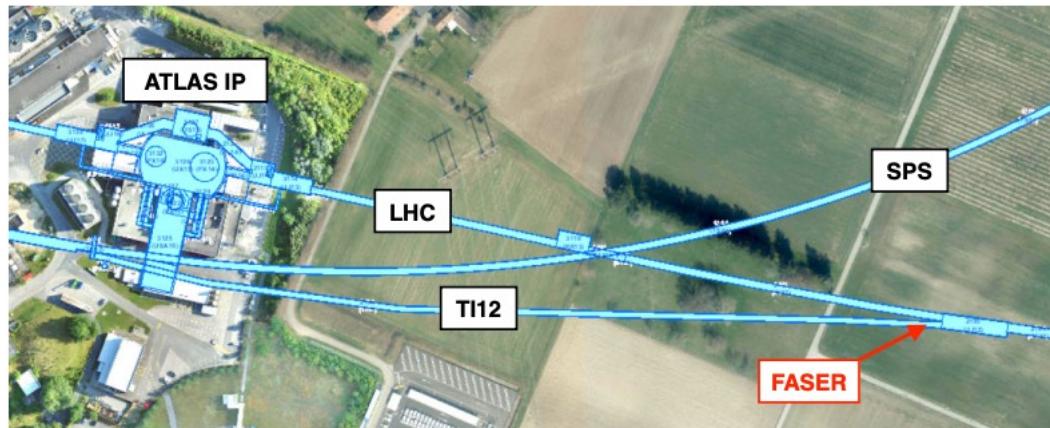
Oct 26, 2023

# Light Scalars @ LHC

Many Beyond Standard Models including extended Higgs sector permit the light and weakly coupled scalars, such as Dark Higgs (SM+Singlet), 2HDM, 2HDM+(P)S, NMSSM, ....

Simplest prototype model:  
Dark Higgs

$$\mathcal{L} = -m_\phi^2 \phi^2 - \sin \theta \frac{m_f}{v} \phi \bar{f} f - \lambda v h \phi \phi + \dots$$



# Light cP-even Scalar

**Effective  
Lagrangian**

$$\mathcal{L} = -\frac{1}{2}m_\phi^2\phi^2 - \sum_f \xi_\phi^f \frac{m_f}{v} \phi \bar{f} f + \xi_\phi^W \frac{2m_W^2}{v} \phi W^\mu W_\mu^- + \xi_\phi^Z \frac{m_Z^2}{v} \phi Z^\mu Z_\mu \\ + \xi_{\phi\phi}^W \frac{g^2}{4} \phi \phi W^\mu W_\mu^- + \xi_{\phi\phi}^Z \frac{g^2}{8 \cos^2 \theta_W} \phi \phi Z^\mu Z_\mu + \xi_\phi^g \frac{\alpha_s}{12\pi v} \phi G_{\mu\nu}^a G^{a\mu\nu} + \xi_\phi^\gamma \frac{\alpha_{ew}}{4\pi v} \phi F_{\mu\nu} F^{\mu\nu}$$

coupling modifiers

loop generated

Production  
at Hadron Collider

- decay of mesons, hadrons, radiative bottomonium
- Bremsstrahlung: small for high beam energies
- photon/gluon fusion: smaller, small in forward region
- h/Z/W decay: small in forward region

$$\mathcal{L}_{eff} = \frac{\phi}{v} \sum \xi_\phi^{ij} m_{f_j} \bar{f}_i P_R f_j + h.c. \quad \mathcal{L} \supset \xi_{\phi\phi}^{ij} \frac{\phi^2}{v^2} m_j \bar{f}_i P_R f_j + h.c.$$

effective coupling for flavor changing quark interactions

# Numbers of Mesons Produced at (Future) colliders

$b$ -hadrons	Belle II	LHCb ( $300 \text{ fb}^{-1}$ )	Tera-Z
$B^0, \bar{B}^0$	$5.4 \times 10^{10}$ ( $50 \text{ ab}^{-1}$ on $\Upsilon(4S)$ )	$3 \times 10^{13}$	$1.2 \times 10^{11}$
$B^\pm$	$5.7 \times 10^{10}$ ( $50 \text{ ab}^{-1}$ on $\Upsilon(4S)$ )	$3 \times 10^{13}$	$1.2 \times 10^{11}$
$B_s^0, \bar{B}_s^0$	$6.0 \times 10^8$ ( $5 \text{ ab}^{-1}$ on $\Upsilon(5S)$ )	$1 \times 10^{13}$	$3.1 \times 10^{10}$
$B_c^\pm$	-	$1 \times 10^{11}$	$1.8 \times 10^8$
$\Lambda_b^0, \bar{\Lambda}_b^0$	-	$2 \times 10^{13}$	$2.5 \times 10^{10}$

[Wang et al. 2208.08327](#)

## Forward Region at ATLAS (FASER) for LHC Run 3 ( $150 \text{ fb}^{-1}$ )

$$N_{\pi^0} \approx 2.3 \times 10^{17}, \quad N_\eta \approx 2.5 \times 10^{16}, \quad N_D \approx 1.1 \times 10^{15}, \quad \text{and} \quad N_B \approx 7.1 \times 10^{13}$$

For HL-LHC ( $a \text{ ab}^{-1}$ ), 20-fold increase can be expected.

At FCC-hh, the amount of produced B mesons at FCC-hh will be at least 30 times larger, assuming  $20 \text{ ab}^{-1}$  total integrated luminosity.

[Boyarsky et al. 2204.01622](#)

# Light Scalars @ Forward Physics Facility (FPF)

**Model-independent framework with the most general interactions  
for CP-even and CP-odd scalar under EFT/coupling modifier.**

- developed general formalism for scalar production and decay
- CP-odd A mix with light meson states
- developed a program to calculate scalar decay, can be used for other new physics models
- more complicated comparing to the simplest scenario
- case study of 2HDM.

# $\phi$ Production

- Heavy B meson decay

$$B \rightarrow X_s \phi \quad \xi_{\phi}^{bs}$$

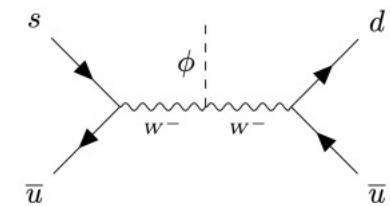
- Semileptonic decay of mesons

$$X \rightarrow \phi e \nu \quad \xi_{\phi}^W$$

- Kaon decay

$$K \rightarrow \pi \phi$$

$$\xi_{\phi}^{ds} \quad \xi_{\phi}^W$$



- $\eta^{(\prime)}$  decay

$$\eta^{(\prime)} \rightarrow \pi \phi$$

$$g_{\phi \eta^{(\prime)} \pi}$$

- Radiative bottomonium decay

$$\Upsilon \rightarrow \gamma \phi \quad \xi_{\phi}^b$$

- Double scalar production

$$B \rightarrow X_s \phi \phi \quad K \rightarrow \pi \phi \phi \quad \xi_{\phi \phi}^{ij}$$

# $\phi$ Decay

Decay into a pair of photons, leptons, pair of quarks (gluons)/multiple hadrons

- Decay into diphoton

$$\Gamma_{\gamma\gamma} = \frac{G_F \alpha_{ew}^2 m_\phi^3}{32\sqrt{2}\pi^3} |\xi_\phi^\gamma|^2$$

- Decay into dilepton

$$\Gamma_{\ell^+\ell^-} = \frac{G_F m_\phi m_\ell^2 \beta_\ell^3}{4\sqrt{2}\pi} |\xi_\phi^\ell|^2$$

$m_\phi > 2$  GeV: perturbative spectator model

- Decay into diquark

$$\Gamma_{\ell^+\ell^-} : \Gamma_{s\bar{s}} : \Gamma_{c\bar{c}} : \Gamma_{b\bar{b}} = |\xi_\phi^\ell|^2 m_\ell^2 \beta_\ell^3 : 3|\xi_\phi^s|^2 m_s^2 \beta_K^3 : 3|\xi_\phi^c|^2 m_c^2 \beta_D^3 : 3|\xi_\phi^b|^2 m_b^2 \beta_B^3$$

- Decay into digluon

$$\Gamma_{gg} = \frac{G_F \alpha_s^2 m_\phi^3}{36\sqrt{2}\pi^3} |\xi_\phi^g|^2$$

$m_\phi < 2$  GeV: dispersive analyses

- Hadronic decay into pions and kaons

$$\Gamma_\pi \quad \Delta_\pi \quad \Theta_\pi$$

$$\xi_\phi^u \quad \xi_\phi^d \quad \xi_\phi^s \quad \xi_\phi^d$$

- Further hadronic decays

$$\phi \rightarrow 4\pi, \eta\eta, KK\pi\pi, \rho\rho \dots$$

$$\Gamma_{4\pi,\eta\eta,\rho\rho,\dots} = C |\xi_\phi^g|^2 m_\phi^3 \beta_{2\pi}$$

# 2HDM

## Two Higgs Doublet Model (CP-conserving): $\phi_{1,2}$

After EWSB, 5 physical Higgses:

**CP-even Higgses:  $h$ ,  $H$ , CP-odd Higgs:  $A$ , charged Higgses:  $H^\pm$**

parameters (CP-conserving, flavor limit,  $Z_2$  symmetry)

$v, \tan \beta, \alpha, m_h, m_H, m_A, m_{H^\pm}$  soft  $Z_2$  breaking:  $m_{12}^2$

Alignment limit:  $h$  is 125 GeV Higgs,  $\cos(\beta - \alpha) \sim 0$

- Type I:  $\phi_1$  couples quarks and leptons  
all fermion couplings suppressed at large  $\tan \beta \Rightarrow$  LLP
- Type II, L, F:  $\phi_{1,2}$  couples to at least one type of quarks or leptons  
unsuppressed couplings of scalars to at least one type of fermions for the entire region of  $\tan \beta \Rightarrow$  difficult to realize very weakly coupled long-lived scalars

# constraints

- Theoretical constraints: unitarity, perturbativity, vacuum stability
- EW precision constraints
- Flavor constraints
- Invisible Higgs decay
- LEP & LHC  $H^\pm$  search

## Two benchmark scenarios

Light  $H$  :  $\cos(\beta - \alpha) = \frac{1}{\tan \beta}$ ,  $m_A = m_{H^\pm} = 600$  GeV,  $\lambda v^2 = 0$

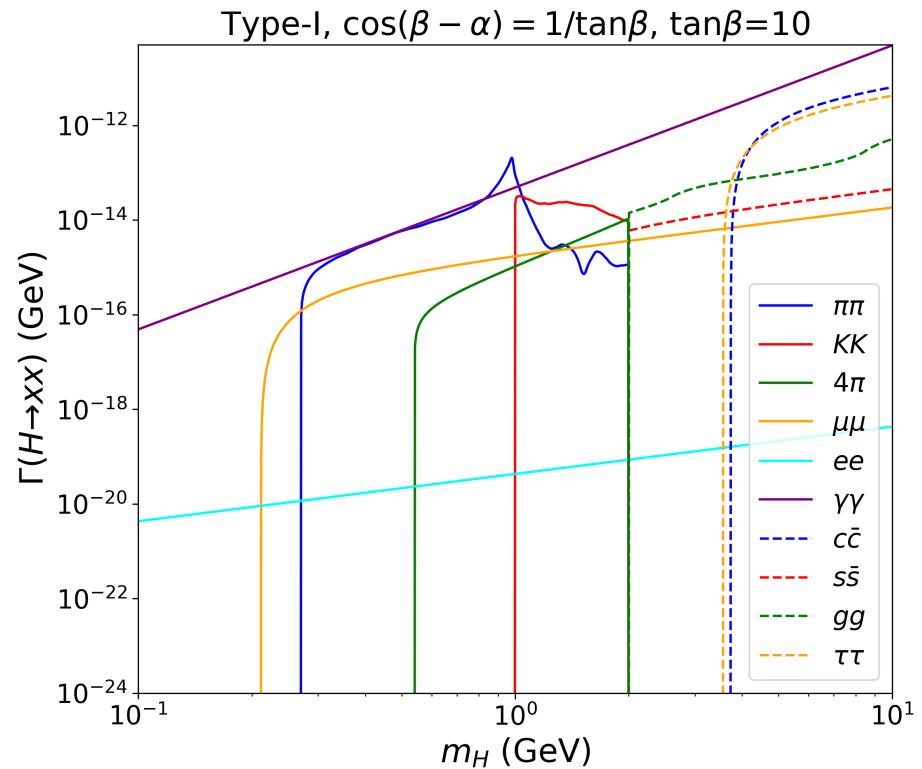
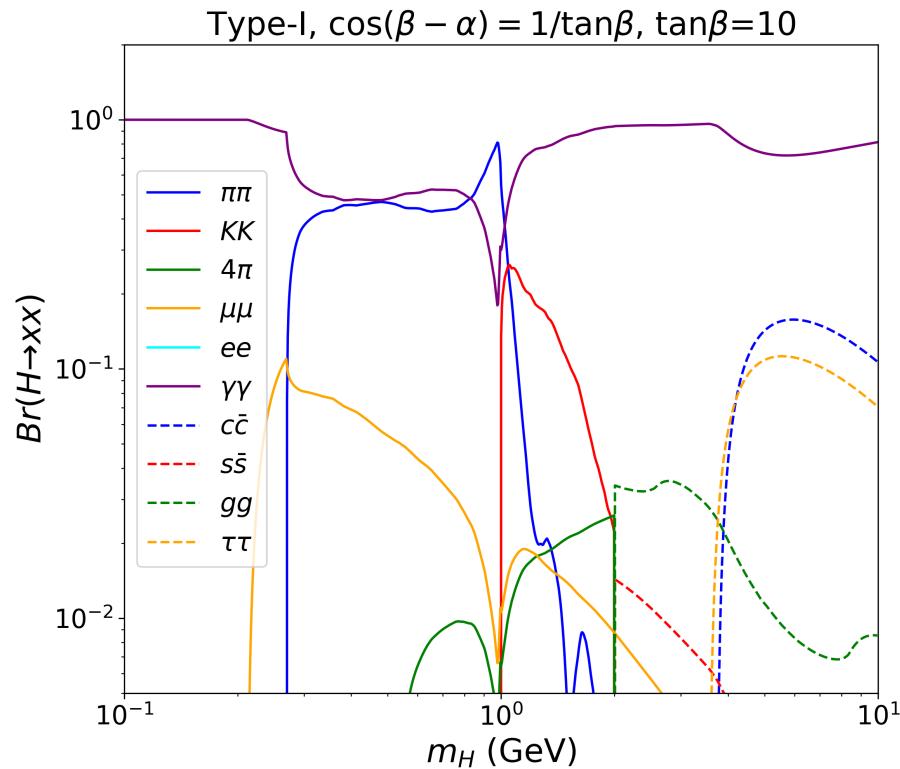
Light  $A$  :  $\cos(\beta - \alpha) = 0$ ,  $m_H = m_{H^\pm} = 90$  GeV,  $\lambda v^2 = 0$ ,

$$\xi_A^f|_{\cos(\beta-\alpha)=0} = 1/\tan \beta,$$

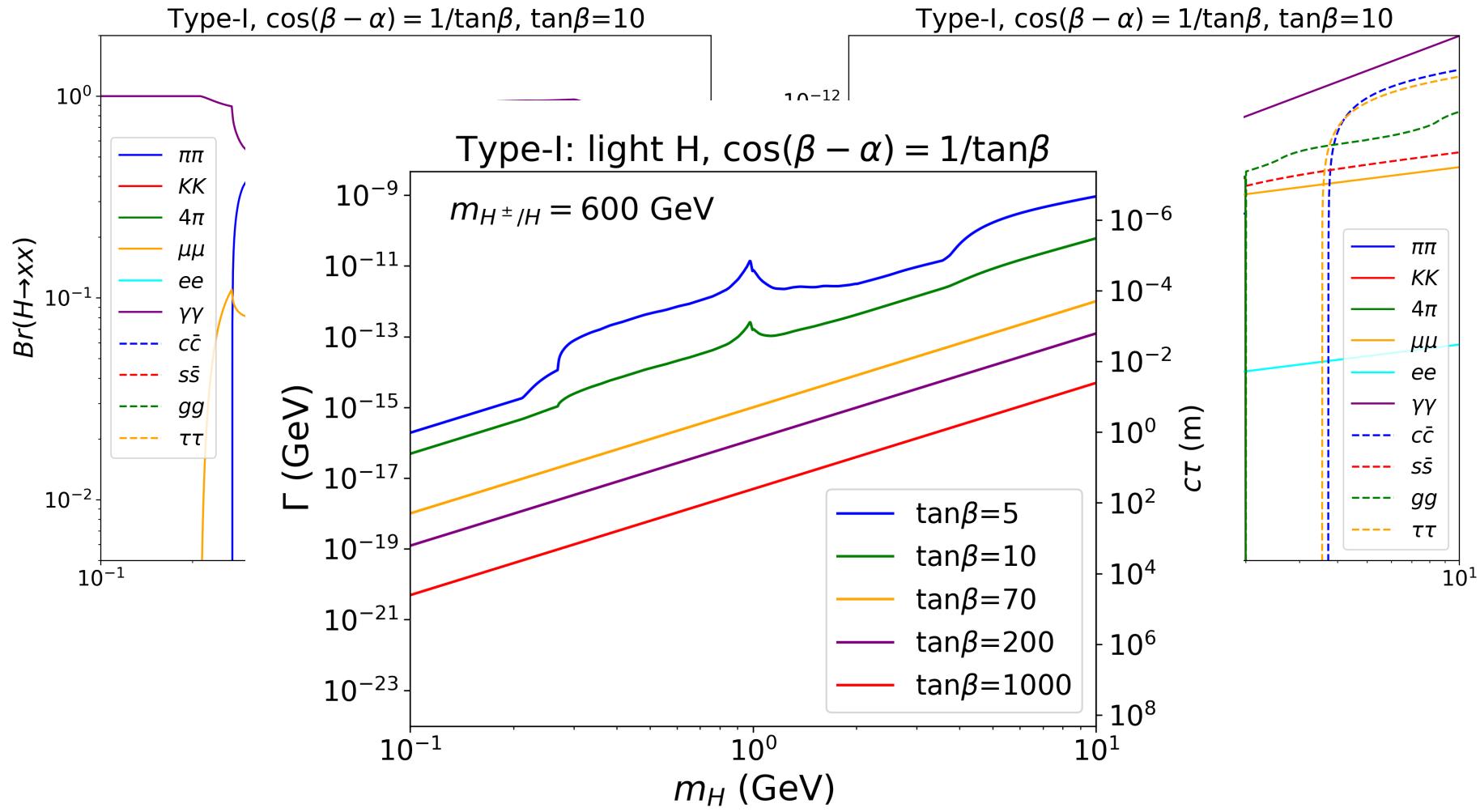
$$\xi_H^V = c_{\beta-\alpha} = 1/\tan \beta,$$

$$\xi_H^f = c_{\beta-\alpha}(1 - s_{\beta-\alpha}) \approx 1/(2 \tan^3 \beta) + \mathcal{O}(c_{\beta-\alpha}^5)$$

# Light cP-even Scalar



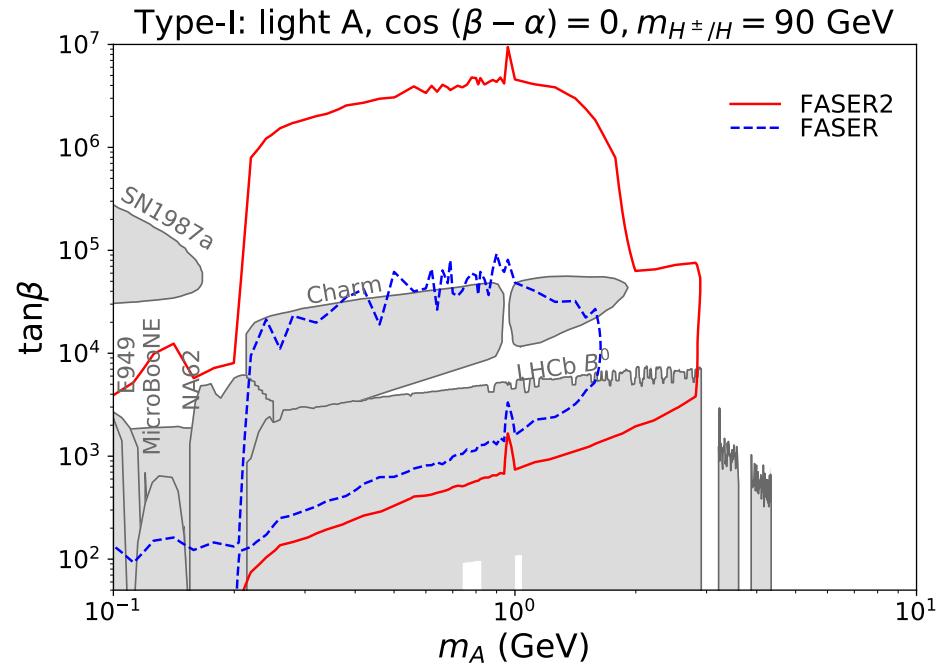
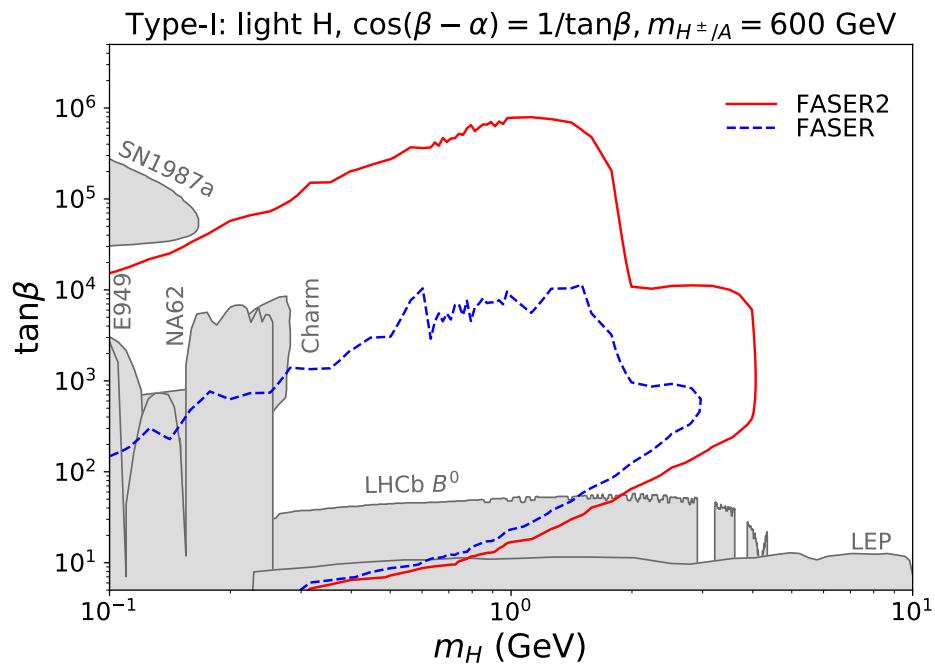
# Light cP-even Scalar



# Other constraints on Light Scalar Searches

- **CHARM bounds: light ALP** CHARM, PLB 157 (1985) 458
- **Supernova:  $NN \rightarrow NNS(A)$**  Turner, PRL 60 (1988) 1797
- **B meson decays:  $B \rightarrow K^* \phi$  (LHCb)** LHCb, 1508.04094, 1612.07818
- **D meson decays:  $D^+ \rightarrow \pi^+ \phi$  (LHCb)** PDG, LHCb, 2011.00217  
NA62, 2103.15389
- **Kaon decays:  $K^+ \rightarrow \pi^+ \phi$  (NA62, MicroBooNE, E949)** MicroBooNE, 2106.00568  
BNL-E949, 0903.0030
- **LEP:  $e^- e^+ \rightarrow Z^* \phi$**  Winkler, 1809.01876  
Clarke, Foot and Volkas, 1310.8042

# Light Scalars Reaches at FPF

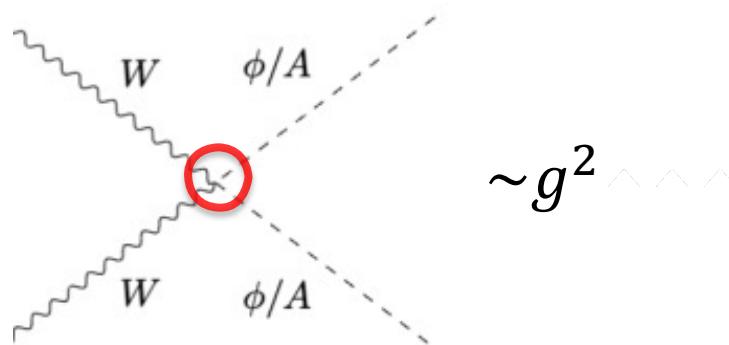


$$\xi_A^f|_{\cos(\beta-\alpha)=0} = 1/\tan\beta,$$

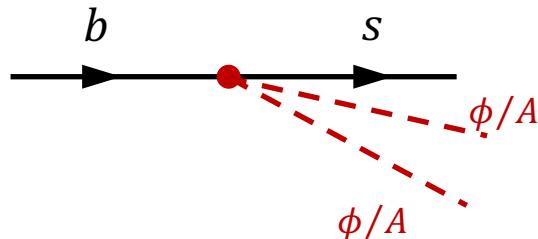
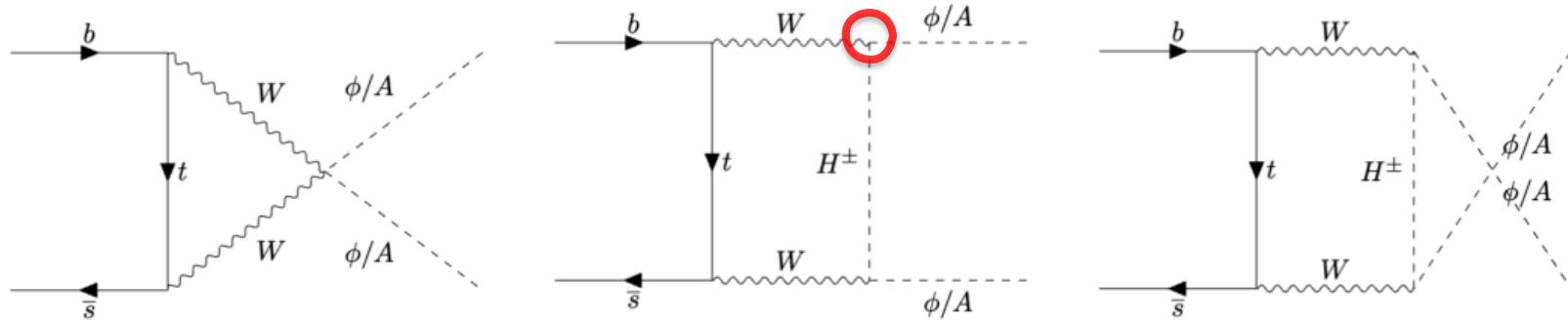
$$\xi_H^V = c_{\beta-\alpha} = 1/\tan\beta,$$

$$\xi_H^f = c_{\beta-\alpha}(1 - s_{\beta-\alpha}) \approx 1/(2\tan^3\beta) + \mathcal{O}(c_{\beta-\alpha}^5)$$

# Double Scalar Production



Governed by gauge symmetry  
and not suppressed



$$\mathcal{L} \supset \xi_{\phi\phi}^{ij} \frac{\phi^2}{v^2} m_j \bar{f}_i P_R f_j + \xi_{AA}^{ij} \frac{A^2}{v^2} m_j \bar{f}_i P_R f_j + h.c.$$

# More on Lepton colliders

- Z associated production (like LEP  $e^-e^+ \rightarrow Z^*\phi$ )
- h/Z/W decay (isotropic, commonly considered)
- decay of mesons, hadrons, radiative bottomonium (from h/Z/W decay)
- photon fusion (not important)

New detectors: HERmetic CAvern TrackEr (HECATE)

[Chrząszcza et al. 2011.01005](#)

A large volume cavern is needed for FCC-hh/SppC detectors, while the detectors at the ee phase are rather small. Thus a MATHUSLA-like detector can be installed.

- Origins of the LLPs: two bottoms or charms, one of which can be tagged in the standard detector
- Complementary to MET search at the main detector
- More sensitive to lighter and longer lifetime particles, compared to displaced vertices search at the main detector in the

# More on Scalar EFTs

$$\begin{aligned}\mathcal{L} = & -\frac{1}{2}m_\phi^2\phi^2 - \sum_f \xi_\phi^f \frac{m_f}{v} \phi \bar{f} f + \xi_\phi^W \frac{2m_W^2}{v} \phi W^\mu{}^+ W_\mu^- + \xi_\phi^Z \frac{m_Z^2}{v} \phi Z^\mu Z_\mu \\ & + \xi_{\phi\phi}^W \frac{g^2}{4} \phi \phi W^\mu{}^+ W_\mu^- + \xi_{\phi\phi}^Z \frac{g^2}{8 \cos^2 \theta_W} \phi \phi Z^\mu Z_\mu + \xi_\phi^g \frac{\alpha_s}{12\pi v} \phi G_{\mu\nu}^a G^{a\mu\nu} + \xi_\phi^\gamma \frac{\alpha_{ew}}{4\pi v} \phi F_{\mu\nu} F^{\mu\nu}\end{aligned}$$

Dark Higgs:  $\xi = \sin \theta$

2HDM (Type-I):

$$\begin{aligned}\xi_H^V &= \cos(\beta - \alpha) = \cot \beta \\ \xi_H^f &= \cot^3 \beta \\ \xi_{HH}^V &= 1\end{aligned}$$

$$\begin{aligned}\xi_A^V &= \cos(\beta - \alpha) = 0 \\ \xi_A^f &= \cot \beta \\ \xi_{AA}^V &= 1\end{aligned}$$

$$\begin{aligned}sH^\dagger{}^i (d_{cp}{}^a Q_{rai}) \\ s^2 H^\dagger{}^i (\dot{d}_{cp}{}^a Q_{rai})\end{aligned}$$

2HDM (Type-II)+a:

[HS, Wei Su, 2311.xxxxx](#)

$$\begin{aligned}\xi_a^V &= \cos(\beta - \alpha) \sin \theta \\ \xi_A^u &= \cot \beta \sin \theta, \xi_A^d = \tan \beta \sin \theta\end{aligned}$$

D meson physics?

Scalar (singlet) extension of the SMEFT  $\longrightarrow$   $\phi$ EFT

[HS, Sun, Yu, 2305.16770](#)

[HS, Sun, Yu, 2306.05999](#)

- CHARM (FASER-like) bounds: reinterpretation
- Supernova bound:  $NN \rightarrow NNS(A)$  suppressed,  $NN \rightarrow NNSS(AA)$ ?

# conclusion

- ❖ Light LLP appear in many new physics scenarios
- ❖ Light particle copiously produced in the forward region of Hadron colliders (LHC), and FASER/FASER2 (FPF): new experiments to detect light LLP
- ❖ Light (pseudo)scalar
  - Model-independent framework, coupling modified in EFT
  - Scalar production and decay (hadronic)
  - Public code to calculate decay  
([https://github.com/shiggs90/Light\\_scalar\\_decay.git](https://github.com/shiggs90/Light_scalar_decay.git))
- ❖ 2HDM case study: large  $\tan\beta$  region of Type-I 2HDM
  - decay length:  $10^{-8}$  to  $10^5$  m, probe very large  $\tan\beta$
  - FASER2 vs. FASER: higher Lum, larger detector
- ❖ Complementary to prompt search, LLP search in transverse region, and fixed target exp at low energies, or other astrophysical processes (e.g. supernova)



# Backup Slides

# Light cP-odd Scalar

## Effective Lagrangian

$$\mathcal{L}_A = -\frac{1}{2}m_A^2 A^2 + \sum_{f=u,d,e} \xi_A^f \frac{im_f}{v} \bar{f} \gamma_5 f A + \xi_{AA}^W \frac{g^2}{4} A A W^{\mu+} W_\mu^- + \xi_{AA}^Z \frac{g^2}{8 \cos^2 \theta_W} A A Z^\mu Z_\mu$$

$$+ \xi_A^g \frac{\alpha_s}{4\pi v} A G_{\mu\nu}^a \tilde{G}^{a\mu\nu} + \xi_A^\gamma \frac{\alpha_{ew}}{4\pi v} A F_{\mu\nu} \tilde{F}^{\mu\nu}$$

**loop generated**

**coupling modifiers**

## Mixing

$$A \approx O_{A\pi^0}\pi^0 + O_{A\eta}\eta + O_{A\eta'}\eta' + O_{AAA}A_{CP-odd}$$

typically small except in the resonant region  $m_A \sim m_i$

## Production

- Production via meson mixing  $\sigma_A \approx |O_{A\pi^0}|^2 \sigma_{\pi^0} + |O_{A\eta}|^2 \sigma_\eta + |O_{A\eta'}|^2 \sigma_{\eta'}$
- B meson and Kaon decay  $K \rightarrow \pi A \quad B \rightarrow X_s A \quad \xi_A^{ij}$
- Bottomonium decay  $\Upsilon \rightarrow \gamma A \quad J/\psi \rightarrow \gamma A \quad \xi_A^f$
- Double pseudoscalar production  $B \rightarrow X_s A A \quad K \rightarrow \pi A A \quad \xi_{AA}^{ij}$

# A Decay

**Decay into a pair of photons, leptons, pair of quarks (gluons)/multiple hadrons**

- **Decay into diphoton**

$$\Gamma(A \rightarrow \gamma\gamma) = \frac{\alpha_{ew}^2 m_A^3}{64\pi^3} \left| O_{AA} C_A^\gamma + O_{A\pi^0} C_{\pi^0}^\gamma + O_{A\eta} C_\eta^\gamma + O_{A\eta'} C_{\eta'}^\gamma \right|^2$$

- **Decay into dilepton**

$$\Gamma(A \rightarrow \ell^+ \ell^-) = \frac{G_F m_A m_\ell^2 \beta_\ell}{4\sqrt{2}\pi} |\xi_A^\ell|^2$$

$m_A > 3 \text{ GeV}$ : perturbative spectator model

- **Decay into diquark**

$$\Gamma_{\bar{\ell}\ell} : \Gamma_{\bar{s}s} : \Gamma_{\bar{c}c} : \Gamma_{\bar{b}b} = (\xi_A^\ell)^2 m_\ell^2 \beta_\ell : 3(\xi_A^s)^2 m_s^2 \beta_s : 3(\xi_A^c)^2 m_c^2 \beta_c : 3(\xi_A^b)^2 m_b^2 \beta_b$$

- **Decay into digluon**

$$\Gamma(A \rightarrow gg) = \frac{G_F \alpha_s^2 m_A^3}{4\sqrt{2}\pi^3} |\xi_A^g|^2$$

$1.3 \text{ GeV} < m_A < 3 \text{ GeV}$ : spectator model with partonic dynamic and hadronic kinematics

- **Hadronic decay**

$$\mathcal{L}_{\text{spect.}} = \frac{i}{\sqrt{2}} A_1 (\mathcal{Y}_u^A \bar{u} \gamma_5 u + \mathcal{Y}_d^A \bar{d} \gamma_5 d + \mathcal{Y}_s^A \bar{s} \gamma_5 s)$$

$$\mathcal{Y}_u^A \approx \frac{\sqrt{2}B}{\sqrt{3}v f_\pi^2} m_u \xi_A^u$$

# *A* Decay continued

$m_A < 1.3 \text{ GeV}$ : chiral perturbation theory

- Hadronic decay into tri-meson

$$\Gamma(A \rightarrow \Pi_i \Pi_j \Pi_k) = \frac{1}{256 S_{ijk} \pi^3 m_A} \int_{(m_j+m_k)^2}^{(m_A-m_i)^2} ds |\mathcal{M}_A^{ijk}|^2$$

$$\sqrt{1 - \frac{2(m_j^2 + m_k^2)}{s} + \frac{(m_j^2 - m_k^2)^2}{s^2}} \times \sqrt{\left(1 + \frac{s - m_i^2}{m_A^2}\right)^2 - \frac{4s}{m_A^2}}$$

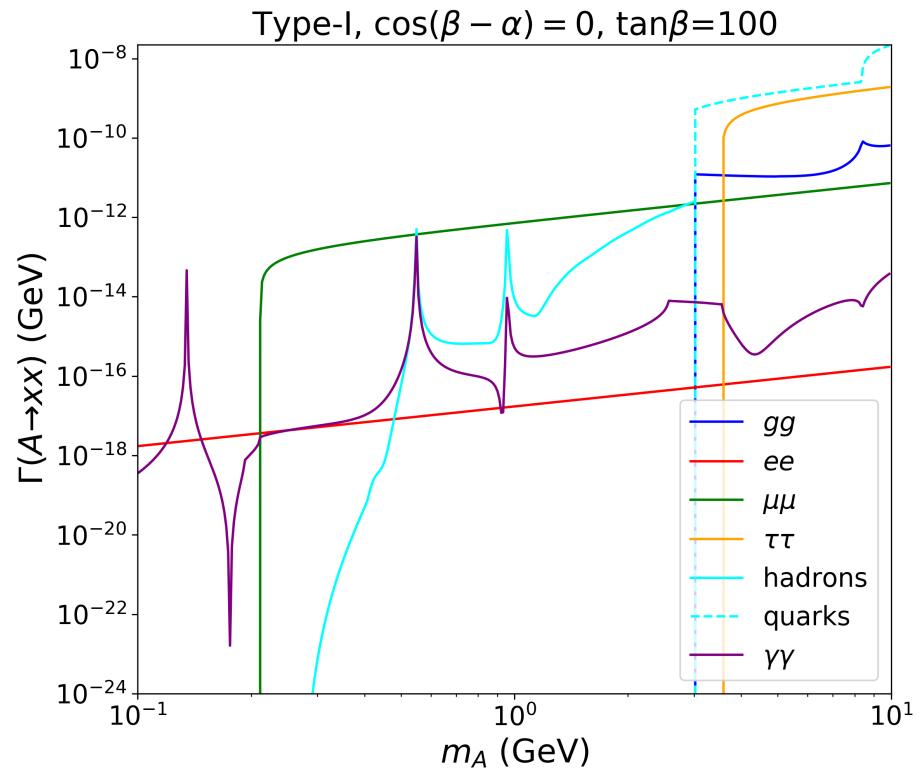
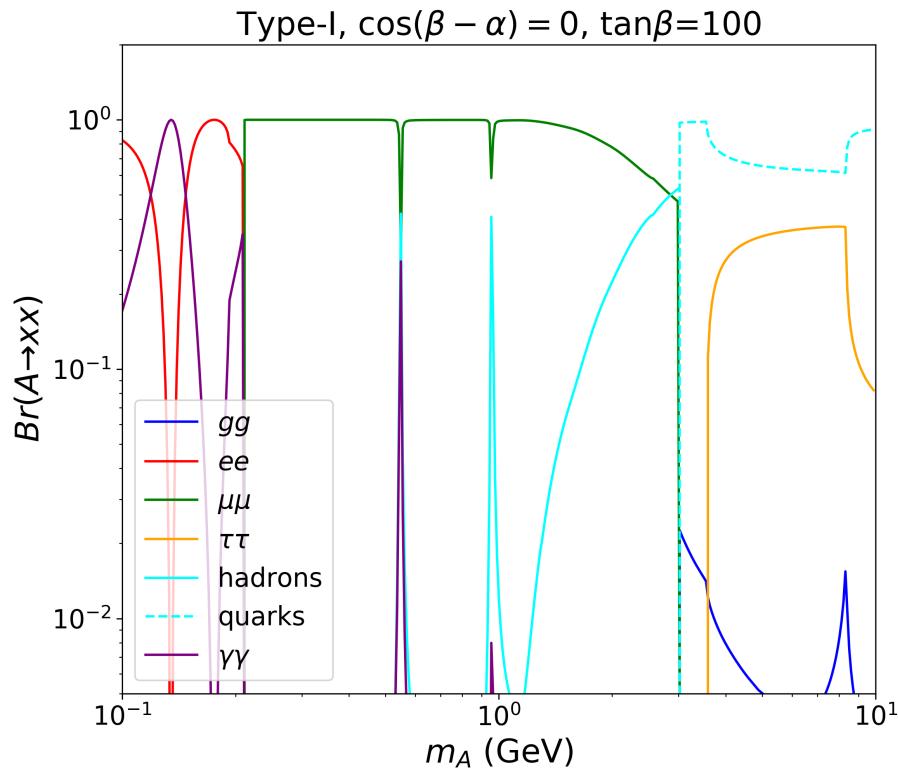
$$\mathcal{M}_A^{ijk} \propto O_{AA} \mathcal{A}_A^{ijk} + \sum_l O_{Al} \mathcal{A}^{ijkl}$$

- Radiative hadronic decay

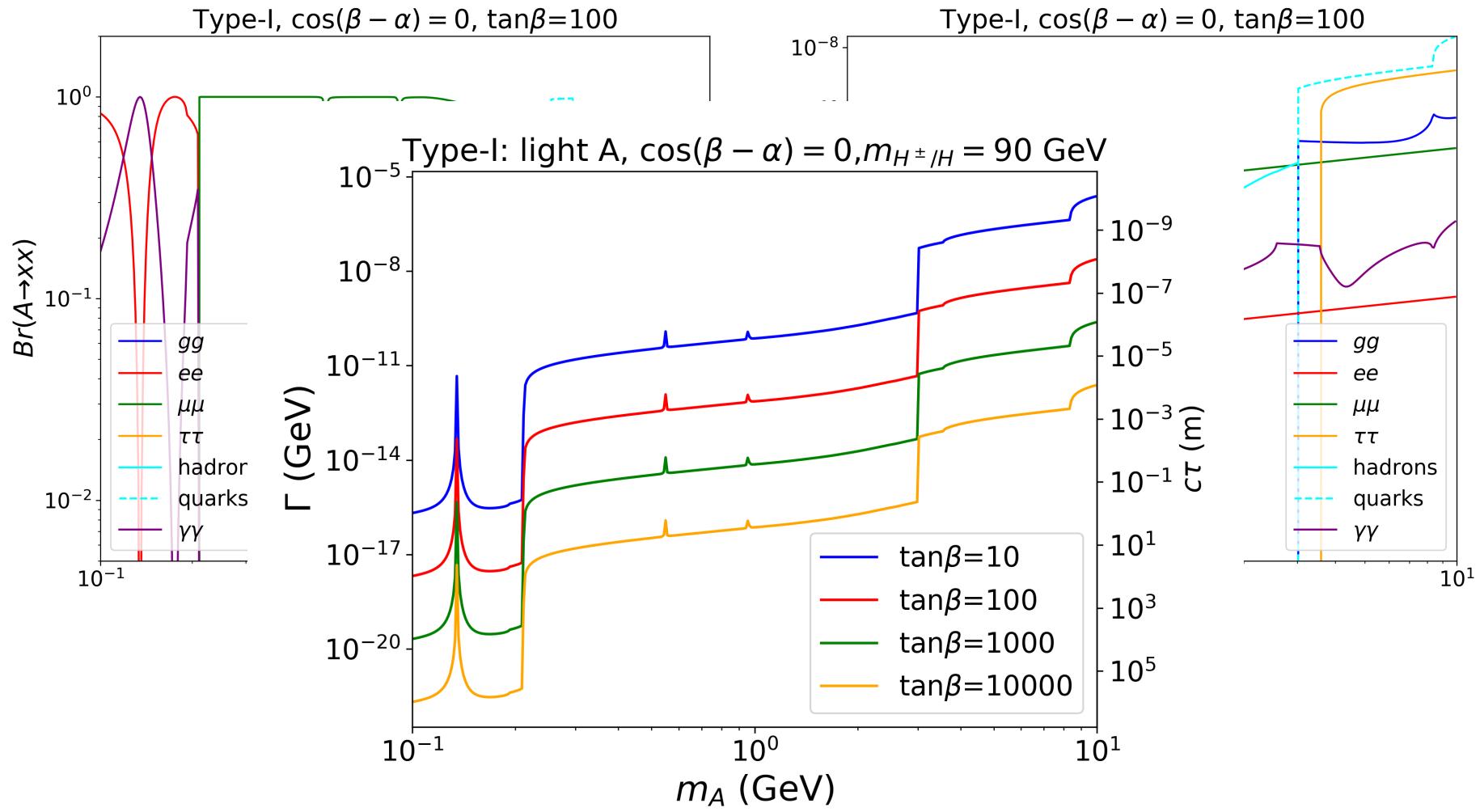
$$A \rightarrow \pi^+ \pi^- \gamma$$

$$\Gamma(A \rightarrow \pi^+ \pi^- \gamma) = \int_{4m_\pi^2}^{m_A^2} ds \Gamma_0(s) |O_{A\eta} B_\eta(s) + O_{A\eta'} B_{\eta'}(s)|^2$$

# Light cP-odd Scalar

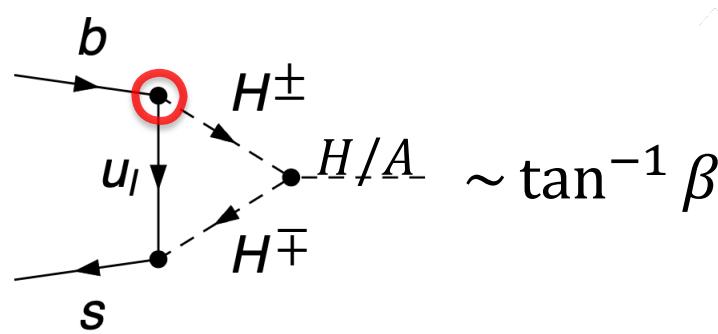


# Light cP-odd Scalar

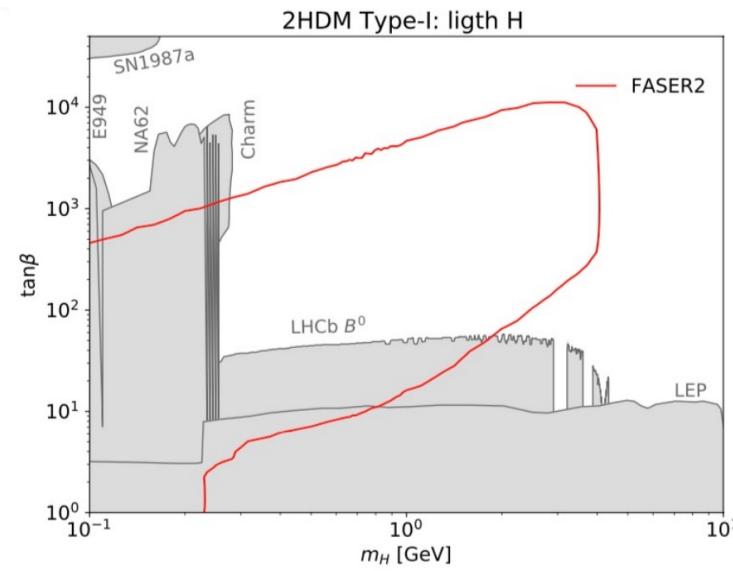
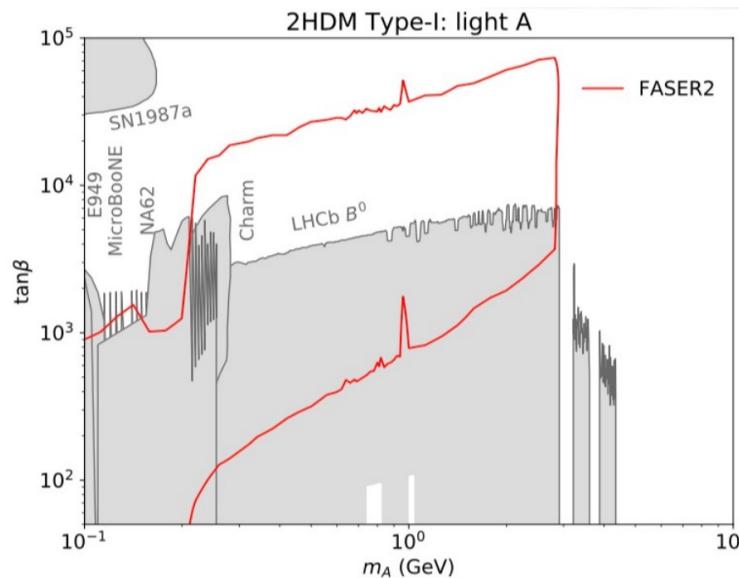


# without Double Scalar Production

In Type-I 2HDM

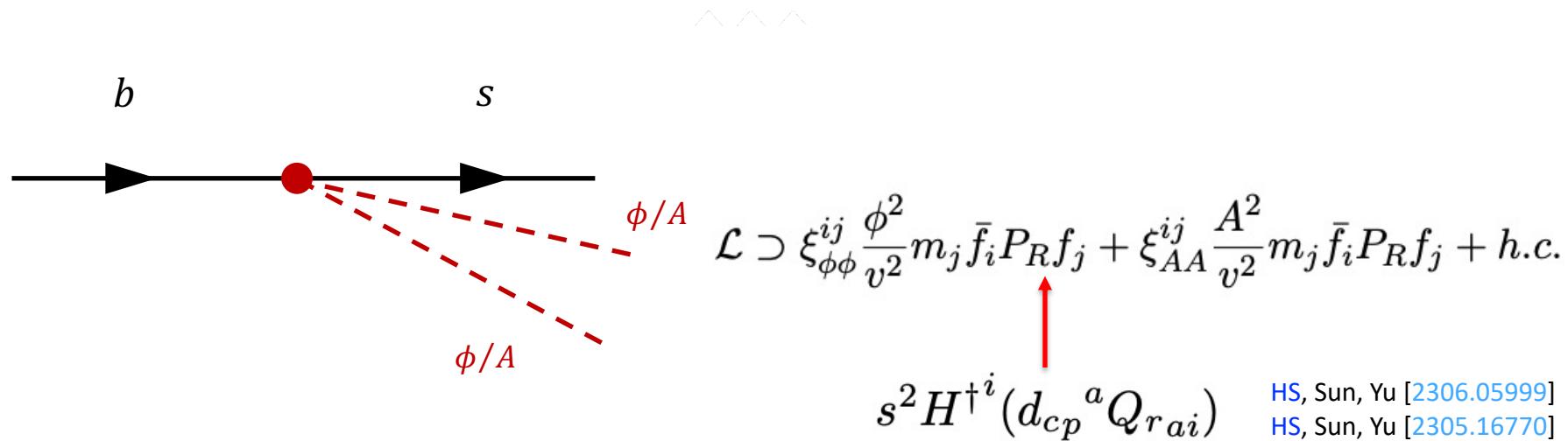


Similar to minimal model  
(Dark Higgs)



# Effective couplings

In Type-I 2HDM

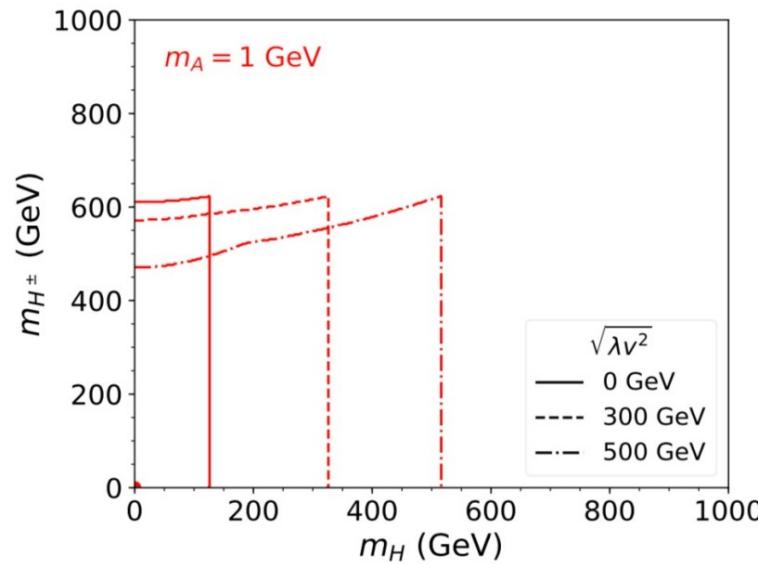
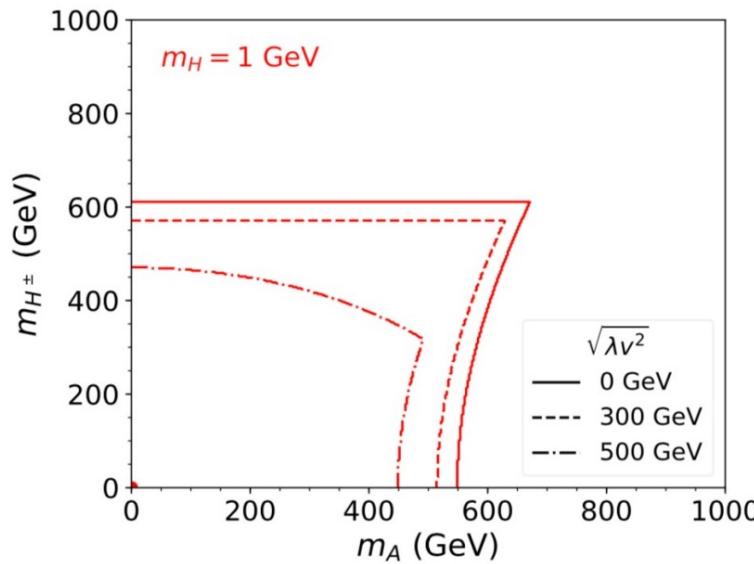


$$\begin{aligned} \xi_{\phi\phi}^{ij} \simeq \xi_{AA}^{ij} \simeq \frac{g^2}{64\pi^2} \sum_k V_{ki}^* & [f_0(x_k, x_{H^\pm}) + f_1(x_k, x_{H^\pm}) \log x_k \\ & + f_2(x_k, x_{H^\pm}) \log x_{H^\pm}] V_{kj} + \mathcal{O}(\cos(\beta - \alpha), 1/\tan\beta) \end{aligned}$$

# constraints

## Theoretical constraints

$$\lambda v^2 \equiv m_H^2 - m_{12}^2 / s_\beta c_\beta = 0$$



$$m_H \sim 0 : \quad m_{A/H^\pm} \lesssim 600 \text{ GeV}$$

$$m_A \sim 0 : \quad m_{H^\pm} \lesssim 600 \text{ GeV}, \quad m_H \lesssim m_h$$

# constraints

## Invisible Higgs decays

$$\text{Br}(h \rightarrow \phi\phi) = \frac{\Gamma(h \rightarrow \phi\phi)}{\Gamma_h} \approx \frac{1}{\Gamma_h^{\text{SM}}} \frac{g_{h\phi\phi}^2}{8\pi m_h^2} \left(1 - \frac{4m_H^2}{m_h^2}\right)^{1/2} \simeq 4700 \cdot \left(\frac{g_{h\phi\phi}}{v}\right)^2 < 0.24$$

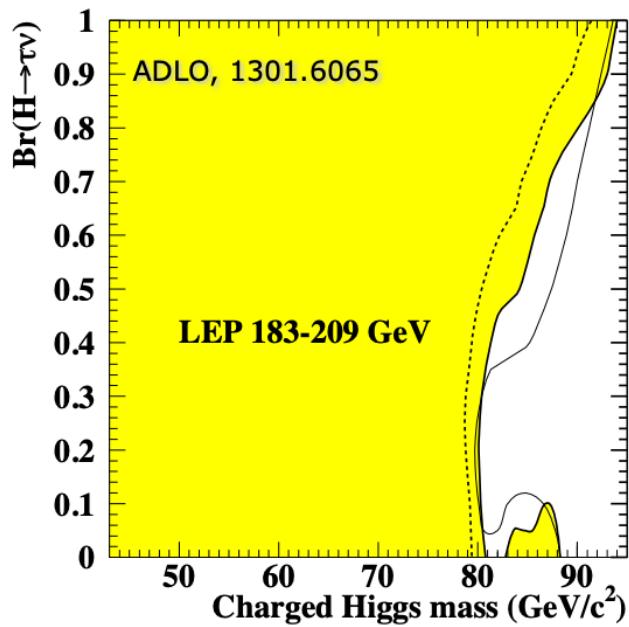
$$\text{Br}(h \rightarrow \phi\phi) = 0$$

$$\text{Light } H : \cos(\beta - \alpha) = \tan 2\beta \frac{2\lambda v^2 + m_h^2}{2(m_H^2 - 3\lambda v^2 - m_h^2)} \approx \frac{1}{\tan \beta},$$

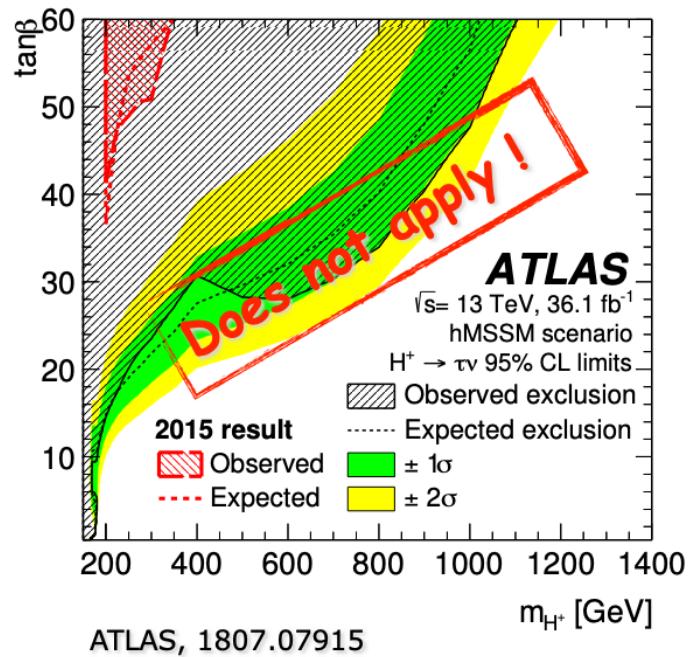
$$\text{Light } A : \cos(\beta - \alpha) = \tan 2\beta \frac{2\lambda v^2 + m_h^2 + 2m_A^2 - 2m_H^2}{2(m_H^2 - \lambda v^2 - m_h^2)} \approx \frac{1}{\tan \beta} \frac{2m_H^2 - m_h^2}{m_H^2 - m_h^2},$$

# constraints

**LEP H $\pm$  search:**  
 $m_{H^\pm} > 85 \text{ GeV}$  viable

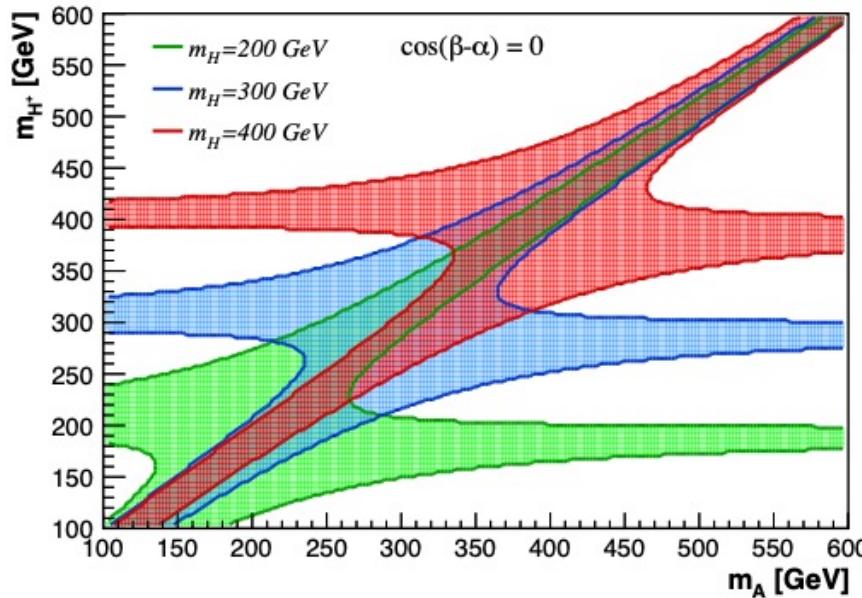


**LHC H $\pm$  search**



# constraints

- EW precision constraints:  
 $m_{H^\pm} \sim m_H \text{ or } m_A$



$m_H \sim 0 : m_A \sim m_{H^\pm} \lesssim 600 \text{ GeV}$

$m_A \sim 0 : m_{H^\pm} \sim m_H \lesssim m_h,$

$$\lambda v^2 \approx 0 \quad |\cos(\beta - \alpha)| \sim 0.$$