

# Quarkonium sequential suppression and heavy-quark potential in p-Pb and Pb-Pb

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# Outline

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## 1. Introduction

heavy ion collisions & Schrodinger equation + complex V

## 2. Wave functions of charmonium in p-Pb

Color screening

parton inelastic scatterings ( imaginary potential )

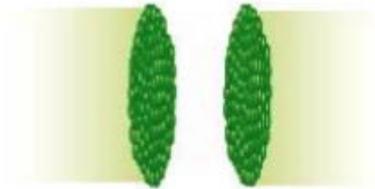
$R_{AA}$  of  $J/\psi$  and  $\psi(2S)$

## 3. Bottomonium (1S, 2S, 3S) in Pb-Pb

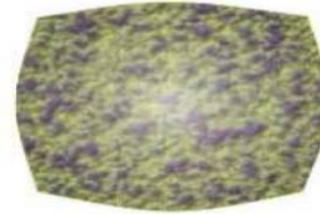
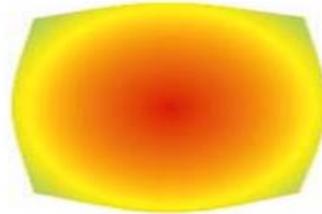
## 4. Summary

# outline

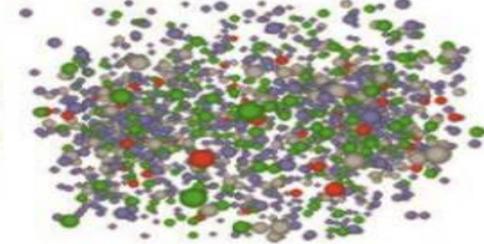
Initial state



Hydro expansion  
of QGP or hadron gas



Freeze-out

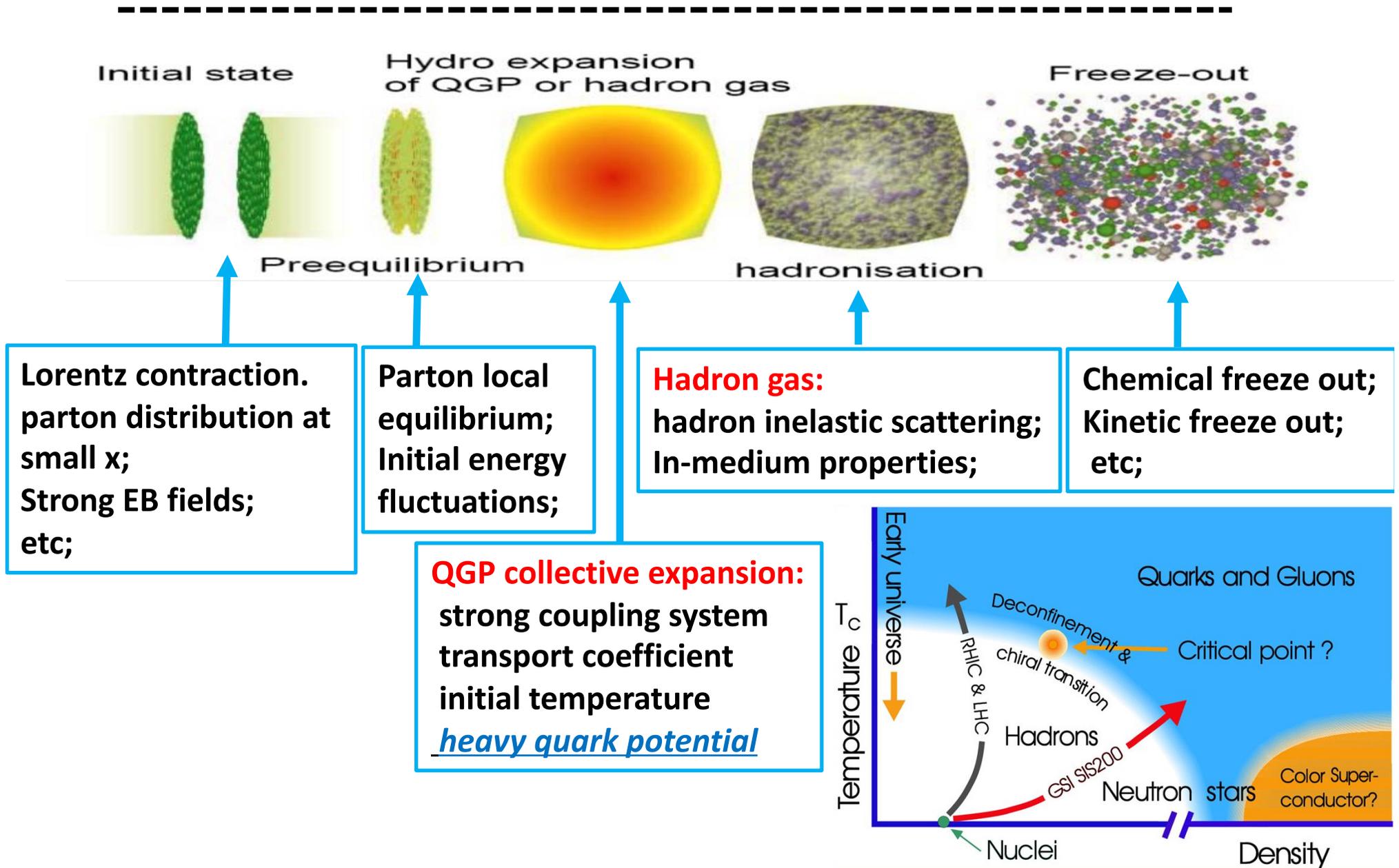


Preequilibrium

hadronisation



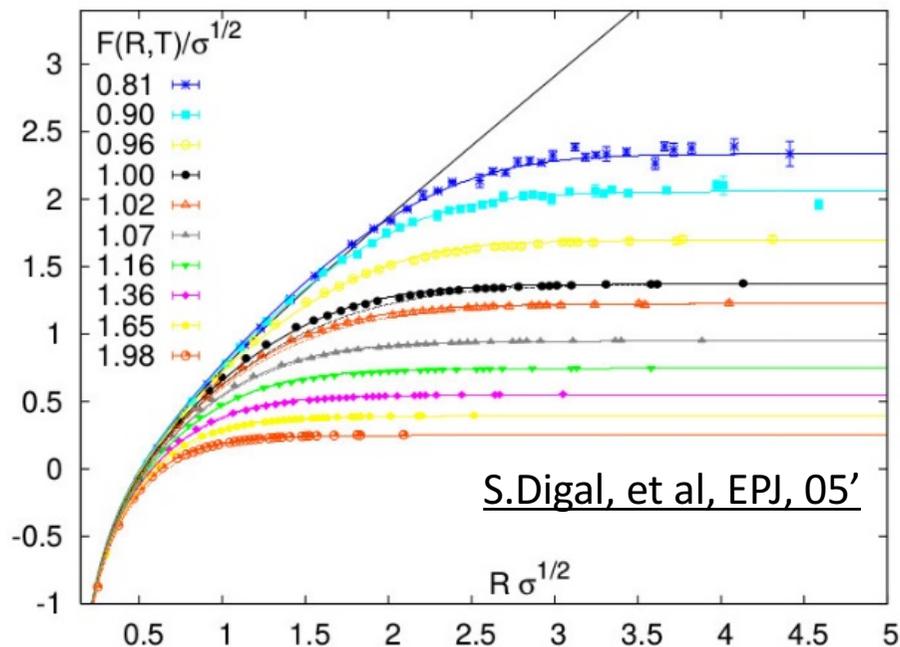
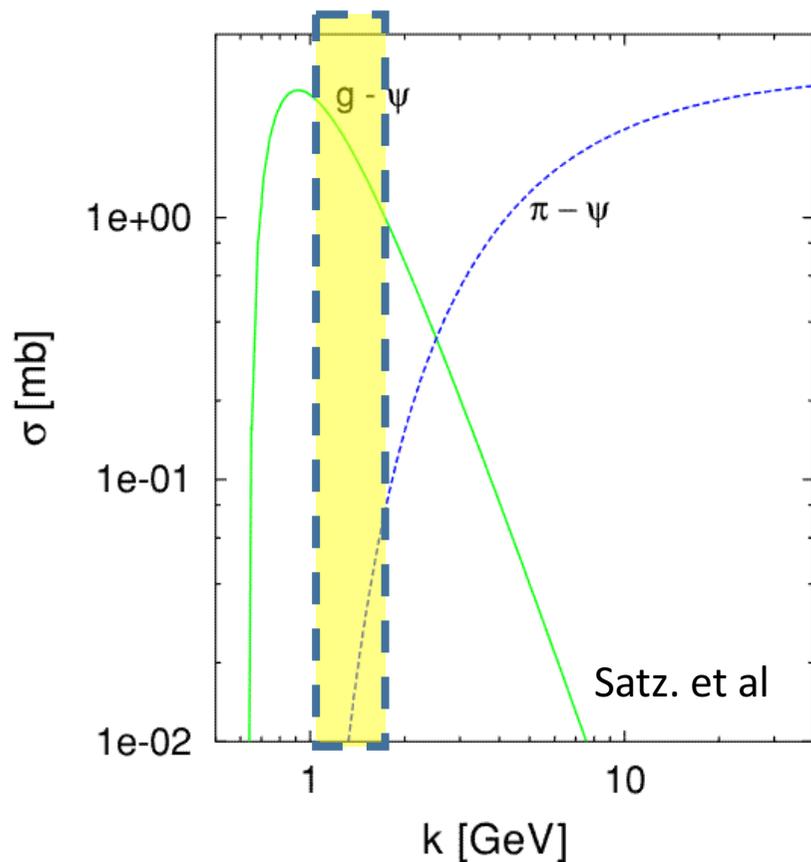
# outline



Quark gluon plasma created in HIC is a very strong coupling medium.

# Abnormal suppression of charmonium

Abnormal suppression of J/psi: **one signal of QGP** by Matsui & Satz



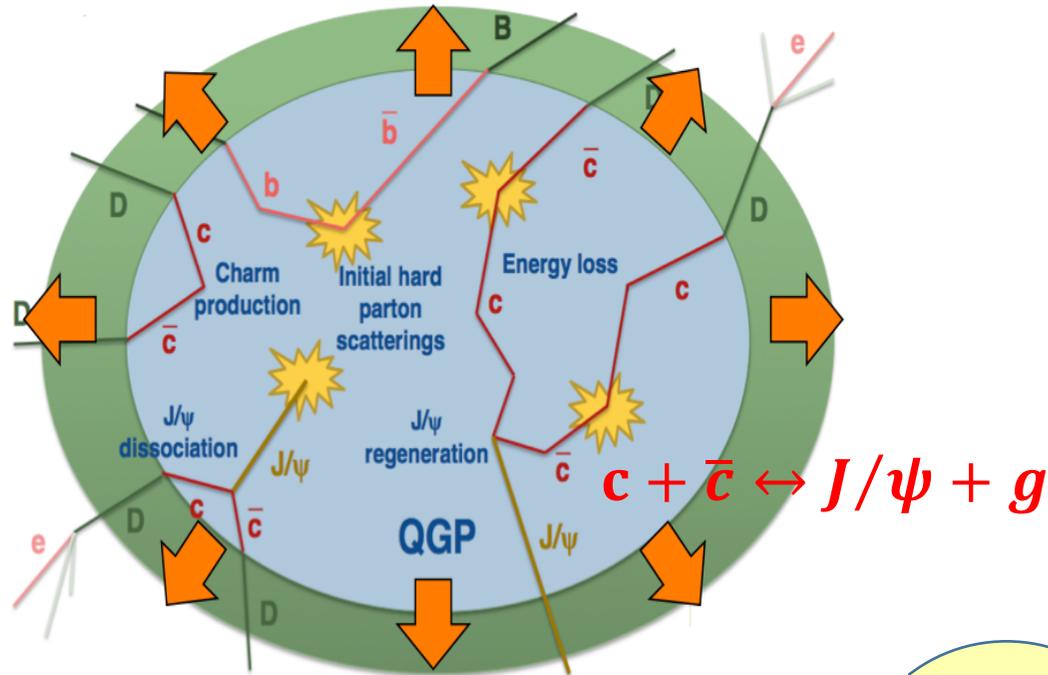
- Parton scatterings:  
medium temperature (LHC)  $\sim 0.3-0.5$  GeV,

- Color screening:  
no attractive force inside "bound states"  
at high T

$$V_{c\bar{c}} = -\frac{\alpha}{r} + \sigma r$$

# Quarkonium in hot medium

## Heavy quark in-medium potential



(Cornell potential)  
J/ψ

QGP evolution  
(transitions)

time →

$$|c\bar{c}\rangle = c_{1S}(t)|J/\psi\rangle + c_{2S}(t)|\psi(2S)\rangle + \dots$$

**$c\bar{c}$  dipole potential in QGP is COLOR SCREENED. Wave function evolution**

# Schrodinger type models

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## Previous studies:

(1) X. Guo, S. Shi, P. Zhuang, et al

**Time-independent relativistic Schrodinger** *Phys.Lett.B* 2012

J/ψ dissociation temperature is changed by ~ 10% after considering relativistic correction

(2) P. Gaussian, R. Katz, et al

**Schrodinger-Langevin equation** *Annals Phys.* 368 (2016) 267-295

Hamiltonian includes a white noise term and a damping term, which affects the expansion and contraction of the wave function

(3) A. Rothkopf, Y. Akamatsu, et al,

**Stochastic Schrodinger equation** *Phys.Rev.D* 97 (2018) 1, 014003

Potential includes stochastic terms, wave function decoherence to dissociate quarkonium states

(4) M. Strickland et al,

**Time-dependent Schrodinger, with complex potential** *Phys.Lett.B* 2020

Bottomonium suppression with real and imaginary potential

And many other references.....

# Time-dependent Schrodinger equation

## Radial Schrodinger equation:

$$i\hbar \frac{\partial}{\partial t} \psi(r, t) = \left[ -\frac{\hbar^2}{2m_\mu} \frac{\partial^2}{\partial r^2} + \frac{L(L+1)\hbar^2}{2m_\mu r^2} + V(r, t) \right] \psi(r, t)$$

$r$ : relative distance between  $c$  and  $\bar{c}$

$m_\mu = m_c/2$ : scaling mass

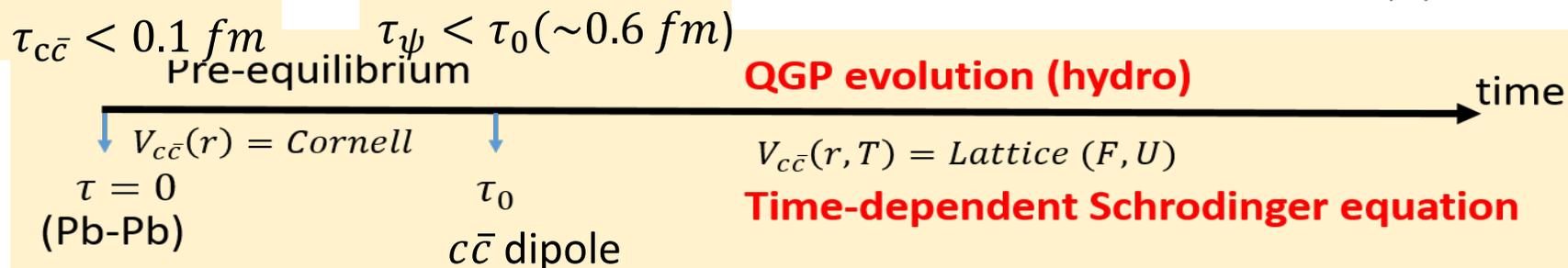
$$\frac{\psi(r, t)}{r} = \sum_m c_m(t) e^{-iE_m t} R_{mS}(r)$$

Wavefunction of eigenstates:

$$\Psi_{klm}(\vec{r}) = R_{kl}(r) Y_{lm}(\theta, \varphi)$$

## Numerical form: Crank-Nicolson method

$$i \frac{\psi_j^{n+1} - \psi_j^n}{\Delta t} = \frac{1}{2} \left[ -\frac{1}{2m_\mu} \frac{\psi_{j+1}^n - 2\psi_j^n + \psi_{j-1}^n}{(\Delta x)^2} + V_j^n \psi_j^n \right. \\ \left. - \frac{1}{2m_\mu} \frac{\psi_{j+1}^{n+1} - 2\psi_j^{n+1} + \psi_{j-1}^{n+1}}{(\Delta x)^2} + V_j^{n+1} \psi_j^{n+1} \right]$$



# Time-dependent Schrodinger equation

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Simplify the numerical form as:

$$\begin{pmatrix} \mathbf{T}_{0,0}^{n+1} & \mathbf{T}_{0,1}^{n+1} & 0 & 0 & \dots \\ \mathbf{T}_{1,0}^{n+1} & \mathbf{T}_{1,1}^{n+1} & \mathbf{T}_{1,2}^{n+1} & 0 & \dots \\ 0 & \mathbf{T}_{2,1}^{n+1} & \mathbf{T}_{2,2}^{n+1} & \mathbf{T}_{2,3}^{n+1} & \dots \\ \dots & \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots & \dots \end{pmatrix} \begin{pmatrix} \psi_0^{n+1} \\ \psi_1^{n+1} \\ \psi_2^{n+1} \\ \psi_3^{n+1} \\ \dots \end{pmatrix} = \begin{pmatrix} \Gamma_0^n \\ \Gamma_1^n \\ \Gamma_2^n \\ \Gamma_3^n \\ \dots \end{pmatrix}$$

Matrix elements:

$$\mathbf{T}_{j,j}^{n+1} = 2 + 2a + bV_j^{n+1} \quad a = i \Delta t / (2m_\mu (\Delta r)^2)$$

$$\mathbf{T}_{j,j+1}^{n+1} = \mathbf{T}_{j+1,j}^{n+1} = -a \quad b = i \Delta t$$

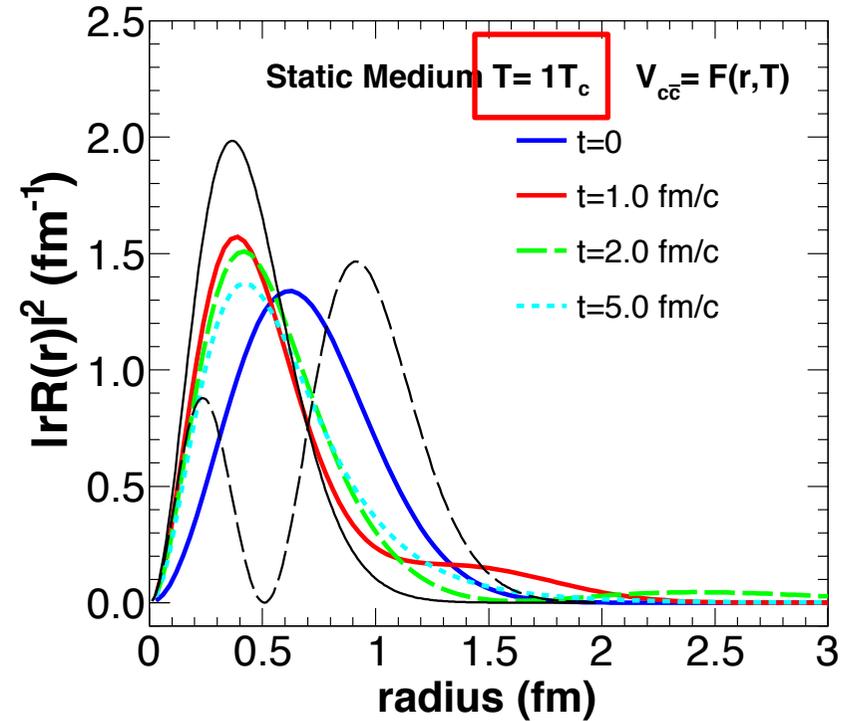
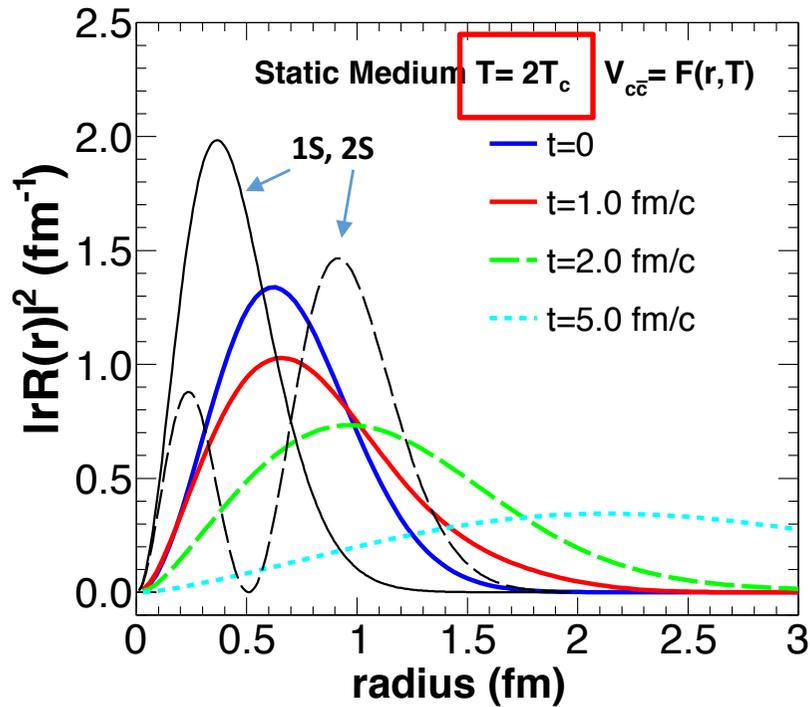
$$\Delta t = 0.001 \text{ fm/c}$$

$$\Delta r = 0.03 \text{ fm}$$

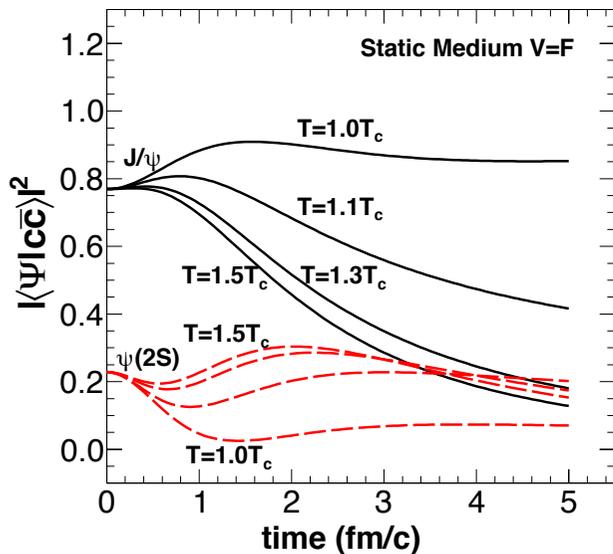
- **mS eigenstate components** in one dipole:

$$c_{mS}(t) = \langle R_{mS}(r) | \frac{\psi(r,t)}{r} \rangle = \int R_{mS}(r) \psi(r,t) \cdot r dr$$

# Evolution in static medium



Snapshot of the  $c\bar{c}$  wavefunction at different time



At high  $T$ , wavefunction expand outside,  $J/\psi \rightarrow \psi(2S)$   
 At low  $T$ , wavefunction contracts,  $\psi(2S) \rightarrow J/\psi$

# Initial conditions (heavy-ion)

## 1. $c\bar{c}$ internal Initial wavefunction:

Taken as quarkonium eigenstates  
(neglect the pre-equilibrium effect)

$$\psi_{c\bar{c}}(\tau = \tau_0) = \phi_{1S,2S}(\mathbf{r})$$

Initial direct yields

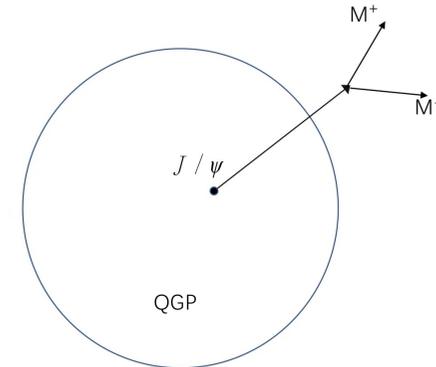
$$f_{pp}^{J/\psi} : f_{pp}^{\chi_c} : f_{pp}^{\psi(2S)} = 0.68 : 1 : 0.19$$

## 2. The initial momentum and spatial distribution of the center of $c\bar{c}$ dipole

$$f_{\Psi}(\mathbf{p}, \mathbf{x} | \mathbf{b}) = (2\pi)^3 \delta(z) T_p(\mathbf{x}_T) T_A(\mathbf{x}_T - \mathbf{b})$$

$$\times \mathcal{R}_g(x_g, \mu_F, \mathbf{x}_T - \mathbf{b}) \frac{d\bar{\sigma}_{pp}^{\Psi}}{d^3\mathbf{p}},$$


  
Shadowing effect from EPS09 NLO



The initial momentum of  $c\bar{c}$  dipoles in pp,  
(neglect the mass difference)

$$\frac{dN_{J/\psi}}{2\pi p_T dp_T} = \frac{(n-1)}{\pi(n-2)\langle p_T^2 \rangle_{pp}} \left[ 1 + \frac{p_T^2}{(n-2)\langle p_T^2 \rangle_{pp}} \right]^{-n}$$

$$n = 3.2 \quad \langle p_T^2 \rangle(y) = \langle p_T^2 \rangle(y=0) \left[ 1 - \left( \frac{y}{y_{max}} \right)^2 \right]$$

Including Cronin effect

$$\frac{d\bar{\sigma}_{pp}^{\Psi}}{d^3\mathbf{p}} = \frac{1}{\pi a_{gN} l} \int d^2\mathbf{q}_T e^{\frac{-q_T^2}{a_{gN} l}} \frac{d\sigma_{pp}^{\Psi}}{d^3\mathbf{p}}$$

$$a_{gN} = 0.15 (\text{GeV}/c)^2$$

$$\ln(\sqrt{s_{NN}}/m_{\Psi})$$

# RAA definition

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- The initial yields of charmonium eigenstates

$$n_{mS}^{t=0}(\mathbf{x}_T, p_T | \mathbf{b}, y) = n_{c\bar{c}}(\mathbf{x}_T, p_T | \mathbf{b}) \times |\langle R_{mS}(r) | \phi_0(r) \rangle|^2$$

$$|c_{mS}(t=0 | \mathbf{b})|^2 = \int d\mathbf{x}_T \int_{p_{T1}}^{p_{T2}} dp_T n_{mS}(\mathbf{x}_T, p_T | \mathbf{b})$$

- Charmonium **direct**  $R_{AA}$  with hot medium effects,

$$R_{pA}^{\text{direct}}(nl) = \frac{\langle |c_{nl}(t)|^2 \rangle_{\text{en}}}{\langle |c_{nl}(t_0)|^2 \rangle_{\text{en}}}$$

$$= \frac{\int d\mathbf{x}_\Psi d\mathbf{p}_\Psi |c_{nl}(t, \mathbf{x}_\Psi, \mathbf{p}_\Psi)|^2 \frac{dN_{pA}^\Psi}{d\mathbf{x}_\Psi d\mathbf{p}_\Psi}}{\int d\mathbf{x}_\Psi d\mathbf{p}_\Psi |c_{nl}(t_0, \mathbf{x}_0, \mathbf{p}_\Psi)|^2 \frac{dN_{pA}^\Psi}{d\mathbf{x}_\Psi d\mathbf{p}_\Psi}}$$

$$R_{pA}(J/\psi) = \frac{\sum_{nl} \langle |c_{nl}(t)|^2 \rangle_{\text{en}} f_{pp}^{nl} \mathcal{B}_{nl \rightarrow J/\psi}}{\sum_{nl} \langle |c_{nl}(t_0)|^2 \rangle_{\text{en}} f_{pp}^{nl} \mathcal{B}_{nl \rightarrow J/\psi}}$$

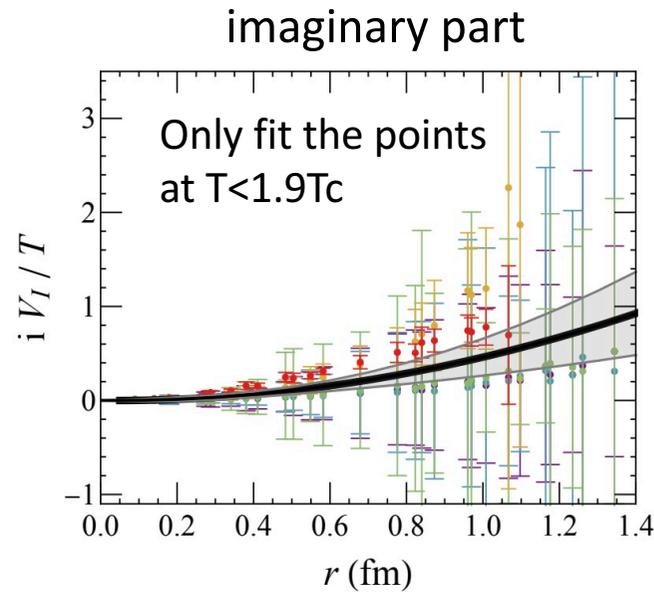
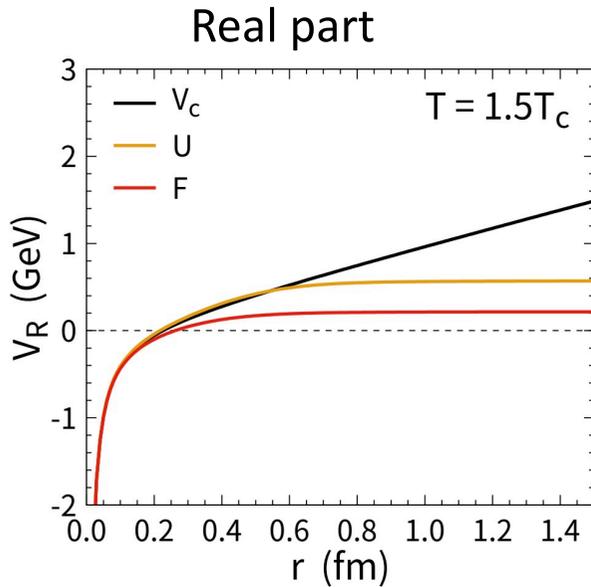
$c\bar{c}$  dipoles move inside QGP

$$\mathbf{R}_{c\bar{c}}(\tau + \Delta\tau) = \mathbf{R}_{c\bar{c}} + \mathbf{v}_{c\bar{c}} \cdot \Delta\tau$$

# Charmonium in p-Pb collisions

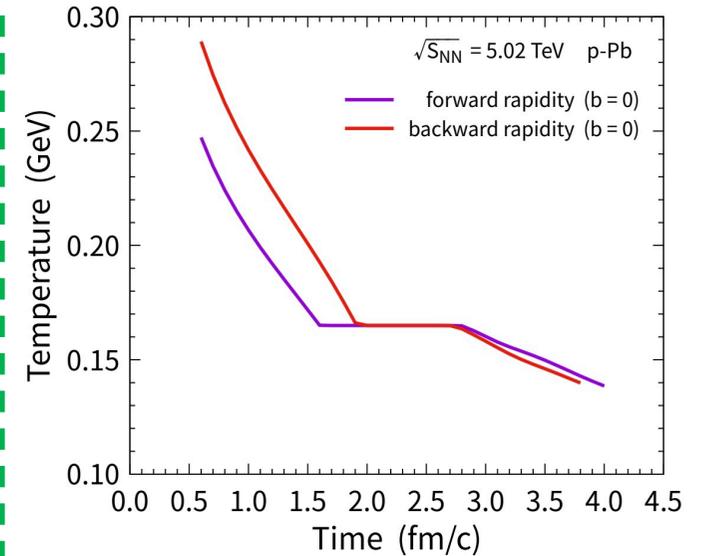
- Is charmonium **1S and 2S states color screened** (weak potential) in the **small collision system** ?

Color screening V.S. Inelastic scatterings



$$F(T, r) = -\frac{\alpha}{r} [e^{-\mu r} + \mu r] - \frac{\sigma}{2^{3/4} \Gamma[3/4]} \left(\frac{r}{\mu}\right)^{1/2} K_{1/4}[(\mu r)^2] + \frac{\sigma}{2^{3/2} \mu} \frac{\Gamma[1/4]}{\Gamma[3/4]}$$

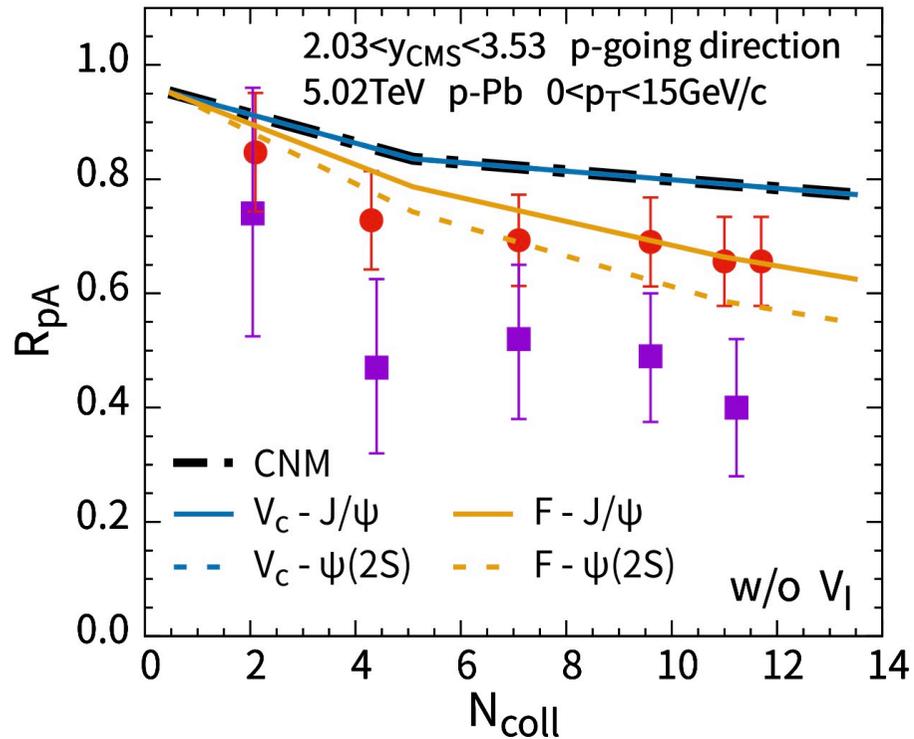
$$V_I(T, \bar{r}) = -i T (a_1 \bar{r} + a_2 \bar{r}^2)$$



**Hot medium in p-Pb ( $x=y=0$ )**

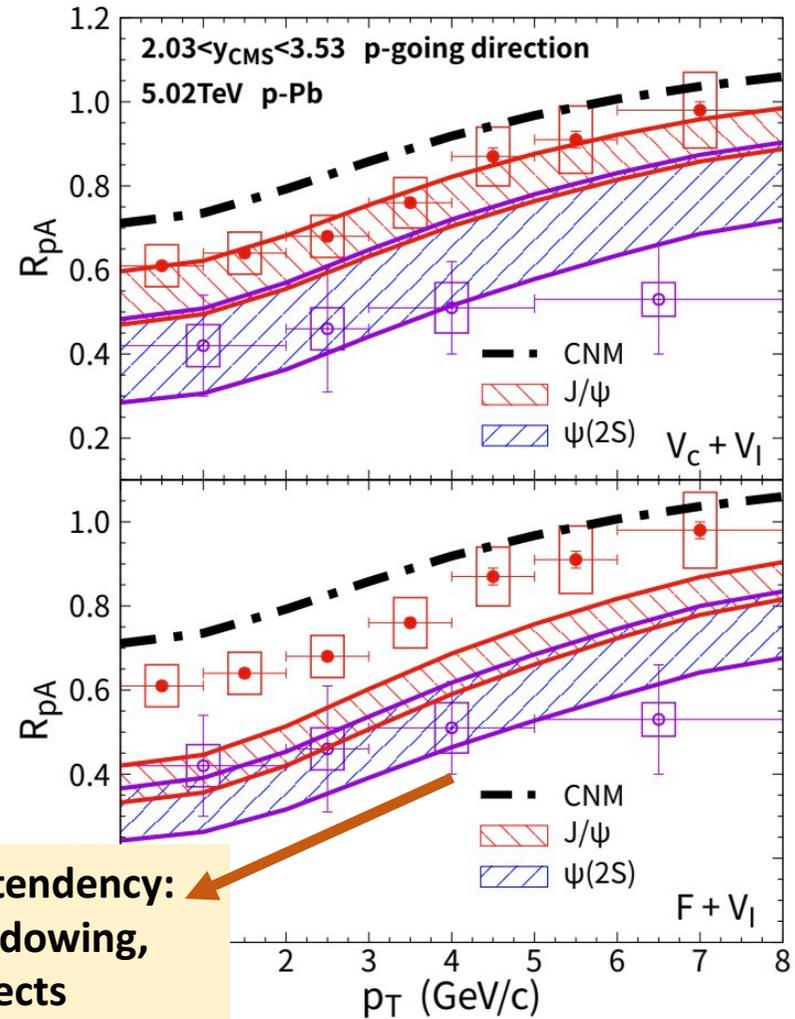
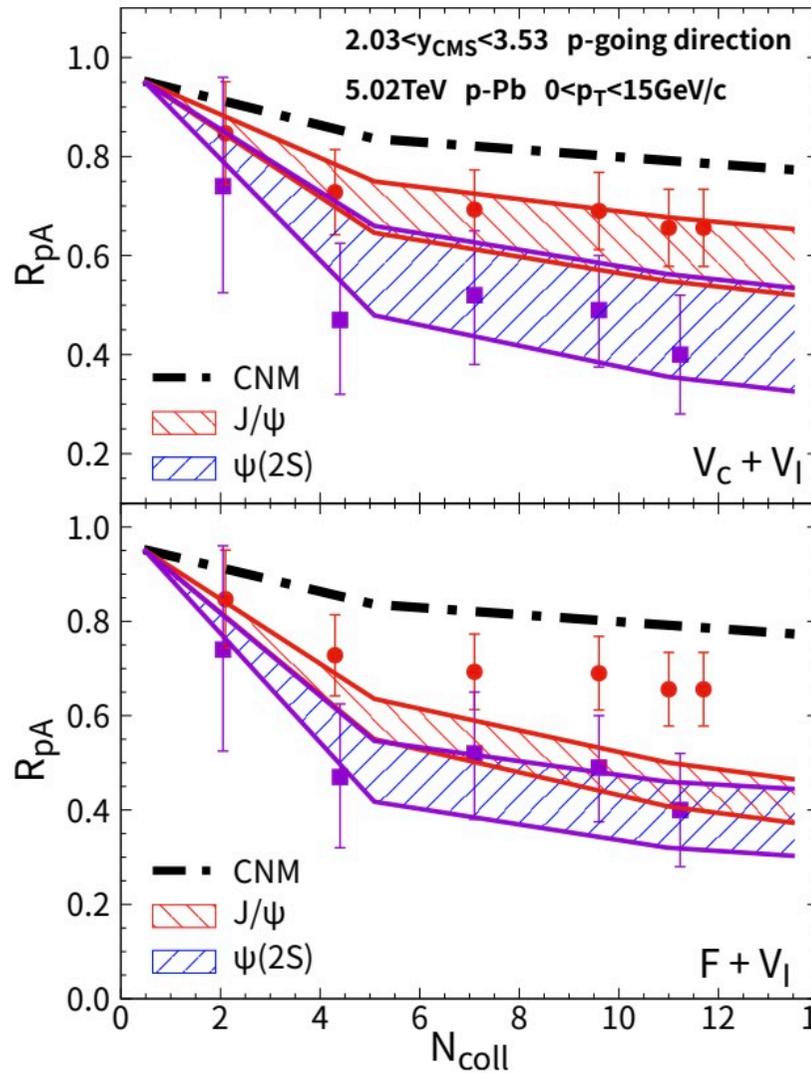
2+1 dimensional ideal hydrodynamic equations

# Charmonium in p-Pb collisions



**Only color screening effect  
+ cold nuclear effect  
(Cronin+shadowing)**

# Charmonium in p-Pb collisions



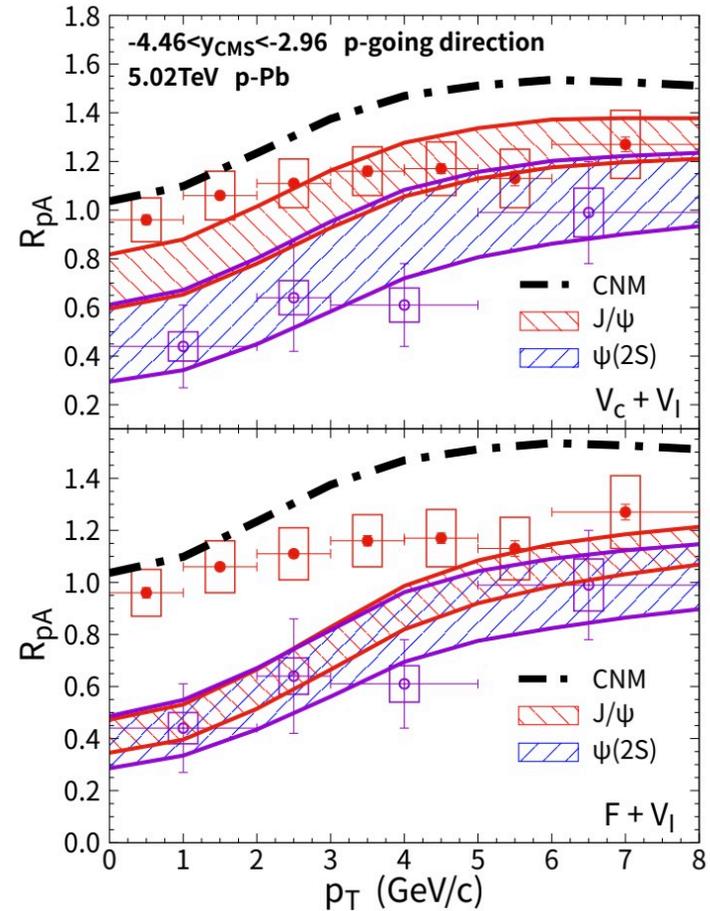
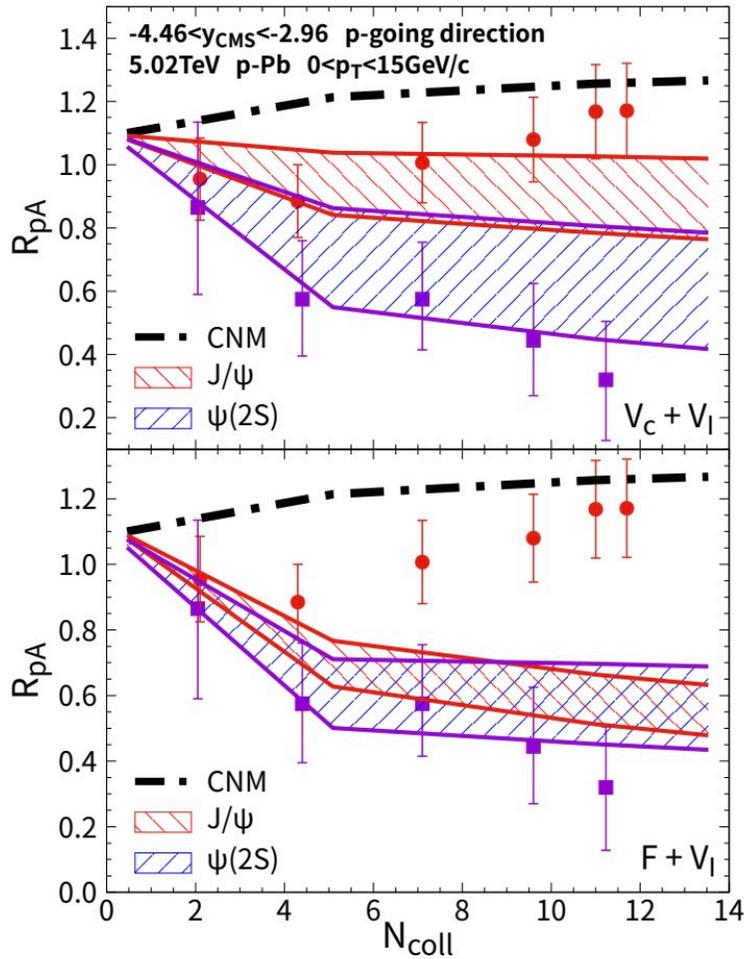
Increasing tendency:  
Cronin, shadowing,  
leakage effects

Band comes from the uncertainty in  $V_I$

- $R_{pA}$  as a function of  $N_{coll}$
- $R_{pA}$  as a function of  $p_T$

Very **weak** in-medium potential  $V=F$   
**Strong** in-medium potential  $V=V_c$

# Charmonium in p-Pb collisions



Backward rapidity

- $R_{pA}$  as a function of  $N_{\text{coll}}$
- $R_{pA}$  as a function of  $p_T$

Strong potential (in the limit  $V=U$ )  
 can explain data relatively well

# Bottomonium in Pb-Pb collisions

- Initial momentum distribution in pp

$$\frac{dN_{pp}^{\Upsilon}}{d\phi p_T dp_T} = \frac{(n-1)}{\pi(n-2)\langle p_T^2 \rangle_{pp}} \left[ 1 + \frac{p_T^2}{(n-2)\langle p_T^2 \rangle_{pp}} \right]^{-n}$$

$$\langle p_T^2 \rangle = (80, 55, 28) (GeV/c)^2$$

At 5020, 2760, 200 GeV

$$n = 2.5$$

- Direct yields of bottomonium states at 5.02 TeV

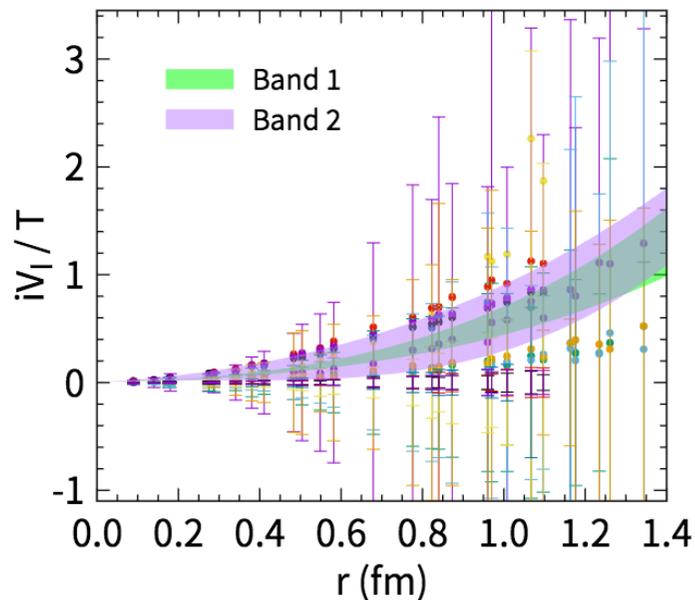
State	$\Upsilon(1s)$	$\chi_b(1p)$	$\Upsilon(2s)$	$\chi_b(2p)$	$\Upsilon(3s)$
$\sigma_{\text{exp}}(nb)$	57.6	33.51	19	29.42	6.8
$\sigma_{\text{direct}}(nb)$	37.97	44.2	18.27	37.68	8.21

Medium temperature  
(b=0)

T(5.02TeV)=510 MeV

T(2.76TeV)=484 MeV

T(200GeV)=390 MeV

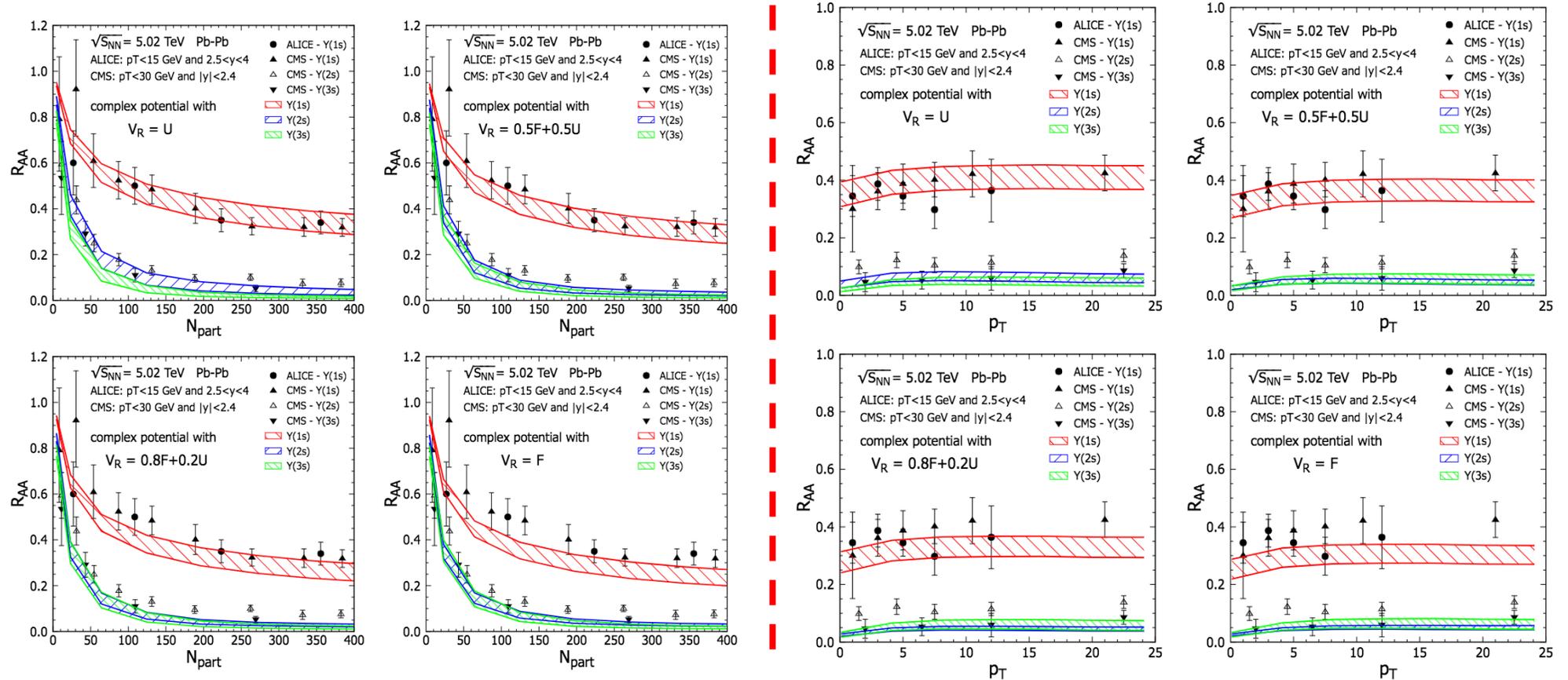


This ratio between different states are also used in 2.76 TeV and 200 GeV

Two kinds of imaginary potential are fitted

- Smaller band: fit the central value and shifted upward slightly to consider partial uncertainty.
- Larger band: one sigma uncertainty is included.

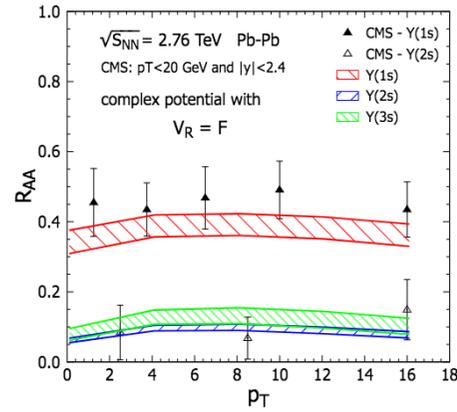
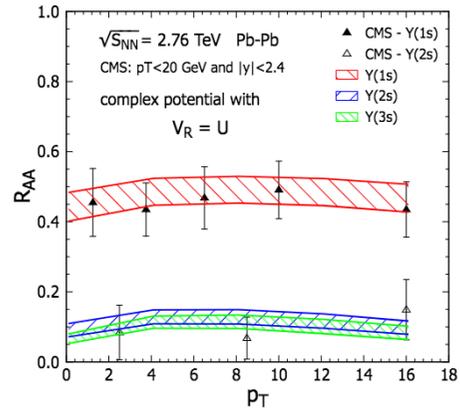
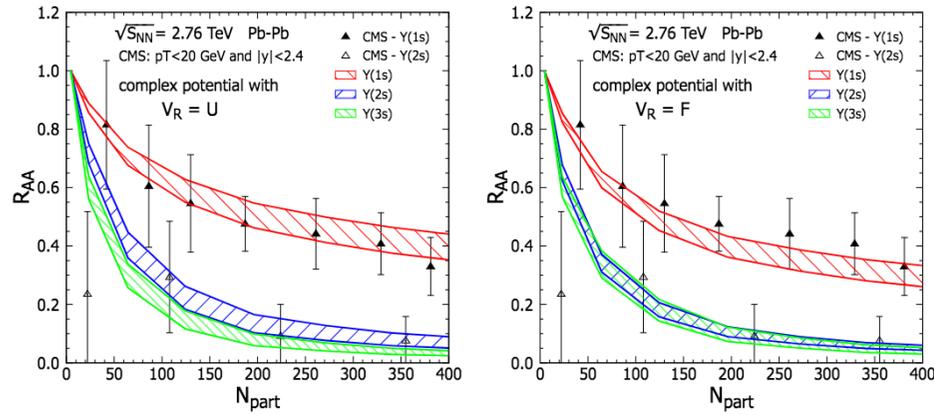
# Bottomonium in Pb-Pb collisions



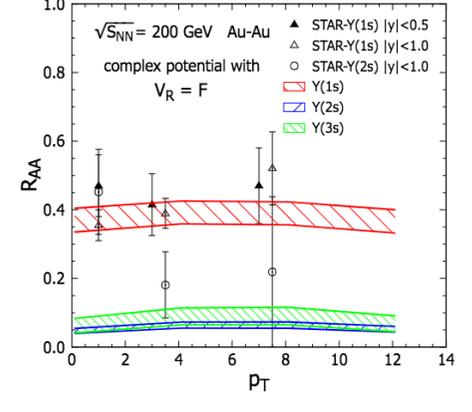
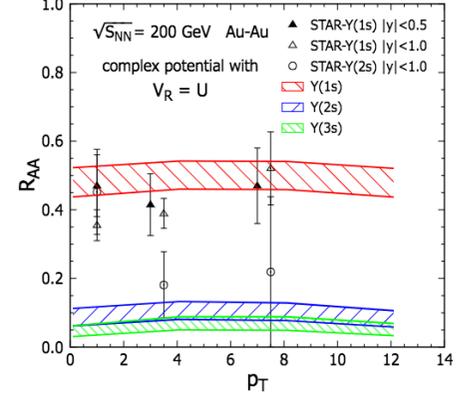
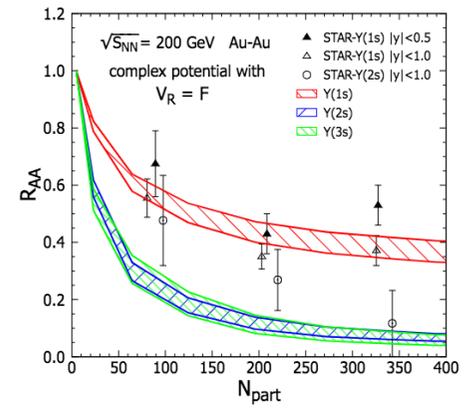
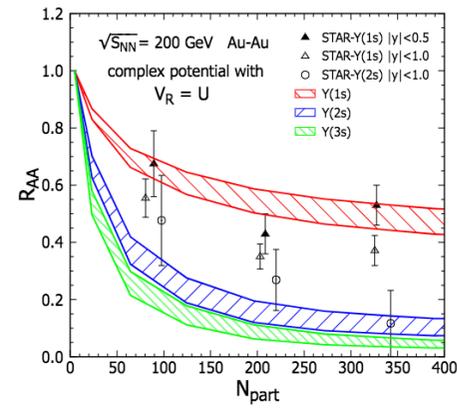
## 5.02 TeV Pb-Pb

- Clear sequential suppression pattern is observed with  $V=U$
- With  $V=F$ , weak potential makes the wave function expand outside.

# Bottomonium in Pb-Pb collisions

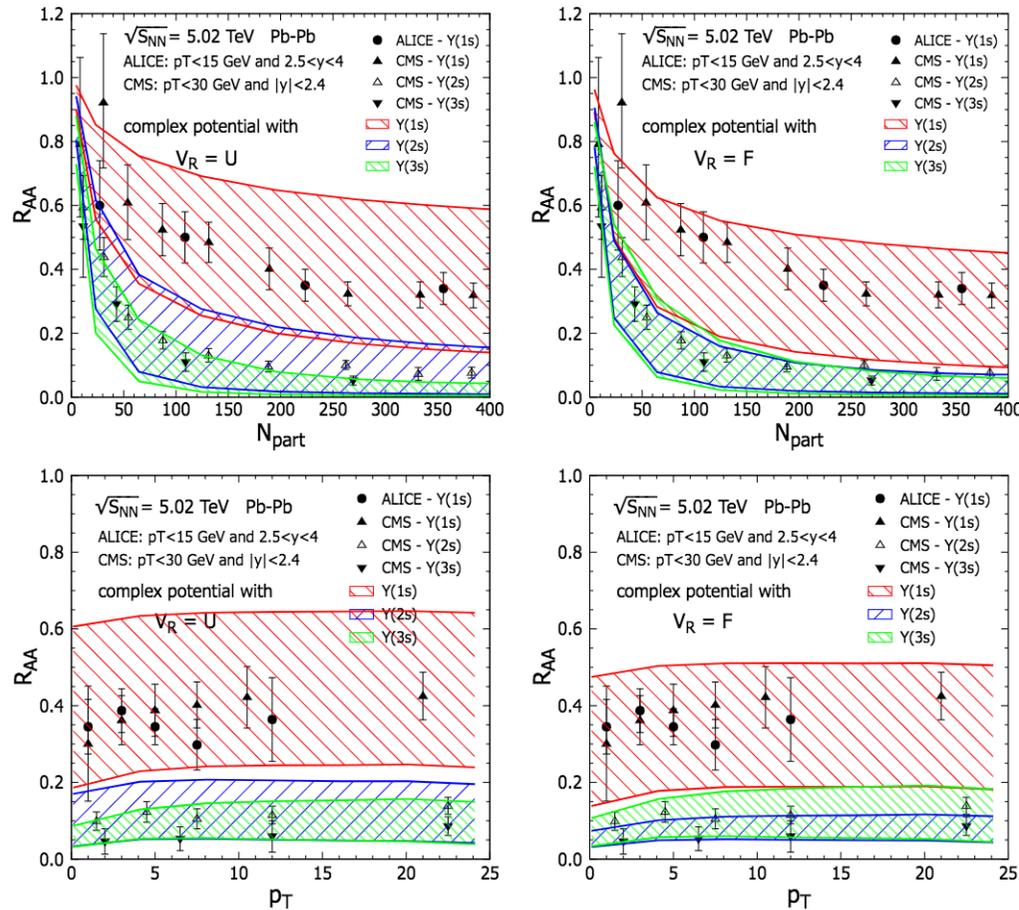


2.76 TeV Pb-Pb

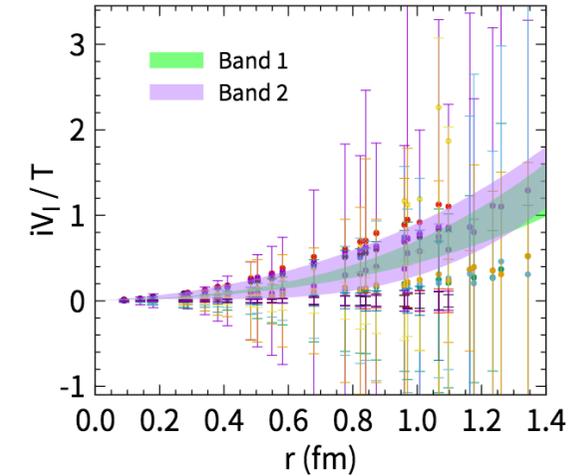


200 GeV Au-Au

# Bottomonium in Pb-Pb collisions



## Calculation with band 2



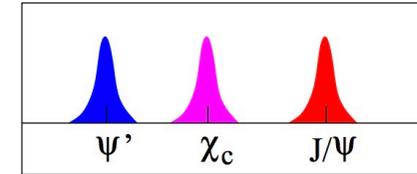
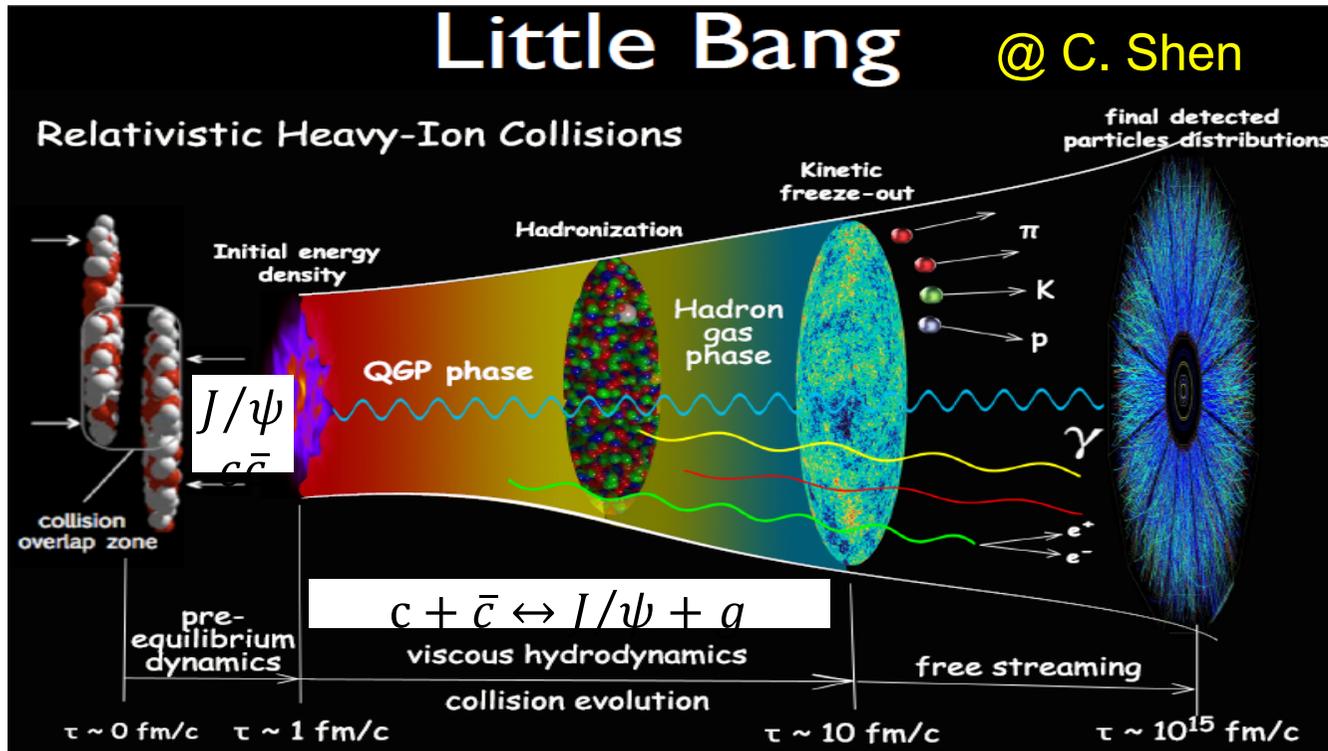
- RAA with larger uncertainty in the imaginary potential.
- The sequential suppression pattern is still observed.
- Using quarkonium data to extract the imaginary potential ?

# Summary

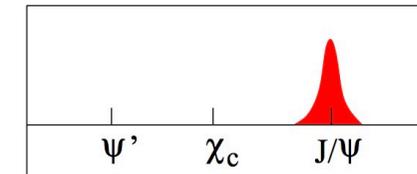
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- We study the charmonium and bottomonium evolutions in **the small (p-Pb) and large (Pb-Pb) collision systems** respectively with the time-dependent Schrodinger equation. Both **color screened effect** and **inelastic scatterings** are included in the real and imaginary potential.
- In small collision system, **color screening effect is expected to be small**. While imaginary potential dominates the suppression.
- In large collision system, **a strong heavy quark potential is still expected** to get the sequential suppression pattern, which contains the quarkonium wave function in the medium.

# Heavy ion collisions and heavy flavors



$T < T_c$



$T \sim 1.1 T_c$

Satz. 2005

- significant **color screening** + **parton inelastic scatterings**