



Zaher Salman :: Paul Scherrer Institute

Muon Spin Spectroscopy with Vertex Reconstruction

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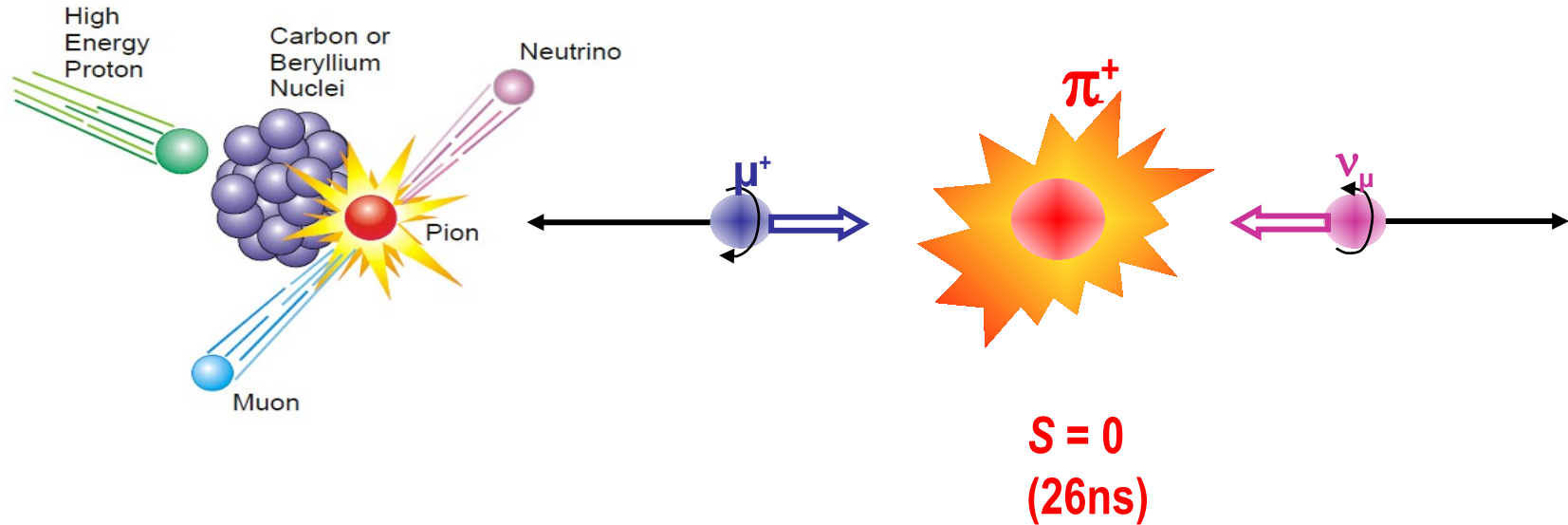
Outline

- Muon Spin Rotation / Relaxation (μ SR) technique
 - Current limitations
- Overcoming current μ SR limitations
 - Rate limitation
 - Sample size limitation
- Si-Pixel detectors for μ SR to break limitations
- Recent results
 - Lateral resolution
 - First μ SR with Si-Pixel detectors

What do we use μ SR for?

- Muons are implanted, not scattered, and they interact with the local magnetic fields that they experience.
- Muons are local magnetic probe. It allows determination of magnetic / superconducting / other volume fraction.
- μ SR can be performed at any temperature and/or magnetic field in any sample (solid, liquid or gas).
- Muons are highly sensitive, can detect magnetic fields from moments as small as 10^{-3} – $10^{-4} \mu_B$, and magnetic fluctuations in the range 10^5 – 10^9 Hz.
- The muon can also act as a hydrogen-like isotope, to study energy materials and semiconducting devices.

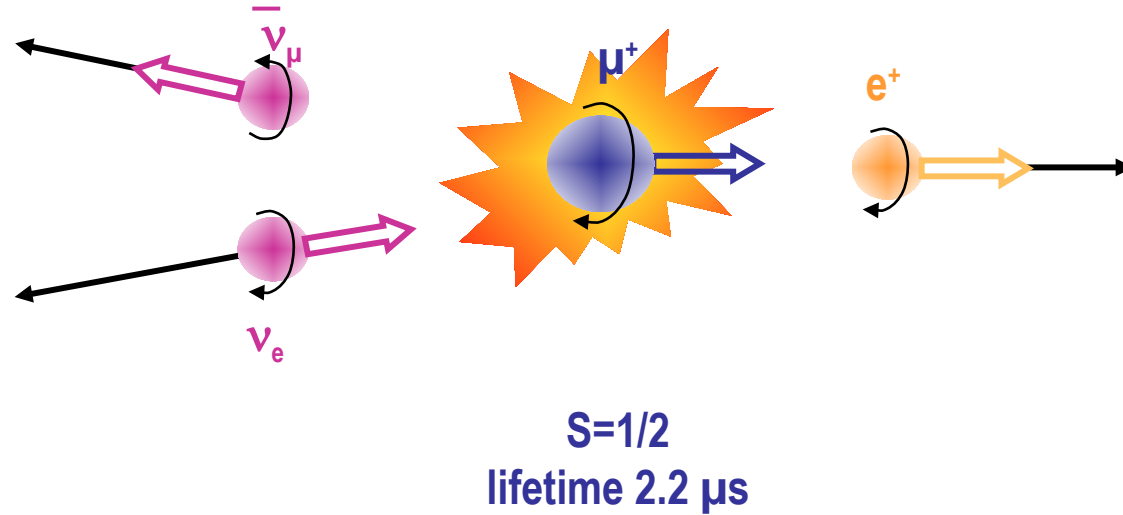
Production of Muon



Two-body decay ► muon has always the energy 4.1 MeV in the reference frame of the pion (assuming $m_\nu = 0$)

Spin pion = 0 ► muon has a **spin 1/2 and is 100% polarized** (since only left-handed neutrinos exist)

β -Decay of the Muon



Three-body decay



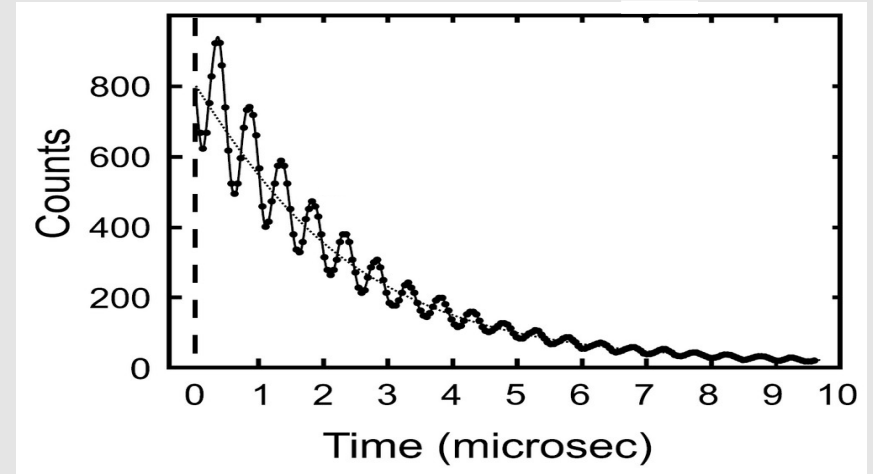
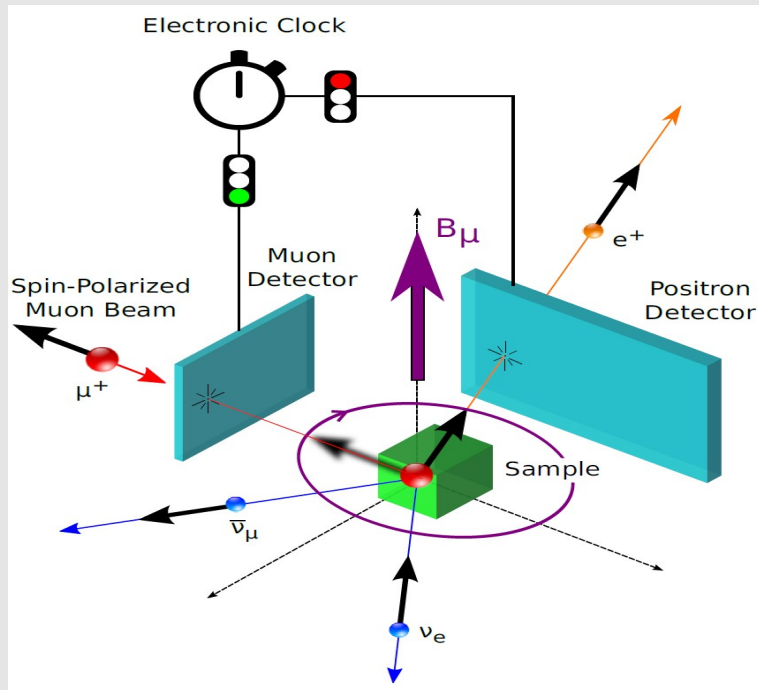
Distribution of positrons energies

Weak-decay of muon



Parity-violation leading to **positrons emitted preferentially along spin direction.**

The μ SR Technique

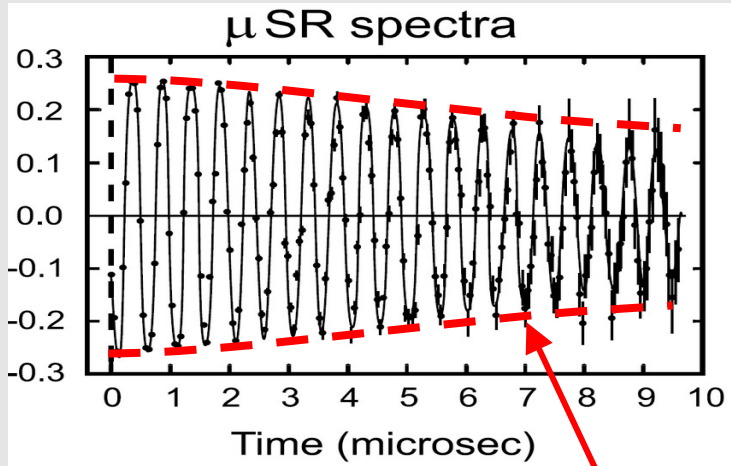


$$N(t) = Bkg + N_0 \exp(-t/\tau_\mu) [1 + a \hat{n} \cdot P(t)]$$

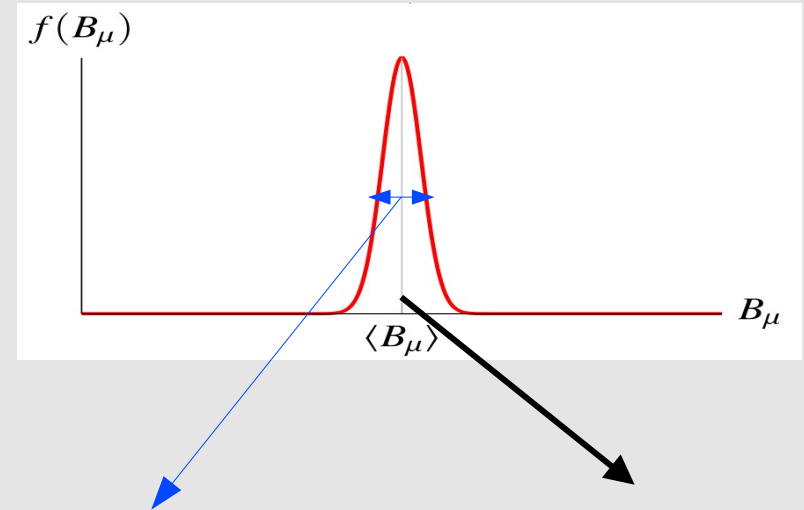
\hat{n} - direction of detector

μ SR Spectra

$aP_x(t) \sim$ Muon Spin Polarization



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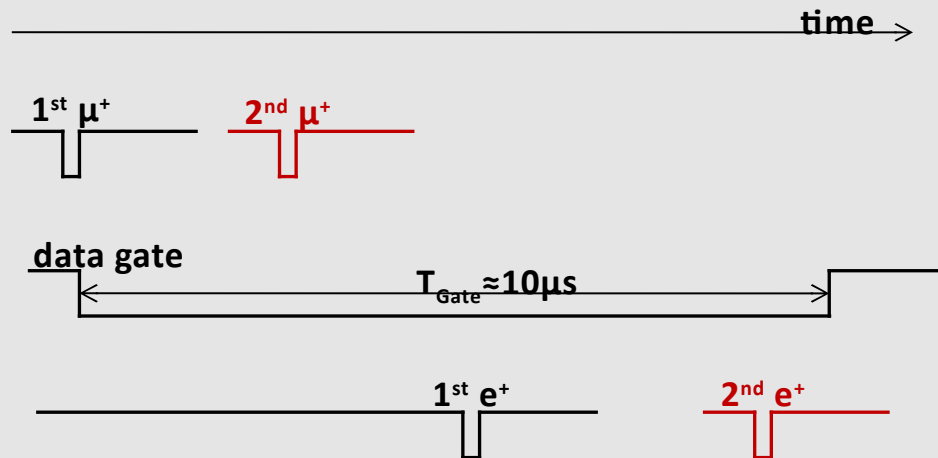
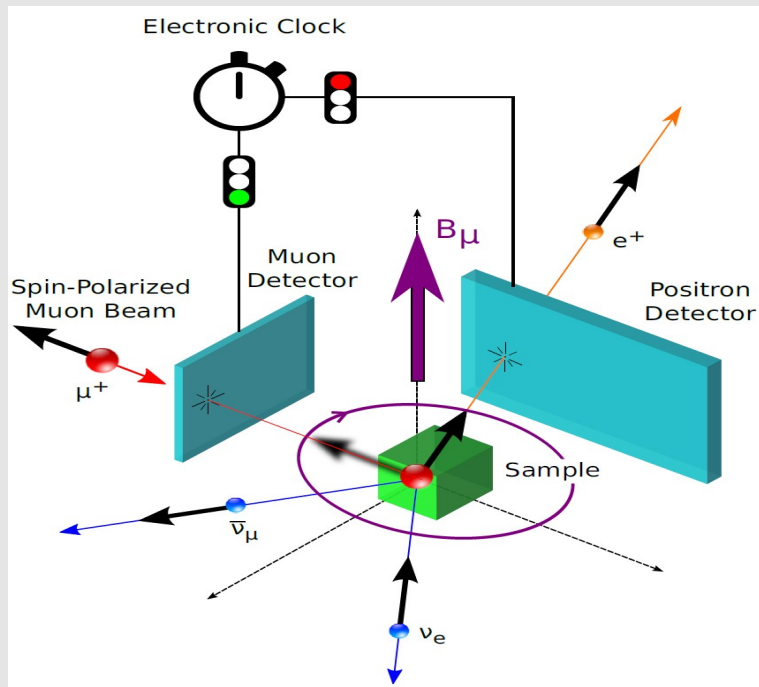


Damping or dynamics

Frequency / γ_μ

Current Rate of Muon at a Typical μ SR Spectrometer at PSI

Rate Limitation on μ SR at PSI

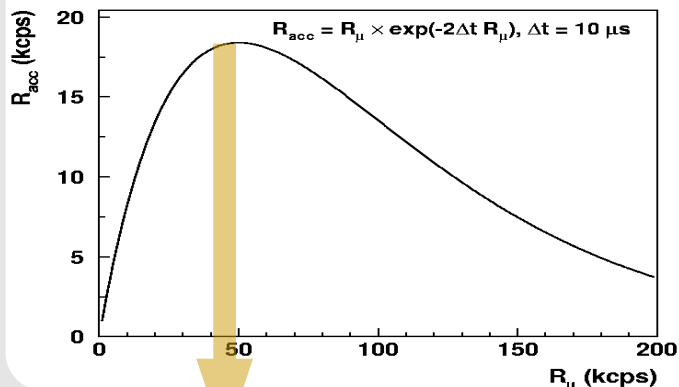


- 1st μ^+ : there was **no** other μ^+ for at least T_{Gate} in the past
- Single muon detection: only **one** μ^+ and **one** e^+ in observation window ($T_{\text{Gate}} \approx 10 \mu\text{s}$)
- Second μ^+ / e^+ rejection electronically and by rate limitation

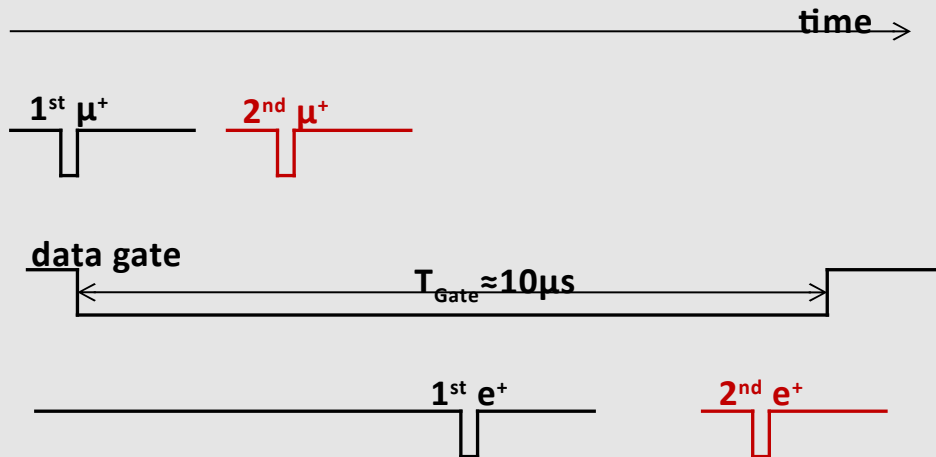
$$\text{Good Event} = (\text{data gate}) \wedge (1^{\text{st}} e^+) \wedge (\text{no } 2^{\text{nd}} \mu^+) \wedge (\text{no } 2^{\text{nd}} e^+)$$

Rate Limitation on μ SR at PSI

Accepted rate (R_{acc})
versus
incoming rate (R_{μ})



Current rate limit for $T_{Gate} = 10 \mu s$ is $\sim 40k \mu^+/s$



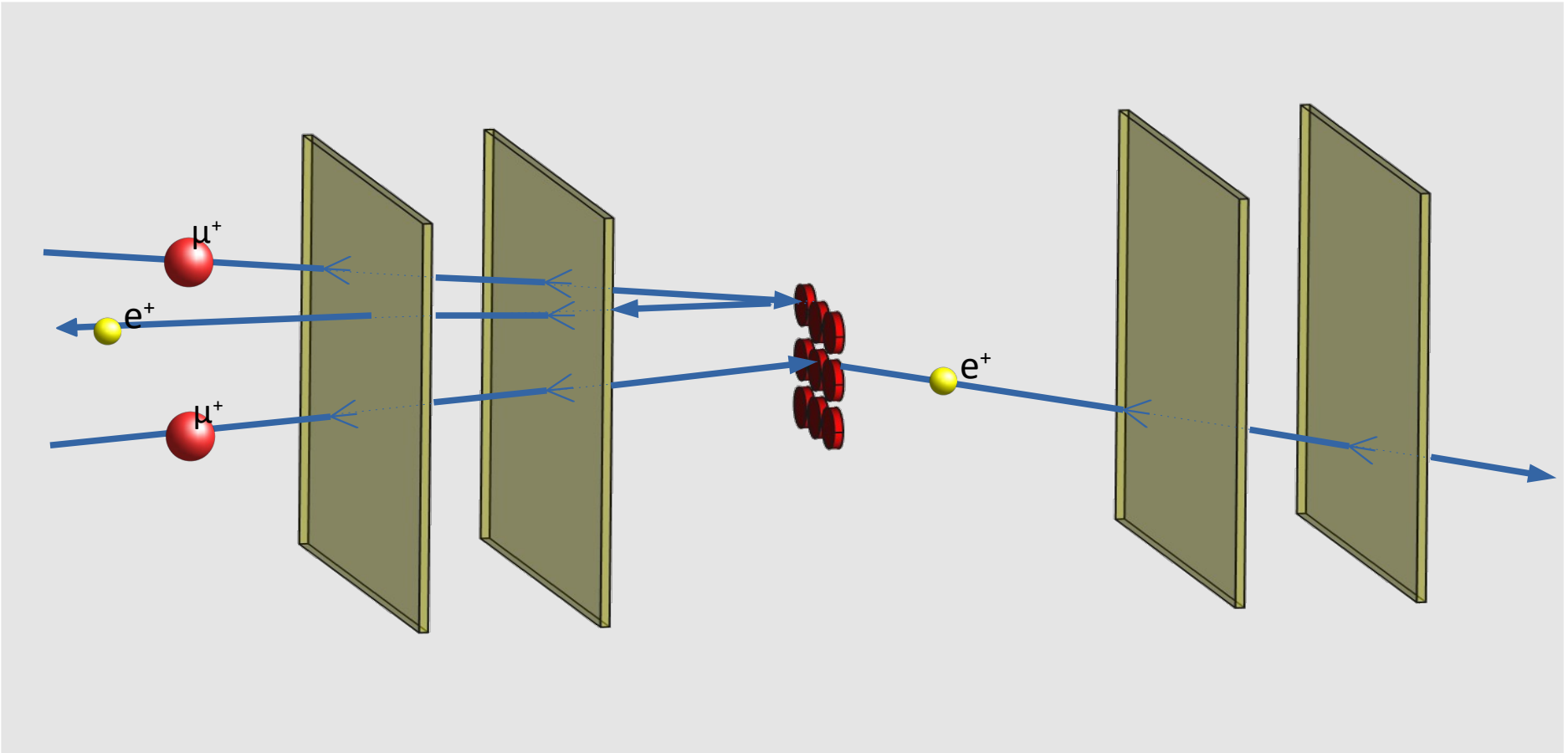
- 1st μ^+ : there was **no** other μ^+ for at least T_{Gate} in the past
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Good Event = (data gate) \wedge (1st e^+) \wedge (no 2nd μ^+) \wedge (no 2nd e^+)

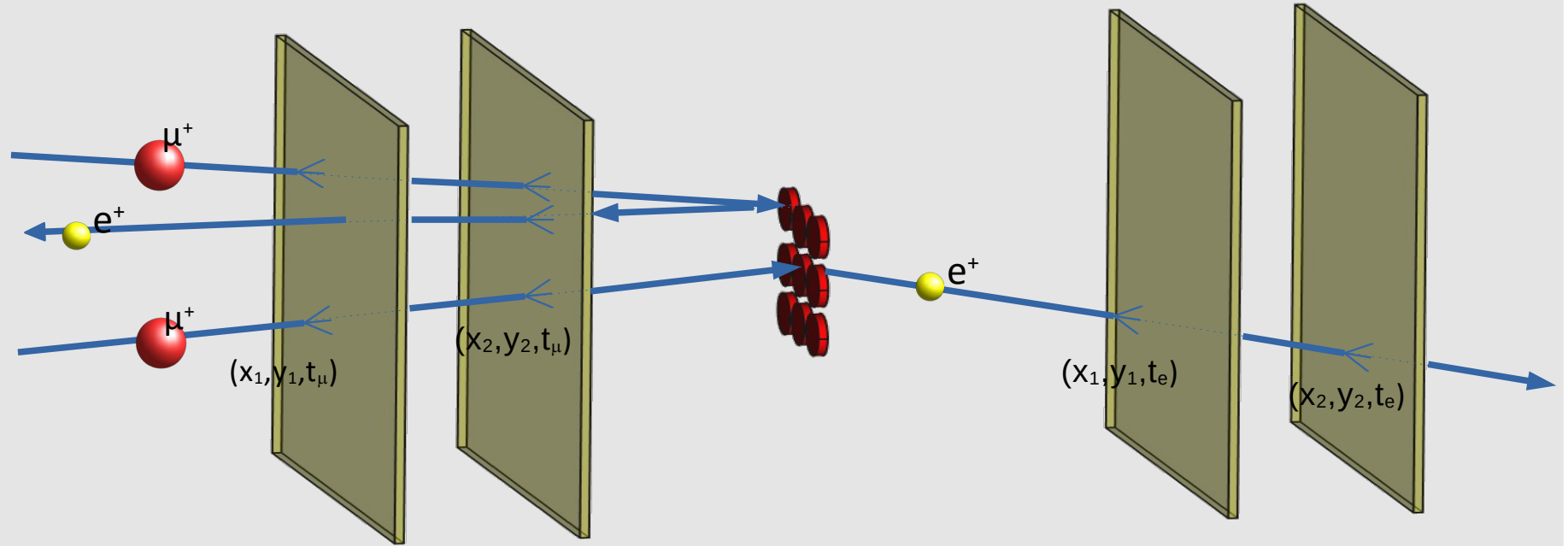
Only 40k Muons/s!

Can we use more?

Vertex Reconstruction Scheme



Vertex Reconstruction Scheme

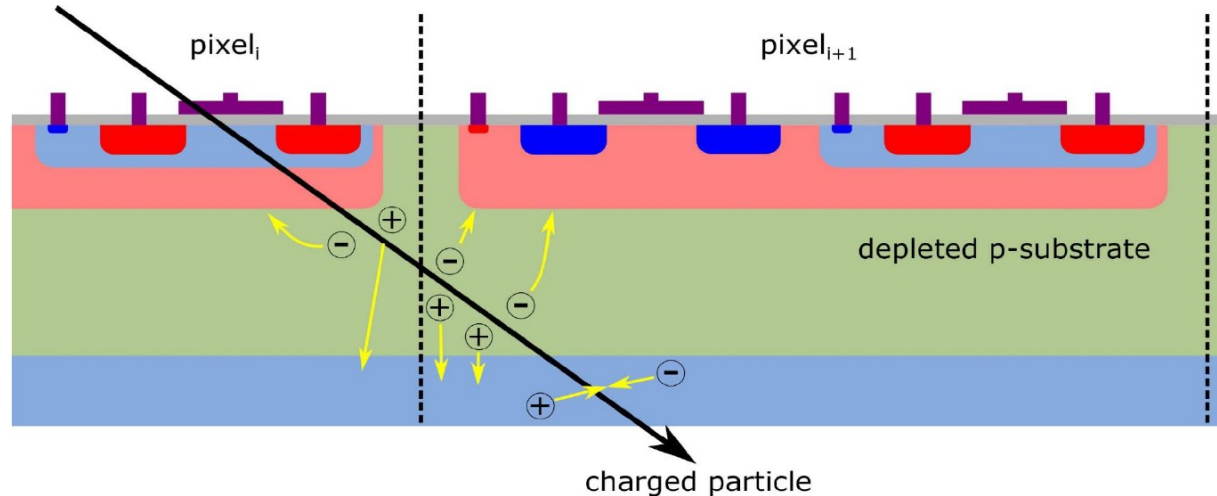
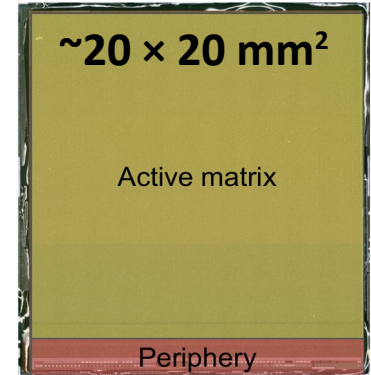


We need detectors that give the position and time of a hit with minimal scattering.

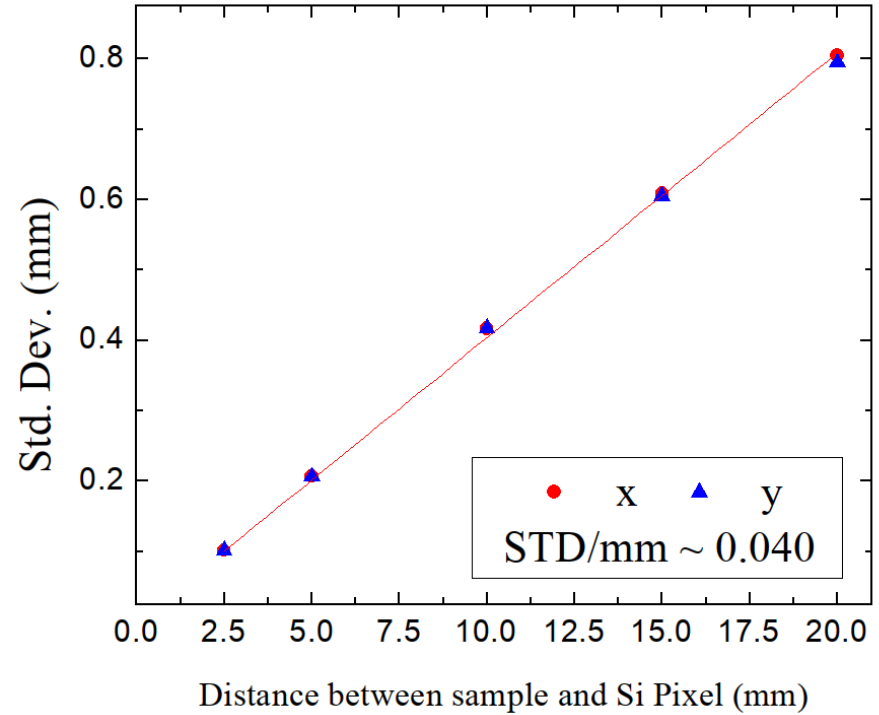
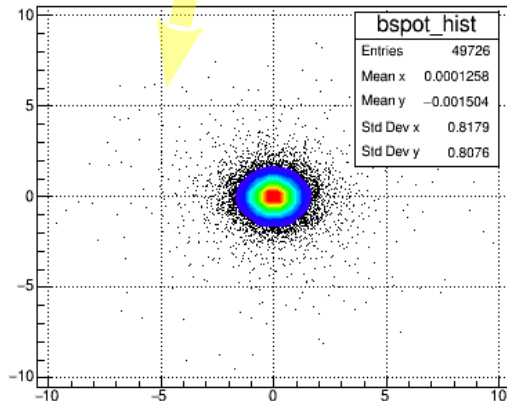
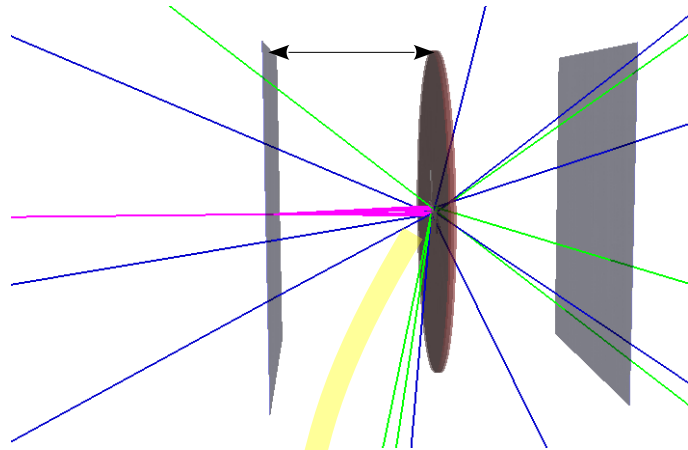
High-voltage monolithic active pixel sensor (HV-MAPS)

Si-Pixel detectors – MuPix11

- Developed by the Mu3e collaboration.
- 180 nm HV-CMOS process
- Fully integrated digital readout
- **Can be as thin as 50 micrometers with $80 \times 80 \mu\text{m}^2$ pixel size**
- Continuous readout without trigger
- Less than 20ns time resolution

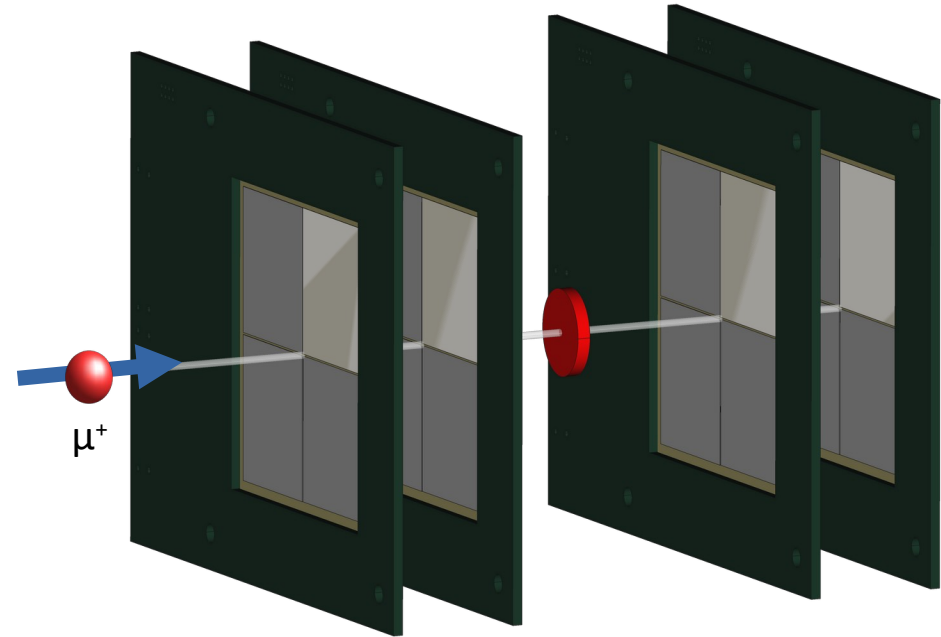
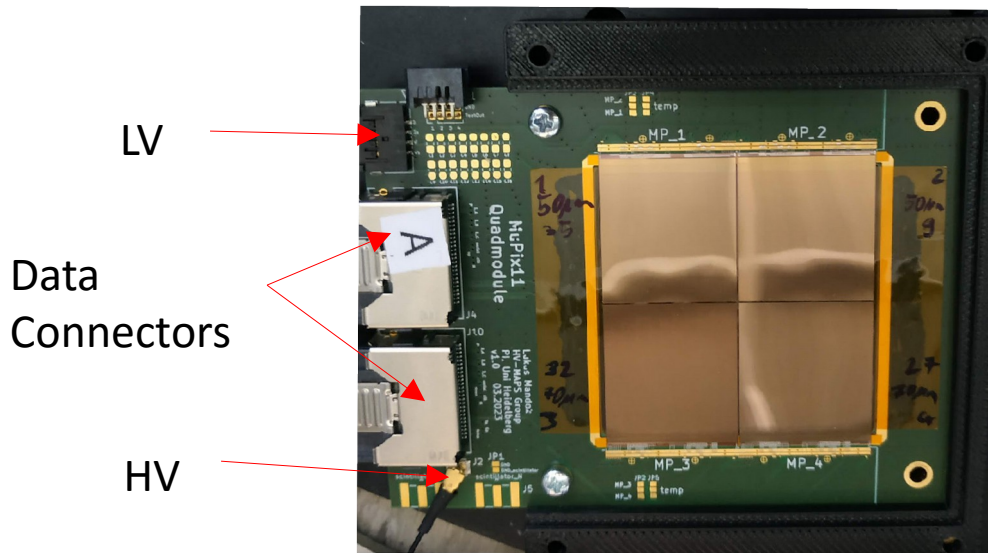


Lateral Resolution Limited by Scattering due to Inner Detectors

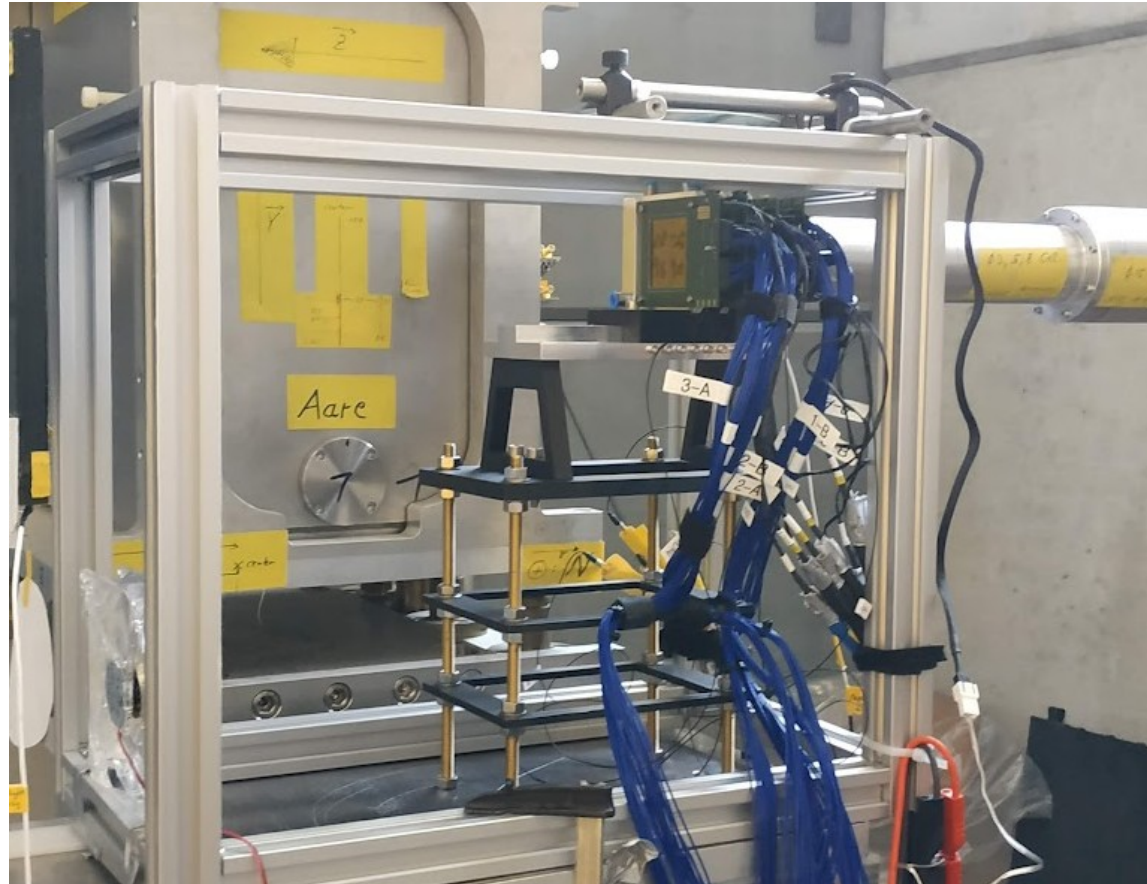


First μ SR Experiment with Si-Pixel Detectors

- We constructed a four layer setup.
- Each layer is made of four MuPix11 chips (thickness 50-100 μ m) glued onto a 25 μ m Kapton foil.

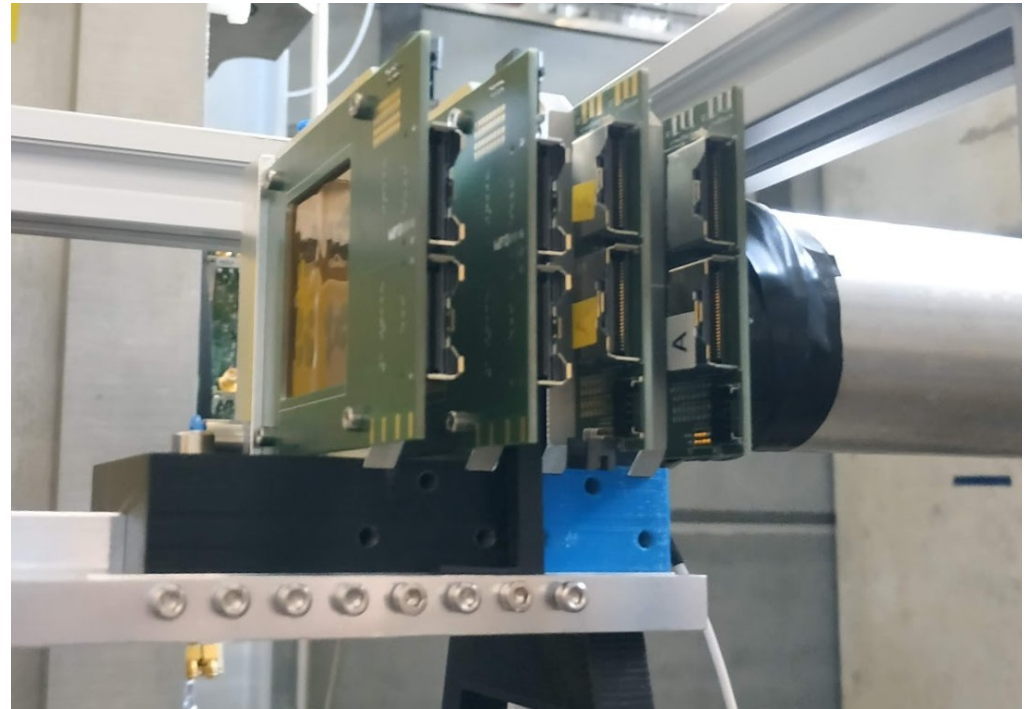
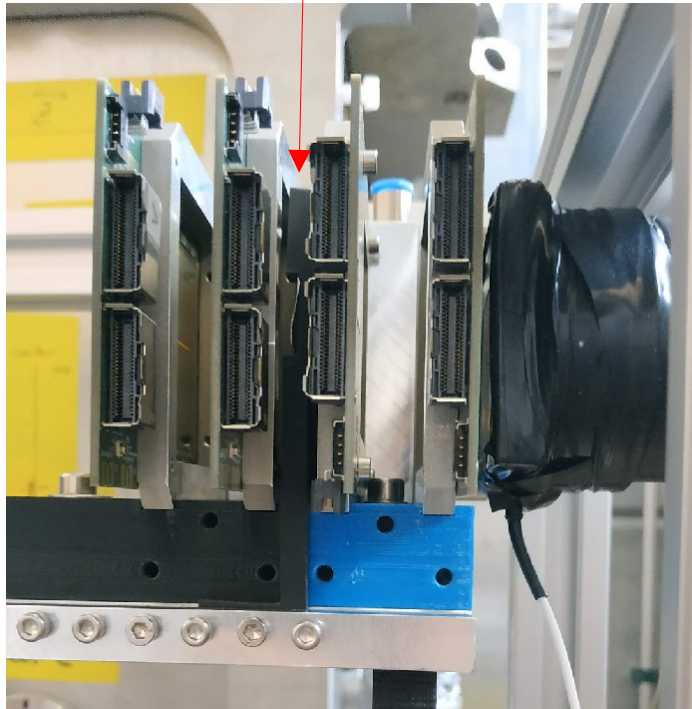


First μ SR Experiment with Si-Pixel Detectors



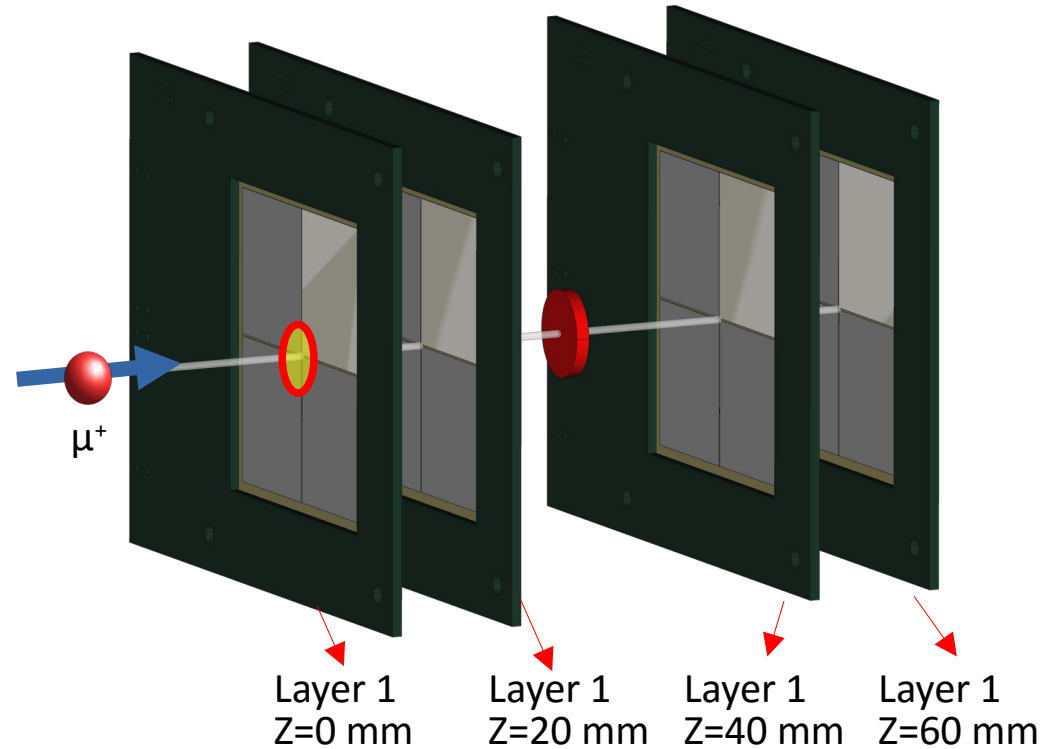
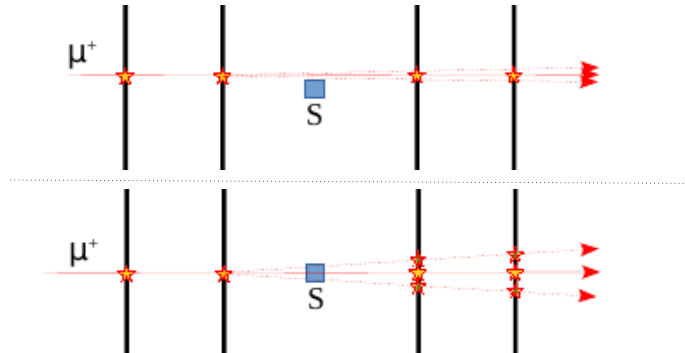
First μ SR Experiment with Si-Pixel Detectors

Sample goes here



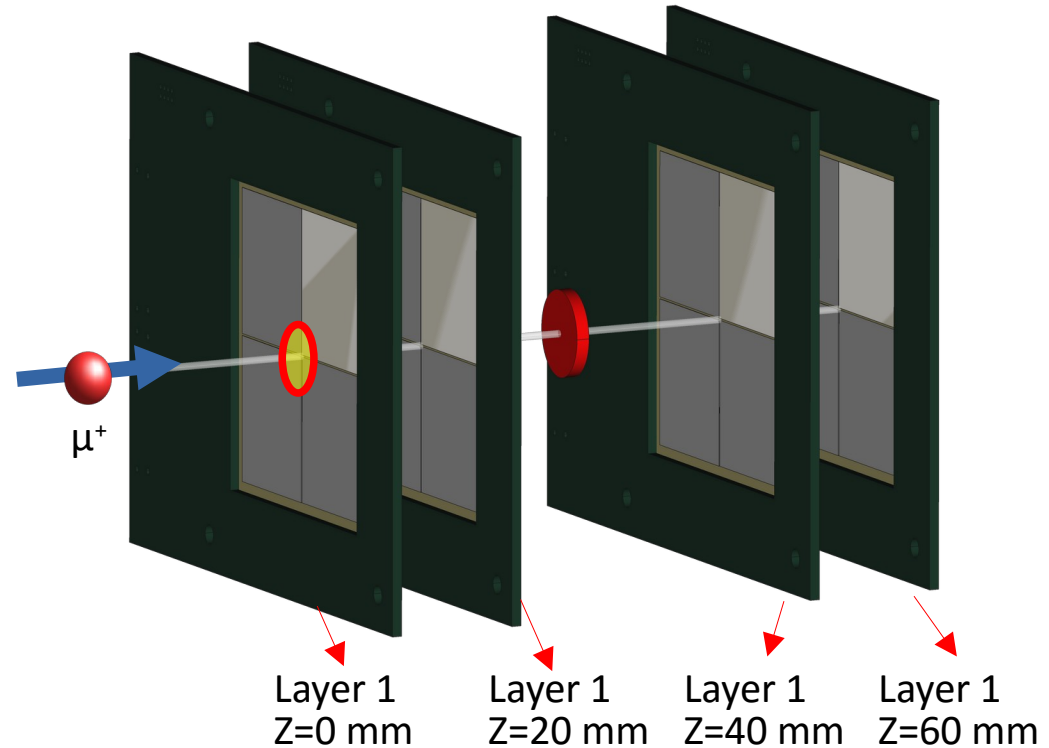
How does the data look like?

- The data collected from the layers comes out as a series of events, position and time stamp:
 (x_i, y_i, t_i) and of course the layer (z_i)
- Allowed tracks **must be** coincidence events in layers **(1&2)** or **(3&4)**.



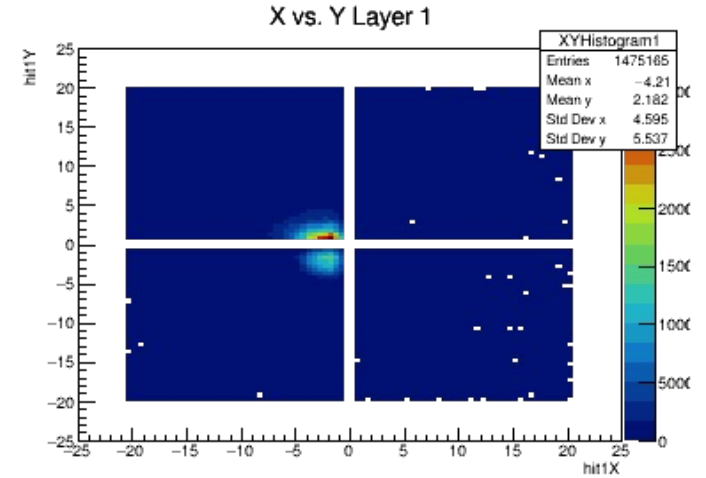
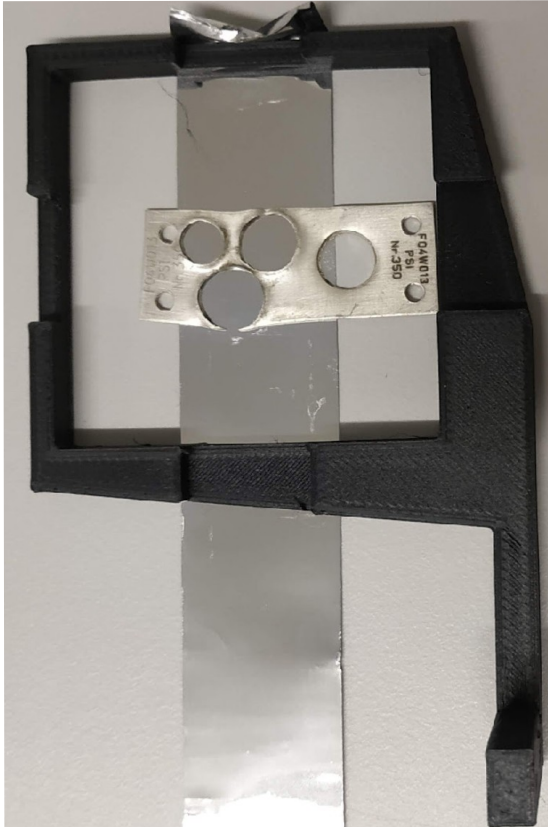
Proposed Algorithm to Extract μ SR Spectra

- Any track starting in Layer 1 within a radius of 2 mm from the beam center is a muon.
- Extrapolate this track to the sample position (x_s, y_s) .
- Open a (software) data gate of $13 \mu\text{s}$
- Within this time, look for tracks (extrapolated to sample - x_s, y_s) starting within 1mm from (x_s, y_s) .
- There should be only one such track, if so, it is the emitted positron. If not ignore and move on...



**Does this actually
work?**

First Example – Can we resolve geometric details?

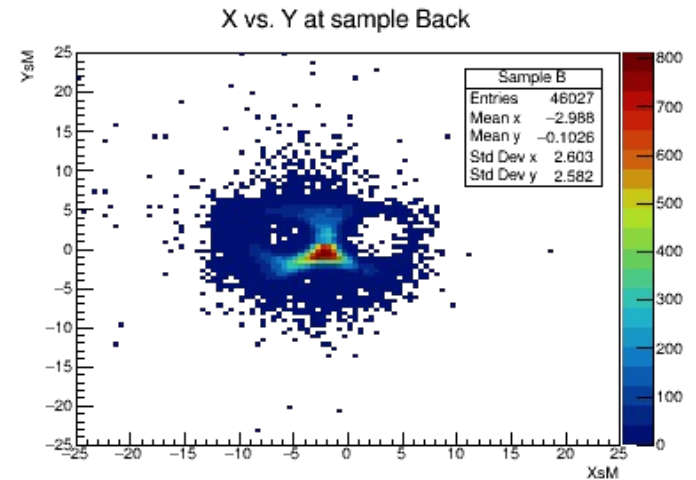
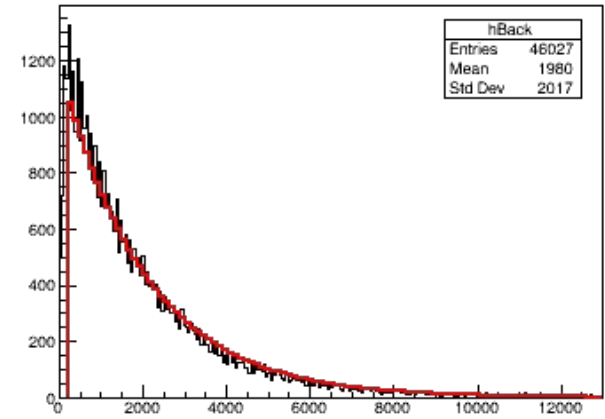


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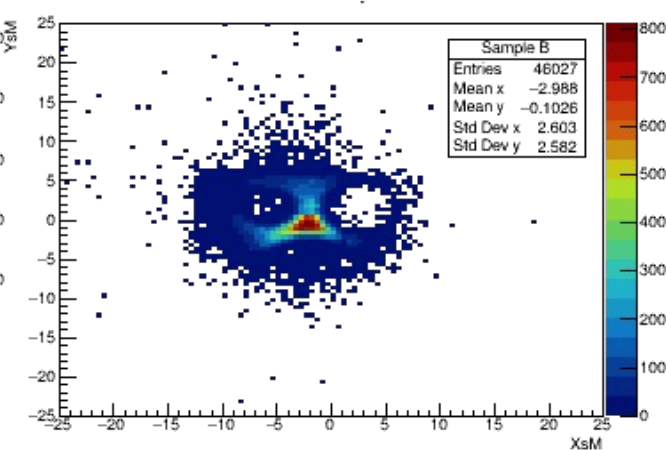
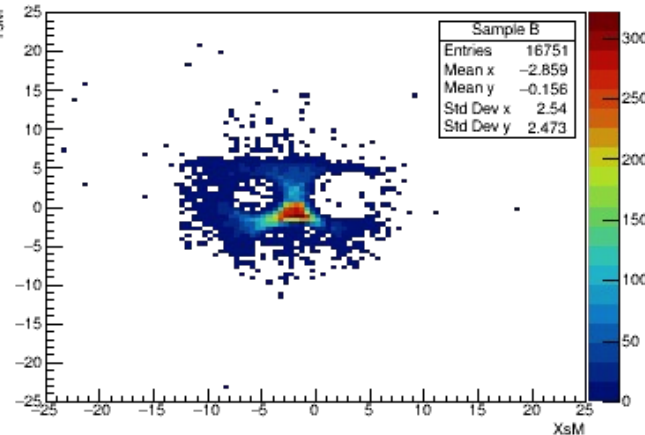
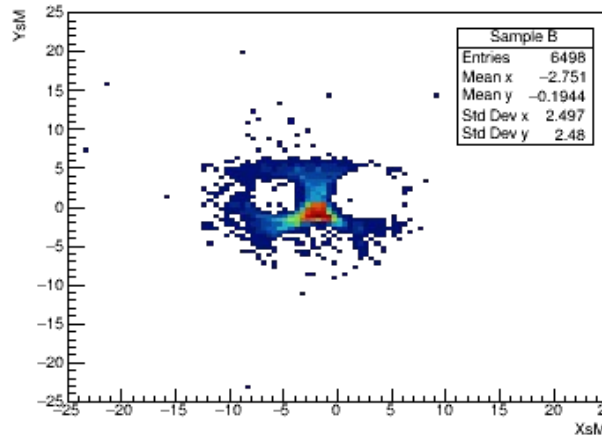
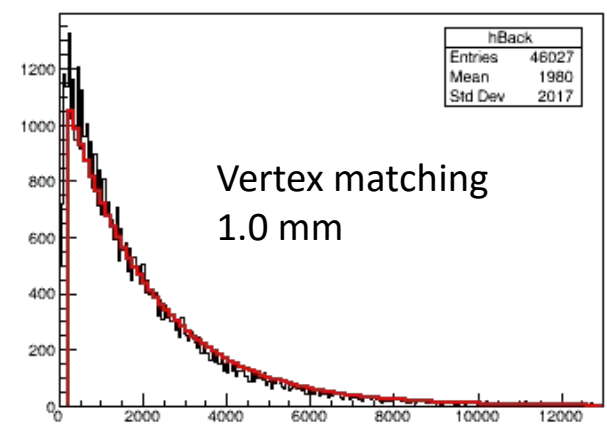
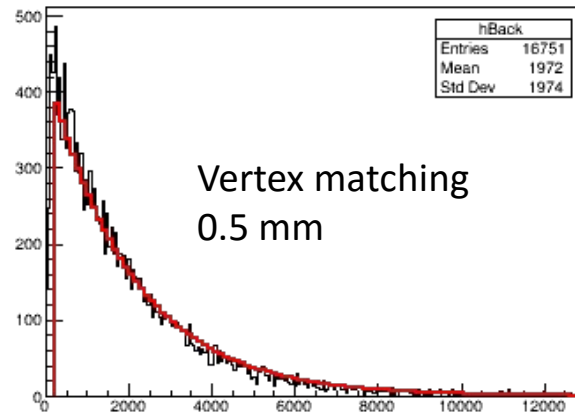
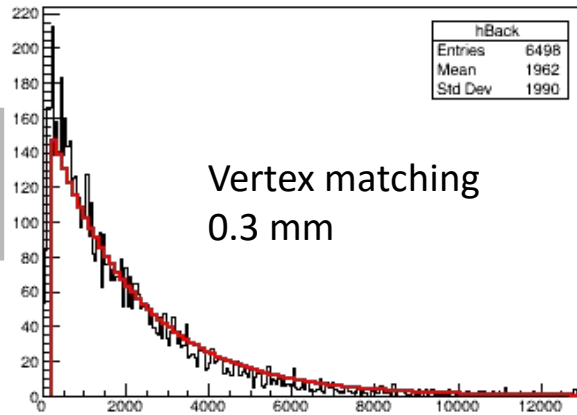


Time ($t_{\text{positron}} - t_{\text{muon}}$) histogram

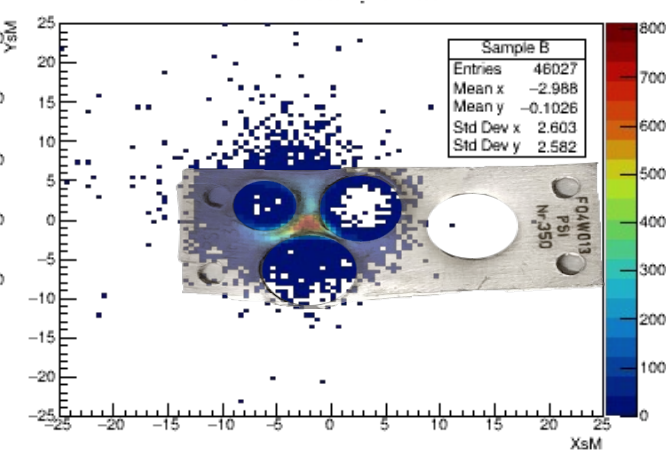
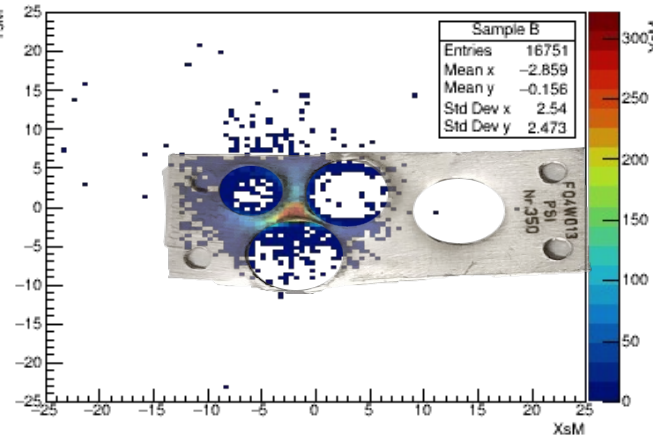
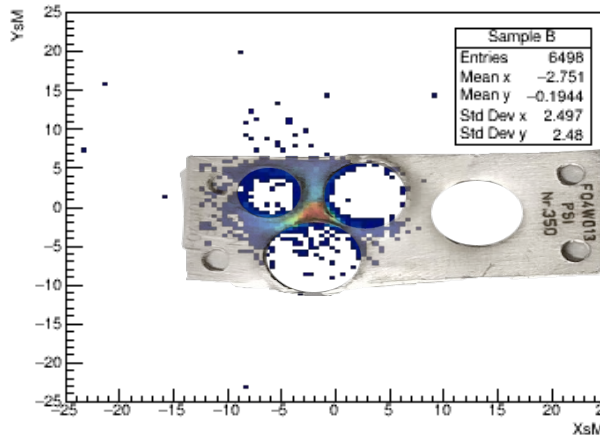
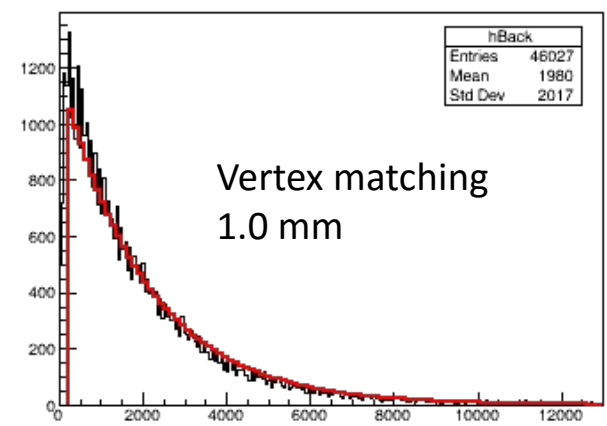
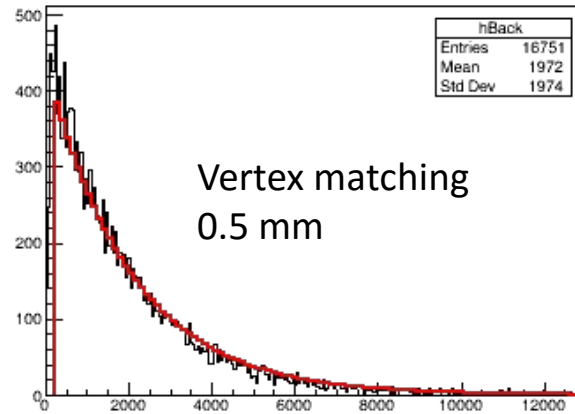
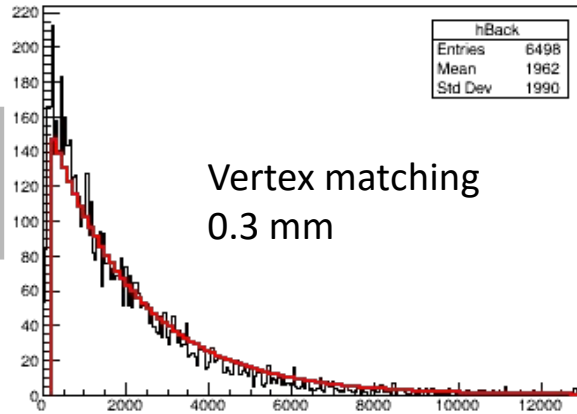
Vertex of valid events recorded in the upstream set of detectors



First Example – Can we resolve sample details?

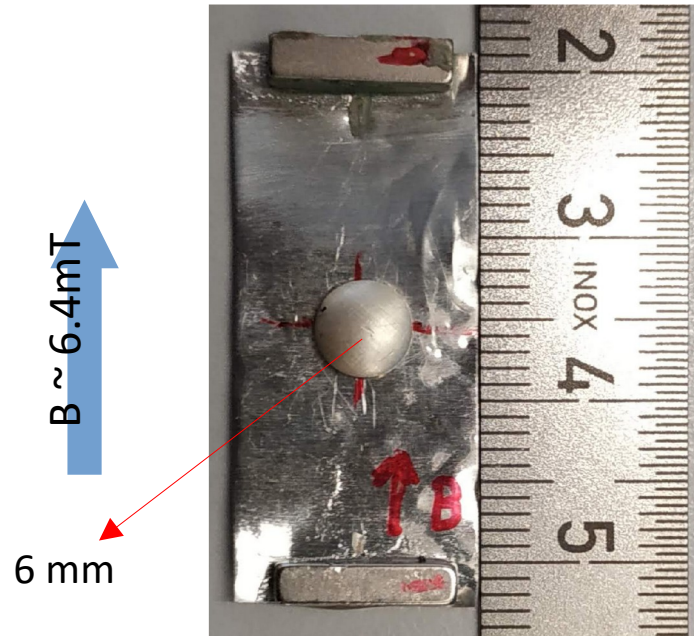


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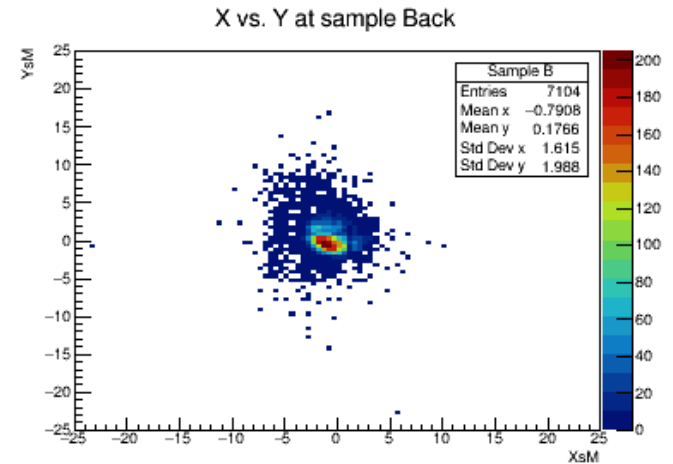
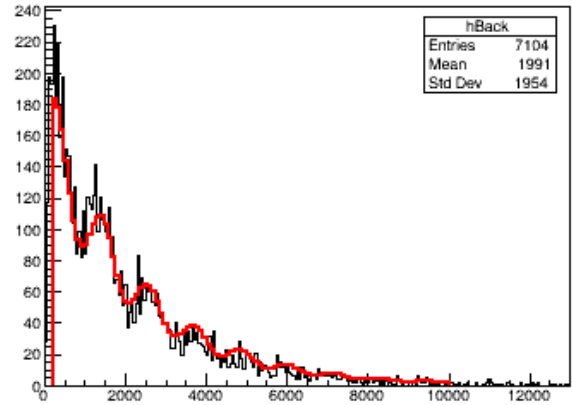
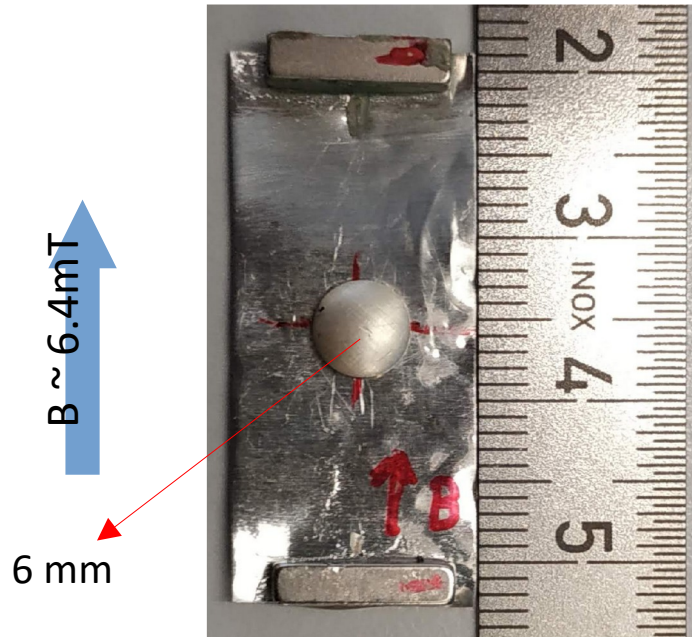
Second Example - μ SR Precession Signal

- For a precession we need a magnetic field... using magnets.



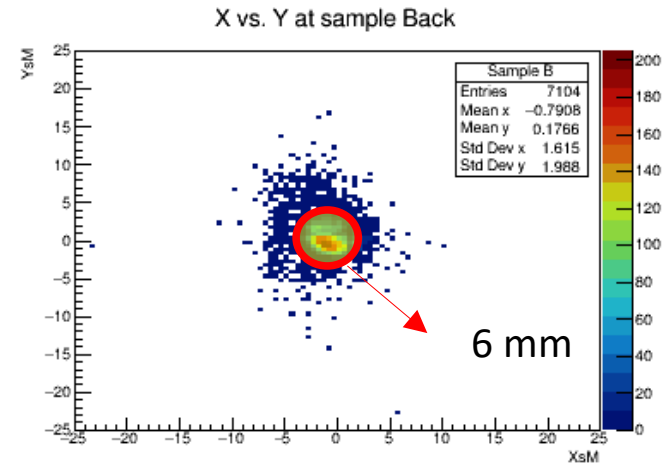
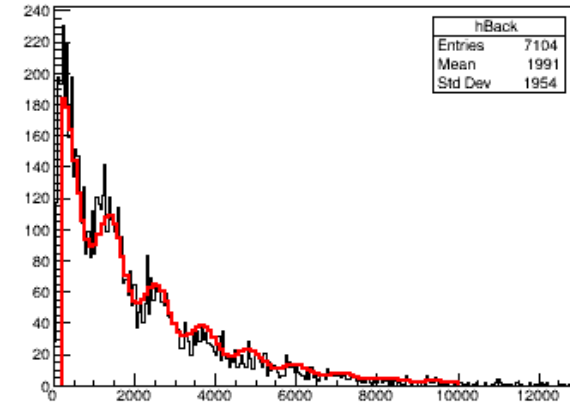
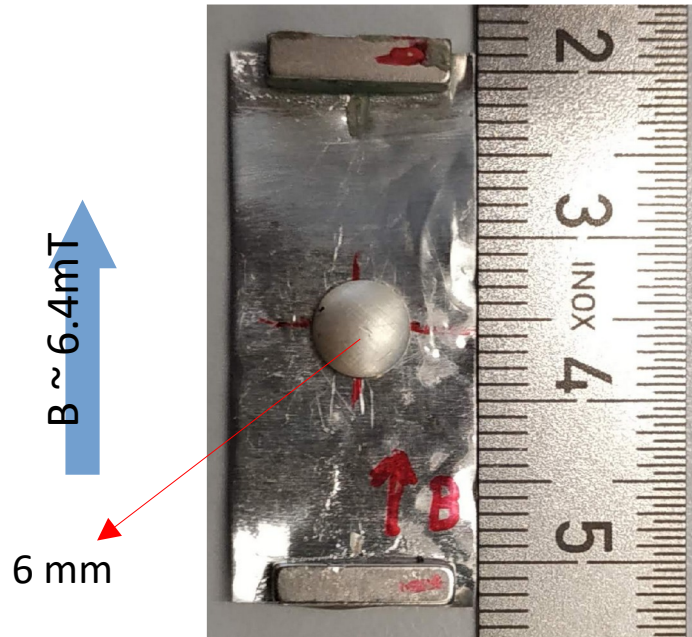
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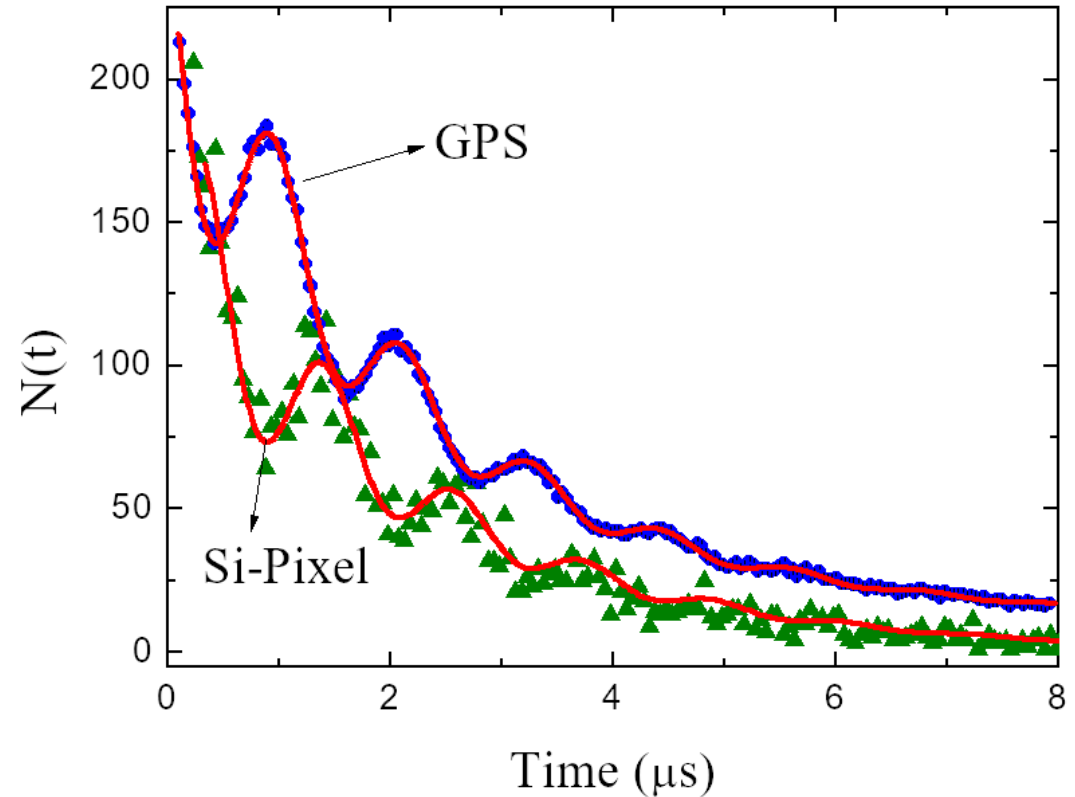
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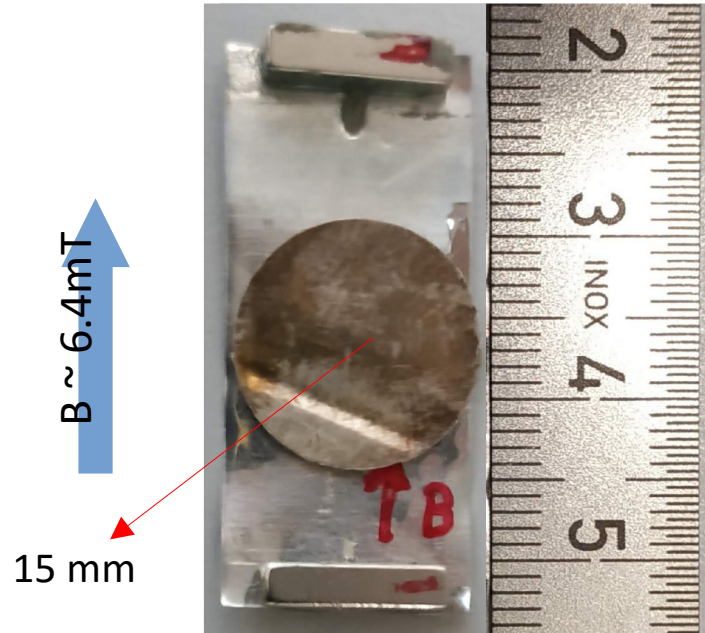
Second Example - μ SR Precession Signal

- Comparison between a standard spectrometer (GPS) and our Si-Pixel spectrometer shows:
 - Same precession frequency and damping, i.e. the same magnetic field and width of field distribution on the sample.
 - Lifetime of muon
 - Si-Pixel has **no accidental background**



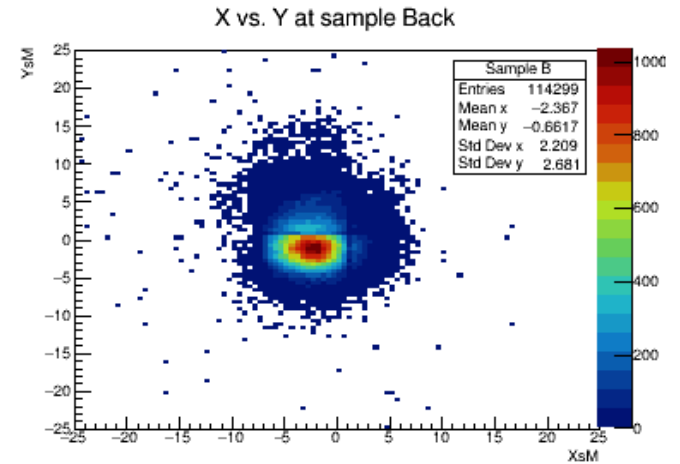
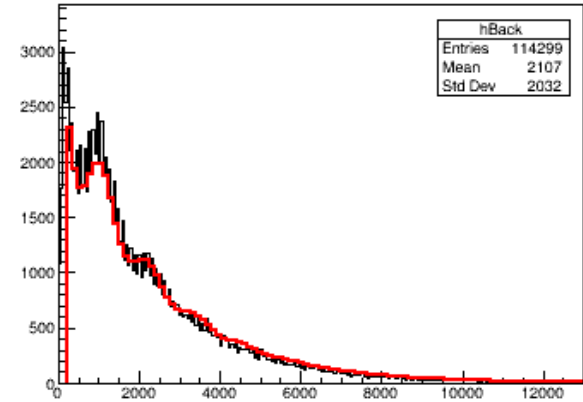
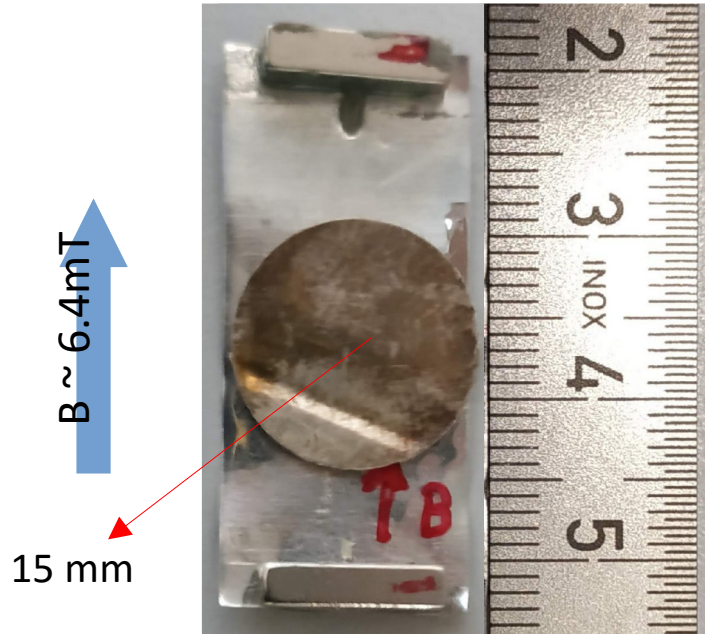
Third Example - μ SR Precession Signal, Magnetic Imaging

- The larger samples show less «wiggles» due to the large field distribution.



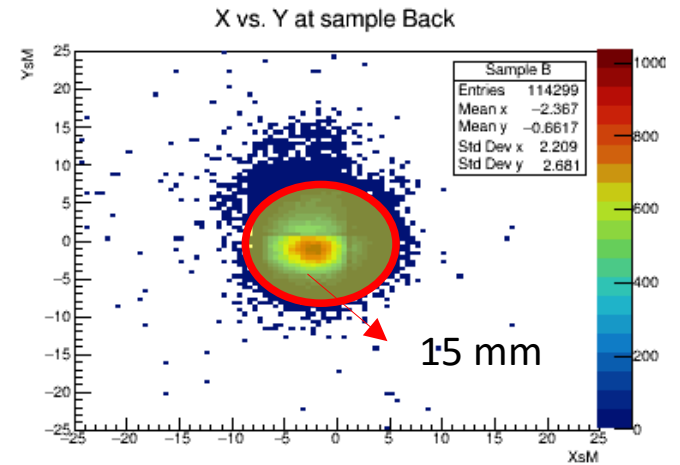
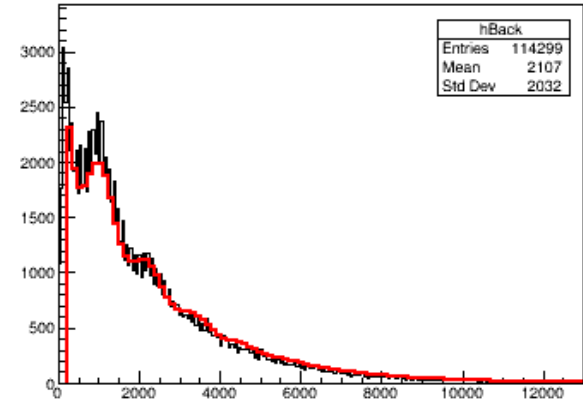
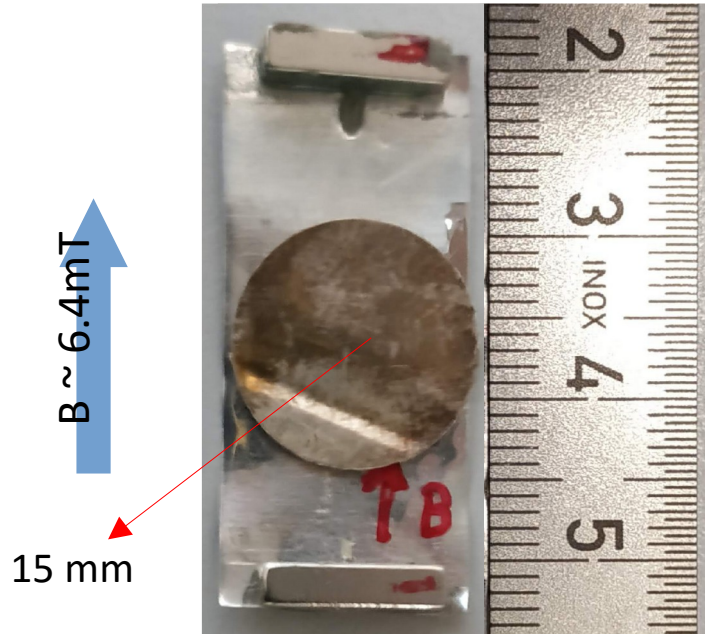
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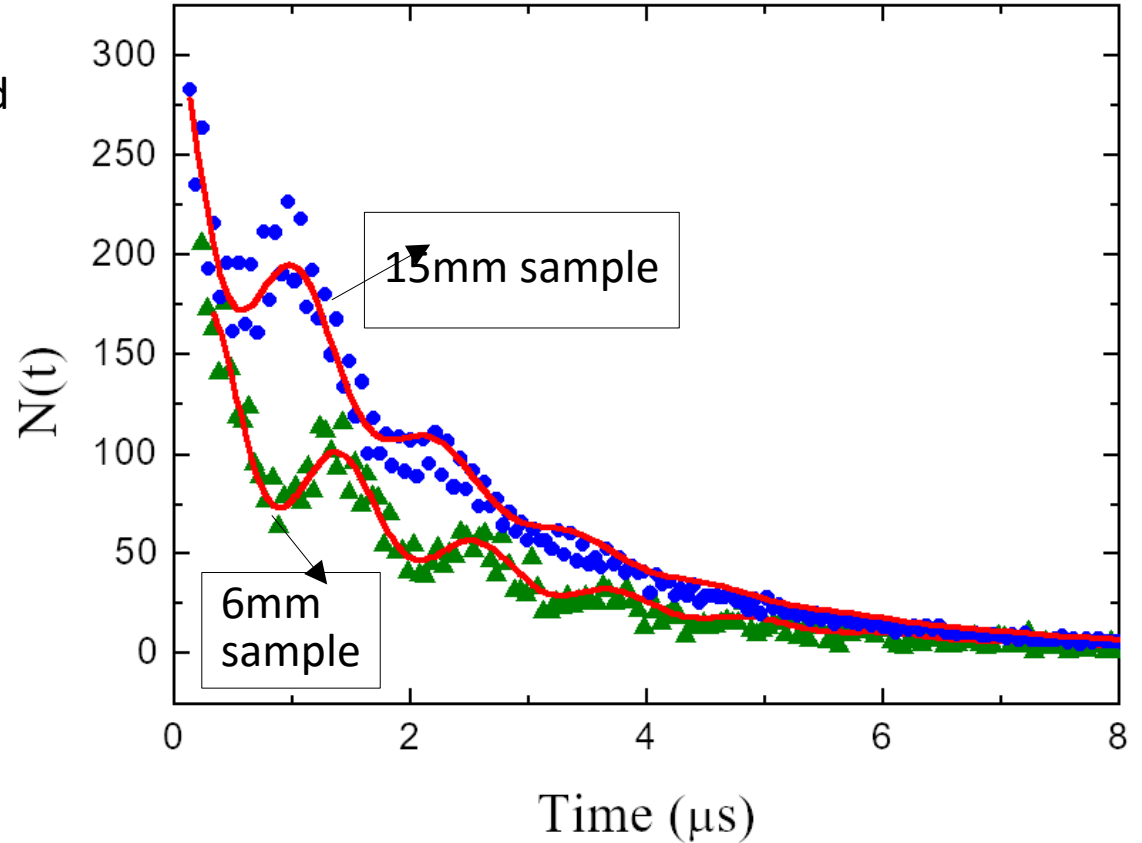
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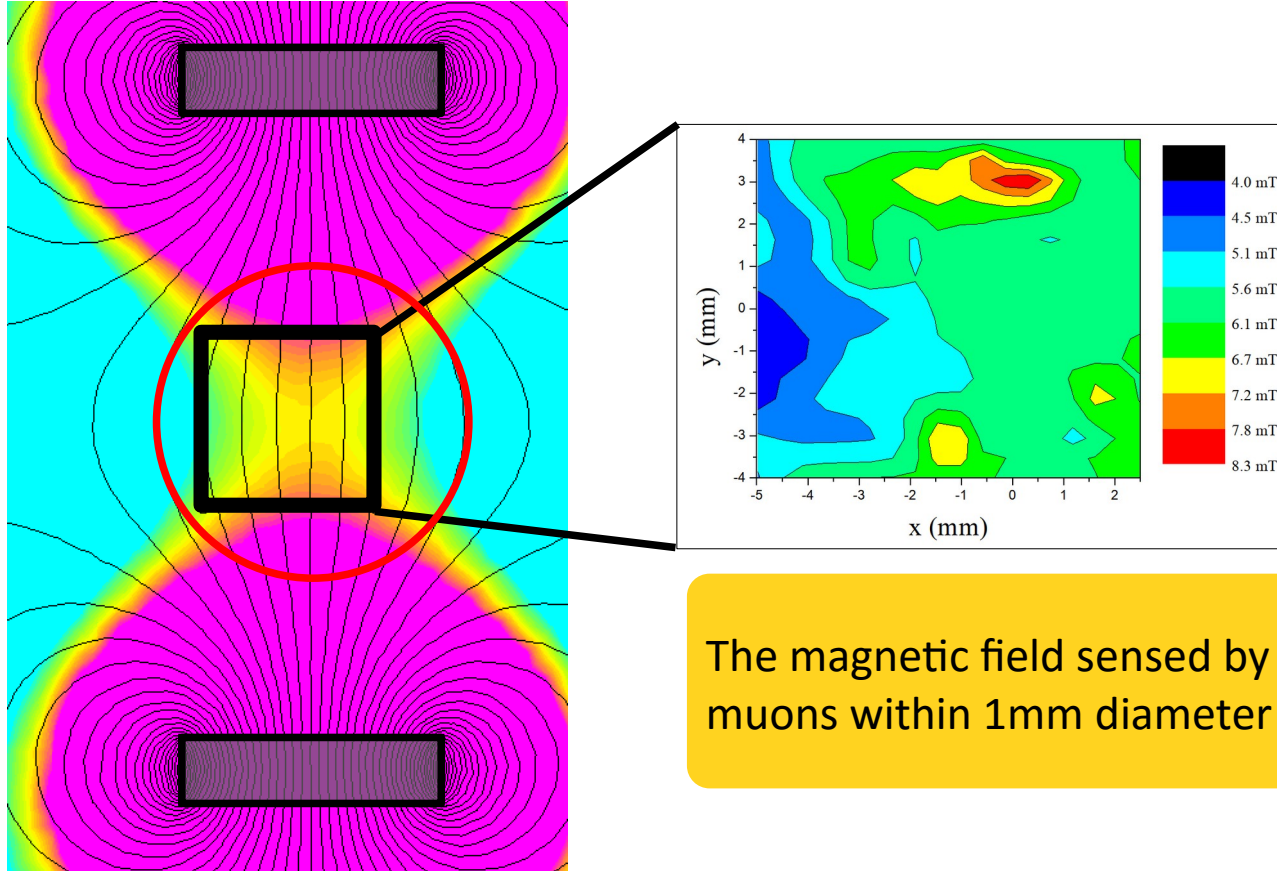


Third Example - μ SR Precession Signal, Magnetic Imaging

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Third Example - μ SR Precession Signal, Magnetic Imaging



Summary and Conclusions

- We can do μ SR using vertex reconstruction schemes
- We can reach at least ~ 1 mm lateral resolution
- Si-Pixel detectors should give a quantum leap in our ability to perform μ SR measurements.
- We will be able to measure millimeter sized sample, perform measurements on multiple sample simultaneously and much more...

Thanks to ...

PSI

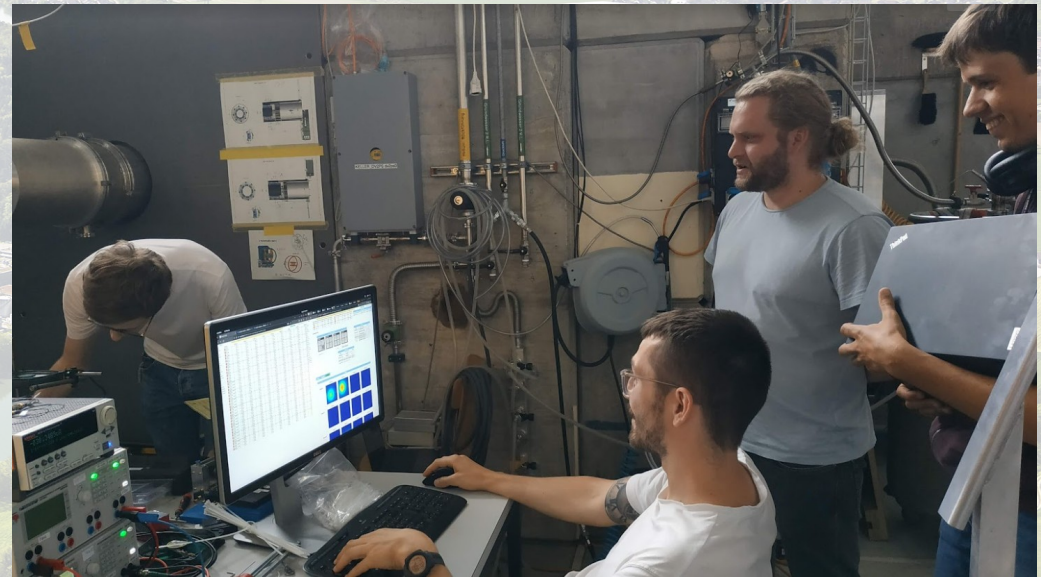
Thomas Prokscha
Hubertus Luetkens
Jonas Krieger
Lea Caminada (UZH)
Hans-Christian Kaestli
Tilman Rohe
Frank Meier

Heidelberg

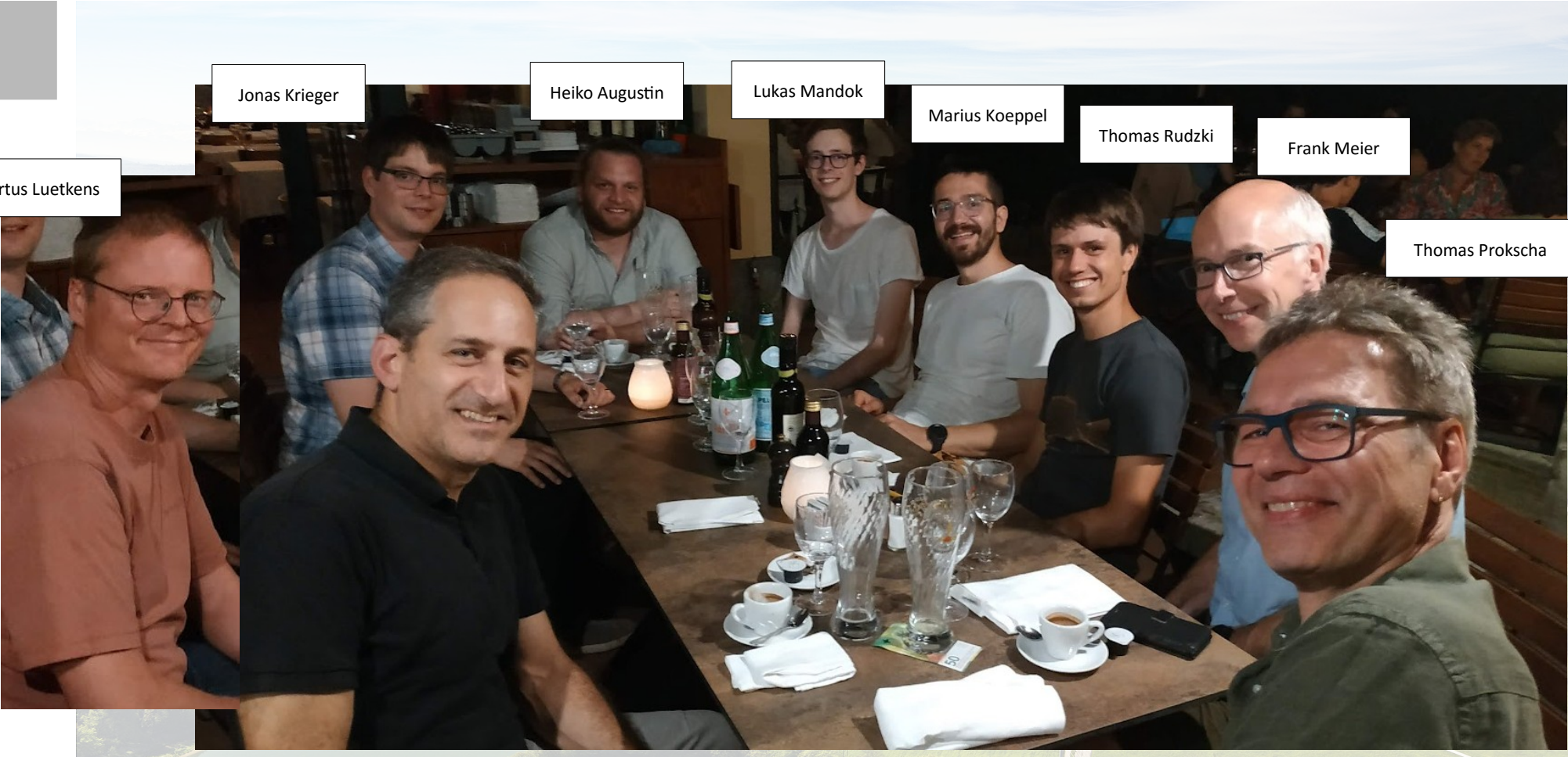
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Lukas Mandok (MSc)
Heiko Augustin (Postdoc)
Andre Schoening

Mainz

Marius Koeppel (PhD)



Thanks



Jonas Krieger

Heiko Augustin

Lukas Mandok

Marius Koeppel

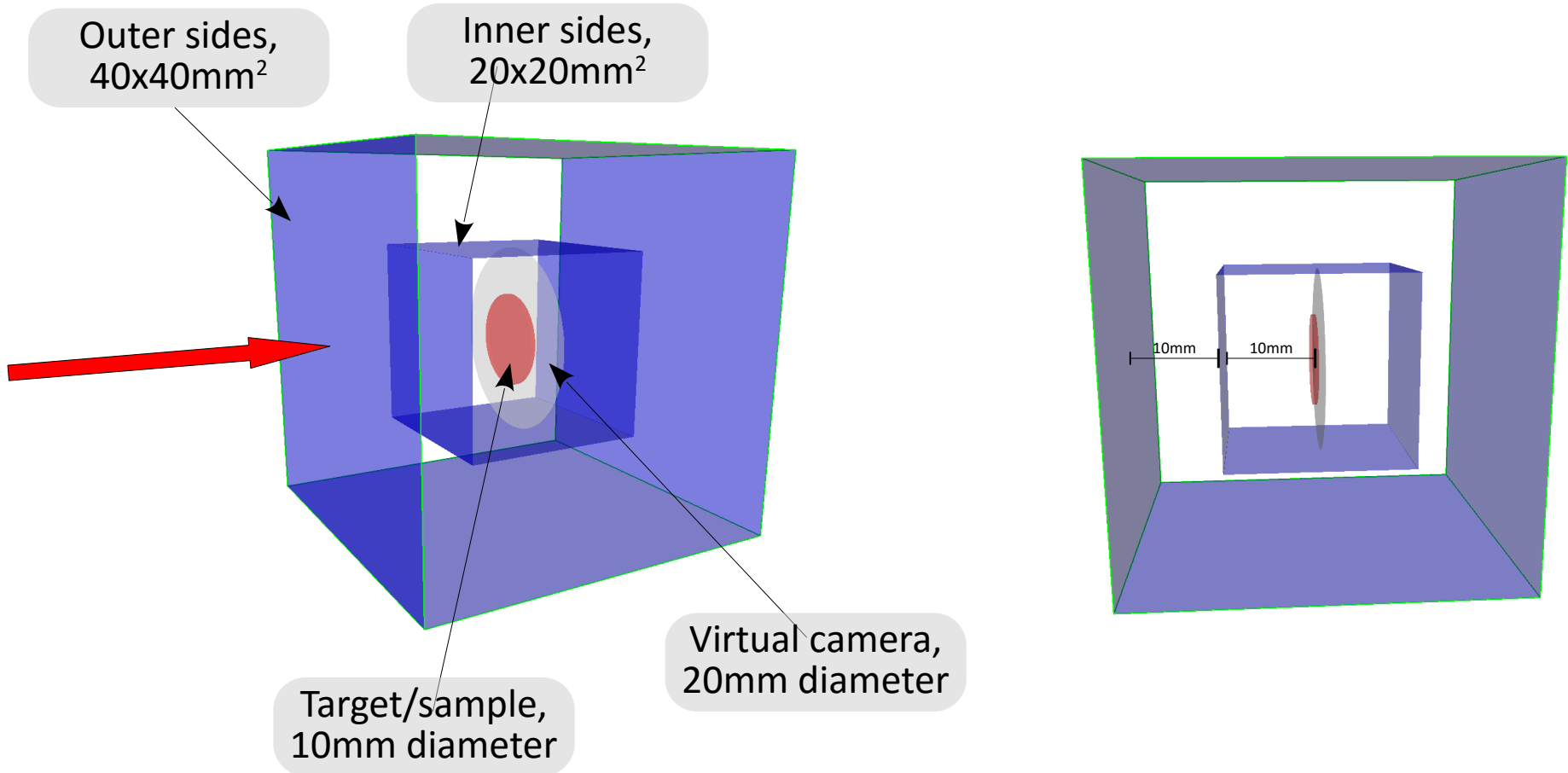
Thomas Rudzki

Frank Meier

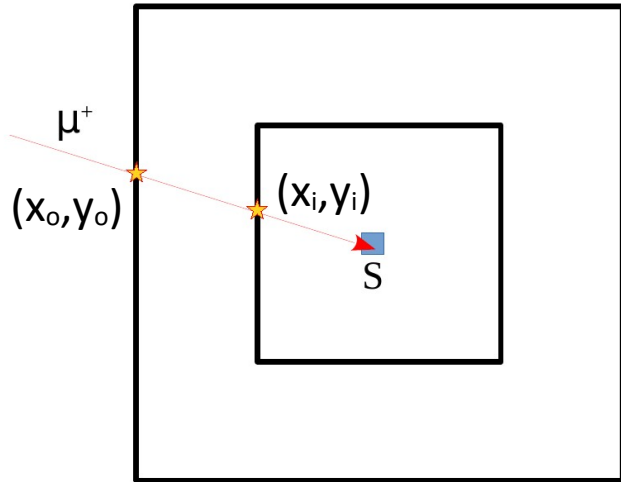
Thomas Prokscha

Hubertus Luetkens

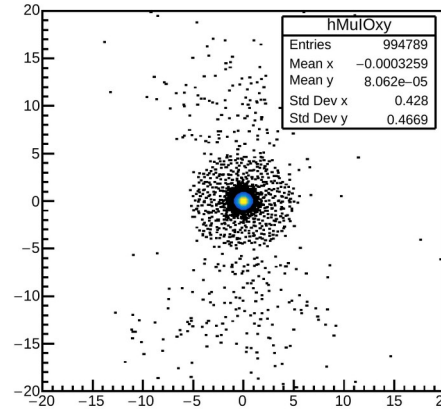
Simulated detector geometry



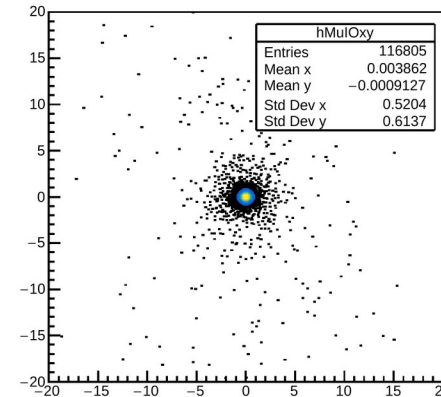
How well does vertex reconstruction work?



- From (x_0, y_0) and (x_i, y_i) extrapolate to sample position $\rightarrow (x_s, y_s)$
- How far is (x_s, y_s) from the actual landing position of the muon (taken from the “camera”).
- Even with a large beam profile we get $\text{RMS} \sim 0.6$ mm with average zero.
- Adding 20μ Kapton adds $\sim 10\%$ to the RMS.

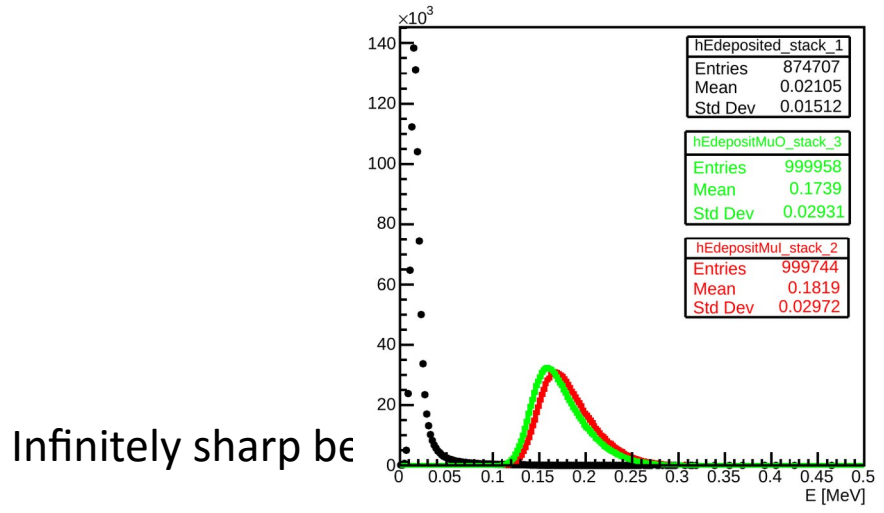
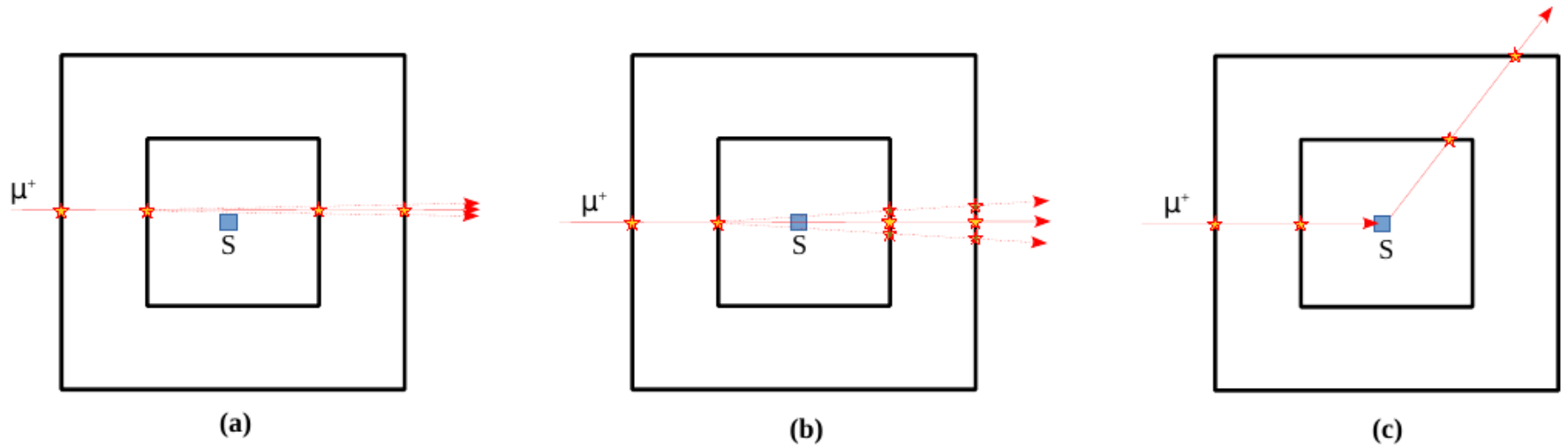


Infinitely sharp beam

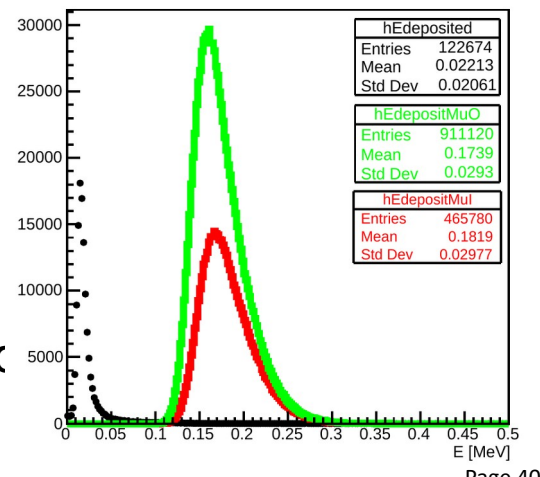


Gaussian beam profile
with $\sigma_{x,y} = 10$ mm

Veto events



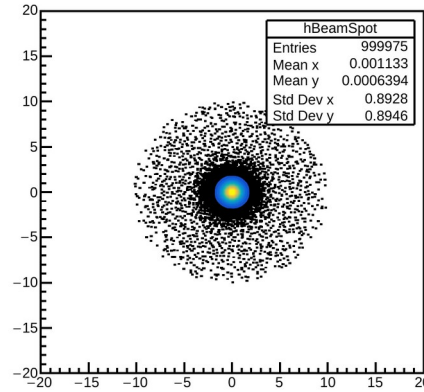
n beam profile with ϵ



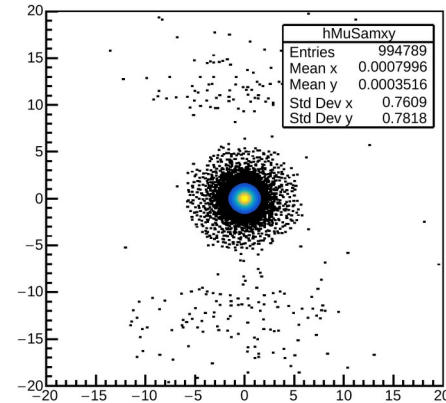
Beam size

Infinitely sharp beam

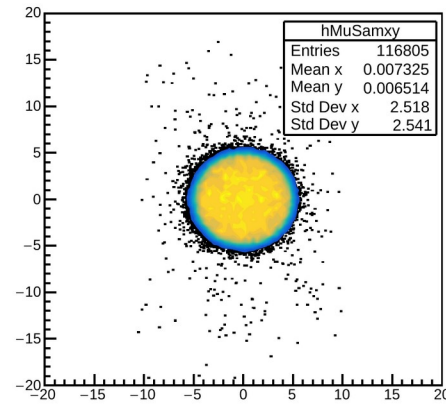
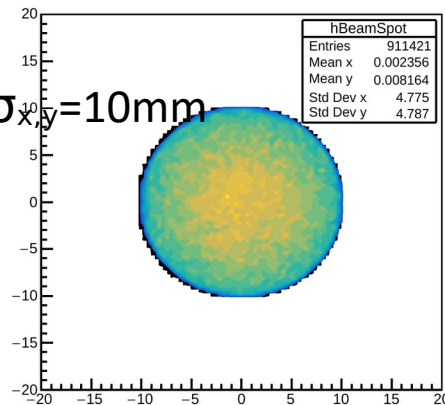
On "camera"



On sample with veto

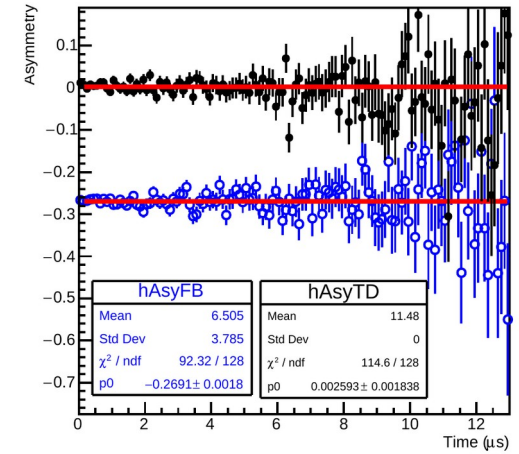
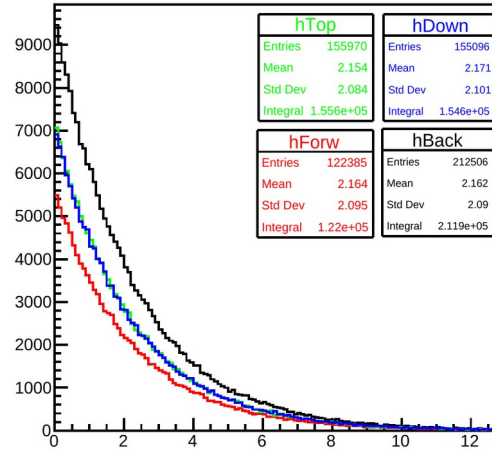


Gaussian beam profile with $\sigma_{xy}=10\text{mm}$

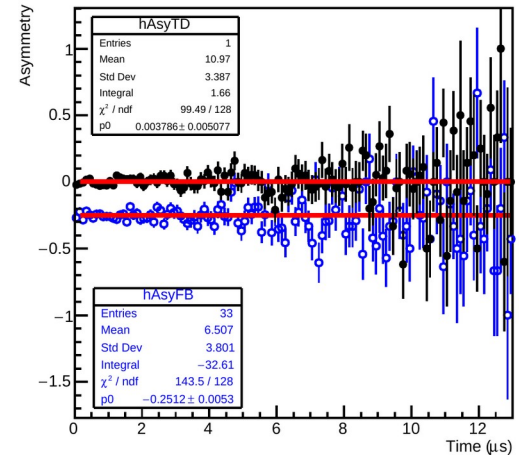
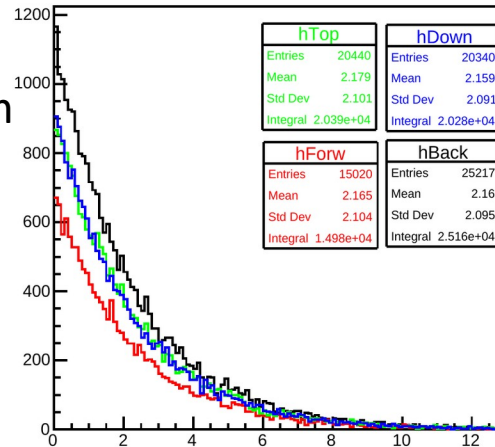


What about μ SR measurements

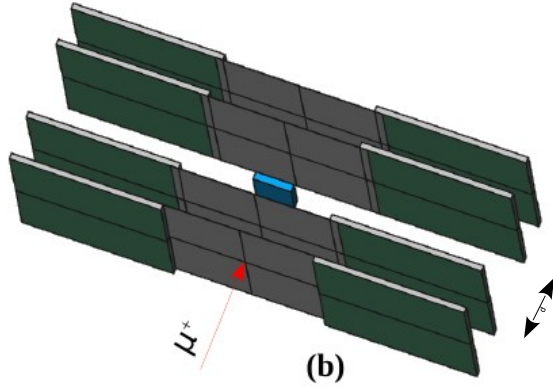
Infinitely sharp beam



Gaussian beam profile with $\sigma_{x,y}=10\text{mm}$

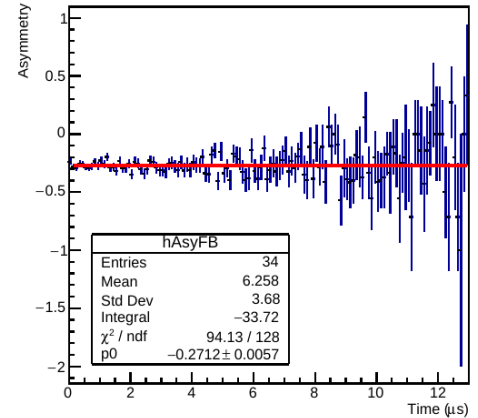
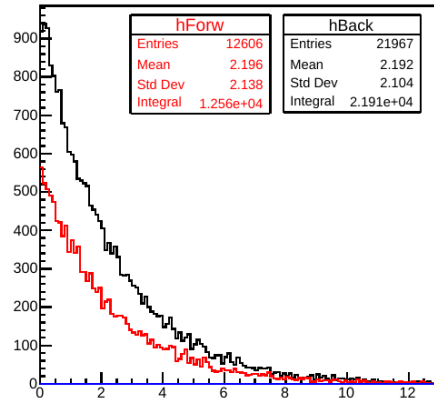
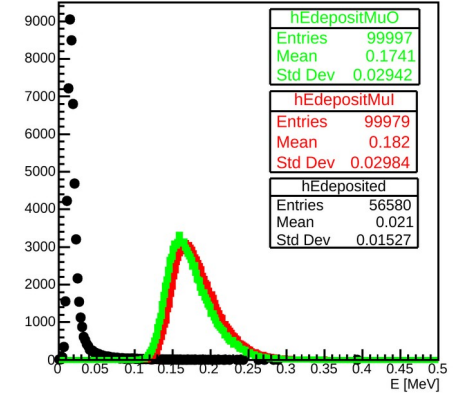
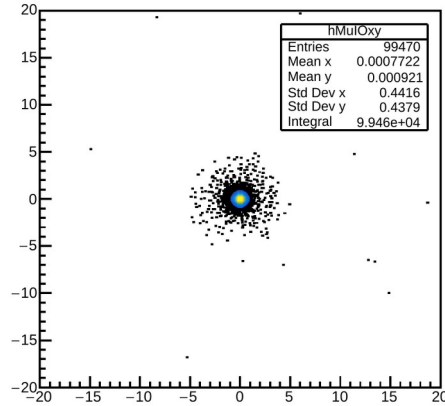


What about the quads?

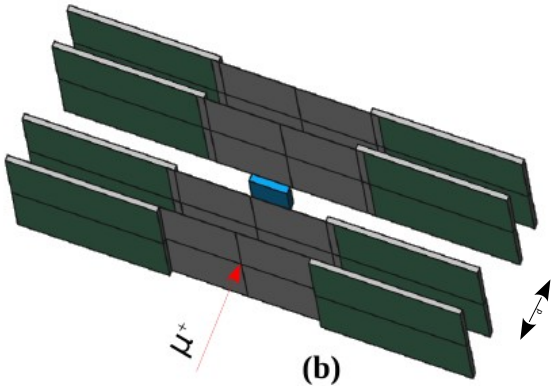


Infinitely sharp beam

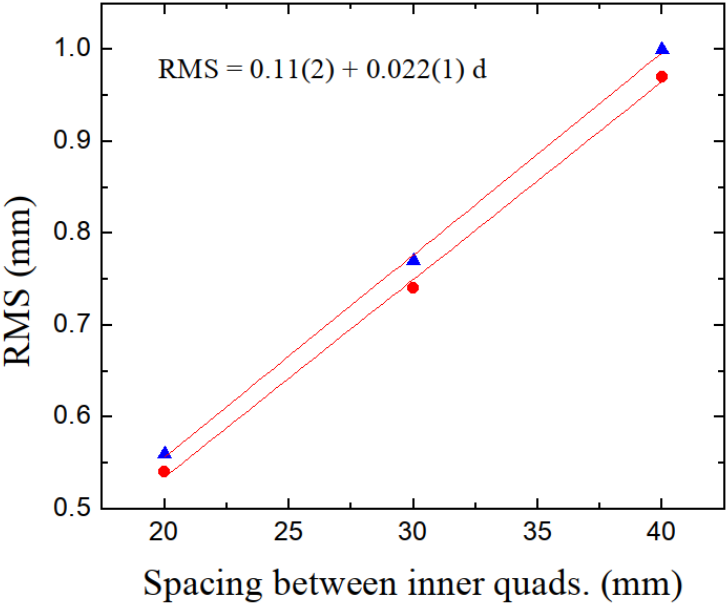
Deviation between vertex and actual hit



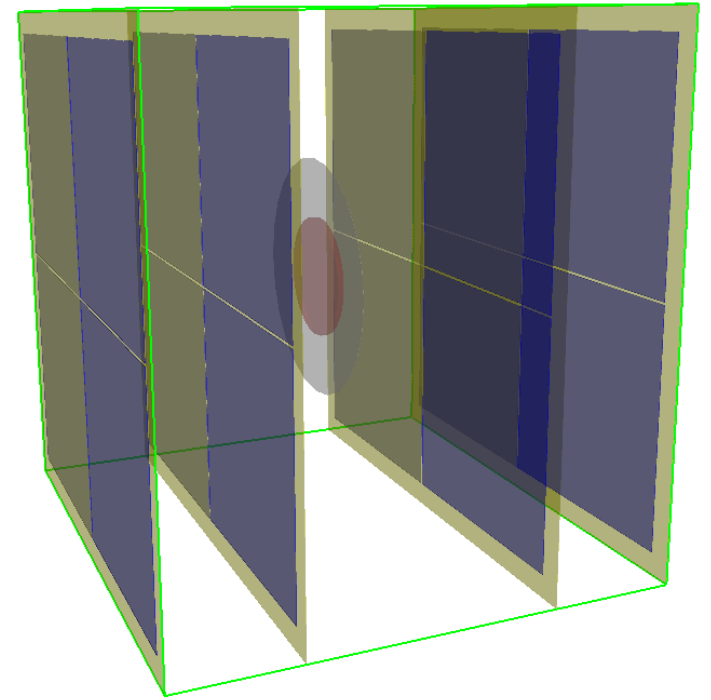
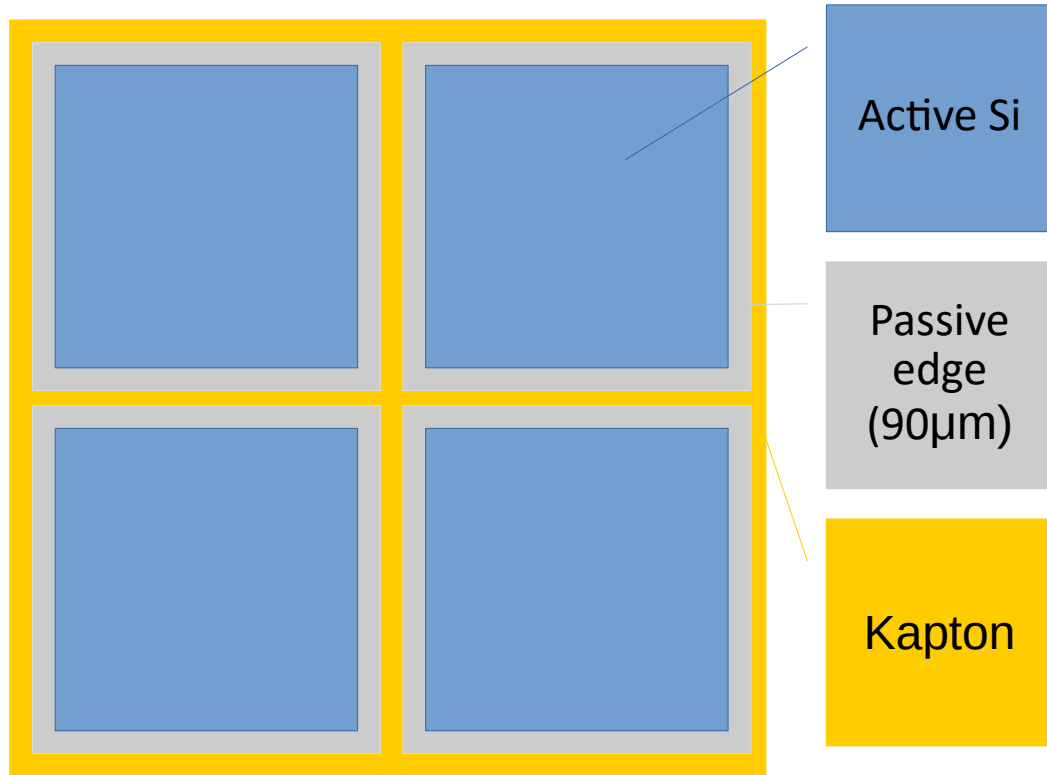
Vertex reconstruction, how far can we go?



Infinitely sharp beam

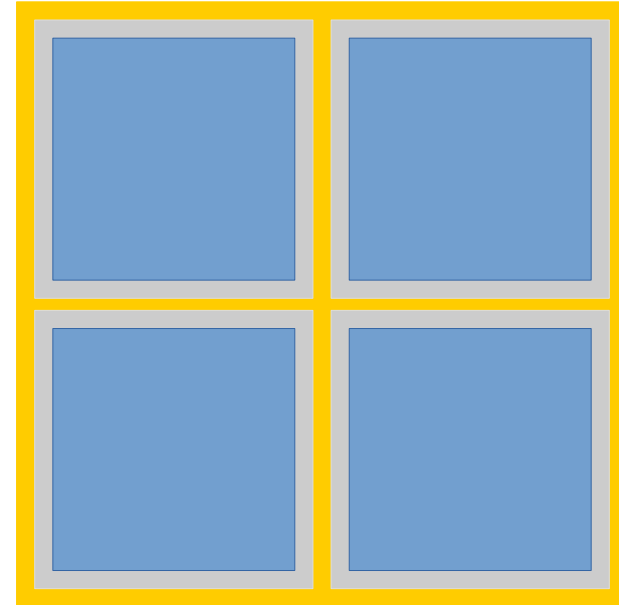


Simulation of realistic quads



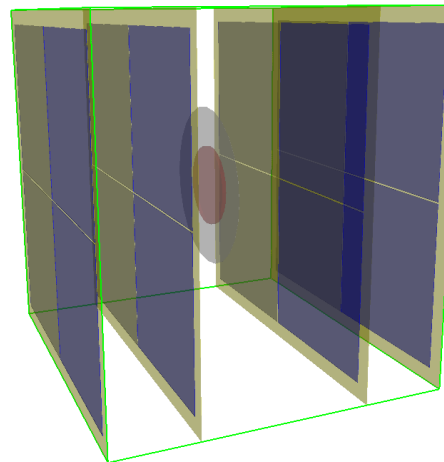
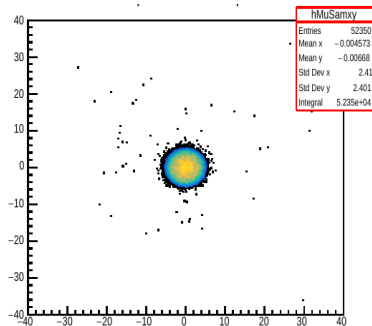
Simulation of realistic quads

- Passive edge fixed at 90 μm .
- Spacing between the chips varied (0, 50, ..., 250 μm).
- Kapton layer is 20 μm , Si layer is 50 μm .

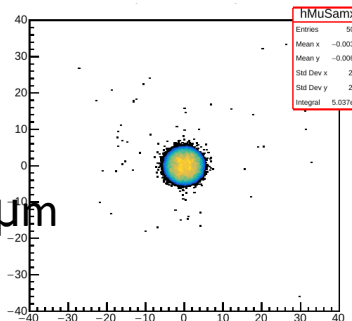


The effect of the gaps visible with veto

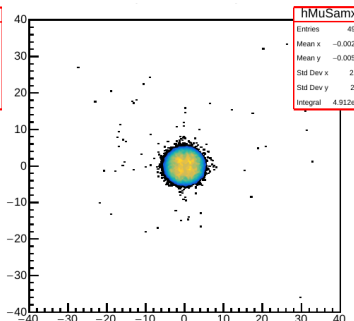
- Beam with 4mm $\sigma_{x,y}$
- No spacing
- No passive edge



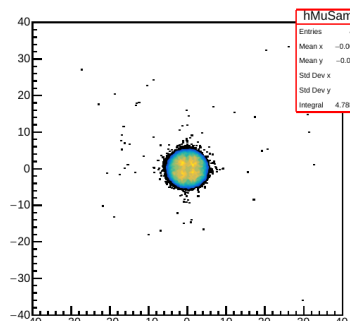
Beam with 4mm $\sigma_{x,y}$
Passive edge fixed at 90 μm



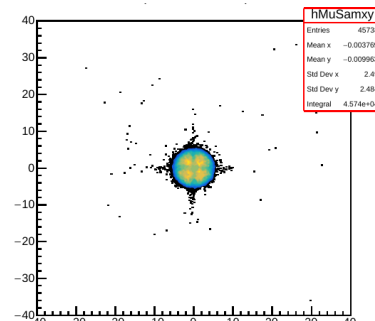
0 μm



50 μm



100 μm

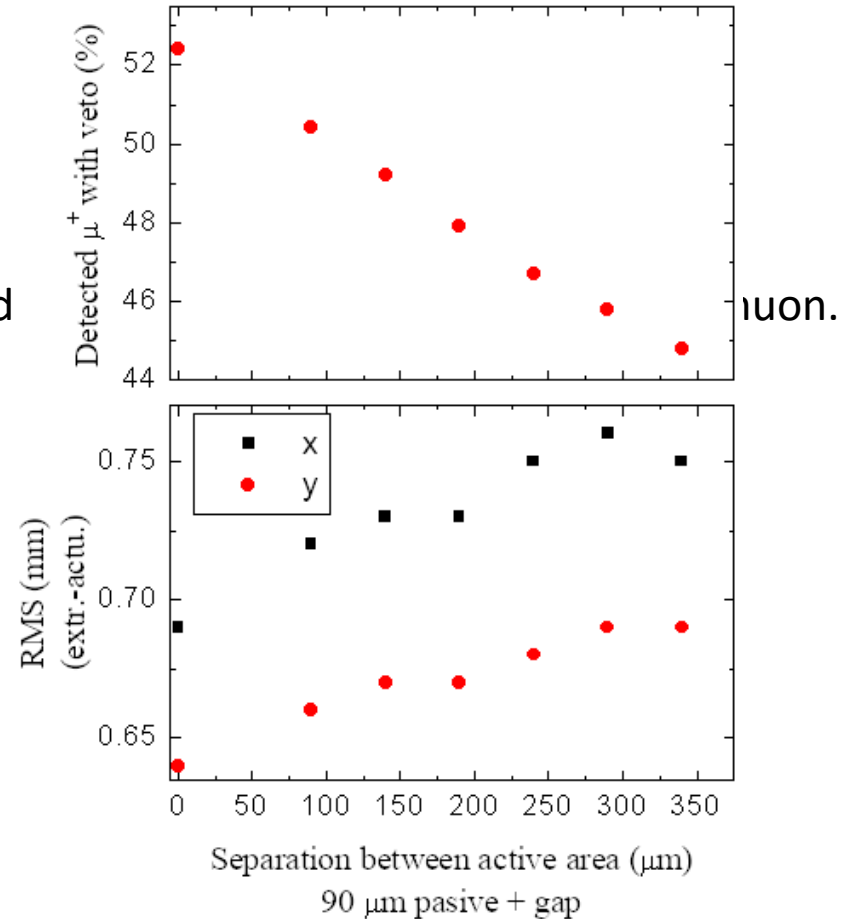


200 μm

Spacing:

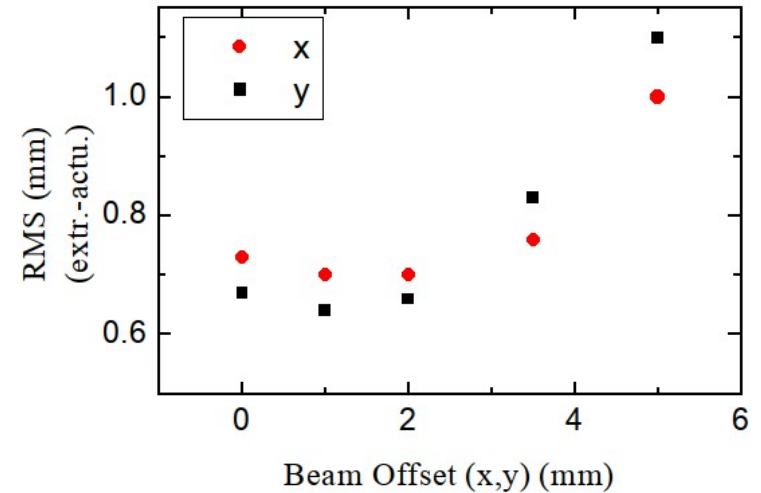
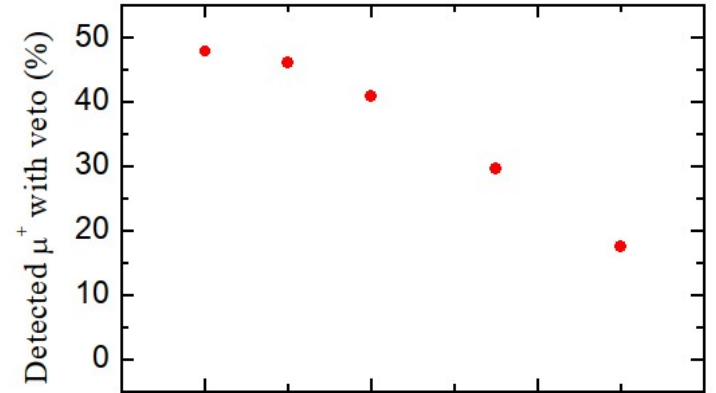
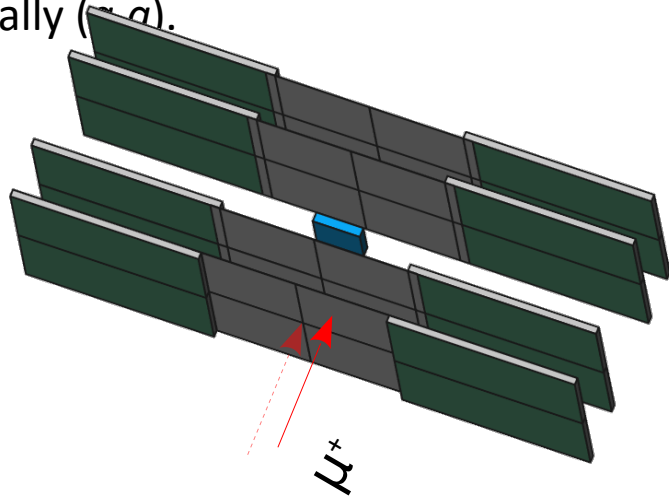
What changes as a function of spacing

the gaps but mainly due the veto algorithm.
function resolution, i.e. RMS of the difference between extrapolated



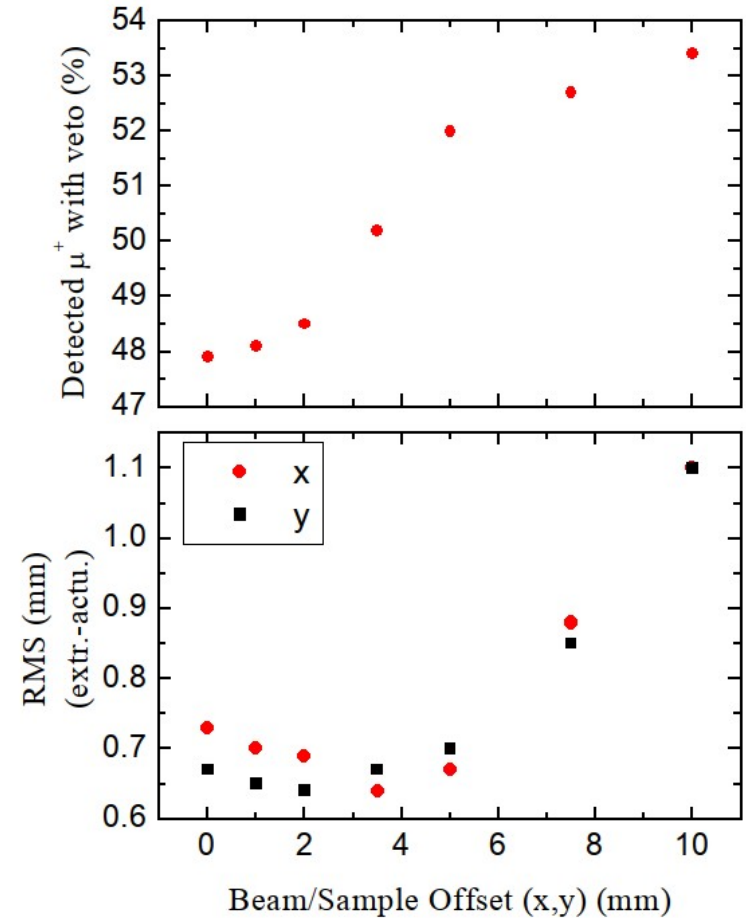
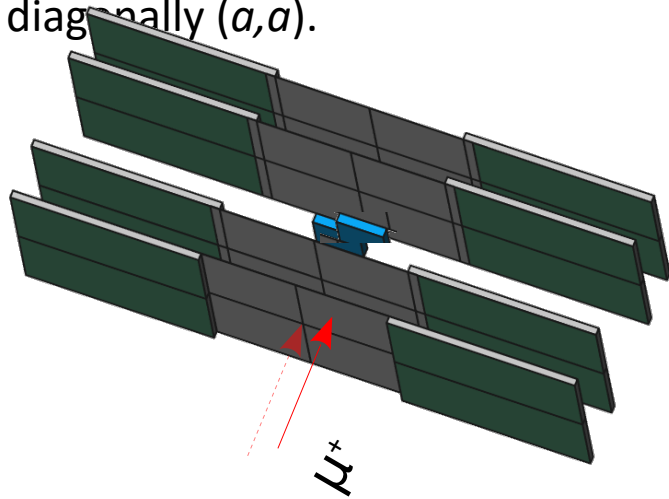
What if we offset the beam from sample

the region with passive edge fixed at $90\mu\text{m}$. Spacing between pixels is $10\mu\text{m}$. **beam** offset diagonally (μ^+).



What if we offset the beam from sample

... region with passive edge fixed at $90\mu\text{m}$. Spacing between pixels μ^+ and **Sample** offset diagonally (a,a) .

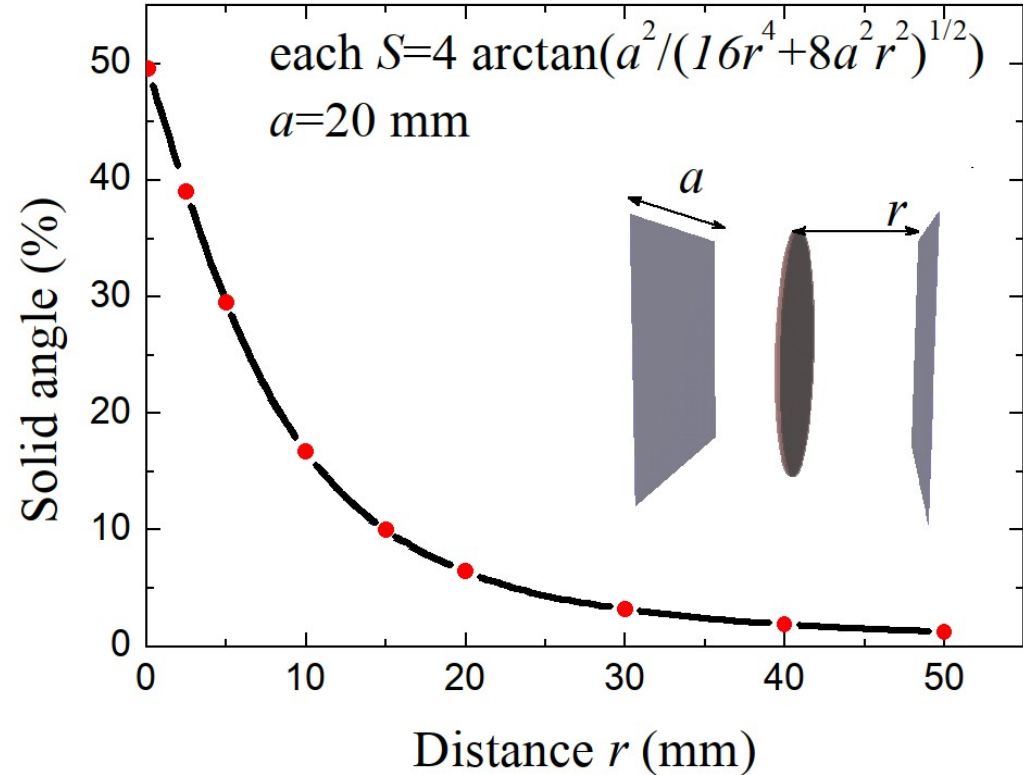


Solid Angle Calculation

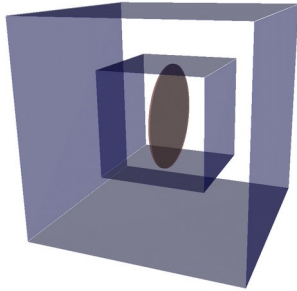
Assuming Si Pixel detectors of 20x20 mm², placed 10 mm from the sample (center):

- The solid angle for each is 1/6
- A solid angle of 1/3 from the Forward/Backward set.
- The outer set should cover the same solid angle, i.e. 40x40 mm², placed 20 mm from the sample.

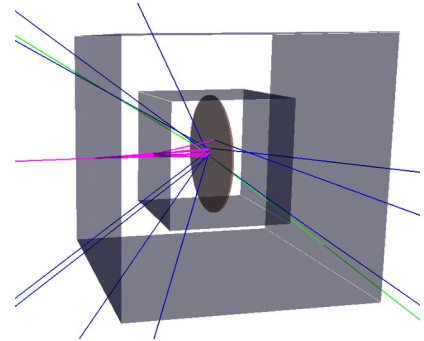
It is also possible double this by adding a Top/Down set as well, with the exact same geometry of the Forward/Backward



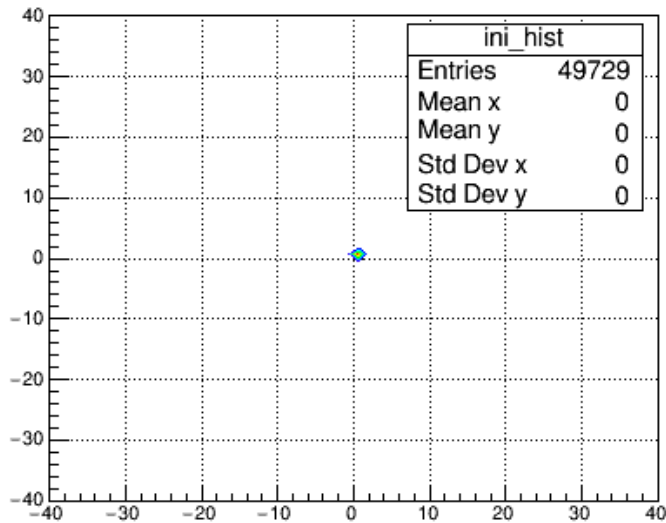
Scattering due to Outer/Inner Detectors



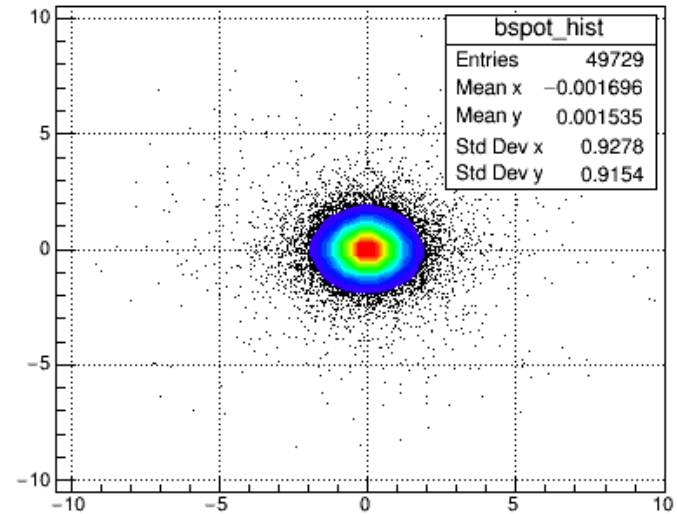
10 mm between target and inner set
10 mm between inner and outer set



Muon initial beam cross section [mm]



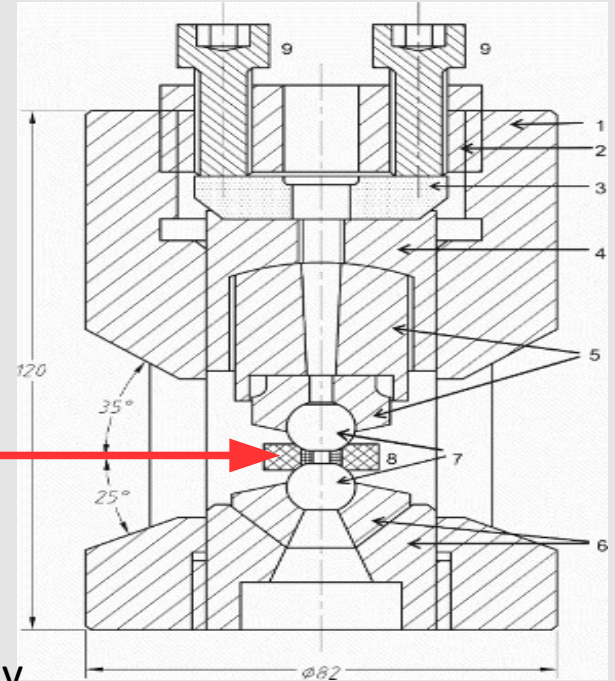
Muon beam cross section [mm]



Microbeam for Small Samples...

Microbeam for

- Very small samples
- Extreme condition studies, e.g.,
- pressure up to 10 GPa using anvil cells (currently 3GPa).



- Scanning across samples to detect variation and homogeneity