

Role of quark anomalous magnetic moment in chiral phase transition under magnetic field

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Outline

1. Introduction

- QCD phase diagram

2. QCD at temperatures

- Physical observables
- First principle vs effective model (my previous studies)

3. QCD under magnetic field

- Magnetic effect on phase transition
- Our work

4. Summary and outlook

*Note that NO rotation effect in my talk.
Magnetic fields mimic rotation effect.

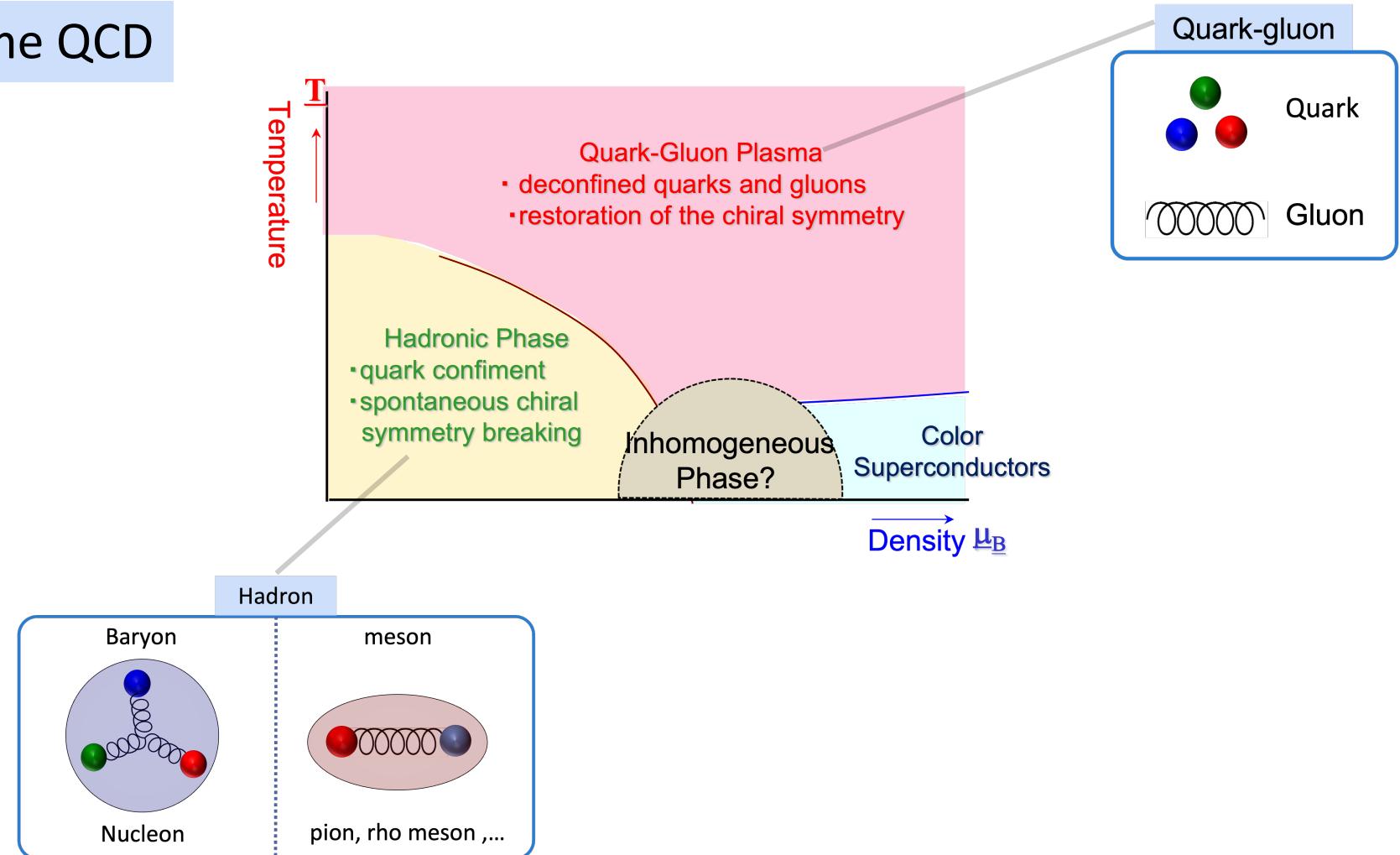
1. Introduction

- QCD phase diagram

QCD phase diagram

1

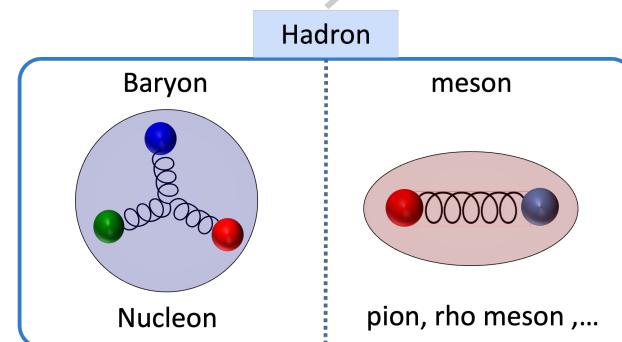
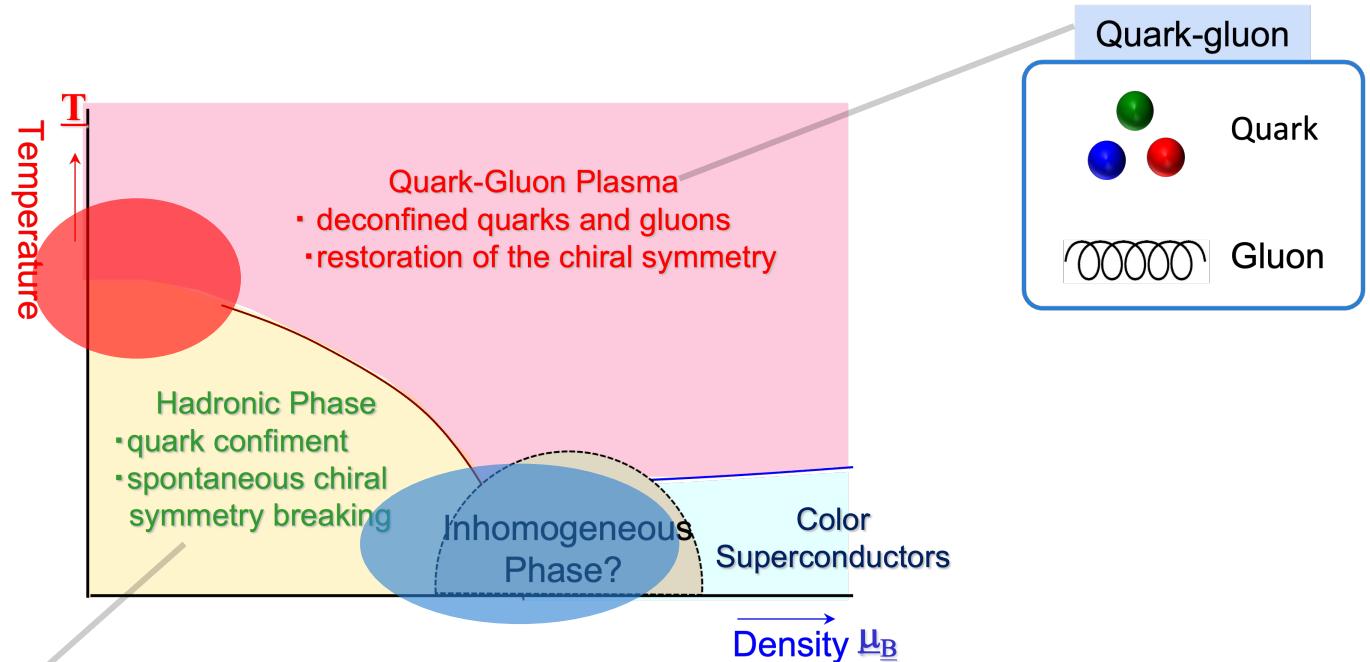
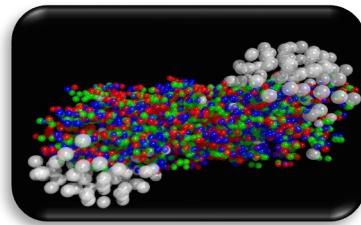
Phase transition in extreme QCD



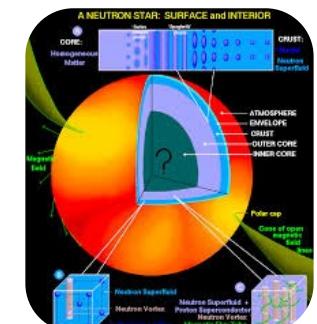
QCD phase diagram

Phase transition in extreme QCD

Extreme temperatures:
heavy ion collisions

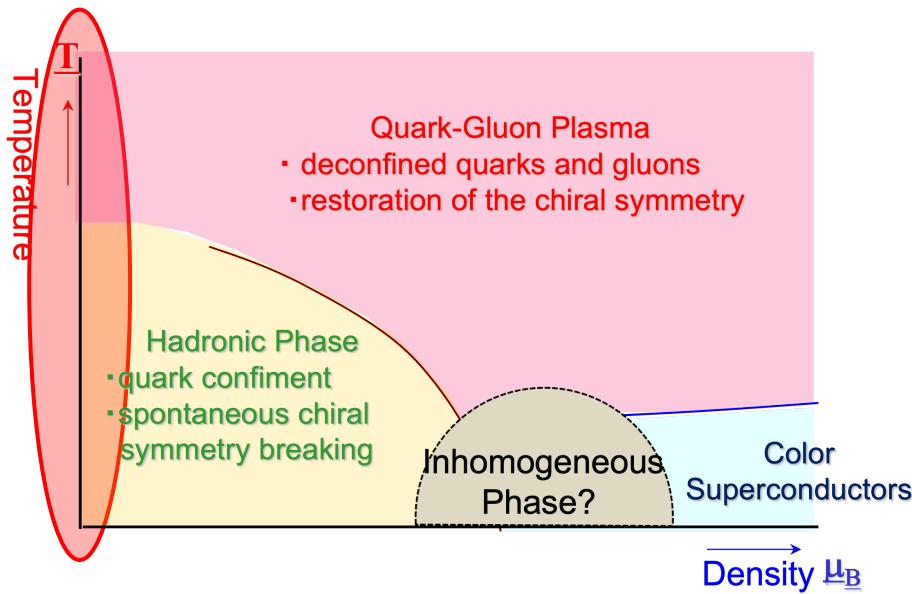


Superdense matter:
neutron star



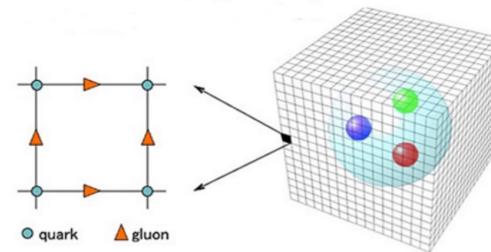
QCD phase diagram

Phase transition in hot QCD



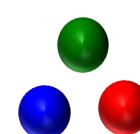
First-principle calculation is powerful tool.

Lattice QCD simulation



Directly solve underlying QCD theory.

$$\mathcal{L}_{\text{QCD}} = \bar{q}(i\gamma^\mu D_\mu - m_l)q - \frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu}$$



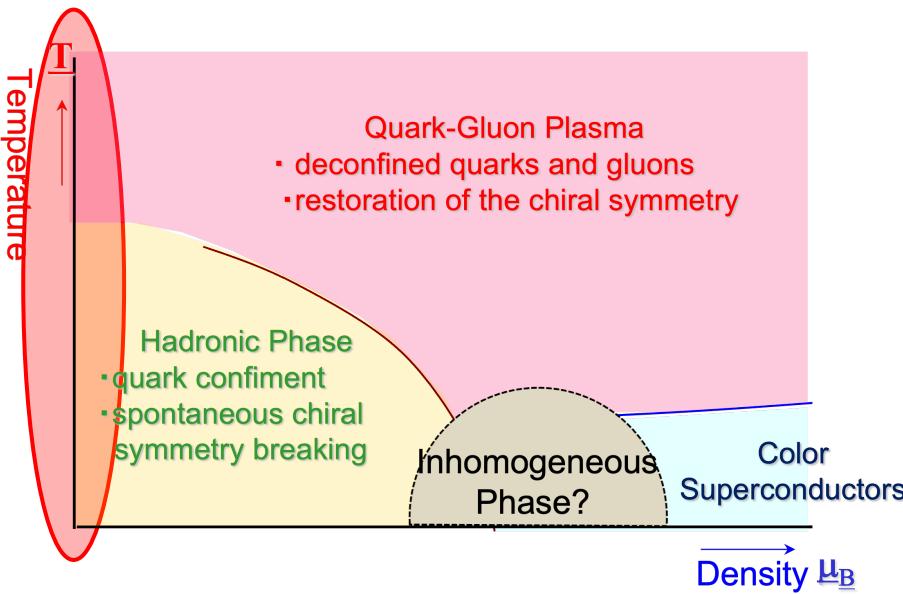
Quark



Gluon

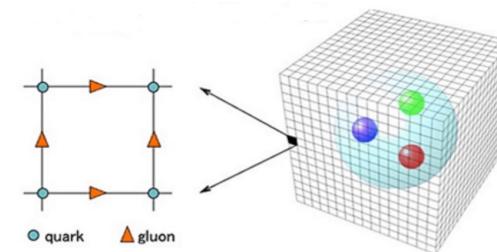
QCD phase diagram

Phase transition in hot QCD



First-principle calculation is powerful tool.

Lattice QCD simulation



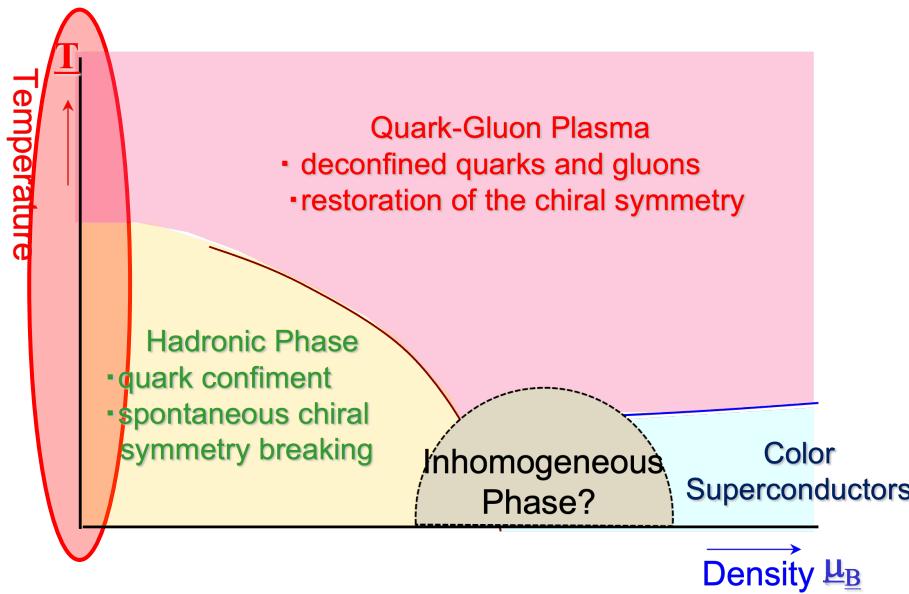
Physical quantities have been observed:

- Quark condensate
- Susceptibilities

$\left(\begin{array}{c} \text{Meson susceptibility} \\ \text{Topological susceptibility} \end{array} \right)$

QCD phase diagram

Phase transition in hot QCD



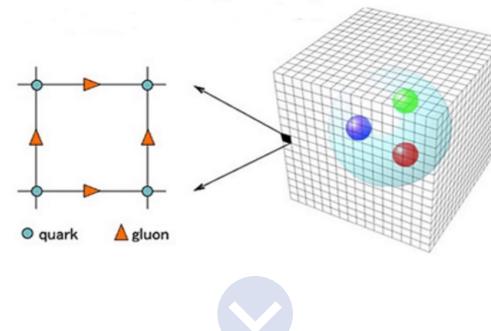
Physical quantities have been observed:

- Quark condensate
- Susceptibilities

Meson susceptibility
Topological susceptibility

First-principle calculation is powerful tool.

Lattice QCD simulation



Thermal phase transition is observed: crossover.

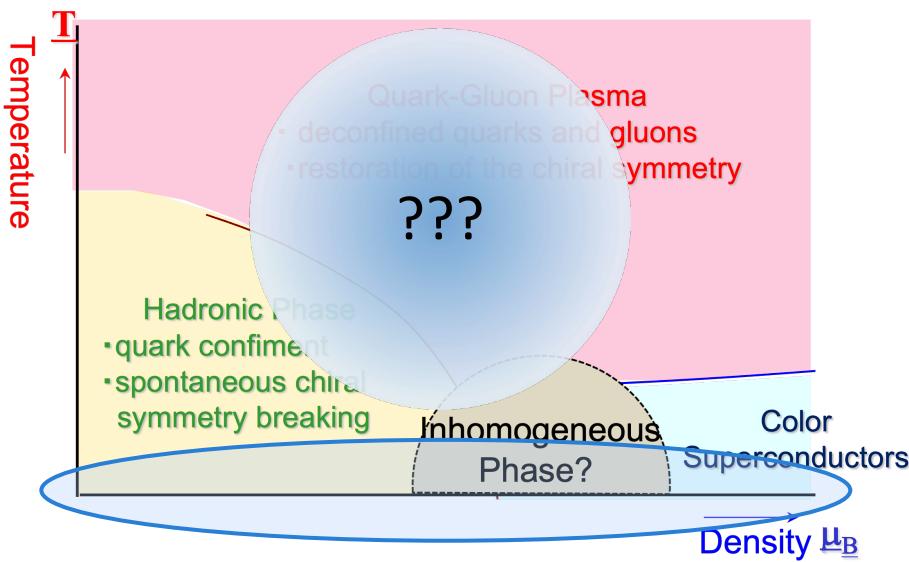


Part of phase diagram has been clarified.

QCD phase diagram

3

Phase transition in dense QCD...



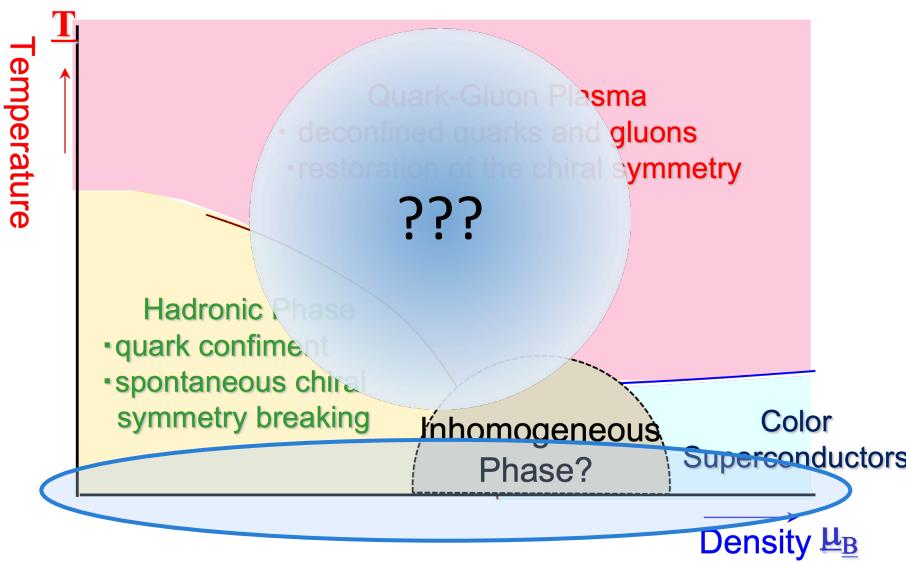
First-principle calculation is powerful tool.

But...

QCD phase diagram

3

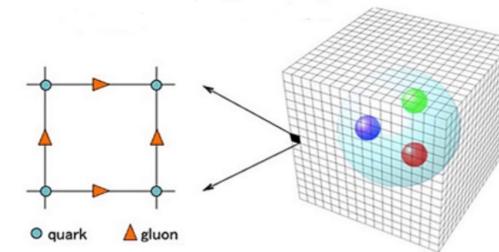
Phase transition in dense QCD...



First-principle calculation is powerful tool.

But...

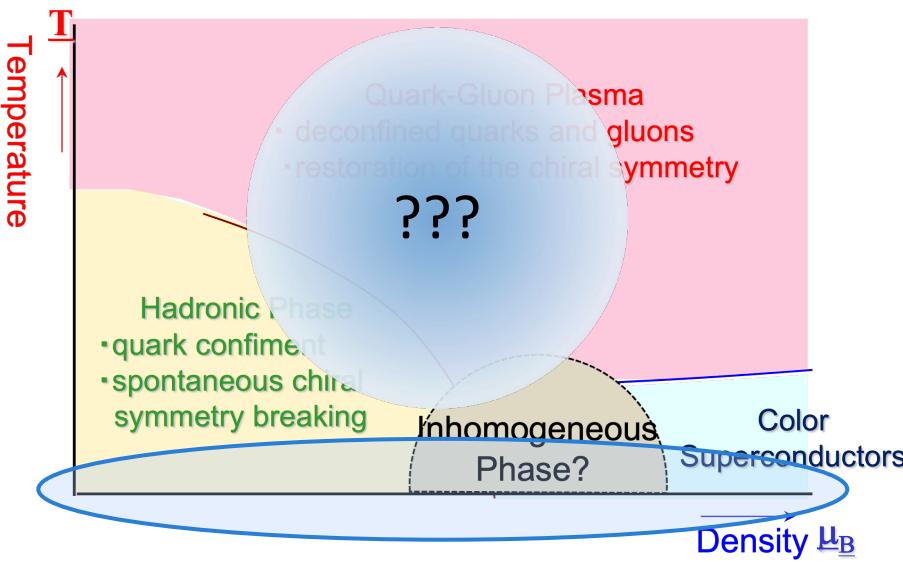
Cannot be applied to μ_B -axis.



This is due to sign problem.

QCD phase diagram

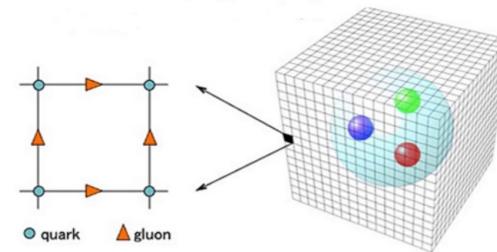
Phase transition in dense QCD...



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But...

Cannot be applied to μ_B -axis.



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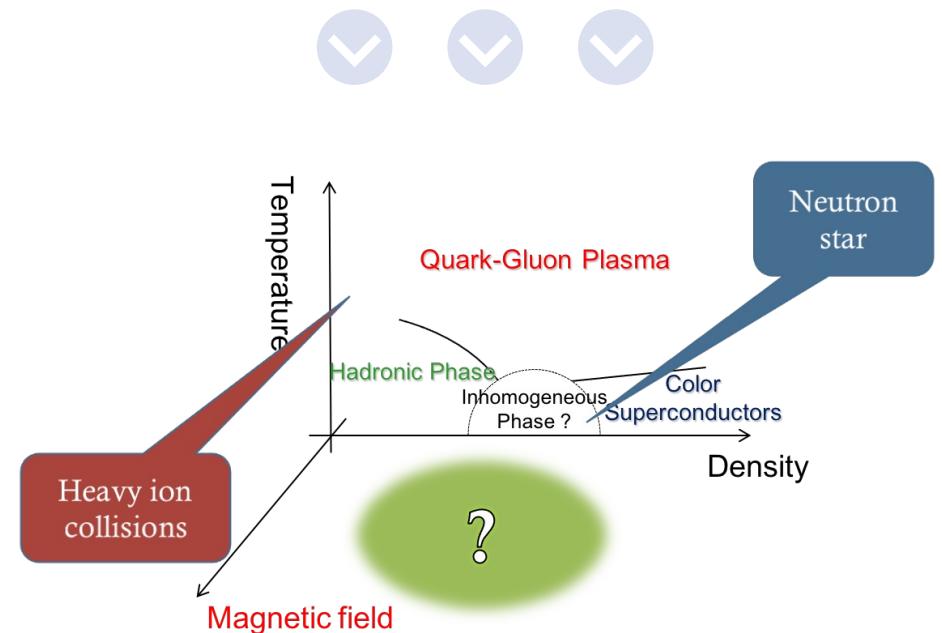
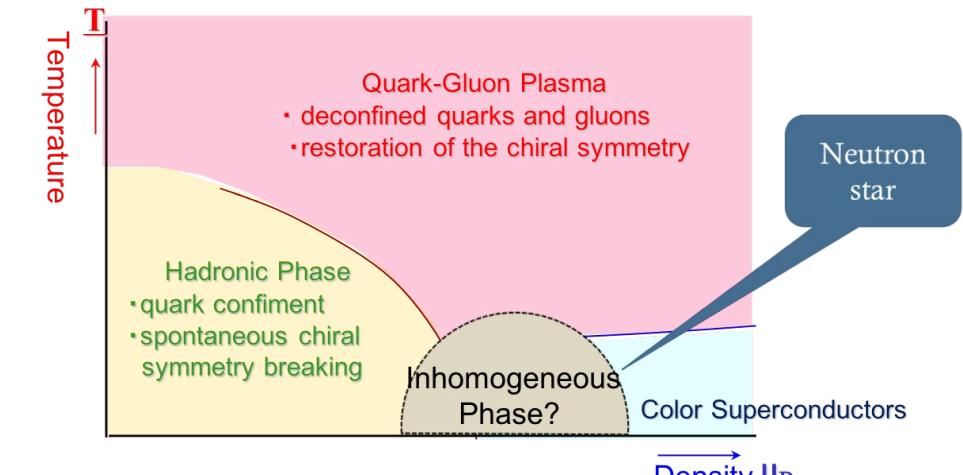
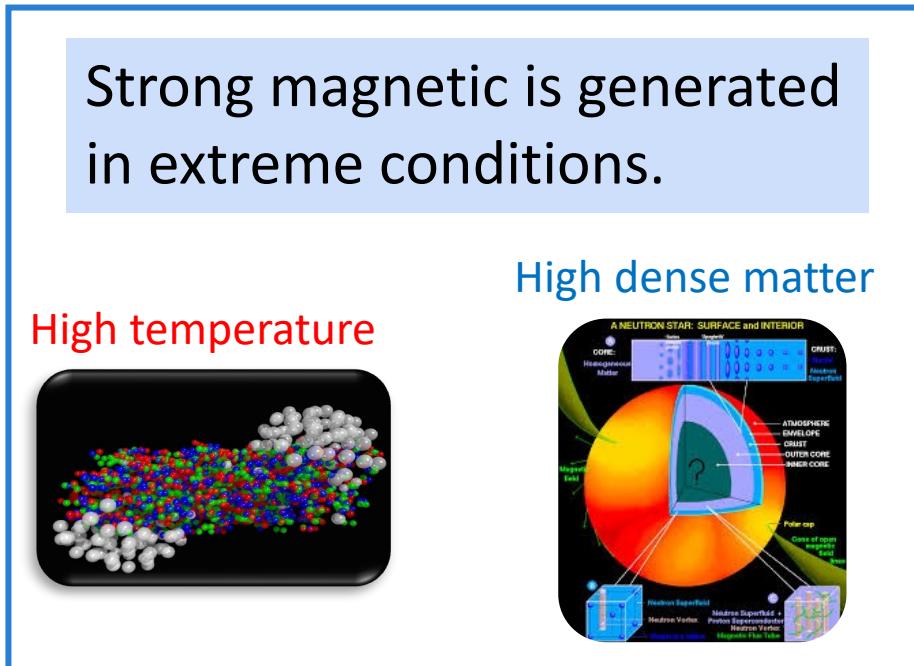
Phase diagram is still unclear...



Effective model analyses are also useful.

QCD phase diagram

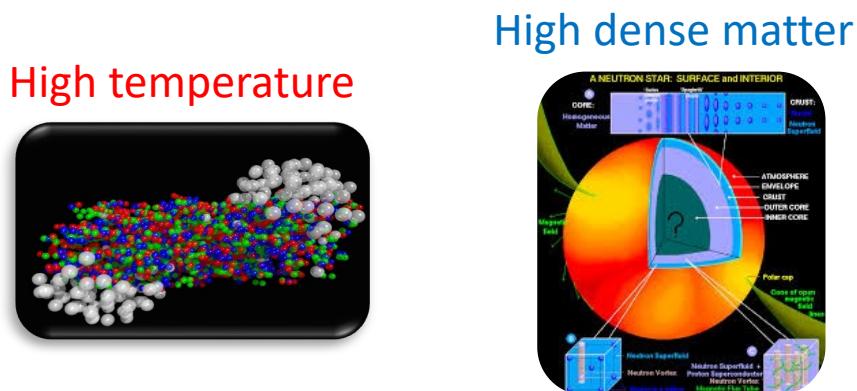
4



QCD phase diagram

4

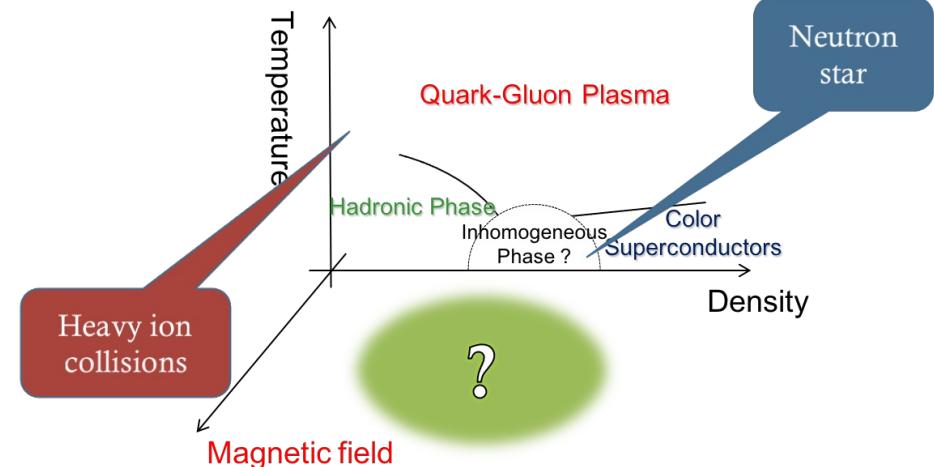
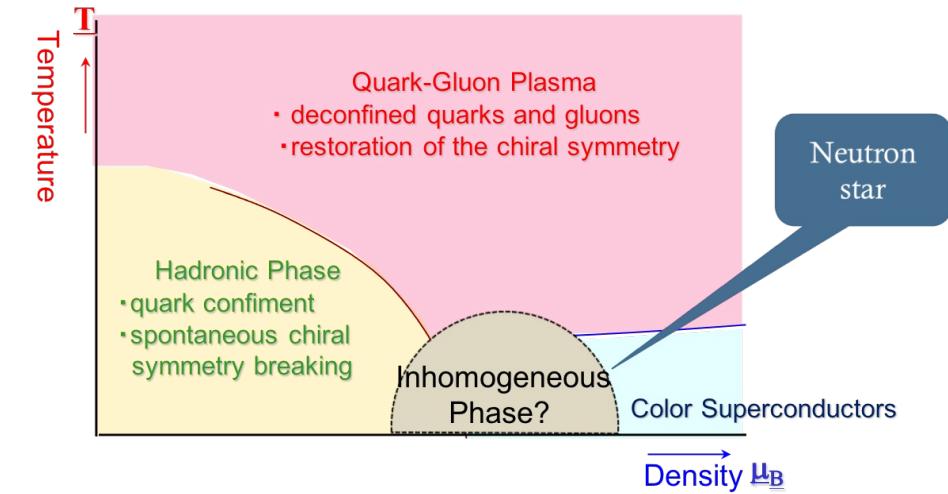
Strong magnetic is generated in extreme conditions.



Phase diagram becomes a rich structure.



Much attention has been drawn to exploring QCD phase diagram.

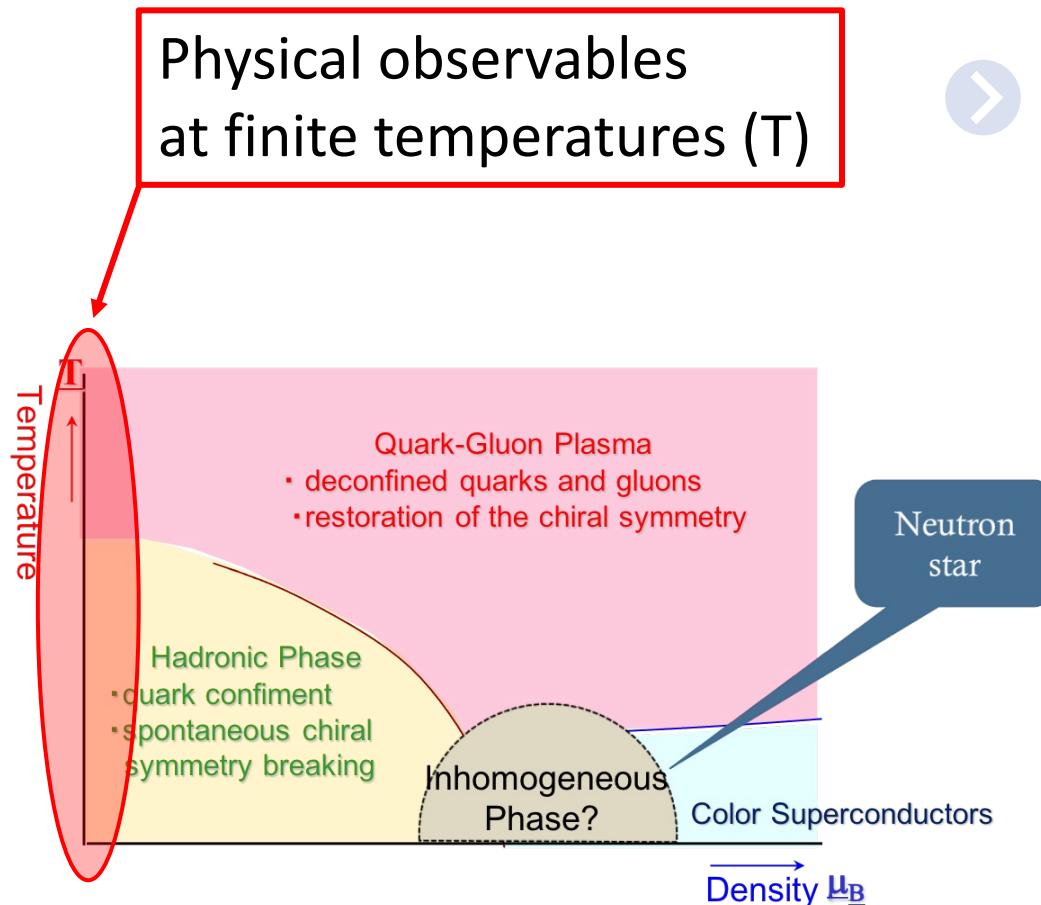


2. QCD at temperatures

- Physical observables
- First principle vs effective model (my previous studies)

QCD at finite-T

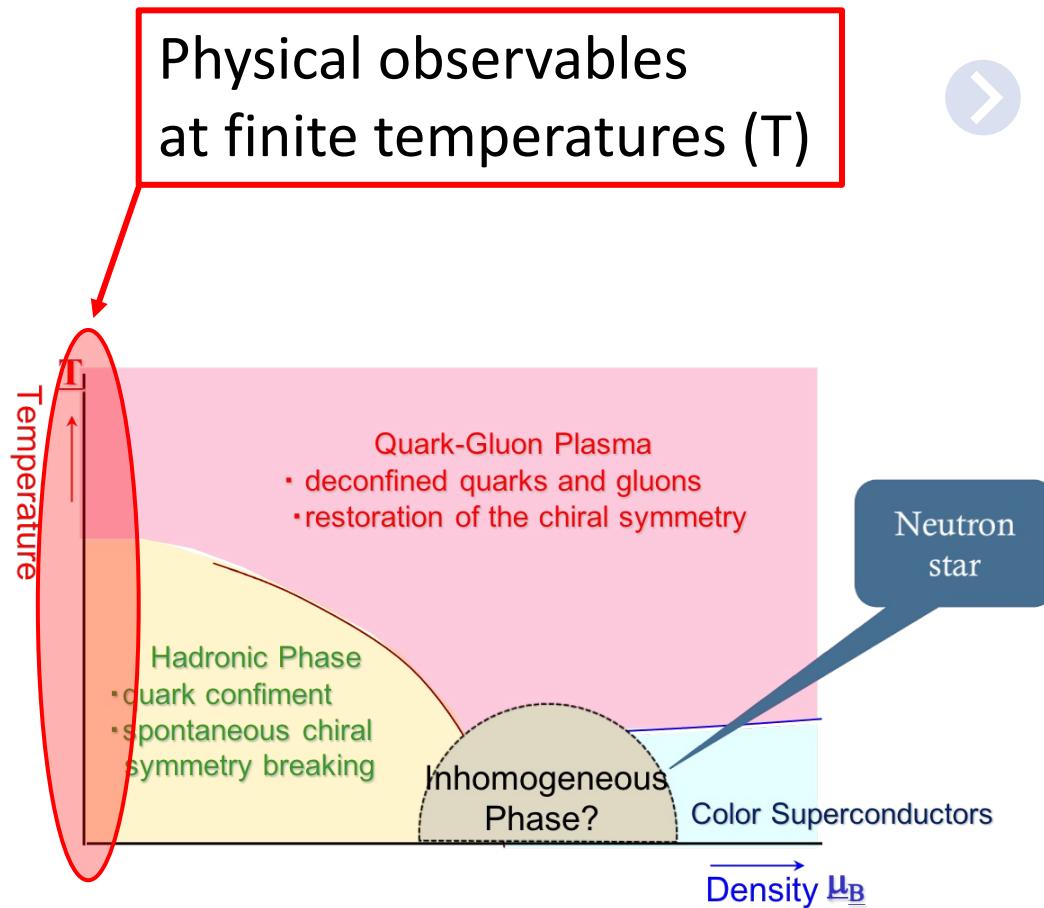
5



- Quark condensate
- Meson susceptibility
- Topological susceptibility

QCD at finite-T

5



- Quark condensate

Order parameter for spontaneous chiral symmetry breaking:
it is responsible to the origin of hadron masses.

- Meson susceptibility

• Meson property (mass) can be read from susceptibility.

- Topological susceptibility

• It is related to QCD topological structure.

QCD at finite-T

6

Lattice QCD observations

Quark condensate

- JHEP06(2009)088

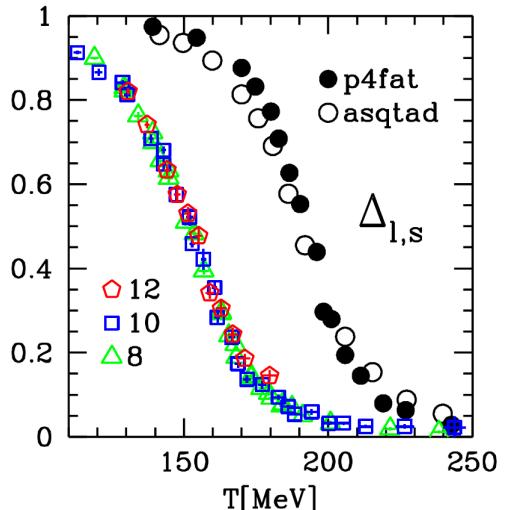
Meson susceptibility

- PRL 113 (2014) 8, 082001

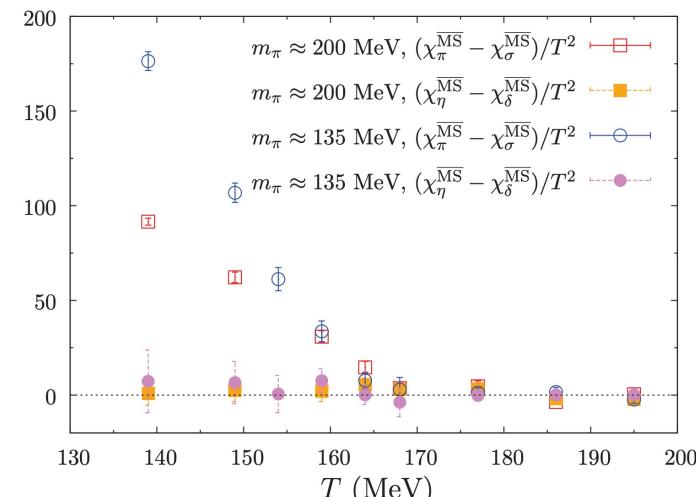
Topological susceptibility

- C. Bonati et al, JHEP 11, 170 (2018), 1807.07954.
- S. Borsanyi et al., Nature 539, no. 7627, 69 (2016).
- P. Petreczky et al, Phys. Lett. B 762, 498-505 (2016)

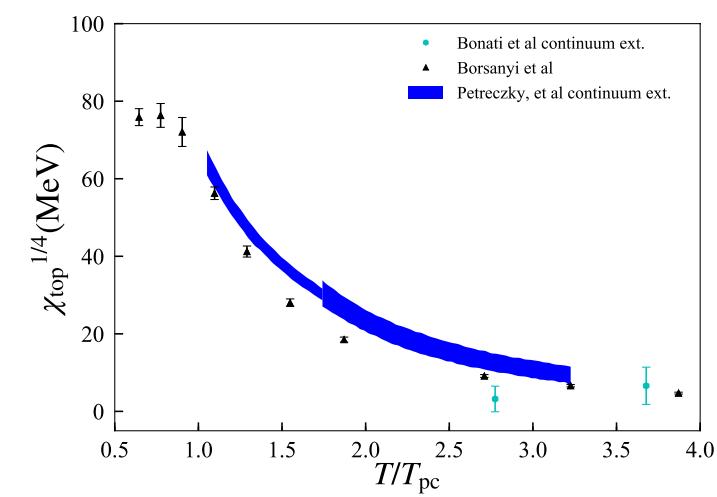
Quark condensate



Meson susceptibility



Topological susceptibility



QCD at finite-T

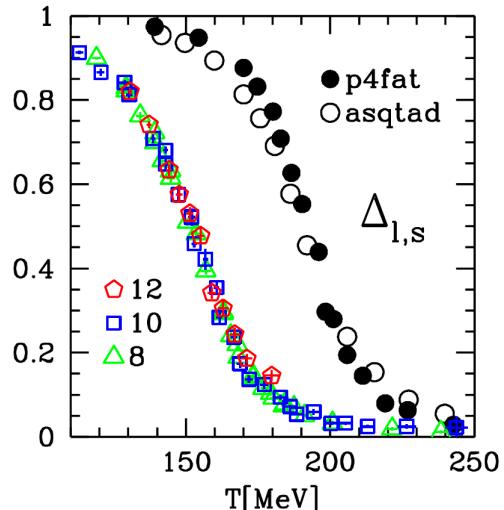
6

Lattice QCD
observations

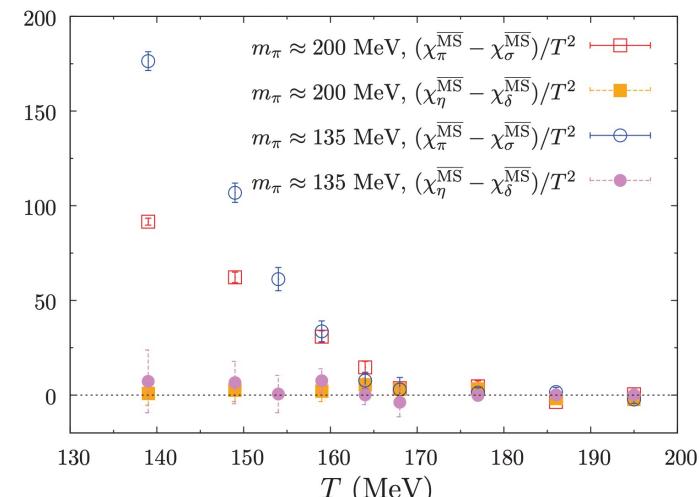


What do lattice data tell us?

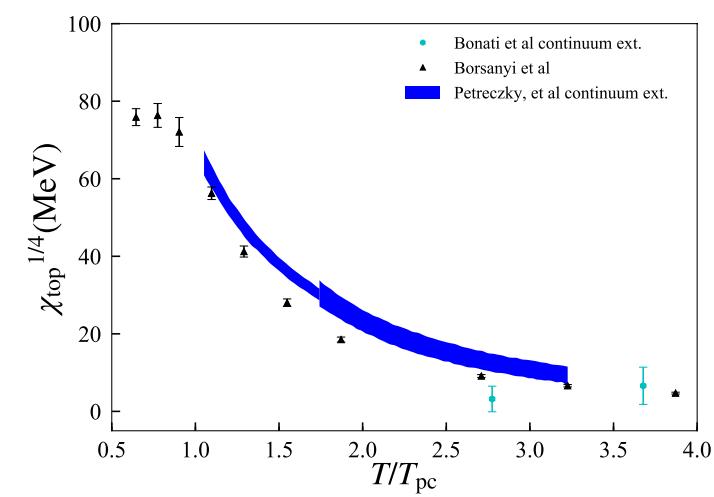
Quark condensate



Meson susceptibility



Topological susceptibility



QCD at finite-T

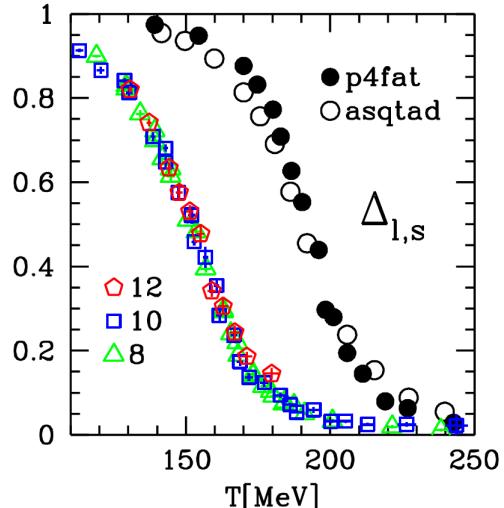
6

Lattice QCD
observations

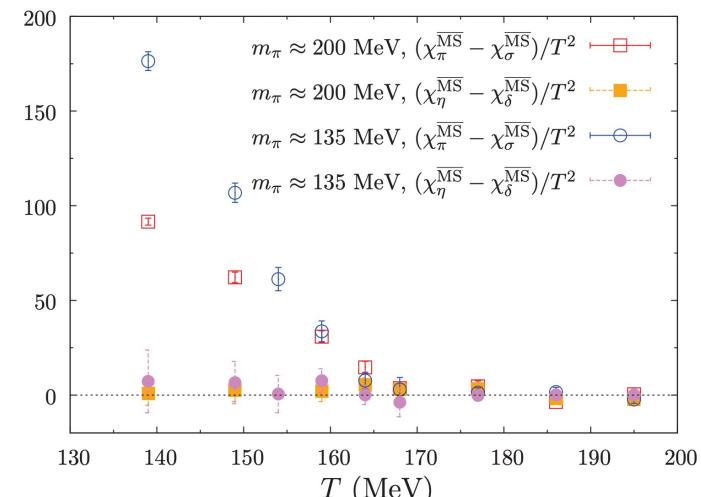
What do lattice data tell us?

Effective model is useful
for understanding data.

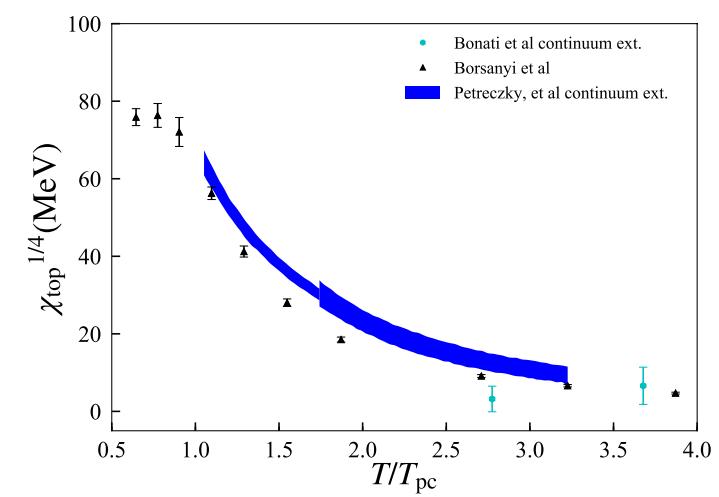
Quark condensate



Meson susceptibility



Topological susceptibility



Effective model at finite-T

7

QCD at low energy

Spontaneous chiral symmetry breaking



$$\text{U(1) axial: } \partial_\mu j_A^\mu = \boxed{2i \sum_f \bar{q}^f m_f \gamma_5 q^f} + \boxed{N_f \frac{g^2}{16\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu}}$$

$$\text{Chiral SU(2): } \partial_\mu j_A^{a\mu} = \boxed{i\bar{q} \left\{ M, \frac{\tau^a}{2} \right\} \gamma_5 q}$$

Effective model at finite-T

7

QCD at low energy



Spontaneous chiral symmetry breaking



Nambu-Jona-Lasinio (NJL) model

$$\text{U(1) axial: } \partial_\mu j_A^\mu = \boxed{2i \sum_f \bar{q}^f m_f \gamma_5 q^f} + \boxed{N_f \frac{g^2}{16\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu}}$$

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$$\begin{aligned} \mathcal{L} &= \bar{q}(i\gamma_\mu \partial^\mu - \boxed{\mathbf{m}})q + \mathcal{L}_{4f} + \boxed{\mathcal{L}_{\text{KMT}}} \\ \mathcal{L}_{4f} &= \frac{g_s}{2} \sum_{a=0}^8 [(\bar{q}\lambda^a q)^2 + (\bar{q}i\gamma_5 \lambda^a q)^2] \\ \mathcal{L}_{\text{KMT}} &= g_D [\det_{i,j} \bar{q}_i (1 + \gamma_5) q_j + \text{h.c.}] \end{aligned}$$

- NJL is based on **symmetry structure** of quarks.

Effective model at finite-T

8

Nambu-Jona-Lasinio (NJL) model

Is based on **chiral symmetry**.

$$\mathcal{L} = \bar{q}(i\gamma_\mu\partial^\mu - \mathbf{m})q + \mathcal{L}_{4f} + \mathcal{L}_{\text{KMT}}$$

$$\mathcal{L}_{4f} = \frac{g_s}{2} \sum_{a=0}^8 [(\bar{q}\lambda^a q)^2 + (\bar{q}i\gamma_5\lambda^a q)^2]$$

$$\mathcal{L}_{\text{KMT}} = g_D \left[\det_{i,j} \bar{q}_i (1 + \gamma_5) q_j + \text{h.c.} \right]$$

*Model parameters are fixed
to provide physical meson masses.

We evaluate...

- Quark condensate
- Meson susceptibility
- Topological susceptibility.

Chuan-Xin Cui, Jin-Yang Li, Shinya Matsuzaki,
[M.K.](#), Akio Tomiya, *PRD* 105 (2022) 11, 114031

Effective model at finite-T

8

Nambu-Jona-Lasinio (NJL) model

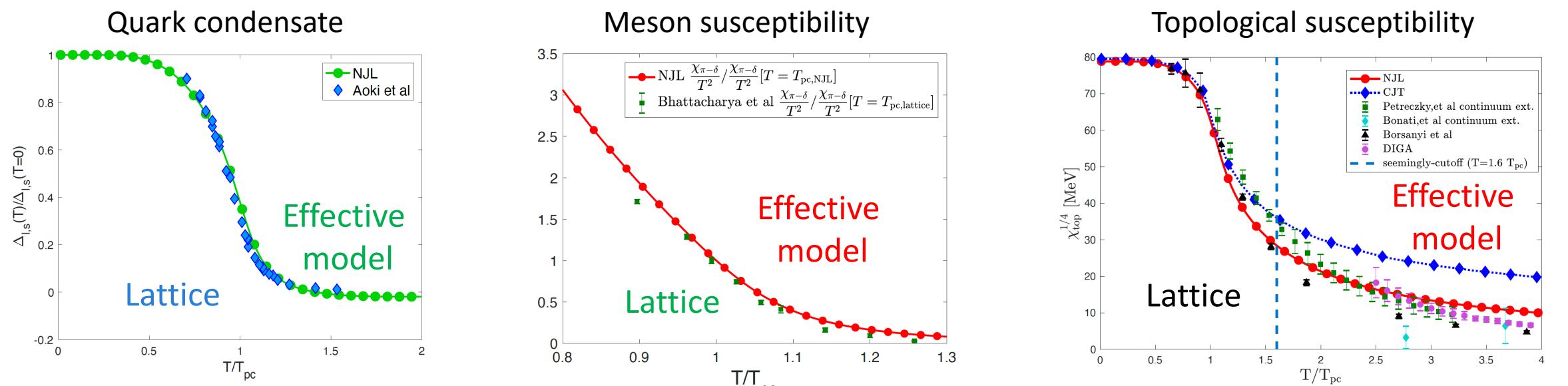


NJL results are in good agreement with lattice observations.

We evaluate...

- Quark condensate
- Meson susceptibility
- Topological susceptibility.

Chuan-Xin Cui, Jin-Yang Li, Shinya Matsuzaki,
M.K., Akio Tomiya, *PRD* 105 (2022) 11, 114031



QCD and chiral symmetry

8

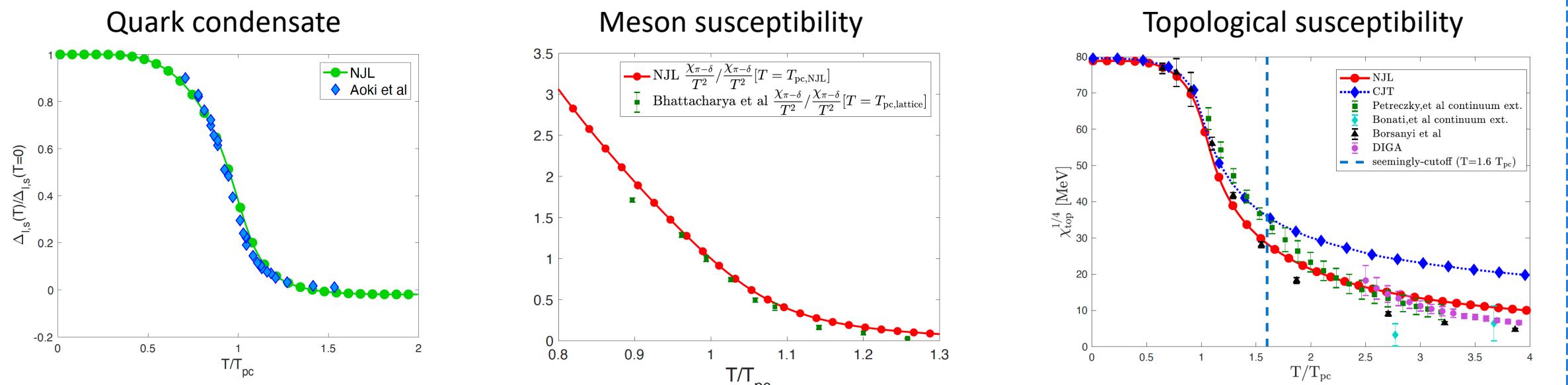
Lattice QCD
observations



What do lattice data tell us?



Effective model analysis
based on symmetry



QCD and chiral symmetry

8

Lattice QCD observations

QCD vacuum

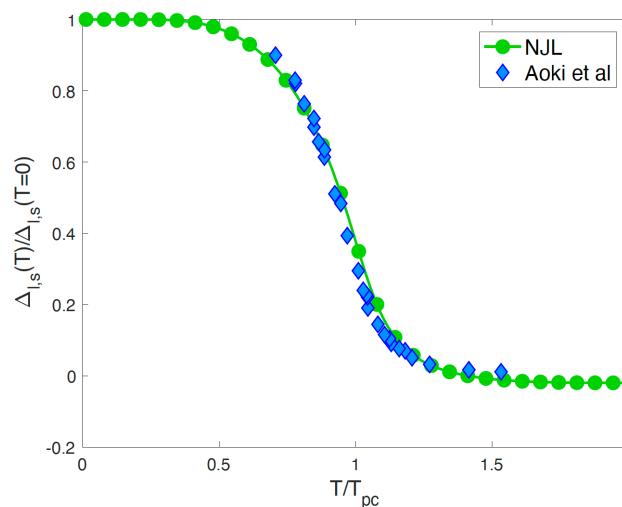
Meson property

Topological structure

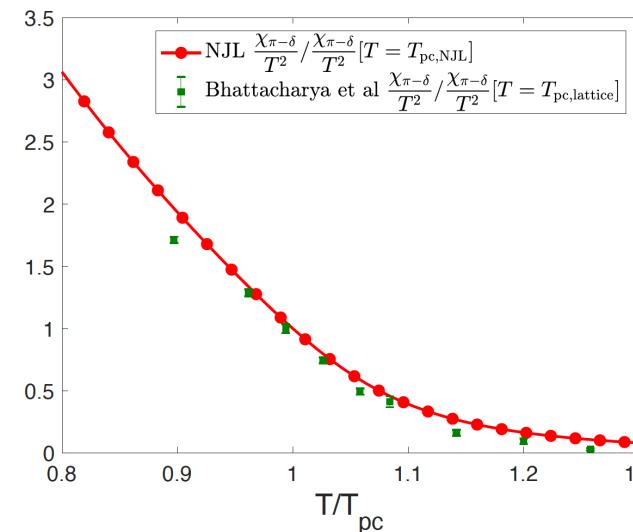
Effective model analysis based on symmetry

Are governed by chiral symmetry.

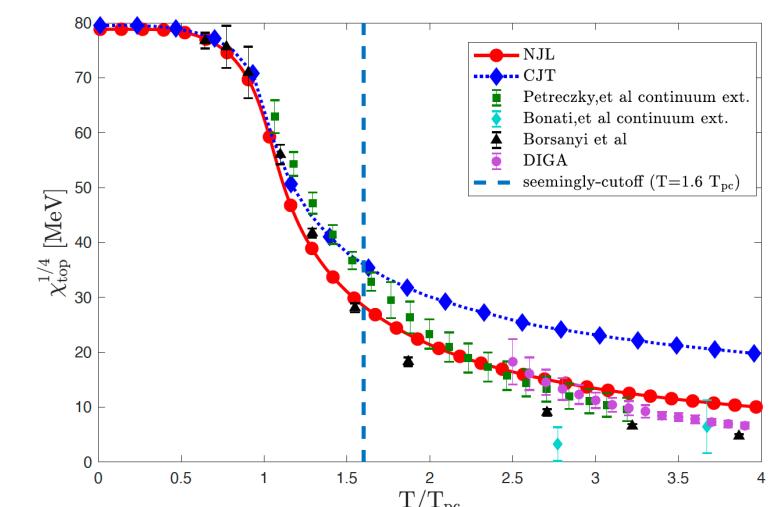
Quark condensate



Meson susceptibility



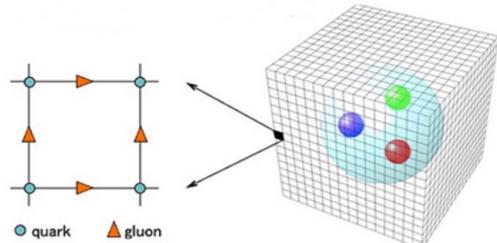
Topological susceptibility



3. QCD under magnetic field

- Magnetic effect on phase transition
- Our work

Lattice QCD simulation



How do magnetic fields
affect the chiral symmetry?

Effective model analysis

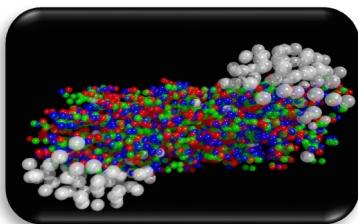
- NJL model...

QCD phase diagram at eB

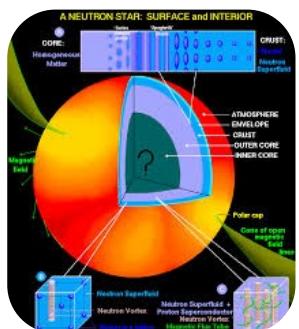
9

Strong magnetic is generated in extreme conditions.

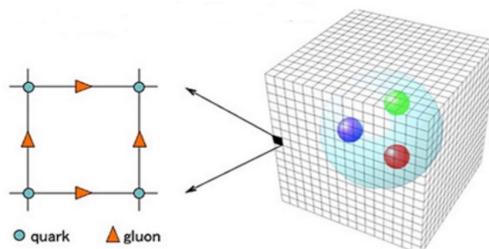
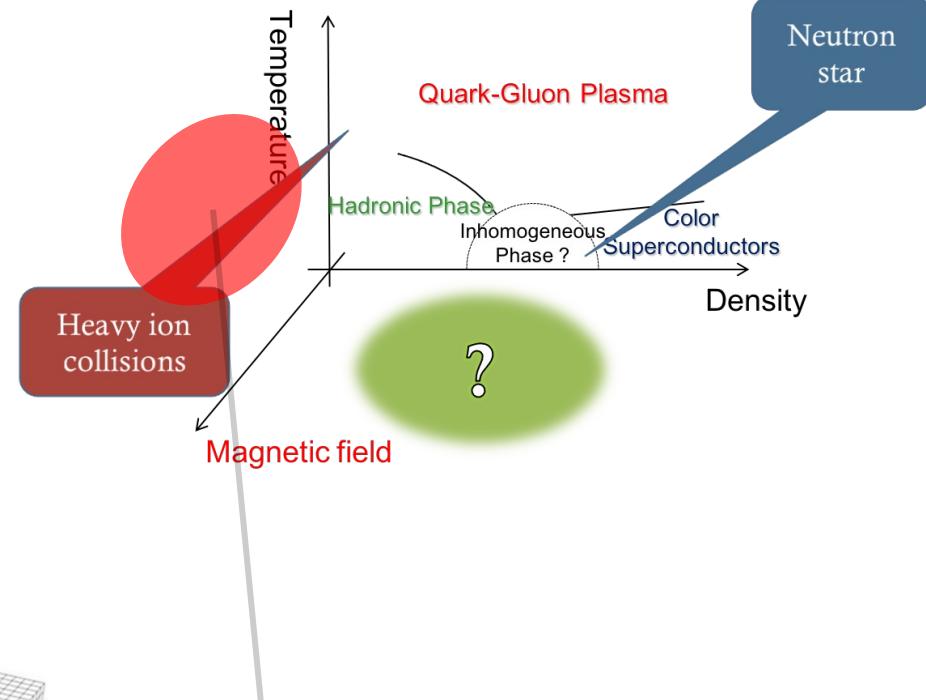
High temperature



High dense matter



Phase diagram with magnetic field

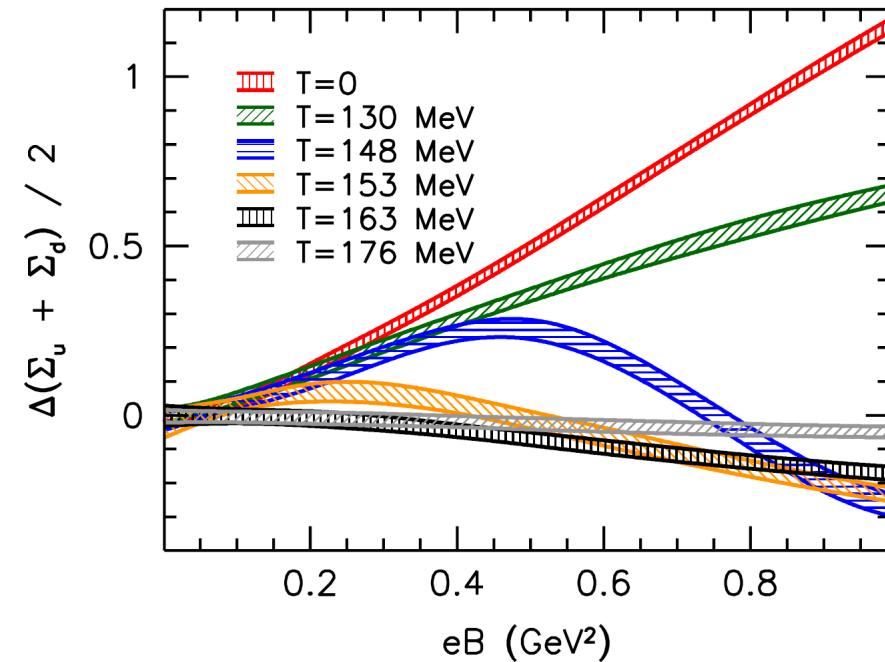


Lattice QCD simulation work at finite T and eB.

Quark condensate in eB

10

Lattice observation



Magnetic effect on (subtracted) quark condensate
at finite temperatures

Phys.Rev.D 86 (2012) 071502

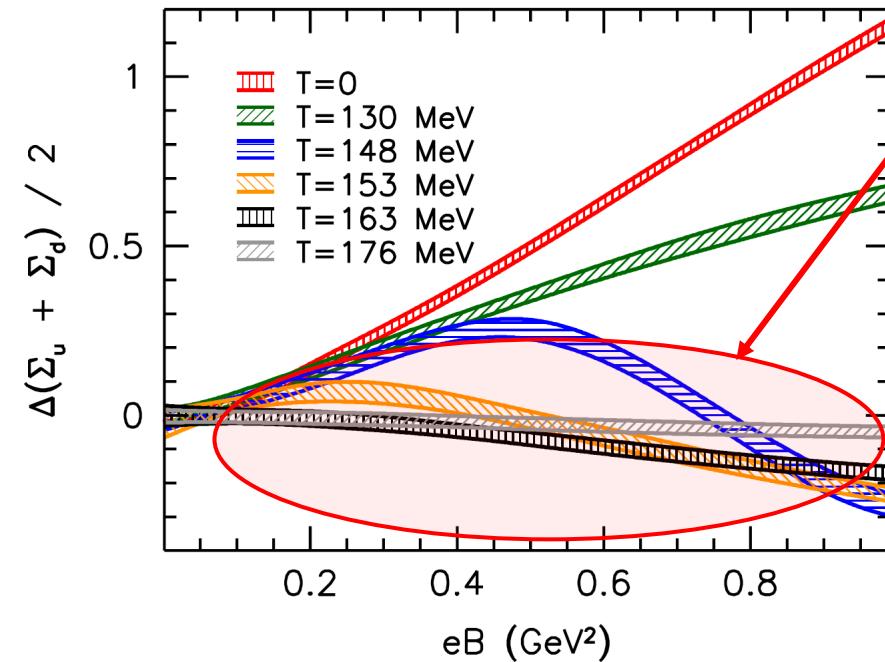
Normalized quark condensate: $\Sigma_{u,d}(B, T) = \frac{2m_{ud}}{M_\pi^2 F^2} [\bar{\psi}\psi_{u,d}(B, T) - \bar{\psi}\psi_{u,d}(0, 0)] + 1$

Subtracted quark condensate: $\Delta\Sigma_{u,d}(B, T) = \Sigma_{u,d}(B, T) - \Sigma_{u,d}(0, T)$

Quark condensate in eB

10

Lattice observation



Magnetic effect on (subtracted) quark condensate
at finite temperatures

Around T_{pc} , quark condensate is suppressed.



✓ eB promotes the chiral restoration.

in contrast to low-temperature results

Phys.Rev.D 86 (2012) 071502

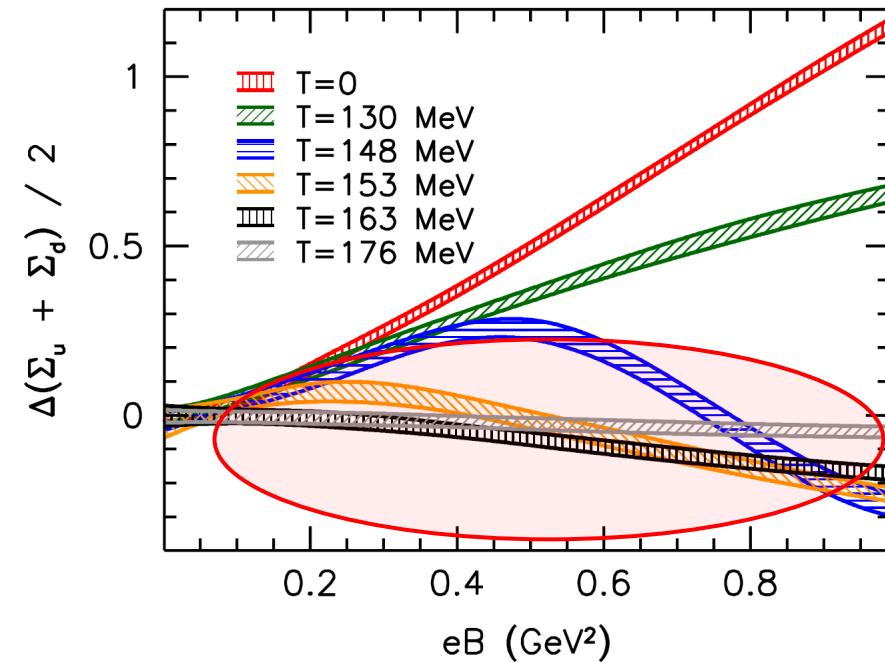
Normalized quark condensate: $\Sigma_{u,d}(B, T) = \frac{2m_{ud}}{M_\pi^2 F^2} [\bar{\psi}\psi_{u,d}(B, T) - \bar{\psi}\psi_{u,d}(0, 0)] + 1$

Subtracted quark condensate: $\Delta\Sigma_{u,d}(B, T) = \Sigma_{u,d}(B, T) - \Sigma_{u,d}(0, T)$

T-eB phase diagram

11

Lattice observation

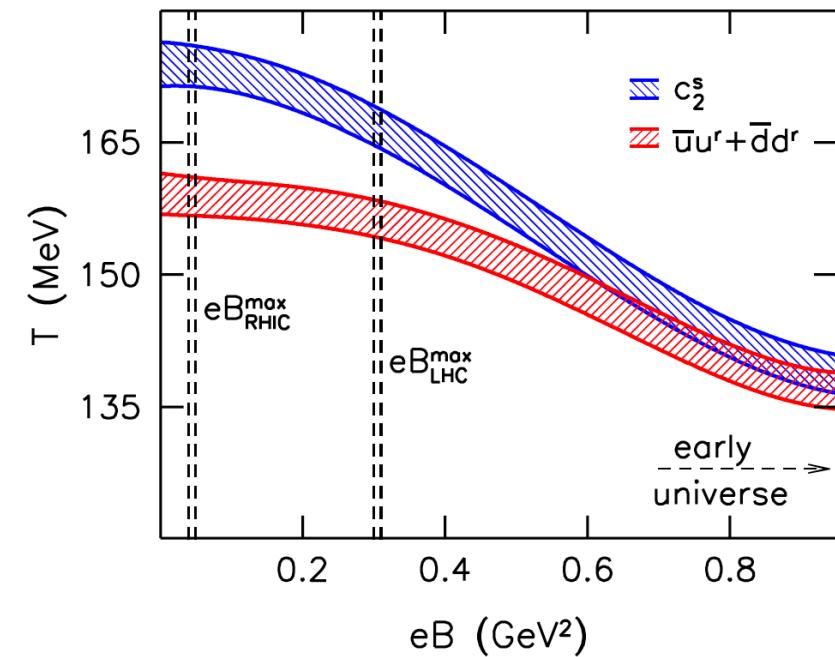


Phys.Rev.D 86 (2012) 071502

We can describe
T-eB phase diagram.



Phase diagram (Lattice observation)



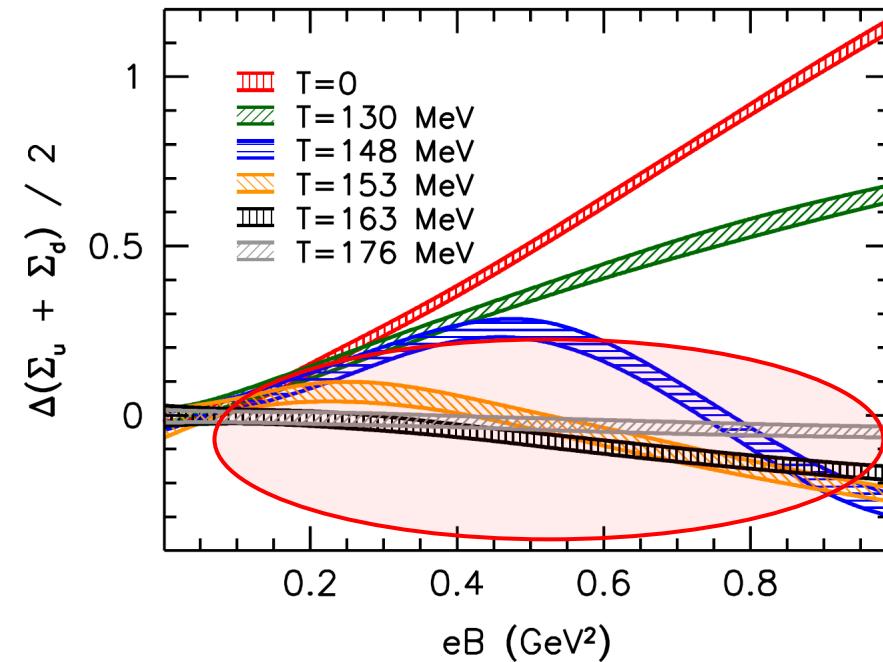
JHEP 02 (2012) 044

Magnetic field reduces T_{pc} .

T-eB phase diagram

11

Lattice observation

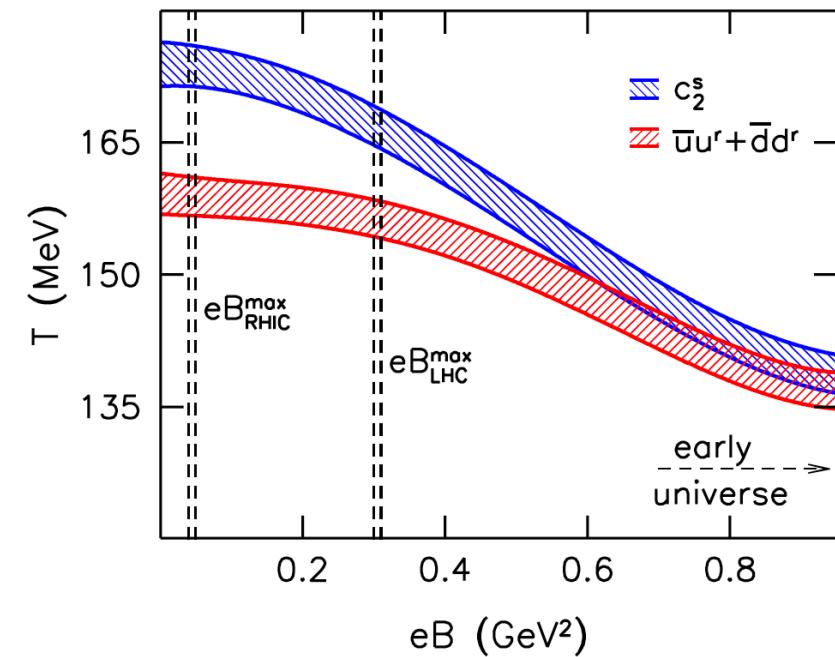


Phys. Rev. D 86 (2012) 071502

We can describe
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Phase diagram (Lattice observation)



JHEP 02 (2012) 044

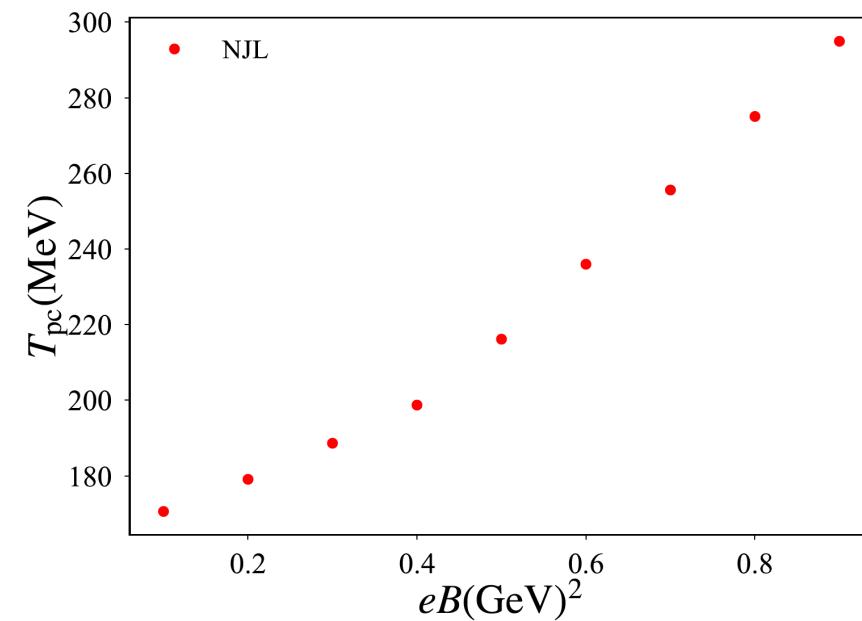
What about
effective model analysis?

Magnetic field reduces T_{pc} .

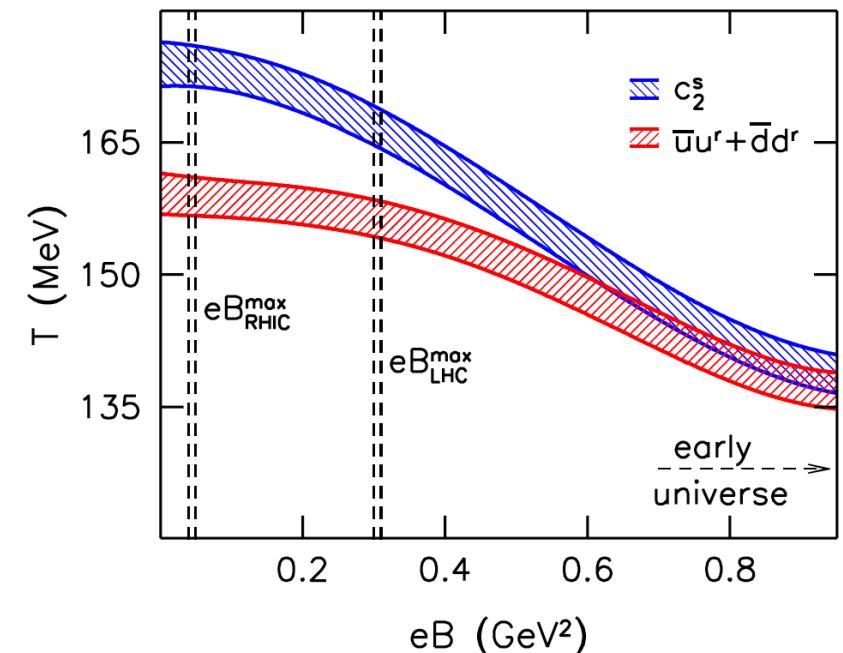
NJL v.s. lattice QCD

12

Phase diagram (conventional NJL)



Phase diagram (Lattice observation)



JHEP 02 (2012) 044

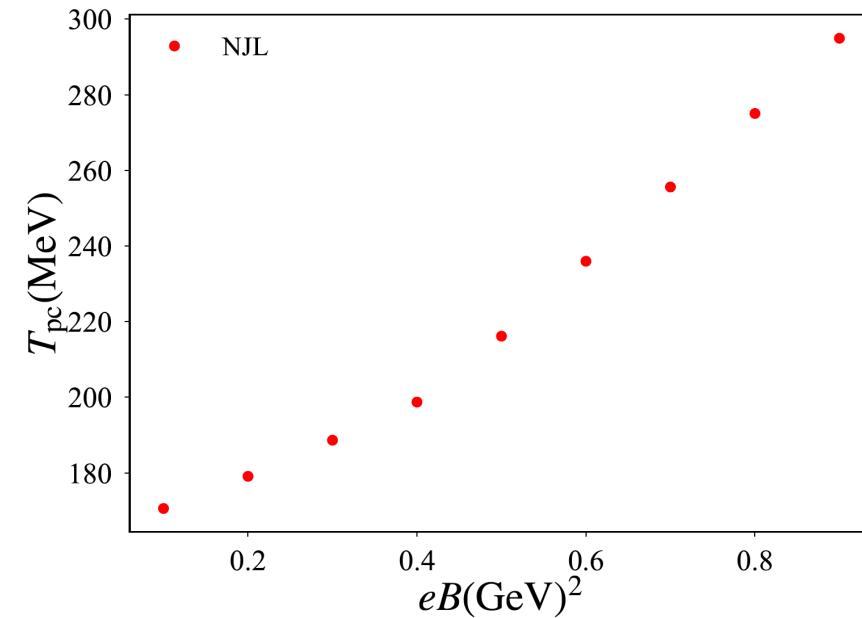
Magnetic field enhances T_{pc} .

Magnetic field reduces T_{pc} .

NJL v.s. lattice QCD

12

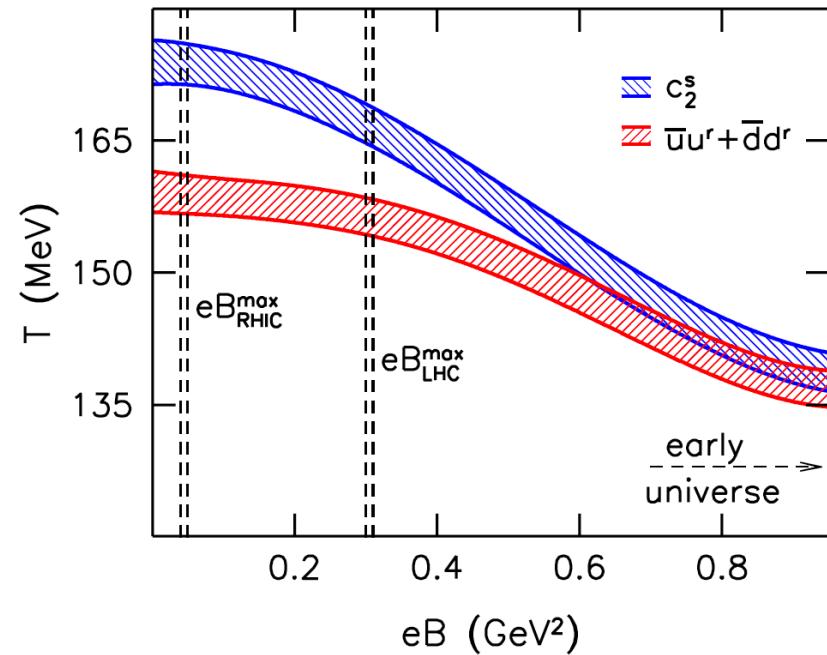
Phase diagram (conventional NJL)



Magnetic field enhances T_{pc} .



Phase diagram (Lattice observation)



JHEP 02 (2012) 044

Discrepancy in
observables...



Magnetic field reduces T_{pc} .

We should add **new contributions, effects or interactions** to NJL model.



Missing ingredients would be a new aspect of thermomagnetic QCD.

Proposals:

- Pion fluctuation PRL, 110(3):031601, 2013
- Chirality imbalance PRD, 88:054009, 2013
- Intrinsic eB-dependence on coupling constant PRD, 91(5):054006, 2015.

⋮

Still unclear...

Anomalous Magnetic Moment of quarks

14

We add Anomalous Magnetic Moment (AMM) of quarks to NJL model.

$$\mathcal{L}_{\text{int}}^{(\text{AMM})} = \frac{1}{2} \kappa_f q_f \bar{\psi} F_{\mu\nu} \sigma^{\mu\nu} \psi \quad (F_{\mu\nu} \sim B)$$

Anomalous Magnetic Moment of quarks

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We add Anomalous Magnetic Moment (AMM) of quarks to NJL model.



$$\mathcal{L}_{\text{int}}^{(\text{AMM})} = \frac{1}{2} \kappa_f q_f \bar{\psi} F_{\mu\nu} \sigma^{\mu\nu} \psi \quad (F_{\mu\nu} \sim B)$$

Quark-AMM κ_f is dynamically generated through spontaneous chiral symmetry breaking
PRL, 106:072001, 2011. (based on Bethe-Salpeter approach)

Dynamical generation of quark AMM κ_f has also been studied in the gauged NJL model,
PRD, 103:116008, 2021.
(AMM is evaluated at quark one-loop level for the photon-quark-antiquark vertex function.)

Anomalous Magnetic Moment of quarks

14

We add Anomalous Magnetic Moment (AMM) of quarks to NJL model.



$$\mathcal{L}_{\text{int}}^{(\text{AMM})} = \frac{1}{2} \kappa_f q_f \bar{\psi} F_{\mu\nu} \sigma^{\mu\nu} \psi \quad (F_{\mu\nu} \sim B)$$

Quark-AMM κ_f is dynamically generated through spontaneous chiral symmetry breaking
PRL, 106:072001, 2011. (based on Bethe-Salpeter approach)

Dynamical generation of quark AMM κ_f has also been studied in the gauged NJL model,
PRD, 103:116008, 2021.
(AMM is evaluated at quark one-loop level for the photon-quark-antiquark vertex function.)



Quark-AMM κ_f becomes vanishingly small
after the chiral restoration.



Quark-AMM would be significant
in thermomagnetic phase transition.

Influence of quark-AMM

15

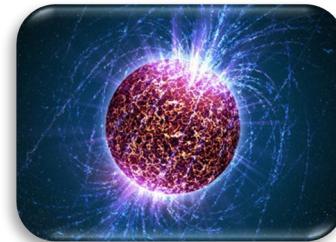
Influence of quark-AMM on...

- Meson mass under eB
- Magnetic susceptibility
 - NJL with AMM
(Phys. Rev. D, 103(7):076015, 2021.
Phys. Rev. D 106, 016005, 2022.)
- Generation mechanism of strong eB in magnetars
 - Spontaneous magnetization based on NJL with AMM
(PTEP, 2015(10):103D01, 2015)



Meson mass and mag. sus.
have been observed in Lattice simulation

- PoS, LATTICE2019:250, 2020
- JHEP, 07:183, 2020



Magnetar

Influence of quark-AMM

15

Influence of quark-AMM on...

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- Magnetic susceptibility

- NJL with AMM
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Meson mass and mag. sus.
have been observed in Lattice simulation

- PoS, LATTICE2019:250, 2020
- JHEP, 07:183, 2020

?

?



However, exact form of AMM is still unknown...



Understanding quark-AMM is important in extreme conditions of QCD.

3. QCD under magnetic field

- Magnetic effect on phase transition
- Our work

Our study

16

Motivation:

How much does quark-AMM contribute to chiral restoration in magnetized QCD?

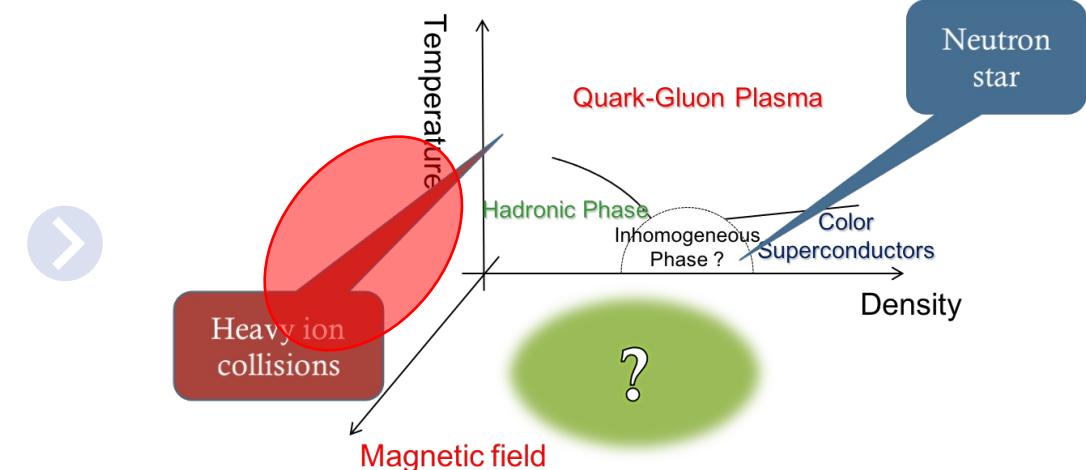
- Quark-AMM interaction

$$\mathcal{L}_{\text{int}}^{(\text{AMM})} = \frac{1}{2} \kappa_f q_f \bar{\psi} [F_{\mu\nu} \sigma^{\mu\nu}] \psi$$

Magnetic field

Spontaneous chiral symmetry breaking

But, κ_f is unknown...



Our study

16

Motivation:

Reveal the effective form of quark-AMM linked with chiral symmetry breaking.

- Quark-AMM interaction

$$\mathcal{L}_{\text{int}}^{(\text{AMM})} = \frac{1}{2} \kappa_f q_f \bar{\psi} F_{\mu\nu} \sigma^{\mu\nu} \psi$$

At $T = 0$ AMM is evaluated from proton and neutron magnetic moment by using constituent quark model.

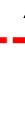
$$\kappa_u = 0.29016 \text{ GeV}^{-1}$$

$$\kappa_d = 0.35986 \text{ GeV}^{-1}$$

PRD, 90(10):105030, 2014



Quark AMM would take $\kappa_{u,d} \sim O(0.1 \text{ GeV}^{-1})$.



Benchmark values

Our study

16

Motivation:

Reveal the effective form of quark-AMM linked with chiral symmetry breaking.

- Quark-AMM interaction

$$\mathcal{L}_{\text{int}}^{(\text{AMM})} = \frac{1}{2} \kappa_f q_f \bar{\psi} F_{\mu\nu} \sigma^{\mu\nu} \psi$$



What would happen
if $\kappa_{u,d}$ take constant?

At $T = 0$ AMM is evaluated from proton and neutron magnetic moment by using constituent quark model.

$$\kappa_u = 0.29016 \text{ GeV}^{-1}$$

$$\kappa_d = 0.35986 \text{ GeV}^{-1}$$

PRD, 90(10):105030, 2014



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Benchmark values

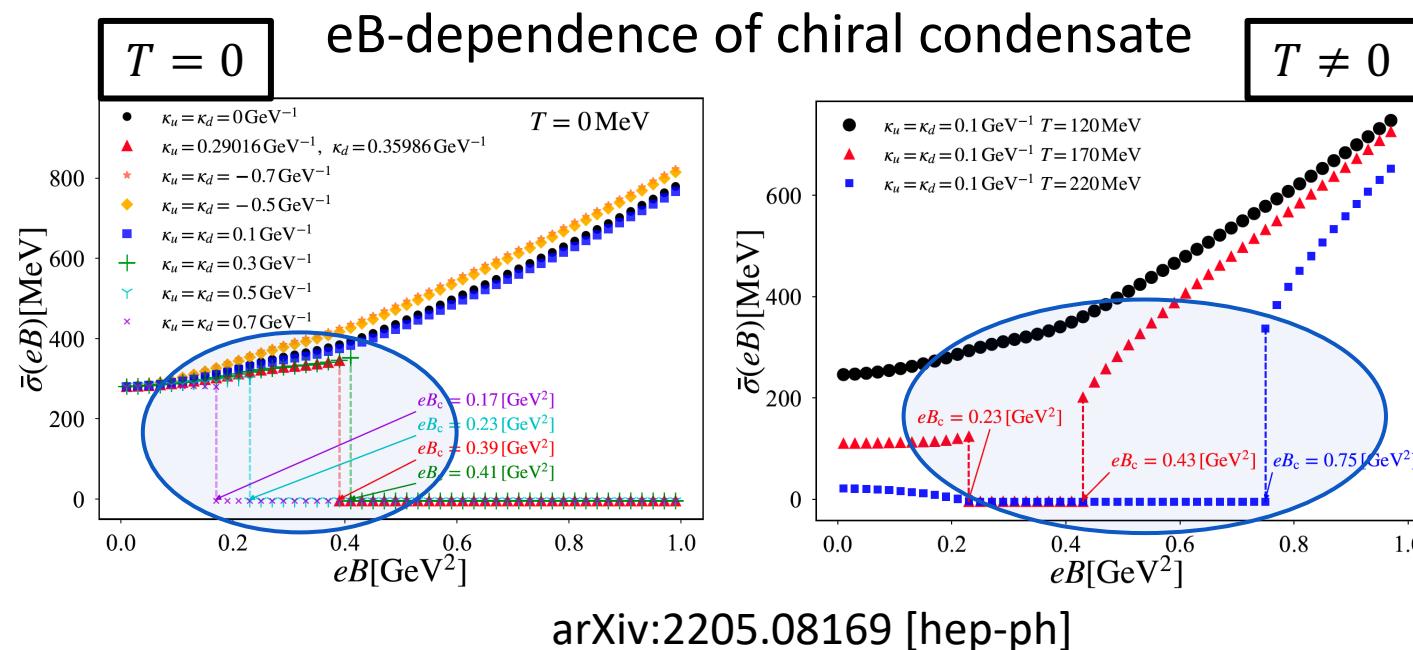
Constant AMM and induced-phase transition

17

Constant AMM induces first order phase transition.

- M.K. and M. Huang, arXiv:2205.08169 [hep-ph].
- PRD, 90(10):105030, 2014
- ...

- Quark AMM takes $\kappa_{u,d} \sim O(0.1\text{GeV}^{-1})$.
- NJL is based on smooth regularization.



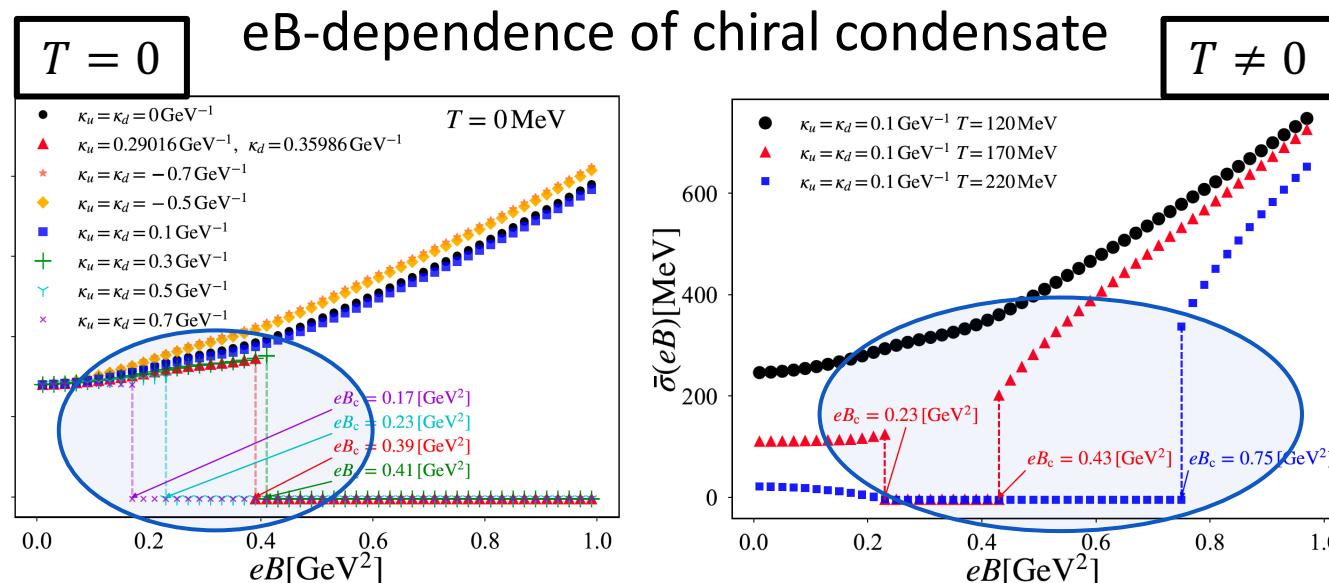
Constant AMM and induced-phase transition

17

Constant AMM induces first order phase transition.

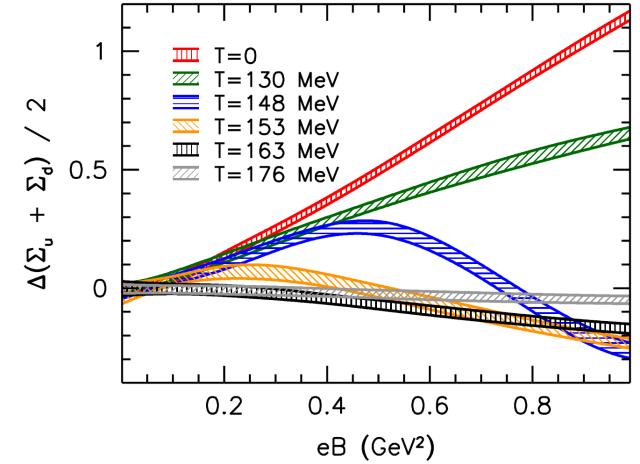
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- ...

- Quark AMM takes $\kappa_{u,d} \sim O(0.1\text{GeV}^{-1})$.
- NJL is based on smooth regularization.



Discrepancy

Crossover observed
in lattice observation



AMM depending on chiral condensate

18

Suppose that $\kappa_{u,d}$ depends on chiral (quark) condensate σ :

$$\kappa_{u,d}(\sigma) = O(1) + O(\sigma) + O(\sigma^2) + O(\sigma^3) + \dots \quad (\text{AMM is generally expanded as a series of } \sigma.)$$

$O(\sigma)$ and $O(\sigma^2)$ have been proposed in the NJL analyses,
but the higher order terms have not been fully taken into account in the phase transition.
Phys. Rev. D, 103(7):076015, 2021.
Phys. Rev. D 106, 016005, 2022.

AMM depending on chiral condensate

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Suppose that $\kappa_{u,d}$ depends on chiral (quark) condensate σ :

$$\kappa_{u,d}(\sigma) = \cancel{O(1)} + O(\sigma) + O(\sigma^2) + \cancel{O(\sigma^3) + \dots} \quad (\text{AMM is generally expanded as a series of } \sigma.)$$

- $O(1)$ term induces unexpected-first order phase transition.
- Higher order terms like $O(\sigma^3)$ would become negligible compared with $O(\sigma)$ and $O(\sigma^2)$.



Discard constant term and higher order terms.

AMM depending on chiral condensate

18

Suppose that $\kappa_{u,d}$ depends on chiral (quark) condensate σ :

$$\kappa_{u,d}(\sigma) = \cancel{O(1)} + \boxed{O(\sigma) + O(\sigma^2)} + \cancel{O(\sigma^3) + \dots} \quad (\text{AMM is generally expanded as a series of } \sigma.)$$

- $O(1)$ term induces unexpected-first order phase transition.
- Higher order terms like $O(\sigma^3)$ would become negligible compared with $O(\sigma)$ and $O(\sigma^2)$.



Discard constant term and higher order terms.



Evaluate the contribution of $O(\sigma)$ and $O(\sigma^2)$, respectively.

AMM $O(\sigma)$ contribution

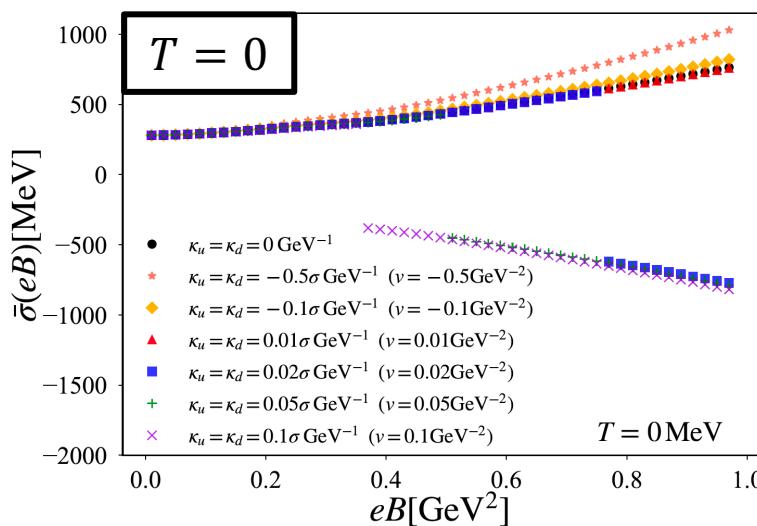
19

Contribution of $O(\sigma)$ on chiral condensate

$$\kappa_{u,d} = v\sigma \sim O(0.1\text{GeV}^{-1}) \text{ at } T = 0.$$

$$\kappa_{u,d}(\sigma) = \cancel{O(1)} + \boxed{O(\sigma)} + O(\sigma^2) + \cancel{O(\sigma^3)} + \dots$$

eB-dependence of chiral condensate
including $\kappa_{u,d} = v\sigma$ (v is parameter)



AMM $O(\sigma)$ contribution

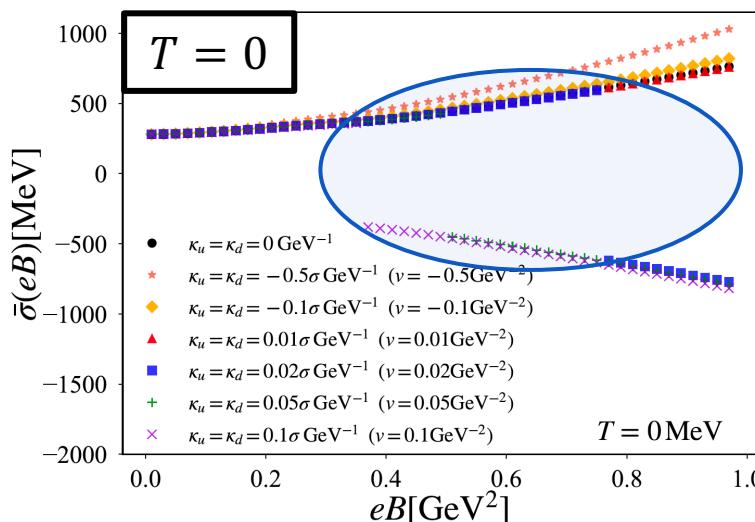
19

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$$\kappa_{u,d}(\sigma) = \cancel{O(1)} + \boxed{O(\sigma)} + O(\sigma^2) + \cancel{O(\sigma^3) + \dots}$$

eB-dependence of chiral condensate
including $\kappa_{u,d} = v\sigma$ (v is parameter)



$\kappa_{u,d} \sim \sigma$ also induces **jump** in chiral condensate.



However...

Jump is not observed in lattice QCD simulation.



$\kappa_{u,d} \sim \sigma$ is discarded.

AMM $O(\sigma^2)$ contribution

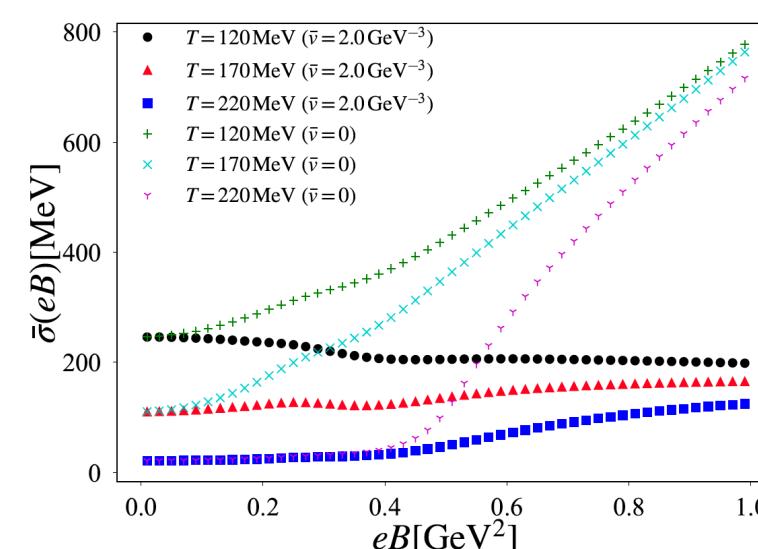
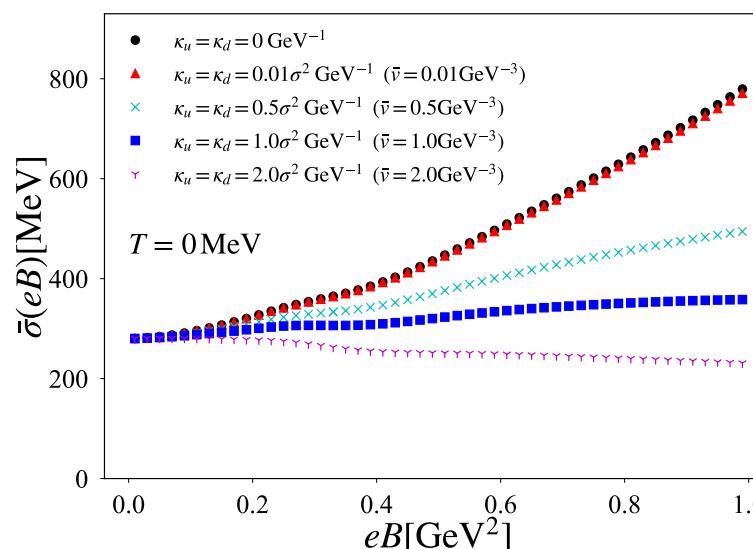
20

Contribution of $O(\sigma^2)$ on chiral condensate

$$\kappa_{u,d} = \bar{v}\sigma^2 \sim O(0.1\text{GeV}^{-1}) \text{ at } T = 0.$$

$$\kappa_{u,d}(\sigma) = \boxed{O(1)} + \boxed{O(\sigma)} + \boxed{O(\sigma^2)} + \boxed{O(\sigma^3)} + \dots$$

eB-dependence of chiral condensate
including $\kappa_{u,d} = \bar{v}\sigma^2$ (\bar{v} is parameter)



AMM $O(\sigma^2)$ contribution

20

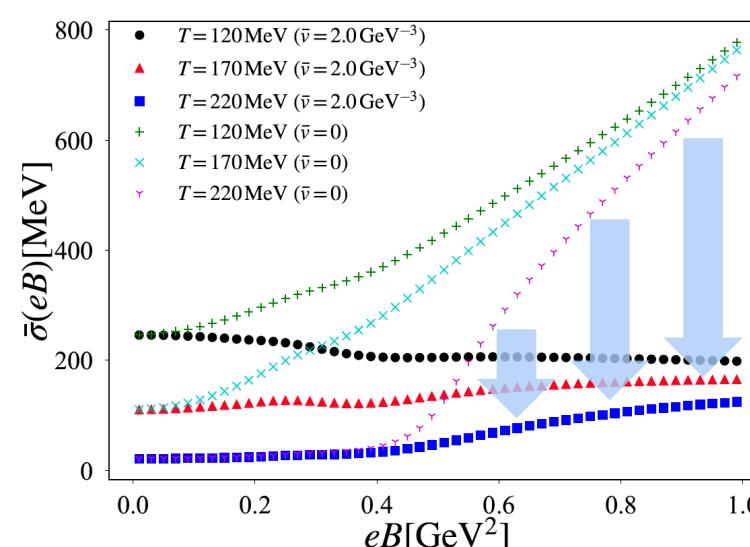
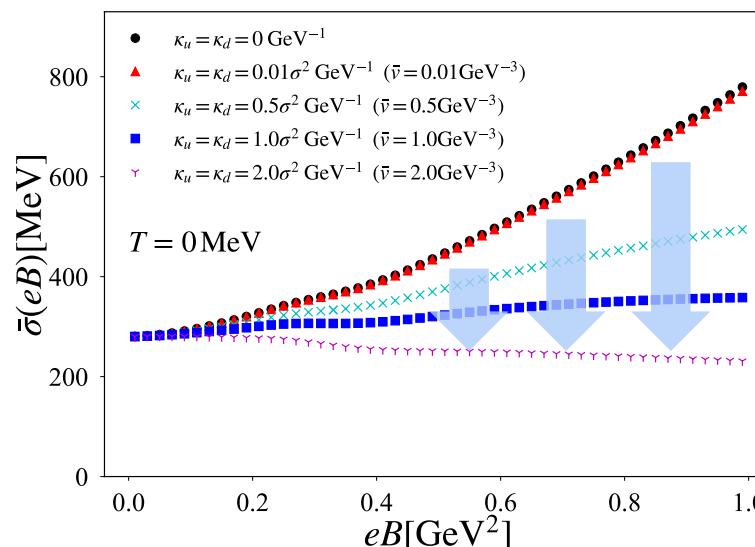
Contribution of $O(\sigma^2)$ on chiral condensate

$$\kappa_{u,d} = \bar{v}\sigma^2 \sim O(0.1\text{GeV}^{-1}) \text{ at } T = 0.$$

$$\kappa_{u,d}(\sigma) = \boxed{O(1)} + \boxed{O(\sigma)} + \boxed{O(\sigma^2)} + \boxed{O(\sigma^3)} + \dots$$

eB-dependence of chiral condensate
including $\kappa_{u,d} = \bar{v}\sigma^2$ (\bar{v} is parameter)

Accidental jumps do not show up.
 $\kappa_{u,d} \sim \sigma^2$ suppresses chiral symmetry breaking.



$\kappa_{u,d} \sim \sigma^2$ acts as suppressor
for chiral symmetry breaking.

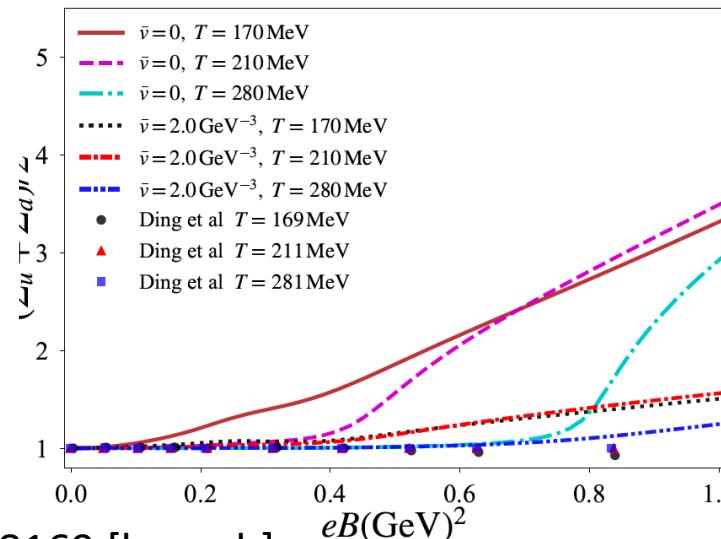
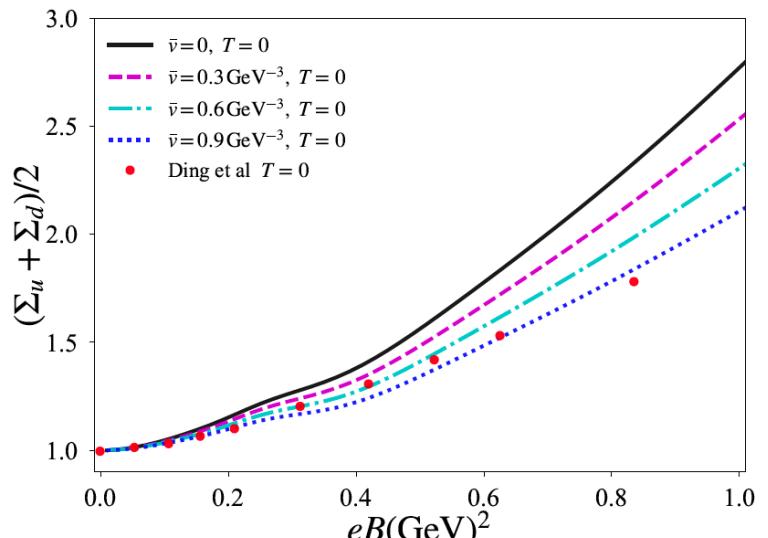
Comparison with lattice data

21

Contribution of $O(\sigma^2)$ on chiral condensate

$$\kappa_{u,d}(\sigma) = \boxed{O(1)} + \boxed{O(\sigma)} + \boxed{O(\sigma^2)} + \boxed{O(\sigma^3)} + \dots$$

Subtracted quark condensate
including $\kappa_{u,d} = \bar{v}\sigma^2$ (\bar{v} is parameter)



arXiv:2205.08169 [hep-ph]

By tuning \bar{v} ...

NJL model can quantitatively reproduce the lattice results.

\bar{v} would have intrinsic T-dependence: $\bar{v}(T)$.

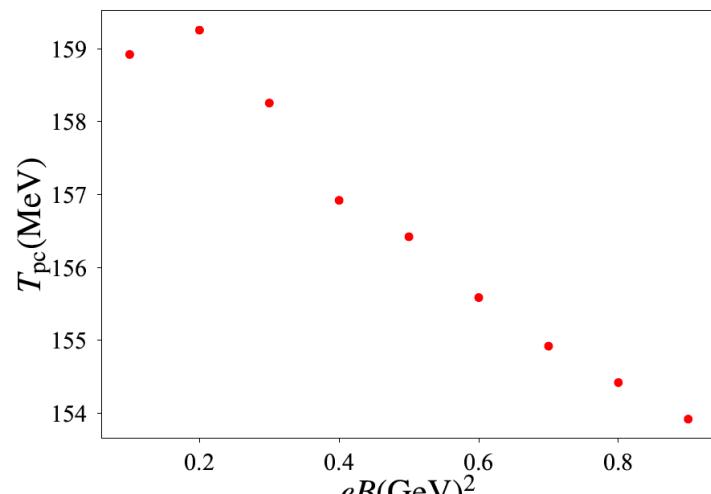
lattice results:
PRD, 104(1):014505, 2021.
PRD, 105(3):034514, 2022.

IMC in NJL, but...

22

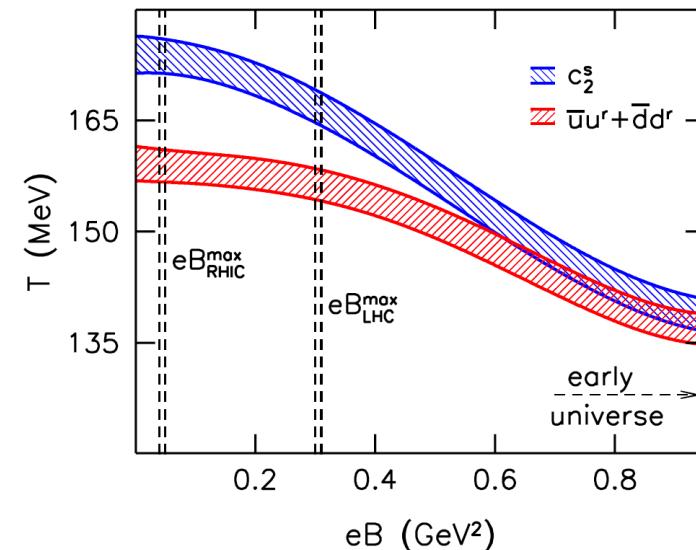
Tuned quark-AMM inhibits magnetic catalysis.

NJL w/ $\kappa_{u,d} = \bar{v}\sigma^2$ (tuned $\bar{v}(T)$)



arXiv:2205.08169 [hep-ph]

Lattice observation



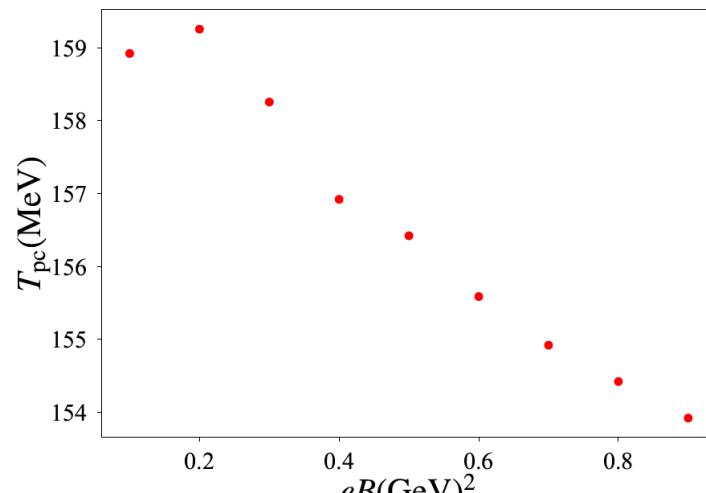
JHEP 02 (2012) 044

IMC in NJL, but...

22

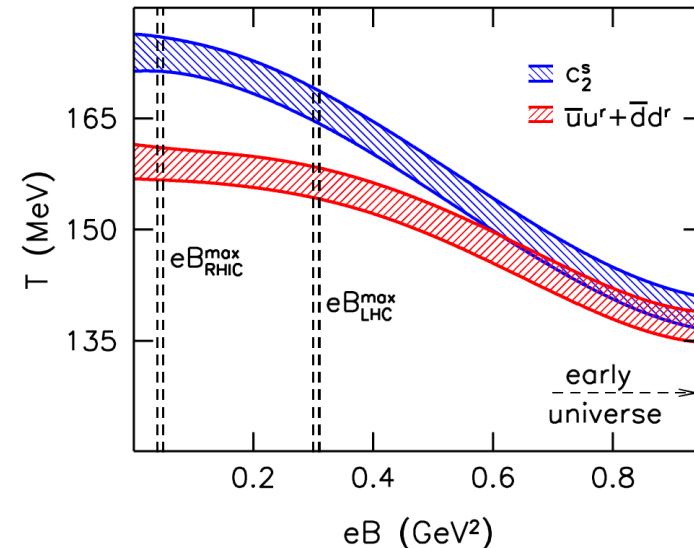
Tuned quark-AMM inhibits magnetic catalysis.

NJL w/ $\kappa_{u,d} = \bar{v}\sigma^2$ (tuned $\bar{v}(T)$)



arXiv:2205.08169 [hep-ph]

Lattice observation



JHEP 02 (2012) 044

To perfectly agree
with lattice observation...

Extra mechanism would be needed.
(like magnetic dependent coupling constant)

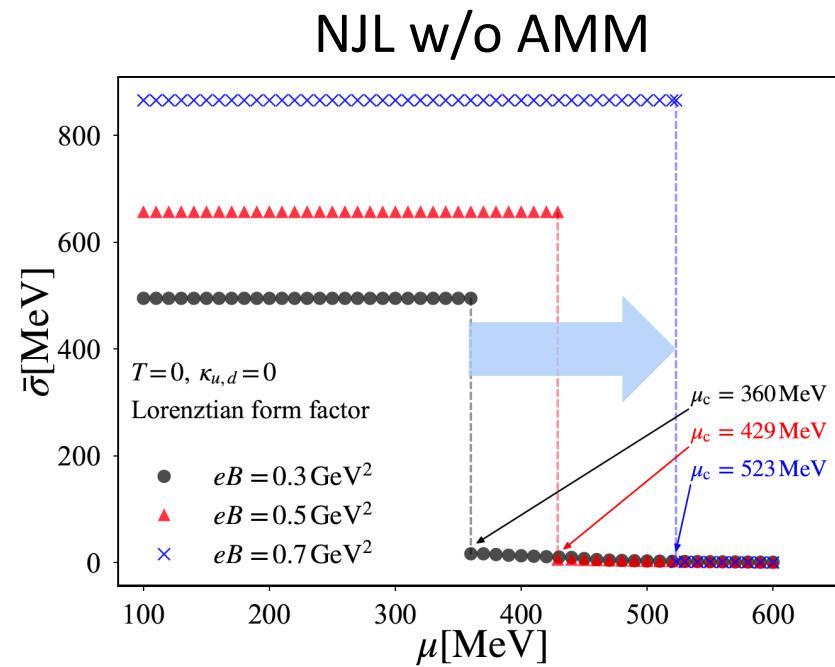
AMM effect in finite chemical potential

23

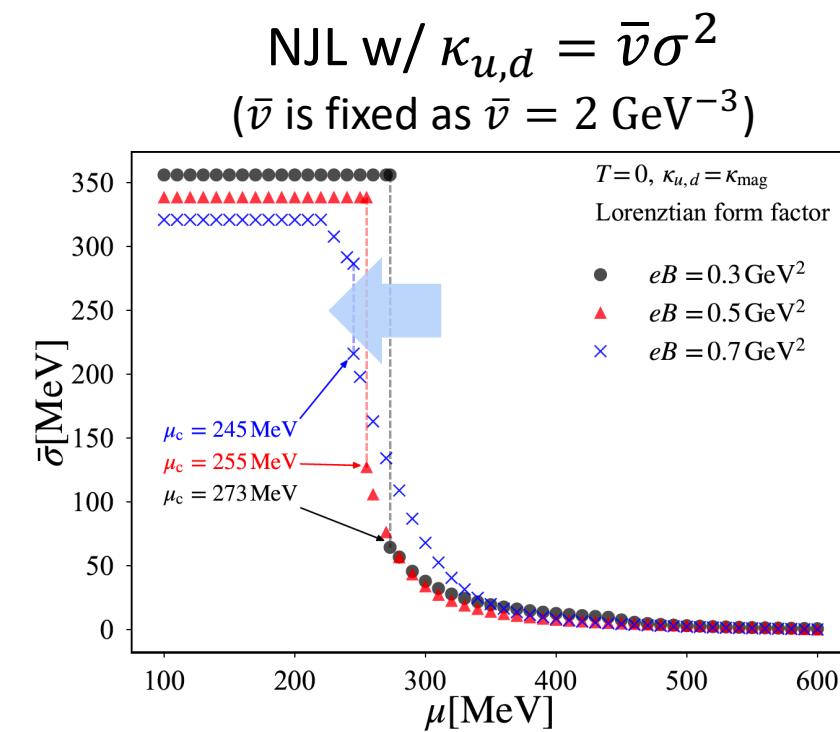
Let's move onto finite quark chemical potential.

*Similar behavior is observed in PRD 106, no.11, 116023 (2022).

➤ μ -dependence on chiral condensate



Preliminary
results



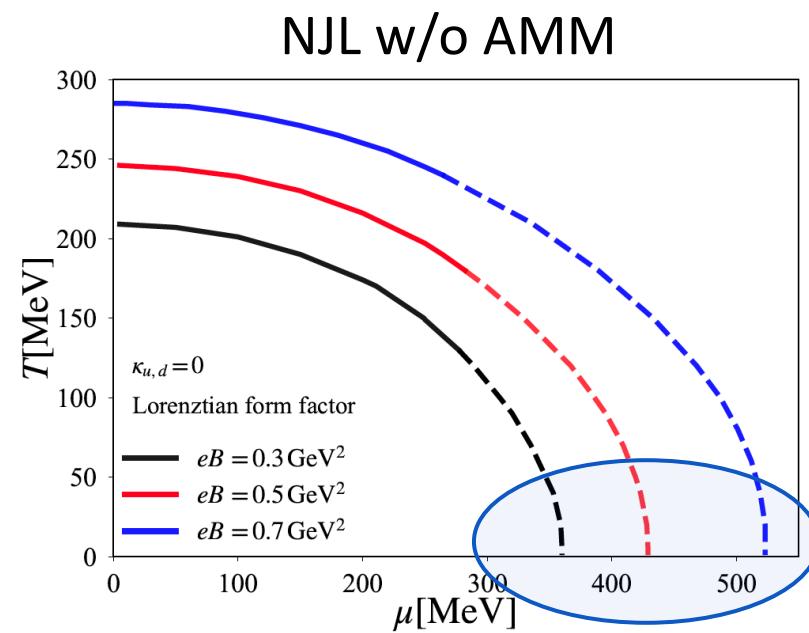
μ_c increases.
(Magnetic catalysis)

AMM reduces μ_c .
(Inverse magnetic catalysis)

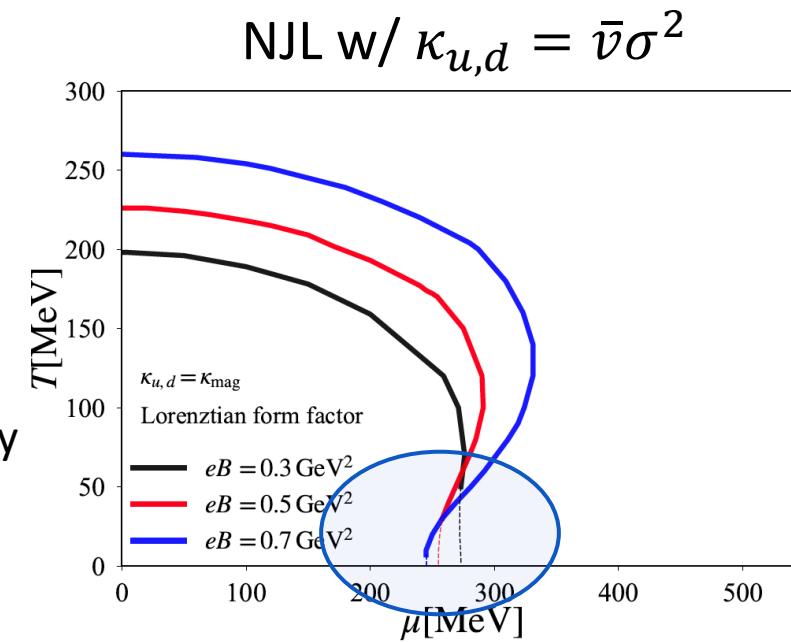
AMM effect in T- μ phase diagram

24

Phase diagram in T- μ plane



Preliminary
results



Quark AMM significantly affects phase diagram at finite μ -region.

Summary

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Motivation:

How much does quark-AMM $\kappa_{u,d}$ contribute to phase transition under eB?

Restricted the form of $\kappa_{u,d}$ from the observed chiral phase transition.

✓ Quark-AMM reduces chiral symmetry breaking.



NJL results can not perfectly agree with lattice data at finite- T .

✓ Quark AMM provides the inverse magnetic catalysis for μ_c .



AMM potentially affects magnetized QCD phase diagram.

Outlook

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Quark-AMM
linked with chiral symmetry

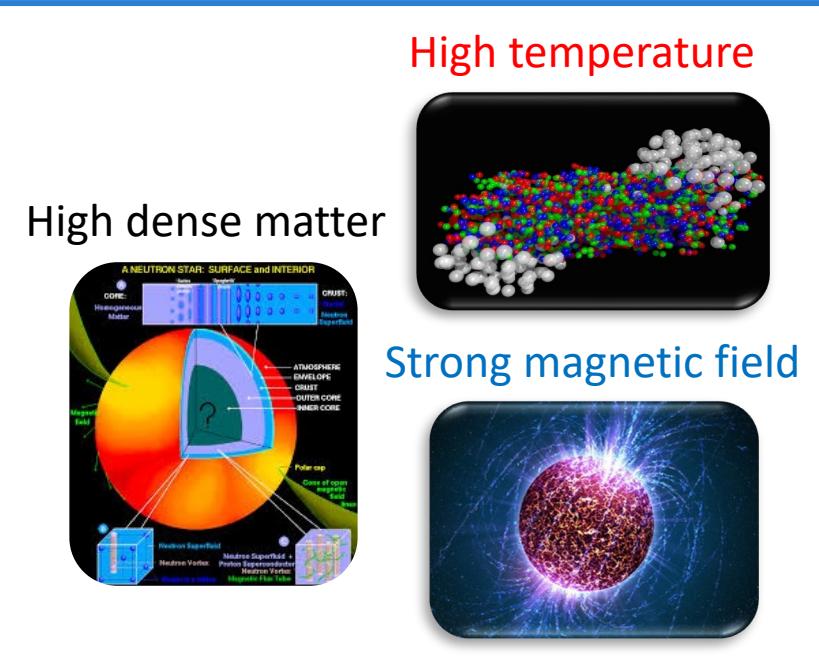


Phase structure is still unclear...



There would exist
undiscovered ingredients.

- Improve AMM.
- Provide new mechanism.



Hadron/QCD properties
in extreme conditions

Thank you.