### CEPC EW physics: towards White Paper

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mainly based on an earlier draft of the EW white paper and the CEPC Snowmass report [2205.08553]



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#### The current status of the CEPC EW white paper

#### An earlier draft (last updated in 2019) with outdated run scenarios

- Z-pole measurements
- W mass measurements (threshold and kinematic reconstruction)
- Oblique parameter fit
- SMEFT fit
- New physics implications (Natural SUSY)
- The CEPC Snowmass report [2205.08553]
  - Updated measurement inputs
  - Updated SMEFT fit
  - New physics implications (see the previous talk by Xuai)

• Z pole:  $\sim 8 \, \mathrm{ab}^{-1}$ ?  $\rightarrow 100 \, \mathrm{ab}^{-1}$ 

- Many measurements are dominated by systematics, but A<sub>θ</sub> and A<sub>τ</sub> from final state tau polarization measurements are significantly improved. (They were already considered in the earlier draft but were not official...)
- WW threshold:  $3.2 \, \mathrm{ab}^{-1} \rightarrow 6 \, \mathrm{ab}^{-1}$ 
  - W mass: 1 MeV → 0.5 MeV (We also got more optimistic?)
- ▶ 240 GeV:  $5.6 \, \text{ab}^{-1} \rightarrow 20 \, \text{ab}^{-1}$ 
  - Higgs and diboson ( $e^+e^- \rightarrow WW$ ) measurements
- Top threshold run: no  $\rightarrow$  yes
  - The top mass measurement is an important input for EW fits!
  - (see Xiaohu's talk on Tuesday)

## The measurement inputs CEPC Snowmass report [2205.08553]

Observable	current precision	CEPC precision (Stat. Unc.)	CEPC runs	main systematic	
$\Delta m_Z$	2.1 MeV [37–41]	$0.1 { m MeV} (0.005 { m MeV})$	${\cal Z}$ threshold	$E_{beam}$	
$\Delta\Gamma_Z$	2.3 MeV [37–41]	$0.025~{\rm MeV}~(0.005~{\rm MeV})$	${\cal Z}$ threshold	$E_{beam}$	
$\Delta m_W$	9 MeV [42–46]	$0.5 { m MeV} (0.35 { m MeV})$	WW threshold	$E_{beam}$	
$\Delta \Gamma_W$	49 MeV [46–49]	$2.0 { m MeV} (1.8 { m MeV})$	$WW\ {\rm threshold}$	$E_{beam}$	
$\Delta m_t$	$0.76 {\rm ~GeV} [50]$	O(10) MeV <sup>a</sup>	$t\bar{t}$ threshold		
$\Delta A_e$	$4.9\times 10^{-3} \ \ [\textbf{37, 51-55}]$	$1.5\times 10^{-5}~(1.5\times 10^{-5})$	$Z$ pole $(Z \to \tau \tau)$	Stat. Unc.	
$\Delta A_{\mu}$	0.015 [ <b>37</b> , <b>53</b> ]	$3.5\times 10^{-5}~(3.0\times 10^{-5})$	$Z$ pole $(Z \to \mu \mu)$	point-to-point Unc.	
$\Delta A_{\tau}$	$4.3\times 10^{-3} \ \ [\textbf{37}, \ \textbf{51}\textbf{-}\textbf{55}]$	$7.0\times 10^{-5}~(1.2\times 10^{-5})$	$Z$ pole $(Z \to \tau \tau)$	tau decay model	
$\Delta A_b$	0.02 [37, 56]	$20\times 10^{-5}~(3\times 10^{-5})$	Z pole	QCD effects	
$\Delta A_c$	0.027 [37, 56]	$30\times 10^{-5}~(6\times 10^{-5})$	Z pole	QCD effects	
$\Delta \sigma_{had}$	37 pb [37–41]	2  pb (0.05  pb)	Z pole	lumiosity	
$\delta R_b^0$	0.003 [37, 57–61]	$0.0002~(5\times 10^{-6})$	${\cal Z}$ pole	gluon splitting	
$\delta R_c^0$	$0.017 \ [37, 57, 62-65]$	$0.001~(2\times 10^{-5})$	Z pole	gluon splitting	
$\delta R_e^0$	0.0012 [37-41]	$2\times 10^{-4}~(3\times 10^{-6})$	Z pole	$E_{beam}$ and t channel	
$\delta R^0_\mu$	0.002 [37-41]	$1\times 10^{-4}~(3\times 10^{-6})$	${\cal Z}$ pole	$E_{beam}$	
$\delta R_{ au}^0$	0.017 [37-41]	$1\times 10^{-4}~(3\times 10^{-6})$	${\cal Z}$ pole	$E_{beam}$	
$\delta N_{\nu}$	0.0025 [ <b>37</b> , <b>66</b> ]	$2\times 10^{-4}~(3\times 10^{-5}$ )	$ZH$ run $(\nu\nu\gamma)$	Calo energy scale	

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- $\Delta$ : absolute uncertainties,  $\delta$ : relative uncertainties
- ► The constraints on  $A_e$  and  $A_\tau$  mainly come from  $e^+e^- \rightarrow \tau^+\tau^-$  with final state tau polarization measurements.
- $A_{\mu}$ ,  $A_{b}$  and  $A_{c}$  are derived from the  $A^{\text{FB}}$  measurements and  $A_{e}$ .
  - Best way to present the results?

# S & T parameters (earlier draft)



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#### S & T parameters (earlier draft)



▶ What's the impact of the *m*<sup>t</sup> measurement?

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C	$\begin{split} \chi &= -\frac{1}{2} \int_{\infty} F^{*} \\ &+ i \mathcal{F} \mathcal{D} \mathcal{J} + k_c \\ &+ \mathcal{J}_c \mathcal{G}_{ij} \mathcal{J}_j \mathcal{J} + k_c \\ &+  \mathbf{P}_{ij}\mathbf{f}^{T} - V(\mathcal{G}) \end{split}$	+
-		

	$X^{3}$		$\varphi^4$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$		(LL)(LL)		$(\bar{R}R)(\bar{R}R)$		(LL)(RR)
Qc	$f^{ABC}G^{A\nu}_{\nu}G^{S\mu}_{\nu}G^{C\mu}_{\nu}$	9,	$(\varphi^{\dagger}\varphi)^{3}$	Q.,	$(\varphi^{\dagger}\varphi)(\overline{l_{p}e_{r}}\varphi)$	$Q_{V}$	$(\bar{l}_{\rm f} \gamma_{\rm s} \bar{l}_{\rm r}) (\bar{l}_{\rm s} \gamma^{\mu} l_{\rm t})$	$Q_{ee}$	$(\tilde{e}_{\mu}\gamma_{\mu}e_{\tau})(\tilde{e}_{\nu}\gamma^{*}e_{\ell})$	$Q_{1c}$	$(\tilde{l}_{\mu}\gamma_{\mu}l_{\nu})(\tilde{e}_{\mu}\gamma^{\mu}e_{\mu})$
90	1 ABC GA GA GA GC	80	$(\varphi^{\dagger}\varphi) \Box (\varphi^{\dagger}\varphi)$	Que	$(\varphi^{\dagger}\varphi)(\bar{q}_{\mu}u_{\mu}\bar{\varphi})$	$Q_{ee}^{(1)}$	$(\bar{q}_{\mu}\gamma_{\mu}q_{\nu})(\bar{q}_{\nu}\gamma^{\mu}q_{\nu})$	$Q_{in}$	$(\hat{u}_{\mu}\gamma_{\mu}v_{\nu})(\hat{u}_{e}\gamma^{\mu}s_{i})$	$Q_{he}$	$(\tilde{l}_p \gamma_p \tilde{l}_r)(\hat{u}_s \gamma^{\mu} u_t)$
Qu	SIJKWDWJeWKE	Que	$(\varphi^{\dagger}D^{\mu}\varphi)^{\dagger}(\varphi^{\dagger}D_{\mu}\varphi)$	Que	$(\varphi^{\dagger}\varphi)(\bar{q}_{s}d_{s}\varphi)$	$Q_{ii}^{(0)}$	$(\bar{q}_{\mu}\gamma_{\mu}\tau^{I}q_{\nu})(\bar{q}_{e}\gamma^{\mu}\tau^{I}q_{e})$	$Q_{M}$	$(\tilde{d}_{\mu}\gamma_{\mu}d_{r})(\tilde{d}_{e}\gamma^{\mu}d_{l})$	$Q_{1d}$	$(\bar{l}_{\mu}\gamma_{\mu}l_{\tau})(\bar{d}_{e}\gamma^{\mu}d_{l})$
0.0	LIKWINW JOWKY					$Q_{lg}^{(1)}$	$(\tilde{l}_p \gamma_p l_r)(\tilde{q}_i \gamma^\mu q_i)$	$Q_{ci}$	$(\tilde{e}_{\mu}\gamma_{\mu}e_{\tau})(\tilde{a}_{\mu}\gamma^{\mu}u_{\ell})$	$Q_{\ell^{\mathrm{H}}}$	$(\bar{q}_j \gamma_{j\ell} q_{\ell})(\bar{e}_i \gamma^{\mu} e_l)$
	12.2	-	d <sup>2</sup> Y.c	-	±2.20	$Q_{iq}^{(2)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r) (\bar{q}_i \gamma^\mu \tau^I q_i)$	$Q_{et}$	$(\bar{e}_y \gamma_p e_r)(\bar{d}_s \gamma^s d_b)$	$Q_{qu}^{(1)}$	$(\bar{q}_t \gamma_p q_r)(\bar{u}_s \gamma^\mu u_t)$
0	t at atm	0	d as s I wi	-000	118 10 111			$Q_{ud}^{(1)}$	$(\hat{u}_{\mu}\gamma_{\mu}u_{r})(\tilde{d}_{e}\gamma^{\mu}d_{l})$	$Q_{qn}^{(k)}$	$(\bar{q}_{g}\gamma_{\mu}T^{A}q_{r})(\bar{u}_{e}\gamma^{\mu}T^{A}u_{l})$
Q <sub>i</sub> g	$\varphi^{i}\varphi G^{\alpha}_{\mu\nu}G^{\alpha\mu\nu}$	Qav	$(l_p \sigma^{\mu\nu} e_r) \tau^{\nu} \varphi W^{\prime}_{\mu\nu}$	$Q_{q\bar{q}}$	$(\varphi^{\dagger}(D_{\mu}\varphi)(l_{p}\gamma^{*}l_{r})$			22	$(\bar{a}_s \gamma_s T^A u_s)(\bar{d}_s \gamma^{\mu} T^A d_t)$	Q(1)	(40.00)(d. 1+d.)
$Q_{\mu\bar{\Omega}}$	$\varphi^{\dagger} \varphi \widetilde{G}^{A}_{\mu\nu} G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_{\mu}\sigma^{\mu\nu}c_{\nu})\varphi B_{\mu\nu}$	$Q_{gl}^{(3)}$	$(\varphi^{\dagger}iD^{I}_{\mu}\varphi)(\bar{l}_{\rho}\tau^{I}\gamma^{\mu}l_{r})$					02	(a.n.T^a.)(d. v*T^d.)
$Q_{qW}$	$\varphi^{\dagger}\varphi W^{I}_{\mu\nu}W^{I}\mu\nu$	$Q_{uG}$	$(\bar{q}_{\mu}\sigma^{\mu\nu}T^A u_{\tau})\widetilde{\varphi} G^A_{\mu\nu}$	$Q_{qq}$	$(\varphi^{\dagger}i \vec{D}_{\mu} \varphi)(\vec{e}_{\mu} \gamma^{\mu} e_{\nu})$	(LR)	(RL) and (LR)(LR)	-	B-rio	ating	
$Q_{\sqrt{H}}$	$\varphi^{\dagger}\varphi \widetilde{W}^{I}_{\mu\nu}W^{I}\omega^{\nu}$	$Q_{uW}$	$(\bar{q}_{p}\sigma^{\mu\sigma}u_{r})\tau^{I}\widetilde{\varphi}W^{I}_{\mu\nu}$	$Q_{qq}^{(1)}$	$(\varphi^{\dagger}i D_{\mu} \varphi)(\bar{q}_{\rho} \gamma^{\mu} q_{r})$	Que	$(Ee_i)(d_i a^i)$	an	5""" Eu [(de)	FOug	$[(q_{i}^{sj})^{T}Cl_{i}^{k}]$
9,0	$\varphi^{\dagger}\varphi B_{\mu\nu}B^{\mu\nu}$	$Q_{vS}$	$(q_p \sigma^{\mu\nu} u_r) \overline{\varphi} B_{\rho\nu}$	$Q_{ m eq}^{(3)}$	$(\varphi^{\dagger}i \overset{i}{D}{}^{I}_{\mu} \varphi)(q_{\nu}\tau^{I}\gamma^{\mu}q_{\nu})$	Q <sup>(1)</sup>	$(\phi_i^i v_r) e_{i0}(\phi_i^i d_i)$	0	50.57 E. ((g0)	Cell	$[(a_i)^T C a_i]$
$Q_{\mu\bar{\mu}}$	$\varphi^{\dagger}\varphi  \overline{B}_{\mu\nu} B^{\mu\nu}$	$Q_{AT}$	$(\bar{q}_{\mu}\sigma^{\mu\nu}T^{A}d_{r})\varphi G^{A}_{\mu\nu}$	$Q_{\varphi \pi}$	$(\varphi^{\dagger}i D_{\mu} \varphi)(\bar{u}_{\rho} \gamma^{\mu} u_{\tau})$	Q <sup>IN</sup>	$\langle q_i^{i}T^{ii}v_r \rangle e_{ii} \langle q_i^{k}T^{ii}d_i \rangle$	Q(1)	2037 E 418 cm [(02	i)TCg	*] [(q2m) <sup>7</sup> C22]
$Q_{qWB}$	$\varphi^{\dagger}\tau^{J}\varphi W^{I}_{\mu\nu}B^{\mu\nu}$	$Q_{dW}$	$(q_p\sigma^{\mu\nu}d_r)\tau^J\varphiW^J_{\mu\nu}$	$Q_{qd}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\widetilde{d}_{p}\gamma^{*}d_{r})$	$Q_{logs}^{(0)}$	$(l_{\mu}^{i}c_{r})c_{\mu}(\hat{q}_{s}^{k}a_{t})$	$Q_{\rm HH}^{\rm IN}$	$\varepsilon^{\alpha\beta\gamma}(\tau^{\dagger}\varepsilon)_{\mu}(\tau^{\dagger}\varepsilon)_{cm}$	[(q23)]	$Cq_{r}^{(h)}$ [( $q_{r}^{(m)}$ ) <sup>T</sup> $Cl_{r}^{m}$ ]
Q.Ra	$\varphi^{l}\tau^{l}\varphi \widetilde{W}^{l}_{\mu\nu}B^{\mu\nu}$	$Q_{d3}$	$(\bar{q}_{\mu}\sigma^{\mu\nu}d_{\nu})\varphi B_{\mu\nu}$	Que	$i(\hat{\varphi}^{\dagger}D_{\mu}\varphi)(\hat{u}_{\mu}\gamma^{\mu}d_{\tau})$	$Q_{logu}^{(2)}$	$(\bar{\ell}_{p}^{i}\sigma_{\mu\nu}e_{\nu})e_{\mu}(q_{\mu}^{i}\sigma^{\mu\nu}u_{i})$	Qen	$\varepsilon^{\alpha\beta\gamma} [(d^a_\mu)^3$	Cu <sup>3</sup>	$[(u_i^*)^T C v_i]$

- Write down all possible (non-redundant) dimension-6 operators ...
- 59 operators (76 parameters) for 1 generation, or 2499 parameters for 3 generations. [arXiv:1008.4884] Grzadkowski, Iskrzyński, Misiak, Rosiek, [arXiv:1312.2014] Alonso, Jenkins, Manohar, Trott.
- A full global fit with all measurements to all operator coefficients?
  - ▶ We usually only need to deal with a subset of them, *e.g.* ~ 20-30 parameters for **Higgs and electroweak** measurements.
- Do a global fit and present the results with some fancy bar plots!

### You can't really separate Higgs from the EW gauge bosons!

 $\begin{array}{l} \bullet \quad \mathcal{O}_{H\ell} = iH^{\dagger} \overrightarrow{D_{\mu}} H \overline{\ell}_{L} \gamma^{\mu} \ell_{L}, \\ \mathcal{O}_{H\ell}' = iH^{\dagger} \sigma^{a} \overrightarrow{D_{\mu}} H \overline{\ell}_{L} \sigma^{a} \gamma^{\mu} \ell_{L}, \\ \mathcal{O}_{He} = iH^{\dagger} \overrightarrow{D_{\mu}} H \overline{e}_{R} \gamma^{\mu} e_{R} \end{array}$ 

(or the ones with quarks)

- modifies gauge couplings of fermions,
- also generates hVff type contact interaction.



- $\mathcal{O}_{HW} = ig(D^{\mu}H)^{\dagger}\sigma^{a}(D^{\nu}H)W^{a}_{\mu\nu}, \\ \mathcal{O}_{HB} = ig'(D^{\mu}H)^{\dagger}(D^{\nu}H)B_{\mu\nu}$ 
  - generate **aTGCs**  $\delta g_{1,Z}$  and  $\delta \kappa_{\gamma}$ ,
  - also generates *HVV* anomalous couplings such as hZ<sub>μ</sub>∂<sub>ν</sub>Z<sup>μν</sup>.



# $e^+e^- ightarrow WW$ with Optimal Observables

- TGCs (and additional EFT parameters) are sensitive to the differential distributions!
  - One could do a fit to the binned distributions of all angles.
  - Not the most efficient way of extracting information.
  - Correlations among angles are sometimes ignored.
- What are optimal observables?

(See e.g. Z.Phys. C62 (1994) 397-412 Diehl & Nachtmann)

In the limit of large statistics (everything is Gaussian) and small parameters (linear contribution dominates), the best possible reaches can be derived analytically!

$$rac{d\sigma}{d\Omega} = S_0 + \sum_i S_{1,i} \, g_i \,, \qquad c_{ij}^{-1} = \int d\Omega rac{S_{1,i} S_{1,j}}{S_0} \cdot \mathcal{L}$$

- Current work on an improved analysis with machine learning. (Shengdu Chai, JG, Lingfeng Li)
- A more realistic experimental analysis is needed!





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- 28-parameter fit projected on Higgs couplings and anomalous triple gauge couplings.
- ►  $\delta g_H^{ZZ} \approx \delta g_H^{WW}$  from theoretical constraints (gauge invariance & custodial symmetry) and EW measurements.
- ▶ Non-negligible improvement from the 360 GeV run.

# SMEFT global fit (Vff couplings) (earlier draft)



#### precision reach on the Vff couplings from the full EFT fit

• U(2) symmetry imposed on first two generation quarks.

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- 20-parameter fit (assuming flavor universality in gauge-fermion couplings).
- See next page for the operator basis.

$\mathcal{O}_{H} = \frac{1}{2} (\partial_{\mu}  H^{2} )^{2}$	$\mathcal{O}_{GG}=g_{s}^{2} \mathcal{H} ^{2}G_{\mu u}^{A}G^{A,\mu u}$
$\mathcal{O}_{WW}=g^2 \mathcal{H} ^2 W^a_{\mu u} W^{a,\mu u}$	$\mathcal{O}_{y_u} = y_u  H ^2 \bar{q}_L \tilde{H} u_R + \text{h.c.}  (u \to t, c)$
$\mathcal{O}_{BB}=g^{\prime2} H ^2B_{\mu u}B^{\mu u}$	$\mathcal{O}_{y_d} = y_d  H ^2 \bar{q}_L H d_R + \text{h.c.}  (d \to b)$
$\mathcal{O}_{HW} = ig(D^{\mu}H)^{\dagger}\sigma^{a}(D^{\nu}H)W^{a}_{\mu\nu}$	$\mathcal{O}_{y_e} = y_e  H ^2 \overline{l}_L He_R + \text{h.c.}  (e \to \tau, \mu)$
$\mathcal{O}_{HB} = ig'(D^{\mu}H)^{\dagger}(D^{\nu}H)B_{\mu\nu}$	$\mathcal{O}_{3W}=rac{1}{3!}g\epsilon_{abc}W^{a u}_{\mu}W^{b}_{ u ho}W^{c ho\mu}$
$\mathcal{O}_{W} = \frac{ig}{2} (H^{\dagger} \sigma^{a} \overleftrightarrow{D_{\mu}} H) D^{\nu} W^{a}_{\mu\nu}$	$\mathcal{O}_{B} = \frac{ig'}{2} (H^{\dagger} \overleftarrow{D_{\mu}} H) \partial^{\nu} B_{\mu\nu}$
$\mathcal{O}_{WB} = gg' H^{\dagger}_{\mu\nu} \sigma^a H W^a_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_{H\ell} = iH^{\dagger} \overleftrightarrow{D_{\mu}} H \bar{\ell}_L \gamma^{\mu} \ell_L$
$\mathcal{O}_{T} = \frac{1}{2} (H^{\dagger} \overrightarrow{D_{\mu}} H)^{2}$	$\mathcal{O}'_{H\ell} = iH^{\dagger}\sigma^{a}\widetilde{D_{\mu}}H\bar{\ell}_{L}\sigma^{a}\gamma^{\mu}\ell_{L}$
$\mathcal{O}_{\ell\ell} = (\bar{\ell}_L \gamma^\mu_\ell \ell_L) (\bar{\ell}_L \gamma_\mu \ell_L)$	$\mathcal{O}_{He} = i H^{\dagger} \overleftarrow{D_{\mu}} H \overline{e}_R \gamma^{\mu} e_R$
$\mathcal{O}_{Hq} = i H^{\dagger} \overleftrightarrow{D_{\mu}} H \overline{q}_L \gamma^{\mu} q_L$	$\mathcal{O}_{Hu} = iH^{\dagger} \overleftrightarrow{D_{\mu}} H \overline{u}_R \gamma^{\mu} u_R$
$\mathcal{O}_{Hq}^{\prime} = i H^{\dagger} \sigma^{a} \overrightarrow{D_{\mu}} H \overline{q}_{L} \sigma^{a} \gamma^{\mu} q_{L}$	$\mathcal{O}_{Hd} = i H^{\dagger} \widetilde{D_{\mu}'} H \overline{d}_R \gamma^{\mu} d_R$

- ▶ SILH' basis (eliminate  $\mathcal{O}_{WW}$ ,  $\mathcal{O}_{WB}$ ,  $\mathcal{O}_{H\ell}$  and  $\mathcal{O}'_{H\ell}$ )
- ▶ Modified-SILH' basis (eliminate  $\mathcal{O}_W$ ,  $\mathcal{O}_B$ ,  $\mathcal{O}_{H\ell}$  and  $\mathcal{O}'_{H\ell}$ ) (used here)
- Warsaw basis (eliminate  $\mathcal{O}_W$ ,  $\mathcal{O}_B$ ,  $\mathcal{O}_{HW}$  and  $\mathcal{O}_{HB}$ )

## Results from the recent snowmass SMEFT global fit study

[2206.08326] de Blas, Du, Grojean, JG, Miralles, Peskin, Tian, Vos, Vryonidou



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#### Impacts of (lack of) the Z-pole run

[2206.08326] de Blas, Du, Grojean, JG, Miralles, Peskin, Tian, Vos, Vryonidou



- Without good Z-pole measurements, the eeZh contact interaction may have a significant impact on the Higgs coupling determination.
- Current (LEP) Z-pole measurements are not good enough for CEPC Higgs measurements!
- The CEPC Z-pole measurements are!



Update measurement inputs (if any)

- Any updates to the numbers in CEPC Snowmass report [2205.08553] ?
- This is the most essential part!
- More measurements?
  - Top mass measurement
  - Diboson measurement ( $e^+e^- 
    ightarrow WW$ )
  - $\blacktriangleright \ e^+e^- \to \gamma\gamma/Z\gamma/ZZ \dots$
  - ► ...
- More interpretations?
  - Overlap with the new physics white paper?
- Timeline/deadline?

# backup slides

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CEPC EW physics: towards White Paper

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