

REVIEW  
**CHARMONIUM DECAYS**  
BY 9 PAPERS

**Celebration Ceremony of the 500 Publications  
of BESIII Collaboration**

2023-5-31, IHEP & on-line Joint

Kai Zhu



- ▶ arXiv: 0809.1869
- ▶ **2008-10-10**

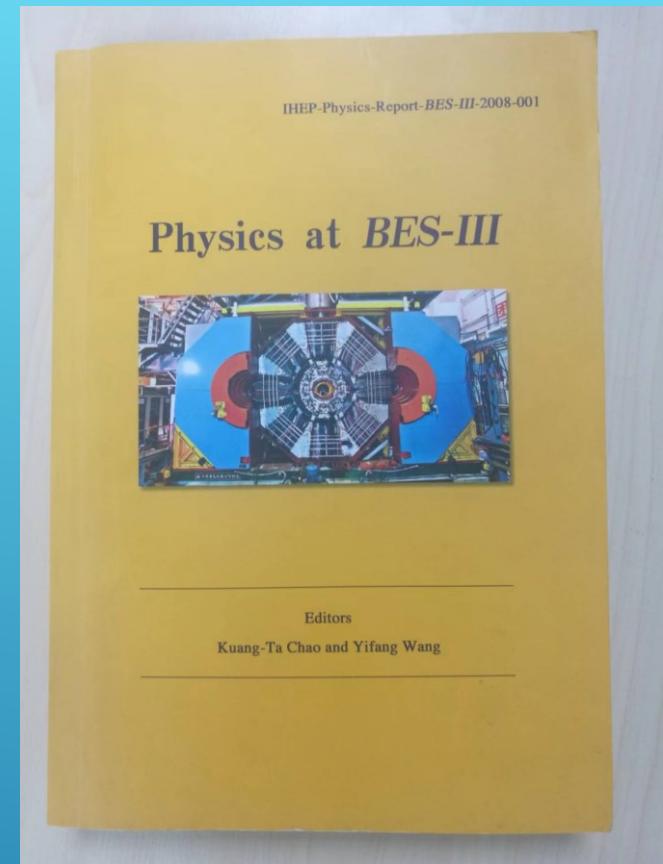
# 0# PAPER OF BESIII

2

# Chapter 13

## Theoretical Frameworks of Charmonium Physics

Two heavy quarks, i.e. heavy quarkonia, play a prominent role in investigations of QCD dynamics both within and beyond the Standard Model [1]. These are multi-scale systems that probe all of the energy regimes of QCD: from the hard region, where expansions in the coupling constant are legitimate, to the low-energy region, where nonperturbative effects dominate. Heavy quark-antiquark states are thus an ideal, and to some extent unique, laboratory where our understanding of nonperturbative QCD and its interplay with perturbative QCD can be tested in a controlled framework. In correspondence with the hierarchy of energy scales in quarkonia, a hierarchy of nonrelativistic effective field theories (NR EFT) may be constructed, each one with fewer degrees of freedom that are left dynamical and thus simpler. Some of these physical scales are large and may be treated with perturbation theory. Therefore, one can obtain information about the



# “PHYSICS AT BES-III” (YELLOW BOOK)

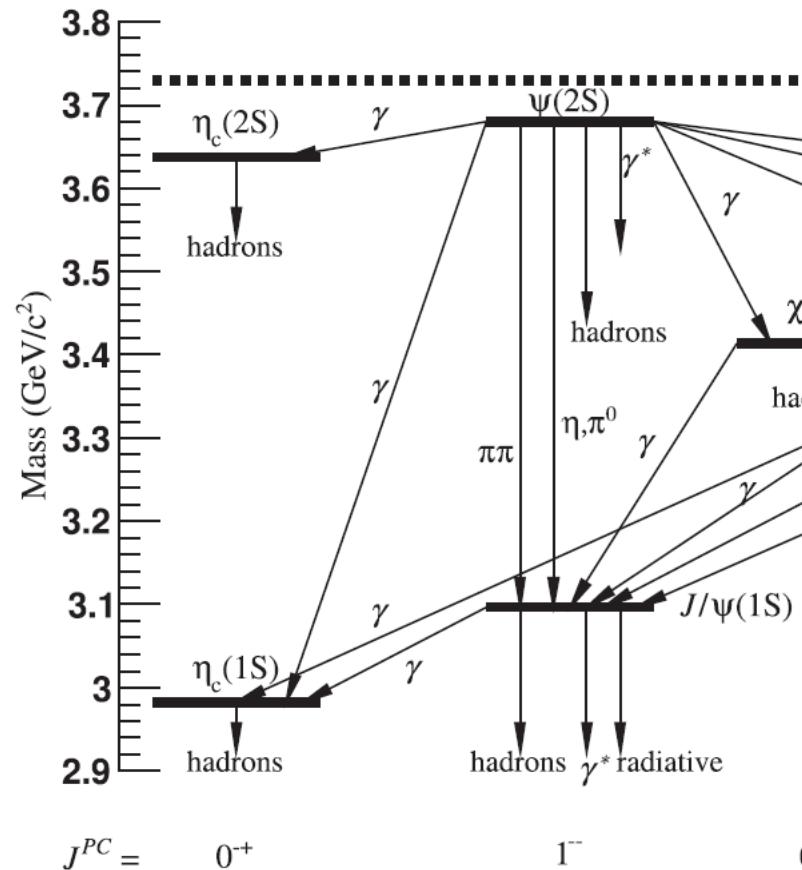
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## 15 Charmonium transitions

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## 18 Hadronic decays

## 16 Charmonium Leptonic and EM Decays

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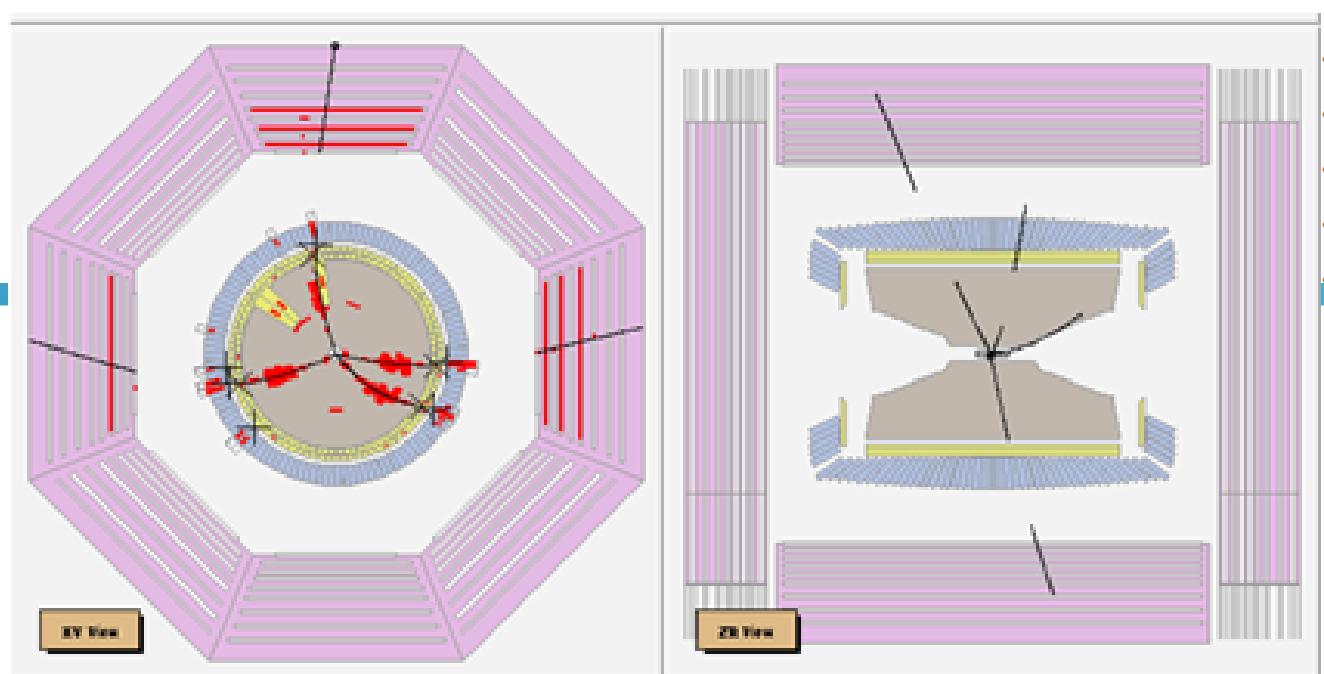
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$\psi'$  samples are desired

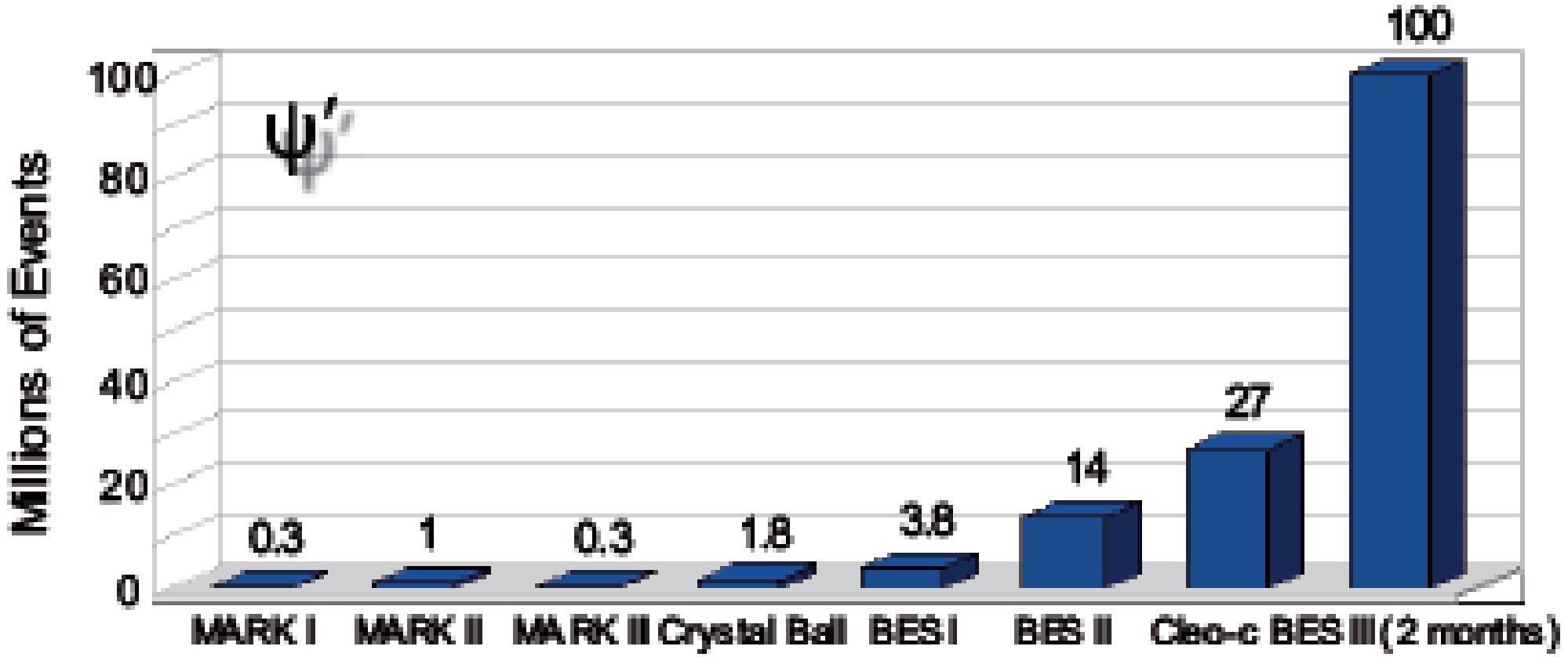
$J^{PC} =$	$0^+$	$1^-$	$0^{++}$	$1^{++}$	$1^{+-}$	$2^{++}$	
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* runno	status	start-time	end-time	no-of-evts	no-of-had	lumi :
0007958	0	2009-03-03 19:14:23	2009-03-03 20:39:01	6107517	-1	-1.000 :
0007959	0	2009-03-03 20:47:00	2009-03-03 20:56:22	344811	-1	-1.000 :
0007960	0	0000-00-00 00:00:00	0000-00-00 00:00:00	-1	-1	-1.000 :
0007961	0	0000-00-00 00:00:00	0000-00-00 00:00:00	1	1	-1.000 :
0008092	2	2009-03-06 03:24:00	2009-03-06 04:15:00	42	894.400	:
MDC HV warned once at 4:15 AM						
0008093	3	2009-03-06 06:14:00				.600 :
0008094	-2	0000-00-00 00:00:00				.000 :
0008095	-2	0000-00-00 00:00:00				.000 :
0008096	-2	0000-00-00 00:00:00				.000 :
0008097	-2	0000-00-00 00:00:00				.000 :
0009022	-3	2009-04-14 01:28:49				000 :
0009023	2	2009-04-14 02:11:05				336 :
MUC BD4 no HV						
0009024	2	2009-04-14 04:42:21				745 :
MUC BD4 no HV, TOF T east high noise level						
0009025	2	2009-04-14 06:21:35				753 :
MUC BD4 no HV, beam lost, MDC trip-- stop						

$\psi'$  data taking



## 8093: First Physics Run @ BESIII



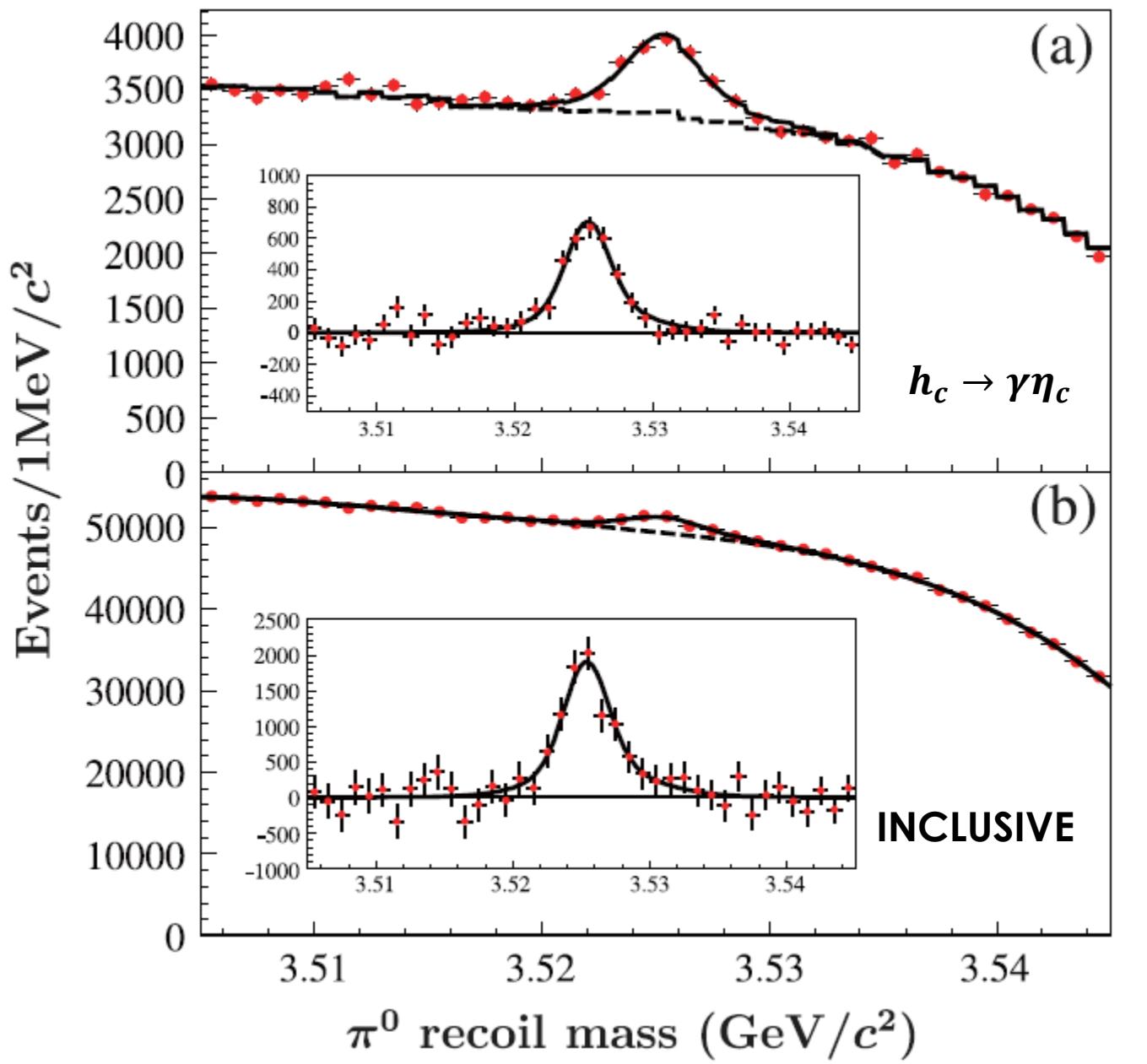
Copy from MESON 2010

7

- ▶ arXiv: 1002.0501
- ▶ **2010-02-02**
- ▶ Phys. Rev. Lett. 104, 132002 (2010)

# 1# PAPER OF BESIII

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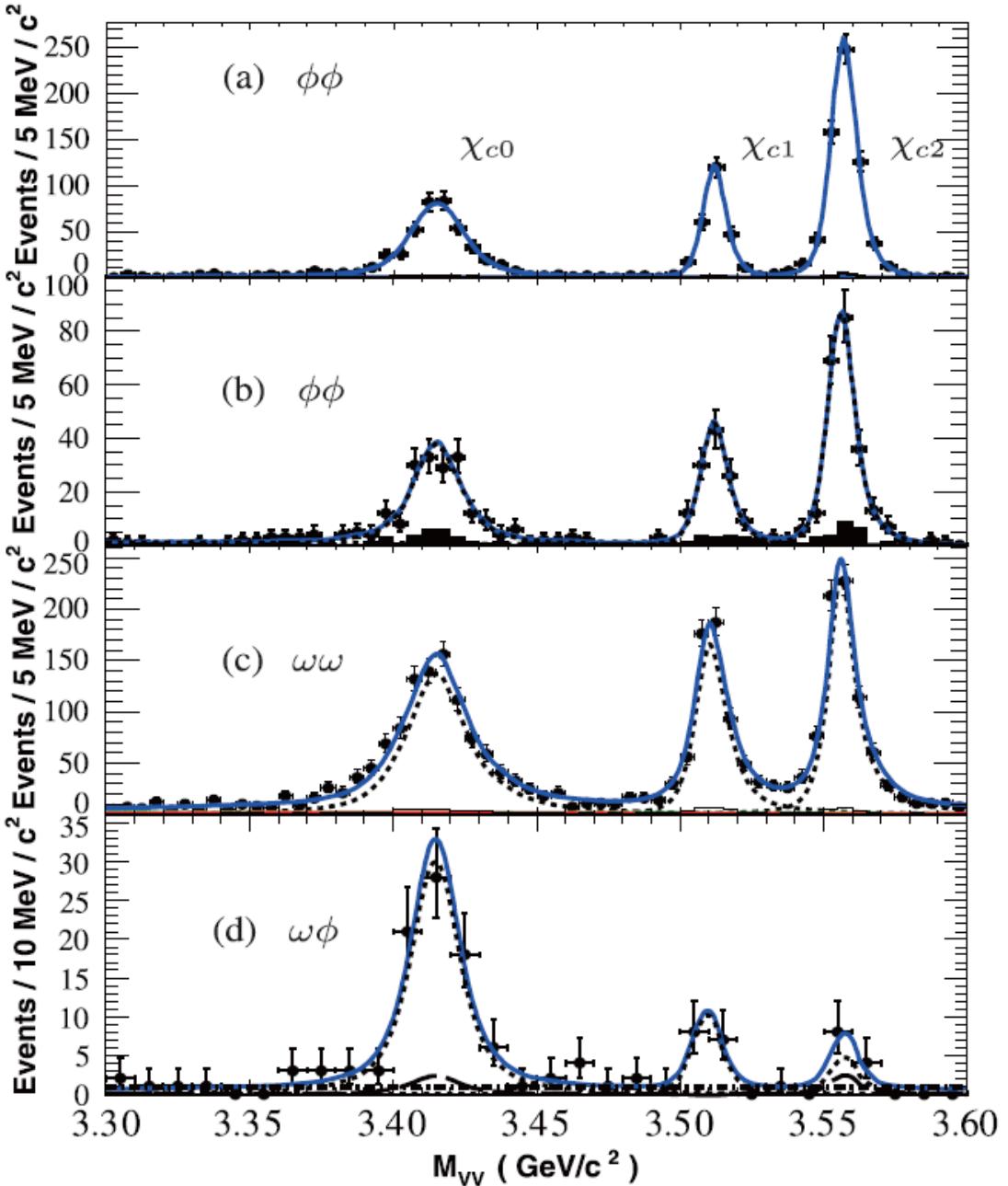


First measurement:  
 $B(\psi(3686) \rightarrow \pi^0 h_c) = (8.4 \pm 1.3 \pm 1.0) \times 10^{-4}$   
 $B(h_c \rightarrow \gamma\eta_c) = (54.3 \pm 6.7 \pm 5.2)\%$

Measurement of  
 $h_c$  in  $\psi(3686)$   
decay

- ▶ arXiv: [1104.5068](https://arxiv.org/abs/1104.5068)
- ▶ **2011-04-28**
- ▶ Phys. Rev. Lett. 107, 092001 (2011)

## 9# PAPER



$$\begin{aligned}B(\chi_{c1} \rightarrow \phi\phi) &= (4.4 \pm 0.3 \pm 0.5) \times 10^{-4} \\B(\chi_{c1} \rightarrow \omega\omega) &= (6.0 \pm 0.3 \pm 0.7) \times 10^{-4} \\B(\chi_{c1} \rightarrow \omega\phi) &= (2.2 \pm 0.6 \pm 0.2) \times 10^{-5}\end{aligned}$$

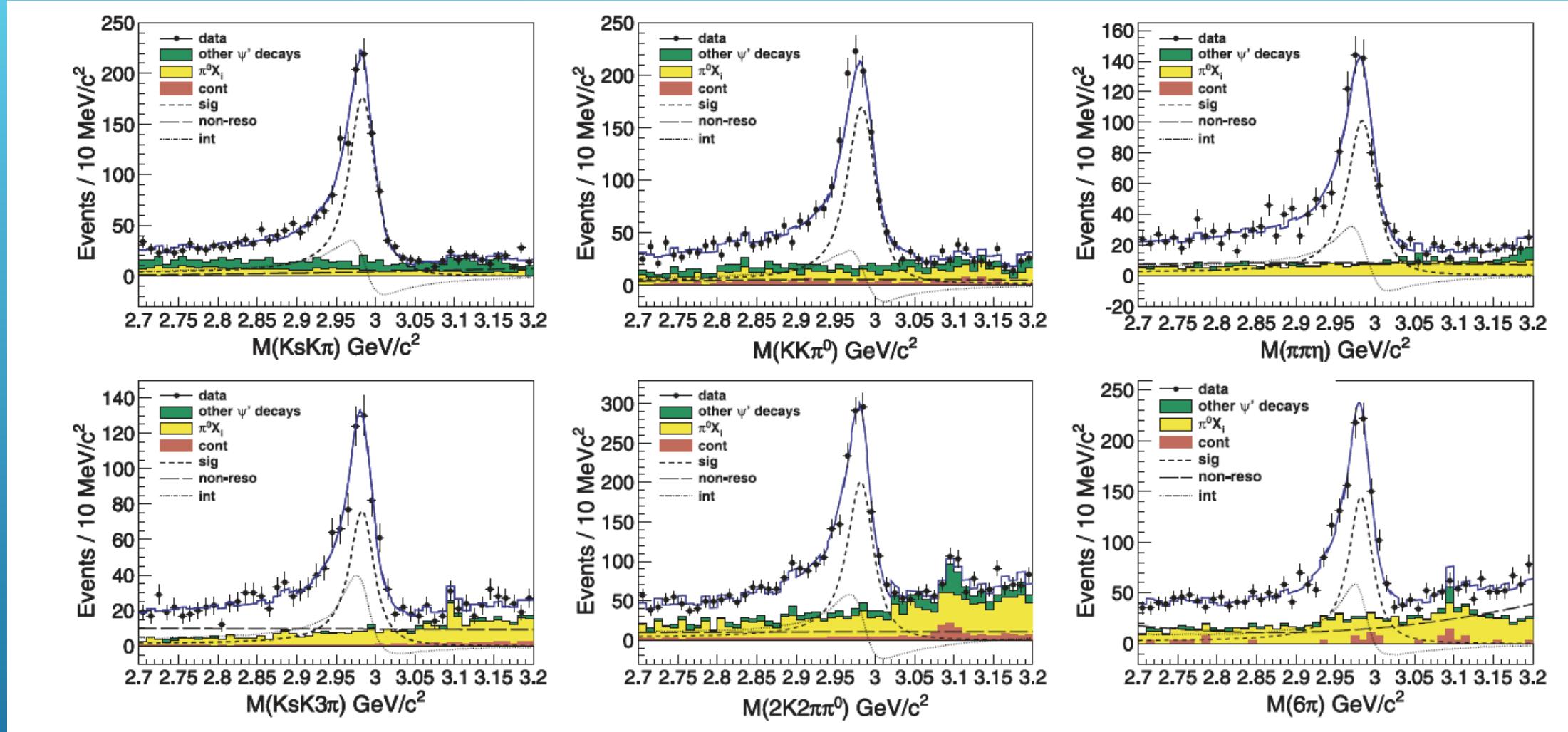
Observations  
of  $\chi_{c1} \rightarrow VV$   
violate helicity  
selection rule

- ▶ arXiv:1111.0398
- ▶ **2011-11-02**
- ▶ Phys. Rev. Lett. 108, 222002 (2012)

## 14# PAPER

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$$M: 2984.3 \pm 0.6 \pm 0.6 \text{ MeV}; \Gamma: 32.0 \pm 1.2 \pm 1.0 \text{ MeV}$$

$\eta_c$  parameters: consider interference

- ▶ arXiv: [1205.5103](https://arxiv.org/abs/1205.5103)
- ▶ **2012-05-23**
- ▶ [Phys. Rev. Lett. 109, 042003 \(2012\)](https://doi.org/10.1103/PhysRevLett.109.042003)

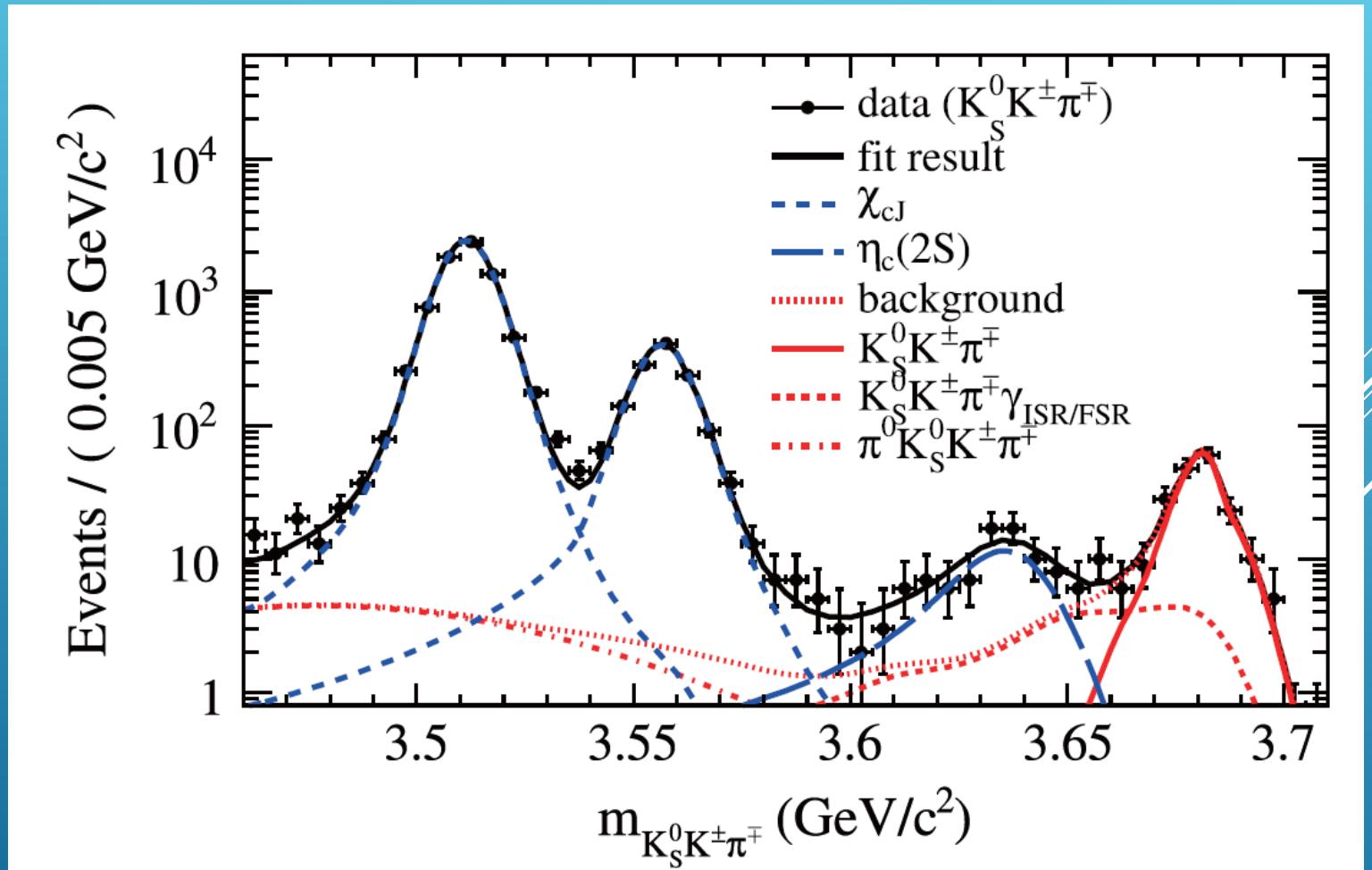
## 22# PAPER

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$$B(\psi(3686) \rightarrow \gamma\eta_c(2S)) \times B(\eta_c(2S) \rightarrow K\bar{K}\pi) = (1.30 \pm 0.20 \pm 0.30) \times 10^{-5}$$

First observation  
of the M1 transition  
 $\psi(3686) \rightarrow \gamma\eta_c(2S)$



- ▶ Run: 25338-27090
- ▶ **Time: 2011-12-31 to 2012-03-30**
- ▶ Lum: 600/pb
- ▶ Nev<sub>t</sub>: 341 M

More  $\psi'$  data set: total 448M (2009+2012)

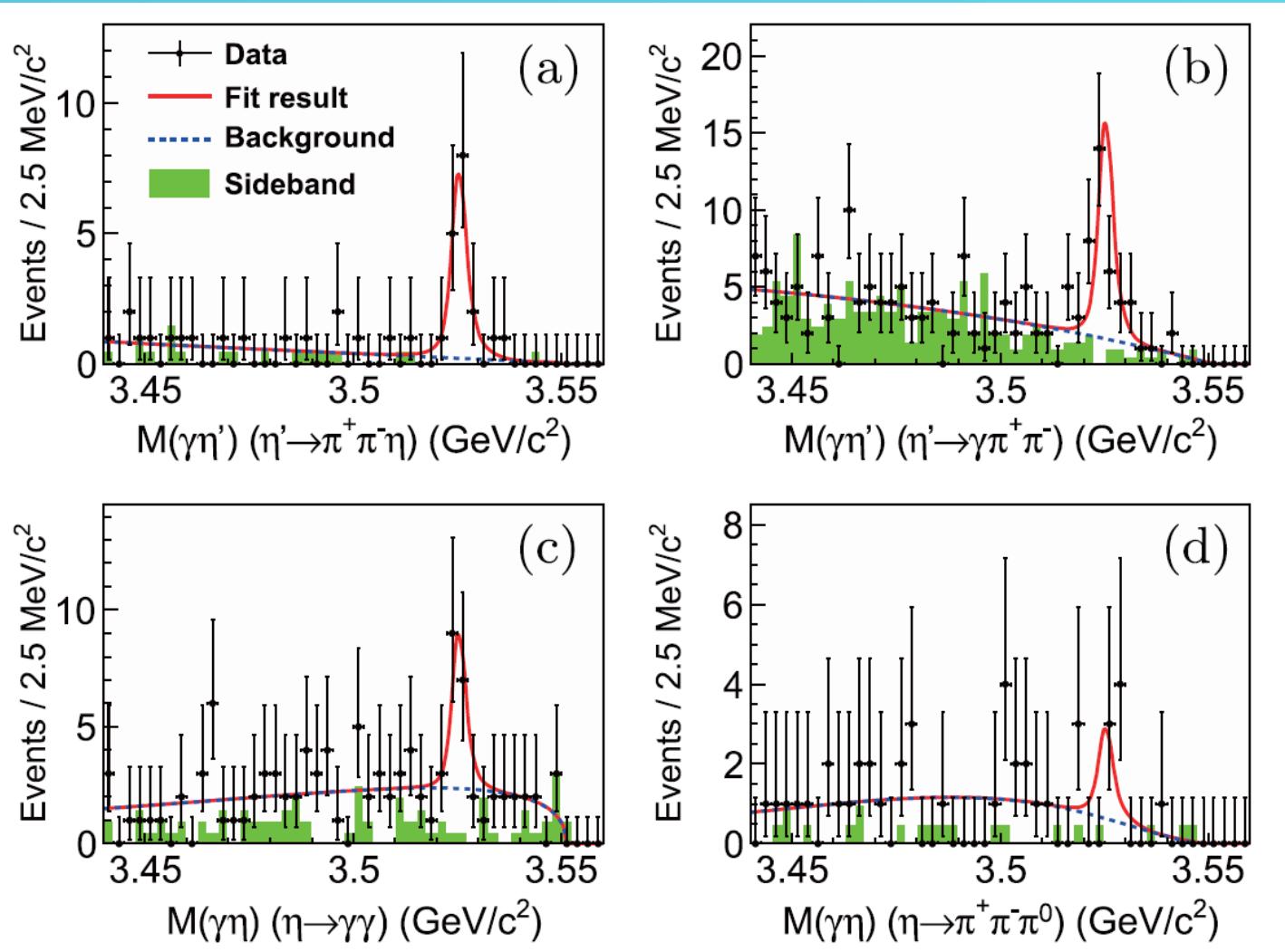
- ▶ arXiv: [1603.04936](#)
- ▶ **2016-03-17**
- ▶ [Phys.Rev.Lett. 116, 251802 \(2016\)](#)

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$$B(h_c \rightarrow \gamma\eta') = (1.52 \pm 0.27 \pm 0.29) \times 10^{-3}$$

$$B(h_c \rightarrow \gamma\eta) = (4.7 \pm 1.5 \pm 1.4) \times 10^{-4}$$

$h_c \rightarrow \gamma\eta'$ :  $8.4\sigma$

$h_c \rightarrow \gamma\eta$ :  $4.0\sigma$

# Observation of $h_c$ radiative decay

based on 448M  $\psi'$

- ▶ arXiv: 1912.05983
- ▶ **2019-12-12**
- ▶ Chin. Phys. C 44, 040001 (2020)

## 288# PAPER

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The charmonium observables can be taken from spectroscopy (e.g. masses and widths), transitions (e.g. transition rates), leptonic and electromagnetic decays, radiative decays, hadronic decays, rare and forbidden decays, and some miscellaneous topics such as the Bell inequalities in high energy physics and special topics in  $B\bar{B}$  final states, where  $B$  refers to baryon. BESIII is well suited to address the remaining experimental questions that are related to the low-mass charmonium spectrum, i.e. below the open-charm threshold, such as a precise determination of the mass and width of  $\eta_c$ ,  $h_c$ , and  $\eta_c(2S)$ . The QCD multipole expansion (QCDME) [15, 16] is a feasible approach for the charmonium hadronic transitions. Its results can be examined via observations at BESIII such as the  $\pi\pi$  transitions of  $S$ -wave ( $P$ -wave or  $D$ -wave) charmonium states, the  $\eta$  transition  $\psi(3686) \rightarrow \eta J/\psi$ , and the iso-spin violating  $\pi^0$  transition  $\psi(3686) \rightarrow \pi^0 h_c$ . Many ra-

# FUTURE PHYSICS PROGRAMME OF BESIII (WHITE PAPER)

measurement	expected sensitivity on branching fraction
$h_c \rightarrow \text{hadrons}$	observation of $5 \times 10^{-4}$
$\eta_c(2S) \rightarrow X$	observation of $1 \times 10^{-6}$
$\chi_{c1} \rightarrow \pi^+ \pi^- \eta_c$	evidence of $3 \times 10^{-3}$
$h_c \rightarrow \pi^+ \pi^- J/\psi$	evidence of $2 \times 10^{-3}$
$\chi_{cJ} \rightarrow \gamma V$	observation of $1 \times 10^{-6}$
$h_c \rightarrow p\bar{p}$	evidence of $2 \times 10^{-4}$

plan	data sets
$XYZ$ plan (1)	$500 \text{ pb}^{-1}$ at a large number of points between 4.0 and 4.6 GeV
$XYZ$ plan (2)	$5 \text{ fb}^{-1}$ at 4.23, 4.42 GeV for large $Z_c$ samples
$XYZ$ plan (3)	$5 \text{ fb}^{-1}$ above 4.6 GeV
charmonium plan	$3 \times 10^9 \psi(3686)$ decays

2021 psi(2S), 3.4/fb (on-line), 2.26 B (preliminary)\_

66257-69292

2022 3.65, 3.682 (ON-LINE) [\[edit\]](#)

Sample	Runno	Ecms(MeV)	luminosity(1/pb)	location
3650	69612-70132	3650	410	/bes3fs/offline/data/709-1/3650/round15/
3682	70133-70505	3682	404	/bes3fs/offline/data/709-1/3682/round15/

large continuum

Total ~2.7B  $\psi'$ (2009+2012+2021)

measurements based on whole data are on-going

21

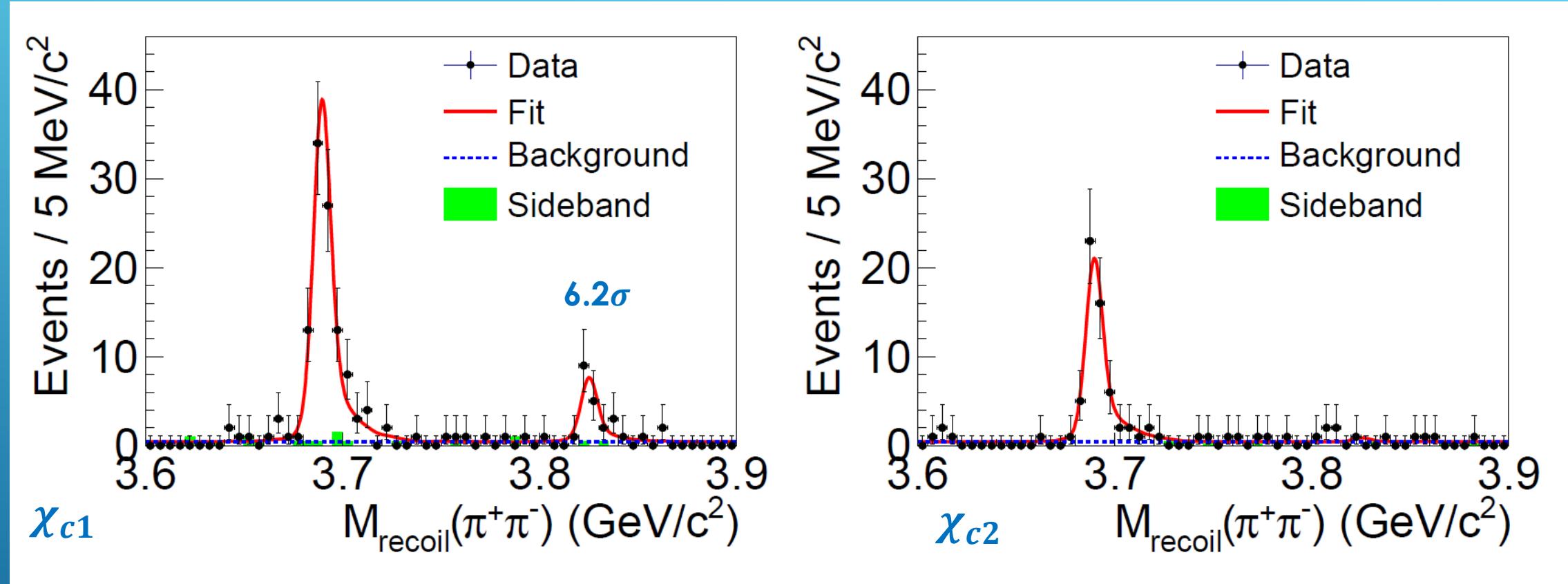
- ▶ arXiv: [1503.08203](#)
- ▶ **2015-03-26**
- ▶ [Phys. Rev. Lett. 115, 011803 \(2015\)](#)

## 85# PAPER

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2023/5/31

$\sqrt{s} = 4.23, 4.26, 4.36, 4.42, 4.60$  GeV  
 $M: (3821.7 \pm 1.3 \pm 0.7)$  MeV,  $\Gamma: < 16$  MeV



$$e^+ e^- \rightarrow \pi^+ \pi^- X(3823), X(3823) \rightarrow \gamma \chi_{c1}$$

$$\psi_2(1^3D_2)$$

- ▶ arXiv: 2212.12165
- ▶ **2022-12-23**
- ▶ Phys. Rev.D 107, L091101 (2023)

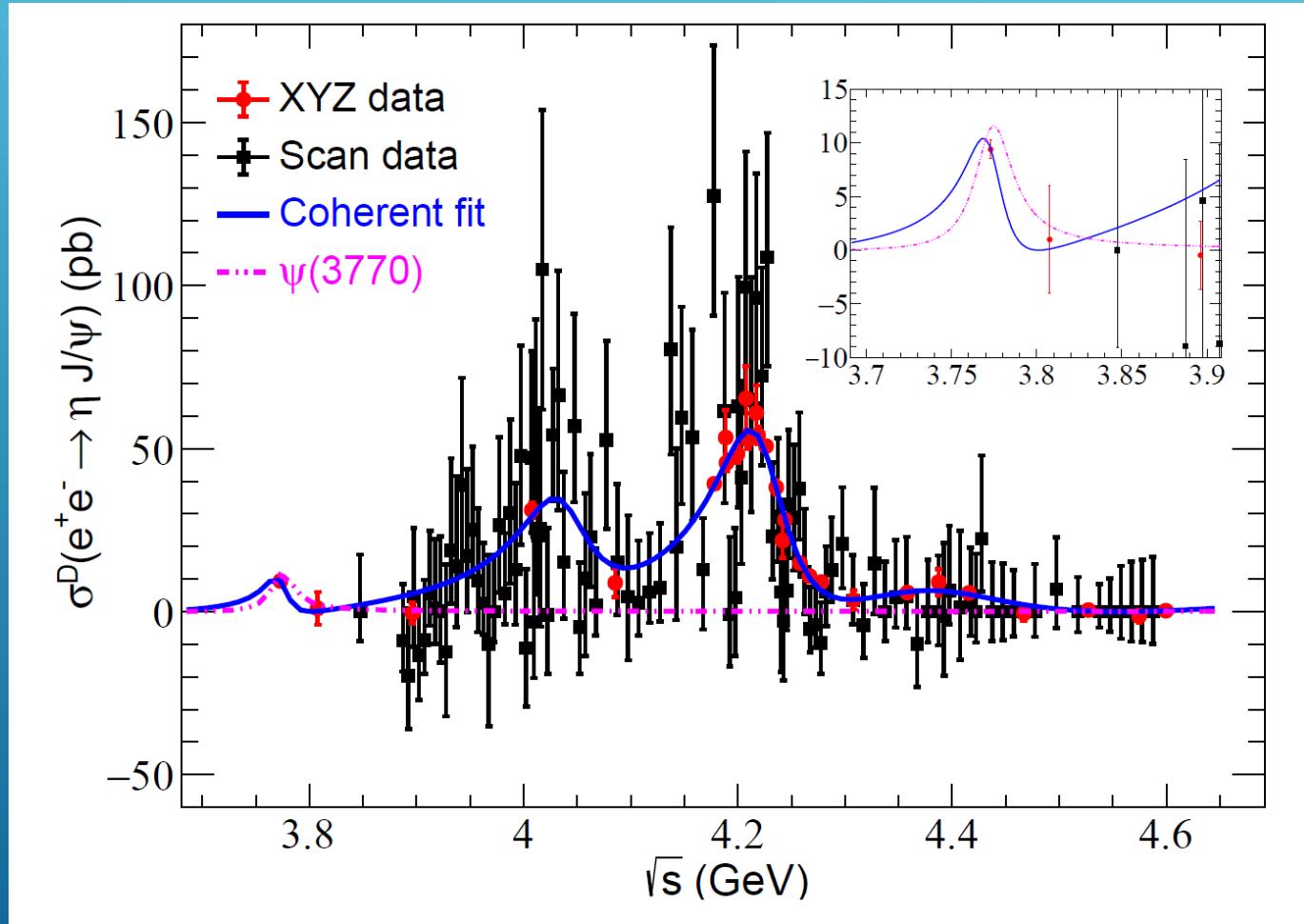
## 470# PAPER

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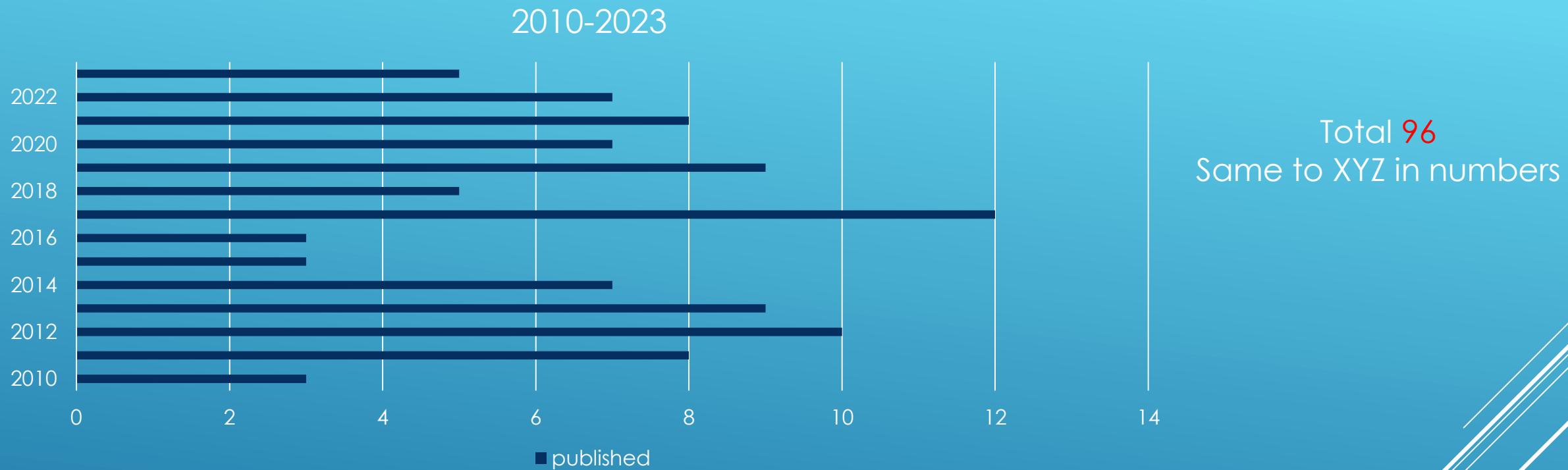
$$\sigma^B(e^+e^- \rightarrow \eta J/\psi) = (8.88 \pm 0.87 \pm 0.42) pb, \sqrt{s} = 3.773 GeV$$

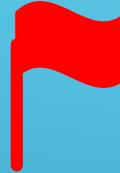
$$B(\psi(3770) \rightarrow \eta J/\psi) = (11.3 \pm 5.9 \pm 1.1) \times 10^{-4}$$



$\psi(3770) \rightarrow \eta J/\psi$   
interference with  
continuum  
and  
higher vector states

# VARIOUS MEASUREMENTS





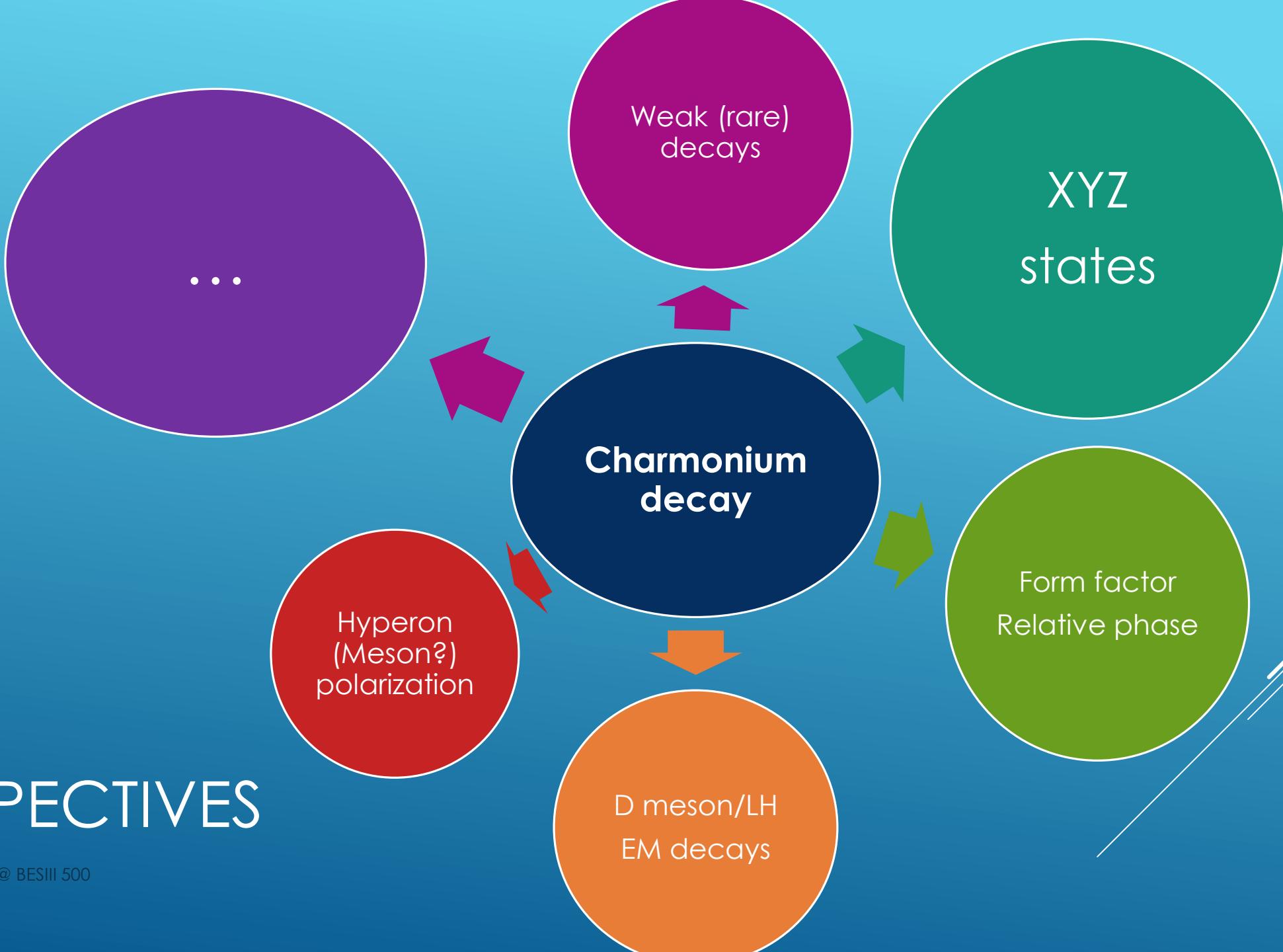
We are excited, we are proud, but we are still far away from the target.

Matching LQCD for non-perturbative part  
Test predictions based perturbative calculations  
Inputs for phenomenological (potential) models  
Check features from EFT (NRQCD, pNRQCD), etc.

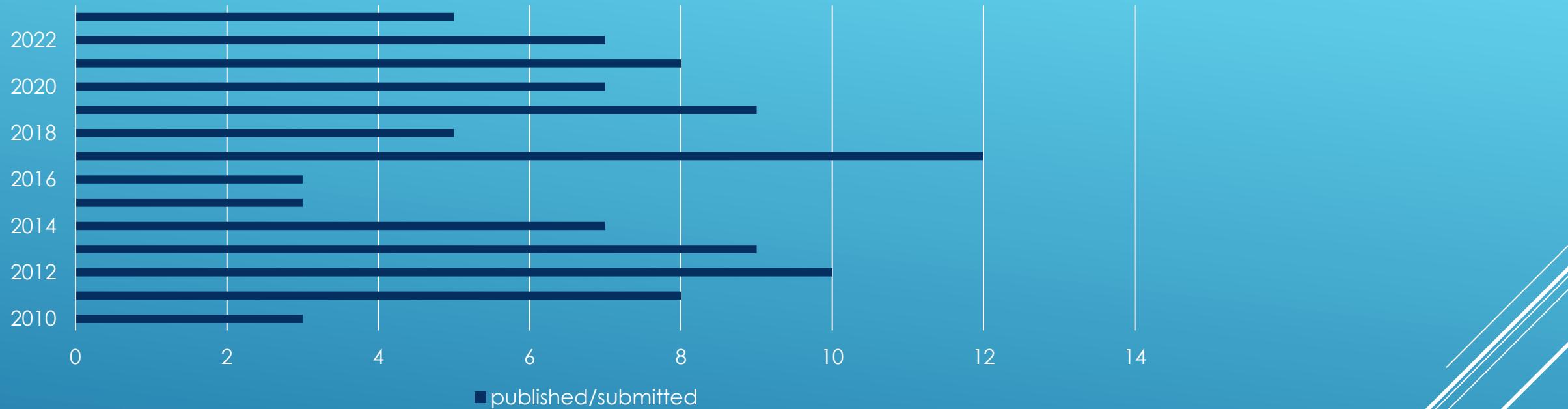
...

# PERSPECTIVES

KAI ZHU @ BESIII 500



2010-20xx



OPEN MIND, WORK HARD, PUBLISH MORE, UNDERSTAND BETTER

# THANK YOU!

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2023/5/31

# BACKUP

# Measurement of the Branching Fraction for the Decay $\psi(3686) \rightarrow \phi K_S^0 K_S^0$

- [arXiv: 2303.08317](https://arxiv.org/abs/2303.08317)
- **2023-03-15**
- Submitted to Phys. Rev. D
- Most recent charmonium decay paper till 2023-5-31

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